Neutral meson mixing (Beauty)

IPPP workshop on Flavour and the 4th family



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Mixing formalism in a nutshell

- neutral meson mixing: matter changes spontaneously into anti-matter!
- occurs in SM via this 2nd order diagram



mixing and decay generically described by Schrodinger-like equation

$$i\frac{\mathrm{d}}{\mathrm{d}t} \begin{pmatrix} \langle B^{0}|B(t)\rangle\\ \langle \bar{B}^{0}|B(t)\rangle \end{pmatrix} = \begin{pmatrix} M_{11} - \frac{i}{2}\Gamma_{11} & M_{12} - \frac{i}{2}\Gamma_{12}\\ M_{21} - \frac{i}{2}\Gamma_{21} & M_{22} - \frac{i}{2}\Gamma_{22} \end{pmatrix} \begin{pmatrix} \langle B^{0}|B(t)\rangle\\ \langle \bar{B}^{0}|B(t)\rangle \end{pmatrix}$$

$$\begin{pmatrix} \bullet & \text{M and } \Gamma \text{ are hermitian:} & M_{ij} = M_{ji}^{*} & \Gamma_{ij} = \Gamma_{ij}^{*}\\ \bullet & \text{CPT invariance:} & M_{11} = M_{22} & \Gamma_{11} = \Gamma_{22} \end{pmatrix}$$

$$\bullet \text{ phase difference of B0 and B0-bar is arbitrary}$$

--> 5 physical parameters: $M \ \Gamma \ |M_{12}| \ |\Gamma_{12}| \ \phi = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right)$

From parameters to observables

time-evolution --> mass eigenstates

$$|B_L\rangle = p|B^0\rangle + q|\overline{B}^0\rangle |B_H\rangle = p|B^0\rangle - q|\overline{B}^0\rangle$$

with eigenvalues

$$m_L + \frac{i}{2}\Gamma_L$$
$$m_H + \frac{i}{2}\Gamma_H$$

usually characterised by observables

$$M \equiv \frac{m_H + m_L}{2} \qquad \Delta M \equiv m_H - m_L \qquad \Gamma \equiv \frac{\Gamma_H + \Gamma_L}{2} \qquad \Delta \Gamma \equiv \Gamma_L - \Gamma_H \qquad \frac{q}{p}$$

that can (within reasonable approximation) be expressed as

$$\begin{split} \Delta M \simeq 2|M_{12}| & \Delta \Gamma \simeq 2|\Gamma_{12}|\cos\phi & 1 - \left|\frac{q}{p}\right|^2 \simeq \left|\frac{\Gamma_{12}}{M_{12}}\right|\sin\phi \\ & & & & & \\ & & & & & \\ mixing \ frequency & decay \ width \ difference & CP \ violation \ in \ mixing \ frequency & & \\ \end{split}$$

From parameters to observables

observables sensitive to NP in mixing



 $M_{12} = M_{12}^{\rm SM} r^{\rm NP} e^{i\phi^{\rm NP}} \qquad \phi = \phi^{\rm SM} + \phi^{\rm NP}$

- in the SM, the phase ϕ is small both in Bd and in Bs
- NP models usually only consider contributions to M₁₂

constrained by mixing frequency

 $\frac{b}{q} \stackrel{W^+}{\longrightarrow} \frac{q}{W} \frac{q}{b}$

constrained by CPV and $\Delta\Gamma$

Experimental observables: mixing frequency

decay time allows to observe time-evolution



Experimental observables: mixing frequency

decay time allows to observe time-evolution



"tagging B" can be charged or neutral

Iook at "flavour specific" decays, e.g.





Experimental observables: mixing frequency

decay time allows to observe time-evolution



mixing frequency: count 'mixed' versus 'unmixed'

$$A^{ ext{mix}}(t) \;=\; rac{N^{ ext{unmixed}} - N^{ ext{mixed}}}{N^{ ext{unmixed}} + N^{ ext{mixed}}} \;=\; \cos\Delta M t$$

measurement requires flavour tagging and decay time measurement

Experimental observables: A_{SL}

decay time allows to observe time-evolution



from same observables, create CP asymmetry

$$a_{fs} \equiv \frac{N^{++} - N^{-}}{N^{++} + N^{-}} = \frac{1 - |q/p|^4}{1 + |q/p|^4}$$
 decay time independent

- to probe CPV in mixing, use final state with zero predicted CPV in decay
- sometimes also called "semi-leptonic" asymmetry
- measurement requires very precise knowledge of detection asymmetries

Experimental observables: TD CPV

now consider "non-flavour specific decays"



interference between mixing and decay: "time-dependent CP violation"

$$A_{CP}(t) \;\equiv\; rac{N(\overline{B}
ightarrow f) - N(B
ightarrow f)}{N(\overline{B}
ightarrow f) + N(B
ightarrow f)} \;=\; m{S} \; \sin(\Delta m_q t)$$

- gives access to phase of mixing diagram
- measurement requires not only tagging and decay time, but also knowledge of their respective *dilutions*

Di-muon charge asymmetry

mixing leads to 'wrong charge' combinations in B->X mu



measure CPV in mixing via wrong charge asymmetry

$$A_{\rm fs}^b \equiv \frac{N_b(\mu^+\mu^+) - N_b(\mu^-\mu^-)}{N_b(\mu^+\mu^+) + N_b(\mu^-\mu^-)}$$
 CPV

at hadron collider: method does not distinguish between Bd and Bs
 --> measure linear combination with physics in

$$A_{\rm fs}^b = C a_{\rm fs}^d + (1 - C) a_{\rm fs}^s$$

function of fragmentation fractions, mixing parameters, lifetimes and decay time acceptance

• with value of C at Tevatron: $A^b_{sl}(SM) = (-0.023^{+0.005}_{-0.006})\%$

parameter

 $a_{\rm fs}^q = \frac{\Delta \Gamma_q}{\Delta M_z} \tan \phi$

Di-muon charge asymmetry at D0

- experimentally very challenging
 - asymmetries in muon detection efficiency
 - asymmetries in backgrounds (e.g. muons from Kaon decay)
- main player: D0 at Tevatron
 - Iow detection asymmetry due frequent field polarity changes
 - control of background asymmetries using single muon asymmetry
- recent D0 update, arXiv:1106.6308, subm. to PRD:

$$A_{sl}^b = (-0.787 \pm 0.172 \pm 0.093)\%$$

3.9 σ deviation from SM

- consistent with other measurements
 ... but single one of its kind
- burning question: is it B_d or B_s?

need to be controlled to better than 0.001!



Di-muon charge asymmetry at D0

Entries

• to probe origin, split sample by IP cut to change fraction of Bd



- IP>120 (both muons)
 - less background
 - higher Bd fraction
- result consistent with main result
- extract

 $a_{sl}^d = (-0.12 \pm 0.52)\%$ $a_{sl}^s = (-1.81 \pm 1.06)\%$

with large correlation $\rho_{ds} = -0.799$

uncertainties too large to be conclusive ...



LHCb plans for a_{fs}

- additional experimental challenge: <u>production</u> asymmetry (no problem for Bs)
- studies concentrate on B -> D I nu, with fully reconstructed D
 - less background than inclusive muons
 - can distinguish Bs from Bd
 - reasonable decay time resolution --> can do time-dependent measurement
- but ... exclusive reconstruction has a price
 - to regain statistics, perform <u>untagged</u> measurements
 - untagged rate related to flavour-specific asymmetry by

$$a_{\rm fs,unt}(t) = \frac{a_{\rm fs}}{2} \left(1 - \frac{\cos(\Delta M t)}{\cosh(\Delta \Gamma t/2)} \right)$$

note: in contrast to a_{fs} , not constant in time

LHCb plans for a_{fs}

- two strategies to tackle production/detection asymmetries
 - 1. take only Bs, measure detection asymmetry in control samples
 - 2. measure the (time-dependent) difference

 $\Delta A = A(B_s \to D_s(KK\pi)\mu X) - A(B_d \to D(KK\pi)\mu^- X)$



actual attainable uncertainties still very unclear

Oscillations in the Bs system

- oscillation frequency places strong constraints on new physics
 - SM prediction: $\Delta m_s^{
 m SM} = 16.8^{+2.6}_{-1.5}~{
 m ps}^{-1}$ PRD.83, 036004 (211)
- method: time-dependence of mixing asymmetry for a flavour-specific final state

$$A^{ ext{mix}} \ = \ rac{N^{ ext{unmixed}}(t) - N^{ ext{mixed}}(t)}{N^{ ext{unmixed}}(t) + N^{ ext{mixed}}(t)} \ = \ \cos(\Delta m t)$$

- experimental requirements
 - flavour tag at 'production'
 - reconstruction of decay time

$$A^{ ext{mix}} = (1 - 2w) \times e^{-\Delta m^2 \sigma_t^2/2} \times \cos(\Delta m t)$$

finite decay time resolution
probability for wrong flavor tag

- optimal time resolution requires fully reconstructed final state
 - ${}$ most easily accessible: $B_s o D_s^- \pi^+$

ignoring $\Delta\Gamma$

Bs mixing: latest measurement

LHCb update in 341/pb, presented at Lepton-Photon 2011



- average time resolution: ~44 fs
- flavour tagger performance:
 - OST: $\epsilon(1-2w)^2 = (3.2\pm0.8)~\%$
 - SST: $\epsilon (1-2w)^2 = (1.3 \pm 0.4) \%$

reduction in signal ➤ efficiency due to loss/dilution from taggin_{\$6}

Bs mixing: latest measurement

LHCb, preliminary result, 341/pb (LHCb-CONF-2011-050)



Oscillations in the Bd system





LHCb preliminary result, using Bd->Dpi in 37/pb

 $\Delta M_d ~=~ 0.499 \pm 0.032 \pm 0.003$

(LHCb-CONF-2011-010, prelim.)

- first priority is to get much more stats; systematics can probably be reduced too
- Bd->D*μν gives much higher yields, but systematics not clear yet

CPV in mixing via time-dependent CPV

mixing induced CPV due to interference in decays to common final state

$$B^{0} \xrightarrow{\phi_{D}} f$$
if f is CP eigenstate, time dependent CP violation with pattern
$$A_{CP}(t) \equiv \frac{N(\overline{B} \to f) - N(B \to f)}{N(\overline{B} \to f) + N(B \to f)} = S \sin(\Delta m_{q}t)$$
flavor at production
$$S = \sin(\phi_{M} - 2\phi_{D})$$

- b->ccs transitions: decay dominated by TREE amplitude ==> expect no NP in ϕ_{D} ==> CPV probes mixing phase ϕ_{M}
- 'golden' modes: $B_d o \psi K_s: S = \sin 2\beta$ $B_s o \psi \phi: S = \sin 2\beta_s$

sin2 β from J/ Ψ K_s, J/ Ψ K_L (etc)

final Belle/Babar datasets



one part of the problem: correlation with the measurement of B->tau nu in the fits



penguin pollution

suppressed contributions may 'pollute' expected CPV

 $S_{\Psi K} = \sin(2eta + \delta^{ ext{SM penguins}} + \phi^{ ext{NP}}_{m{d}})$

[need picture plus result of U-spin symmetry]

- can estimate contributions with BF of suppressed modes related by symmetry
 - Bd --> J/psi pi0 and Bs --> J/psi Ks (PRD79 (2009) 014030)



(question: based on this, what are estimates of 'penguin' polution?)

CPT and $\Delta \Gamma_{d}/\Gamma_{d}$

introduce complex parameter for CPT violation (see e.g. PRD70(2004)012007)

$$\mathbf{Z} = \frac{\delta m - \frac{i}{2}\,\delta\Gamma}{\Delta m - \frac{i}{2}\Delta\Gamma} \longrightarrow \begin{vmatrix} |B_L\rangle &= p\sqrt{1-\mathbf{z}}|B^0\rangle + q\sqrt{1+\mathbf{z}}|\overline{B}^0\rangle \\ |B_H\rangle &= p\sqrt{1+\mathbf{z}}|B^0\rangle - q\sqrt{1-\mathbf{z}}|\overline{B}^0\rangle$$

- extract from simultaneous analysis of CP and flavour specific states
- new result, Belle EPS2011 (prelim.):

```
\operatorname{Re}(z) = (+1.9 \pm 3.7 \pm 3.2) \times 10^{-2}
   Im(z) = (-5.7 \pm 3.3 \pm 6.0) \times 10^{-3}
\Delta \Gamma_d / \Gamma_d = (-1.7 \pm 1.8 \pm 1.1) \times 10^{-2}
                                 535 x 10<sup>6</sup> BB pairs
```

compatible with Babar analysis on 88M/232M BBbar pairs

bonus: strongest single-experiment constraint on $\Delta\Gamma/\Gamma$ compare SM:

$$rac{\Delta \Gamma_d}{\Gamma_d}^{
m SM} = (5.8^{+1.1}_{-2.1}) \cdot 10^{-3}$$

(my comp. using $\Delta\Gamma$ from SM fit in PRD83,036004 (2011) and PDG lifetime)

time-dependent CPV in the B_s-system

• time-dependent CPV in $B_s
ightarrow J/\psi \phi\,$ allows to NP in mixing in Bs system

 $S_{\Psi\phi}\equiv "\sin\phi_s"=\sin(-2eta_s^{
m SM}+\phi_s^{
m NP})$

• in contrast to β , CKM-angle β_s is very small

 $-2\beta_s^{
m SM}~=~(-2.08\pm0.10)^\circ$

(PRD83, 036004 (2011))

two most interesting modes



- narrow resonance --> clean
- vector-vector final state ("P-wave")
 - requires time-dependent angular analysis
 - measure also $\Delta \Gamma_s$ w/o external input



- bit lower branching fraction
- vector-pseudoscaler final state ("S-wave")
 - no angular analysis needed

β_s with $B_s^{-->}J/\Psi\phi$

- status quo, before LP2011
 - CDF 5.2/fb, about 6500 events, $\sigma(\phi_s) \sim 0.5$ rad
 - D0 9/fb, about 5000 events, $\sigma(\phi_s) \sim 0.35$ rad
 - LHCb 37/pb, about 800 events, , $\sigma(\phi_{s})$ ~ 0.7 rad



- LHCb at LP2011: update with 341/pb
 - about 10x more statistics
 - important improvement: account for S-wave contribution

$B_s ightarrow J/\psi \phi\,$ at LHCb

including S-wave: from 6 to 10 terms in angular/time distributions

LHCb-CONF-2011-049

k	$h_k(t)$	$f_k(\theta, \psi, \varphi)$
1	$ A_0 ^2(t)$	$2\cos^2\psi(1-\sin^2\theta\cos^2\phi)$
2	$ A_{\parallel}(t) ^2$	$\sin^2\psi(1-\sin^2\theta\sin^2\phi)$
3	$ A_{\perp}(t) ^2$	$\sin^2 \psi \sin^2 \theta$
4	$\Im(A_{\parallel}(t) A_{\perp}(t))$	$-\sin^2\psi\sin2\theta\sin\phi$
5	$\Re(A_0(t)A_{\parallel}(t))$	$\frac{1}{2}\sqrt{2}$ sin $2\psi \sin^2 \theta \sin 2\phi$
6	$\Im(A_0(t)A_{\perp}(t))$	$\frac{1}{2}\sqrt{2} \sin 2\psi \sin 2\theta \cos \phi$
7	$ A_{s}(t) ^{2}$	$\frac{2}{3}(1 - \sin^2\theta \cos^2\phi)$
8	$\Re(A_s^*(t)A_{\parallel}(t))$	$\frac{1}{3}\sqrt{6}\sin\psi\sin^2\theta\sin 2\phi$
9	$\Im(A^*_{s}(t)A_{\perp}(t))$	$\frac{1}{3}\sqrt{6}\sin\psi\sin 2\theta\cos\phi$
10	$\Re(A^*_s(t)A_0(t))$	$\frac{4}{\pi}\sqrt{3}\cos\psi(1-\sin^2\theta\cos^2\phi)$

The terms 7–10 are related to the description of the S-wave component, which has been added to this analysis. Expressed in terms of the size $|A_t(0)|$ and phase δ_t of the transversity and S-wave amplitudes at t = 0, the time dependent amplitudes are given by

$$\begin{split} |A_0|^2(t) &= |A_0|^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta m t)], \quad (4) \\ |A_{\parallel}(t)|^2 &= |A_{\parallel}|^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta m t)], \quad (5) \\ |A_{\perp}(t)|^2 &= |A_{\perp}|^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t)], \quad (6) \\ \Im(A_{\parallel}(t)A_{\perp}(t)) &= |A_{\parallel}||A_{\perp}|e^{-\Gamma_s t} [-\cos(\delta_{\perp} - \delta_{\parallel})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\cos(\delta_{\perp} - \delta_{\parallel})\cos\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{\parallel})\cos(\Delta m t)], \quad (7) \\ \Re(A_0(t)A_{\parallel}(t)) &= |A_0||A_{\parallel}|e^{-\Gamma_s t} \cos(\delta_{\parallel} - \delta_{0})[\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &+\sin\phi_s \sin(\Delta m t)], \quad (8) \\ \\ \Im(A_0(t)A_{\perp}(t)) &= |A_0||A_{\perp}|e^{-\Gamma_s t} [-\cos(\delta_{\perp} - \delta_{0})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\cos(\delta_{\perp} - \delta_{0})\cos\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{0})\cos(\Delta m t)], \quad (10) \\ \Re(A_s(t)|^2 &= |A_s|^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t), \\ &+\cos(\delta_{\parallel} - \delta_s)\cos(\Delta m t)], \quad (11) \\ \Re(A_s^*(t)A_{\parallel}(t)) &= |A_s||A_{\parallel}|e^{-\Gamma_s t} [-\sin(\delta_{\parallel} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin(\delta_{\parallel} - \delta_s)\cos\phi_s \sin(\Delta m t) \\ &+\cos(\delta_{\parallel} - \delta_s)\cos(\Delta m t)], \quad (12) \\ \Re(A_s^*(t)A_{\perp}(t)) &= |A_s||A_{\parallel}|e^{-\Gamma_s t} [-\sin(\delta_{\parallel} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\sin\phi_s \sin(\Delta m t)], \quad (12) \\ \Re(A_s^*(t)A_{0}(t)) &= |A_s||A_{\parallel}|e^{-\Gamma_s t} [-\sin(\delta_{0} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\sin(\delta_{0} - \delta_{0})\cos\phi_s \sin(\Delta m t) + \cos(\delta_{0} - \delta_{0})\cos(\Delta m t)]. \quad (13) \end{aligned}$$

where we have chosen a phase convention such that $\delta_0 = 0$. The decay time dependent decay rates for an initial $\overline{B_s^0}$ decaying to $J/\psi\phi$ can be obtained from those above by inserting a factor -1 in front of the terms involving mixing $(\sin(\Delta m_s t) \operatorname{and} \cos(\Delta m_s t))$.

accounts for ~4% "non-resonant" KK in 12 MeV mass window around phi



note: S-wave contribution identified by angular distribution, not by KK mass

ML fit to LHCb the data

Events / 0.13 ps

Events / 0.1 600

500

300

200

100

10²

- ML fit with 10 physics parameters
 - 7 angular amplitudes and phases
 - $\Gamma_{\varsigma}, \Delta \Gamma_{\varsigma}, \phi_{\varsigma}$
- proper-time resolution, calibrated on prompt J/psi gives $\sigma(t) \sim 50$ ps
- only OS flavour tagging used, calibrated on J/psiK+ $\varepsilon_{\rm tag} \mathcal{D}^2 = (2.08 \pm 0.41)\%$
- goodness of fit, using "pointto-point dissimilarity test" (*) gives P-value of 0.44







Standard Model (Lenz, Nierste: arXiv:1102.4274)



S



slight inconsistency in Γ between direct measurement and measurement with flavour specific decays?

$B_s \rightarrow J/\psi f^0$ at LHCb



some history

LHCb

Preliminary

√s = 7 TeV Data

COS0,I/w

- predicted by Stone, Zhang (2009) 2
- first seen by LHCb (PLB689(2011)115) 2
- LP2011: first measurement of CPV



π±π

1500

1000

LHCB-CONF-2011-051

candidates in f(980) region look pure scalar --> no angular analysis needed

LHCb

-0.5

Preliminary

√s = 7 TeV Data

0.5

50

500

0 cosθ_f

2000

 $m(\pi^{+}\pi^{-})$ (MeV/c²)

$B_s ightarrow J/\psi f^0$ at LHCb



some history

∆log(L)

14⊢

12 10

> 6 4 2

- predicted by Stone, Zhang (2009)
- first seen by LHCb (PLB689(2011)115)
- LP2011: first measurement of CPV
- result from the LL fit

LHCb

Preliminary

-4

-3

-2



LHCB-CONF-2011-051

beware: hadronic uncertainties, e.g. arXiv:1109.1112 [hep-ph]

 $\frac{1}{\phi_s}$ (rad)

 $\phi_s = -0.44 \pm 0.44 \pm 0.02$

combination of J/psiphi and J/psif0

- Bs -> J/psi f0 alone cannot constraint both Γ_s , $\Delta\Gamma_s$ and ϕ_s
 - requires combination with J/psi phi
- simultaneous fit to both samples
 $\phi_s = 0.03 \pm 0.16 \pm 0.07$

(prelim, LHCb-CONF-2011-056)

- TDCPV gives no evidence (yet) for NP in Bs mixing
- next steps
 - add more data
 - use same-side Kaon tagger
 - resolve two-fold ambiguity by relative S-wave strong phase in bins of M(KK) (Y. Xie et al., JHEP 0909:074, (2009))



conclusions/summary

- precision measurements of mixing observables:
 - mixing frequencies
 - CP asymmetries in final states with no expected CPV from decay amplitude
 - time-dependence CP asymmetries to CP eigenstates dominates by tree diagram
- one tantalizing result: D0 A_SL is 3.9s from SM prediction
- LHCb experiment is working on measurements in all these areas

backup



current HFAG average

 $|q/p| = 1.0002 \pm 0.0028$ A_{SL} = -0.0005 ± 0.0056

many measurements, most constraining:

 $|q/p| - 1 = (-0.8 \pm 2.7 (\text{stat.}) \pm 1.9 (\text{syst.})) \times 10^{-3},$

Babar, 232M BBbar

B. Aubert *et al.* (BaBar Collab.), Phys. Rev. Lett. **96**, 251802 (2006).

 $A_{\rm sl} = (-1.1 \pm 7.9(\text{stat}) \pm 8.5(\text{sys})) \times 10^{-3},$ $|q/p| = 1.0005 \pm 0.0040(\text{stat}) \pm 0.0043(\text{sys}).$

Belle, 87M BBbar PHYSICAL REVIEW D 73, 112002 (2006)

B factories still have quite a bit more data ...