Improving dark matter direct detection analysis

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University of Nottingham

arXiv:1207.2039 with Anne M. Green

Speed dependence

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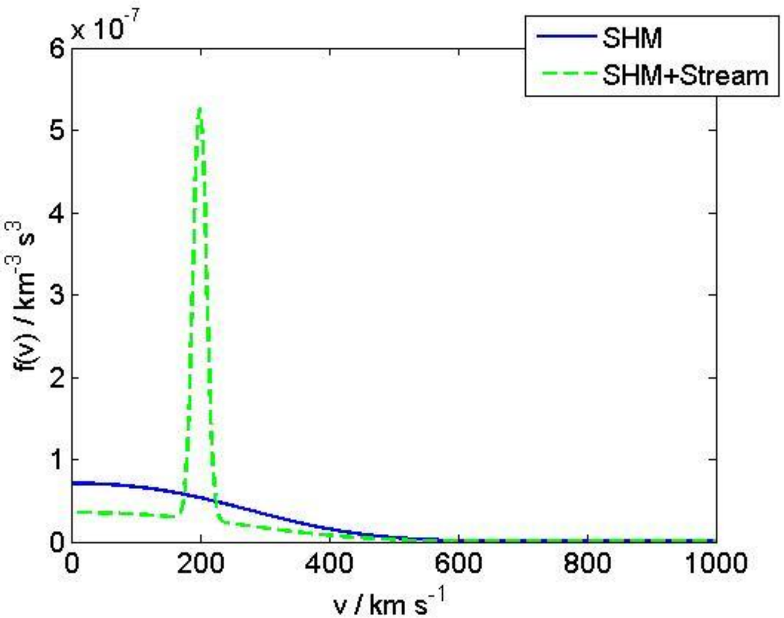

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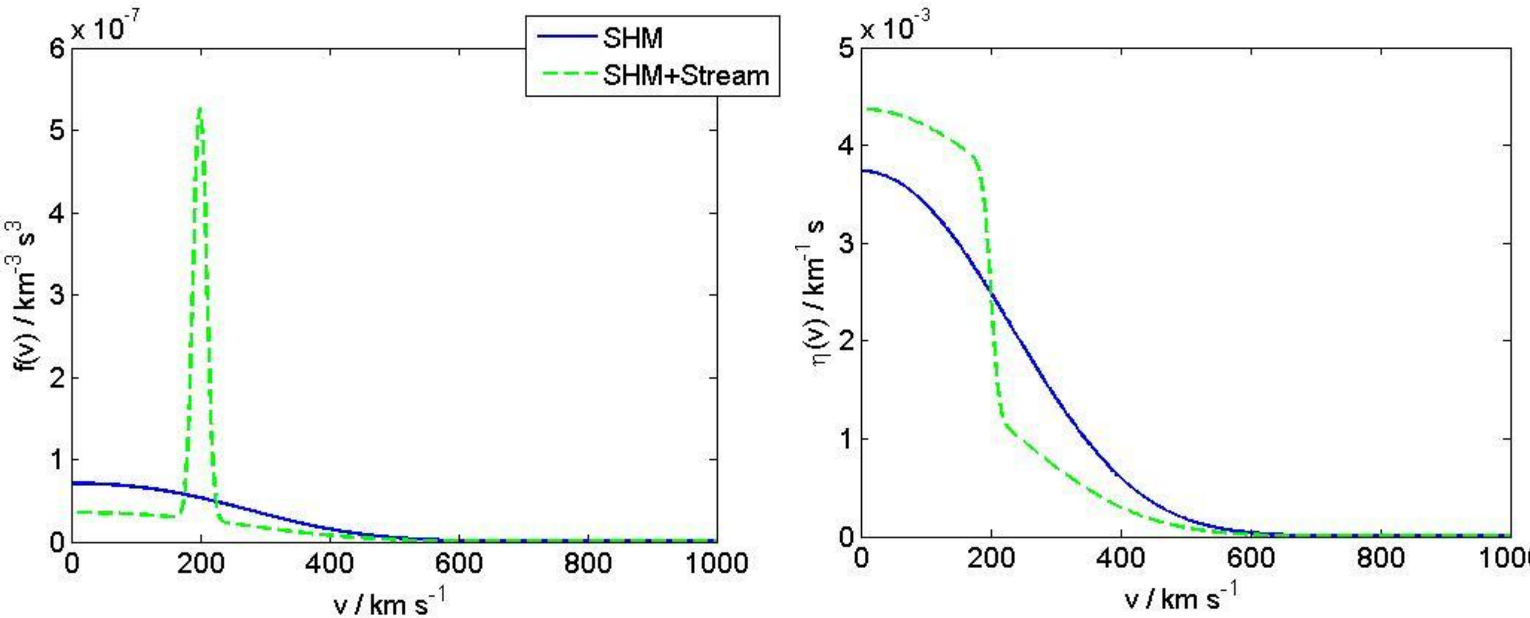

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Speed parametrisation method

A. H. G. Peter – arXiv:0910.4765, arXiv:1103.5145

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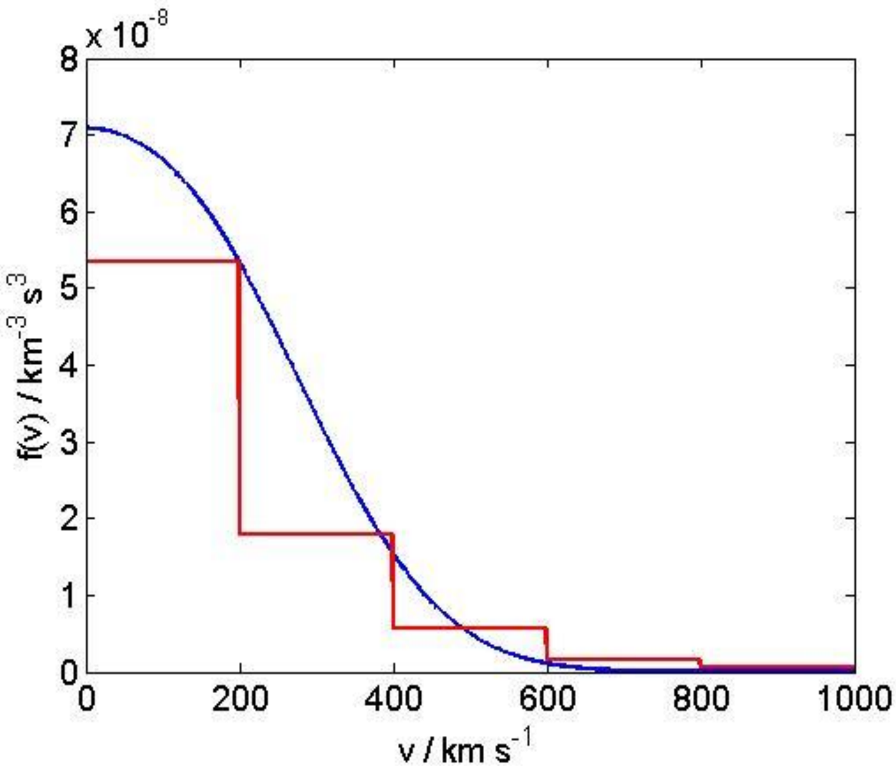

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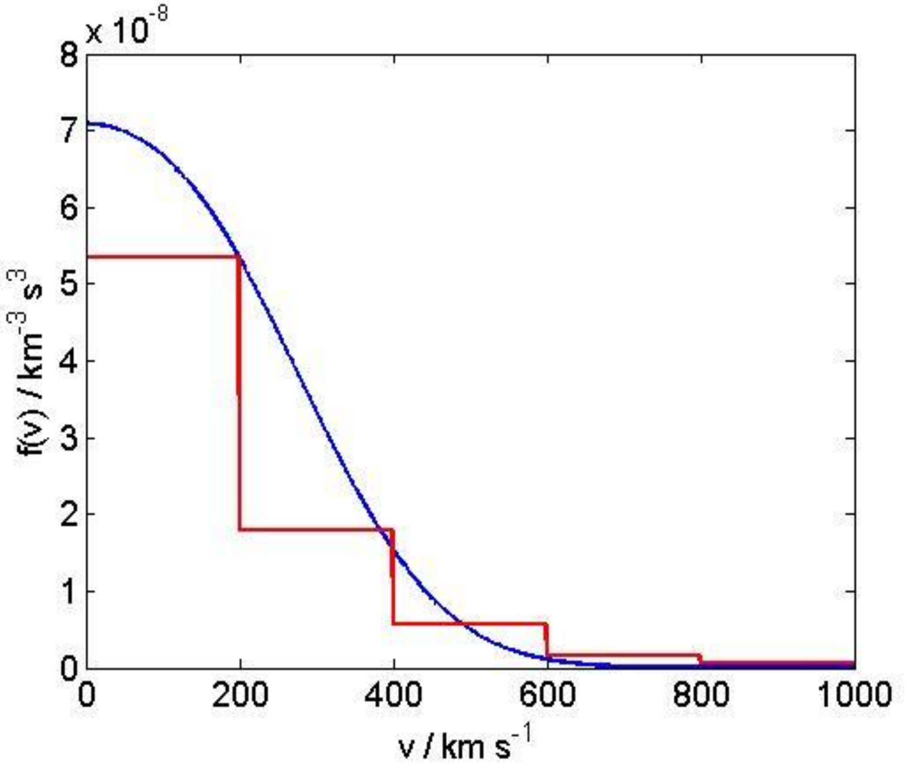

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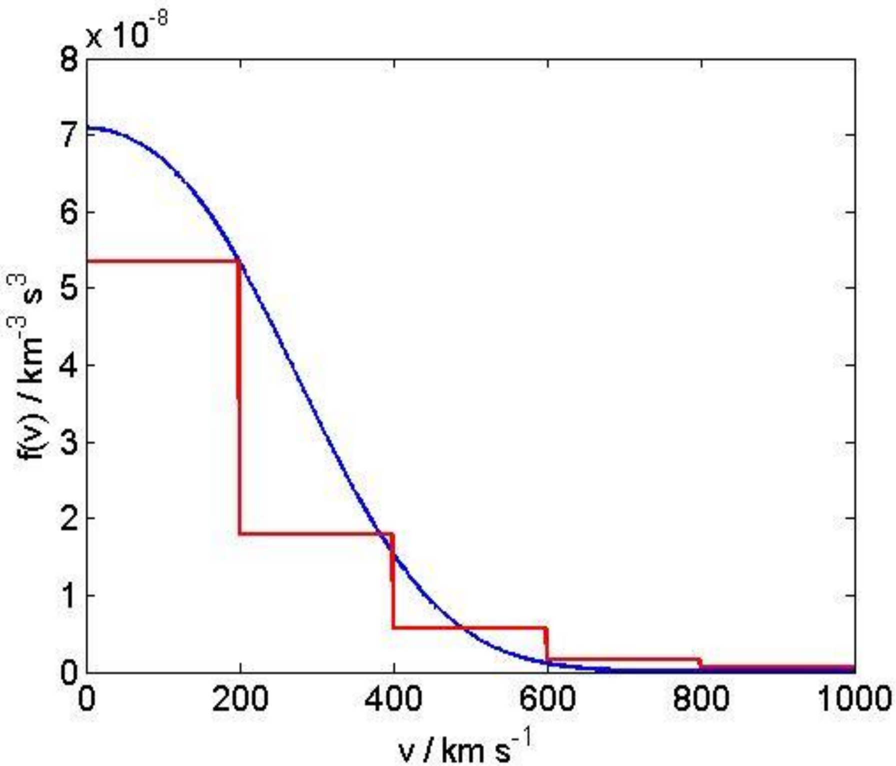

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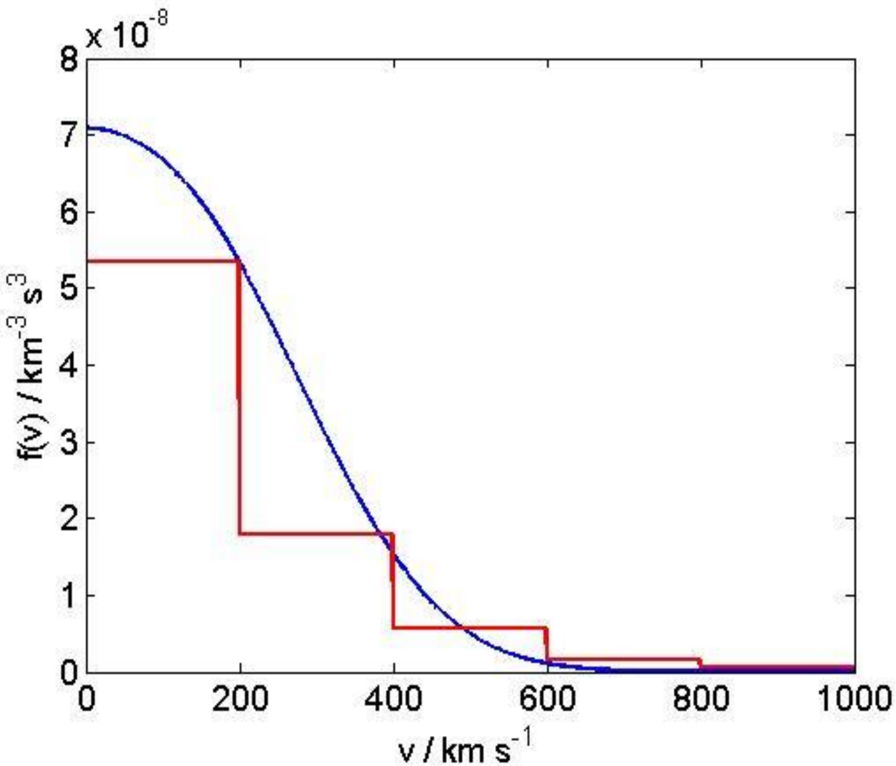

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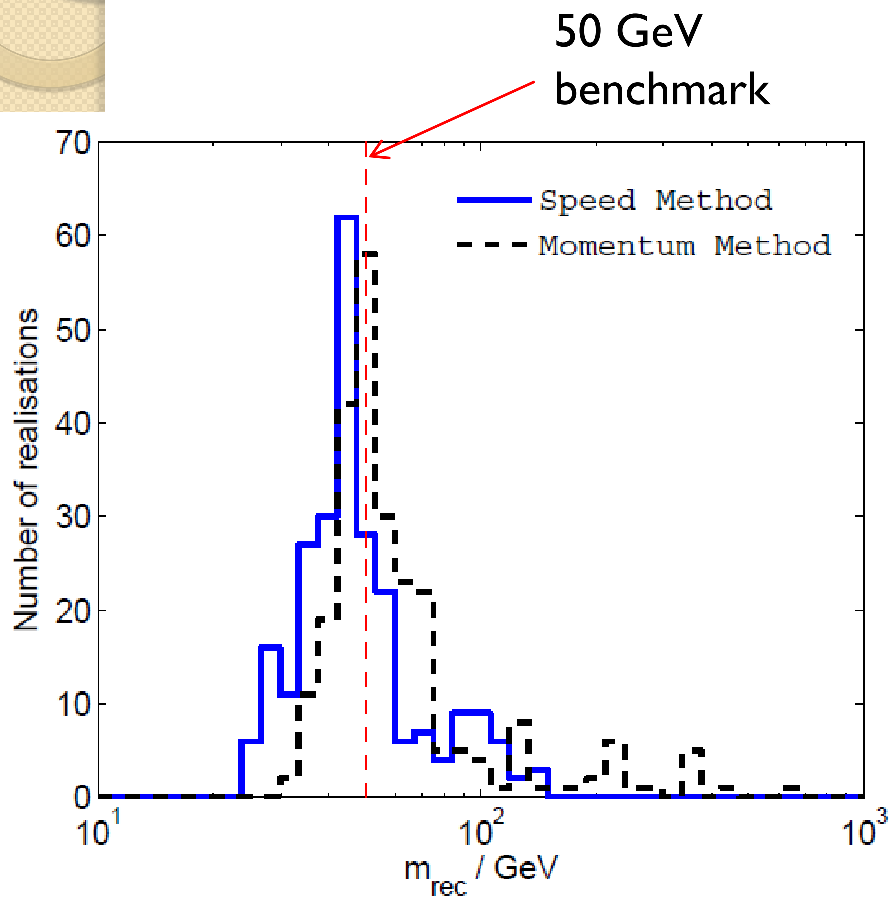

SHM

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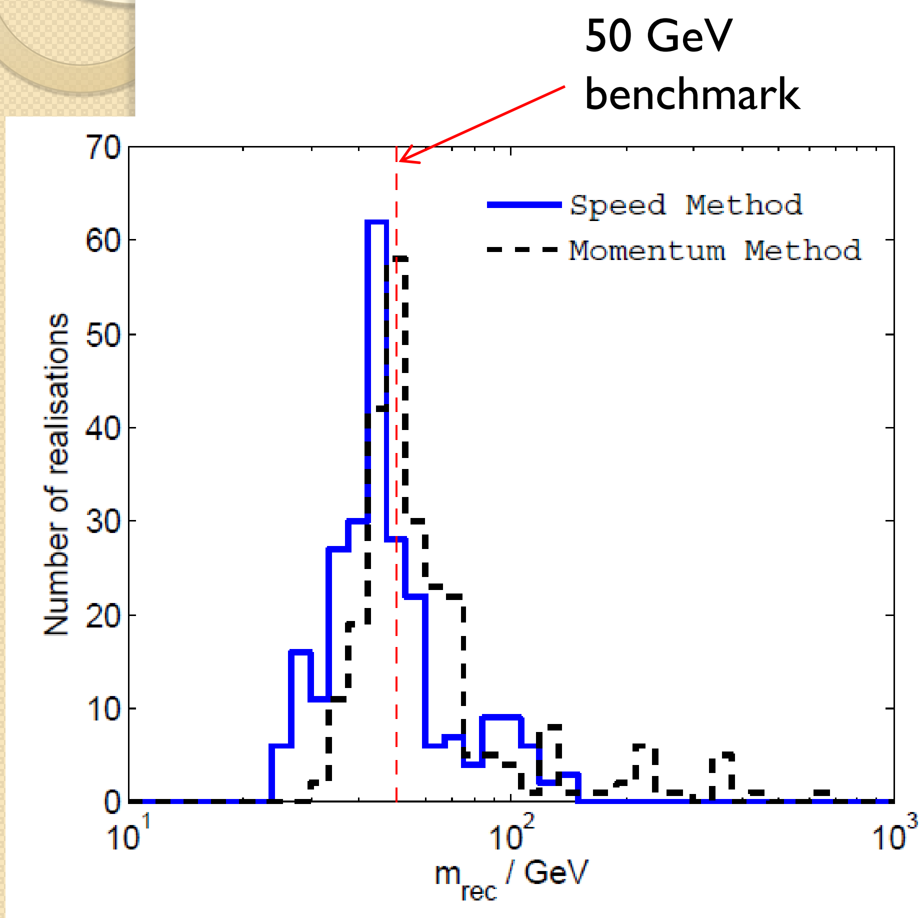

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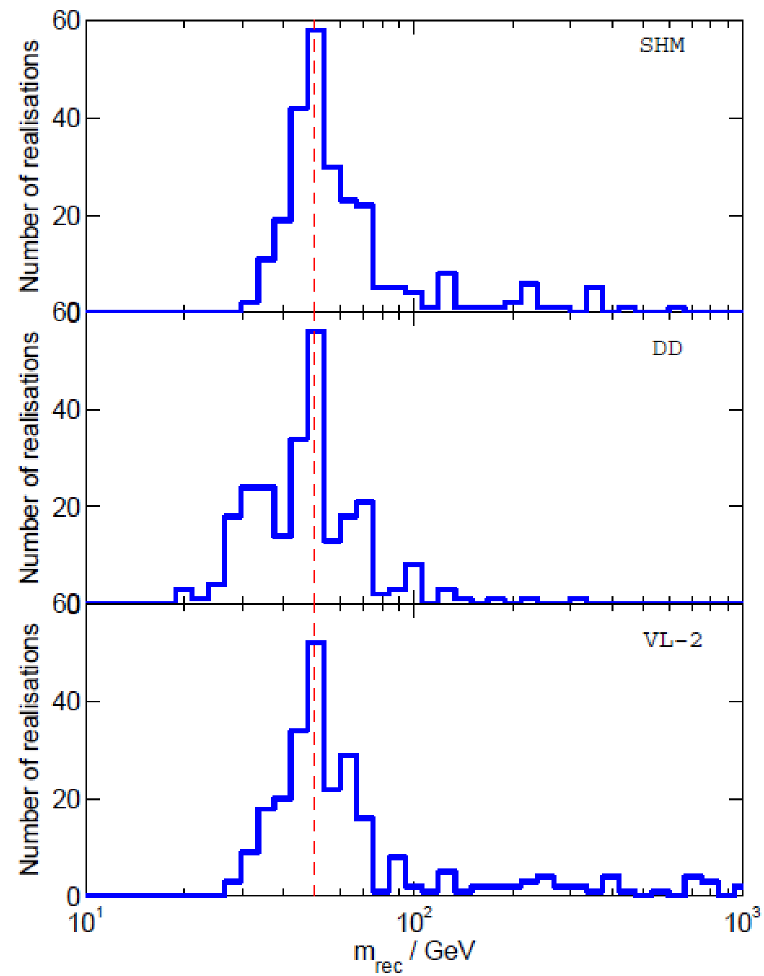

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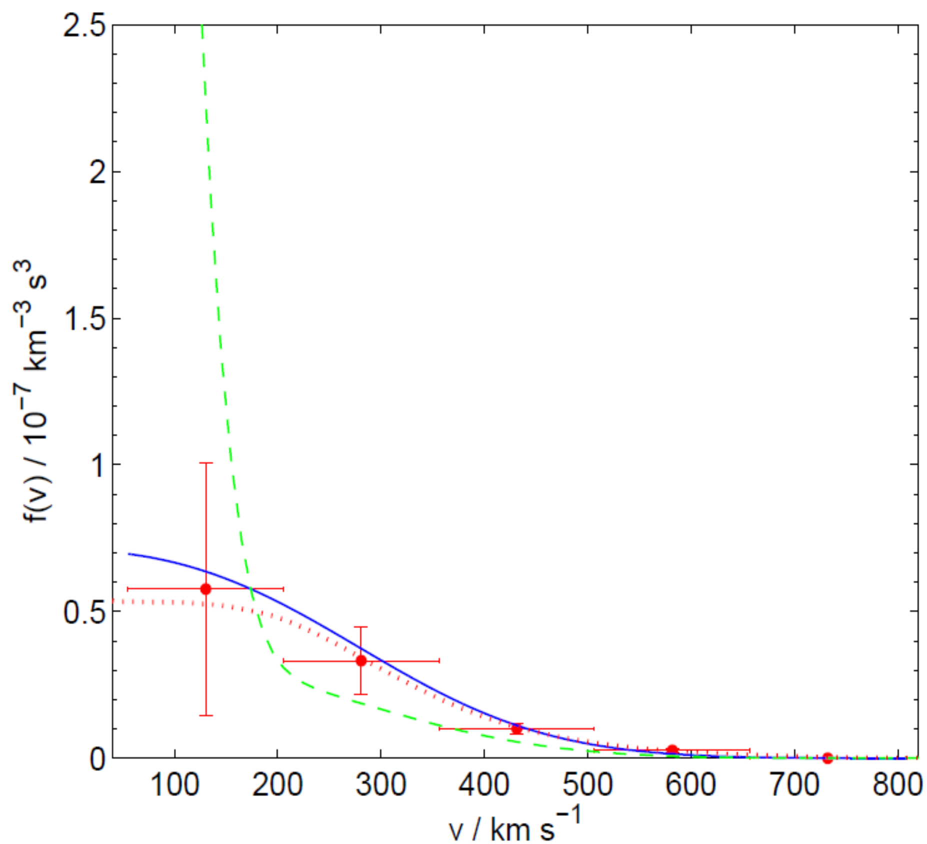

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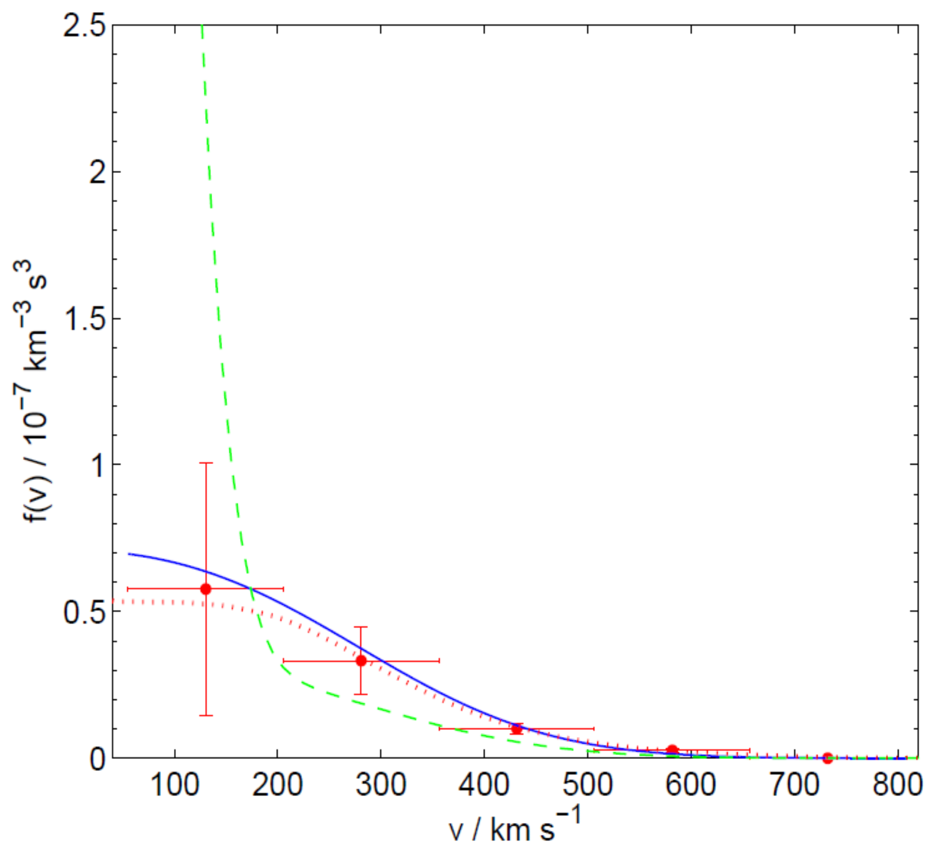
- Small statistics means discriminating between underlying f(v) is difficult



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- Future – extending to directional detectors which give full 3D information about f(**v**)

Thanks for listening