

CTEQ



# **CTEQ-TEA Update**

C.-P. Yuan

Michigan State University

In collaboration with

J. Gao, M. Guzzi, J. Huston, H.-L. Lai, Z. Li,  
Z. Liang, P. Nadolsky, J. Pumplin, D. Soper, D. Stump

September 26, 2012 @

PDF4LHC Meeting

# Outline

- Much has been said in Joey Huston's talk, such as benchmark studies.
- CT10 NNLO and CT12 BLO/NLO PDFs
- Some comparisons to data

# Two sets of CT NNLO error PDFs

## 1. CT10 NNLO eigenvector set

**Available at** [http://hep.pa.msu.edu/cteq/public/ct10\\_2012.html](http://hep.pa.msu.edu/cteq/public/ct10_2012.html); **is being submitted to LHAPDF; main focus of this talk**

Complements the CT10/CT10W NLO PDF sets (*Lai et al., PRD82, 074024 (2010)*)

- **Includes only “pre-LHC” CT10 data.** Can be used to predict LHC cross sections based on pre-LHC experimental inputs
- Same input parameters, functional forms for input PDFs as in the CT10 NLO PDFs
  - ▶  $\alpha_s(M_Z) = 0.118 \pm 0.002$ ,  $m_c^{pole} = 1.3$  GeV,  $m_b^{pole} = 4.75$  GeV
  - ▶ Simpler assumptions about the PDF flavor composition at  $\mu_0 = m_c^{pole} = 1.3$  GeV, e.g.,  $\bar{u}(x)/\bar{d}(x) \rightarrow 1$  as  $x \rightarrow 0$

# Two sets of CT NNLO error PDFs

## 2. CT12 NLO and NNLO eigenvector sets

### To be released within a few months

- Include LHC W and Z rapidity data, ATLAS and CMS jet data, HERA'2011  $F_L$  data
- Updated  $\alpha_s, m_c, m_b$  values
- Flexible  $\bar{d}/\bar{u}$  ratio at  $x \rightarrow 1$ , updated  $(s + \bar{s})/(\bar{u} + \bar{d})$  at  $x \lesssim 10^{-2}$ 
  - ▶ Constrained by the LHC  $W/Z$  rapidity distributions

## The CT10-NNLO global analysis of QCD

**Parametrization** of PDFs at  $Q = 1.3$  GeV, with 25 parameter values to be chosen; there are from 4 to 6 parameters for each parton type.

**Many data sets**, for short distance interactions.

**Perturbative QCD**, using NNLO approximations wherever available.

Taking account of **experimental errors**, statistical and systematic.

(Not so strong on systematic **theoretical errors**.)

Heavy flavor mass effects are included using the **S-ACOT- $\chi$**  factorization formalism (extended to NNLO).

28 data sets used for the CT10-NNLO global analysis

CT10-NNLO Table			Ndp	Chi <sup>2</sup>	Nsy	
1/	159	HERA1X0	579	617.	114	Combined HERA1 NC+CC DIS (2009)
2/	101	BcdF2pCor	339	392.	5	BCDMS collaboration
3/	102	BcdF2dCor	251	291.	5	BCDMS collaboration
4/	103	NmcF2pCor	201	333.	11	NMC collaboration
5/	104	NmcRatCor	123	151.	5	NMC collaboration
6/	108	cdhswf2	85	70.5	0	P Berge et al Z Phys C49 187 (1991)
7/	109	cdhswf3	96	77.9	0	P Berge et al Z Phys C49 187 (1991)
8/	110	ccfrf2.mi	69	67.8	5	Yang&Bodek model-independent
9/	111	ccfrf3.md	86	34.8	0	Shaevitz&Seligman model-dependent processed by SK
10/	201	e605	119	95.7	0	DY Q <sup>3</sup> dSig/dQ dy proton on heavy target
11/	203	e866f	15	9.7	0	E866 experiment: pd / 2pp
12/	225	cdfLasy	11	13.4		W production: decay lepton asymmetry CDF Run-1
13/	140	HN+67F2c	8	9.3	0	H1 neutral current charm
14/	143	HN+90X0c	10	16.3	8	H1 neutral current charm
15/	156	ZN+67F2c	18	13.4	0	ZEUS neutral current charm
16/	157	ZN+80F2c	27	16.7	0	ZEUS neutral current charm
17/	124	NuTvNuChXN	38	29.6	0	NuTev Neutrino Dimuon Reduced xSec
18/	125	NuTvNbChXN	33	28.4	0	NuTev Neutrino Dimuon Reduced xSec
19/	126	CcfrNuChXN	40	48.0	0	Ccfr Neutrino Dimuon Reduced xSec
20/	127	CcfrNbChXN	38	26.4	0	Ccfr Neutrino Dimuon Reduced xSec
21/	204	e866ppxf	184	234.	0	E866 experiment: DY pp: Q <sup>3</sup> dSig/dQ dx
22/	260	ZyD02a	28	15.6	6	Z rapidity dist. (D0 TeV II-a)
23/	261	ZyCDF2	29	46.5	6	Z rapidity dist. (CDF TeV II)
24/	227	cdfLasy2	11	11.4	0	W production: decay lepton asymmetry CDF Run-2
25/	231	d02Easy1	12	26.0	0	W production: decay elec asymmetry D0 Run-2 Pt>25
26/	234	d02Masy1	9	14.8	0	W production: decay muon asymmetry D0 Run-2 Pt>20
27/	504	cdf2jtCor2	72	101.	24	(run II: cor.err; ptmin & ptmax)
28/	514	d02jtCor2	110	114.	23	(run II: cor.err; ptmin & ptmax)

# CT10 NNLO PDFs

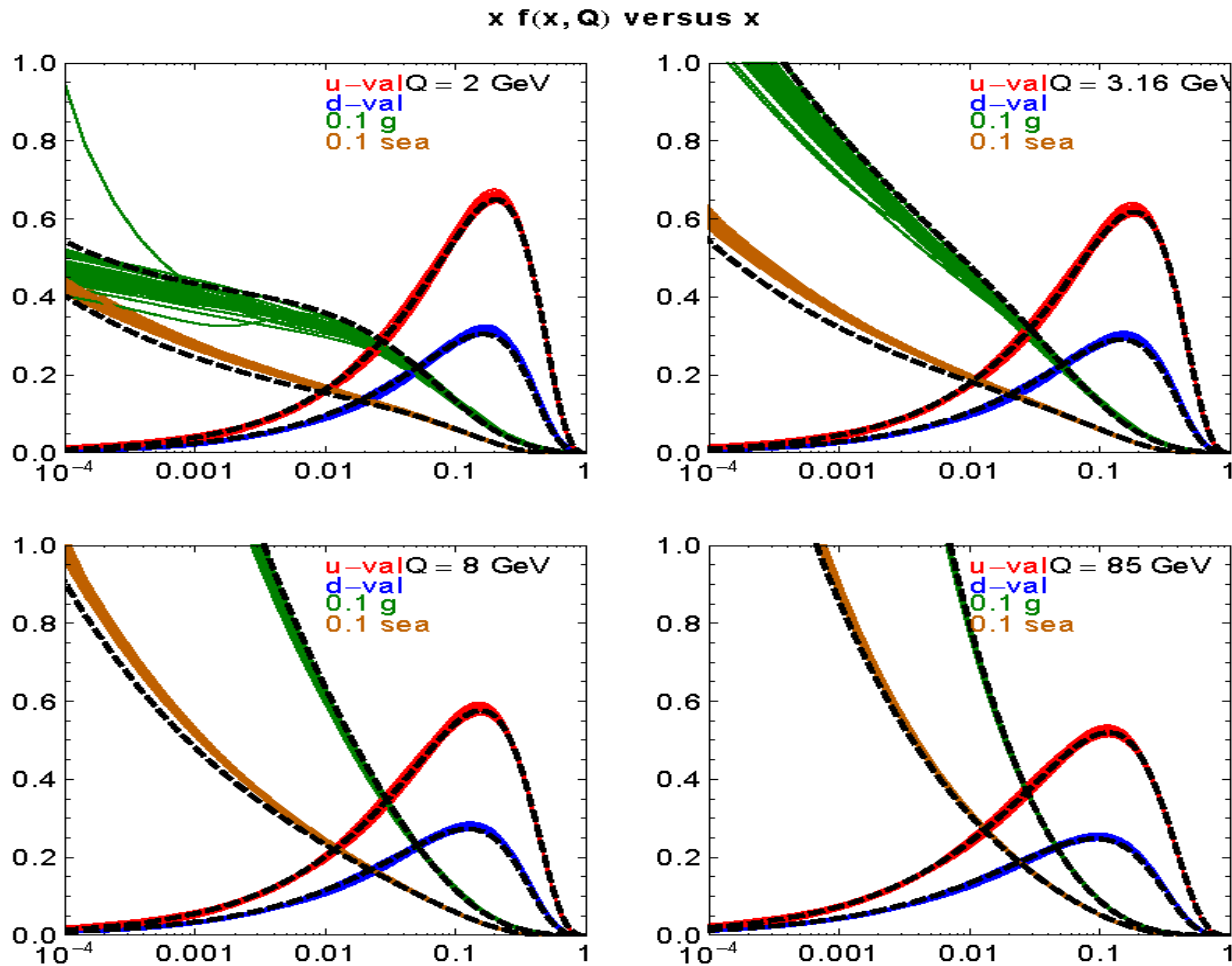
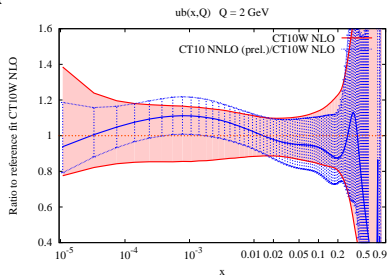
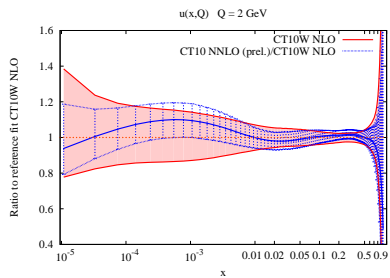
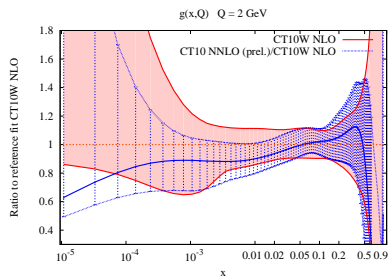


Figure 3: CT10-NNLO parton distribution functions. These figures show the *alternate fits* for the CT10-NNLO analysis. Each graph shows  $x u_{\text{valence}} = x(u - \bar{u})$ ,  $x d_{\text{valence}} = x(d - \bar{d})$ ,  $0.10 x g$  and  $0.10 x \bar{q}_{\text{sea}}$  as functions of  $x$  for a fixed value of  $Q$ . The values of  $Q$  are 2, 3.16, 8, 85 GeV. Sea =  $2(\bar{d} + \bar{u} + \bar{s})$ . The dashed curves are the central NLO fit, CT10.

# CT10 NNLO error PDFs (compared to CT10W NLO)





## Experimental “Errors” (or, Uncertainties)

An experiment publishes N measurements,

$$\{M_i ; i = 1, 2, 3, \dots, N\}.$$

Each measurement has several parts,

$$M_i = \{D_i ; \sigma_{0i} ; \{\sigma_{1i}, \sigma_{2i}, \sigma_{3i}, \dots\}\}$$

= {central value; SD of statistical error; SDs of correlated systematic errors};

that is,

$$D_i = True_i + \sigma_{0i} r_{0i} + \sum_{k=1}^{N_{sy}} \sigma_{ki} r_k$$

...where  $r_{0i}$  and  $\{r_k\}$  are random variables (gaussian?)

Define 
$$\chi^2 = \sum_i (D_i - \sum_k \sigma_{ki} r_k - T_i)^2 / \sigma_{0i}^2 + \sum_k r_k^2$$

...and minimize with respect to both the normalized systematic shifts  $\{r_k\}$  and the theory parameters.

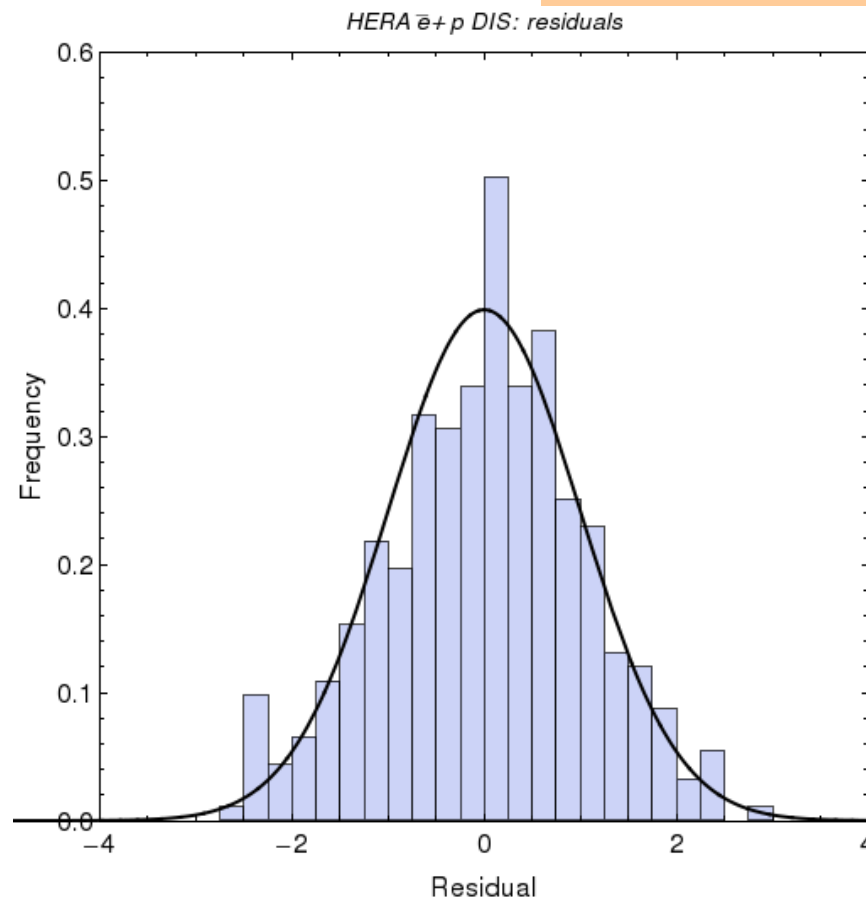
## “Histogram of Residuals”

We define the *residual* by

$$\text{Residual}_i = \frac{sD_i - T_i}{\sigma_{0i}}$$

( $i = 1, 2, 3, \dots, NDP$ )

For good agreement between data and theory, the residuals should have a Gaussian distribution with mean = 0 and standard deviation = 1.



Theory = CT10-NNLO, i.e., ***the central fit***;  
 sData = Data **MINUS** the optimized systematic errors;  
 Black curve = ideal Gaussian distribution

# HERA Combined Data: $e^\pm p$ deep inelastic scattering

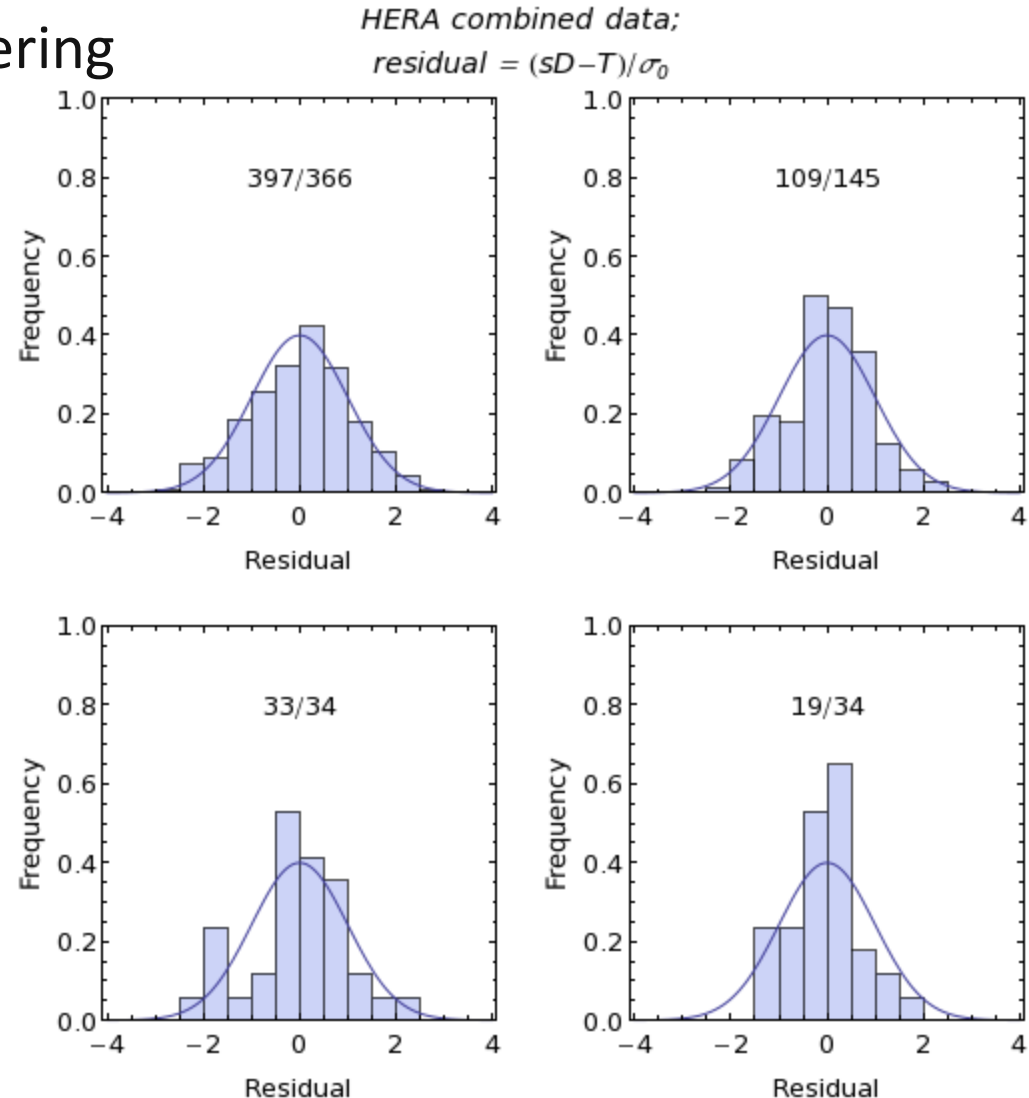
$e^+ p$  , NC DIS  
 $\chi^2 / N = 397/366$

$e^- p$  , NC DIS  
 $\chi^2 / N = 109/145$

$e^+ p$  , CC DIS  
 $\chi^2 / N = 33/34$

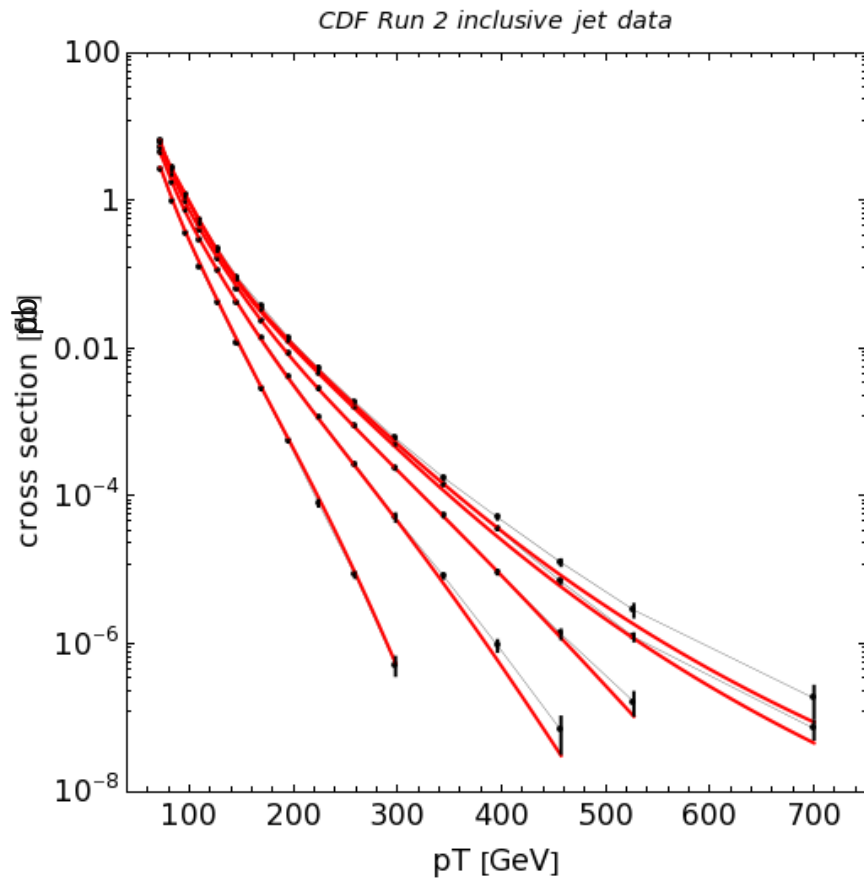
$e^- p$  , CC DIS  
 $\chi^2 / N = 19/34$

The CT10-NNLO central fit

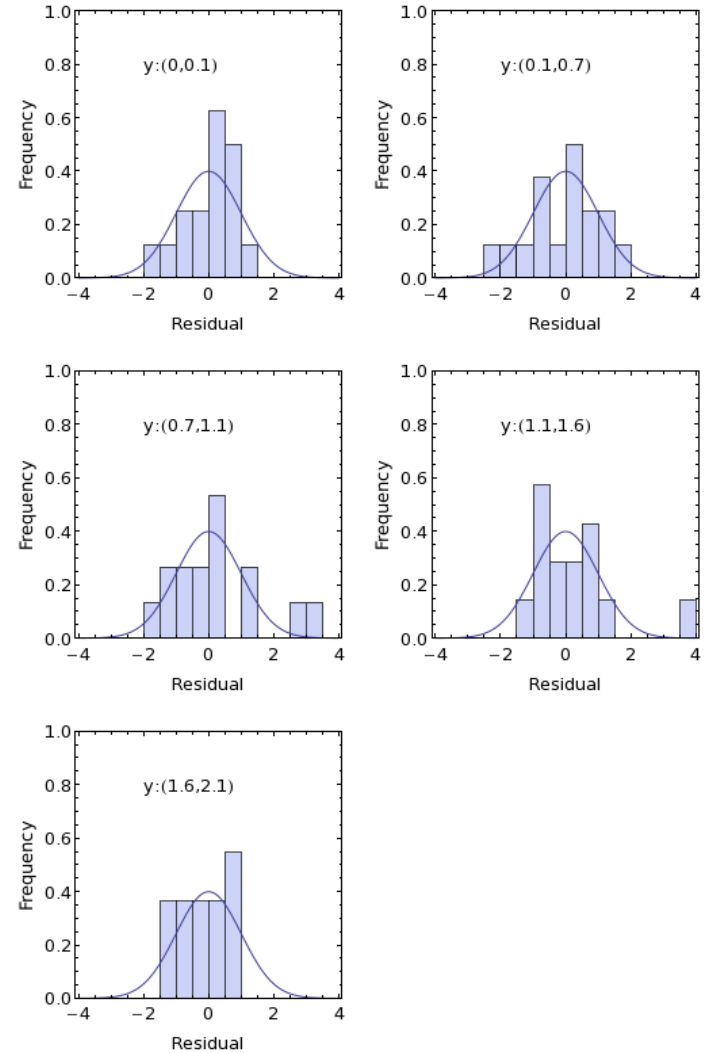


$(N_{dp}, N_{sy}) = (579, 114)$

# Inclusive Jet Production in Run 2 at the Tevatron Collider - CDF

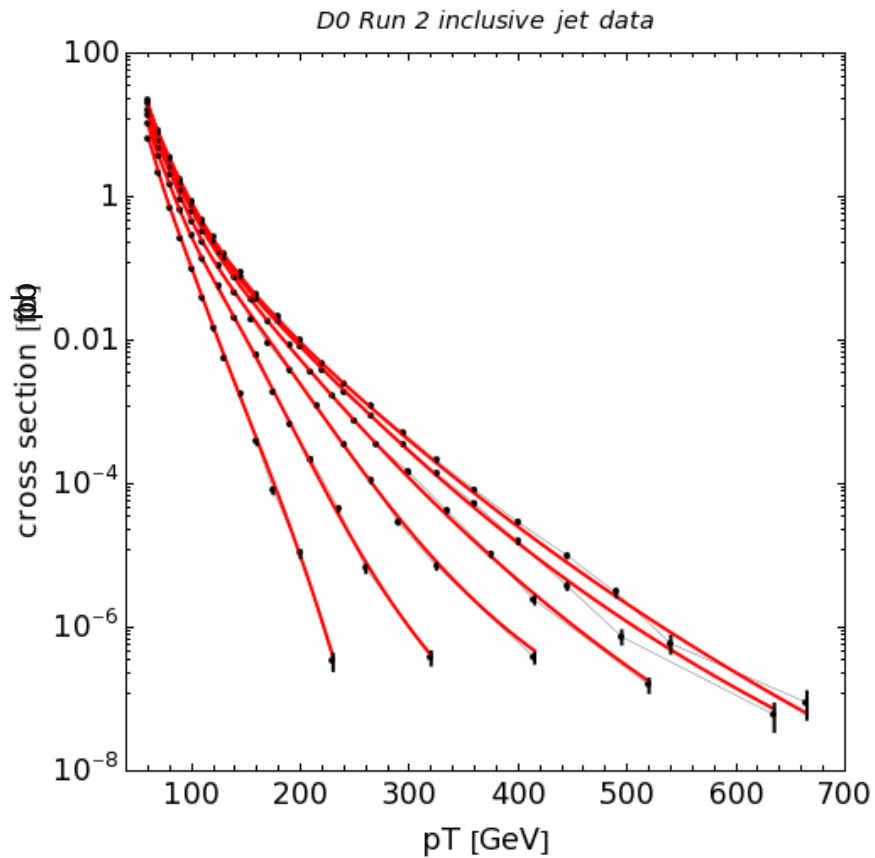


The red curves are the theoretical calculations with CT10-NNLO PDFs, i.e., **the central fit**.

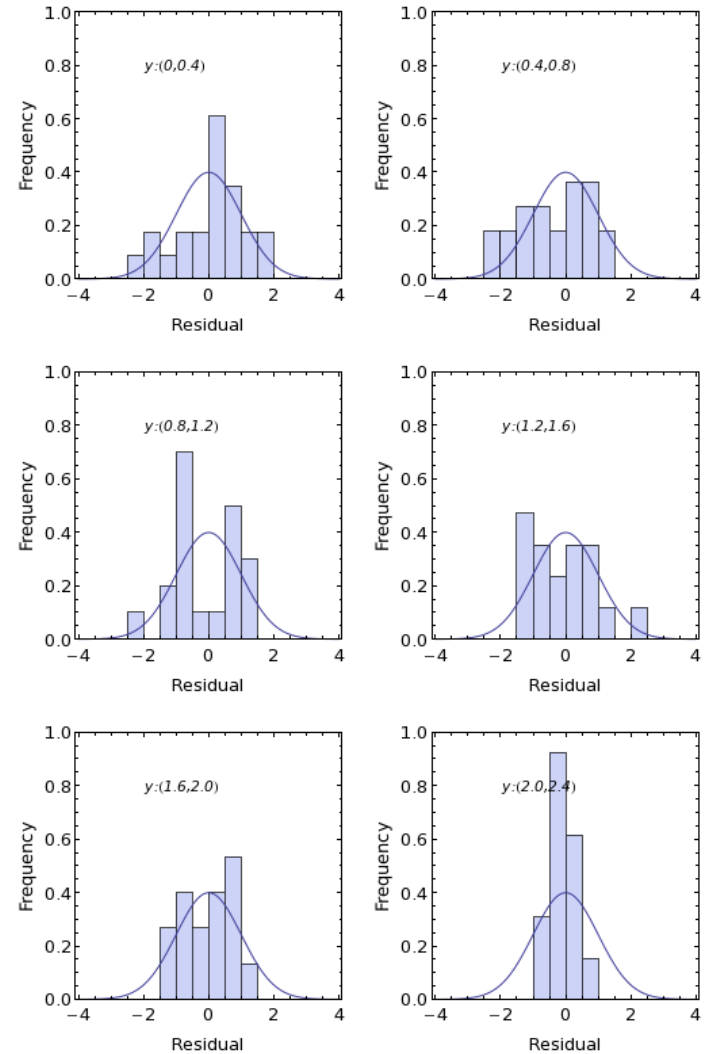


$$(N_{dp}, N_{sy}) = (72, 25)$$

# Inclusive Jet Production in Run 2 at the Tevatron Collider – D0

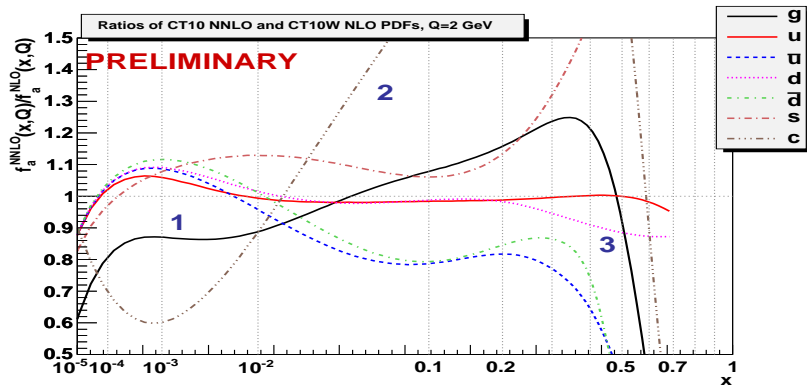


The red curves are the theoretical calculations with CT10-NNLO PDFs, i.e., **the central fit**.



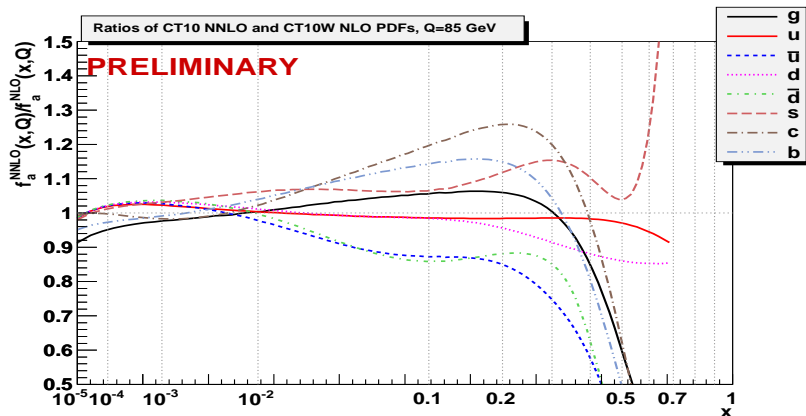
$$(N_{dp}, N_{sy}) = (110; 23)$$

## CT10 NNLO central PDFs, as ratios to NLO, $Q=2$ GeV



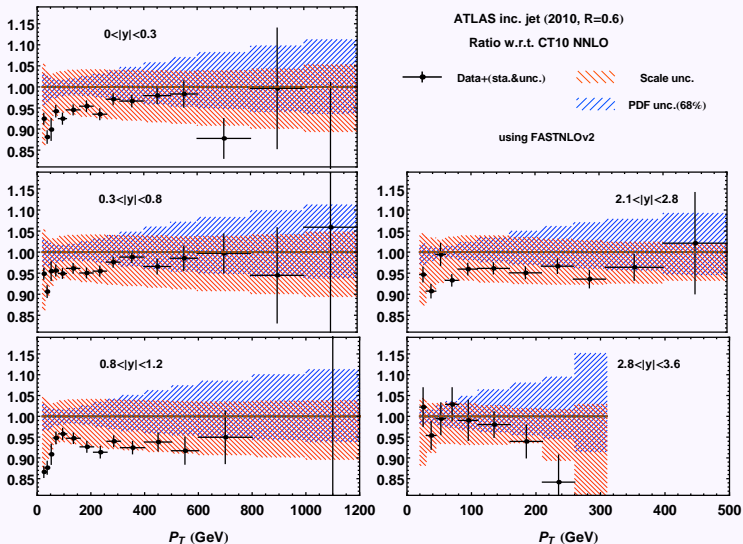
1. At  $x < 10^{-2}$ ,  $\mathcal{O}(\alpha_s^2)$  evolution suppresses  $g(x, Q)$ , increases  $q(x, Q)$
2.  $c(x, Q)$  and  $b(x, Q)$  change as a result of the  $\mathcal{O}(\alpha_s^2)$  GM VFN scheme
3. In large  $x$  region,  $g(x, Q)$  and  $d(x, Q)$  are reduced by not including Run-1 inclusive jet data, revised EW couplings, alternative treatment of correlated systematic errors, scale choices.

## CT10 NNLO central PDFs, as ratios to NLO, $Q=85$ GeV



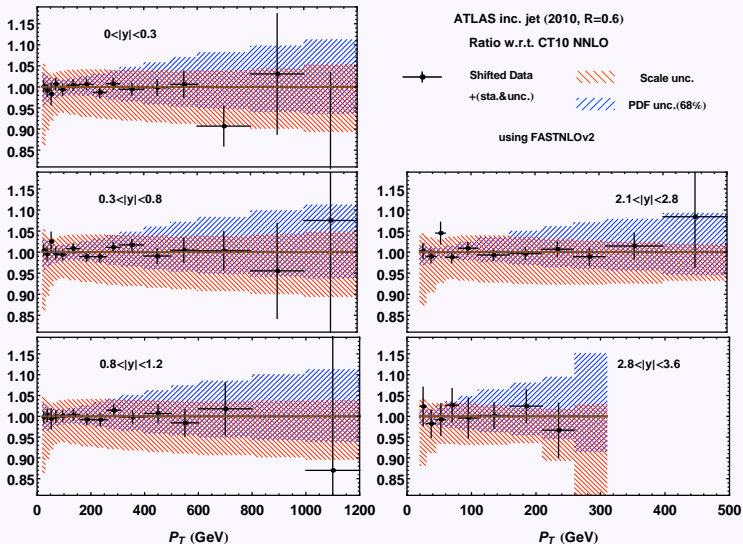
At  $x > 0.1$ ,  $d(x, Q)$ ,  $\bar{u}(x, Q)$  and  $\bar{d}(x, Q)$  are reduced.  
 $g(x, Q)$  is also reduced in large  $x$  region.

# Comparison of CT10 predictions with unshifted ATLAS jet data:



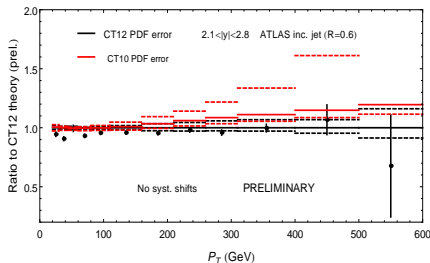
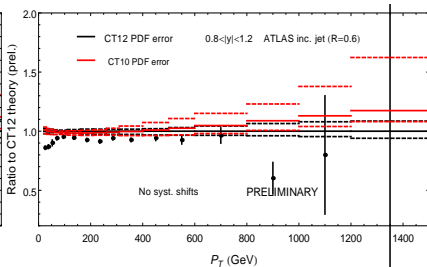
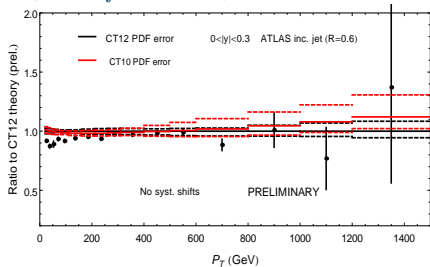


■ Comparison of CT10 predictions with shifted ATLAS jet data:



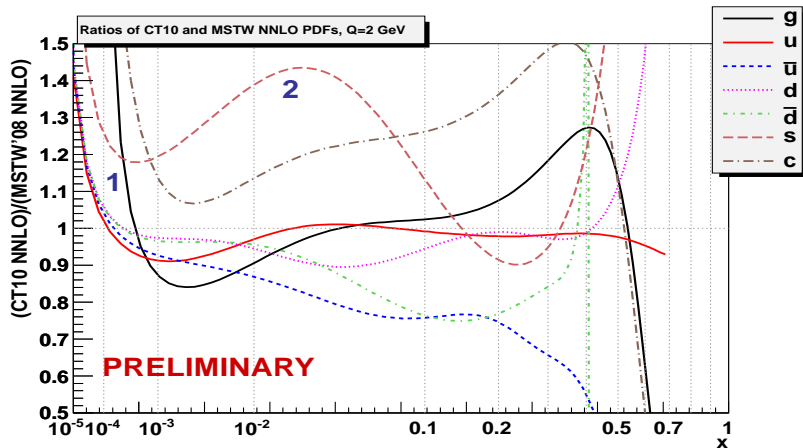
# CT12 NLO predictions for LHC jet production

ATLAS single-inclusive jet production (*arXiv:1112.6297*); FastNLO 2;  $R=0.6$ ;  
 $\chi^2/N_{d.o.f} = 0.72 (0.98)$  for CT12 NLO (CT10 NLO)



CT10 NNLO and CT12 PDFs (black lines) predict smaller jet cross sections at large  $p_T$ , as a result of reduced  $g(x, Q)$  in large  $x$  region.

# CT10 NNLO PDFs compared to MSTW NNLO

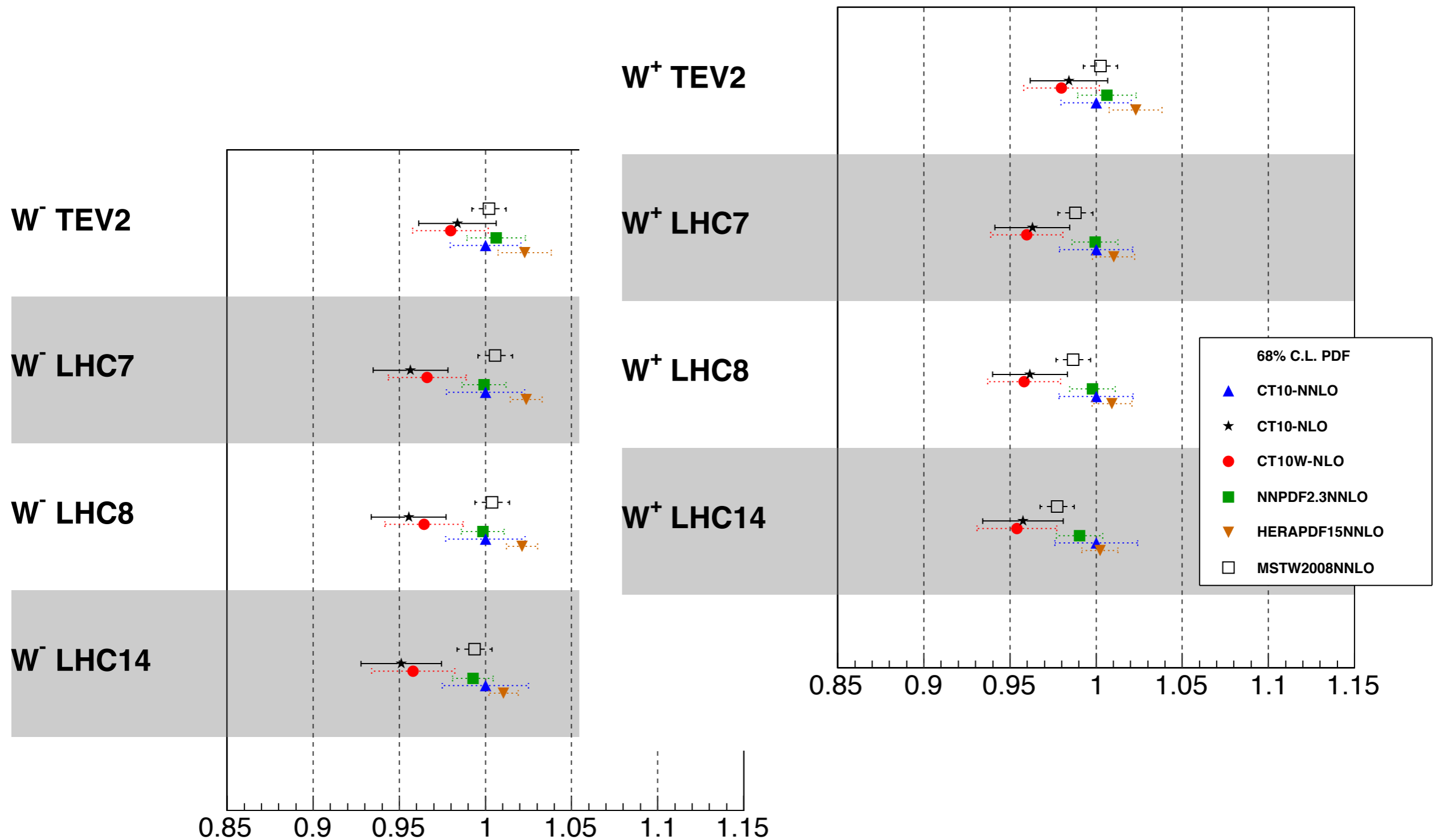


1. CT10 gluon and quarks are harder at  $x \rightarrow 0$ ;

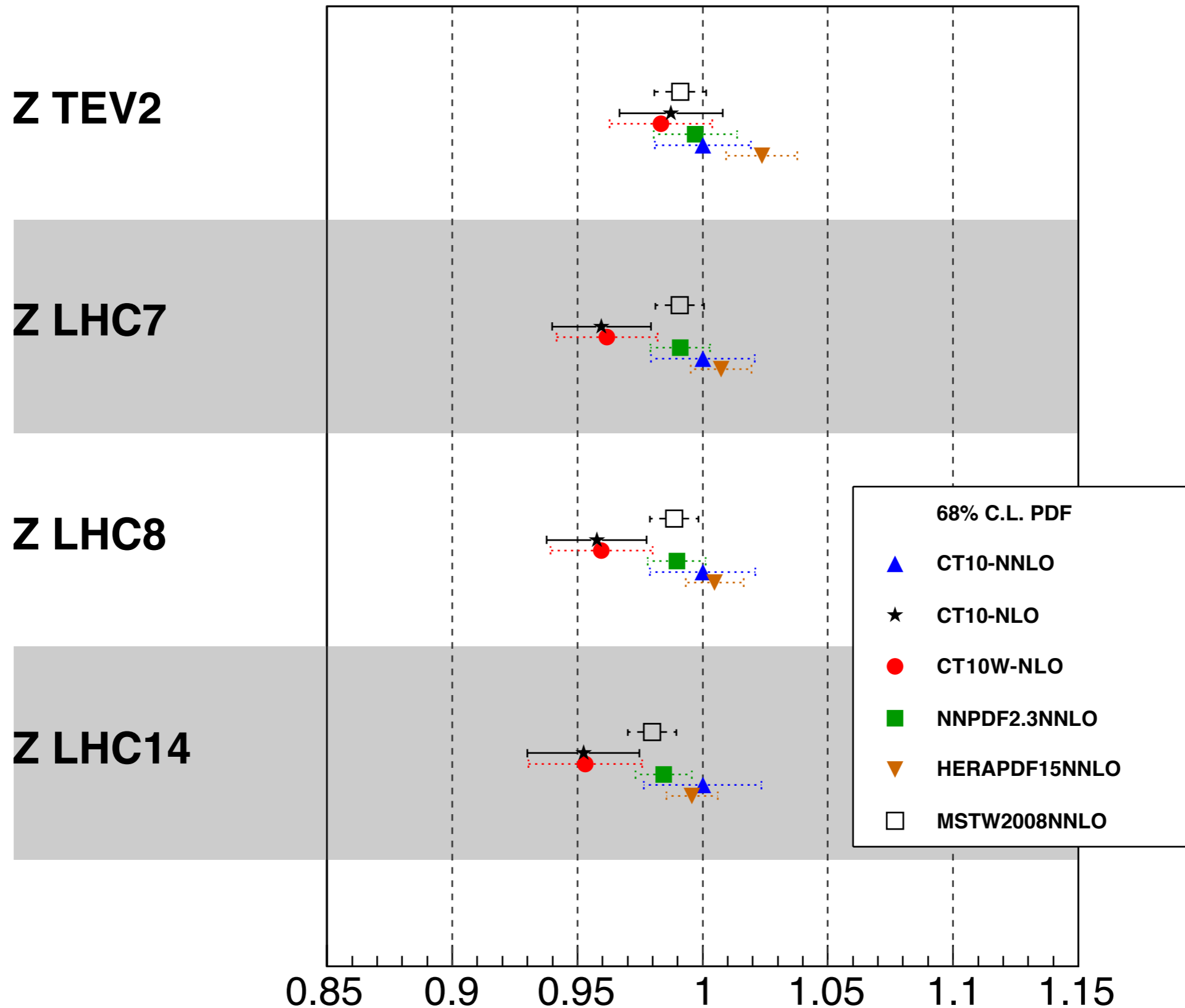
$$g(x, Q_0) > 0 \text{ at } 10^{-5} \leq x \leq 1$$

2. The CT10 strange PDF is larger at  $x \sim 10^{-3}$

# CT10-NNLO compared with other PDFs for W boson production (NNLO)



# CT10-NNLO compared with other PDFs for Z boson production (NNLO)



# CT10-NNLO compared with other PDFs

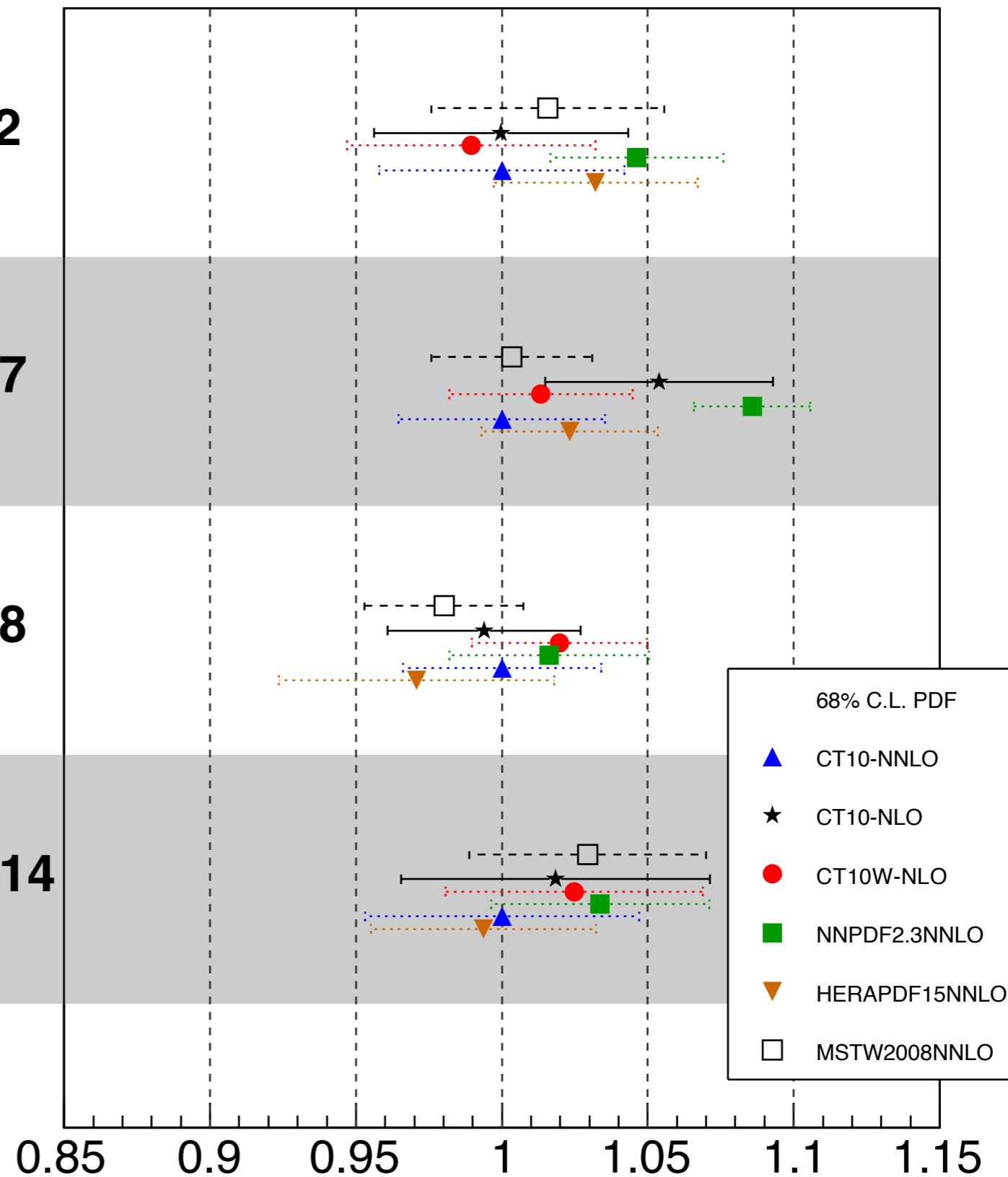
Use  
HNNLO1.3

$gg \rightarrow H^0$  TEV2

$gg \rightarrow H^0$  LHC7

$gg \rightarrow H^0$  LHC8

$gg \rightarrow H^0$  LHC14



# NNLO cross section and PDF induced uncertainty for $gg \rightarrow H$ (using ResBos2 program)

$$\Delta\sigma_{\text{PDF}} = \frac{1}{2} \sqrt{\sum_{i=1}^d \left( \sigma_i^{(+)} - \sigma_i^{(-)} \right)^2}.$$

arXiv:1205.4311 [hep-ph]

$M=125$  GeV

	CTEQ6.6	CT10 NLO	CT10W NLO	CT10 NNLO	MSTW2008NNLO	NNPDF2.3NNLO
Tevatron	$0.77 \pm 6.9\%$	$0.77 \pm 6.9\%$	$0.76 \pm 7.0\%$	$0.77 \pm 6.9\%$	$0.78 \pm 6.4\%$	$0.80 \pm 4.6\%$
LHC 7 TeV	$12.80 \pm 6.1\%$	$13.33 \pm 6.1\%$	$12.82 \pm 5.1\%$	$12.65 \pm 5.8\%$	$12.69 \pm 4.5\%$	$13.73 \pm 3.0\%$
LHC 8 TeV	$16.31 \pm 5.5\%$	$16.53 \pm 5.5\%$	$16.95 \pm 4.8\%$	$16.63 \pm 5.6\%$	$16.30 \pm 4.5\%$	$16.90 \pm 5.5\%$
LHC 14 TeV	$42.39 \pm 8.5\%$	$42.64 \pm 8.5\%$	$42.91 \pm 7.1\%$	$41.87 \pm 7.7\%$	$43.10 \pm 6.4\%$	$43.28 \pm 5.9\%$

TABLE II: The total cross sections (in pb) for Higgs boson production via  $g + g \rightarrow H + X$  at the Tevatron (1.96 TeV) and LHC (7 TeV, 8 TeV and 14 TeV) by using different PDF sets in ResBos2. The PDF induced uncertainties are estimated at 90% confidence-level, and expressed in the form of percentages.

# Uncertainties of cross sections for $gg \rightarrow H$ (using ResBos2 program)

$$\Delta\sigma_{\alpha_s} = \frac{1}{2} \sqrt{[\sigma_0(A_{-2}) - \sigma_0(A_2)]^2}.$$

(at 90% CL, with the range of 0.116 to 0.120)

$$(\Delta\sigma)^2 = (\Delta\sigma_{\text{PDF}})^2 + (\Delta\sigma_{\alpha_s})^2.$$

M=125 GeV

CT10-NNLO	$\sigma_0$	$\Delta\sigma_{\text{PDF}}$	$\Delta\sigma_{\alpha_s}$	$\Delta\sigma = \sqrt{(\Delta\sigma_{\text{PDF}})^2 + (\Delta\sigma_{\alpha_s})^2}$
Tevatron	0.77	$\pm 6.9\%$	$\pm 1.8\%$	$\pm 7.1\%$
LHC 7 TeV	12.65	$\pm 5.8\%$	$\pm 2.5\%$	$\pm 6.3\%$
LHC 8 TeV	16.63	$\pm 5.6\%$	$\pm 3.5\%$	$\pm 6.6\%$
LHC 14 TeV	41.87	$\pm 7.7\%$	$\pm 5.3\%$	$\pm 9.3\%$



# Total NNLO cross section for $gg \rightarrow H$ (comparing various codes)

	$m_H$ (GeV)	ResBos2	ResBos	HNNLO (NNLO)	HqT2 (NNLL+NLO)
Tevatron	115	$0.98^{+9.2\%}_{-6.1\%}$	$0.91^{+15.7\%}_{-6.9\%}$	$0.96^{+13.6\%}_{-13.7\%}$	$0.97^{+14.2\%}_{-13.8\%}$
	120	$0.87^{+9.2\%}_{-6.9\%}$	$0.80^{+15.8\%}_{-6.6\%}$	$0.84^{+13.4\%}_{-13.7\%}$	$0.85^{+13.9\%}_{-13.8\%}$
	125	$0.77^{+9.1\%}_{-6.5\%}$	$0.71^{+15.9\%}_{-6.5\%}$	$0.75^{+13.5\%}_{-14.2\%}$	$0.75^{+13.8\%}_{-13.8\%}$
	130	$0.68^{+10.3\%}_{-5.9\%}$	$0.63^{+15.9\%}_{-6.4\%}$	$0.66^{+14.5\%}_{-13.1\%}$	$0.67^{+13.9\%}_{-13.8\%}$
LHC 7 TeV	115	$15.11^{+7.8\%}_{-5.8\%}$	$14.21^{+8.3\%}_{-5.9\%}$	$15.16^{+9.0\%}_{-10.7\%}$	$15.19^{+10.8\%}_{-10.4\%}$
	120	$13.89^{+7.8\%}_{-5.7\%}$	$13.06^{+8.4\%}_{-5.8\%}$	$13.80^{+10.6\%}_{-10.5\%}$	$13.94^{+10.2\%}_{-10.4\%}$
	125	$12.80^{+7.7\%}_{-5.5\%}$	$12.03^{+8.5\%}_{-5.6\%}$	$12.72^{+10.2\%}_{-10.6\%}$	$12.83^{+10.7\%}_{-10.4\%}$
	130	$11.83^{+7.7\%}_{-5.4\%}$	$11.12^{+8.6\%}_{-5.5\%}$	$11.75^{+10.8\%}_{-10.7\%}$	$11.84^{+9.9\%}_{-10.4\%}$
LHC 8 TeV	115	$19.15^{+7.5\%}_{-6.5\%}$	$17.58^{+8.1\%}_{-7.1\%}$	$19.05^{+9.9\%}_{-9.2\%}$	$19.25^{+10.8\%}_{-9.8\%}$
	120	$17.65^{+7.5\%}_{-6.5\%}$	$16.21^{+8.1\%}_{-7.1\%}$	$17.59^{+9.7\%}_{-9.9\%}$	$17.76^{+9.8\%}_{-10.1\%}$
	125	$16.31^{+7.5\%}_{-6.4\%}$	$14.98^{+8.1\%}_{-7.0\%}$	$16.26^{+10.2\%}_{-10.4\%}$	$16.39^{+9.8\%}_{-10.1\%}$
	130	$15.11^{+7.5\%}_{-6.4\%}$	$13.89^{+8.1\%}_{-7.0\%}$	$15.07^{+10.9\%}_{-10.6\%}$	$15.17^{+10.3\%}_{-10.1\%}$
LHC 14 TeV	115	$48.84^{+7.6\%}_{-5.7\%}$	$46.03^{+10.0\%}_{-5.3\%}$	$49.24^{+9.4\%}_{-9.8\%}$	$48.90^{+9.0\%}_{-9.8\%}$
	120	$45.45^{+7.5\%}_{-5.5\%}$	$42.84^{+9.8\%}_{-5.2\%}$	$45.57^{+10.4\%}_{-9.5\%}$	$45.52^{+10.3\%}_{-8.4\%}$
	125	$42.39^{+7.4\%}_{-5.4\%}$	$39.96^{+9.6\%}_{-5.0\%}$	$42.61^{+9.6\%}_{-9.7\%}$	$42.57^{+9.7\%}_{-8.8\%}$
	130	$39.65^{+7.3\%}_{-5.2\%}$	$37.38^{+9.4\%}_{-4.8\%}$	$39.93^{+11.1\%}_{-9.8\%}$	$39.75^{+9.7\%}_{-8.9\%}$

TABLE I: The ResBos2, ResBos, HNNLO and HqT2 predictions on the total cross sections (in pb) for Higgs boson production via  $g+g \rightarrow H+X$  at the Tevatron (1.96 TeV) and LHC (7 TeV, 8 TeV and 14 TeV). The upper (lower) uncertainties, expressed in the form of percentages, are obtained by dividing (multiplying) the canonical scale by a factor of two.

# Transverse momentum distribution of Higgs boson via $gg \rightarrow H$

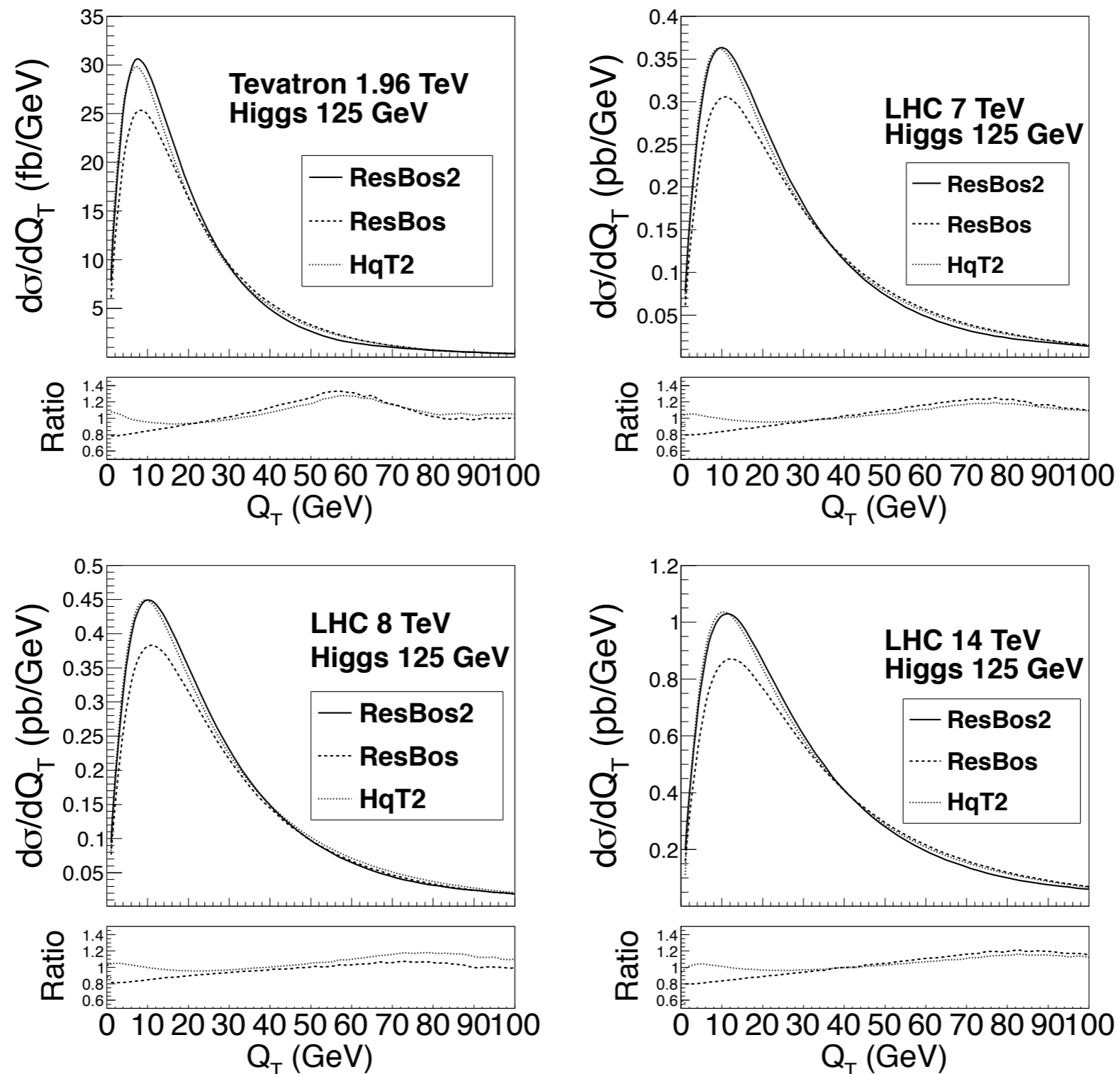
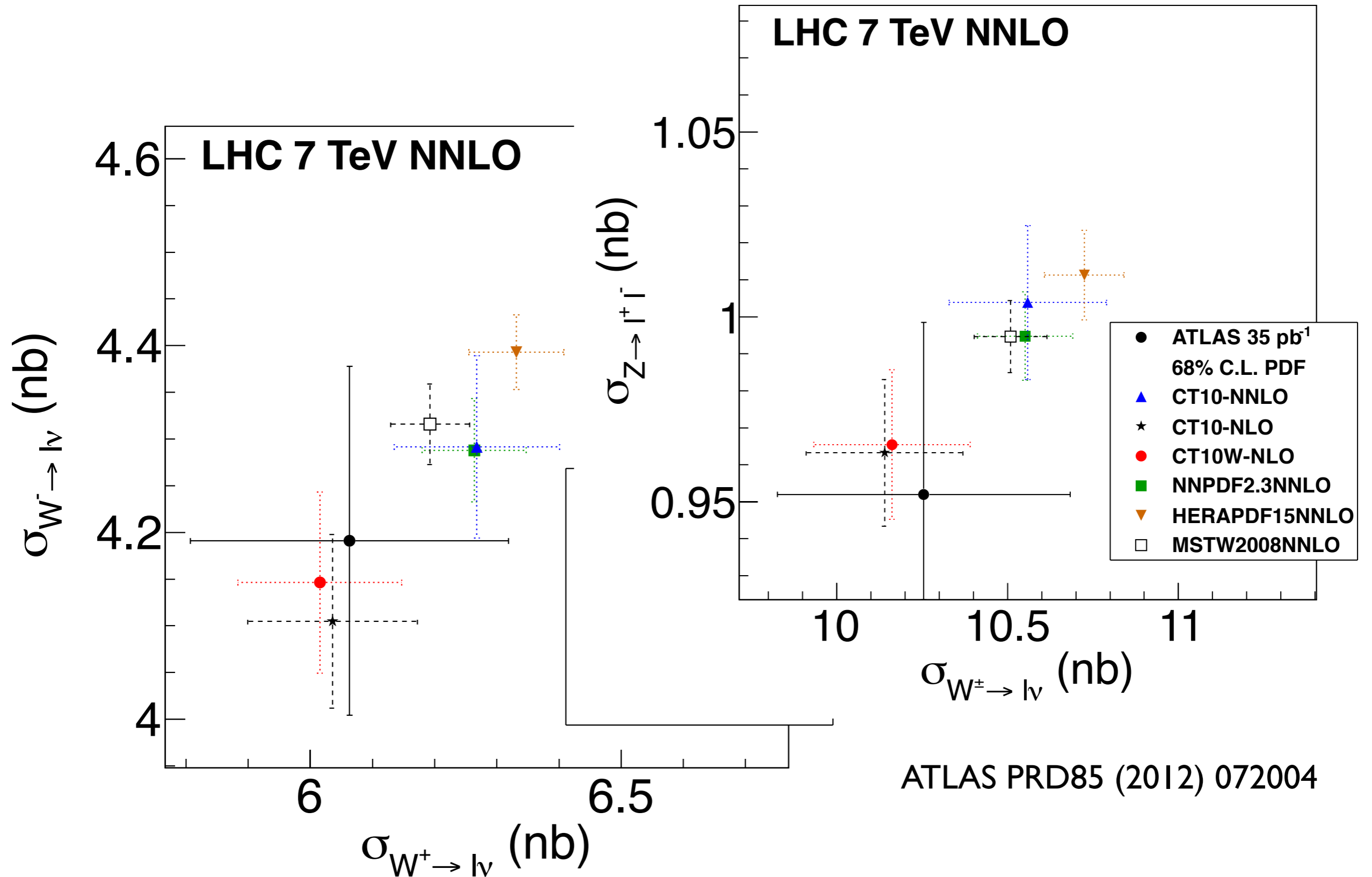
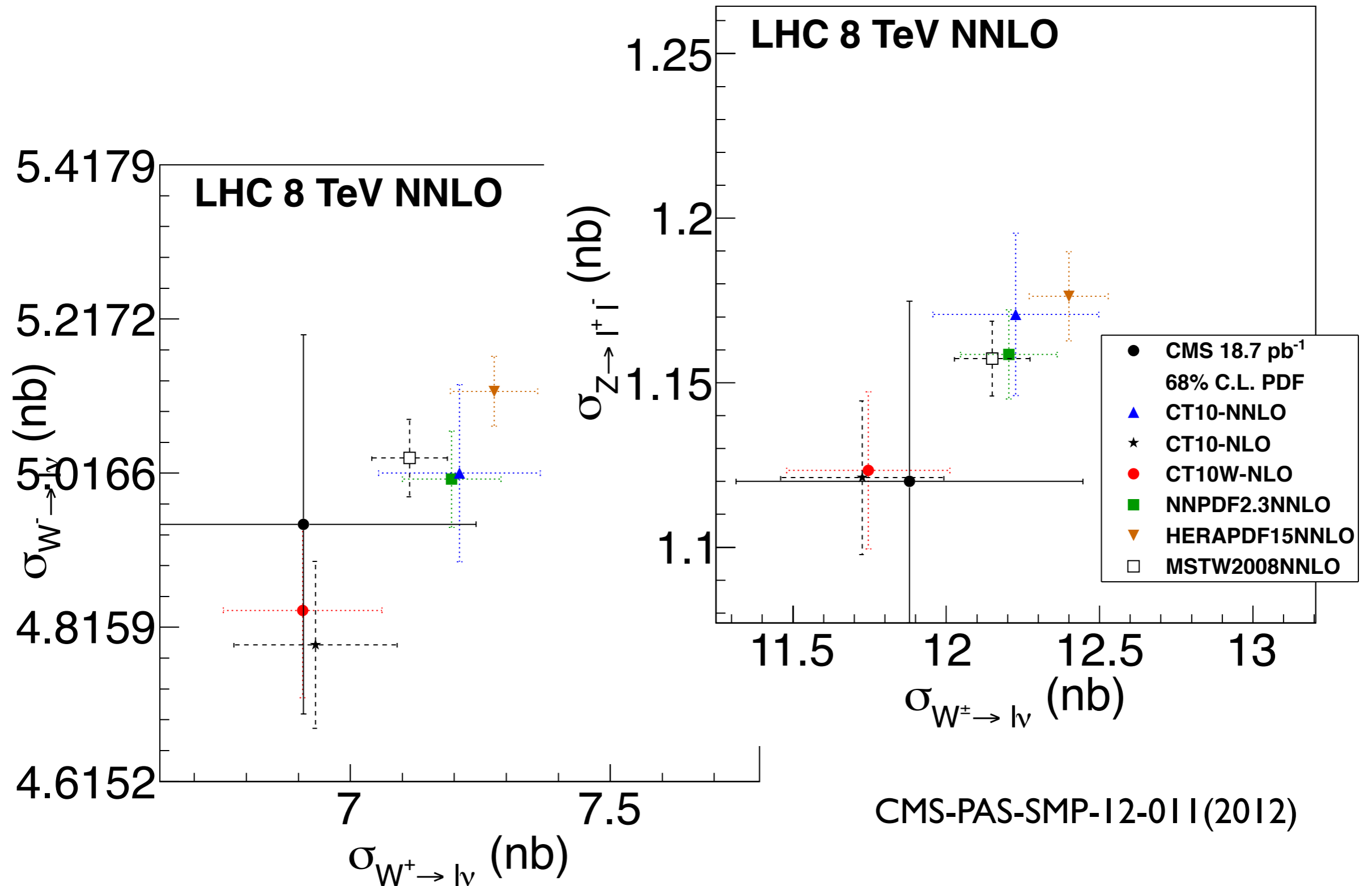


FIG. 1: The different theoretical predictions on the transverse momentum distributions for the Higgs boson production at the Tevatron (1.96 TeV) and the LHC (7 TeV, 8 TeV and 14 TeV). In the bottom of each plot, the ratios to ResBos2 predictions are also shown.

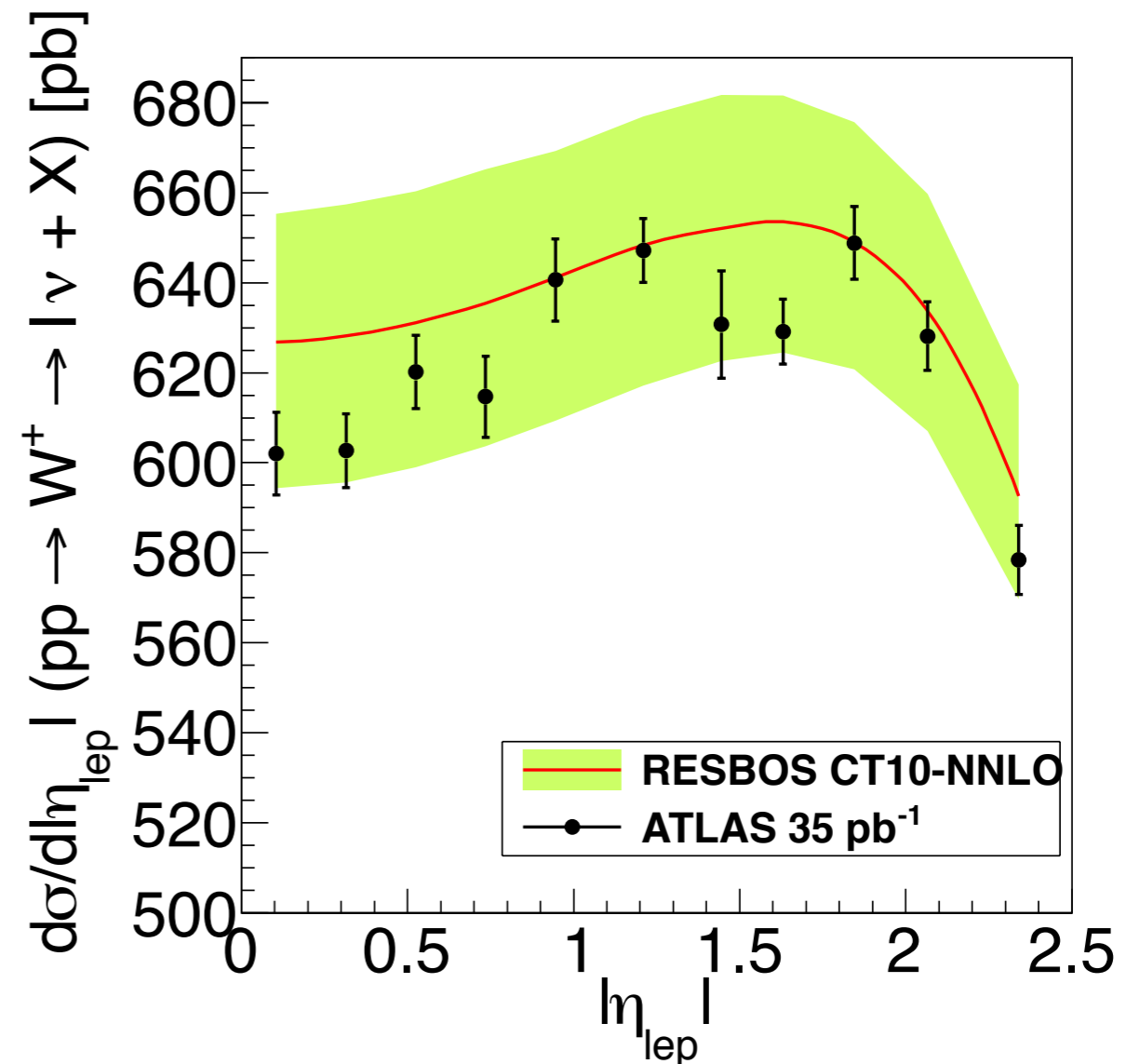
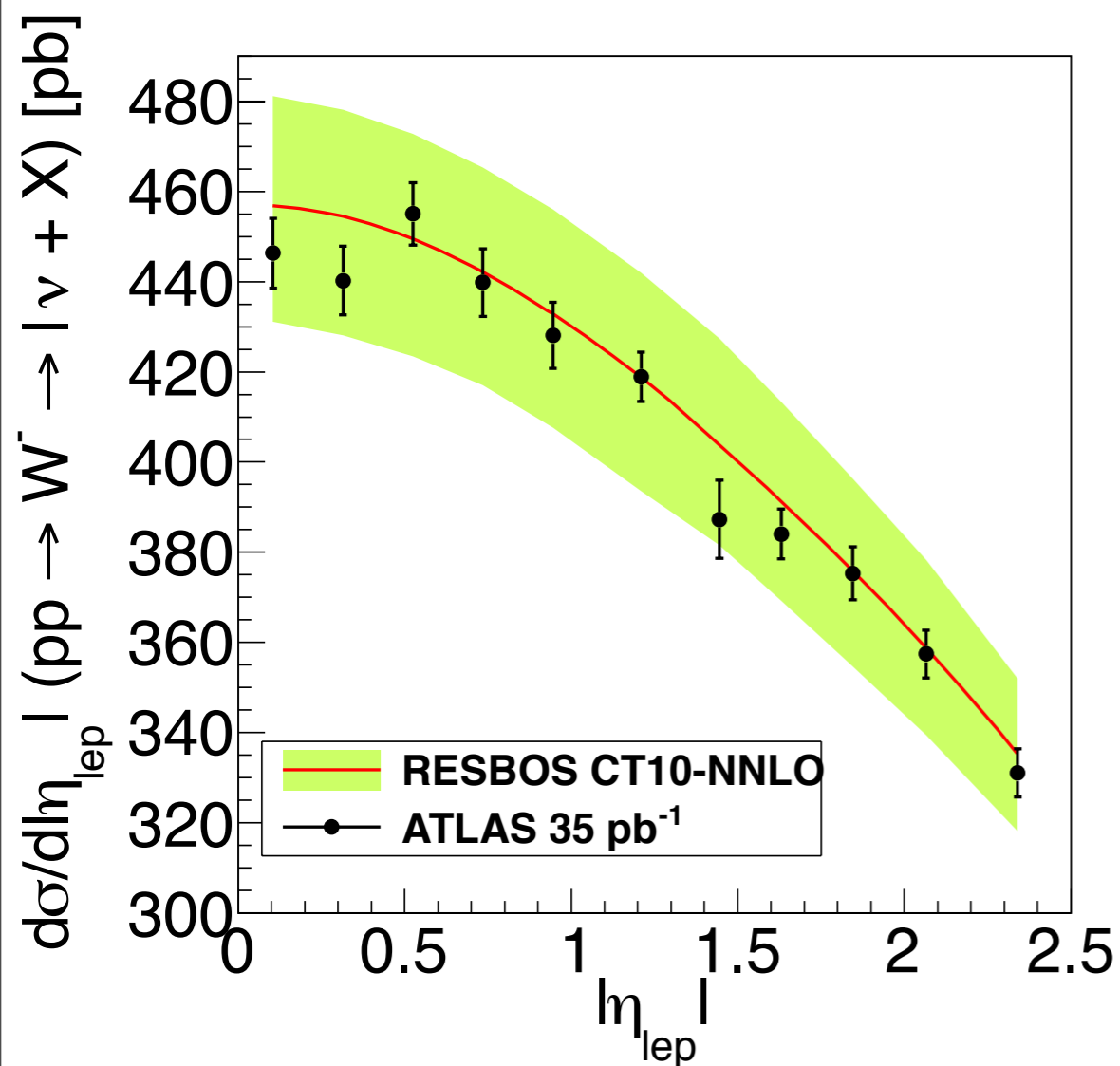
# Comparison between Z and W NNLO cross sections (7 TeV)



# Comparison between Z and W NNLO cross sections (8 TeV)

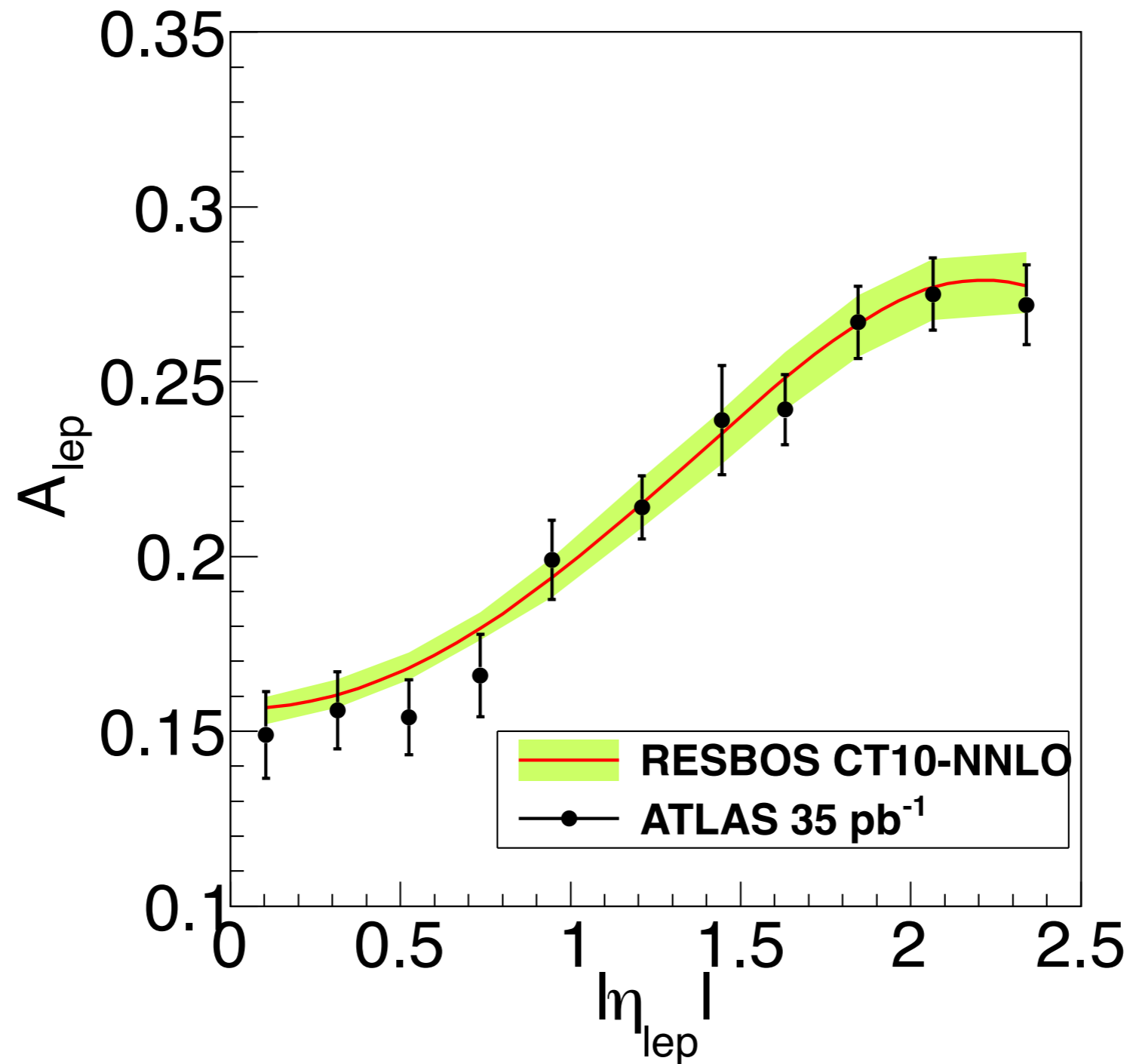


# ResBos predictions for W-lepton rapidity distribution using CT10-NNLO



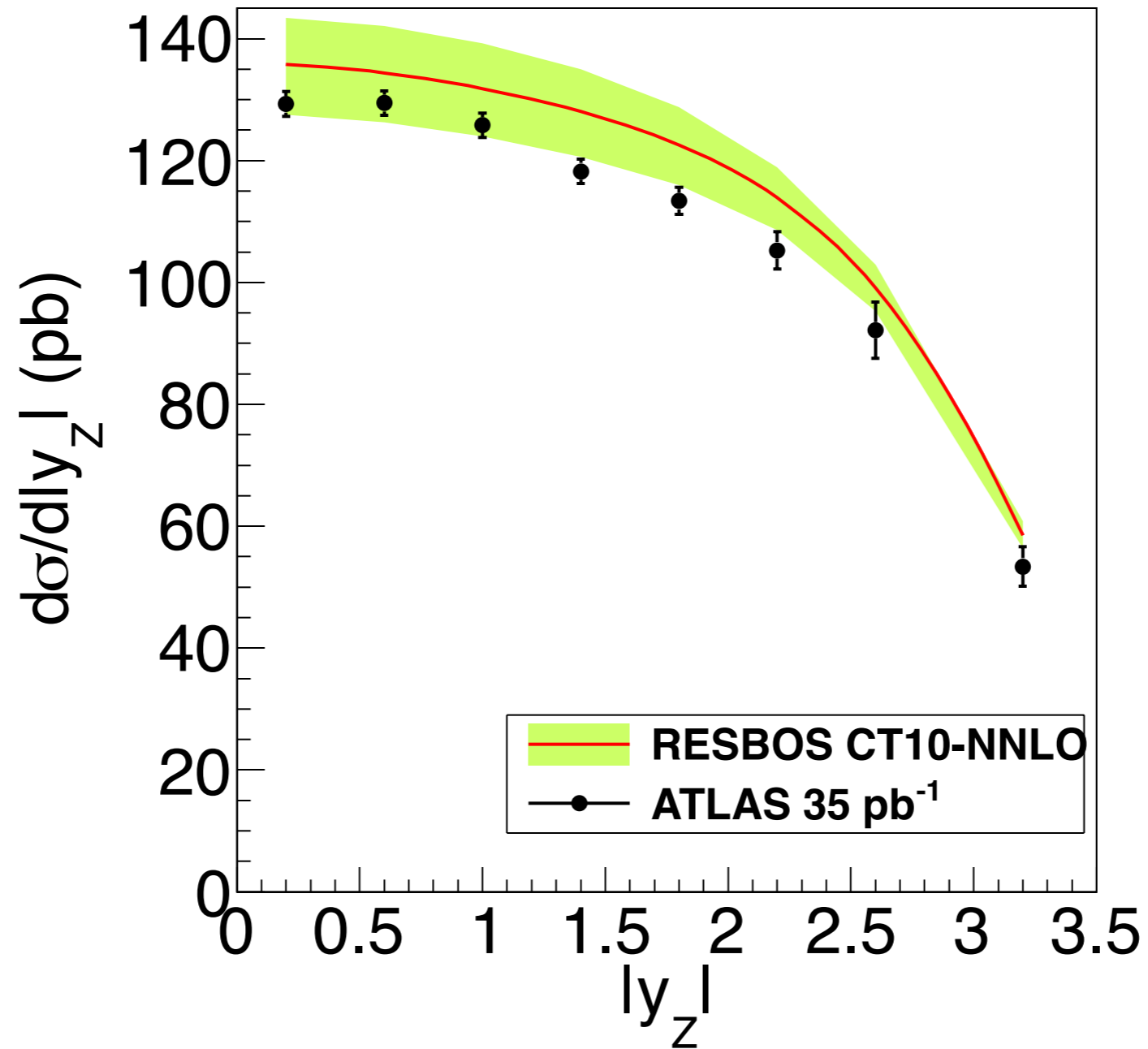
ATLAS Collaboration, PRD85 (2012) 072004

# ResBos predictions for W-lepton charge asymmetry using CT10-NNLO



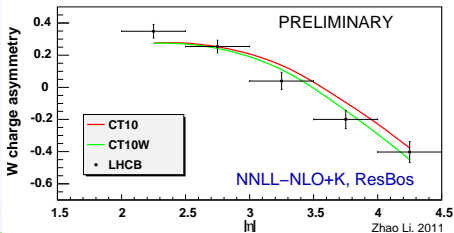
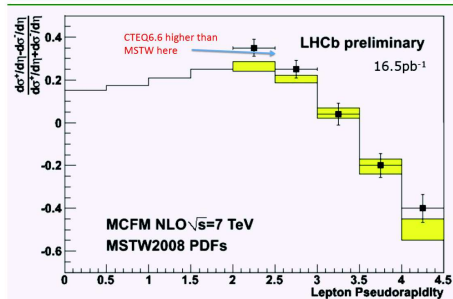
ATLAS Collaboration, PRD85 (2012) 072004

# ResBos predictions for Z rapidity distribution using CT10-NNLO



# CT10(W) vs. $A_\ell$ : LHC-B

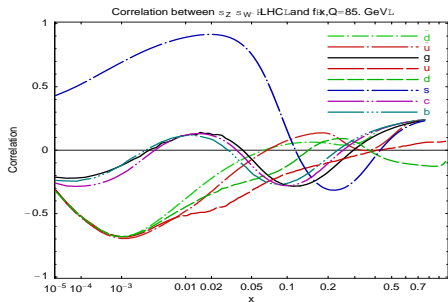
LHCb asymmetry measurement; from PDF4LHC Mar 7



LHC-B marginally prefers CT10W

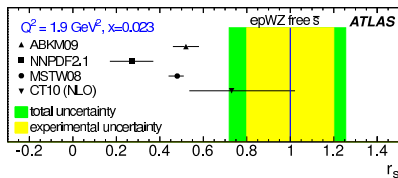


## Strangeness in CT12 PDFs and LHC $W/Z$ cross sections



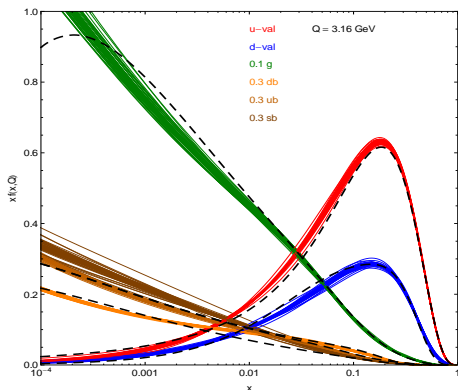
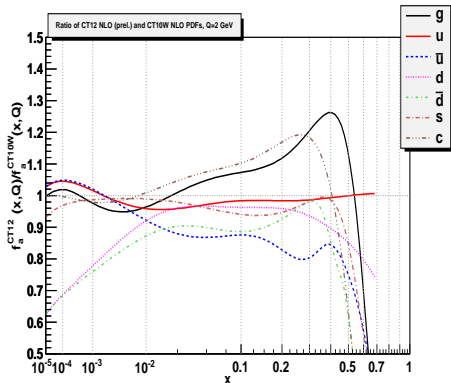
In 2008, our CTEQ6.6 PDF correlation analysis pointed out the sensitivity of ratios  $\sigma_W/\sigma_Z$  at the LHC to the strangeness PDF, with implications to EW precision measurements (Nadolsky, Lai, Cao, Huston, Pumplin, Tung, Yuan, PRD, 78 (2008) 013004).

The ATLAS analysis (arXiv:1203.4051) of  $W$  and  $Z$  production suggests that  $\bar{s}(x, Q)/\bar{d}(x, Q) = 1.00^{+0.25}_{-0.28}$  at  $x = 0.023$  and  $Q^2 = 1.9 \text{ GeV}^2$



What is the impact of LHC  $W$  and  $Z$  data on CT12 PDFs?

# Small- $x$ limits of $\bar{d}(x, Q)/\bar{u}(x, Q)$ and $\bar{s}(x, Q)/\bar{u}(x, Q)$ in the CT12 analysis (PRELIMINARY)



The CT12 analysis explores the possibility of  $\lim_{x \rightarrow 0} \bar{d}/\bar{u} \neq 1$ . Some “unbiased” CT12 candidate fits have  $\bar{s}(x, Q)/\bar{u}(x, Q) > 1$  at  $x < 10^{-3}$ .

We would like to better understand the flavor decomposition at small  $x$  before releasing the CT12 PDFs.

## Conclusions

- The CT10 NNLO PDF analysis (based on pre-LHC data only) is released. It is based on a new streamlined implementation of heavy-quark DIS contributions at two loops (*Guzzi et al., arXiv:1108.5112*).
- The CT12 NLO and NNLO analysis (in progress) will include latest LHC data on  $W$ ,  $Z$ , and jet production. Possible impact on  $SU(3)$  properties of quark sea at  $x < 10^{-3}$ .
- Several factors that are comparable to NNLO contributions (treatment of percentage corr. syst. errors, choices of scales, electroweak radiative contributions, ...) have been thoroughly examined in this analysis
- We use a specific choice to evaluate these factors in the CT12 (N)NLO fits. The uncertainty associated with this choice need to be examined in the future