

# Resummed predictions for the jet-veto Higgs cross section

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Precision Physics, Fundamental Interactions and Structure of Matter



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An Effective Field Theory Assault on the  
Zeptometer Scale: Exploring the Origins of  
Flavor and Electroweak Symmetry Breaking

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Durham, UK (22-27 September 2013)*

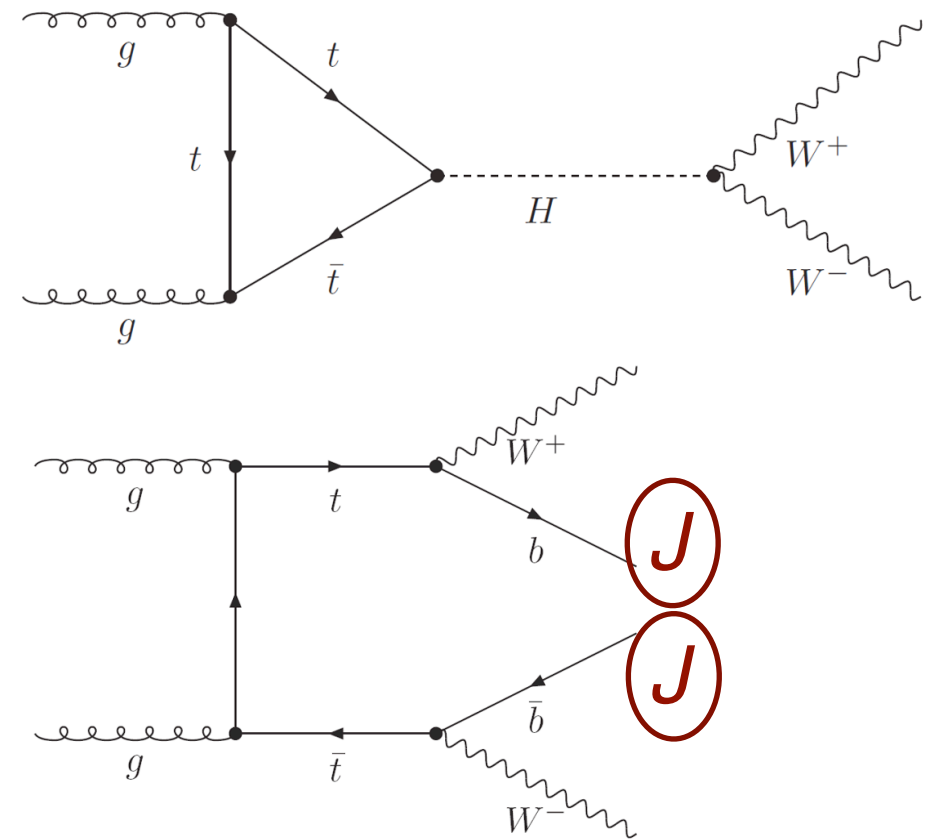
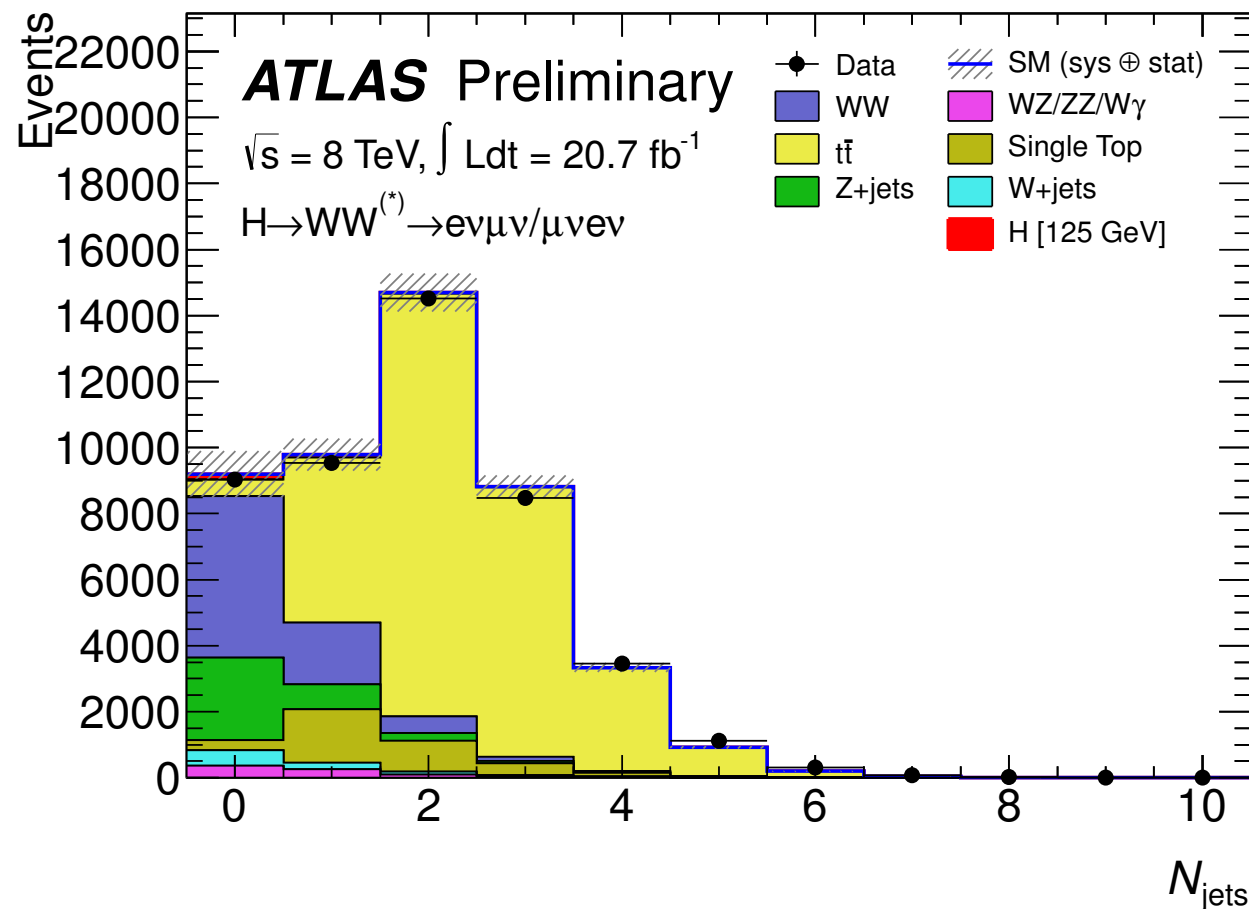




Why vetoing against jets can be important ...

Becher, MN 1205.3806 (JHEP)  
Becher, MN, Rothen 1307.0025 (JHEP)

# Jet veto in Higgs production

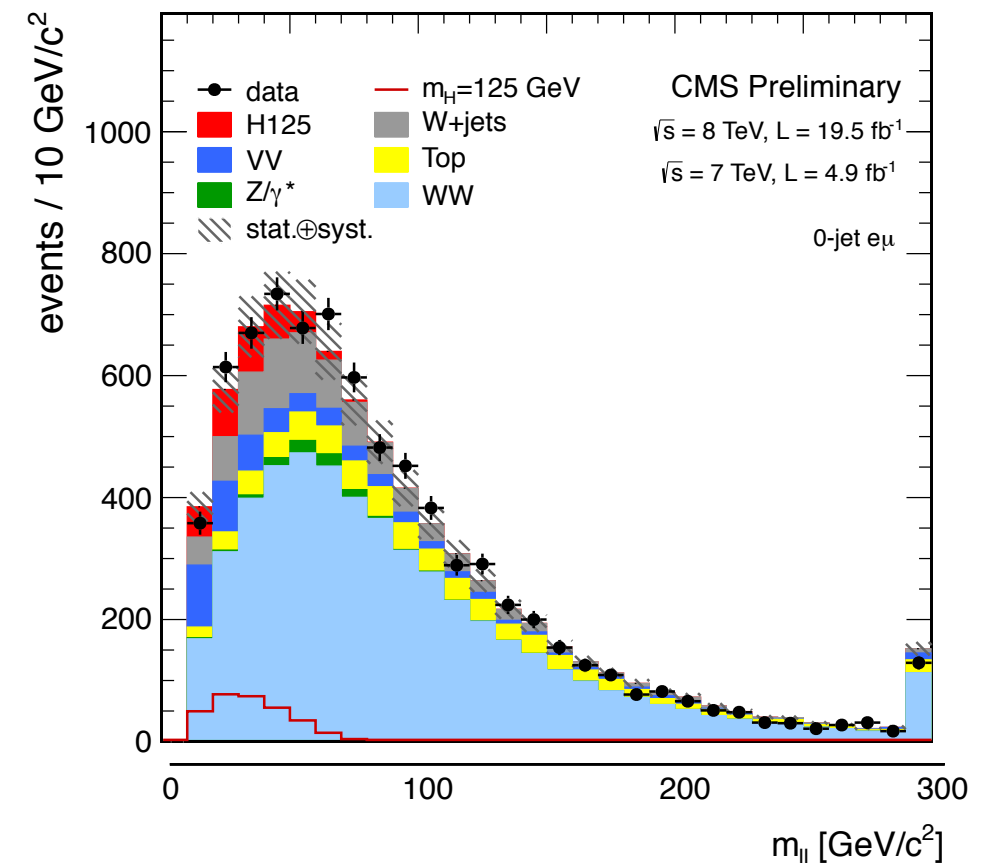
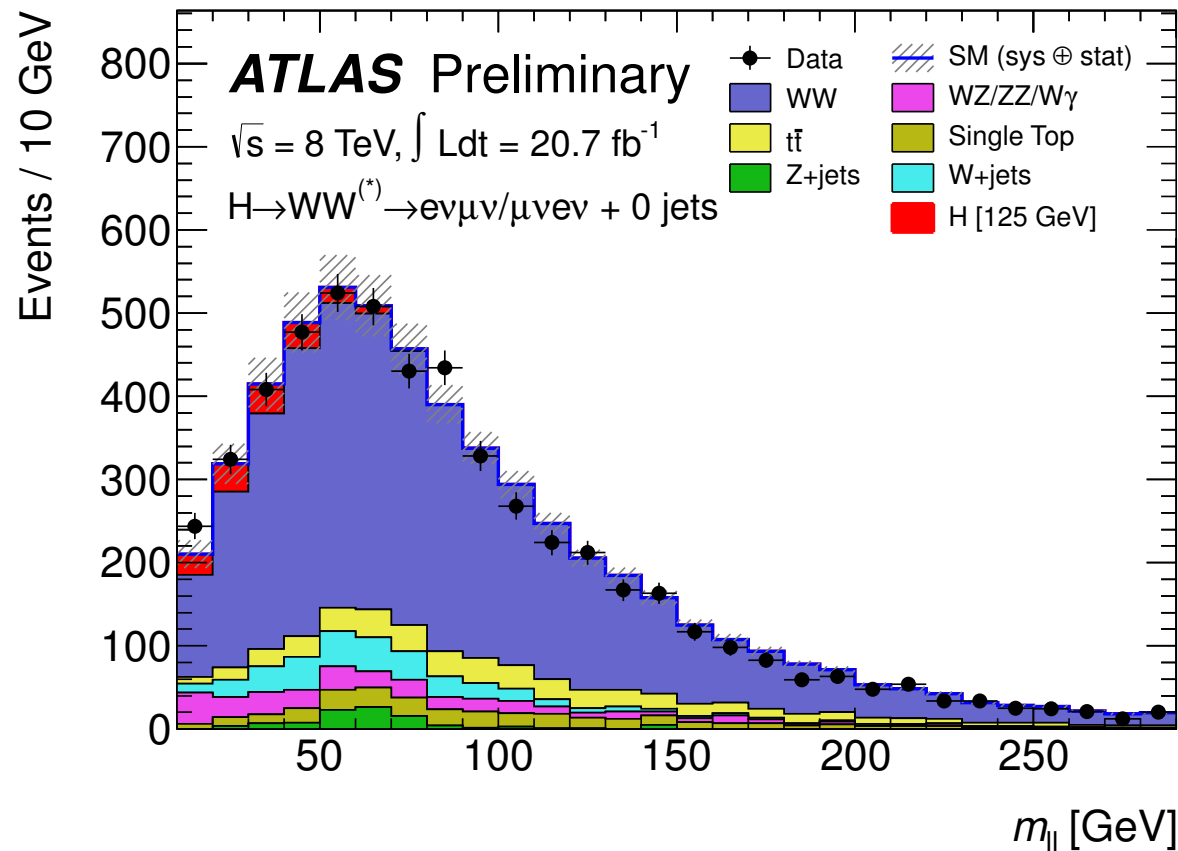


Analysis is done in jet bins, since background is very different when Higgs is produced in association with jets

Need precise predictions for  $H + n$  jets, in particular for the 0-jet bin, i.e. the cross section defined with a jet veto:

$$p_T^{\text{jet}} < p_T^{\text{veto}} \sim 20\text{-}30 \text{ GeV}$$

# Jet veto in Higgs production



**ATLAS:** significance  $3.8\sigma$  (exp:  $3.7\sigma$ )

$$\mu_{\text{obs}} = 1.01 \pm 0.21 \text{ (stat.)} \pm 0.19 \text{ (theo. syst.)} \pm 0.12 \text{ (expt. syst.)} \pm 0.04 \text{ (lumi.)}$$

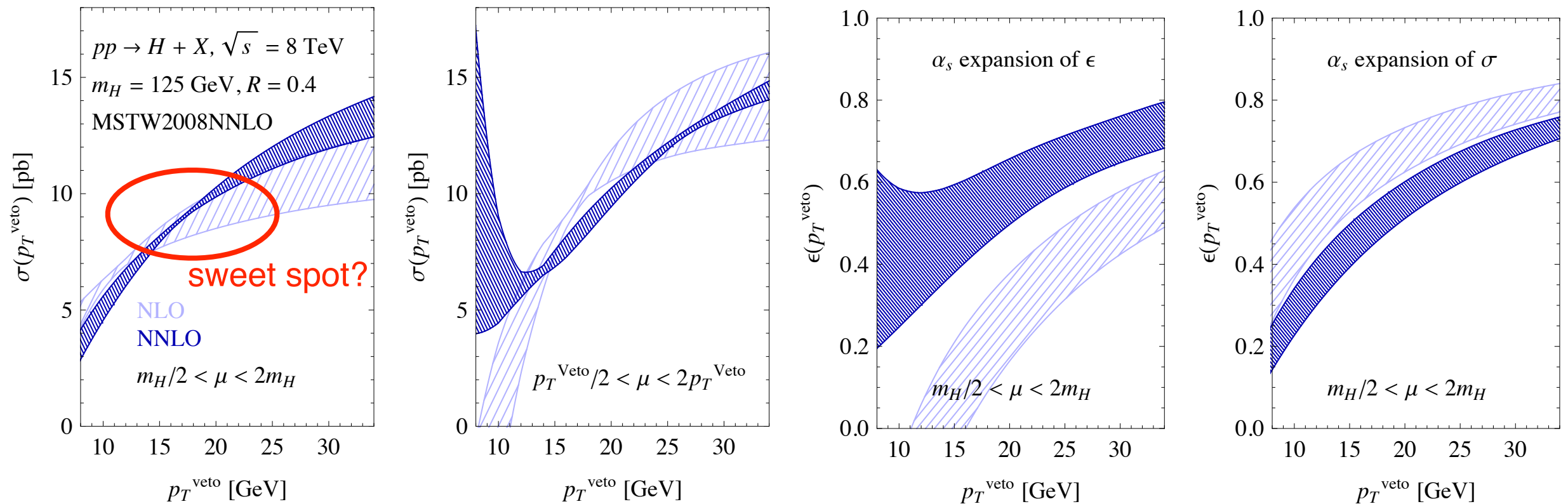
$$= 1.01 \pm 0.31$$

**CMS:** significance  $4.0\sigma$  (exp:  $5.1\sigma$ )

$$\mu_{\text{obs}} = 0.76 \pm 0.21$$



# Fixed-order predictions



Smaller scale uncertainty than  $\sigma_{\text{tot}}$ , due to accidental cancellation:

- **large positive corrections** to  $\sigma_{\text{tot}}$  from analytic continuation of scalar form factor [Ahrens, Becher, MN, Yang '09](#)
- **large negative corrections** from collinear logs

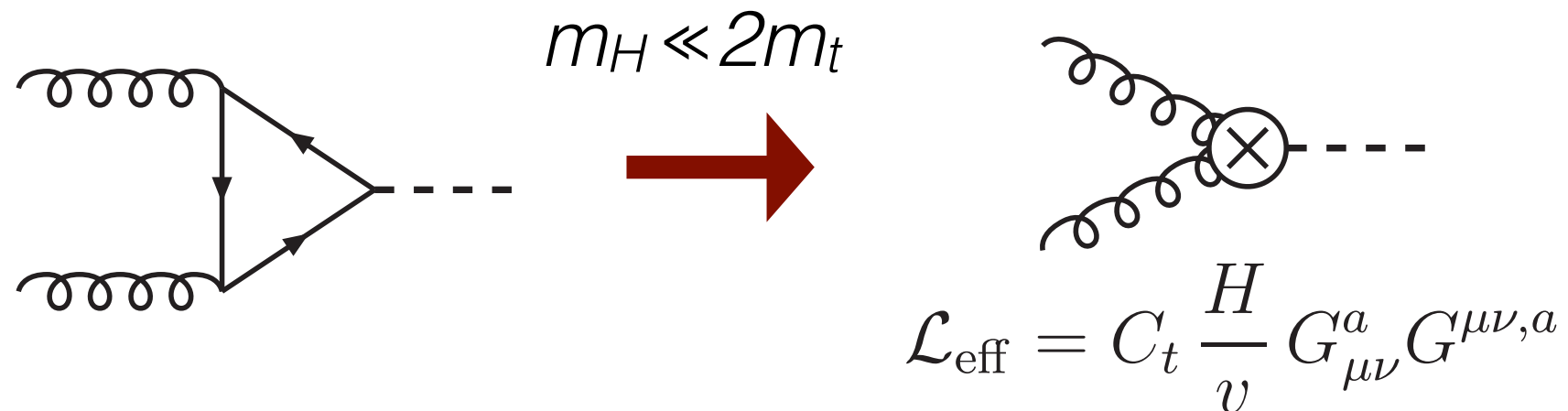
$$\alpha_s^n \ln^{2n} \frac{p_T^{\text{Veto}}}{m_H}$$

Equivalent schemes give quite different predictions, hence **scale-variation bands do not reflect true uncertainties!**

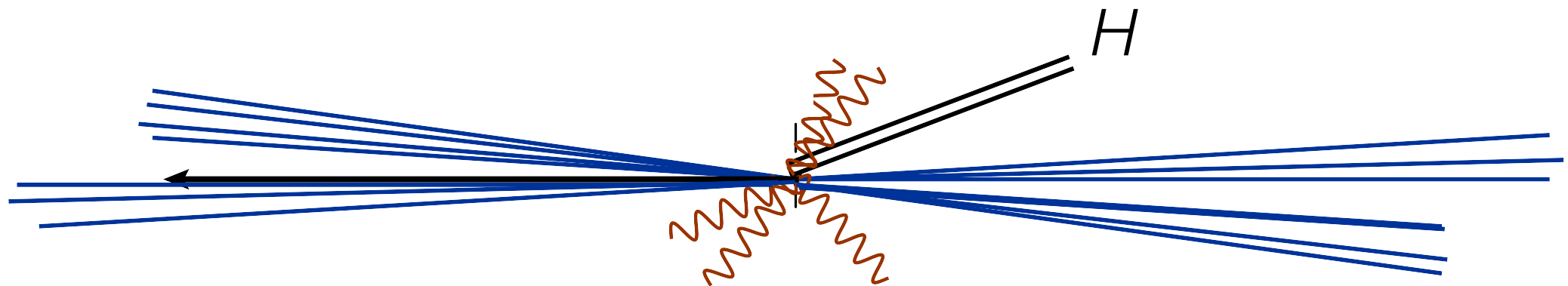
(see also: [Stewart, Tackmann '10](#))

# Scale hierarchies and EFTs

Heavy top quark:



Small  $p_T \ll m_H$ :

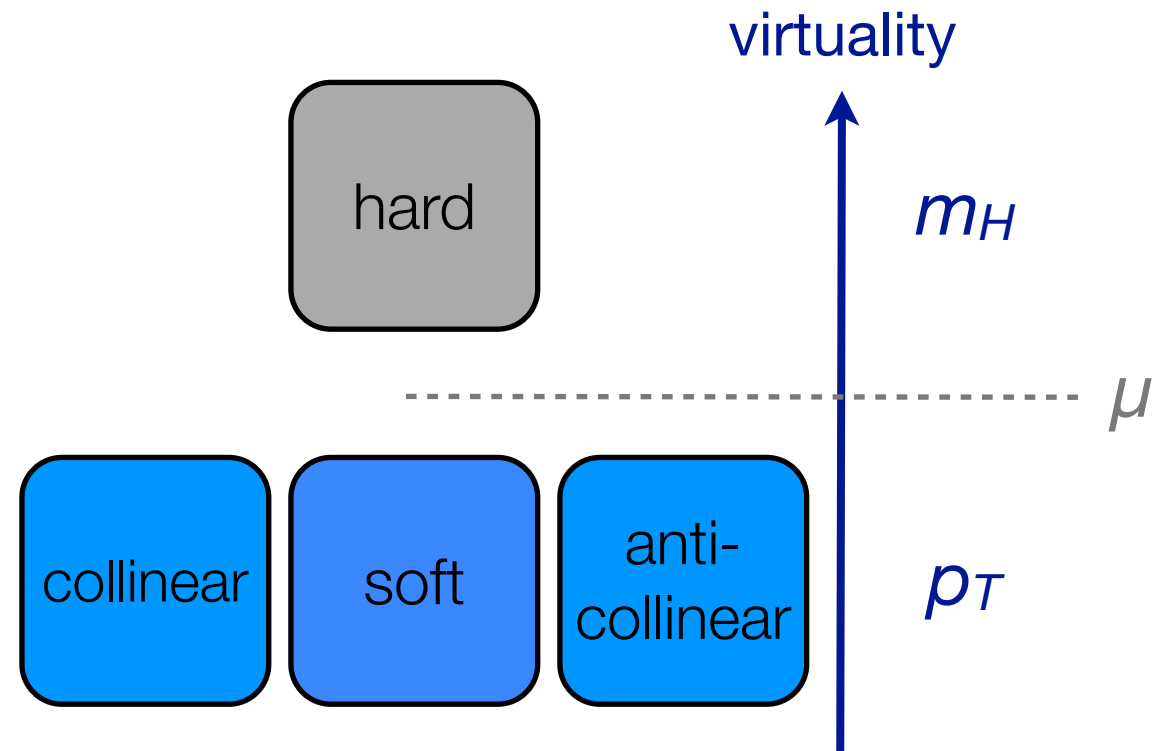


Only soft and (anti-)collinear emissions:

factorization & resummation using  
**Soft-Collinear Effective Theory**

# “Anomalous” ( $p_T$ ) factorization (SCET<sub>II</sub>)

Applicable for observables probing parton transverse momenta



**Puzzle:** The cross section can only be  $\mu$  independent if also the low-energy part is  $m_H$  dependent:

$$\ln^2 \frac{m_H^2}{p_T^2} = \ln^2 \frac{m_H^2}{\mu^2} - \ln^2 \frac{p_T^2}{\mu^2} + ?$$

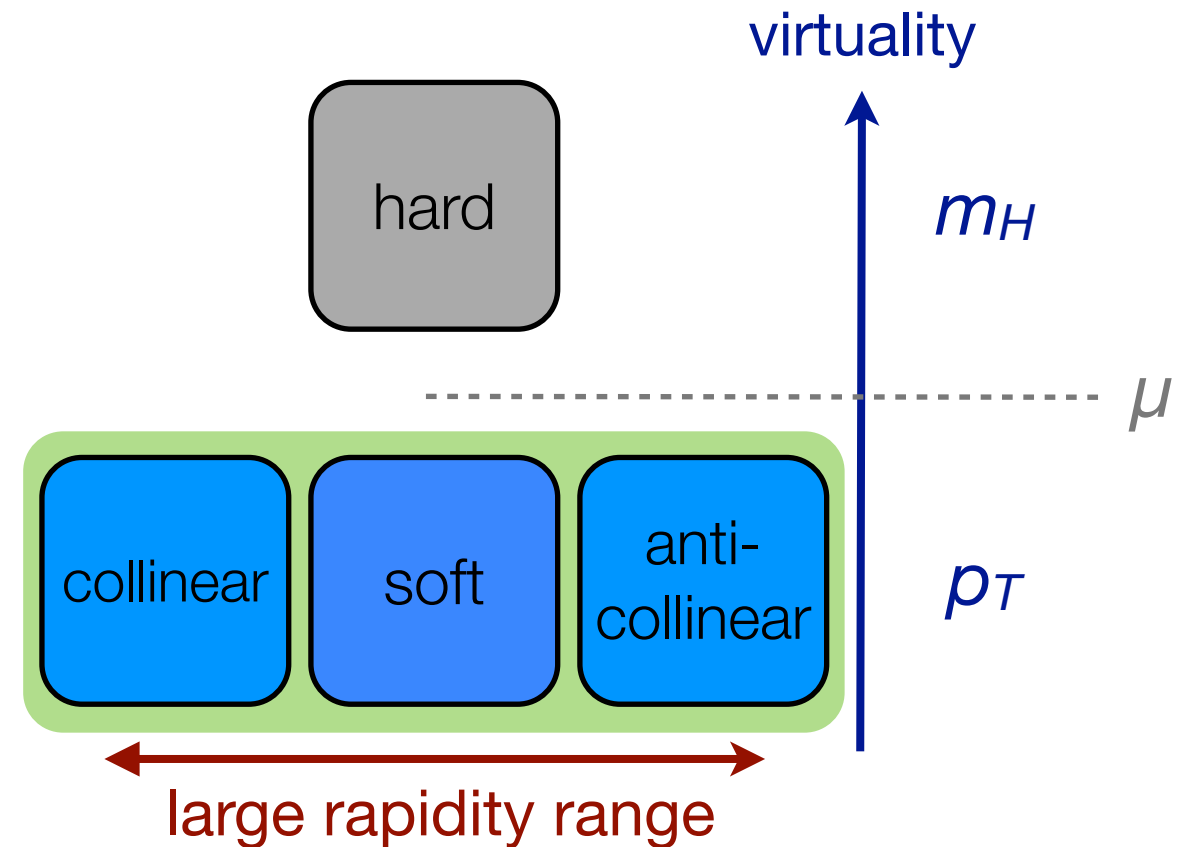
hard

collinear/soft

region decomposition of a Sudakov double logarithm

# “Anomalous” ( $p_T$ ) factorization (SCET<sub>II</sub>)

Applicable for observables probing parton transverse momenta



**Resolution:**  $m_H$  dependence arises from a **collinear factorization anomaly** in the effective theory

Becher, MN '10

$$\ln^2 \frac{m_H^2}{p_T^2} = \ln^2 \frac{m_H^2}{\mu^2} - \ln^2 \frac{p_T^2}{\mu^2} - 2 \ln \frac{p_T^2}{\mu^2} \ln \frac{m_H^2}{p_T^2}$$

hard

collinear/soft

region decomposition of a Sudakov double logarithm



# Examples of “anomalous” factorization

SCET computations for many transverse-momentum observables are now available:

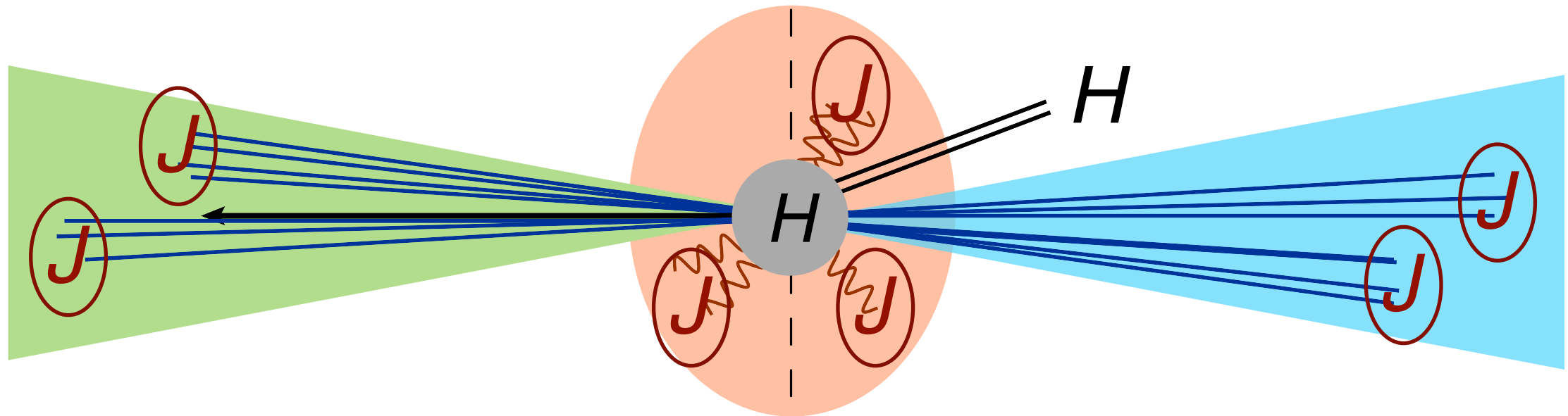
- NNLL  $q_T$  spectra for  $W$ ,  $Z$ ,  $H$  [Becher, MN '11](#); + [Wilhelm '12](#)
- 2-loop matching of TPDFs [Gehrmann, Lübbert, Yang '12](#)  
(important ingredient for N<sup>3</sup>LL resummation and NNLO matching for  $q_T$  spectra) → [talk by T. Lübbert \(Monday pm\)](#)
- Jet broadening at NNLL [Becher, MN '11](#); [Becher, Bell '12](#)
- Transverse-momentum resummation for  $\bar{t}t$  production  
[Li, Li, Shao, Yang, Zhu '12](#)

# Resummation for the jet veto

A lot of progress over the last year:

- **NLL resummation based on CAESAR**  
Banfi, Salam and Zanderighi (BSZ) 1203.5773
- **All-order factorization theorem in SCET**  
Becher and MN (BN) 1205.3806
- **NNLL resummation**  
BSZ + Monni (BSZM) 1206.4998
- **Clustering logarithms spoil factorization (?)**  
Tackmann, Walsh, Zuberi (TWZ) 1206.4312
- **Absence of clustering logarithms at NNLL and beyond**  
Becher, MN and Rothen 1307.0025
- **NLL for  $n$ -jet bins with  $n > 0$**   
Liu and Petriello 1210.1906, 1303.4405  
(but without resummation of non-global logarithms)

# Factorization theorem



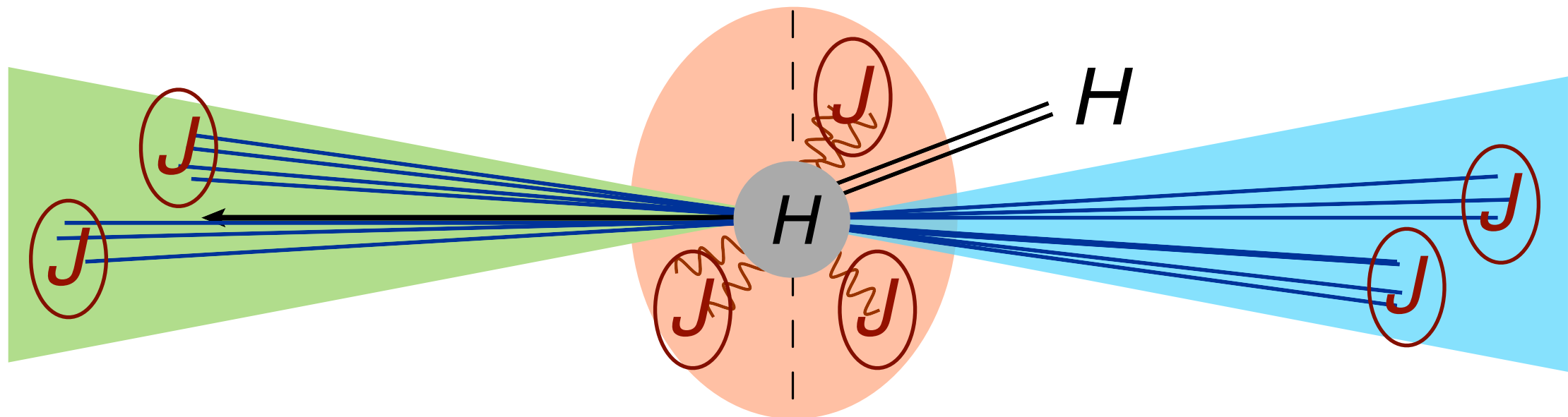
- Work with usual sequential recombination jet algorithms:

$$d_{ij} = \min(p_{Ti}^n, p_{Tj}^n) \frac{\sqrt{\Delta y_{ij}^2 + \Delta \phi_{ij}^2}}{R}, \quad d_{iB} = p_{Ti}^n$$

with  $n=1$  ( $k_T$ ),  $n=-1$  (anti- $k_T$ ), or  $n=0$  (Cambridge-Aachen)

- As long as  **$R < \ln(m_H/p_T)$  parametrically**, such an algorithm will **cluster soft and collinear radiation separately**

# Factorization theorem



The jet veto thus translates into a veto in each individual sector (collinear, anti-collinear, and soft):

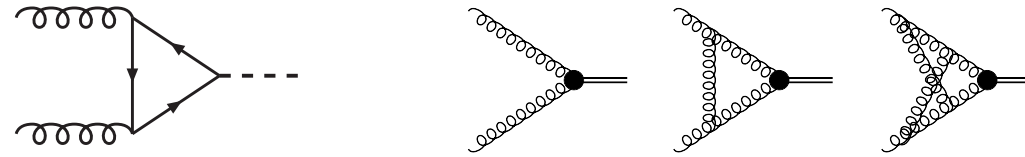
$$\sigma(p_T^{\text{veto}}) \propto H(m_H, \mu) \left[ \mathcal{B}_c(\xi_1, p_T^{\text{veto}}, \mu) \mathcal{B}_{\bar{c}}(\xi_2, p_T^{\text{veto}}, \mu) \mathcal{S}(p_T^{\text{veto}}, \mu) \right]_{q^2=m_H^2}$$

longitudinal momentum fractions:  $\xi_{1,2} = \frac{m_H}{\sqrt{s}} e^{\pm y_H}$

Becher, MN '12

# Factorization theorem

Hard function:



$$H(m_H, \mu) = C_t^2(m_t^2, \mu) |C_S(-m_H^2, \mu)|^2$$

Collinear beam function:

$$\mathcal{B}_{c,g}(z, p_T^{\text{veto}}, \mu) = -\frac{z \bar{n} \cdot p}{2\pi} \int dt e^{-izt\bar{n} \cdot p} \sum_{X_c, \text{reg.}} \mathcal{M}_{\text{veto}}(p_T^{\text{veto}}, R, \{\underline{p}_c\})$$

measurement function

$$\times \langle P(p) | \mathcal{A}_{c\perp}^{\mu,a}(t\bar{n}) | X_c \rangle \langle X_c | \mathcal{A}_{c\perp\mu}^a(0) | P(p) \rangle ,$$

Soft function:

$$\mathcal{S}(p_T^{\text{veto}}, \mu) = \frac{1}{d_R} \sum_{X_c, \text{reg.}} \mathcal{M}_{\text{veto}}(p_T^{\text{veto}}, R, \{\underline{p}_s\}) \langle 0 | (S_n^\dagger S_{\bar{n}})^{ab}(0) | X_s \rangle \langle X_s | (S_{\bar{n}}^\dagger S_n)^{ba}(0) | 0 \rangle$$



# Analytic phase-space regularization

Presence of measurement functions gives rise to **light-cone (rapidity) divergences** in SCET phase-space integrals, which are not regularized dimensionally; introduce **analytic regulator**:

$$\int d^d k \, \delta(k^2) \theta(k^0) \rightarrow \int d^d k \left( \frac{\nu}{k_+} \right)^\alpha \delta(k^2) \theta(k^0) = \frac{1}{2} \int dy \int d^{d-2} k_\perp \left( \frac{\nu}{k_T} \right)^\alpha e^{-\alpha y}$$

Becher, Bell '12

Divergences in  $\alpha$  cancel when the different sectors of SCET are combined, but an **anomalous dependence on  $m_H$**  remains


- consistency conditions (DEQs) fix the all-order form of the  $m_H$  dependence    Chiu, Golf, Kelley, Manohar '07; Becher, MN '10

**Alternative scheme:** “Rapidity renormalization group” based on regularization of Wilson lines    Chiu, Jain, Neill, Rothstein '12

# Collinear anomaly

Refactorization theorem:

$$\begin{aligned}
 & \left[ \mathcal{B}_c(\xi_1, p_T^{\text{veto}}, \mu) \mathcal{B}_{\bar{c}}(\xi_2, p_T^{\text{veto}}, \mu) \mathcal{S}(p_T^{\text{veto}}, \mu) \right]_{q^2=m_H^2} \\
 &= \left( \frac{m_H}{p_T^{\text{veto}}} \right)^{-2F_{gg}(p_T^{\text{veto}}, \mu)} e^{2h_A(p_T^{\text{veto}}, \mu)} \bar{B}_g(\xi_1, p_T^{\text{veto}}) \bar{B}_g(\xi_2, p_T^{\text{veto}})
 \end{aligned}$$


 RG invariant

Becher, MN '12

- first term (the “anomaly”) provides an extra source of large logarithms!
- without loss of generality, the soft function has been absorbed into the final, RG-invariant beam function  $\bar{B}_g(\xi, p_T)$

# Collinear anomaly

Refactorization theorem:

$$\begin{aligned}
 & \left[ \mathcal{B}_c(\xi_1, p_T^{\text{veto}}, \mu) \mathcal{B}_{\bar{c}}(\xi_2, p_T^{\text{veto}}, \mu) \mathcal{S}(p_T^{\text{veto}}, \mu) \right]_{q^2=m_H^2} \\
 &= \left( \frac{m_H}{p_T^{\text{veto}}} \right)^{-2F_{gg}(p_T^{\text{veto}}, \mu)} e^{2h_A(p_T^{\text{veto}}, \mu)} \bar{B}_g(\xi_1, p_T^{\text{veto}}) \bar{B}_g(\xi_2, p_T^{\text{veto}})
 \end{aligned}$$

RG invariant

Becher, MN '12

RG invariance of the cross section is ensured by the evolution equations:

$$\frac{d}{d \ln \mu} F_{gg}(p_T^{\text{veto}}, \mu) = 2\Gamma_{\text{cusp}}^A(\mu)$$

$$\frac{d}{d \ln \mu} h_A(p_T^{\text{veto}}, \mu) = 2\Gamma_{\text{cusp}}^A(\mu) \ln \frac{\mu}{p_T^{\text{veto}}} - 2\gamma^g(\mu)$$

# Collinear anomaly

Refactorization theorem:

$$\left[ \mathcal{B}_c(\xi_1, p_T^{\text{veto}}, \mu) \mathcal{B}_{\bar{c}}(\xi_2, p_T^{\text{veto}}, \mu) \mathcal{S}(p_T^{\text{veto}}, \mu) \right]_{q^2=m_H^2}$$

$$= \left( \frac{m_H}{p_T^{\text{veto}}} \right)^{-2F_{gg}(p_T^{\text{veto}}, \mu)} e^{2h_A(p_T^{\text{veto}}, \mu)} \bar{B}_g(\xi_1, p_T^{\text{veto}}) \bar{B}_g(\xi_2, p_T^{\text{veto}})$$

RG invariant

Becher, MN '12

General solutions, with  $a_s = \alpha_s(\mu)/(4\pi)$  and  $L_\perp = 2 \ln(\mu/p_T^{\text{veto}})$ :

$$F_{gg}(p_T^{\text{veto}}, \mu) = a_s \left[ \Gamma_0^A L_\perp + d_1^{\text{veto}}(R) \right] + a_s^2 \left[ \Gamma_0^A \beta_0 \frac{L_\perp^2}{2} + \Gamma_1^A L_\perp + d_2^{\text{veto}}(R) \right]$$

$$+ a_s^3 \left[ \Gamma_0^A \beta_0^2 \frac{L_\perp^3}{3} + (\Gamma_0^A \beta_1 + 2\Gamma_1^A \beta_0) \frac{L_\perp^2}{2} + L_\perp (\Gamma_2^A + 2\beta_0 d_2^{\text{veto}}(R)) + d_3^{\text{veto}}(R) \right]$$

$$h_A(p_T^{\text{veto}}, \mu) = a_s \left[ \Gamma_0^A \frac{L_\perp^2}{4} - \gamma_0^g L_\perp \right] + a_s^2 \left[ \Gamma_0^A \beta_0 \frac{L_\perp^3}{12} + (\Gamma_1^A - 2\gamma_0^g \beta_0) \frac{L_\perp^2}{4} - \gamma_1^g L_\perp \right]$$

# Final factorization theorem

Complete **all-order factorization theorem** for  $R=O(1)$ :

$$\frac{d\sigma(p_T^{\text{veto}})}{dy} = \sigma_0(p_T^{\text{veto}}) \bar{H}(m_t, m_H, p_T^{\text{veto}}) \bar{B}_g(\xi_1, p_T^{\text{veto}}) \bar{B}_g(\xi_2, p_T^{\text{veto}})$$

**New!**

RG-invariant, resummed hard function (with  $\mu \sim p_T^{\text{veto}}$ ):

$$\begin{aligned} \bar{H}(m_t, m_H, p_T^{\text{veto}}) = & \left( \frac{\alpha_s(\mu)}{\alpha_s(p_T^{\text{veto}})} \right)^2 C_t^2(m_t^2, \mu) |C_S(-m_H^2, \mu)|^2 \\ & \times \left( \frac{m_H}{p_T^{\text{veto}}} \right)^{-2F_{gg}(p_T^{\text{veto}}, \mu)} e^{2h_A(p_T^{\text{veto}}, \mu)} \end{aligned}$$



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For  $p_T^{\text{veto}} \gg \Lambda_{\text{QCD}}$ , the beam function can be further factorized as:

$$\bar{B}_g(\xi, p_T^{\text{veto}}) = \sum_{i=g,q,\bar{q}} \int_{\xi}^1 \frac{dz}{z} \bar{I}_{g \leftarrow i}(z, p_T^{\text{veto}}, \mu) \phi_{i/P}(\xi/z, \mu)$$

perturbative    standard PDFs

# Final factorization theorem

Complete **all-order factorization theorem** for  $R=O(1)$ :

$$\frac{d\sigma(p_T^{\text{veto}})}{dy} = \sigma_0(p_T^{\text{veto}}) \bar{H}(m_t, m_H, p_T^{\text{veto}}) \bar{B}_g(\xi_1, p_T^{\text{veto}}) \bar{B}_g(\xi_2, p_T^{\text{veto}})$$

Inclusion of power corrections in  $p_T^{\text{veto}}/m_H$  by matching to fixed-order perturbation theory (known to NNLO):

$$\frac{\sigma(p_T^{\text{veto}})}{\bar{H}(m_t, m_H, p_T^{\text{veto}})} \equiv \bar{\sigma}_\infty(p_T^{\text{veto}}) + \Delta\bar{\sigma}(p_T^{\text{veto}}) \quad \leftarrow \text{power corrections}$$

$$\bar{\sigma}_\infty(p_T^{\text{veto}}) = \sigma_0(p_T^{\text{veto}}) \int_{-y_{\text{max}}}^{y_{\text{max}}} dy \bar{B}_g(\tau e^y, p_T^{\text{veto}}) \bar{B}_g(\tau e^{-y}, p_T^{\text{veto}})$$

 **RG invariant and free of large logs;  
can be evaluated in fixed-order perturbation theory**

# Resummation at NNLL order

Ingredients required for NNLL resummation:

- one-loop  $\bar{H}$  and  $\bar{I}_{g \leftarrow i}$  (known analytically)
- three-loop cusp anomalous dimension and other two-loop anomalous dimensions (known)
- two-loop anomaly coefficient  $d_2^{\text{veto}}(R)$ , which in [BN](#) we extracted from the results of [BSZM](#); we have now calculated this coefficient independently within SCET, finding complete agreement
- find that factorization-breaking soft-collinear mixing terms, claimed by [TWZ](#) to arise at NNLL order, **do not exist!**

# Resummation at NNLL order

Analytic result for  $d_2^{\text{veto}}(R)$  as a power expansion in  $R$ :

$$d_2^{\text{veto}}(R) = d_2^B - 32C_B f_B(R); \quad B = F, A$$

with:

$$f_B(R) = C_A \left( c_L^A \ln R + c_0^A + c_2^A R^2 + c_4^A R^4 + \dots \right) + C_B \left( -\frac{\pi^2 R^2}{12} + \frac{R^4}{16} \right) \\ + T_F n_f \left( c_L^f \ln R + c_0^f + c_2^f R^2 + c_4^f R^4 + \dots \right)$$

Expansion coefficients:

$$c_L^A = \frac{131}{72} - \frac{\pi^2}{6} - \frac{11}{6} \ln 2,$$

$$c_L^f = -\frac{23}{36} + \frac{2}{3} \ln 2$$

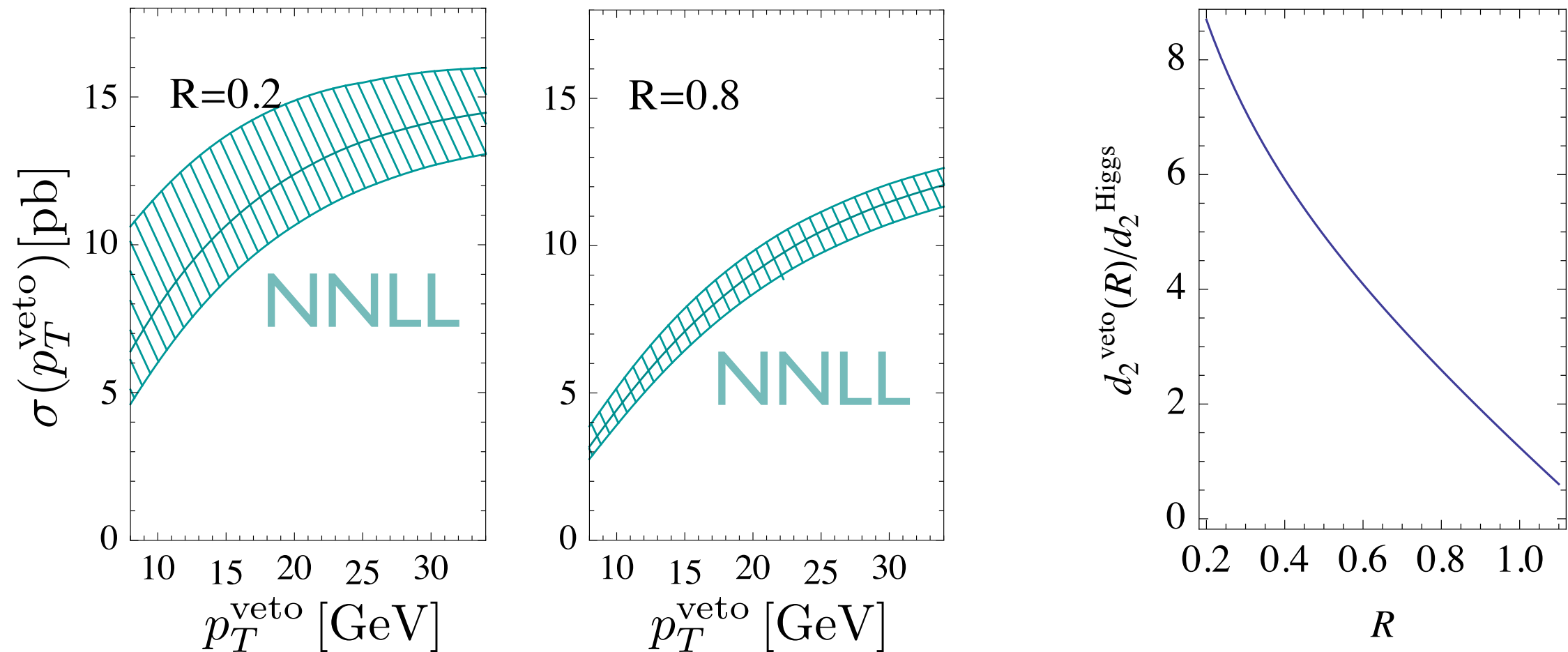
$$c_0^A = -\frac{805}{216} + \frac{11\pi^2}{72} + \frac{35}{18} \ln 2 + \frac{11}{6} \ln^2 2 + \frac{\zeta_3}{2},$$

$$c_0^f = \frac{157}{108} - \frac{\pi^2}{18} - \frac{8}{9} \ln 2 - \frac{2}{3} \ln^2 2$$

$$c_2^A = \frac{1429}{172800} + \frac{\pi^2}{48} + \frac{13}{180} \ln 2,$$

$$c_2^f = \frac{3071}{86400} - \frac{7}{360} \ln 2$$

# Resummation at NNLL order



$d_2^{\text{veto}}(R)$  gets very large at small  $R$ , introducing a significant scale dependence to the NNLL resummed cross section!



# Resummation at N<sup>3</sup>LL order

Ingredients required for N<sup>3</sup>LL resummation:

- two-loop  $\bar{H}$  (known) and  $\bar{I}_{g \leftarrow i}$  functions
- three-loop anomaly exponent  $d_3^{\text{veto}}(R)$
- four-loop cusp anomalous dimension  $\Gamma_3^A$  and other (known) three-loop anomalous dimensions

We have extracted the two-loop convolutions  $(\bar{I}_{g \leftarrow i} \otimes \phi_{i/P})^2$  numerically using the **HNNLO** fixed-order code by [Grazzini](#) (run at different  $m_H$  to disentangle power corrections)

# Resummation at N<sup>3</sup>LL order

The only missing ingredients for complete N<sup>3</sup>LL result are the four-loop cusp anomalous dimension and the three-loop anomaly coefficient  $d_3^{\text{veto}}(R)$

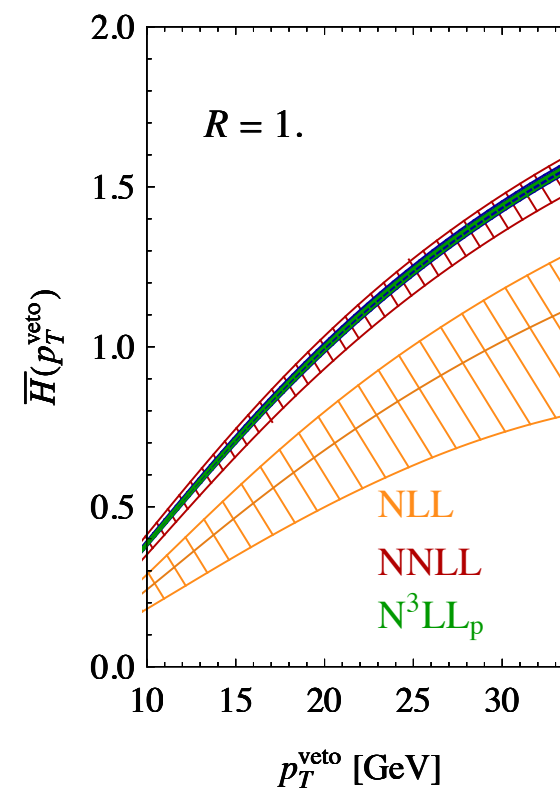
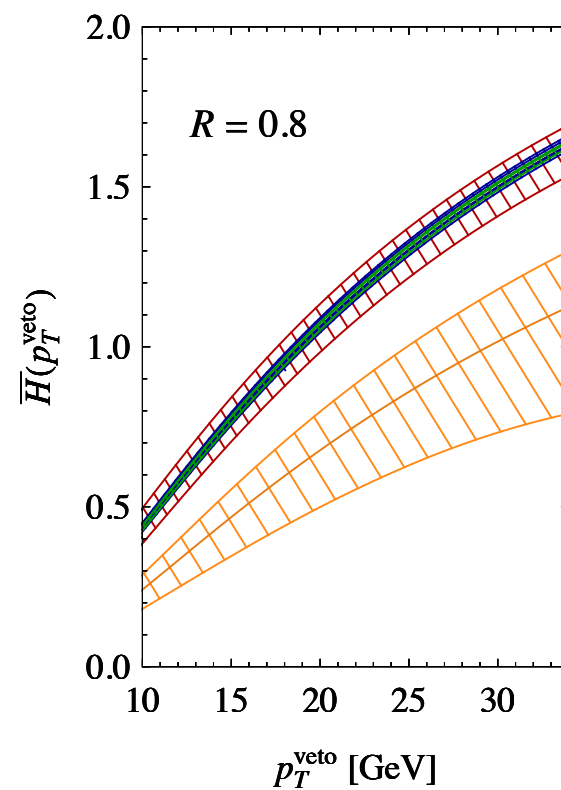
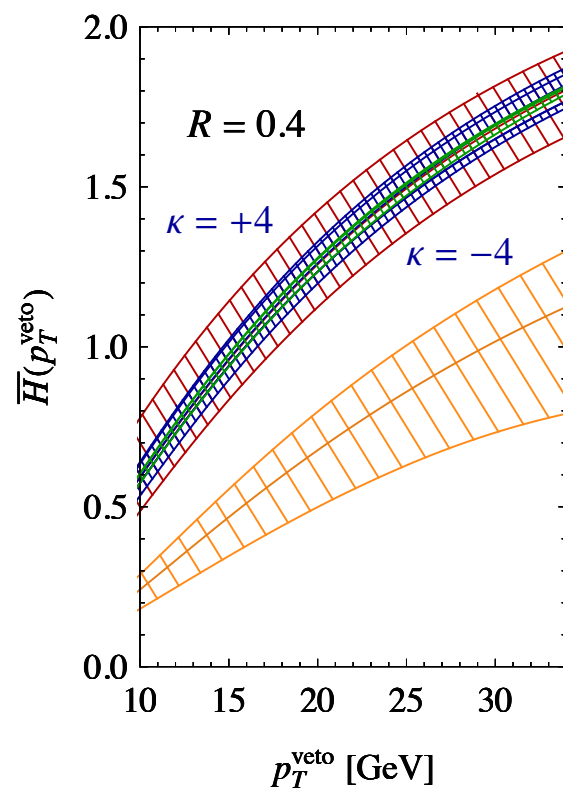
Estimates (thus “N<sup>3</sup>LL<sub>p</sub>”):

$$\Gamma_3^A|_{\text{Padé}} = \frac{(\Gamma_2^A)^2}{\Gamma_1^A} = 3494.4 \quad \text{tiny impact}$$

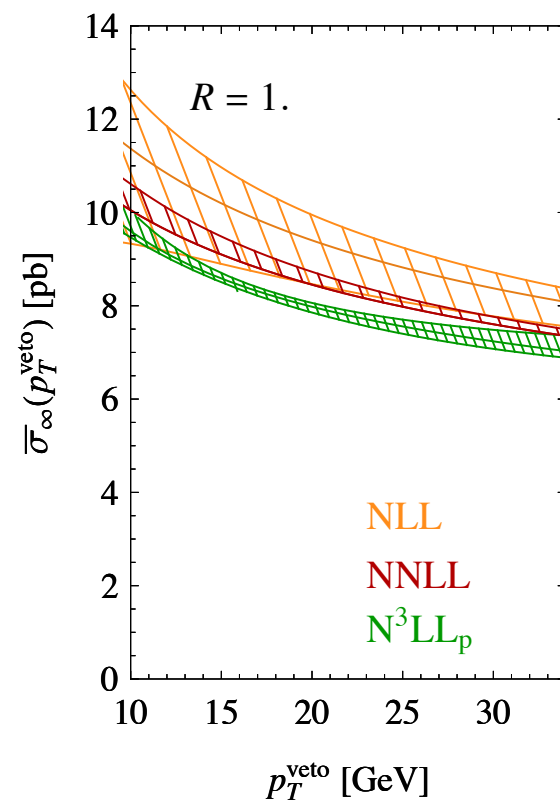
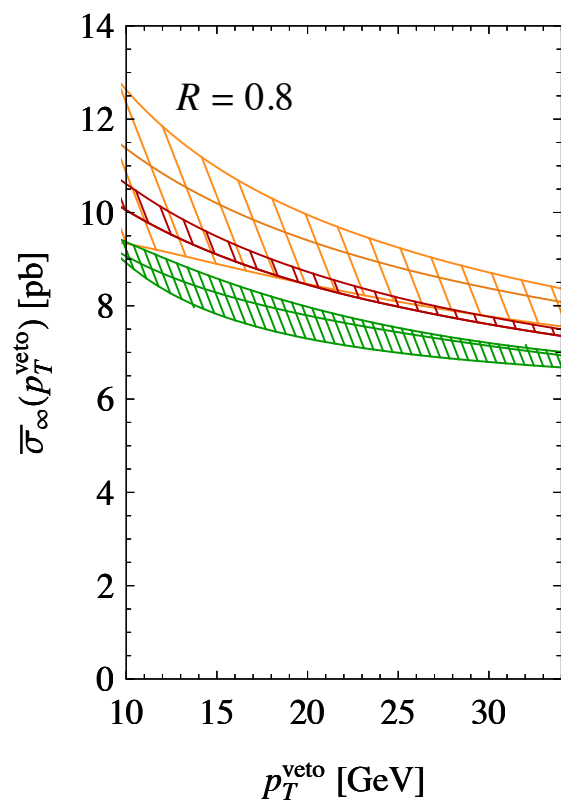
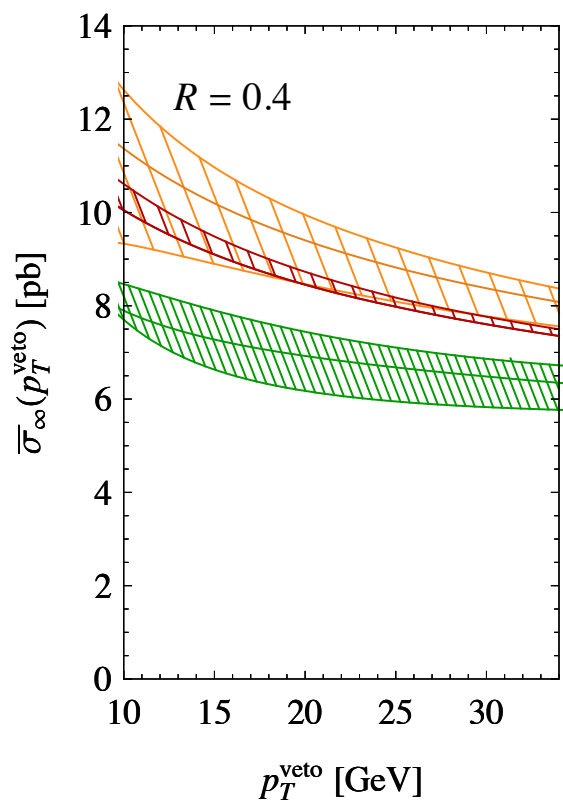
$$d_3^{\text{veto}}(R) = \kappa (4C_A)^3 \ln^2 \frac{2}{R} \quad \text{with } -4 < \kappa < 4$$

- our estimate for  $d_3$  is generous and captures the leading dependence for small  $R$ ; even for  $R=1$ , the value is six times larger than the three-loop cusp anomalous dimension

# Resummation at N<sup>3</sup>LL<sub>p</sub> order



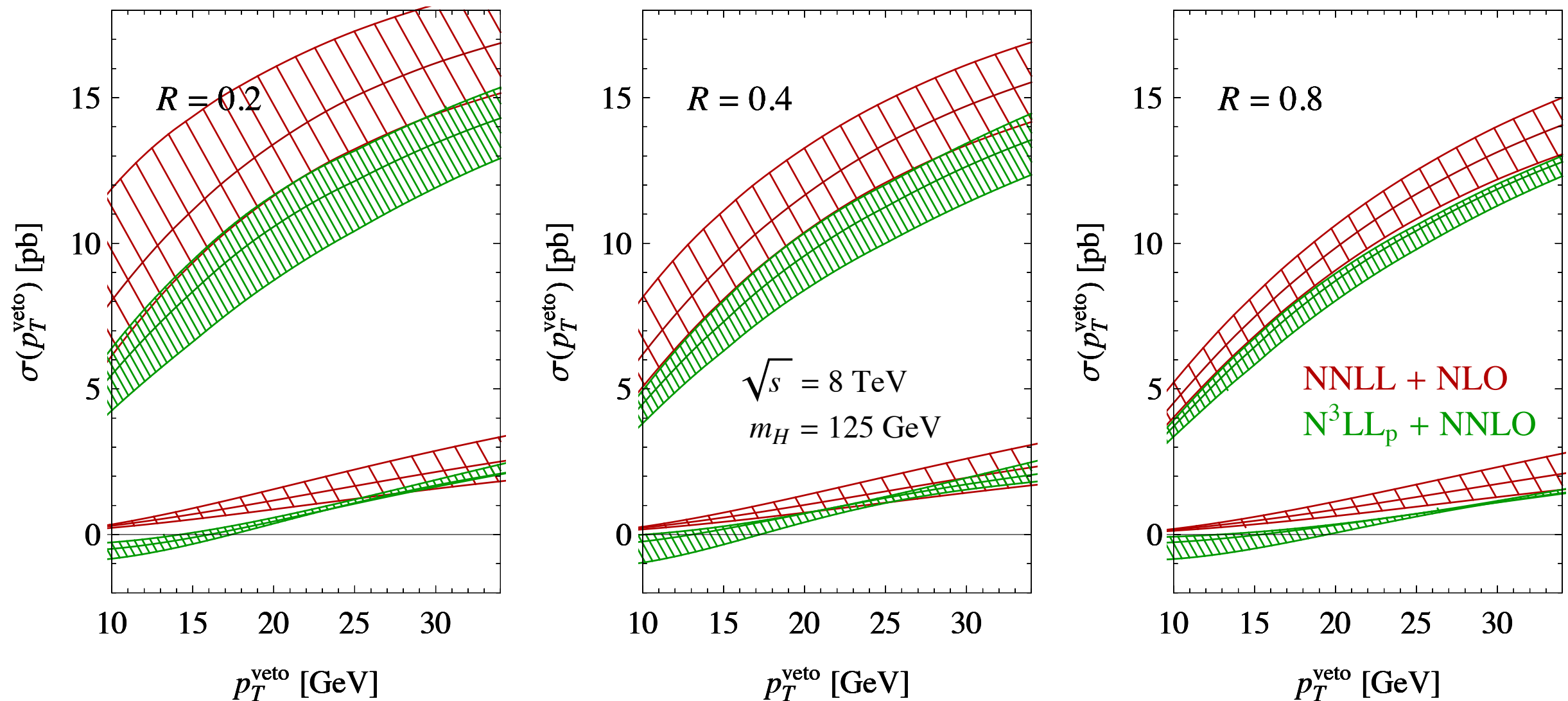
all large logs  
resummed



fixed-order  
expansion  
( $R$  dependence  
arises first at  
N<sup>3</sup>LL order !)

# N<sup>3</sup>LL<sub>p</sub>+NNLO matched predictions

Becher, MN, Rothen '13



- Lower bands show the  $p_T^{\text{veto}}/m_H$  power corrections (small!)
- Seizable uncertainty at very small  $R$  due to large  $\ln^n R$  terms (experiments use  $R \sim 0.4$ )

# N<sup>3</sup>LL<sub>p</sub>+NNLO matched predictions

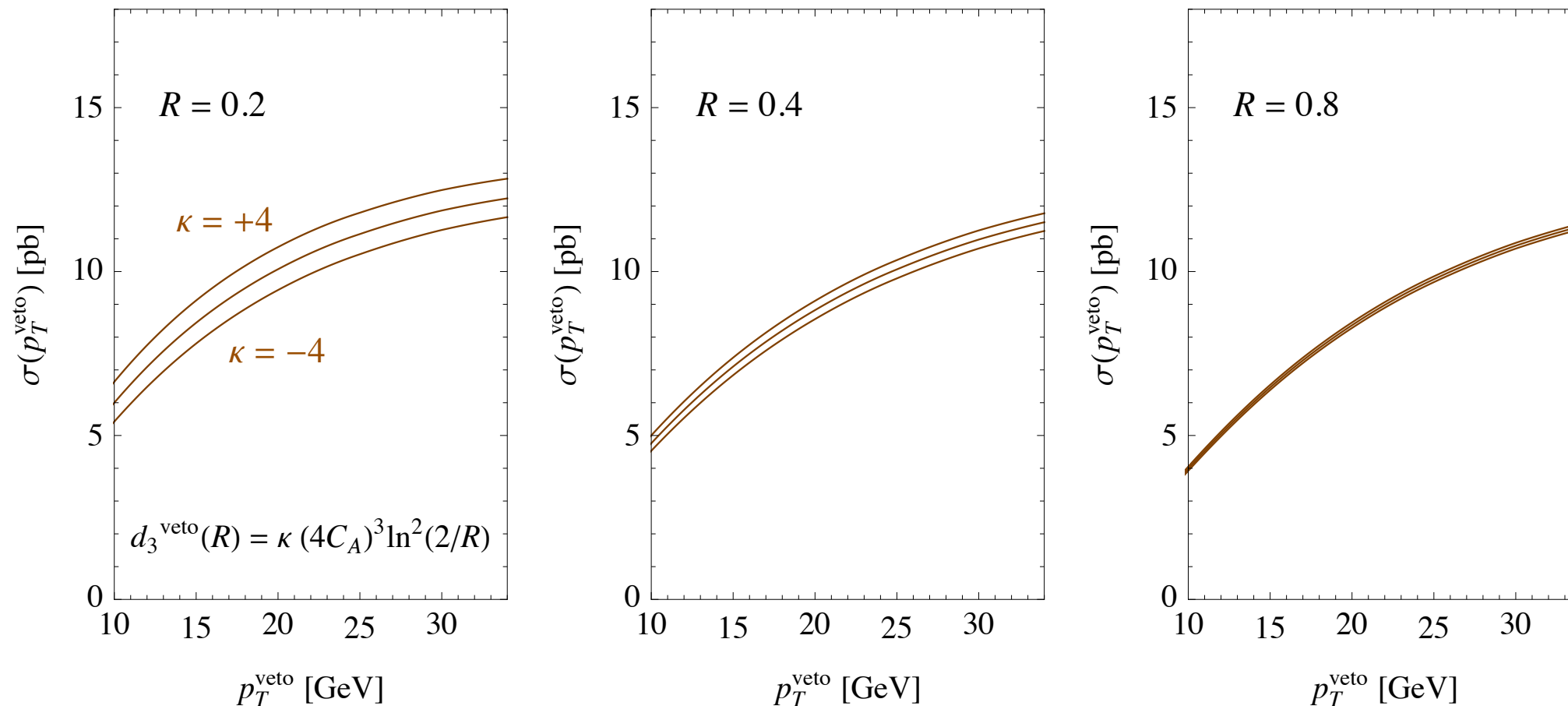
Numerical results:

$p_T^{\text{veto}}$ [GeV]	$R = 0.4$		$R = 0.8$	
	$\sigma(p_T^{\text{veto}})$ [pb]	$\epsilon(p_T^{\text{veto}})$	$\sigma(p_T^{\text{veto}})$ [pb]	$\epsilon(p_T^{\text{veto}})$
10	$4.48^{+0.46 (+0.37)}_{-0.67 (-0.48)}$	$0.228^{+0.023 (+0.019)}_{-0.034 (-0.024)}$	$3.71^{+0.21 (+0.19)}_{-0.35 (-0.34)}$	$0.189^{+0.011 (+0.010)}_{-0.018 (-0.017)}$
15	$7.31^{+0.72 (+0.63)}_{-1.00 (-0.85)}$	$0.371^{+0.036 (+0.031)}_{-0.051 (-0.043)}$	$6.44^{+0.30 (+0.28)}_{-0.61 (-0.59)}$	$0.328^{+0.015 (+0.014)}_{-0.031 (-0.030)}$
20	$9.57^{+0.78 (+0.66)}_{-1.18 (+1.07)}$	$0.487^{+0.040 (+0.034)}_{-0.060 (-0.055)}$	$8.71^{+0.25 (+0.21)}_{-0.69 (-0.67)}$	$0.443^{+0.013 (+0.011)}_{-0.035 (-0.034)}$
25	$11.25^{+0.77 (+0.65)}_{-1.25 (-1.15)}$	$0.572^{+0.039 (+0.033)}_{-0.063 (-0.059)}$	$10.43^{+0.19 (+0.13)}_{-0.64 (-0.62)}$	$0.531^{+0.010 (+0.007)}_{-0.033 (-0.032)}$
30	$12.64^{+0.80 (+0.67)}_{-1.25 (-1.15)}$	$0.643^{+0.040 (+0.034)}_{-0.063 (-0.059)}$	$11.86^{+0.18 (+0.10)}_{-0.57 (-0.55)}$	$0.603^{+0.009 (+0.005)}_{-0.029 (-0.028)}$
35	$13.75^{+0.94 (+0.84)}_{-1.18 (-1.08)}$	$0.700^{+0.048 (+0.043)}_{-0.060 (-0.055)}$	$13.00^{+0.23 (+0.18)}_{-0.46 (-0.43)}$	$0.662^{+0.012 (+0.009)}_{-0.024 (-0.022)}$

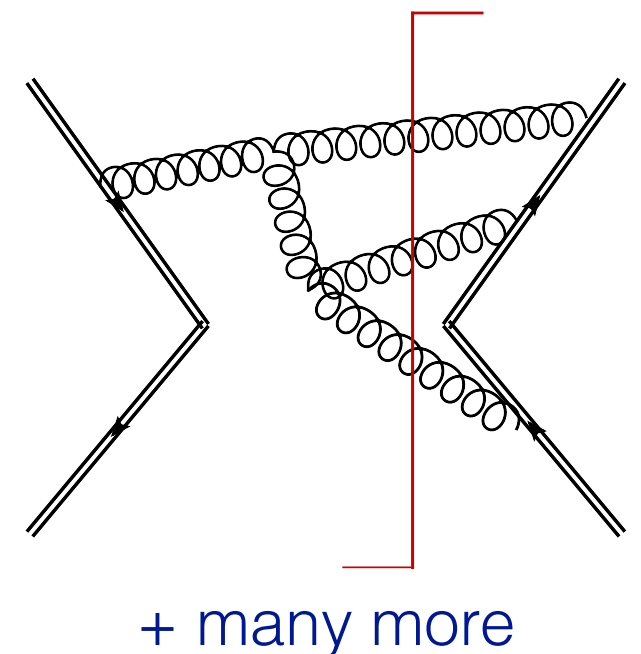
Table 2: Numerical results for the jet-veto cross section and efficiency. The uncertainty is obtained by varying  $p_T^{\text{veto}}/2 < \mu < 2p_T^{\text{veto}}$  and the coefficient  $d_3^{\text{veto}}(R)$  according to the estimate (66). The numbers in brackets are obtained if only  $\mu$  is varied.



# $d_3^{\text{veto}}$ uncertainty



- for  $R$  not too small, this is a subleading uncertainty
- seems possible to extract the leading  $\ln^2 R$  term from three-emission diagrams in the soft function



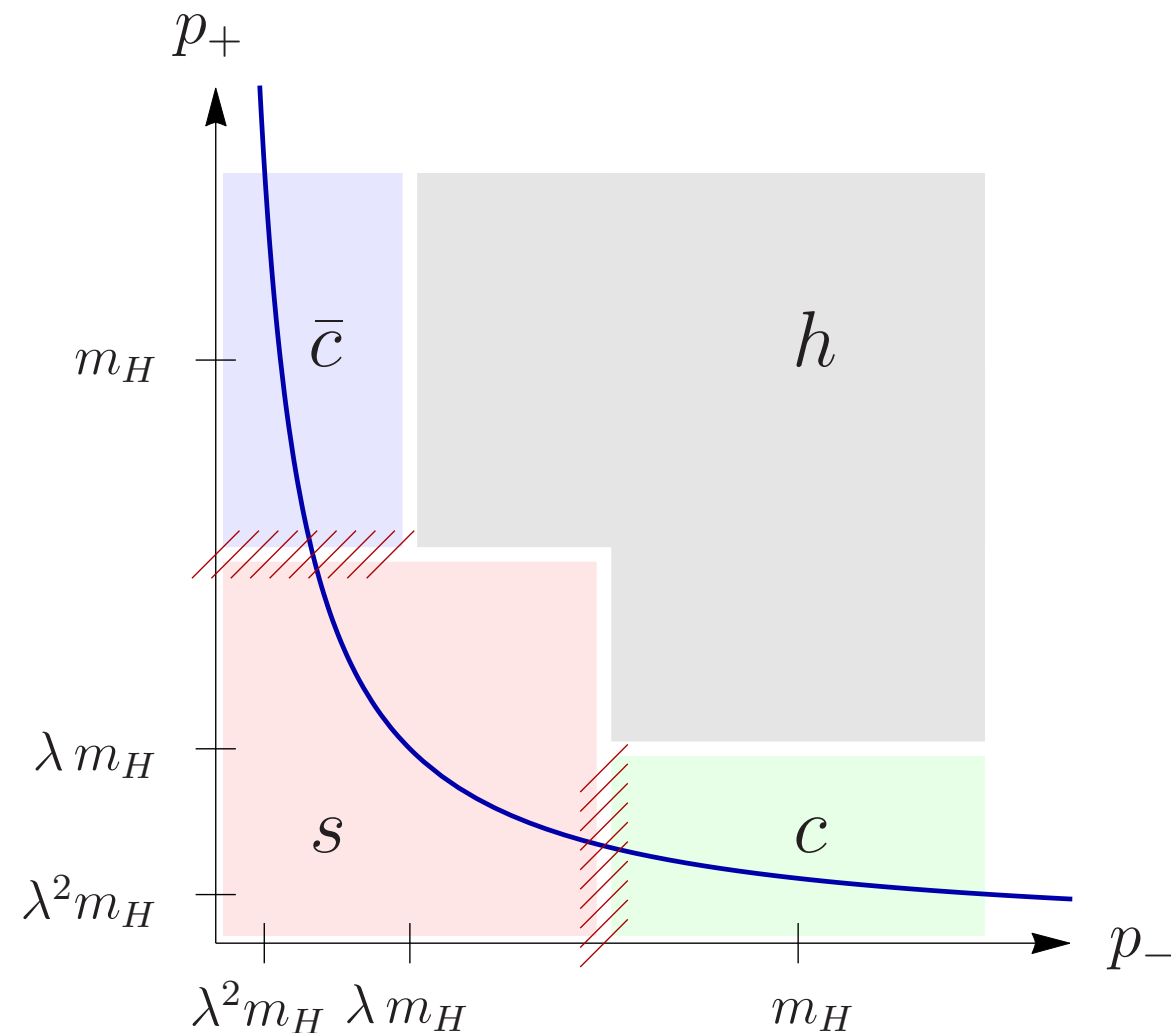
# Soft-collinear clustering terms ?

Tackmann, Walsh, Zuberi (TWZ) 1206.4312

Becher, MN and Rothen 1307.0025

# Soft-collinear clustering terms?

- Both soft and collinear contributions are integrated over full phase space in SCET
- Avoid double counting by:
  - ✦ **multi-pole expanding** integrands
  - ✦ or by performing **“zero-bin” subtractions** of overlap regions

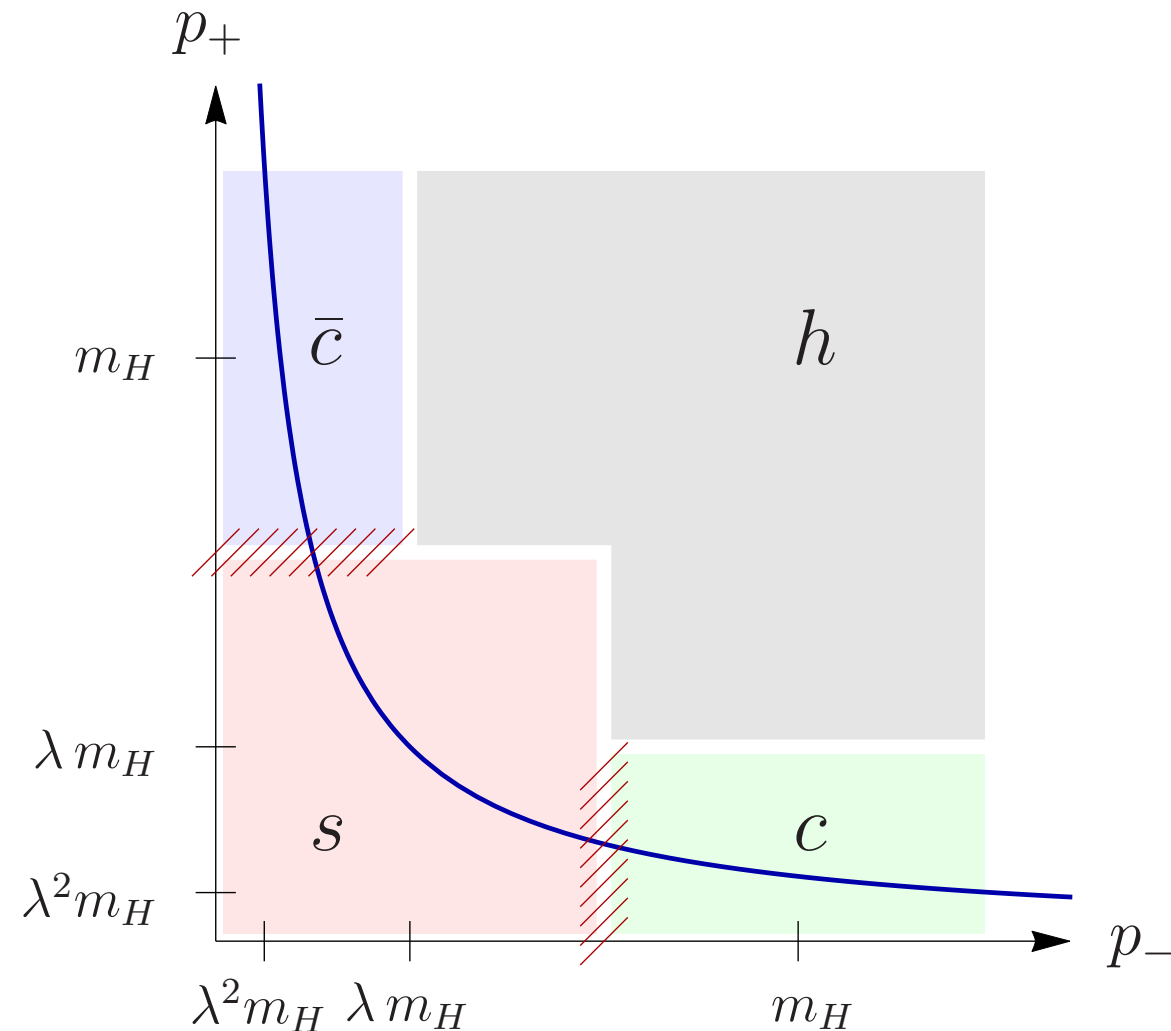


- Find that soft-collinear mixing contribution found by **TWZ** **cancels against zero-bin subtraction** of collinear region
- If integrand is expanded in small soft rapidities, both terms are absent

# Soft-collinear clustering terms?

For concrete example, consider the emission of a collinear gluon ( $y_c \gg 1$ ) along with some other gluon

- according to our factorization formula, clustering only occurs if the second gluon is also collinear
- this is indeed the case, provided the distance measure



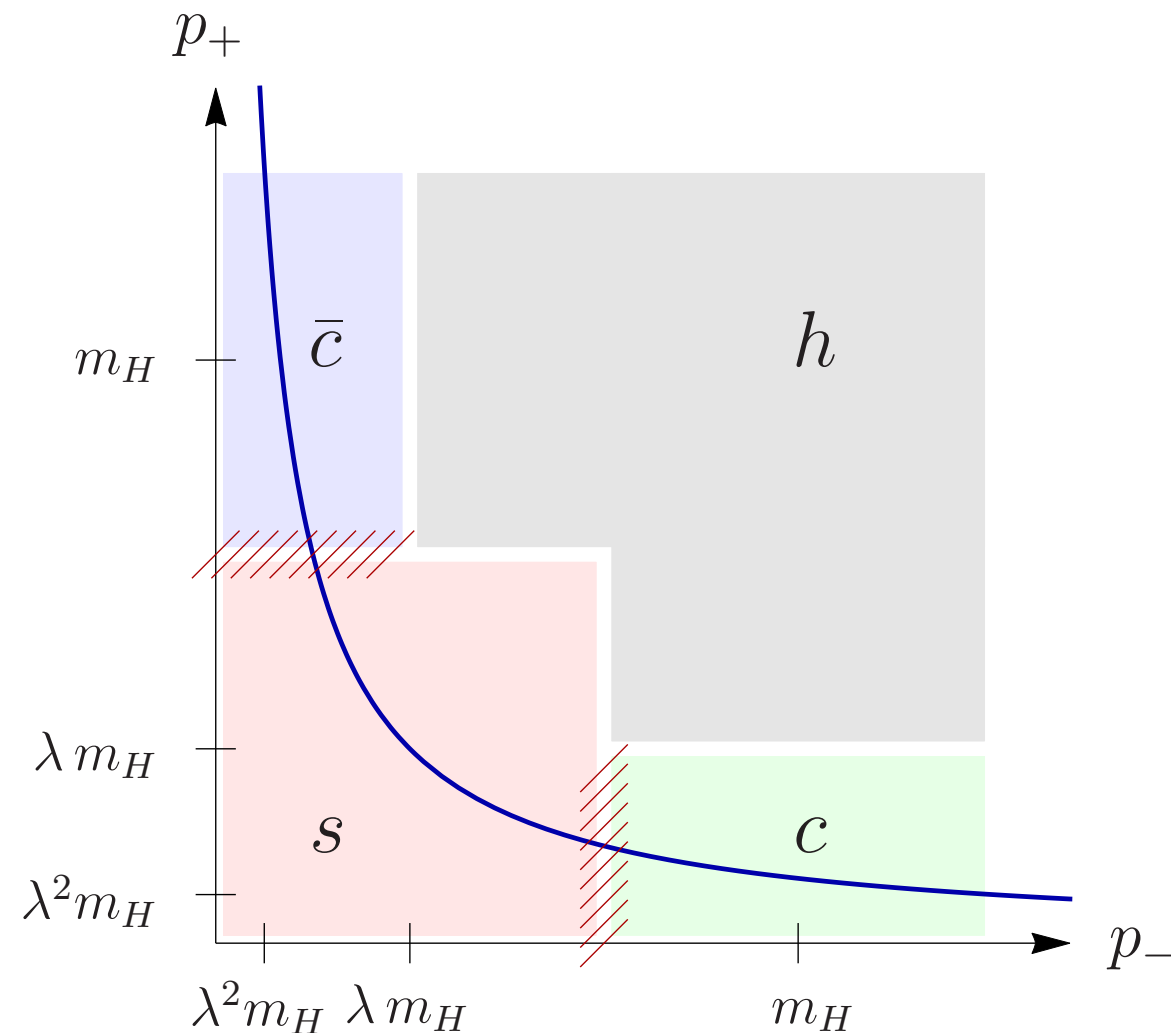
$$\theta(R^2 - (y - y_c)^2 - \Delta\phi^2) = \theta(-(y - y_c)^2) + \dots$$

is multi-pole expanded

# Soft-collinear clustering terms?

For concrete example, consider the emission of a collinear gluon ( $y_c \gg 1$ ) along with some other gluon

- without a proper multi-pole expansion, one also finds non-zero contributions from soft and anti-collinear emissions
- at same time, one must perform a variety of **zero-bin subtractions** of various overlap regions:



$$I = I_c + I_s + I_{\bar{c}} - I_{(cs)} - I_{(\bar{c}s)} - I_{(\bar{c}c)} + I_{(\bar{c}cs)}$$

cancel ! (from  $I_s$  to  $I_{(cs)}$ )  
cancel ! (from  $I_{\bar{c}}$  to  $I_{(\bar{c}s)}$ )  
cancel ! (from  $I_{(\bar{c}c)}$  to  $I_{(\bar{c}cs)}$ )

**TWZ** have only shown that this is non-zero

# Soft-collinear clustering terms?

In public, TWZ still claim that for  $R=O(1)$  our factorization formula is violated starting at NNLL order

Stewart, Tackmann, Walsh, Zuberi 1307.1808

In private, they agree that soft-collinear clustering terms are absent at two-loop order, but they still believe they will arise at higher loops ...

F.T. said that he would believe our formula if we could show the absence of soft-collinear clustering terms at NNLL order for the observable beam thrust (where this could not possibly be the case)

This has now indeed been demonstrated by explicit calculation and communicated to F.T. by email more than one month ago, so far with no response ...

# Soft-collinear clustering terms?

For  $\Delta\Phi=0$ , the arguments of the  $\theta$ -functions can be rewritten in terms of light-cone components of the gluon momenta:

$$\begin{aligned}\theta(R^2 - (y - y_c)^2) &= \theta(R - (y - y_c)) \theta(y - y_c) + \theta(R - (y_c - y)) \theta(y_c - y) \\ &= \theta(\underbrace{e^R p_T k_+}_{\lambda^3} - \underbrace{p_+ k_T}_{\lambda^2}) \theta(\underbrace{p_+ k_T}_{\lambda^2} - \underbrace{p_T k_+}_{\lambda^3}) + \theta(\underbrace{p_+ k_T}_{\lambda^2} - \underbrace{e^{-R} p_T k_+}_{\lambda^3}) \theta(\underbrace{p_T k_+}_{\lambda^3} - \underbrace{p_+ k_T}_{\lambda^2}) \\ &= \theta(-p_+ k_T) \theta(p_+ k_T) + \theta(p_+ k_T) \theta(-p_+ k_T) + \dots\end{aligned}$$

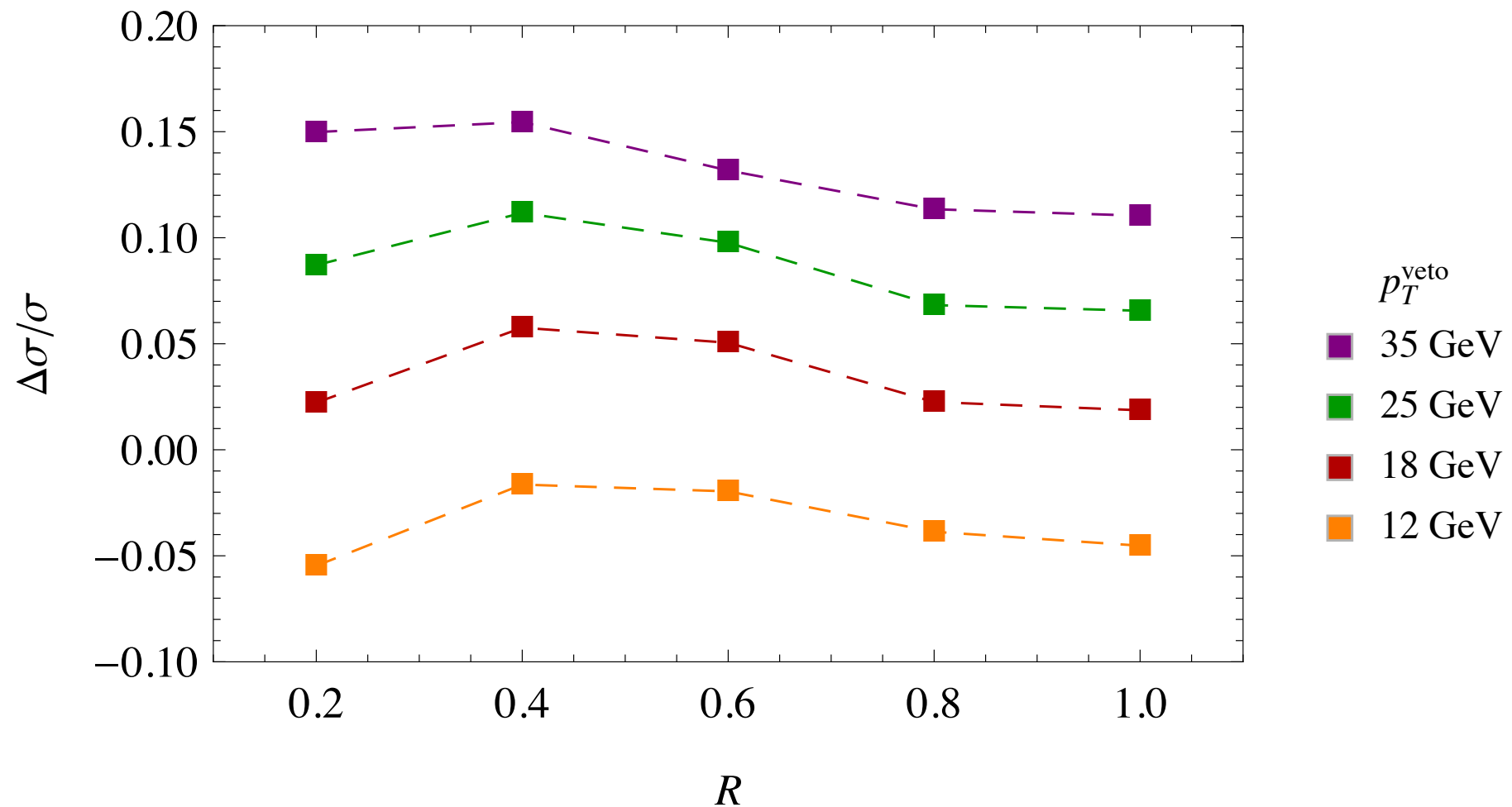
- these have the same form as imaginary parts of propagators
- hence the multi-pole expansion is not different from other, more familiar applications of SCET !

**Existence of power corrections enhanced by  $e^R$  ?**



# $R$ dependence of power corrections

Numerically, we find no evidence for  $e^R$ -enhanced power corrections in  $p_T^{\text{veto}}/m_H$  to the factorization formula:



Power corrections controlled by  $p_T^{\text{veto}}/m_H$ , as usual!



# Summary

Higher-order resummed and matched predictions for the Higgs jet-veto cross section are now available from different groups (state-of-the art is  $N^3LL_p+NNLO$ )

All-order factorization theorem derived within SCET (Becher, MN: 1205.3806, + Rothen: 1307.0025)

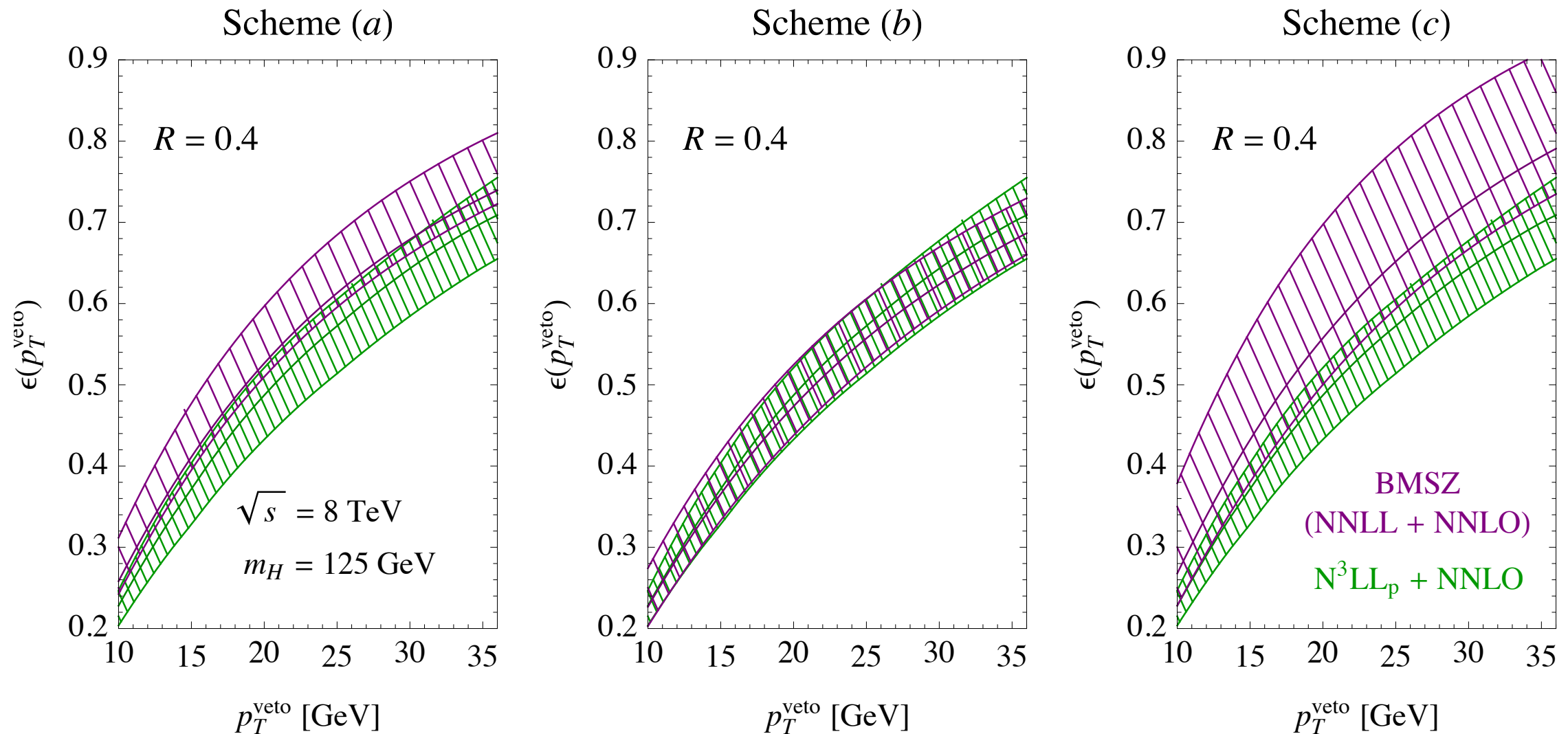
We find:

- complete agreement with BMZS at NNLL
- no factorization-breaking soft-collinear mixing terms, even for  $R=O(1)$
- uncertainty in cross section about 10% for  $R=0.4$ , could be reduced by increasing  $R$

# Backup slides

Comparison with other groups

# Comparison with Banfi et al. (BMSZ)



- The three different schemes used by BMSZ correspond to different prescriptions for how to expand the veto efficiency  $\epsilon(p_T^{\text{veto}})$  in  $\alpha_s$  (implemented in `JetVHeto` code)
- Better to work with cross section itself instead of  $\epsilon(p_T^{\text{veto}})$

# Comparison with Stewart et al.

Comparison for  $p_T^{\text{veto}}=25$  GeV and  $R=0.4$ :


$$\sigma(p_T^{\text{veto}}) = (11.25^{+0.65}_{-1.15} {}^{+0.44}_{-0.49}) \text{ pb}$$

Becher, MN, Rothen 1307.0025

$$\sigma(p_T^{\text{veto}}) = (12.67 \pm 1.22 \pm 0.46) \text{ pb}$$

Stewart, Tackmann, Walsh,  
Zuberi 1307.1808

 perturbative  
uncertainties

 estimate of  
 $\alpha_s^3 \ln^2 R$  terms

We have  $\sigma_{\text{tot}} = (19.66^{+0.55}_{-0.16}) \text{ pb}$  in agreement with HXSWG,  
while they find  $\sigma_{\text{tot}} = (21.68 \pm 1.49) \text{ pb}$ ; rescaling their total  
cross section to ours, we obtain:

$$\sigma(p_T^{\text{veto}}) = (11.49 \pm 1.11 \pm 0.42) \text{ pb}$$