

Diphoton + 2jets production at NLO

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on behalf of the BlackHat Collaboration



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$\gamma\gamma + 2j$ @ NLO

Background to the production of the Higgs boson via Vector Boson Fusion (VBF)

Born matrix element and real emission corrections known since '90s

NLO needed to reduce the large dependence on scales
and have the first quantitative prediction.

- $pp \rightarrow \gamma\gamma + 0j$
DIPHOX (Binoth, Guillet, Pilon, Werlen)
2gammaMC (Bern, Dixon, Schmidt)
MCFM (Campbel, Ellis, Williams)
Catani, Cieri, de Florian, Ferrera, Grazzini (2011) (NNLO)
- $pp \rightarrow \gamma\gamma + 1j$
Del Duca, Maltoni, Nagy, Trocsanyi (2003)
Gehrman, Greiner, Heinrich (2013)
- $pp \rightarrow \gamma\gamma + 2j$
Gehrman, Greiner, Heinrich (2013)
BH collaboration: to appear

NLO calculations with BlackHat+Sherpa

$$\sigma_n^{\text{NLO}} = \int_n \sigma_n^{\text{born}} + \int_n (\sigma_n^{\text{virt}} + \Sigma_n^{\text{subtr}}) + \int_{n+1} (\sigma_{n+1}^{\text{real}} - \sigma_{n+1}^{\text{subtr}})$$

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used to manage the partonic subprocesses and to integrate over phase space.

COMIX package (Gleisberg,Höche) used to compute Born and real-emission matrix elements, along with the Catani–Seymour dipole subtraction terms.

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BlackHat used to compute the virtual (one-loop) contribution

Numerical implementation of on-shell methods for one-loop amplitudes

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Numerical implementation of on-shell methods for one-loop amplitudes

Used previously for			
$W, Z/\gamma^* + 3j,$ high- p_T W polarization ,	$W, Z/\gamma^* + 4j,$ $\gamma + n\text{-jet} / Z + n\text{-jet}$ ratios	$W+5j,$	4 Jet ,

On-Shell Methods

Britto et al. (BCFW, 2005), Bern,Dixon,Dunbar,Kosower (1994), Bern,Dixon,Kosower (1998,2006),
Brandhuber,McNamara,Spence,Travaglini (2005), Anastasiou,Britto,Feng,Kunszt,Mastrolia (2007);
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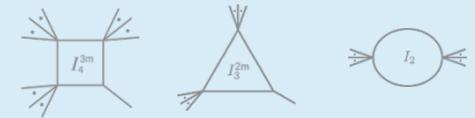
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$\text{Int}_j \rightarrow$ Known integral basis (Passarino-Veltman):

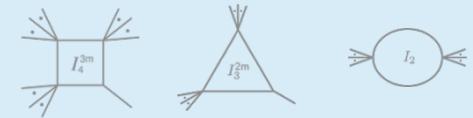


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Integrals universal and
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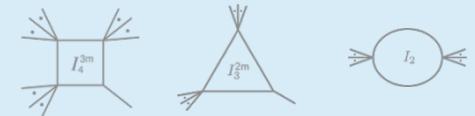
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$c_j \rightarrow$ Unitarity in D=4 : rational functions of spinors.

Rational \rightarrow On-shell Recursion; D-dimensional unitarity

BlackHat

1) BH computes *primitive amplitudes*:

Integrals given by analytic formulae.

- Coefficients: computed using contour integral at ∞ [D. Forde ('07)]
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3) Sum of the loop-tree interference over colours (full/leading)

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BH-Sherpa n -tuple branches
id, nparticle, px, py, pz, E, x1, x2, x1p, x2p, id1, id2, kf alpha_power, alpha_s, fac_scale, ren_scale, weight, weight2, me_wgt, me_wgt2, nuwgt, usr_wgts, part

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Sufficient information can be stored
to re-evaluate cross sections and distributions
without the need of re-computing the hard matrix elements

$\gamma\gamma + 2j$ with BlackHat

Must isolate photons from surrounding hadronic radiation.

We use Frixione cone: radially-dependent E_T limit

$$\sum_p E_{Tp} \theta(\delta - R_{p\gamma}) \leq E(\delta) \quad \text{with} \quad E(\delta) = E_T^\gamma \epsilon \left(\frac{1 - \cos \delta}{1 - \cos \delta_0} \right)^n$$

$$(\epsilon = 0.5, \delta_0 = 0.4, n = 1)$$

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The five lighter quarks treated as massless

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$\gamma\gamma + 0\text{-jet}$:

confirmed HELAC (PS points) and MCFM (PS points & after integration)

$\gamma\gamma + 1\text{-jet}$: confirmed GoSam (PS points & after integration)

$\gamma\gamma q\bar{q}g$ also confirmed against previous analytic calculation (L. Dixon)

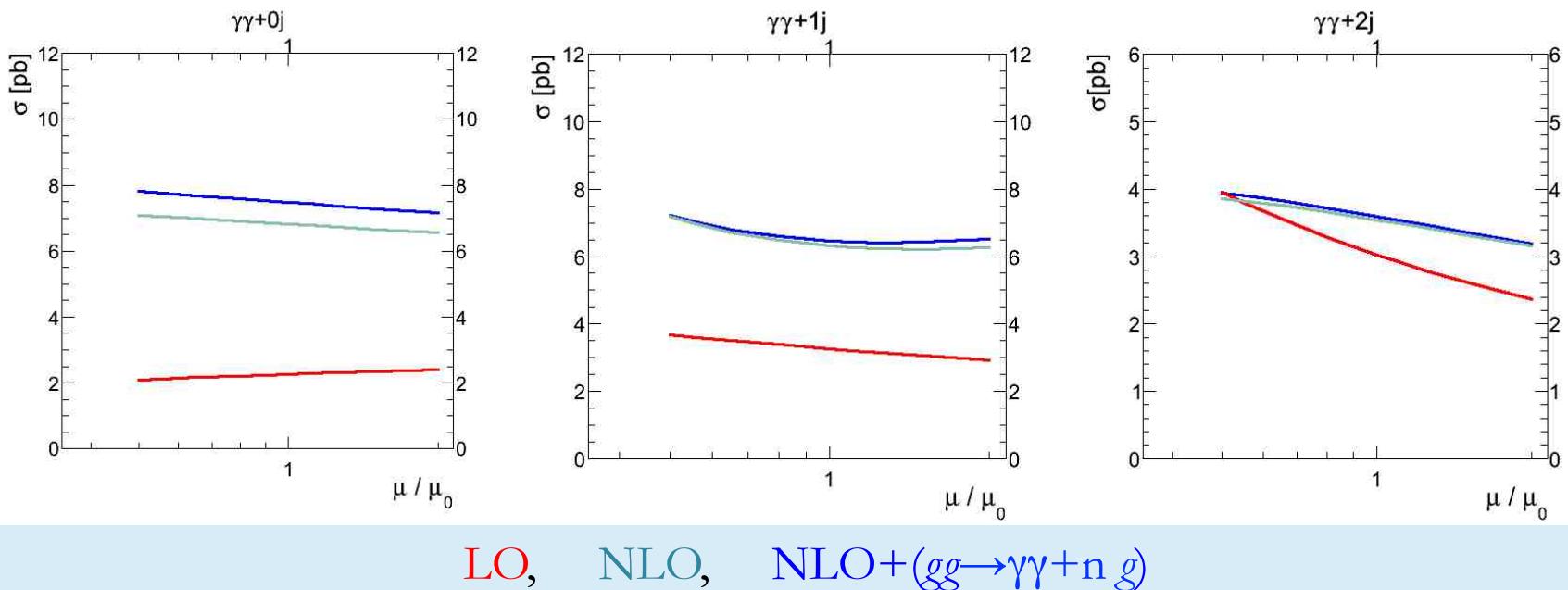
$\gamma\gamma + 2\text{-jet}$: confirmed GoSam (PS points)

$\gamma\gamma + \text{jets}$ (incl.) @ LO&NLO : cross sections

$$\text{PDF} = \text{MSTW}(2008), \quad \mu_0 = \frac{1}{2} \left(p_T^{\gamma_1} + p_T^{\gamma_2} + \sum_m p_T^m \right), \quad \sqrt{s} = 8 \text{ TeV}$$

$$p_T^{\gamma_1} > 50 \text{ GeV}, \quad p_T^{\gamma_2} > 25 \text{ GeV}, \quad |\eta^\gamma| < 2.5, \quad |\eta^{\text{jet}}| < 4.5,$$

$$p_T^{\text{jet}_1} > 40 \text{ GeV}, \quad p_T^{\text{jet}_2} > 25 \text{ GeV}, \quad (M_{jj} > 400 \text{ GeV}, \quad \Delta\eta_{jj} > 2.8)$$



$\gamma\gamma+2\text{jet}$ production: modest NLO correction

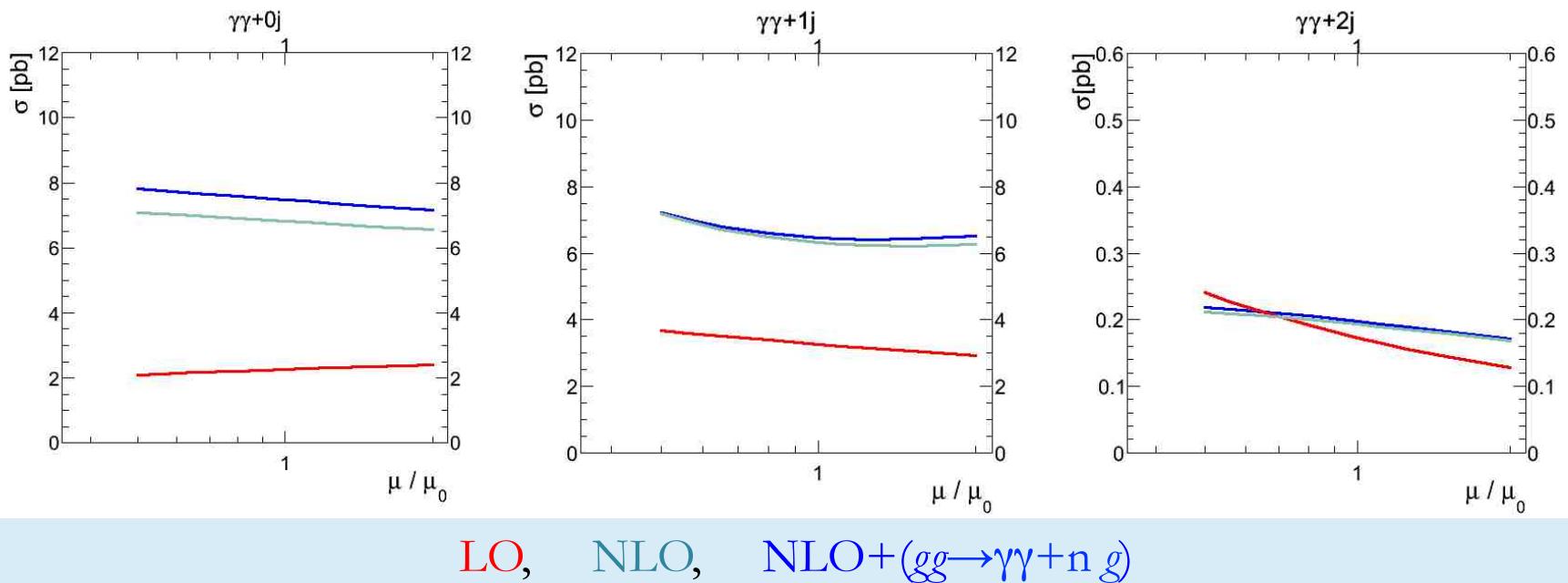
small $gg \rightarrow \gamma\gamma gg$ contribution ($\sim 2\%$ of total cross section)

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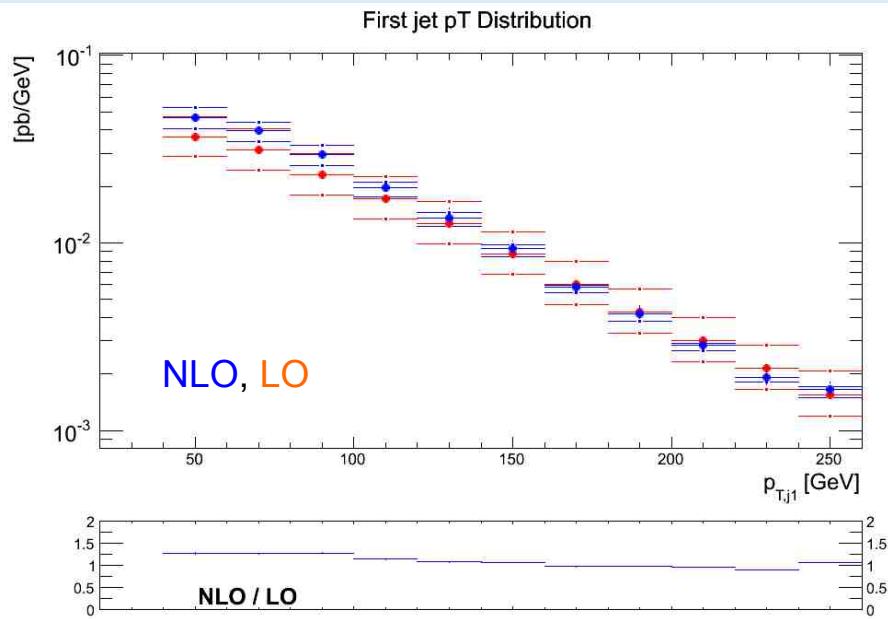
Leading Jet's p_T -distribution

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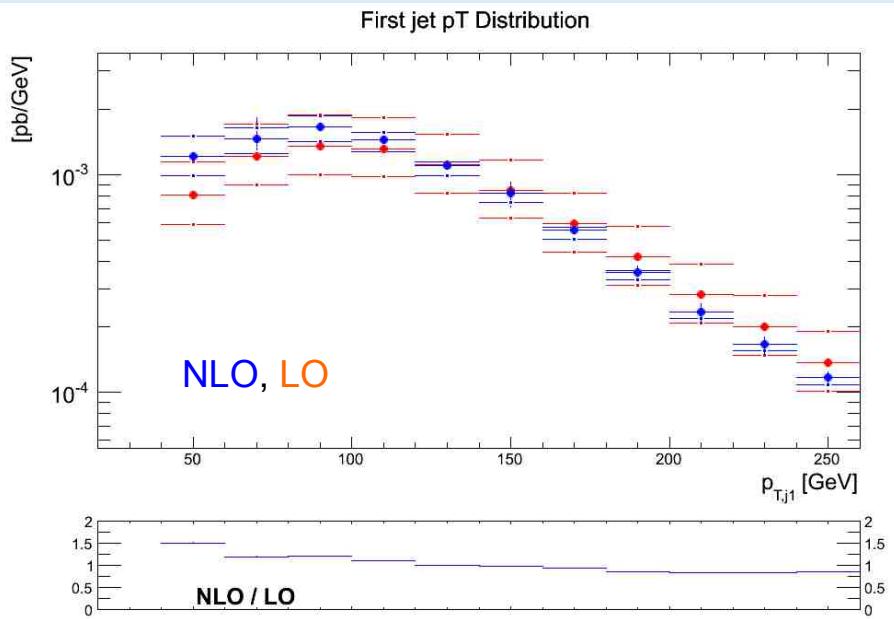
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Without VBF cuts



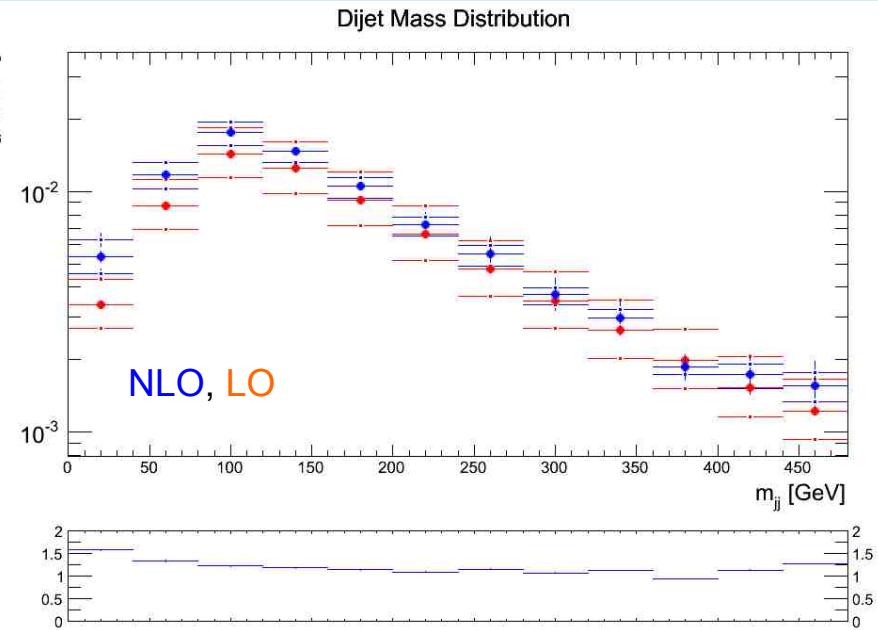
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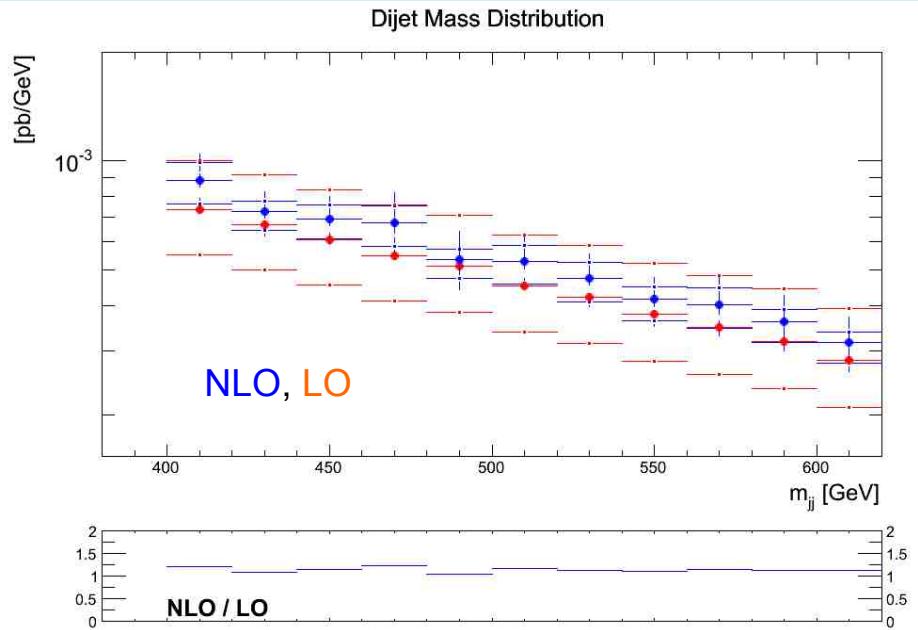
Dijet invariant mass distributions

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Without VBF cuts



With VBF cuts

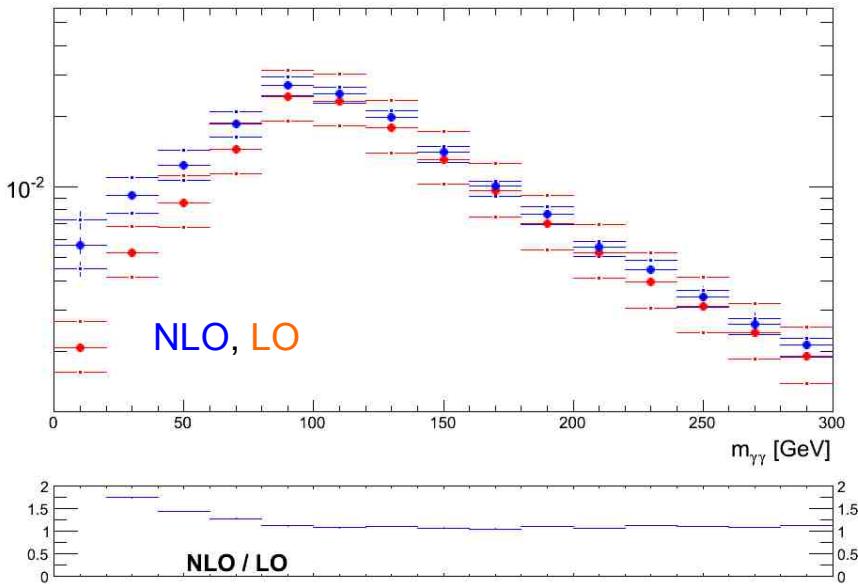


Diphoton invariant mass distributions

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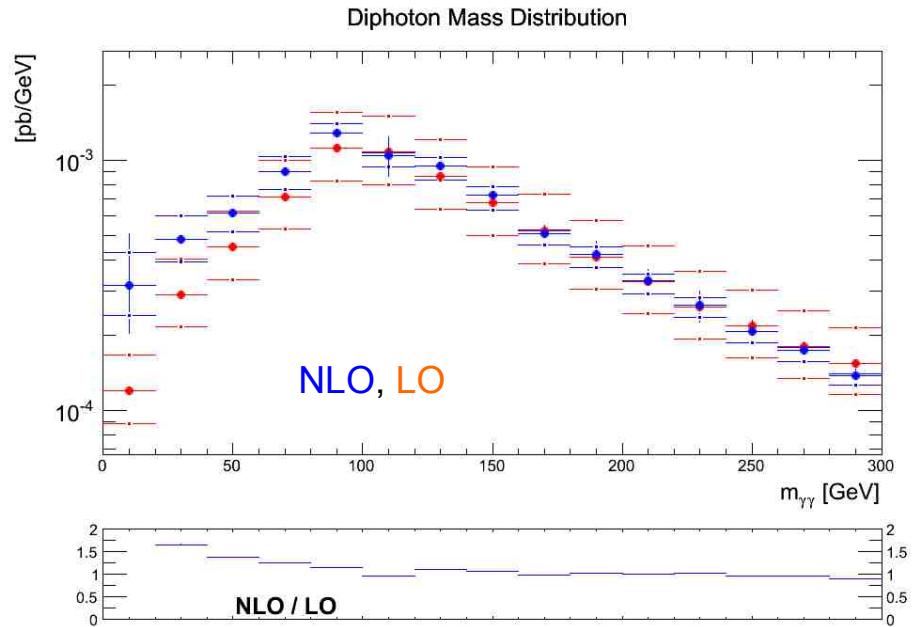
Without VBF cuts

Diphoton Mass Distribution



With VBF cuts

Diphoton Mass Distribution

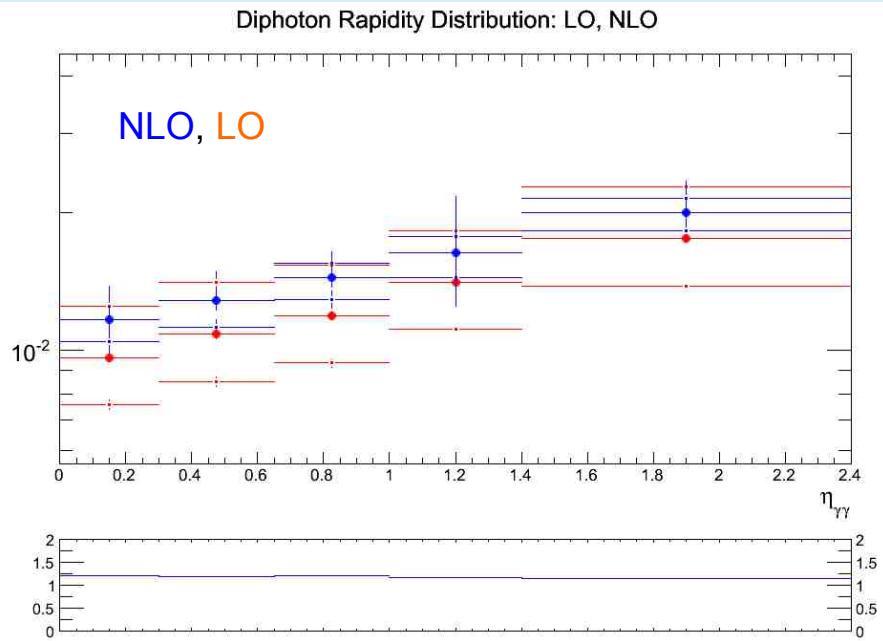


Large NLO correction for low values of diphoton mass.

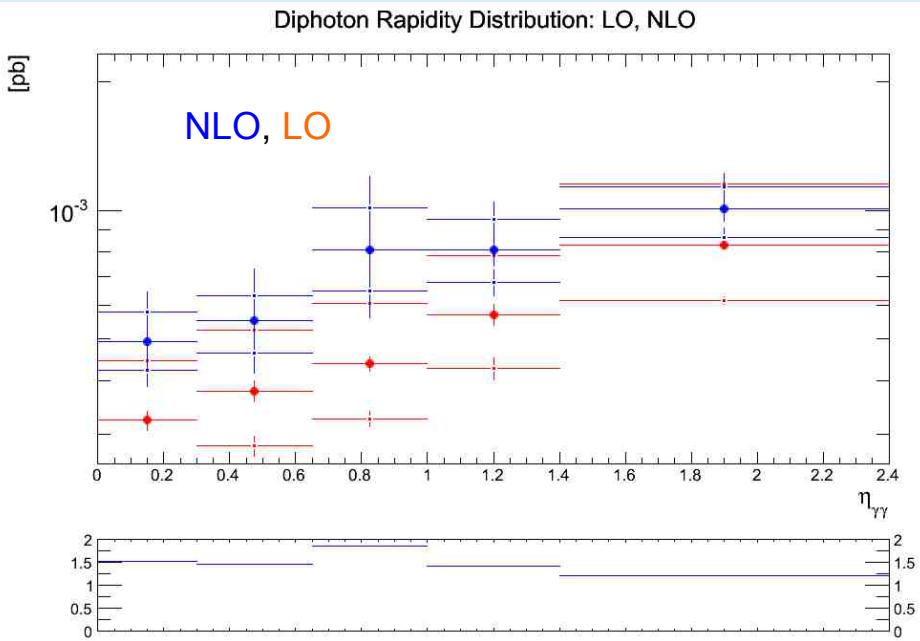
Diphoton Rapidity distribution – altern. cuts

$$\begin{aligned}
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 p_T^{\gamma_1} &> 0.35 m_{\gamma\gamma}, & p_T^{\gamma_2} &> 0.25 m_{\gamma\gamma}, & |\eta^\gamma| &< 2.37, & |\eta^{\text{jet}}| &< 4.4, \\
 p_T^{\text{jets}} &> 30 \text{ GeV}, & 122 \leq m_{\gamma\gamma} \leq 130 \text{ GeV}, & & \left(M_{jj} > 400 \text{ GeV}, \quad \Delta \eta_{jj} > 2.8 \right)
 \end{aligned}$$

Without VBF cuts



With VBF cuts



Large NLO correction for small values of η , especially after VBF cuts

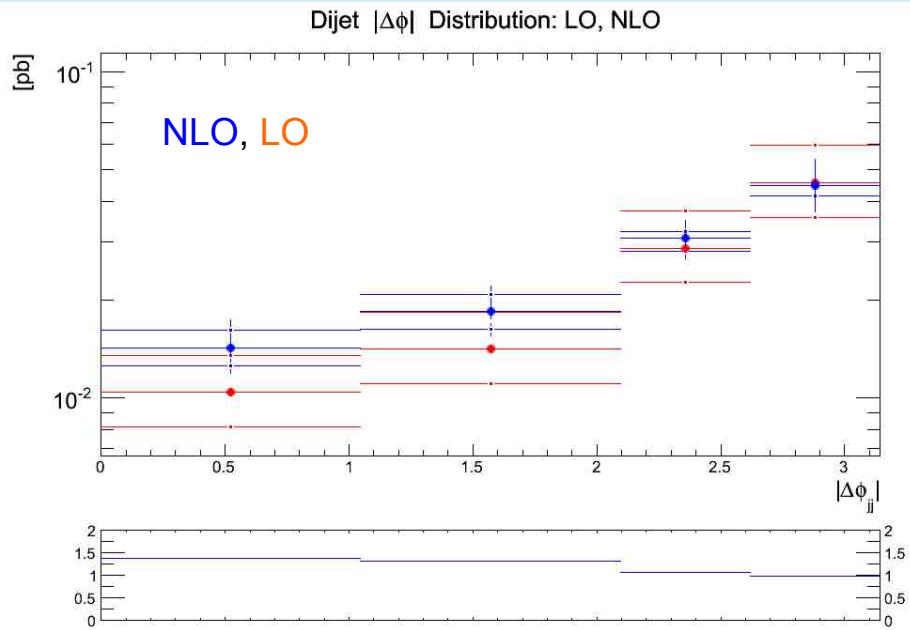
$|\Delta\phi_{jj}|$ distribution – altern. cuts

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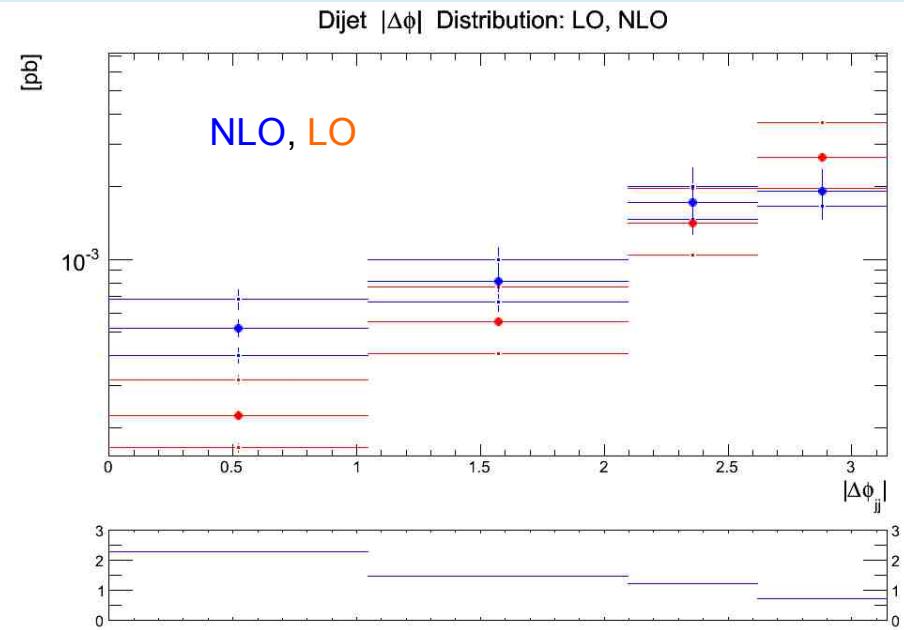
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Without VBF cuts



With VBF cuts



Large NLO correction for small values of $\Delta\phi$, especially after VBF cuts

Summary

- We have presented a full NLO calculation for $pp \rightarrow \gamma\gamma + 2\text{jets}$
- We have included the one loop $gg \rightarrow \gamma\gamma gg$ contribution
 - It contributes to the $\sim 2\%$ of the total cross section
- We have considered cuts on m_{jj} and $\Delta\eta_{jj}$ to highlight kinematic region where Vector Boson Fusion (VBF) dominates
- The NLO corrections : $\sim 20\%$ (without VBF cuts)
 $\sim 10\%$ (with VBF cuts)
- Larger corrections at small leading-jet's p_T and small diphoton and dijet invariant masses

Outlook:

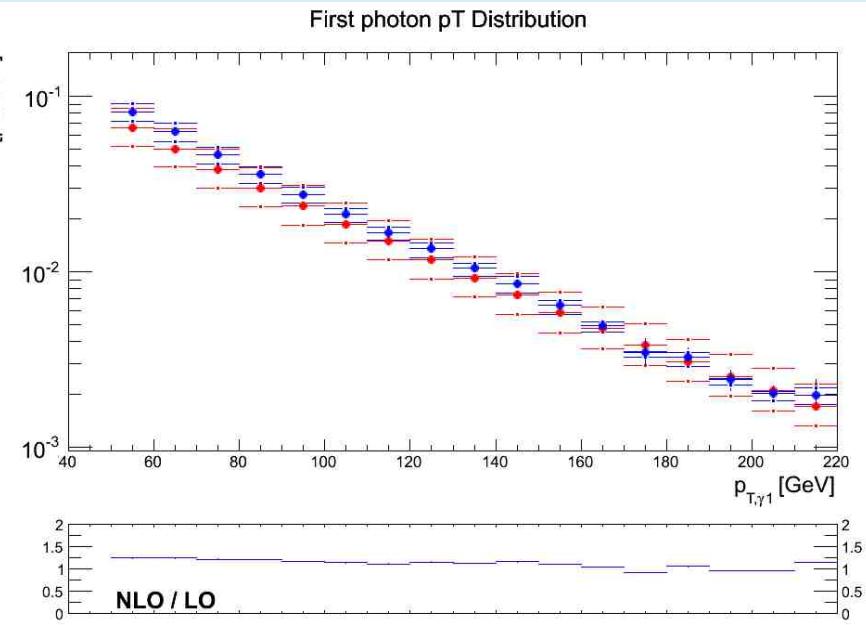
- dependence on Frixione cone's parameters (or other isolation criteria)
- estimate effect of including top-quark loops
- ...

Backup slides

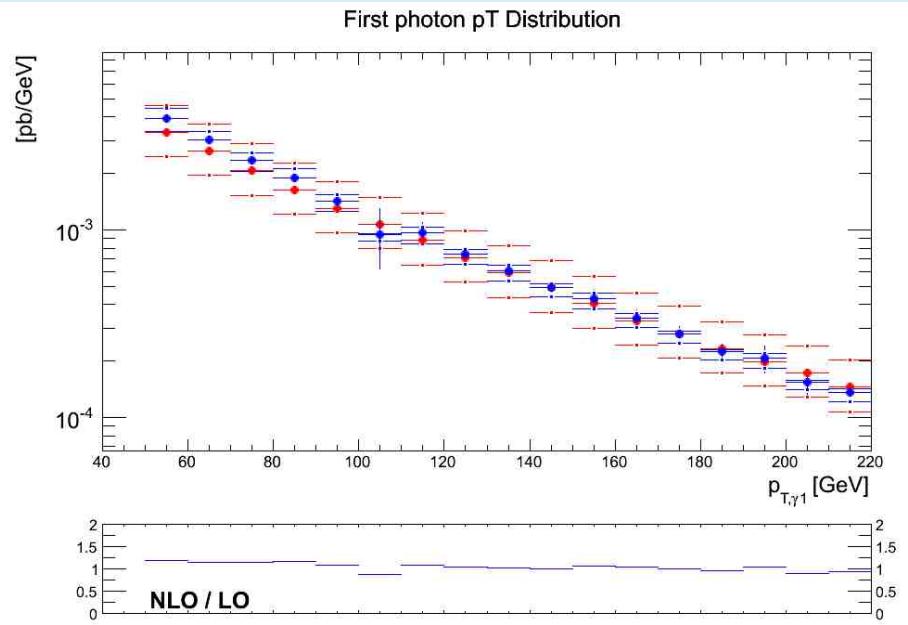
Leading photon's pT-distributions

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Without VBF cuts



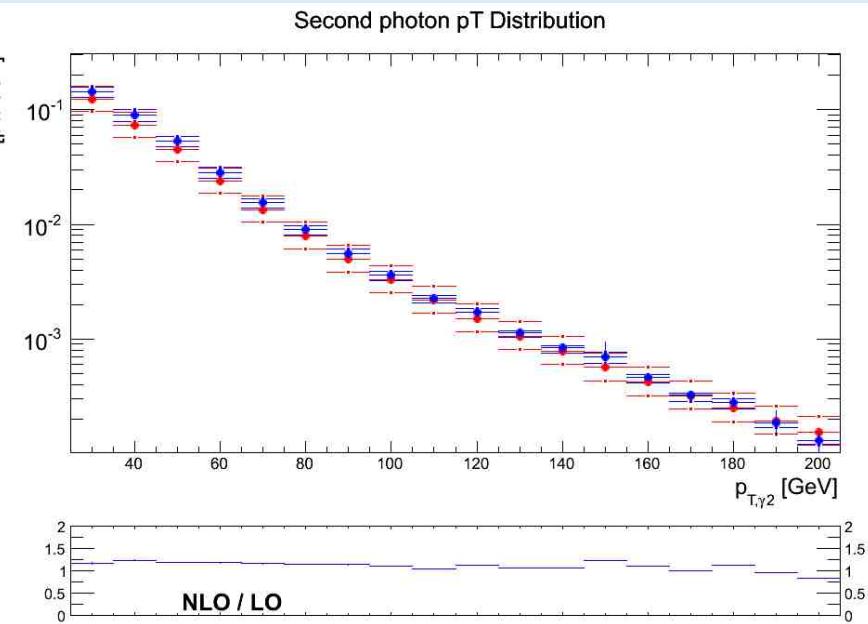
With VBF cuts



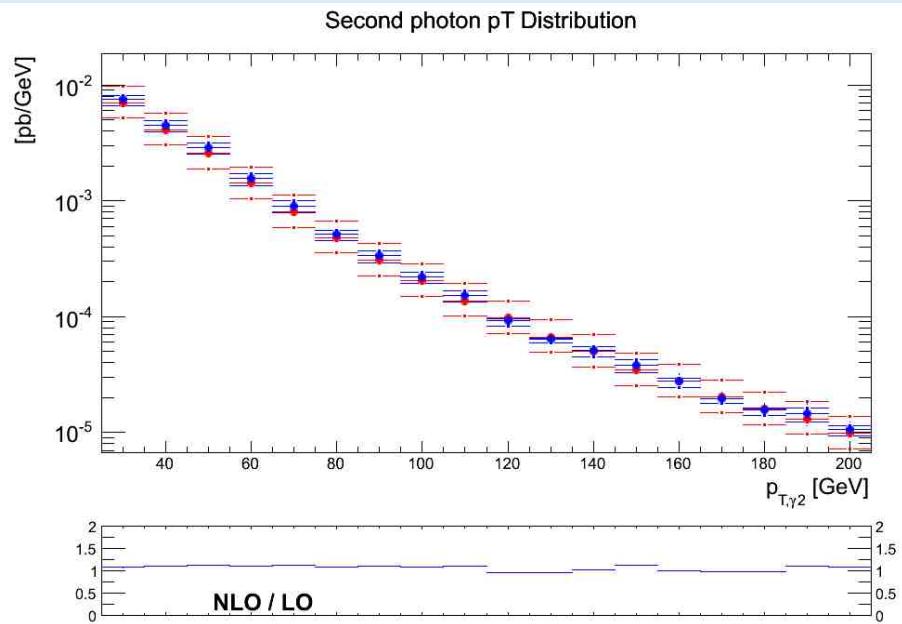
Second photons' pT-distributions

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Without VBF cuts



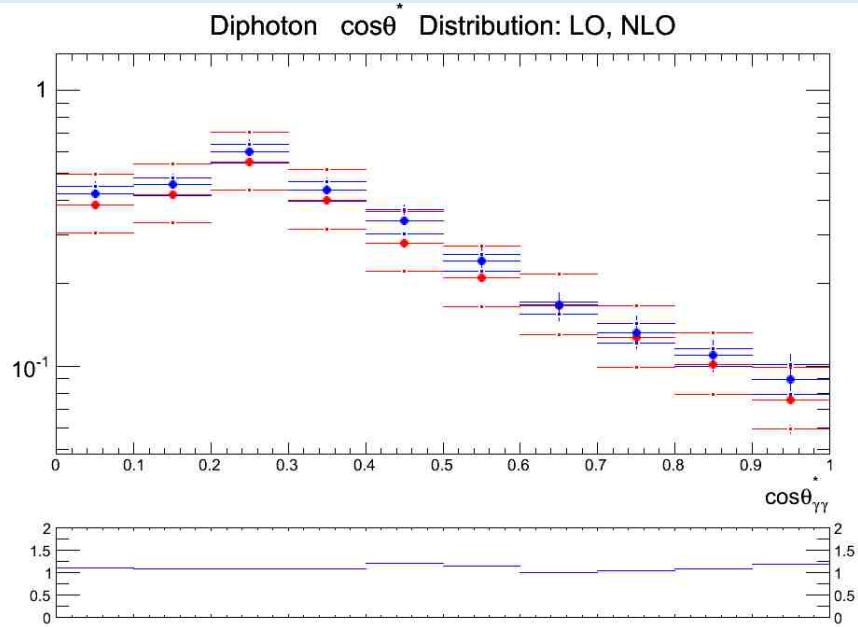
With VBF cuts



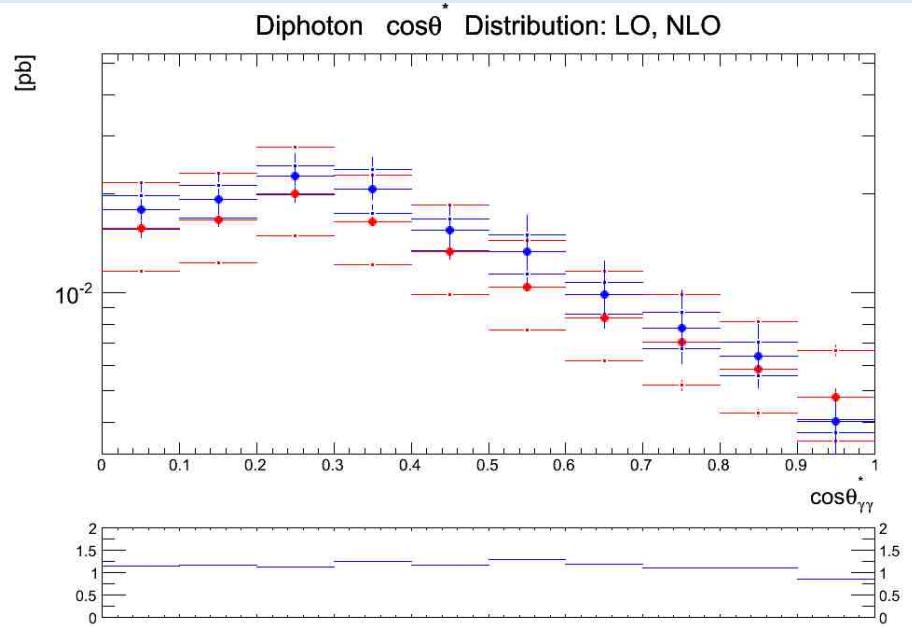
Alternative cuts

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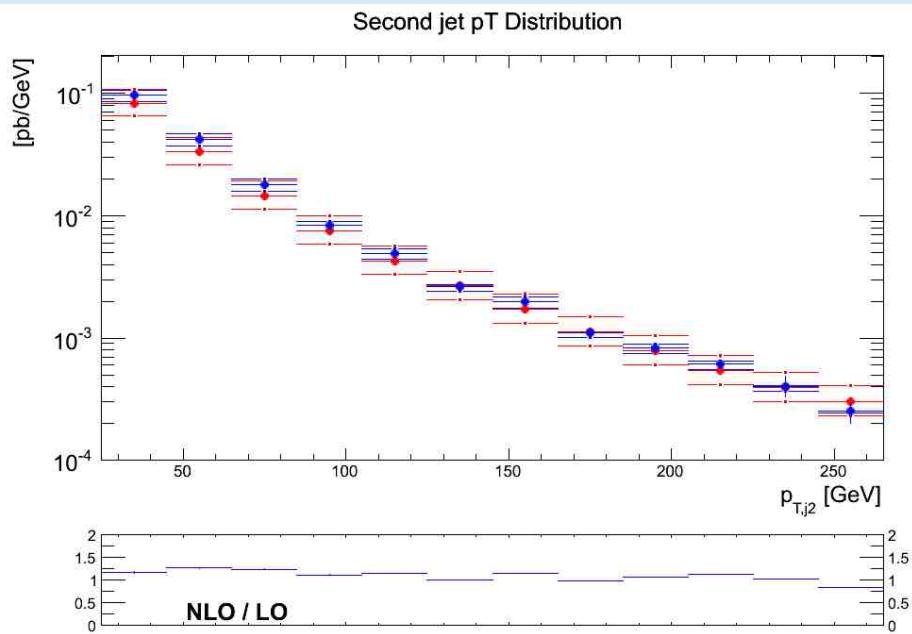
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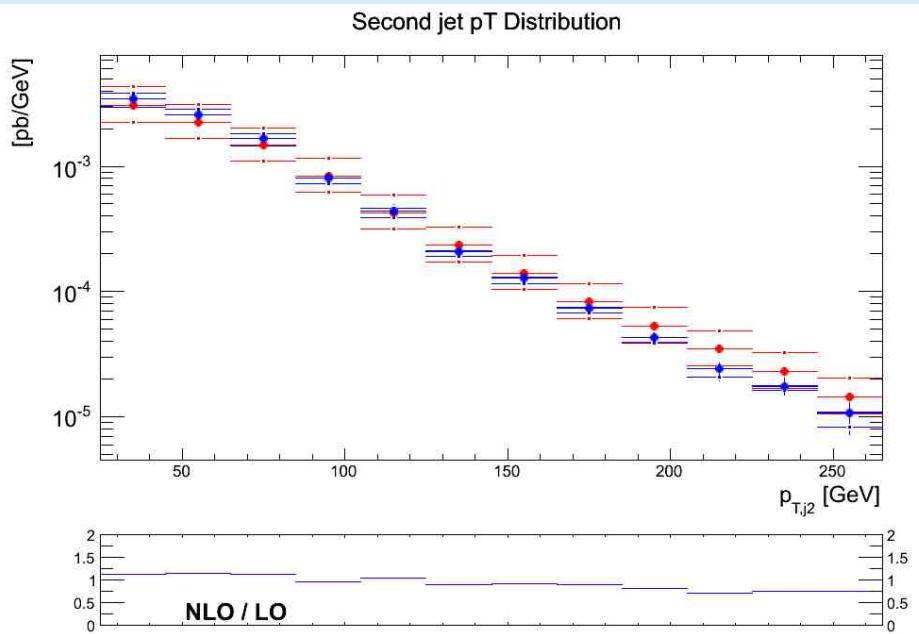
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$$\begin{aligned}
 \text{PDF} &= \text{MSTW}(2008), & \mu_0 &= \frac{1}{2} \left(p_T^{\gamma_1} + p_T^{\gamma_2} + \sum_m p_T^m \right), & \sqrt{s} &= 8 \text{ TeV} \\
 p_T^{\gamma_1} > 50 \text{ GeV}, & & p_T^{\gamma_2} > 25 \text{ GeV}, & & |\eta^\gamma| < 2.5, & & |\eta^{\text{jet}}| < 4.5, \\
 p_T^{\text{jet}_1} > 40 \text{ GeV}, & & p_T^{\text{jet}_2} > 25 \text{ GeV}, & & \left(M_{jj} > 400 \text{ GeV}, \quad \Delta \eta_{jj} > 2.8 \right)
 \end{aligned}$$

Without VBF cuts



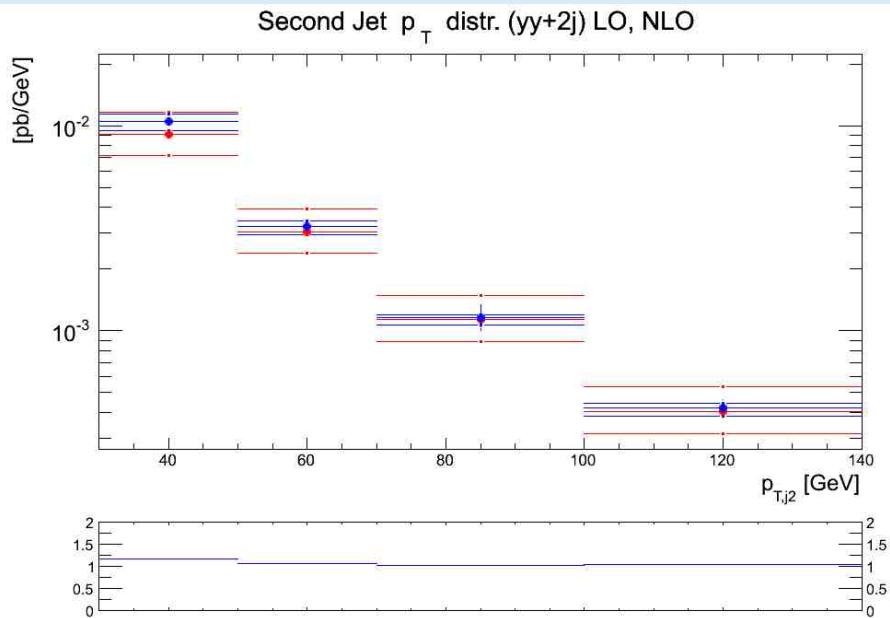
With VBF cuts



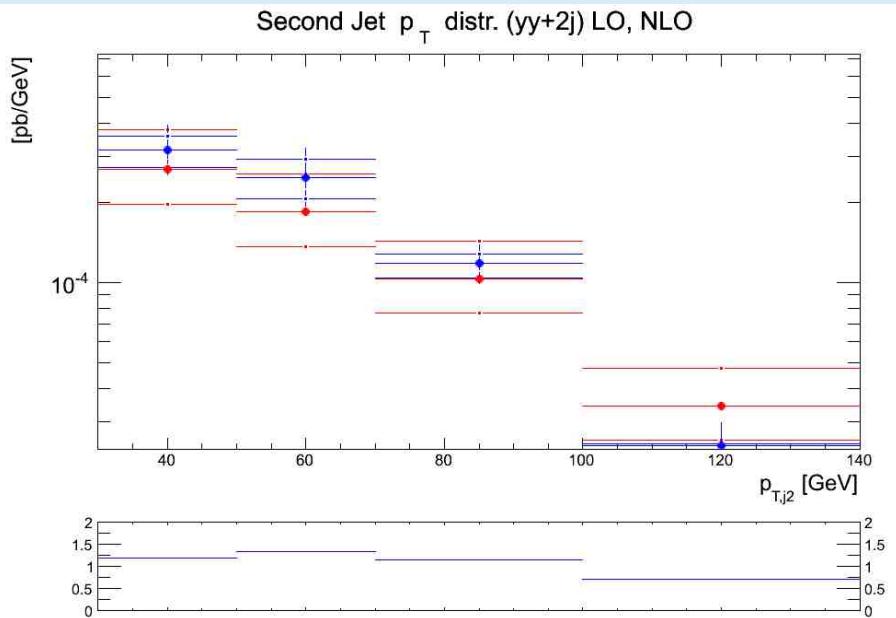
Second Jet's pT distribution with alternative cuts

$$\begin{aligned}
 \text{PDF} &= \text{MSTW}(2008), & \mu_0 &= \frac{1}{2} \left(p_T^{\gamma_1} + p_T^{\gamma_2} + \sum_m p_T^m \right), & \sqrt{s} &= 8 \text{ TeV} \\
 p_T^{\gamma_1} &> 0.35 m_{\gamma\gamma}, & p_T^{\gamma_2} &> 0.25 m_{\gamma\gamma}, & |\eta^\gamma| &< 2.37, & |\eta^{\text{jet}}| &< 4.4, \\
 p_T^{\text{jets}} &> 30 \text{ GeV}, & 122 \leq m_{\gamma\gamma} \leq 130 \text{ GeV}, & & & \left(M_{jj} > 400 \text{ GeV}, \quad \Delta \eta_{jj} > 2.8 \right)
 \end{aligned}$$

Without VBF cuts



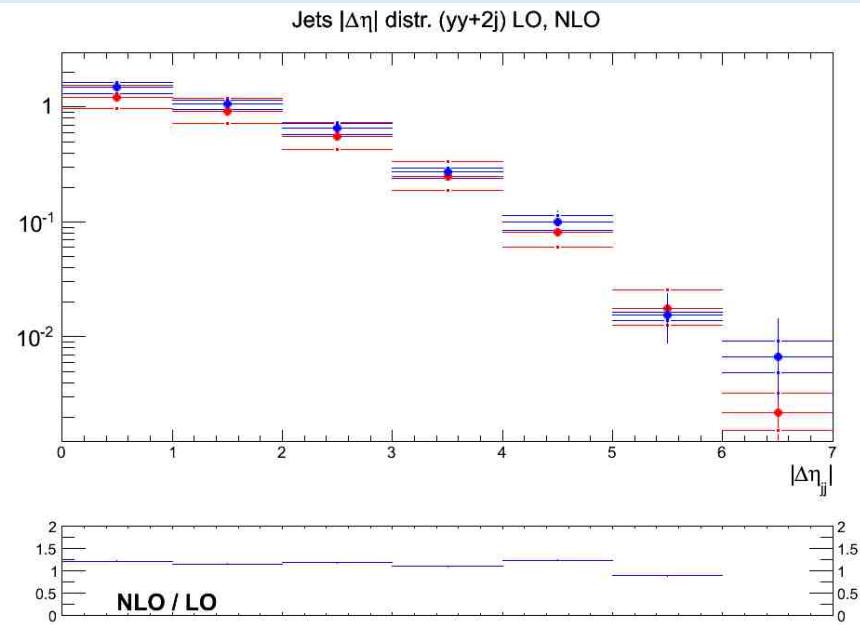
With VBF cuts



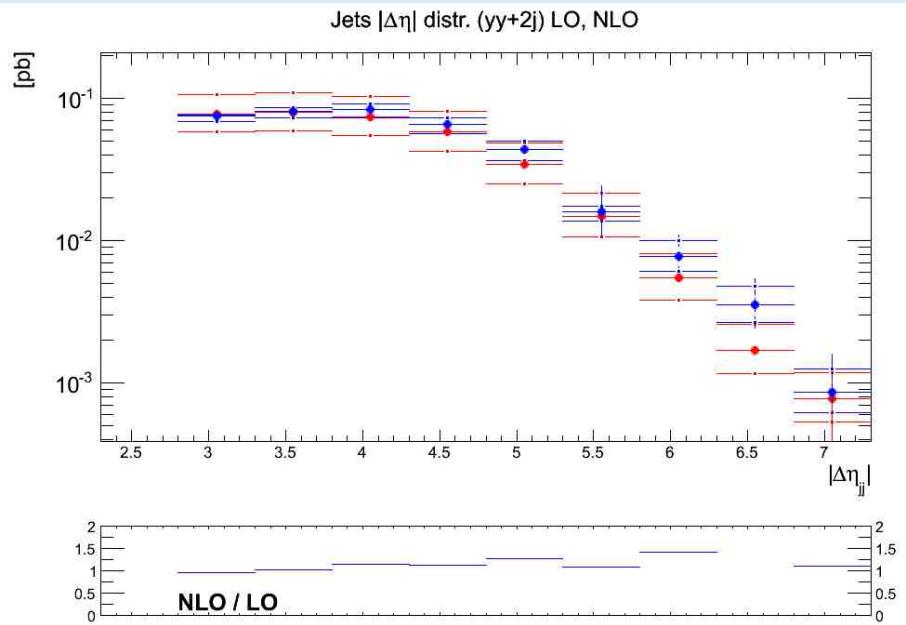
$\Delta\eta_{jj}$ -distributions

$$\begin{aligned}
 \text{PDF} &= \text{MSTW}(2008), & \mu_0 &= \frac{1}{2} \left(p_T^{\gamma_1} + p_T^{\gamma_2} + \sum_m p_T^m \right), & \sqrt{s} &= 8 \text{ TeV} \\
 p_T^{\gamma_1} &> 50 \text{ GeV}, & p_T^{\gamma_2} &> 25 \text{ GeV}, & |\eta^\gamma| &< 2.5, & |\eta^{\text{jet}}| &< 4.5, \\
 p_T^{\text{jet}_1} &> 40 \text{ GeV}, & p_T^{\text{jet}_2} &> 25 \text{ GeV}, & (M_{jj} &> 400 \text{ GeV}, & \Delta\eta_{jj} &> 2.8)
 \end{aligned}$$

Without VBF cuts



With VBF cuts



BH-Sherpa n -tuples

BH-Sherpa
 n -tuple branches

- id,
- nparticle,
- px, py, pz, E,
- x1, x2,
- x1p, x2p,
- id1, id2,
- kf
- alpha_power,
- alpha_s,
- fac_scale,
- ren_scale,
- weight,
- weight2,
- me_wgt,
- me_wgt2,
- nuwgt,
- usr_wgts,
- part

Changing the scale: Born and Real contribution

$$w = \mathbf{me_wgt2} \cdot f(\mathbf{id1}, \mathbf{x1}, \mu_F) F(\mathbf{id2}, \mathbf{x2}, \mu_F) \frac{\alpha_s(\mu_R)^n}{(\mathbf{alphas})^n}$$

BH-Sherpa n -tuples

BH-Sherpa
 n -tuple branches

id,
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px, py, pz, E,
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part

Changing the scale: Virtual contribution

$$w = m \cdot f(\mathbf{id1}, \mathbf{x1}, \mu_F) F(\mathbf{id2}, \mathbf{x2}, \mu_F) \frac{\alpha_s(\mu_R)^n}{(\mathbf{alphas})^n}$$

$$m = \mathbf{me_wgt2} + l \mathbf{usr_wgts[0]} + \frac{l^2}{2} \mathbf{usr_wgts[1]}$$

$$l = \ln \left(\frac{\mu_R^2}{\mathbf{ren_scale}^2} \right)$$

BH-Sherpa n -tuples

BH-Sherpa
 n -tuple branches

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- x1p, x2p,
- id1, id2,
- kf
- alpha_power,
- alpha_s,
- fac_scale,
- ren_scale,
- weight,
- weight2,
- me_wgt,
- me_wgt2,
- nuwgt,
- usr_wgts,
- part

Changing the scale: Integrated subtraction contribution

$$w = m \cdot \frac{\alpha_s(\mu_R)^n}{(\text{alphas})^n}$$

$$\begin{aligned} m = & \omega_0 \cdot f(\mathbf{id1}, \mathbf{x1}, \mu_F) F(\mathbf{id2}, \mathbf{x2}, \mu_F) \\ & + \left(f_a^1 \omega_1 + f_a^2 \omega_2 + f_a^3 \omega_3 + f_a^4 \omega_4 \right) F_b(x_b) \\ & + \left(F_b^5 \omega_1 + F_b^6 \omega_2 + F_b^7 \omega_3 + F_b^8 \omega_4 \right) F_a(x_a) \end{aligned}$$

$$\omega_0 = \mathbf{me_wgt2} + l \mathbf{usr_wgts}[0] + \frac{l^2}{2} \mathbf{usr_wgts}[1]$$

$$l = \ln \left(\frac{\mu_R^2}{\mathbf{ren_scale}^2} \right)$$

$$\omega_i = \mathbf{usr_wgts}[i+1] + \mathbf{usr_wgts}[i+9] \ln \left(\frac{\mu_F^2}{\mathbf{fac_scale}^2} \right)$$

BH-Sherpa n -tuples

BH-Sherpa
 n -tuple branches

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alpha_s,
fac_scale,
ren_scale,
weight,
weight2,
me_wgt,
me_wgt2,
nuwgt,
usr_wgts,
part

No need to repeat the entire computation at each scale:
Possible to evaluate cross sections and distributions for
different scales and PDFs !