



# NNPDF $\alpha_s$

- PDFs &  $\alpha_s$
- $\alpha_s$  @ NLO & NNLO

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# Monte Carlo PDFs (eg NNPDF)

Giele & Kosower 1998

Forte & Latorre 2002

- Choose a very flexible functional form for each PDF:  
(eg a neural network:  $\sim 250$  params)
  - Generate data replicas ( $\sim 100-1000$ ) using exp uncertainties
  - Find a **good** fit to each data replica by optimising  $\chi^2$   
(best fit useless – fitting statistical noise:  
instead use genetic algorithm + cross-validation)
  - Treat resulting PDF replicas as statistical ensemble:  
each equally probable (importance sampling).
- So simple averages give central values, uncertainties etc.

**Advantages:**

**No theoretical bias due to parametrization**

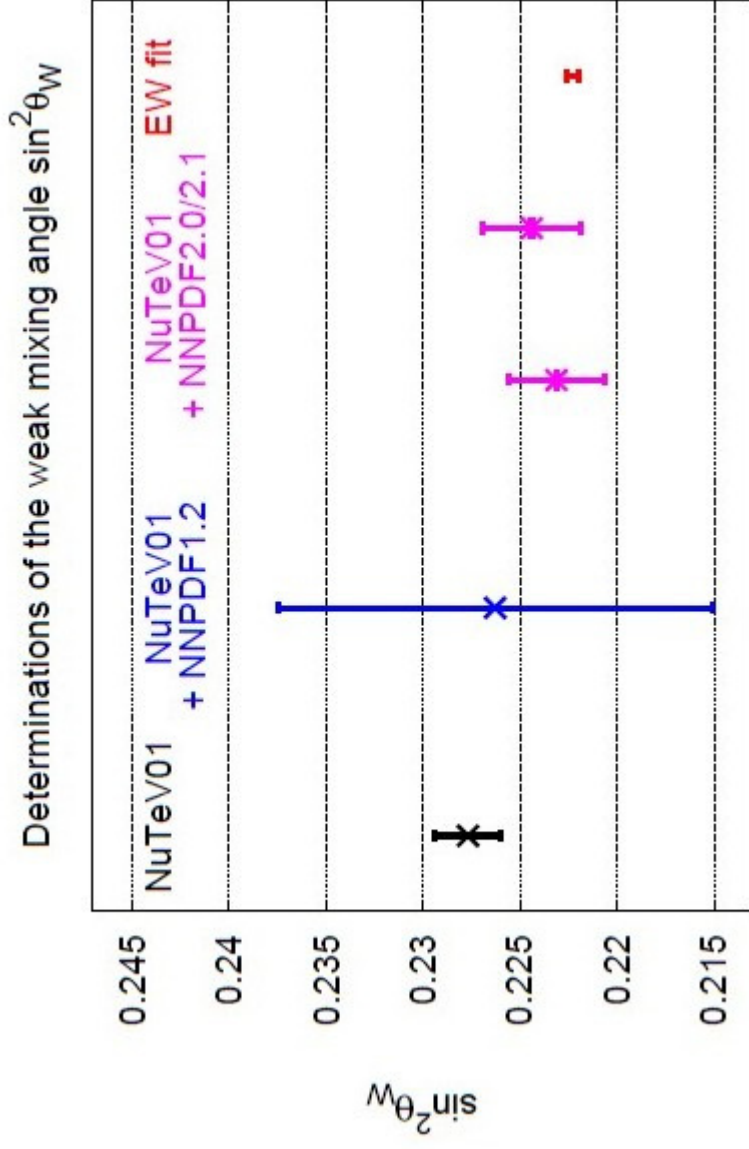
**Statistically meaningful uncertainties: no need for tolerance**

**Technical stability: vary data or theory, same parametrization**

# The NuTeV Anomaly

Determination of  $\sin^2 \theta_W$  using neutrino DIS data: assumed  $s = \bar{s}$ :

**found 3-sigma discrepancy: new physics?**



Include  $s \neq \bar{s}$  using NNPDF1.2/2.0/2.1: discrepancy disappears!

**More flexible (NN)PDFs: more precise physics!**

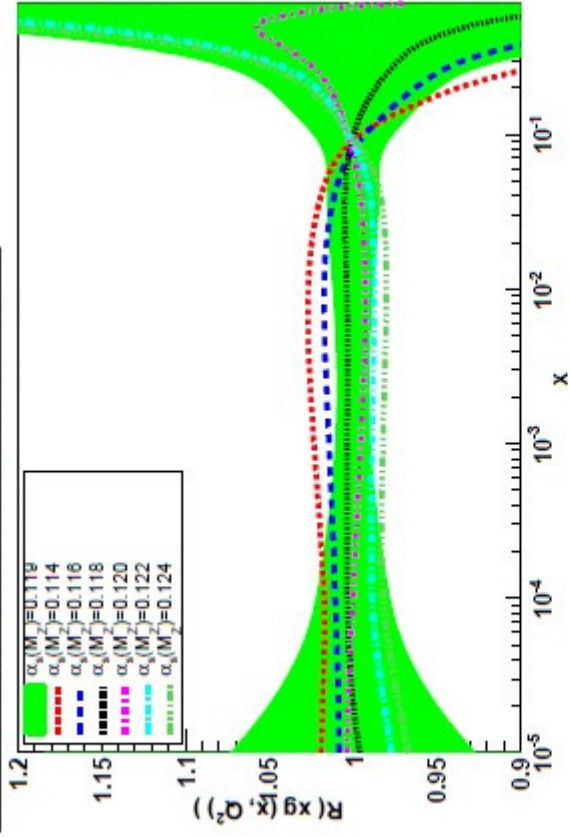
# PDFs and $\alpha_s$

- $P(\text{fl}\alpha_s)$ : PDFs for given  $\alpha_s$   
e.g. NNPDF2.1 supplied for  $\alpha_s=0.114, 0.115, \dots, 0.123, 0.124$
- $P(\text{f}) = \int P(\text{fl}\alpha_s) P(\alpha_s)$   
Overall PDF uncertainty: need correlation of PDFs with  $\alpha_s$   
Also prior  $P(\alpha_s)$  : e.g. from PDG (includes e+e- etc)  
e.g. own determination from PDF fit
- $P(\alpha_s)$ :  $\alpha_s$  from global dataset in PDF fit

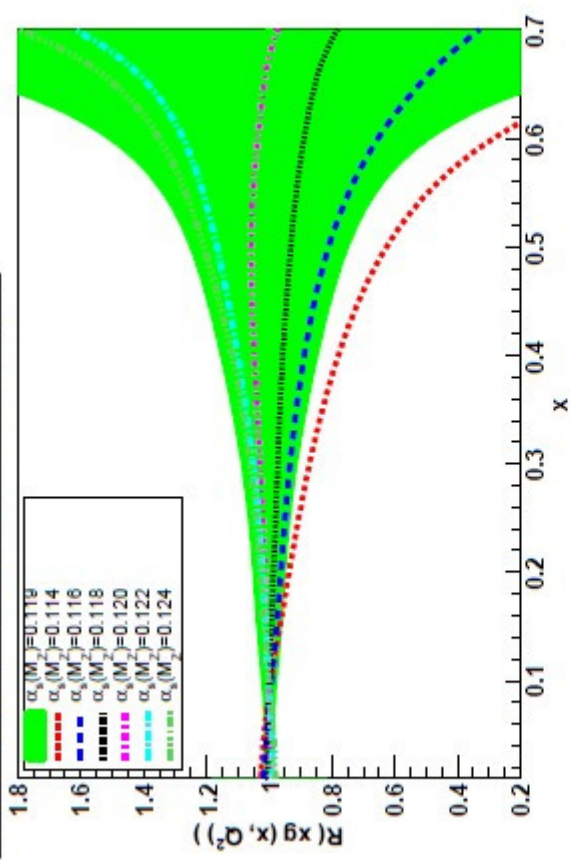
**N.B.** All these comments also apply to any other external parameters:  $m_c, m_b, \theta_W, V_{qq}, \dots$

# PDFs vs $\alpha_s$

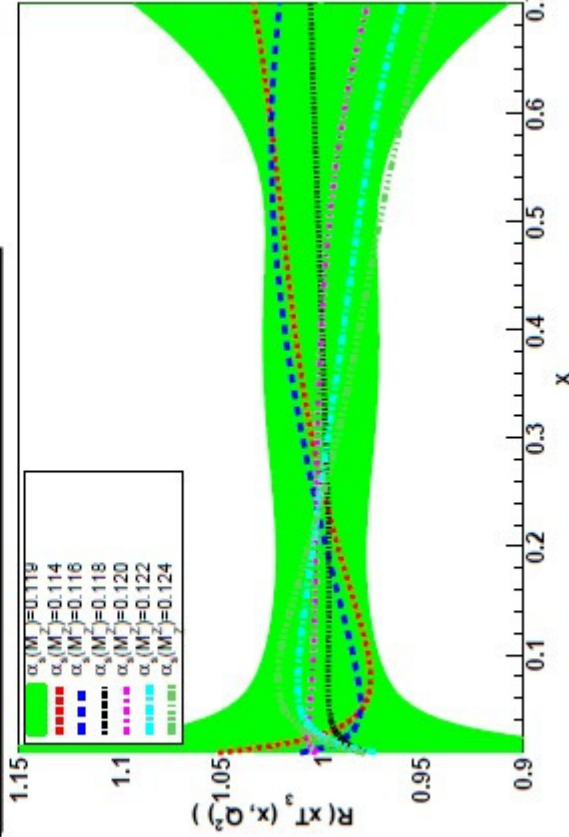
Ratio to NNPDF2.1 NNLO,  $Q^2 = 10^4 \text{ GeV}^2$



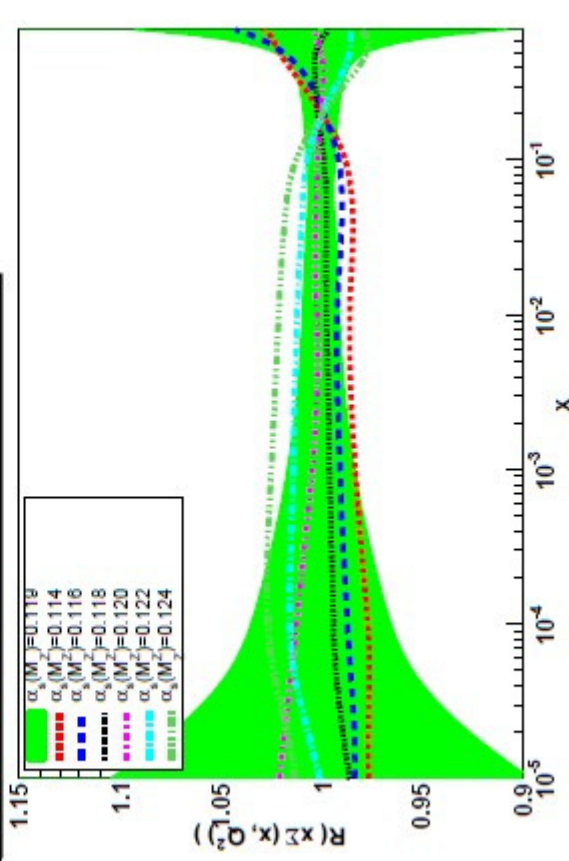
Ratio to NNPDF2.1 NNLO,  $Q^2 = 10^4 \text{ GeV}^2$



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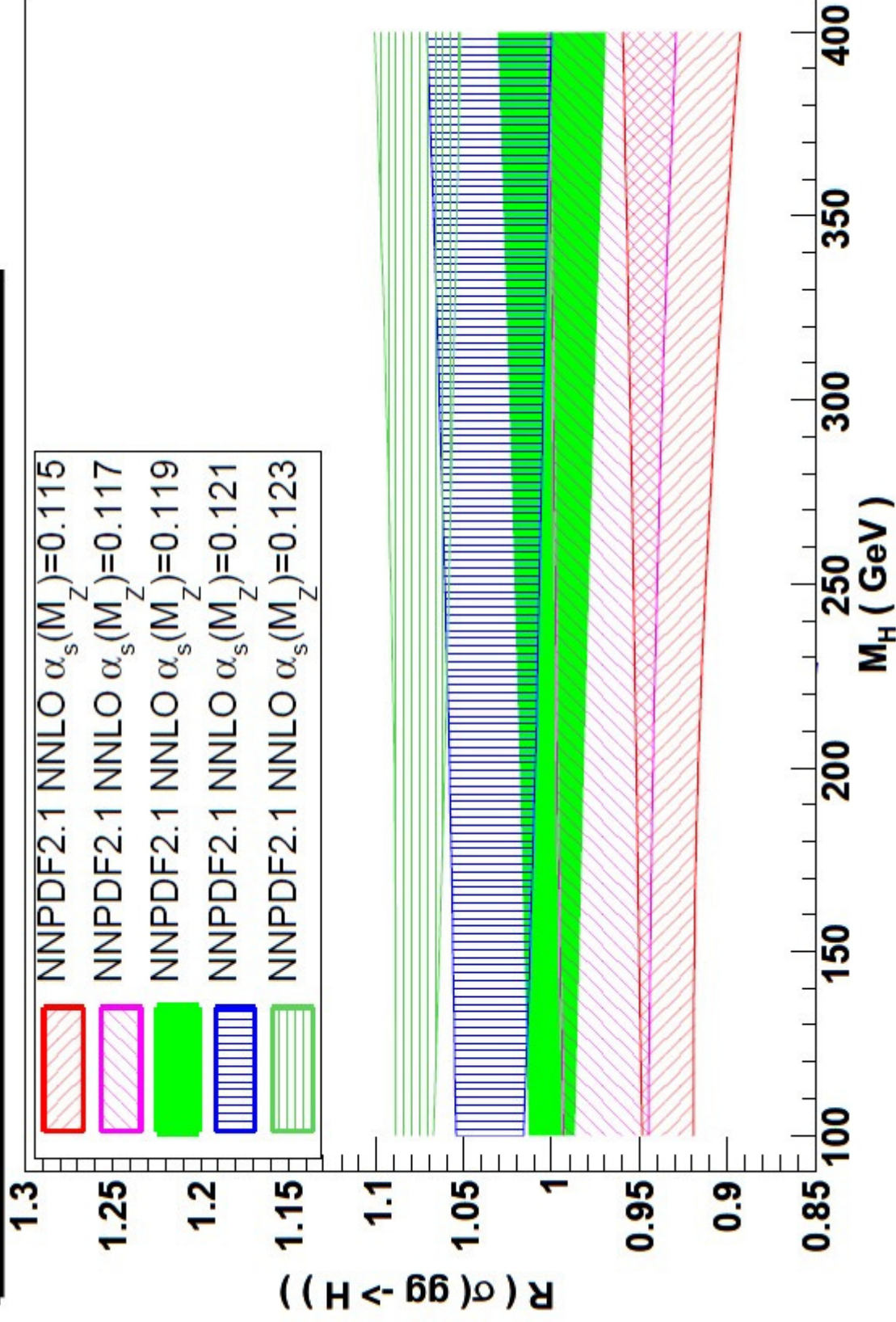
Ratio to NNPDF2.1 NNLO,  $Q^2 = 10^4 \text{ GeV}^2$



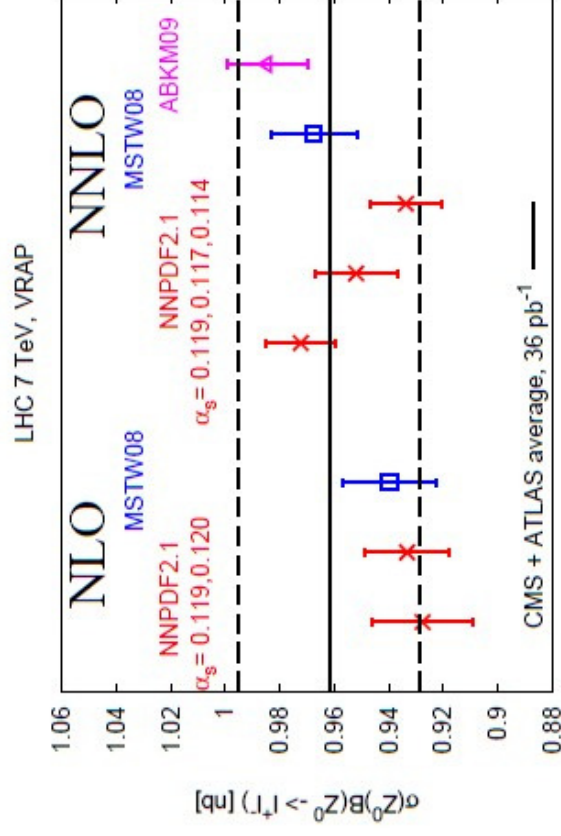
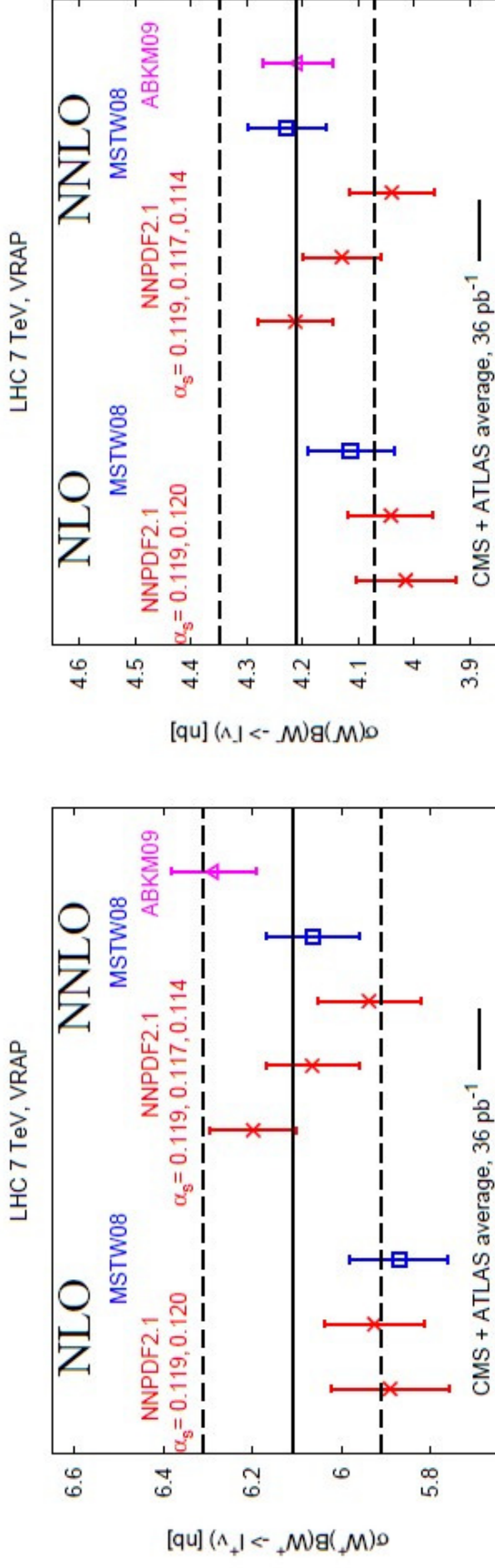


# $\sigma_{ggH}$ VS $\alpha_s$

LHC 7 TeV, Ratio to NNPDF2.1 NNLO  $\alpha_s(M_Z)=0.119$



# Meaningful comparison of PDFs requires common $\alpha_s$



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Also prior  $P(\alpha_s)$  : e.g. from PDG (includes e+e- etc)  
e.g. own determination from PDF fit
- $P(\alpha_s)$ :  $\alpha_s$  from global dataset in PDF fit

**N.B.** All these comments also apply to any other external parameters:  $m_c$ ,  $m_b$ ,  $\theta_W$ ,  $V_{qq}$ , ...

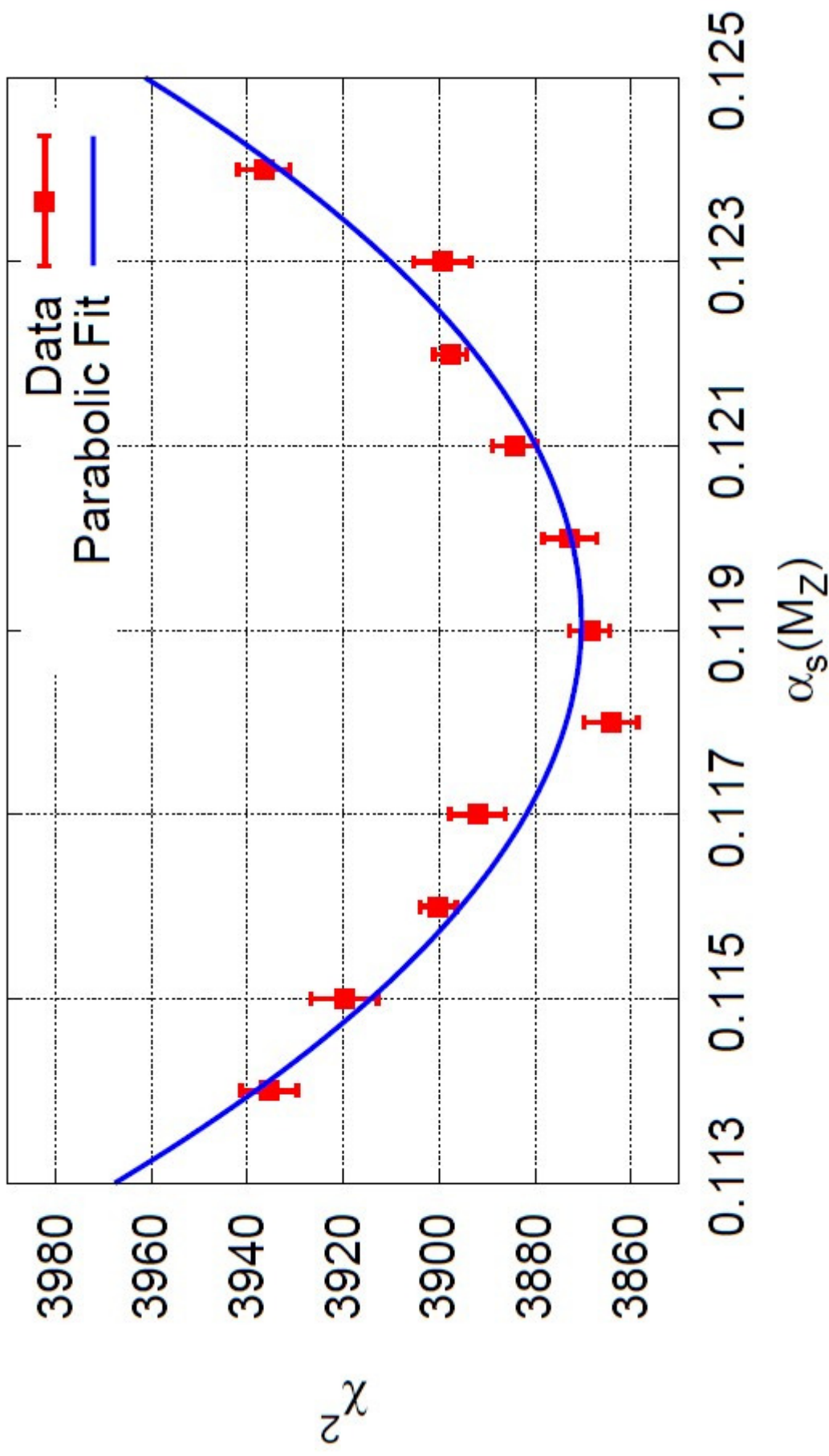


NLO

$\chi^2$  vs  $\alpha_s$

arXiv:1103.2369

NNPDF2.1 Total Dataset

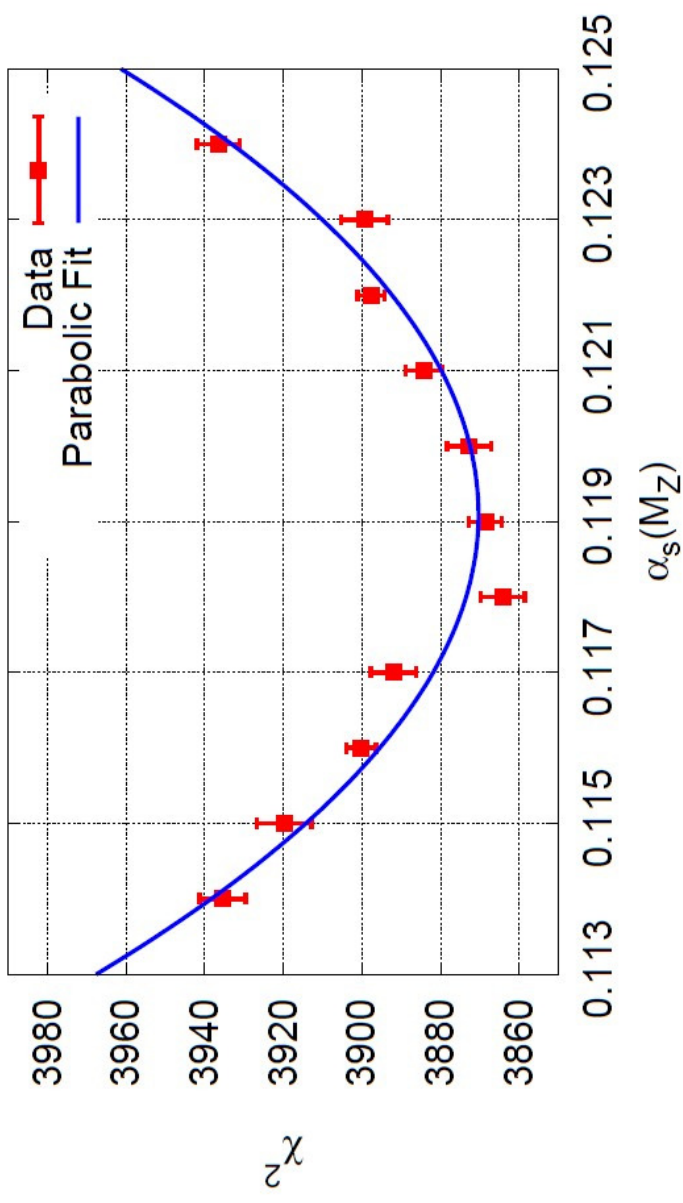


# NLO

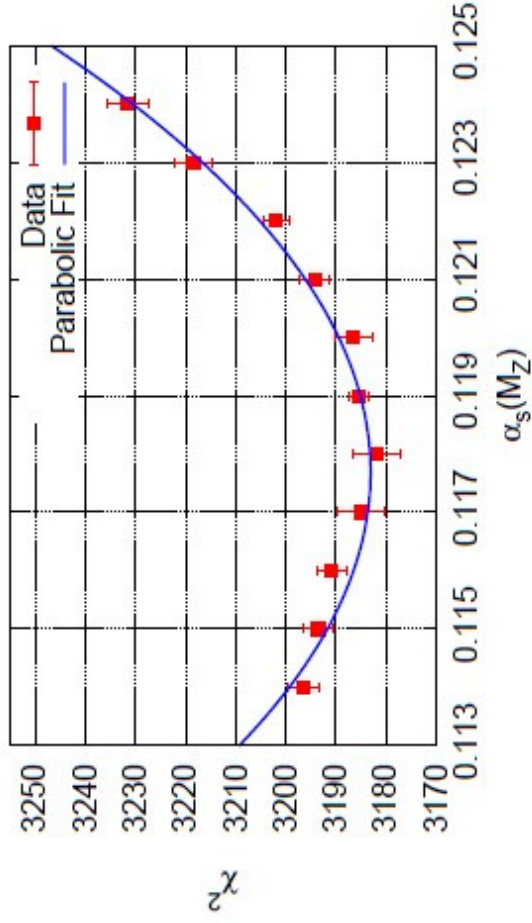
## $\chi^2$ VS $\alpha_s$

arXiv:1103.2369

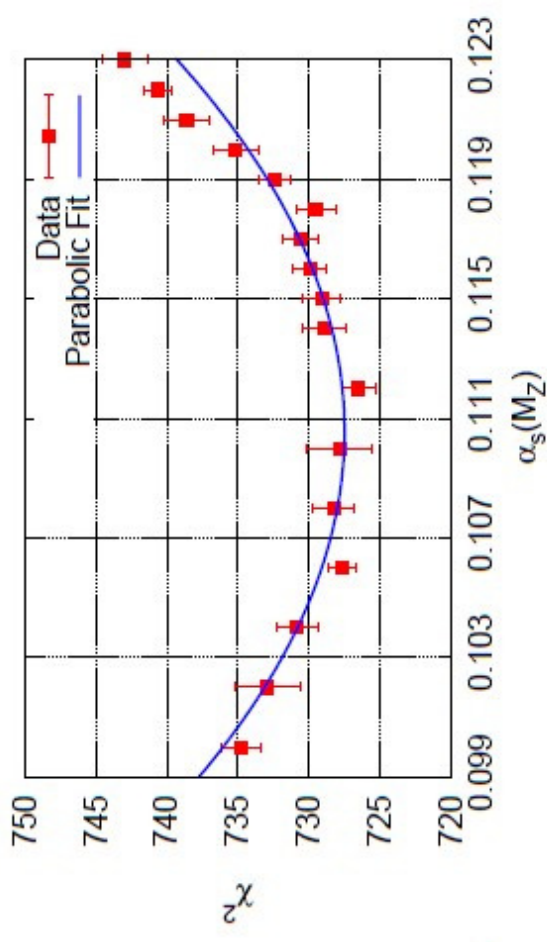
NNPDF2.1 Total Dataset



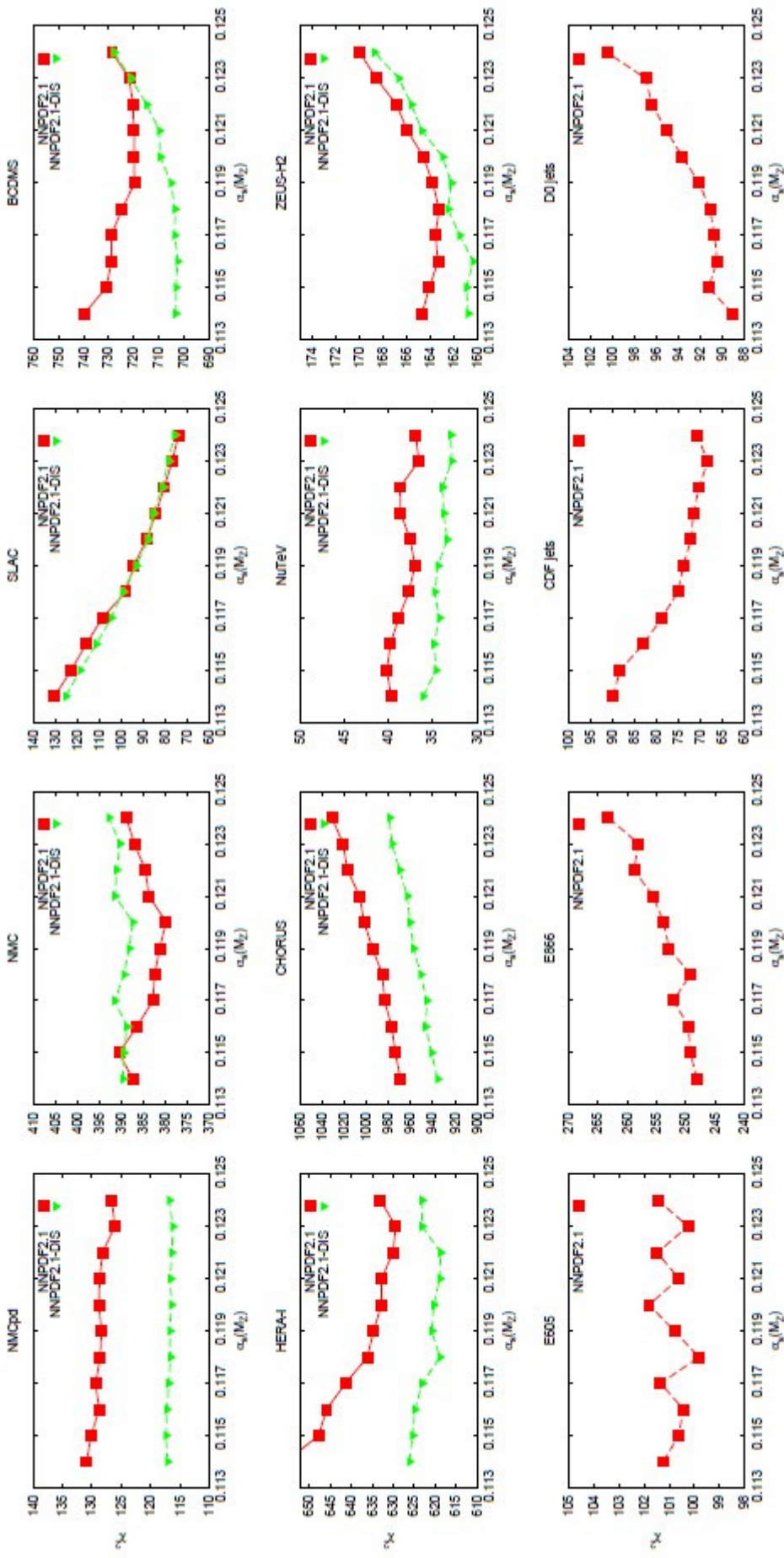
NNPDF2.1 - DIS data only



NNPDF2.1 - HERA data only



# $\chi^2(\alpha_s)$ for individual datasets



**N.B. no min in BCDMS for DIS-only**

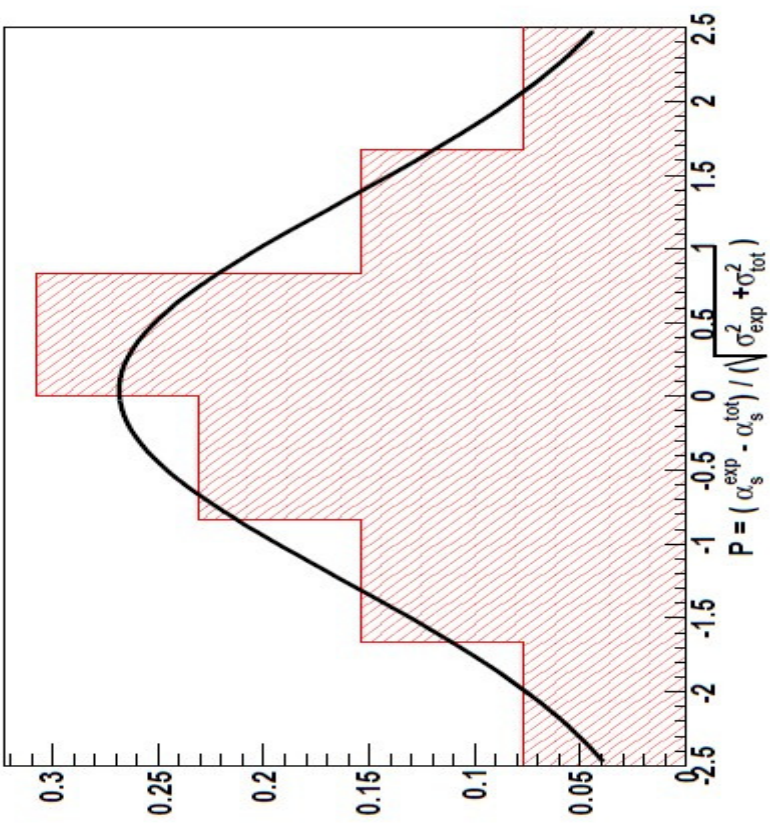


# Pulls:

$$P_i \equiv \frac{\alpha_s^i(M_Z) - \alpha_s^{\text{tot}}(M_Z)}{\sqrt{\sigma_{\alpha_s}^{i,2} + \sigma_{\alpha_s}^{\text{tot},2}}}$$

Experiment	$\alpha_s^i \pm \sigma_{\alpha_s}^i$	$P_i$
NMCp	$0.1192 \pm 0.0018$	-0.05
BCDMS	$0.1204 \pm 0.0015$	-0.78
HERA-I	$0.1223 \pm 0.0018$	-1.65
ZEUS-H2	$0.1170 \pm 0.0027$	0.75
NuTeV	$0.1252 \pm 0.0068$	-0.89
ZEUSF2C	$0.1144 \pm 0.0060$	0.77
E605	$0.1168 \pm 0.0100$	0.22
E866	$0.1135 \pm 0.0029$	1.87
CDFWASY	$0.1181 \pm 0.006$	0.16
CDFZRAP	$0.1150 \pm 0.0034$	1.18
D0ZRAP	$0.1227 \pm 0.0067$	-0.53
CDFR2KT	$0.1228 \pm 0.0021$	-1.67
D0R2CON	$0.1141 \pm 0.0031$	1.57

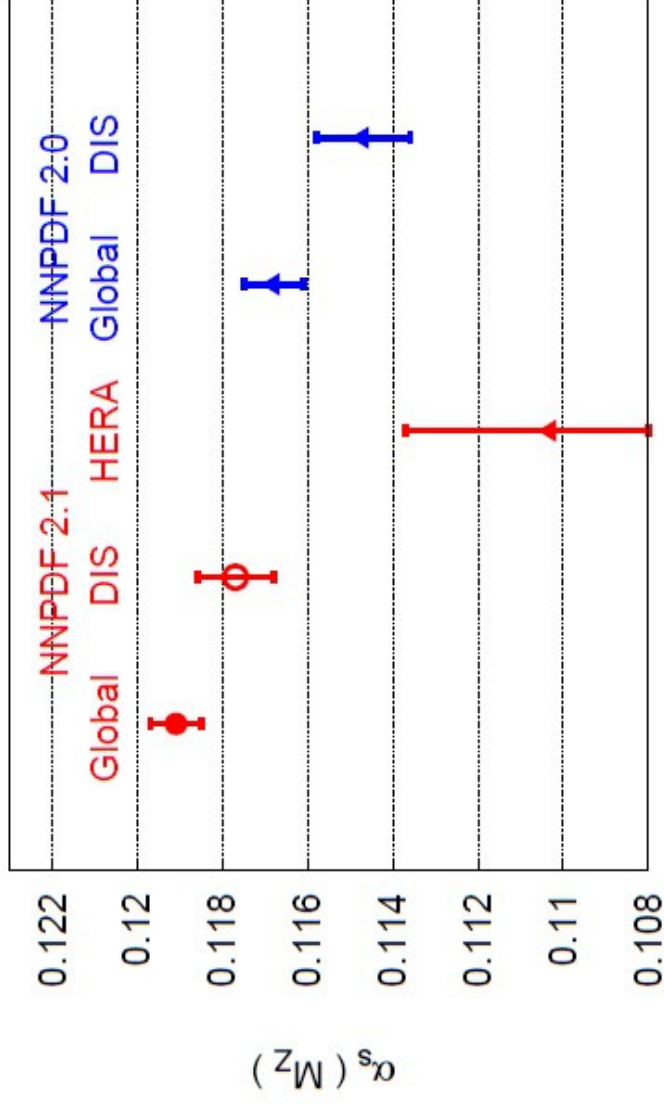
Distribution of pulls with global fit  $\alpha_s$



# Results (NLO)

	$\alpha_s (M_Z)$	$\chi^2_{\text{par}}/N_{\text{dof}}$
NNPDF2.1	$0.1191 \pm 0.0006^{\text{exp}} \pm 0.0001^{\text{proc}}$	1.6
NNPDF2.1 DIS-only	$0.1178 \pm 0.0009^{\text{exp}} \pm 0.0002^{\text{proc}}$	0.8
NNPDF2.1 HERA-only	$0.1101 \pm 0.0033^{\text{exp}} \pm 0.0003^{\text{proc}}$	1.1
NNPDF2.0	$0.1168 \pm 0.0007^{\text{exp}} \pm 0.0001^{\text{proc}}$	0.4
NNPDF2.0 DIS-only	$0.1145 \pm 0.0010^{\text{exp}} \pm 0.0003^{\text{proc}}$	1.4.

NNPDF NLO determinations of  $\alpha_s (M_Z)$

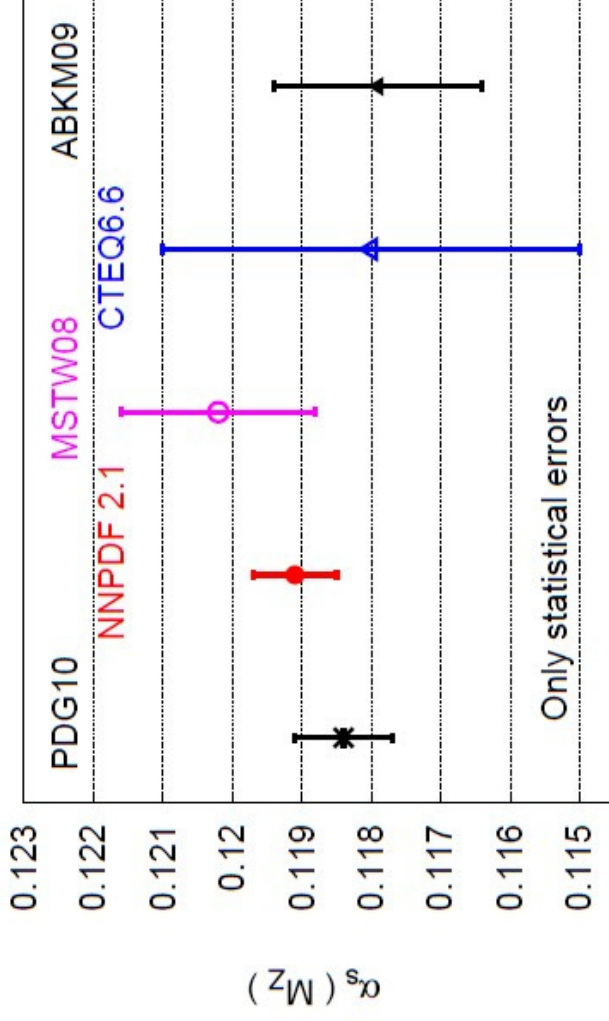




# Results (NLO)

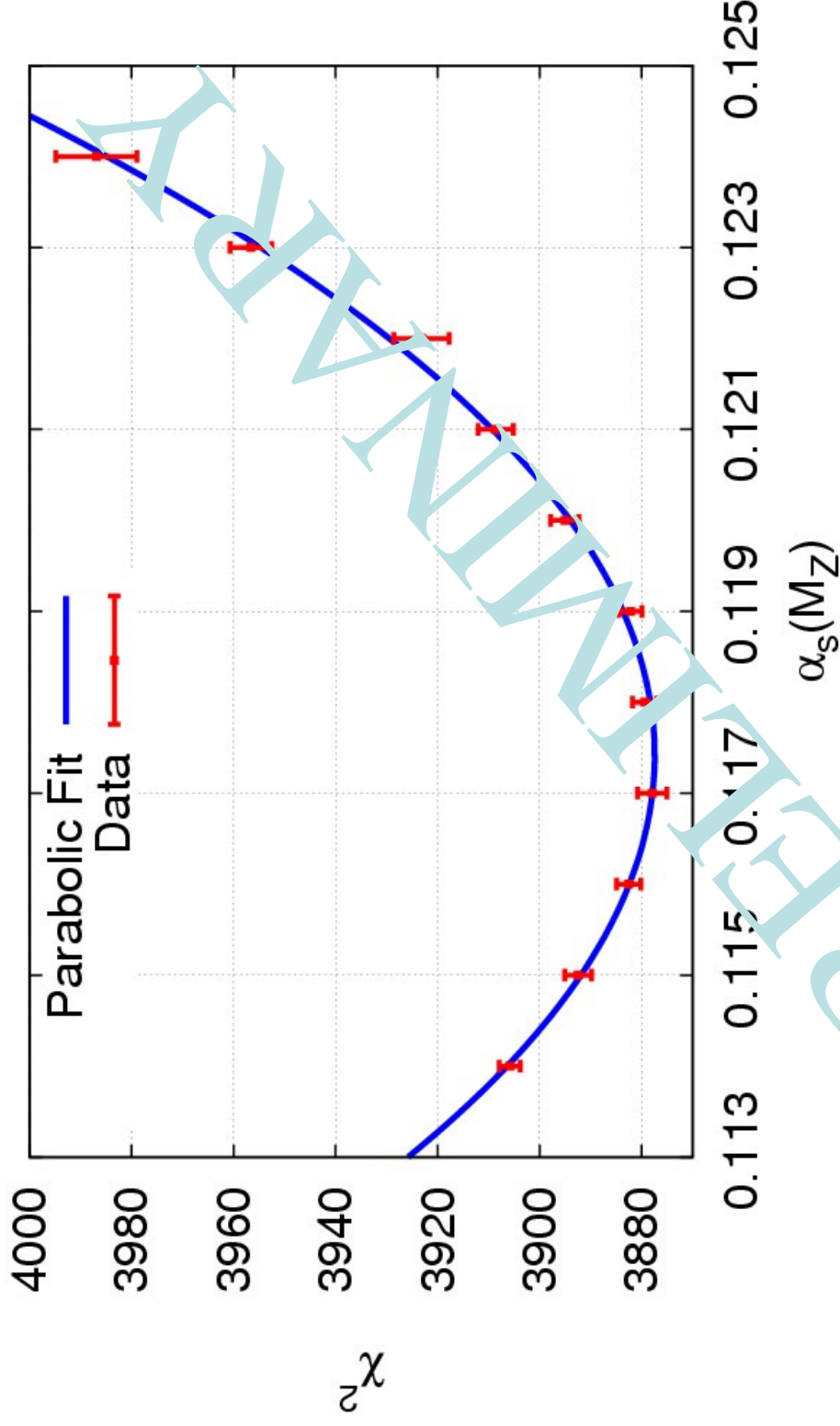
	$\alpha_s (M_Z)$	$\chi^2_{\text{par}}/N_{\text{dof}}$
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NLO determinations of  $\alpha_s (M_Z)$  from PDF Analyses



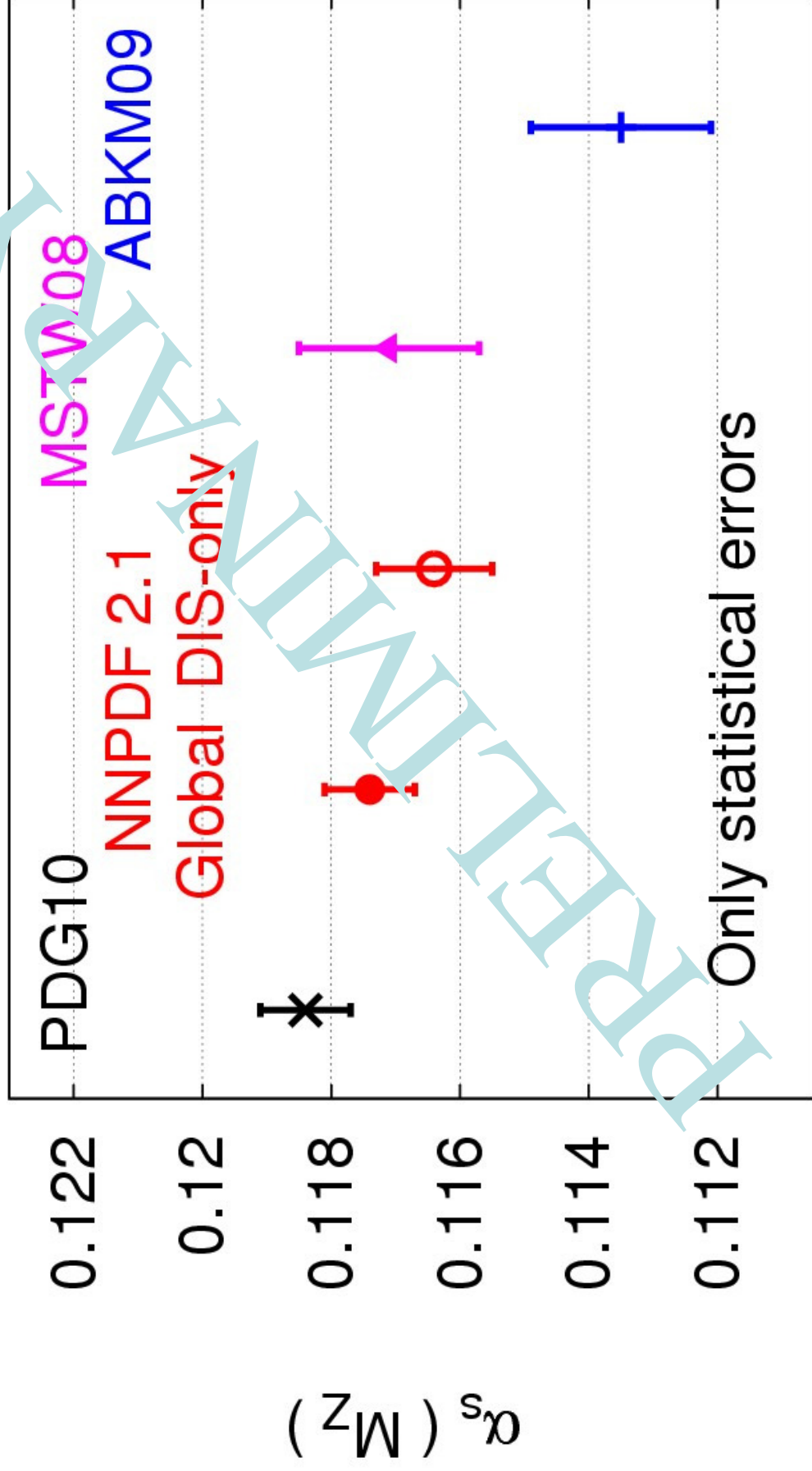
More flexible (NN)PDFs: more precise physics!

# NNPDF2.1 NNLO Global



	$\alpha_s(M_Z)$	$\chi^2_{\text{par}}/N_{\text{dof}}$
NNPDF2.1 NNLO	$0.1174 \pm 0.0006^{\text{exp}} \pm 0.0001^{\text{proc}}$	0.6
NNPDF2.1 NNLO DIS-only	$0.1164 \pm 0.0009^{\text{exp}} \pm 0.0002^{\text{proc}}$	1.1

# NNLO $\alpha_s (M_Z)$ from PDF Analyses





## Summary & Outlook

$$\text{NLO: } \alpha_s = 0.1191 \pm 0.0006$$

$$\text{NNLO: } \alpha_s = 0.1174 \pm 0.0006$$

Theory uncertainty:  $\sim 0.0017$  (conservative?)