

Jet Substructure and Boosted Objects



Peter Loch
University of Arizona
Tucson, Arizona
USA





Motivation

High p_T (fat) jets as search tool at LHC

Jet substructure techniques

Jet grooming – filtering, trimming, pruning

Experimental limitations

Detector effects on jet signals

First results from CMS & ATLAS

First hints on reconstruction quality for internal jet variables useful for substructure analysis

Disclaimer

This is not an in-depth review talk – focus on experimental aspects and concerns/challenges to be addressed in the very near future

First indications look promising but there is still a lot to learn concerning systematic uncertainties and resolution effects



More from Jets: Mass and Substructure



Particle flow inside a jet hints to source

Jet can be a discovery tool by itself

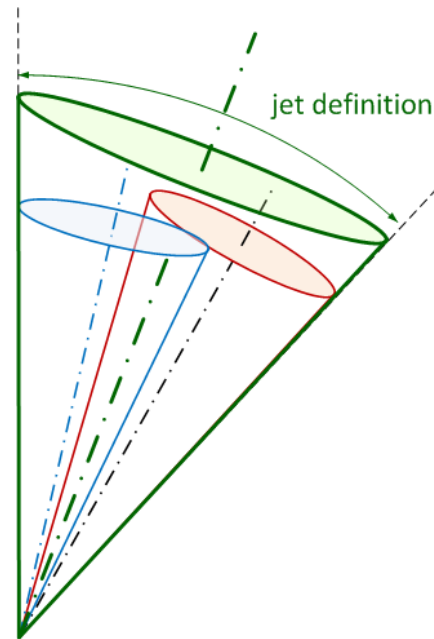
In particular most interesting for boosted (new) heavy particle like Kaluza-Klein excitations

But also interesting for Standard Model particles like boosted top quarks

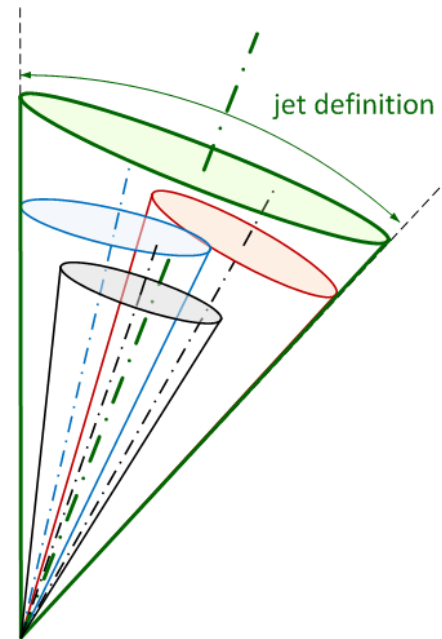
Usefulness depends on the ability to resolve decay structure

E.g., 2-prong (like W) or 3-prong (top) decays

Resolution scale given by mass of particle (or by particle hypothesis) – to be reflected with detector capabilities



2 – prong decay inside reconstructed jet, e.g. from $W \rightarrow q\bar{q}$ (SM) or heavy new object like $\phi \rightarrow gg$ or $Z' \rightarrow q\bar{q}$ (BSM)



3 – prong decay inside reconstructed jet, e.g. from $t \rightarrow q\bar{q}b$ (SM) or heavy new object like $\phi_{KK} \rightarrow Q\bar{Q}b + X$ or $t' \rightarrow q\bar{q}b$ (BSM)



Observables and tools

Single jet mass

Mass generated by four-momentum recombination should reflect heavy source
Scales proportional to p_T for light quark or gluon jet

Subject to severe detector effects

Lateral energy spread by individual particle cascades reduces single jet mass resolution

Calorimeter signal definition choices on top of shower spread can enhance or reduce sensitivity to in-jet particle flow and thus improve or worsen single jet mass resolution

$$\begin{pmatrix} E_{\text{jet}} \\ \vec{p}_{\text{jet}} \end{pmatrix} = \begin{pmatrix} \sum_{\text{constituents}} E_{\text{constituent}} \\ \sum_{\text{constituents}} \vec{p}_{\text{constituent}} \end{pmatrix} \Rightarrow m_{\text{jet}} = \sqrt{E_{\text{jet}}^2 - |\vec{p}_{\text{jet}}|^2}$$

mass of gluon/light quark jets:

LO 1-parton jets have vanishing mass

NLO 2-parton configurations at given p_{jet} generate average invariant jet mass:

$$\langle m_{\text{jet}}^2 \rangle_{\text{NLO}} \approx \bar{C} \left(p_{\text{jet}} / \sqrt{s} \right) \alpha_s \left(p_{\text{jet}} / 2 \right) p_{\text{jet}}^2 R_{\text{cone}}^2$$

with:

$\bar{C} \left(p_{\text{jet}} / \sqrt{s} \right)$ pre-function of magnitude $\mathcal{O}(1)$ (absorbes color charges and pdf, slowly decreases with rising p_{jet})

$\alpha_s \left(p_{\text{jet}} / 2 \right)$ strong coupling at scale $\mu = p_{\text{jet}} / 2$

\Rightarrow expect linear mass in NLO to scale with p_{jet} :

$$\sqrt{\langle m_{\text{jet}}^2 \rangle_{\text{NLO}}} \approx \sqrt{\bar{C} \alpha_s} p_{\text{jet}} R_{\text{cone}}$$

rule of thumb at $\sqrt{s} = 7 \text{ TeV}$:

$$\sqrt{\langle m_{\text{jet}}^2 \rangle_{\text{NLO}}} \approx (0.1 - 0.2) \cdot p_{\text{jet}} R_{\text{cone}}$$



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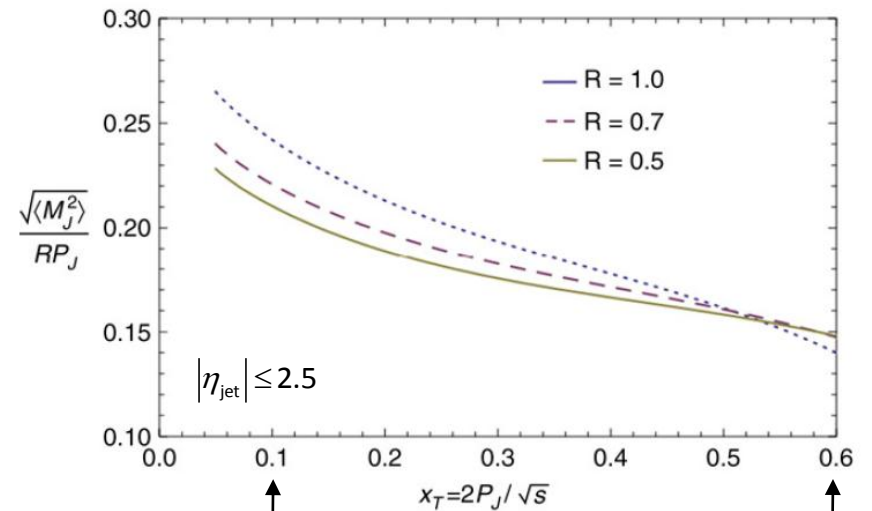
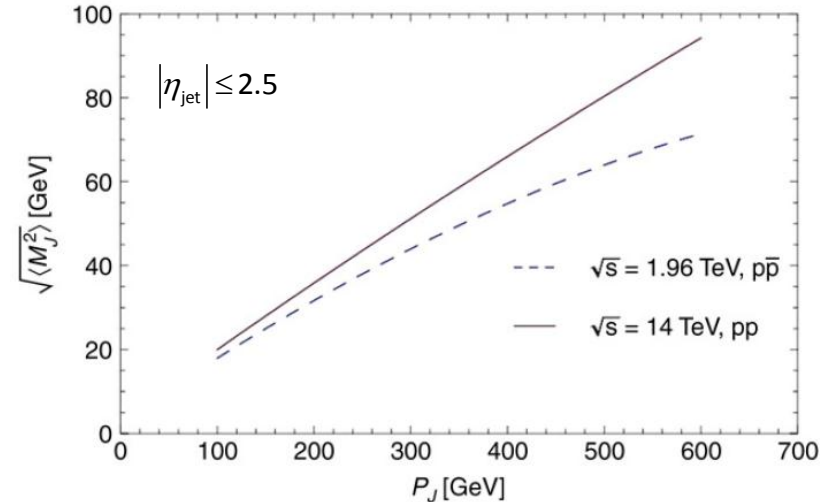
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S.D.Ellis, J.Huston, K.Hatakeyama, P.Loch, and M.Tönnemann,
*Prog.Part.Nucl.Phys.***60** 484-551 (2008)

NLO Jet Mass Calculations



$p_{T,\text{jet}}^{\text{min}} \approx 115$ GeV \longrightarrow $p_{T,\text{jet}}^{\text{min}} \approx 685$ GeV

$p_{\text{jet}} = 700$ GeV \longrightarrow $p_{\text{jet}} = 4.2$ TeV



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- requires good reconstruction of particle flow in jet by detector signal \rightarrow depends on chosen calorimeter signal definition, e.g. test

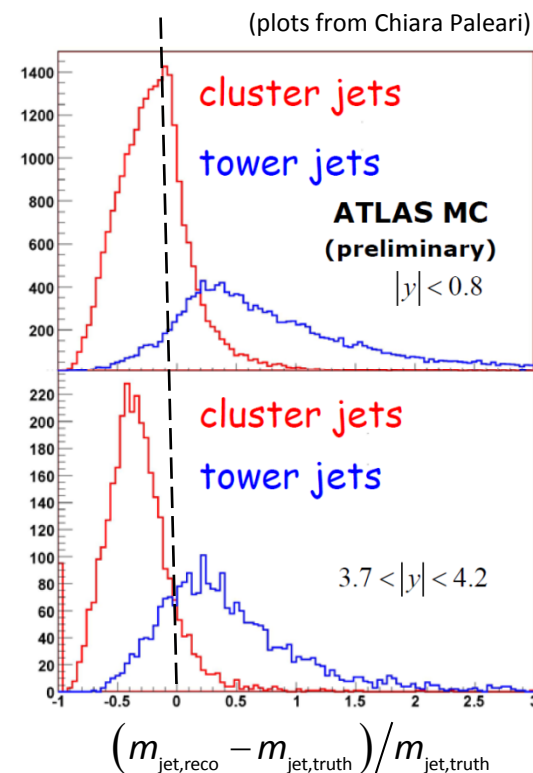
$$\frac{m_{\text{jet,reco}} - m_{\text{jet,truth}}}{m_{\text{jet,truth}}}$$

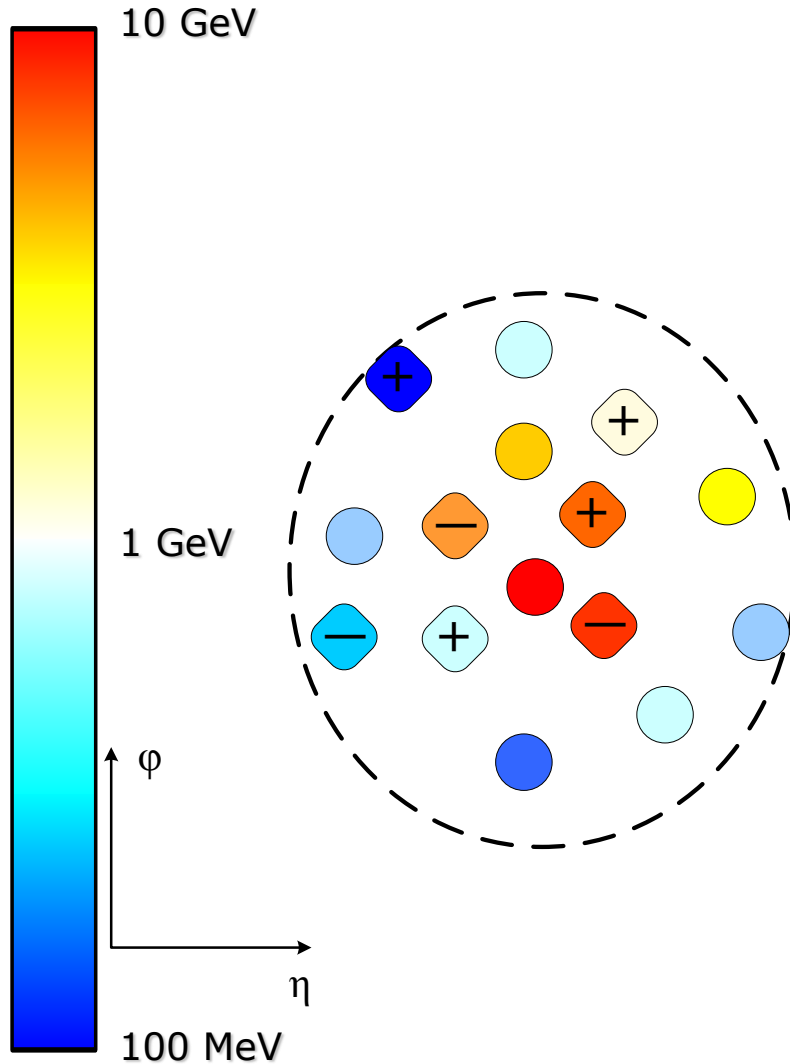
for matching truth and

calorimeter jets

- plot on the right shows the spectrum of this relative mass difference for simulated QCD di-jets (kT, $R = 0.6$) in ATLAS

(old plot, educational purpose only!)





Change of composition

Radiation and decay inside detector volume
 "Randomization" of original particle content

Defocusing changes shape in lab frame

Charged particles bend in solenoid field

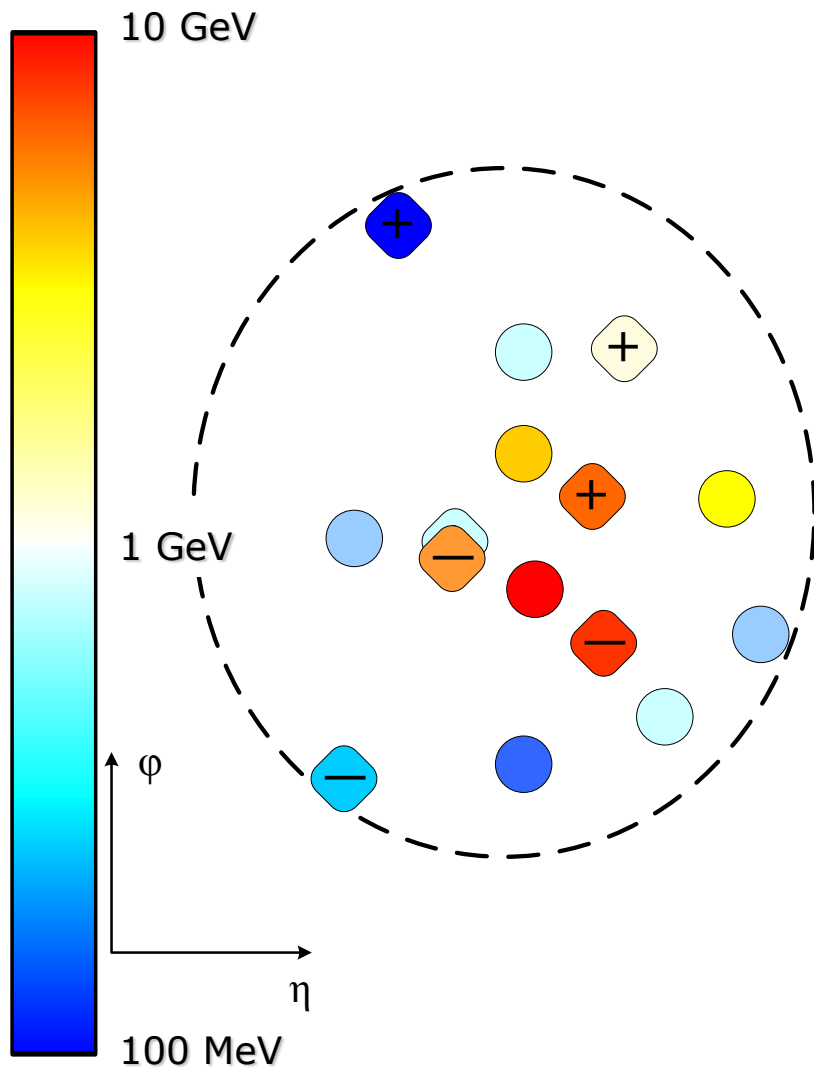
Attenuation changes energy

Total and partial loss of soft charged particles in magnetic field

Partial and total energy loss of charged and neutral particles in inactive upstream material

Hadronic and electromagnetic cascades in calorimeters

Distribute energy spatially
 Lateral particle shower overlap



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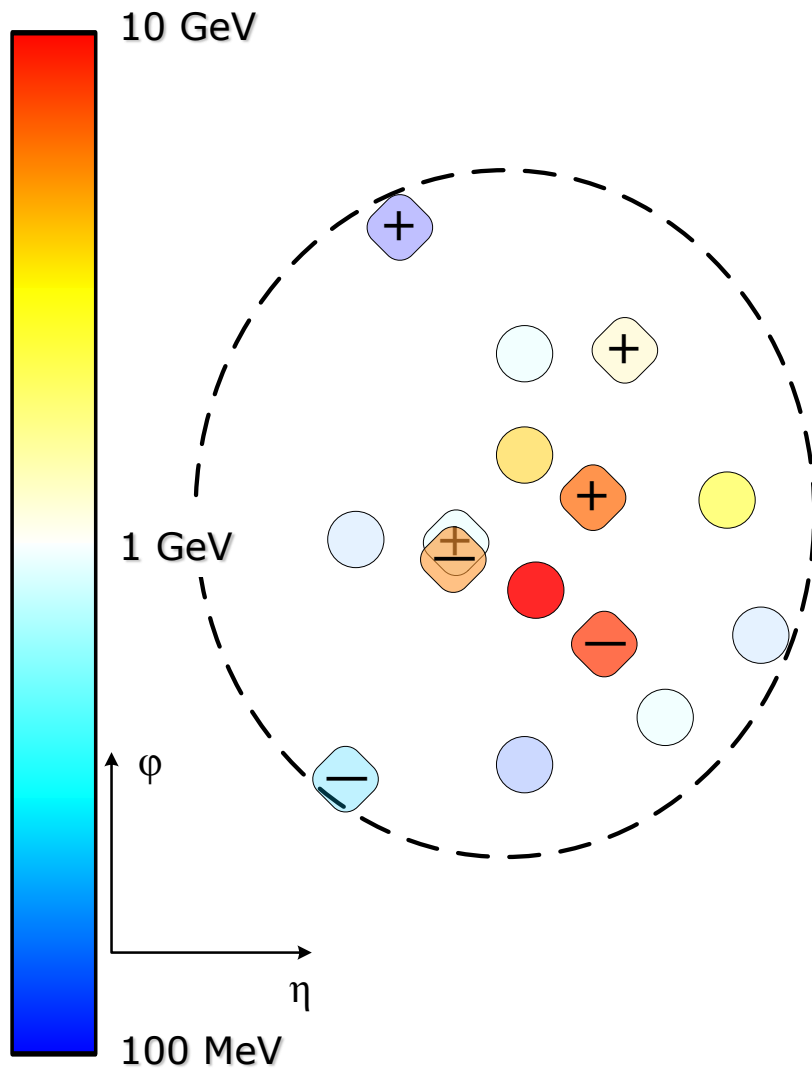
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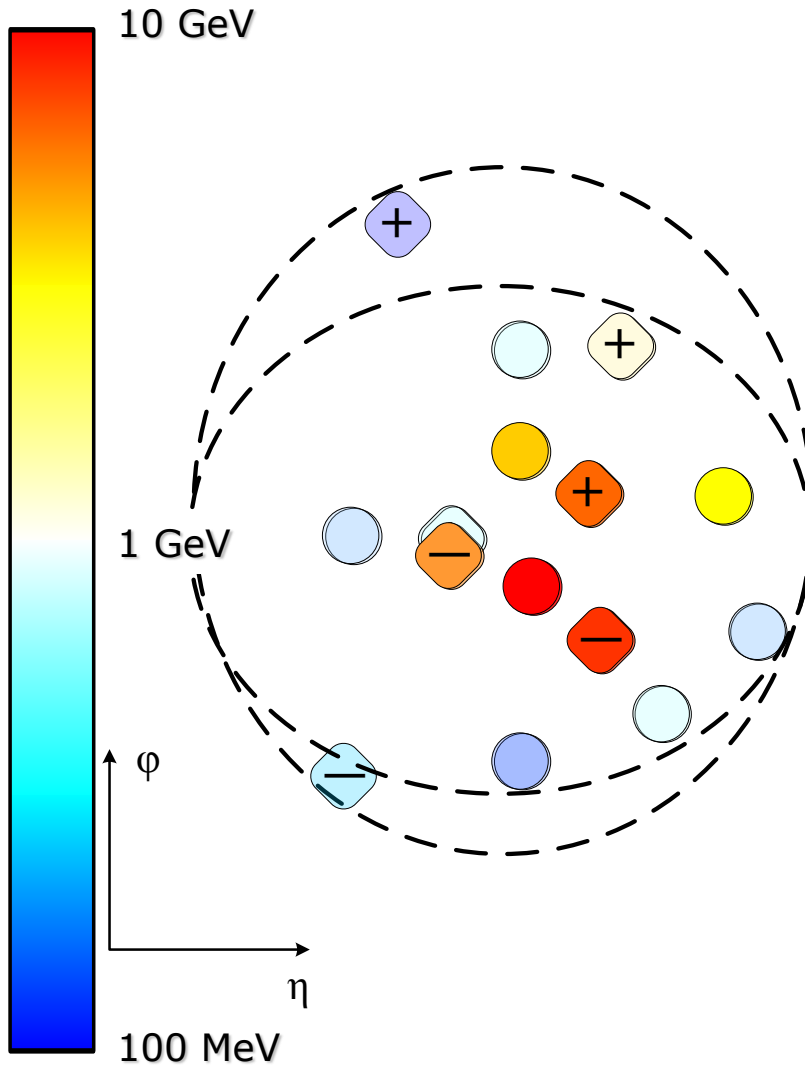
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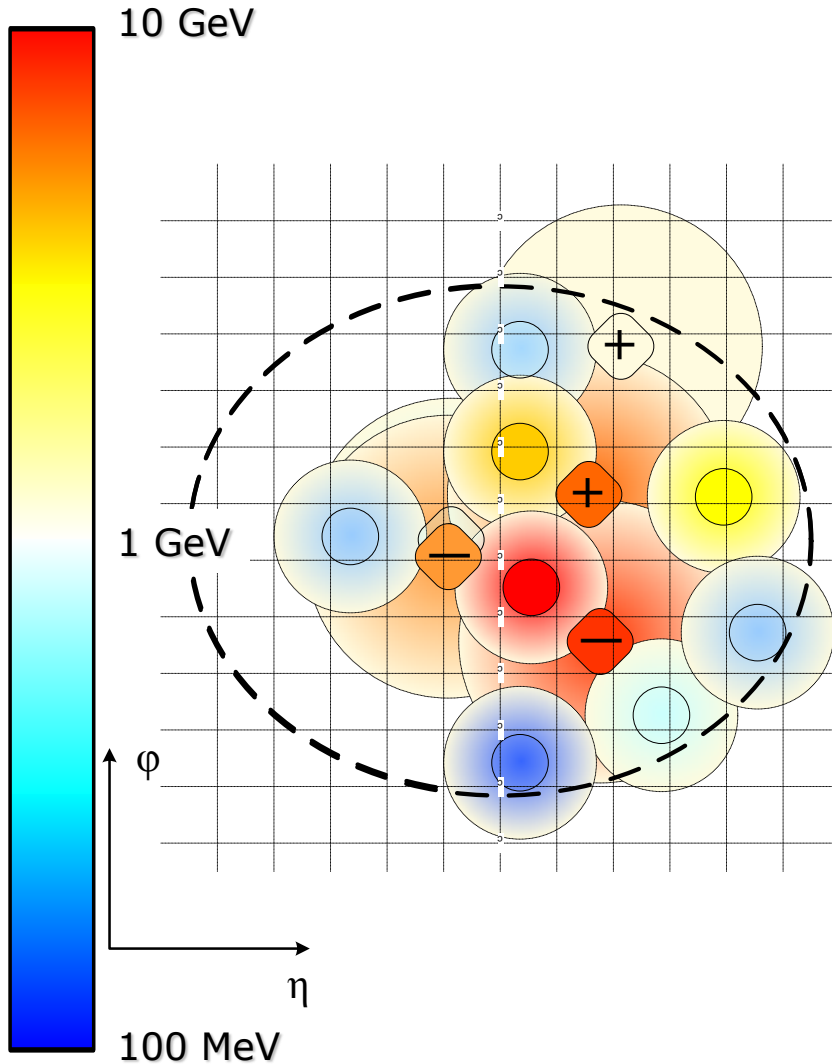
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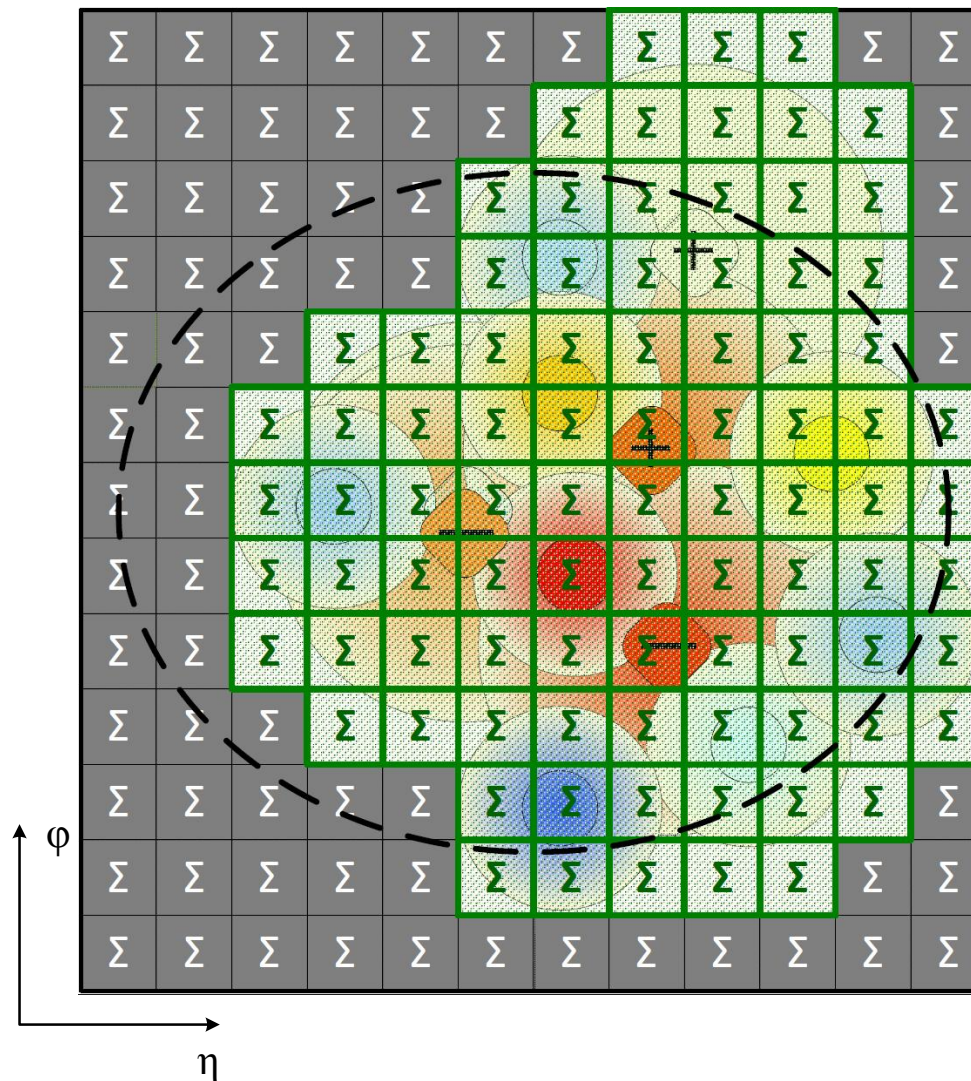
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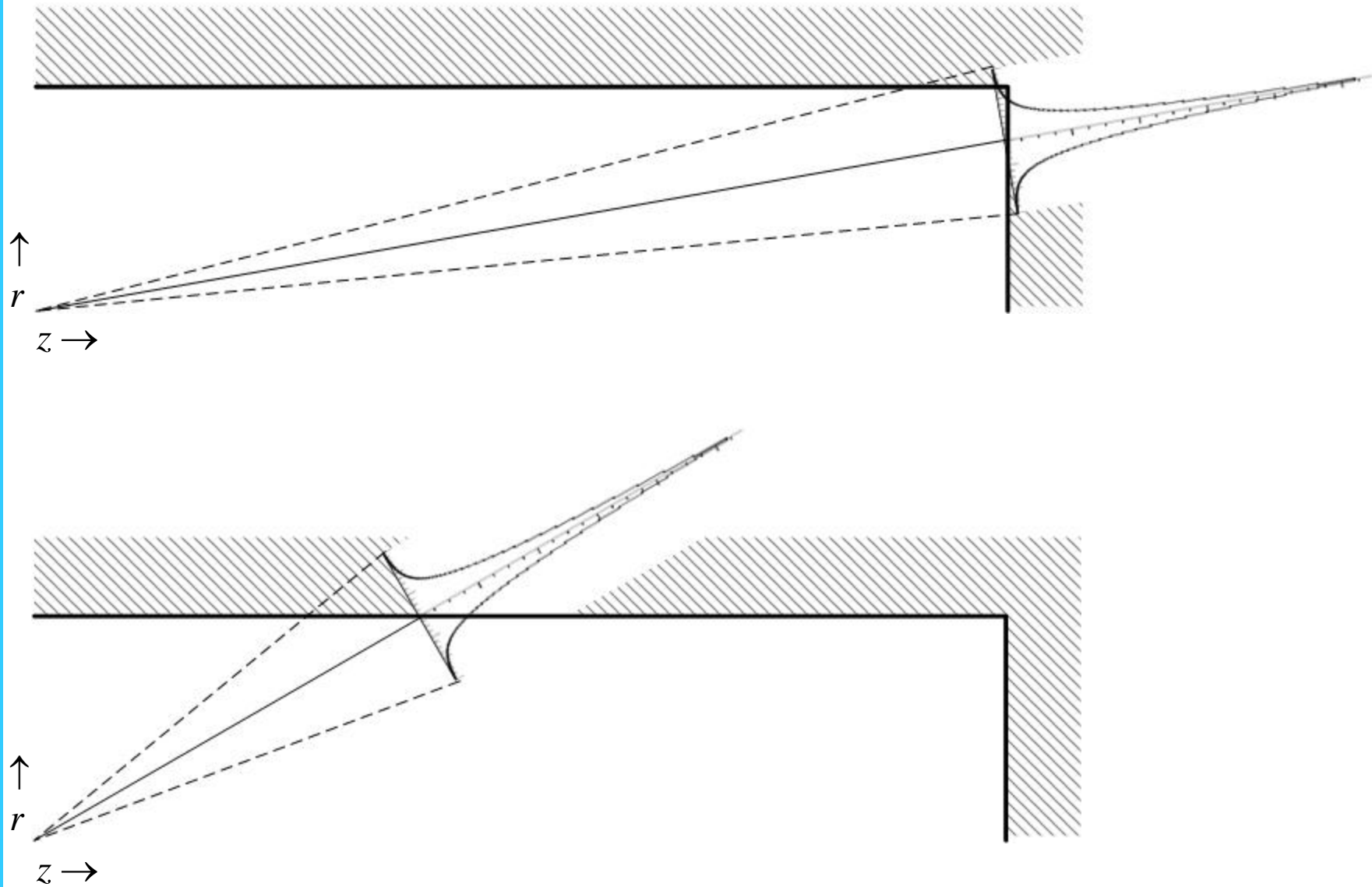
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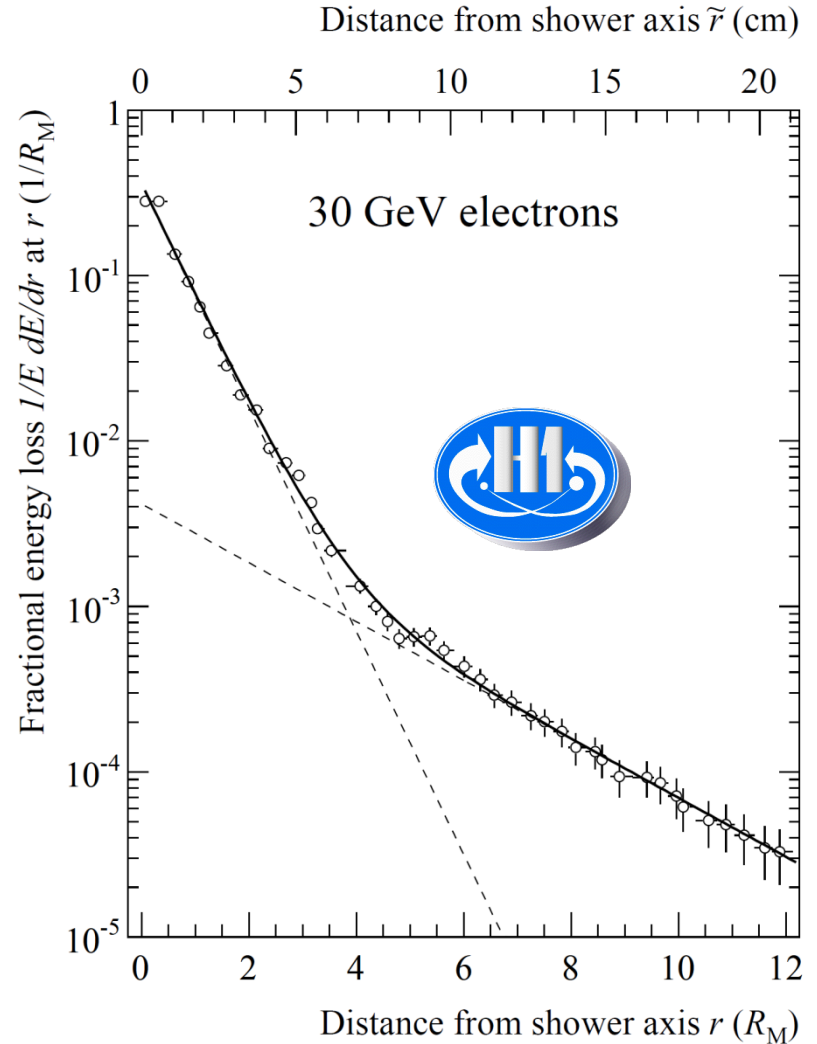
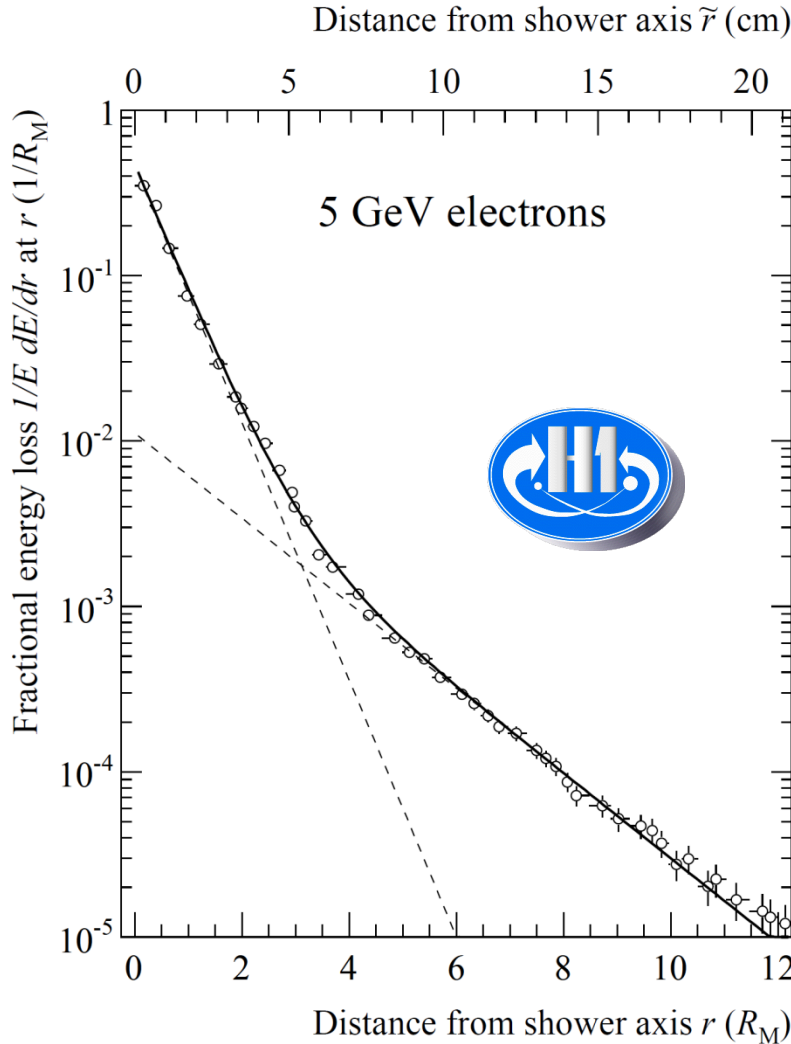
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Radial (transverse) electron shower profile in H1 calorimeter (test beam data)

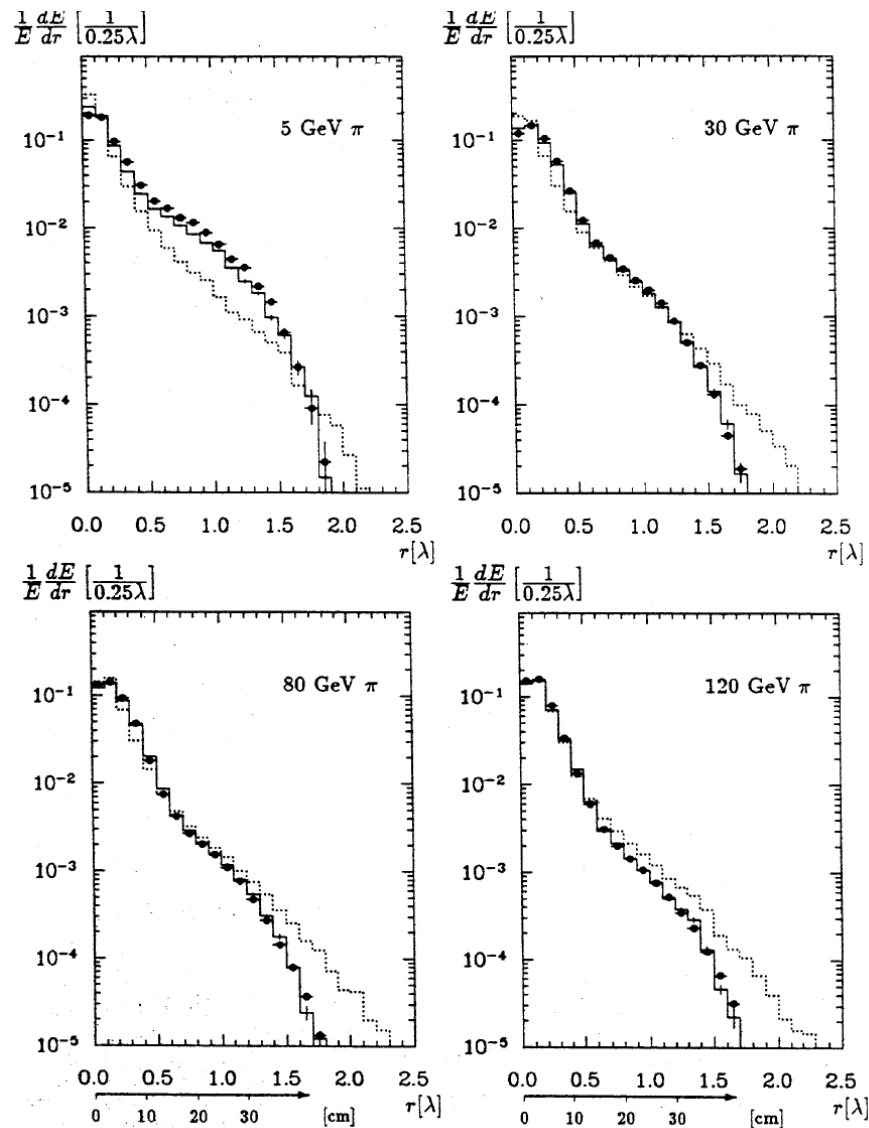


$$\frac{dE}{dr}(r) = E \left(a(E)e^{-\alpha(E)r} + b(E)e^{-\beta(E)r} \right)$$



Points/solid line histogram:
data + simulated signal with
noise cuts

Dashed line histogram:
simulated shower
development, no noise or cuts





Observables and tools

Recombination scales and order in kT like algorithms

Jet decomposition tracing back the (recursive) recombination

Can be considered resolving fragmentation to a given scale

Scale of last clustering step relates to mass of source in two-prong decay

Scale of next-to-last clustering step relates to mass of source in three-prong decay

Can be expected to correlate with jet mass in heavy particle decays

But different resolution – likely less sensitive to detector effects!

y – scale in kT algorithms provides a p_T scale at which a given recombination can be undone
recall variables:

$$d_i = p_{T,i}^2 \text{ and } d_{ij} = \min(d_i, d_j) \frac{\Delta R_{ij}}{R}$$

principal kT clustering rules:

- (1) build list of d_i and d_{ij} from all protojets
- (2) if common minimum is a d_i , call i from list and call it a jet
- (3) else combine i and j to a jet and add to list, and remove the previous protojets i and j
- (4) repeat from (1) until no protojets are left

define y – scale

$$y_{\text{scale}}^2 = y_n \times p_{T,\text{jet}}^2, \text{ with } n \text{ being a resolution parameter}$$

example: $n = 2$ refers to the last recombination in the clustering sequence, i.e. $d_{12} < d_1, d_2$:

$$y_{\text{scale}}^{1 \rightarrow 2} = \sqrt{y_2} \times p_{T,\text{jet}} = \sqrt{\min(d_1, d_2)}$$

relates to mass in two-prong decays



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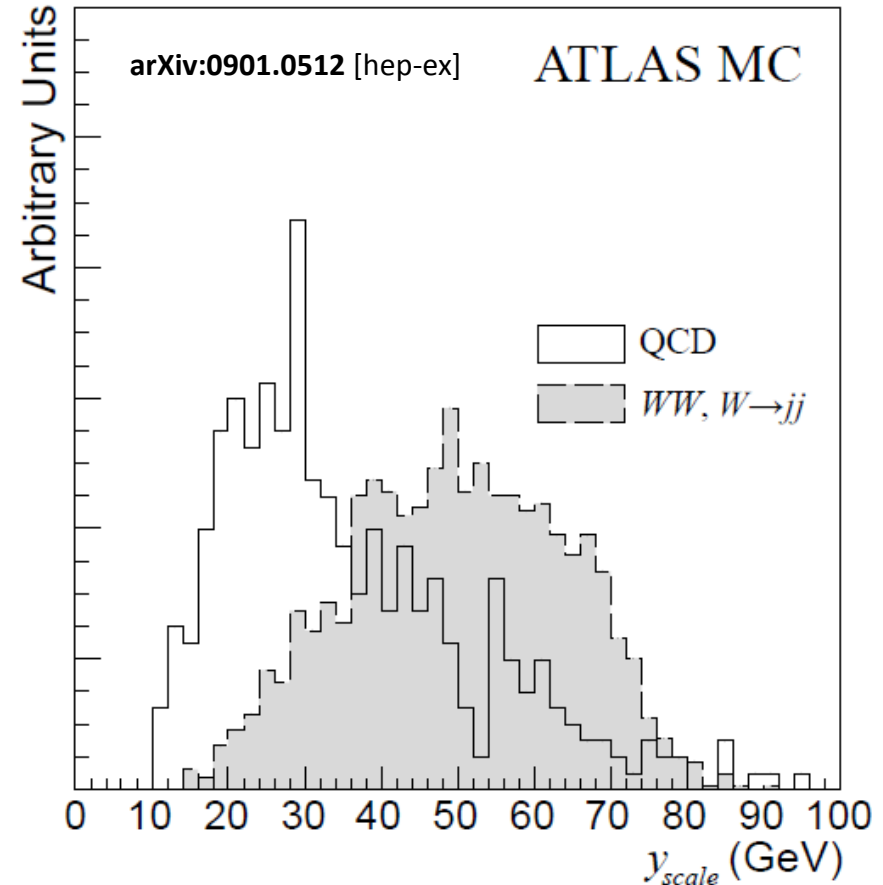
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$y_{scale}^{1 \rightarrow 2}$ for jets with $m_{jet} > 40$ GeV, for QCD and hadronically
decaying boosted W .

Note that for QCD $y_{scale}^{1 \rightarrow 2}$ is logarithmically below $p_{T,jet}$ due
to the strong ordering (in k_T) in QCD evolution, while

$\langle y_{scale}^{1 \rightarrow 2} \rangle \approx m_W$ reflects the 2-prong decay of the W boson



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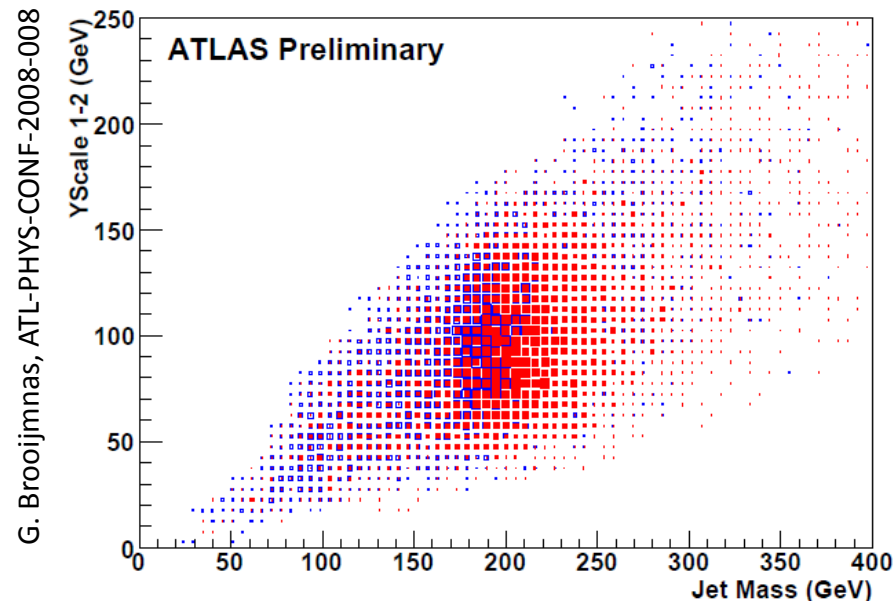
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ATLAS simulation:

$Z' \rightarrow t\bar{t}$, $m_{Z'} = 2(3)$ TeV

$p_T(t) > 300$ GeV

- $y_{\text{scale}}^{1 \rightarrow 2}$ probes **top decay**,

peaks at ≈ 100 GeV $\approx \frac{m_{\text{top}}}{2}$

- $y_{\text{scale}}^{2 \rightarrow 3}$ probes **W decay**,

peaks at ≈ 40 GeV $\approx \frac{m_W}{2}$



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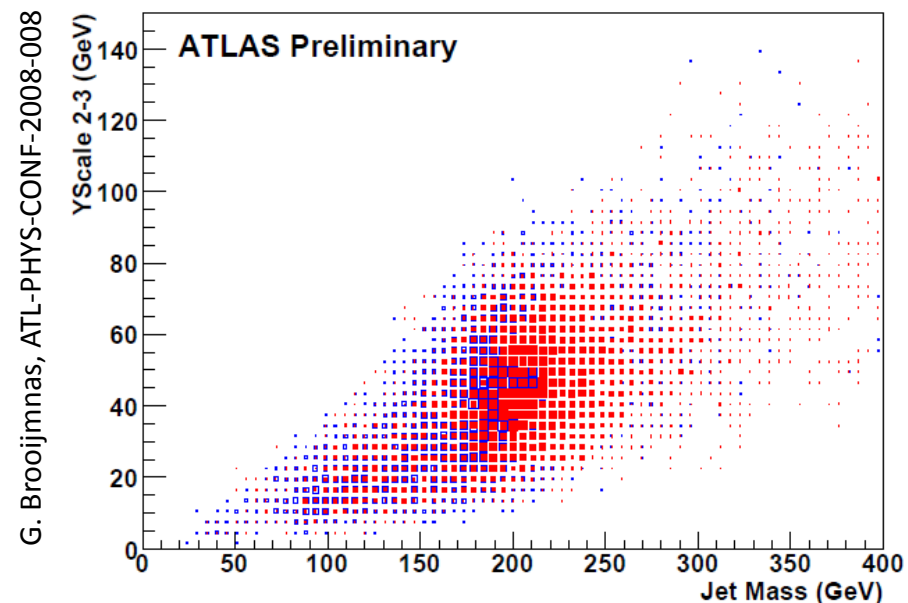
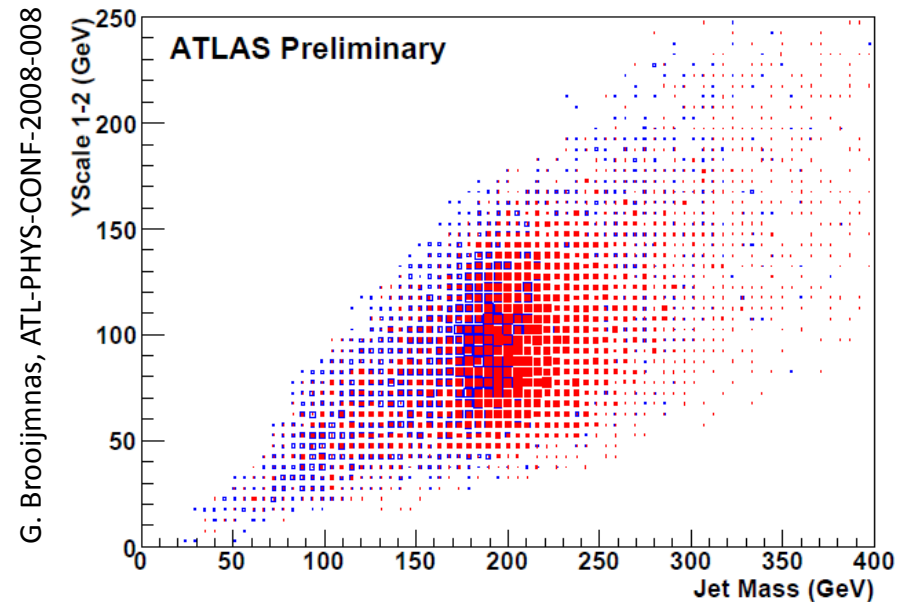
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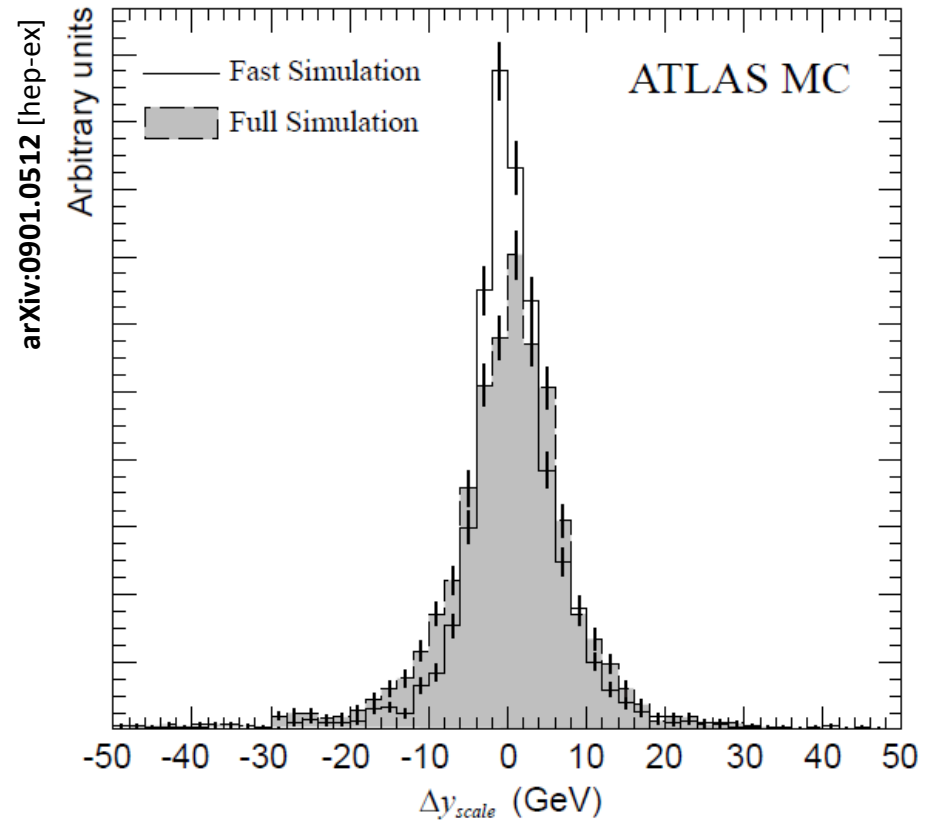
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$$\Delta y_{\text{scale}} = y_{\text{scale}}^{1 \rightarrow 2} \Big|_{\text{particle}} - y_{\text{scale}}^{1 \rightarrow 2} \Big|_{\text{calo}} \quad \text{for jets with}$$

$m_{\text{jet}} > 40$ GeV from hadronically decaying boosted W .

$y_{\text{scale}}^{1 \rightarrow 2} \Big|_{\text{calo}}$ is calculated for parameterized, response
smearing simulation (fast, no lateral shower spread)
and from detailed full simulation → indications that

$y_{\text{scale}}^{1 \rightarrow 2}$ is little sensitive to details of showering.



Observables and tools

Direct attempt to reconstruct sub-jets within jet

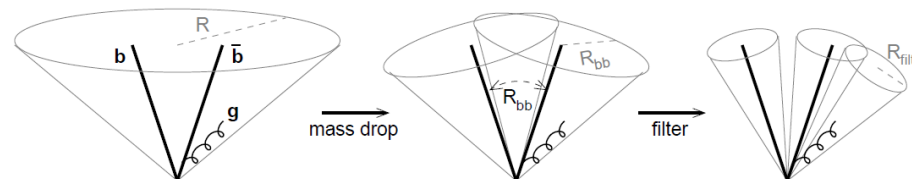
Narrow jet reconstruction in bigger jet motivated by mass drop

Includes signal enhancement strategy

Requires additional (3rd) jet from gluon radiation in the decay system

J.M. Butterworth, A.R. Davison, M.Rubin, G.P.Salam,
Phys.Rev.Lett.100:242001,2008

Look for $H \rightarrow b\bar{b}g$ with $p_{T,H} > 200$ GeV in WH / ZH production - about 5% of total cross-section:



$$R_{bb} \approx \frac{1}{\sqrt{z(1-z)}} \frac{m_H}{p_T}, \quad p_T \gg m_H$$

use Cambridge/Aachen kT flavour jet finder to find large jet ($R = 1.2$), $p_T > 200$ GeV for sub-jet analysis

- (1) break jet j into two subjects j_1, j_2 , with $m_{j_1} > m_{j_2}$, by undoing last recombination
- (2) if there is a significant mass drop such that $m_{j_1} < \mu m_j$, and the splitting $j \rightarrow (j_1, j_2)$ is not too asymmetric, i.e.

$$\min(p_{j_1}^2, p_{j_2}^2) / m_j^2 \Delta R_{j_1, j_2}^2 > y_{\text{cut}},$$

then the jet j is assumed to be the heavy particle neighbourhood and the analysis stops

- (3) else, set $j = j_1$ and go back to step (1)
- apply filter to all heavy particle neighbourhoods, with a finer angular scale $R_{\text{filter}} < R_{bb}$, e.g., $R_{\text{filter}} = \min(0.3, R_{bb}/2)$ seems to be good for LHC, and take the 3 hardest objects that appear $\rightarrow H \rightarrow b\bar{b}g$, including the hardest ($\mathcal{O}(\alpha_s)$) radiation. Tag the b jets and calculate the invariant mass.



Observables and tools

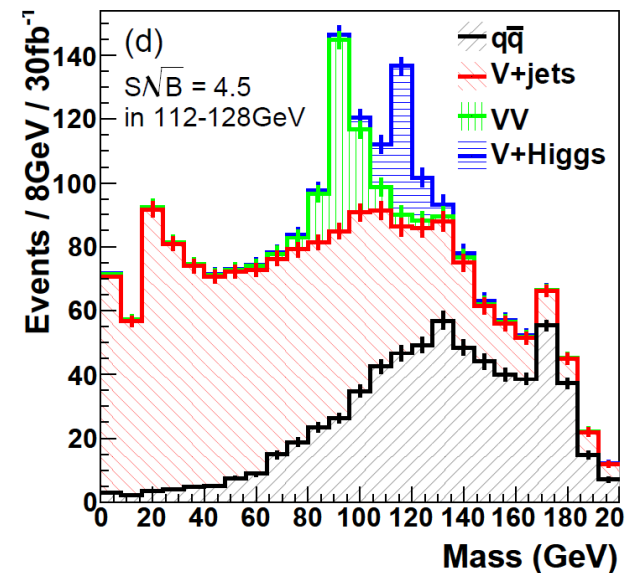
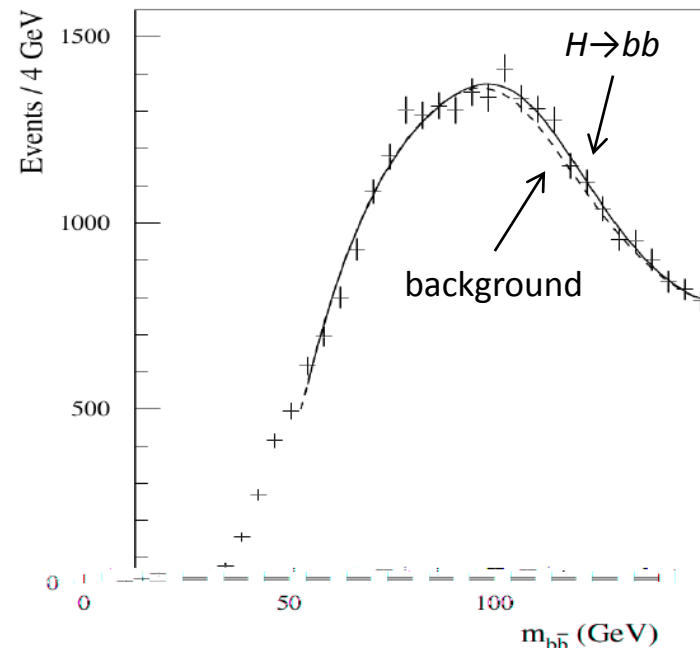
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Jet pruning

Enhancement of jet components
to increase substructure resolution

Applied in kT-style jet clustering
procedure

Jet trimming

Applies a filter by removing soft
sub-jets in a jet

Soft pT cut-off evaluated
dynamically jet by jet

Jet Pruning

- attempt to suppress underlying event and pile-up contributions to jets
- cleans jets by vetoing spurious recombinations during clustering → kT and C/A jets only!
- sensitive variables are angular distance $\phi = \Delta R_{12}$ and relative p_T hierarchy $z \equiv \min(p_{T,1}, p_{T,2})/p_{T,p}$, in recombination $1,2 \rightarrow p$
- suppress large distances and large hierarchies at each clustering iteration

$$\phi > R_{\text{cut}}$$

$$z < z_{\text{cut}}$$

works better for heavy particle decays than for QCD:

- not clear what R_{cut} is for QCD – $R_{\text{cut}} \approx m/p_T$ for heavy particle decays
- also not clear what z_{cut} should be – contamination looks hard early in clustering, especially for kT; for heavy particles, $z_{\text{cut}} = 0.1(0.15)$ works well for kT(C/A) jets from boosted top



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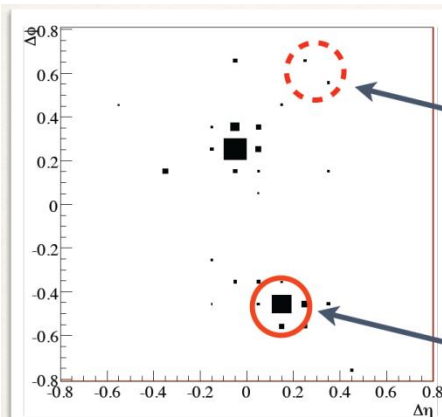
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Pruning would throw this away because it's wide angle and much softer than the core of the jet.

It would keep this because although it's at a wide angle, it's not soft.

Boosted Higgs Jet

D.Krohn, *Jet Trimming*, talk given at the *Theoretical-experimental workshop on jet & jet substructure at LHC*, University of Washington, January 10-15, 2010 (based on D.Krohn, J.Thaler, L.T. Wang, [arXiv:0912.1342](https://arxiv.org/abs/0912.1342))



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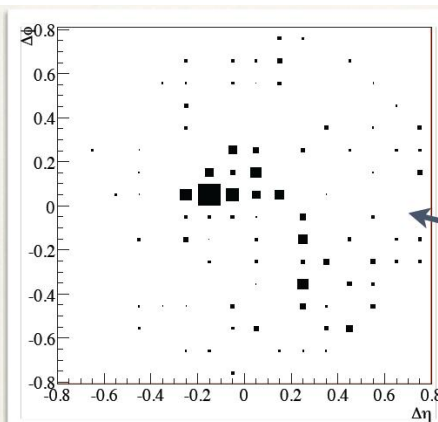
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QCD Jet

It's harder to get Pruning to work here.

What is the appropriate R_{cut} ?

What is the appropriate z_{cut} ?

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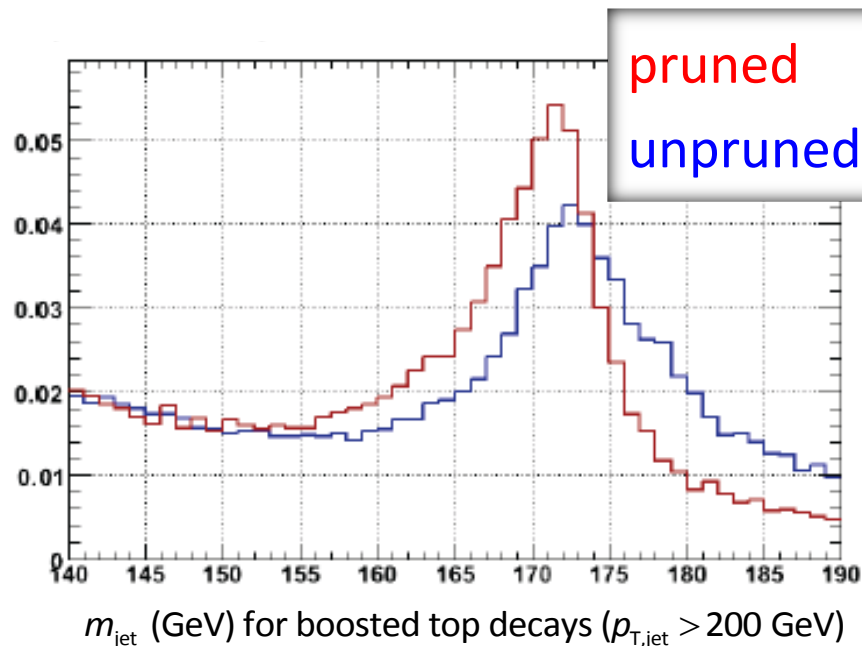
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Jet Pruning

- improves jet mass measurement for boosted top etc.



J. Walsh, *Understanding Jet Substructure*, talk given at the *Theoretical-experimental TeraScale workshop on event shapes*, University of Oregon, February 23-27, 2009



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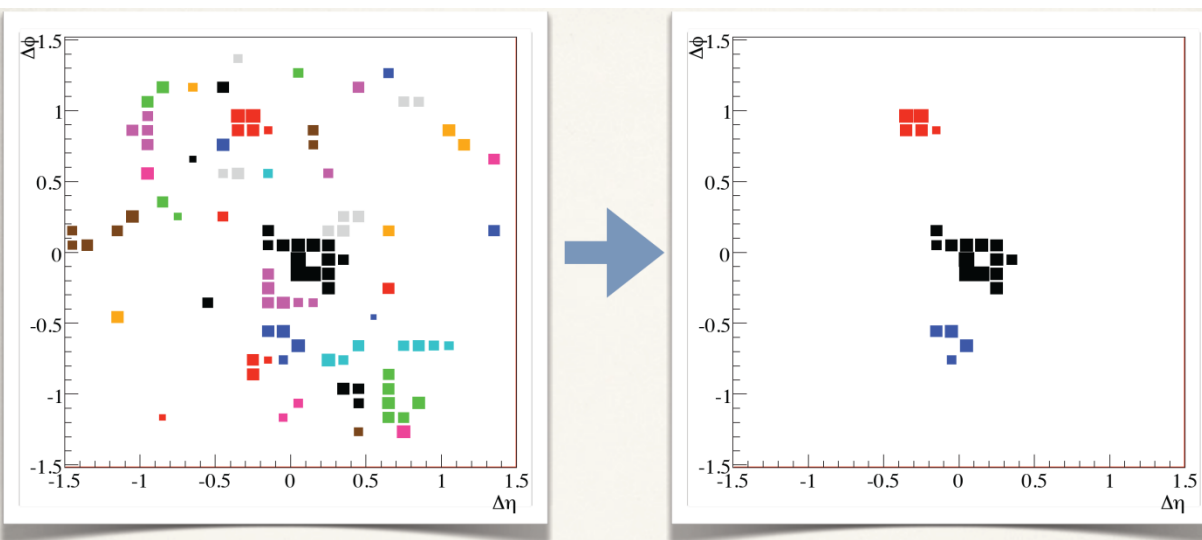
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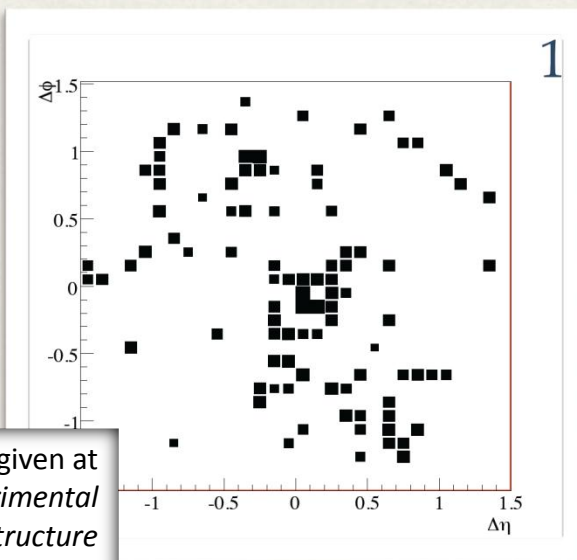
Jet Trimming

- main motivation is removing contaminations from e.g. pile-up and underlying event, from a fully reconstructed jet
- measures softness/hardness of contamination relative to whole jet – no judgements at the clustering stage
- approach:
 - (1) fully reconstruct jet from calorimeter signals
 - (2) cluster narrow sub-jets, typically with $R_{\text{sub}} = 0.2$
 - (3) discard sub-jets i with $p_{T,i} < f_{\text{cut}} \Lambda_{\text{hard}}$
 - (4) rebuild jet from surviving sub-jets
- typical choice for Λ_{hard} is $\Lambda_{\text{hard}} = p_{T,\text{jet}}$

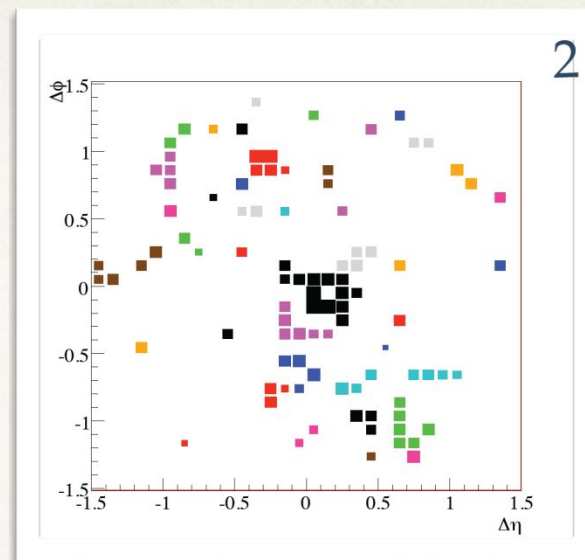
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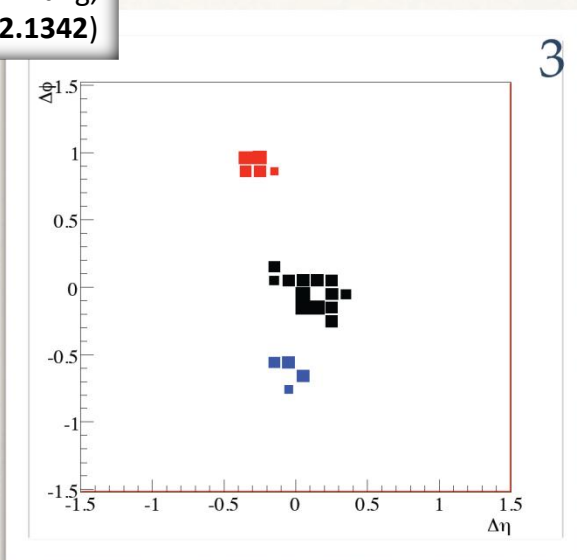
Start



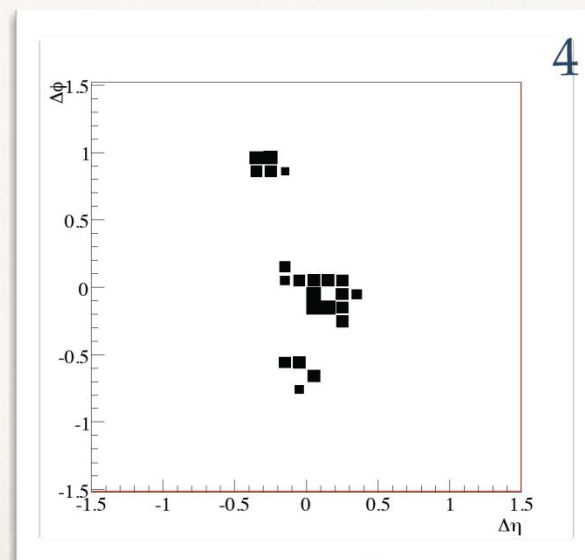
D.Krohn, *Jet Trimming*, talk given at the *Theoretical-experimental workshop on jet & jet substructure at LHC*, University of Washington, January 10-15, 2010 (based on D.Krohn, J.Thaler, L.T. Wang, [arXiv:0912.1342](https://arxiv.org/abs/0912.1342))



Cluster into subjets

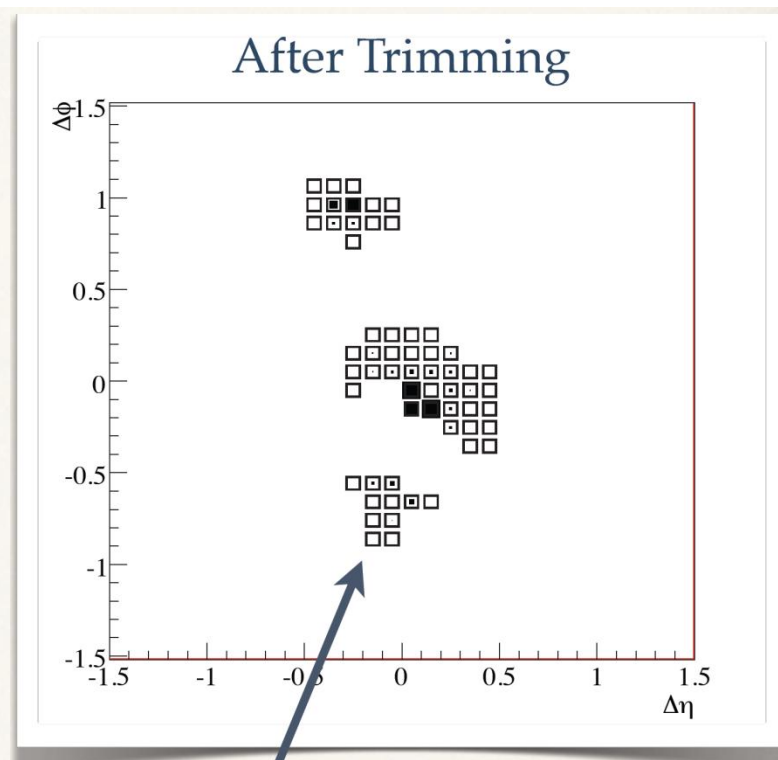
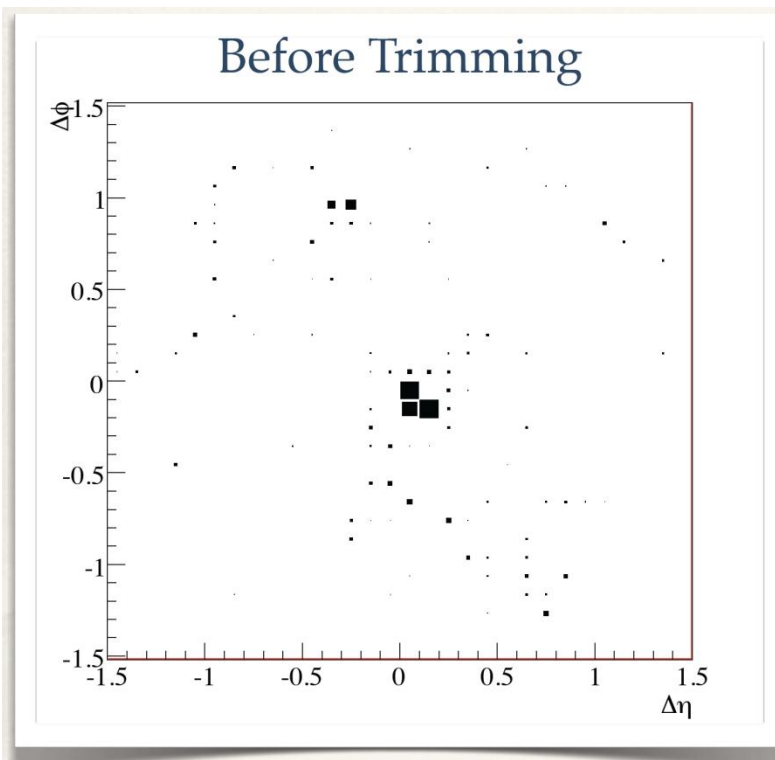


Discard soft subjets



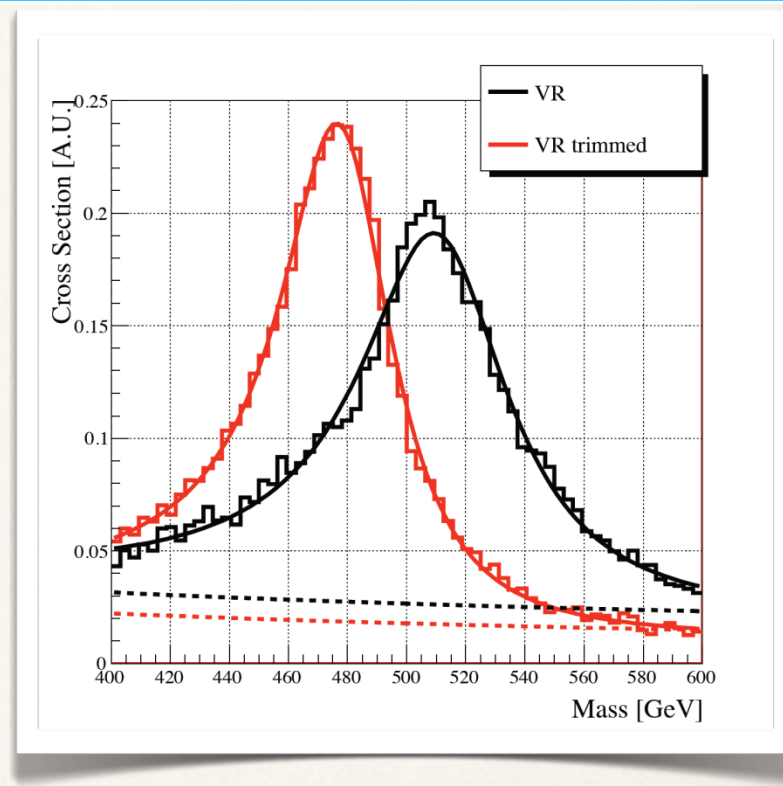
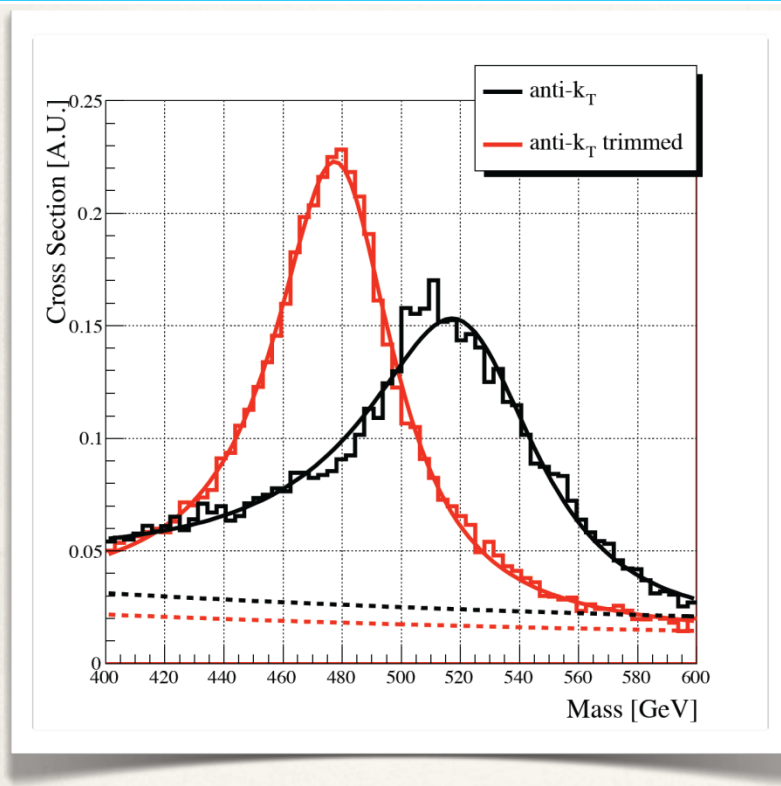
Reassemble





Empty squares
denote extent
of jet area

D.Krohn, *Jet Trimming*, talk given at the *Theoretical-experimental workshop on jet & jet substructure at LHC*, University of Washington, January 10-15, 2010 (based on D.Krohn, J.Thaler, L.T. Wang, [arXiv:0912.1342](https://arxiv.org/abs/0912.1342))



D.Krohn, *Jet Trimming*, talk given at the *Theoretical-experimental workshop on jet & jet substructure at LHC*, University of Washington, January 10-15, 2010 (based on D.Krohn, J.Thaler, L.T. Wang, [arXiv:0912.1342](https://arxiv.org/abs/0912.1342))

Trimmed and variable radius (VR) jets from $\phi \rightarrow qq, gg$
 (for VR, see D. Krohn, J. Thaler, and L.-T. Wang, *Jets with Variable R* , JHEP 06 (2009) 059)



A. Larkoski, M. Jankowiak (BOOST2011) *arXiv:1104.1646*

Angular Correlations

- For any IRC safe set of particles $\{i\}$:

$$\mathcal{G}(R) \equiv \frac{\sum_{i \neq j} p_{Ti} p_{Tj} \Delta R_{ij}^2 \Theta(R - \Delta R_{ij})}{\sum_{i \neq j} p_{Ti} p_{Tj} \Delta R_{ij}^2} \approx \frac{\sum_{i \neq j} p_i \cdot p_j \Theta(R - \Delta R_{ij})}{\sum_{i \neq j} p_i \cdot p_j}$$

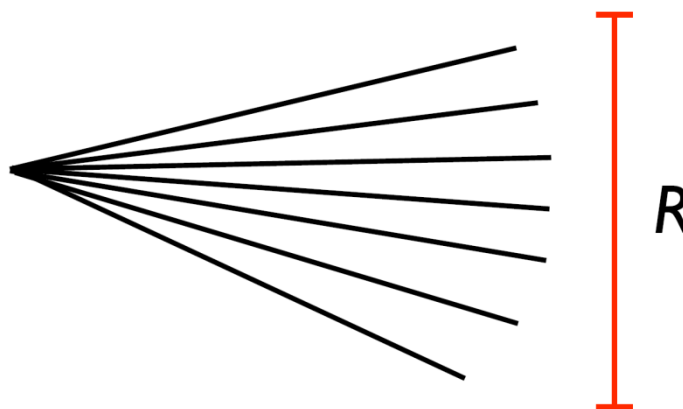
- R is **not** measured wrt jet center
- Distinct from angular profile
- Quantifies jet scaling in an IRC safe way



A. Larkoski, M. Jankowiak (BOOST2011) *arXiv:1104.1646*

Angular Correlations

- What is the physical picture?
- Jet with \sim no substructure



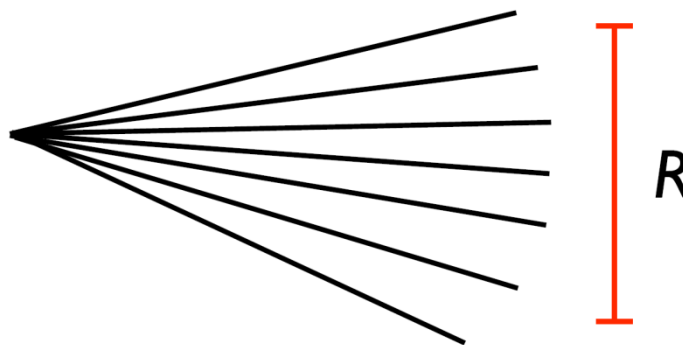
- Angular correlation function is smooth
- In QCD, $\mathcal{G}(R) \sim R^2$



A. Larkoski, M. Jankowiak (BOOST2011) *arXiv:1104.1646*

Angular Correlations

- What is the physical picture?
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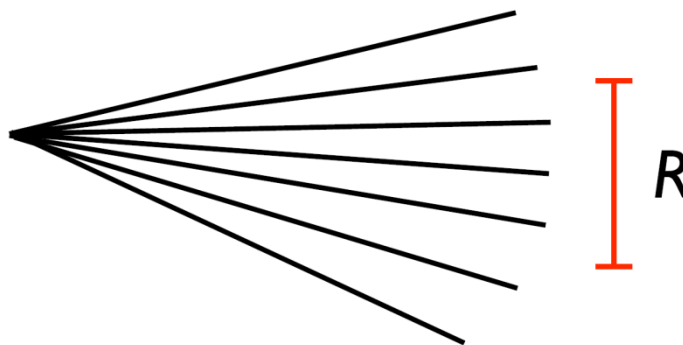
- Angular correlation function is smooth
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A. Larkoski, M. Jankowiak (BOOST2011) *arXiv:1104.1646*

Angular Correlations

- What is the physical picture?
- Jet with \sim no substructure



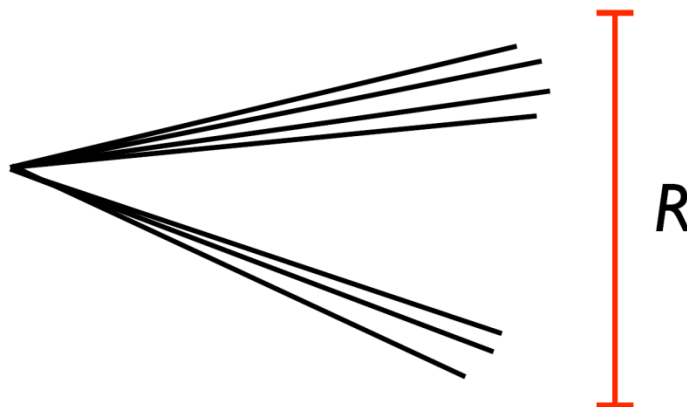
- Angular correlation function is smooth
- In QCD, $\mathcal{G}(R) \sim R^2$



A. Larkoski, M. Jankowiak (BOOST2011) *arXiv:1104.1646*

Angular Correlations

- What is the physical picture?
- Jet with substructure



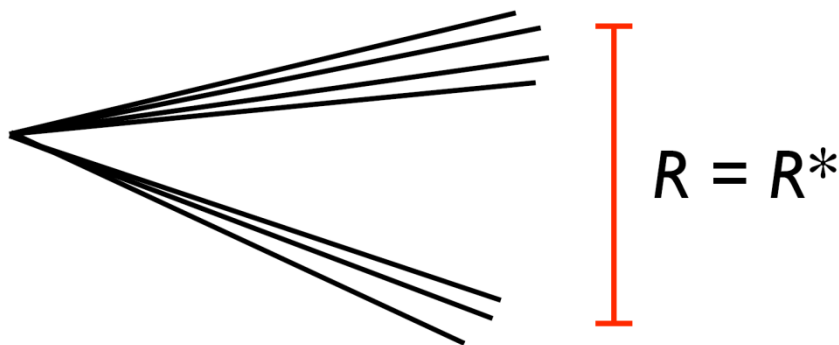
- $\mathcal{G}(R) \sim 1$



A. Larkoski, M. Jankowiak (BOOST2011) *arXiv:1104.1646*

Angular Correlations

- What is the physical picture?
- Jet with substructure



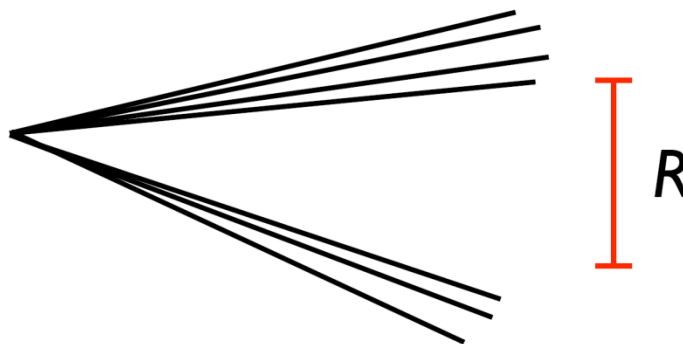
- $\mathcal{G}(R) \sim 1$



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Angular Correlations

- What is the physical picture?
- Jet with substructure



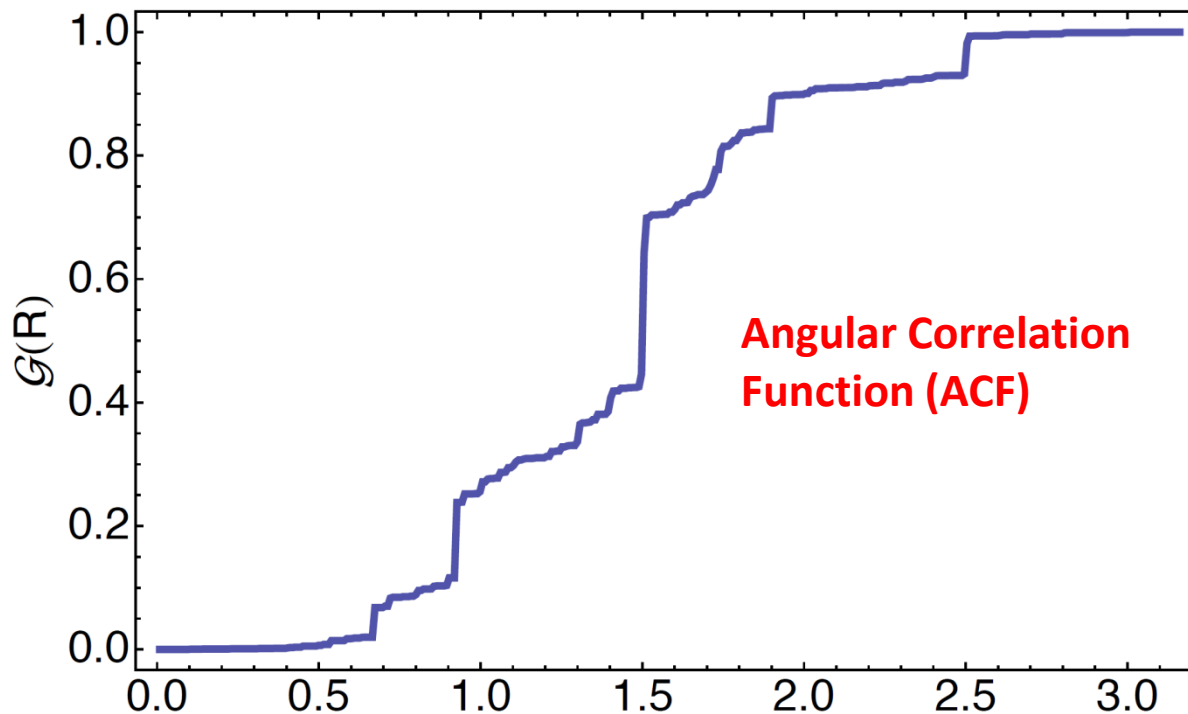
- $\mathcal{G}(R) \sim 0$
- Angular correlation is discontinuous at R^*



A. Larkoski, M. Jankowiak (BOOST2011) *arXiv:1104.1646*

Angular Correlations

- Ledges in $\mathcal{G}(R)$ = separation of hard subjects

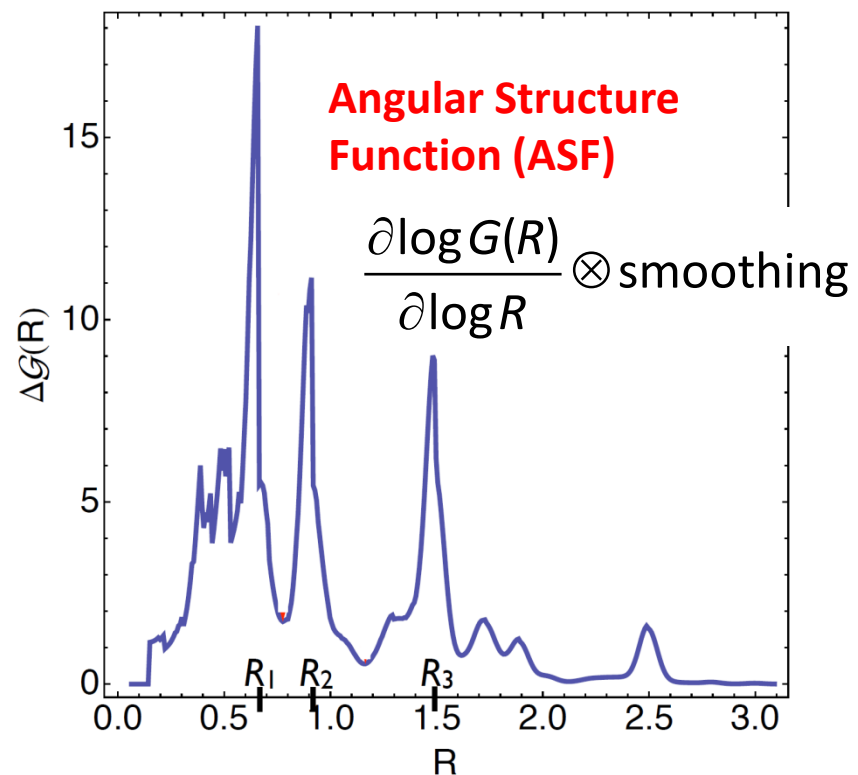
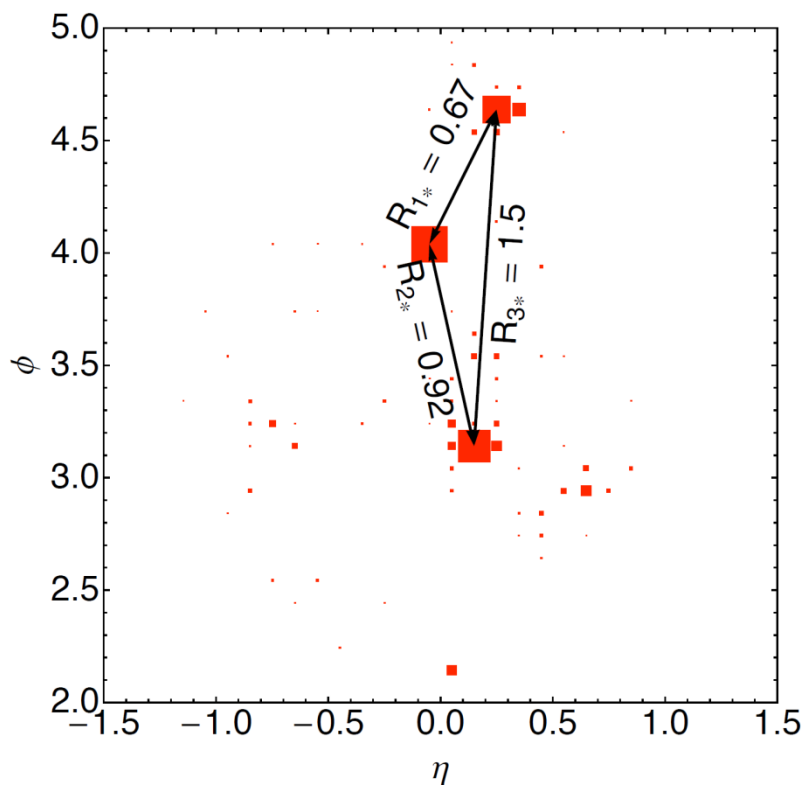


- $\mathcal{G}(R)$ for a top quark jet

A. Larkoski, M. Jankowiak (BOOST2011) *arXiv:1104.1646*

Angular Structure

Question: Does $\Delta\mathcal{G}(R)$ determine interesting ledges?



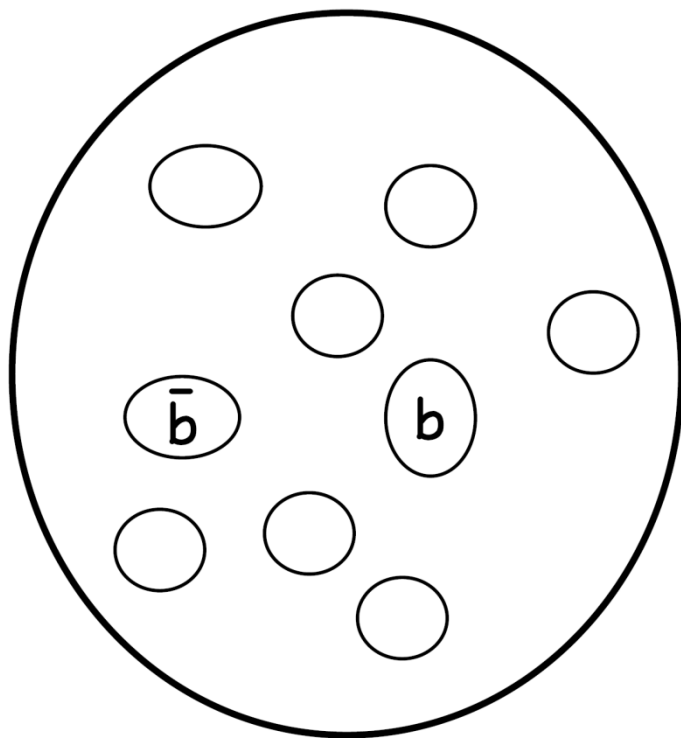
Answer: Yes!



M. Spannowsky & D. Soper (BOOST2011) *arXiv:1102.3480*

Analysis of radiation & decay patterns in a jet

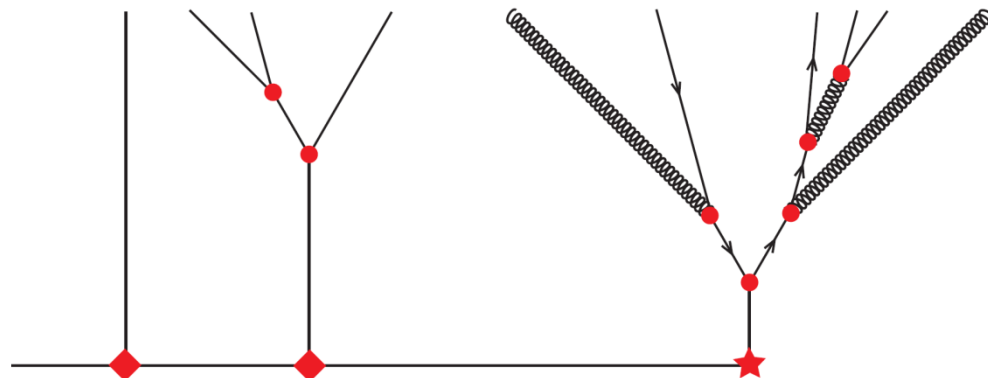
Fat jet: $R=1.2$, anti- k_T



microjets
 $R=0.15$, k_T

ISR/UE

hard interaction

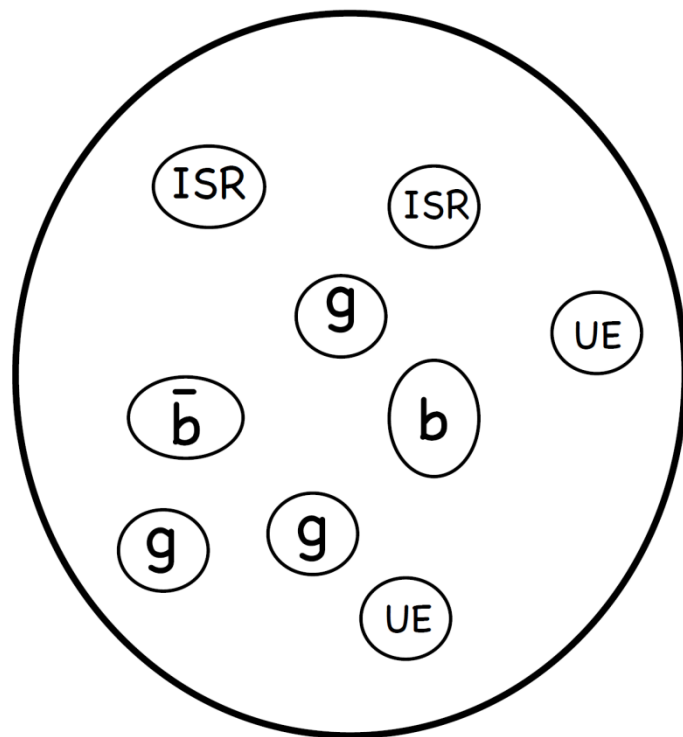
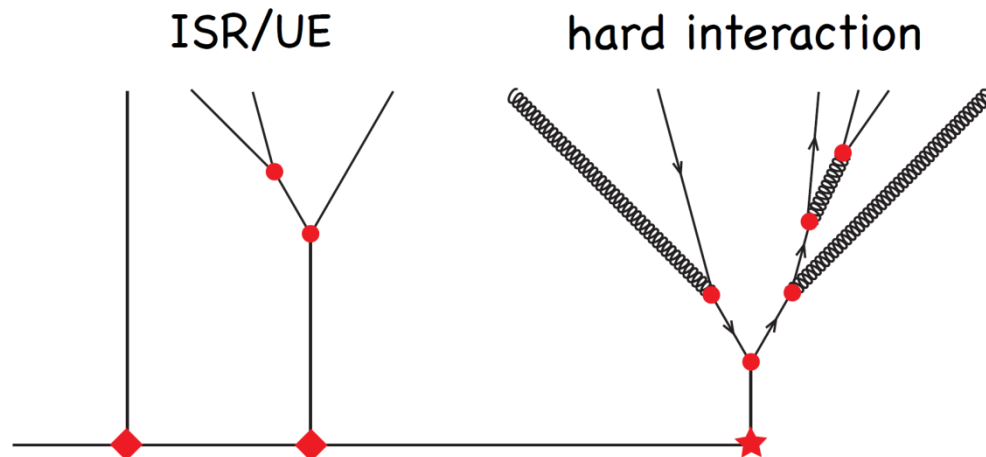


Build all possible shower histories

signal vs background hypothesis
based on:

- ▶ Emission probabilities
- ▶ Color connection
- ▶ Kinematic requirements
- ▶ b-tag information


 M. Spannowsky & D. Soper (BOOST2011) *arXiv:1102.3480*
Analysis of radiation & decay patterns in a jet

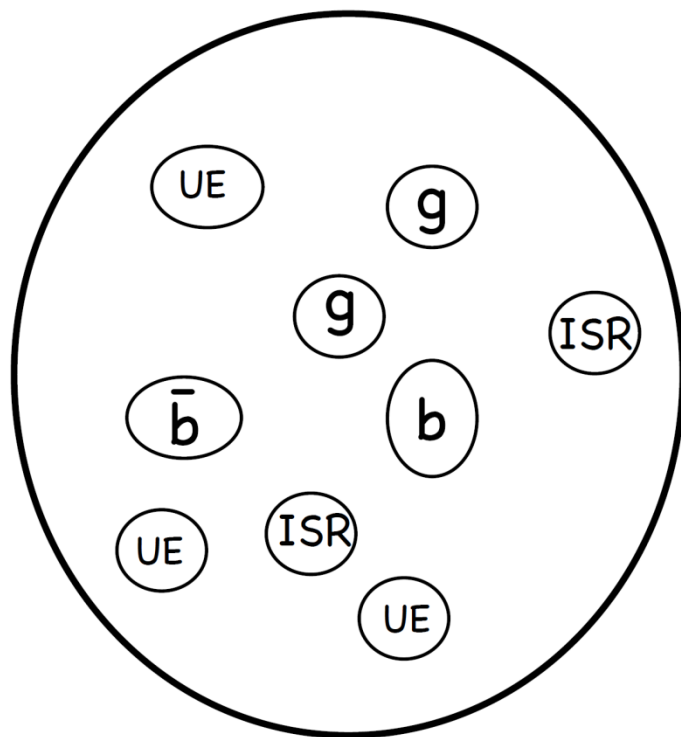
 Fat jet: $R=1.2$, anti- k_T

 microjets
 $R=0.15$, k_T


Build all possible shower histories

 signal vs background hypothesis
based on:

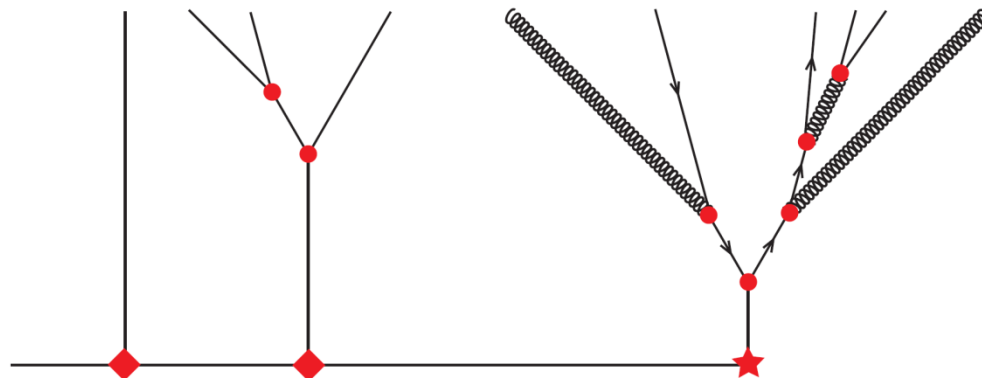
- ▶ Emission probabilities
- ▶ Color connection
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 M. Spannowsky & D. Soper (BOOST2011) *arXiv:1102.3480*
**Analysis of radiation & decay
patterns in a jet**

 Fat jet: $R=1.2$, anti- k_T

 microjets
 $R=0.15$, k_T

ISR/UE

hard interaction



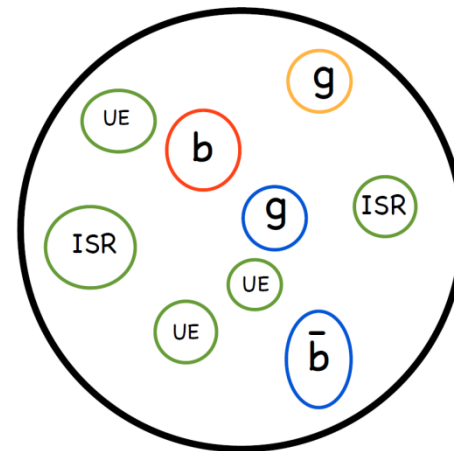
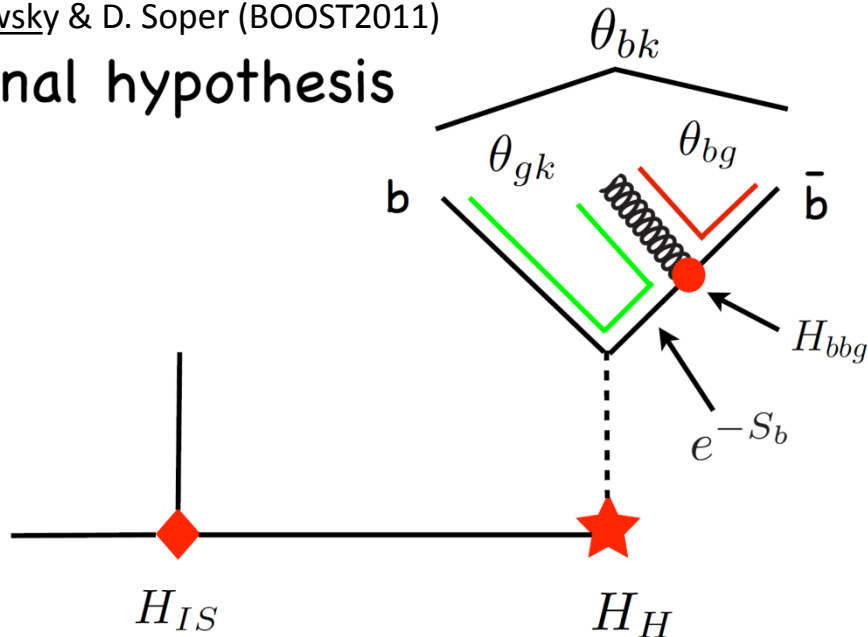
Build all possible shower histories

 signal vs background hypothesis
 based on:

- ▶ Emission probabilities
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- ▶ Kinematic requirements
- ▶ b-tag information

M. Spannowsky & D. Soper (BOOST2011)

Signal hypothesis



b-quarks radiate gluons

See Dave's talk [Link](#)

$$\int d\mathcal{P} = \int d\mu_J^2 \int d\Delta\phi \int d\Delta y \sum_s J H e^{-S}$$

$$S \approx \int d\bar{\mu}_J^2 \Theta(\mu_J^2 < \bar{\mu}_J^2) \int d\Delta\bar{y} \int d\Delta\bar{\phi} \sum_{\bar{s}} J(\bar{p}_A, \bar{p}_B) H(\bar{p}_A, \bar{p}_B) \Theta(\{\bar{p}_A, \bar{p}_B\} \in \text{fat jet})$$

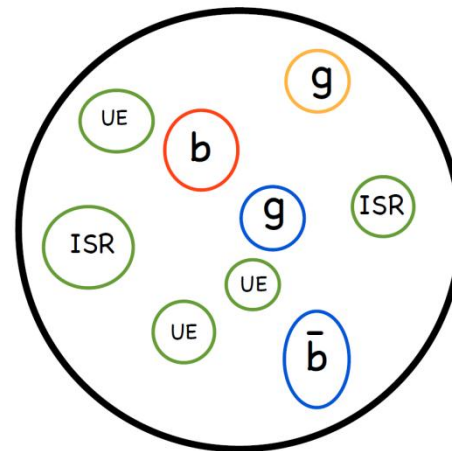
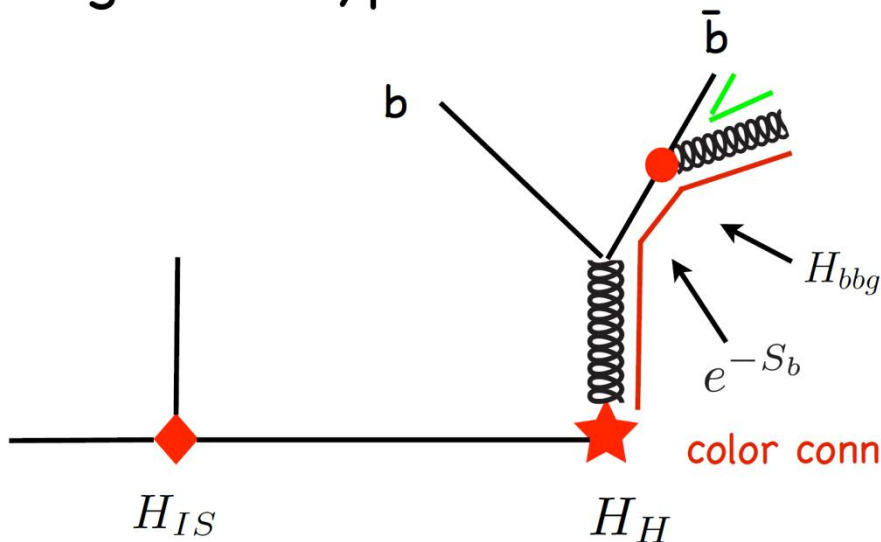
$$H_{bbg} = H_{\bar{b}g\bar{b}} = \frac{C_A \alpha_s(\mu_J^2)}{2} \frac{1}{\mu_J^2} \frac{k_J^2}{k_b k_g} \frac{\theta_{bk}^2}{\theta_{gb}^2 + \theta_{gk}^2} \Theta(k_g < k_b) \Theta\left(2 \frac{\mu_J^2}{k_J} < \frac{\mu_K^2}{k_K}\right)$$





M. Spannowsky & D. Soper (BOOST2011) [arXiv:1102.3480](https://arxiv.org/abs/1102.3480)

Background hypothesis



color connected partner outside fat jet

b-quarks radiate gluons

See Dave's talk [Link](#)

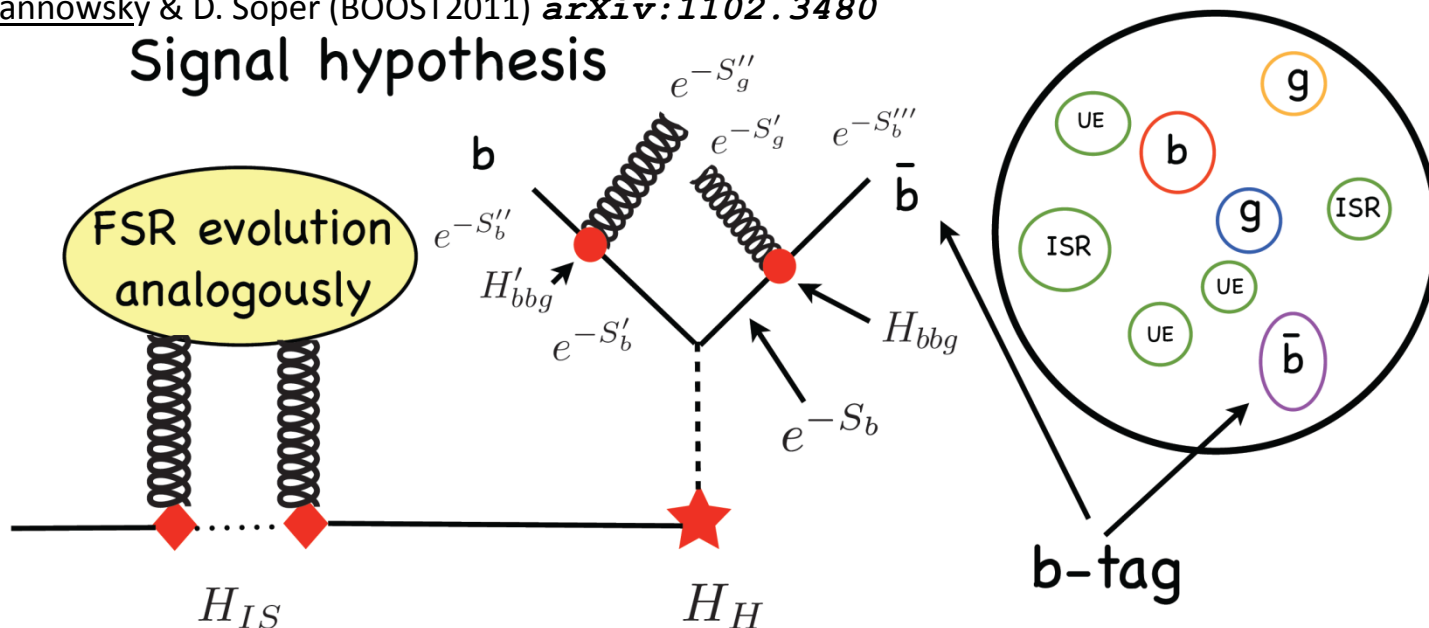
$$\int d\mathcal{P} = \int d\mu_J^2 \int d\Delta\phi \int d\Delta y \sum_s J H e^{-S}$$

$$S \approx \int d\bar{\mu}_J^2 \Theta(\mu_J^2 < \bar{\mu}_J^2) \int d\Delta\bar{y} \int d\Delta\bar{\phi} \sum_{\bar{s}} J(\bar{p}_A, \bar{p}_B) H(\bar{p}_A, \bar{p}_B) \Theta(\{\bar{p}_A, \bar{p}_B\} \in \text{fat jet})$$

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 M. Spannowsky & D. Soper (BOOST2011) [arXiv:1102.3480](https://arxiv.org/abs/1102.3480)

Signal hypothesis



Wrapping up all factors gives weight for shower history

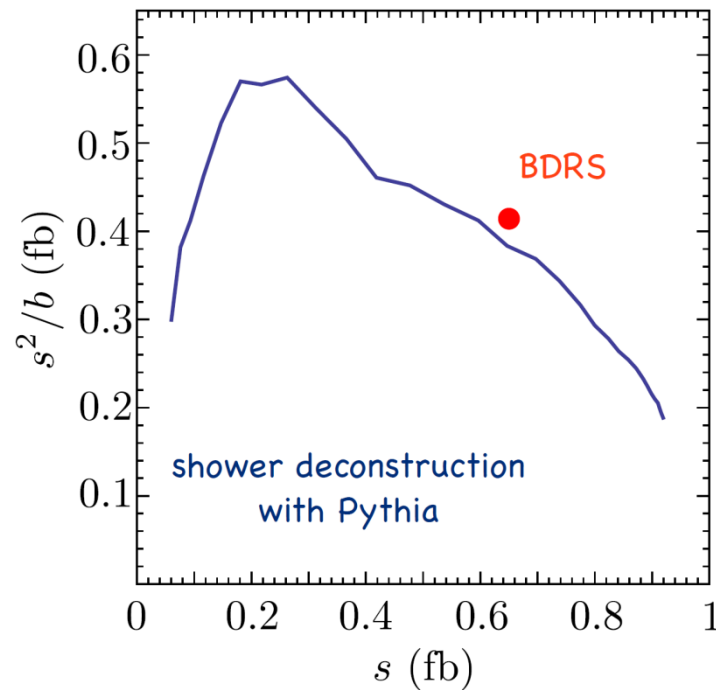
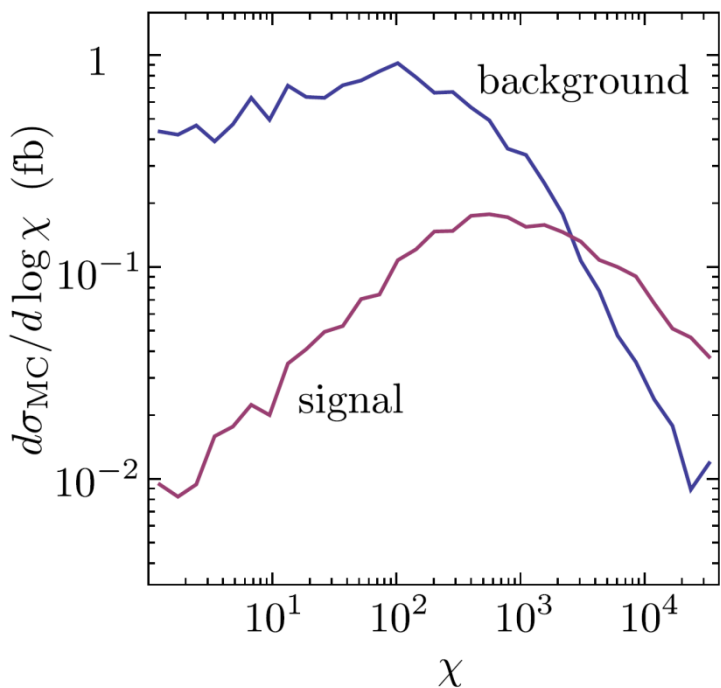
$$\chi = \frac{\sum_{ISR/Hard} \left(\sum_i ISR_i \times \sum_j \text{Signal}_j \right)}{\sum_{ISR/Hard} \left(\sum_i ISR_i \times \sum_j \text{Backg}_j \right)}$$

Here $\text{Signal}_1 = H_H H_{\text{split}} e^{-S_{\text{split}}} H_{\text{bbg}} e^{-S'_b} e^{-S''_b} e^{-S'_g} H'_{\text{bbg}} e^{-S''_b} e^{-S_b} e^{-S''_g}$



M. Spannowsky & D. Soper (BOOST2011) *arXiv:1102.3480*

perfect b-tagging 2 b-tagged microjets



► Profits more from information than BDRS, e.g. b-tagging

Additional info and updated plots from Michael tomorrow!



Jet reconstruction

Energy scale and direction well controlled

Detector response, pile-up, UE, ...

Jet shapes can be reconstructed

Not too dependent on signal definition
(calorimeter towers/clusters, particle flow, tracks...)

Jet mass more challenging

Spatial energy distribution by em and had showers, noise, pile-up,...

Stronger dependence on signal definition

Fat jet reconstruction (high p_T)

Global jet easy to find (= trigger & reconstruct) but maybe not so easy to calibrate

Occupies large regions of the detector with different response characteristics (local calibrated energy scale needed?)

Much larger global pile-up contributions

Internal jet structures, sub-jets

Structure reconstruction

Spatial and energy resolution inside jet – larger local signal fluctuations, dependence on signal definition

Some small distance scales suggested – experimental limitations need to be considered

Internal kinematic, thrusts and flows

Sub-jet calibration non-trivial – e.g., full jet calibration depends on neighbouring activity, how does this translate to sub-jets?

Signal definition crucial – e.g., can cell clusters merge internal energy flow too much?

How much is detector image disturbed by pile-up – adds internal jet structure but with different dynamics/scales...

Systematic uncertainties

Internal (sub-)jet scales need to be validated

Not clear how to do this without fat jets from (boosted) massive decay, e.g. hadronic W, full hadronic top

Angular measurement error folds with response uncertainty

Quite some activity in the experiments

Understanding effect of signal definition

Finding limitations in distance scales

Calibration of sub-jets

...



Jet reconstruction

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Signal definition crucial – e.g., can cell clusters in jet be reconstructed? (too difficult)

How much is detector image disturbed by pile-up – adds internal jet structure but with different characteristics

Systematic uncertainties

Internal (sub-)jet scales need to be validated
Not clear how to do this without fat jets from (boosted) massive decay, e.g. hadronic W, full hadronic top

Angular measurement error folds with response uncertainty

Quite some activity in the experiments

Understanding effect of signal definition

Finding limitations in distance scales

Calibration of sub-jets

...

In general calibrated jet constituents help with several issues – new/improved signal definitions for hadron colliders at LHC (CMS – particle flow, ATLAS – local hadronic cluster calibration)!



High p_T jet sample

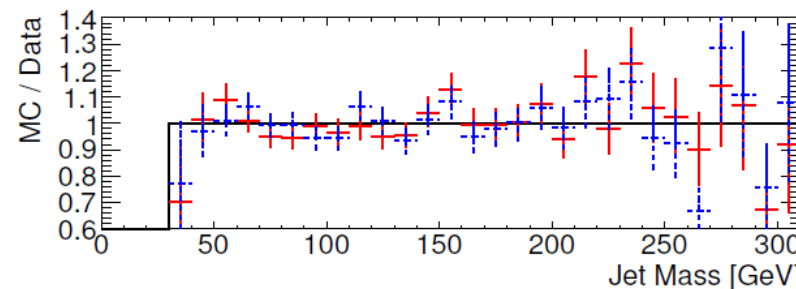
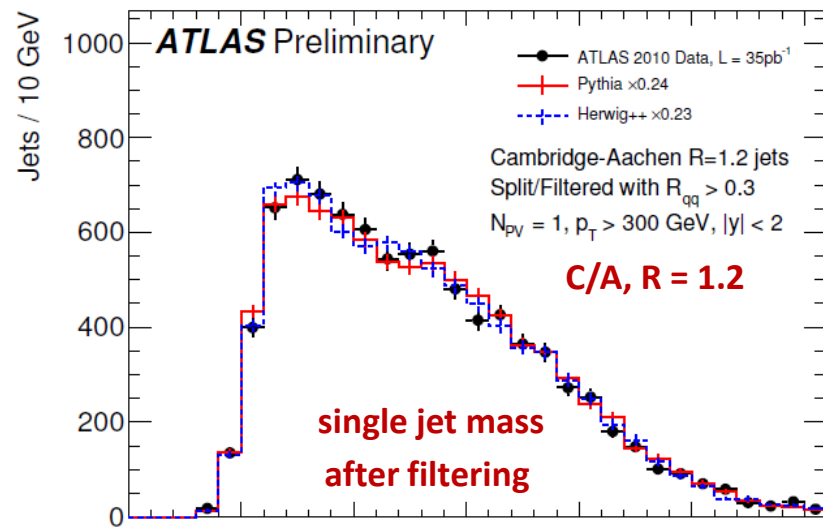
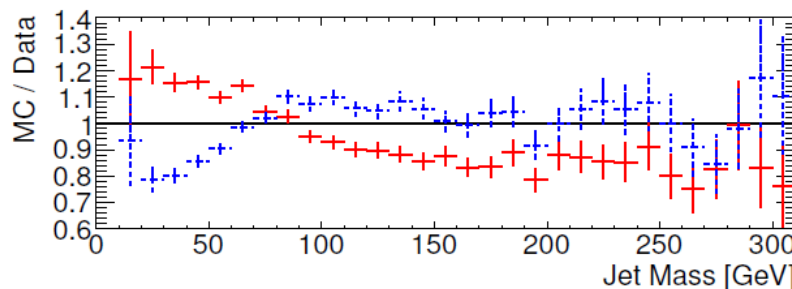
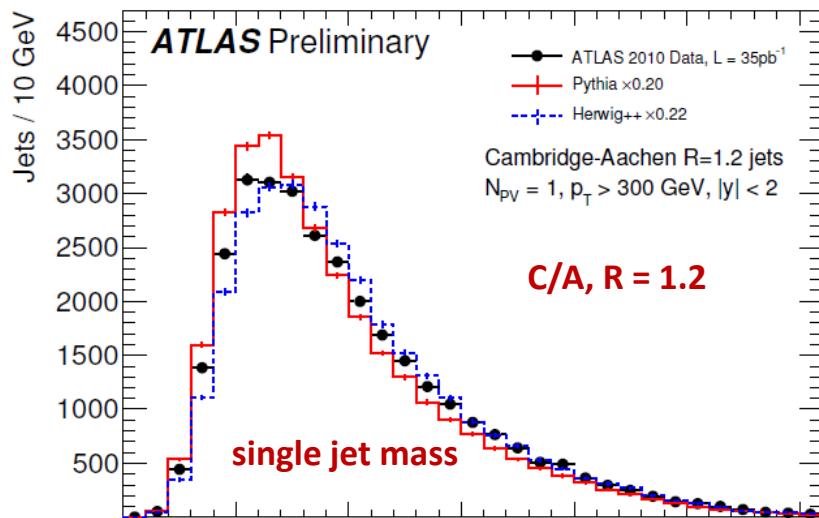
Motivated by boosted object search

Relevant scale for massive particle is (fat) jet distance parameter $R = m_{\text{jet}}/\rho_{T,\text{jet}}$

Jet filtering used to measure mass

Compare mass from all constituents with mass from filtered subjet recombination

(all plots from ATLAS CONF-2011-073)





Mass and internal resolution scales for Anti-k_T

High p_T jets reconstructed w/o meaningful clustering sequence

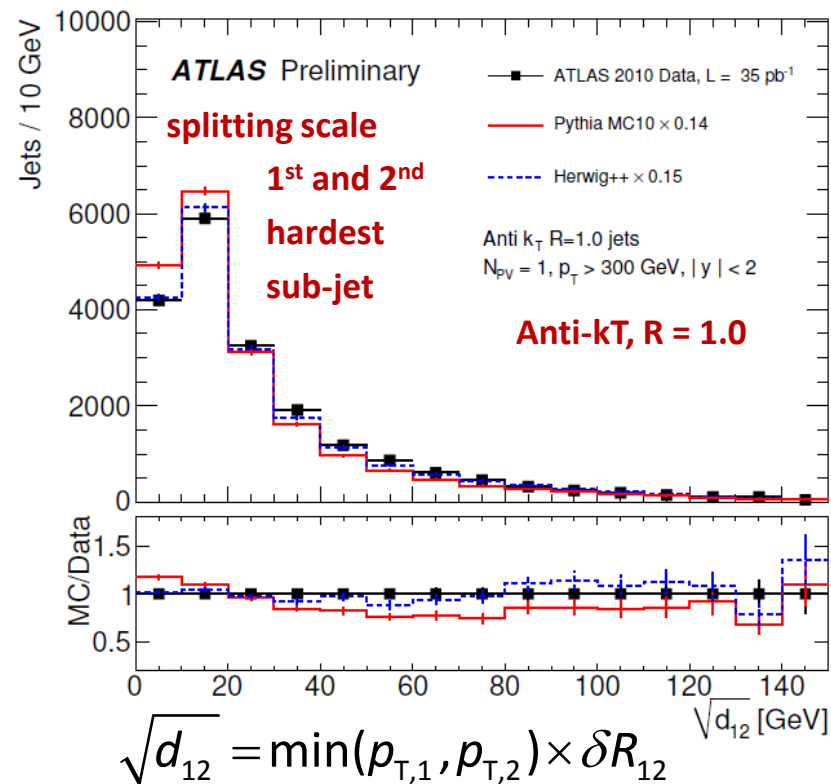
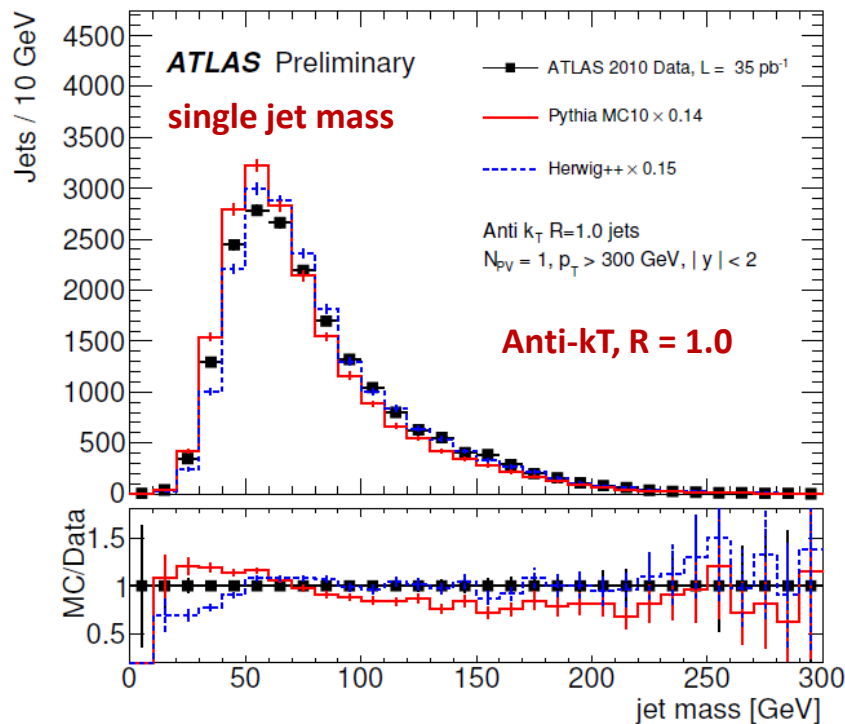
C/A, k_T – meaningful cluster sequences based on distance scales

Anti-k_T – regularly shaped jets with no specific meaning for the clustering sequence

Internal distance scale experimentally challenging

Requires sufficient spatial resolution in clustering

(all plots from ATLAS CONF-2011-073)



$$\sqrt{d_{12}} = \min(p_{T,1}, p_{T,2}) \times \delta R_{12}$$



Not easy to determine

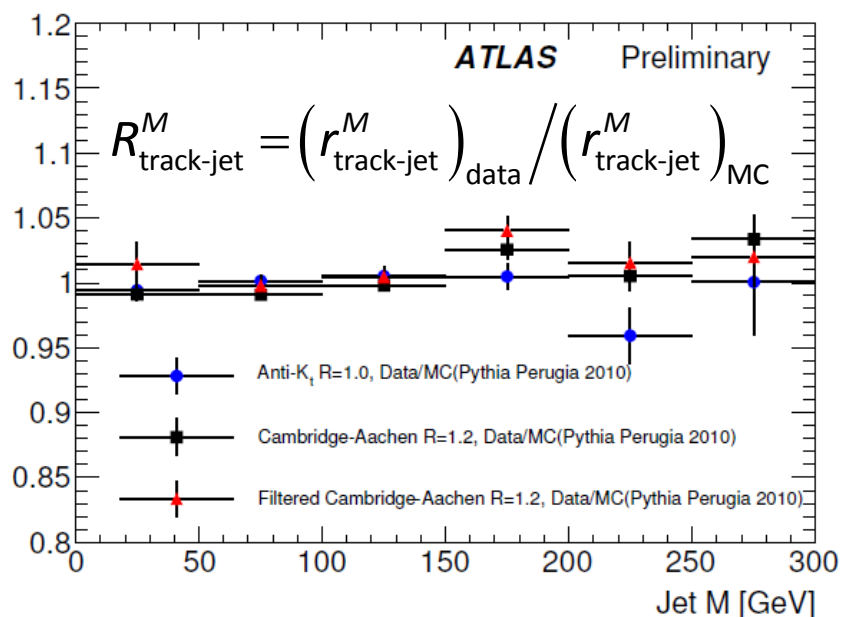
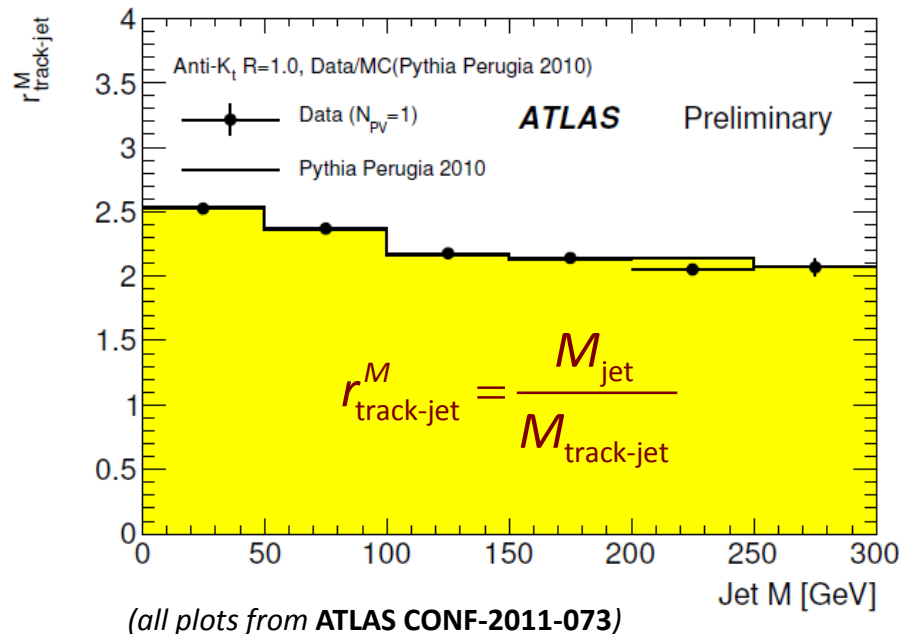
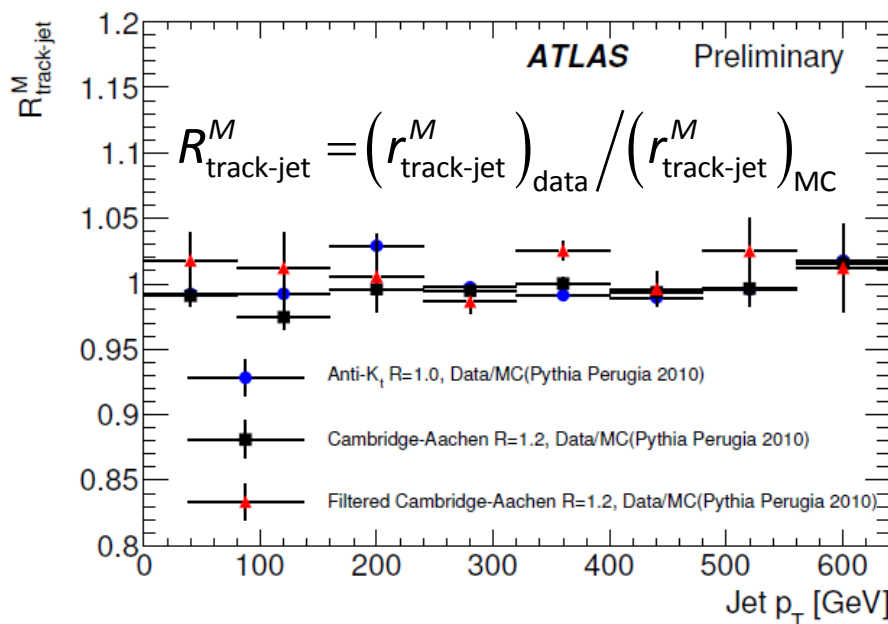
Only full jet systematic uncertainties available

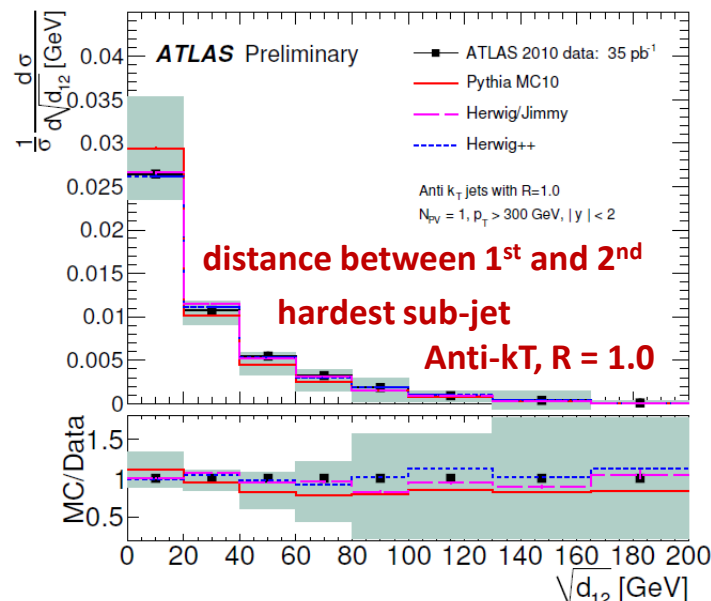
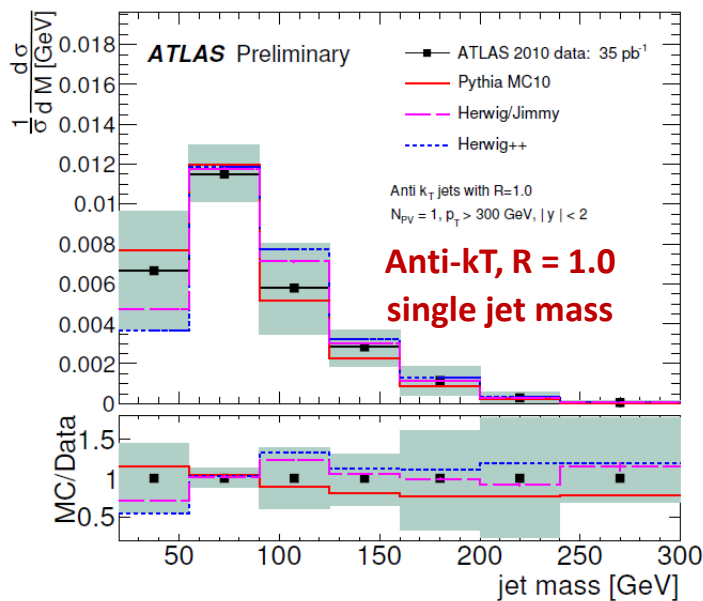
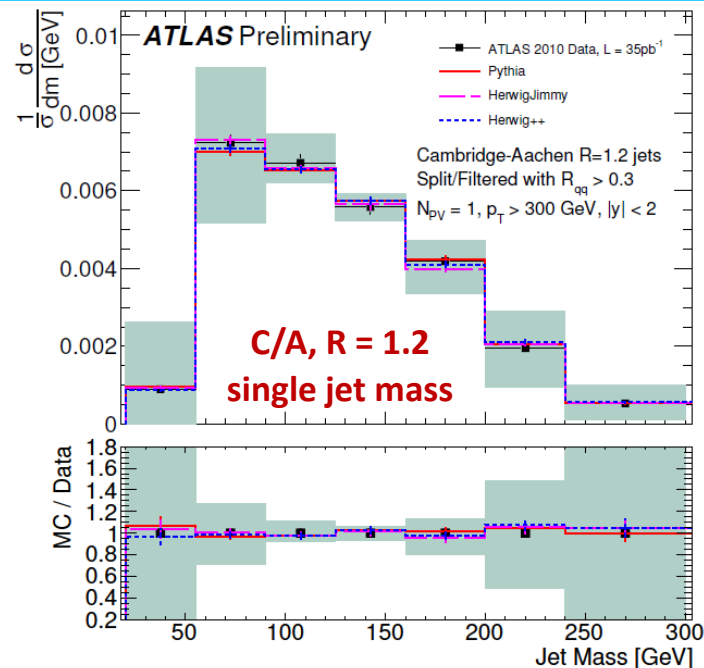
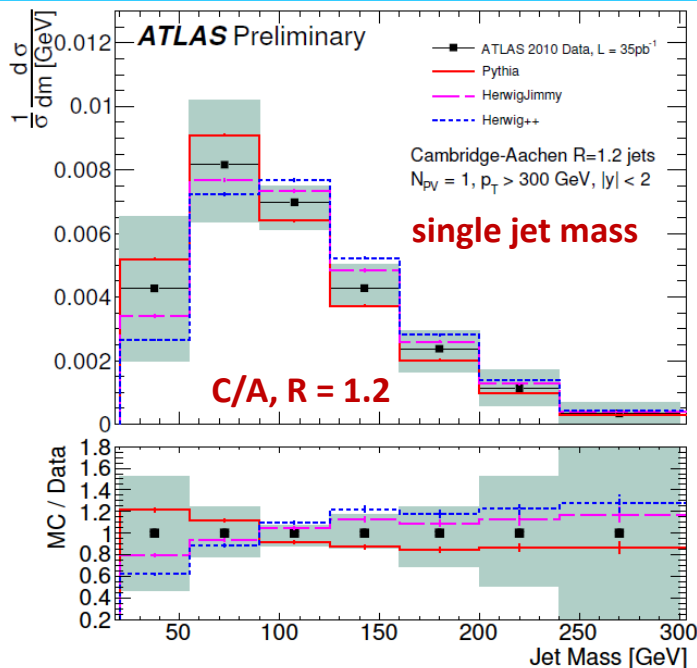
Local energy scales inside jet not well known

Use track jet mass as unbiased reference for calorimeter mass measurement

$$r_{\text{track-jet}}^M = \frac{M_{\text{jet}}}{M_{\text{track-jet}}}$$

Double-ratio MC/data establishes systematics







Pile-up “disturbs” particle flow inside jet

Gain of mass with increasing pile-up expected

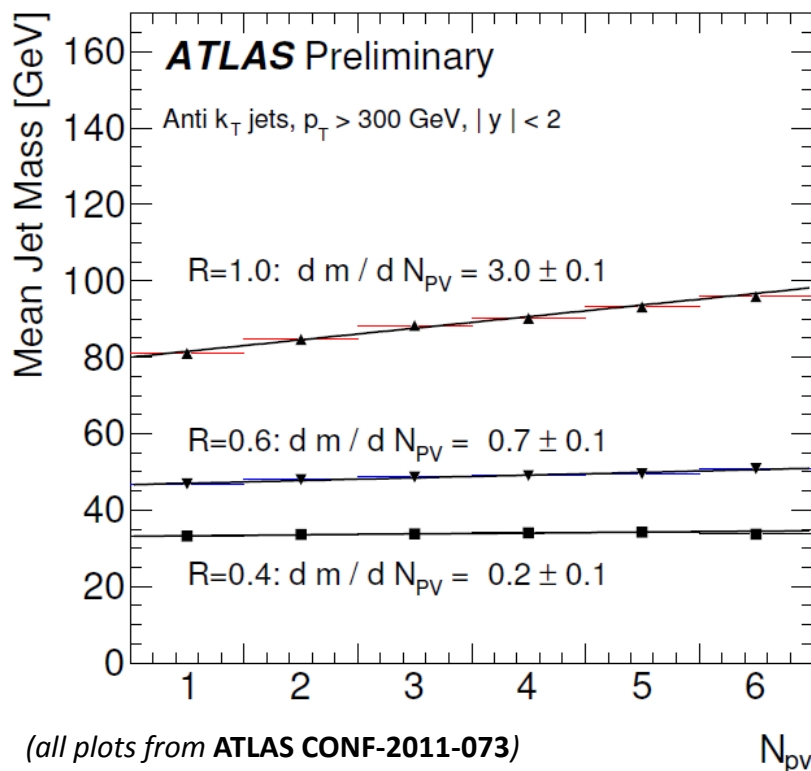
More energy added at larger distance from jet axis

Pure in-time pile-up considered here

ATLAS 2010 data, no pile-up history

Effect strongly reduced for narrow jets

That’s why like Anti-k_T with small distance parameter!



Boosted object search

Prefers substructure in “fat jets”

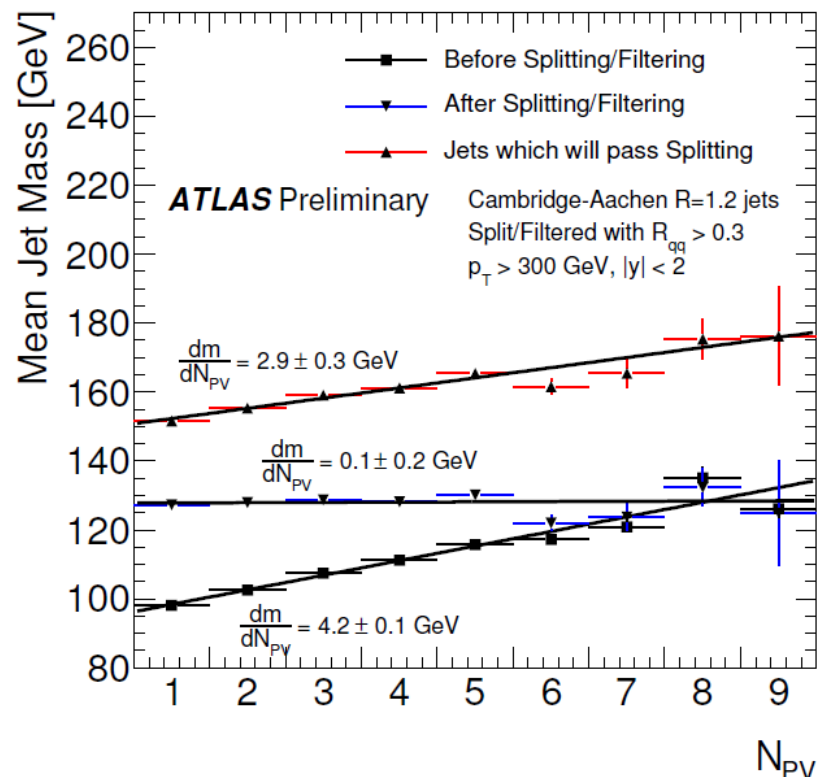
Better extraction of decay structure

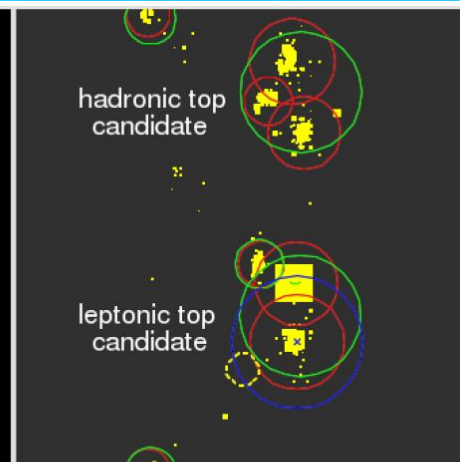
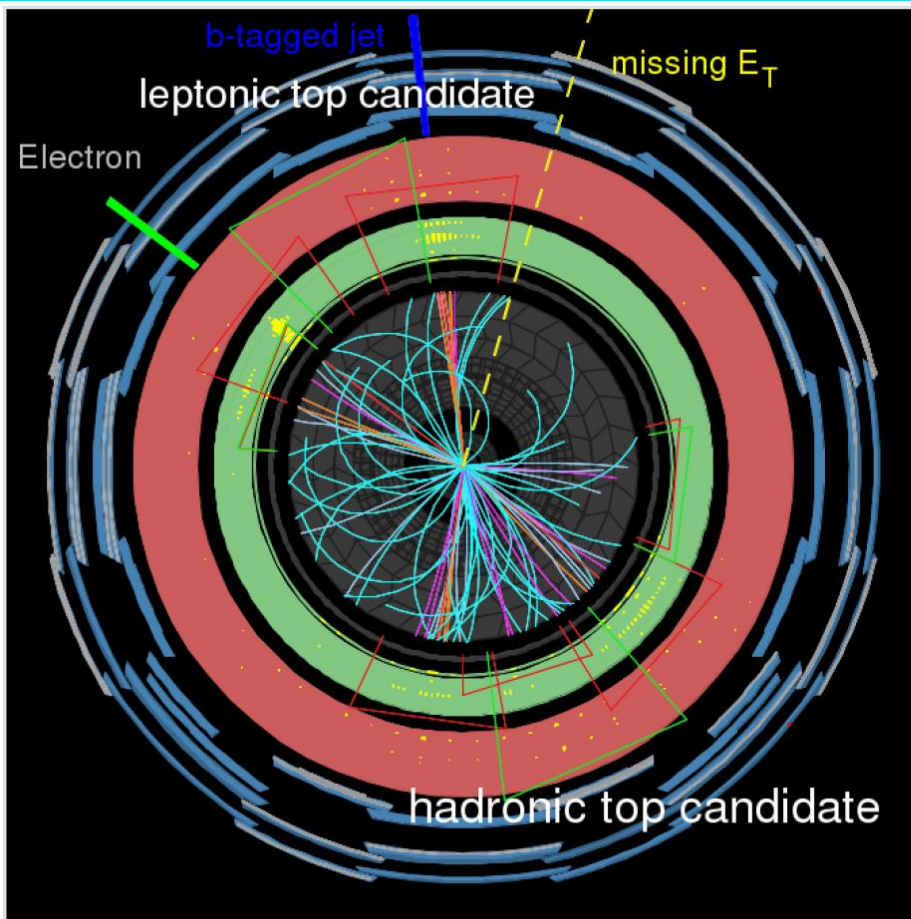
Jet grooming suppresses pile-up

Focuses on hard sub-jet structure

Suppresses soft (pile-up and UE) contributions in jet

First hints that cluster jets are useful for sub-structure analysis in more hostile environment

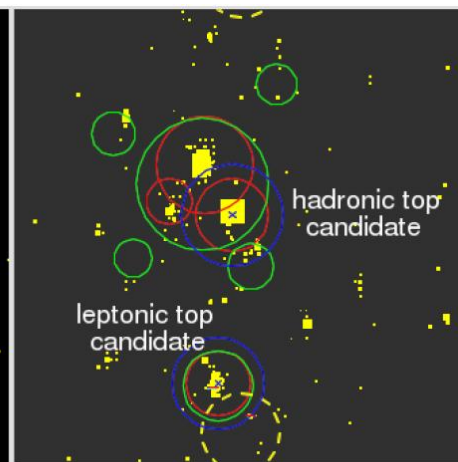
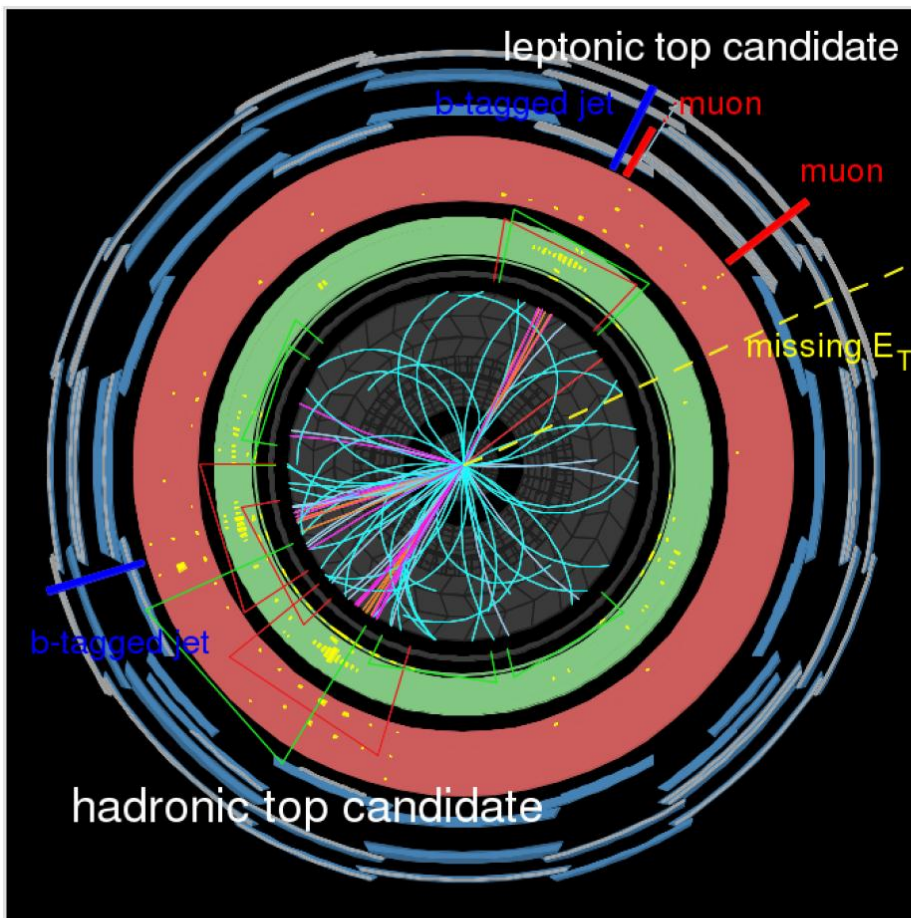





Run Number: 166658, Event Number: 34533931

Date: 2010-10-11 23:57:42 CEST

Leptonic top	$E_T^{miss}: E_T = 36 \text{ GeV}, \phi = -1.5$ electron: $p_T = 145 \text{ GeV}, \eta = 1.1, \phi = 2.5$ jet: index = 1, $E_T = 194 \text{ GeV}, \eta = 1.2, \phi = 1.7, m_j = 17 \text{ GeV}$
Hadronic top ($R = 0.4$ clustering)	jet 2, $E_T = 155 \text{ GeV}, \eta = 1.1, \phi = -0.7 \text{ rad}, m_j = 22.7 \text{ GeV}$ + jet 3, $E_T = 113 \text{ GeV}, \eta = 1.3, \phi = -1.7 \text{ rad}, m_j = 14 \text{ GeV}$ + jet 4, $E_T = 54 \text{ GeV}, \eta = 0.6, \phi = -1.7 \text{ rad}, m_j = 8 \text{ GeV}$
Hadronic top ($R = 1.0$ clustering)	jet 1, $E_T = 356 \text{ GeV}, \eta = 1.3, \phi = -1.1 \text{ rad}, m_j = 197 \text{ GeV}$ $\sqrt{d_{12}} = 110, \sqrt{d_{23}} = 40$



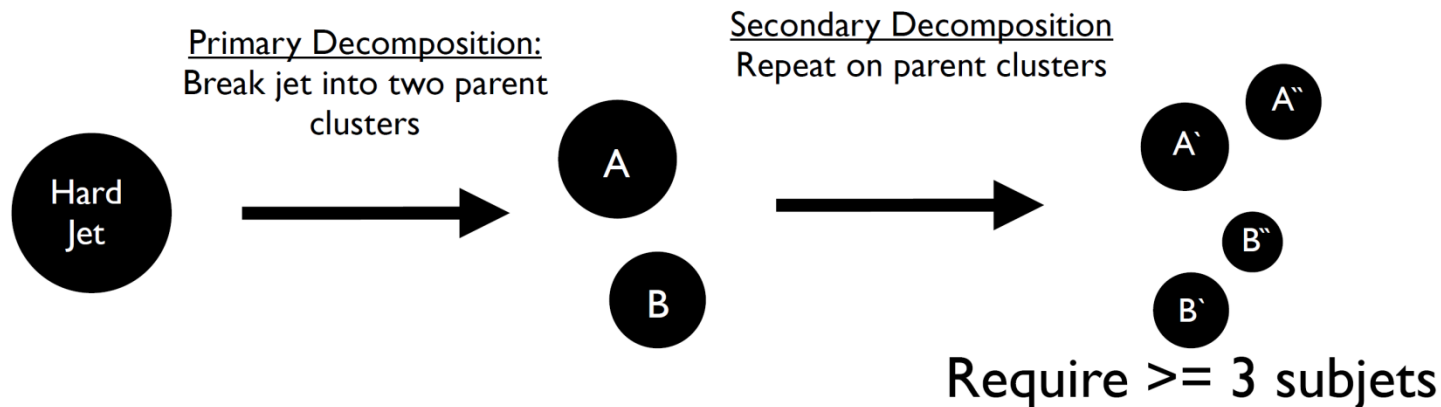
Run Number: 167576, Event Number: 106929590

Date: 2010-10-24 12:10:09 EDT

Leptonic top	$E_T^{miss}: E_T = 159 \text{ GeV}, \phi = 0.4$ muon: $p_T = 114 \text{ GeV}, \eta = 0.21, \phi = 0.66$ jet: index = 3, $E_T = 90 \text{ GeV}, \eta = -0.5, \phi = 1.1, m_j = 11 \text{ GeV}$
Hadronic top ($R = 0.4$ clustering)	jet 1, $E_T = 205 \text{ GeV}, \eta = -0.8, \phi = -2.2 \text{ rad}, m_j = 18.3 \text{ GeV}$ + jet 2, $E_T = 115 \text{ GeV}, \eta = -0.2, \phi = -2.8 \text{ rad}, m_j = 10 \text{ GeV}$ + jet 4, $E_T = 49 \text{ GeV}, \eta = -1.3, \phi = -2.7 \text{ rad}, m_j = 11 \text{ GeV}$
Hadronic top ($R = 1.0$ clustering)	jet 1, $E_T = 418 \text{ GeV}, \eta = -0.8, \phi = -2.4 \text{ rad}, m_j = 225 \text{ GeV}$ $\sqrt{d_{12}} = 105, \sqrt{d_{23}} = 44$

Top Tagging Details

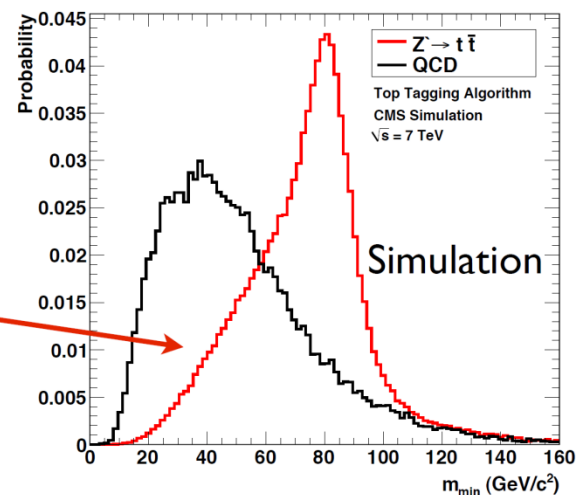
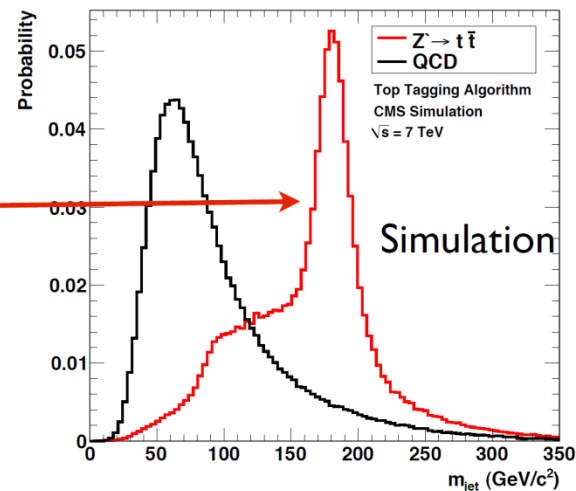
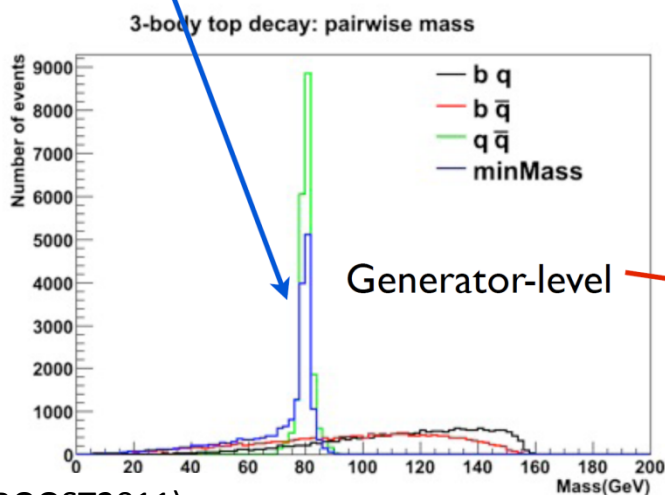
- ✦ Based on Kaplan et al. (arXiv:0806.0848)
- ✦ Cluster particle flow candidates using Cambridge Aachen
- ✦ Reverse the clustering sequence in order to find substructure
- ✦ Subjets must satisfy two requirements
 - Momentum fraction criterion: $p_{T\text{subjet}} > 0.05 \times p_{T\text{hard jet}}$ ← Removes soft clusters
 - Adjacency criterion: $\Delta R(A, B) > 0.4 - 0.0004 \times p_T$ ← Removes wide angle clusters
- ✦ Iterative process - throw out objects that fail momentum fraction cut and try to decluster again



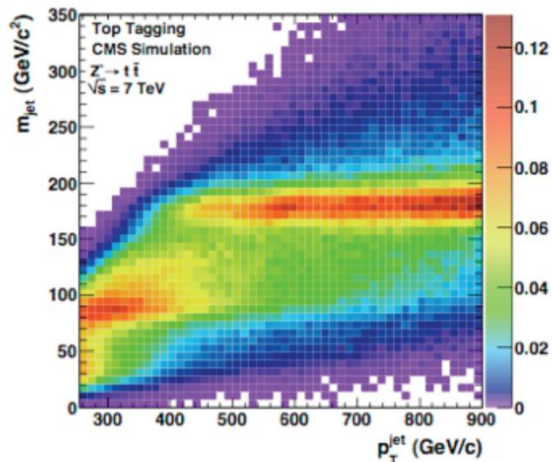
Top Tagging Details

- Discriminating variables:
 - Number of subjets: 3 or 4
 - Top Mass: Approximated by jet mass
 - › Mass in 100-250 GeV/c²
 - W Mass: Approximated by min pairwise mass
 - › Min mass > 50 GeV/c²

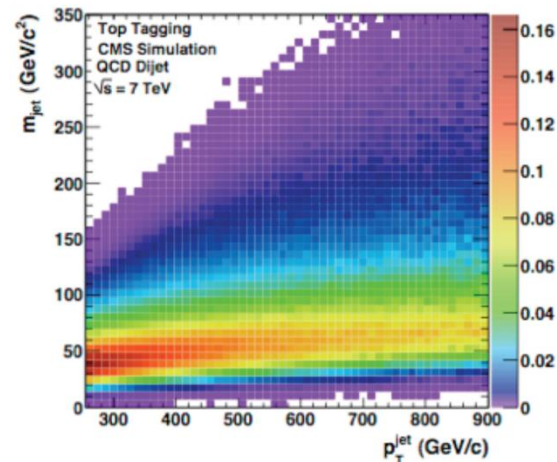
$$m_{\min} = \min[m_{12}, m_{13}, m_{23}]$$



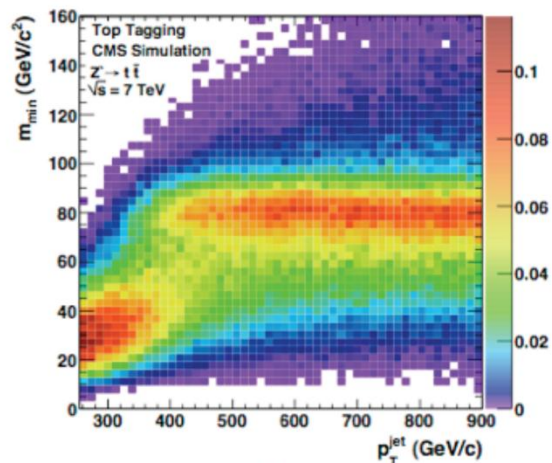
Top Tagging Details



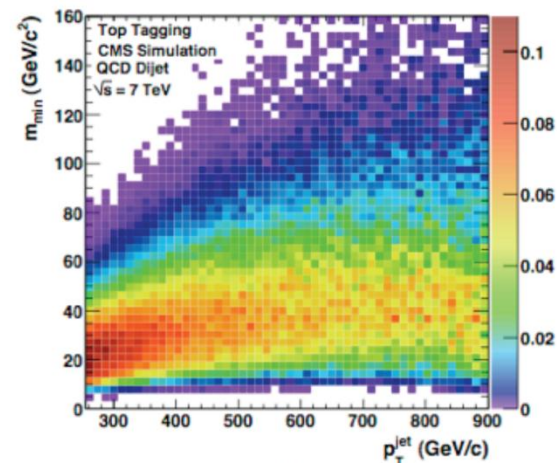
(a)



(b)



(c)



(d)



Top Tagging Mistag Rate

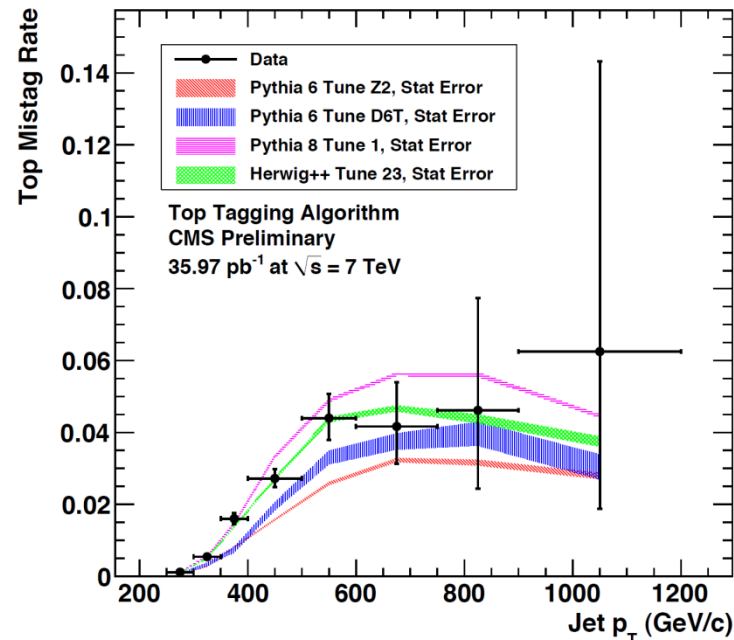
- Anti-tag and probe method
 - Randomly select one jet, check if its tagged
 - If the random jet is vetoed, the opposite jet is the probe jet



Anti-tagged jet
(mass < 140 or mass > 250 or
minmass < 50 or nsubjets < 3)

Probe jet

$$\text{Mistag Rate} = \frac{\text{Number of probe jets that are tagged}}{\text{Number of probe jets}}$$



Dependence on shower model and
tune, overall good agreement





First look at jet substructure in LHC collision data

Very promising indications of sufficient experimental performance to be useful

Limitations not yet quite understood – need massive and well known jet sources for performance evaluations

It's all kind of new for experimentalists...

All standard substructure tools (filtering, trimming, pruning) are evaluated

Newer approaches are under study (decomposition w/o trees, N sub-jettiness...)

Future experimental focus

Next on the list: boosted top

First events available – allows to understand resolution, scales, pile-up,...

Sub-structure tools for in-jet pile-up suppression

Non-search paradigm – which tool(s) are useful to suppress jet structure introduced by pile-up? Trimming and simple filtering may be candidates...

Must be applicable to gluon/quark jets

Improve general jet mass reconstruction

More tagging

Gluon/(light) quark jet tagging with sub-structure tools (e.g., N sub-jettiness)

Combining detectors (outside of particle flow reconstruction a la CMS)

Use of track sub-jets to guide calorimeter sub-jet finding, reconstruction and calibration

Generic testbeds

Quick evaluation of new strategies wrt typical experimental signal features and limitations

Particle level may not be sufficient for evaluation – lateral (and longitudinal) energy distributions important for sub-jets,...

Hard to provide realistic fast simulation of generic (“typical”) LHC detector

We are looking into it in the context of the BOOST workshops...



Additional Slides



Electromagnetic showers

Particle cascade generated by electrons/positrons and photons in matter

Developed by bremsstrahlung & pair-production

Compact signal expected

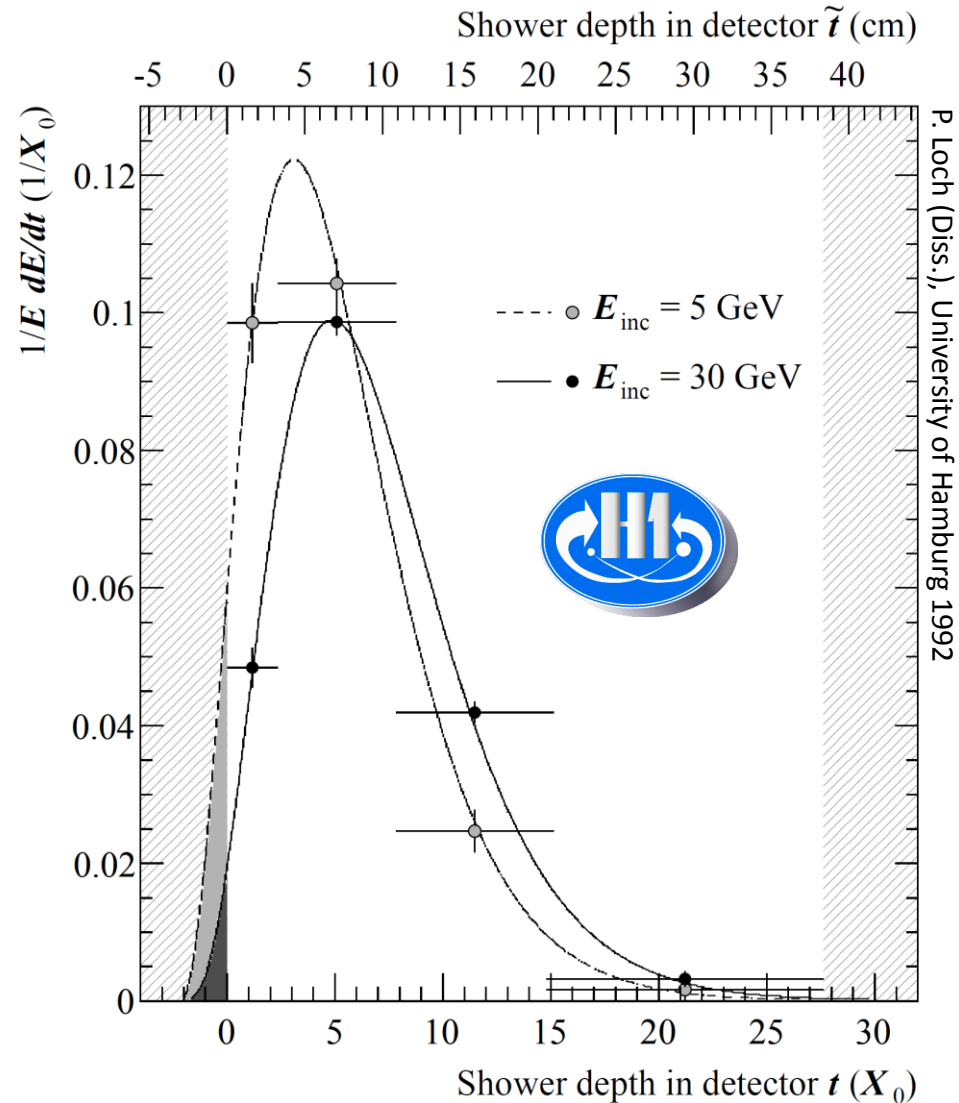
Regular shower shapes

Small shower-to-shower fluctuations

Strong correlation between longitudinal and lateral shower spread



RD3 note 41, 28 Jan 1993





Electromagnetic showers

Particle cascade generated by electrons/positrons and photons in matter

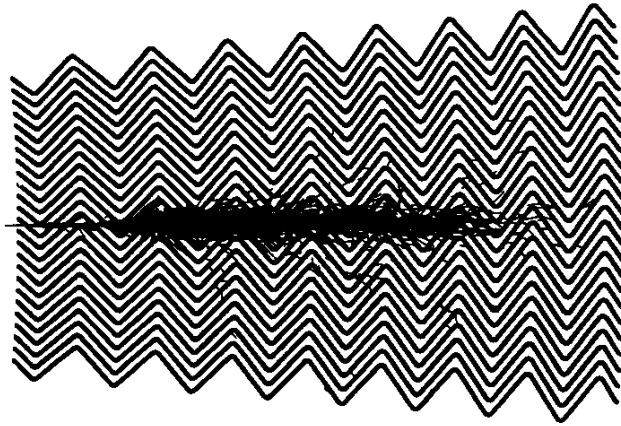
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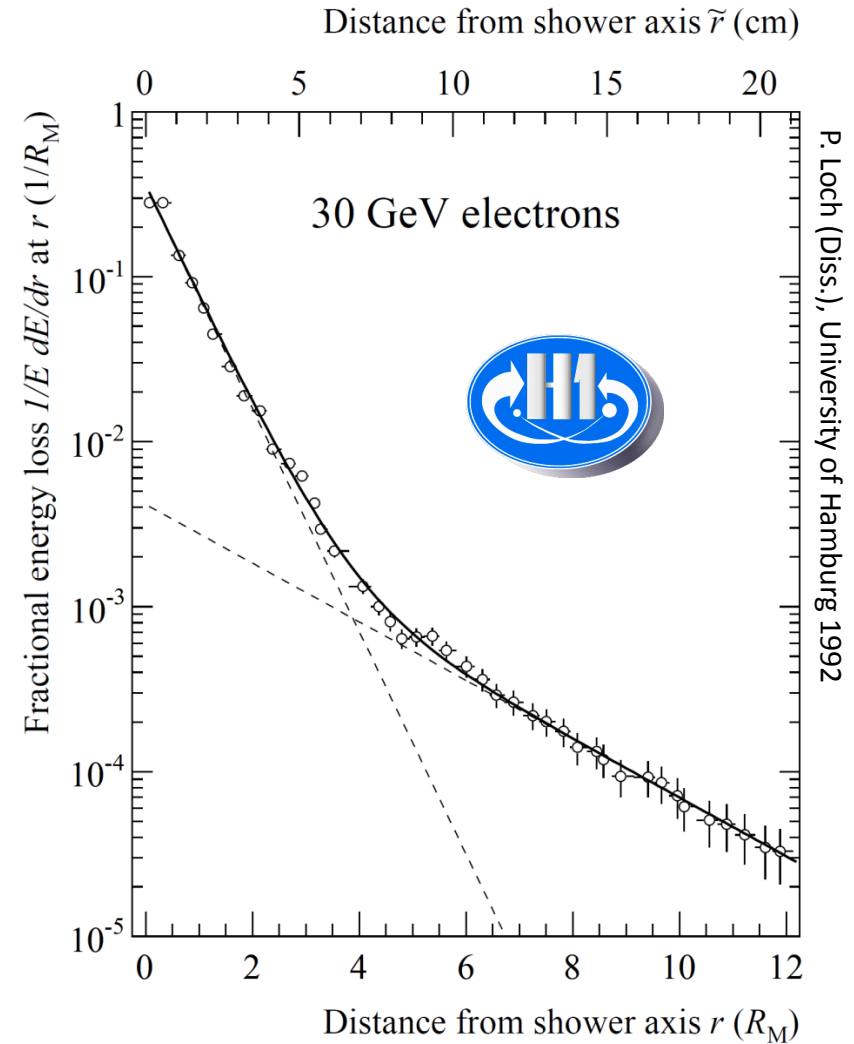
Regular shower shapes

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RD3 note 41, 28 Jan 1993



$$\frac{1}{E} \frac{dE}{dr} = a(E) \cdot e^{-\alpha(E)r} + b(E) \cdot e^{-\beta(E)r}$$



Hadronic signals

Much larger showers

- Need deeper development
- Wider shower spread

Large energy losses without signal generation in hadronic shower component

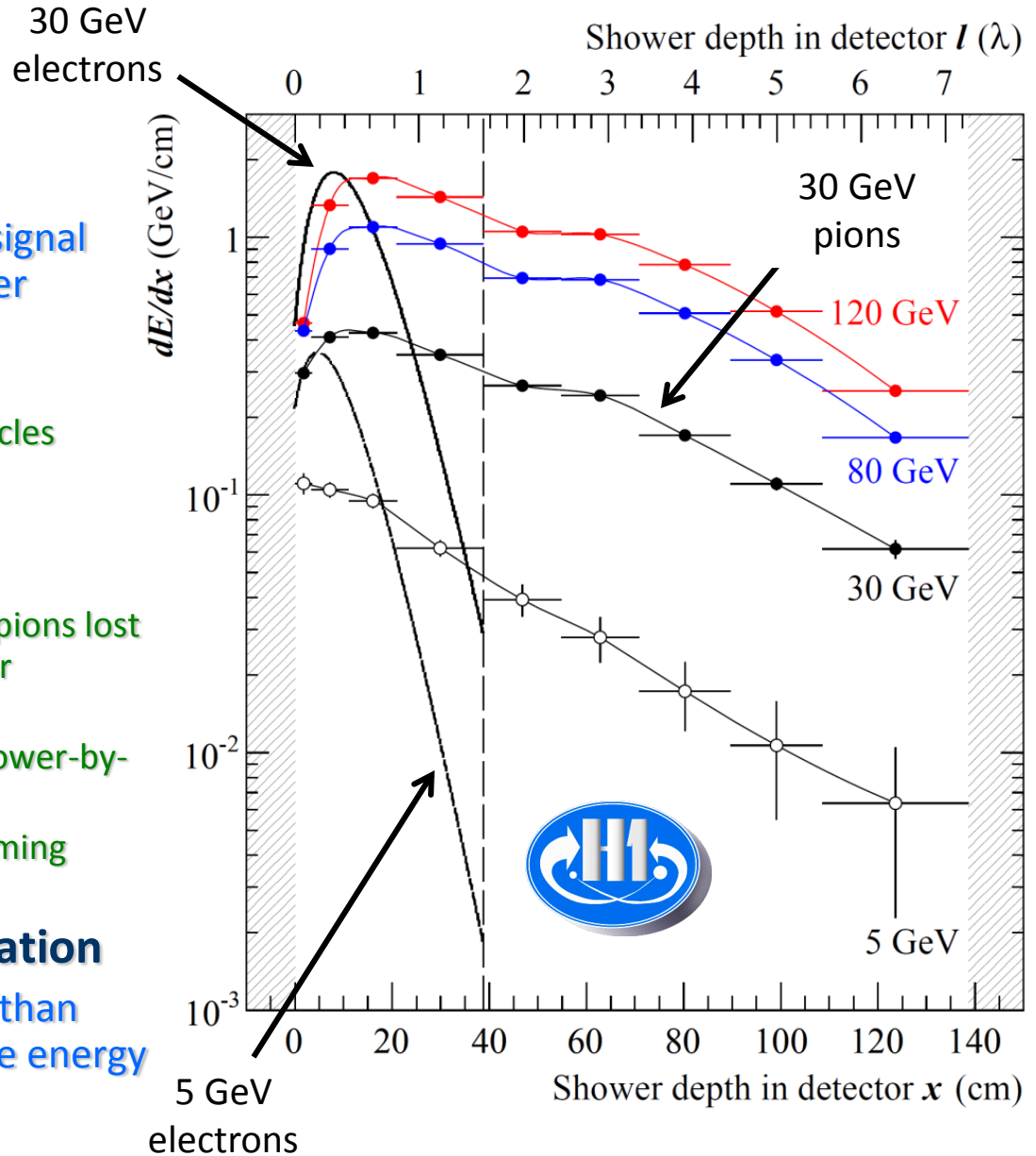
- Binding energy losses
- Escaping energy/slow particles (neutrinos/neutrons)

Signal depends on size of electromagnetic component

- Energy invested in neutral pions lost for further hadronic shower development
- Fluctuating significantly shower-by-shower
- Weakly depending on incoming hadron energy

Consequence: non-compensation

Hadrons generate less signal than electrons depositing the same energy





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