

# Some Thoughts About Rare Kaon Decays

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# Theoretical Expectations

- Clearly an oxymoron, because every theorist expects different TeV-scale new physics
  - motivated by naturalness of electroweak scale
  - motivated by precision unification of couplings
  - not motivated, but why not
  - based on her/his personal taste(s) or prejudice(s)



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- Experiments should try to falsify theories - especially true for indirect (as opposed to production) probes!
- Imagine to kill supersymmetry, extra dimensions & technicolor at once by signal defying expectations



# Two Ways to Study New Physics



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Top-down approach:

- concrete model of new physics
- predict observables & correlations directly
- are smoking gun signals possible?

⇒ discussed only sporadically



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## Bottom-up approach:

- what data can be obtained?
- how is it parametrized efficiently?
- what can be learned about model classes?

⇒ main theme of this talk



# Bottom-Up Approach

- Fix minimal set of assumptions:
  - new physics enters at  $M_{\text{NP}} = O(1 \text{ TeV})$ , allowing for systematic expansion in powers of  $M_W/M_{\text{NP}} \ll 1$
  - standard model (SM) is weakly coupled to new sector (technical assumption could be relaxed)

Assumptions satisfied in many SM extensions



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Assumptions satisfied in many SM extensions

- Use effective  $SU(2)_L \times U(1)_Y$  invariant Lagrangian

$$\mathcal{L}_{\text{eff}} = \sum_i C_i Q_i$$

Similar to weak Hamiltonian with simple matching between two, but fewer operators per coefficient



# Bottom-Up Approach Cont'd

- Effective framework takes care of assumptions, but no further prejudice



# Bottom-Up Approach Cont'd

- Effective framework takes care of assumptions, but no further prejudice
- In setup can now ask & answer important questions:
  - to what degree are  $K \rightarrow \pi \nu \bar{\nu}$  channels linked to other kaon modes, such as  $K_L \rightarrow \pi^0 l^+ l^-$ ,  $\Delta M_K$ ,  $\epsilon_K$  &  $\epsilon'/\epsilon$ ?
  - in particular, do these constraints rule out large effects in neutrino modes?
  - can one design models that break correlations & if so, does this lead to other observable signatures?
  - ...



# Kaon Scoresheet

Operator		Observable					$P_T(K^+ \rightarrow \pi^0 \mu^+ \nu)$	$\Delta_{\text{CKM}}$	$\epsilon'/\epsilon$	$\epsilon_K$	in MSSM?
		$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	$K_L \rightarrow \pi^0 \nu \bar{\nu}$	$K_L \rightarrow \pi^0 l^+ l^-$	$K_L \rightarrow l^+ l^-$	$K^+ \rightarrow l^+ \nu$					
$Q_{lq}^{(1)}$	$(\bar{D}_L \gamma_\mu S_L)(\bar{L}_L \gamma^\mu L_L)$	✓	✓	✓	hs	—	—	—	—	—	✓
$Q_{lq}^{(3)}$	$(\bar{D}_L \gamma_\mu \sigma^i S_L)(\bar{L}_L \gamma^\mu \sigma^i L_L)$	✓	✓	✓	hs	hs	✓	✓	—	—	✓
$Q_{qe}$	$(\bar{D}_L \gamma_\mu S_L)(\bar{l}_R \gamma^\mu l_R)$	—	—	✓	hs	hs	✓	✓	—	—	small
$Q_{ld}$	$(\bar{d}_R \gamma_\mu s_R)(\bar{L}_L \gamma^\mu L_L)$	✓	✓	✓	hs	—	—	—	—	—	small
$Q_{ed}$	$(\bar{d}_R \gamma_\mu s_R)(\bar{l}_R \gamma^\mu l_R)$	—	—	✓	hs	—	—	—	—	—	small
$Q_{lq}^\dagger$	$(\bar{u}_R S_L)(\bar{l}_R L_L)$	—	—	—	—	✓	✓	✓	—	—	tiny
$(Q_{lq}^t)^\dagger$	$(\bar{u}_R \sigma_{\mu\nu} S_L)(\bar{l}_R \sigma^{\mu\nu} L_L)$	—	—	—	—	—	?	?	—	—	tiny
$Q_{qde}$	$(\bar{d}_R S_L)(\bar{L}_L l_R)$	—	—	✓	✓	—	—	—	—	—	tiny
$Q_{qde}^\dagger$	$(\bar{D}_L s_R)(\bar{l}_R L_L)$	—	—	✓	✓	✓	✓	✓	—	—	large $\tan \beta$
$Q_{\phi q}^{(1)}$	$(\bar{D}_L \gamma_\mu S_L)(\phi^\dagger D^\mu \phi)$	✓	✓	✓	hs	—	—	—	✓	(✓)	✓
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$Q_{\phi d}$	$(\bar{d}_R \gamma_\mu s_R)(\phi^\dagger D^\mu \phi)$	✓	✓	✓	hs	—	—	—	✓	(✓)	large $\tan \beta$ (non-MFV)

[see S. Jäger, talk at NA62 Physics Handbook Workshop]



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6 operators, 6 observables

[see S. Jäger, talk at NA62 Physics Handbook Workshop]

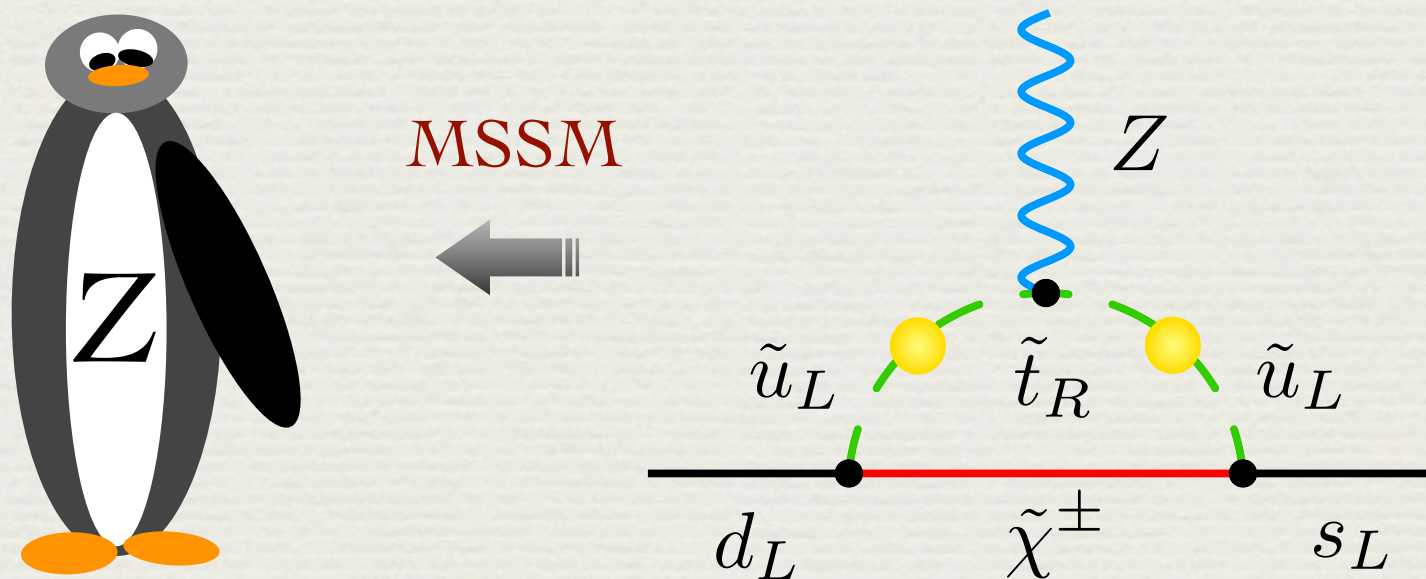


# Z-Penguin Operators

- Three operators involving Higgs field affect largest number of observables, so let's focus on them
- After electroweak symmetry breaking, one has

$$(\bar{D}_L \gamma_\mu S_L)(\phi^\dagger D^\mu \phi) \implies \bar{d}_L \gamma_\mu s_L Z^\mu + \bar{u}_L \gamma_\mu c_L Z^\mu + \dots$$

which is left-handed (LH) Z-penguin well-known from MSSM, Randall-Sundrum (RS) models, ...



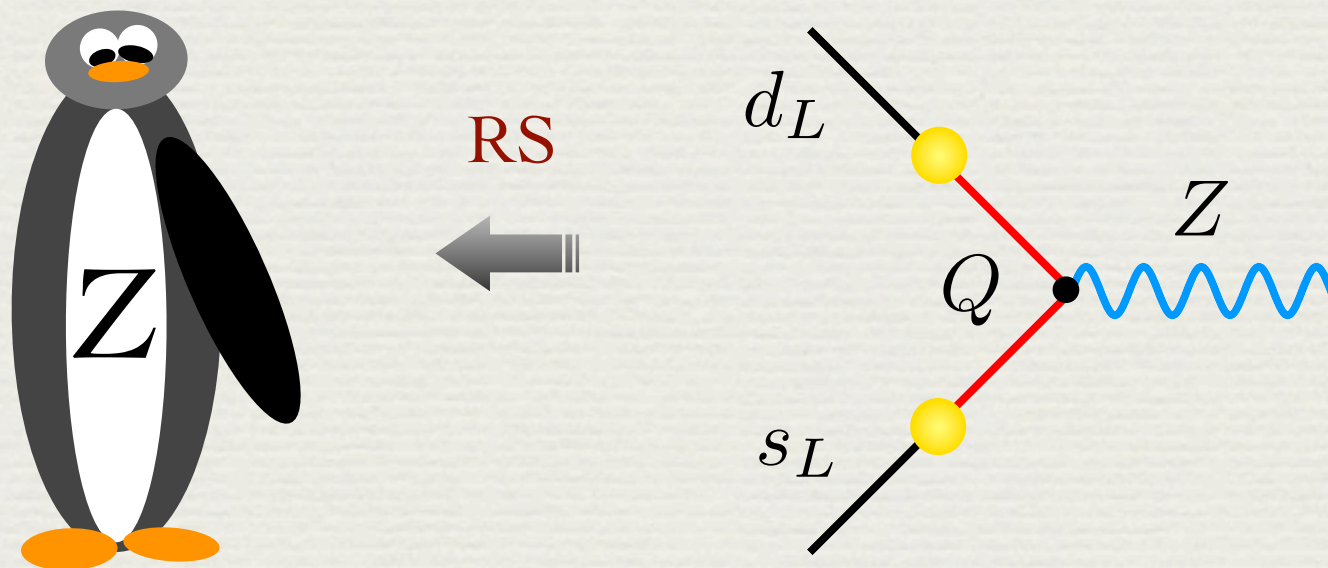


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- Similarly, there is right-handed (RH) Z-penguin

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- Parametrize flavor-changing Z-boson vertices by

$$(V_{ts}^* V_{td} C_{\text{SM}} + C_{\text{NP}}) \bar{d}_L \gamma_\mu s_L Z^\mu + \tilde{C}_{\text{NP}} \bar{d}_R \gamma_\mu s_R Z^\mu$$

where  $V_{ij}$  are Cabibbo-Kobayashi-Maskawa (CKM) elements &  $C_{\text{SM}} \approx 0.8$  is value of Inami-Lim function characterizing LH Z-penguin in SM



# Anatomy of Neutrino Modes

- After summation over neutrino flavors, branching ratios of  $K \rightarrow \pi \nu \bar{\nu}$  channels can be written as

$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \propto (\text{Im } X)^2$$

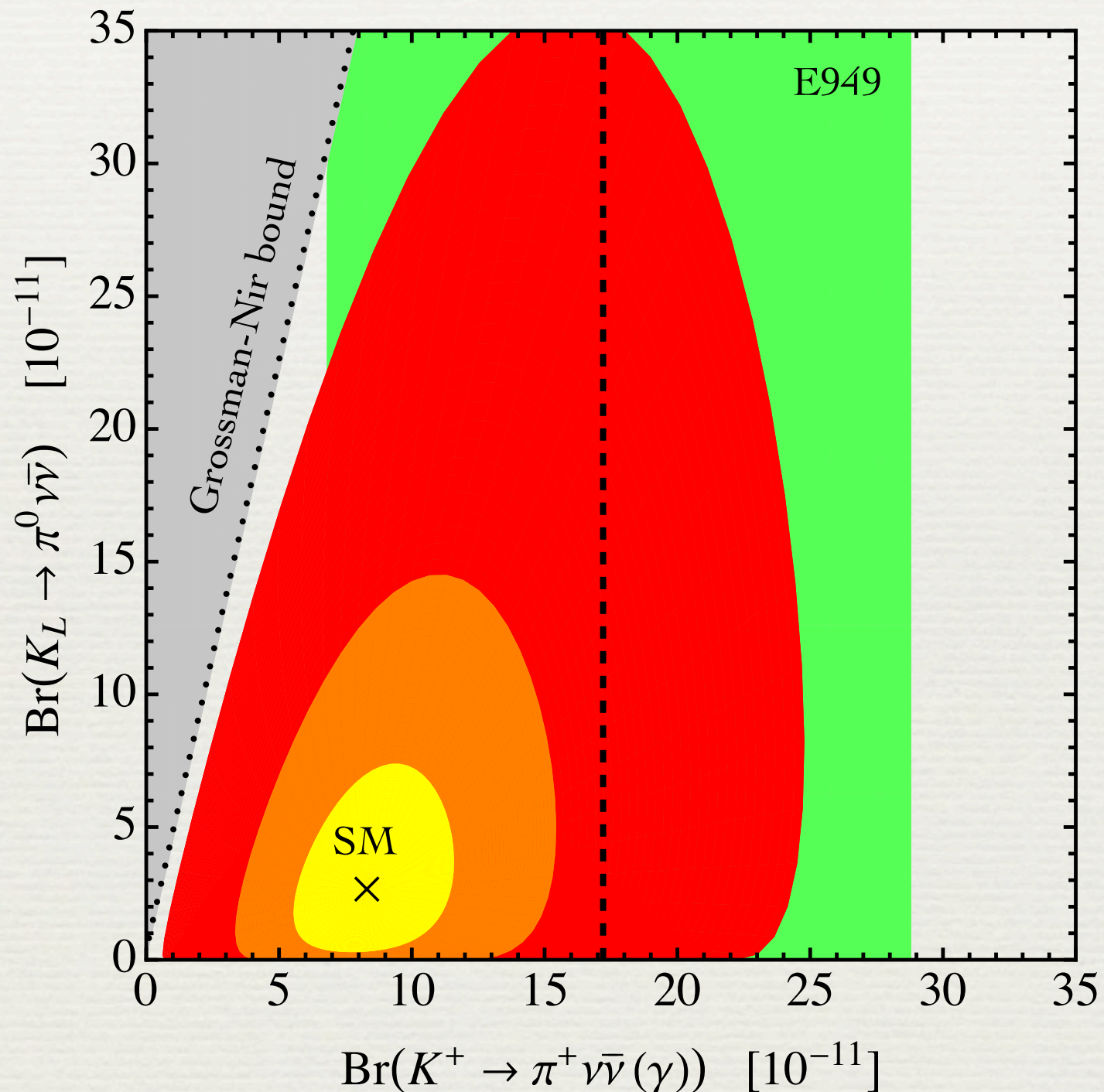
$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}(\gamma)) \propto |X|^2$$

$$X = \frac{\lambda_t}{\lambda^5} X_t + \frac{\text{Re} \lambda_c}{\lambda} P_{c,u} + \frac{1}{\lambda^5} \left( C_{\text{NP}} + \tilde{C}_{\text{NP}} \right)$$

$$\lambda_i = V_{is}^* V_{id}, \quad \lambda \approx 0.23, \quad X_t \approx 1.5, \quad P_{c,u} \approx 0.4$$



# Z-Penguins in Neutrino Modes



$$\text{Yellow region: } |C_{\text{NP}}| \leq 0.5 |\lambda_t C_{\text{SM}}|$$

$$\text{Orange region: } |C_{\text{NP}}| \leq |\lambda_t C_{\text{SM}}|$$

$$\text{Red region: } |C_{\text{NP}}| \leq 2 |\lambda_t C_{\text{SM}}|$$

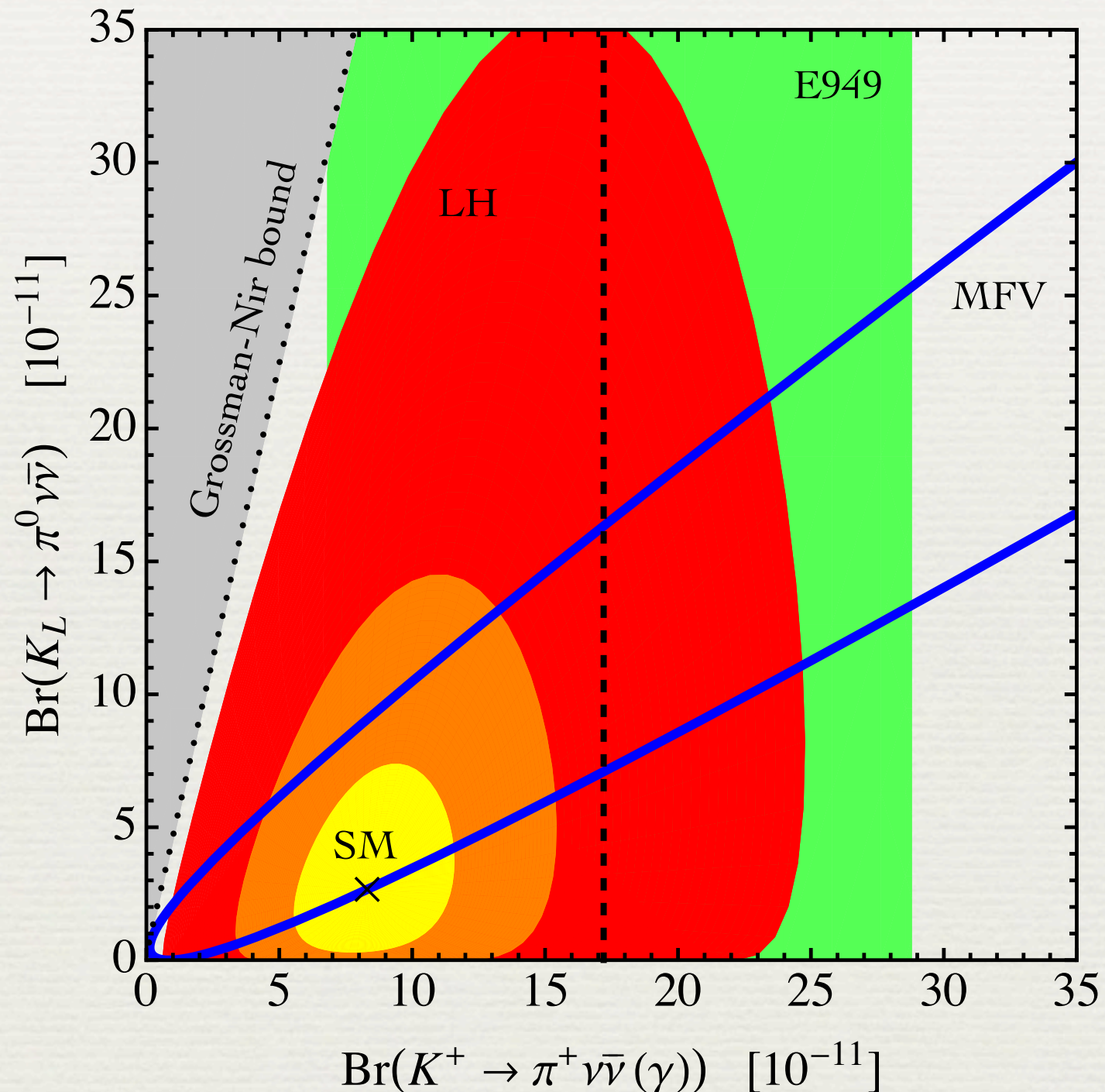
$$C_{\text{NP}} = |C_{\text{NP}}| e^{i\phi_C}$$

same results obtained  
for RH Z-penguin

[see S. Jäger, talk at NA62 Physics Handbook Workshop]



# Z-Penguins in Neutrino Modes



Yellow region:  $|C_{\text{NP}}| \leq 0.5 |\lambda_t C_{\text{SM}}|$

Orange region:  $|C_{\text{NP}}| \leq |\lambda_t C_{\text{SM}}|$

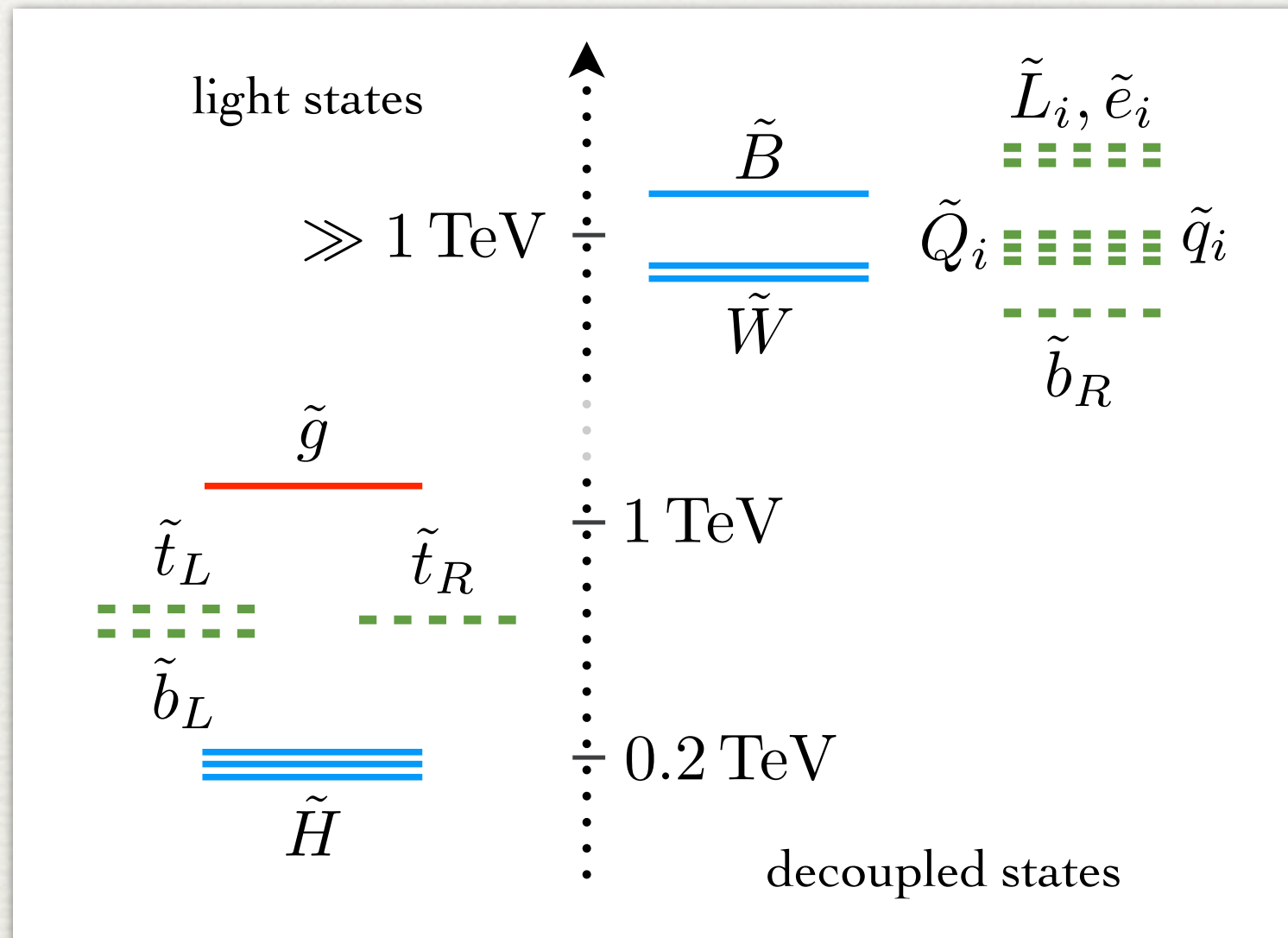
Red region:  $|C_{\text{NP}}| \leq 2 |\lambda_t C_{\text{SM}}|$

Blue line:  $C_{\text{NP}} \propto \lambda_t C_{\text{SM}}$

in minimal-flavor  
violating (MFV)  
models deviations  
very constraint



# “Natural SUSY”



- To avoid destabilizing weak scale only higgsinos ( $\tilde{H}$ ), stops ( $\tilde{t}_L, \tilde{t}_R$ ), LH sbottom ( $\tilde{b}_L$ ) & gluino ( $\tilde{g}$ ) need to be TeVish

[see for example Brust et al. 1110.6670; Papucci, Ruderman & Weiler, 1110.6926]



# “Natural SUSY”

- Light stops & charginos lead to specific pattern of deviations in flavor observables:

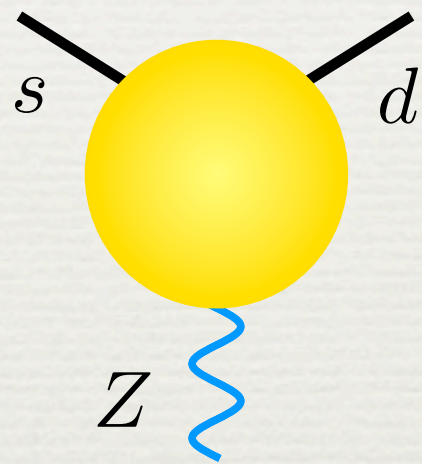
$$\frac{\Delta C}{C_{\text{SM}}} \approx \frac{m_t^2 A_t^2}{12 s_\beta^2 m_{\tilde{t}_1}^4}$$

Due to hierarchy  $|M_2| \gg |\mu|$ , stop-chargino effects in LH Z-penguin below 10% level. Predictions for rare kaon decays (as well as  $B_s \rightarrow \mu^+ \mu^-$  &  $B \rightarrow K^* l^+ l^-$ ) essentially unaltered in MFV MSSM



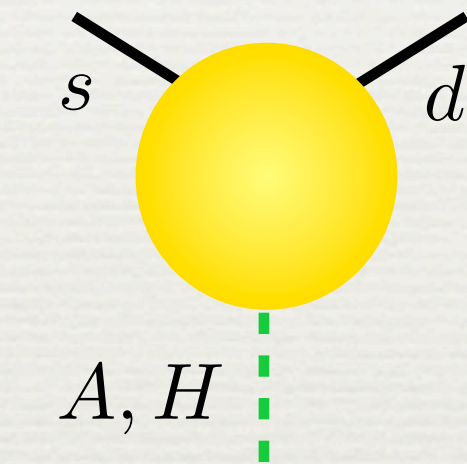
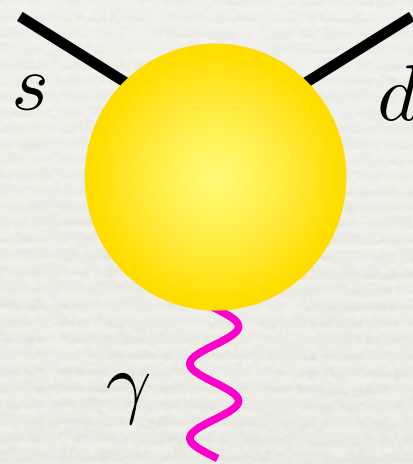
# Anatomy of Leptonic Modes

- $K_L \rightarrow \pi^0 l^+ l^-$  modes receive contributions from (axial-) vector (A, V), (pseudo-)scalar (P, S), ... operators:



$$Q_V = (\bar{d}\gamma_\mu s)(\bar{l}\gamma^\mu l)$$

$$Q_A = (\bar{d}\gamma_\mu s)(\bar{l}\gamma^\mu \gamma_5 l)$$



$$Q_S = (\bar{d}s)(\bar{l}l)$$

$$Q_P = (\bar{d}s)(\bar{l}\gamma_5 l)$$



# Anatomy of Leptonic Modes Cont'd

- In many explicit SM extensions such as RS scenarios, little Higgs models, scenarios with extra chiral/vector-like matter, ..., contribution from  $Q_A$  dominates over those of  $Q_V$ ,  $Q_S$  &  $Q_P$ :

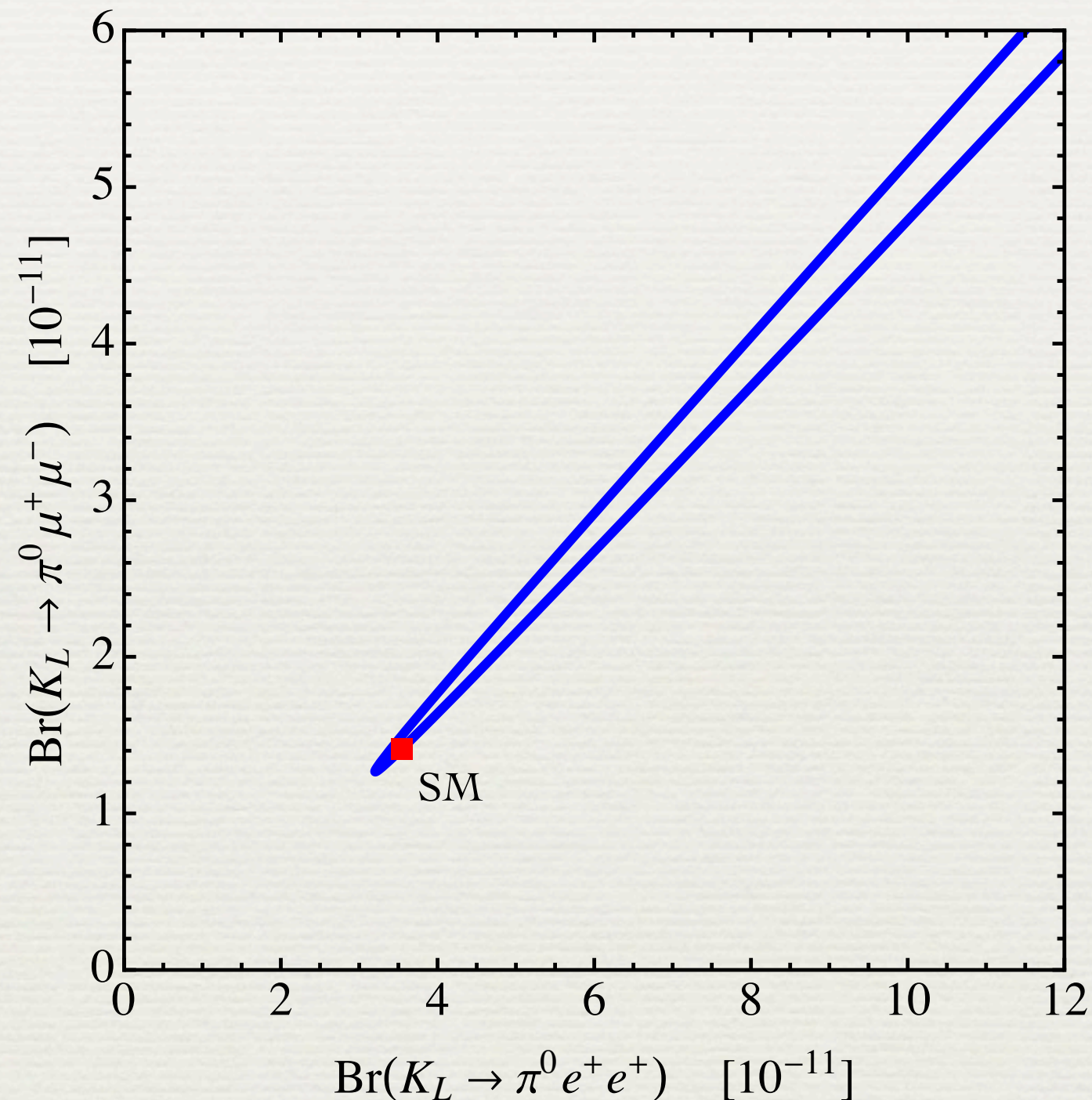
$$C_V \propto \left( \frac{1}{s_w^2} - 4 \right) \left( C_{\text{NP}} + \tilde{C}_{\text{NP}} \right) \approx 0.4 \left( C_{\text{NP}} + \tilde{C}_{\text{NP}} \right)$$

$$C_A \propto -\frac{1}{s_w^2} \left( C_{\text{NP}} - \tilde{C}_{\text{NP}} \right) \approx -4.4 \left( C_{\text{NP}} - \tilde{C}_{\text{NP}} \right)$$

$$C_{S,P} \propto m_s m_l$$



# Correlations of Leptonic Modes

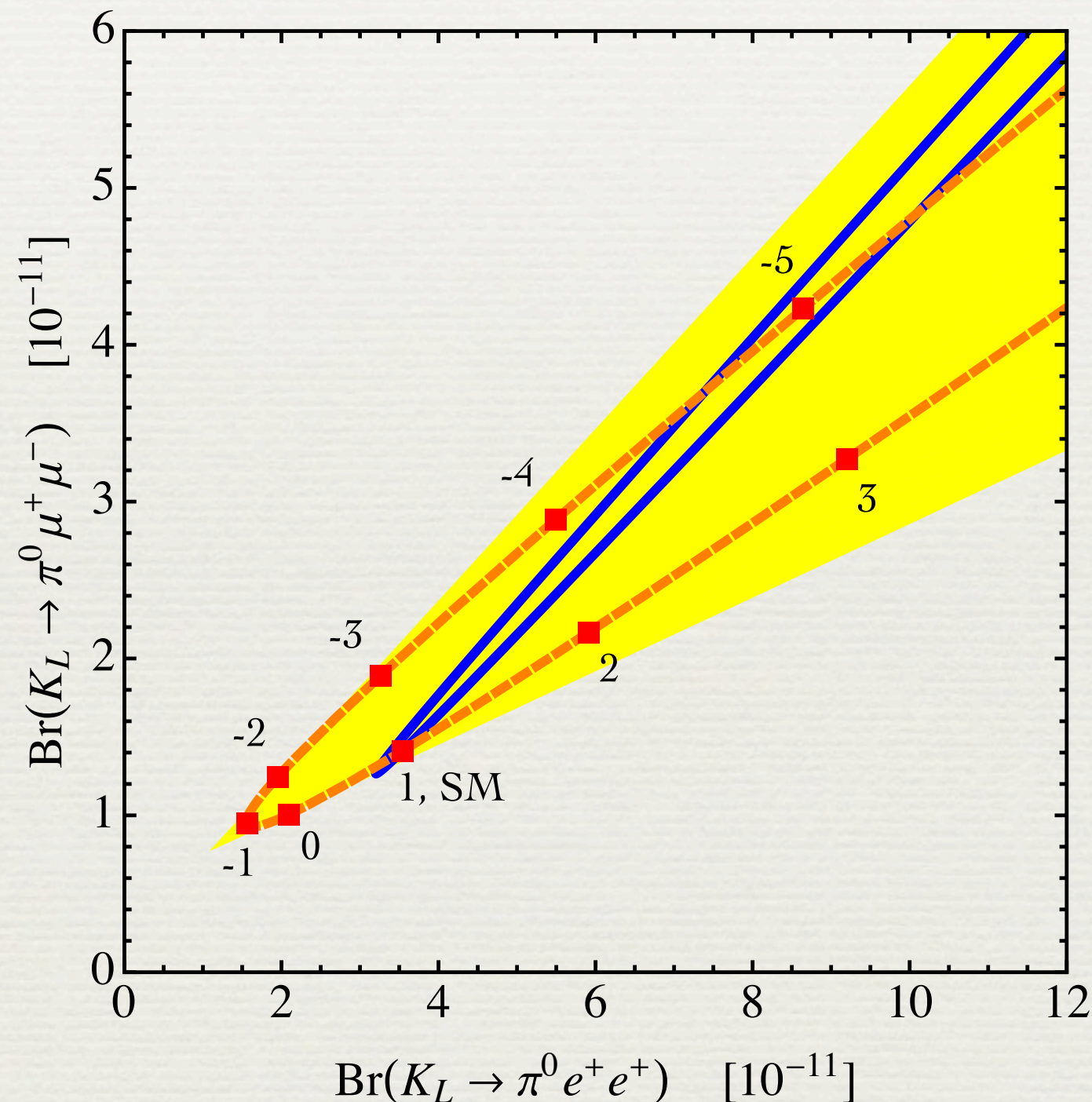


— LH Z-penguin

in scenarios with  $Q_A$  dominance, deviations in  $K_L \rightarrow \pi^0 l^+ l^-$  channels strongly correlated



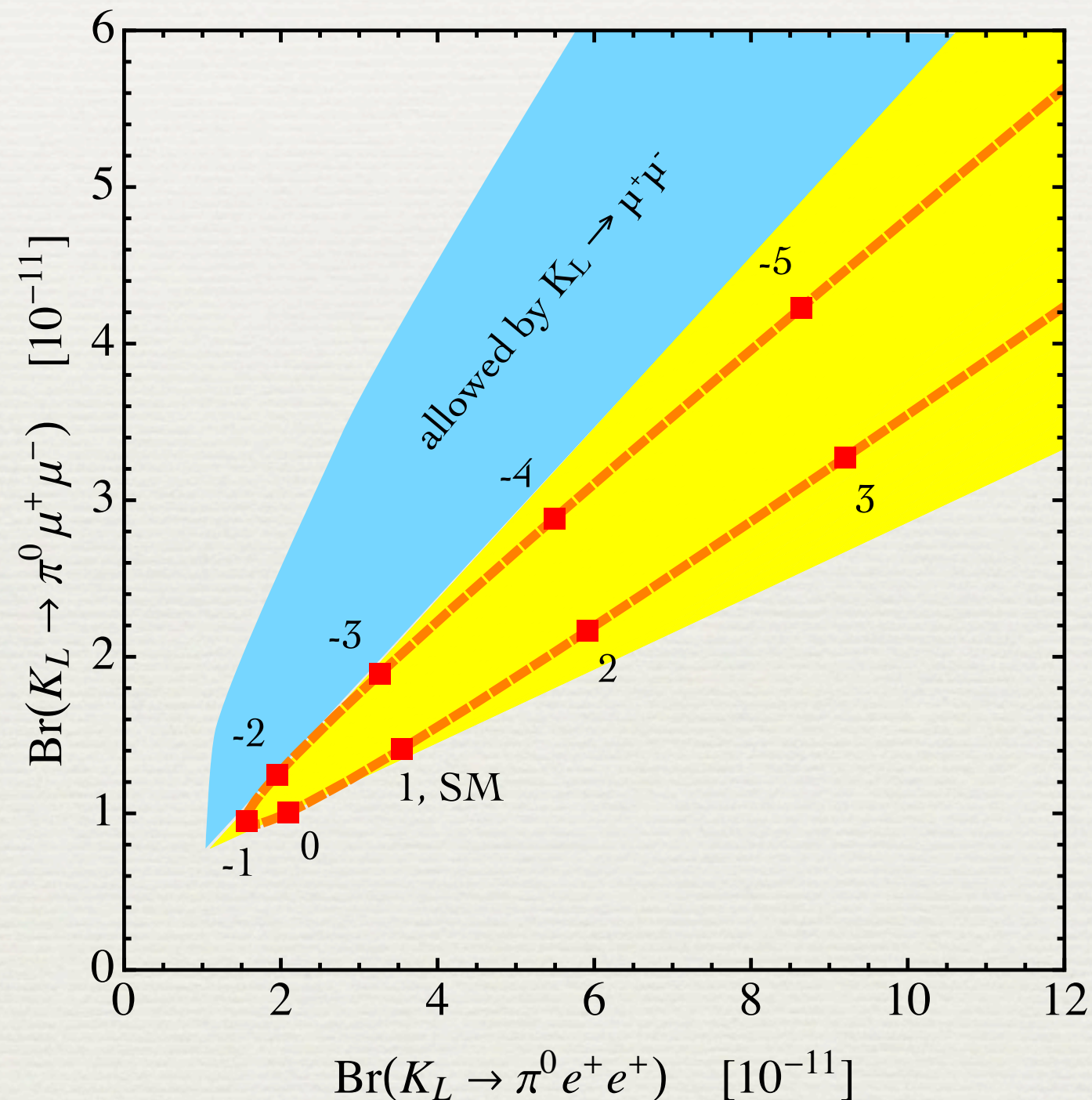
# Correlations of Leptonic Modes



presence of photon  
penguin can break  $Q_A$   
dominance & opens up  
parameter space



# Correlations of Leptonic Modes



rare semileptonic kaon channels also allow to disentangle  $S, P$  from  $V, A$  contributions

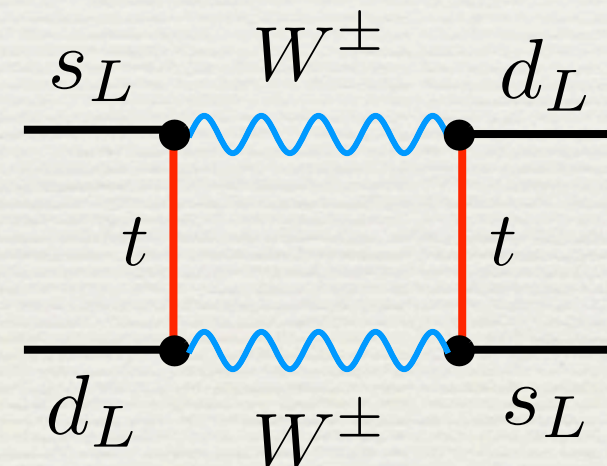


# Anatomy of $\epsilon_K$

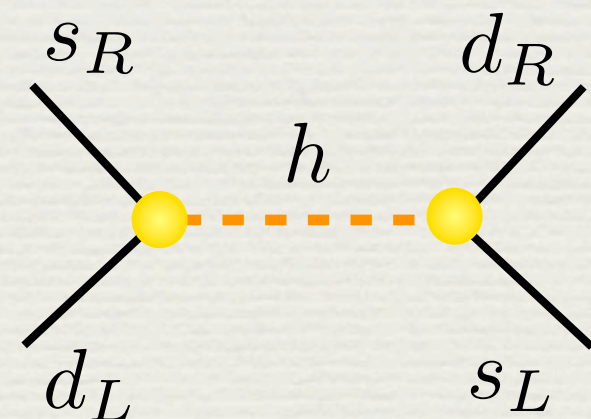
- Most severe constraints on flavor structure in many non-MFV models due to CP violation in kaon sector:

$$\epsilon_K \propto \text{Im} (C_{LL}^{sd} + 115 C_{LR}^{sd})$$

$$Q_{LL}^{sd} = (\bar{s}_L \gamma_\mu d_L)(\bar{s}_L \gamma^\mu d_L) \quad \xleftarrow{\text{SM}}$$



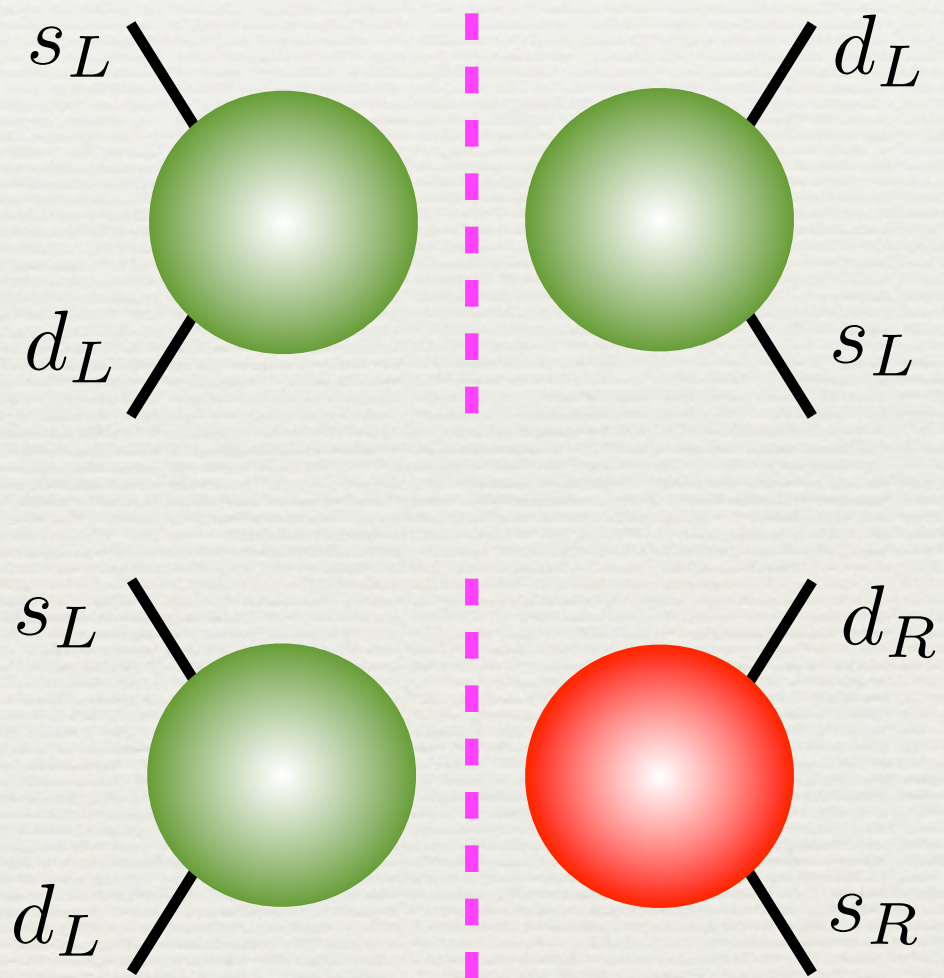
$$Q_{LR}^{sd} = (\bar{s}_R d_L)(\bar{s}_L d_R) \quad \xleftarrow{\text{RS}}$$





# $\epsilon_K$ & Rare K Decay Link

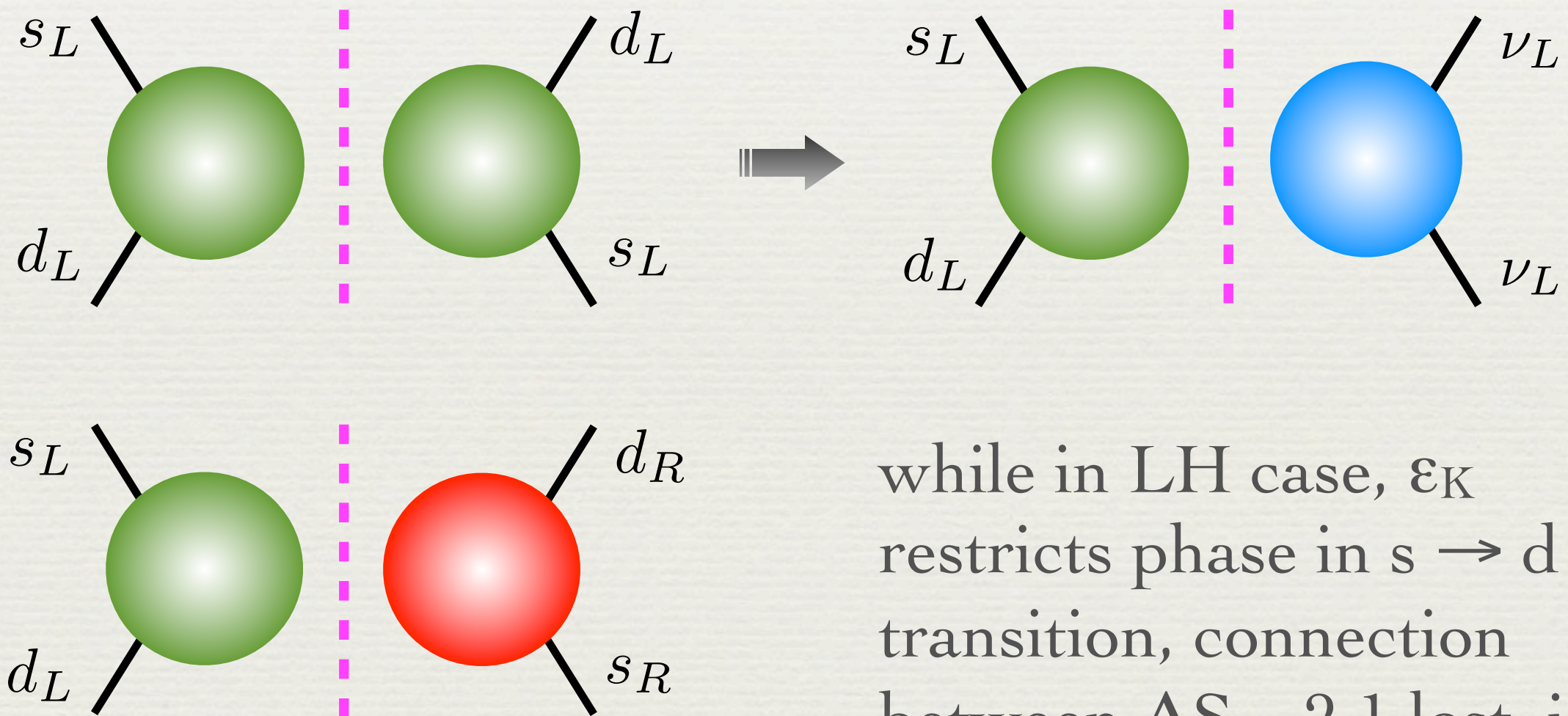
- SM extensions fall into two classes, those with pure LH structure & those with both LH & RH currents:





# $\epsilon_K$ & Rare K Decay Link

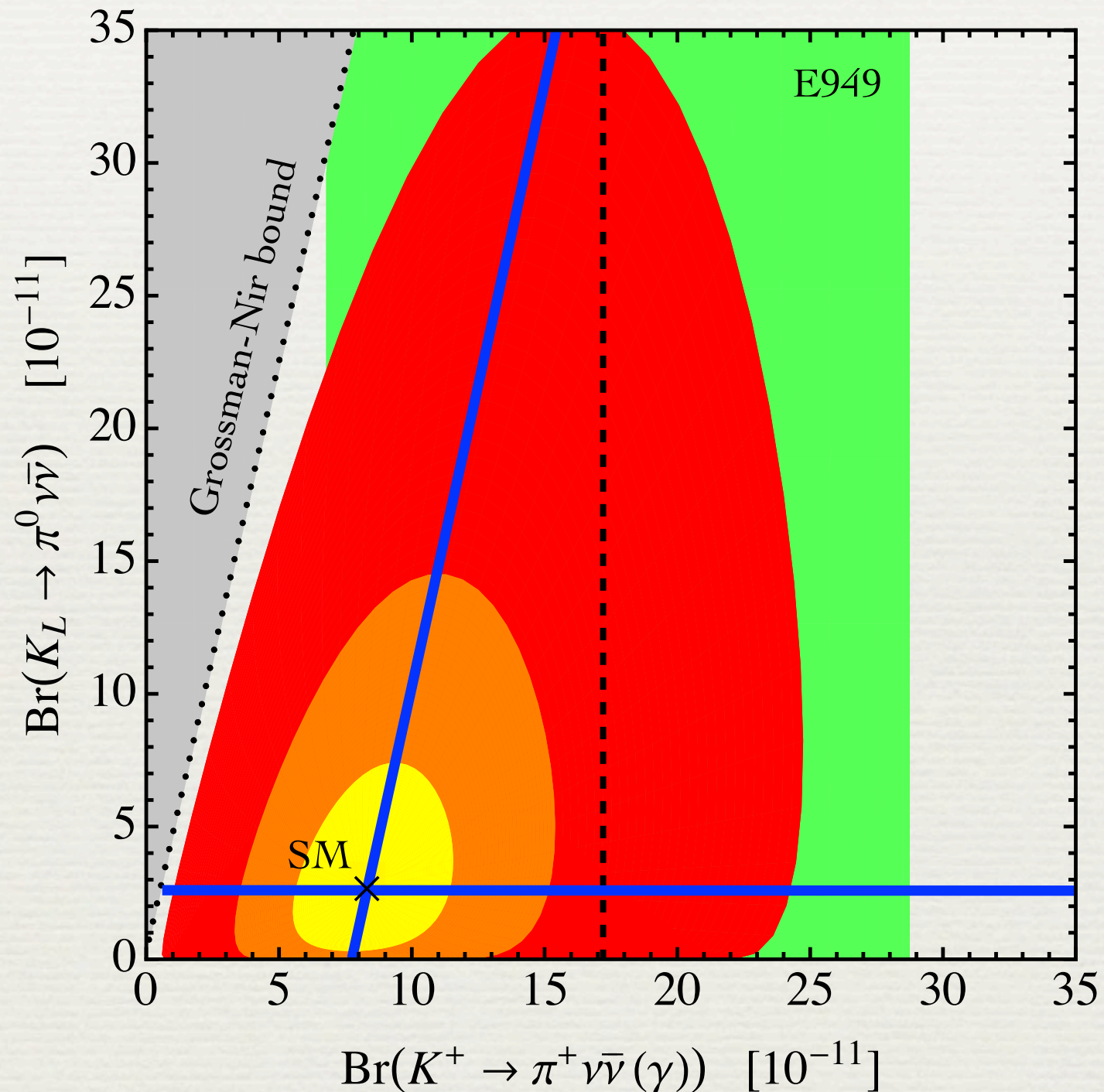
- SM extensions fall into two classes, those with pure LH structure & those with both LH & RH currents:



while in LH case,  $\epsilon_K$  restricts phase in  $s \rightarrow d$  transition, connection between  $\Delta S = 2, 1$  lost, if RH interactions present



# $\varepsilon_K$ & Rare K Decay Link Cont'd



Yellow:  $|C_{\text{NP}}| \leq 0.5 |\lambda_t C_{\text{SM}}|$

Orange:  $|C_{\text{NP}}| \leq |\lambda_t C_{\text{SM}}|$

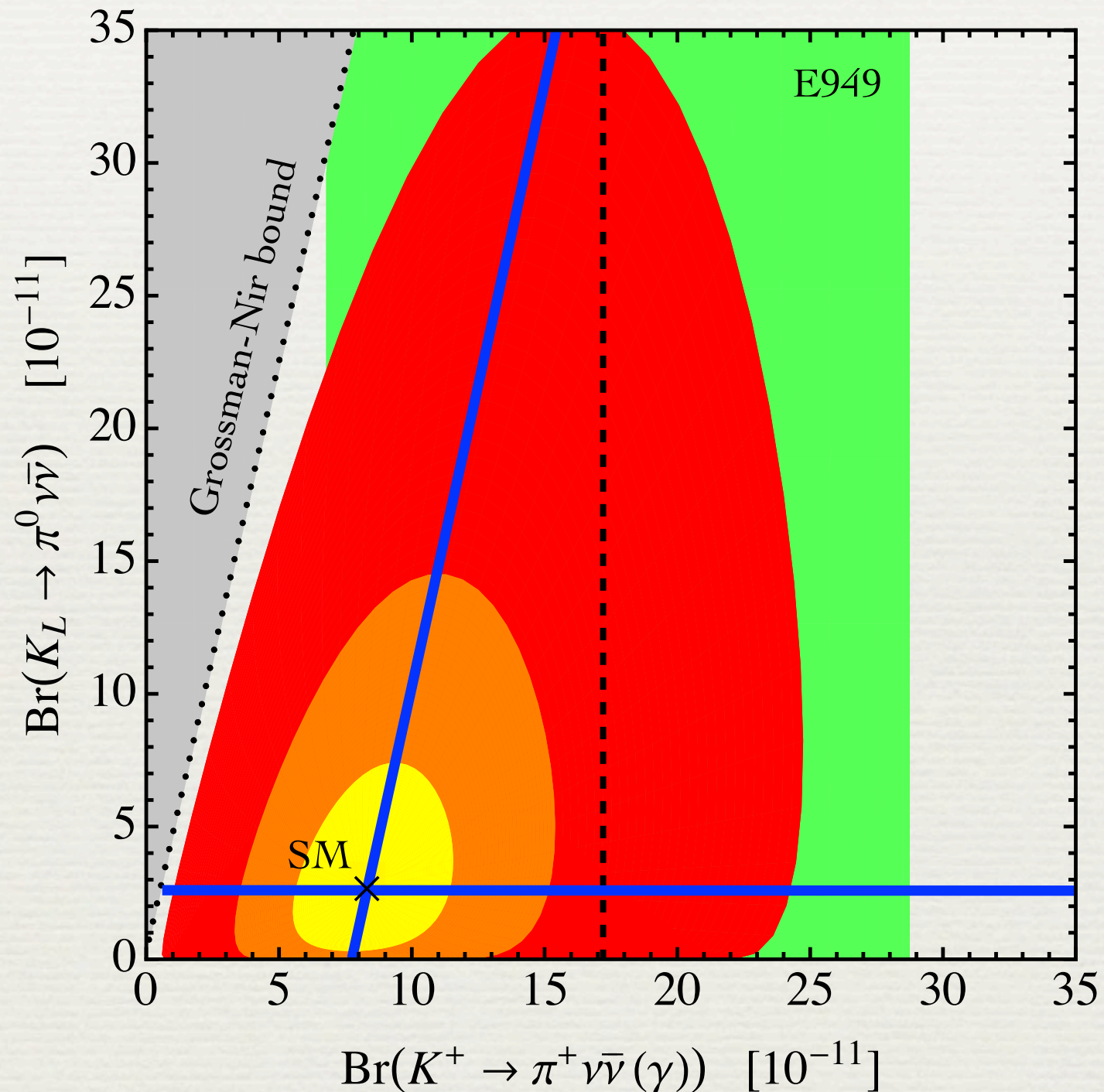
Red:  $|C_{\text{NP}}| \leq 2 |\lambda_t C_{\text{SM}}|$

Blue line: LH currents only

if new physics in  $\varepsilon_K$  is  
LH, only two branches  
of solution allowed for  
 $K \rightarrow \pi \nu \bar{\nu}$



# $\varepsilon_K$ & Rare K Decay Link Cont'd



$|C_{\text{NP}}| \leq 0.5 |\lambda_t C_{\text{SM}}|$

$|C_{\text{NP}}| \leq |\lambda_t C_{\text{SM}}|$

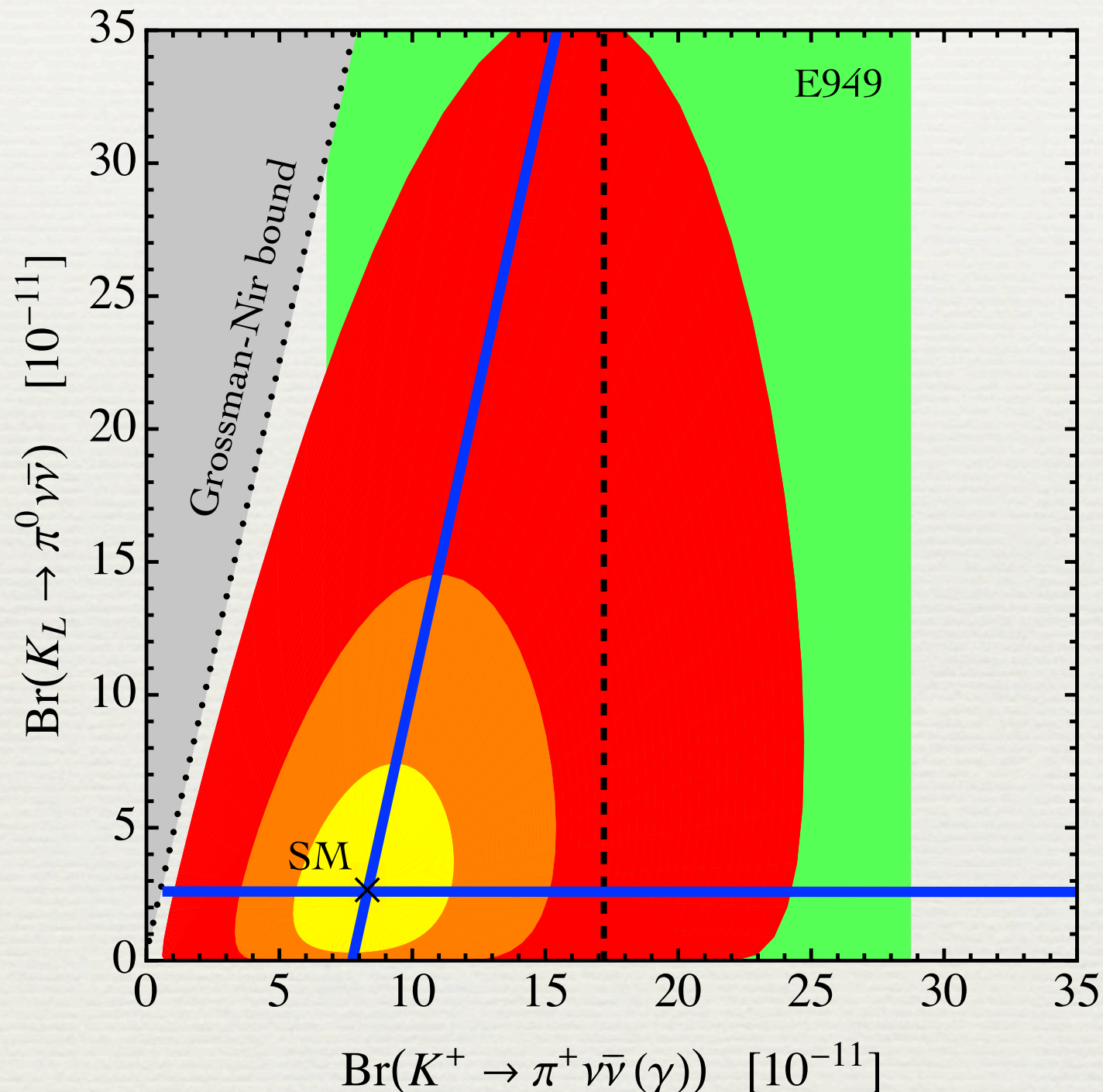
$|C_{\text{NP}}| \leq 2 |\lambda_t C_{\text{SM}}|$

LH currents only

pattern of deviations  
is found in certain  $Z'$ -  
boson scenarios, little  
Higgs models, ...



# $\varepsilon_K$ & Rare K Decay Link Cont'd



Yellow:  $|C_{\text{NP}}| \leq 0.5 |\lambda_t C_{\text{SM}}|$

Orange:  $|C_{\text{NP}}| \leq |\lambda_t C_{\text{SM}}|$

Red:  $|C_{\text{NP}}| \leq 2 |\lambda_t C_{\text{SM}}|$

Blue line: LH currents only

but pattern not generic  
& absent in MSSM,  
RS, ..., as  $Q_{\text{LR}}^{\text{sd}}$  renders  
dominant effect in  $\varepsilon_K$

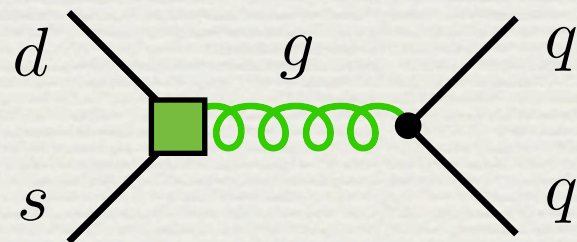
[see M. Blanke, arXiv:0904.2528 [hep-ph]]



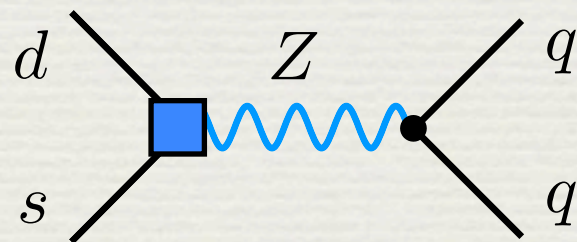
# Anatomy of $\epsilon'/\epsilon$

- Prediction for  $\epsilon'/\epsilon$  very sensitive to interplay between QCD ( $Q_6$ ) & electroweak ( $Q_8$ ) penguin operators:

$$\frac{\epsilon'}{\epsilon} \propto -\text{Im} \left[ \lambda_t \left( -1.4 + 13.8 R_6 - 6.6 R_8 \right) + \left( 1.5 + 0.1 R_6 - 13.3 R_8 \right) \left( C_{\text{NP}} - \tilde{C}_{\text{NP}} \right) \right]$$



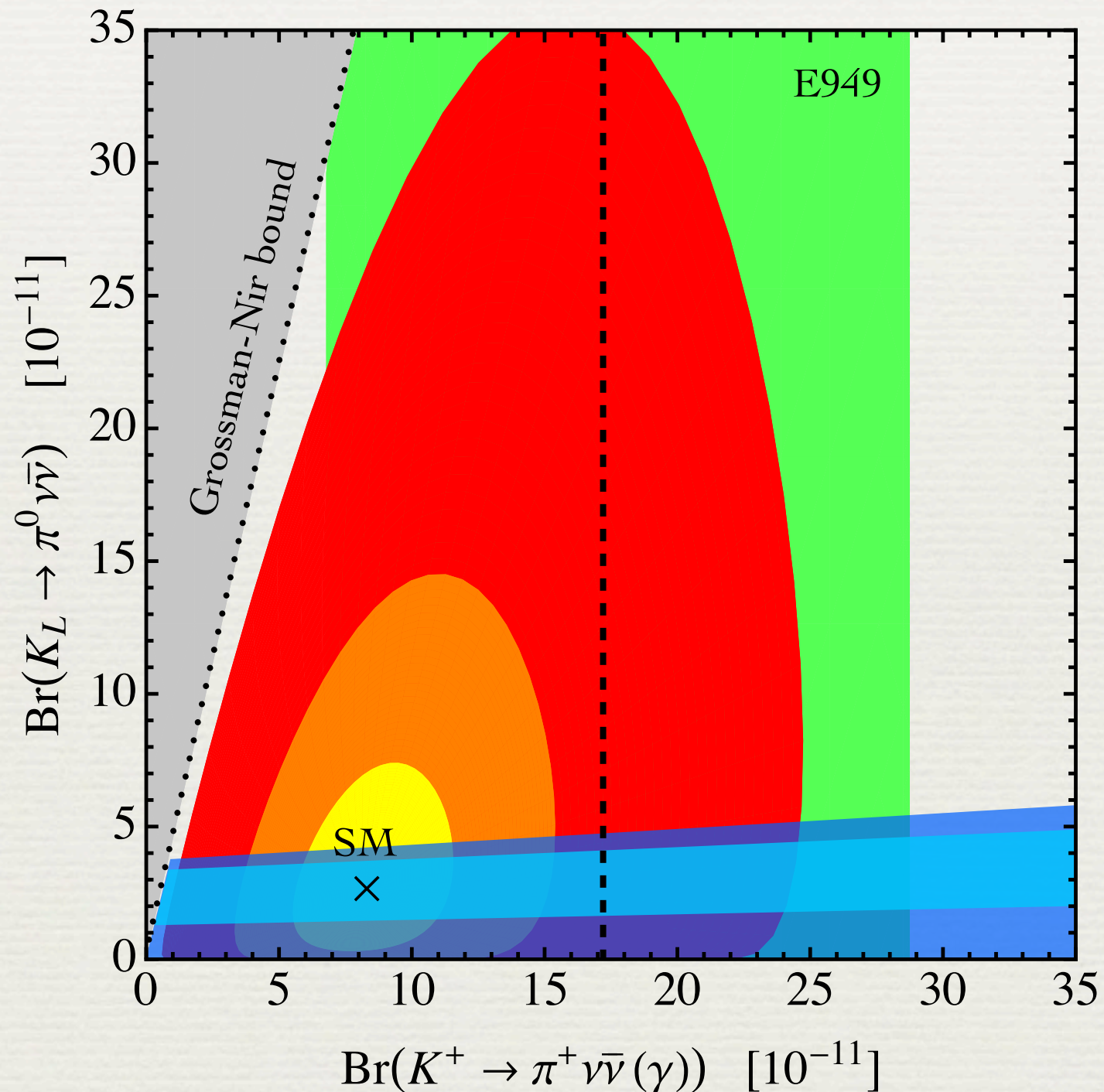
$$\Rightarrow R_6 \propto \langle (\pi\pi)_{I=0} | Q_6 | K \rangle \in [0.8, 2.0]$$



$$\Rightarrow R_8 \propto \langle (\pi\pi)_{I=2} | Q_8 | K \rangle \in [0.8, 1.2]$$



# $\epsilon'/\epsilon$ Strikes Back



$$\text{Yellow: } |C_{\text{NP}}| \leq 0.5 |\lambda_t C_{\text{SM}}|$$

$$\text{Orange: } |C_{\text{NP}}| \leq |\lambda_t C_{\text{SM}}|$$

$$\text{Red: } |C_{\text{NP}}| \leq 2 |\lambda_t C_{\text{SM}}|$$

$$C_{\text{NP}} = |C_{\text{NP}}| e^{i\phi_C}$$

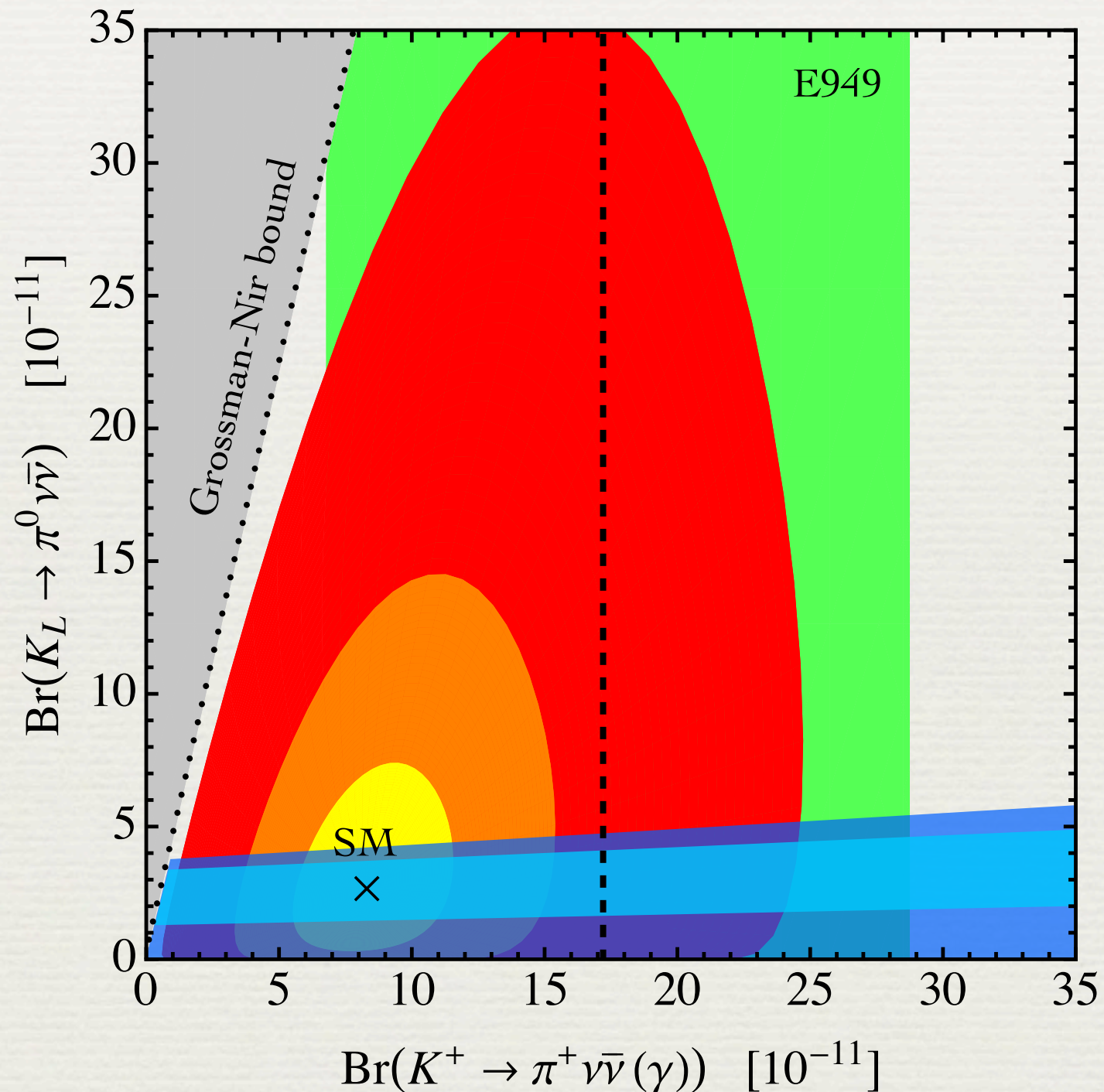
$$\text{Light blue: } \epsilon'/\epsilon \in [0.5, 2] (\epsilon'/\epsilon)_{\text{SM}}$$

$$\text{Dark blue: } \epsilon'/\epsilon \in [0.2, 5] (\epsilon'/\epsilon)_{\text{SM}}$$

[see S. Jäger, talk at NA62 Physics Handbook Workshop; M. Bauer et al., arXiv:0912.1625 [hep-ph]]



# $\varepsilon'/\varepsilon$ Strikes Back



stringent correlation  
between CP-violating  
kaon observables  
present in MSSM,  
RS, compositeness, ...

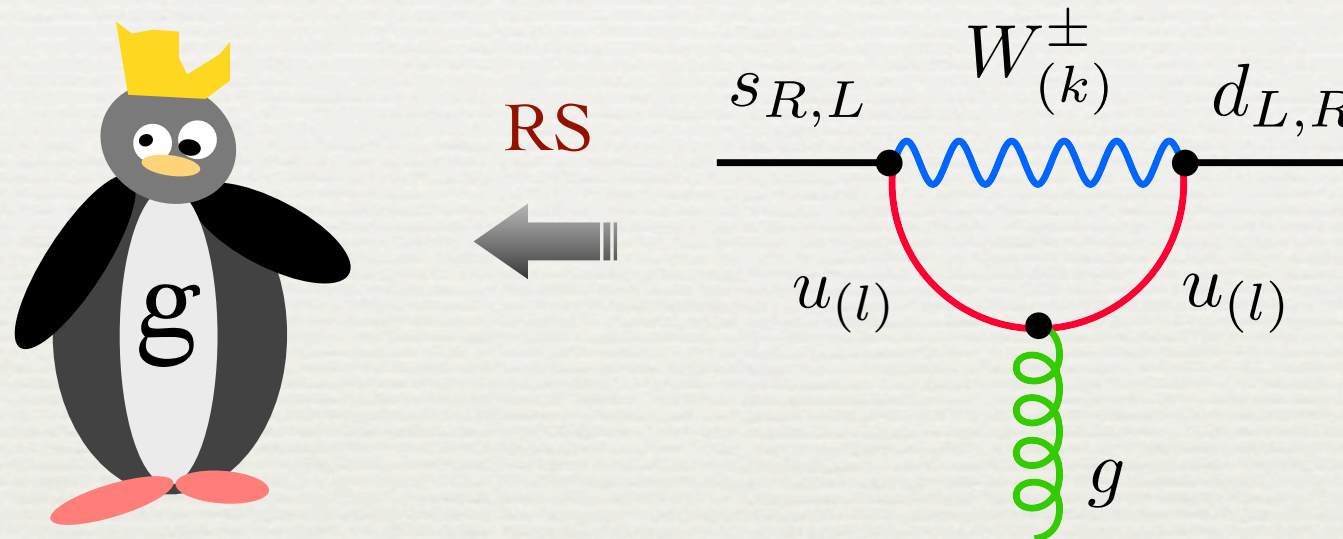


$\varepsilon'/\varepsilon$  “sleeping beauty”  
of flavor physics:  
when will lattice’s kiss  
wake her?

[see S. Jäger, talk at NA62 Physics Handbook Workshop; M. Bauer et al., arXiv:0912.1625 [hep-ph]]



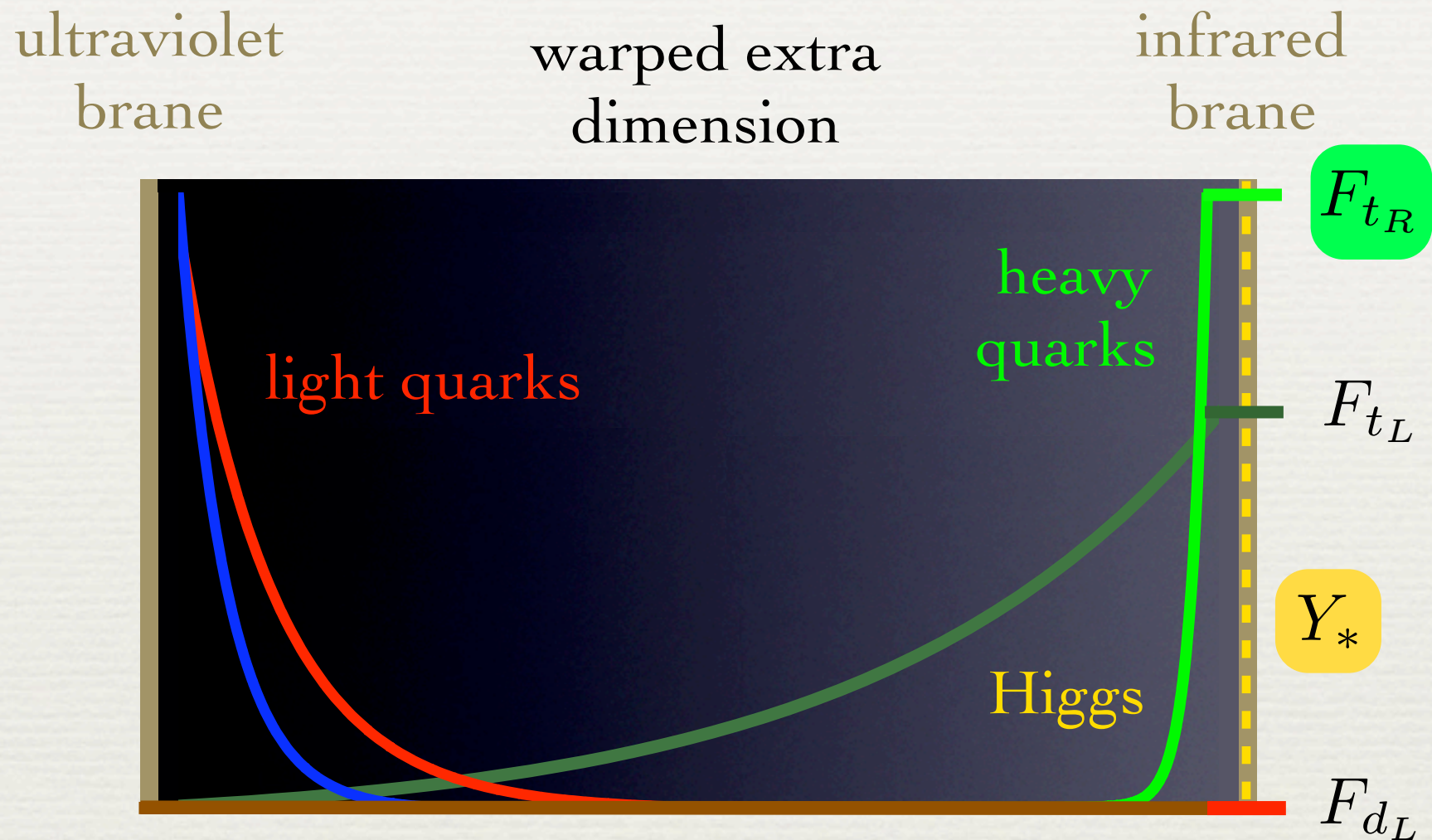
# Gluonic Penguins in $\varepsilon'/\varepsilon$



- Chromomagnetic penguin operators ( $\mathcal{Q}_{8g}, \tilde{\mathcal{Q}}_{8g}$ ) can also give large correction to  $\varepsilon'/\varepsilon$ . But in general (meaning MSSM, RS, ...) there is no correlation with Z penguin. In fact, often possible to decouple effects



# Gluonic Penguins in $\varepsilon'/\varepsilon$



$$\{C_{8g}, \tilde{C}_{8g}\} \propto \left\{ \lambda m_s, \frac{m_s}{\lambda} \right\} \frac{Y_*^2}{m_t}, \quad C \propto \frac{A^2 \lambda^5}{Y_*^2 F_{t_R}^2}, \quad \tilde{C} \propto \frac{m_d m_s F_{t_R}^2}{A^2 \lambda^5 m_t^2}$$

[see M. Bauer et al., arXiv:0912.1625 [hep-ph]]



# Conclusions & Outlook

- In view of “textbook measurements” of CP phase in  $B_s$  system,  $B \rightarrow K^* \mu^+ \mu^-$  &  $B_s \rightarrow \mu^+ \mu^-$  by LHCb, rare decays of kaons last place where indisputable signals of new physics could show up



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- Effects of  $O(50\%)$  in both  $K \rightarrow \pi \nu \bar{\nu}$  modes are not at variance with other existing constraints ( $\epsilon'/\epsilon$ , ...). In view of cleanness of rare kaon modes, such deviations would provide smoking-gun signal for new physics



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- Effects of  $O(50\%)$  in both  $K \rightarrow \pi \nu \bar{\nu}$  modes are not at variance with other existing constraints ( $\epsilon'/\epsilon$ , ...). In view of cleanness of rare kaon modes, such deviations would provide smoking-gun signal for new physics
- Since kaon observables feature testable correlations, mandatory to measure as many rare kaon modes as possible. Only experiment can unravel flavor mystery!

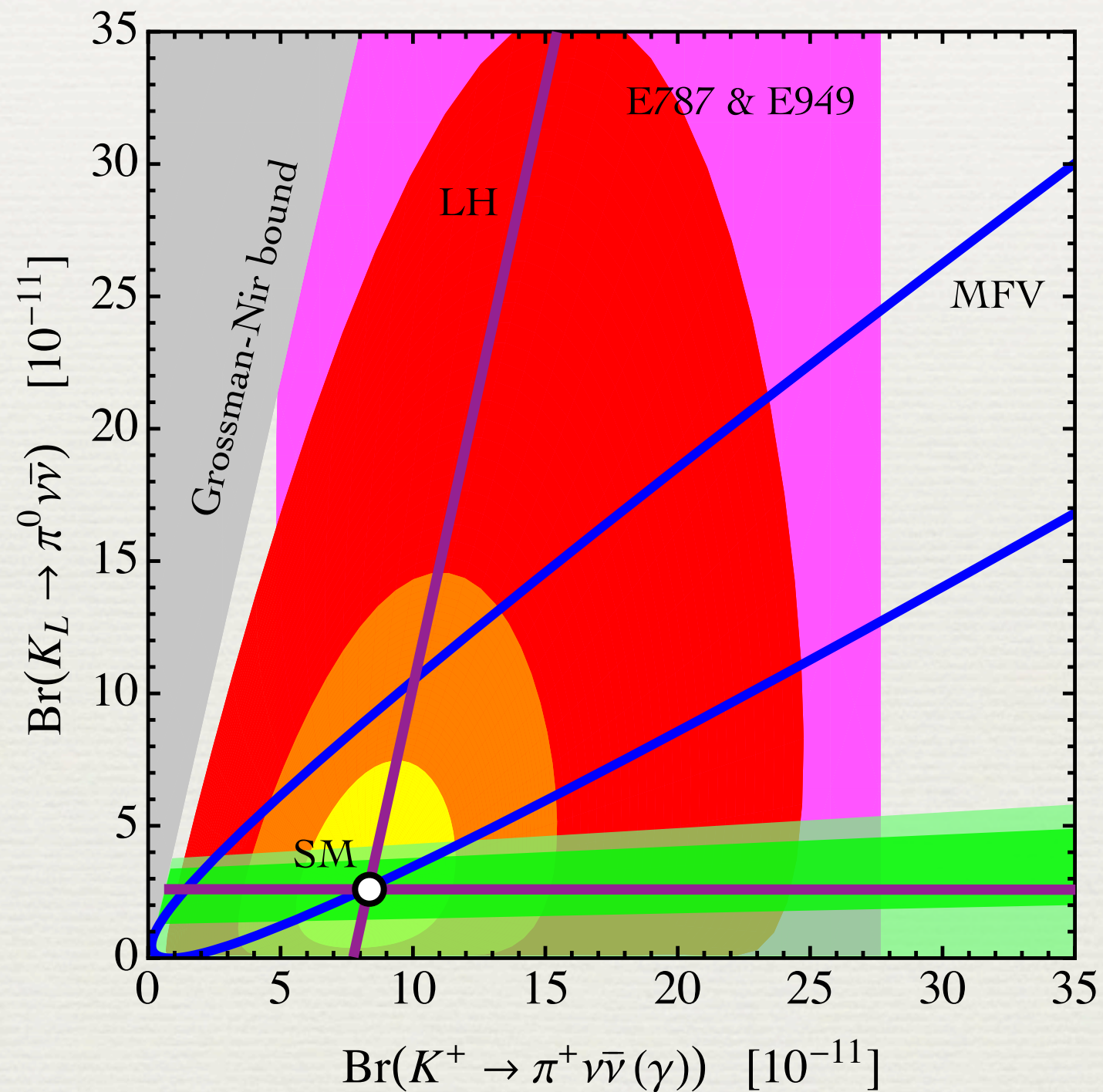


# Sources of Inspiration

- Talk by S. Jäger given at NA62 Physics Handbook Workshop, 10–12 December 2009 CERN
- F. Mescia, C. Smith & S. Trine, hep-ph/0606081
- M. Blanke, arXiv:0904.2528 [hep-ph]
- M. Bauer, S. Casagrande, U. Haisch & M. Neubert, arXiv:0912.1625 [hep-ph]
- ...



# Neutrino Modes: Summary





# Leptonic Modes: Summary

