

# Fourth generation neutrinos

Heinrich Päs



Workshop on Flavor and the Fourth family, IPPP Durham 2011

- ▶ Fourth generation neutrinos
  - A. Lenz, D. Schalla, H. Päs, arXiv:1104.2465
- ▶ Baryon asymmetry of the Universe and new neutrino states
  - S. Hollenberg, D. Schalla, H. Päs, work in progress

# Outline

- ▶ Neutrinos and the 4th generation
- ▶ Majorana-ness and double beta decay
- ▶ Baryon asymmetry washout
- ▶ A simple extra-dimensional model

# Neutrino status review

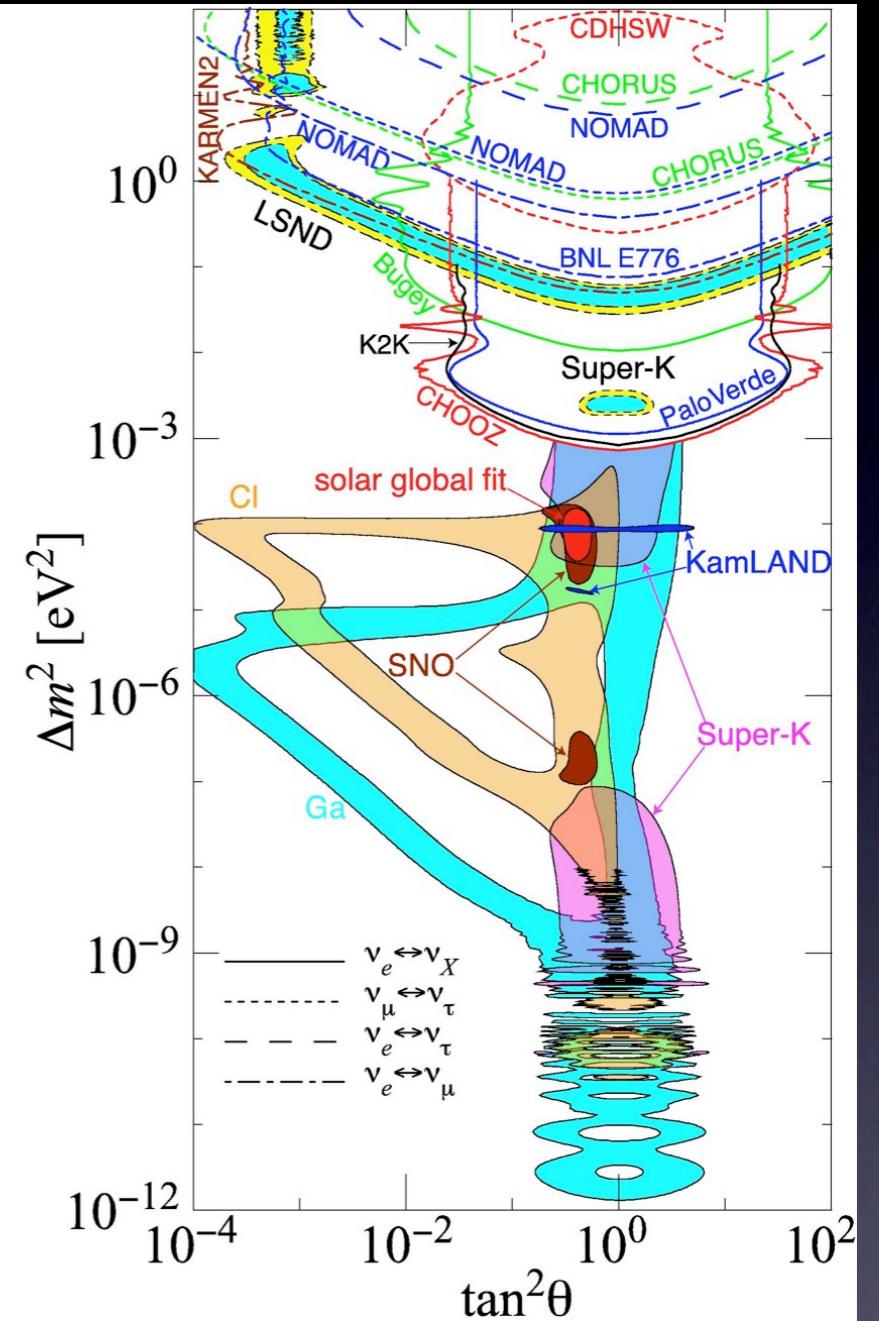
- ▶ Solar neutrino oscillations  
→ large mixing
- ▶ Atmospheric neutrino oscillations  
→ maximal mixing
- ▶ No short-baseline  $\nu_e$  disappearance  
→ small mixing

$$\nu_\alpha = \sum_i U_{\alpha i} \nu_i$$

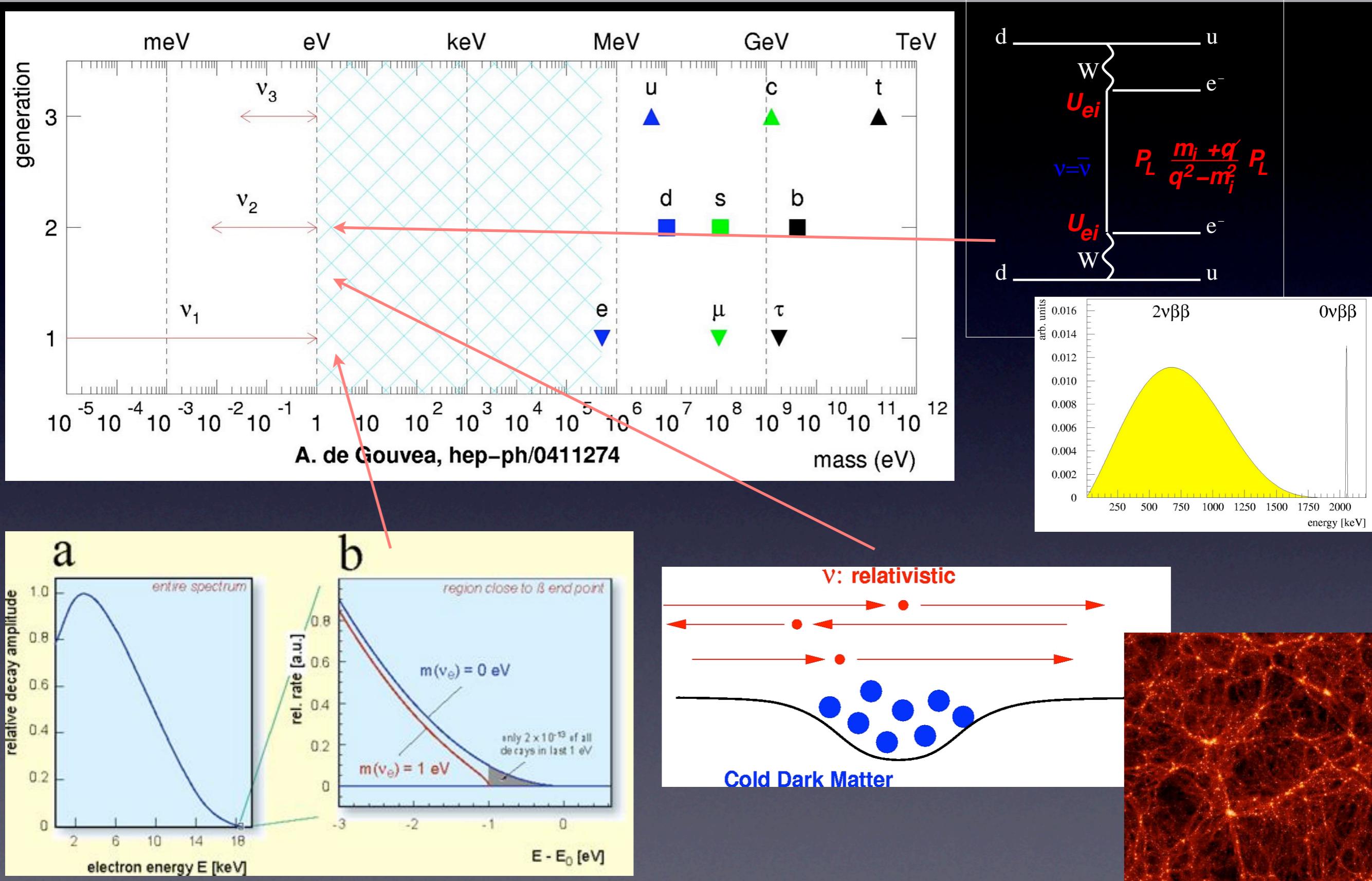
$$|U_{ij}| \approx \begin{pmatrix} \sqrt{\frac{2}{3}} & \sqrt{\frac{1}{3}} & < 0.2 \\ -\sqrt{\frac{1}{6}} & \sqrt{\frac{1}{3}} & -\sqrt{\frac{1}{2}} \\ -\sqrt{\frac{1}{6}} & \sqrt{\frac{1}{3}} & \sqrt{\frac{1}{2}} \end{pmatrix}$$

⇒ Neutrinos have masses

⇒ Mass eigenstates ≠ Flavor eigenstates



# Neutrino status review



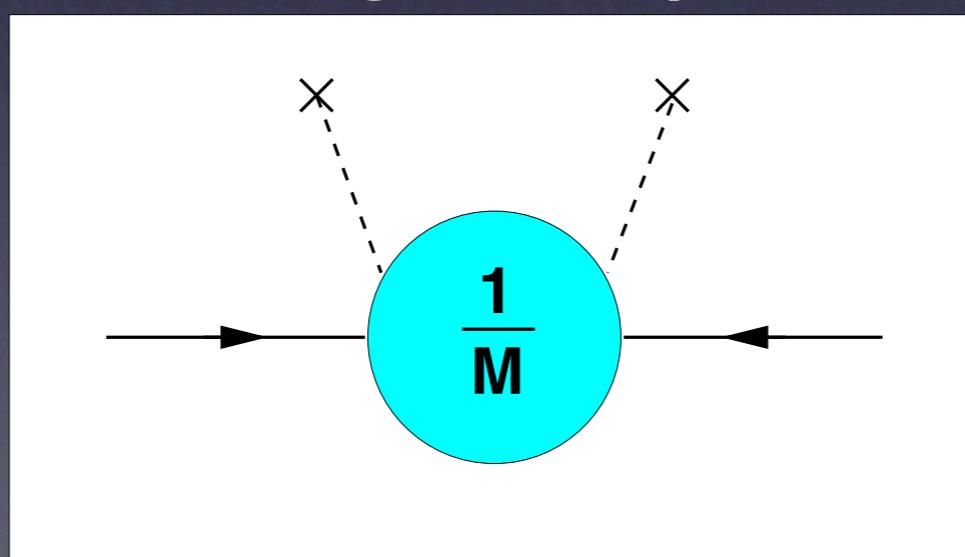
# Neutrino status review

Neutrinos are special in 2 respects:

- ▶ only neutral among elementary fermions
- ▶  $m_\nu \ll m_{q,e,\mu,\tau}$

→ is there any connection ?

Weinberg 5D operator:



with  $M$  big  
e.g. various  
Seesaws....

## Seesaw I mechanism

Both Dirac and Majorana masses:

$$-\mathcal{L} = \frac{1}{2} \begin{pmatrix} \bar{\nu}_L & \bar{N}_L^C \end{pmatrix} \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu_R^C \\ N_R \end{pmatrix}$$

$$M_R \sim M_{GUT} \gg m_D \quad \Rightarrow \quad m_\nu = m_D^2/M_R$$

- ▶  $\Rightarrow$  theoretical prejudice: Neutrinos are Majorana
- ▶ nice: Baryogenesis via Leptogenesis
- ▶ also nice: helps for 4th generation EW precision data (see Talk J. Rohrwild)

# Neutrinos and the 4th generation

But - a 4th generation neutrino is different:

- ▶ an SU(2) doublet neutrino contributes to the Z decay width → LEP bound

$$m_{\nu_4} > \frac{m_Z}{2} \approx 45 \text{ GeV}$$

- ▶  $|m_{\ell_4} - m_{\nu_4}| < 140 \text{ GeV}$  (Eberhardt, Lenz, Rohrwild: arXiv:1005.3505)

⇒ charged and neutral leptons have similar mass

$$\Rightarrow m_{\nu_4} \sim \mathcal{O}(100 \text{ GeV})$$

# Neutrinos and the 4th generation

$$-\mathcal{L} = \frac{1}{2} \begin{pmatrix} \bar{\nu}_L & \bar{N}_L^C \end{pmatrix} \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu_R^C \\ N_R \end{pmatrix}$$

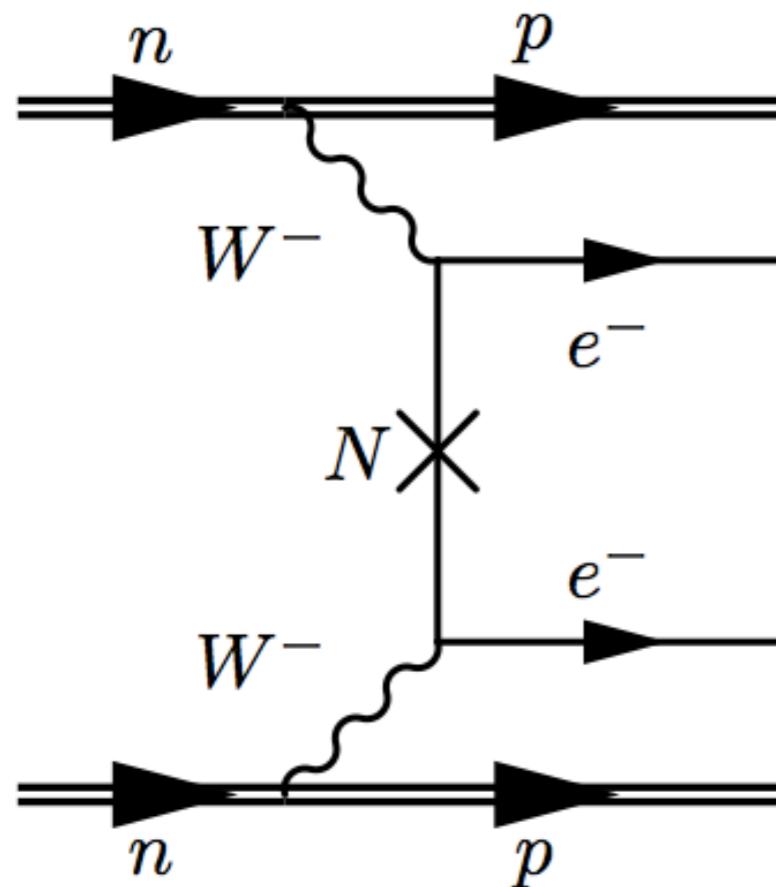
$$m = \frac{1}{2} \left( \sqrt{4m_D^2 + M_R^2} - M_R \right) \quad \& \quad M = \frac{1}{2} \left( \sqrt{4m_D^2 + M_R^2} + M_R \right)$$
$$\Rightarrow m \equiv m_{\nu_4} \sim \mathcal{O}(100 \text{ GeV})$$

Majorana mass free parameter

$m_D = y \cdot v \sim \mathcal{O}(100 \text{ GeV}) \Rightarrow M_R$  must be small

# Neutrinos and the 4th generation

Quantifying Majorana mass from  $0\nu\beta\beta$ :



contribution of heavy neutrino:

$$[T_{1/2}^{0\nu\beta\beta}]^{-1} = \left( \frac{m_p}{\langle m_N \rangle} \right)^2 C_{mm}^{NN}$$

$$\text{with } \langle m_N \rangle^{-1} = U_{e4}^2 m^{-1}$$

and using  $2\sigma$ -fits from Lacker, Menzel: 1003.4532

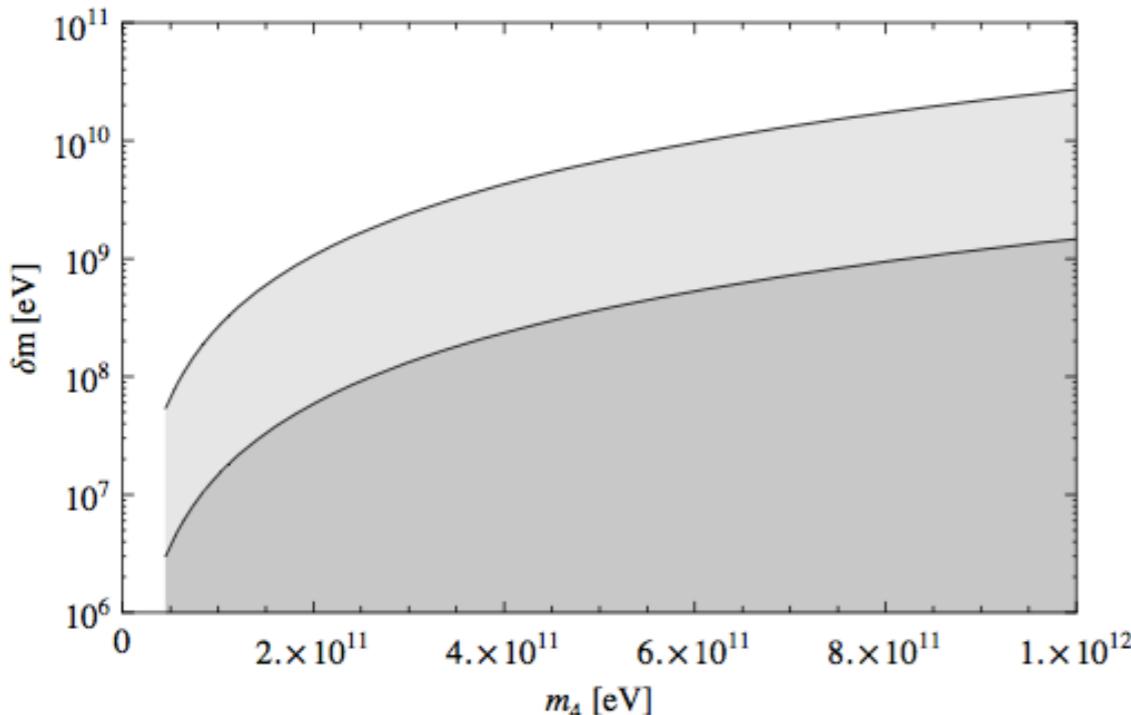
$$0.021 \leq U_{e4} \leq 0.089$$

- $\Rightarrow m > \mathcal{O}(10^4 \text{ GeV})$  to avoid signal in current experiments
- contributions from light neutrinos too small
- $\Rightarrow M$  must cancel contribution of  $m$

# Neutrinos and the 4th generation

efficient cancellation  $\Leftrightarrow m \sim M \Leftrightarrow M_R$  small

$$\Rightarrow [T_{1/2}^{0\nu\beta\beta}]^{-1} = \left( \frac{m_p}{\langle m \rangle} - \frac{m_p}{\langle M \rangle} \right)^2 C_{mm}^{NN}$$



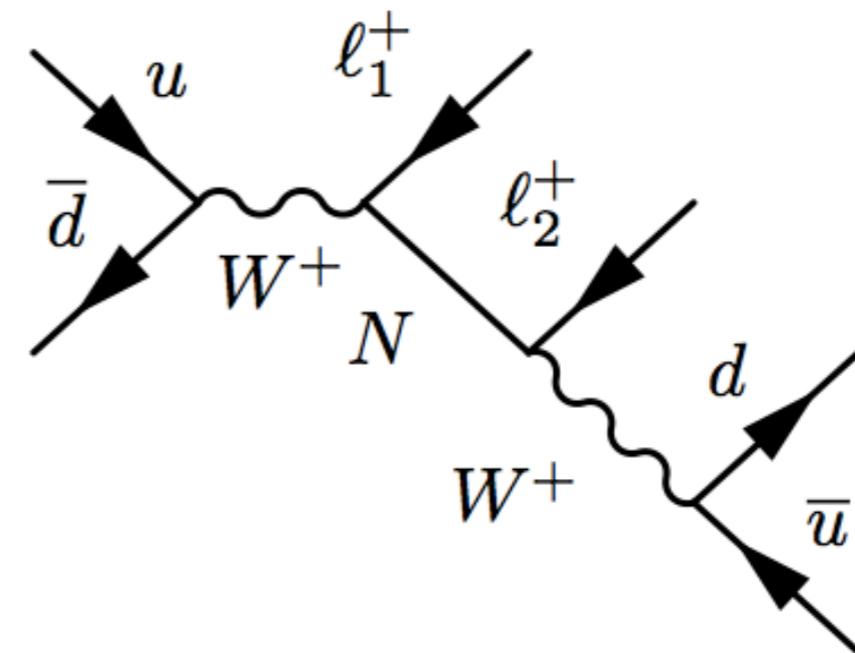
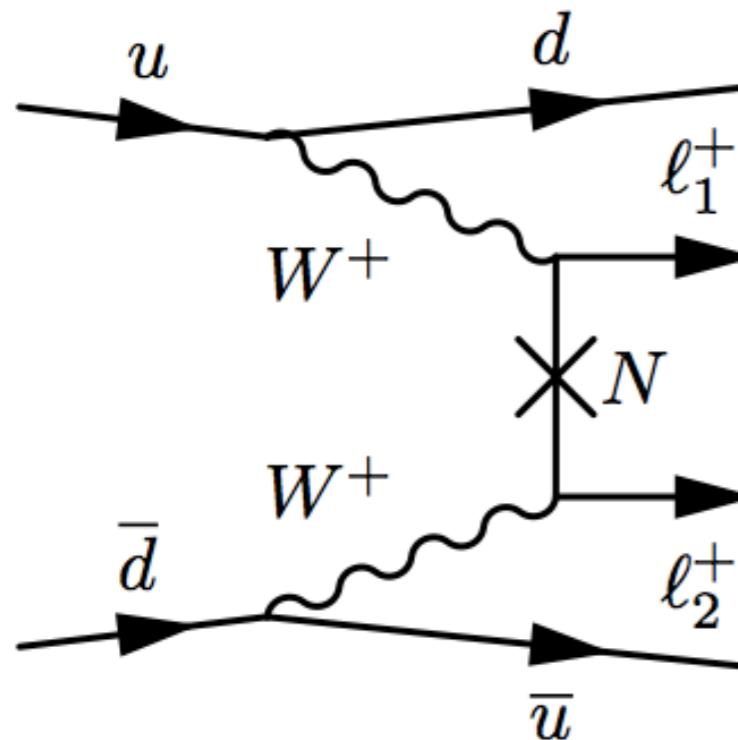
$$\Rightarrow \delta m \equiv M - m < \mathcal{O}(1 \text{ GeV})$$

thus a fourth generation neutrino must be either a pure Dirac or a pseudo-Dirac particle

$\Rightarrow$  lepton number violating processes are allowed but suppressed

# Neutrinos and the 4th generation

$$pp \rightarrow \ell_1^+ \ell_2^+ X$$



single heavy Majorana neutrino:

$$\sigma_{single} (pp \rightarrow \ell_1^+ \ell_2^+ X) = \frac{G_F^4 m_W^6}{8\pi^5} \left(1 - \frac{1}{2}\delta_{\ell_1 \ell_2}\right) |U_{\ell_1 N} U_{\ell_2 N}|^2 F(E, m_N)$$

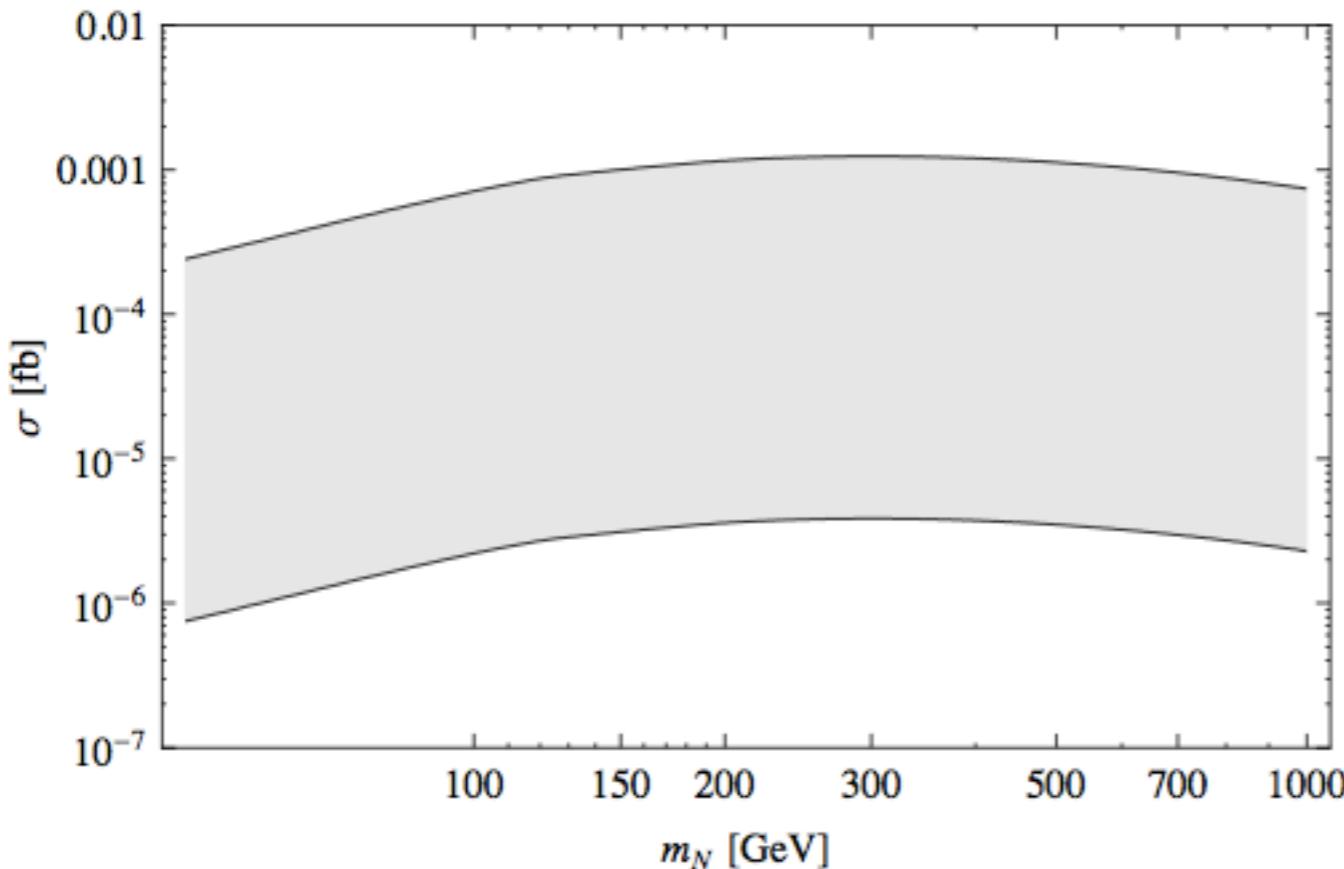
Ali, Eur. Phys. J. C21. 123 (2001)

# Neutrinos and the 4th generation

$\Delta_{pD}$  reduces like-sign dilepton production drastically

like-sign dielectron production

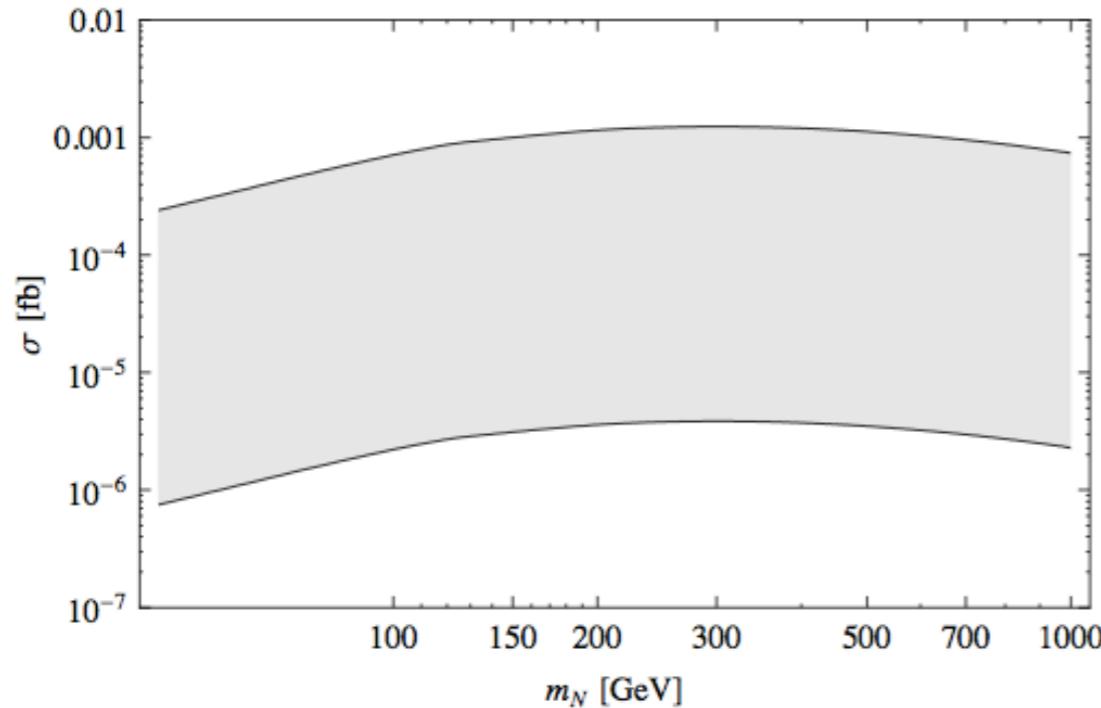
Majorana neutrino  
(w/o  $0\nu\beta\beta$  constraints)



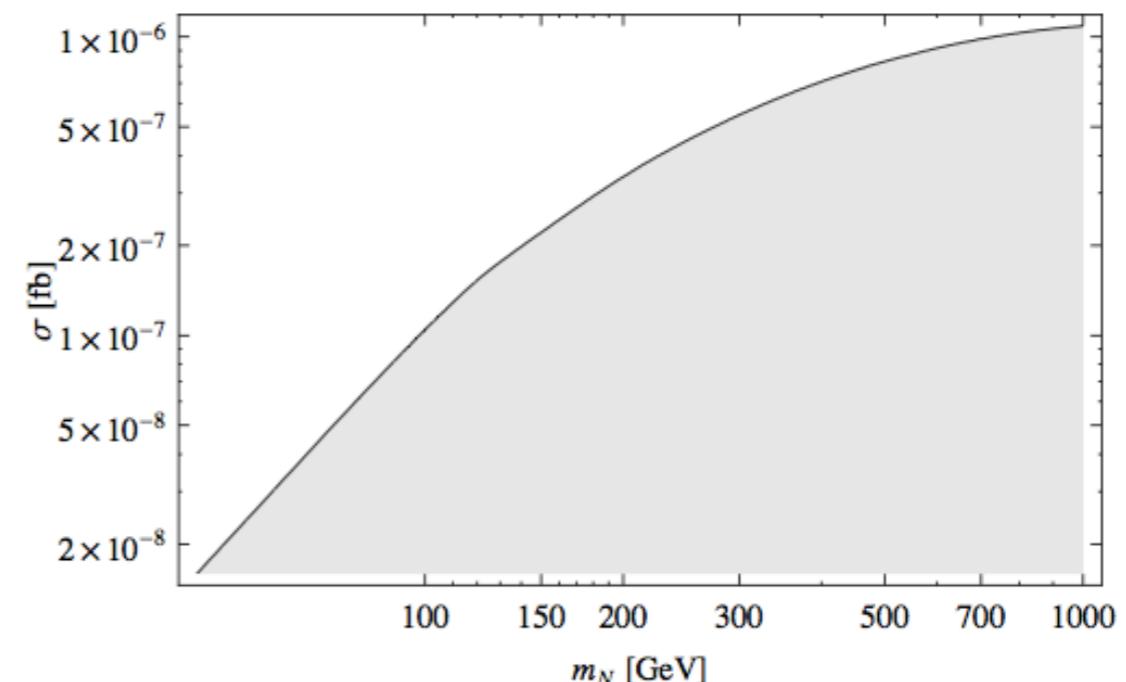
# Neutrinos and the 4th generation

$\Delta_{pD}$  reduces like-sign dilepton production drastically

Majorana neutrino  
(w/o  $0\nu\beta\beta$  constraints)



like-sign dielectron production  
pseudo-Dirac neutrino  
(with  $0\nu\beta\beta$  constraints)



⇒ observation from  $0\nu\beta\beta$  gives hard constraints on collider experiments

# Neutrinos and the 4th generation

Our universe today:

number of baryons  $\neq$  number of antibaryons

$$Y_{\Delta B} \equiv \frac{n_B - n_{\bar{B}}}{s} = (8.75 \pm .23) \cdot 10^{-11}$$

numerous viable models to explain this value

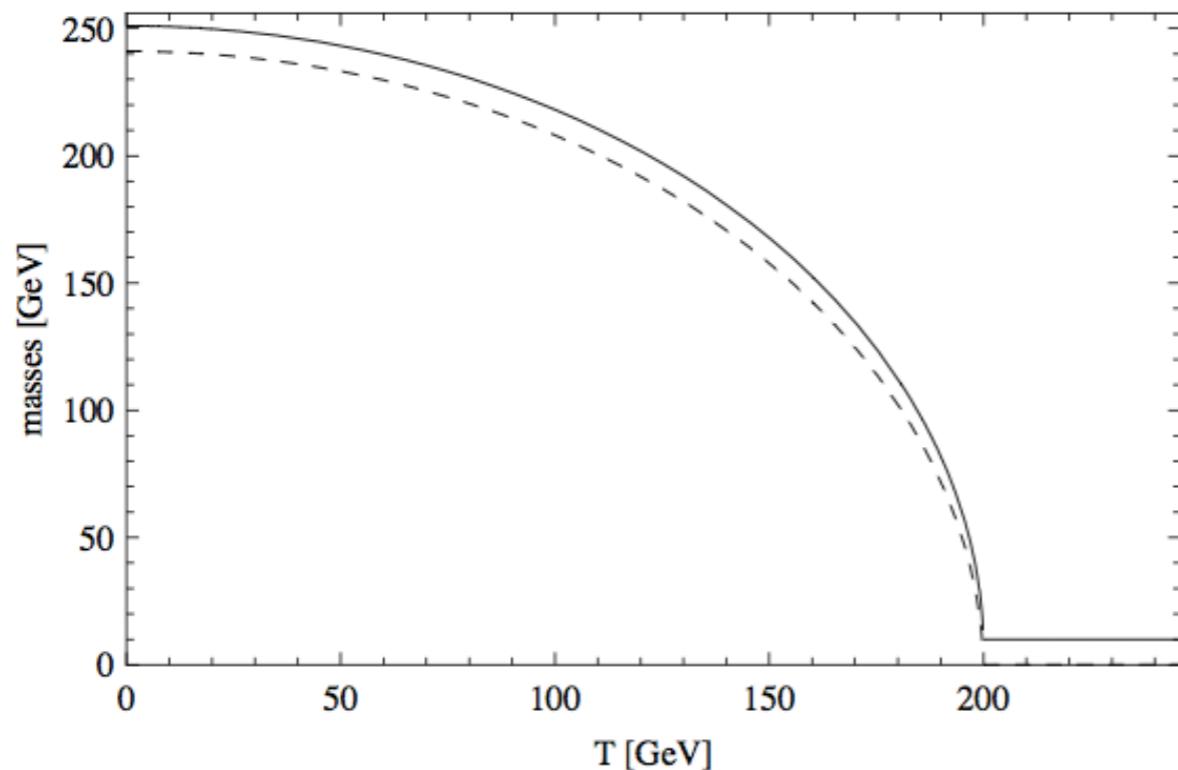
( $\rightarrow$  Baryogenesis/Leptogenesis scenarios)

most of them create this asymmetry at high temperatures  $\sim T_{GUT}$

The fourth generation neutrino is too light/freezes out too early to actively produce this asymmetry, but might erase any pre-existing asymmetry in the early universe due to their lepton number violating interactions.

# Neutrinos and the 4th generation

above the electroweak phase transition the Higgs-vev vanishes and the two mass eigenstates decouple



$$m \xrightarrow{T > T_{EW}} 0$$

$$M \xrightarrow{T > T_{EW}} M_R$$

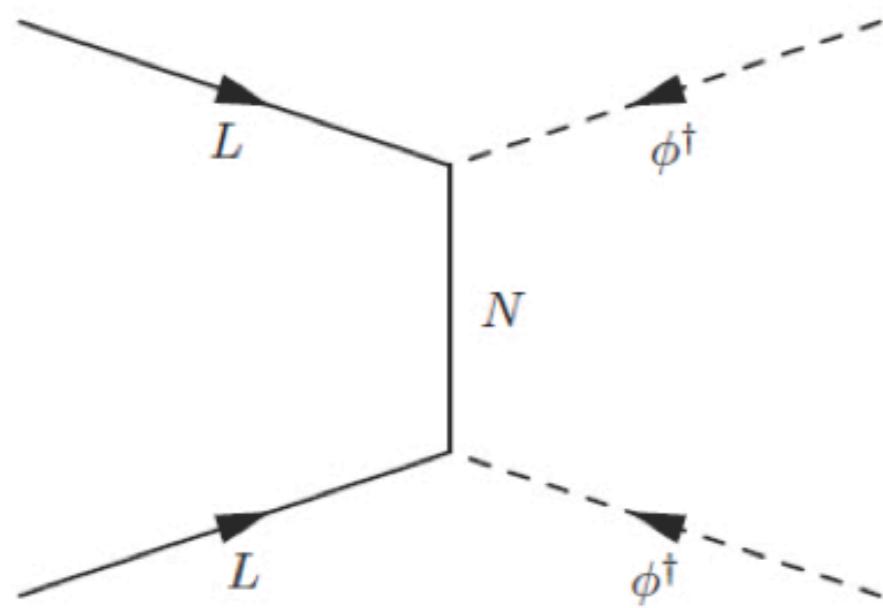
the mass splitting is unaffected:

$$\delta m = M_R = \text{const.}$$

- ⇒ above the EW phase transition a heavy pseudo-Dirac and a light sterile neutrino with mass  $\delta m$  are indistinguishable
- ⇒ following discussion not solely applies to fourth generation neutrinos

# Neutrinos and the 4th generation

We will not specify the mechanism of baryogenesis  
→ assume pre-existing asymmetry of the right amount at  $T_{GUT}$ .  
LNV processes mediated by additional neutrino species may dilute such asymmetry



$$\Delta L = 2$$

$$\langle \sigma | v | \rangle \sim \frac{\delta m^2}{(T^2 + \delta m^2)^2} = \frac{1}{\delta m^2} \frac{z^4}{(1 + z^2)^2}$$

with  $z \equiv \delta m / T$

Such processes are efficient in thermal equilibrium

# Neutrinos and the 4th generation

The strongest constraint is obtained by demanding that no washout should occur at all.

⇒ Process should not reach equilibrium while sphaleron transitions are effective

$$\Rightarrow H(T) > \Gamma(T) \text{ for } T_{EW} < T < T_{GUT}$$

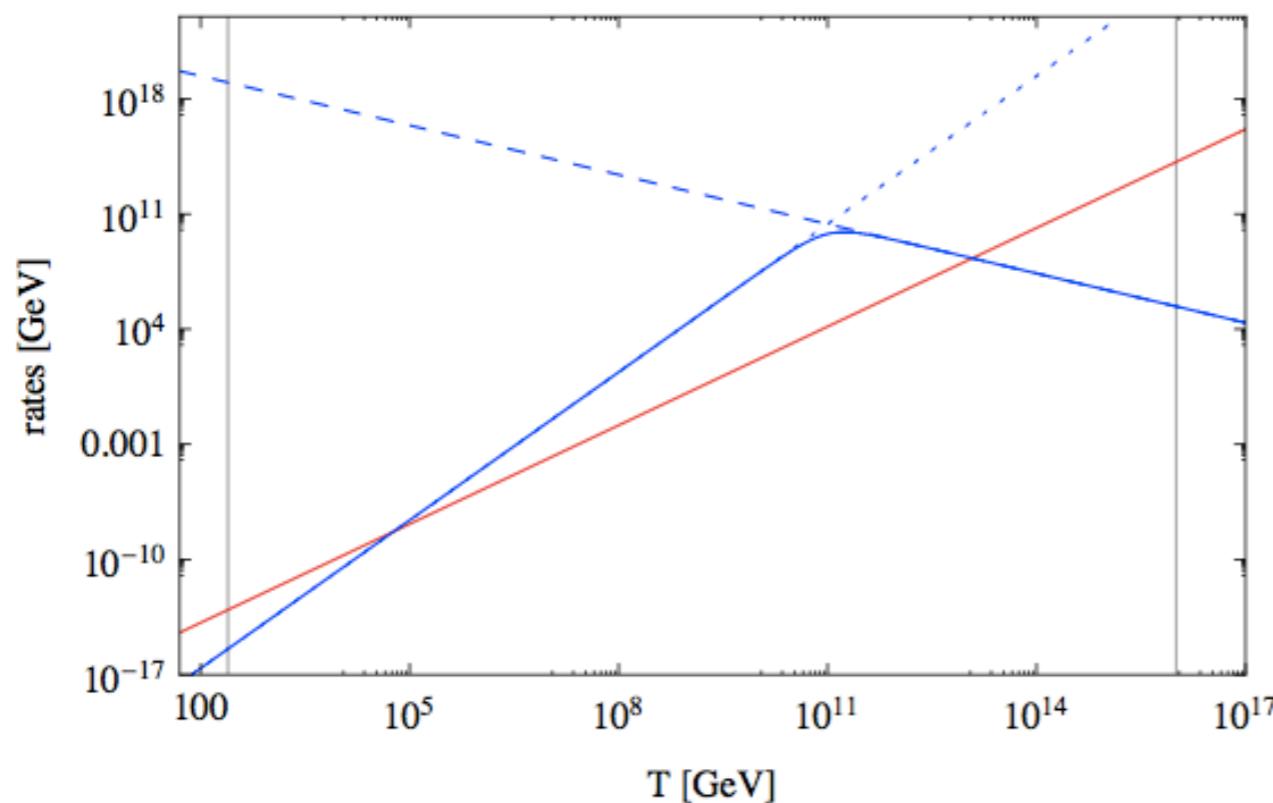
$$H(T) = \sqrt{\frac{8\pi^3 g_*}{90}} \frac{T^2}{m_{Pl}} \quad \Gamma(T) \sim n_\phi \langle \sigma | v | \rangle \text{ with } n_\phi \approx 2\zeta(3) T^3 / \pi^2$$

$$\Rightarrow \left( \frac{\delta m}{10 \text{ keV}} \right)^2 < 1 \times \left( \frac{T}{246 \text{ GeV}} \right)^3$$

# Neutrinos and the 4th generation

When the scattering rate exceeds the expansion rate while sphaleron transitions are effective LNF depletes the existing asymmetry

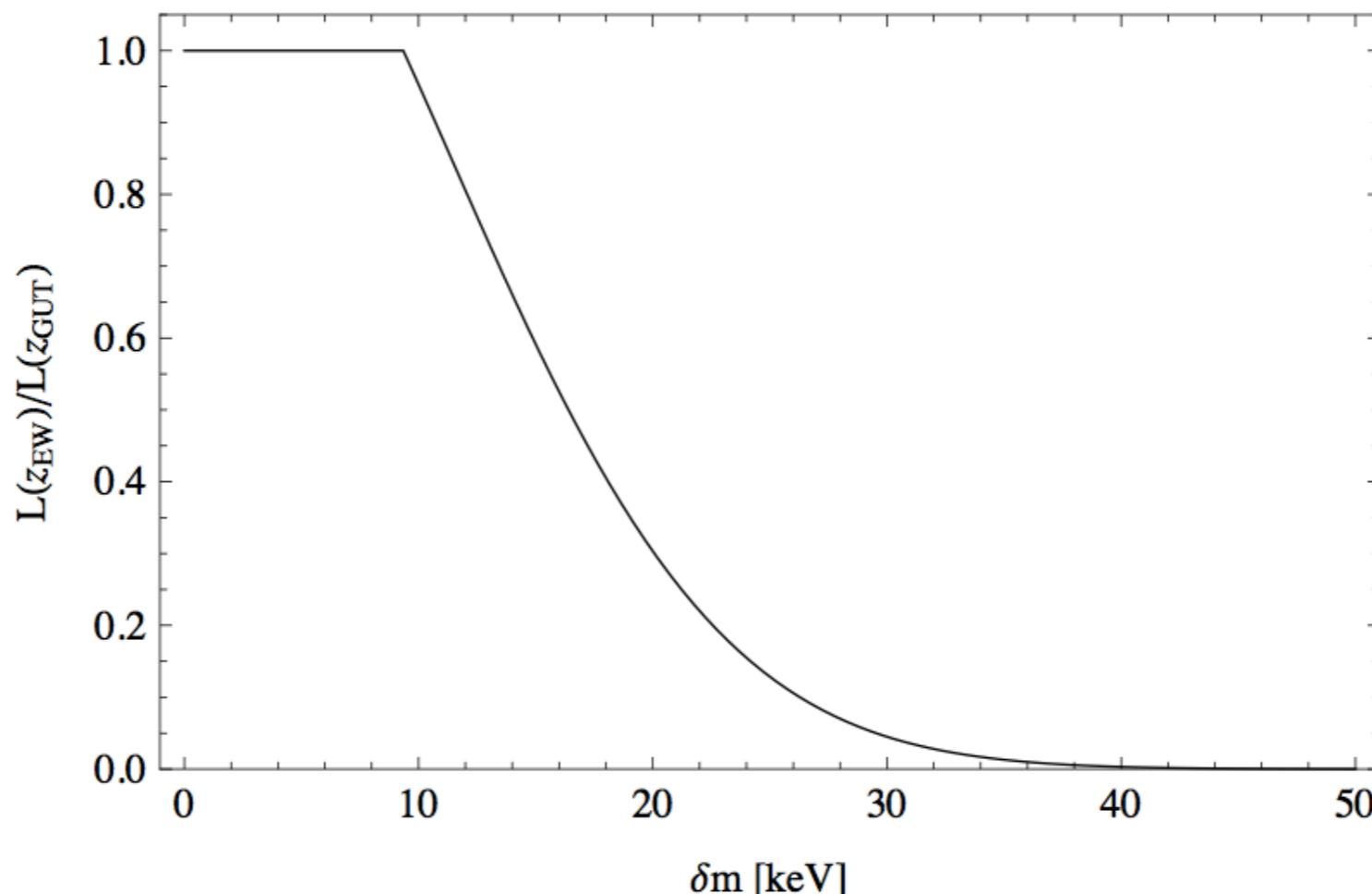
$$\ln \left( \frac{L(z_{EW})}{L(z_{GUT})} \right) = -\frac{1}{H(z=1)} \int_{z_{GUT}}^{z_{EW}} dz' z' n_\gamma \langle \sigma | v | \rangle (z')$$



careful treatment of  
integration limits crucial

# Neutrinos and the 4th generation

combined washout for small neutrino masses

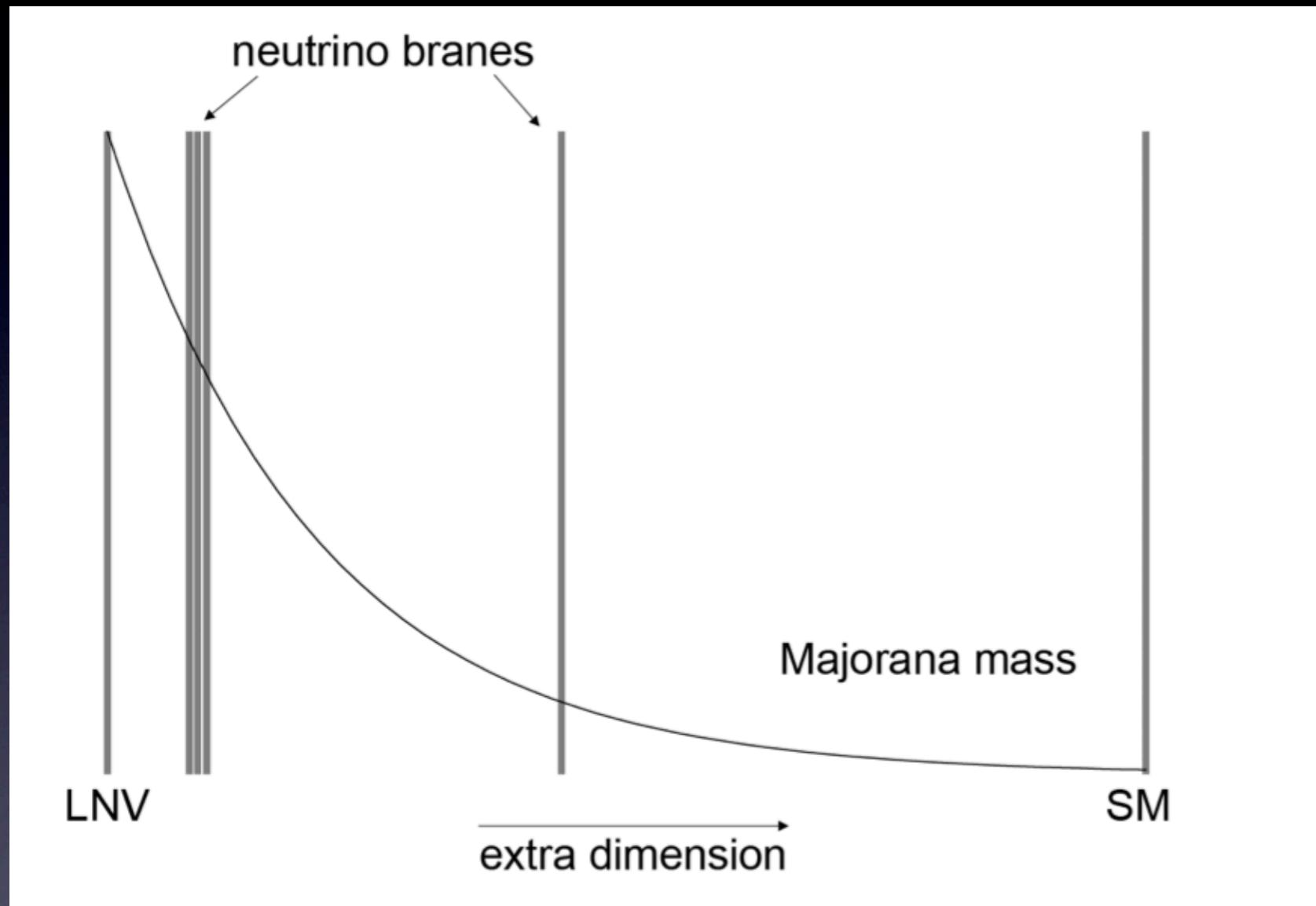


Amount of allowed washout depends on capability of model

constrained to  $< 10$  keV

# A simple extra-dimensional realization

## Breaking of lepton number on a distant brane



See e.g. [Arkani-Hamed,  
Dvali, Dimopoulos, March-  
Russell, 1998]

$$\langle \chi \rangle \propto e^{-mr}$$

$$M_{Ri} = \Lambda_{LNV} e^{-\alpha_i}$$

$i$	$\alpha_i$	$m_i$ [GeV]	$M_i$ [GeV]
4	$\sim 43.7$	246	247
3	9.6	$5.0 \cdot 10^{-11}$	$6.7 \cdot 10^{14}$
2	8.7	$9.1 \cdot 10^{-12}$	$1.7 \cdot 10^{15}$
1	$\leq 7.9$	$\leq 4.1 \cdot 10^{-12}$	$\geq 3.7 \cdot 10^{15}$

TABLE II: Localizations of the neutrino branes in the extra-dimensional bulk and corresponding mass eigenvalues for  $\Lambda_{LNV} = 10^{19}$  GeV.

# Conclusions

- ▶ Fourth generation neutrinos are heavier
- ▶ → bound from double beta decay
- ▶ → bound from washout of baryon asymmetry
- ▶ 4G  $\nu$ 's are Dirac or Pseudo-Dirac
- ▶ Simple realization: Extra-dimensional breaking of lepton number
- ▶ Also: radiative  $\nu$  masses for 3G due to 4th & 5th G neutrinos (see Talk by A. Aparici)