

# Upgrade on Fragmentation Functions

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LHCphenOnet



# Outline

- ◆ Introduction/Motivation
- ◆ Constraining FFs with SIA, SIDIS and Hadron-Hadron Collisions
- ◆ Global Fits of FFs
- ◆ Conclusions

# FFs ( $D_q^h(z, \mu)$ )

- ◆ FFs are relevant any time a hadron is produced in High Energy Collisions.
- ◆ Non-perturbative objects to be extracted from data (like PDFs). They are scale dependent predicted by QCD.
- ◆ Describe the collinear transition of a massless parton “q” into a massless hadron “h” carrying fractional momentum “z”.
- ◆ The fragmentation is independent of other colored particles.
- ◆ Needed to consistently absorb final-state collinear singularities.
- ◆ Precise FFs are needed to extract PDFs more precisely.

# ete- Single Inclusive Annihilation

The distribution is given in terms of the structure functions,

$$\frac{1}{\sigma_{tot}} \frac{d\sigma^h}{dz} = \frac{\sigma^0}{\sum_q \hat{e}_q^2} [2F_1^H(z, Q^2) + F_L^H(z, Q^2)] \quad \sigma_{tot} = \sum_q \frac{4\pi\alpha_s^2}{s} \hat{e}_q^2 \left( 1 + \frac{\alpha_s}{\pi} \dots \right)$$

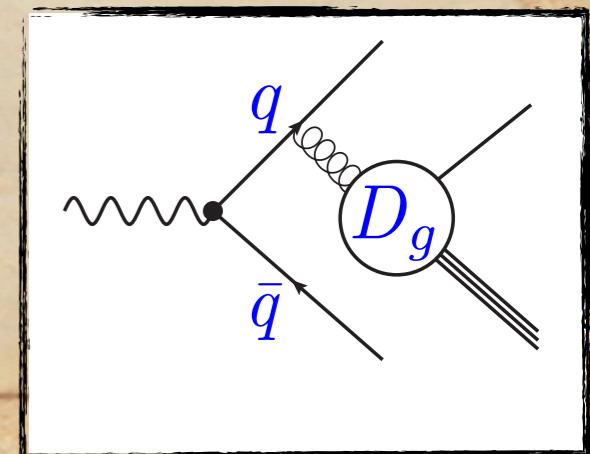
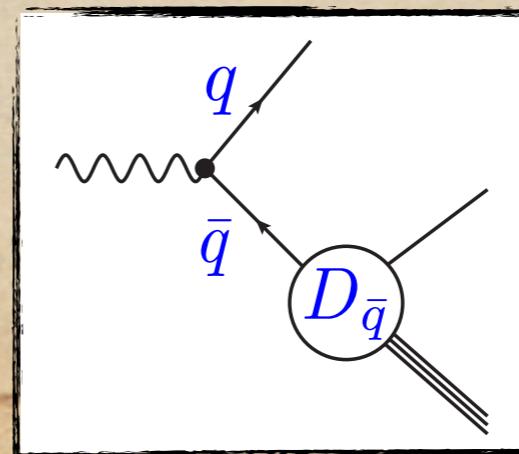
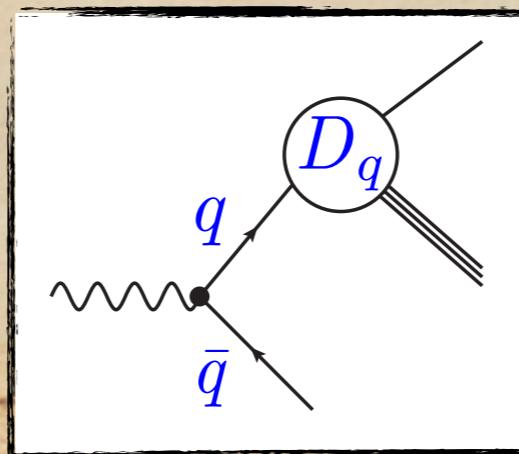
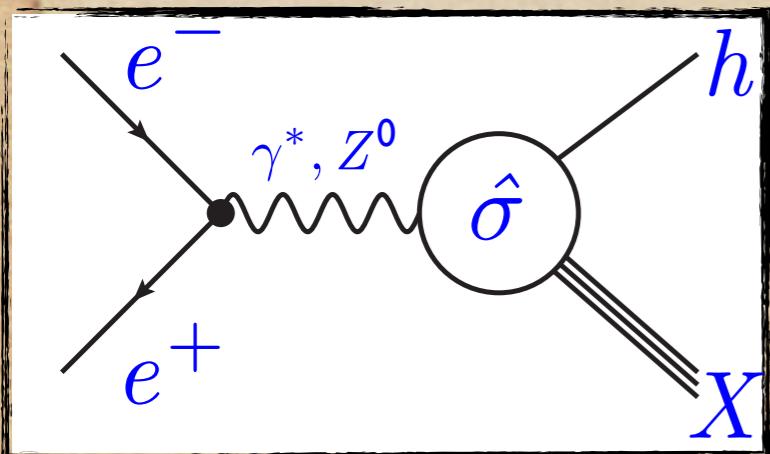
@NLO

$$2F_1^H(z, Q^2) = \sum_q \hat{e}_q^2 \left\{ [D_q^H(z, Q^2) + D_{\bar{q}}^H(z, Q^2)] + \frac{\alpha_s(Q^2)}{2\pi} [C_q^I \otimes [D_q^H + D_{\bar{q}}^H] + C_g^I \otimes D_g^H](z, Q^2) \right\}$$

FFs depend on energy fraction and energy scale: AP evolution

$$\frac{d}{d \ln Q^2} \mathbf{D}^H = [\hat{P} \otimes \mathbf{D}^H](z, Q^2)$$

Not possible to separate  $\mathcal{D}_q^h(z, \mu)$  and  $\mathcal{D}_{\bar{q}}^h(z, \mu)$



# SIDIS

Distributions for SIDIS are given by

$$\frac{d\sigma^H}{dxdydz^H} = \frac{2\pi\alpha_s}{Q^2} \left[ \frac{1 + (1 - y)^2}{y} 2F_1^H(x, z_H, Q^2) + \frac{2(1 - y)}{y} F_L^H(x, z_H, Q^2) \right]$$

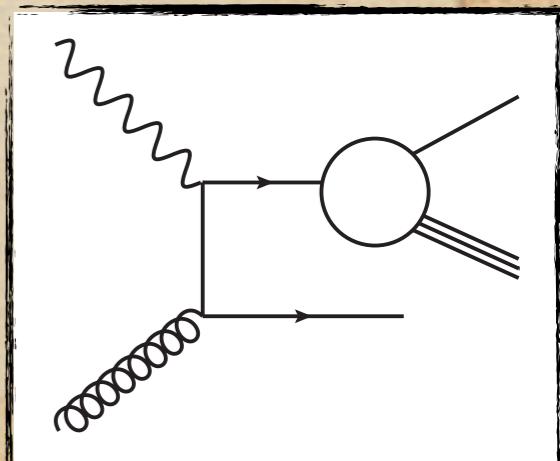
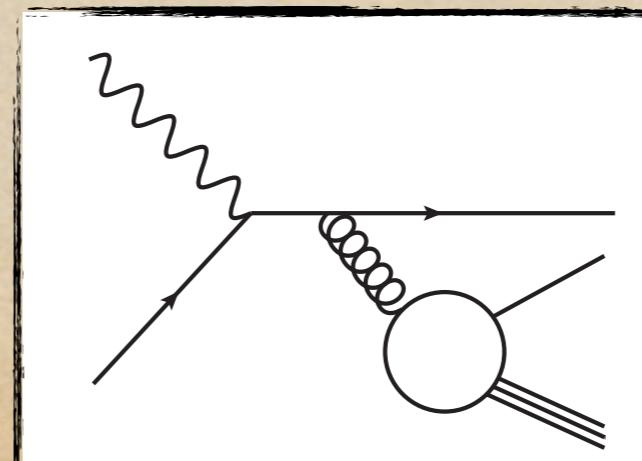
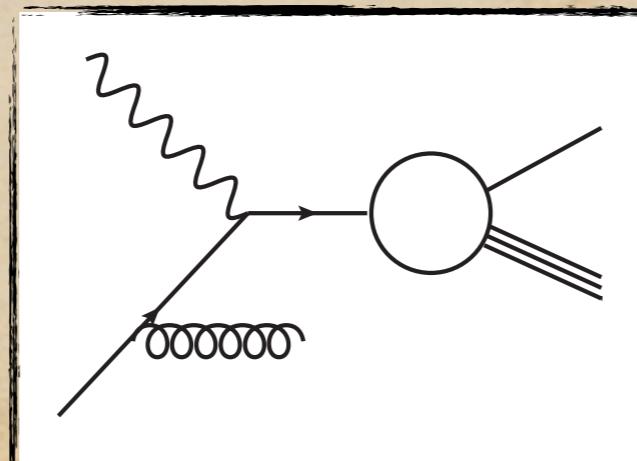
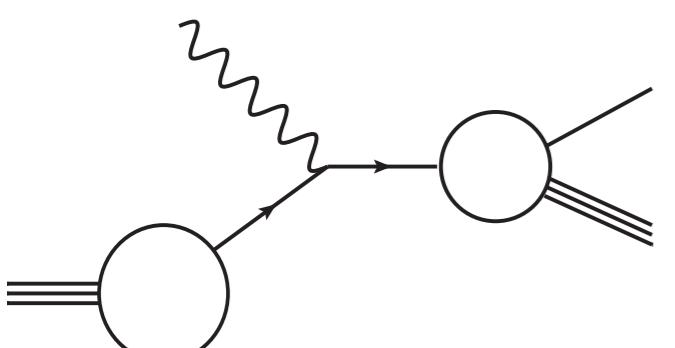
@LO  $2F_1^H(x, z_H, Q^2) = \sum_{q, \bar{q}} \hat{e}_q^2 \cdot q(x, Q^2) D_q^H(z_H, Q^2)$

effective charge

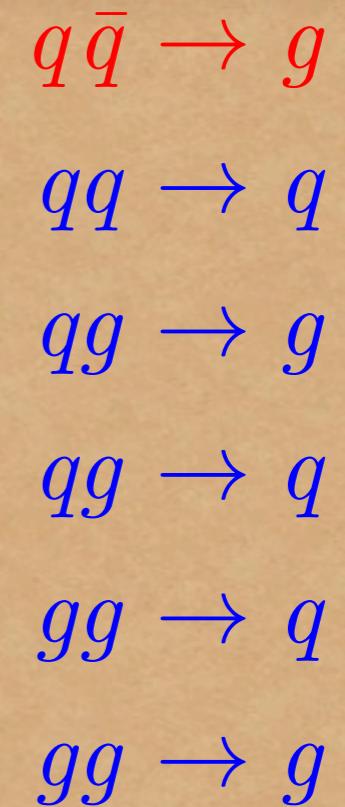
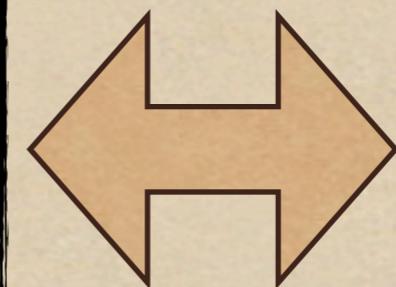
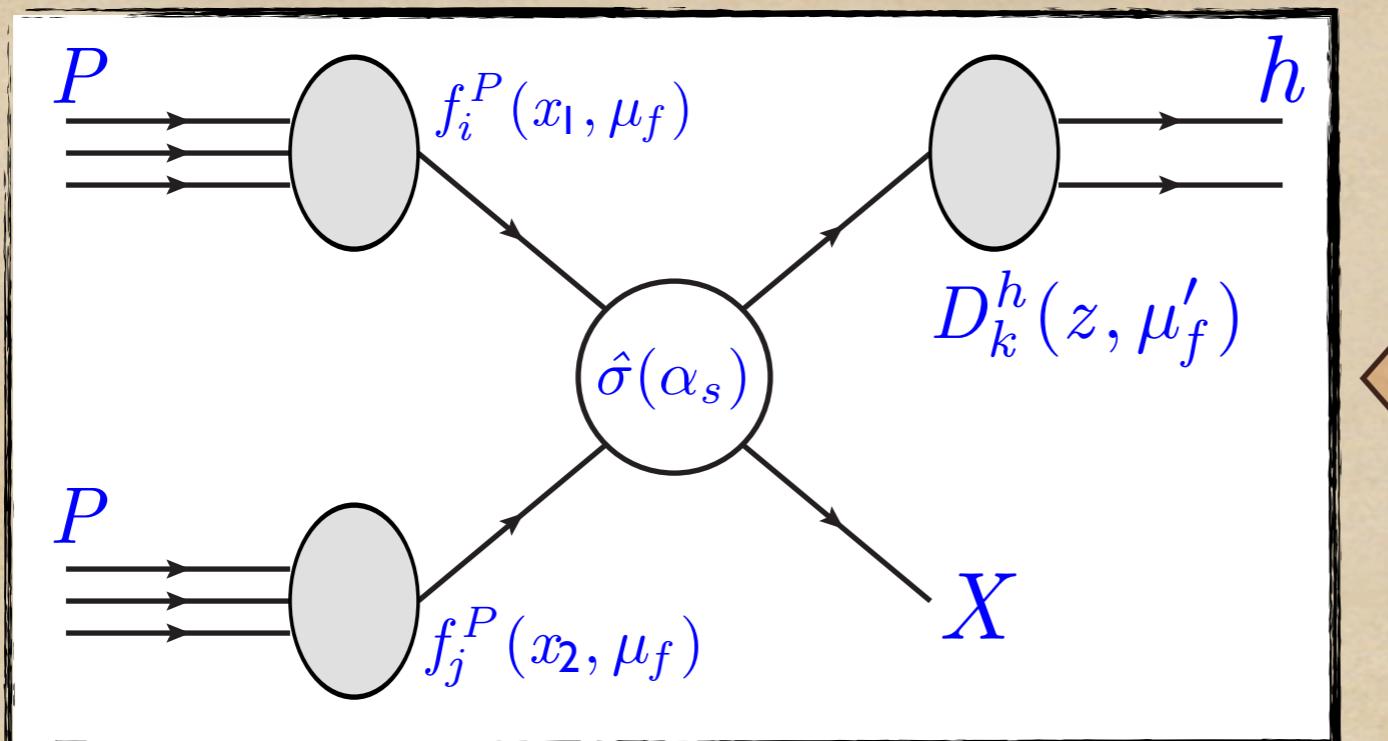
*Allows charge/flavor separation.*

@NLO

*Altarelli et al.'79;  
Furmanski, Petronzio'82;  
de Florian, Stratmann, Vogelsang'98*



# Hadron-Hadron Collisions



Transverse momentum distribution is

$$\frac{d\sigma(pp \rightarrow hX)}{dp_T d\eta} = \sum_{i,j,k} \int_0^1 dx_1 f_i^P(x_1, \mu_f) \int_0^1 f_j^P(x_2, \mu_f) \int_0^1 dz D_k^h(z, \mu'_f) \frac{d\hat{\sigma}(ij \rightarrow kX')}{dp_T d\eta}$$

It also allows charge/flavor separation.

It contains large contributions from gluons.

# Global Analyses

- Constrain FFs with almost all available data.
- Check of pQCD framework
- Precise determination of the distributions

Data are taken from the experiments,

- SIA : TPC, TASSO, SLD, ALEPH, DELPHI, OPHAL
- SIDIS: HERMES, COMPASS
- Hadron-Hadron Collisions: PHENIX, STAR, BRAHMS, ,  
UA1

# Global analysis method

Parametrization

$$\mathcal{D}_i^H(z, Q_0^2) = N_i z^{\alpha_i} (1-z)^{\beta_i} [1 + \gamma_i (1-z)^{\delta_i}]$$

at scale

$$Q_0^2 = 1 \text{ GeV}^2 \quad u, d, s, g$$

$$Q_0^2 = m_Q^2 \quad c, b$$

Normalization for different experiments

Allowing for possible breaking of  $SU(3)$  of sea and  $SU(2)$  in favored distributions,

$$\mathcal{D}_{d+\bar{d}}^{\pi^+} = N \mathcal{D}_{u+\bar{u}}^{\pi^+} \quad \mathcal{D}_s^{\pi^+} = \mathcal{D}_{\bar{s}}^{\pi^+} = N' \mathcal{D}_{\bar{u}}^{\pi^+}$$

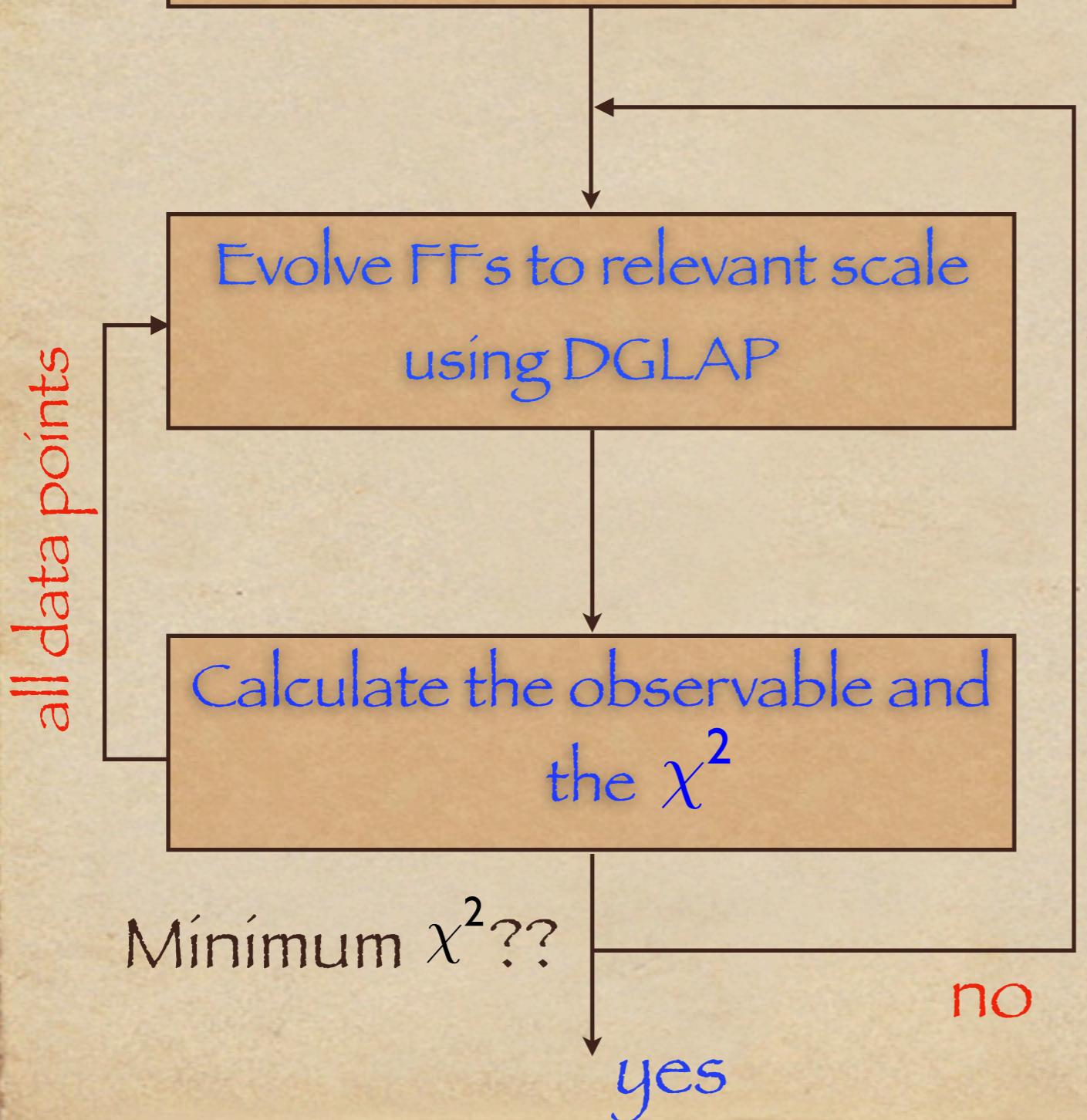
Allow flexible distributions for unfavored fragmentations,

$$\mathcal{D}_{\bar{u}}^{\pi^+} = N_{ud} (1-z)^{\epsilon_{ud}} \mathcal{D}_d^{\pi^+} \quad \mathcal{D}_{\bar{u}}^{K^+} = N_{us} (1-z)^{\epsilon_{us}} \mathcal{D}_s^{K^+} = \mathcal{D}_d^{K^+} = \mathcal{D}_{\bar{d}}^{K^+}$$

Model Ansatz for FFs with  
initial set of parameters

$$\mathcal{D}_i^H(z, Q_0^2) = N_i z^{\alpha_i} (1-z)^{\beta_i} [1 + \gamma_i (1-z)^{\delta_i}]$$

33 parameters to fit

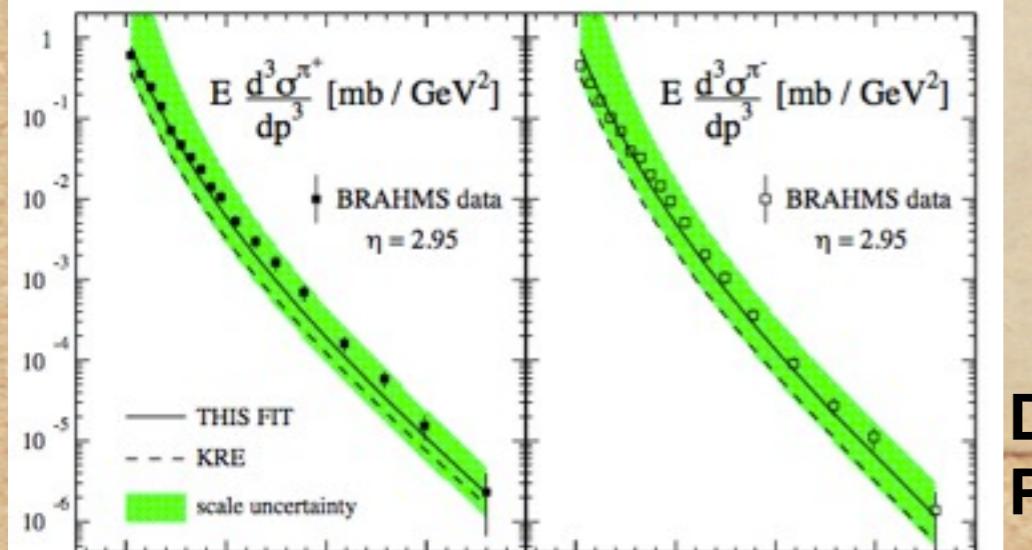
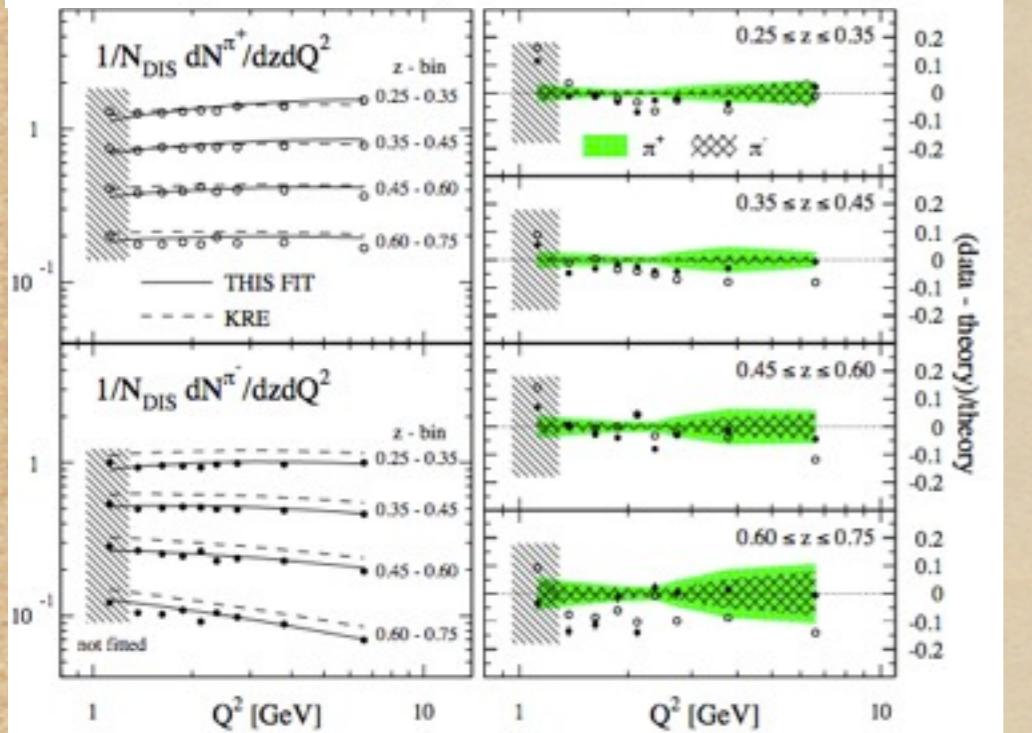
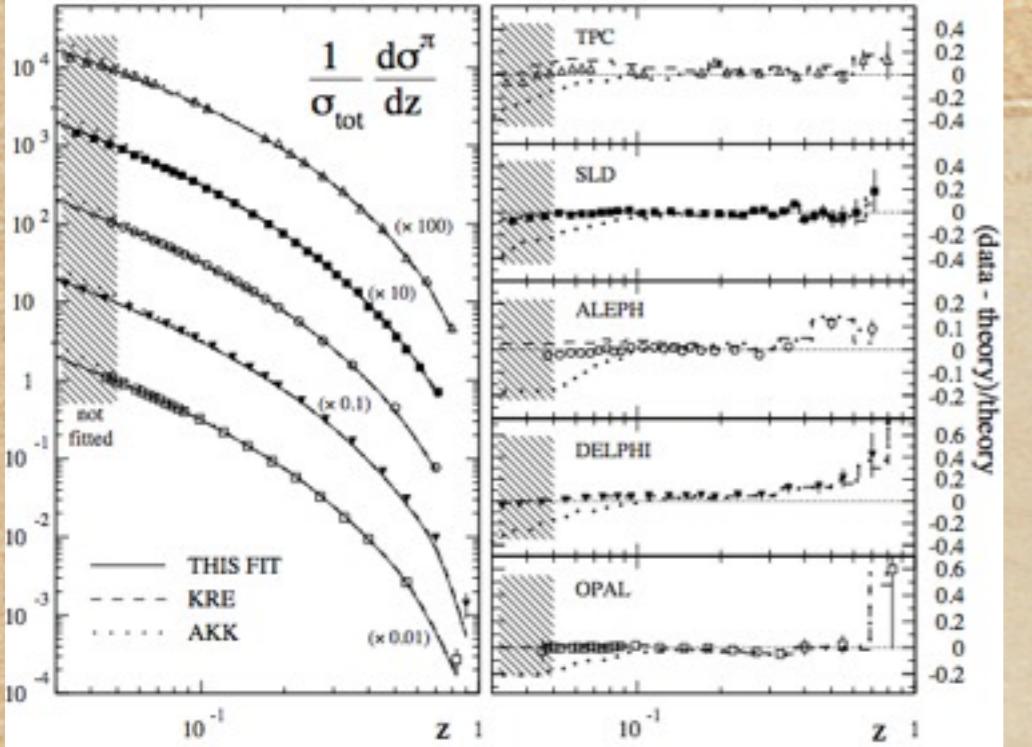


adjust parameters

Integration using the  
Mellin Technique  
 $\otimes \rightarrow \cdot$

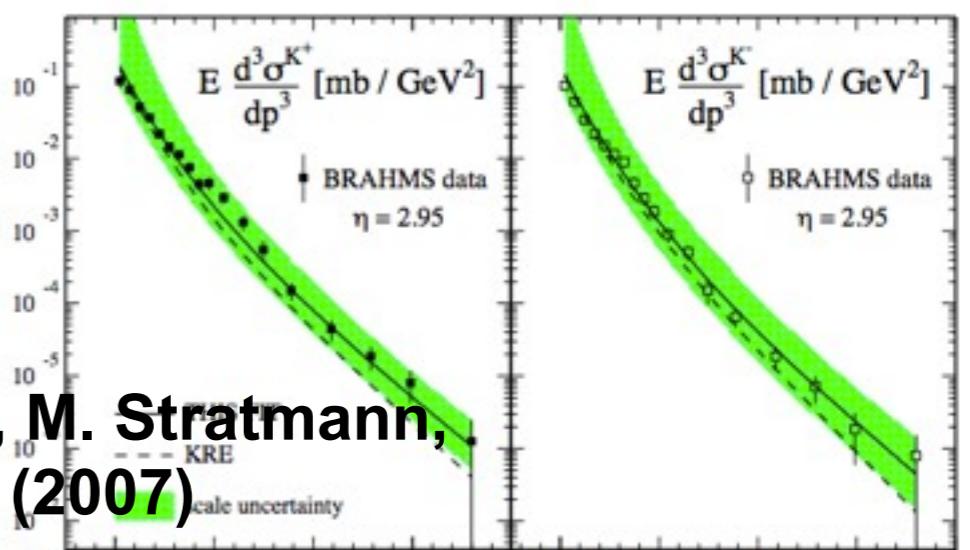
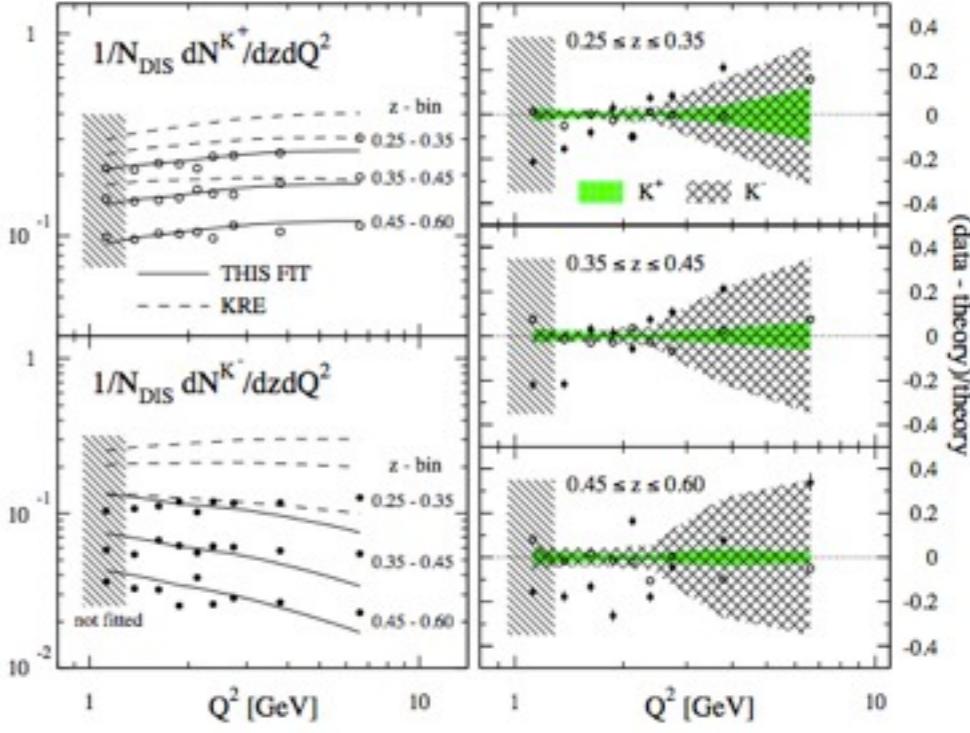
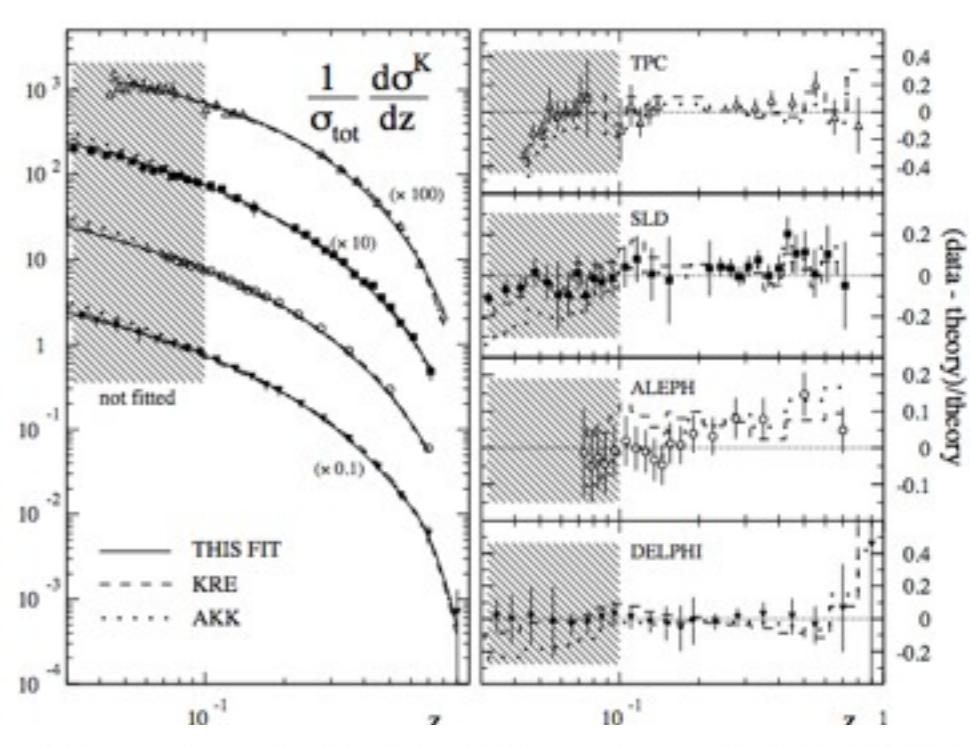
New grids using NLO  
MSTW2008 PDFs

Standard  $\chi^2$  minimization  
(MINUIT)

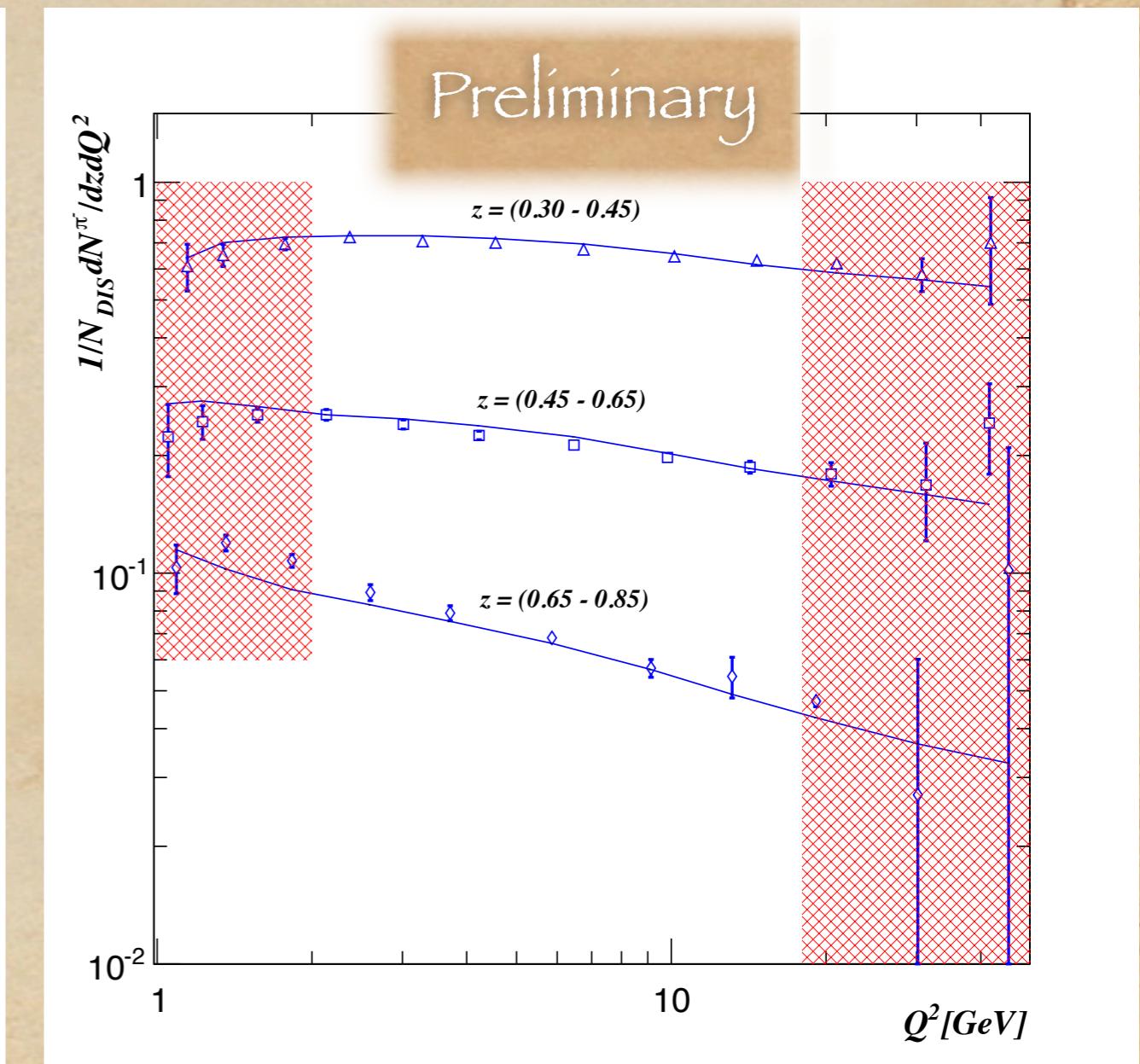
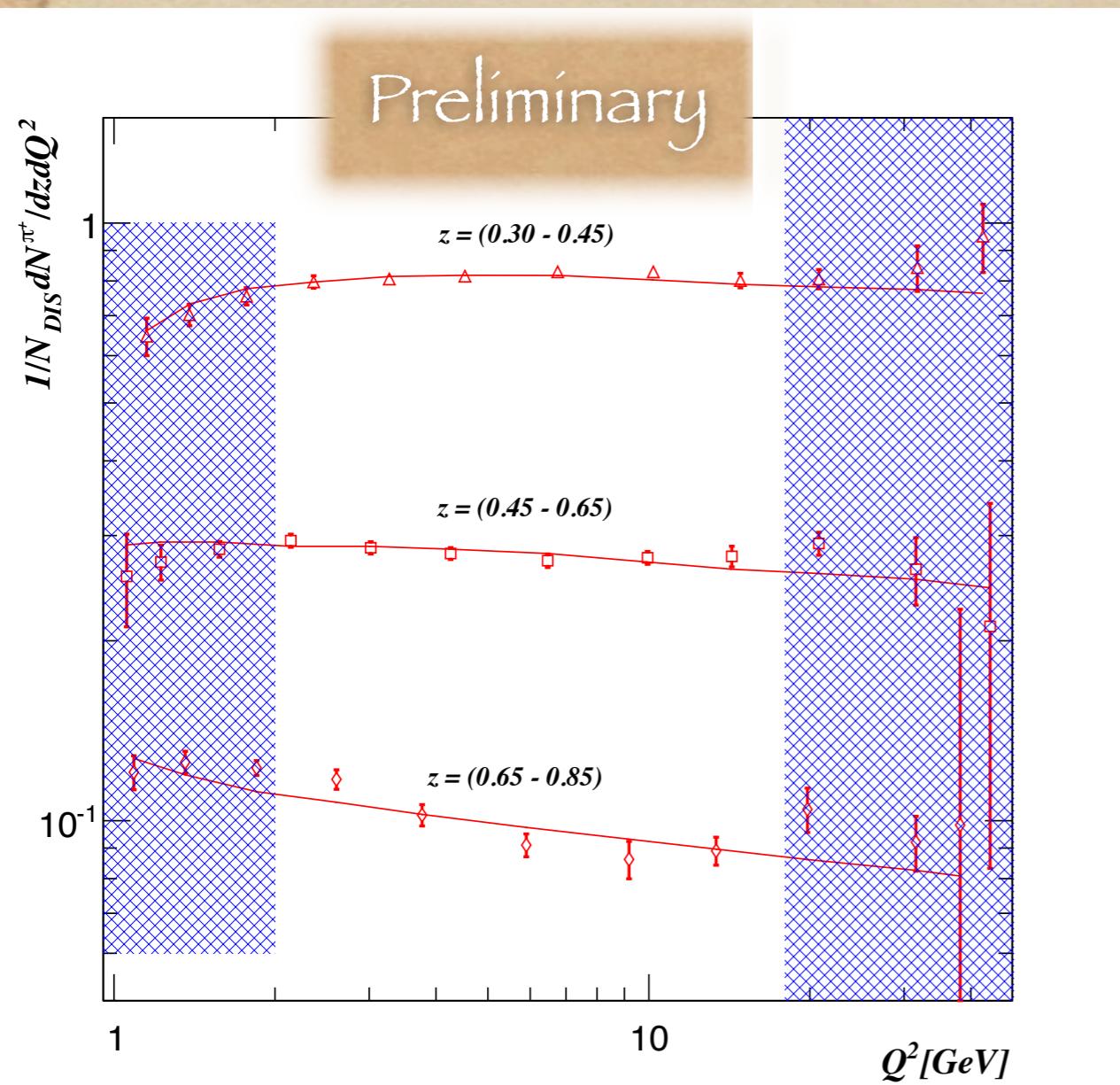


DSS  
Fit

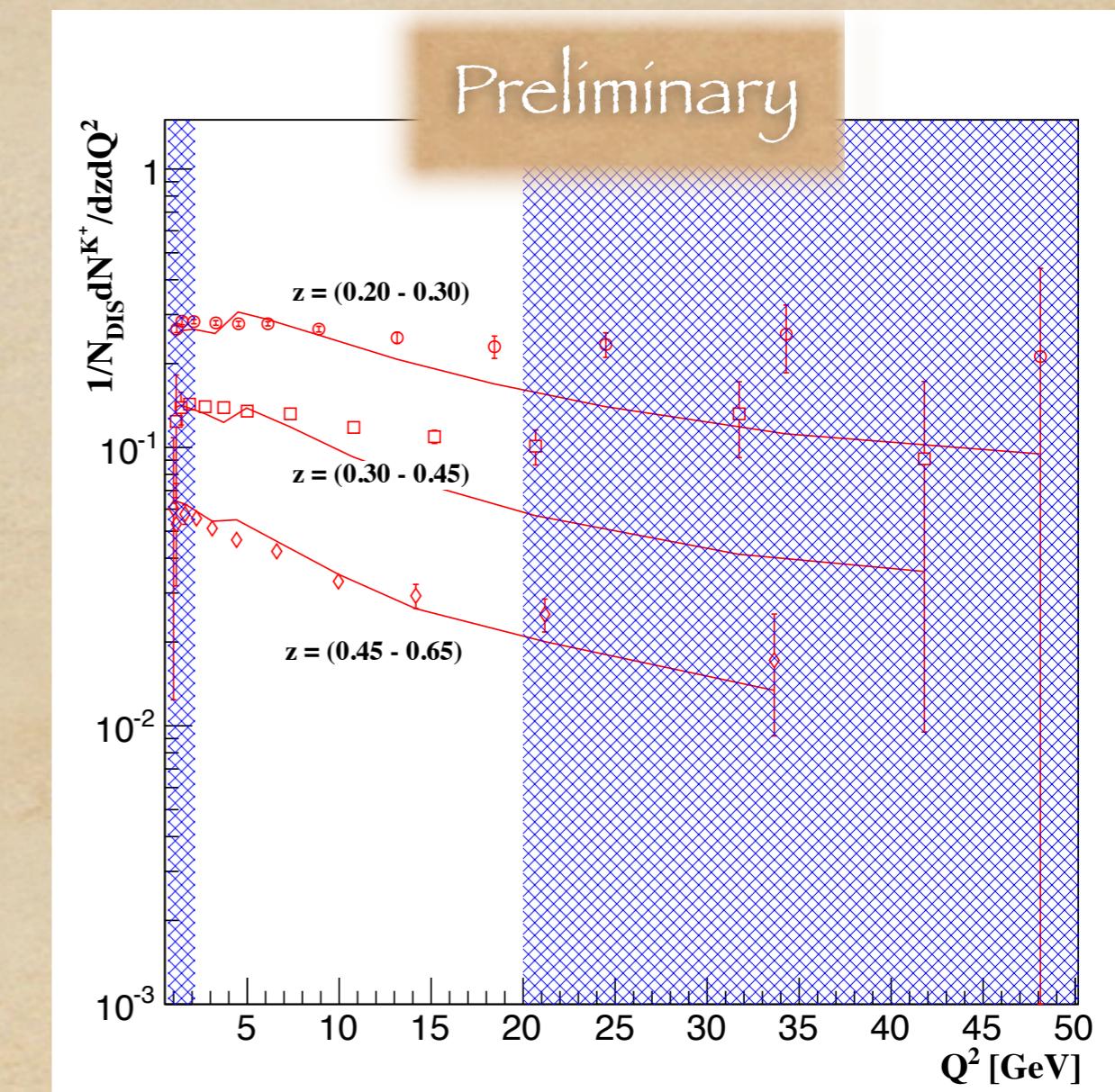
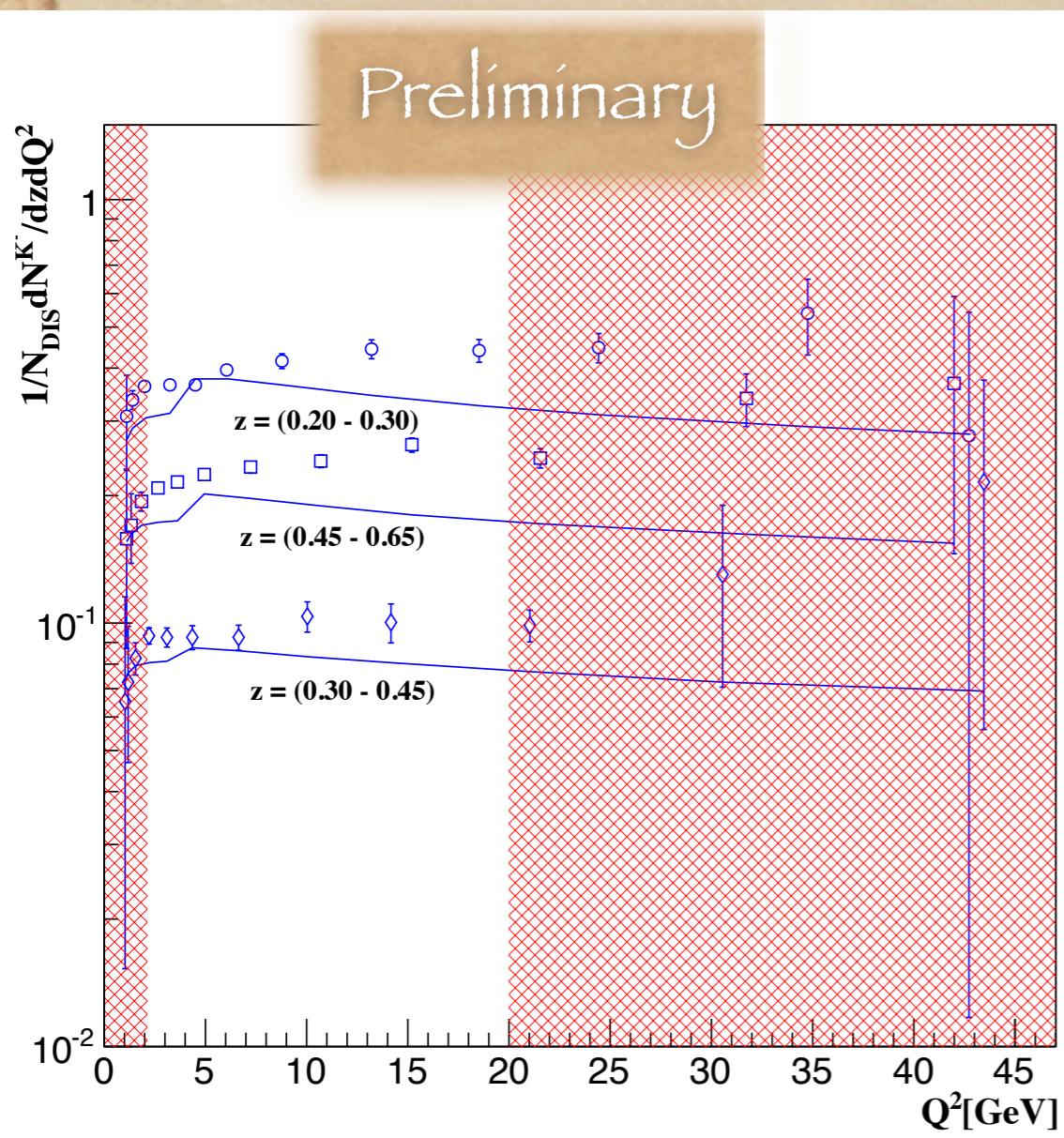
D. de Florian, R. Sassot, M. Stratmann,  
Phys. Rev. D 75, 114010 (2007)

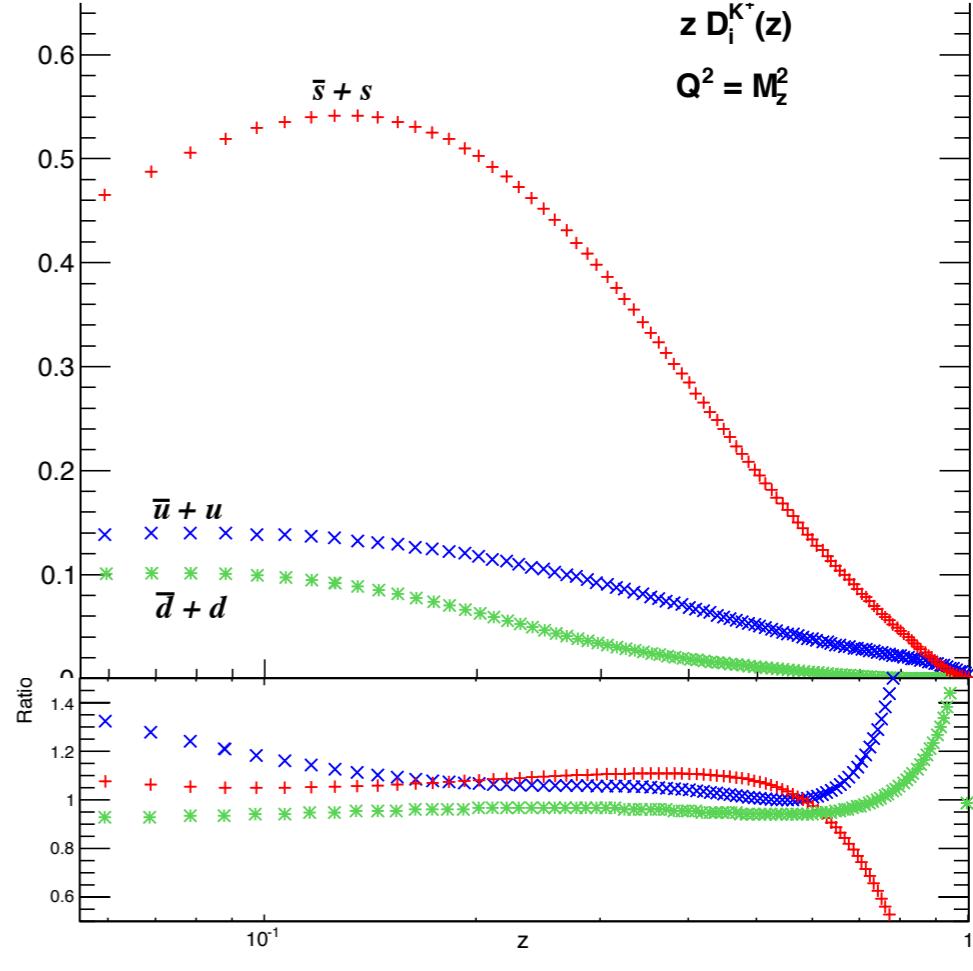
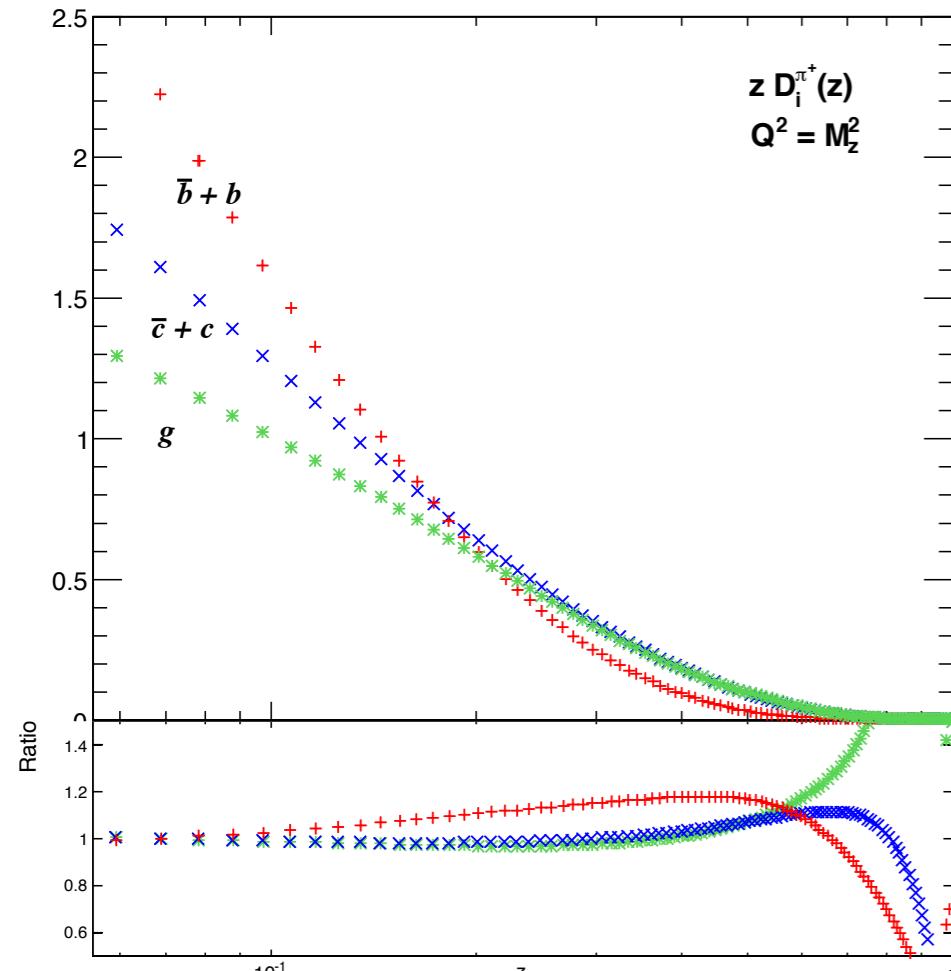
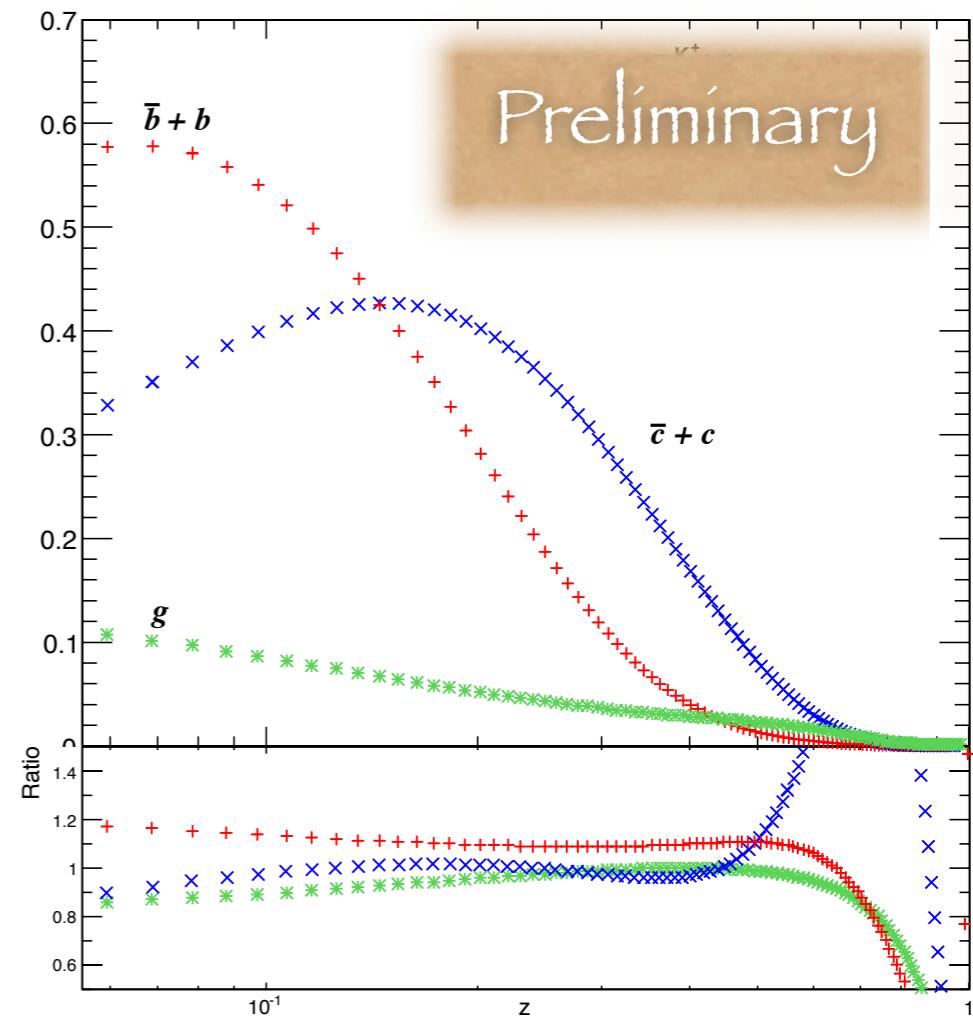
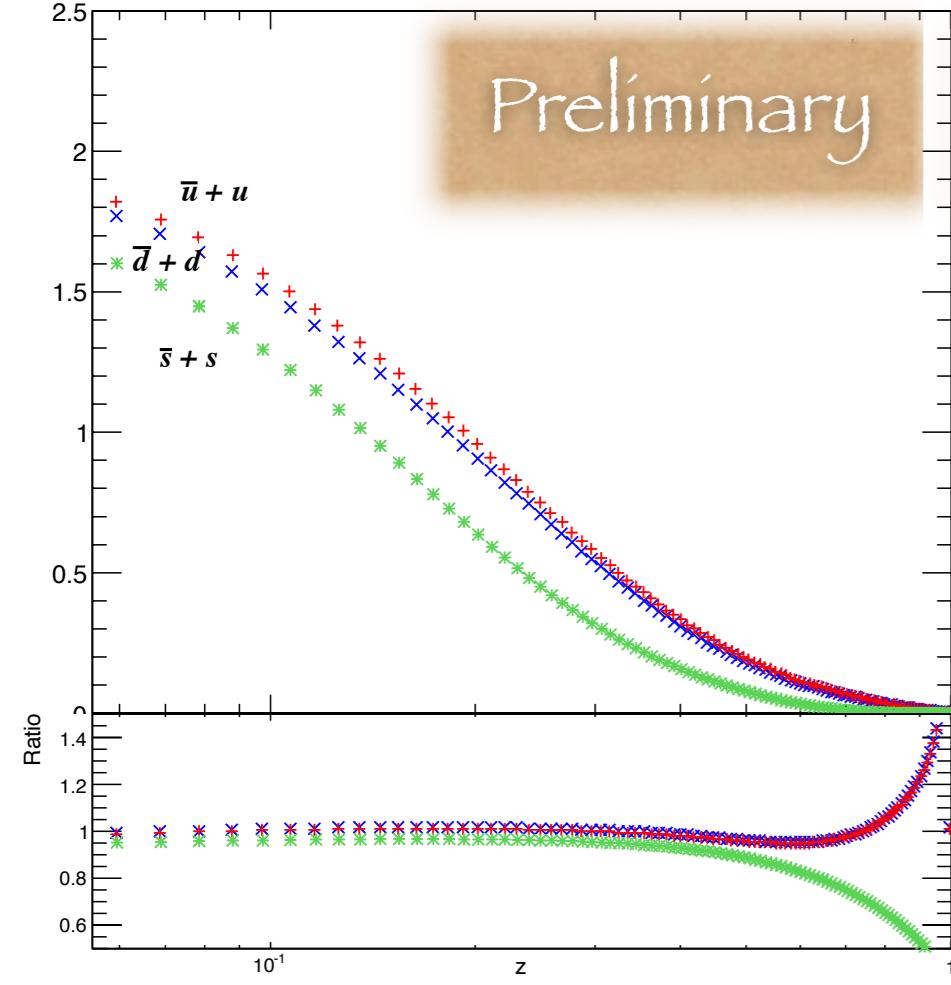


# Upgrade with COMPASS (1)



# Upgrade with COMPASS (2)





# Conclusions & Perspectives

- ◆ FFs are an important tool for describing observables within pQCD.
- ◆ NLO (LO) FFs can be extracted precisely only when global analyses are implemented.
- ◆ Charge/Flavor separation can be achieved when SIDIS and Hadron-Hadron collisions are considered in the global fit.
  
- ◆ Better understanding of Kaon FFs.
- ◆ Study of theoretical uncertainties with more data.

Thank you...