

# Recent Progress in Matching and Merging

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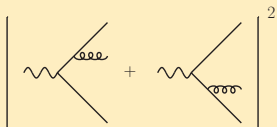
# Outline

- ① ME+PS: CKKW & MLM
- ② NLO+PS: POWHEG & MC@NLO
- ③ MENLOPS
- ④ Conclusions

# (NLO)ME vs. PS

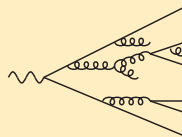
## Approaches to real emission corrections

### (NLO) Matrix Element



- + **Exact** to fixed order
- Perturbative series breaks down due to **large logarithms**

### Parton Shower



- + Resums logarithms to **all orders**
- Only **approximation** to real emission ME

## Combine Advantages $\Rightarrow$ $\text{ME} \otimes \text{PS}$ , $\text{NLO} \otimes \text{PS}$ , MENLOPS

- avoid double-counting by dividing phase space  $\Rightarrow Q_{\text{cut}}$
- **ME** to describe **hard radiation**, **PS** for **intrajet evolution**

# ME+PS: CKKW & MLM

- 1 ME+PS: CKKW & MLM
- 2 NLO+PS: POWHEG & MC@NLO
- 3 MENLOPS
- 4 Conclusions

# ME+PS: CKKW & MLM

$$\langle O \rangle = \int d\Phi_B B(\Phi_B) \left[ \Delta(t_0) O(\Phi_B) + \int d\Phi_{R|B} \mathcal{K}(t, z, \phi) \Delta(t) O(\Phi_R) \right]$$

- ordinary LO+PS restricted to soft emissions with  $Q < Q_{\text{cut}}$
- phase space  $Q > Q_{\text{cut}}$  filled by ME
- supplement Sudakov suppression  $\Delta(t)$  to recover unitarity at (N)LL level
- **preserves LO accuracy of every ME emission and LL accuracy of PS**
- PS Sudakov form factor  $\Delta(t) = \exp \left[ - \sum \int d\Phi_{R|B} \mathcal{K}(t, z, \phi) \right]$
- unitarity of PS violated at  $\mathcal{O}(\alpha_s)$  beyond (N)LL

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 & \underbrace{+ \int d\Phi_{R|B} \mathcal{K}(t, z, \phi) \Delta(t) \Theta(Q_{\text{cut}} - Q) O(\Phi_R)}_{\text{PS domain}} \\
 & \left. + \underbrace{\int d\Phi_{R|B} \frac{R(\Phi_R)}{B(\Phi_B)} \Delta(t) \Theta(Q - Q_{\text{cut}}) O(\Phi_R)}_{\text{ME domain}} \right]
 \end{aligned}$$

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# ME+PS: CKKW & MLM

## CKKW-like implementations

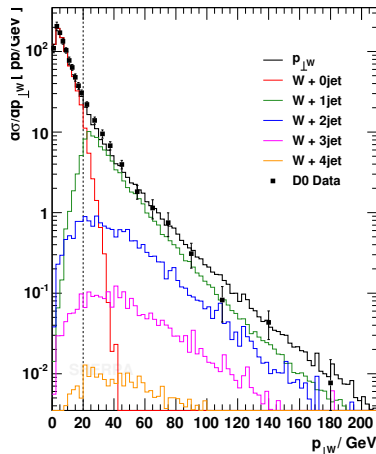
JHEP05(2009)053, JHEP11(2009)038, JHEP11(2001)063, JHEP08(2002)015, JHEP05(2002)046, JHEP07(2005)054

- direct implementation
- phase space separation via arbitrary parton-measure  
→ PS and ME treated alike
- Sudakov weight via vetoed shower
- truncated showering if  $Q$  and  $t$  differ

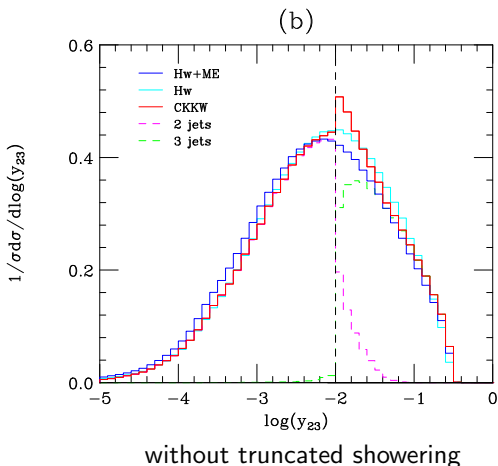
## MLM-like implementations

JHEP01(2007)013, NBP632(2002)343, JHEP02(2009)017

- geometric approximation
- phase space separation via  
→ parton-measure on ME multiplicitywise  
→ jet-measure on PS after full PS
- Sudakov weight via “jet matching”

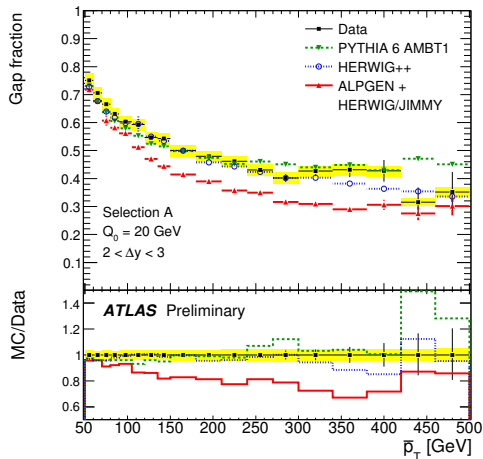


# Importance of truncated showering



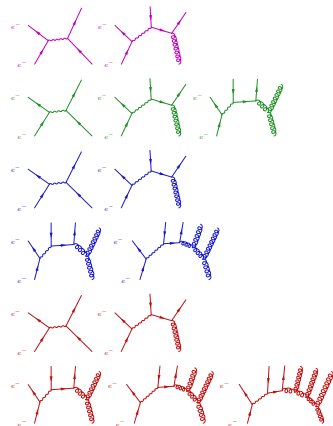
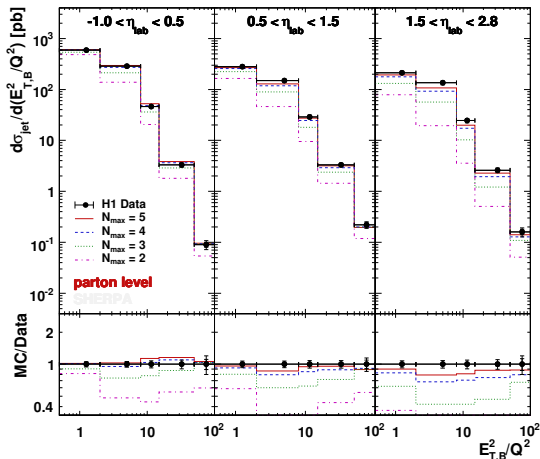
- truncated showering necessary to maintain logarithmic accuracy if separation measure deviates from evolution measure
- most prominent in HERWIG/HERWIG++:  
 $Q_{\text{cut}} \sim y_{ij}$  vs.  $t \sim \theta^2$
- studied by [Hamilton, Richardson, Tully] JHEP11(2009)038

# Importance of truncated showering



- [ATLAS-CONF-2011-038](#)
- gap fraction sensitive to resummation effects
- resummation should be identical for HERWIG and ALPGEN+HERWIG
- proper phase space separation crucial  
 → neither holes nor doubly filled regions
- truncated showering crucial

# SHERPA – DIS



$\Rightarrow$  higher-order MEs needed to open radiative phase space  
 data from H1 [PLB542\(2002\)193-206](#)

# NLO+PS: POWHEG & MC@NLO

- ① ME+PS: CKKW & MLM
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# MC@NLO Algorithm

$$\langle O \rangle = \int d\Phi_B B(\Phi_B) \left[ \Delta(t_0) O(\Phi_B) + \sum \int_{t_0} d\Phi_{R|B} \mathcal{K}(t, z, \phi) \Delta(t) O(\Phi_R) \right] \\ + \int d\Phi_R [R(\Phi_R) - R^{(\text{PS})}(\Phi_R)] O(\Phi_R)$$

- [Frixione, Webber] JHEP06(2002)029
  - PS approximation  $R^{(\text{PS})} = \sum B \cdot \mathcal{K}$
  - modified subtraction with  $\bar{B}^{(\text{PS})} = B + V + \int d\Phi_{R|B} R^{(\text{PS})}$   
→ parton shower needs to be correct in the soft limit
  - resums exactly as the parton shower
  - implemented for HERWIG/HERWIG++ and PYTHIA showers  
[Frixione et al.] JHEP01(2011)053, [Torelli et al.] JHEP04(2010)110
  - correction events to restore NLO accuracy
- ⇒ preserves both NLO and (N)LL accuracy

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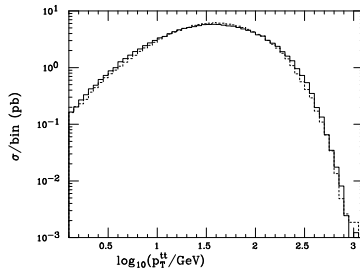
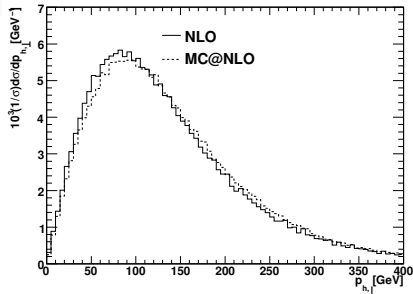
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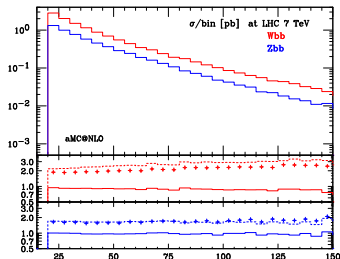
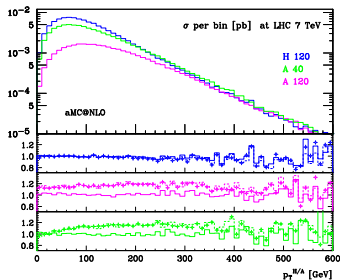
## MC@NLO

IPROD	IV	IL <sub>1</sub>	IL <sub>2</sub>	Spin	Process
-1350-IL				✓	$H_1 H_2 \rightarrow (Z/\gamma^*) \rightarrow h_u h_u + X$
-1360-IL				✓	$H_1 H_2 \rightarrow (Z \rightarrow \nu_h \bar{\nu}_h) + X$
-1370-IL				✓	$H_1 H_2 \rightarrow (\gamma^*) \rightarrow h_u h_u + X$
-1460-IL				✓	$H_1 H_2 \rightarrow (W^+ \rightarrow \bar{l}_i^+ \nu_l) + X$
-1470-IL				✓	$H_1 H_2 \rightarrow (W^- \rightarrow \bar{\nu}_l l_i) + X$
-1396				✓	$H_1 H_2 \rightarrow \gamma^* (\rightarrow \sum_{f,j} f_j \bar{f}_j) + X$
-1397				✗	$H_1 H_2 \rightarrow Z^0 + X$
-1497				✗	$H_1 H_2 \rightarrow W^+ + X$
-1498				✗	$H_1 H_2 \rightarrow W^- + X$
-1600-ID					$H_1 H_2 \rightarrow H^0 + X$
-1705					$H_1 H_2 \rightarrow b\bar{b} + X$
-1706		7	7	✗	$H_1 H_2 \rightarrow t\bar{t} + X$
-2000-IC		7		✗	$H_1 H_2 \rightarrow l\bar{l} + X$
-2001-IC		7		✗	$H_1 H_2 \rightarrow t + X$
-2004-IC		7		✗	$H_1 H_2 \rightarrow t + X$
-2030		7	7	✗	$H_1 H_2 \rightarrow tW^+ + X$
-2031		7	7	✗	$H_1 H_2 \rightarrow tW^+ + X$
-2034		7	7	✗	$H_1 H_2 \rightarrow tW^- + X$
-2040		7	7	✗	$H_1 H_2 \rightarrow tH^+ + X$
-2041		7	7	✗	$H_1 H_2 \rightarrow tH^+ + X$
-2044		7	7	✗	$H_1 H_2 \rightarrow tH^- + X$
-2600-ID	1	7		✗	$H_1 H_2 \rightarrow H^0 W^+ + X$
-2600-ID	1			✓	$H_1 H_2 \rightarrow H^0 (W^+ \rightarrow \bar{l}_i^+ \nu_l) + X$
-2600-ID	-1	7		✗	$H_1 H_2 \rightarrow H^0 W^- + X$
-2600-ID	-1			✓	$H_1 H_2 \rightarrow H^0 (W^- \rightarrow \bar{\nu}_l l_i) + X$
-2700-ID	0	7		✗	$H_1 H_2 \rightarrow H^0 Z + X$
-2700-ID	0			✓	$H_1 H_2 \rightarrow H^0 (Z \rightarrow \bar{l}_i l_i) + X$
-2850		7	7	✗	$H_1 H_2 \rightarrow W^+ W^- + X$
-2860		7	7	✗	$H_1 H_2 \rightarrow Z^0 Z^0 + X$
-2870		7	7	✗	$H_1 H_2 \rightarrow W^+ Z^0 + X$
-2880		7	7	✗	$H_1 H_2 \rightarrow W^- Z^0 + X$
-1706		i	j	✓	$H_1 H_2 \rightarrow (t \rightarrow) b_i f_j f_j' (t \rightarrow) b_i f_j f_j' + X$
-2000-IC		i		✓	$H_1 H_2 \rightarrow (t \rightarrow) b_i f_j f_j' (t \rightarrow) b_i f_j f_j' + X$
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-2030		i	j	✓	$H_1 H_2 \rightarrow (t \rightarrow) b_i f_j f_j' (W^- \rightarrow) f_j f_j'$ $(t \rightarrow) b_i f_j f_j' (W^+ \rightarrow) f_j f_j' + X$
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-2040		i		✓	$H_1 H_2 \rightarrow (t \rightarrow) b_i f_j f_j' H^- /$ $(t \rightarrow) b_i f_j f_j' H^+ + X$
-2041		i		✓	$H_1 H_2 \rightarrow (t \rightarrow) b_i f_j f_j' H^+ + X$
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-2870		i	j	✓	$H_1 H_2 \rightarrow (W^+ \rightarrow) \bar{l}_i^+ \nu_l (Z^0 \rightarrow) \bar{l}_i^+ l_j + X$
-2880		i	j	✓	$H_1 H_2 \rightarrow (W^+ \rightarrow) \bar{l}_i^+ \nu_l (Z^0 \rightarrow) \bar{l}_i^+ l_j + X$



# aMC@NLO

- automated version of MC@NLO
- uses MADGRAPH/MADLOOP framework  
[Alwall et al.] JHEP09(2007)028  
[Frederix et al.] JHEP05(2011)044
- results published for  
 $pp \rightarrow ttH$   
[Frederix et al.] PLB 701(2011)427-433  
and  $pp \rightarrow V + b\bar{b}$   
[Frederix et al.] arXiv:1106.6019
- code not public yet



# POWHEG Algorithm

$$\langle O \rangle = \int d\Phi_B \bar{B}(\Phi_B) \left[ \Delta^{(\text{ME})}(t_0) O(\Phi_B) + \sum \int_{t_0} d\Phi_{R|B} \frac{R(\Phi_R)}{B(\Phi_B)} \Delta^{(\text{ME})}(t) O(\Phi_R) \right]$$

- [Nason] JHEP11(2004)040, [Frixione et al.] JHEP11(2007)070
  - NLO event weight  $\bar{B} = B + V + \int d\Phi_{R|B} R$  defined on  $\Phi_B$   
→ wrong observable dependence on  $R(\Phi_R)$
  - POWHEG Sudakov  $\Delta^{(\text{ME})}(t) = \exp \left[ - \sum \int_t d\Phi_{R|B} \frac{R(\Phi_R)}{B(\Phi_B)} \right]$   
→ intricate cancellation to correct observable dependence on  $R(\Phi_R)$
  - $\Delta^{(\text{ME})} = \Delta^{(\text{PS})}$  at LL level  
→ resums as PS if interface ensures continuous evolution in phase space and colour space  
→ importance of truncated showering [Nason] JHEP11(2004)040
- ⇒ preserves both NLO and (N)LL accuracy

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## Ambiguities/freedom/choices in the exponentiation

- divide  $R(\Phi_R)$  into singular and regular [Alioli et al.] JHEP07(2008)060

$$R(\Phi_R) = R^{(s)}(\Phi_R) + R^{(r)}(\Phi_R)$$

then

$$\langle O \rangle = \int d\Phi_B \bar{B}^{(s)}(\Phi_B) \left[ \Delta_{(s)}^{(ME)}(t_0) O(\Phi_B) + \sum \int_{t_0} d\Phi_{R|B} \frac{R^{(s)}(\Phi_R)}{B(\Phi_B)} \Delta_{(s)}^{(ME)}(t) O(\Phi_R) \right] \\ + \int d\Phi_R R^{(r)}(\Phi_R) O(\Phi_R)$$

with  $\bar{B}^{(s)} = B + V + \int d\Phi_{R|B} R^{(s)}$

and  $\Delta_{(s)}^{(ME)}(t) = \exp \left[ - \sum \int_t d\Phi_{R|B} \frac{R^{(s)}(\Phi_R)}{B(\Phi_B)} \right]$

- different  $K$ -factors for reweighted PS, different exponentiation behaviour  
→ beyond NLO and (N)LL accuracy
- specific choice:

$$R^{(s)}(\Phi_R) = R^{(PS)}(\Phi_R) \quad \Rightarrow \quad \text{MC@NLO [Frixione, Webber] JHEP06(2002)029}$$

# POWHEG-BOX – toolkit for POWHEG implementations

Toolkit to implement new process given

- Born matrix elements, flavour structures & phase space
- colour and spin correlated Born matrix elements  $B_{ij}$  and  $B_{\mu\nu}$
- virtual matrix elements
- real matrix elements and flavour structures
- Born colour structures in  $N_c \rightarrow \infty$

⇒ internal FKS subtraction and real emission phase space integration

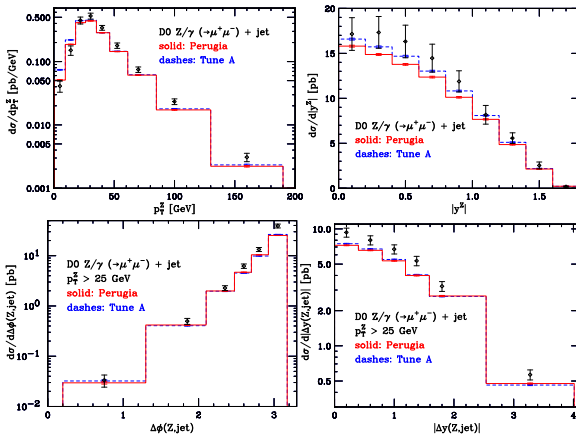
⇒ generates radiation using POWHEG Sudakov form factor

## Wide range of processes

- $V, VV, Q\bar{Q}, Wb\bar{b}, W^+W^+jj, H(\text{GF}, \text{VBF}),$  single-top
- $Vj,$  dijets
- $t\bar{t}H, t\bar{t}j$
- interface to HERWIG/PYTHIA  
→ truncated showering needed but not available



# POWHEG-BOX – $pp \rightarrow \ell^+ \ell^- j$



$pp \rightarrow Z + j$

$D0 Z + j$  analyses

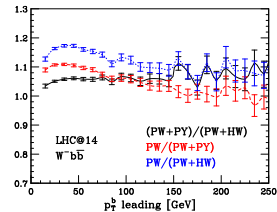
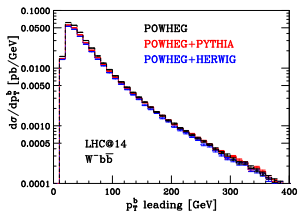
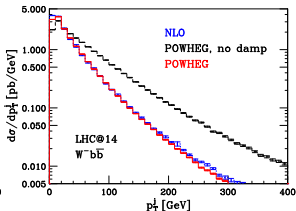
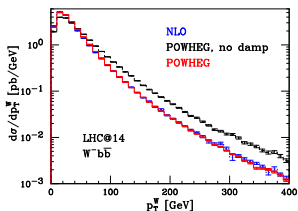
[Phys.Lett.B669\(2008\)278-286](#)

[Phys.Lett.B682\(2010\)370-380](#)

good description of data

some dependence on  
PYTHIA tune

# POWHEG-BOX – $pp \rightarrow Wb\bar{b}$



$pp \rightarrow Wb\bar{b}$

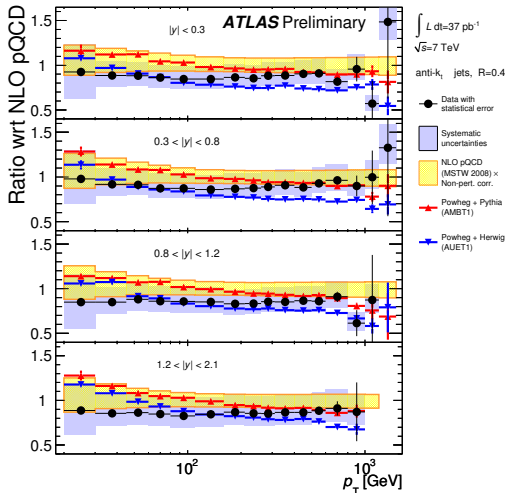
large ratio  $\bar{B}/B$

→ large effect of choice  
what to exponentiate  
and what to generate  
explicitly

small deviation of  
POWHEG-BOX ⊗ HERWIG  
& POWHEG-BOX ⊗ PYTHIA

# POWHEG-BOX – dijets

ATLAS-CONF-2011-047:



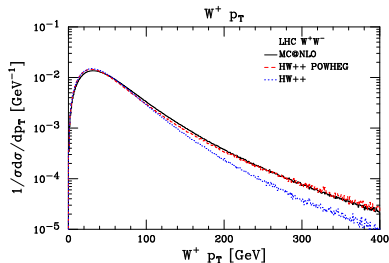
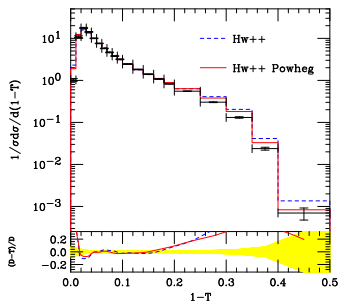
- $p_{\perp,j}$  supposedly described at NLO $\otimes$ LL
- $\sim 20\%$  difference between using HERWIG or PYTHIA for parton showering

Issues for logarithmic accuracy:

- truncated showering implemented neither for HERWIG or PYTHIA interfaces  $\rightarrow$  especially important for HERWIG's angular ordering
- consistent settings for PDFs,  $\mu_R$  and  $\mu_F$  scales, etc.
- no conclusive answers so far

# POWHEG in HERWIG++

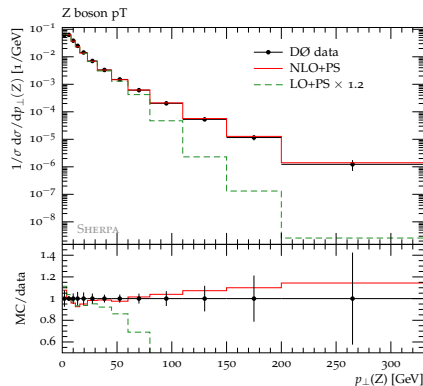
- Processes:
  - $V, VV, H(\text{GF}, \text{VBF}), VH$
  - $ee \rightarrow q\bar{q}$ , DIS
  - $H \rightarrow q\bar{q}$  decay
- includes truncated showering



# POWHEG – Automation in SHERPA

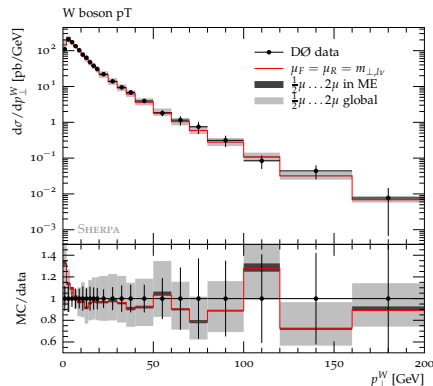
- [Höhe,Krauss,MS,Siegert] JHEP04(2011)024
- reinterpret POWHEG as ME reweighted PS with local  $K$ -factor
- NLO event weight  $\bar{B} = B + V + I + \int d\Phi_{R|B} [R - S]$ 
  - **B**orn, **R**Real from automated tree-level generators
  - automated phase space
  - **V**irtual e.g. via Binoth Les Houches Accord CPC181(2010)1612  
→ for results here BLACKHAT & MCFM libraries interfaced
  - **I**ntegrated/**S**ubtraction terms from automated implementation of Catani-Seymour subtraction terms EPJC53(2008)501
  - dedicated automated CS-like phase-space for  $R - S$  integral
- correct PS to ME via weight  $w(\Phi_R) = R(\Phi_R)/R^{(PS)}(\Phi_R)$   
→ alleviated by good approximation of CSSHOWER++ JHEP03(2008)038  
→ truncated showering not needed
- included since SHERPA-1.2.3 (Nov '10)

# SHERPA – inclusive $W/Z$ production at Tevatron



Data from DØ :

Phys.Lett.B693(2010)522-530

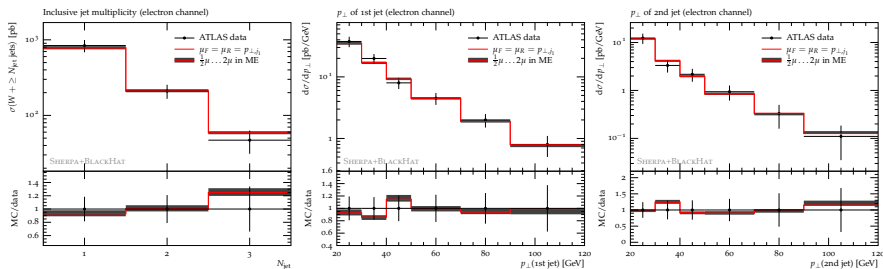


Data from DØ :

Phys.Lett.B513(2001)292-300

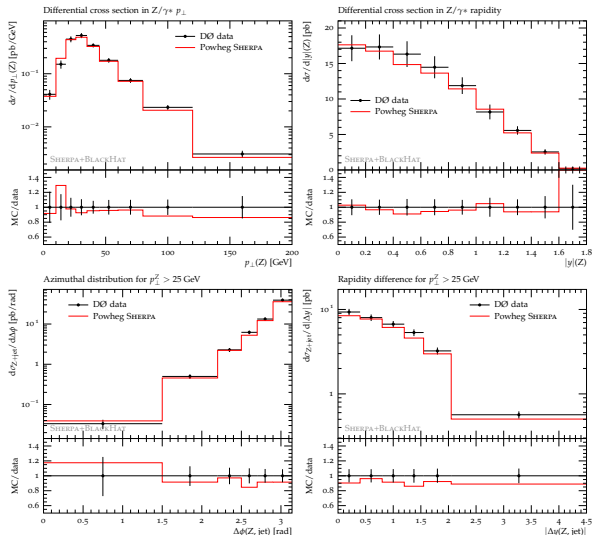
# SHERPA – Non-trivial colour structures – $pp \rightarrow Wj$

- POWHEG method sufficiently general
- Subtraction and PS need to have identical phase space maps
- $N_c \rightarrow \infty$  in parton shower vs.  $N_c = 3$  in matrix elements
  - no issue for  $O(\Phi_R)$  if parton shower can fill full phase space
  - $O(\Phi_B)$  formally at LC-NLO $\otimes$ (N)LL accuracy



inclusive jet multiplicity and  $p_{\perp}$  of 1st & 2nd jet in  $W$ +jets events,  
 data from ATLAS [Phys.Lett.B698\(2011\)325-345](#)

# SHERPA – $p\bar{p} \rightarrow Zj$ at Tevatron



$$p\bar{p} \rightarrow Z + j$$

DØ  $Z + j$  analyses

[Phys.Lett.B669\(2008\)278-286](#)

[Phys.Lett.B682\(2010\)370-380](#)

LC-NLO $\otimes$ (N)LL  
accuracy



# MENLOPS

- ① ME+PS: CKKW & MLM
- ② NLO+PS: POWHEG & MC@NLO
- ③ MENLOPS**
- ④ Conclusions

# Multijet Merging with NLO MEs – MENLOPS

$$\begin{aligned}
 \langle O \rangle = & \int d\Phi_B \bar{B}(\Phi_B) \left[ \Delta^{(\text{ME})}(t_0) O(\Phi_B) \right. \\
 & + \overbrace{\int d\Phi_{R|B} \frac{R(\Phi_R)}{B(\Phi_B)} \Delta^{(\text{ME})}(t) \Theta(Q_{\text{cut}} - Q) O(\Phi_R)}^{\text{POWHEG domain}} \\
 & \left. + \underbrace{\int d\Phi_{R|B} \frac{R(\Phi_R)}{B(\Phi_B)} \Delta^{(\text{PS})}(t) \Theta(Q - Q_{\text{cut}}) O(\Phi_R)}_{\text{ME domain}} \right]
 \end{aligned}$$

- [Hamilton,Nason] JHEP06(2010)039, [Höche,Krauss,MS,Siegert] arXiv:1009.1127
- POWHEG domain restricted to soft emissions  $Q < Q_{\text{cut}}$   
 $\Rightarrow$  **NLO accuracy preserved for inclusive observables**
- $\text{ME} \otimes \text{PS}$  used for hard emission & higher order emissions  
 $\Rightarrow$  **preserves LO accuracy of every ME emission & LL accuracy of PS**
- higher order emissions receive **local** K-factor  $\frac{\bar{B}(\Phi_B)}{B(\Phi_B)}$
- inherits unitarity violation from  $\text{ME} \otimes \text{PS}$   
 $\rightarrow$  pushed to  $\mathcal{O}(\alpha_s^2)$  beyond (N)LL

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 \end{aligned}$$

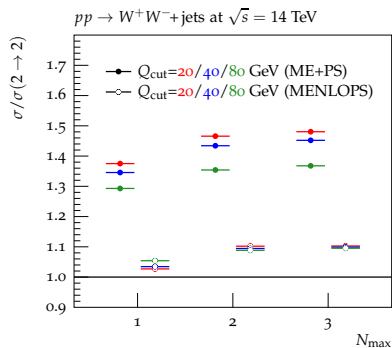
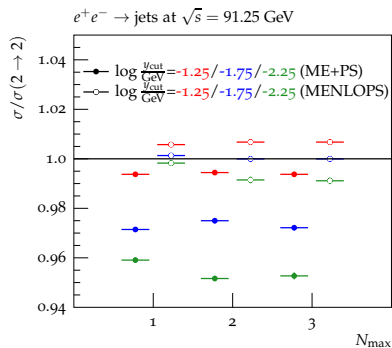
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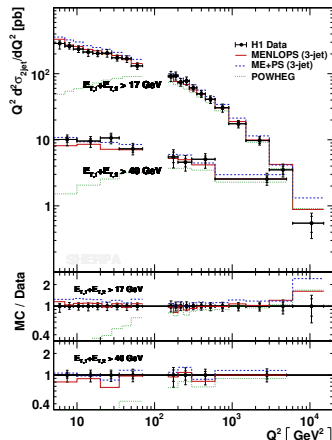
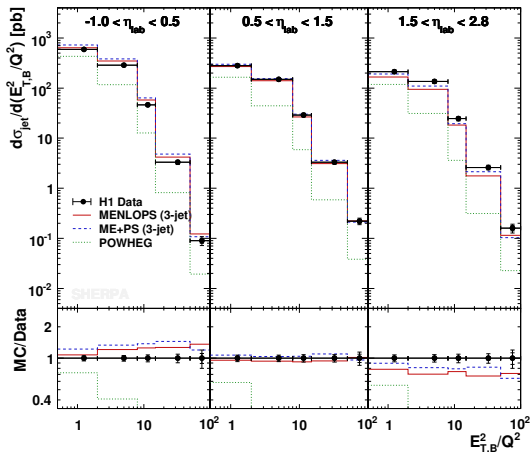
# MENLOPS – Unitarity violations



$\Rightarrow$  reduced unitarity violation

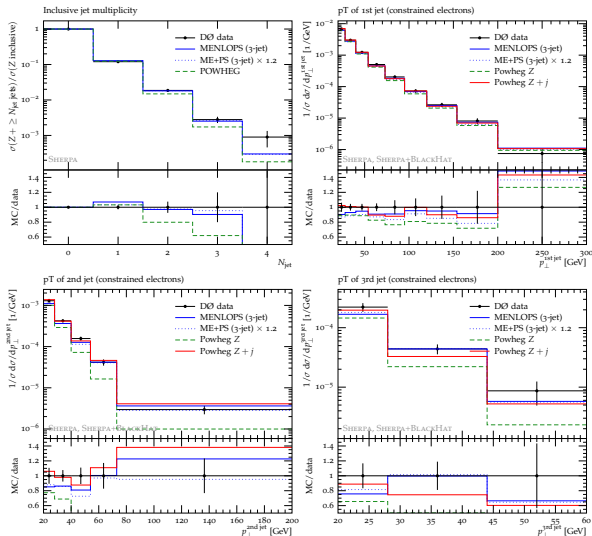
$\mathcal{O}(\alpha_s)$  and beyond (N)LL for ME $\otimes$ PS  
 $\mathcal{O}(\alpha_s^2)$  and beyond (N)LL for MENLOPS

# SHERPA – DIS



⇒ good description, data from H1 [PLB542\(2002\)193-206](#), [EPJC19\(2001\)289-311](#)

# SHERPA - $p\bar{p} \rightarrow \ell^+ \ell^- + X$



Data from DØ :

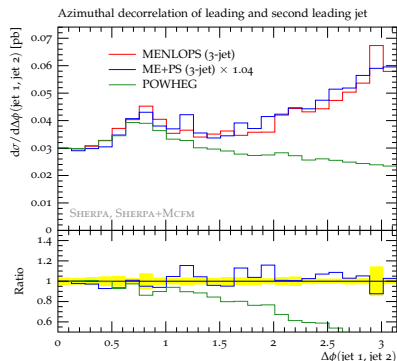
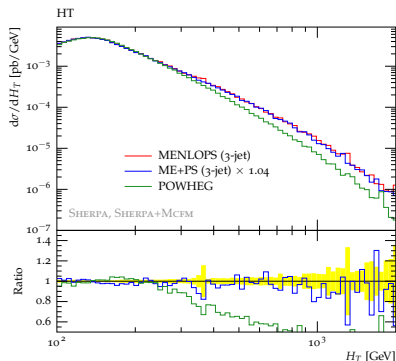
[Phys.Lett.B658\(2008\)112-119](#)

[Phys.Lett.B678\(2009\)45-54](#)

POWHEG and MENLOPS  
agree well on  $p_{\perp}$  of  
hardest jet

MENLOPS superior for  
2nd and 3rd jet

# SHERPA – $pp \rightarrow W^+W^- + X$



⇒ considerable corrections from higher-order tree-level matrix elements



# Conclusions

- $ME \otimes PS$  works well for shapes, but needs K-factor
  - truncated showering essential to recover PS resummation
- MC@NLO & POWHEG reproduce NLO cross section and shape of first emission, but additional hard jets at (N)LL only
- various implementations with various degrees of automation
- MENLOPS combines  $ME \otimes PS$  and POWHEG
  - ⇒ NLO accuracy in core process
  - ⇒ multijet observables as in  $ME \otimes PS$
- $ME \otimes PS$ , POWHEG & MENLOPS automated (except V) in SHERPA framework
  - ⇒ for trivial colour structures included in current release v1.3.0
  - ⇒ for new process need function  $V(\Phi_B, \mu_R) \rightarrow$  (BLHA) interface
- also want NLO accuracy in higher order emission in inclusive sample
  - ⇒ multijet emission dependent observables described at NLO
- crucial to recover desired accuracies for arbitrary observables
  - ... working on it

# Available processes\*

Process	POWHEG			MC@NLO	
	POWHEG-BOX	HERWIG++	SHERPA	MC@NLO	aMC@NLO
$e^+e^- \rightarrow jj$	X	✓	✓	X	X
DIS	X	✓	✓	✓	X
$pp \rightarrow W/Z$	✓	✓	✓	✓	X
$pp \rightarrow H$ (GF)	✓	✓	✓	✓	X
$pp \rightarrow V + H$	X	✓	✓	✓	X
$pp \rightarrow VV$	X	✓	✓	✓	X
VBF	✓	✓	in prep.	X	X
$pp \rightarrow Q\bar{Q}$	✓	X	X	✓	X
$pp \rightarrow Q\bar{Q} + j$	✓	X	X	X	X
single-top	✓	X	X	✓	X
$pp \rightarrow V + j$	✓	X	in prep.	X	X
$pp \rightarrow V + jj$	in prep.	X	in prep.	X	X
$pp \rightarrow H + j$ (GF)	X	X	in prep.	X	X
$pp \rightarrow H + t\bar{t}$	✓	X	X	X	✓
$pp \rightarrow W^+W^+jj$	✓	X	X	X	X
$pp \rightarrow V + b\bar{b}$	✓	X	in prep.	X	✓
diphotons	?	✓	in prep.	X	X
dijets	✓	X	in prep.	X	X

\* Table includes SM processes presented so far. Automated codes and toolkits can, in principle, be used for any process.

Thank you.

## Backup: ME $\otimes$ PS Merging – Scales

**Divide phase space using jet measure  $Q_{\text{cut}}$ :**

→ emissions with  $Q > Q_{\text{cut}}$  by ME

→ emissions with  $Q < Q_{\text{cut}}$  by PS

**Shower on top of higher order ME:**

**Problem:** ME only gives final state,  
no history as PS input

**Solution:** Backward clustering  
(inverted probabilistic PS splittings)

⇒ **ME final state with branching history and PS starting scale  $\mu$  and branching scales  $t_i$**

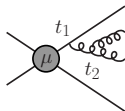
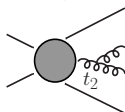
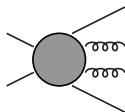
$$\alpha_s^{k+n}(\mu_{\text{eff}}) = \alpha_s^k(\mu) \alpha_s(t_1) \cdots \alpha_s(t_n)$$

**Veto PS emissions with  $Q > Q_{\text{cut}}$**

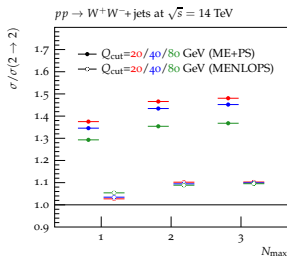
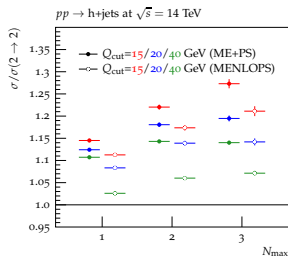
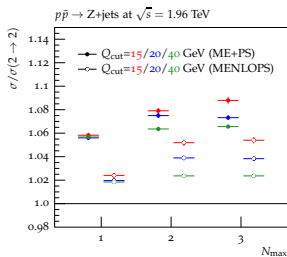
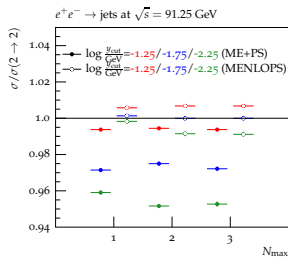
→ Reject event → Sudakov suppression

If  $t \neq Q^2$  then truncated shower necessary

Scales:



# Backup: Unitarity Violation in MENLOPS & ME+PS



Formally of  $\mathcal{O}(\alpha_s^2)$  in  
MENLOPS

$\rightarrow N_{\text{max}} = 1$  shows size  
of unitarity violation in  
MENLOPS alone

Due to mismatch in  
non-logarithmic terms in  
ME and PS in real  
emission correction and  
Sudakov

Indicates potential size  
of higher order  
corrections