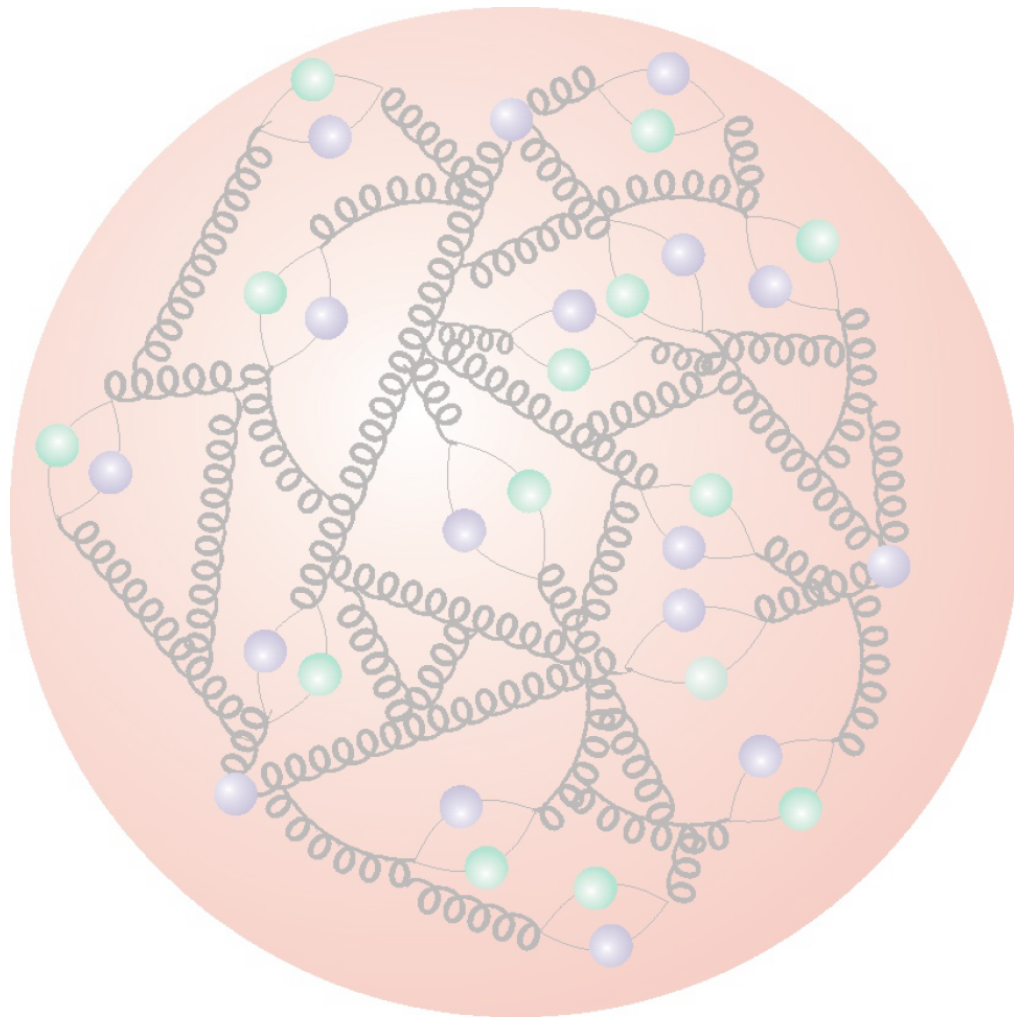
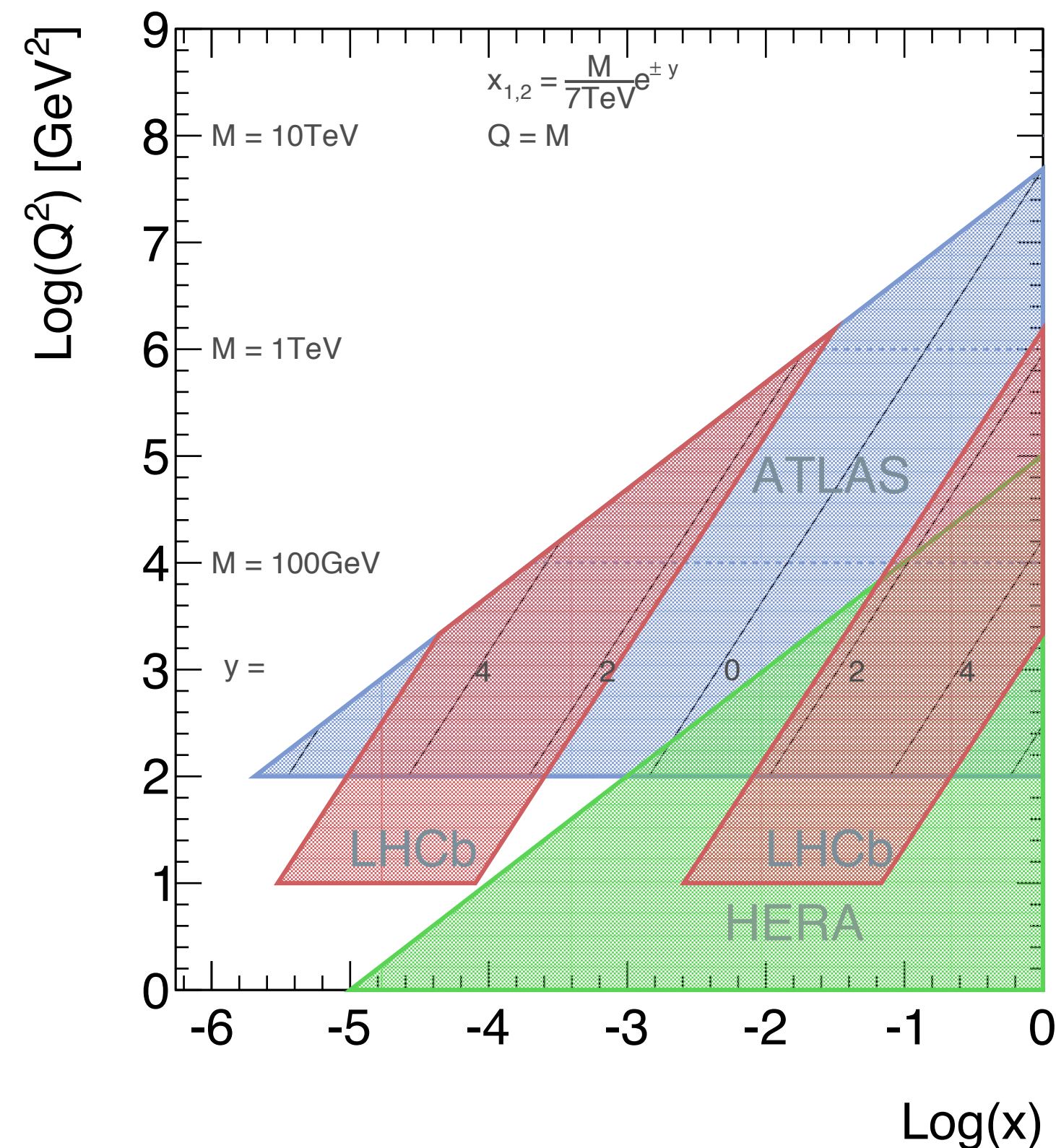


# Precision QCD in DIS at HERA



- Introduction
- HERA-II Updates
- H1 NC/CC  $e^\pm p$
- H1 NC High  $y$   $e^\pm p$
- ZEUS NC  $e^+ p$
- HERAPDF Plans





LHC: largest mass states at large  $x$

For central production  $x=x_1=x_2$

$$M=x\sqrt{s}$$

i.e.  $M > 1\text{TeV}$  probes  $x > 0.1$

Searches for high mass states require precision knowledge at high  $x$

$Z'$  / quantum gravity / susy searches...

DGLAP evolution allows predictions to be made

High  $x$  predictions rely on

- data (DIS / fixed target)
- sum rules
- behaviour of PDFs as  $x \rightarrow 1$



$$\frac{d\sigma_{NC}^{\pm}}{dx dQ^2} = \frac{2\pi\alpha^2}{x} \left[ \frac{1}{Q^2} \right]^2 \left[ Y_+ \tilde{F}_2 \mp Y_- x \tilde{F}_3 - y^2 \tilde{F}_L \right]$$

$$\frac{d\sigma_{CC}^{\pm}}{dx dQ^2} = \frac{G_F^2}{4\pi x} \left[ \frac{M_W^2}{M_W^2 + Q^2} \right]^2 \left[ Y_+ \tilde{W}_2^{\pm} \mp Y_- x \tilde{W}_3^{\pm} - y^2 \tilde{W}_L^{\pm} \right]$$

$$Y_{\pm} = 1 \pm (1-y)^2$$

$$\tilde{F}_2 \propto \sum (xq_i + x\bar{q}_i)$$

Dominant contribution

$$x\tilde{F}_3 \propto \sum (xq_i - x\bar{q}_i)$$

Only sensitive at high  $Q^2 \sim M_Z^2$

$$\tilde{F}_L \propto \alpha_s \cdot xg(x, Q^2)$$

Only sensitive at low  $Q^2$  and high  $y$

The NC reduced cross section defined as:

$$\tilde{\sigma}_{NC}^{\pm} = \frac{Q^2 x}{2\alpha\pi^2} \frac{1}{Y_+} \frac{d^2\sigma^{\pm}}{dx dQ^2}$$

$$\tilde{\sigma}_{NC}^{\pm} \sim \tilde{F}_2 \mp \frac{Y_-}{Y_+} x\tilde{F}_3$$

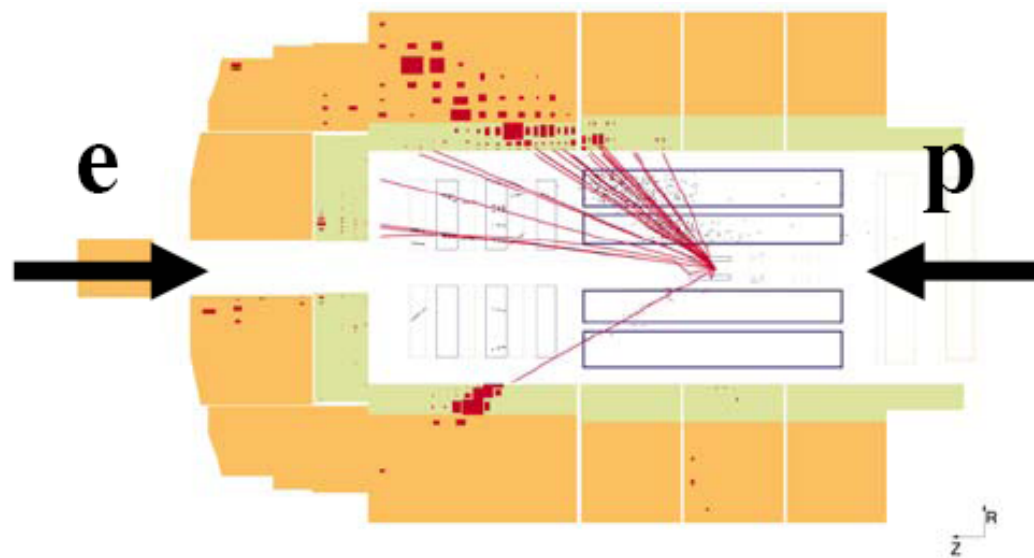
The CC reduced cross section defined as:

$$\sigma_{CC}^{\pm} = \frac{2\pi x}{G_F^2} \left[ \frac{M_W^2 + Q^2}{M_W^2} \right]^2 \frac{d\sigma_{CC}^{\pm}}{dx dQ^2}$$

$$\frac{d\sigma_{CC}^{\pm}}{dx dQ^2} = \frac{1}{2} \left[ Y_+ W_2^{\pm} \mp Y_- x W_3^{\pm} - y^2 W_L^{\pm} \right]$$

similarly for pure weak CC analogues:

$$W_2^{\pm}, xW_3^{\pm} \text{ and } W_L^{\pm}$$



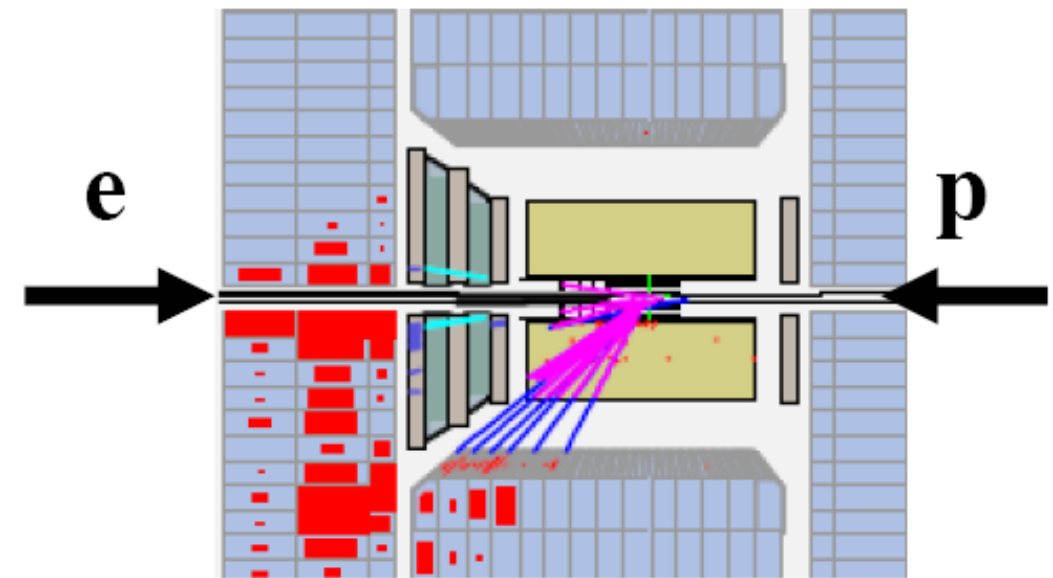
Neutral current event selection:

High  $P_T$  isolated scattered lepton  
 Suppress huge photo-production background by imposing longitudinal energy-momentum conservation

Kinematics may be reconstructed in many ways:  
 energy/angle of hadrons & scattered lepton  
 provides excellent tools for sys cross checks

Removal of scattered lepton provides a  
 high stats “pseudo-charged current sample”  
 Excellent tool to cross check CC analysis

Final selection:  $\sim 10^5$  events per sample at high  $Q^2$   
 $\sim 10^7$  events for  $10 < Q^2 < 100 \text{ GeV}^2$



Charged current event selection:

Large missing transverse momentum (neutrino)  
 Suppress huge photo-production background  
 Topological finders to remove cosmic muons

Kinematics reconstructed from hadrons  
 Final selection:  $\sim 10^3$  events per sample



## HERA-I operation 1993-2000

$E_e = 27.6 \text{ GeV}$

$E_p = 820 / 920 \text{ GeV}$

$\int \mathcal{L} \sim 110 \text{ pb}^{-1}$  per experiment

## HERA-II operation 2003-2007

$E_e = 27.6 \text{ GeV}$

$E_p = 920 \text{ GeV}$

$\int \mathcal{L} \sim 330 \text{ pb}^{-1}$  per experiment

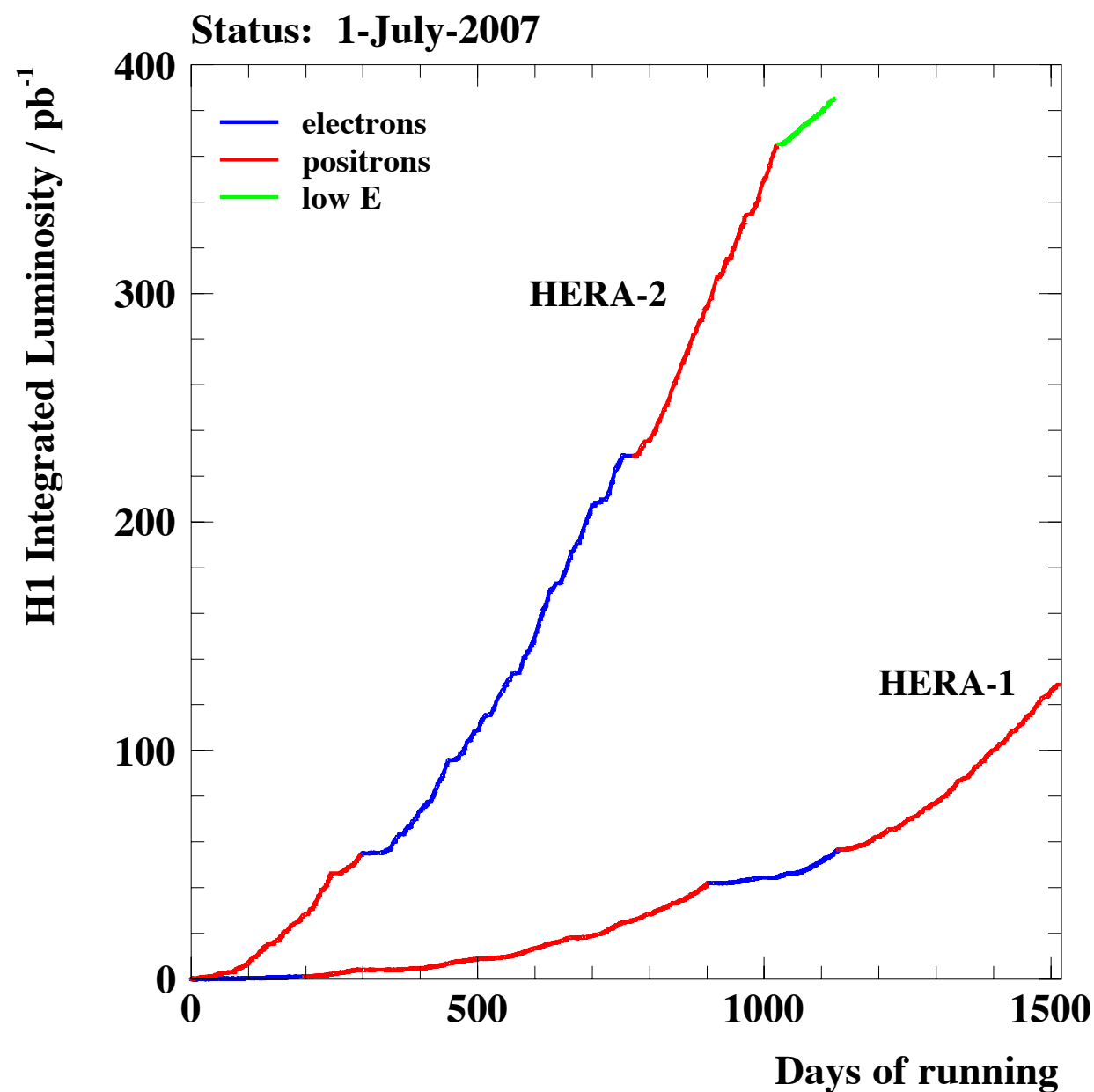
Longitudinally polarised leptons

## Low Energy Run 2007

$E_e = 27.6 \text{ GeV}$

$E_p = 575 \text{ \& } 460 \text{ GeV}$

Dedicated  $F_L$  measurement



## Summary of HERA-I datasets Combined in HERAPDF1.0

Available since 2009

| Data Set     |       | $x$ Range            |                    | $Q^2$ Range<br>GeV <sup>2</sup> |       | $\mathcal{L}$<br>pb <sup>-1</sup> | $e^+/e^-$ | $\sqrt{s}$<br>GeV |
|--------------|-------|----------------------|--------------------|---------------------------------|-------|-----------------------------------|-----------|-------------------|
| H1 svx-mb    | 95-00 | $5 \times 10^{-6}$   | 0.02               | 0.2                             | 12    | 2.1                               | $e^+p$    | 301-319           |
| H1 low $Q^2$ | 96-00 | $2 \times 10^{-4}$   | 0.1                | 12                              | 150   | 22                                | $e^+p$    | 301-319           |
| H1 NC        | 94-97 | 0.0032               | 0.65               | 150                             | 30000 | 35.6                              | $e^+p$    | 301               |
| H1 CC        | 94-97 | 0.013                | 0.40               | 300                             | 15000 | 35.6                              | $e^+p$    | 301               |
| H1 NC        | 98-99 | 0.0032               | 0.65               | 150                             | 30000 | 16.4                              | $e^-p$    | 319               |
| H1 CC        | 98-99 | 0.013                | 0.40               | 300                             | 15000 | 16.4                              | $e^-p$    | 319               |
| H1 NC HY     | 98-99 | 0.0013               | 0.01               | 100                             | 800   | 16.4                              | $e^-p$    | 319               |
| H1 NC        | 99-00 | 0.0013               | 0.65               | 100                             | 30000 | 65.2                              | $e^+p$    | 319               |
| H1 CC        | 99-00 | 0.013                | 0.40               | 300                             | 15000 | 65.2                              | $e^+p$    | 319               |
| ZEUS BPC     | 95    | $2 \times 10^{-6}$   | $6 \times 10^{-5}$ | 0.11                            | 0.65  | 1.65                              | $e^+p$    | 301               |
| ZEUS BPT     | 97    | $6 \times 10^{-7}$   | 0.001              | 0.045                           | 0.65  | 3.9                               | $e^+p$    | 301               |
| ZEUS SVX     | 95    | $1.2 \times 10^{-5}$ | 0.0019             | 0.6                             | 17    | 0.2                               | $e^+p$    | 301               |
| ZEUS NC      | 96-97 | $6 \times 10^{-5}$   | 0.65               | 2.7                             | 30000 | 30.0                              | $e^+p$    | 301               |
| ZEUS CC      | 94-97 | 0.015                | 0.42               | 280                             | 17000 | 47.7                              | $e^+p$    | 301               |
| ZEUS NC      | 98-99 | 0.005                | 0.65               | 200                             | 30000 | 15.9                              | $e^-p$    | 319               |
| ZEUS CC      | 98-99 | 0.015                | 0.42               | 280                             | 30000 | 16.4                              | $e^-p$    | 319               |
| ZEUS NC      | 99-00 | 0.005                | 0.65               | 200                             | 30000 | 63.2                              | $e^+p$    | 319               |
| ZEUS CC      | 99-00 | 0.008                | 0.42               | 280                             | 17000 | 60.9                              | $e^+p$    | 319               |

High  $Q^2$  NC and CC data limited to  
100 pb<sup>-1</sup>  $e^+p$   
16 pb<sup>-1</sup>  $e^-p$



Up till now HERA-II datasets only partially published

|                |                      |                         |
|----------------|----------------------|-------------------------|
| ZEUS CC $e^-p$ | 175 pb <sup>-1</sup> | EPJ C 61 (2009) 223-235 |
| ZEUS CC $e^+p$ | 132 pb <sup>-1</sup> | EPJ C 70 (2010) 945-963 |
| ZEUS NC $e^-p$ | 170 pb <sup>-1</sup> | EPJ C 62 (2009) 625-658 |
| ZEUS NC $e^+p$ | 135 pb <sup>-1</sup> | ZEUS-prel-II-003        |
| H1 CC $e^-p$   | 149 pb <sup>-1</sup> | H1prelim-09-043         |
| H1 CC $e^+p$   | 180 pb <sup>-1</sup> | H1prelim-09-043         |
| H1 NC $e^-p$   | 149 pb <sup>-1</sup> | H1prelim-09-042         |
| H1 NC $e^+p$   | 180 pb <sup>-1</sup> | H1prelim-09-042         |



|                |                      |                         |
|----------------|----------------------|-------------------------|
| ZEUS CC $e^-p$ | 175 pb <sup>-1</sup> | EPJ C 61 (2009) 223-235 |
| ZEUS CC $e^+p$ | 132 pb <sup>-1</sup> | EPJ C 70 (2010) 945-963 |
| ZEUS NC $e^-p$ | 170 pb <sup>-1</sup> | EPJ C 62 (2009) 625-658 |
| ZEUS NC $e^+p$ | 135 pb <sup>-1</sup> | <b>arXiv:1208.6138</b>  |
| H1 CC $e^-p$   | 149 pb <sup>-1</sup> | <b>arXiv:1206.7007</b>  |
| H1 CC $e^+p$   | 180 pb <sup>-1</sup> |                         |
| H1 NC $e^-p$   | 149 pb <sup>-1</sup> |                         |
| H1 NC $e^+p$   | 180 pb <sup>-1</sup> |                         |



HERA-II datasets  
Combined in HERAPDF1.5  
(except ZEUS NC  $e^+p$ )

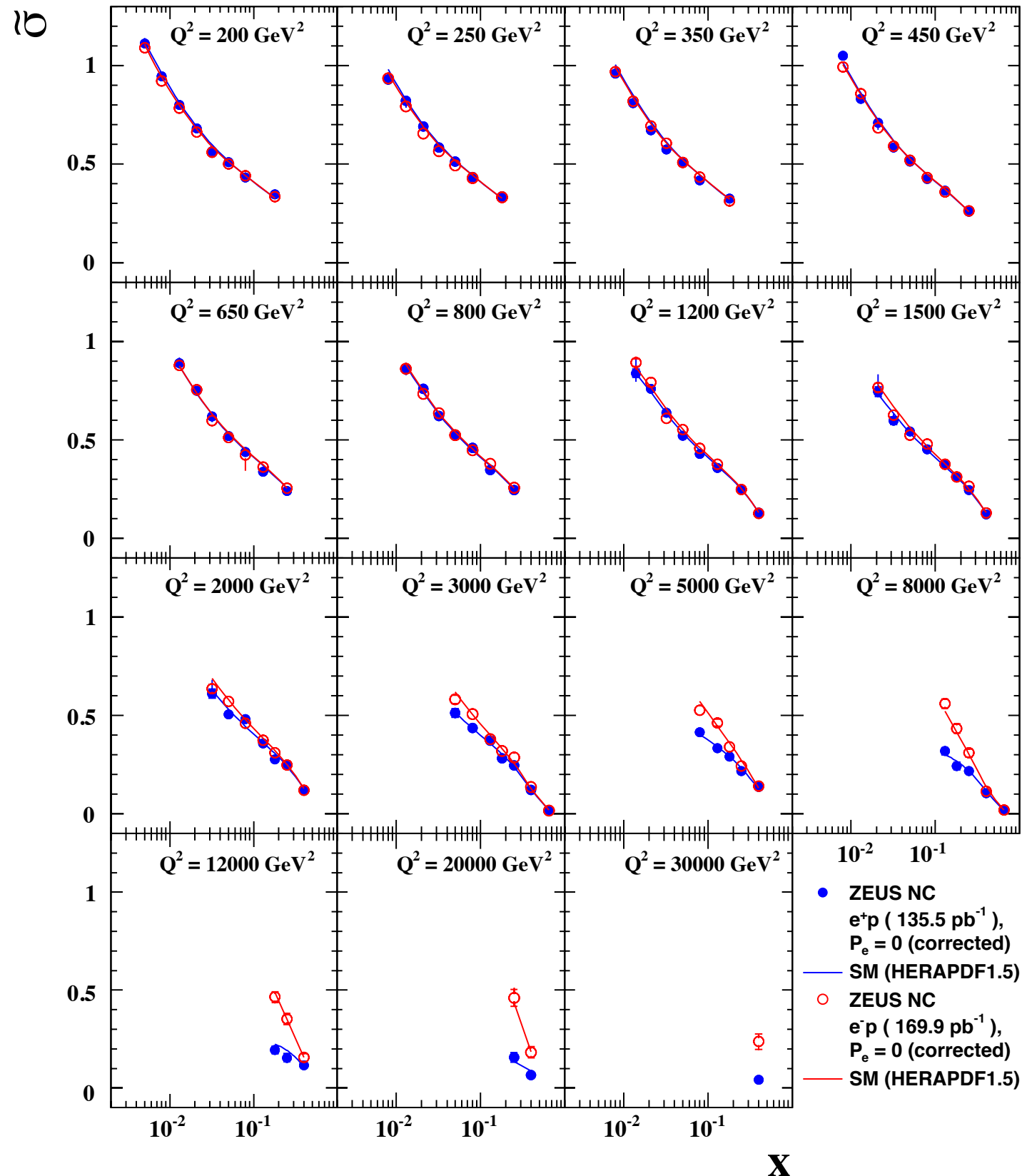
breakdown of HERA-II data samples

|        | $R$  | $L$  |
|--------|--|--|
| $e^-p$ | $\mathcal{L} = 47.3 \text{ pb}^{-1}$<br>$P_e = (+36.0 \pm 1.0)\%$  | $\mathcal{L} = 104.4 \text{ pb}^{-1}$<br>$P_e = (-25.8 \pm 0.7)\%$ |
| $e^+p$ | $\mathcal{L} = 101.3 \text{ pb}^{-1}$<br>$P_e = (+32.5 \pm 0.7)\%$ | $\mathcal{L} = 80.7 \text{ pb}^{-1}$<br>$P_e = (-37.0 \pm 0.7)\%$  |

Complete the analyses of HERA high  $Q^2$  inclusive structure function data

New published data increase  $\int \mathcal{L}$  by  
~ factor 3 for  $e^+p$   
~ factor 10 for  $e^-p$   
much improved systematic uncertainties

## ZEUS



High  $Q^2$  is the EW physics regime

Final measurement of ZEUS NC  $e^+p$  data

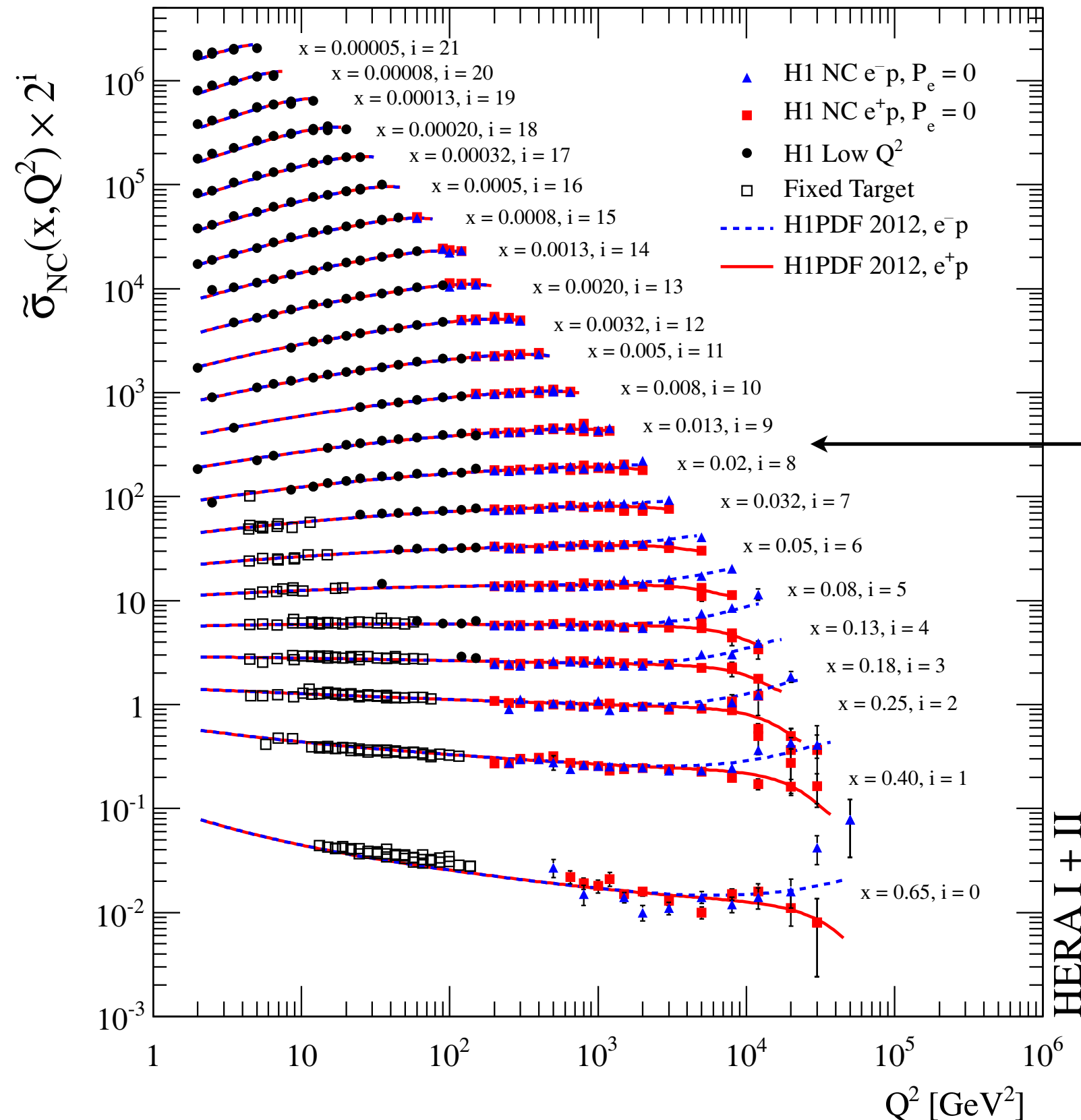
Shown here for  $P=0$

Polarised measurements also available

Compared to published NC  $e^-p$  data



## H1 Collaboration



H1 precision 1.5% for  $Q^2 < 500$  GeV<sup>2</sup>  
 $\Rightarrow$  factor 2 reduction in error wrt HERA-I

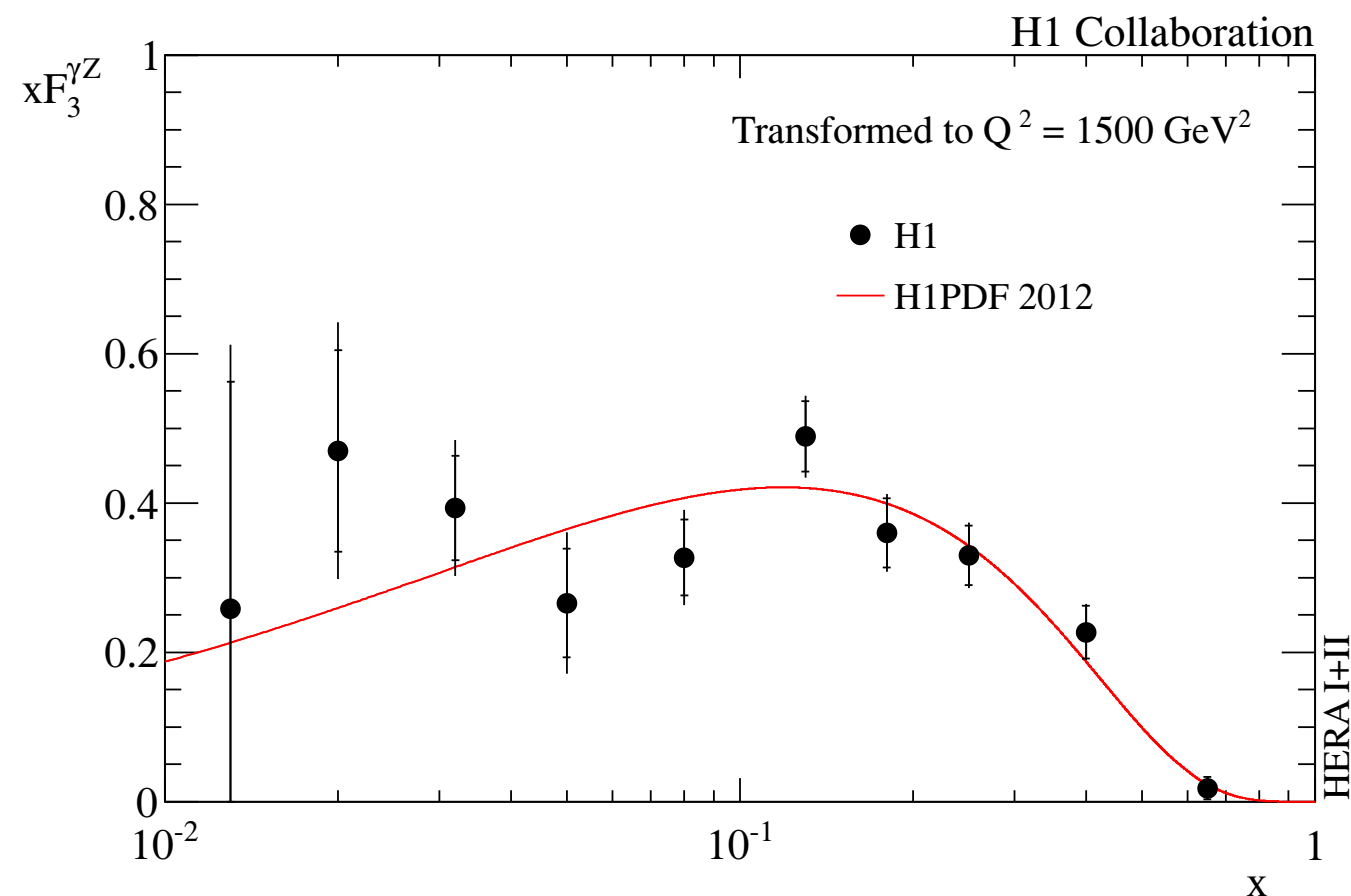
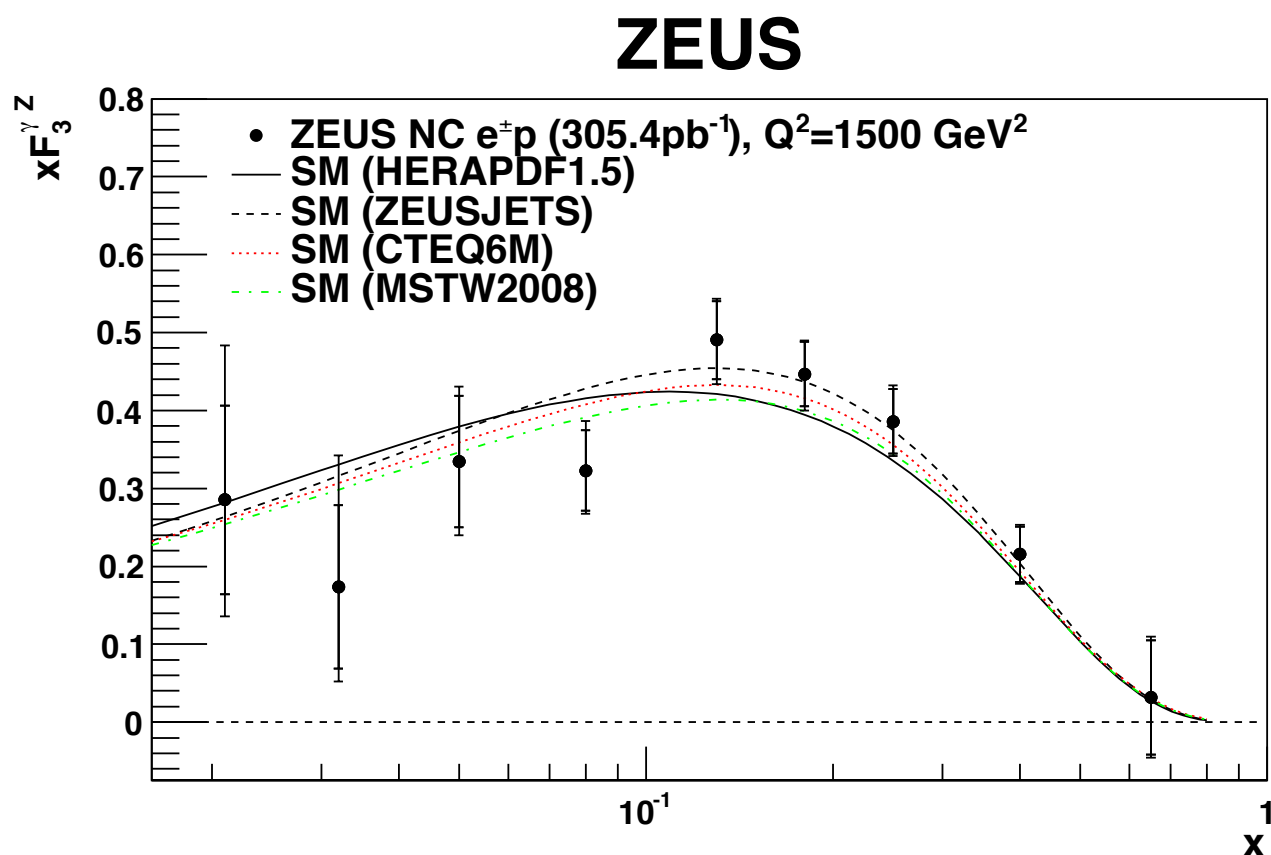
Statistics limited at higher  $Q^2$  and high  $x$

Extended reach at high  $x$  compared to H1 preliminary data

This  $x$  region is the 'sweet spot'  
 High precision with long  $Q^2$  lever arm  
 $x$ -range relevant for Higgs production

Combination of high  $Q^2$  data  
 HERA-I and HERA-II

Larger HERA-II luminosity  
 $\rightarrow$  improved precision at high  $x / Q^2$



At high  $Q^2$   $x\tilde{F}_3$  arises due to  $Z^0$  effects  
 enhanced  $e^-$  cross section wrt  $e^+$   
 Difference is  $x\tilde{F}_3$   
 Sensitive to valence PDFs

$$x\tilde{F}_3 = \frac{Y_+}{2Y_-} (\tilde{\sigma}_{NC}^- - \tilde{\sigma}_{NC}^+) \approx a_e \chi_Z xF_3^{\gamma Z}$$

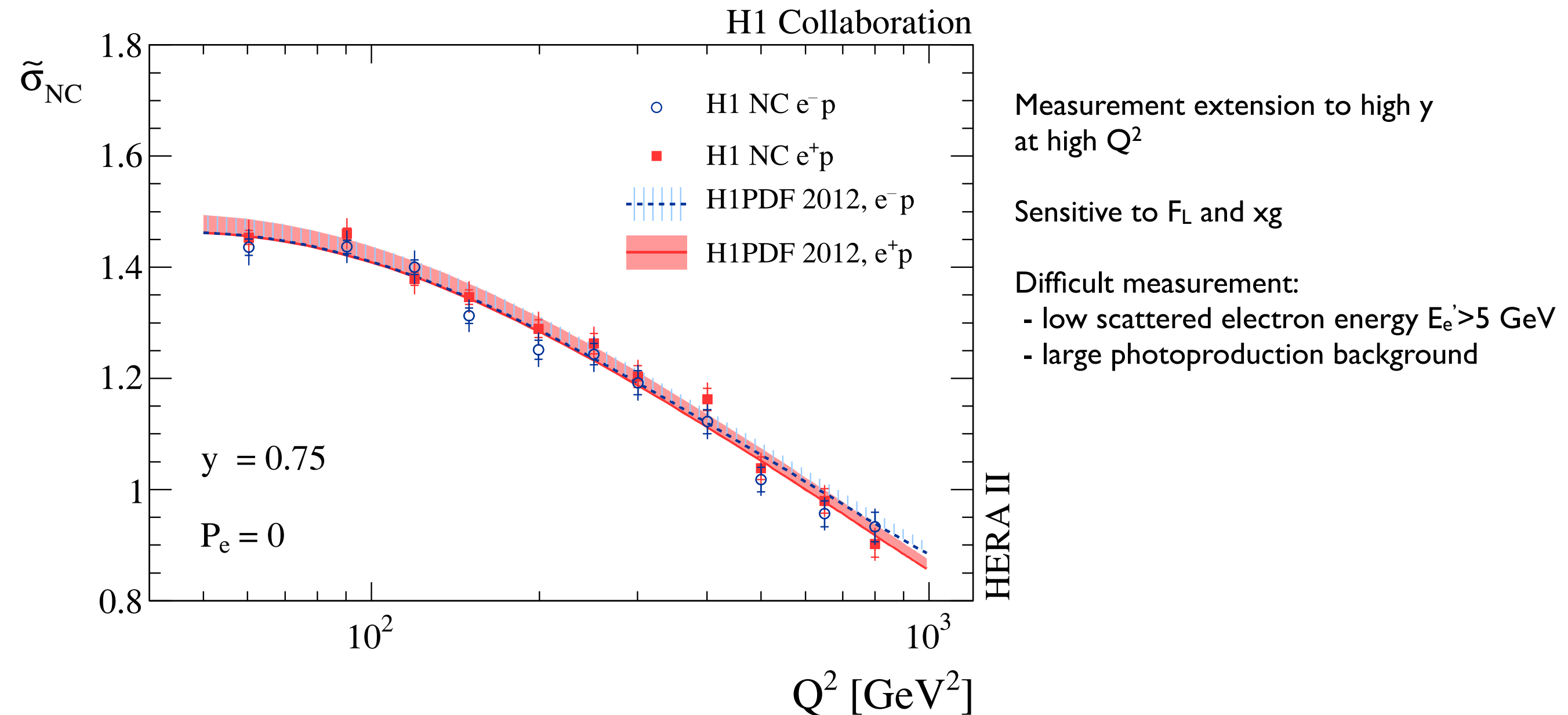
$$x\tilde{F}_3 \propto \sum (xq_i - x\bar{q}_i)$$

H1 measure integral of  $x\tilde{F}_3^{\gamma Z}$  - validate sumrule:

$$\int_{0.016}^{0.725} dx F_3^{\gamma Z}(x, Q^2 = 1500\text{ GeV}^2) = 1.22 \pm 0.09(\text{stat}) \pm 0.07(\text{syst})$$

LO integral predicted to  
 be  $5/3 + \mathcal{O}(\alpha_s/\pi)$





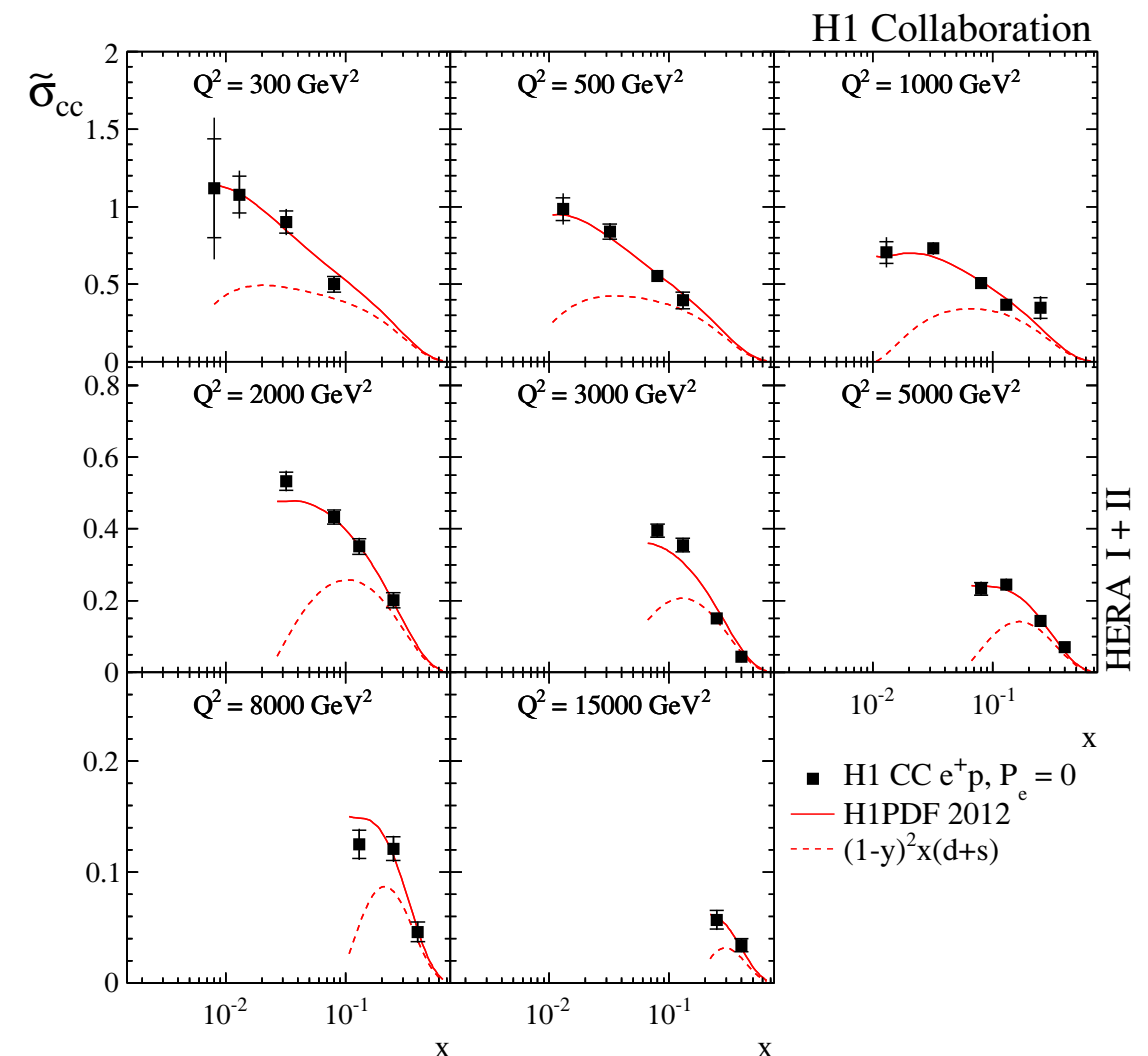
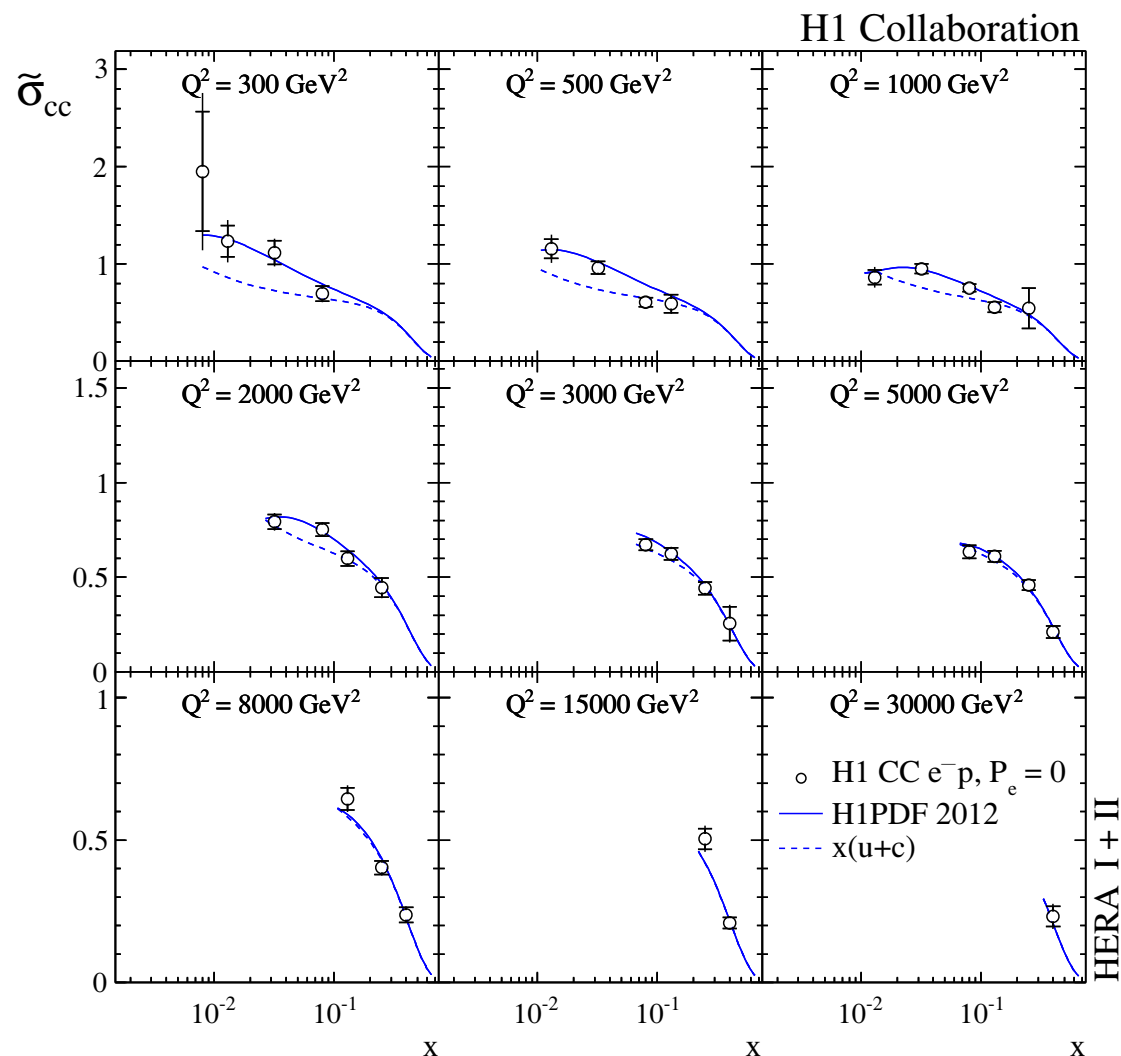
Total uncertainty reduced by factor 2:  
 HERA-I ~4%  
 HERA-II ~2%

## Electron scattering

$$\frac{d^2\sigma_{CC}^-}{dx dQ^2} = \frac{G_F^2}{2\pi} \left( \frac{M_W^2}{M_W^2 + Q^2} \right)^2 \left[ (u + c) + (1 - y)^2 (\bar{d} + \bar{s}) \right]$$

## Positron scattering

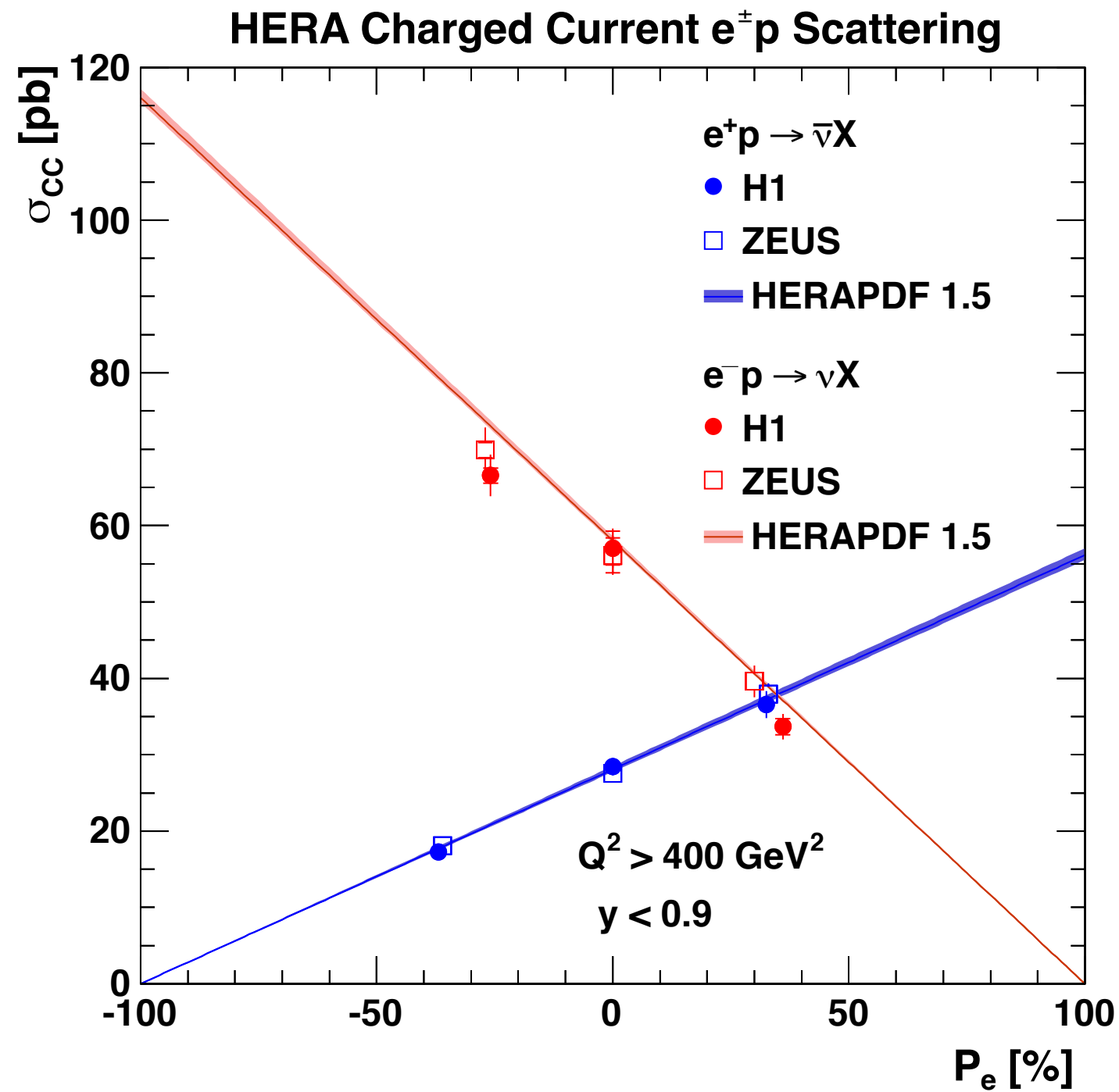
$$\frac{d^2\sigma_{CC}^+}{dx dQ^2} = \frac{G_F^2}{2\pi} \left( \frac{M_W^2}{M_W^2 + Q^2} \right)^2 \left[ (\bar{u} + \bar{c}) + (1 - y)^2 (d + s) \right]$$



H1 combination of high  $Q^2$  CC data (HERA-I+II)  
Improvement of total uncertainty  
Dominated by statistical errors  
Provide important flavour decomposition information

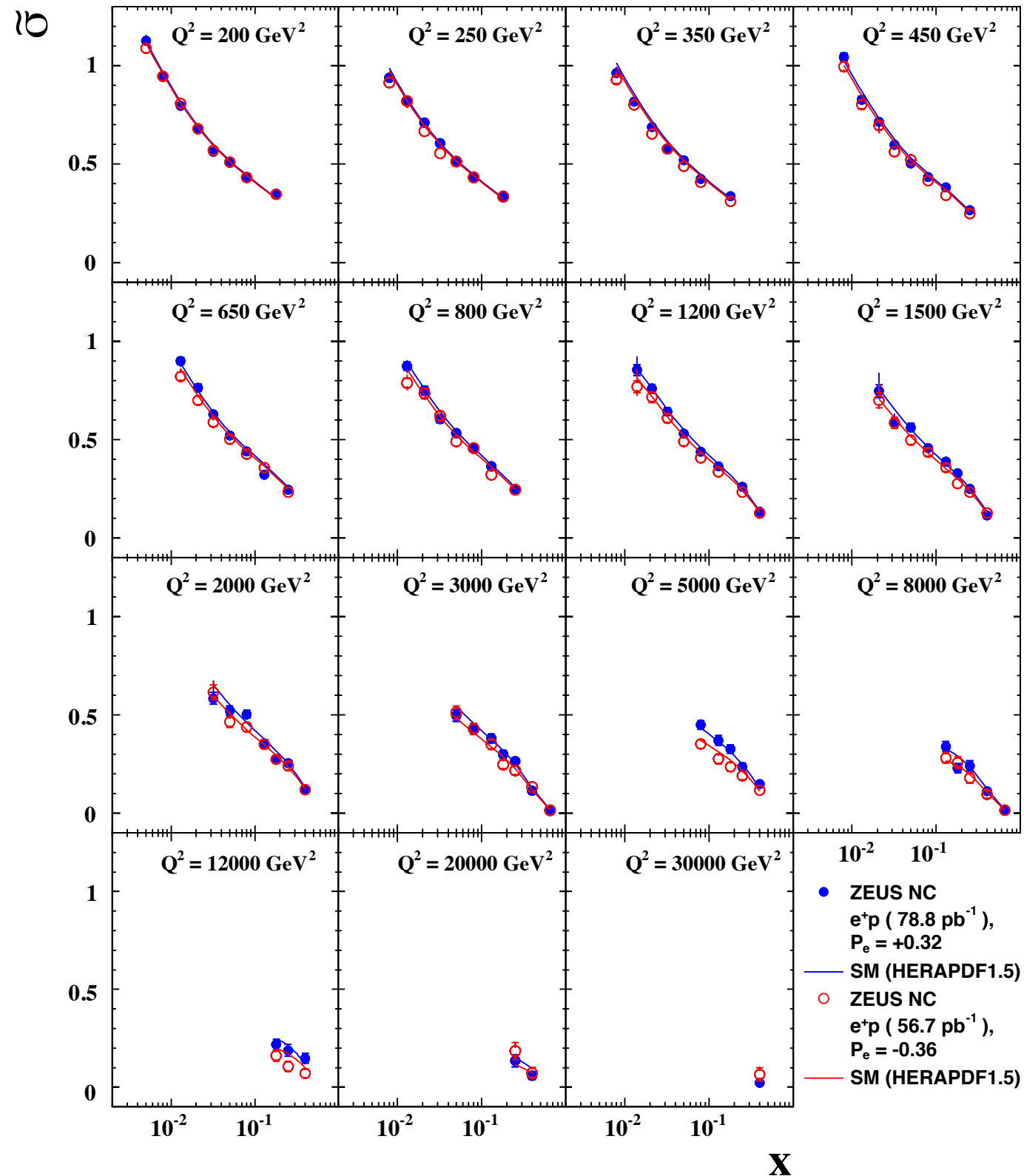
CC  $e^+$  data provide strong  $d_v$  constraint at high  $x$   
Precision limited by statistics: typically 5-10%  
HERA-I precision of 10-15% for  $e^+$   
Large gain to come after combination with ZEUS





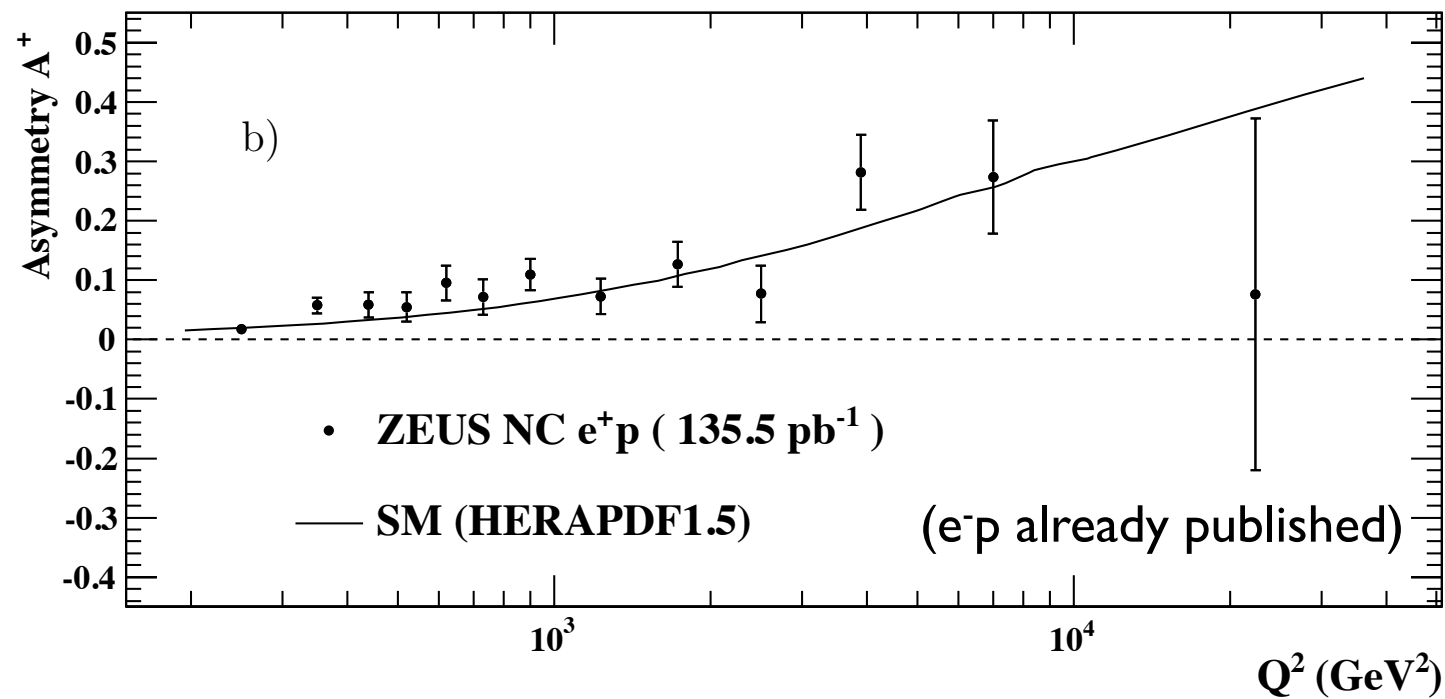
Polarisation dependence of CC cross section  
now final from H1 and ZEUS

## ZEUS



Polarised NC measurements completed  
for  $e^+p$  ,  $e^-p$  , L-handed , R-handed scattering

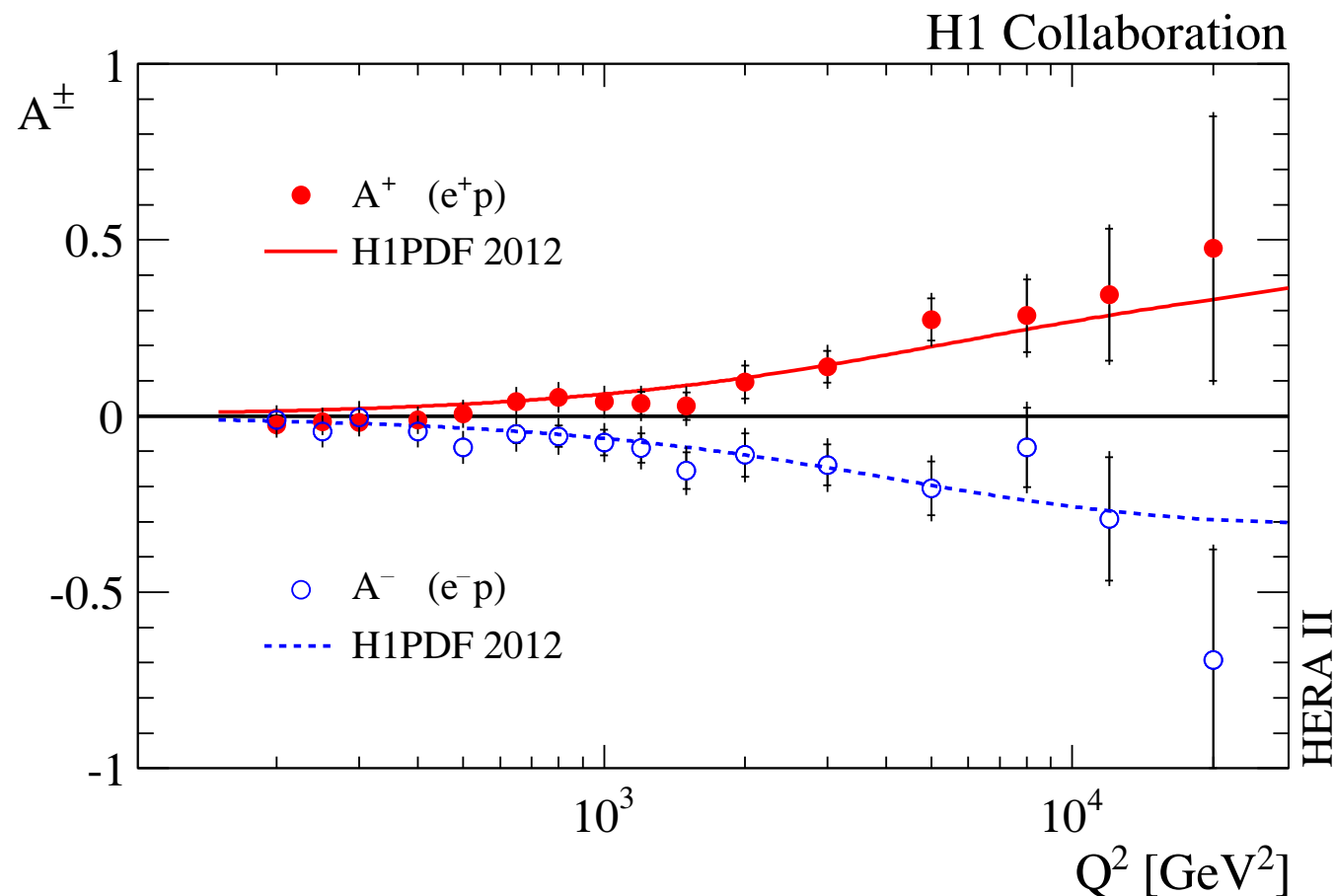
Difference in L,R scattering visible at high  $Q^2$



NC polarisation asymmetry:

$$A^\pm = \frac{2}{P_L^\pm - P_R^\pm} \cdot \frac{\sigma^\pm(P_L^\pm) - \sigma^\pm(P_R^\pm)}{\sigma^\pm(P_L^\pm) + \sigma^\pm(P_R^\pm)}$$

At large  $x$   $A^\pm \propto \pm \kappa \frac{1 + d_v/u_v}{4 + d_v/u_v}$

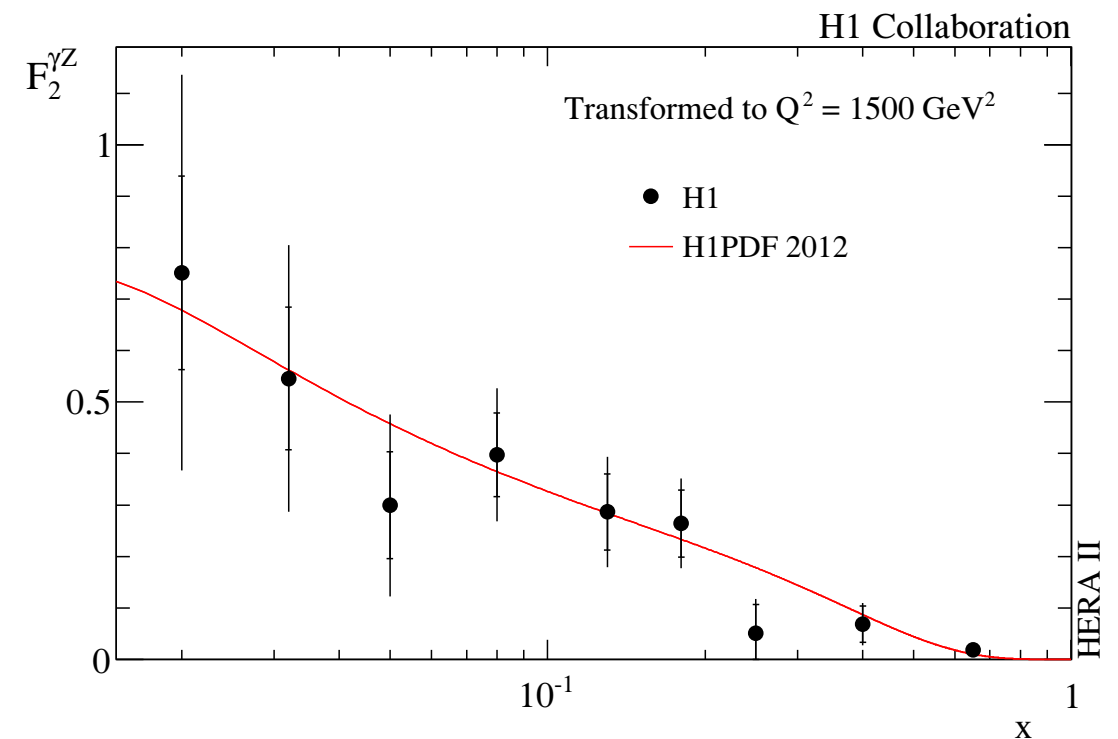
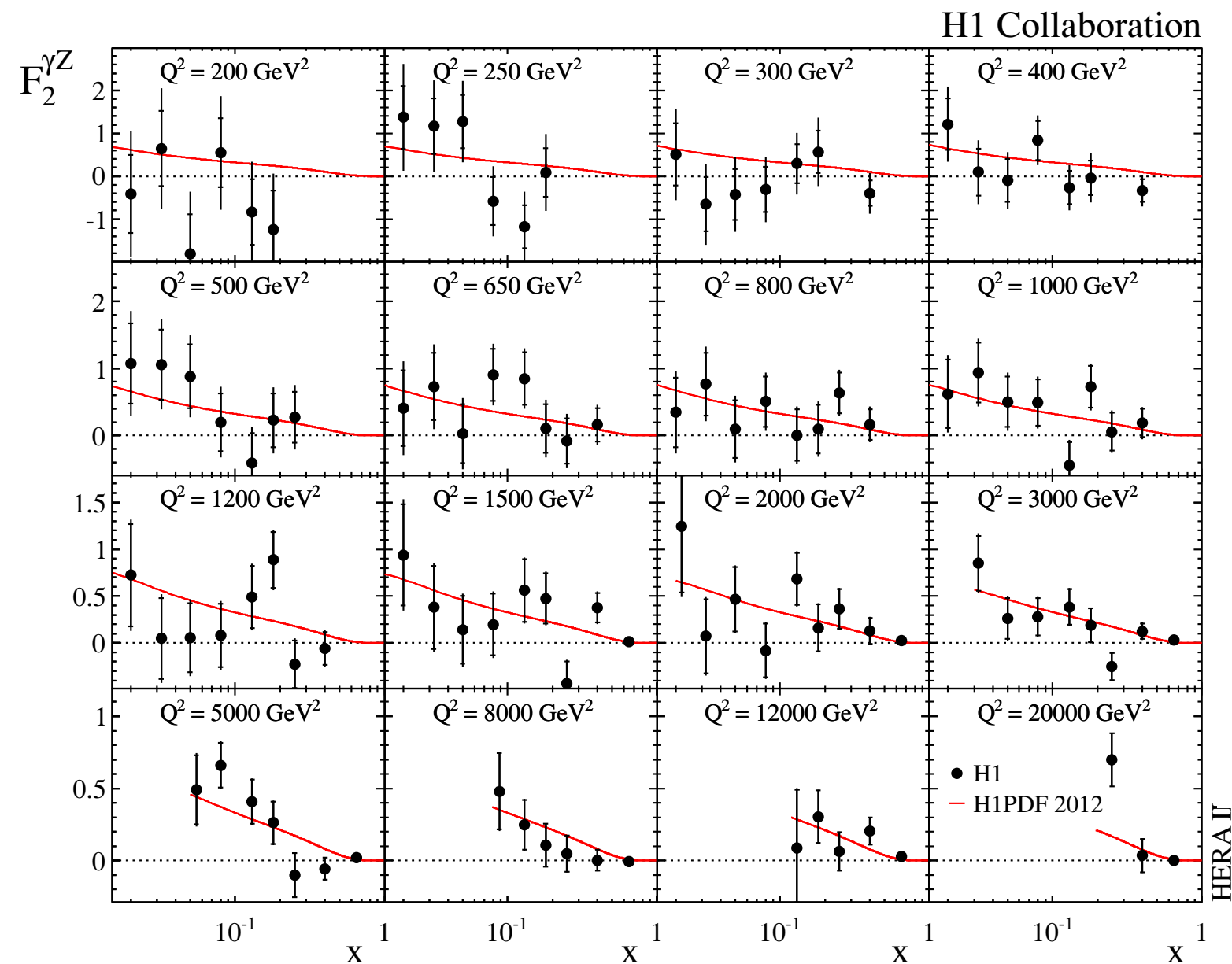




Measuring the difference in NC polarised cross sections gives access to new structure functions:

$$\frac{\sigma^\pm(P_L^\pm) - \sigma^\pm(P_R^\pm)}{P_L^\pm - P_R^\pm} = \frac{\kappa Q^2}{Q^2 + M_Z^2} \left[ \boxed{\mp a_e F_2^{\gamma Z}} + \frac{Y_-}{Y_+} v_e x F_3^{\gamma Z} - \frac{Y_-}{Y_+} \frac{\kappa Q^2}{Q^2 + M_Z^2} (v_e^2 + a_e^2) x F_3^Z \right]$$

$x F_3$  terms eliminated by subtracted  $e^-p$  from  $e^+p$



New H1 data are combined with all previously published H1 inclusive cross section measurements

854 data points averaged to 413 measurements

$$\chi^2/\text{ndf} = 412/441 = 0.93$$

Normalisation shifts for H1 data after averaging

| Source   | Shift in units of standard deviation | Shift in % of cross section |
|--|--------------------------------------|-----------------------------|
| $\delta\mathcal{L}^1$ (BH Theory)                          | -0.39                                | -0.19                       |
| $\delta\mathcal{L}^2$ ( $e^+$ 94-97)                       | -0.46                                | -0.66                       |
| $\delta\mathcal{L}^3$ ( $e^-$ 98-99)                       | -0.69                                | -1.20                       |
| $\delta\mathcal{L}^4$ ( $e^+$ 99-00)                       | -0.07                                | -0.10                       |
| $\delta\mathcal{L}^5$ (QEDC)                               | 0.81                                 | 1.70                        |
| $\delta\mathcal{L}^6, \delta\mathcal{L}^7$ ( $e^+ L + R$ ) | 0.84                                 | 0.80                        |
| $\delta\mathcal{L}^8, \delta\mathcal{L}^9$ ( $e^- L + R$ ) | 0.84                                 | 0.89                        |

Precision medium  $Q^2$   
HERA-I data ~unshifted

New high  $Q^2$  HERA-II  
data shifted by ~1.7%  
(less than 1 std.dev)

New PDF fit performed: can be thought of as a 'stepping-stone' towards HERAPDF2.0

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{25},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}},$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

| Parameter                        | Central Value | Lower Limit                  | Upper Limit                     |
|----------------------------------|---------------|------------------------------|---------------------------------|
| $f_s$                            | 0.31          | 0.23                         | 0.38                            |
| $m_c$ (GeV)                      | 1.4           | 1.35 (for $Q_0^2 = 1.8$ GeV) | 1.65                            |
| $m_b$ (GeV)                      | 4.75          | 4.3                          | 5.0                             |
| $Q_{\min}^2$ (GeV <sup>2</sup> ) | 3.5           | 2.5                          | 5.0                             |
| $Q_0^2$ (GeV <sup>2</sup> )      | 1.9           | 1.5 ( $f_s = 0.29$ )         | 2.5 ( $m_c = 1.6, f_s = 0.34$ ) |

13 parameter fit: additional flexibility given to  $u_v$  and  $d_v$  compared to H1PDF2009 / HERAPDF1.0

Apply momentum/counting sum rules:

$$\int_0^1 dx \cdot (xu_v + xd_v + x\bar{U} + x\bar{D} + xg) = 1$$

$$\int_0^1 dx \cdot u_v = 2 \quad \int_0^1 dx \cdot d_v = 1$$

Parameter constraints:

$$B_{\text{Ubar}} = B_{\text{Dbar}}$$

$$\text{sea} = 2 \times (\text{Ubar} + \text{Dbar})$$

$$\text{Ubar} = \text{Dbar at } x=0$$

$$f_s = \text{sbar/Dbar}$$

$$Q_0^2 = 1.9 \text{ GeV}^2 \text{ (below } m_c)$$

$$Q^2 > 3.5 \text{ GeV}^2$$

$$2 \times 10^{-4} < x < 0.65$$

Fits performed using RT-VFNS

Experimental uncertainties produced using RMS spread of 400 replica fits

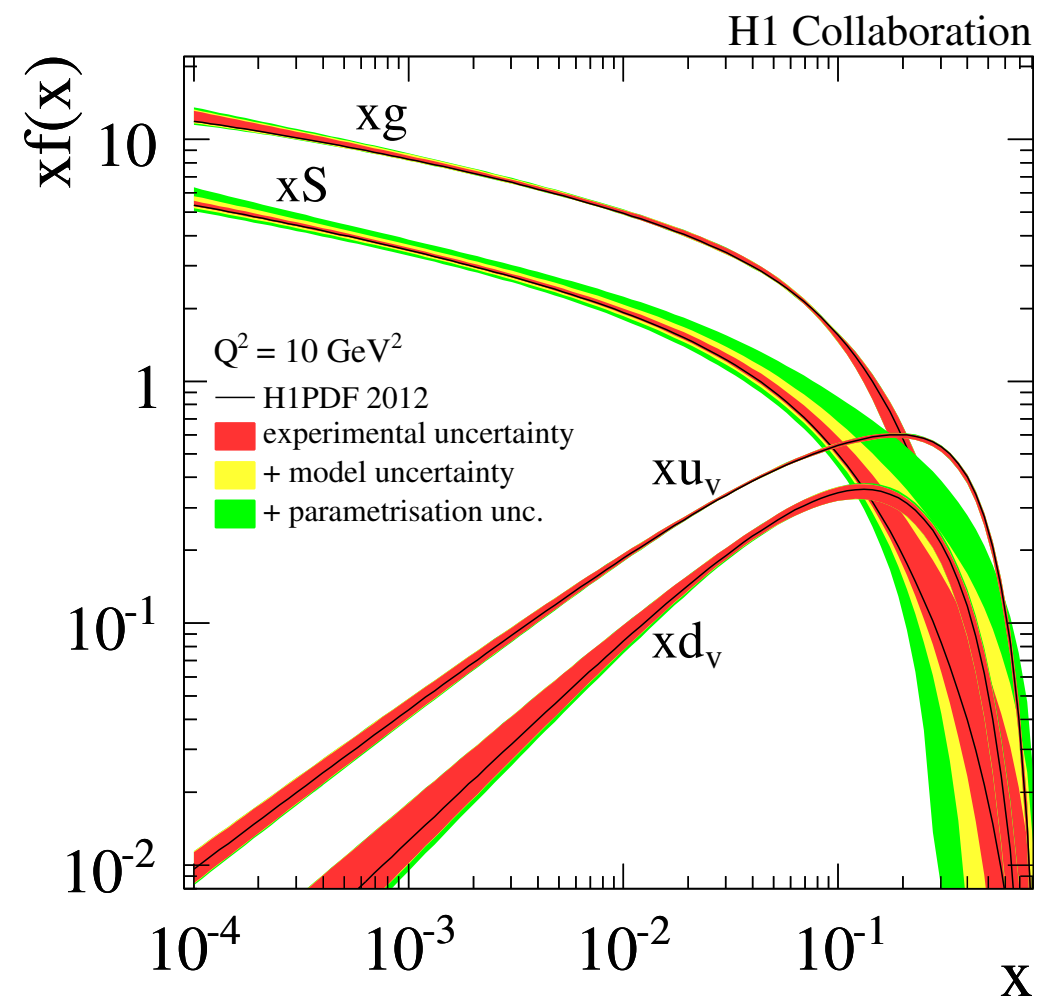
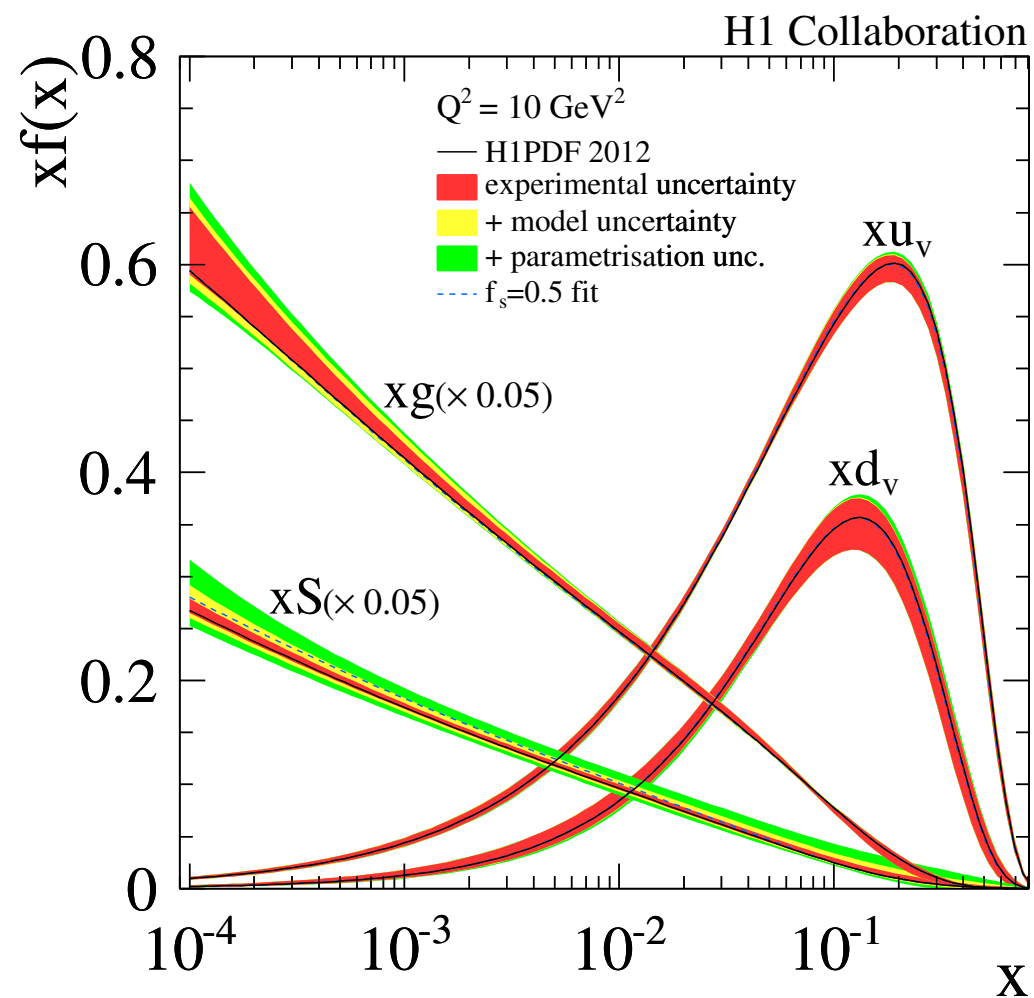
Parameterisation uncertainty determined from envelope of 14 parameter fit &  $Q_0^2$  variations

Error band is applied to central value fit  $\Rightarrow$  asymmetric errors since mean of replicas  $\neq$  central fit

$$\chi^2 = \sum_i \frac{\left[ \mu_i - m_i \left( 1 - \sum_j \gamma_j^i b_j \right) \right]^2}{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i \left( 1 - \sum_j \gamma_j^i b_j \right)} + \sum_j b_j^2 + \sum_i \ln \frac{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i}{\delta_{i,\text{unc}}^2 \mu_i^2 + \delta_{i,\text{stat}}^2 \mu_i^2}$$

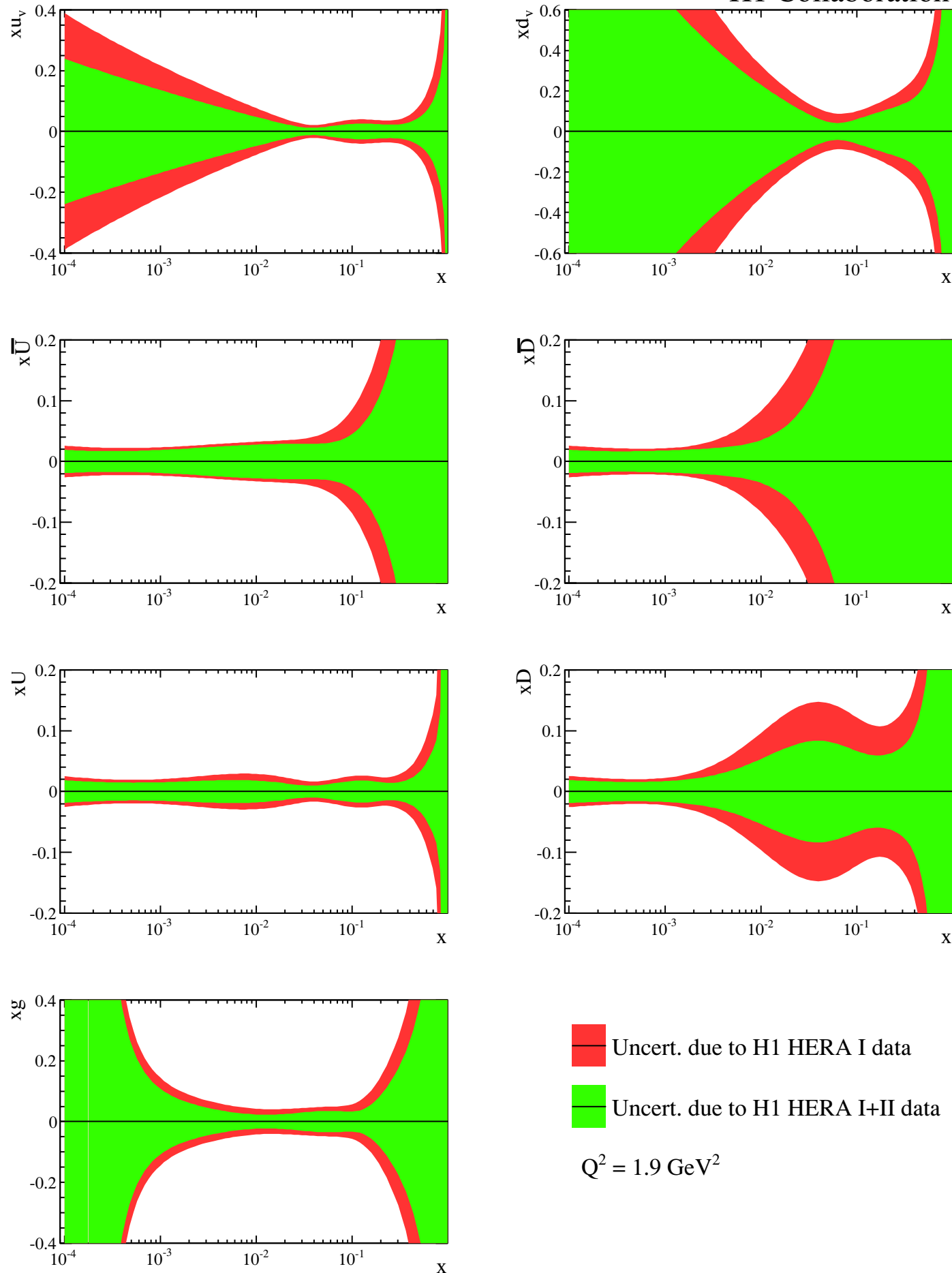
modified  $\chi^2$  definition includes  $\ln$  term to account for likelihood transition to  $\chi^2$  after error scaling





$$\chi^2/\text{ndf} = 1570/1461 = 1.07$$

Fit with unsuppressed strange sea ( $f_s=0.5$ ) is well within error bands



## HERAPDF1.0

Combine NC and CC HERA-I data from H1 & ZEUS

Complete MSbar NLO fit

NLO: standard parameterisation with 10 parameters

$\alpha_s = 0.1176$  (fixed in fit)

## HERAPDF1.5

Include additional NC and CC HERA-II data

Complete MSbar NLO and NNLO fit

NLO: standard parameterisation with 10 parameters

## HERAPDF1.5f

NNLO: extended fit with 14 parameters

## HERAPDF1.6

Include additional NC inclusive jet data  $5 < Q^2 < 15000$

Complete MSbar NLO fit

NLO: standard parameterisation with 14 parameters

$\alpha_s = 0.1202 \pm 0.0013$  (exp)  $\pm 0.004$  (scales) free in fit

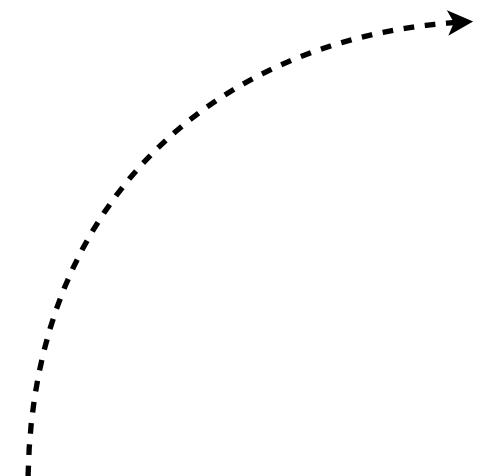
## HERAPDF1.7

Include 41 additional  $F_2^{\text{cc}}$  data  $4 < Q^2 < 1000$

Include 224 combined cross section points  $E_p=575/460$  GeV

Complete MSbar NLO fit

NLO: standard parameterisation with 14 parameters





### HERAPDF2.0

Include final:

HERA-I low/medium  $Q^2$  precision  $F_2$

HERA-II high  $Q^2$  polarised NC/CC data

HERA-II low/medium energy NC data

HERA-I+II  $F_2^{\text{cc}}$  combined data - almost ready

HERA-I+II multijet data - awaiting H1 publication

Combined  $F_2^{\text{cc}}$  now at 2<sup>nd</sup> stage of internal review

Expect journal submission ~ early Nov.

Final structure function measurements from H1 / ZEUS now published

Combination of the data is underway

New combination will include:

HERA-I published data

HERA-II published data

low/medium energy  $E_p=575/460$  GeV run data

Expect several fits:

NLO vs NNLO

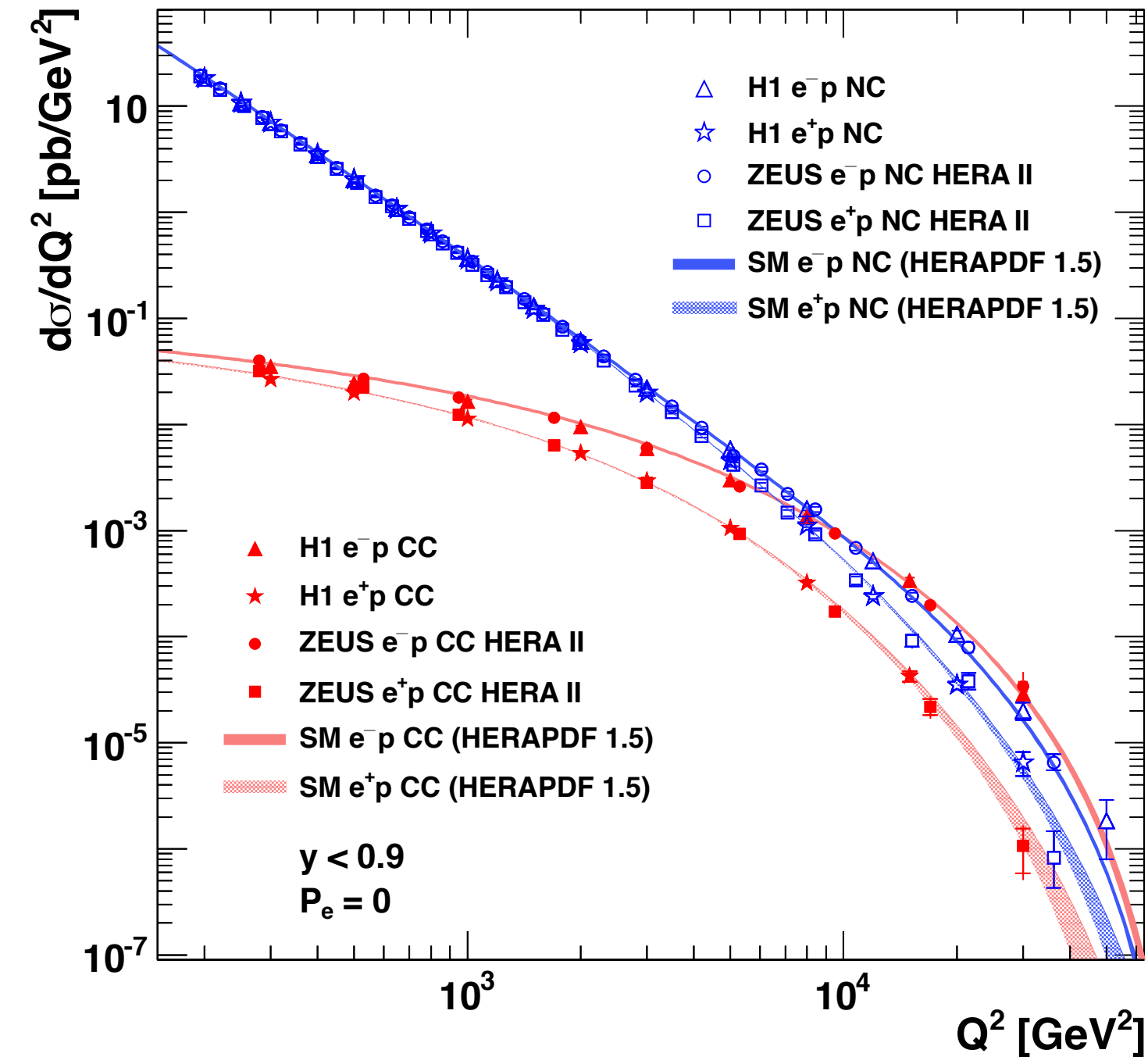
NLO will be: inclusive NC/CC data & inclusive +  $F_2^{\text{cc}}$  (+ jets?)

Include fit to  $\alpha_s$

MC method for experimental errors will be used

Timescale ~ spring 2013 (DIS workshop?)

## HERA



- H1 / ZEUS completed their final SF measurements
- New HERA-II data provide tighter constraints at high  $x / Q^2$
- These data provide some of the most stringent constraints on PDFs
- Stress-test of QCD over 4 orders of mag. in  $Q^2$
- DGLAP evolution works very well
- HERA data provide a self-consistent data set for complete flavour decomposition of the proton
- New combination of HERA data underway
- Combination  $\Rightarrow$  HERAPDF2.0 QCD fit





# H1 Systematic Error Source Correlation



| Data set                     | $\delta\mathcal{L}$   | $\delta E$                                 | $\delta\theta$ | $\delta h$       | $\delta N$   | $\delta B$   | $\delta V$   | $\delta S$   | $\delta\text{pol}$ |
|------------------------------|-----------------------|--|----------------|------------------|--------------|--------------|--------------|--------------|--------------------|
| $e^+$ Combined low $Q^2$     | $\delta\mathcal{L}^1$ |  |                |                  |              |              |              |              |                    |
| $e^+$ Combined low $E_p$     | $\delta\mathcal{L}^1$ |  |                |                  |              |              |              |              |                    |
| $e^+$ NC 94-97               | $\delta\mathcal{L}^1$ | $\delta\mathcal{L}^2$                      | $\delta E^1$   | $\delta\theta^1$ | $\delta h^1$ | $\delta N^1$ | $\delta B^1$ | —            | —                  |
| $e^+$ CC 94-97               | $\delta\mathcal{L}^1$ | $\delta\mathcal{L}^2$                      | —              | —                | $\delta h^1$ | $\delta N^1$ | $\delta B^1$ | $\delta V^1$ | —                  |
| $e^-$ NC 98-99               | $\delta\mathcal{L}^1$ | $\delta\mathcal{L}^3$                      | $\delta E^1$   | $\delta\theta^2$ | $\delta h^1$ | $\delta N^1$ | $\delta B^1$ | —            | —                  |
| $e^-$ NC 98-99 <i>high y</i> | $\delta\mathcal{L}^1$ | $\delta\mathcal{L}^3$                      | $\delta E^1$   | $\delta\theta^2$ | $\delta h^1$ | $\delta N^1$ | —            | —            | $\delta S^1$       |
| $e^-$ CC 98-99               | $\delta\mathcal{L}^1$ | $\delta\mathcal{L}^3$                      | —              | —                | $\delta h^1$ | $\delta N^1$ | $\delta B^1$ | $\delta V^2$ | —                  |
| $e^+$ NC 99-00               | $\delta\mathcal{L}^1$ | $\delta\mathcal{L}^4$                      | $\delta E^1$   | $\delta\theta^2$ | $\delta h^1$ | $\delta N^1$ | $\delta B^1$ | —            | $\delta S^1$       |
| $e^+$ CC 99-00               | $\delta\mathcal{L}^1$ | $\delta\mathcal{L}^4$                      | —              | —                | $\delta h^1$ | $\delta N^1$ | $\delta B^1$ | $\delta V^2$ | —                  |
| $e^+$ NC <i>high y</i>       | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^6, \delta\mathcal{L}^7$ | $\delta E^2$   | $\delta\theta^3$ | $\delta h^2$ | $\delta N^2$ | —            | —            | $\delta S^2$       |
| $e^-$ NC <i>high y</i>       | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^8, \delta\mathcal{L}^9$ | $\delta E^2$   | $\delta\theta^3$ | $\delta h^2$ | $\delta N^2$ | —            | —            | $\delta S^2$       |
| $e^+$ NC <i>L</i>            | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^6$                      | $\delta E^2$   | $\delta\theta^3$ | $\delta h^2$ | $\delta N^2$ | $\delta B^1$ | —            | $\delta P^1$       |
| $e^+$ CC <i>L</i>            | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^6$                      | —              | —                | $\delta h^2$ | $\delta N^3$ | $\delta B^1$ | $\delta V^3$ | $\delta P^1$       |
| $e^+$ NC <i>R</i>            | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^7$                      | $\delta E^2$   | $\delta\theta^3$ | $\delta h^2$ | $\delta N^2$ | $\delta B^1$ | —            | $\delta P^2$       |
| $e^+$ CC <i>R</i>            | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^7$                      | —              | —                | $\delta h^2$ | $\delta N^3$ | $\delta B^1$ | $\delta V^3$ | $\delta P^2$       |
| $e^-$ NC <i>L</i>            | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^8$                      | $\delta E^2$   | $\delta\theta^3$ | $\delta h^2$ | $\delta N^2$ | $\delta B^1$ | —            | $\delta P^3$       |
| $e^-$ CC <i>L</i>            | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^8$                      | —              | —                | $\delta h^2$ | $\delta N^3$ | $\delta B^1$ | $\delta V^3$ | $\delta P^3$       |
| $e^-$ NC <i>R</i>            | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^9$                      | $\delta E^2$   | $\delta\theta^3$ | $\delta h^2$ | $\delta N^2$ | $\delta B^1$ | —            | $\delta P^4$       |
| $e^-$ CC <i>R</i>            | $\delta\mathcal{L}^5$ | $\delta\mathcal{L}^9$                      | —              | —                | $\delta h^2$ | $\delta N^3$ | $\delta B^1$ | $\delta V^3$ | $\delta P^4$       |

correlation of H1 systematic error sources

$\delta\mathcal{L}^1 \rightarrow 0.5\%$  BH theoretical error  
HERA-I

$\delta\mathcal{L}^5 \rightarrow 2.3\%$  Compton lumi error  
HERA-II

$\delta\mathcal{L}^{6-9} \rightarrow 1.5\%$  Compton unc. error  
HERA-II

| Data Period              | Global<br>Normalisation | Per Period<br>Normalisation | Total<br>Normalisation |
|--------------------------|-------------------------|-----------------------------|------------------------|
| $e^+$ Combined low $Q^2$ | 0.993                   | —                           | 0.993                  |
| $e^+$ Combined low $E_p$ | 0.993                   | —                           | 0.993                  |
| HERA I $e^+$ 94-97       | 0.993                   | 0.999                       | 0.992                  |
| HERA I $e^-$ 98-99       | 0.993                   | 1.003                       | 0.996                  |
| HERA I $e^+$ 99-00       | 0.993                   | 1.005                       | 0.998                  |
| HERA II $e^+$ $L$        | 1.029                   | 0.991                       | 1.020                  |
| HERA II $e^+$ $R$        | 1.029                   | 1.013                       | 1.042                  |
| HERA II $e^-$ $L$        | 1.029                   | 1.010                       | 1.039                  |
| HERA II $e^-$ $R$        | 1.029                   | 1.014                       | 1.043                  |

normalisations from H1PDF 2012

Low  $Q^2$  data shifted by -0.7%  
HERA-I high  $Q^2$  by -0.3%  
HERA-II high  $Q^2$  by +2 to +4%

All shifts are <1.3 std.devs

HERAPDF1.0

Combine NC and CC HERA-I data from H1 & ZEUS  
 Complete MSbar NLO fit  
 NLO: standard parameterisation with 10 parameters  
 $\alpha_s = 0.1176$  (fixed in fit)

HERAPDF1.5

Include additional NC and CC HERA-II data  
 Complete MSbar NLO and NNLO fit  
 NLO: standard parameterisation with 10 parameters  
HERAPDF1.5f

NNLO: extended fit with 14 parameters

desy-09-158

H1-10-142 / ZEUS-prel-10-018

$$xf(x, Q_0^2) = A \cdot x^B \cdot (1-x)^C \cdot (1 + Dx + Ex^2)$$

|            |                   |                                  |                   |  |
|------------|-------------------|----------------------------------|-------------------|--|
| $xg$       |                   | $xg$                             |                   | $xg(x) = A_g x^{B_g} (1-x)^{C_g},$                                 |
| $xu_v$     |                   | $xU = xu + xc$                   |                   | $xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$ |
| $xd_v$     | $\longrightarrow$ | $xD = xd + xs$                   | $\longrightarrow$ | $xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$                   |
| $x\bar{U}$ |                   | $x\bar{U} = x\bar{u} + x\bar{c}$ |                   | $x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}},$   |
| $x\bar{D}$ |                   | $x\bar{D} = x\bar{d} + x\bar{s}$ |                   | $x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$   |

$x\bar{s} = f_s x\bar{D}$  strange sea is a fixed fraction  $f_s$  of  $\bar{D}$  at  $Q_0^2$

Apply momentum/counting sum rules:

$$\int_0^1 dx \cdot (xu_v + xd_v + x\bar{U} + x\bar{D} + xg) = 1$$

$$\int_0^1 dx \cdot u_v = 2 \quad \int_0^1 dx \cdot d_v = 1$$

Parameter constraints:

$$B_{uv} = B_{dv}$$

$$B_{Ubar} = B_{Dbar}$$

$$\text{sea} = 2 \times (Ubar + Dbar)$$

$$Ubar = Dbar \text{ at } x=0$$

$$Q_0^2 = 1.9 \text{ GeV}^2 \text{ (below } m_c)$$

$$Q^2 > 3.5 \text{ GeV}^2$$

$$2 \times 10^{-4} < x < 0.65$$

Fits performed using RT-VFNS



HERAPDF1.0 central values:

|            | <i>A</i> | <i>B</i> | <i>C</i> | <i>E</i> |
|------------|----------|----------|----------|----------|
| $xg$       | 6.8      | 0.22     | 9.0      | 9.7      |
| $xu_v$     | 3.7      | 0.67     | 4.7      |          |
| $xd_v$     | 2.2      | 0.67     | 4.3      |          |
| $x\bar{U}$ | 0.113    | -0.165   | 2.6      |          |
| $x\bar{D}$ | 0.163    | -0.165   | 2.4      |          |

$$\chi^2/\text{ndf} = 574/582$$

Experimental systematic sources of uncertainty allowed to float in fit  
Include model assumptions into uncertainty:

$f_s$ ,  $m_c$ ,  $m_b$ ,  $Q_0^2$ ,  $Q_{min}^2$

| Variation                       | Standard Value | Lower Limit         | Upper Limit          |
|---------------------------------|----------------|---------------------|----------------------|
| $f_s$                           | 0.31           | 0.23                | 0.38                 |
| $m_c$ [GeV]                     | 1.4            | 1.35 <sup>(a)</sup> | 1.65                 |
| $m_b$ [GeV]                     | 4.75           | 4.3                 | 5.0                  |
| $Q_{min}^2$ [GeV <sup>2</sup> ] | 3.5            | 2.5                 | 5.0                  |
| $Q_0^2$ [GeV <sup>2</sup> ]     | 1.9            | 1.5 <sup>(b)</sup>  | 2.5 <sup>(c,d)</sup> |

<sup>(a)</sup> $Q_0^2 = 1.8$

<sup>(c)</sup> $m_c = 1.6$

<sup>(b)</sup> $f_s = 0.29$

<sup>(d)</sup> $f_s = 0.34$

Excellent consistency of input data allow standard statistical error definition:

$$\Delta\chi^2 = 1$$

Exclusive jet data required for free  $\alpha_s$  fit  
See talk of Krzysztof Nowak

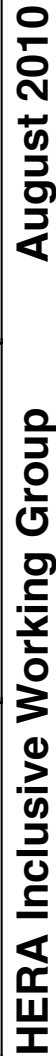
In 14 parameter fit:

release  $B_{uv} = B_{dv}$  constraint

allow more flexible gluon

$$xg(x, Q_0^2) = A \cdot x^B \cdot (1-x)^C - A' \cdot x^{B'} \cdot (1-x)^{25}$$

allows for valence-like or negative gluon at  $Q_0^2$



Spread of LHC Z/W production predictions is reduced  $\sim 4.5\% \rightarrow \sim 0.7\%$  when using optimal value of  $m_c$

|                     |                      |                     |                              |
|---------------------|----------------------|---------------------|------------------------------|
| ZEUS inclusive jets | 39 pb <sup>-1</sup>  | $Q^2 > 125$         | Nucl. Phys. B765 (2007) 1-30 |
| ZEUS inclusive jets | 82 pb <sup>-1</sup>  | $Q^2 > 125$         | Phys. Lett. B649 (2007) 12   |
| H1 inclusive jets   | 395 pb <sup>-1</sup> | $150 < Q^2 < 15000$ | EPJ C65 (2010) 363-383       |
| H1 inclusive jets   | 44 pb <sup>-1</sup>  | $5 < Q^2 < 100$     | EPJ C67 (2010) 1-24          |

Jet data bring significant sensitivity to  $\alpha_s$   
Disentangles correlation between  $xg(x, Q^2)$  and  $\alpha_s$

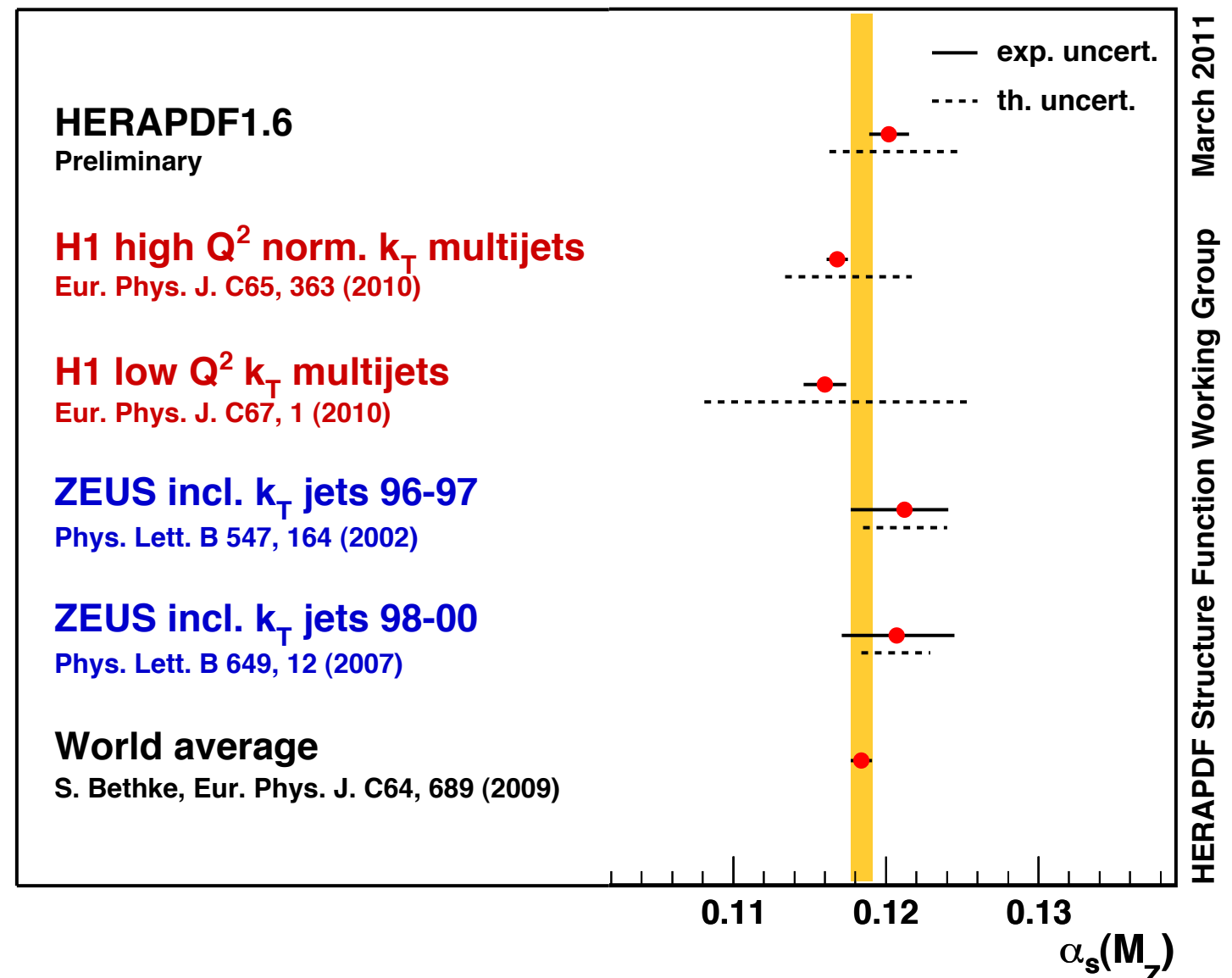
HERAPDF1.6 : Simultaneous NLO QCD fit to

- combined NC inclusive cross section data
- combined CC inclusive cross sections data
- normalised H1/ZEUS inclusive jet data

$$\alpha_s(M_Z) = 0.1202 \pm 0.0013 \text{ (exp)} \\ \pm 0.0007 \text{ (model)} \\ \pm 0.0012 \text{ (hadronisation)} \\ +0.0045 \\ -0.0036 \text{ (scales)}$$

Only combined PDF /  $\alpha_s$  fit on the market

## H1 and ZEUS (prel.)



# High $Q^2$ NC Multi-jets



H1prelim-II-032

New H1 measurement of inclusive, dijet and trijet rates

First measurement of double diff'l trijet cross section

Significantly reduced systematic errors

1% hadronic scale uncertainty

For now - unnormalised cross sections...

Jets in Breit frame:  $5 < P_T < 50$  GeV

$M_{12} > 16$  GeV

Greater sensitivity to  $\alpha_s$  with more jets

High  $Q^2$  and large jet  $P_T \Rightarrow$  multi-scale QCD problem

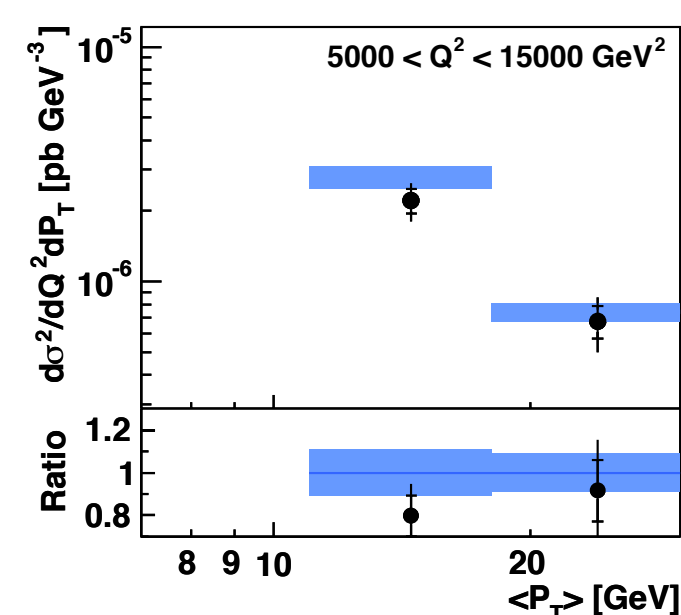
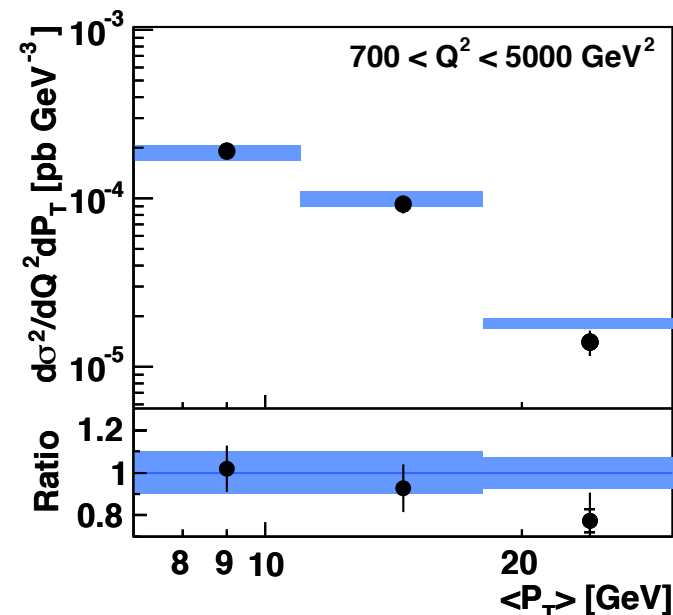
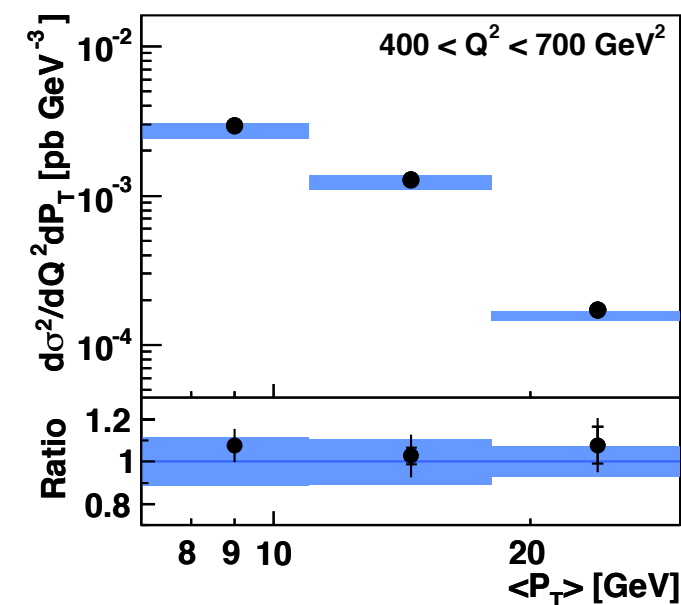
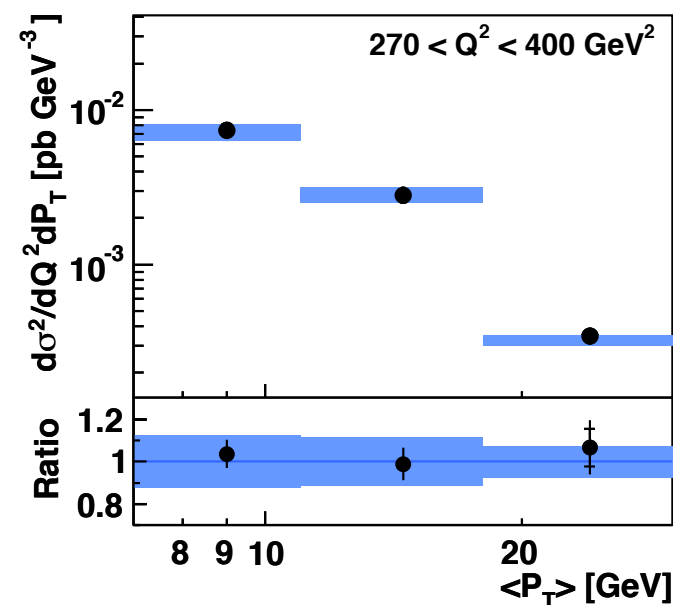
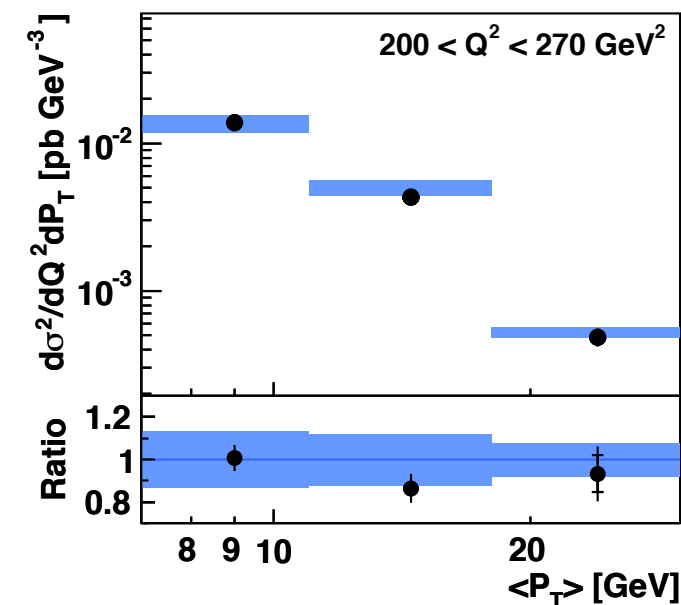
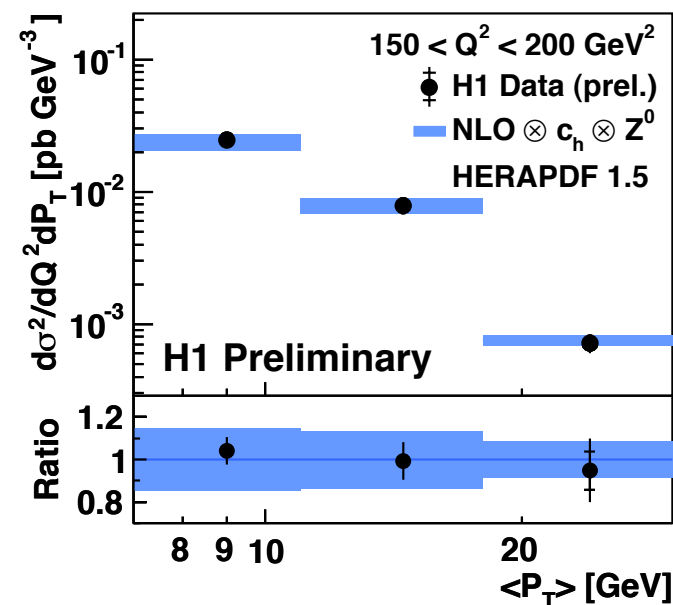
Good description in NLO

(worse for di-jets at low  $\langle P_T \rangle$  ...)

$$\text{NLO calculation } \mu_R = \mu_F = \sqrt{\frac{1}{2}(Q^2 + P_T^2)}$$

scales varied by factors of 2 for uncertainty

## Trijet Cross Section





# High $Q^2$ NC Multi-jets

H1prelim-II-032

Di-jet rates in reasonable agreement

~10% discrepancy at low  $\langle P_T \rangle$

Data want smaller  $\alpha_s$  or smaller  $x_g$  ?

Extract  $\alpha_s$  independently for each jet data set in NLO  
PDF uncertainty from CT10 error propagation

**Inclusive jets:**

$$\alpha_s(M_Z) = 0.1190 \pm 0.0021(\text{exp.}) \pm 0.0020(\text{pdf})^{+0.0050}_{-0.0056}(\text{th.})$$

**Dijets:**

$$\alpha_s(M_Z) = 0.1146 \pm 0.0022(\text{exp.}) \pm 0.0021(\text{pdf})^{+0.0044}_{-0.0045}(\text{th.})$$

**Trijets:**

$$\alpha_s(M_Z) = 0.1196 \pm 0.0016(\text{exp.}) \pm 0.0010(\text{pdf})^{+0.0055}_{-0.0039}(\text{th.})$$

Achieved ~1% experimental precision on  $\alpha_s$   
Theoretical uncertainty (scales) dominate ~4%  
PDF uncertainty ~1%

To come:

Use of normalised cross sections  
cancellation of systematic uncertainties  
→ reduced error for  $\alpha_s$

## Dijet Cross Section

