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Flavour Predictions from SUSY GUTs with Family Symmetry

Steve King, UK Flavour 2013, Durham

The Standard Model



Standard Model Puzzles

1. The origin of mass - the origin of the weak scale, its stability under radiative corrections, and the solution to the hierarchy problem

2. The quest for unification - the question of whether the three known forces of the standard model may be related into a grand unified theory, and whether such a theory could also include a unification with gravity.

3. The problem of flavour - the problem of the undetermined fermion masses and mixing angles (including neutrino masses and mixing angles) together with the CP violating phases, in conjunction with the observed smallness of flavour changing neutral currents and very small strong CP violation.





Relative contributions to ΔM_H^2 for $\Lambda = 5$ TeV





Complementarity of direct and indirect searches for new physics

Generic amplitude for flavor process



Here's the problem Masíero $M(B_{d}-\overline{B}_{d}) \sim c_{SM} \frac{(v_{t} V_{tb}^{*} V_{td})^{2}}{16 \pi^{2} M_{W}^{2}} + c_{new} \frac{1}{\Lambda^{2}}$ If $c_{new} \sim c_{SM} \sim 1$ Isidori $\Lambda > 10^4 \,\text{TeV}$ for $O^{(6)} \sim (\bar{s} \,d)^2$ $\Lambda > 10^3 \text{ TeV} \text{ for } O^{(6)} \sim (\overline{b} d)^2$ [$K^0-\overline{K}^0$ mixing] $[B^0-\overline{B^0} \text{ mixing }]$

UV SM COMPLETION TO STABILIZE THE ELW. SYMM. BREAKING: $\Lambda_{UV} \sim O(1 \text{ TeV})$

**2. EFT analysis of
$$\Delta F=2$$
 transitions** Silvestrivi,
Form
The mixing amplitudes $A_q e^{2i \Phi_q} = \langle \overline{M}_q | H_{eff}^{\Delta F=2} | M_q \rangle$
 $H_{eff}^{\Delta B=2} = \sum_{i=1}^{5} C_i(\mu) Q_i(\mu) + \sum_{i=1}^{3} \widetilde{C}_i(\mu) \widetilde{Q}_i(\mu)$
 $Q_1 = \overline{q}_L^{\alpha} \gamma_{\mu} b_L^{\alpha} \overline{q}_L^{\beta} \gamma^{\mu} b_L^{\beta}$ (SM/MFV)
 $Q_2 = \overline{q}_R^{\alpha} b_L^{\alpha} \overline{q}_R^{\beta} b_L^{\beta}$ $Q_3 = \overline{q}_R^{\alpha} b_L^{\beta} \overline{q}_R^{\beta} b_L^{\beta}$
 $Q_4 = \overline{q}_R^{\alpha} b_L^{\alpha} \overline{q}_R^{\beta} b_R^{\beta}$ $Q_5 = \overline{q}_R^{\alpha} b_L^{\beta} \overline{q}_L^{\beta} b_R^{\beta}$
 $\widetilde{Q}_2 = \overline{q}_L^{\alpha} b_R^{\alpha} \overline{q}_R^{\beta} b_R^{\beta}$ $\widetilde{Q}_3 = \overline{q}_L^{\alpha} b_R^{\beta} \overline{q}_L^{\beta} b_R^{\beta}$
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7 new operators beyond MFV involving
quarks with different chiralities



Take SUSY as an example



SUSY particles





The down squark mass matrix

In the diagonal down quark basis (Super CKM basis)

* * * * * * * * * * * * * * *



A diagonal matrix corresponds to "minimal flavour violation" we say that SUSY is "flavour blind" (FBMSSM) Constrain off-diagonal elements from rare/FC processes $(\delta_{ij}^d)_{LL} = \frac{(\Delta_{ij}^d)_{LL}}{m_{\tilde{d}_{iL}}m_{\tilde{d}_{jL}}} \qquad (\delta_{ij}^d)_{RR} = \frac{(\Delta_{ij}^d)_{RR}}{m_{\tilde{d}_{iR}}m_{\tilde{d}_{jR}}} \qquad (\delta_{ij}^d)_{LR} = \frac{(\Delta_{ij}^d)_{LR}}{m_{\tilde{d}_{iL}}m_{\tilde{d}_{jR}}}$

Mass insertion approximation







SUSY 2013 Trieste

L. Silvestrini





SUSY 2013 Trieste

L. Silvestrini

Why are the off-diagonal squark masses so small?

- Maybe not small just very heavy squarks (especially first and second family)
- Some alignment mechanism as in GMSB or AMSB
- msugra? But not well motivated...
- In general SUGRA need a theory of flavour to understand this - involving a family symmetry

Horizontal

The Flavour Problem Why are there three families of quarks and leptons?



Vertical

The Flavour Problem Why is quark mixing so small?

Cabíbbo Kobayashí Maskawa

 V_{ij} u_{iL} u_{iL} u_{iL}

 $V_{CKM} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$

 $\theta_{12} = 13^{\circ} \pm 0.1^{\circ}$ $\theta_{23} = 2.4^{\circ} \pm 0.1^{\circ}$ $\theta_{13} = 0.20^{\circ} \pm 0.05^{\circ}$

All these angles are pretty small – why? While the CP phase is quite large

 $\delta_{ ext{CP}} \approx$ 70° \pm 5°

The Flavour Problem Why is lepton mixing so large?



Family Symmetry

E.g. SU(3) gauged famíly symmetry c.f. QCD quark colours

t st family 2nd family (green) (blue) t t

зrd famíly (red)



The SUSY CP ProblemAbel, Khalil, Lebedev;
Ross, Vives;
Antusch, SFK, Malinsky, Ross• SUSY neutron EDM
$$d_n \sim \left(\frac{300 \text{ GeV}}{M}\right)^2 \sin \phi \times 10^{-24} e \text{ cm}$$

 $\phi_\mu \sim \phi_A \equiv \phi \ll 1, \tan \beta \sim 3 \rightarrow \phi < 10^{-2}$ Why are SUSY
phases so
small?

• Postulate CP conservation (e.g. $\mu H_u H_d$ real) with CP is spontaneously broken by flavon vevs

• Trilinear soft

$$\tilde{A}_{ij} = A_0 \left(a_3 \frac{\phi_3^i \phi_3^j}{M^2} + a_{23} \frac{\phi_{23}^i \phi_{23}^j}{M^2} + \dots \right)$$

 A_0 , a_3 , a_{23} , real gives real soft masses times complex Yukawa elements \rightarrow no soft phases at leading order

Antusch, SK, Malínsky (AKM) Predictions

rad (CKIVIIIIIer)

0.0015





Antusch, SK, Malínsky (AKM) Predictions







Data greatly constrains these models

Straub 1107.0266



SUSY GUTS $m_Q^2 = m_{\tilde{e}c}^2 = m_{\tilde{u}c}^2 = m_{10}^2$ $m_{\tilde{d}c}^2 = m_L^2 = m_{\overline{5}}^2$ $A_{ij}^e = A_{ji}^d.$ $(\Delta_{ij}^u)_{\text{LL}} = (\Delta_{ij}^u)_{\text{RR}} = (\Delta_{ij}^d)_{\text{LL}} = (\Delta_{ij}^l)_{\text{RR}}$ $(\Delta_{ij}^d)_{\text{RR}} = (\Delta_{ij}^l)_{\text{LR}} = (\Delta_{ij}^l)_{\text{LL}}$

Relations at the weak scale	Relations at $M_{\rm GUT}$
$(\delta^u_{ij})_{\mathrm{RR}} \approx (m^2_{e^c}/m^2_{u^c}) \; (\delta^l_{ij})_{\mathrm{RR}}$	$m^2_{u^c_0} = m^2_{e^c_0}$
$(\delta^q_{ij})_{\mathrm{LL}} \approx (m_{e^c}^2/m_Q^2) \ (\delta^l_{ij})_{\mathrm{RR}}$	$m^2_{Q_0} = m^2_{e^c_0}$
$(\delta^d_{ij})_{\mathrm{RR}} \approx (m_L^2/m_{d^c}^2) \; (\delta^l_{ij})_{\mathrm{LL}}$	$m^2_{d^c_0} = m^2_{L_0}$
$(\delta_{ij}^d)_{\rm LR} \approx (m_{L_{avg}}^2/m_{Q_{avg}}^2) (m_b/m_\tau) (\delta_{ij}^l)_{\rm LR}^{\star}$	$A^e_{ij_0} = A^d_{ji_0}$



u^c -u^c u d u^c u d : u d e^c



Ciuchini,Masiero, Paradisi,Silvestrini, Vempati,Vives

Quark-lepton connection: LFV processes can constrain Quark Flavour Violation via GUTs





 $S_4 \times SU(5) \times U(1)$

Hagedorn, SK, Luhn + work in progress with Dimou

	-	Matte	r field	ls	Higgs fields			Flavon fields								
	$\overline{T_3}$	Т	F	ν ^c	H_5	$H_{\overline{5}}$	$H_{\overline{45}}$	$\overline{\phi^u_2}$	$\widetilde{\phi}_2^{\scriptscriptstyle u}$	ϕ_3^d	$\widetilde{\phi}^d_{3}$	ϕ^d_2	$\phi^{\nu}_{3'}$	$\phi_2^{ u}$	$\phi_1^{ u}$	_η
$ \frac{SU(5)}{S_4} \\ U(1) $	10 1 0	10 2 5	5 3 4	1 3 -4	5 1 0	5 1 0	45 1 1	1 2 -10	1 2 0	1 3 -4	1 3 -11	1 2 1	1 3' 8	1 2 8	1 1 8	1 1 7
Yukav couplin	va .gs ^y	$Y^u =$	$\begin{pmatrix} y_1^u, \\ 0\\ 0 \end{pmatrix}$	$egin{array}{ccc} \lambda^8 & 0 \ & y_2^u\lambda \ & 0 \ & 0 \end{array}$	$\begin{pmatrix} 0 \\ 4 & 0 \\ y_3^u \end{pmatrix}$,			$\frac{A^u}{A_0} =$	$=\left(\begin{array}{c}a_{1}^{\iota}\\ \end{array}\right)$	$egin{array}{ccc} a^k\lambda^8 & 0 \ 0 & a^u_2\lambda \ 0 & 0 \end{array}$	$\begin{pmatrix} 0 \\ 4 & 0 \\ a_3^u \end{pmatrix}$,	Soft S break trílív	sus ríng nears	Y
Y	$Y^{d} = \begin{pmatrix} 0 & y_{3}^{d}\lambda^{5} & -y_{3}^{d}\lambda^{5} \\ -y_{3}^{d}\lambda^{5} & y_{1}^{d}\lambda^{4} & (y_{3}^{d} - yd_{1})\lambda^{4} \\ 0 & 0 & y_{2}^{d}\lambda^{2} \end{pmatrix},$							$\frac{A^d}{A_0} = \begin{pmatrix} 0 & a_3^d \lambda^5 & -a_3^d \lambda^5 \\ -a_3^d \lambda^5 & a_1^d \lambda^4 & (a_3^d - a_1^d) \lambda^4 \\ 0 & 0 & a_2^d \lambda^2 \end{pmatrix}$								
У	$Y^{e} = \begin{pmatrix} 0 & -y_{3}^{e}\lambda^{5} & 0\\ y_{3}^{e}\lambda^{5} & -3y_{1}^{e}\lambda^{4} & 0\\ -y_{3}^{e}\lambda^{5} & (3y_{1}^{e} + y_{3}^{e})\lambda^{4} & y_{2}^{e}\lambda^{2} \end{pmatrix},$							$\frac{A^e}{A_0} =$	= (a 	$egin{array}{c} 0 \ a_3^e\lambda^5 \ a_3^e\lambda^5 \end{array}$	$-a_{3}^{e} \lambda$ $-3a_{1}^{e} \lambda$ $(3a_{1}^{e} + a)$	$\lambda^5 \ \lambda^4 \ a_3^e) \lambda^4 \ a_3^e$	$\begin{pmatrix} 0\\ 0\\ a_2^e\lambda^2 \end{pmatrix}$,		

Squark and slepton mass matrices (at M_{GUT} in <u>non-diagonal</u> Yukawa basis)

$$M_F^2 \sim m_0^2 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + m_0^2 \begin{pmatrix} \lambda^4 & \lambda^4 & \lambda^4 \\ \lambda^4 & \lambda^4 & \lambda^4 \\ \lambda^4 & \lambda^4 & \lambda^4 \end{pmatrix}$$

$$M_T^2 \sim m_0^2 \begin{pmatrix} a & 0 & 0 \\ 0 & a & 0 \\ 0 & 0 & b \end{pmatrix} + m_0^2 \begin{pmatrix} \lambda^2 & \lambda^4 & \lambda^7 \\ \lambda^4 & \lambda^2 & \lambda^5 \\ \lambda^7 & \lambda^5 & 0 \end{pmatrix}$$

Model predicts very small off-diagonal masses with non-universal stop squark masses

Mass insertion parameters (at M_{GUT} in the <u>diagonal</u> Yukawa basis) $(\delta^u)_{LL} = \begin{pmatrix} 1 \ \lambda^4 \ \lambda^7 \\ \cdot \ 1 \ \lambda^5 \\ \cdot \ \cdot \ 1 \end{pmatrix}, \quad (\delta^u)_{RR} = \begin{pmatrix} 1 \ \lambda^4 \ \lambda^7 \\ \cdot \ 1 \ \lambda^5 \\ \cdot \ \cdot \ 1 \end{pmatrix}, \quad (\delta^u)_{LR} = \begin{pmatrix} \lambda^8 \ 0 \ 0 \\ 0 \ \lambda^4 \ 0 \\ 0 \ 0 \ 1 \end{pmatrix}$ $(\delta^d)_{LL} = \begin{pmatrix} 1 \ \lambda^3 \ \lambda^4 \\ \cdot \ 1 \ \lambda^2 \\ \cdot \ \cdot \ 1 \end{pmatrix}, \quad (\delta^d)_{RR} = \begin{pmatrix} 1 \ \lambda^4 \ \lambda^4 \\ \cdot \ 1 \ \lambda^6 \\ \cdot \ \cdot \ 1 \end{pmatrix}, \quad (\delta^d)_{LR} = \begin{pmatrix} \lambda^6 \ \lambda^5 \ \lambda^5 \\ \lambda^5 \ \lambda^4 \ \lambda^4 \\ \lambda^7 \ \lambda^6 \ \lambda^2 \end{pmatrix}$ $(\delta^e)_{LL} = \begin{pmatrix} 1 \ \lambda^4 \ \lambda^4 \\ \cdot \ 1 \ \lambda^6 \\ \cdot \ \cdot \ 1 \end{pmatrix}, \quad (\delta^e)_{RR} = \begin{pmatrix} 1 \ \lambda^3 \ \lambda^4 \\ \cdot \ 1 \ \lambda^2 \\ \cdot \ \cdot \ 1 \end{pmatrix}, \quad (\delta^e)_{LR} = \begin{pmatrix} \lambda^6 \ \lambda^5 \ \lambda^7 \\ \lambda^5 \ \lambda^4 \ \lambda^6 \\ \lambda^5 \ \lambda^4 \ \lambda^2 \end{pmatrix}$ Model predicts very small mass insertion parameters close to the MFV limit

- No evidence for NP, but SM puzzles remain: origin of mass, quest for unification, problem of flavour
- Higgs mass stabilization requires NP at ~ 1 TeV (current LHC limit)
- □ How do we reconcile this with general flavour analyses limits of ~100 TeV?
- We have focussed on SUSY where strong constraints may be derived on the off-diagonal squark masses in the diagonal quark basis
- Sínce SUSY particles appear in loops (R-parity) the constraints are not quite so strong but still require small mass insertion parameters
- SUSY models with family symmetry which describe fermion masses and mixings naturally have small off-diagonal squark masses
- □ IN SU(5) GUTS off-diagonal squark and slepton masses may be related
- In S₄ discrete family symmetry with SU(5) GUTS we find small mass insertion parameters close to the MFV case, allowing TeV scale NP