

Automatic NLO calculations with GoSam

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GoSam release: [arXiv:1111.2034](https://arxiv.org/abs/1111.2034) [hep-ph]



IPPP, University of Durham

LHCPhenoNet Workshop

NLO multi-leg highlights

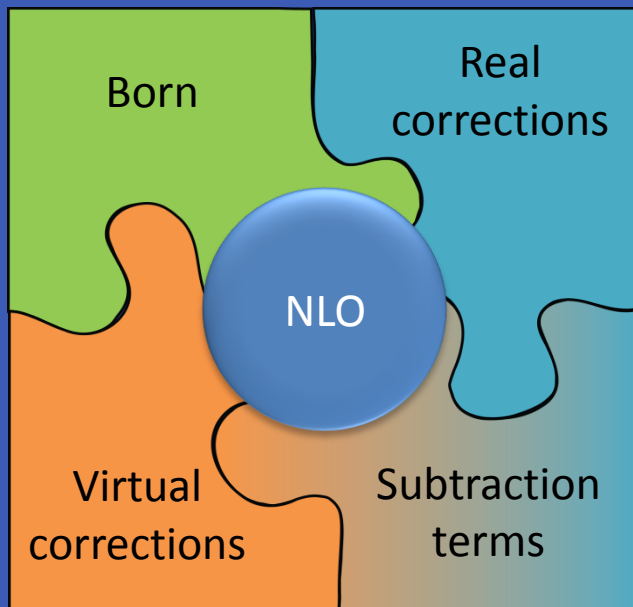
- Progresses in NLO calculation:

- $pp \rightarrow W + 3 \text{ jets}$ Blackhat (09) / Rocket (09)
- $pp \rightarrow t\bar{t}b\bar{b}$ Denner-Dittmaier (09) / HELAC-NLO (09)
- $pp \rightarrow Z(\gamma) + 3 \text{ jets}$ Blackhat (10)
- $pp \rightarrow t\bar{t}jj$ HELAC-NLO (10)
- $pp \rightarrow W^+W^-b\bar{b}$ Denner-Dittmaier (10) / HELAC-NLO (10)
- $e^+e^- \rightarrow 5 \text{ jets}$ Rocket (10)
- $pp \rightarrow W^+W^+jj$ Rocket (10)
- $pp \rightarrow Z(\gamma) / W + 4 \text{ jets}$ Blackhat (11)
- $pp \rightarrow b\bar{b}b\bar{b}$ Golem / Samurai (11)
- $pp \rightarrow W^+W^-jj$ Rocket (11)
- $pp \rightarrow 4 \text{ jets}$ Blackhat (11)

Key Concept
AUTOMATION

Automation in NLO calculations

- Different ingredients of a NLO calculation have also different levels of automation according to their complexity:



- Virtual corrections

- **Automatized recently:**

- FEYNARTS/FORMCALC/LOOPTOOLS (public) [Hahn et al.]
- HELAC-NLO (public) [Bevilacqua, Czakon, van Hameren, Papadopoulos, Pittau, Worek 11]
- MadLoop [Hirschi, Frederix, Frixione, Garzelli, Maltoni, Pittau 11]
- NGLUON (public) [Badger, Biedermann, Uwer 10]
- GoSam (public) [Cullen, Greiner, Heinrich, GL, Mastrolia, Ossola, Reiter, Tramontano 11]

- Dedicated programs also involve high level of automation:

Denner, Dittmaier, Pozzorini et al., VBFNLO (public), MCFM (public), BLACKHAT, ROCKET

Progresses in NLO calculation

- Evolution from collection of **pre-coded** processes...
... to generation of full NLO processes by the user “**on the fly**”!
- Possible thanks to pioneering works:
 - improvements on the computation of tensor integrals,
[Binoth et al. GOLEM95; Denner, Dittmaier]
 - application of unitarity to the computation of the one loop amplitudes,
[Bern, Dixon, Kosower; Britto, Cachazo, Feng]
 - reduction at the integrand level.
[Ossola, Papadopoulos, Pittau; Ellis, Giele, Kunstz, Melnikov]

➡ FOCUS MORE ON PHENOMENOLOGY



The GoSam Project: philosophy

GoSam

Golem (General One Loop Evaluator of Matrix elements)

Samurai (Scattering Amplitudes from Unitarity based Reduction At Integrand level)

An automated amplitude generation based on Feynman diagrams

- Based upon:
 - ➡ Algebraic generation of D-dimensional integrands via Feynman diagrams
 - ➡ Reduction at the integrand level via D-dimensional extension of the OPP method
 - ➡ Generation on the fly of the full rational term

The GoSam Project: goals

- Main targets:
 - Provide an **automated** tool for **stable** evaluation of one-loop matrix elements
 - **Be general** and model independent (QCD, EW, MSSM, ...)
 - **Interface** with existing tools (MadEvent, Sherpa, POWHEG-BOX, ...)
 - Build upon **open source** tools only (next slide)
 - Support **open standards** (for interfacing)

The GoSam Project: the codes

GoSam

Python package to write code (fortran95)

Code generation

- Diagram generation:
QGRAF [Nogueira 92]
- Algebra:
FORM [Vermaseren 91]
SPINNEY [Cullen, Koch-Janusz, Reiter 10]
- Code generator:
HAGGIES [Reiter 09]

Generated code execution

- Loop integral reduction:
SAMURAI [Mastrolia, Ossola, Reiter, Tramontano 10]
GOLEM95 [Binoth, Cullen, Guillet, Heinrich, Pilon, Reiter 08]
PJFRY [Yundin]
- Scalar integral evaluation:
AVHOLO [van Hameren]
QCDLOOP [Ellis, Zanderighi]
GOLEM95C [Cullen, Guillet, Heinrich, Kleinschmidt, Pilon, Reiter, Rodgers 11]

Reduction methods

- **SAMURAI**

[Mastrolia, Ossola, Reiter, Tramontano 10]

Reduction method can
be chosen at runtime

- **Tensorial integrand-level reconstruction**

[Heinrich, Ossola, Reiter, Tramontano 10]

with

- **GOLEM95C** [Binoth, Cullen, Guillet, Heinrich, Kleinschmidt, Pilon, Reiter, Rodgers 11]
- **SAMURAI** [Mastrolia, Ossola, Reiter, Tramontano 10]
- **PJFry** [Yundin]

A Walk through GoSam...

- GoSam as a standalone code
- Interfacing with an external Monte Carlo program:
 - The BLHA-interface
 - An example with Sherpa

GoSam as standalone code

- Preparation of the input card “myprocess.rc” (continued):

```
##### program options #####  
  
extensions=samurai, golem95, dred  
  
# abbrev.level=helicity # group , diagram  
# abbrev.limit=0  
  
form.bin=tform  
form.tempdir=/tmp  
fc.bin=gfortran -O2  
  
samurai.fcflags=-I${HOME}/include/samurai  
samurai.ldflags=-L${HOME}/lib/ -lqcdloop -lavh_olo \  
-lsamurai  
samurai.version=2.1.1  
  
golem95.fcflags=-I${HOME}/include/golem95  
golem95.ldflags=-L${HOME}/lib/ -lgolem
```

Several other extension and options
available.
For further details check our user
manual:

<http://www.hepforge.org/archive/gosam/gosam-1.0.pdf>

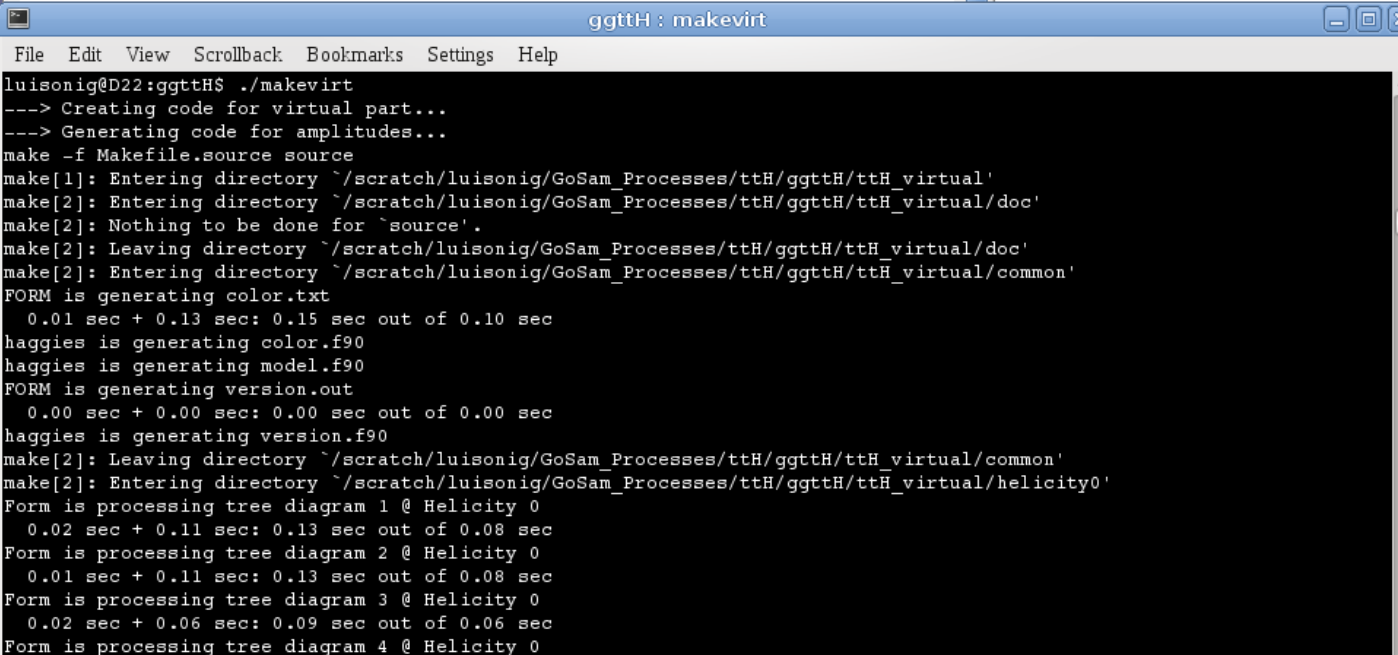
GoSam as standalone code

- Generate code and compile

\$ `gosam.py myprocess.rc` python code generates fortran95 code

\$ `make source` Form & Haggies process diagrams to write code

\$ `make compile` fortran95 code in compiled



```
ggttH : makevirt
File Edit View Scrollback Bookmarks Settings Help
luitonig@D22:ggttH$ ./makevirt
---> Creating code for virtual part...
---> Generating code for amplitudes...
make -f Makefile.source source
make[1]: Entering directory `~/scratch/luisonig/GoSam_Processes/ttH/ggttH/ttH_virtual'
make[2]: Entering directory `~/scratch/luisonig/GoSam_Processes/ttH/ggttH/ttH_virtual/doc'
make[2]: Nothing to be done for `source'.
make[2]: Leaving directory `~/scratch/luisonig/GoSam_Processes/ttH/ggttH/ttH_virtual/doc'
make[2]: Entering directory `~/scratch/luisonig/GoSam_Processes/ttH/ggttH/ttH_virtual/common'
FORM is generating color.txt
  0.01 sec + 0.13 sec: 0.15 sec out of 0.10 sec
haggies is generating color.f90
haggies is generating model.f90
FORM is generating version.out
  0.00 sec + 0.00 sec: 0.00 sec out of 0.00 sec
haggies is generating version.f90
make[2]: Leaving directory `~/scratch/luisonig/GoSam_Processes/ttH/ggttH/ttH_virtual/common'
make[2]: Entering directory `~/scratch/luisonig/GoSam_Processes/ttH/ggttH/ttH_virtual/helicity0'
Form is processing tree diagram 1 @ Helicity 0
  0.02 sec + 0.11 sec: 0.13 sec out of 0.08 sec
Form is processing tree diagram 2 @ Helicity 0
  0.01 sec + 0.11 sec: 0.13 sec out of 0.08 sec
Form is processing tree diagram 3 @ Helicity 0
  0.02 sec + 0.06 sec: 0.09 sec out of 0.06 sec
Form is processing tree diagram 4 @ Helicity 0
```

GoSam as standalone code

- Check produced code with **automatic** generated documentation before the full generation/run

Index	1	2	3	4	5
0	-	-	0	-	-
1	-	-	0	-	+
2	-	-	0	+	-
3	-	-	0	+	+
4	-	+	0	-	-
5	-	+	0	-	+
6	-	+	0	+	-
7	-	+	0	+	+
8 → 4	+	-	0	-	-
9 → 5	+	-	0	-	+
10 → 6	+	-	0	+	-
11 → 7	+	-	0	+	+
12	+	+	0	-	-
13	+	+	0	-	+
14	+	+	0	+	-
15	+	+	0	+	+

GoSam 1.0: $gg \rightarrow Ht\bar{t}$

luisonig

2012-02-19 (22:10:59)

Abstract

This process consists of 8 tree-level diagrams and 160 NLO diagrams. Golem has identified 15 groups of NLO diagrams by analyzing their one-loop integrals.

- Documentation contains information about
 - the generated helicities
 - the colour basis

GoSam as standalone code

- Loop diagrams are grouped into sets of diagrams which share loop propagators

5.4 Group 3 (5-Point)

General Information

The maximum effective rank in this group is 4.

$$r_1 = -k_2 + k_5, \quad m_1 = m_t$$

$$r_2 = -k_2$$

$$r_3 = 0$$

$$r_4 = -k_4, \quad m_4 = m_t$$

$$r_5 = -k_3 - k_4, \quad m_5 = m_t$$

$$S = \begin{pmatrix} S_{1,1} & 0 & S_{1,3} & S_{1,4} & S_{1,5} \\ 0 & 0 & 0 & S_{2,4} & S_{2,5} \\ S_{3,1} & 0 & 0 & 0 & S_{3,5} \\ S_{4,1} & S_{4,2} & 0 & S_{4,4} & S_{4,5} \\ S_{5,1} & S_{5,2} & S_{5,3} & S_{5,4} & S_{5,5} \end{pmatrix}$$

$$S_{1,1} = -2m_t^2$$

$$S_{1,3} = -s_{51} + s_{34} - s_{12}$$

$$S_{1,4} = -2m_t^2 + s_{45} + m_H^2 - s_{23} - s_{12}$$

$$S_{1,5} = -2m_t^2$$

$$S_{2,4} = s_{51} - s_{23} - s_{34} + m_H^2$$

$$S_{2,5} = s_{51} - m_t^2$$

$$S_{3,5} = -m_t^2 + s_{34}$$

$$S_{4,4} = -2m_t^2$$

$$S_{4,5} = -2m_t^2 + m_H^2$$

$$S_{5,5} = -2m_t^2$$

Loop diagrams are grouped into sets of diagrams which share loop-propagators. A loop integral can be written as

$$\int \frac{d^n k}{i\pi^{\frac{n}{2}}} \frac{\mathcal{N}(q)}{\prod_{j=1} N[(k+r_j)^2 - m_j^2 - im_j\Gamma_j + i\delta]} \quad (16)$$

For each group we list r_j , m_j and Γ_j . For m_j and Γ_j only non-vanishing symbols are listed. Furthermore, we give the matrix S which is defined as

$$S_{\alpha\beta} = (r_\alpha - r_\beta)^2 - m_\alpha^2 - im_\alpha\Gamma_\alpha - m_\beta^2 - im_\beta\Gamma_\beta. \quad (17)$$

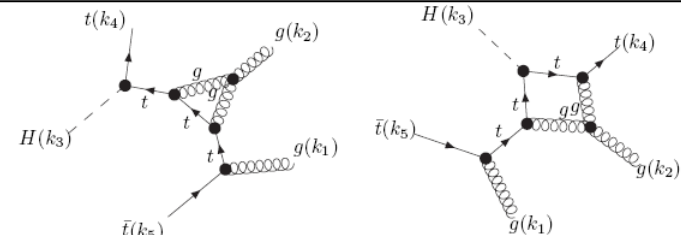


Diagram 23
 $S' = S_{Q \rightarrow -q}^{(1,4)}, \text{rk} = 2$

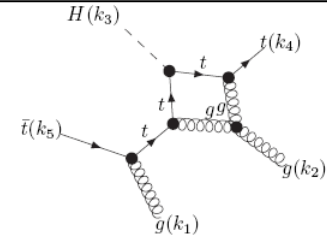


Diagram 58
 $S' = S_{Q \rightarrow -q}^{(1)}, \text{rk} = 3$

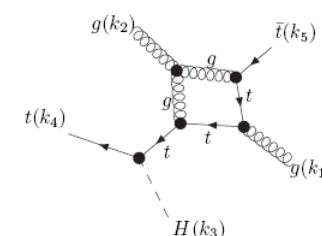


Diagram 69
 $S' = S_{Q \rightarrow -q}^{(4)}, \text{rk} = 3$

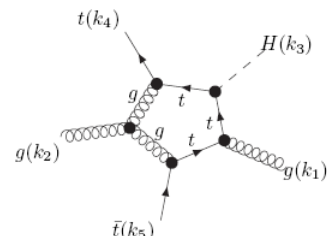


Diagram 158
 $S' = S_{Q \rightarrow -q}^{(1)}, \text{rk} = 4$

GoSam as standalone code

- When the full code is ready:
 - Contributions divided in directories by helicity

```
ttH_virtual : bash
File Edit View Scrollback Bookmarks Settings Help
luisonig@D22:ttH_virtual$ ls
codegen  diagrams-0.hh  diagrams-1.log  helicity1  helicity14  helicity3  helicity6  Makefile.conf  model.hh
common  diagrams-0.log  doc             helicity12  helicity15  helicity4  helicity7  Makefile.source
config.sh diagrams-1.hh  helicity0       helicity13  helicity2   helicity5  Makefile      matrix
luisonig@D22:ttH_virtual$
```

```
File Edit View Scrollback Bookmarks Settings Help
luisonig@D22:matrix$ ls
debug.xml  Makefile  Makefile.source  matrix.f90  test.exe  test.f90~  tth_matrix.mod
ltest.dat  Makefile.dep  matrix.a         matrix.o    test.f90  test.o
luisonig@D22:matrix$
```

➤ Output of *test.exe*:

```
# LO: 0.6918083437862626E-04
# NLO, finite part: 17.78339386183546
# NLO, single pole: -9.484483151742308
# NLO, double pole: -6.000000000000000
# IR, single pole: -9.484483151741490
# IR, double pole: -5.999999999999999
# Time/Event [ms]: 280.000
```

Generated code comes with **test.exe** routine which allows to check cancellation of poles with built-in integrated dipoles:
make test.exe

Example: $pp \rightarrow H t \bar{t}$

Generation time: 1h 20min

Compilation time: 3h 6min

Time for 1 PS point: 280 ms

Machine: Intel Core Quad CPU Q6600 @ 2.4 GHz / 6 GB RAM

Process generated in DRED and converted to CDR at runtime

	E	p_x	p_y	p_z
u/g	250.0	0.0	0.0	250.0
\bar{u}/g	250.0	0.0	0.0	-250.0
H	136.35582793693018	15.133871809486299	27.986733991031045	26.088703626953386
t	181.47665951104506	20.889486679044587	-50.105625289561424	14.002628607367491
\bar{t}	182.16751255202476	-36.023358488530903	22.118891298530357	-40.091332234320859

parameters			
\sqrt{s}	500.0	N_f	5
μ	m_t	$N_{f,h}$	1
m_t	172.6	α_s	0.1076395107858145
m_H	130	v	246.21835258713082

result $gg \rightarrow t\bar{t}H$		
	GoSAM	Ref. [39]
$a_0 \cdot 10^5$	6.127399805961155	6.127400074872043
c_0/a_0	9.006680638719660	9.006680836410272
c_{-1}/a_0	2.986347664537282	2.9863477301662056
c_{-2}/a_0	-6.0000000000000004	-6.000000131659877

Comparison with MadLoop [Hirschi,Frederix,Frixione,Garzelli, Maltoni,Pittau 11]



GoSam: further tested calculations

- $q\bar{q} \longrightarrow b\bar{b}b\bar{b}$
- $g\bar{g} \longrightarrow b\bar{b}b\bar{b}$
- $q\bar{q} \longrightarrow t\bar{t}b\bar{b}$
- $g\bar{g} \longrightarrow t\bar{t}b\bar{b}$
- $u\bar{d} \longrightarrow W^+ ggg$
- $u\bar{u} \longrightarrow H t\bar{t}$
- $g\bar{g} \longrightarrow H t\bar{t}$
- $u\bar{d} \longrightarrow W + s\bar{s} \longrightarrow e^+ \nu_e s\bar{s}$
- $u\bar{d} \longrightarrow W + gg \longrightarrow e^+ \nu_e gg$
- $d\bar{d} \longrightarrow Z gg \longrightarrow e^+ e^- gg$
- $u\bar{d} \longrightarrow W + b\bar{b} \longrightarrow e^+ \nu_e b\bar{b}$ with massive b's
- $u\bar{d} \longrightarrow W + g \longrightarrow e^+ \nu_e g$ EW corrections
- $e^+ e^- \longrightarrow Z \longrightarrow d\bar{d}g$
- $e^+ e^- \longrightarrow Z \longrightarrow b\bar{b}g$ with massive b's
- $\gamma\gamma \longrightarrow \gamma\gamma\gamma\gamma$
- $u\bar{d} \longrightarrow W^+ W^+ s\bar{c} \longrightarrow e^+ \nu_e \mu^+ \nu_\mu s\bar{c}$
- $u\bar{u} \longrightarrow W^+ W^+ c\bar{c} \longrightarrow e^+ \nu_e \mu^+ \nu_\mu c\bar{c}$
- $u\bar{d} \longrightarrow W^+ W^+ \bar{s}c \longrightarrow e^+ \nu_e \mu^+ \nu_\mu \bar{s}c$
- plus a large number of 2 to 2 processes

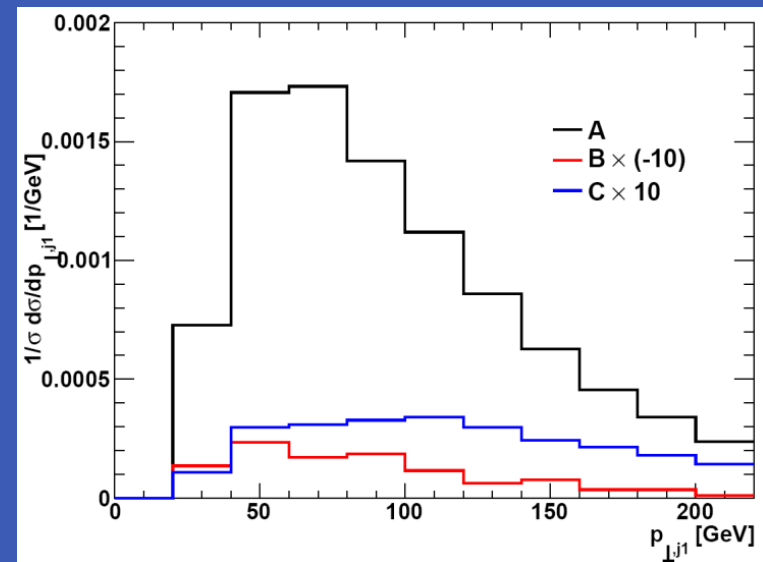
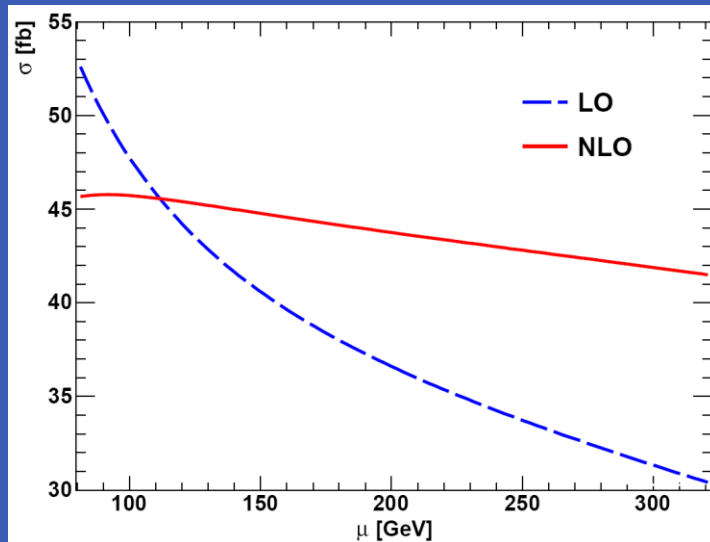
$W^+W^- + 2 \text{ jets @ NLO with GoSam}$

[Greiner, Heinrich, Mastrolia, Ossola, Reiter, Tramontano 12]

- First application of GoSam for the calculation of previously unknown NLO contributions:

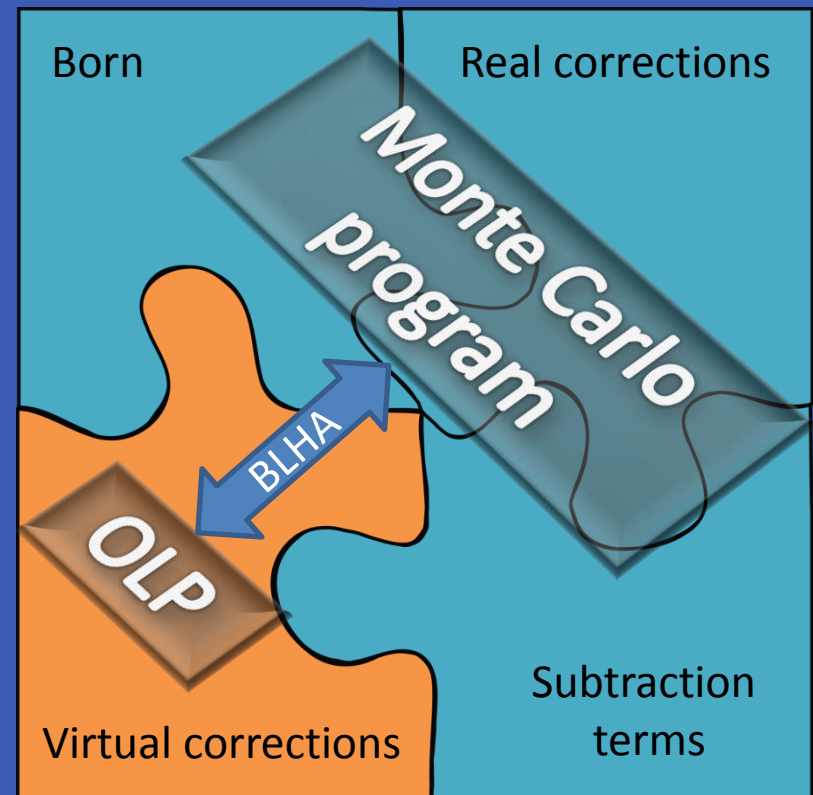
- Part A: no 3rd gen. quarks in fermion loops and VB attached to closed fermion loops, [Melia, Melnikov, Rontsch, Zanderighi 11]
- Part B: VB attached to closed fermion loops,
- Part C: 3rd gen. quarks in the loops.

→ previously unknown

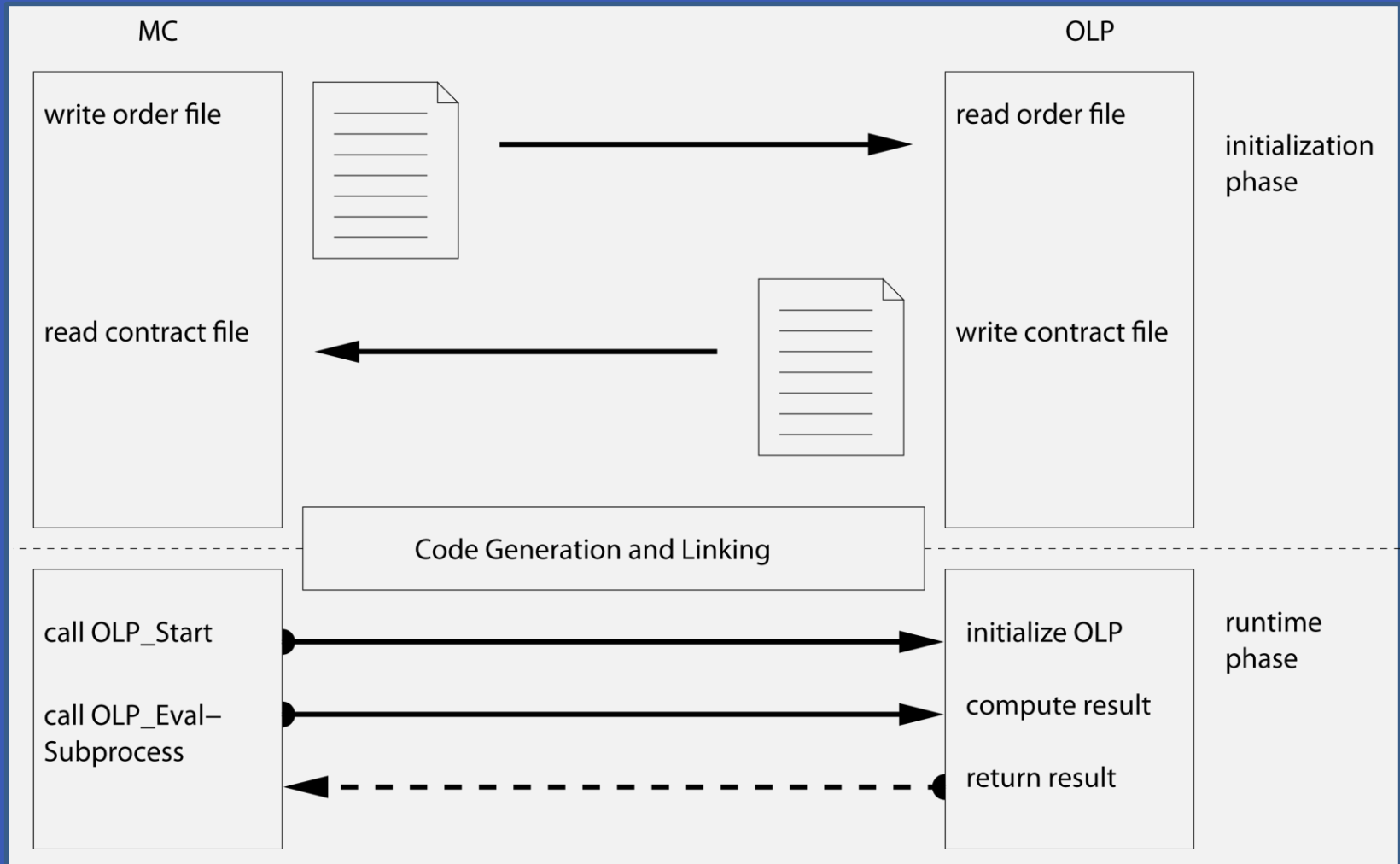


GoSam: interface with MC

- GoSam supports the Binoth-Les-Houches-Accord (BLHA) standards to interface with Monte Carlo generators:
 - Monte Carlo program:
Born / real corr. / sub. terms
 - One-loop Program (OLP):
virtual corr.
 - Pre-runtime communication via
“order” and “contract” files
 - At runtime:
 - `OLP_Start()`
 - `OLP_EvalSubProcess()`



BLHA-interface: order & contract



In practice: GoSam+ Sherpa

Order file

The screenshot shows the Emacs editor interface with two files open. The left file, `OLE_order.lh`, contains parameters for a process list and various physics settings. The right file, `OLE_order.olc`, contains the corresponding code for the OLE model, including syntax definitions and process list entries.

```
# OLE_order.lh
# Created by Sherpa

MatrixElementSquareType CHsummed
CorrectionType QCD
IRregularisation DRED
AlphasPower 1
AlphaPower 2
OperationMode CouplingsStrippedOff

Z_mass 91.118
Z_width 2.49
W_mass 80.419
W_width 2.0476
sin_th_2 0.221051079833

# process list
1 -1 -> 11 -11 21
21 1 -> 11 -11 1
21 -1 -> 11 -11 -1
2 -2 -> 11 -11 21
21 2 -> 11 -11 2
21 -2 -> 11 -11 -2
```

```
vim: syntax=olp
#@OPL GOLEM 1.0
#@IgnoreUnknown True
#@IgnoreCase False
#@SyntaxExtensions
IRregularisation DRED | OK
AlphaPower 2 | OK
sin_th_2 0.221051079833 | OK # Ignored by OLP
Z_width 2.49 | OK # Ignored by OLP
Z_mass 91.118 | OK # Ignored by OLP
W_mass 80.419 | OK # Ignored by OLP
CorrectionType QCD | OK
AlphasPower 1 | OK
W_width 2.0476 | OK # Ignored by OLP
OperationMode CouplingsStrippedOff | OK
MatrixElementSquareType CHsummed | OK
1 -1 -> 11 -11 21 | 1 3
21 1 -> 11 -11 1 | 1 4
21 -1 -> 11 -11 -1 | 1 5
2 -2 -> 11 -11 21 | 1 0
21 2 -> 11 -11 2 | 1 1
21 -2 -> 11 -11 -2 | 1 2
```

Contract file

The terminal window shows the contents of a directory in a virtual environment. The files listed include configuration files, source code, and object files. Two files, `p0_ddbar_enepp` and `p3_uubar_enepp`, are highlighted with a red box.

```
Virtual : bash
File Edit View Scrollback Bookmarks Settings Help
luisonig@D22:Virtual$ ls
aclocal.m4      config.log      configure.ac    libgolem_olp.la  Makefile.am    olp_module.f90
autogen.sh     config.sh      gosam.rc       libtool          Makefile.in    olp_module.lo
autom4te.cache config.status  include        m4              model          olp_module.mod
config.aux     configure     lib           Makefile        olp.h          olp_module.o
luisonig@D22:Virtual$
```

GoSam produces only the code strictly needed avoiding redundancies and exploiting crossing-symmetry



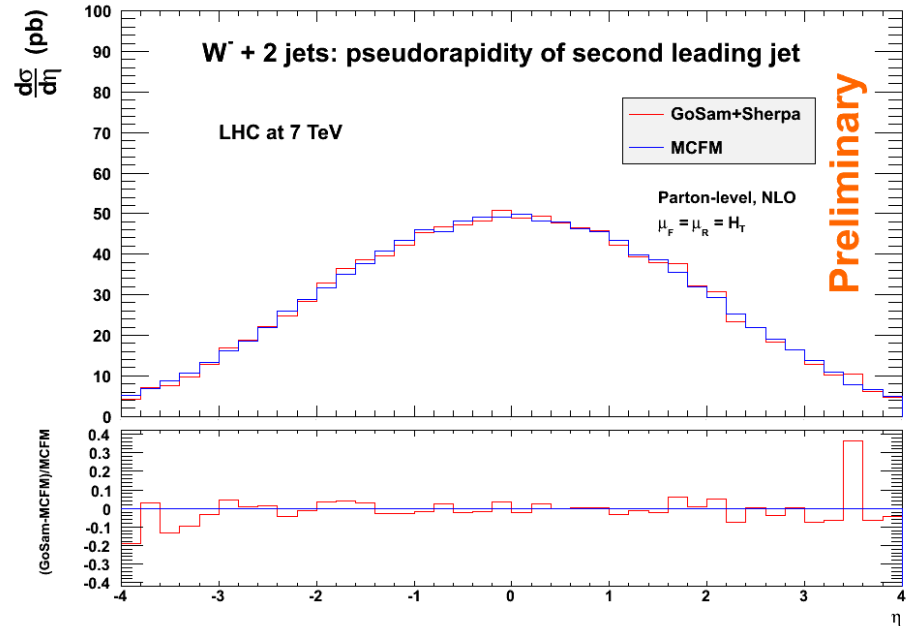
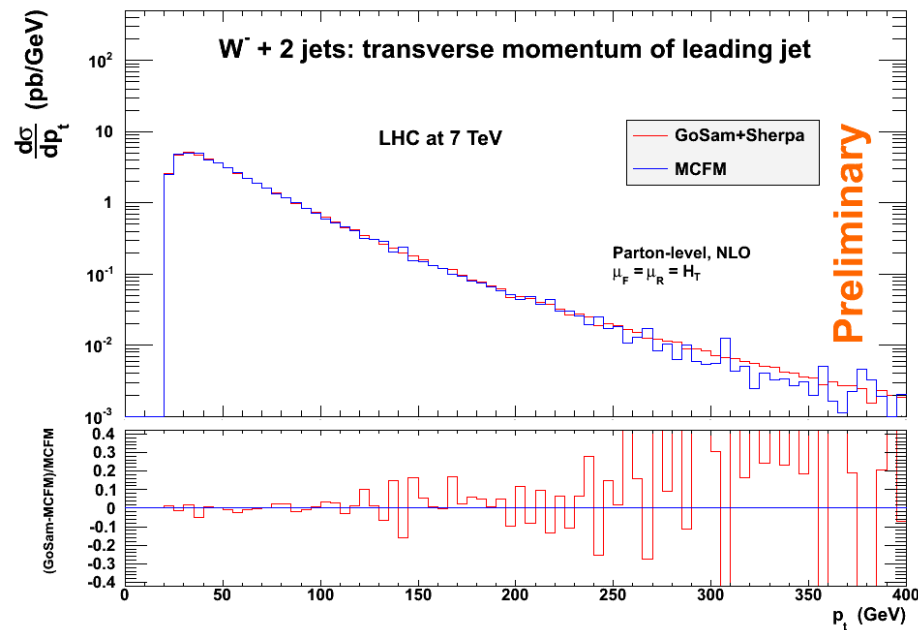
In practice: GoSam+ Sherpa

- Few steps needed to compute e.g. Z+1 jet @NLO:
 - Prepare Sherpa card according to your need and run it once
 - The “order” file and the necessary tree-level code is generated
 - Run GoSam feeding the “order” file and a configuration file with further needed inputs (paths / filtering options / ...)
 - Run GoSam with “autotools” extension will make it easy to produce a dynamical library which can be linked to Sherpa
 - After the virtual code is set up, generate and compile it with **configure / make / make install**
 - The produced library `libgolem_olp.so` must be added to the `SHERPA_LDADD` option in the Sherpa card

➡ HAVE FUN WITH PHENOMENOLOGY



GoSam+Sherpa vs MCFM: $W^- + 2$ jets



TIMINGS:

Set-up	Virtual: < 1 min 30 sec
Generation & Compilation	Virtual: ~ 2h 30 min
Running	Born : ~20 min Real : ~ 18h 30 min Virtual: ~ 13h

Machine Intel(R) Core(TM)2 Quad CPU Q6600 @ 2.40GHz

NUMBER OF EVENTS:

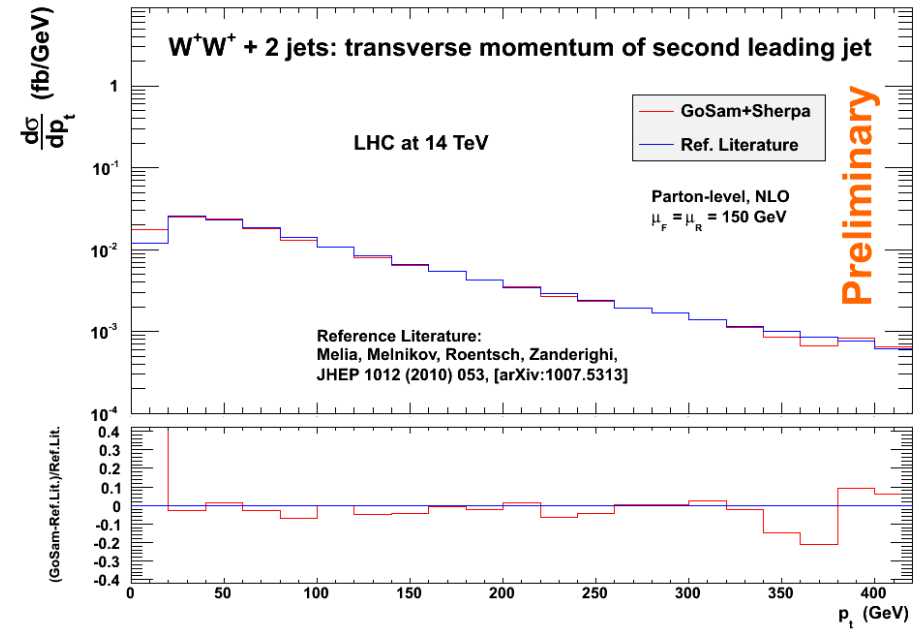
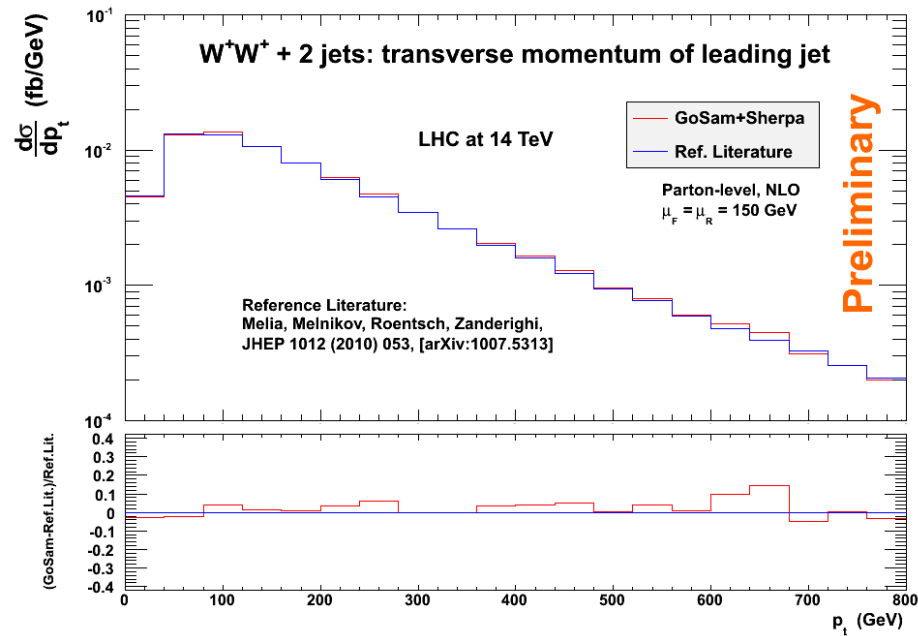
Born :	5'000'000 x 2
Real :	50'000'000 x 20
Virtual:	1'000'000 x 10

PHYSICS:

	LHC 7 TeV
Cuts	pt_jet > 20 GeV eta_jet < 4.0 kt_alg, R=0.7
Scale	H_T
PDFs	CT10.LHgrid



GoSam+Sherpa vs Melia et al.: $W^+W^+ + 2$ jets



TIMINGS:

Set-up
Virtual: < 1 min 30 sec

Generation & Compilation
Virtual: ~ 7h 25 min

Running
Born : ~ 30 min
Real : ~ 13h 30 min
Virtual: ~ 7h

Machine Intel(R) Core(TM)2 Quad CPU Q6600 @ 2.40GHz

NUMBER OF EVENTS:

Born : 1'000'000 x 10
Real : 50'000'000 x 10
Virtual: 1'000'000 x 10

PHYSICS:

LHC 7 TeV

Cuts
pt_lep > 20 GeV
|eta_lep| < 2.4
pt_miss > 30 GeV
antikt_alg, R=0.4

Scale 150 GeV

PDFs MSTW2008nlo.LHgrid



IPPP, University of Durham

GoSam+ Sherpa: comments

- Automated NLO calculations with GoSam+Sherpa
 - Two codes can be linked with very few commands
 - High level of automation and optimization in the generated code
 - Sherpa 1.4.0 (released yesterday!) has the BLHA-interface active and is fully equipped to interface with GoSam
 - Some ready-to-use packages for 2->2, 2->3, 2->4 processes to be used with Sherpa will **soon** become available (no need to run GoSam locally)
[<http://projects.hepforge.org/gosam/proc/>]

Conclusions and Outlook

- **GoSam** is a code for the computation of one-loop multi-leg amplitudes
 - Based on **Feynman diagrams**
 - Uses D-dimensional reduction techniques
 - **Flexible** and broadly applicable tool
 - **Public**
 - **Easy to interface** with MC event generator to perform full NLO calculations
- Possibilities for precision studies using NLO parton-level matched with parton-shower and with hadronization effects just around the corner
 - Possible to steer everything by just editing a single input card
- We look forward to interfacing with other tools and performing NLO analyses for the LHC

<http://projects.hepforge.org/gosam/>

Backup slides...



Reduction methods: Samurai [default]

[Mastrolia, Ossola, Reiter, Tramontano 10]

- OPP reduction algorithm [Ossola, Papadopoulos, Pittau 07]
- D-dimensional extension [Ellis, Giele, Kunszt, Melnikov 08]
- Coefficient of polynomials via DFT [Mastrolia et al. 08]
- Computation of the full rational term in one go [Internal GoSam algebraic handling]

For any one-loop amplitude:

$$\mathcal{A}_n = \int d^d \bar{q} \frac{\mathcal{N}(\bar{q}, \epsilon)}{\bar{D}_0 \bar{D}_1 \cdots \bar{D}_{n-1}} \quad ; \quad \mathcal{N}(\bar{q}, \epsilon) = N_0(\bar{q}) + \epsilon N_1(\bar{q}) + \epsilon^2 N_2(\bar{q})$$

$$\bar{D}_i = (\bar{q} + p_i)^2 - m_i^2 = (q + p_i)^2 - m_i^2 - \mu^2 \quad ; \quad \not{q} = \not{q} + \not{\mu} \quad ; \quad \bar{q}^2 = q^2 - \mu^2$$

Result of integration can be expressed as linear combination of scalar integrals:
boxes, triangles, bubbles, tadpoles and rational terms

Integrals with μ^2 in
the numerator

$$\mathcal{A}_n = \sum_{i_0 < i_1 < i_2 < i_3}^{m-1} d(i_0 i_1 i_2 i_3) D_0(i_0 i_1 i_2 i_3) + \sum_{i_0 < i_1 < i_2}^{m-1} c(i_0 i_1 i_2) C_0(i_0 i_1 i_2) + \sum_{i_0 < i_1}^{m-1} b(i_0 i_1) B_0(i_0 i_1) + \sum_{i_0}^{m-1} a(i_0) A_0(i_0) + \mathcal{R}$$

Reduction methods: Tensorial Reconstr.

[Heinrich, Ossola, Reiter, Tramontano 10]

- Tensorial reconstruction convoluted with tensor integrals:

Rewrite numerator function as linear combination of tensors

$$\mathcal{N}(q) = \sum_{r=0}^R C_{\mu_1 \dots \mu_r} q_{\mu_1} \dots q_{\mu_r}$$

$$C_{\mu_1 \dots \mu_r} q_{\mu_1} \dots q_{\mu_r} = \sum_{(i_1, i_2, i_3, i_4) \vdash r} \hat{C}_{i_1 i_2 i_3 i_4}^{(r)} \cdot (q_1)^{i_1} (q_2)^{i_2} (q_3)^{i_3} (q_4)^{i_4}$$

Determine the coefficients by sampling in q_μ in a bottom-up approach

if $q_\mu = (x, y, z, w)$ then $\mathcal{N}(q) = \mathcal{N}(x, y, z, w)$

Level-0 $q = (0, 0, 0, 0)$; $\mathcal{N}(0, 0, 0, 0) \equiv \mathcal{N}^{(0)} = C_0$

Level-1 4 systems, each sampling a monomial depending on one component of q_μ only

$$\mathcal{N}^{(1)}(q) \equiv \mathcal{N}(q) - \mathcal{N}^{(0)}$$

$$q = (x, 0, 0, 0) \Rightarrow \mathcal{N}^{(1)}(x, 0, 0, 0) \equiv x C_1 + x^2 C_{11} + \dots + x^R \underbrace{C_{11 \dots 1}}_{R \text{ times}}$$

$$q = (0, y, 0, 0) \Rightarrow \mathcal{N}^{(1)}(0, y, 0, 0) \equiv y C_2 + y^2 C_{22} + \dots + y^R \underbrace{C_{22 \dots 2}}_{R \text{ times}}$$

Allows to avoid numerical instabilities due to vanishing Gram determinants

Derive & Numpolvec

- The latest version of GoSam also implements two new features to improve speed and precision:

- **derive**: computes the numerator by expanding it in a Taylor series

$$\mathcal{N}(\hat{q}) = \mathcal{N}(0) + \hat{q}^\mu \frac{\partial}{\partial \hat{q}_\mu} \mathcal{N}(\hat{q})|_{q=0} + \frac{1}{2!} \hat{q}^\mu \hat{q}^\nu \frac{\partial}{\partial \hat{q}_\mu} \frac{\partial}{\partial \hat{q}_\nu} \mathcal{N}(\hat{q})|_{q=0} + \dots$$

one-to-one correspondence between derivatives at $\hat{q} = 0$ and the coefficients of the tensor integrals

- **numpolvec**: uses numerical polarization vectors for external massless gauge bosons
 - this allows to reduce the code by generating only few helicities

3-Steps to the Loop Amplitude

GOSAM

Code set-up

- Python program writes code files from template
 - QGRAPH writes structure of diagrams

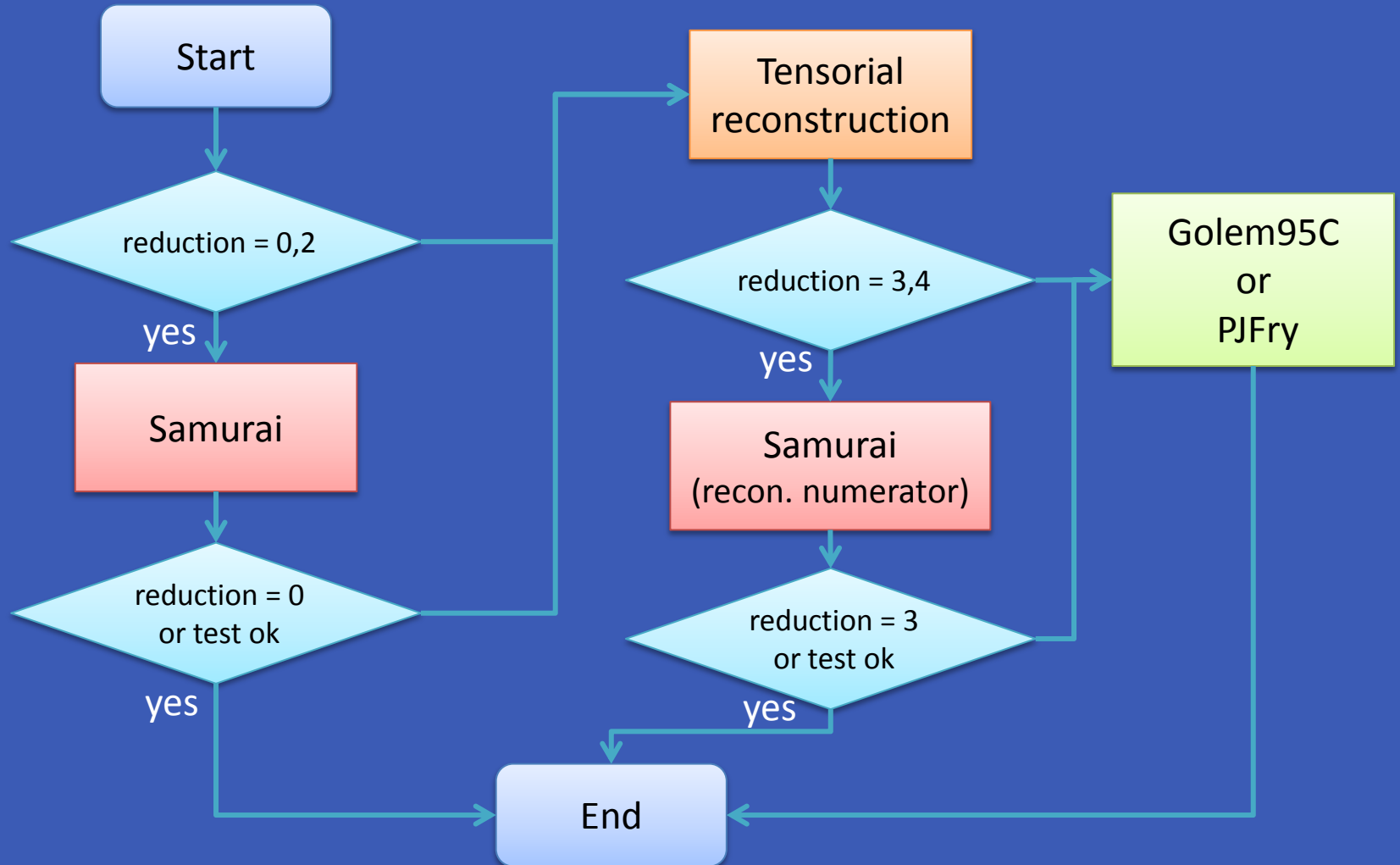
Code creation
and compilation

- Fortran code is compiled and amplitudes are written
 - FORM & SPINNEY read and manipulates amplitudes
 - HAGGIES optimizes expressions and writes fortran code

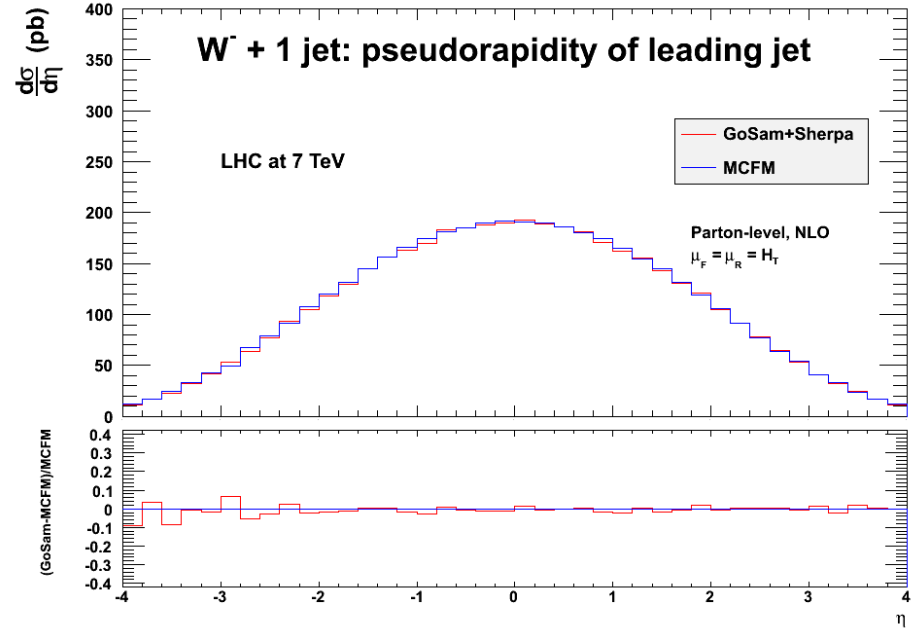
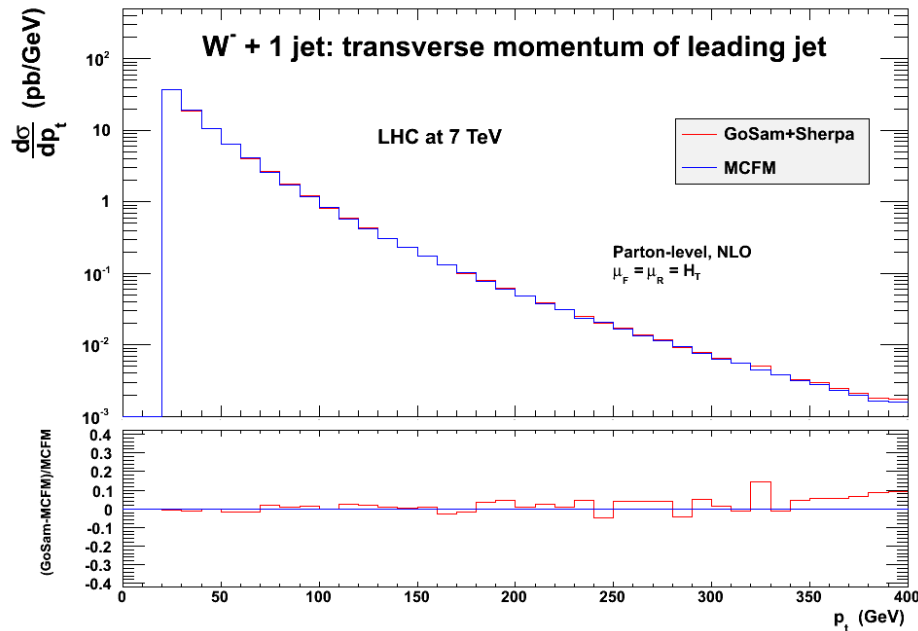
Code execution

- Fortran code computes amplitudes
 - SAMURAI/GOLEM95/... called to reduce integrals
 - AVHOLO/QCDLOOP/... called to evaluate scalar integrals

Reduction: strategies



GoSam+Sherpa vs MCFM: W+1 jet



TIMINGS:

Set-up
 Virtual: < 10 sec

Generation & Compilation
 Virtual: < 2 min

Running
 Born : < 2h
 Real : ~ 4h 20 min
 Virtual: ~ 1h 10 min

Machine Intel(R) Core(TM)2 Quad CPU Q6600 @ 2.40GHz

NUMBER OF EVENTS:

Born : 50'000'000
 Real : 50'000'000 x 5
 Virtual: 5'000'000 x 5

PHYSICS:

LHC 7 TeV

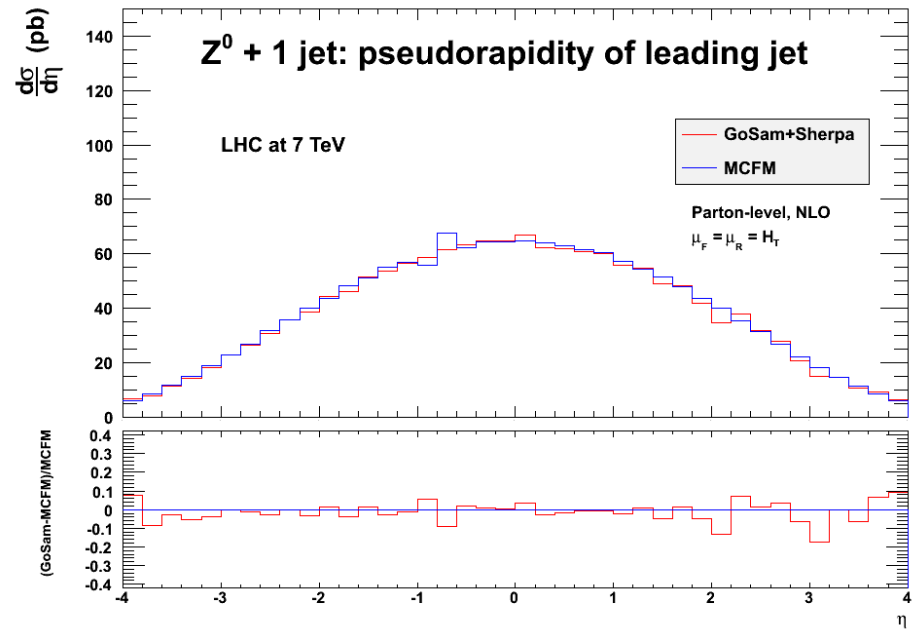
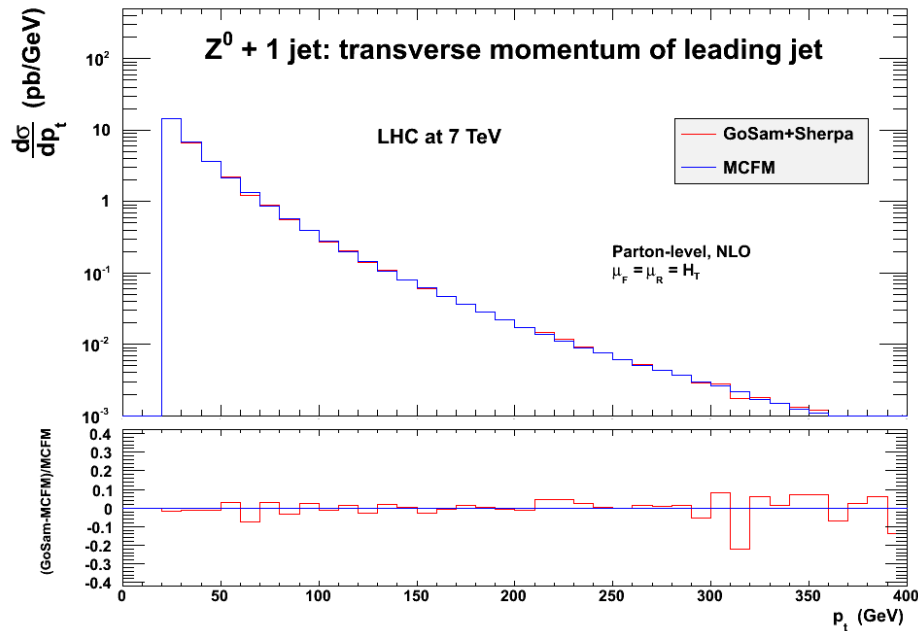
Cuts
 $p_{t_jet} > 20$ GeV
 $\eta_{jet} < 4.0$
 $kt_alg, R=0.7$

Scale H_T

PDFs CT10.LHgrid



GoSam+Sherpa vs MCFM: Z+1 jet



TIMINGS:

Set-up
 Virtual: < 20 sec

Generation & Compilation
 Virtual: < 25 min

Running
 Born : < 2h
 Real : ~ 5h
 Virtual: ~ 15h 30 min

Machine Intel(R) Core(TM)2 Quad CPU Q6600 @ 2.40GHz

NUMBER OF EVENTS:

Born : 5'000'000
 Real : 50'000'000 x 6
 Virtual: 5'000'000 x 6

PHYSICS:

LHC 7 TeV

Cuts
 $p_{t_jet} > 20$ GeV
 $\eta_{jet} < 4.0$
 $kt_alg, R=0.7$
 $m(e+e-) > 15$ GeV

Scale H_T

PDFs CT10.LHgrid



IPPP, University of Durham

BSM physics with GoSam

- New models can be added via **FeynRules** [Christensen, Duhr] **LanHEP** [Semenov]
- Allows to compute one-loop corrections also for BSM phenomenology

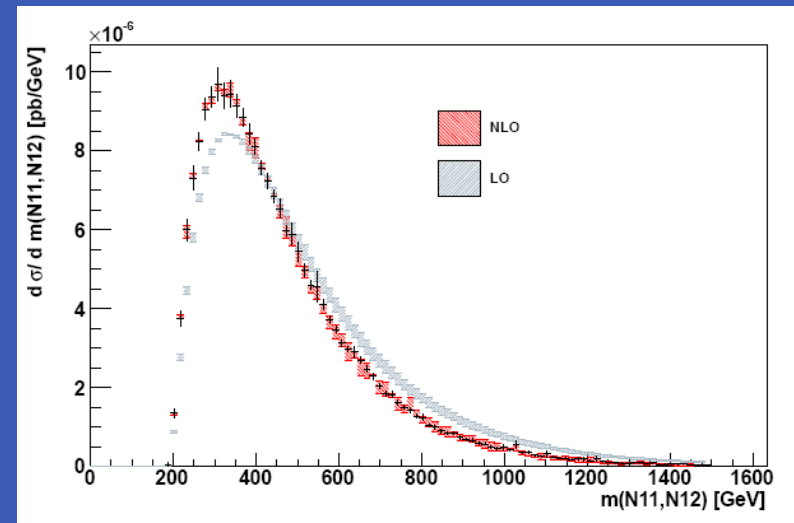
- Example: $pp \longrightarrow \chi_0^1 \chi_0^1$ in MSSM

Veto:

$pt_{jet} > 20 \text{ GeV}$
 $eta_{jet} < 4.5$

Scale

M_z



[Figure by G.Cullen and N.Greiner]