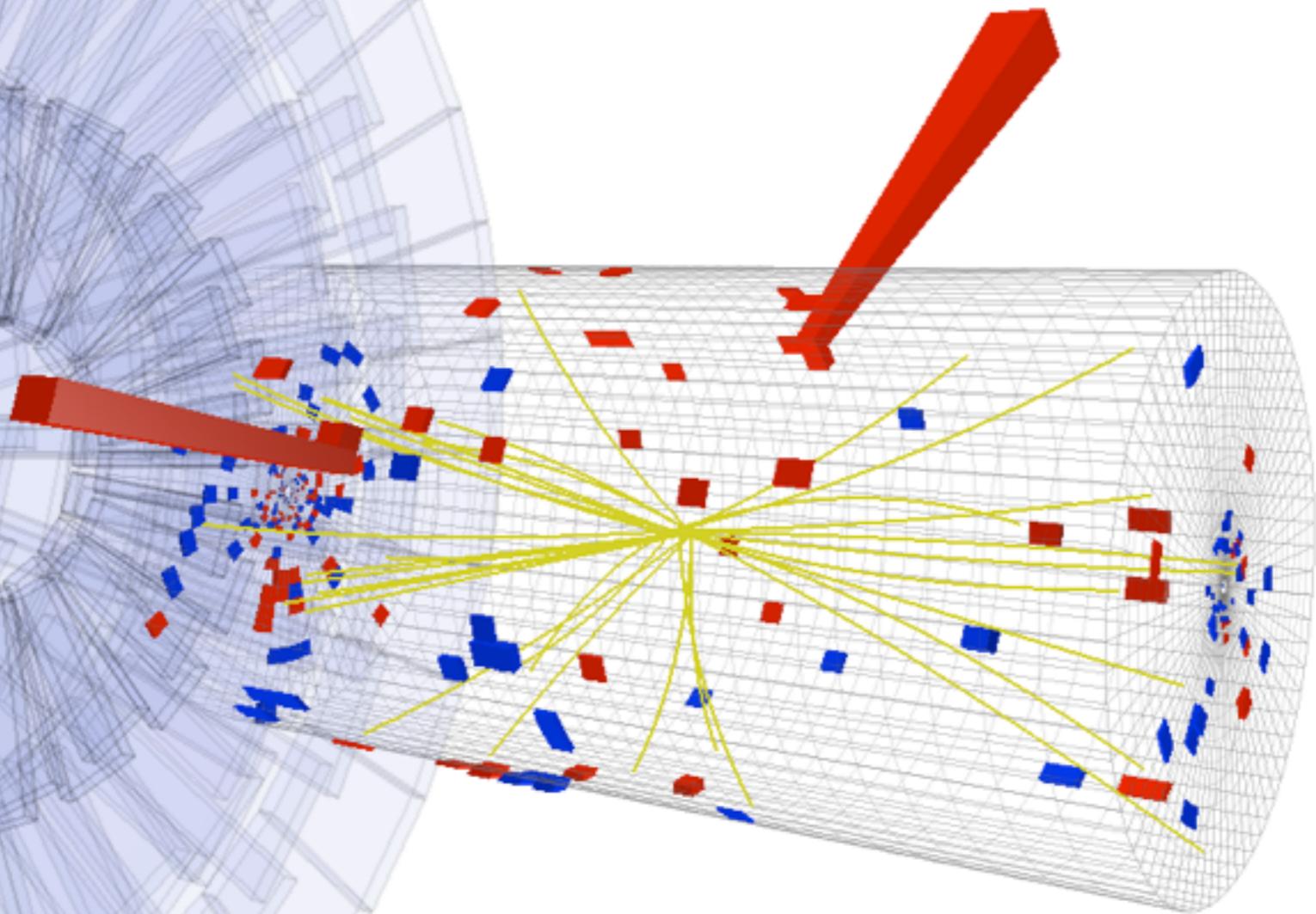


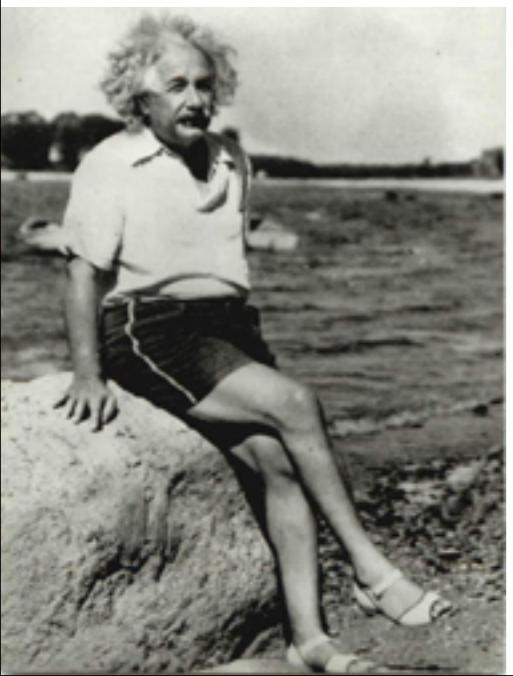
# Beyond the SM after LHC8

Andreas Weiler  
(DESY&CERN)



Annual Theory Meeting, IPPP Durham  
2013/12/16

“I do not mean to say that all these anticipations will withstand the test of experiment on the day such a test would become possible. Since he seeks in all directions one must, on the contrary, expect most of the trails which he pursues to be blind alleys.

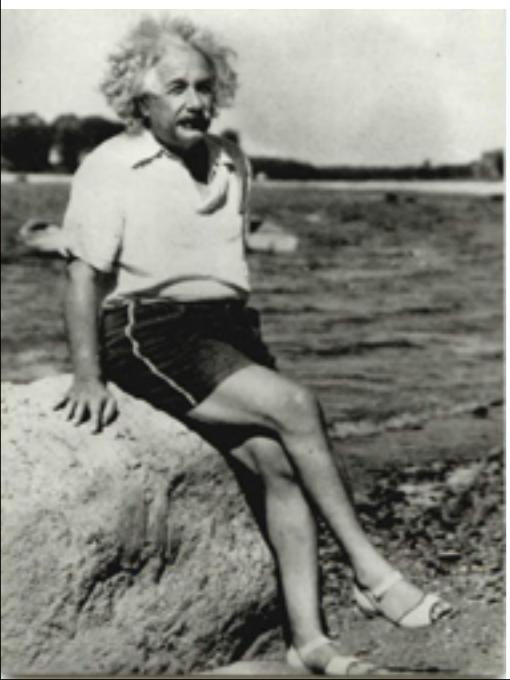


...

*—Henri Poincaré’s letter of recommendation for  
A. Einstein, 1911*



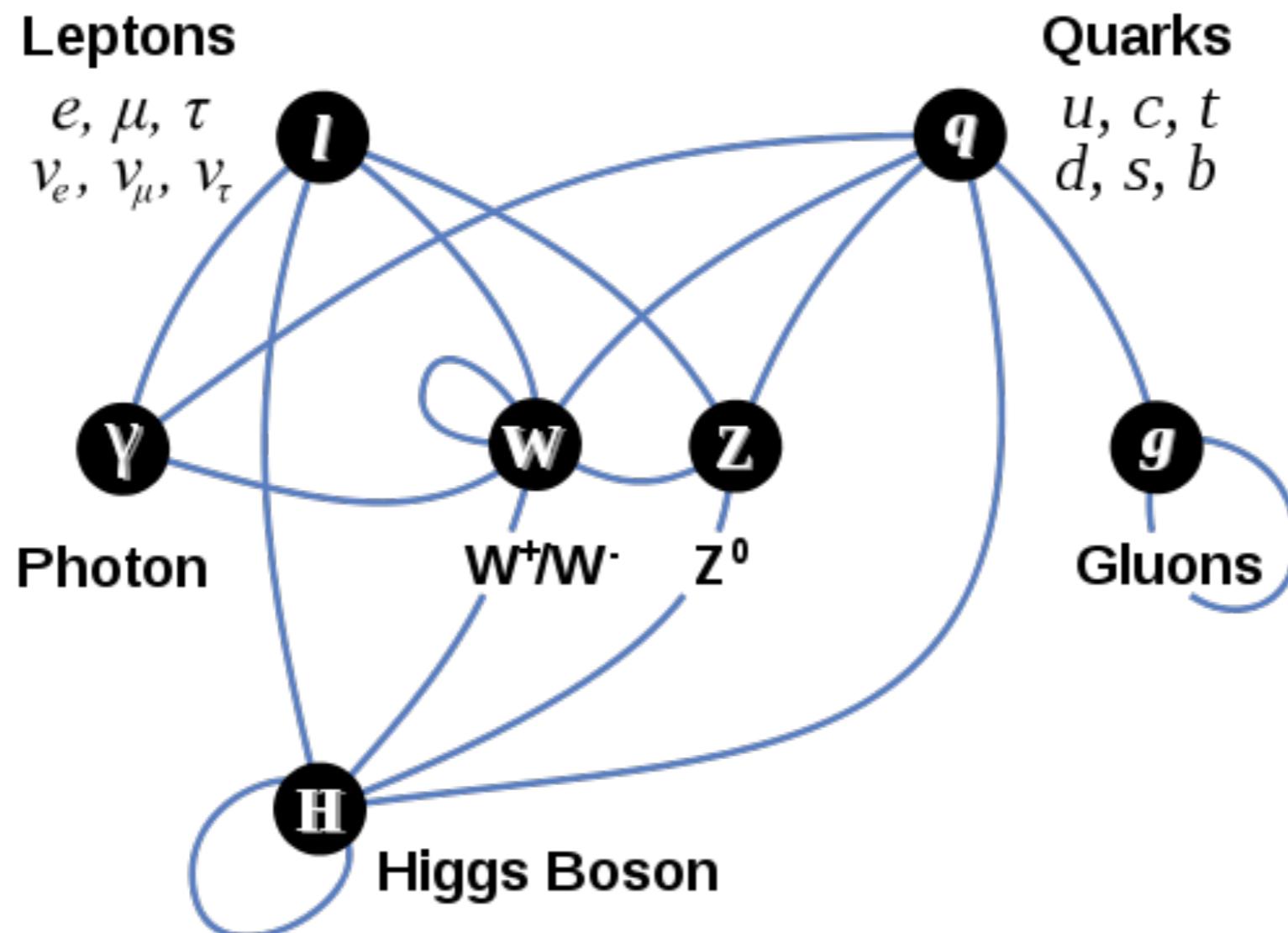
But one must hope at the same time that one of the directions he has indicated may be the right one, and that is enough. This is indeed how one should proceed. The role of mathematical physics is to ask the right questions, and experiment alone can resolve them. ”



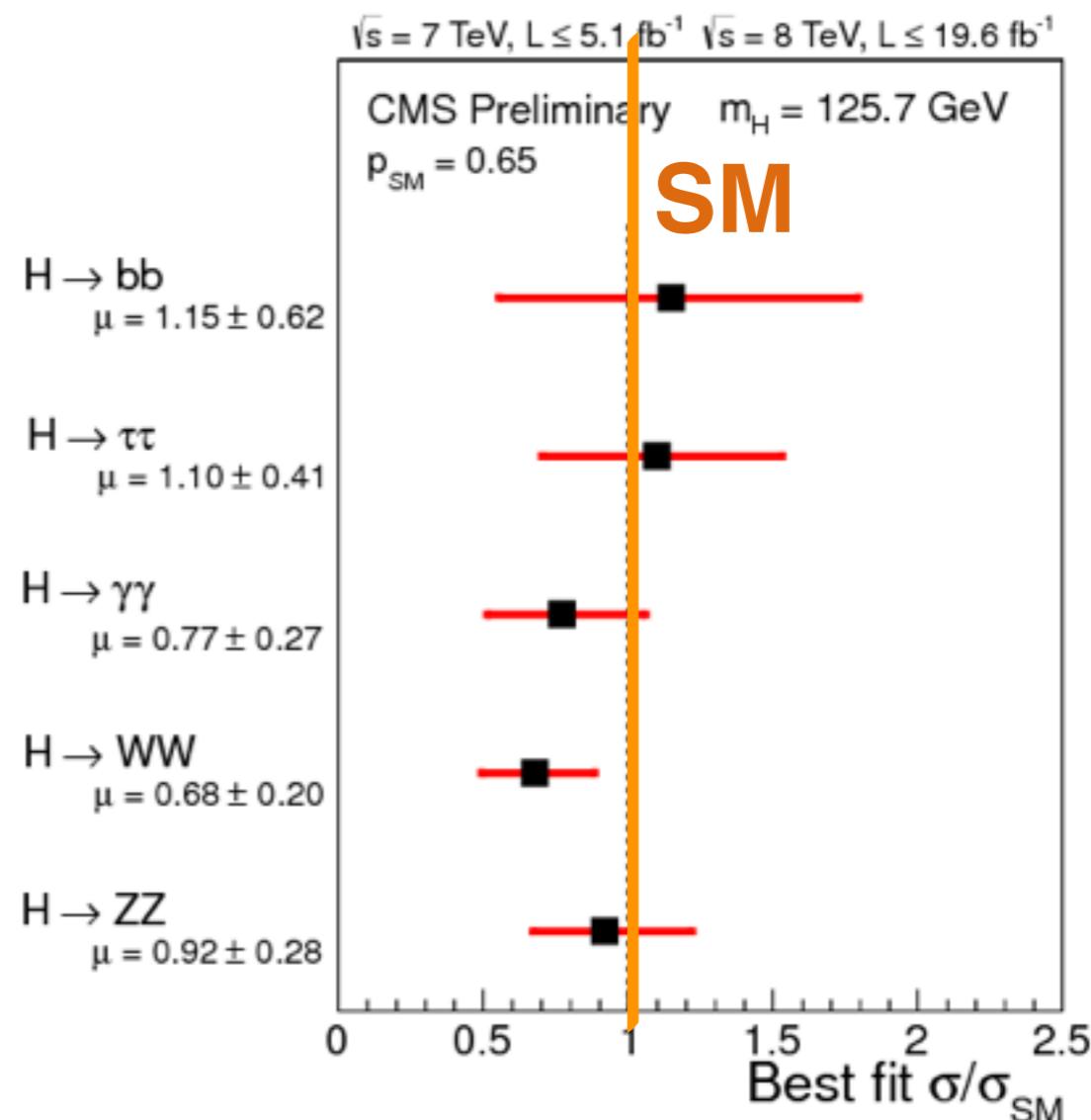
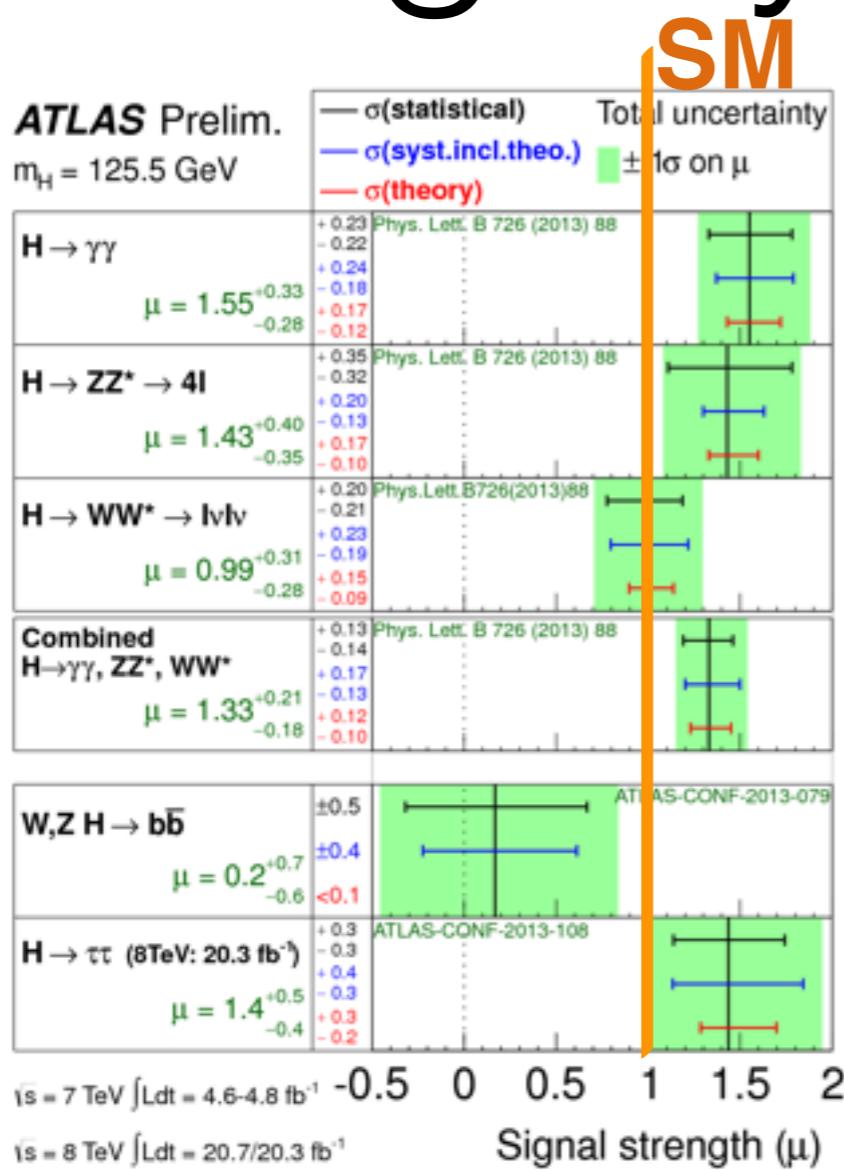
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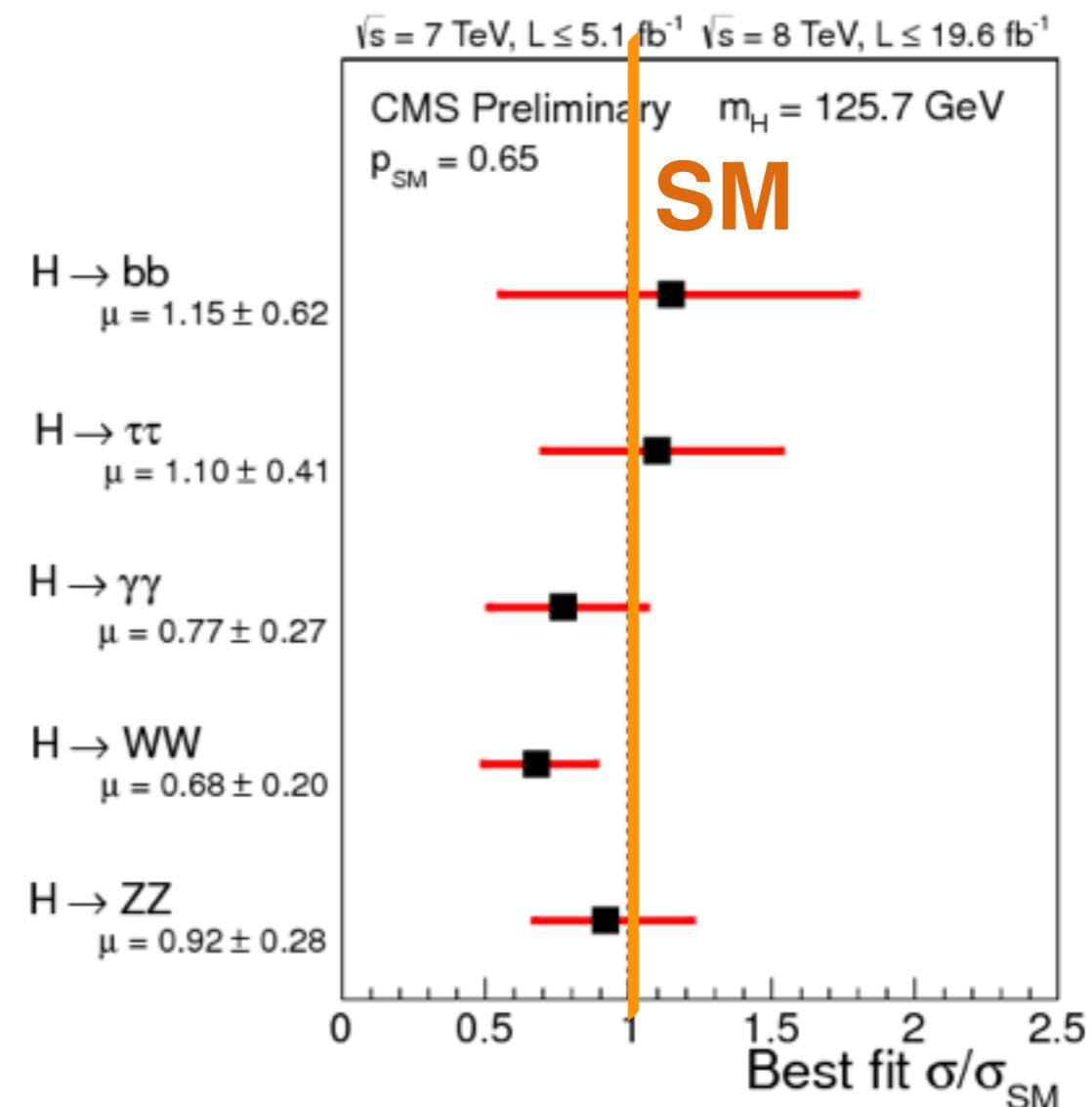
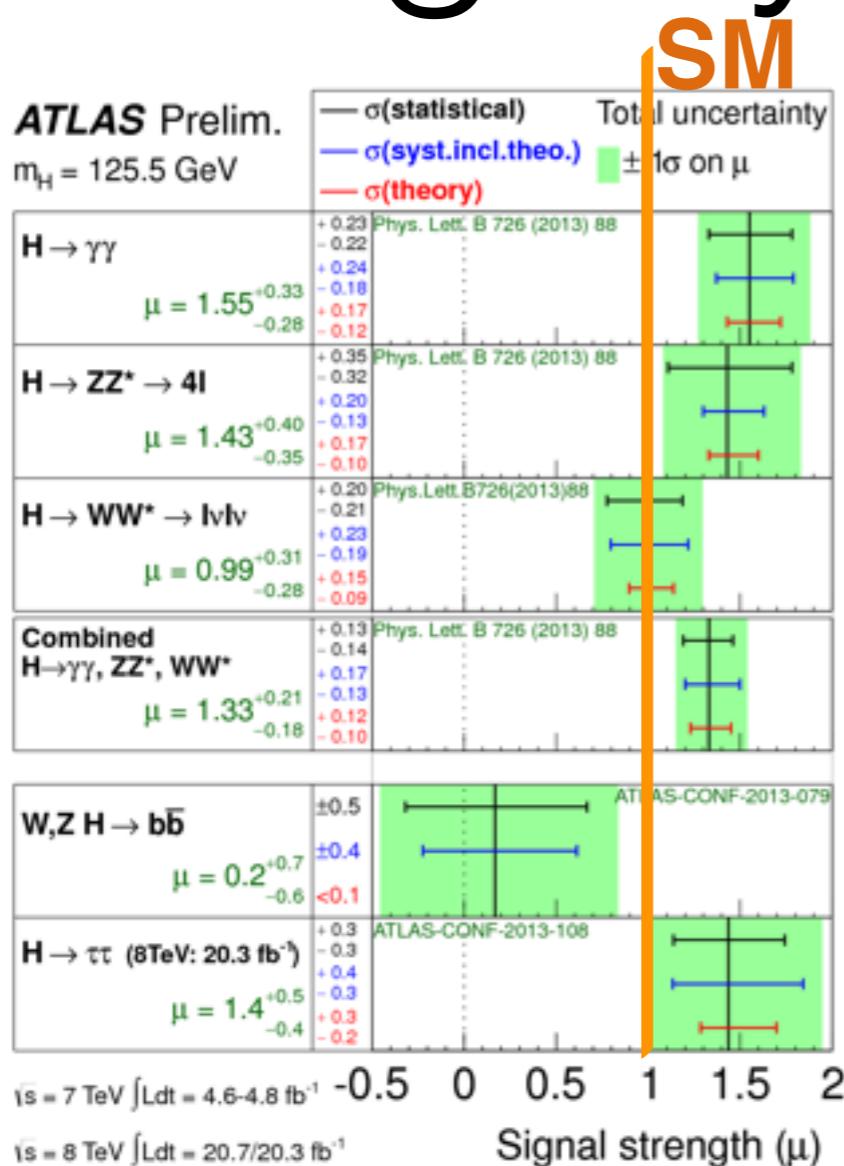
# The SM



# Legacy of run1 LHC



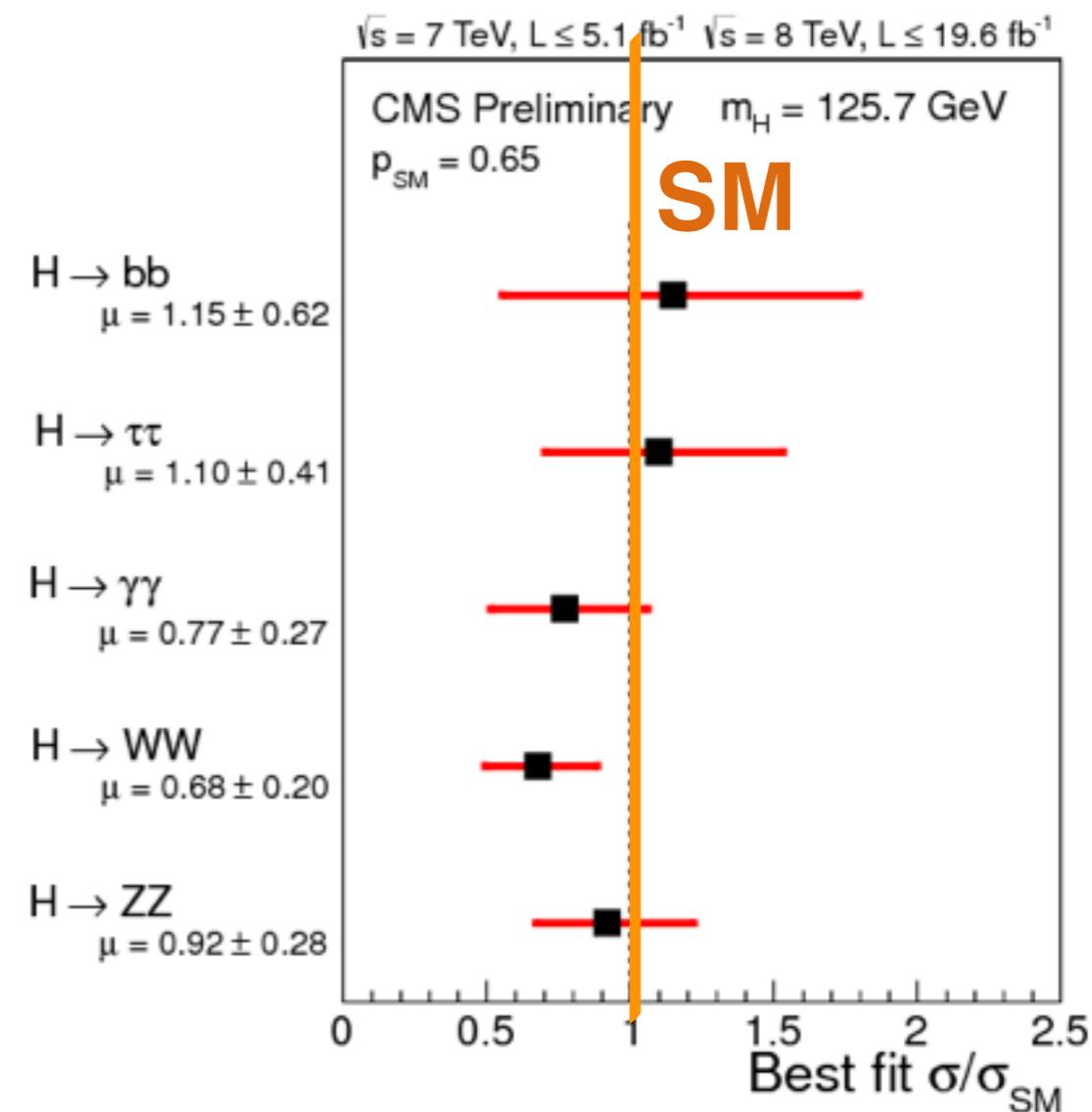
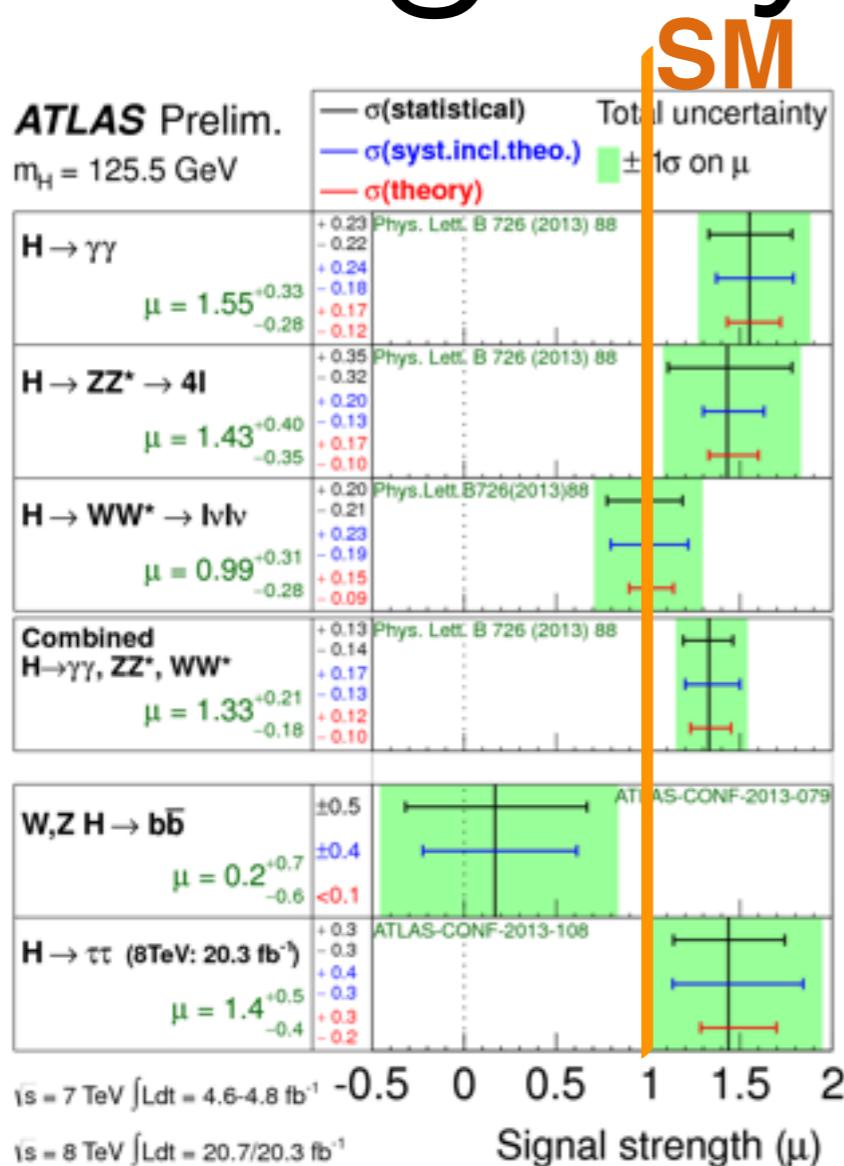
# Legacy of run1 LHC



It is the Higgs!



# Legacy of run1 LHC



It is the Higgs!

*Nobel certified™*



Which one is the Brout impostor?



# The SM



# The SM

$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} \gamma^\mu \psi + h.c. \\ & + \bar{\chi}_i Y_{ij} \chi_j \phi + h.c. \\ & + |\partial_\mu \phi|^2 - V(\phi)\end{aligned}$$

# The SM

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i \bar{\psi} \not{D} \psi + h.c.$$

determined  
by gauge  
symmetry

$$+ X_i Y_{ij} X_j \phi + h.c. \\ + |D_m \phi|^2 - V(\phi)$$

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fermion  
masses  
& mixings

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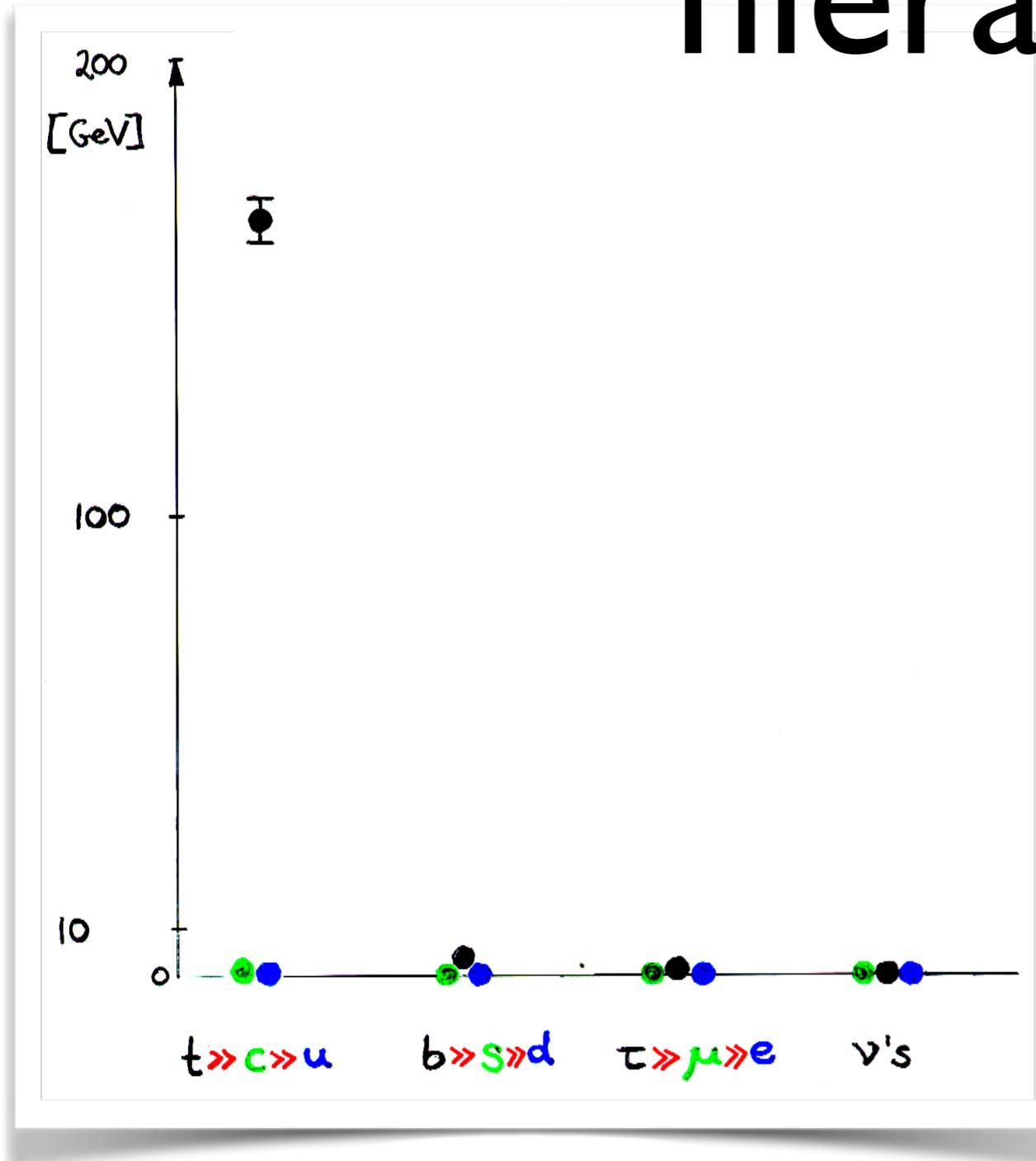
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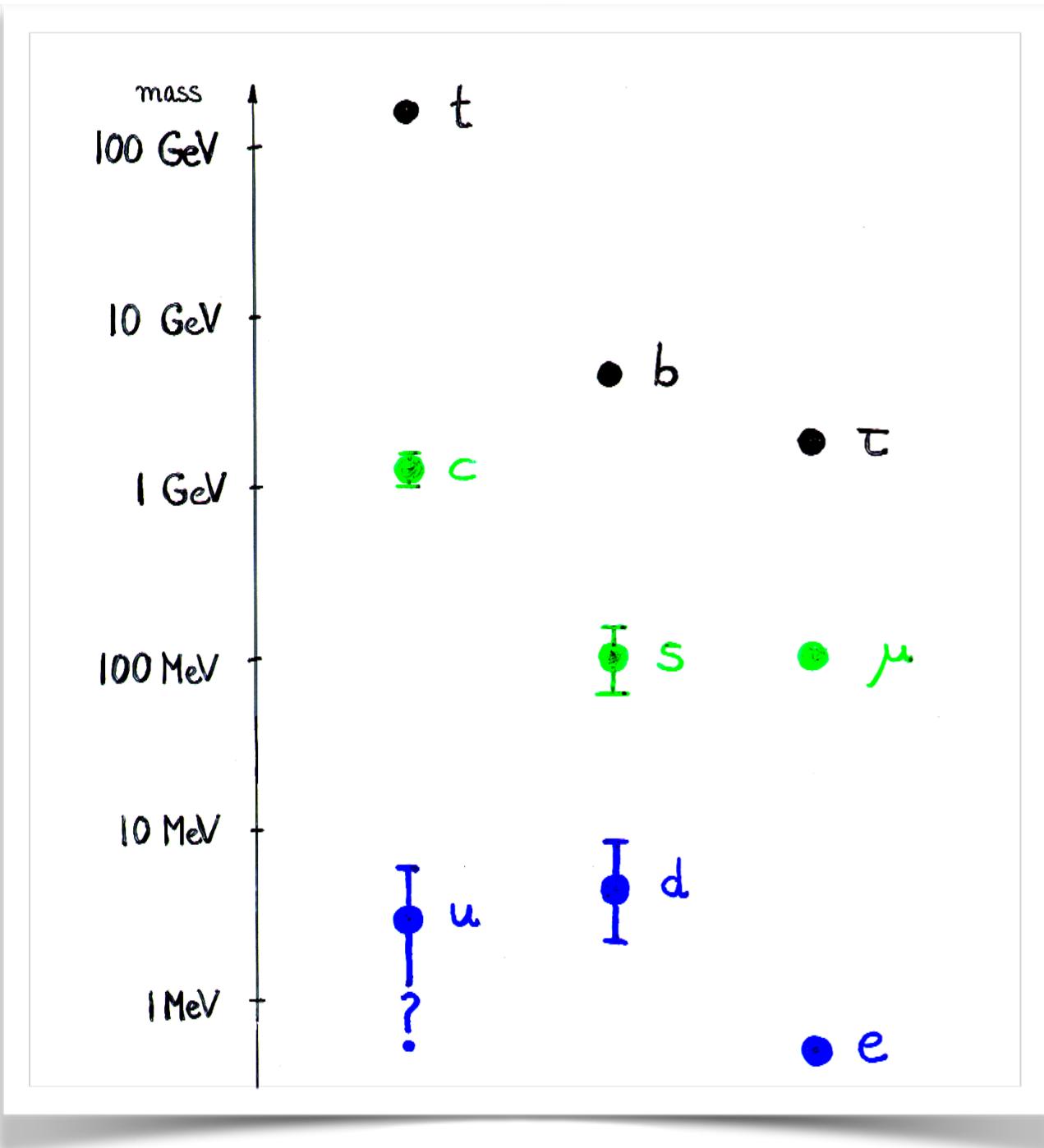
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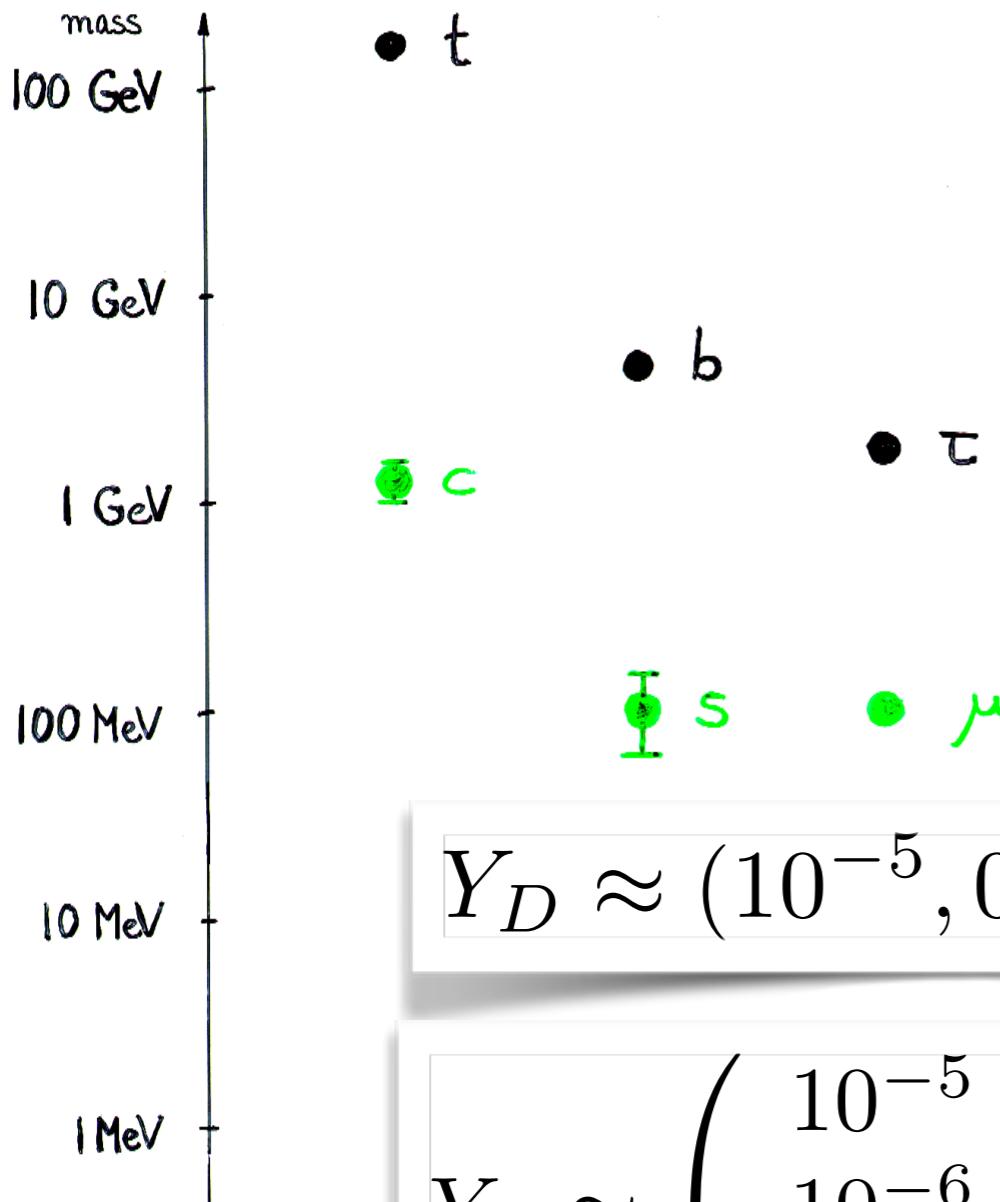
# Quark and lepton mass hierarchy



# Masses on a log scale



# Masses on a log scale

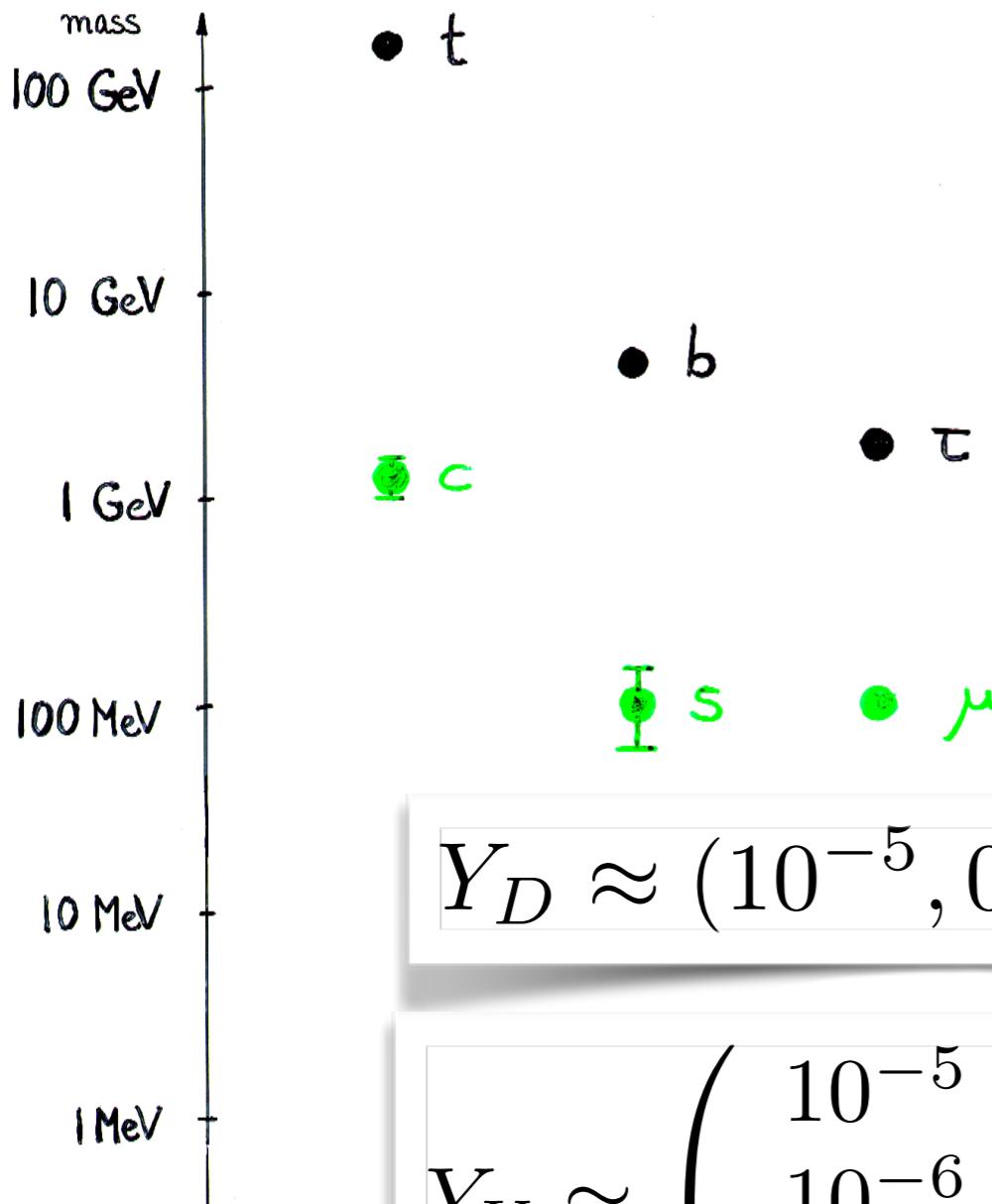


$$\mathcal{L}_{\text{Yuk}} = [Y^U]_{ij} \bar{Q}_i H_c u_j + \dots$$

$$Y_D \approx (10^{-5}, 0.0005, 0.026)$$

$$Y_U \approx \begin{pmatrix} 10^{-5} & -0.002 & 0.007 + 0.004i \\ 10^{-6} & 0.007 & -0.04 + 0.0008i \\ 10^{-8} + 10^{-7}i & 0.0003 & 0.92 \end{pmatrix}$$

# Masses on a log scale



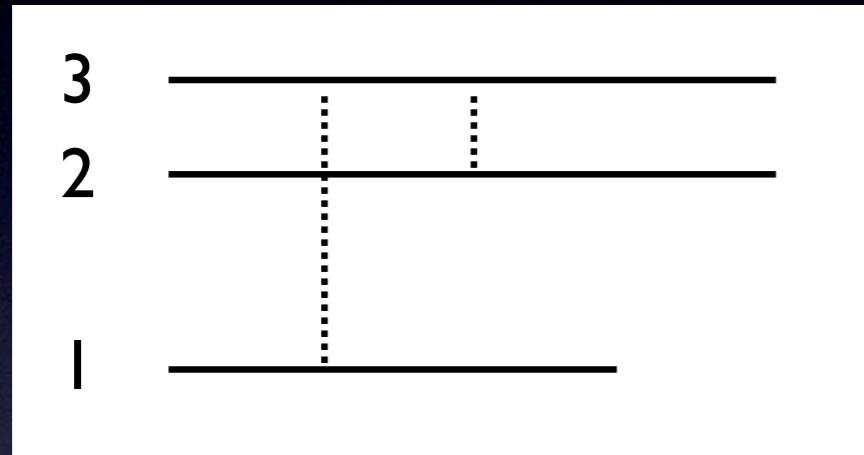
Compare to:  $g_s \sim 1$ ,  $g \sim 0.6$ ,  $g' \sim 0.3$ ,  
 $\lambda_{\text{Higgs}} \sim 1/8$

$$\mathcal{L}_{\text{Yuk}} = [Y^U]_{ij} \bar{Q}_i H_c u_j + \dots$$

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Analog to mysterious spectral lines before QM



$$\nu = \left( \frac{1}{n^2} - \frac{1}{m^2} \right) R$$

Explained by Bohr

$$E_n = -\frac{2\pi^2 e^4 m_e}{h^2 n^2}$$

Is there an analogue to the Bohr atom, we might discover at the LHC?

# Flavor dynamics @ LHC ?

Exciting possibility

I) Lack of scale

$$\mathcal{L}_{\text{flavor}} = [Y^U]_{ij} \bar{Q}_i H_c u_j + \dots$$

$$\text{dim } 0 + 3/2 + 1 + 3/2 = 4$$

2) Very strong constraints from flavor physics:  
Generic flavor dynamics  $\gg 100 \text{ TeV}$

Tev?  $10^3 \text{ TeV? } 10^{16} \text{ GeV?}$

Top as a destabilizing  
agent

# Stability and meta-stability

Tree-level

Cabibbo, Maiani, Parisi, Petronzio, '79;  
Hung '79; Lindner 86; Sher '89; ...

$$V(\phi) = -\mu^2|\phi|^2 + \lambda|\phi|^4$$

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Quantum fluctuations change potential

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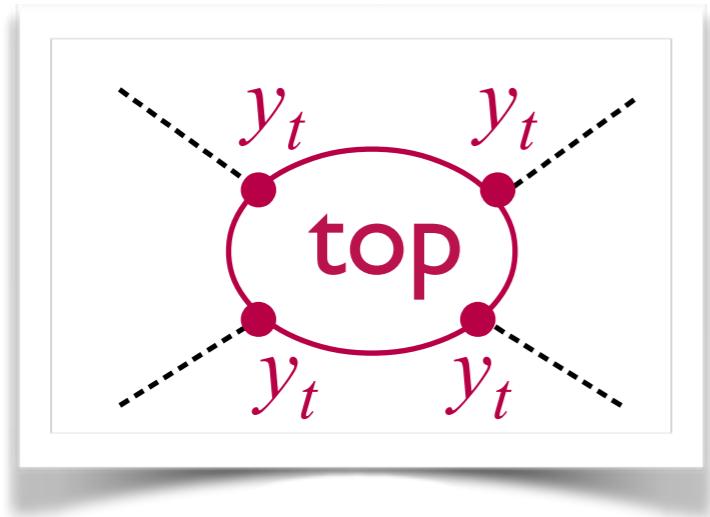
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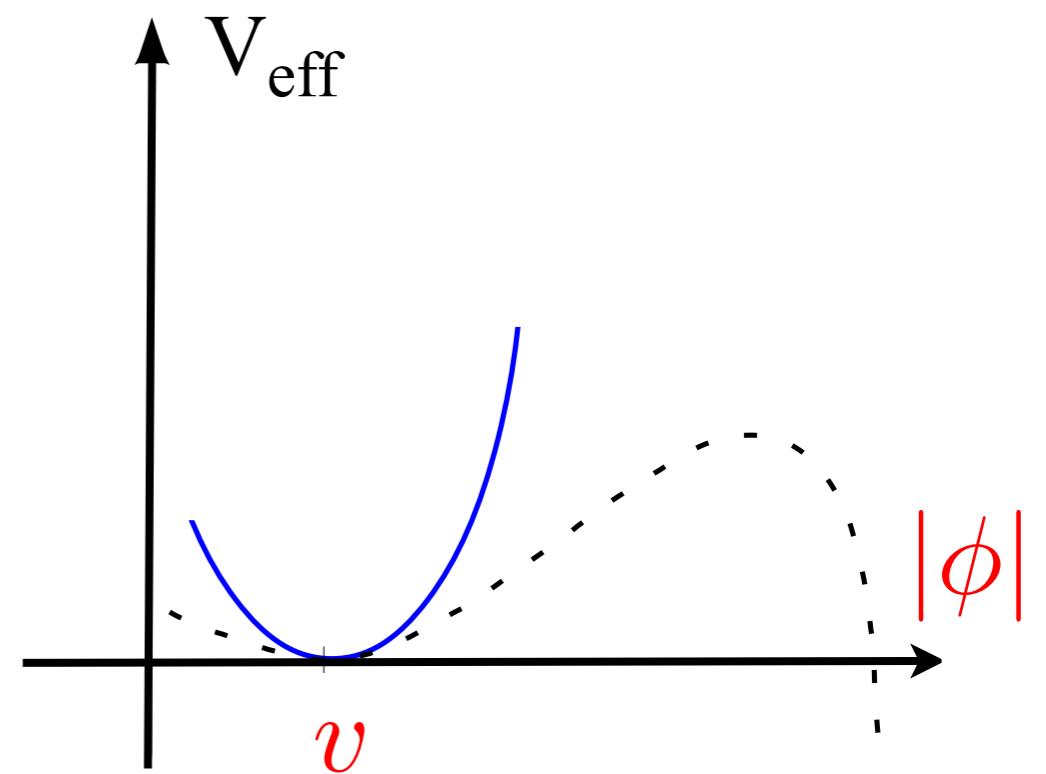
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decreasing  
at large  
Energies  
=>



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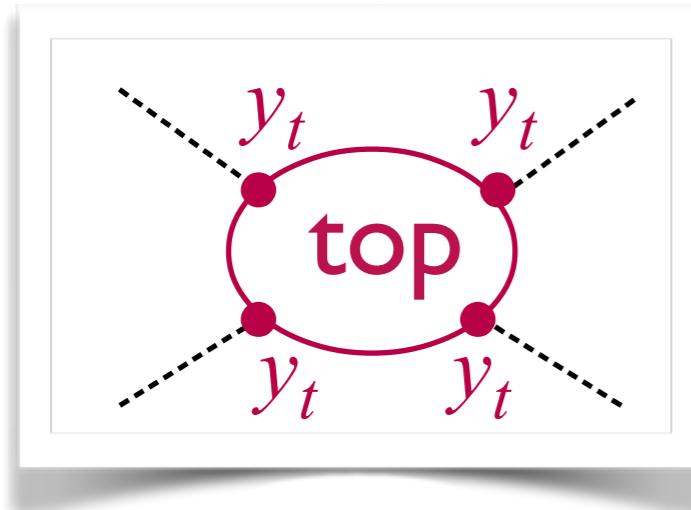
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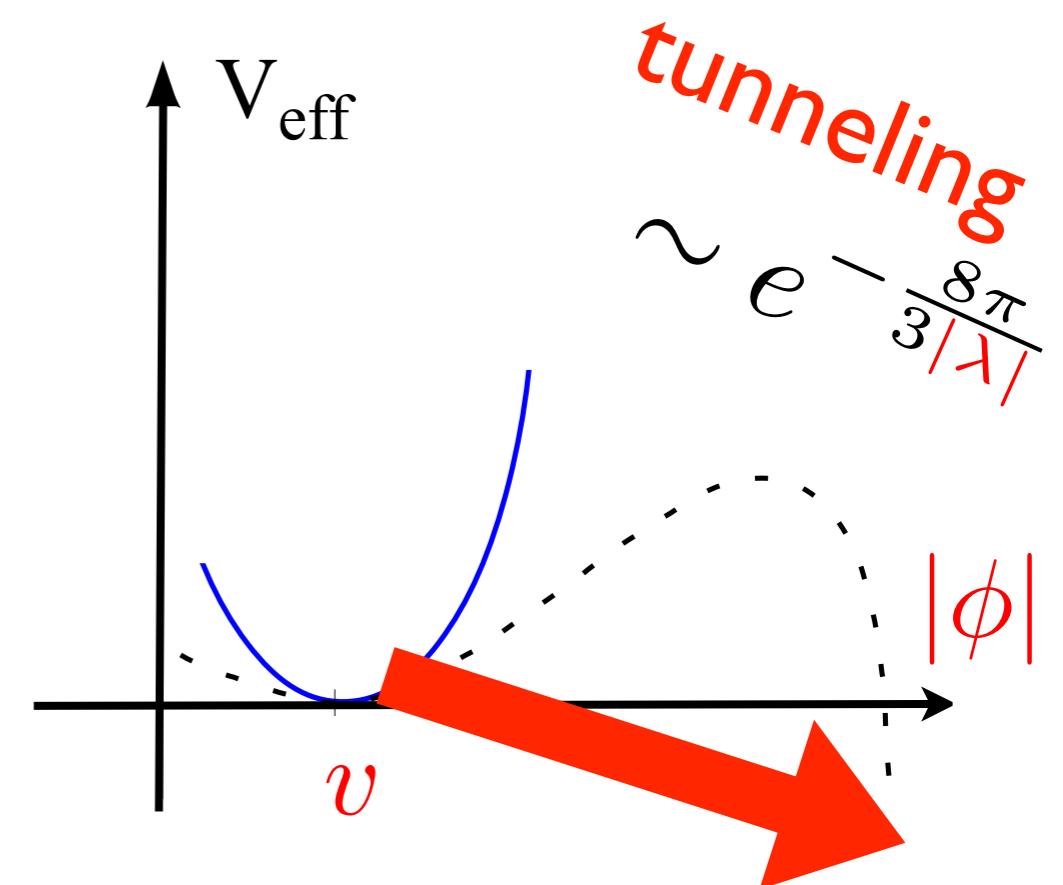
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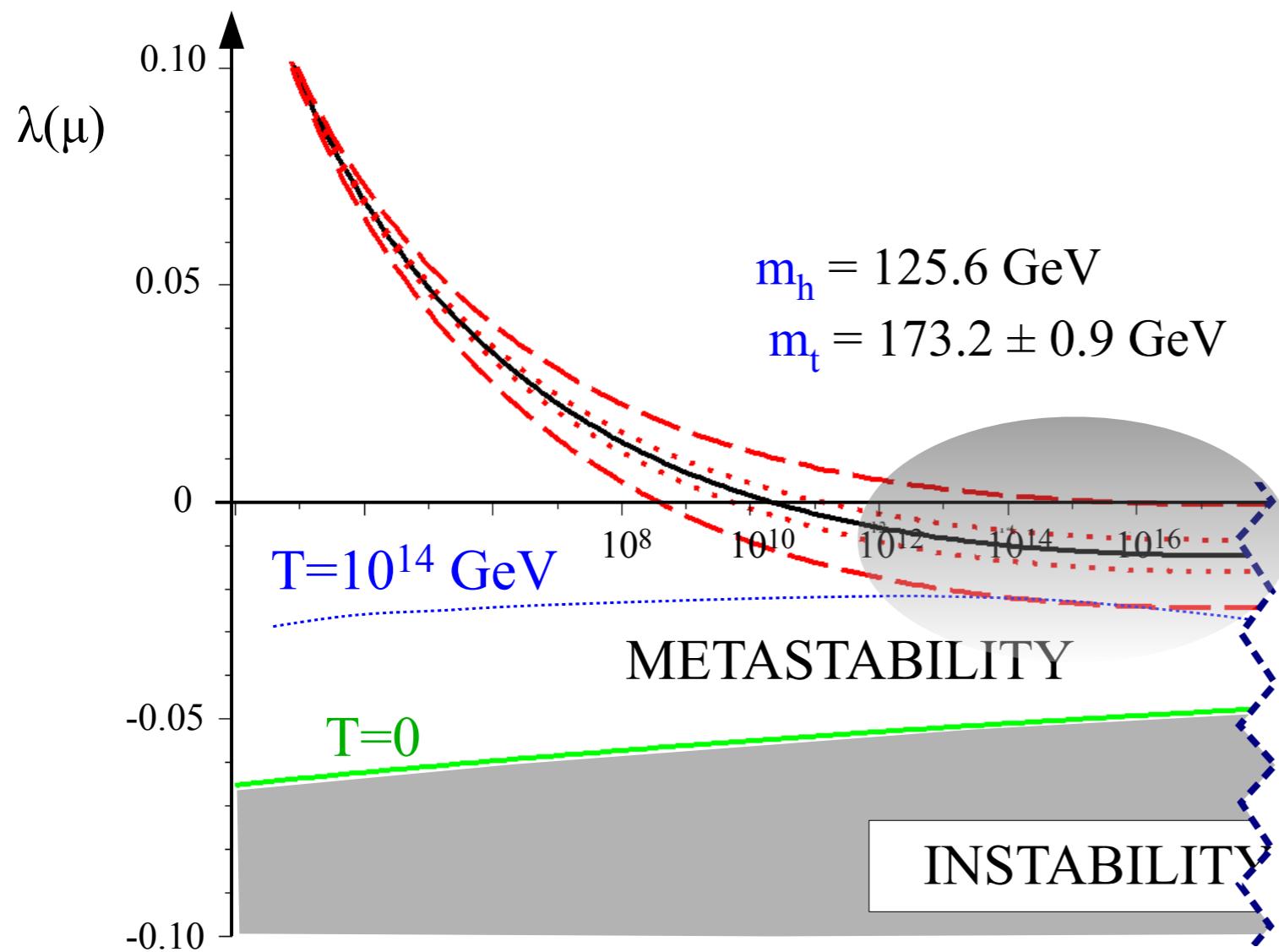


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# Stability and meta-stability

SM vacuum is unstable but sufficiently long-lived,  
(depends on  $m_{top}$ ,  $m_{Higgs}$ )

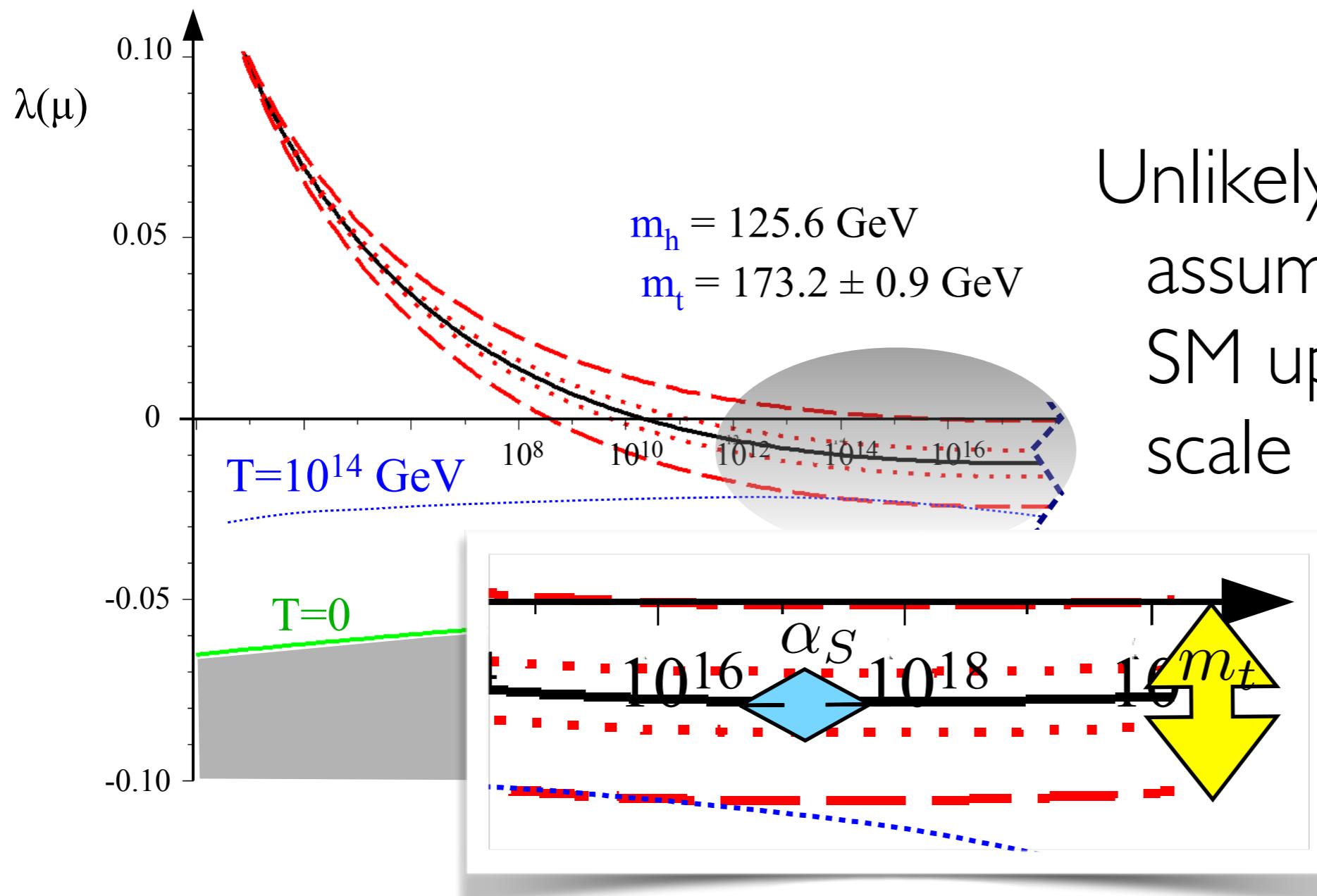


cf Elias-Miro et al. '12  
Degrassi et al. '12  
Buttazzo et al. '12

Unlikely the full story,  
assumes nothing but  
SM up to the Planck  
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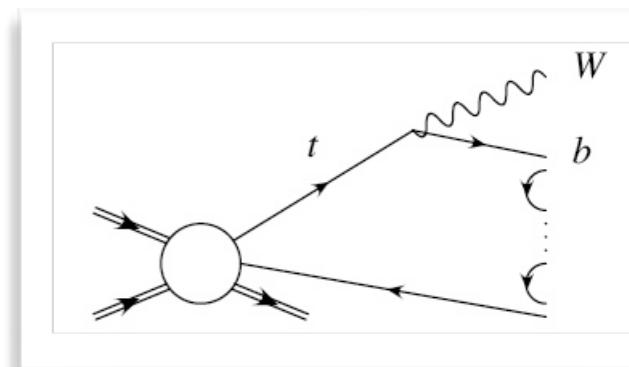
decisive  
uncertainty  
 $m_{top}$

# Absolute stability

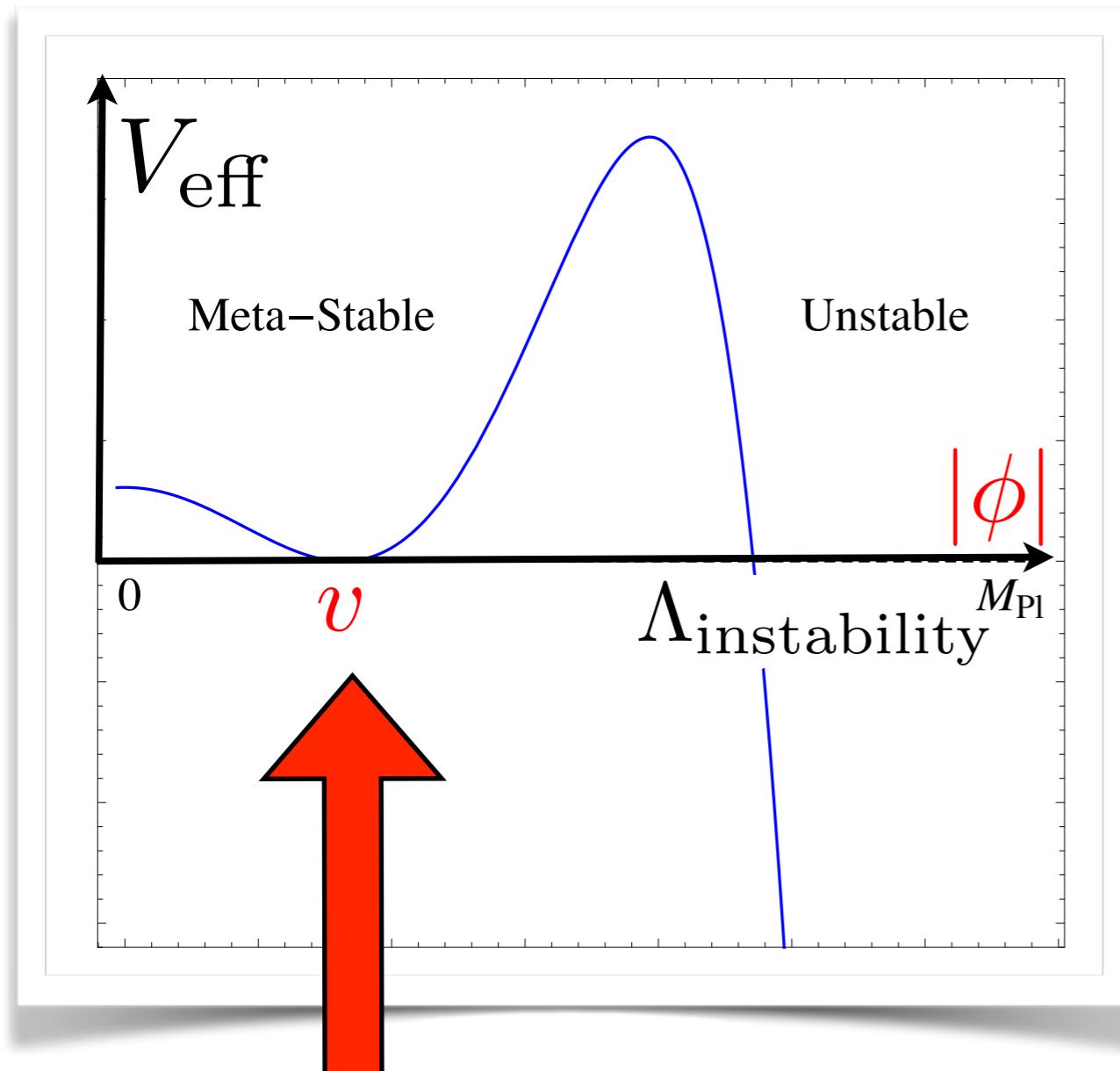
$$M_h \text{ [GeV]} > 129.4 + 2.0 \left( \frac{M_t \text{ [GeV]} - 173.1}{1.0} \right) - 0.5 \left( \frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0_{\text{th}}$$

- Top mass precision very important, convergence of theory and experiment crucial. Pole mass vs. ...

$$m^{\text{exp}} = m_t^{\text{pole}} + ?$$

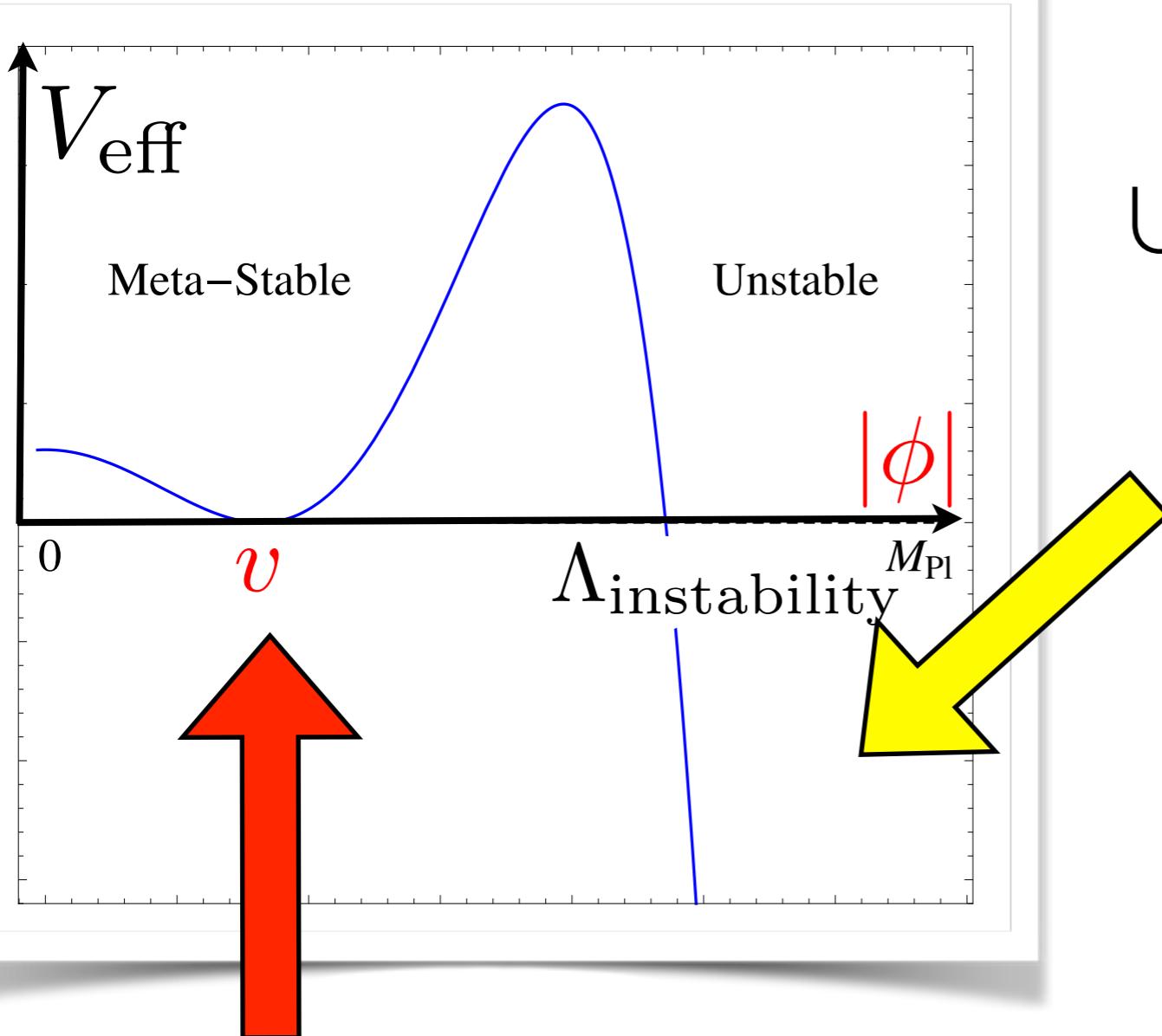


# If metastable: How did we end up in the energetically disfavoured vacuum?



You are here?!

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You are here?!

Universe is overwhelmingly likely to evolve to true ground state

**Fine-tuning of initial conditions?**

$\sim \Lambda_{\text{instability}} / M_{\text{Planck}}$

For  $\Lambda_{\text{instability}} \sim 10^{10} \text{ GeV} \rightarrow 10^{-8}$

## Tree-level

$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

quantum fluctuations  
**destabilise Higgs mass<sup>2</sup>**

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# The hierarchy problem

- The SM is a success also because of its accidental symmetries, all null-tests successful so far
- $B, L, CP$  and flavor are conserved / broken by tiny amounts



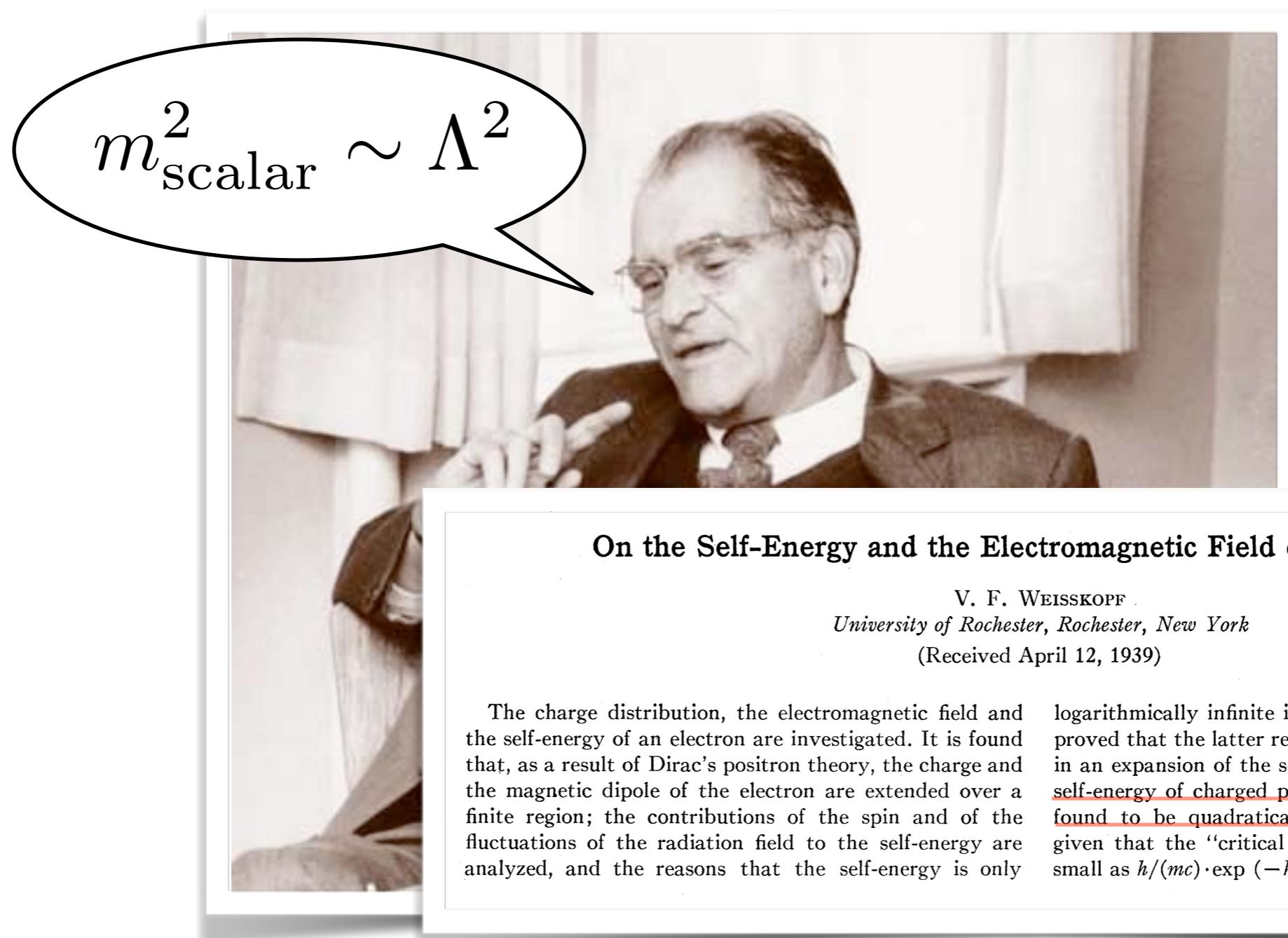
- Broken by irrelevant operators of SM fields, suppressed by a mass scale. Accidental symmetries require a **hierarchy of scales!**

$$\Lambda_{\text{SM}} \ll \Lambda_B$$

# What's the problem?



# What's the problem?


$$m_{\text{scalar}}^2 \sim \Lambda^2$$

**On the Self-Energy and the Electromagnetic Field of the Electron**

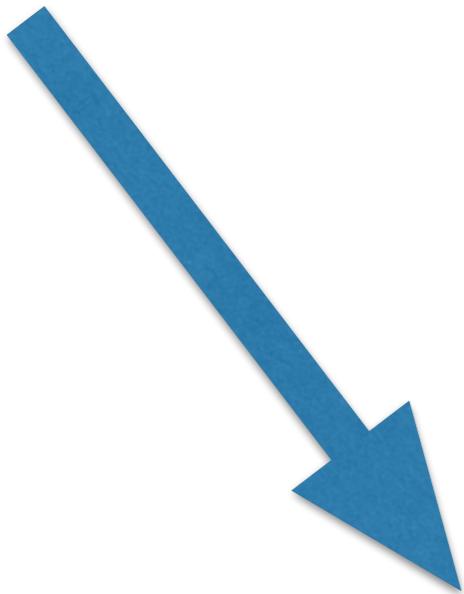
V. F. WEISSKOPF  
*University of Rochester, Rochester, New York*  
(Received April 12, 1939)

The charge distribution, the electromagnetic field and the self-energy of an electron are investigated. It is found that, as a result of Dirac's positron theory, the charge and the magnetic dipole of the electron are extended over a finite region; the contributions of the spin and of the fluctuations of the radiation field to the self-energy are analyzed, and the reasons that the self-energy is only logarithmically infinite in positron theory are given. It is proved that the latter result holds to every approximation in an expansion of the self-energy in powers of  $e^2/hc$ . The self-energy of charged particles obeying Bose statistics is found to be quadratically divergent. Some evidence is given that the "critical length" of positron theory is as small as  $h/(mc) \cdot \exp(-hc/e^2)$ .

Weisskopf, Phys. Rev. 56 (1939) 72

# The hierarchy problem

$$\beta_{m_h^2} = \frac{dm_h^2}{d\log\bar{\mu}} = \frac{3m_h^2}{8\pi^2} \left( 2\lambda + y_t^2 - \frac{3g^2}{4} - \frac{g'^2}{4} \right) \quad (\text{SM})$$

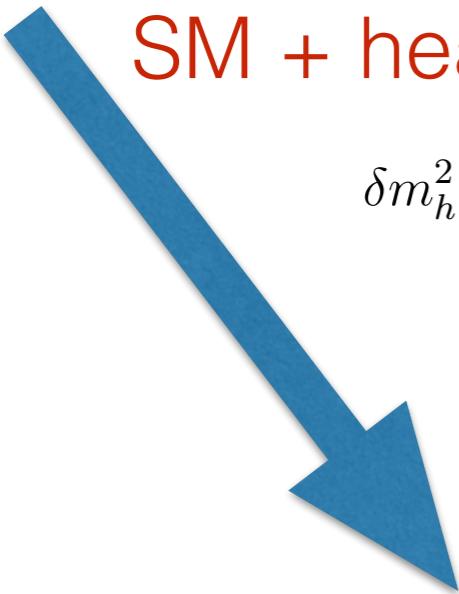


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SM + heavy Dirac fermion of mass  $M \gg m_h$  and yukawa  $y$

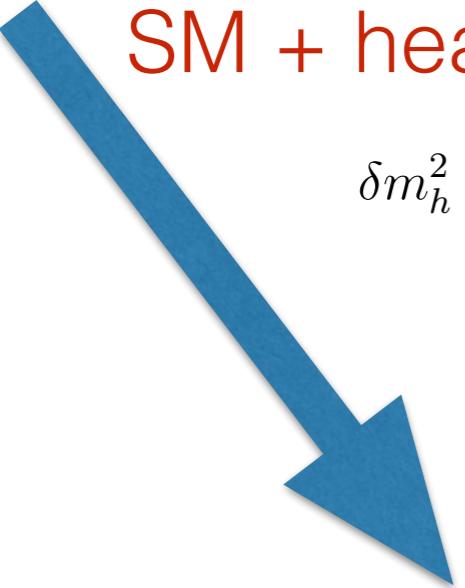
$$\begin{aligned} \delta m_h^2 &= \text{Re } \Pi_{hh}|_{p^2=m_h^2} = \frac{y^2}{2(4\pi)^2} \text{Re} [\Delta_\epsilon + (m_h^2 - 4M^2)B_0(m_h; M, M) - 2A_0(M)] \\ &= \frac{y^2}{2(4\pi)^2} \left( \Delta_\epsilon + (6M^2 - m_h^2) \log \frac{m_h^2}{\bar{\mu}^2} + f(m_h, M) \right), \end{aligned}$$



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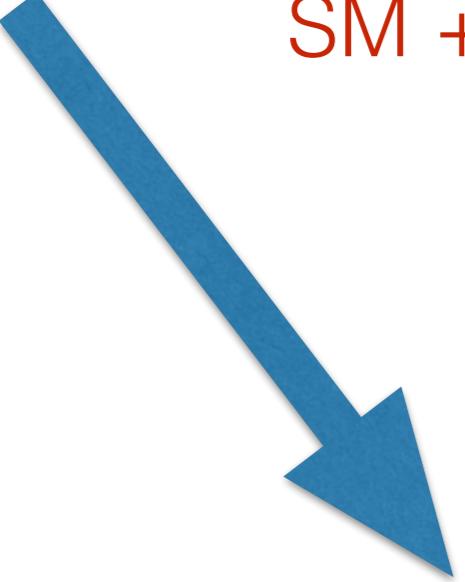

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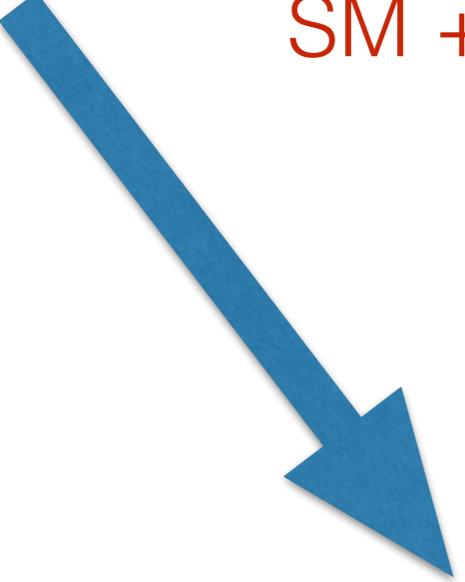
$$m_h^2(\Lambda_{\text{SM}}) \simeq m_h^2(\Lambda_{\text{NP}}) - \mathcal{O}(1) \Lambda_{\text{NP}}^2 \log \frac{\Lambda_{\text{NP}}}{\Lambda_{\text{SM}}}$$

Two contributions in have to balance out with very high accuracy  
to generate a Higgs boson mass much smaller than  $\Lambda_{\text{NP}}$

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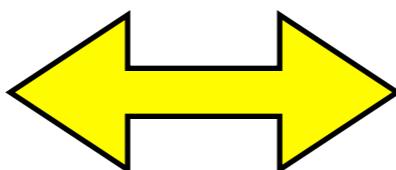
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For  $\Lambda = M_{\text{Planck}}, M_{\text{GUT}}, 10 \text{ TeV} :$      $\epsilon \sim 10^{-32}, 10^{-28}, 10^{-4}$

# Principle: UV insensitivity

**Naturalness** : absence of special conspiracies  
between **phenomena occurring at very different length scales.**



# Hierarchy problem

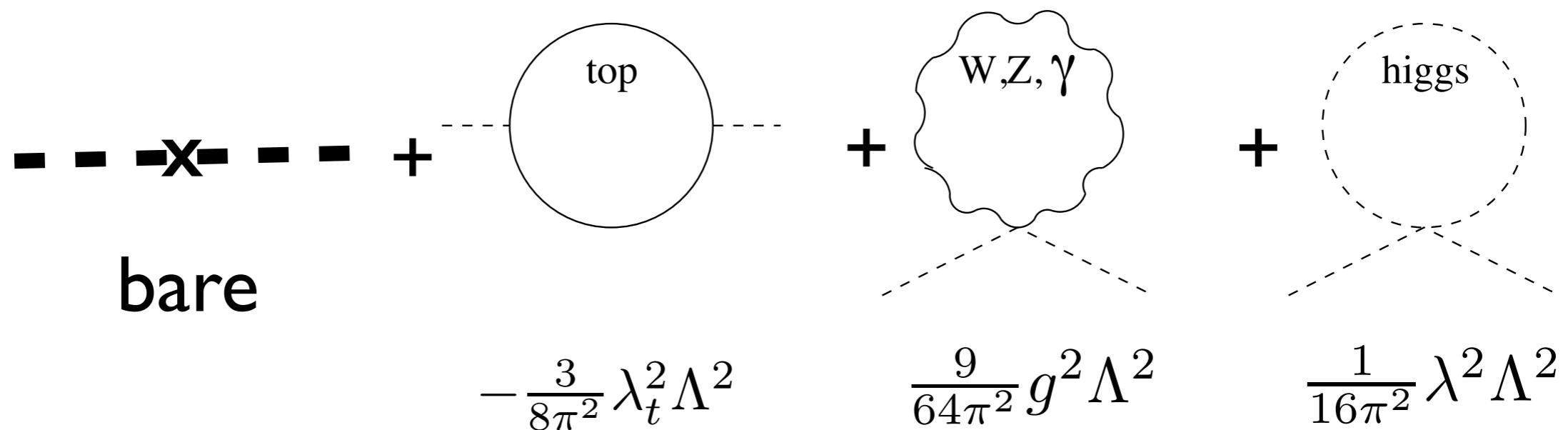
- Higgs mass sensitive to thresholds (GUT, gravity)
- Enormous quantum corrections  $\mathcal{O}(\text{highest scale})$  exceed Higgs mass' physical value: **fine-tuned** parameters

- - **X** - - +

bare

# Hierarchy problem

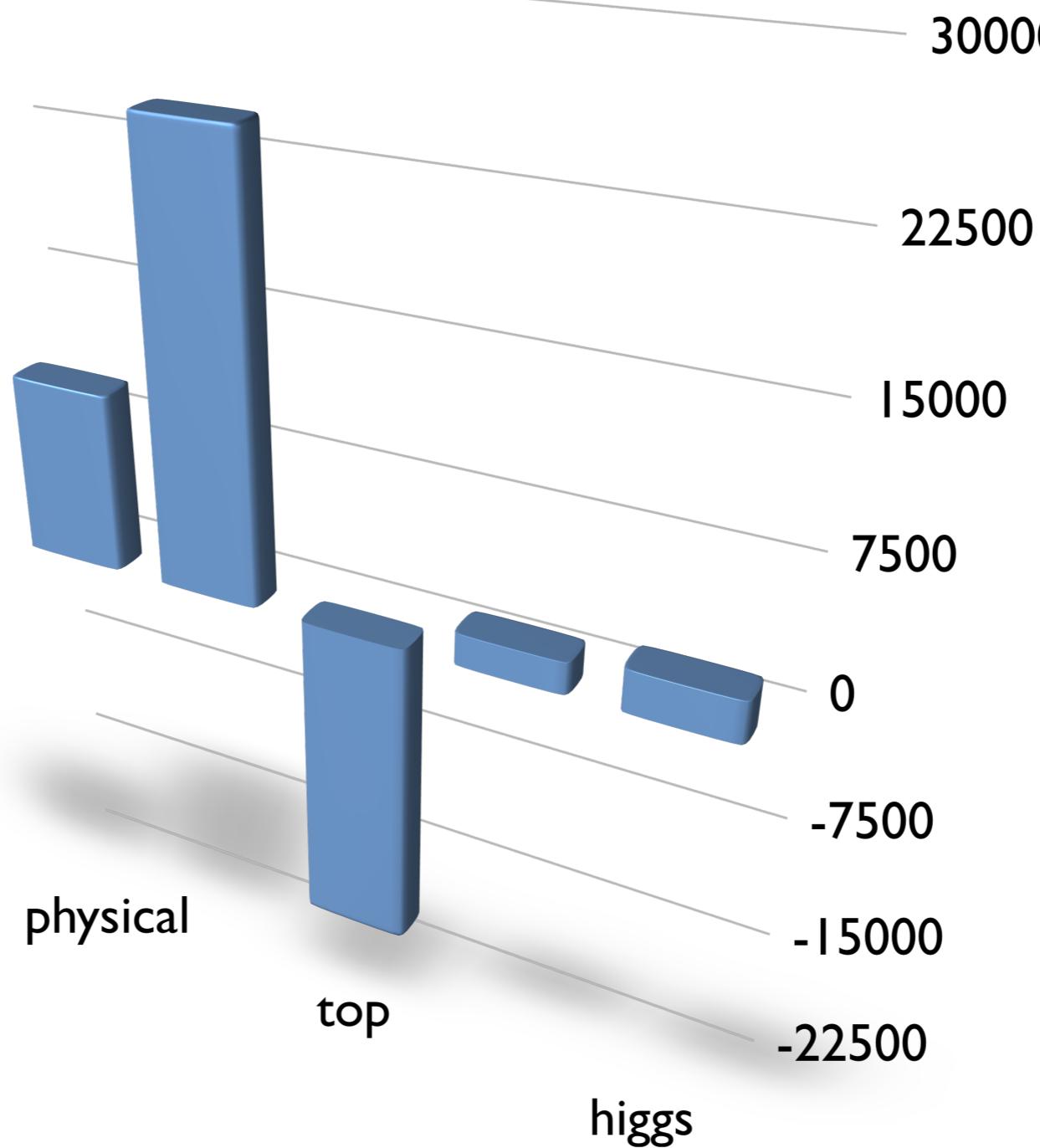
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$$m_h^2(\text{physical}) = m_h^2(\text{bare}) + \sum_i a_i \Lambda^2$$

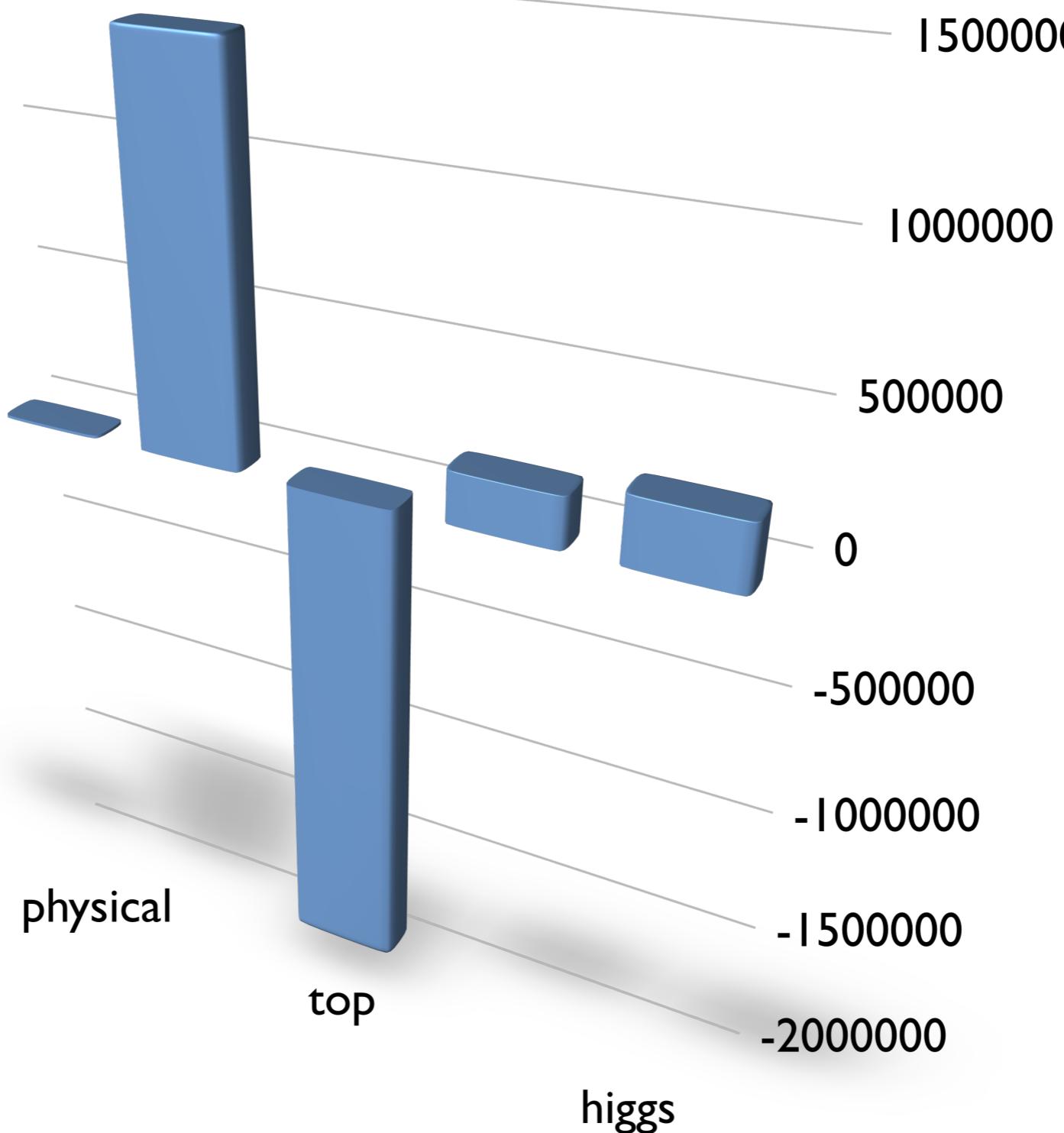
$\Lambda = 1 \text{ TeV}$

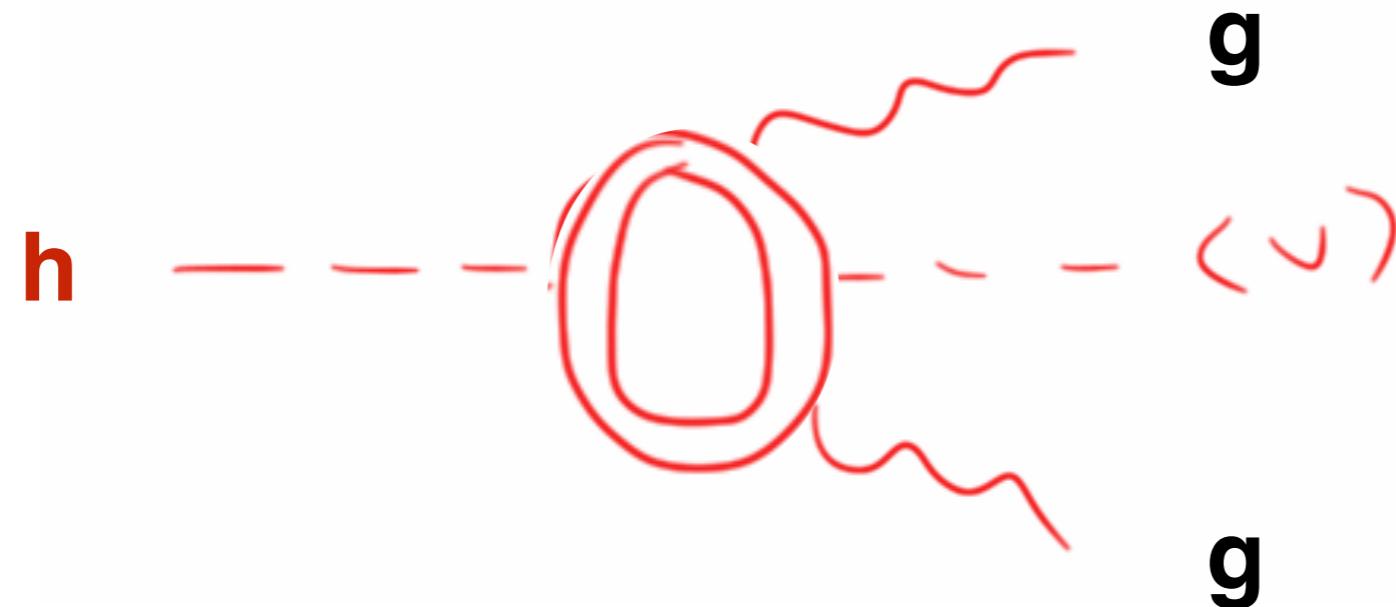
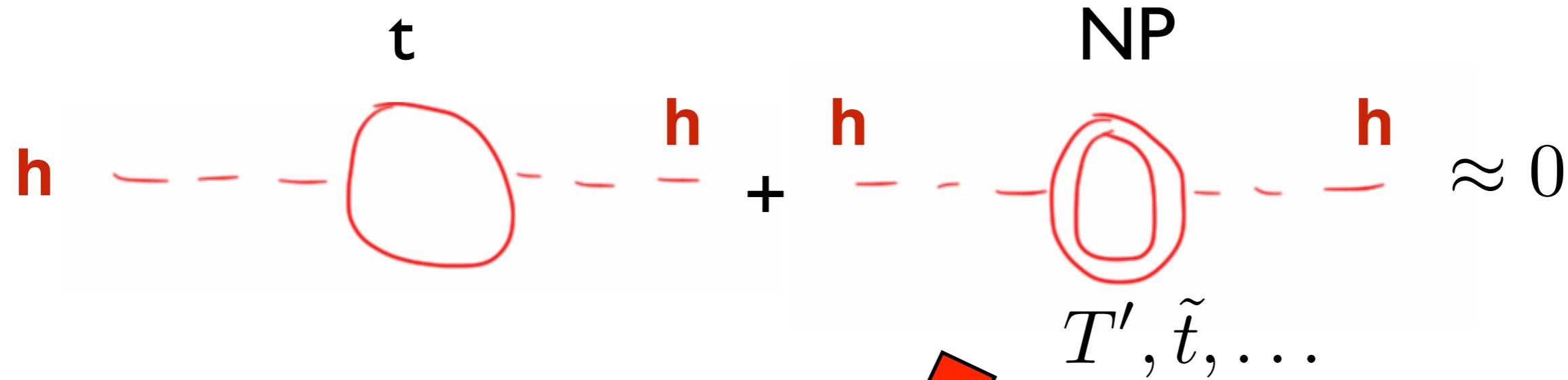
$\text{GeV}^2$



$\Lambda = 10 \text{ TeV}$

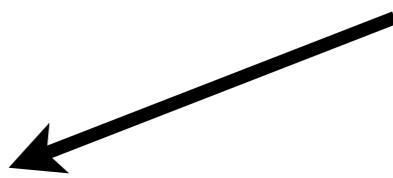
$\text{GeV}^2$





# Higgs precision properties expected to change

**change Higgs  
kin. term:**  
**VV → h**



$\mathcal{O}_H = \frac{1}{2}(\partial^\mu  H ^2)^2$
$\mathcal{O}_T = \frac{1}{2} \left( H^\dagger \overset{\leftrightarrow}{D}_\mu H \right)^2$
$\mathcal{O}_6 = \lambda  H ^6$

**LEP1 + MW  
(per-mille)**

**LEP2: e+e- → W+ W-  
(per-cent)**

**h → γγ** ←  
**GG → h** ←  
**h → ff** ←

$\mathcal{O}_{HW} = ig(D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a$
$\mathcal{O}_{HB} = ig'(D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$
$\mathcal{O}_{BB} = g'^2  H ^2 B_{\mu\nu} B^{\mu\nu}$
$\mathcal{O}_{GG} = g_s^2  H ^2 G_{\mu\nu}^A G^{A\mu\nu}$
$\mathcal{O}_{3W} = \frac{1}{3!} g \epsilon_{abc} W_\mu^{a\nu} W_\nu^{b\rho} W_\rho^{c\mu}$

$\mathcal{O}_{y_u} = y_u  H ^2 \bar{Q}_L \tilde{H} u_R$	$\mathcal{O}_{y_d} = y_d  H ^2 \bar{Q}_L H d_R$	$\mathcal{O}_{y_e} = y_e  H ^2 \bar{L}_L H e_R$
$\mathcal{O}_R^u = (iH^\dagger \overset{\leftrightarrow}{D}_\mu H)(\bar{u}_R \gamma^\mu u_R)$	$\mathcal{O}_R^d = (iH^\dagger \overset{\leftrightarrow}{D}_\mu H)(\bar{d}_R \gamma^\mu d_R)$	$\mathcal{O}_R^e = (iH^\dagger \overset{\leftrightarrow}{D}_\mu H)(\bar{e}_R \gamma^\mu e_R)$
$\mathcal{O}_L^q = (iH^\dagger \overset{\leftrightarrow}{D}_\mu H)(\bar{Q}_L \gamma^\mu Q_L)$		
$\mathcal{O}_L^{(3)q} = (iH^\dagger \sigma^a \overset{\leftrightarrow}{D}_\mu H)(\bar{Q}_L \sigma^a \gamma^\mu Q_L)$		$\mathcal{O}_{LL}^{(3)l} = (\bar{L}_L \sigma^a \gamma^\mu L_L)(\bar{L}_L \sigma^a \gamma_\mu L_L)$

**change Higgs  
kin. term:**

**VV → h**

**h → γγ**

**GG → h**

**h → ff**

$\mathcal{O}_H = \frac{1}{2}(\partial^\mu H ^2)^2$	$\mathcal{O}_T = \frac{1}{2} \left( H^\dagger \overset{\leftrightarrow}{D}_\mu H \right)^2$
$\mathcal{O}_6 = \lambda H ^6$	$\mathcal{O}_8 = \lambda H ^4 \partial^\mu \partial_\mu H$
$\mathcal{O}_{10} = i g' (D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a$	$\mathcal{O}_{11} = i g' (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$
$\mathcal{O}_{BB} = g'^2  H ^2 B_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{GG} = g_s^2  H ^2 G_{\mu\nu}^A G^{A\mu\nu}$
$\mathcal{O}_{3W} = \frac{1}{3!} g \epsilon_{abc} W_\mu^{a\nu} W_\nu^{b\rho} W_\rho^{c\mu}$	

**Probed for the first time at LHC!**

**LEP1 + MW  
(per-mille)**

**LEP2: e+e- → W+ W-  
(per-cent)**

$\mathcal{O}_{y_u} = y_u  H ^2 \bar{Q}_L \tilde{H} u_R$	$\mathcal{O}_{y_d} = y_d  H ^2 \bar{Q}_L H d_R$	$\mathcal{O}_{y_e} = y_e  H ^2 \bar{L}_L H e_R$
$\mathcal{O}_R^u = (i H^\dagger \overset{\leftrightarrow}{D}_\mu H)(\bar{u}_R \gamma^\mu u_R)$	$\mathcal{O}_R^d = (i H^\dagger \overset{\leftrightarrow}{D}_\mu H)(\bar{d}_R \gamma^\mu d_R)$	$\mathcal{O}_R^e = (i H^\dagger \overset{\leftrightarrow}{D}_\mu H)(\bar{e}_R \gamma^\mu e_R)$
$\mathcal{O}_L^q = (i H^\dagger \overset{\leftrightarrow}{D}_\mu H)(\bar{Q}_L \gamma^\mu Q_L)$		
$\mathcal{O}_L^{(3)q} = (i H^\dagger \sigma^a \overset{\leftrightarrow}{D}_\mu H)(\bar{Q}_L \sigma^a \gamma^\mu Q_L)$		$\mathcal{O}_{LL}^{(3)l} = (\bar{L}_L \sigma^a \gamma^\mu L_L)(\bar{L}_L \sigma^a \gamma_\mu L_L)$

# Higgs EFT

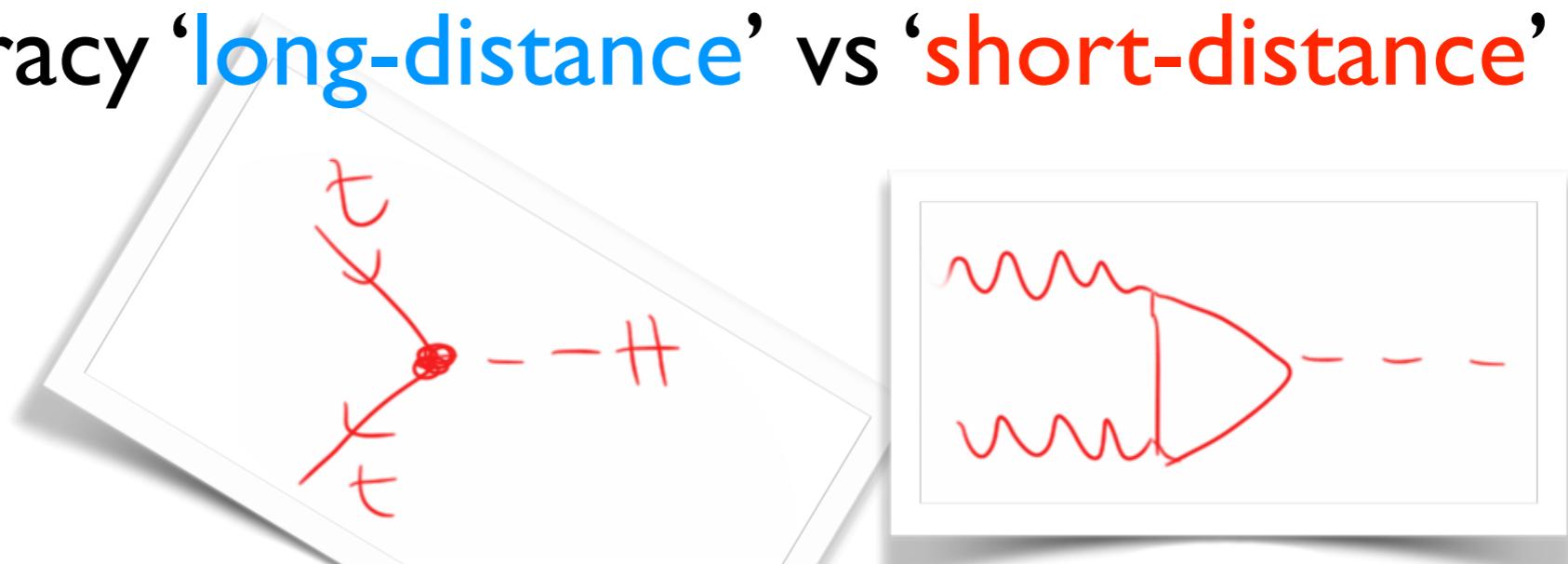
$$\mathcal{O}_t = \frac{y_t}{v^2} |H|^2 \bar{Q}_L \tilde{H} t_R, \quad \mathcal{O}_g = \frac{\alpha_s}{12\pi v^2} |H|^2 G_{\mu\nu}^a G^{a\mu\nu},$$

$$\mathcal{L} = \mathcal{L}_{SM} + (1 - c_t) \mathcal{O}_t + k_g \mathcal{O}_g.$$

$$\mu_{\text{incl}}(c_t, k_g) = \frac{\sigma_{\text{incl}}^{\text{BSM}}(c_t, k_g)}{\sigma_{\text{incl}}^{\text{SM}}} = (c_t + k_g)^2$$

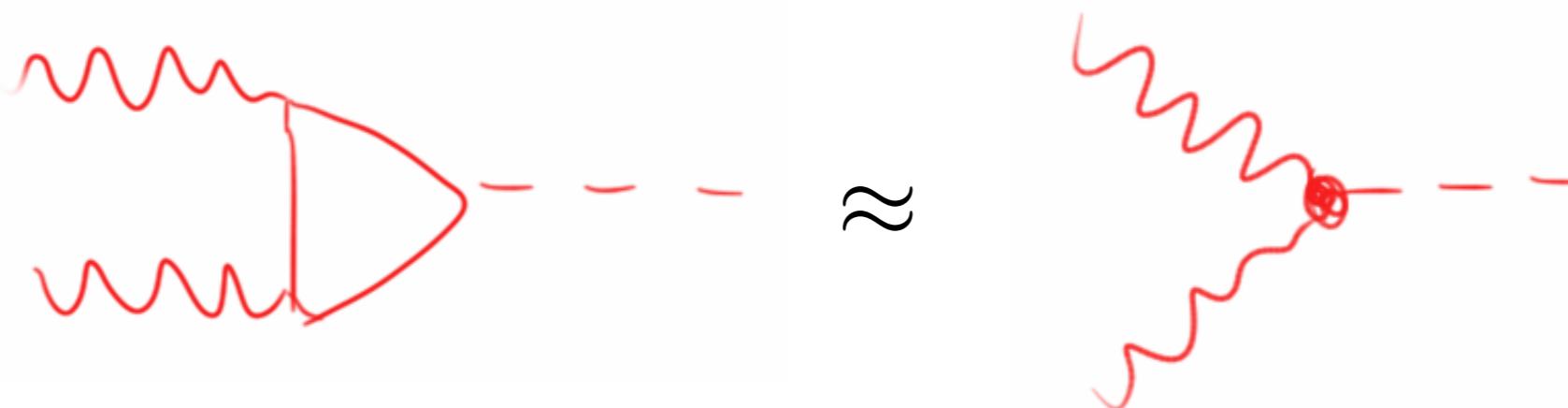


Degeneracy ‘long-distance’ vs ‘short-distance’



$$\sigma(pp \rightarrow H + X)_{\text{inclusive}}$$

Does not resolve short-distance physics

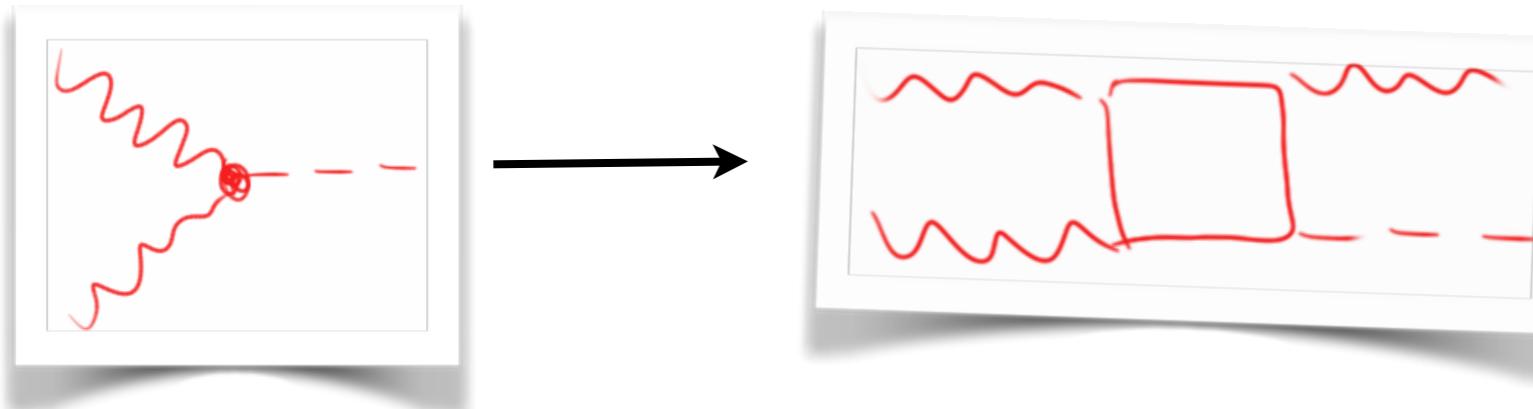


$m_H(\text{GeV})$	$\frac{\sigma_{NLO}(m_t)}{\sigma_{NLO}(m_t \rightarrow \infty)}$	$\frac{\sigma_{NLO}(m_t, m_b)}{\sigma_{NLO}(m_t \rightarrow \infty)}$
125	1.061	0.988
150	1.093	1.028
200	1.185	1.134

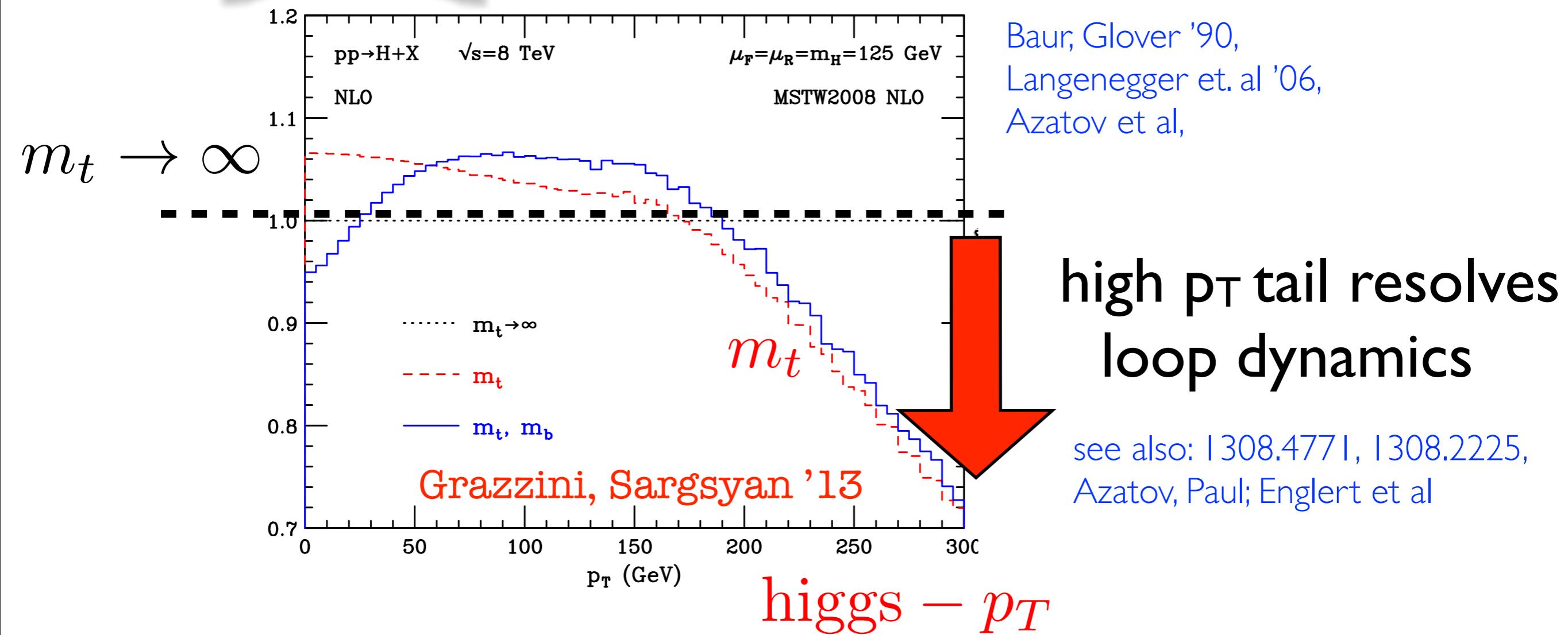
e.g. [1306.4581](#)

# Beyond current observables

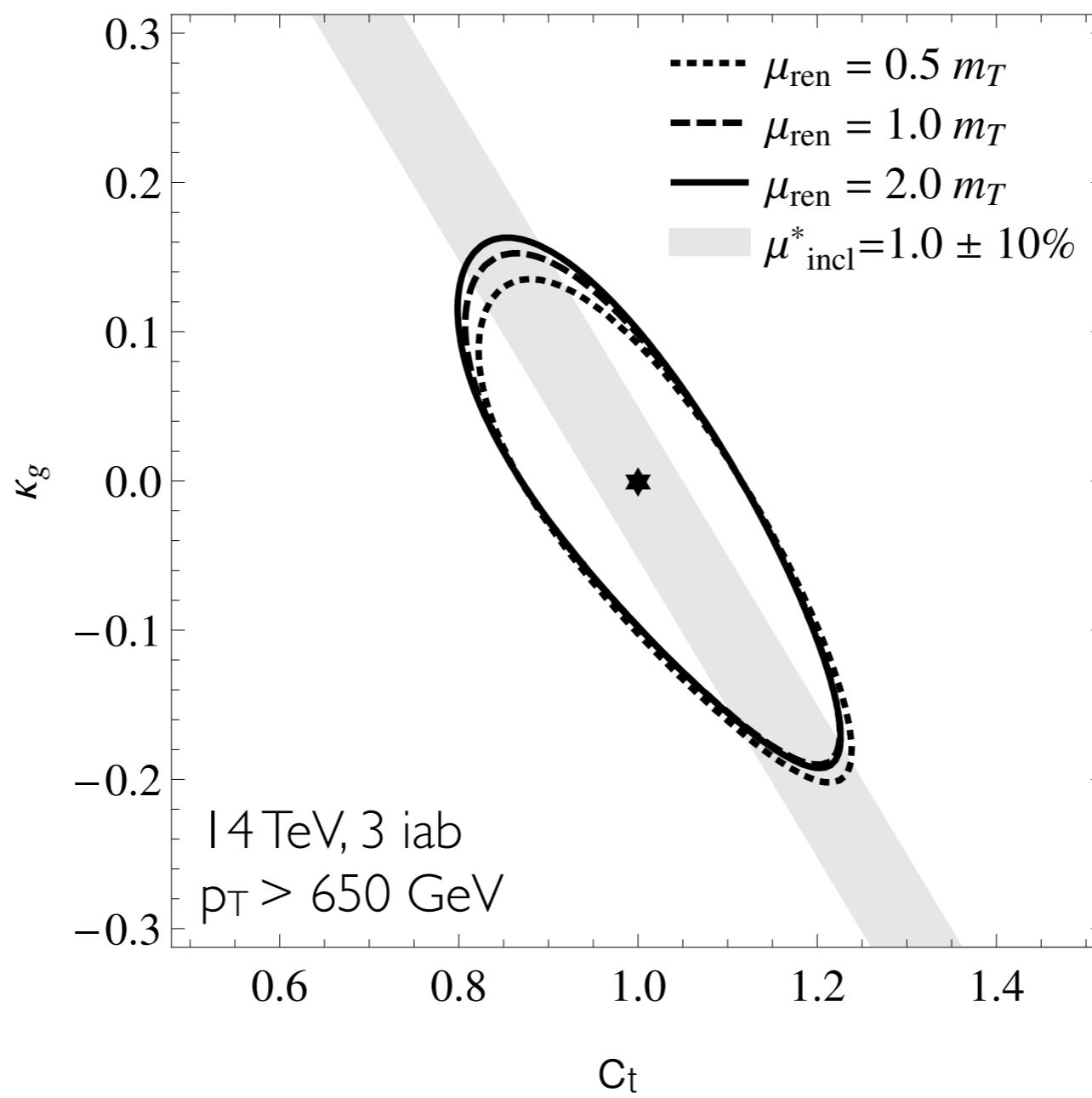
Resolve the loop, recoil against hard jet



$$p_T \gg m_t$$



# Boosted Higgs breaks degeneracy

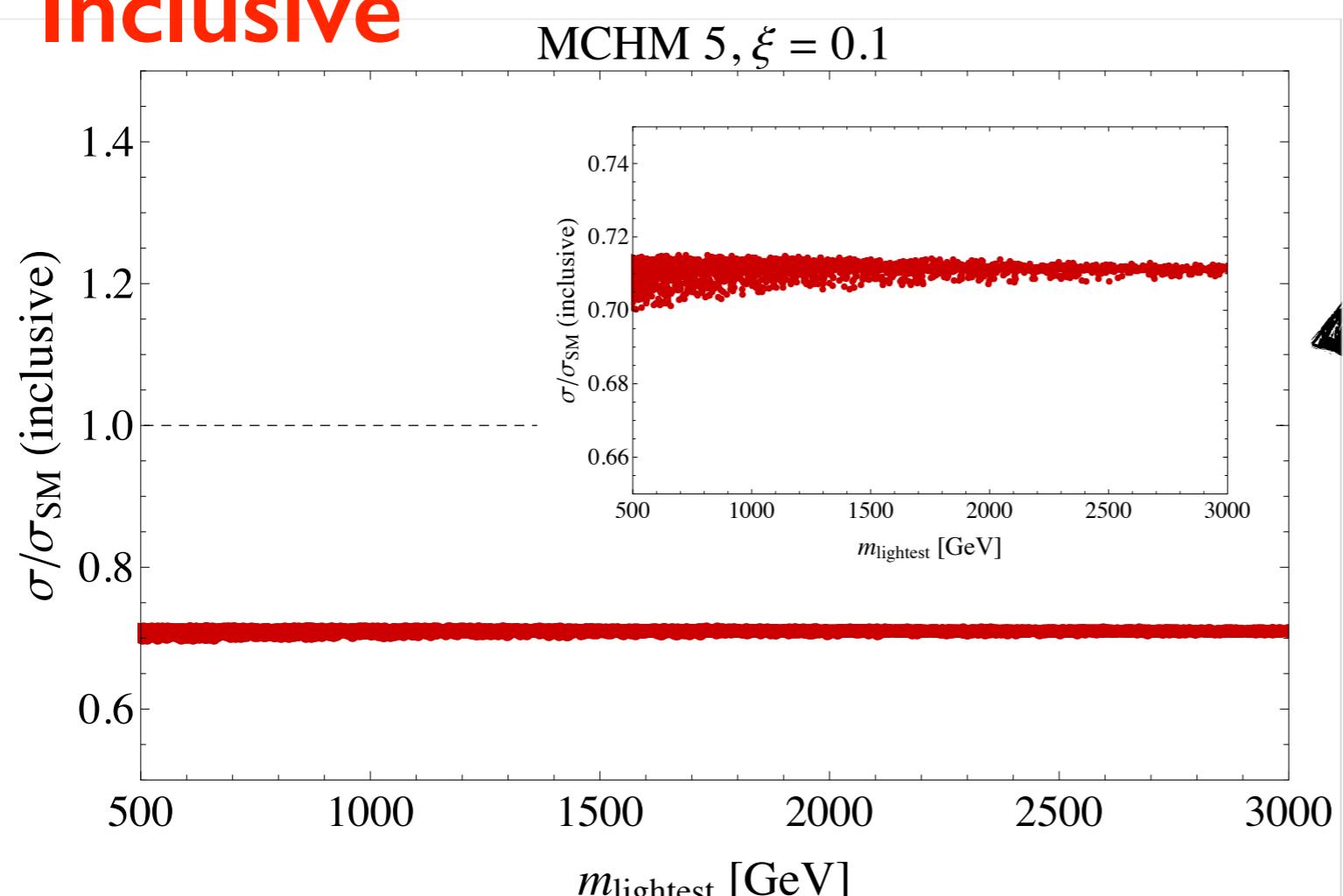


# Top partner example

Inclusive

MCHM 5,  $\xi = 0.1$

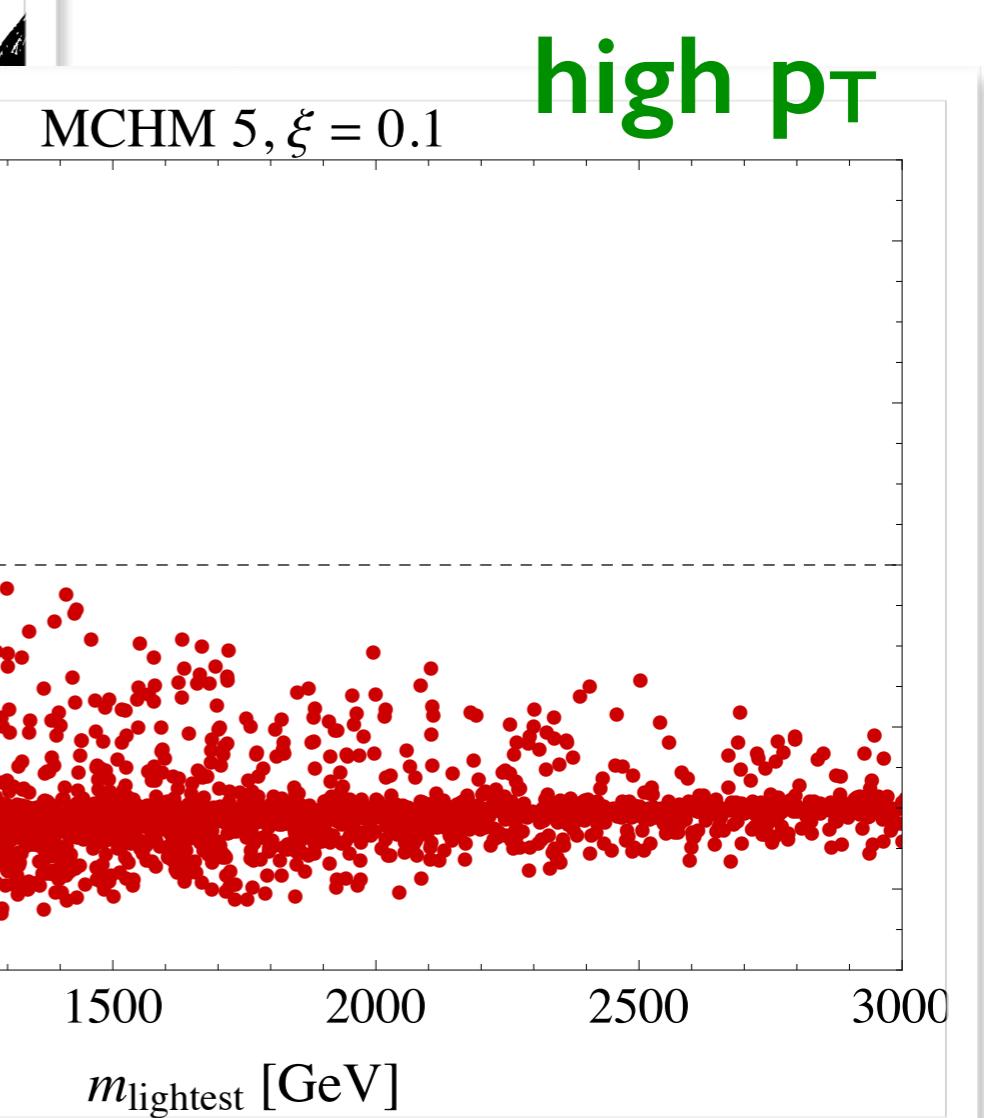
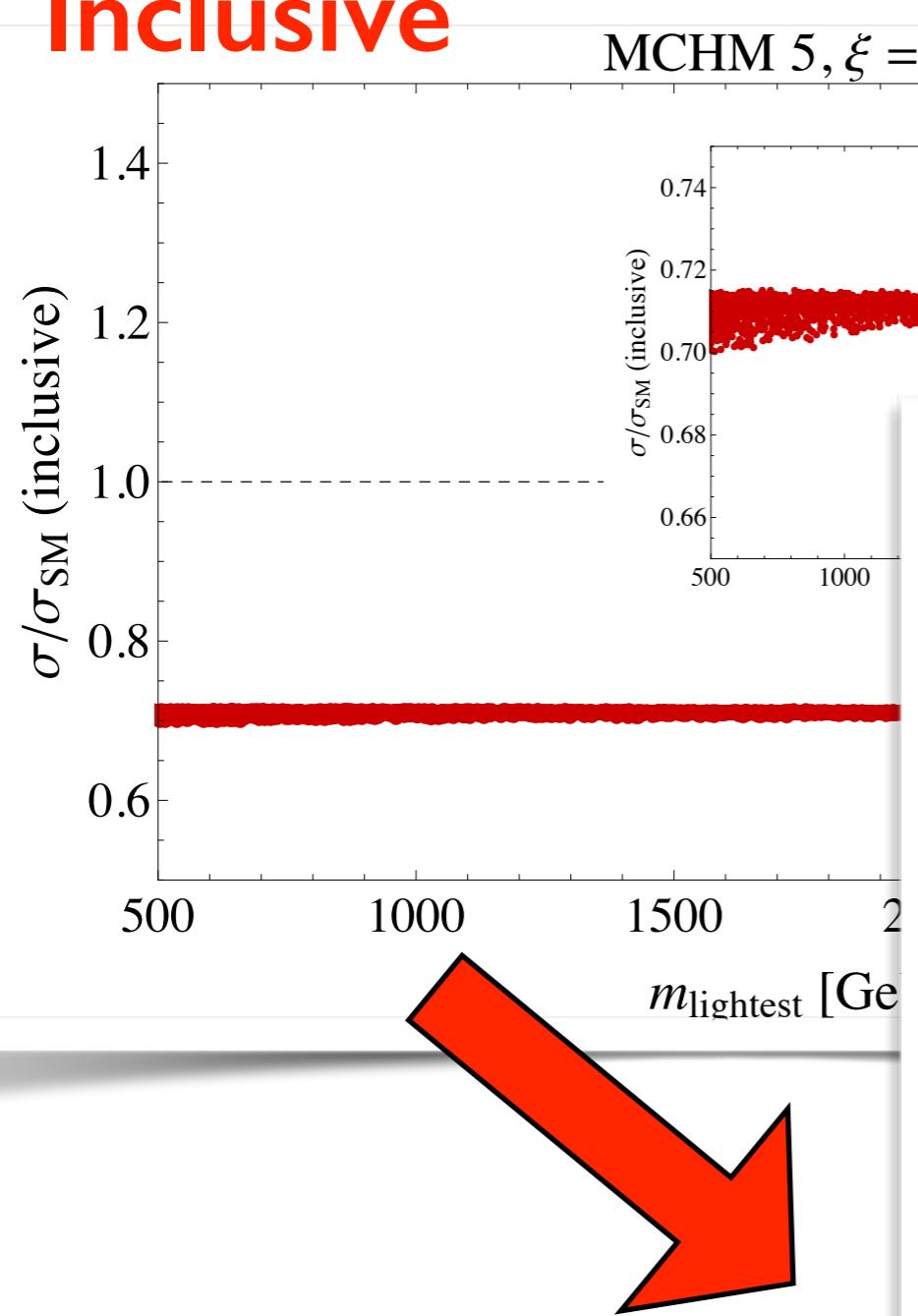
Grojean, Salvioni, Schlaffer, AW



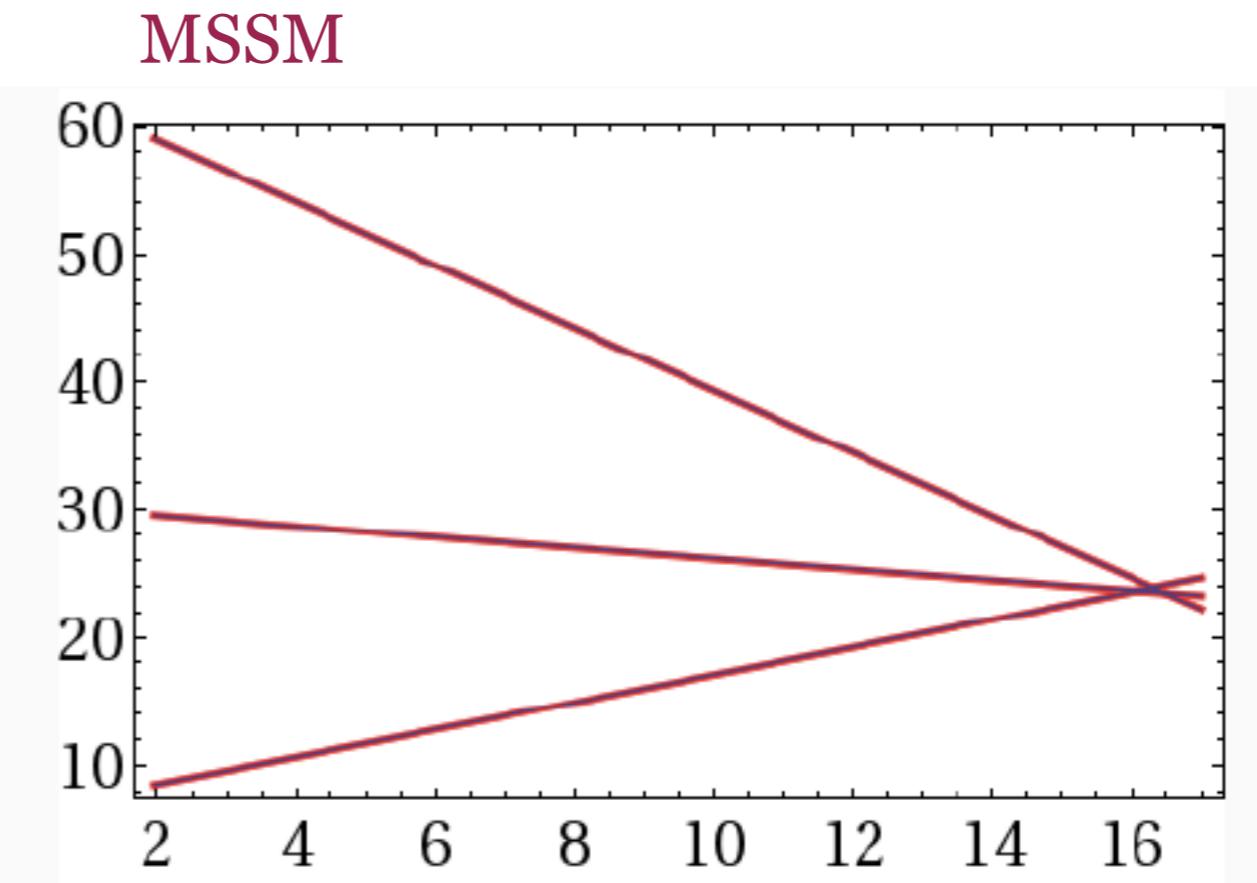
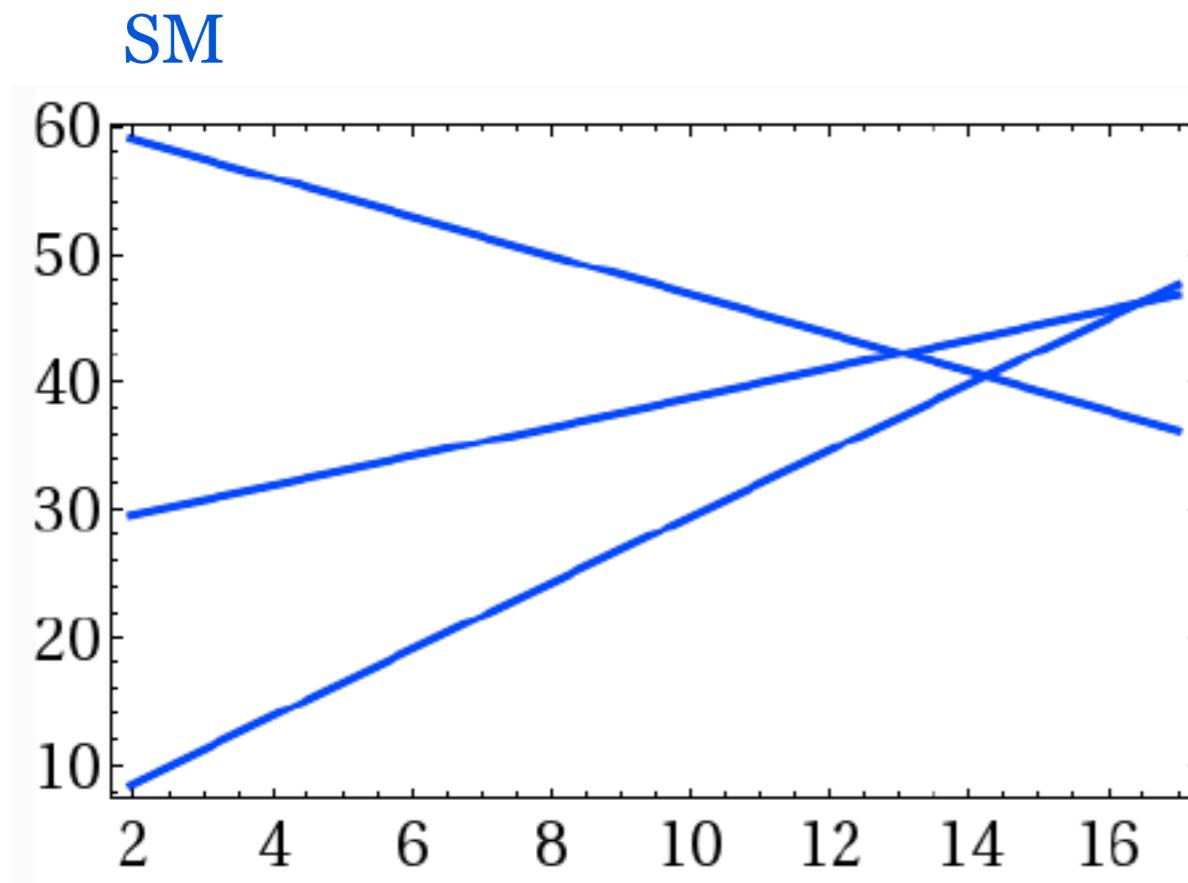
# Top partner example

Grojean, Salvioni, Schlaffer, AW

Inclusive

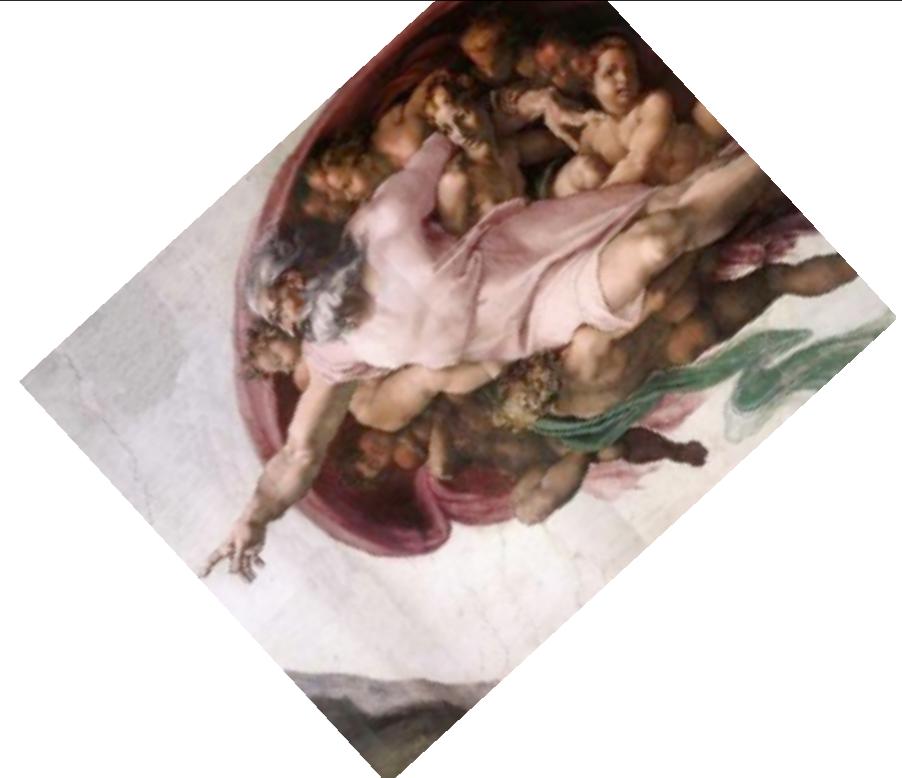


# A hint?

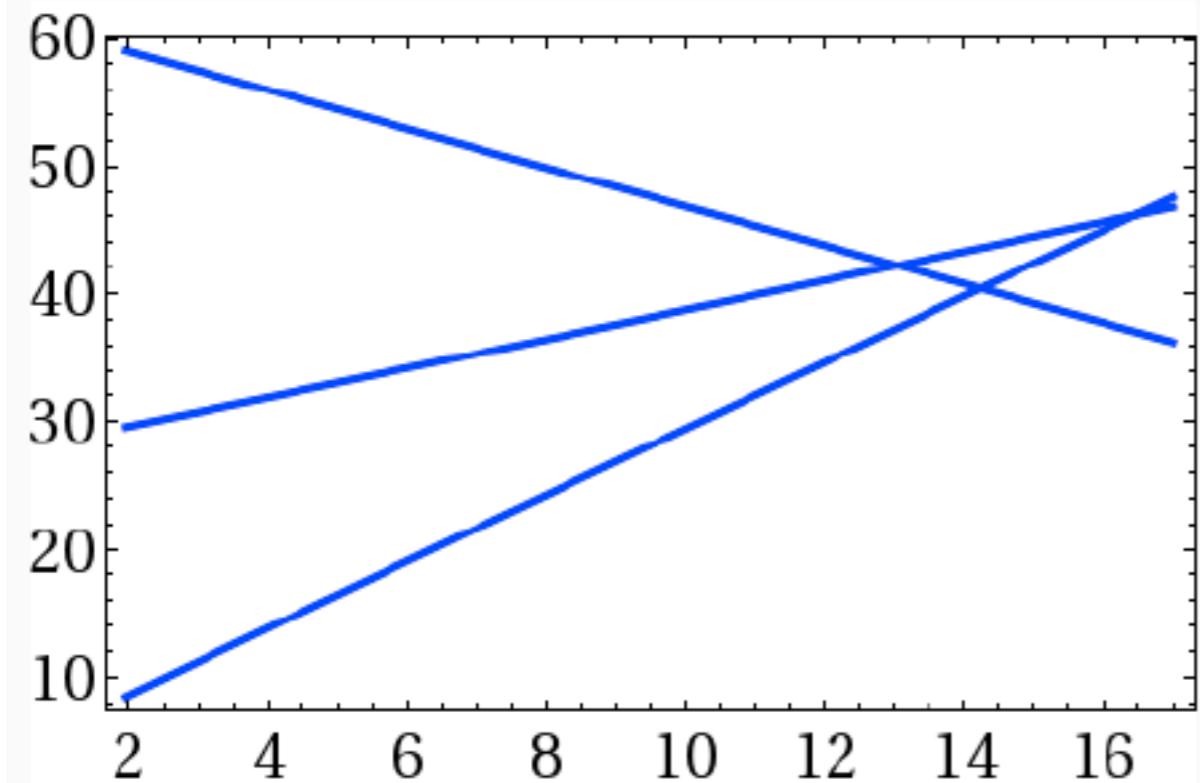


Gauge Coupling running at two loops

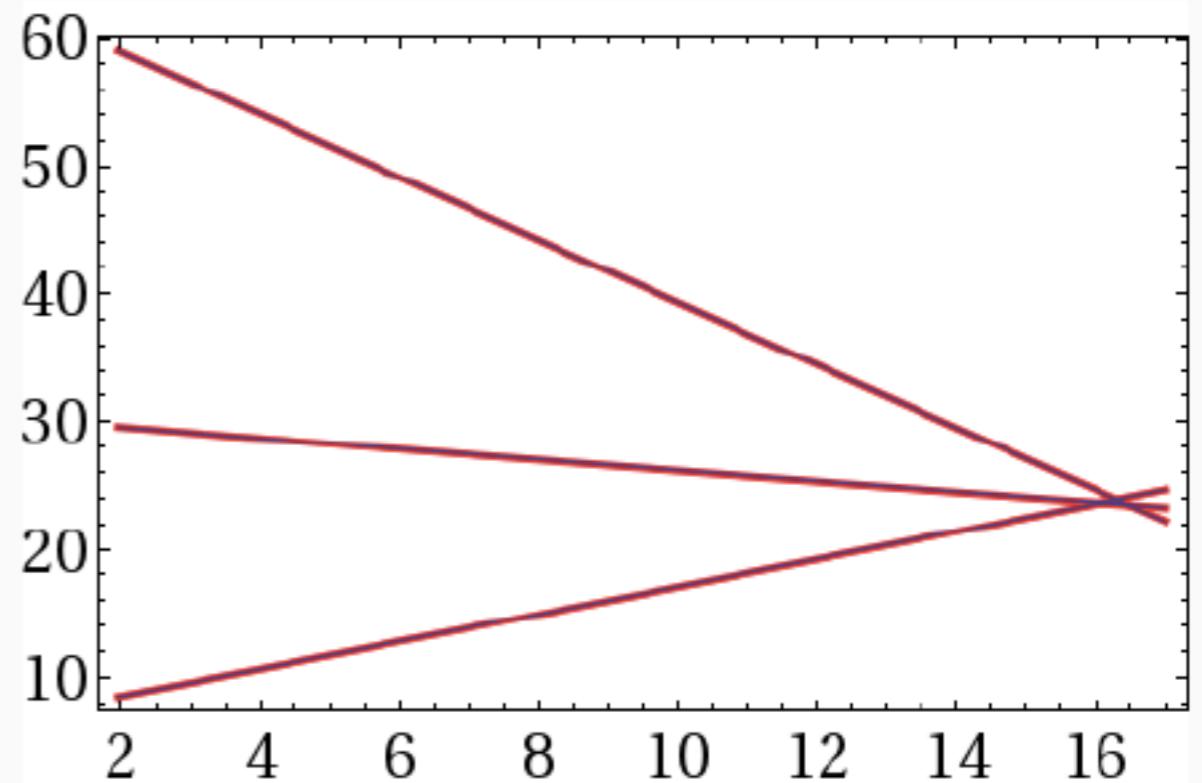
# A hint?



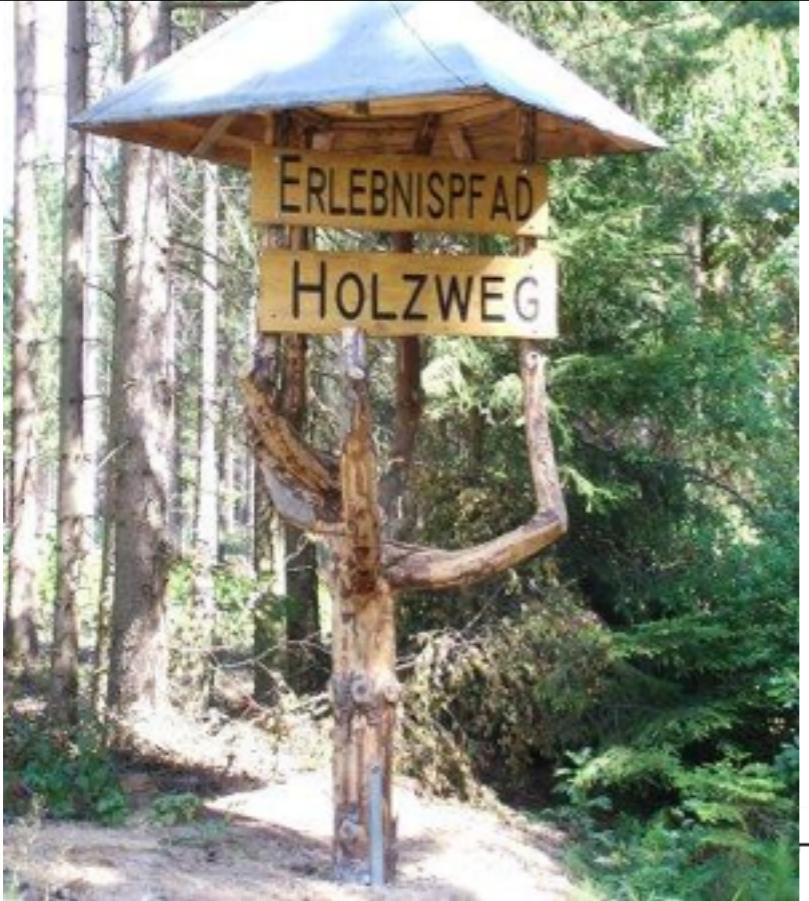
SM



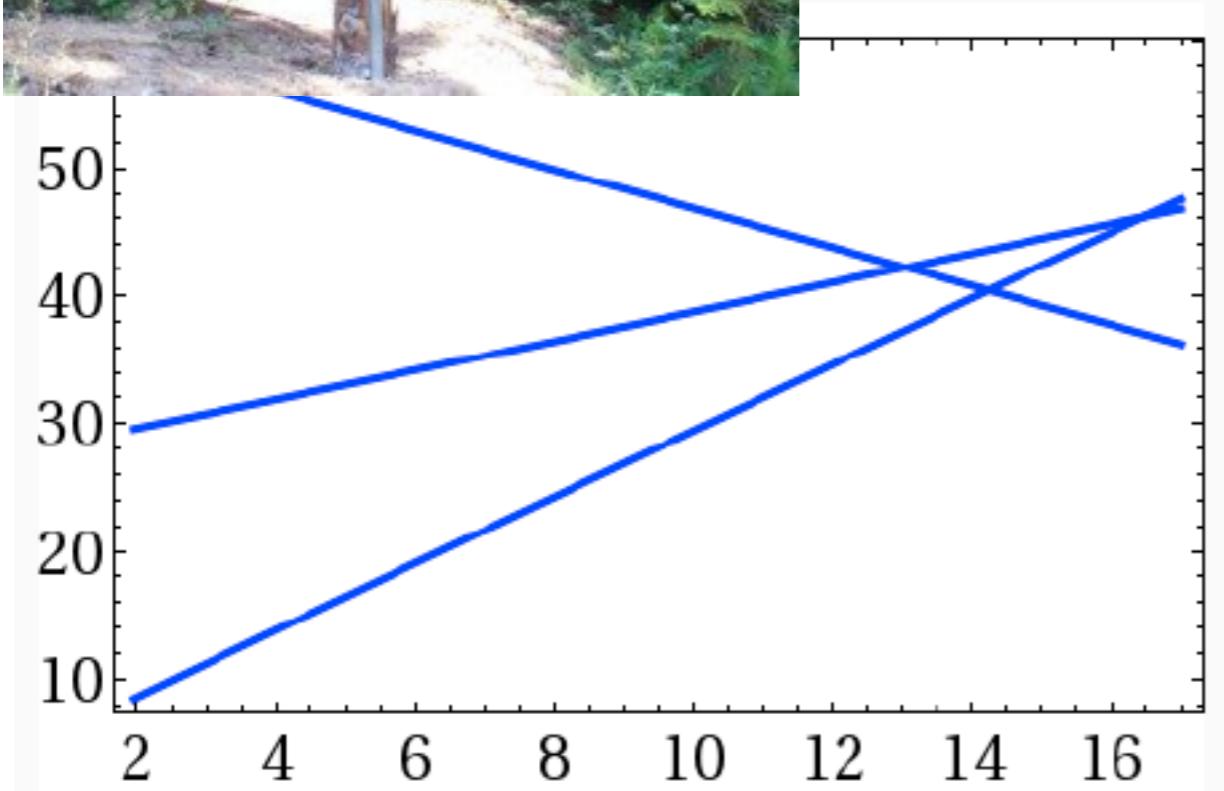
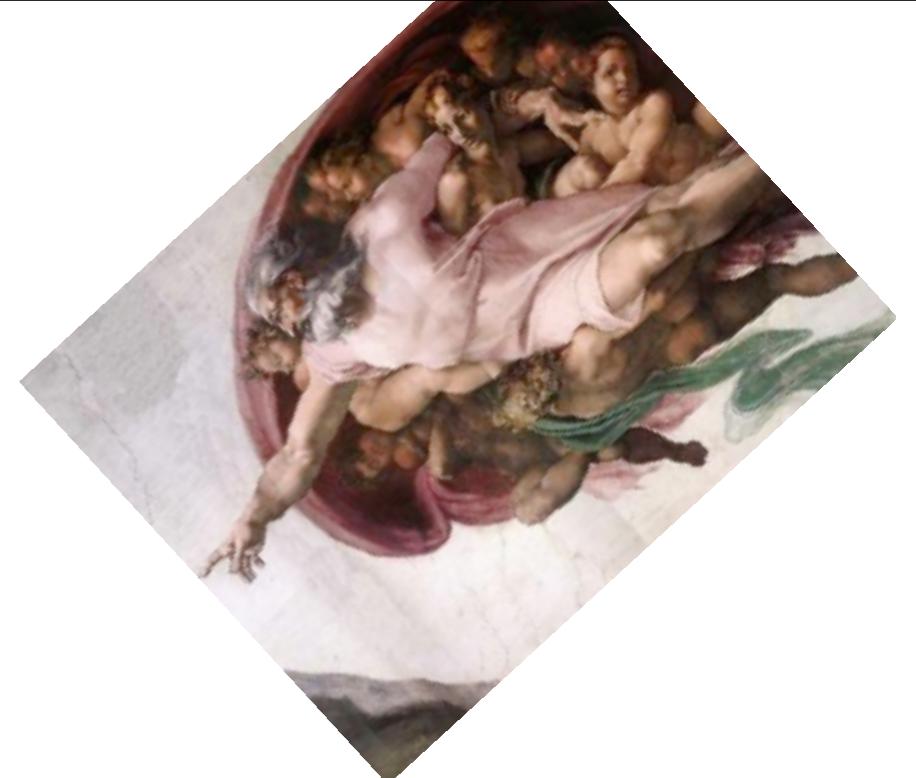
MSSM



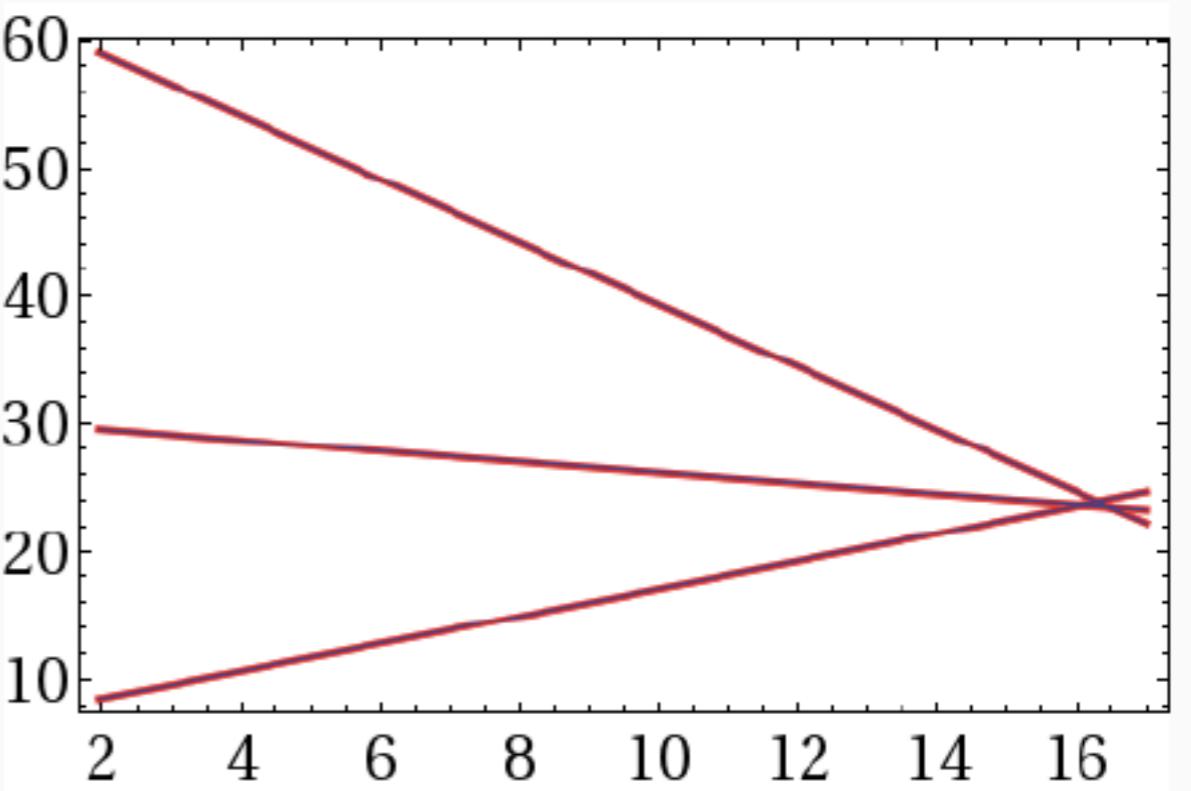
Gauge Coupling running at two loops



# A hint?

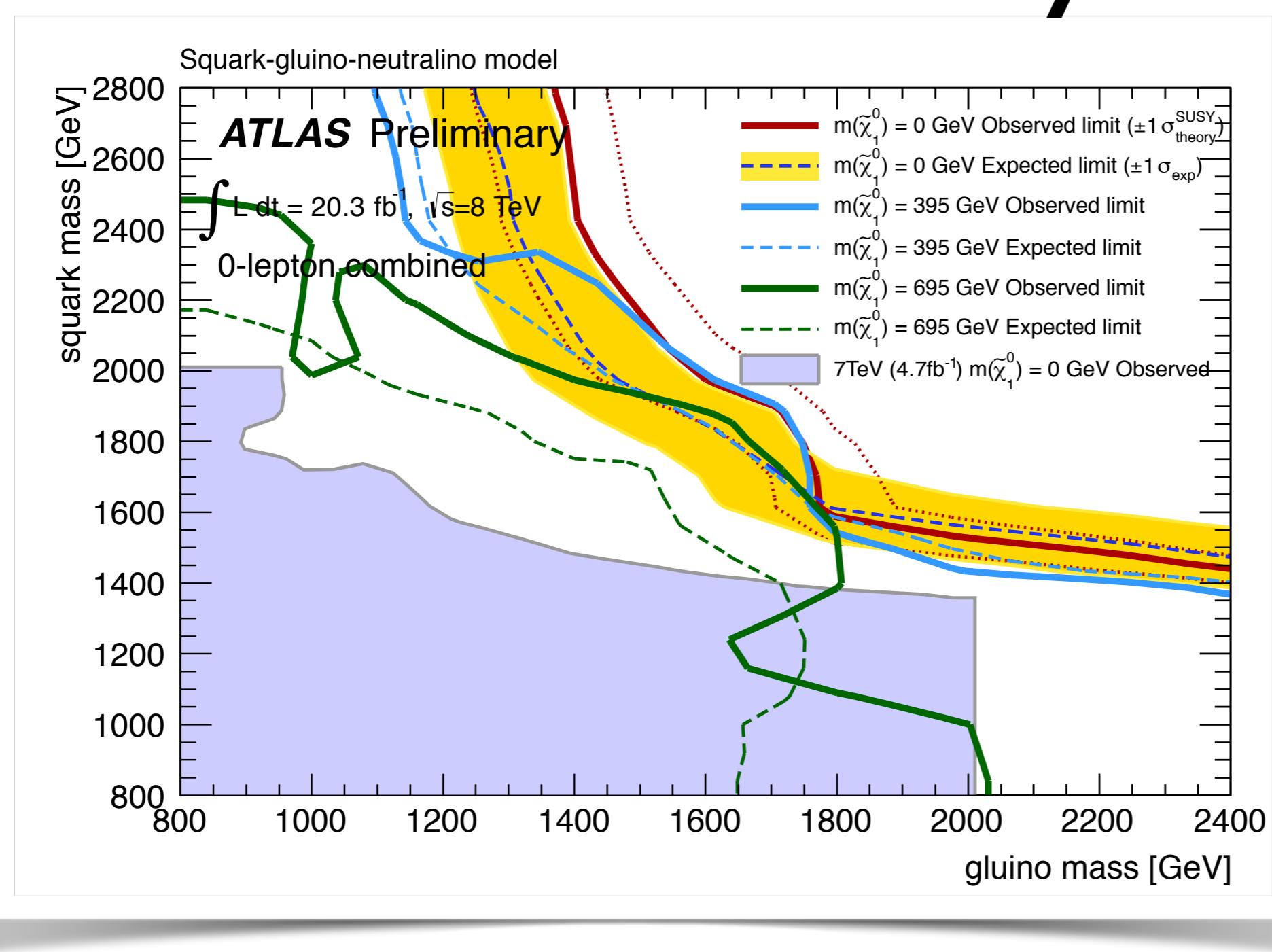


MSSM



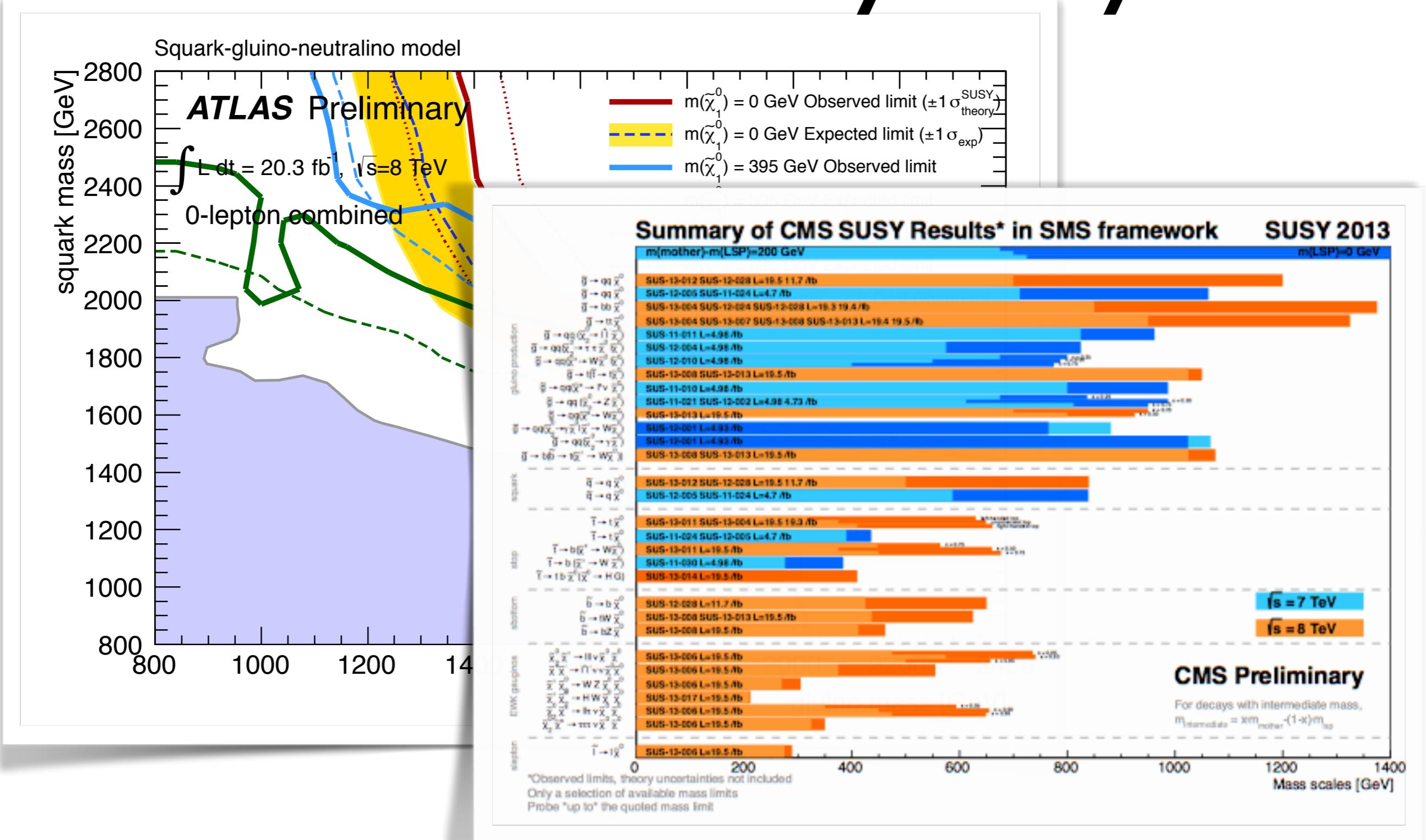
Gauge Coupling running at two loops

# Where is everybody?



Blind spots? Squeezed Spectra? R-parity Violation? Third-Generation? EW-inos?

# Where is everybody?



Blind spots? Squeezed Spectra? R-parity Violation? Third-Generation? EW-inos?

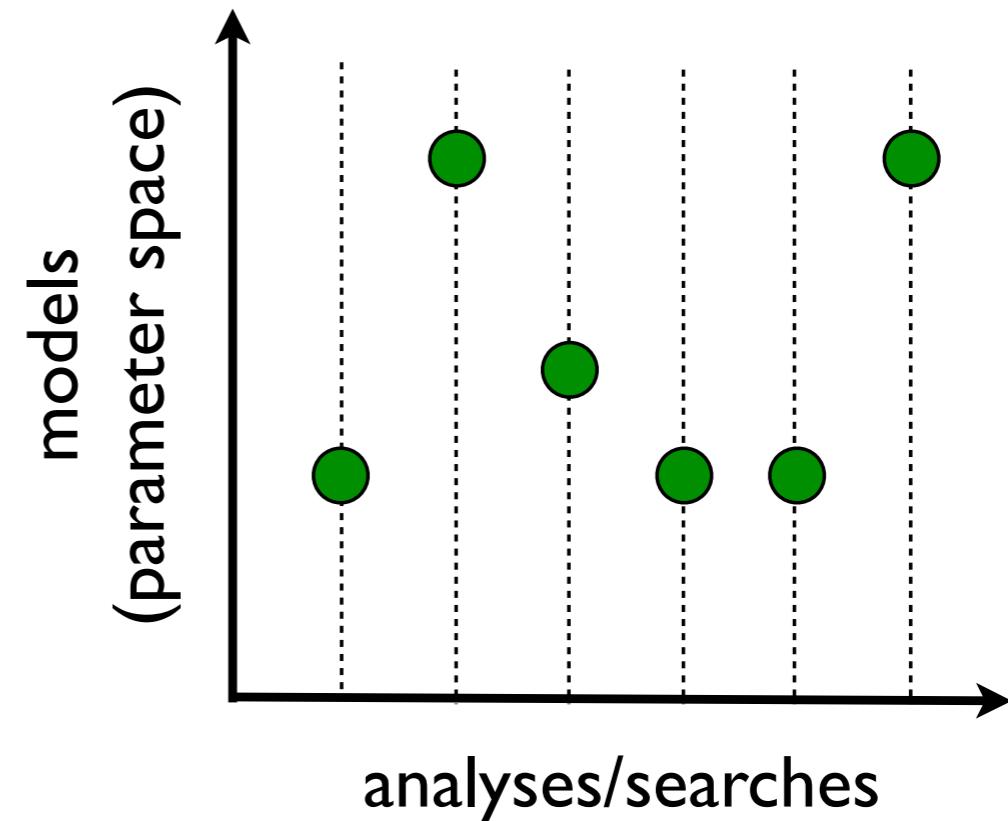
3

# What do we actually know?

ATLAS and CMS present their results only in particular slices of the parameter space of a few models.



Theorists want to constrain as many models (large parameter space) as possible using as many analyses as possible. Are we missing interesting models? Parameter points of low sensitivity?



To address this issue we have developed

**Fastlim**

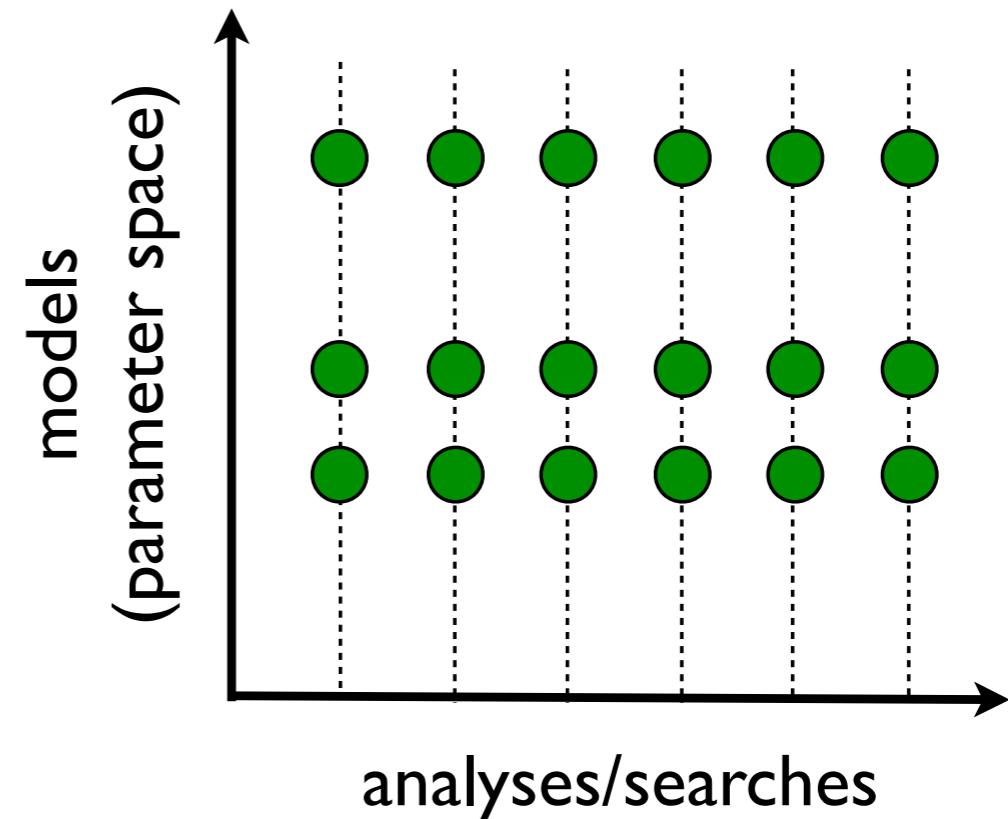
**Atom**

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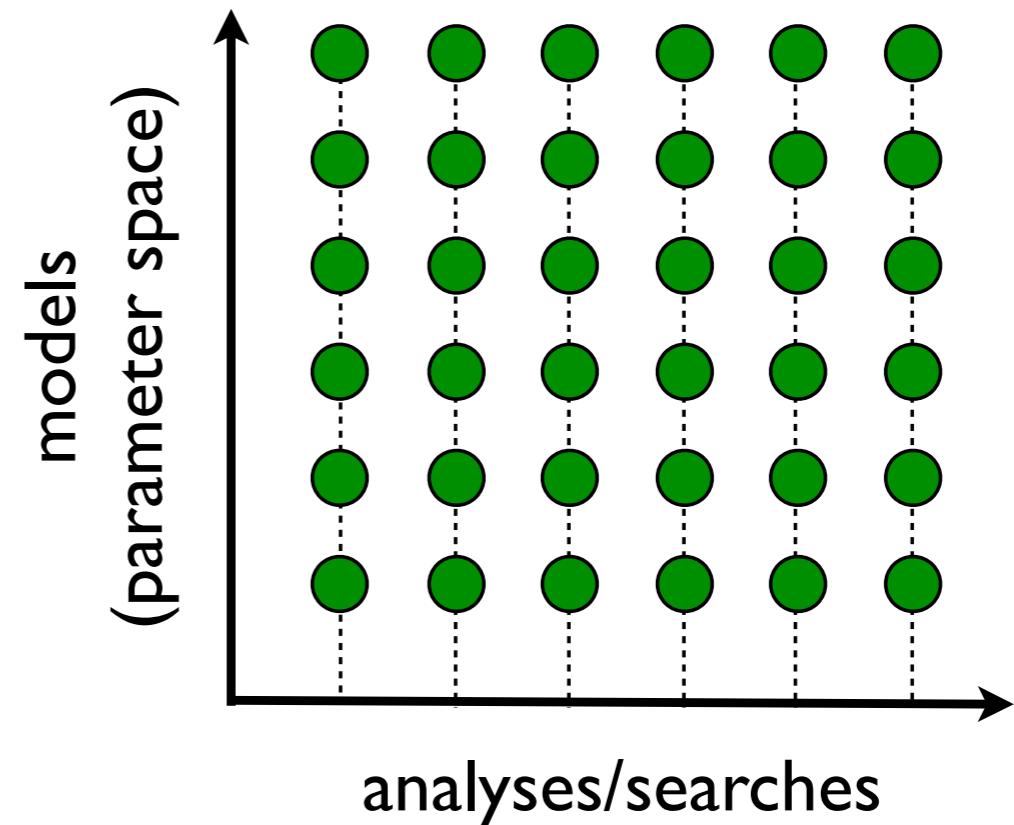
**Atom**

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Theorists want to constrain as many models (large parameter space) as possible using as many analyses as possible. Are we missing interesting models? Parameter points of low sensitivity?



To address this issue we have developed

**Fastlim**

**Atom**

# How to find the limit on your model?

Signal Regions

ATLAS-CONF-2011-086

Signal Region	$\geq 2$ jets	$\geq 3$ jets	$\geq 4$ jets
$E_T^{\text{miss}}$ [GeV]	> 130	> 130	> 130
Leading jet $p_T$ [GeV]	> 130	> 130	> 130
Second jet $p_T$ [GeV]	> 40	> 40	> 40
Third jet $p_T$ [GeV]	–	> 40	> 40
Fourth jet $p_T$ [GeV]	–	–	> 40
$\Delta\phi(\text{jet}_i, E_T^{\text{miss}})_{\min}$ ( $i = 1, 2, 3$ )	> 0.4	> 0.4	> 0.4
$E_T^{\text{miss}}/m_{\text{eff}}$	> 0.3	> 0.25	> 0.25
$m_{\text{eff}}$ [GeV]	> 1000	> 1000	> 1000

Process	Signal Region		
	$\geq 2$ jets	$\geq 3$ jets	$\geq 4$ jets
Prediction	$12.1 \pm 2.8$	$10.1 \pm 2.3$	$7.3 \pm 1.7$
Observed	10	8	7

statistically consistent

# How to evaluate $N_{\text{SUSY}}$ ?

$$N_{\text{SUSY}}^{(i)} = \epsilon_{\text{SUSY}}^{(i)} \cdot \sigma_{\text{SUSY}} \cdot \mathcal{L}_{\text{int}}$$

by Feynman diagram calc.

requires a chain of MC simulations

fixed

$$\epsilon_{\text{SUSY}}^{(i)} = \lim_{N_{\text{MC}}^{\text{gen.}} \rightarrow \infty} \frac{N_{\text{SR}}^{(i)} \left( \begin{array}{l} \text{Events fall into} \\ \text{Signal Region } (i) \end{array} \right)}{N_{\text{MC}}^{\text{gen.}}}$$

HepMC file



## AToM (Automated Testing of Models)

- “Detector simulation”: reconstruct jets, b-jet, iso-leptons, ...
- Event analyses: ATLAS and CMS searches are implemented

efficiencies of all the signal/  
control regions implemented  
together with their uncertainties

Plots

momenta of reco-objects

with Michele Papucci (Berkeley/U. Michigan),  
Kazuki Sakurai (King's College)

# Analyses

- >200 analyses have been implemented and available

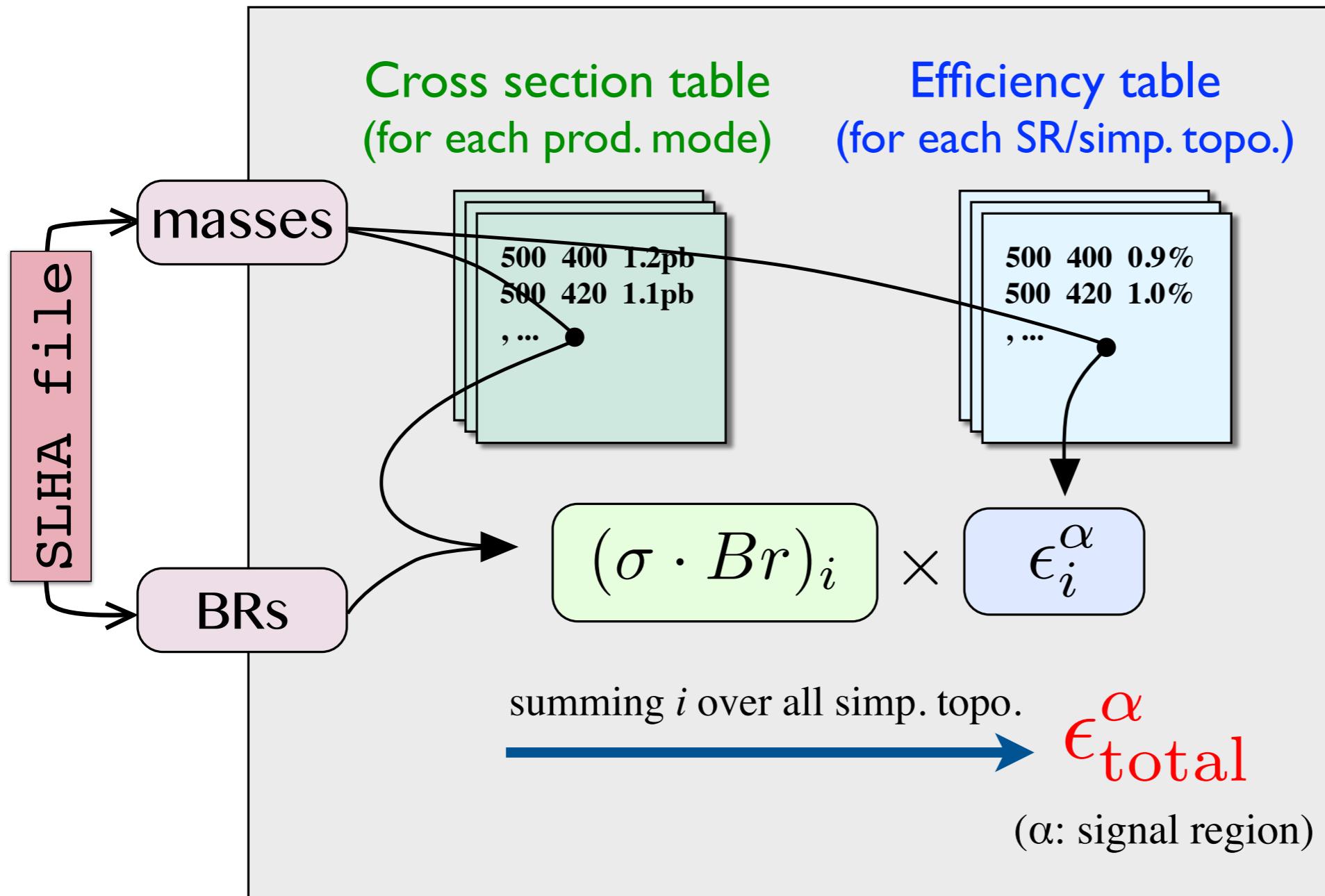
Update: all 2013 ATLAS SUSY MET analyses have been implemented

- Analyses have been validated (thanks to ATLAS's cut-flow tables)

agreements are  
(most of the times)  
as good as 90%

#	Cut Name	$\epsilon_{\text{kazuki}}$	$\epsilon_{\text{lisa}}$	$\pm$ Stat	$\epsilon_{\text{lisa}}/\epsilon_{\text{kazuki}}$	$(\epsilon_{\text{lisa}} - \epsilon_{\text{kazuki}})/\text{Stat}$
1	SRAmCT150	100.	100.	$\pm$		
2	SRAmCT200	82.21	82.18	$\pm$ 1.63	1.	-0.02
3	SRAmCT250					
4	SRAmCT300					
5	SRAmCT350	1	incHL3j_e	100.	100.	$\pm$
6	SRB	2	incHL3j_m	92.19	95.87	$\pm$ 3.83
7	[00]Leptonveto	3	incHL5j	~	~	~
8	[a1]SRAME	4	incHL5j			
9	[a2]SRApT0	5	incHL6j	1	No Cut	100.
10	[a3]SRApT0	5	incHL6j	2	01-base: njet30 >= 4	95.4
11	[a4]SRA2b-	6	incHL6j	3	01-base: $\Gamma^{T1} < \infty$	92.8
12	[a5]SRAdePm1_min>0.4					
13	[a6]SRAMET/meff2>0.25					
14	[a7]SRAmbb>200					
15	[b1]SRBMET>250					
16	[b2]SRBpT(j1,j2,j3)>150,30,					
17	[b3]SRBdelPhi_j1>2.5					
18	[b4]SRB2b-jets	12.75	11.38	4	01-base: MET > 150	88.7
19	[b5]SRBdelPhi_min>0.4	11.45	9.99	5	01-base: lepton veto	88.7
20	[b6]SRBMET/meff3>0.25	10.99	9.65	6	01-base: delphi_4min > 0.5	58.5
21	[b7]SRBHT3<50	6.95	6.33	7	01-base: MET/meff_4j > 0.2	46.2

# What does Fastlim do?



CLs for all the  
SRs implemented

interfaced with  
RooStats  
Prospino2.1

# A fast evaluation of $N_{\text{SUSY}}$

- We propose a new approach to estimate  $N_{\text{SUSY}}$

$$\begin{aligned} Q &= \tilde{q} \\ G &= \tilde{g} \\ N1 &= \tilde{\chi}_1^0 \end{aligned}$$

**Key Idea: to reconstruct  $N_{\text{SUSY}}$  using simplified model processes**

$$N_{SUSY}^{(i)} = \left\{ \begin{array}{l} N_{QqN1:QqN1} \\ + \\ N_{GqqN1:GqqN1} \\ + \\ N_{GqqN1:QqN1} \\ + \\ \vdots \end{array} \right.$$

The equation shows the reconstruction of  $N_{SUSY}$  as a sum of contributions from different model processes. The first term is  $N_{QqN1:QqN1}$ , followed by a plus sign and  $N_{GqqN1:GqqN1}$ . Below that is another plus sign and  $N_{GqqN1:QqN1}$ . At the bottom is a vertical ellipsis. To the right of the equation are four Feynman diagrams. The top-left diagram shows a quark-antiquark pair (q-bar q) interacting with a shaded circle (representing a particle exchange), which then decays into a neutralino (N1). The top-right diagram shows a similar process where the shaded circle is a gluon (G) exchange. The bottom-left diagram shows a gluon (G) exchange between the incoming quark-antiquark pair and the neutralino (N1). The bottom-right diagram shows a quark-antiquark pair (q-bar q) interacting with a shaded circle (Q), which then decays into a gluon (G) exchange, which finally leads to a neutralino (N1).

# A fast evaluation of $N_{\text{SUSY}}$

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**Key Idea: to reconstruct  $N_{\text{SUSY}}$  using simplified model processes**

$$N_{SUSY}^{(i)} = \left\{ \begin{array}{l} N_{QqN1:QqN1} = \epsilon_{QqN1:QqN1}(mQ, mN1) \cdot \sigma_{QQ} \cdot BR_{QqN1:QqN1} \cdot L_{\text{int}} \\ + \\ N_{GqqN1:GqqN1} = \epsilon_{GqqN1:GqqN1}(mG, mN1) \cdot \sigma_{GG} \cdot BR_{GqqN1:GqqN1} \cdot L_{\text{int}} \\ + \\ N_{GqqN1:QqN1} = \epsilon_{GqqN1:QqN1}(mQ, mG, mN1) \cdot \sigma_{GQ} \cdot BR_{GqqN1:QqN1} \cdot L_{\text{int}} \\ + \\ \vdots \end{array} \right.$$

# A fast evaluation of NsusY

$$\begin{aligned} Q &= \tilde{q} \\ G &= \tilde{g} \\ N1 &= \tilde{\chi}_1^0 \end{aligned}$$

Efficiencies for simplified processes  
depend only on a few mass parameters

$$N_{SUSY}^{(i)} = \left\{ \begin{array}{l} N_{QqN1:QqN1} = \epsilon_{QqN1:QqN1}(mQ, mN1) \cdot \sigma_{QQ} \cdot BR_{QqN1:QqN1} \cdot L_{int} \\ + \\ N_{GqqN1:GqqN1} = \epsilon_{GqqN1:GqqN1}(mG, mN1) \cdot \sigma_{GG} \cdot BR_{GqqN1:GqqN1} \cdot L_{int} \\ + \\ N_{GqqN1:QqN1} = \epsilon_{GqqN1:QqN1}(mQ, mG, mN1) \cdot \sigma_{GQ} \cdot BR_{GqqN1:QqN1} \cdot L_{int} \\ + \\ \vdots \end{array} \right.$$

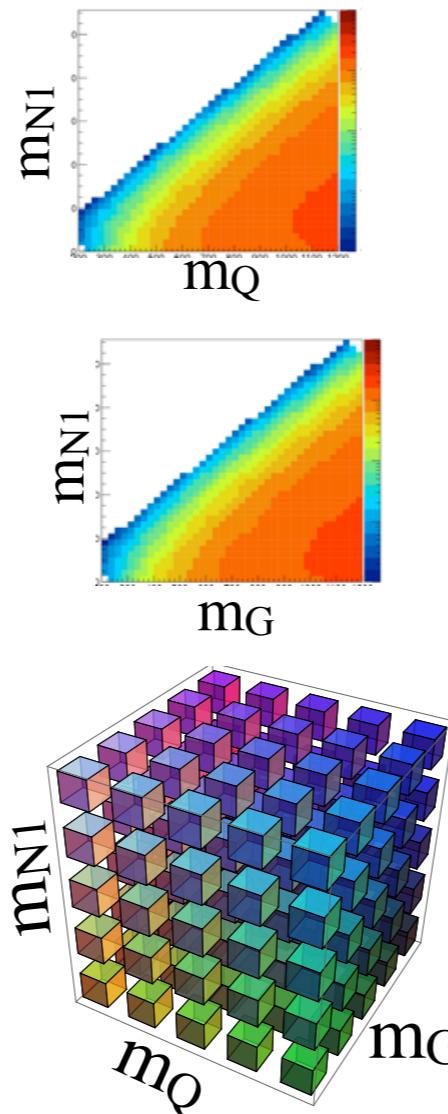
# A fast evaluation of NsusY

- Once one has the efficiency tables for the simplified model processes, one can read off the efficiencies and re-assemble NsusY of your model.

$$\begin{aligned} Q &= \tilde{q} \\ G &= \tilde{g} \\ N1 &= \tilde{\chi}_1^0 \end{aligned}$$

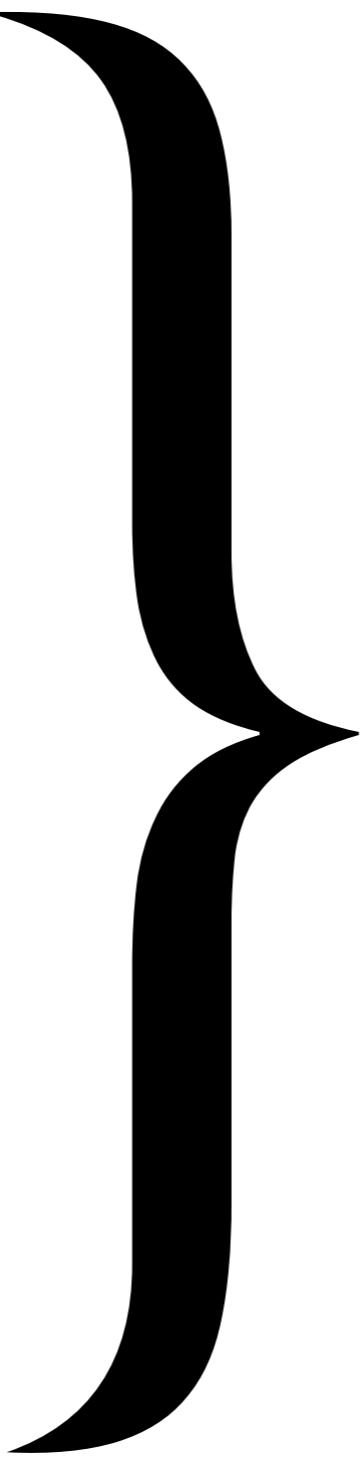
no MC simulation is required !

$$N_{SUSY}^{(i)} = \left\{ \begin{array}{l} N_{QqN1:QqN1} = \\ + \\ N_{GqqN1:GqqN1} = \\ + \\ N_{GqqN1:QqN1} = \\ + \\ \vdots \end{array} \right.$$



- $\sigma_{QQ} \cdot BR_{QqN1:QqN1} \cdot L_{int}$
- $\sigma_{GG} \cdot BR_{GqqN1:GqqN1} \cdot L_{int}$
- $\sigma_{GQ} \cdot BR_{GqqN1:QqN1} \cdot L_{int}$

- If you are interested in testing it, contact Kazuki Sakurai or me



# Natural EWSB & SUSY

Fine-tuning of (Higgs mass)<sup>2</sup>

$$\frac{m_{Higgs}^2}{2} = -|\mu|^2 + \dots + \delta m_H^2$$

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Higgsinos

# Natural EWSB & SUSY

Fine-tuning of (Higgs mass)<sup>2</sup>

$$\frac{m_{Higgs}^2}{2} = -|\mu|^2 + \dots + \delta m_H^2$$

Higgsinos

1loop

$$\delta m_H^2|_{stop} = -\frac{3}{8\pi^2} y_t^2 \left( \underline{m_{U_3}^2 + m_{Q_3}^2 + |A_t|^2} \right) \log \left( \frac{\Lambda}{\text{TeV}} \right)$$

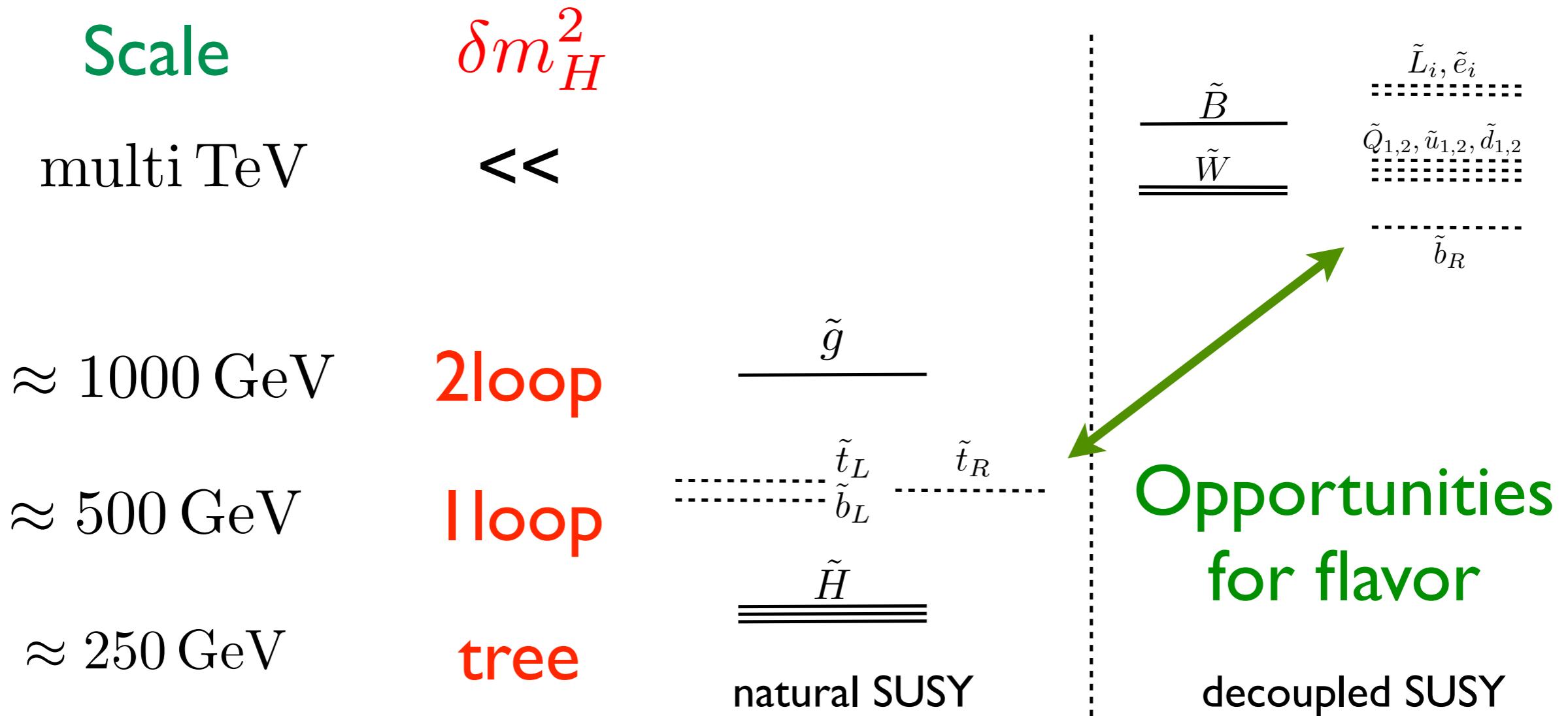
stops, sbottom<sub>L</sub>

2loop

$$\delta m_H^2|_{gluino} = -\frac{2}{\pi^2} y_t^2 \left( \frac{\alpha_s}{\pi} \right) \underline{|M_3|^2} \log^2 \left( \frac{\Lambda}{\text{TeV}} \right)$$

gluino

# Reason for optimism: natural susy



# Splitting via RGE?

Papucci, Ruderman, AW

Splitting via renormalization group does not help

$$\delta m_H^2 \simeq 3(m_{Q_3}^2 - m_{Q_{1,2}}^2) \simeq \frac{3}{2}(m_{U_3}^2 - m_{U_{1,2}}^2)$$

I-loop, LLog,  
 $\tan\beta$  moderate

Higgs fine-tuning = RGE mass splitting

# Splitting via RGE?

Papucci, Ruderman, AW

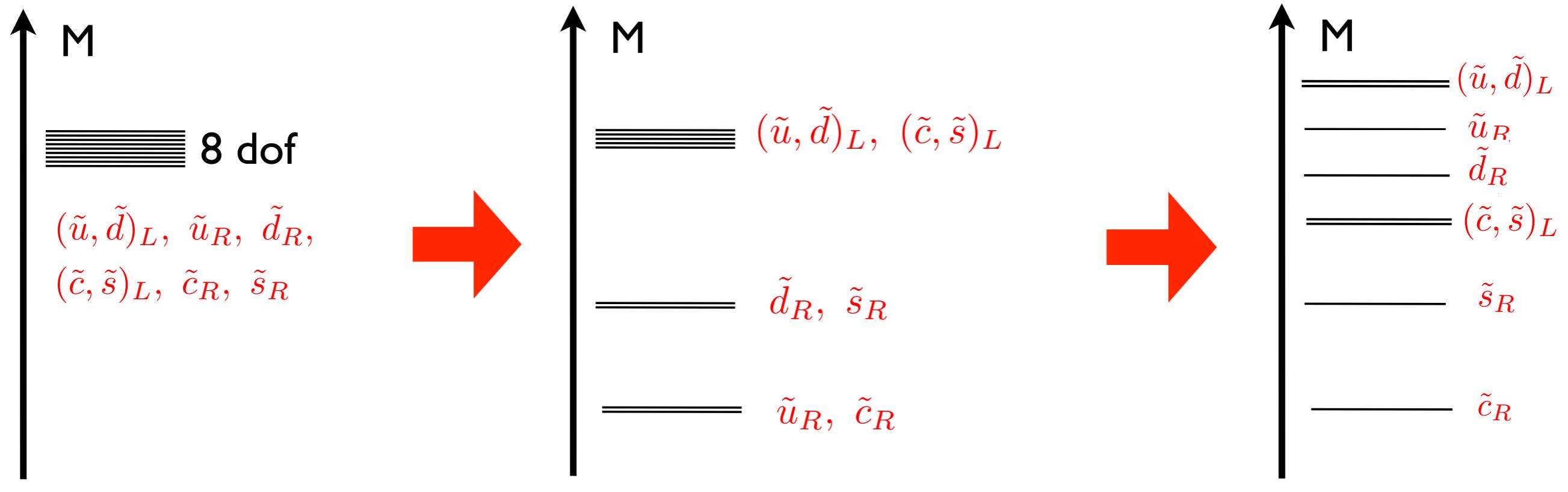
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I-loop, LLog,  
 $\tan\beta$  moderate

Higgs fine-tuning = RGE mass splitting

→ Flavor non-trivial susy breaking!

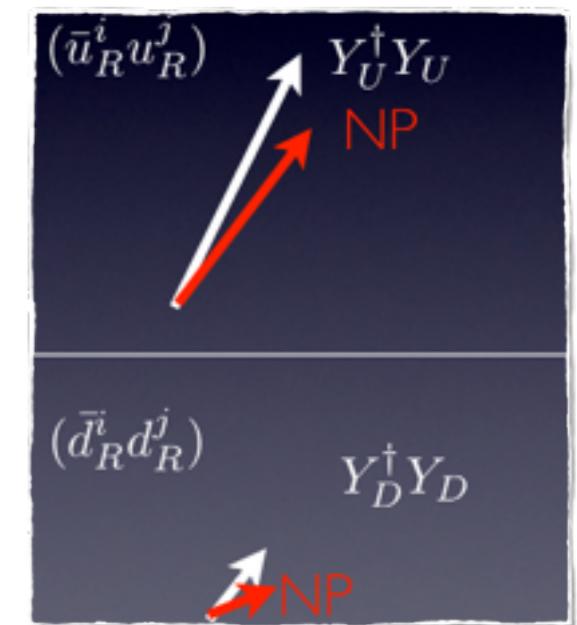


Degenerate

mSugra, CMSSM,  
pMSSM, ...

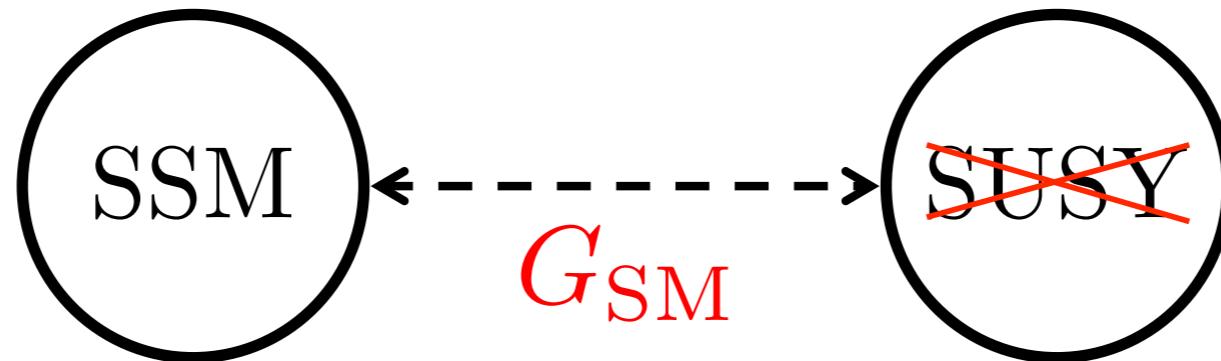
Minimal Flavor

Anarchy!



# Gauge Mediation

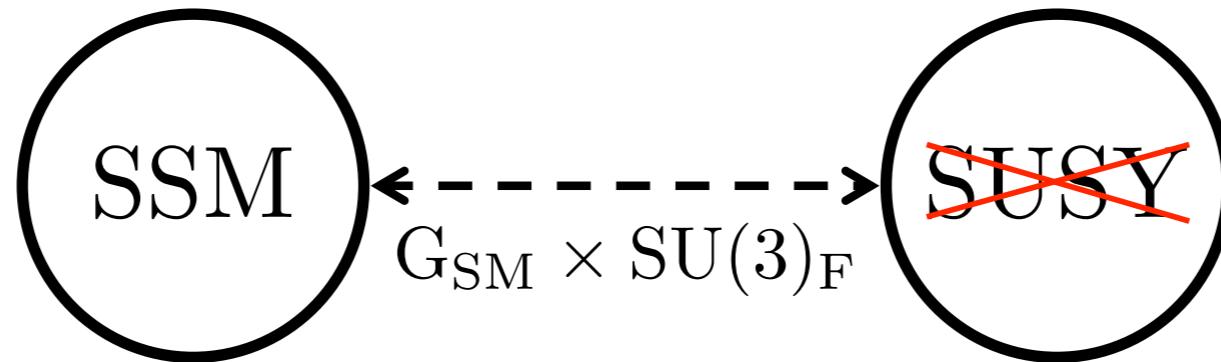
see e.g. Giudice/Rattazzi



$$G_{\text{SM}} = SU(3) \times SU(2) \times U(1)$$

# Flavor Gauge Mediation

U(I): Kaplan, Kribs '99; Craig, McCullough, Thaler '12;  
Brümmer, McGarrie, AW



- o Gauge flavor group  $SU(3)_F$  \*
- o Break flavor and susy simultaneously, e.g.
  - \* Diagonal, anomaly-free subgroup of SM w/o Yukawas  
 $SU(3)_{Q_L} \times SU(3)_{u_R} \times SU(3)_{d_R}$

$$\Sigma,\;\Sigma'\quad\text{in}\quad \bar{\bf 6} \text{ of } {\rm SU}(3)_{\rm F}$$

$$W=\frac{\Sigma}{\Lambda}H_uQU+\frac{\Sigma'}{\Lambda}H_dQD$$

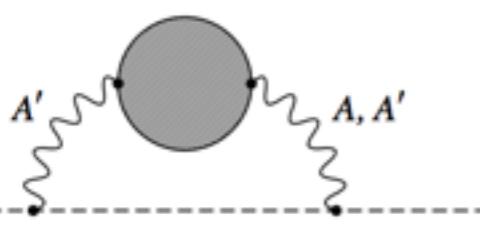
$$\langle\Sigma\rangle/\Lambda=Y_u\qquad\qquad\langle X\rangle=(0,\,0,\,F_X\theta^2)^T$$

$$=> \qquad \delta m_{Q_I}^2 = -\frac{g_{\rm F}^2}{16\pi^2}\frac{|F_X|^2}{|\Sigma_{33}|^2}\left(\begin{array}{ccc} \frac{13}{24} & 0 & 0 \\ 0 & \frac{13}{24} & 0 \\ 0 & 0 & \frac{7}{6} \end{array}\right)$$

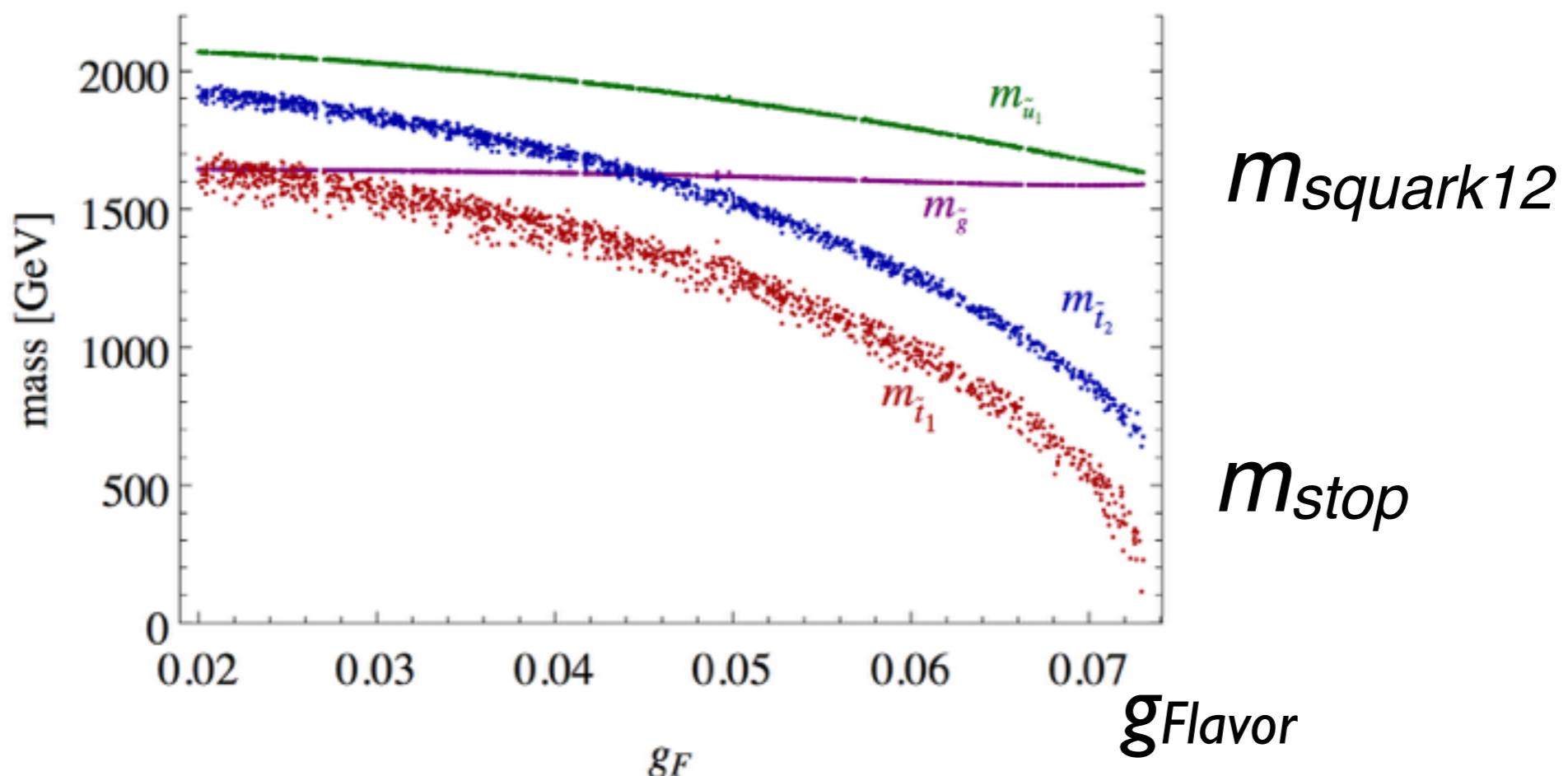
# Natural Split spectrum

Brümmer, McGarrie, Weiler

Tachyonic contribution from gauge messengers



$$\delta m_{Q,U,D}^2 = -\frac{g_F^2}{16\pi^2} \frac{F^2}{M^2} \left[ \begin{pmatrix} \frac{7}{6} & 0 & 0 \\ 0 & \frac{7}{6} & 0 \\ 0 & 0 & \frac{8}{3} \end{pmatrix} + \mathcal{O}(\epsilon^2) \right]$$

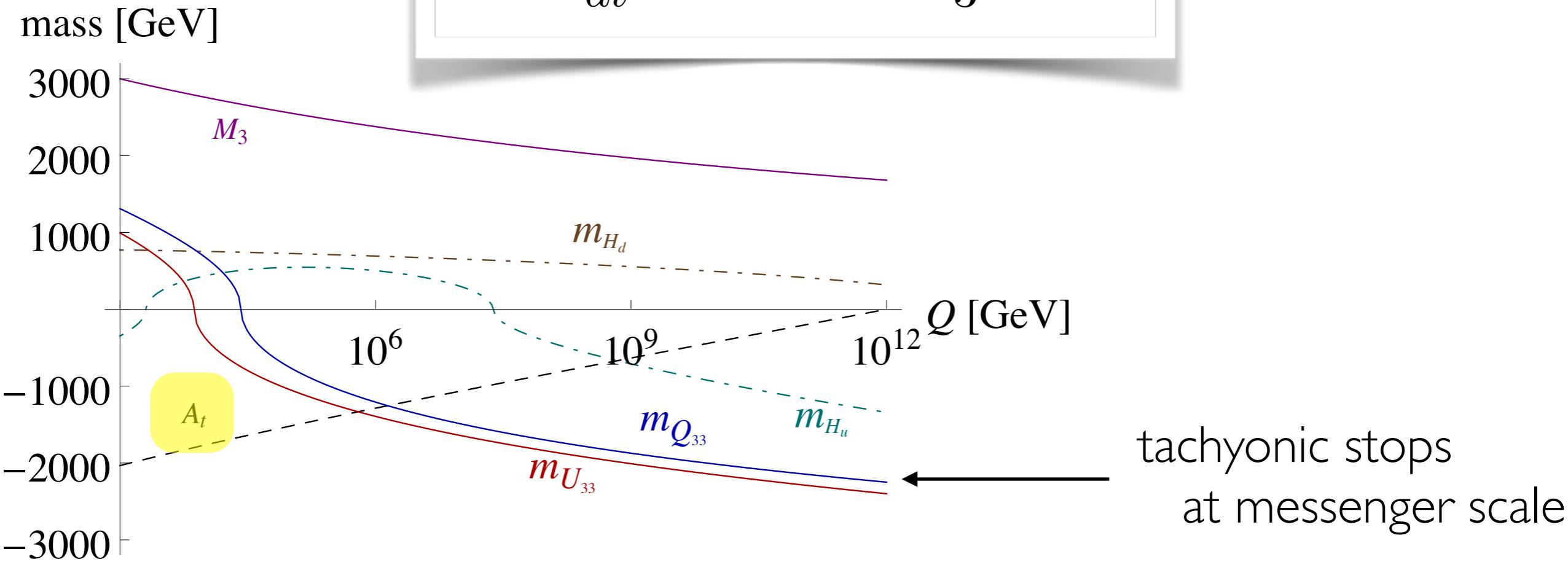


# A-terms through RGE

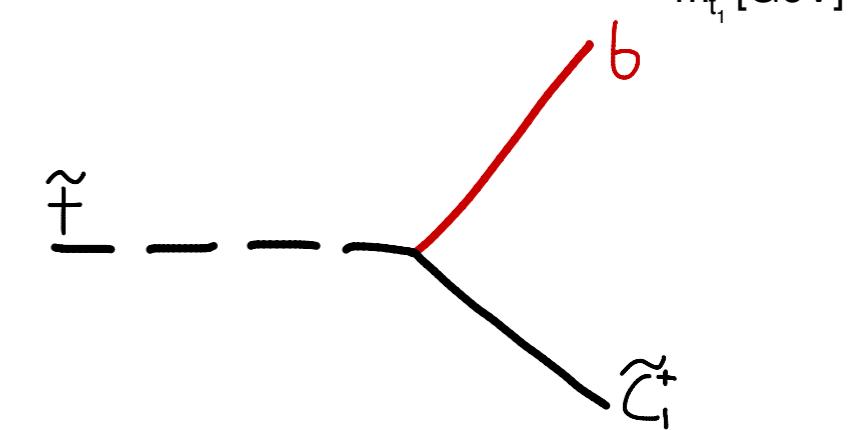
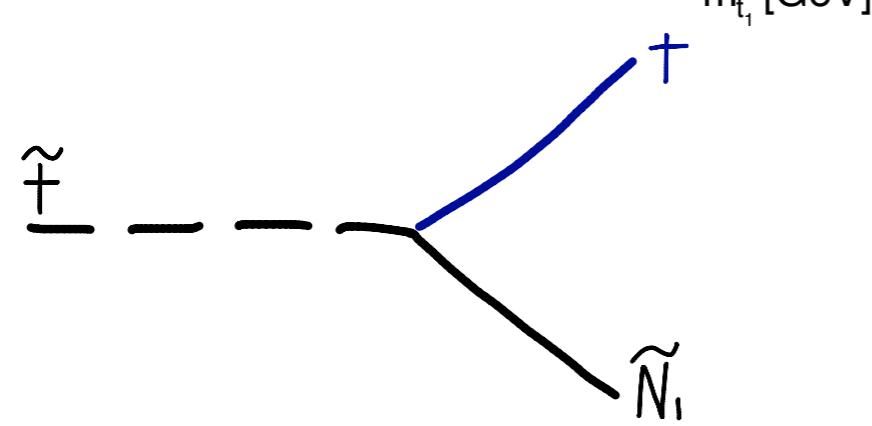
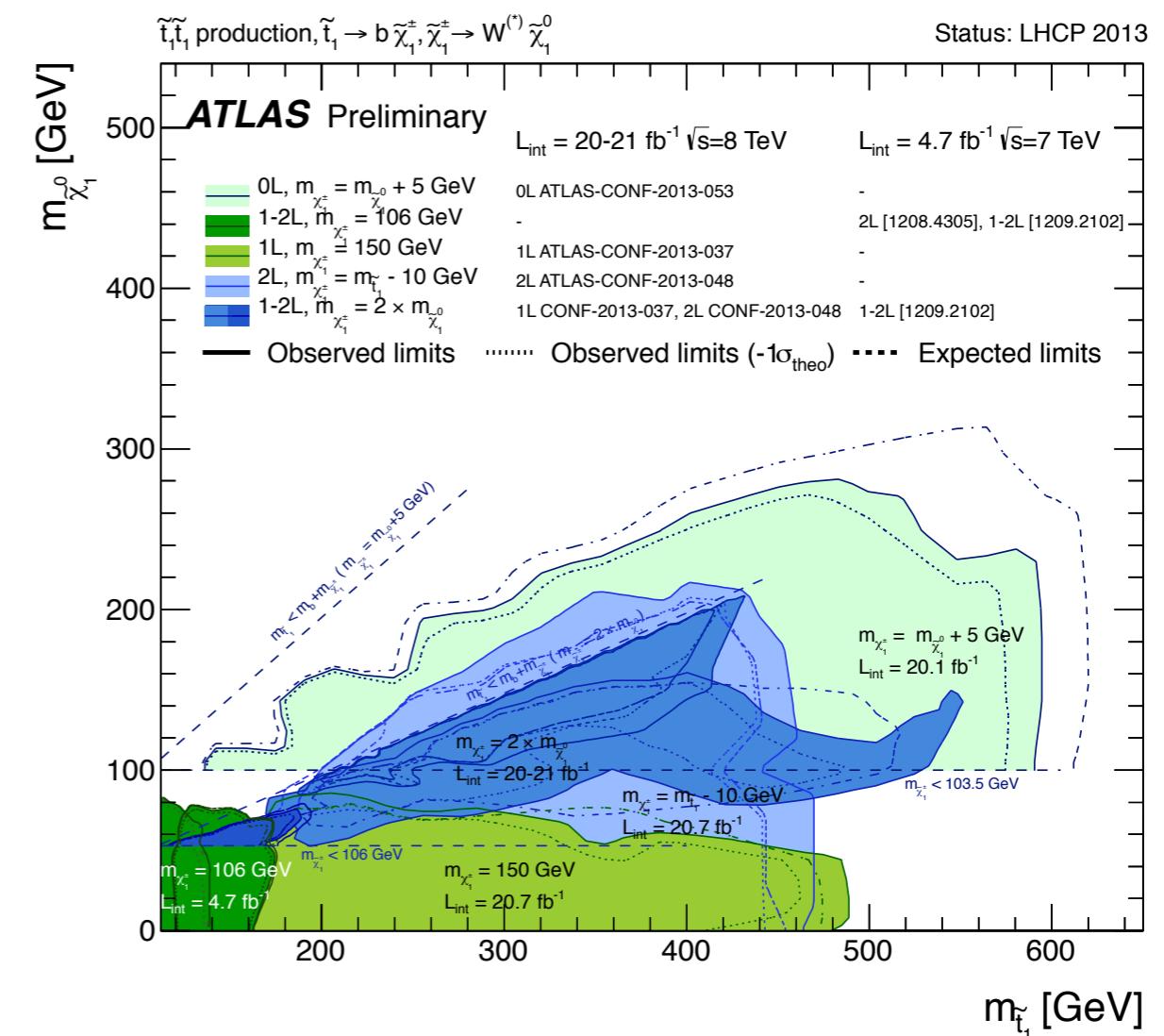
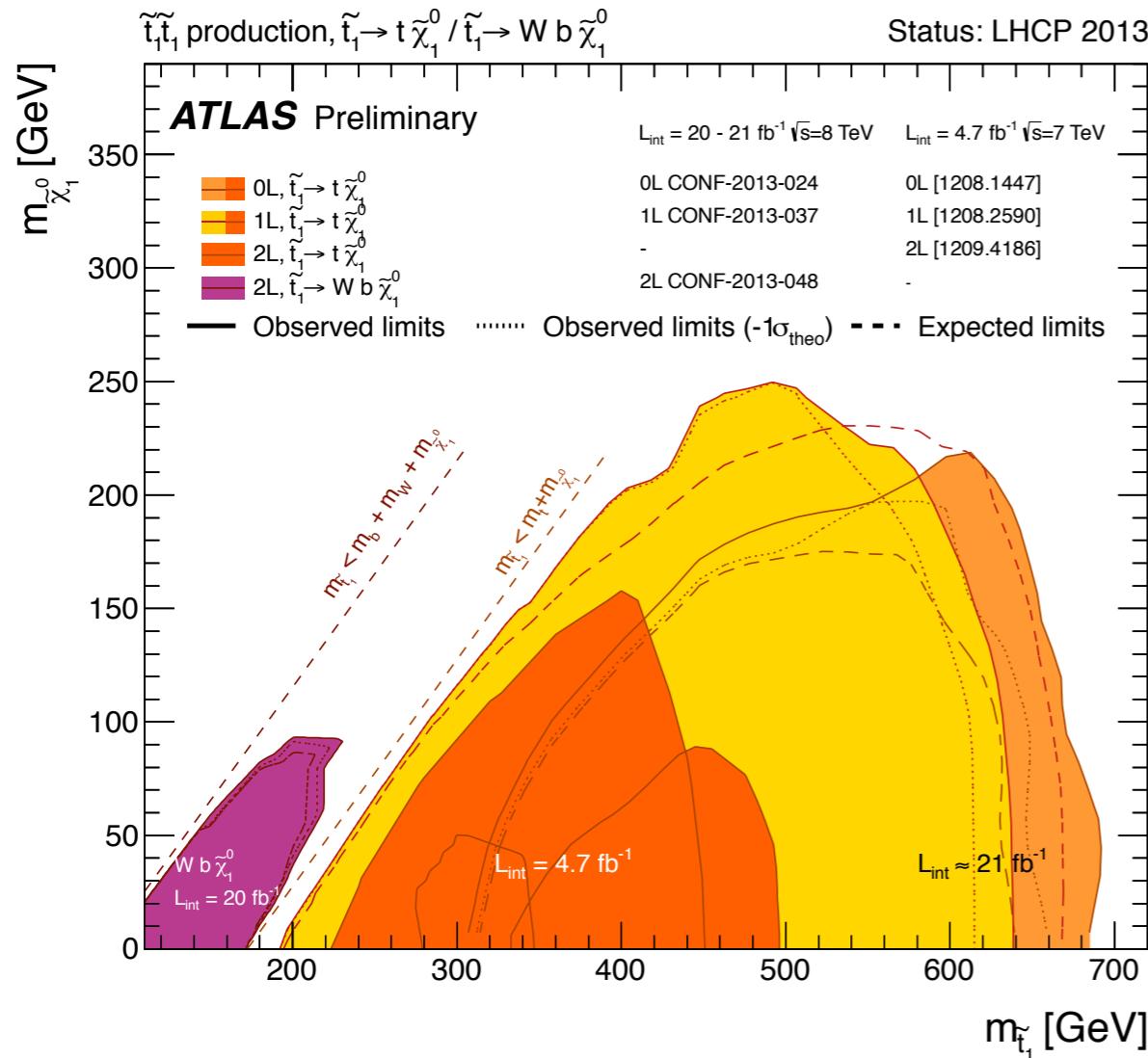
see e.g. Shih et al

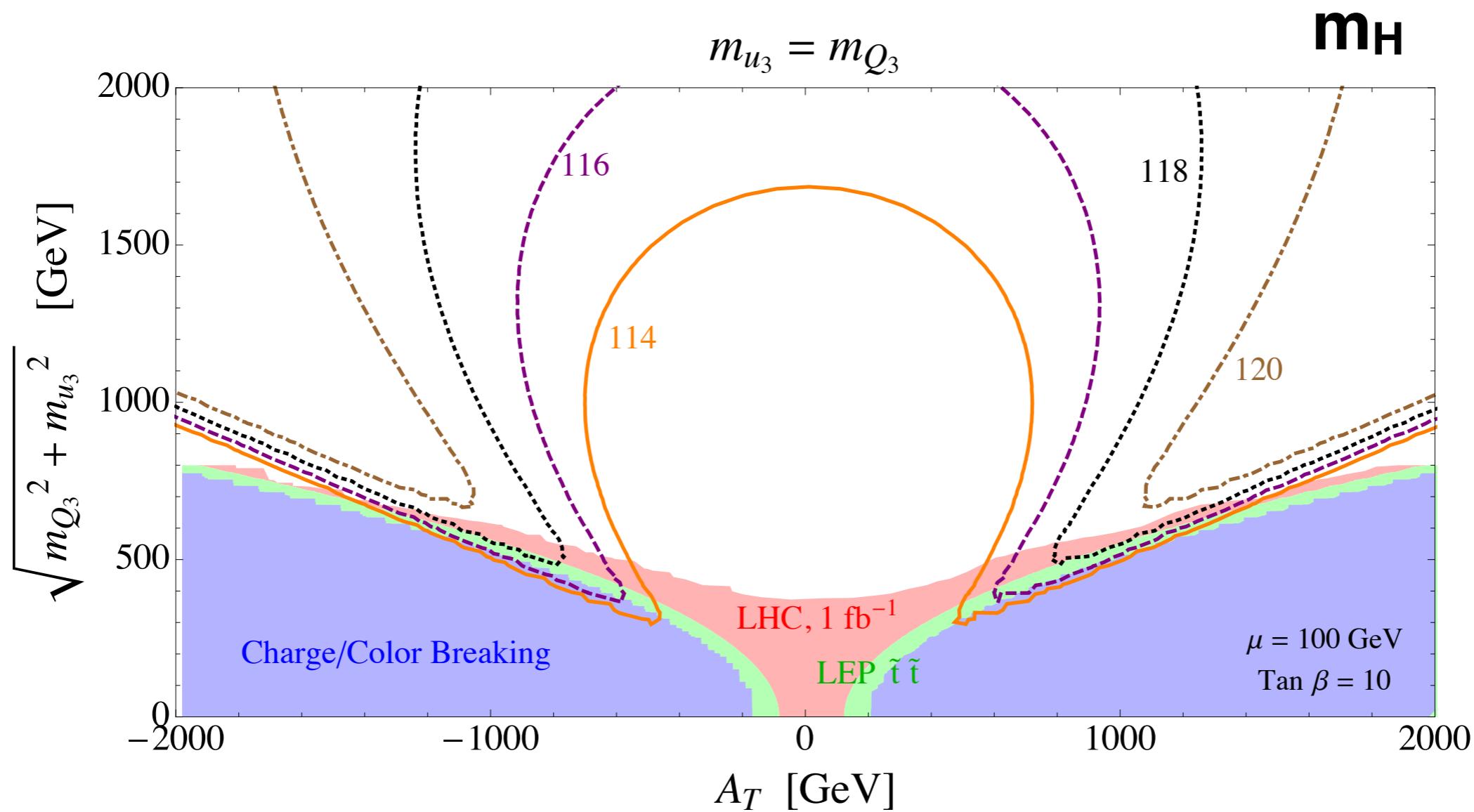
$$m_h^2 = m_Z^2 c_{2\beta}^2$$
$$+ \frac{3m_t^4}{4\pi^2 v^2} \left( \log \left( \frac{M_S^2}{m_t^2} \right) + \frac{X_t^2}{M_S^2} \left( 1 - \frac{X_t^2}{12M_S^2} \right) \right)$$

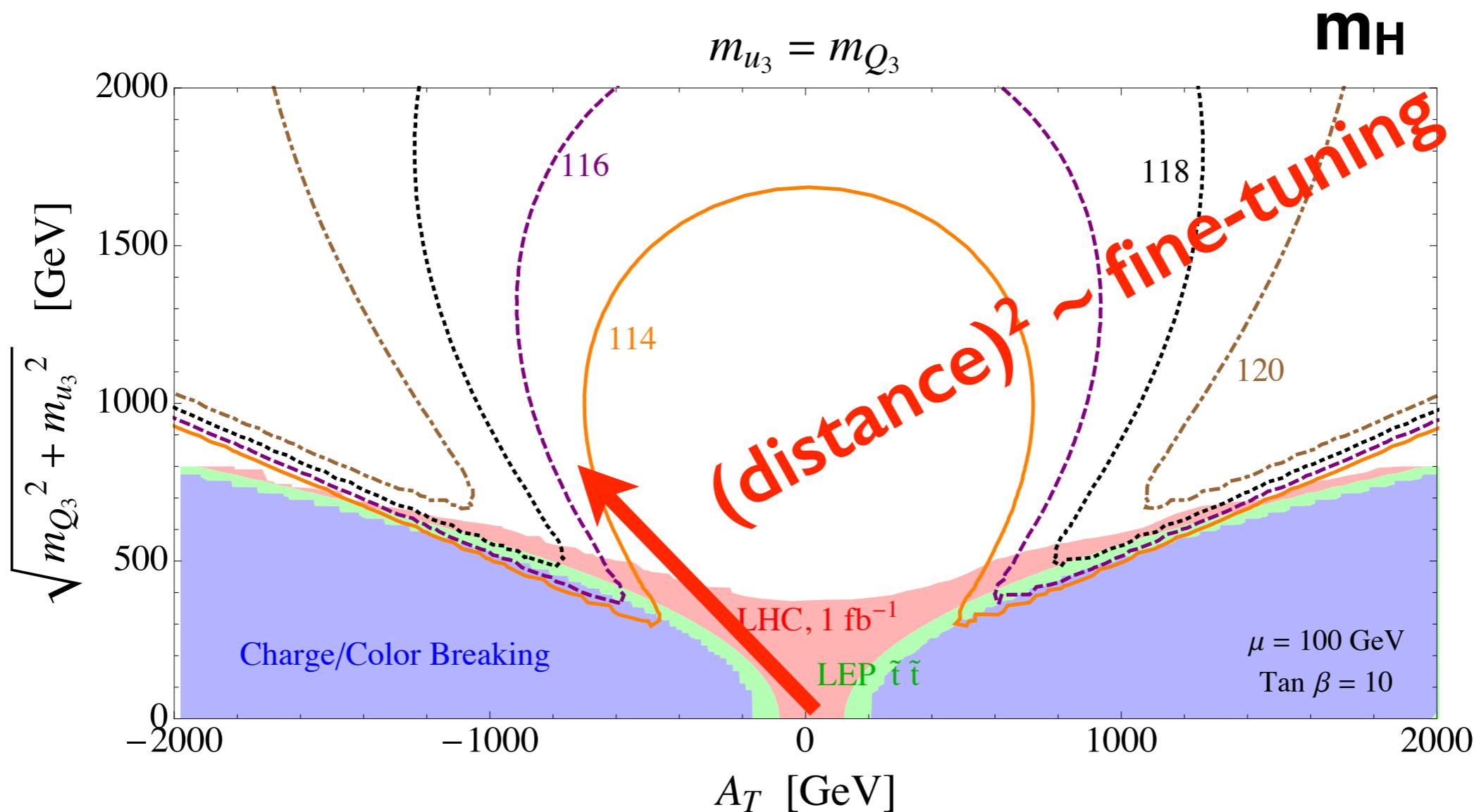
$$16\pi^2 \frac{dA_t}{dt} \approx 12y_t^2 A_t + \frac{32}{3} g_3^2 M_3$$



# stop limits



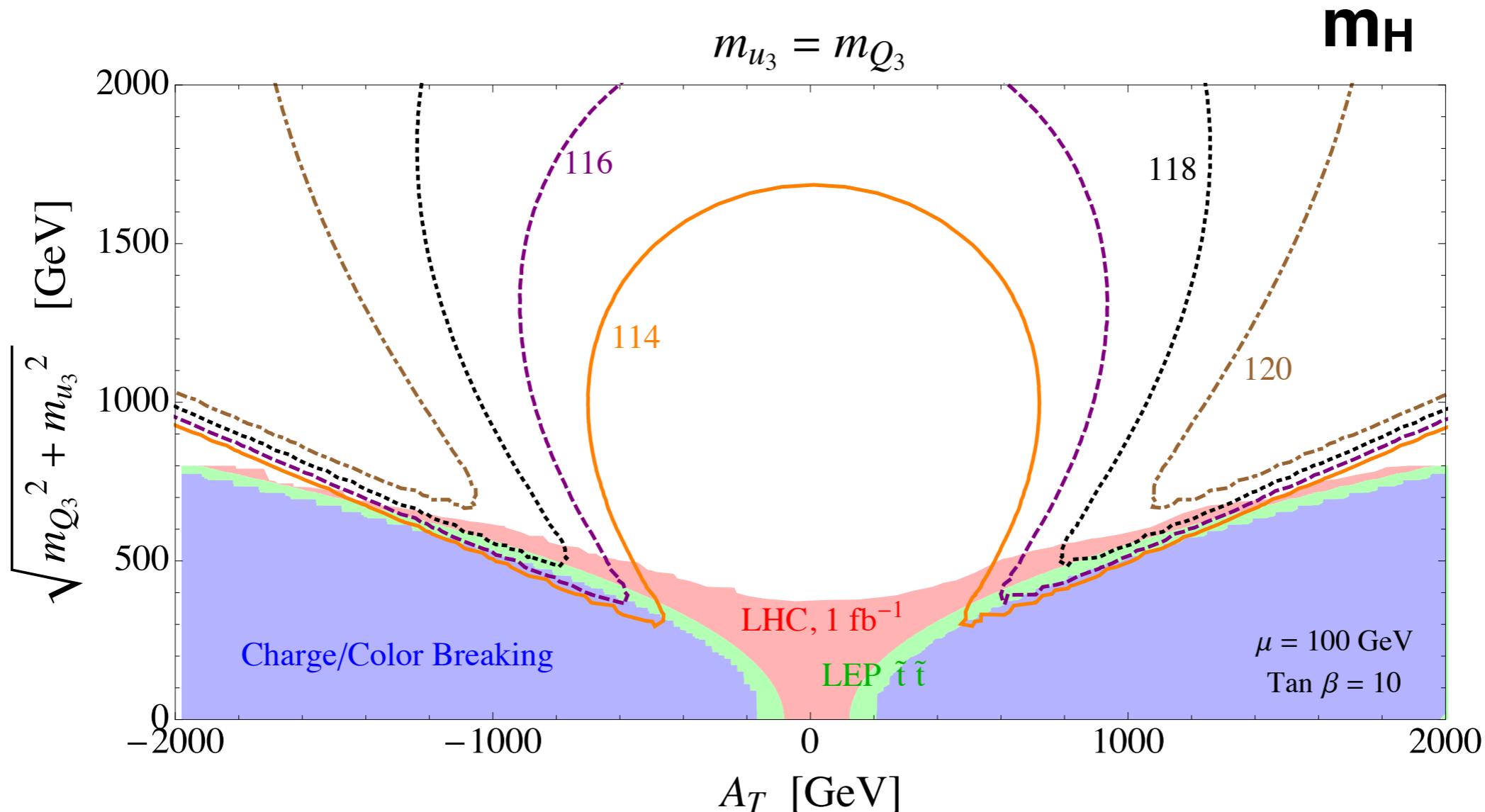




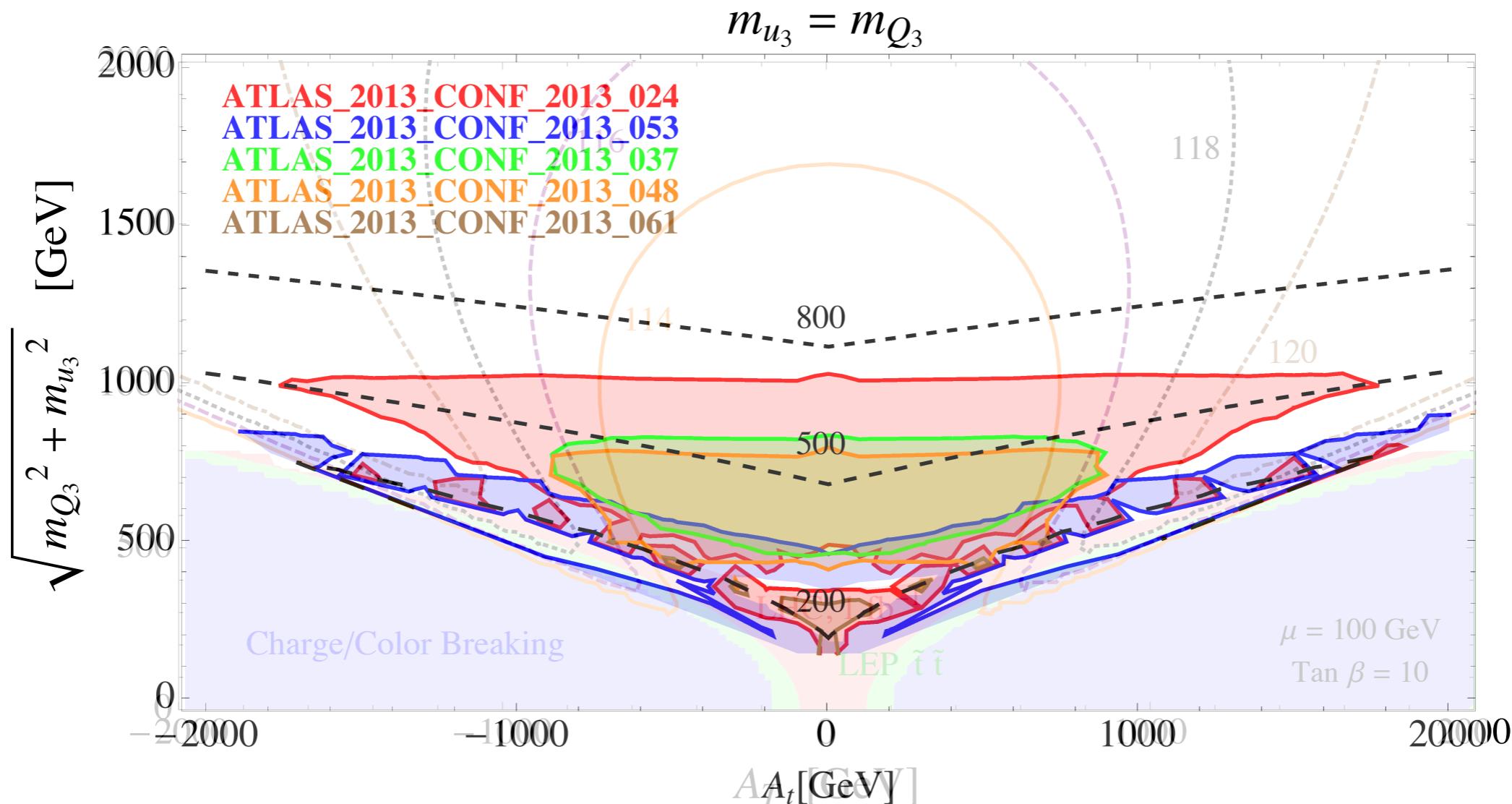
$$\delta m_H^2|_{stop} = -\frac{3}{8\pi^2} y_t^2 \left( m_{U_3}^2 + m_{Q_3}^2 + |A_t|^2 \right) \log \left( \frac{\Lambda}{\text{TeV}} \right)$$

# 1 $\text{fb}^{-1}$ 7 TeV Limits

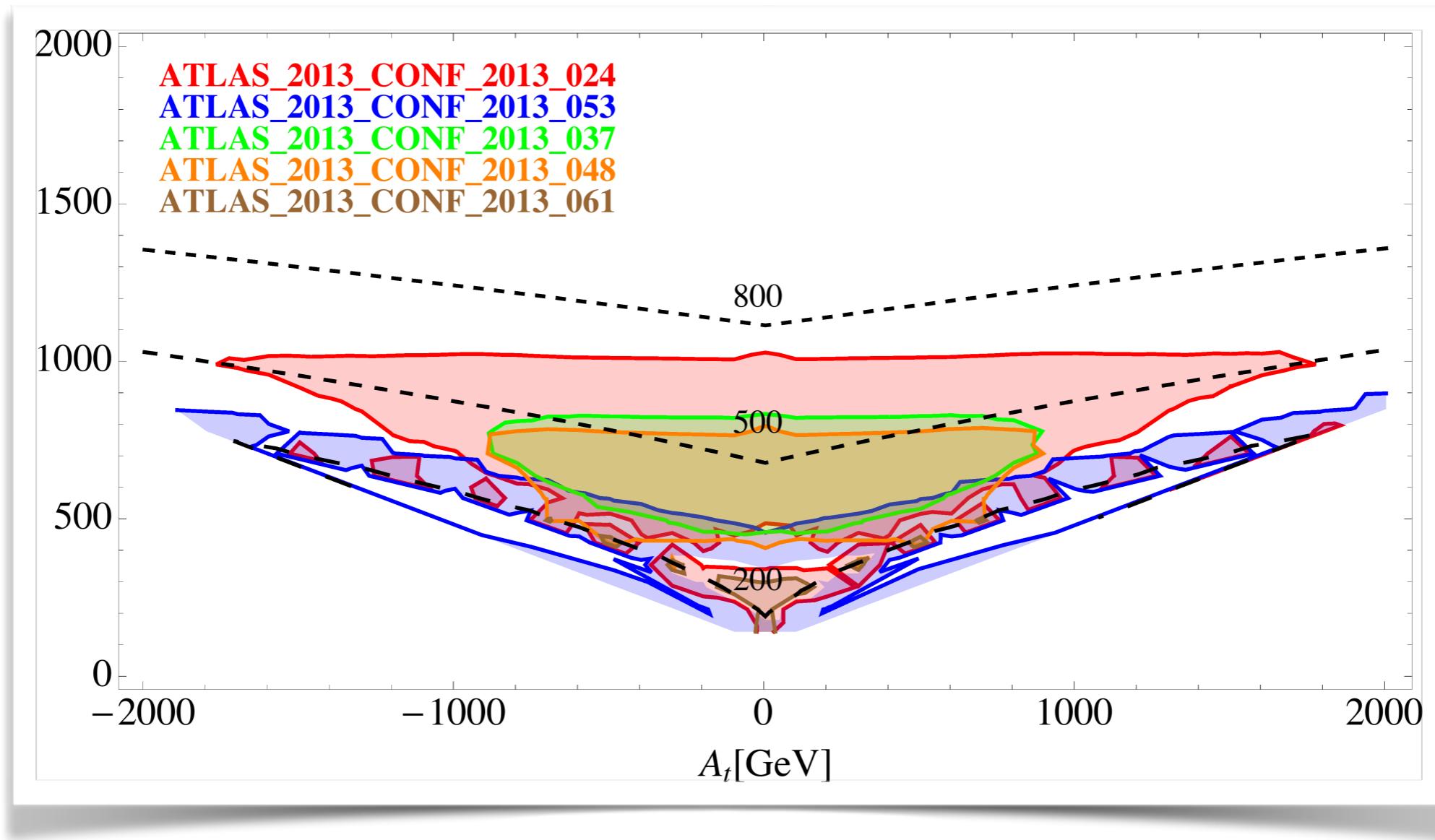
Papucci, Rudermann, AW



# 20 fb<sup>-1</sup> 8 TeV Limits (fastlim)



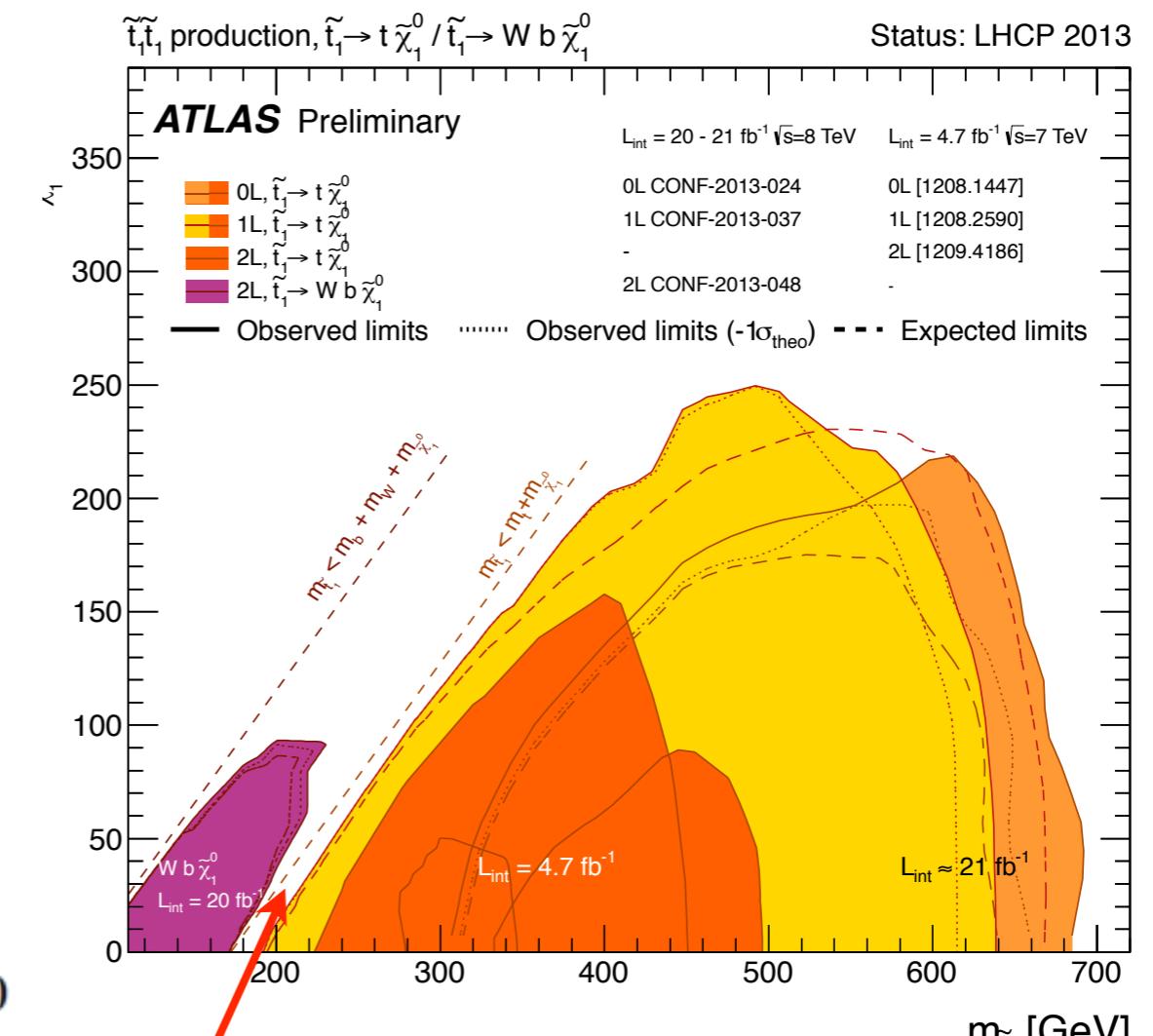
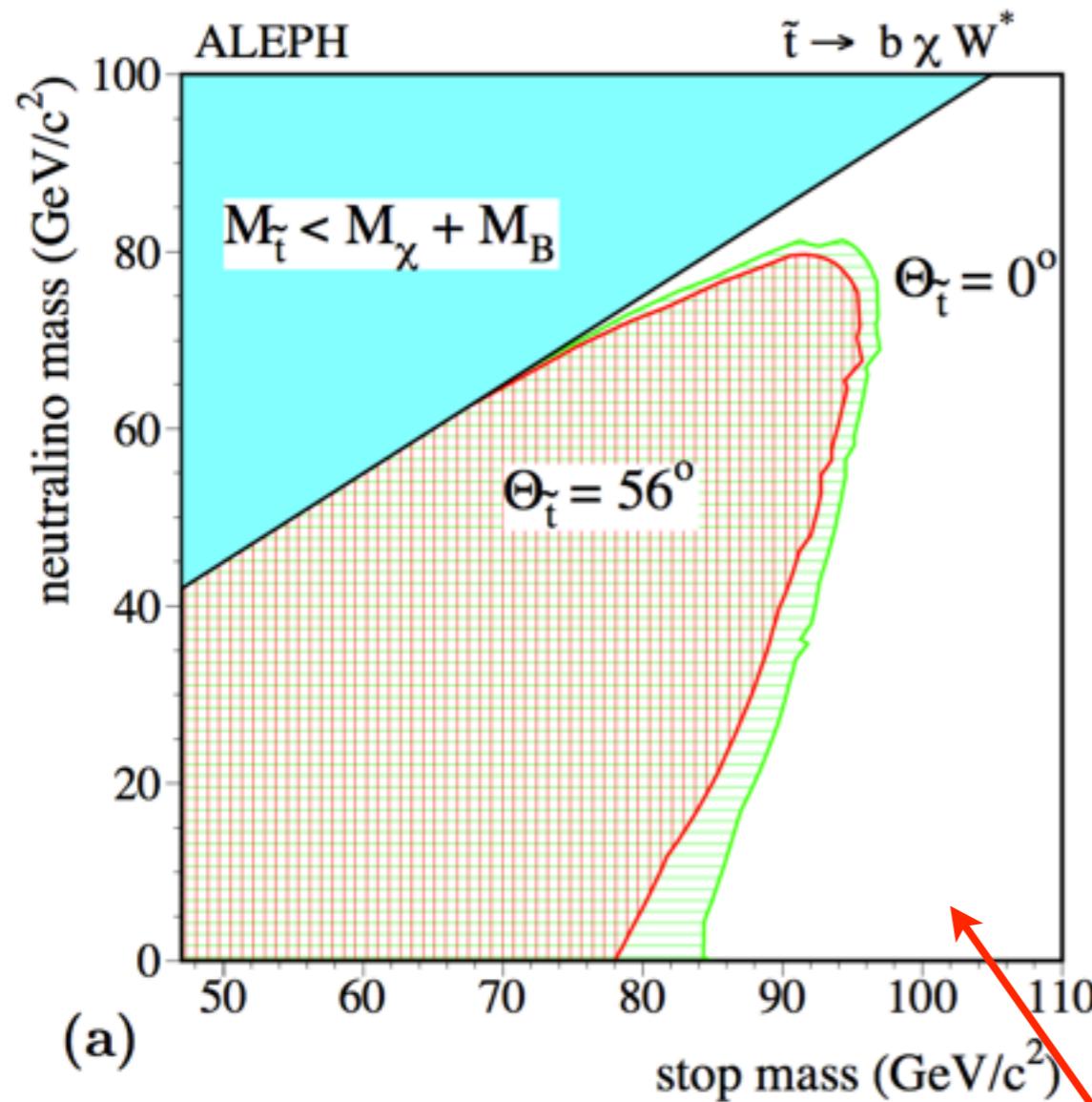
# 20 fb<sup>-1</sup> 8 TeV Limits (fastlim)



Papucci, Sakurai, AW, Zeune

**killing the stealth stop**

# stop gaps



gaps

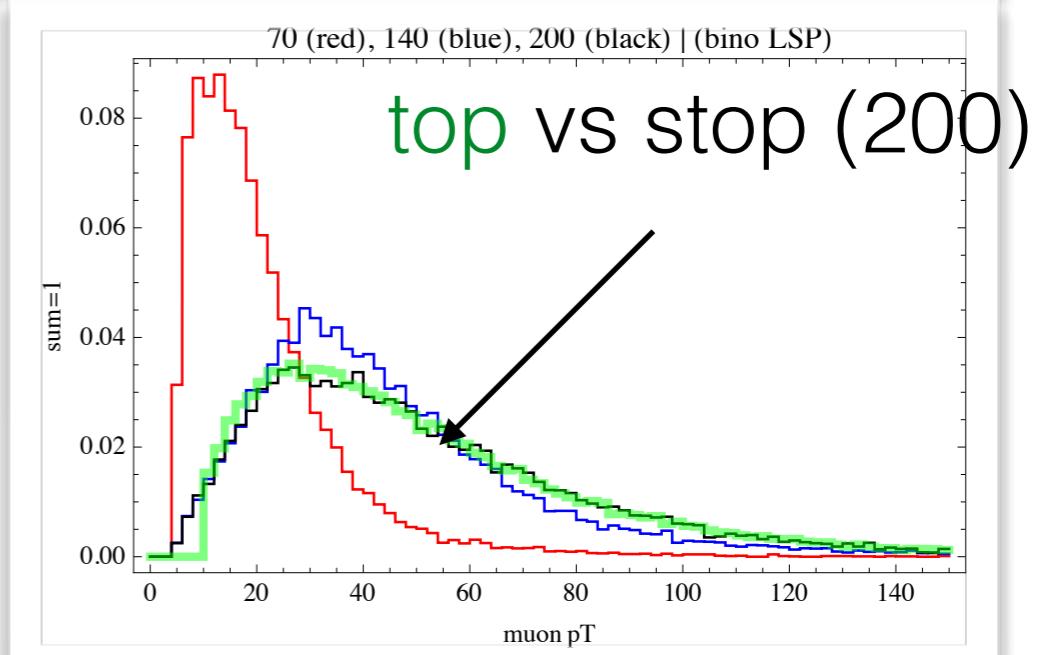
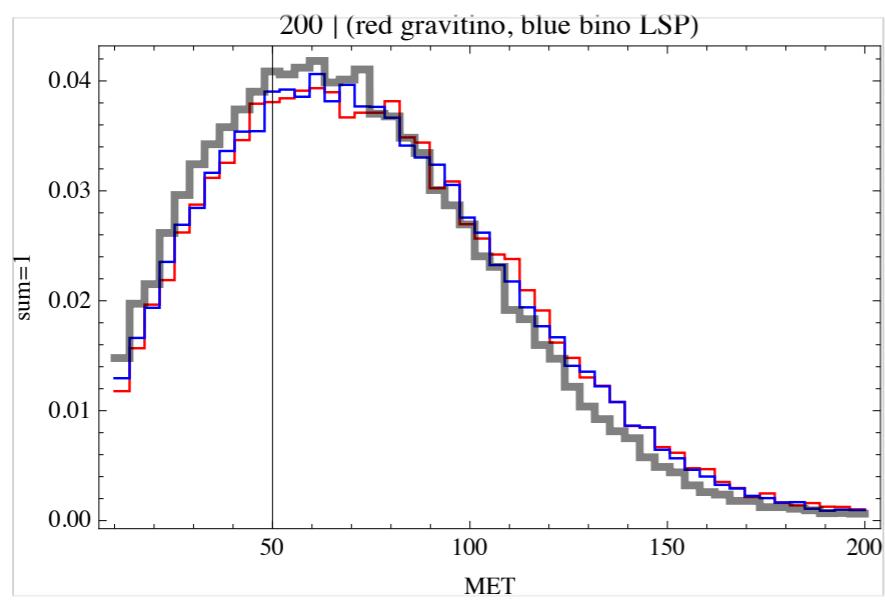
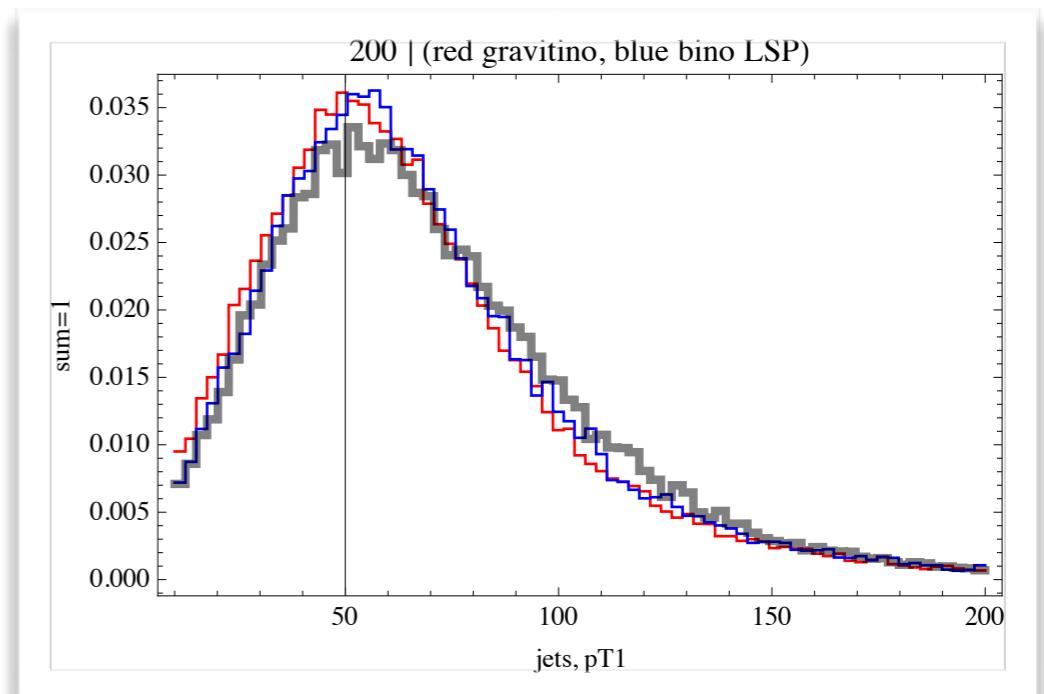
$m_{\tilde{t}} \approx 80 - 110, 170 - 190 \text{ GeV}$

# Stealthy stop



If  $m_{\tilde{t}_1} \approx m_t$ , decay  $\tilde{t}_1 \rightarrow t\chi_0$

is ‘one-body’



**Relax & Wait?**



**Michele\*** vs.

Relax & Wait?



Michele\*

vs.

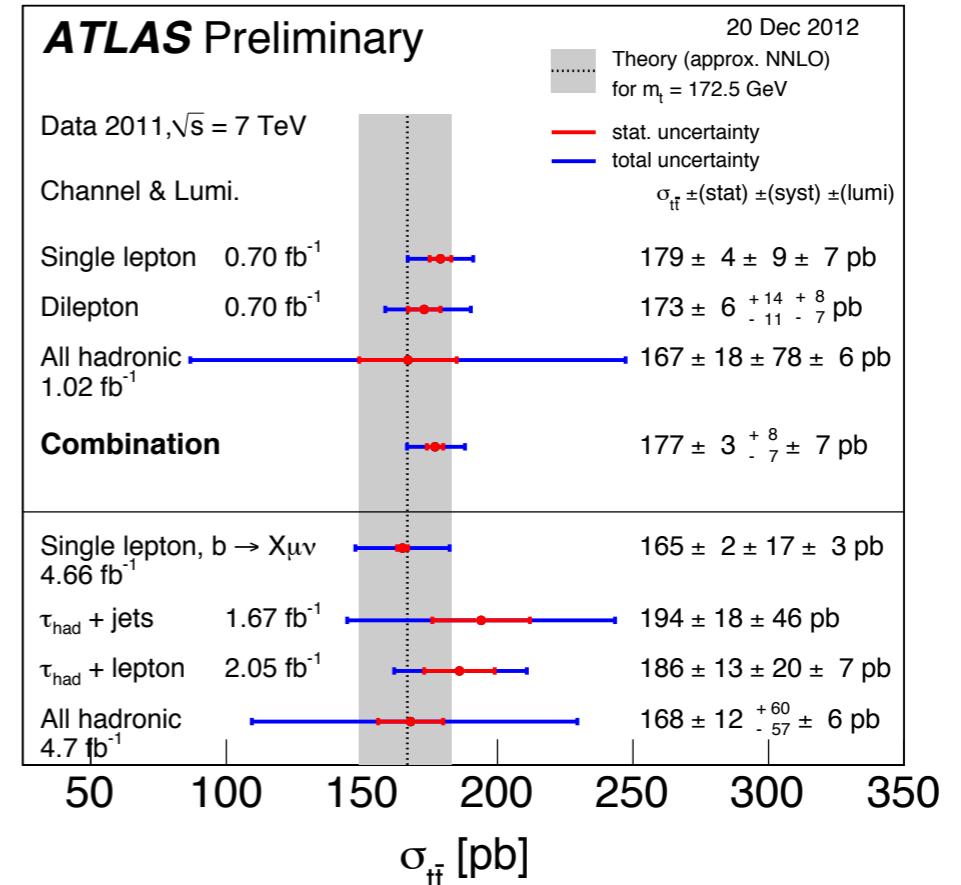
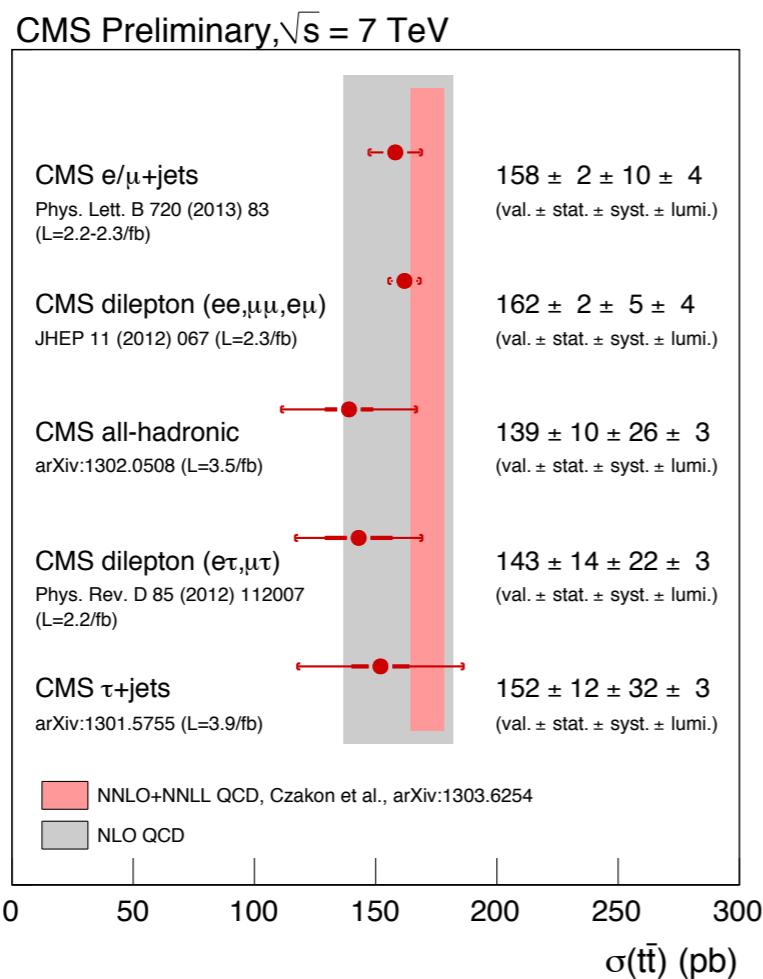


Josh

Let's check!

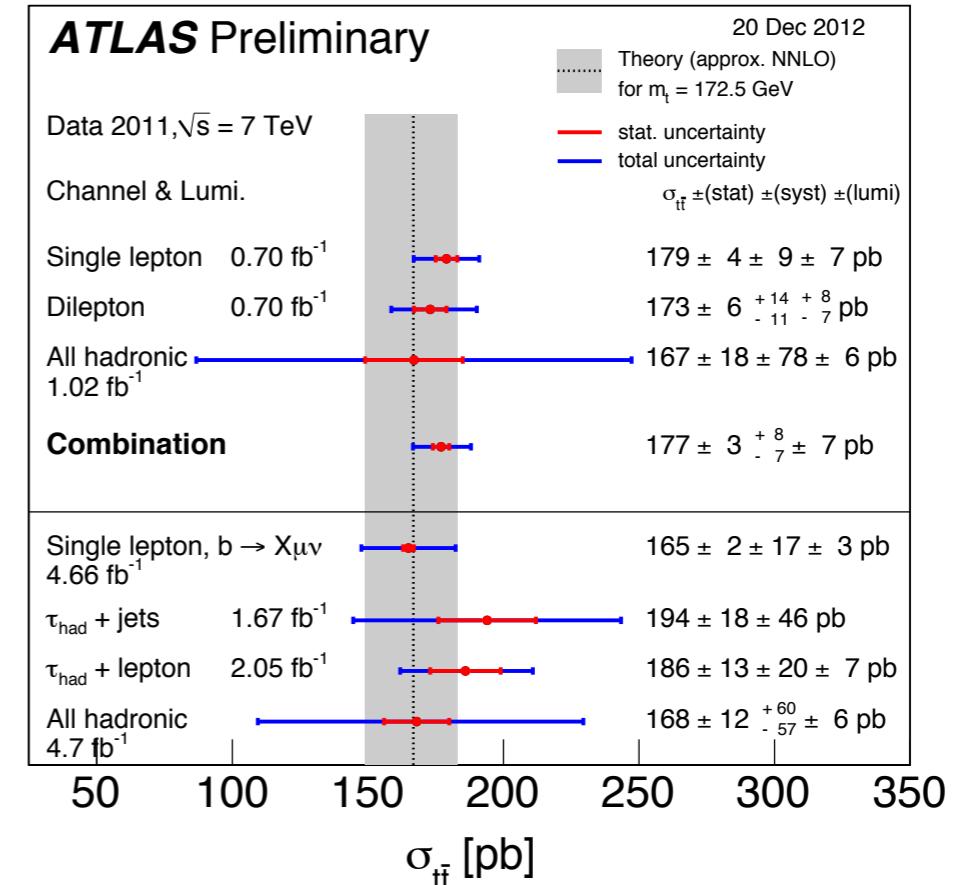
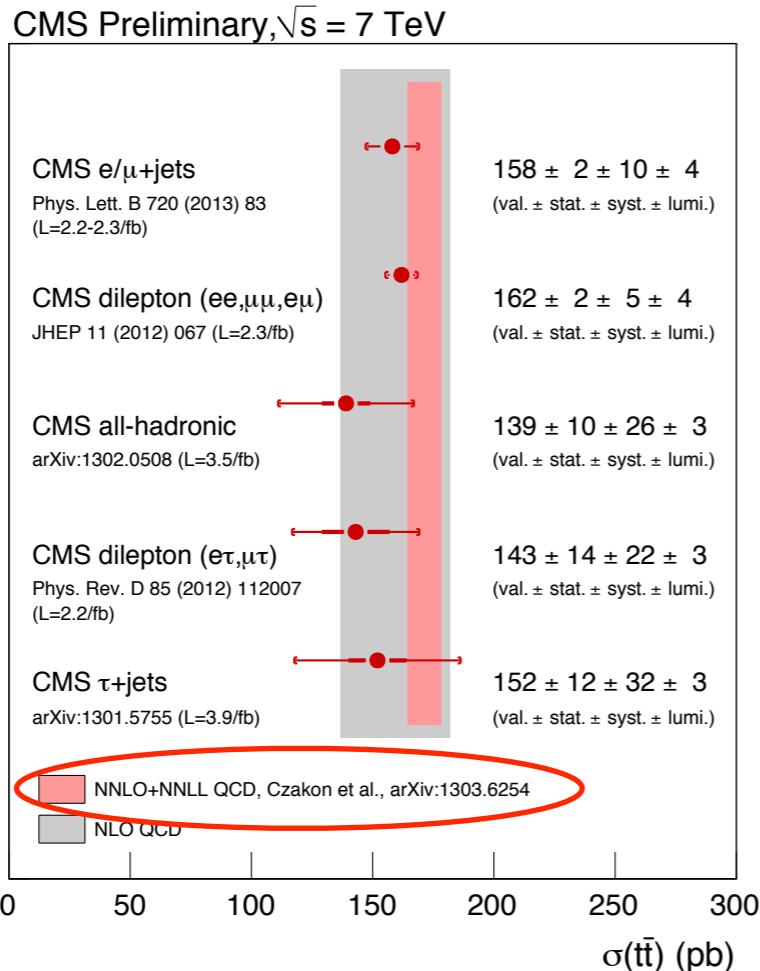
# top cross section

## experiment:



# top cross section

## experiment:



## theory:

The total top quark pair production cross-section at hadron colliders through  $\mathcal{O}(\alpha_S^4)$

Michał Czakon and Paul Fiedler  
*Institut für Theoretische Teilchenphysik und Kosmologie,  
RWTH Aachen University, D-52056 Aachen, Germany*

Alexander Mitov  
*Theory Division, CERN, CH-1211 Geneva 23, Switzerland*  
(Dated: March 26, 2013)

NNLO+NNLL

$$\sigma_{t\bar{t}} = 172^{+4.4}_{-5.8} (\text{scale})^{+4.7}_{-4.8} (\text{pdf}) \text{ pb}$$

# top cross section

the numbers (7 TeV)

$$\sigma_{t\bar{t}} = 172 \text{ pb}$$

NNLO:

$$\delta\sigma_{\text{th}} = 10 \text{ pb} \quad (5.7\%)$$

NLO:

$$\delta\sigma_{\text{th}} = 20 \text{ pb} \quad (12\%)$$

$$\delta\sigma_{\text{exp}} = 7 \text{ pb} \quad (4.2\%)$$

$$\sigma_{\tilde{t}\tilde{t}^*}(m_{\tilde{t}} = m_t) = 26 \text{ pb} \quad (15\%)$$

$$\frac{\sigma_{\text{exp}}^{\text{top}}}{\text{SM}} = 1 + \frac{\epsilon_t}{\epsilon_{\tilde{t}}} \frac{\sigma^{\text{stop}}}{\sigma_{\text{SM}}^{\text{top}}}$$

**MC mockup**

measurement

Theory NNLO+NNLL

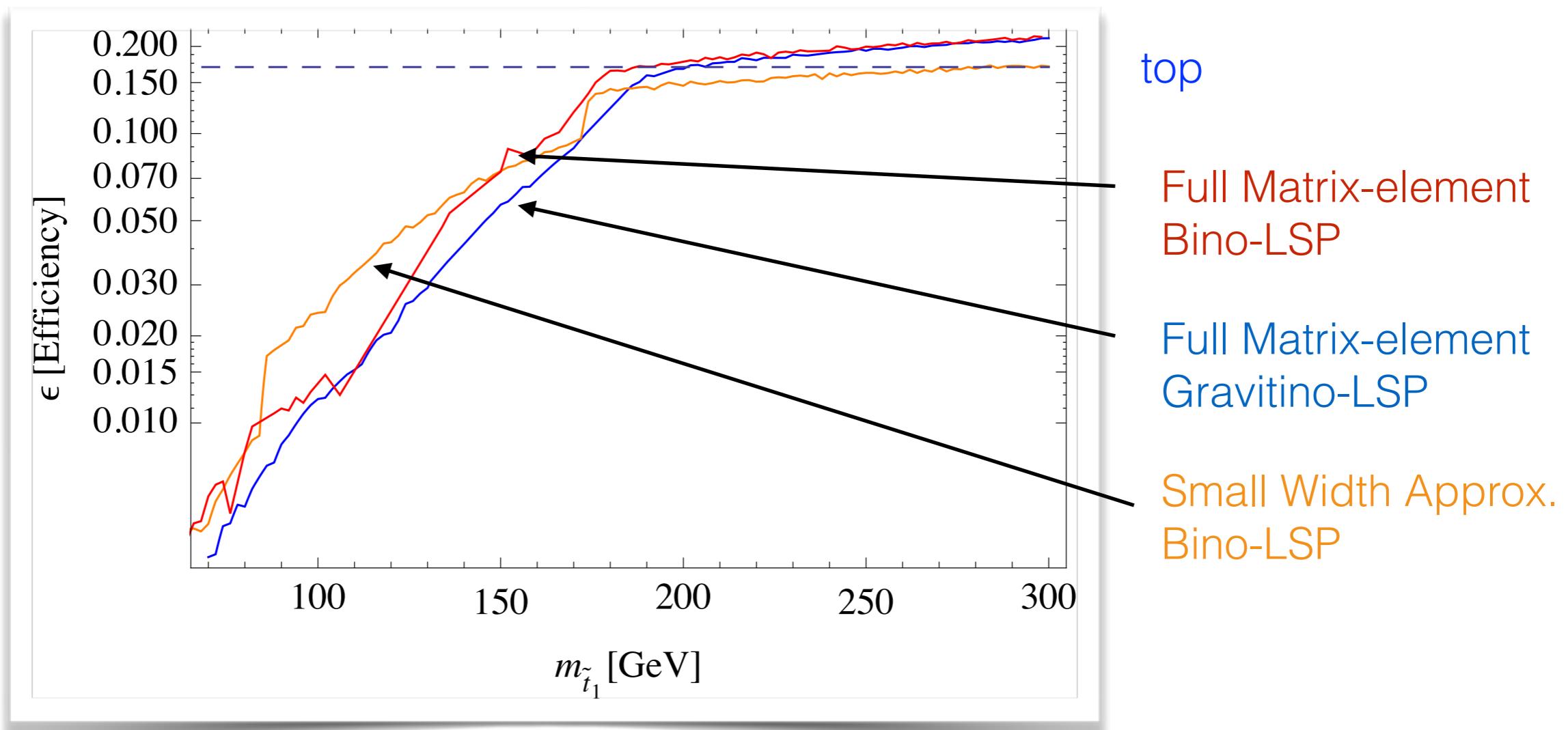
# Re-cast top x-sec measurement

Czakon/Mitov/Papucci/Ruderman/AW '13

Di-leptonic top (CMS-TOP-11-005), cut & count

Efficiency:

$$\tilde{t}_1 \rightarrow t\chi_0$$



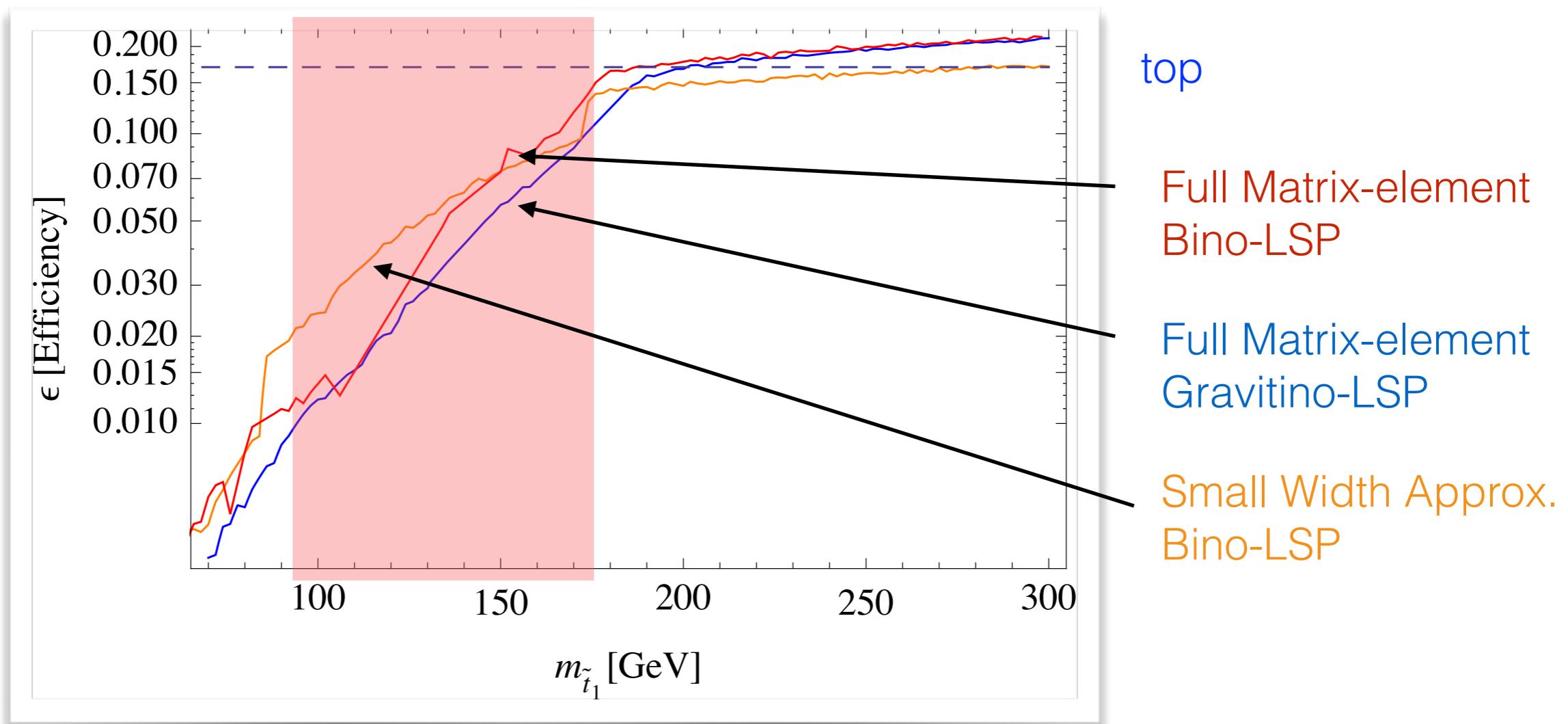
# Re-cast top x-sec measurement

Czakon/Mitov/Papucci/Ruderman/AW '13

Di-leptonic top (CMS-TOP-11-005), cut & count

Efficiency:

$$\tilde{t}_1 \rightarrow W b \chi_0 \quad \tilde{t}_1 \rightarrow t \chi_0$$



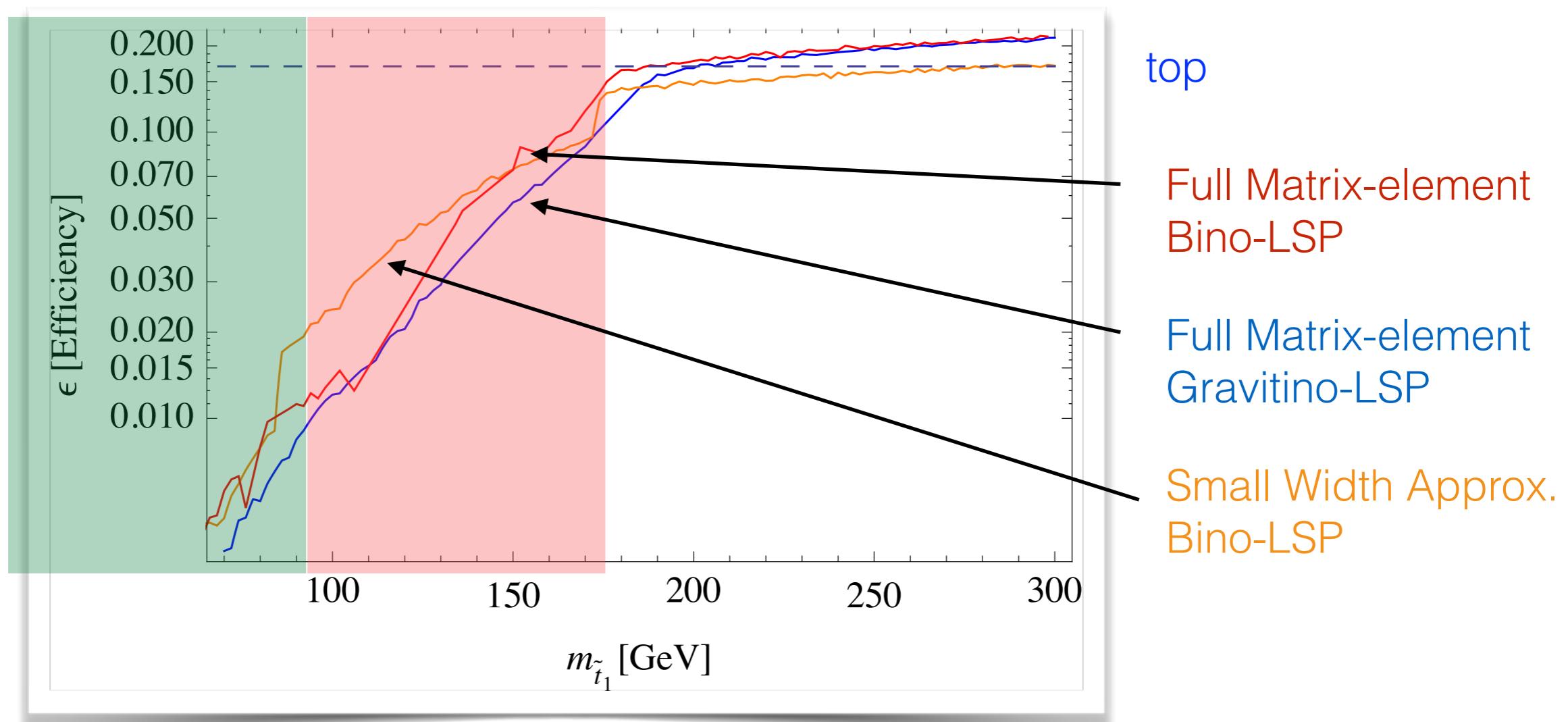
# Re-cast top x-sec measurement

Czakon/Mitov/Papucci/Ruderman/AW '13

Di-leptonic top (CMS-TOP-11-005), cut & count

Efficiency:

$$\tilde{t}_1 \rightarrow l\nu b\chi_0 \quad \tilde{t}_1 \rightarrow W b\chi_0 \quad \tilde{t}_1 \rightarrow t\chi_0$$



stop  $\rightarrow$  gravitino + X

$$\psi_\mu \rightarrow -\sqrt{\frac{2}{3}} \frac{\partial_\mu \psi}{m_{\tilde{G}}}$$

Goldstino limit ( $E \gg m_{3/2}$ )

$$\mathcal{L}_{\tilde{t}t\tilde{G}} = \frac{i}{F} \partial_\nu \tilde{t}^* \partial_\mu \bar{\psi} \gamma^\nu \gamma^\mu (c_{\tilde{t}} P_L + s_{\tilde{t}} P_R) t + \text{h.c.}$$

$$\mathcal{L}_{\tilde{t}Wb\tilde{G}} = \frac{\sqrt{2}}{F} g c_{\tilde{t}} (W_\mu^+ \tilde{t}^* \partial^\mu \bar{\psi} P_L b + W_\mu^- \tilde{t} \bar{b} P_R \partial^\mu \psi)$$

**Couples to susy, additional  $(m_{\tilde{t}_1} - m_t)^2$  suppression**

stop  $\rightarrow$  gravitino + X

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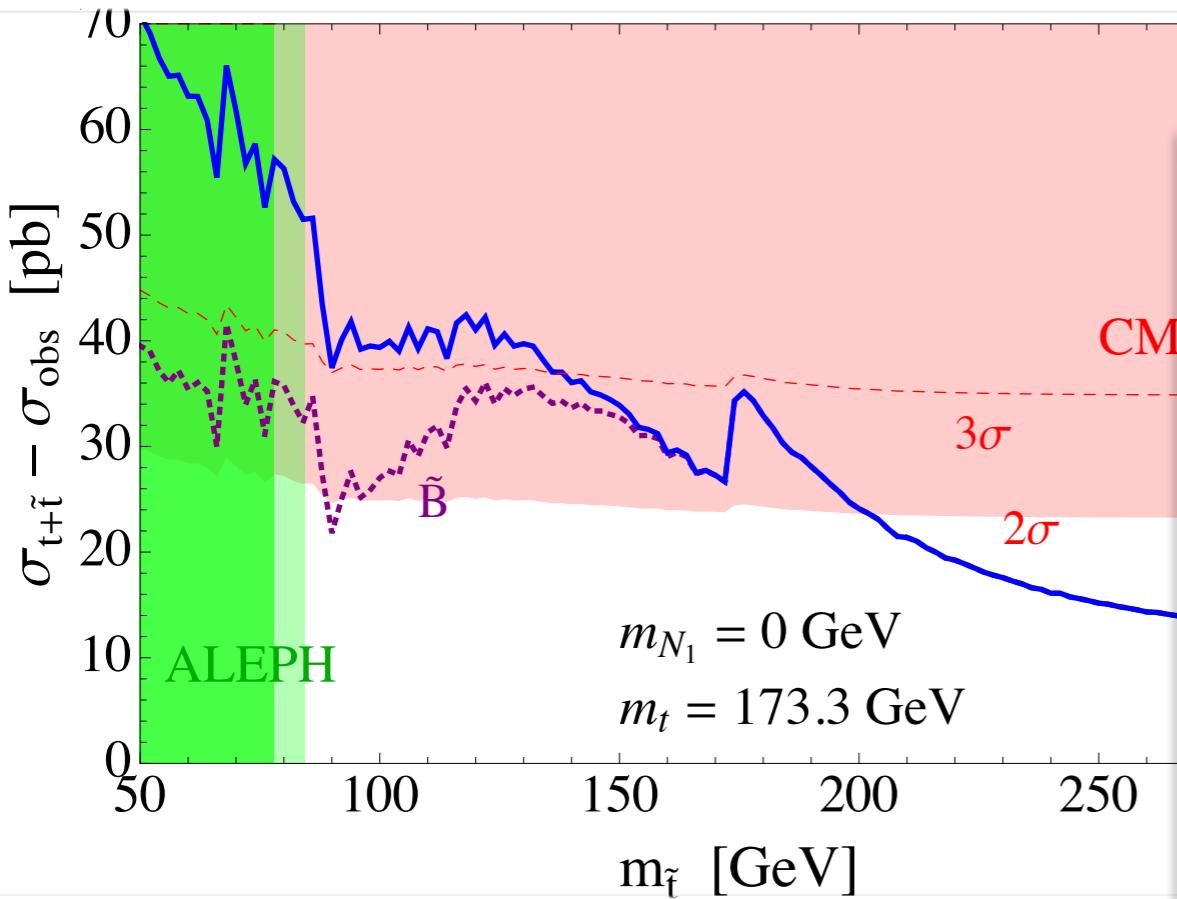
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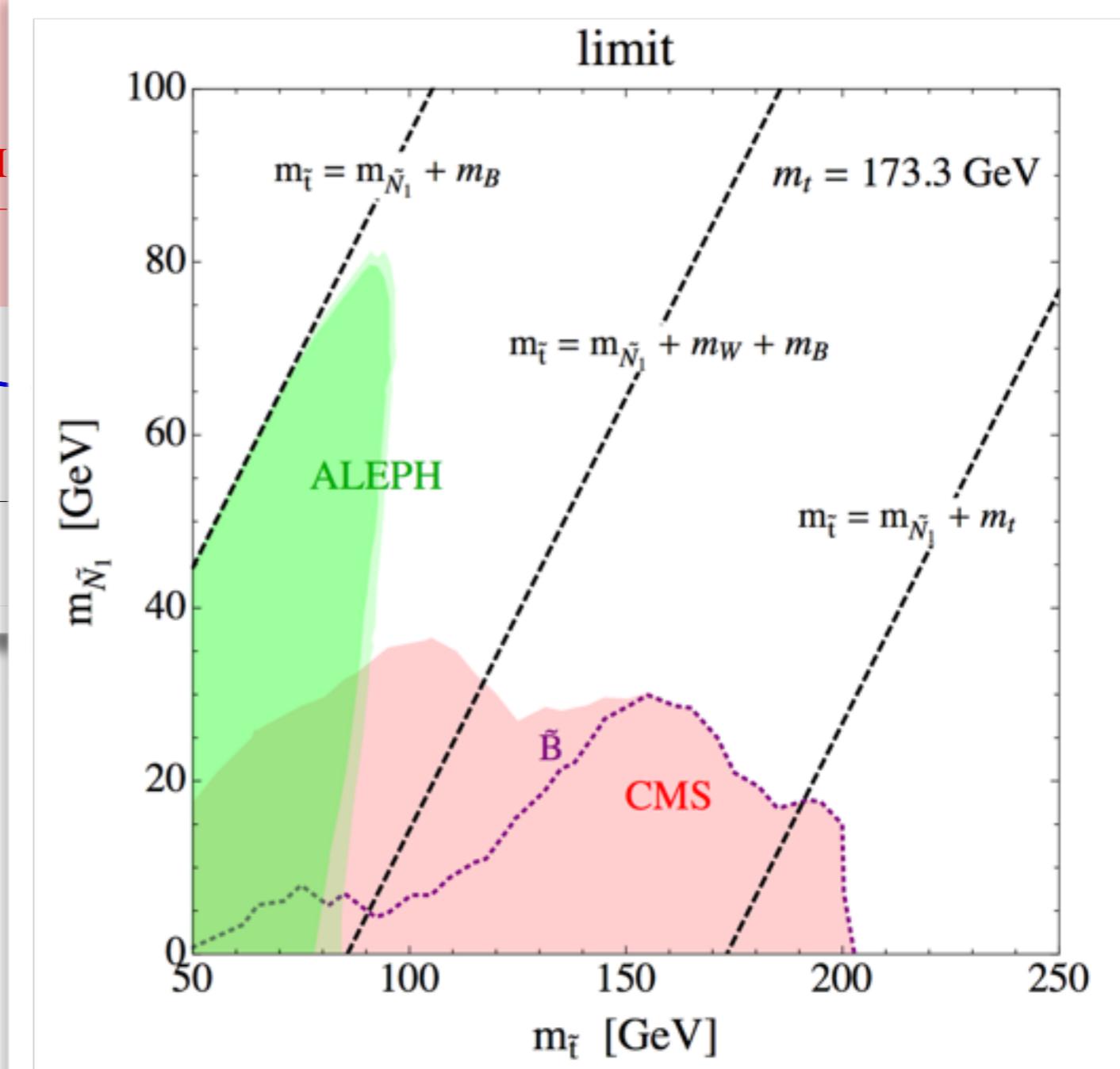
**Couples to susy, additional  $(m_{\tilde{t}_1} - m_t)^2$  suppression**

# Stealth stop exclusion

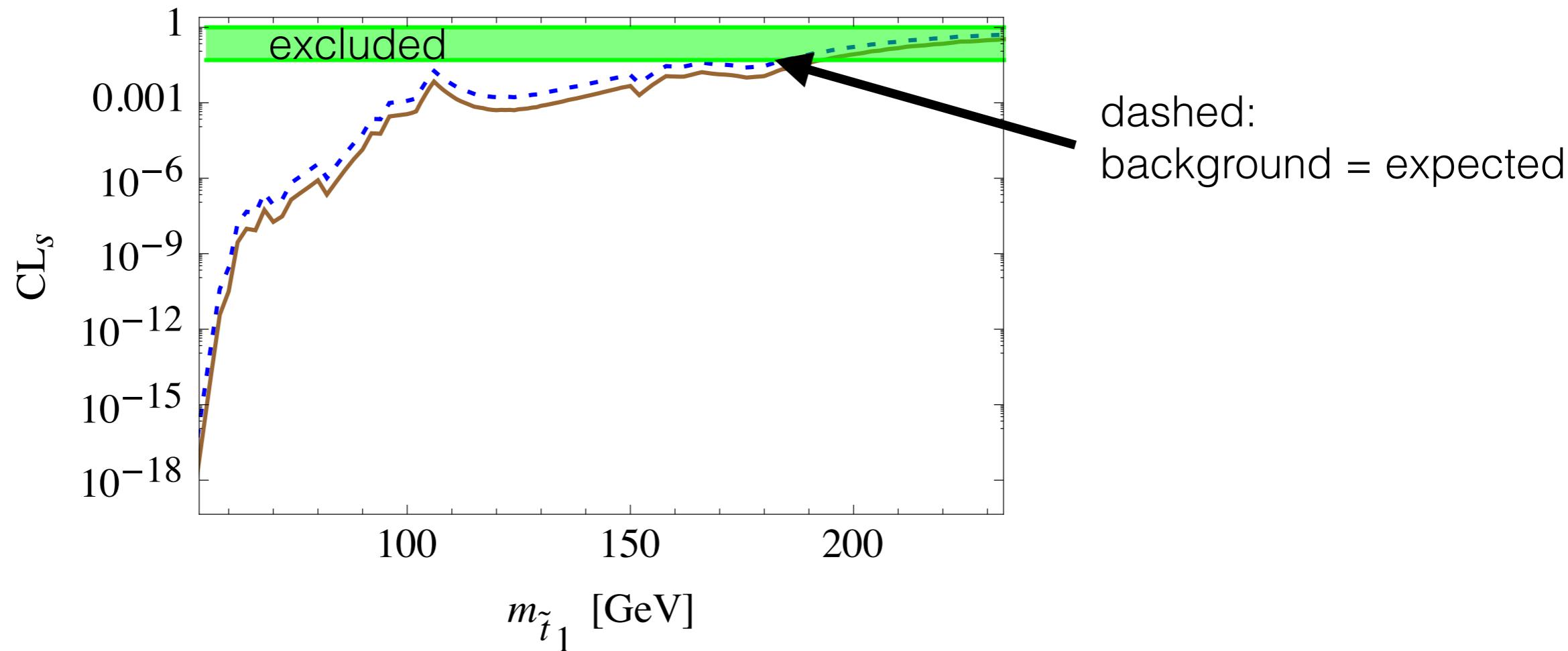
Czakon/Mitov/Papucci/Ruderman/AW '13



$$\rightarrow Br(t \rightarrow \tilde{t}_1 \chi_0) = 0.1$$



# Exclusion vs. fluctuations



$CL_s = CL_{s+b}/CL_s$  reduces impact of under-fluctuation of background. Even if we set background to expectation, exclusion persists.

Natural

I  
Supersymmetry

II  
Strong EWSB dynamics  
(composite Higgs)

III  
Large Extra Dimensions

Un-natural

IV  
Multiverse (anthropic principle)

$10^{1000\dots}$  vacua  
of which many have a hierarchy

Expect: just SM + Higgs  
+ (possibly weak scale DM)

Natural

I  
Supersymmetry

II  
Strong EWSB dynamics  
(composite Higgs)

III  
Large Extra Dimensions

Natural

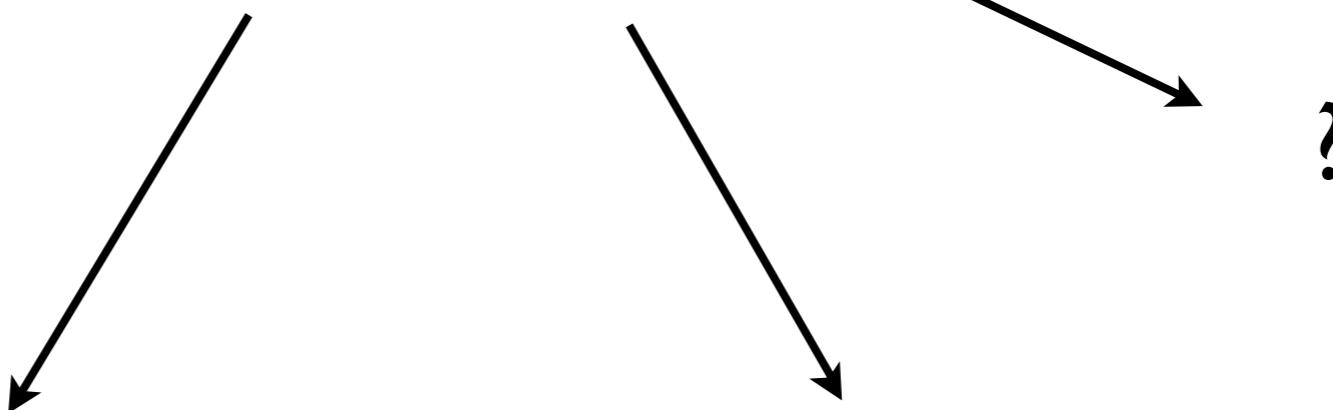
I  
Supersymmetry

II  
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(composite Higgs)

III  
Large Extra Dimensions

# New physics & naturalness

## Light Higgs

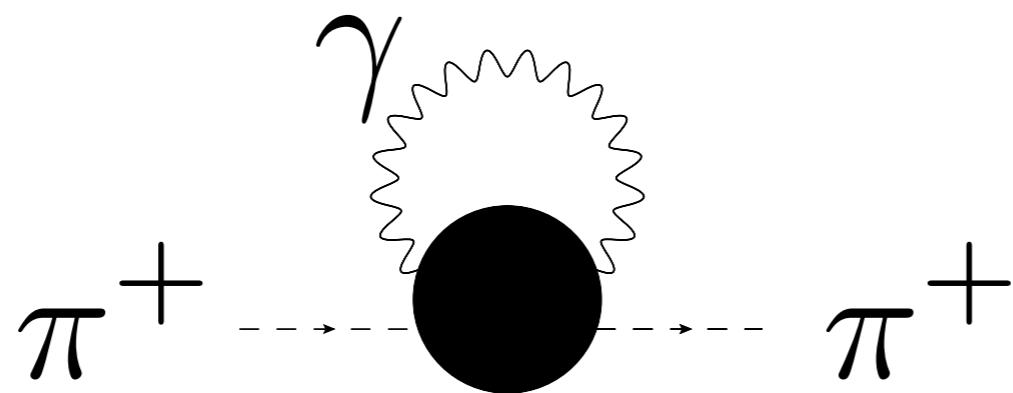


light stops<sub>I,2</sub>, sbottom<sub>L</sub>,  
higgsinos, gluinos, ...

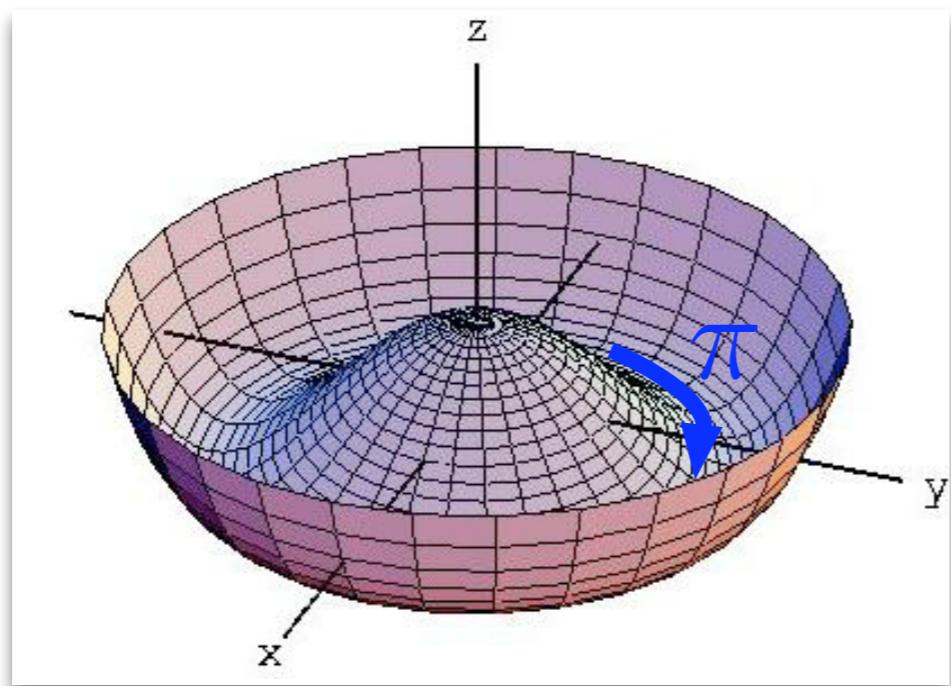
supersymmetry

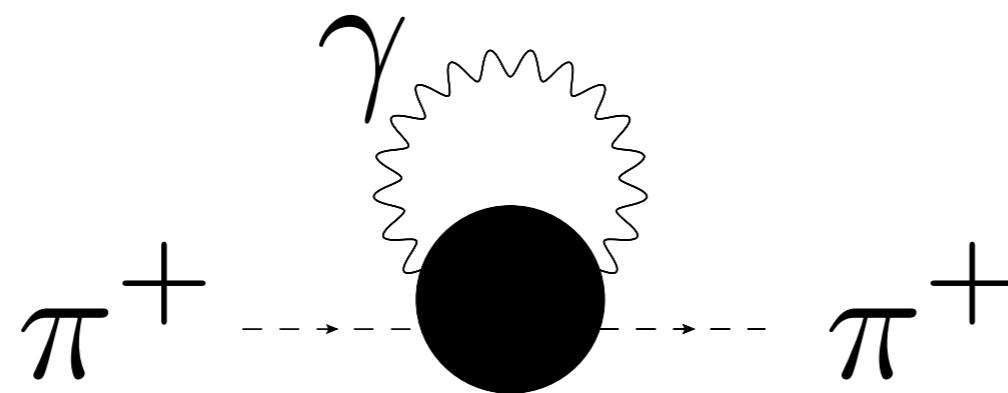
light top partners  
( $Q=5/3,2/3,1/3$ ),  
anything else ?

composite Higgs

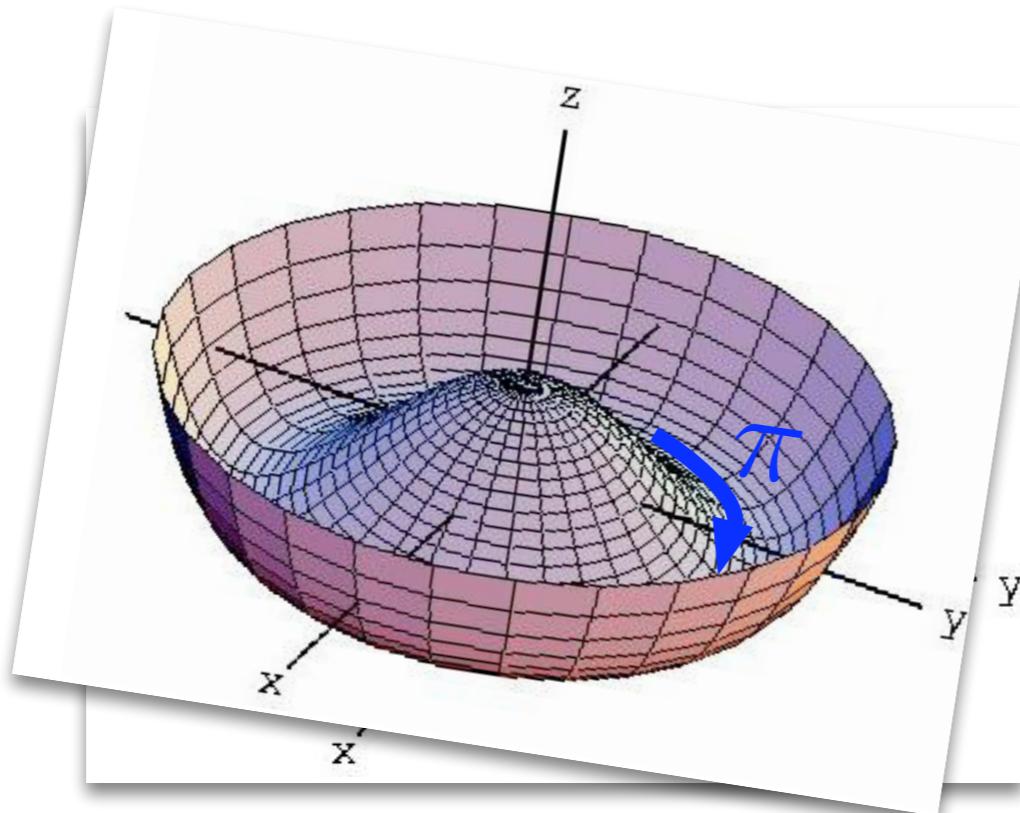


Das et al '67





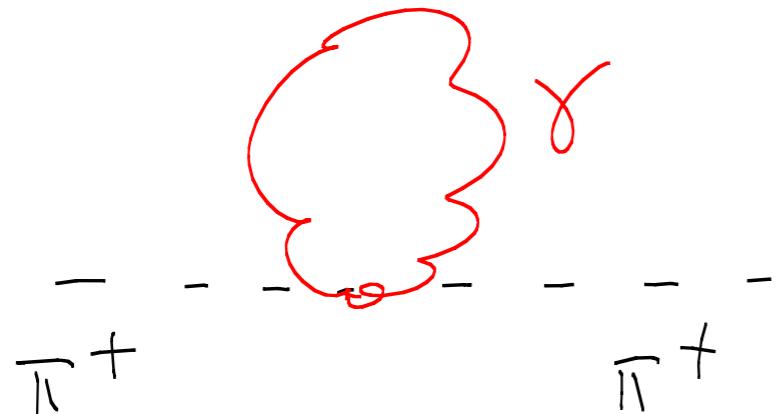
Das et al '67



Potential tilted:  
due to quark masses  
and gauging of EM

$GB \rightarrow pGB$

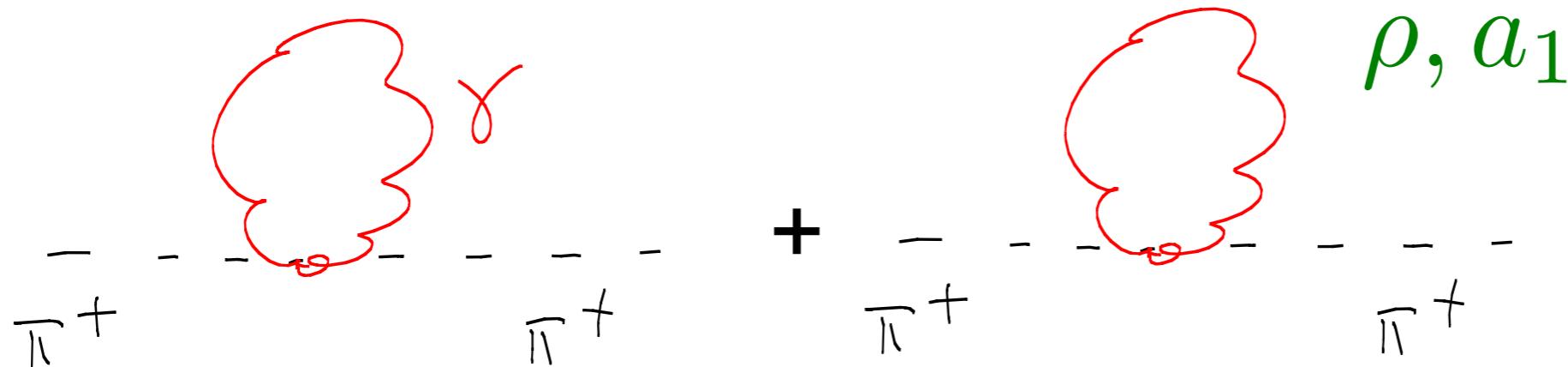
# Neutral-charged pion mass difference: natural resolution



$$\delta m_{\pi^+}^2 \sim \frac{3\alpha}{4\pi} \Lambda^2 < (m_{\pi^+}^2 - m_{\pi^0}^2)_{\text{exp}} \approx (4 \text{ MeV})^2$$

**Expect**  $\rightarrow \Lambda < 850 \text{ MeV}$

# Neutral-charged pion mass difference: natural resolution



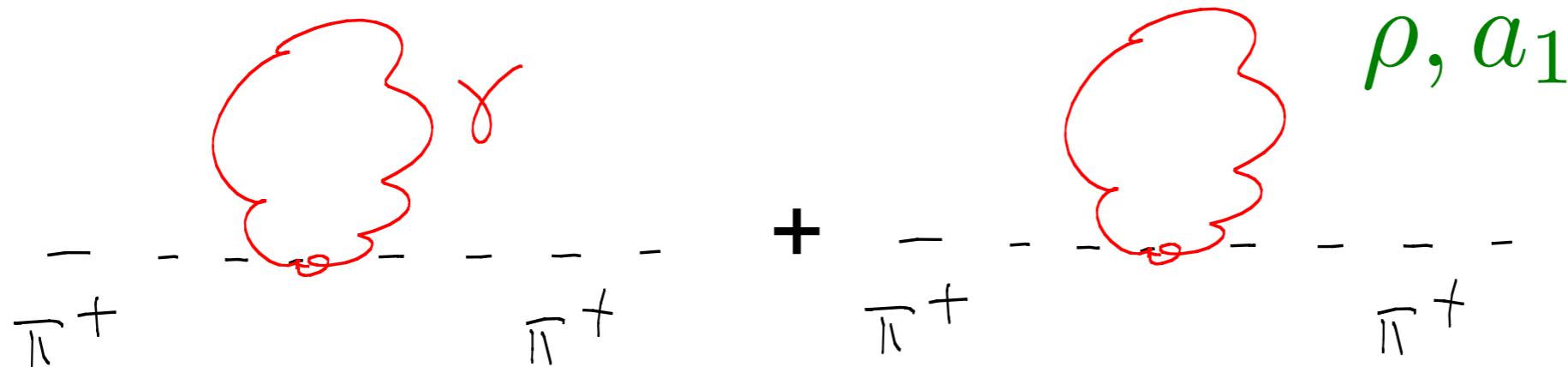
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‘New physics’: comes in at  $m_\rho = 770 \text{ MeV}$

Das et al ‘67

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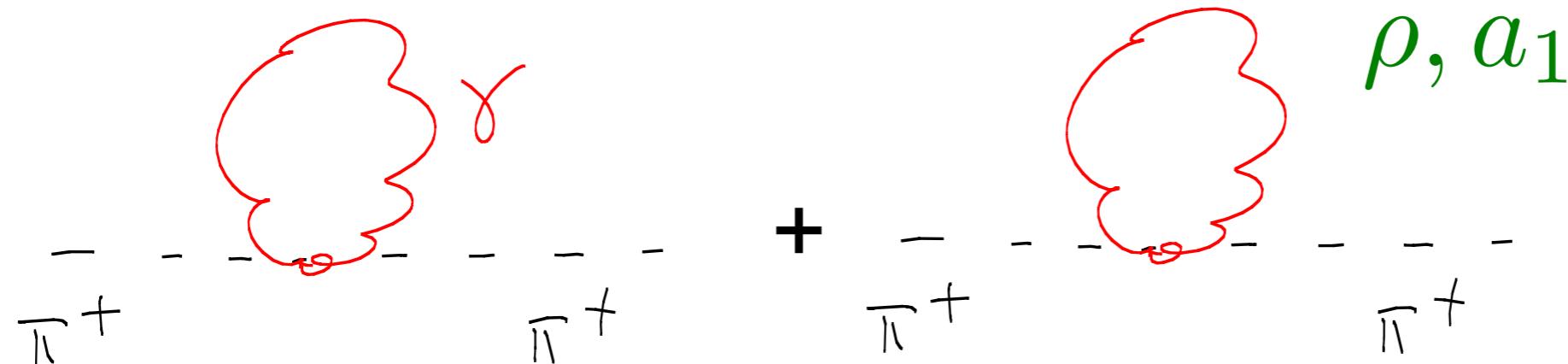
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‘New physics’: comes in at  $m_\rho = 770 \text{ MeV}$

$$m_{\pi^\pm}^2 - m_{\pi^0}^2 \simeq \frac{3\alpha_{em}}{4\pi} \frac{m_\rho^2 m_{a_1}^2}{m_{a_1}^2 - m_\rho^2} \log \left( \frac{m_{a_1}^2}{m_\rho^2} \right) \quad \text{Das et al '67}$$

$$(m_{\pi^\pm} - m_{\pi^0})|_{\text{TH}} \simeq 5.8 \text{ MeV} !$$

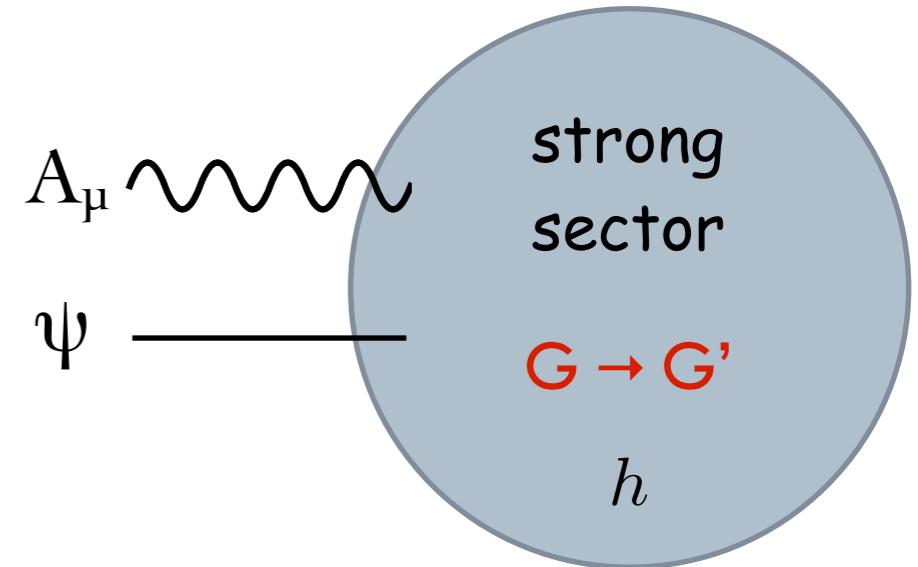
# Why is the Higgs light?

Kaplan; Agashe et. al

Higgs is a pNGB

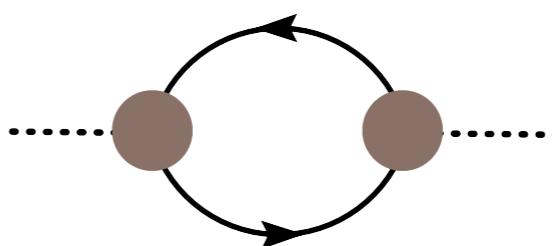
Minimal example

$$SO(5) \rightarrow SO(4) \sim SU(2)_L \times SU(2)_R$$



No pure composite effects,  
vanish due to NG symmetry

$$\dots \text{---} \bullet \text{---} \dots = 0$$

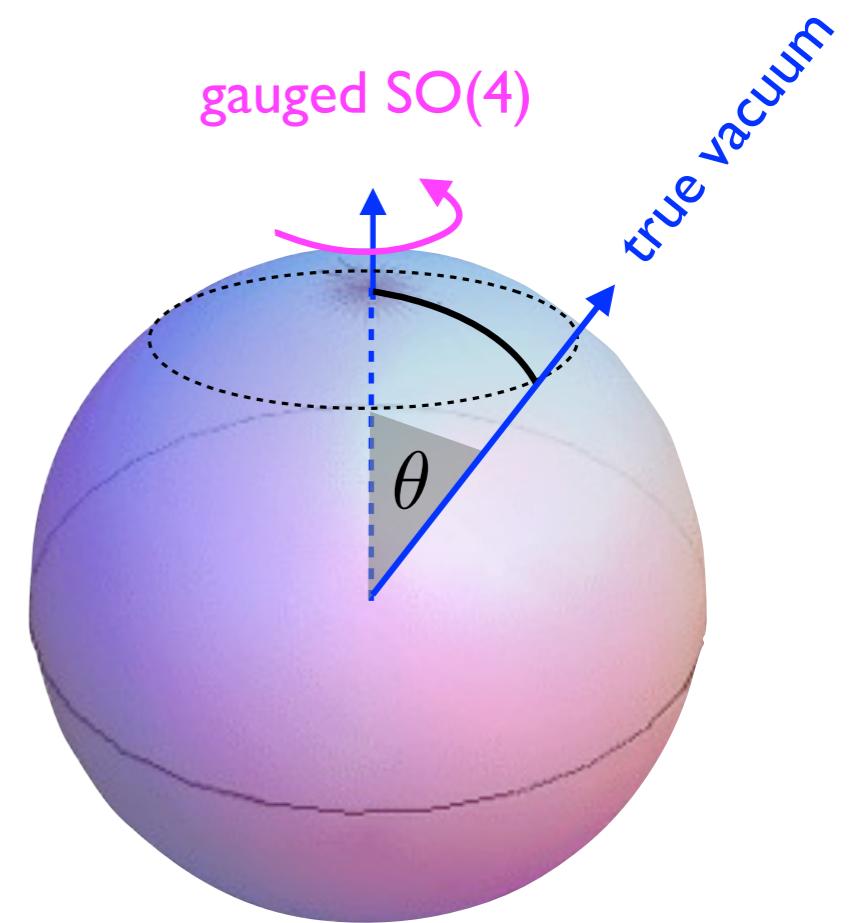


NG symmetry broken by  
elementary-composite couplings:

$$m_h^2 \sim \frac{\lambda^2}{16\pi^2} \Lambda_{comp}^2$$

$$\lambda \ll 4\pi$$

$\theta$ : misalignment between gauged  $\text{SO}(4)$  and  $\text{SO}(4)'$  preserved in the quantum corrected vacuum



Tree level: gauge  $\text{SO}(4)$  aligned

$$\phi = e^{i\pi^{\hat{a}} T^{\hat{a}}/f} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} \sin(\pi/f) \times \begin{pmatrix} \hat{\pi}^1 \\ \hat{\pi}^2 \\ \hat{\pi}^3 \\ \hat{\pi}^4 \end{pmatrix} \\ \cos(\pi/f) \end{pmatrix}$$

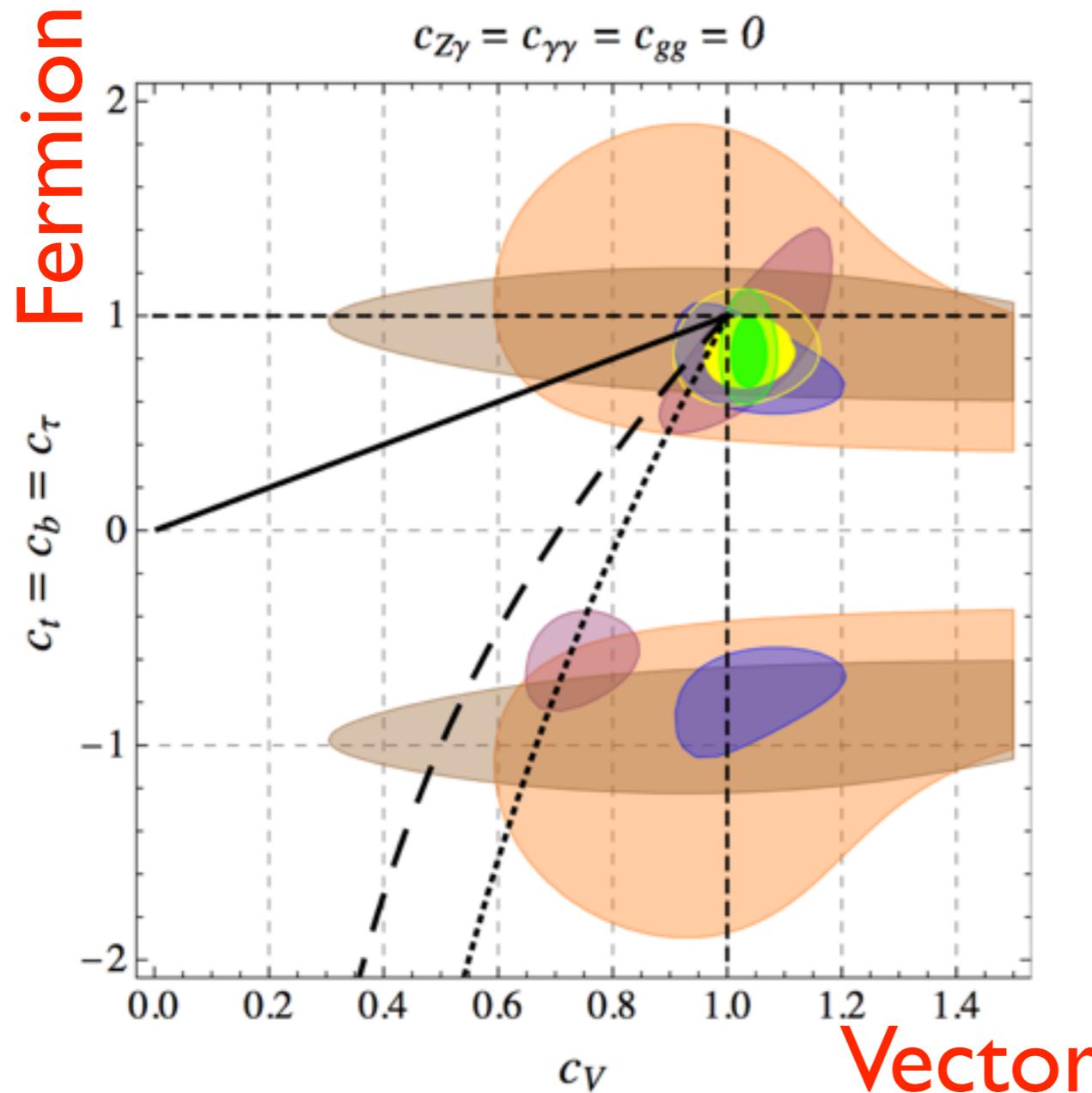
@ 1-loop:  $\langle \hat{\pi}^4 \rangle = \theta * f$

Higgs

$$\begin{pmatrix} \sin(\theta + h(x)/f) & e^{i\chi^i(x)A^i/v} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} \\ \cos(\theta + h(x)/f) \end{pmatrix}$$

eaten by  $W_L, Z_L$

# Composite Higgs vs. LHC data



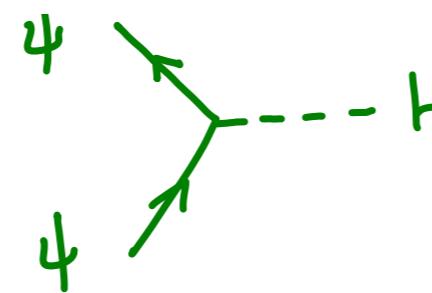
post-Moriond fit: see e.g.  
Giardino et al, Falkowski et  
al

Limit

$f \approx 500 \dots 800 \text{ GeV}$

$$a = \sqrt{1 - \xi}$$

$V$   $\dashv$   $h$   $a g_{hVV}^{\text{SM}}$



$c h_{44h}^{\text{SM}}$

$$c_f = \frac{1 - (1+n)\xi}{1 - \xi}$$

# Implications of $m_H = 125 \text{ GeV}$

Potential is fully radiatively generated

Agashe et. al

$$V_{gauge}(h) = \frac{9}{2} \int \frac{d^4 p}{(2\pi)^4} \log \left( \Pi_0(p) + \frac{s_h^2}{4} \Pi_1(p) \right) \quad s_h \equiv \sin h/f$$

$$\Pi_0(p) = \frac{p^2}{g^2} + \Pi_a(p) , \quad \Pi_1(p) = 2[\Pi_{\hat{a}}(p) - \Pi_a(p)]$$

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$$\int d^4 p \Pi_1(p)/\Pi_0(p) < \infty$$

Higgs dependent term  
UV finite

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Higgs dependent term  
UV finite

→ ‘Weinberg sum rules’

$$\lim_{p^2 \rightarrow \infty} \Pi_1(p) = 0 ,$$

$$\lim_{p^2 \rightarrow \infty} p^2 \Pi_1(p) = 0$$

**UV finiteness requires at least two resonances**

$$\Pi_1(p) = \frac{f^2 m_\rho^2 m_{a_1}^2}{(p^2 + m_\rho^2)(p^2 + m_{a_1}^2)} \quad \text{spin 1}$$

UV finiteness requires at least two resonances

$$\Pi_1(p) = \frac{f^2 m_\rho^2 m_{a_1}^2}{(p^2 + m_\rho^2)(p^2 + m_{a_1}^2)} \quad \text{spin I}$$

Similarly for SO(5) fermionic contribution

Pomarol et al; Marzocca

$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

similar result in deconstruction:  
Matsedonskyi et al; Redi et al

$5 = 4 + 1$  with EM charges  $5/3, 2/3, -1/3$

$Q_4 \ Q_1$

→ solve for  $m_h = 125 \text{ GeV}$

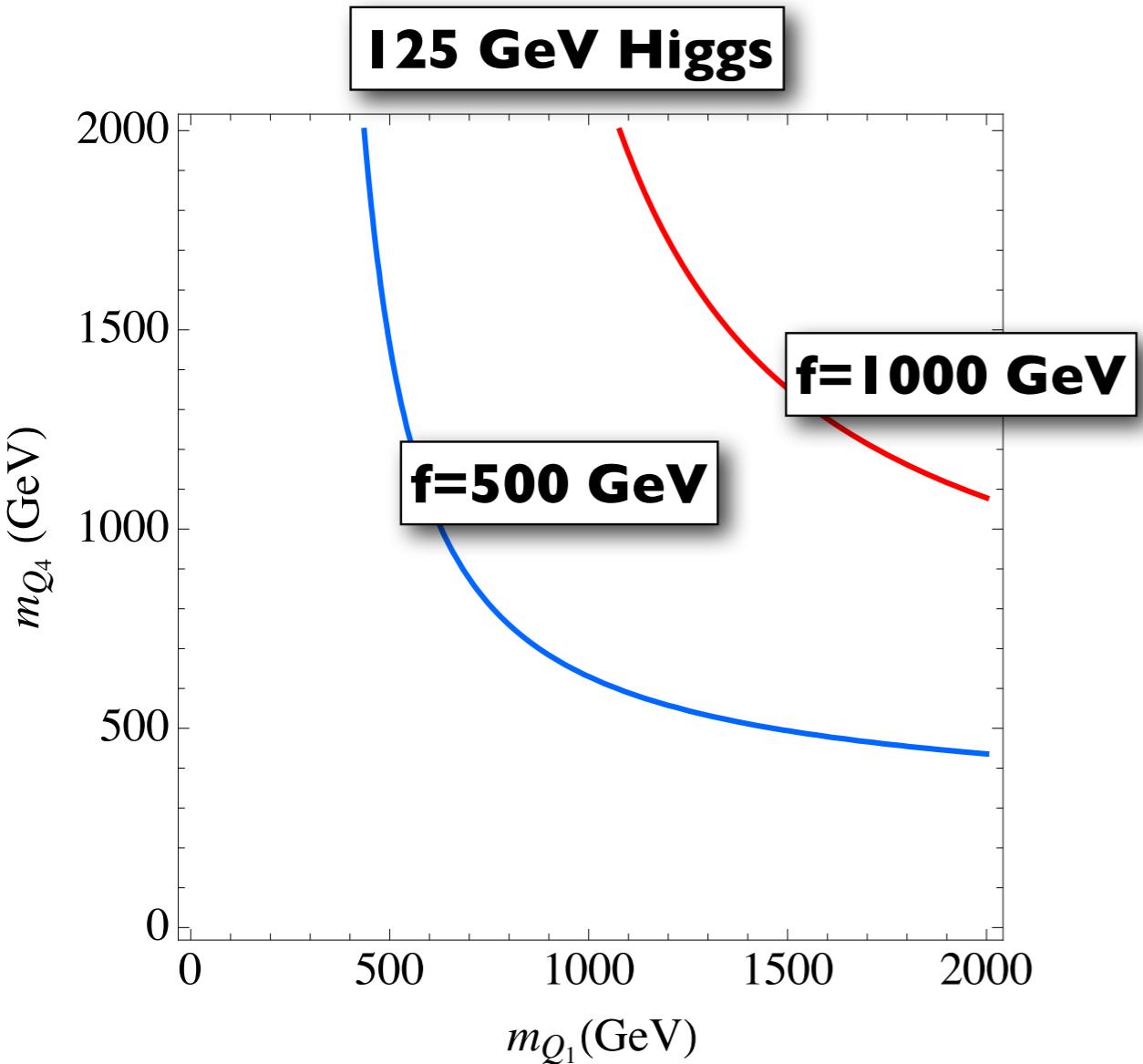
# Light Higgs implies light fermionic top partners

$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

Pomarol et al; Marzocca

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$$\begin{matrix} 5 = 4 + 1 \\ Q_4 \quad Q_1 \end{matrix}$$

with EM charges  $5/3, 2/3, -1/3$

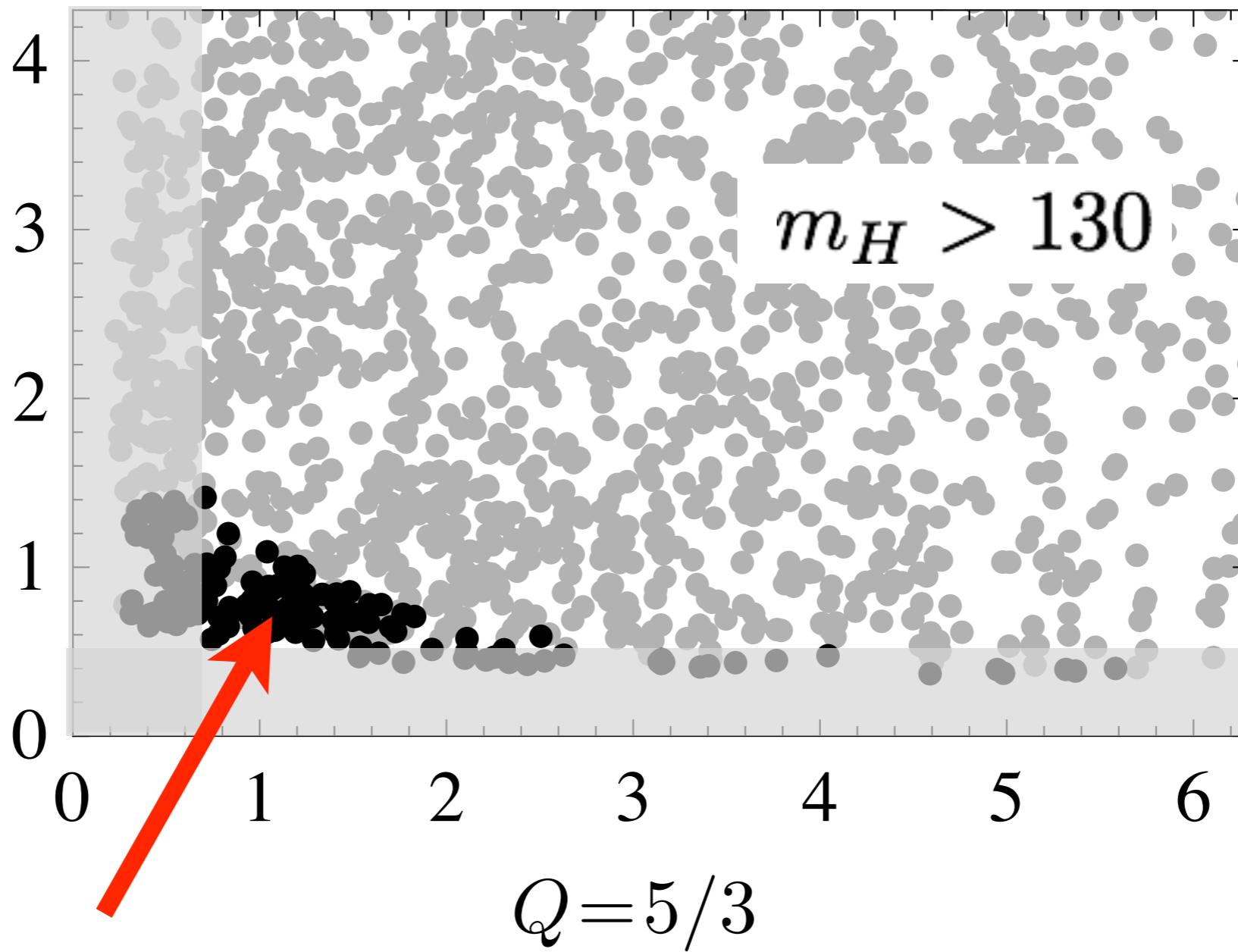
Contino et al; Pomarol, Riva;  
Matsedonskyi, Panico, Wulzer; Redi, Tesi;  
Marzocca, Serone, Shu;

# Scan over composite Higgs parameter space

$\xi = 0.2$

from 1204.6333

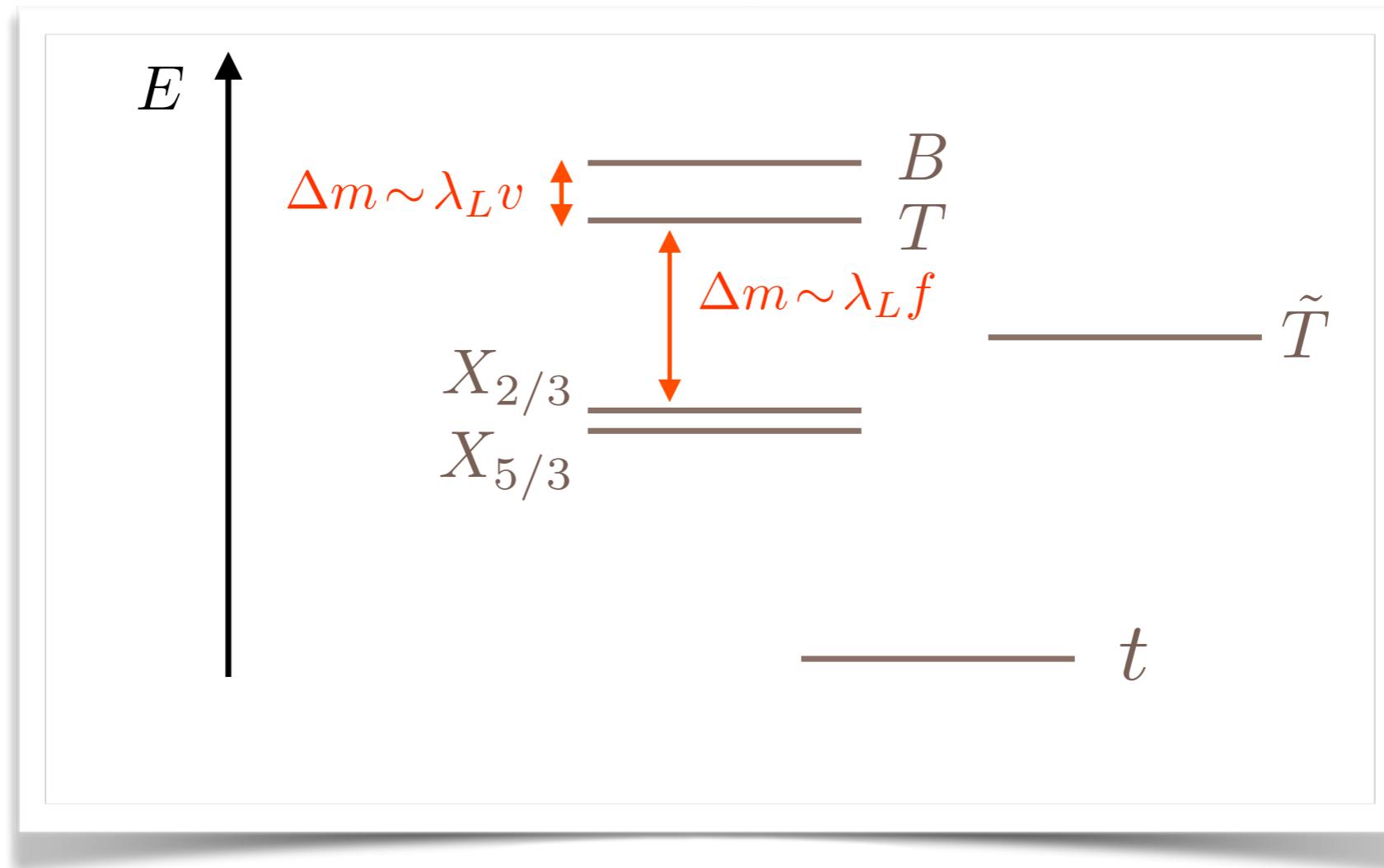
$Q = 2/3$



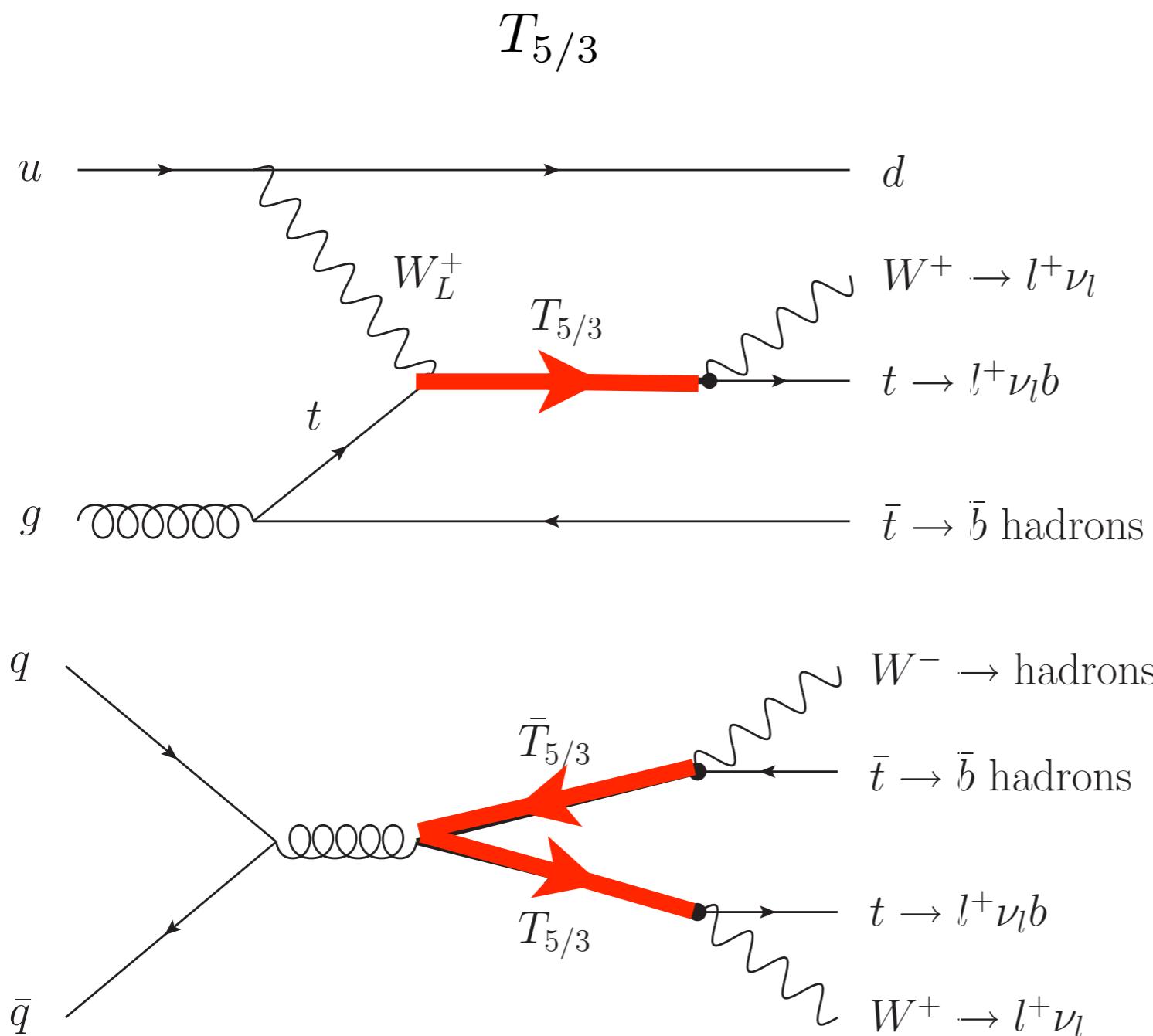
$m_H = 115 \dots 130 \text{ GeV}$

see e.g. ATLAS-CONF-2013-051

# Top partners

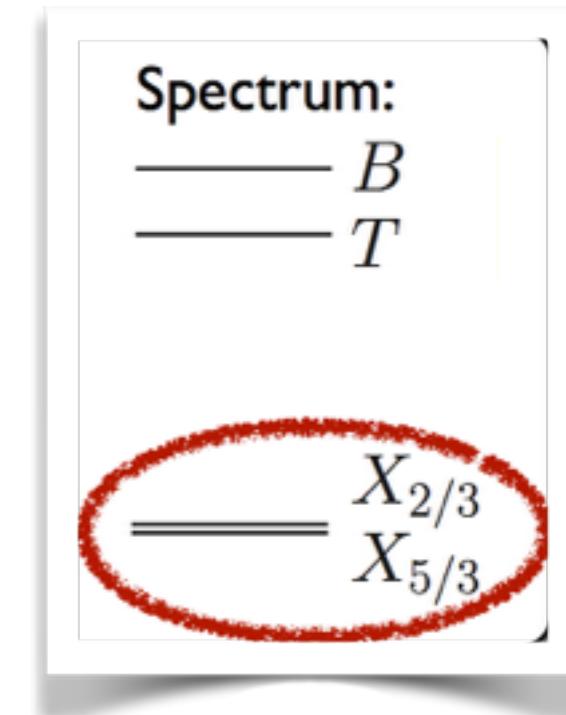


e.g. Perelstein, Pierce, Peskin  
 Contino, Servant; Mrazek, Wulzer;  
 De Simone, Matsedonkyi, Rattazzi, Wulzer;  
 Spannowsky et al

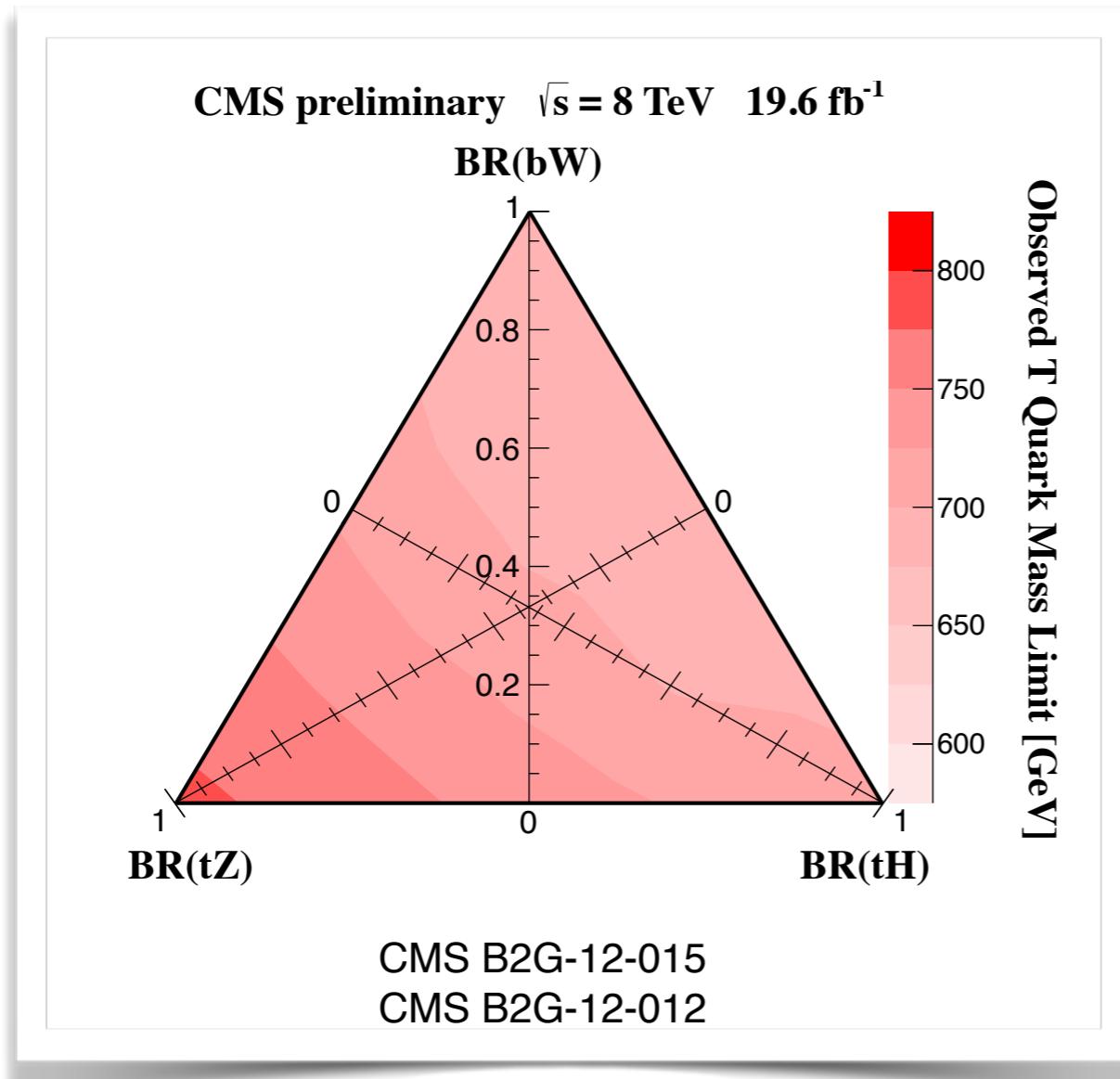
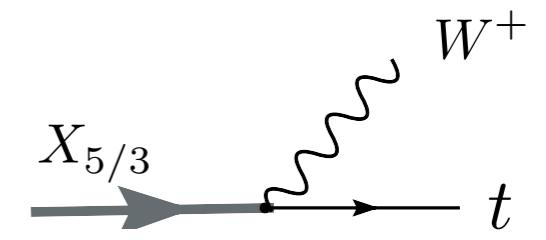
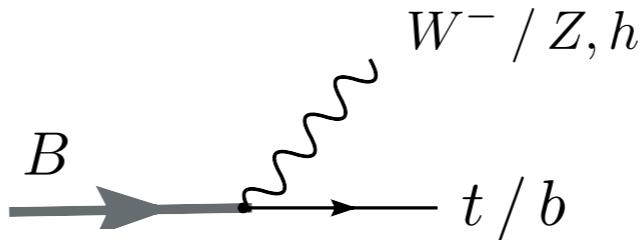
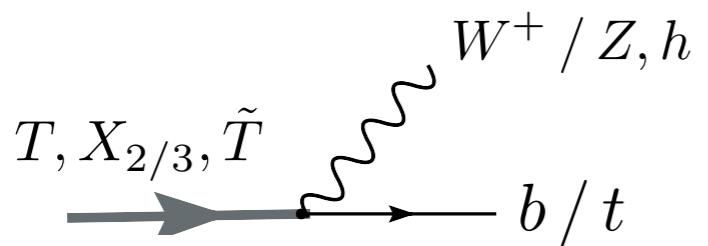


**Single**

**Double**

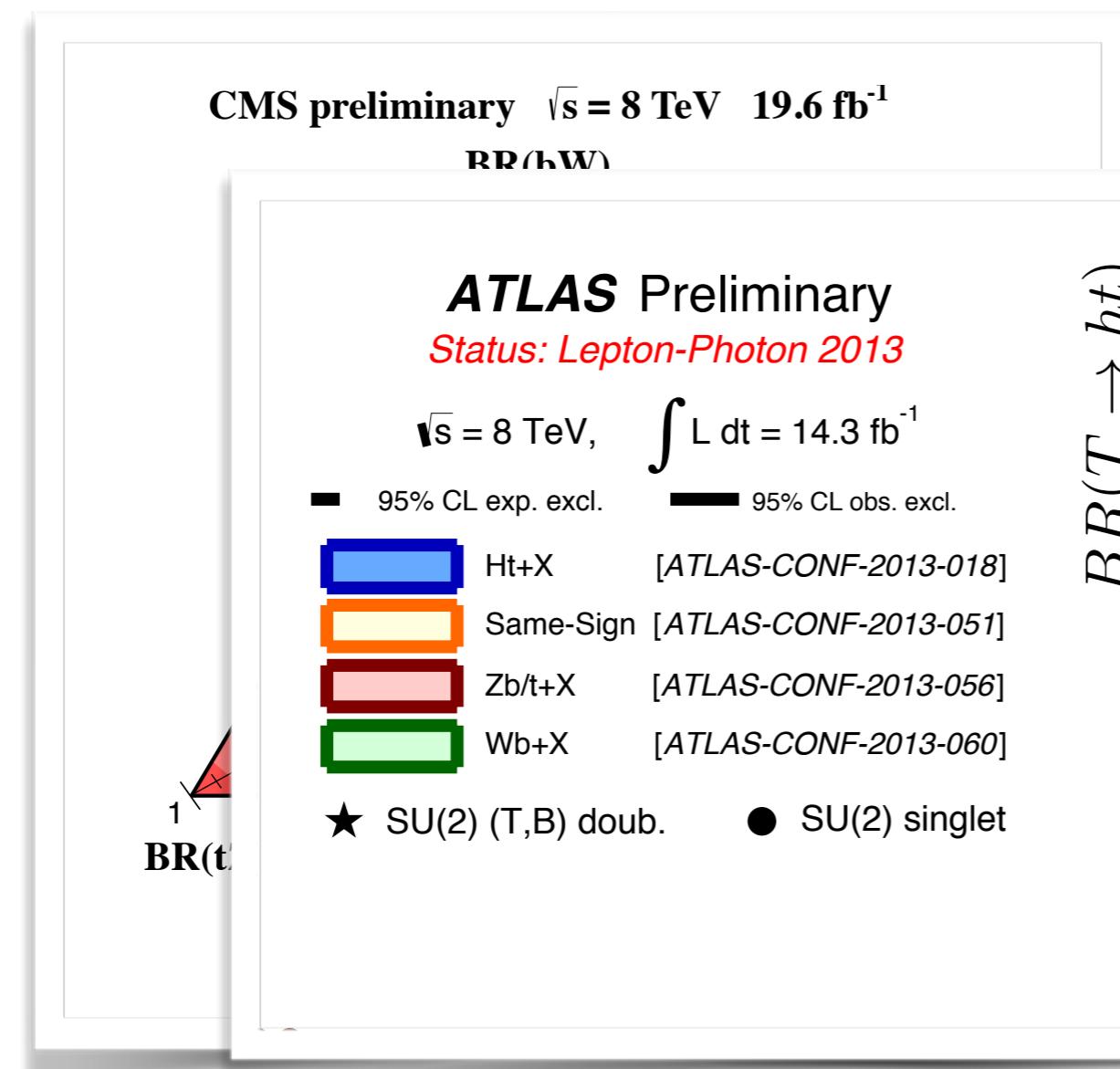
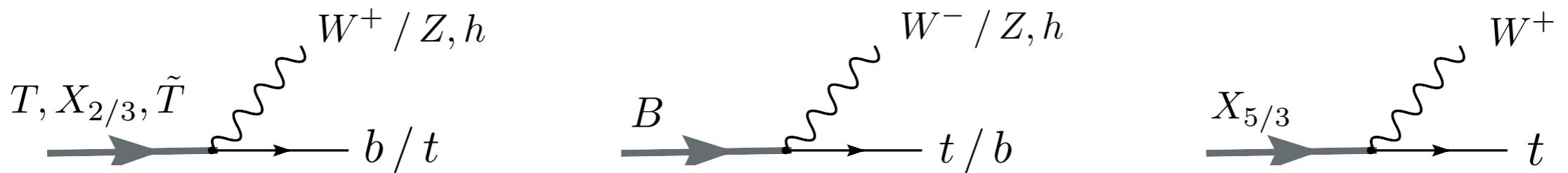


# Decay modes

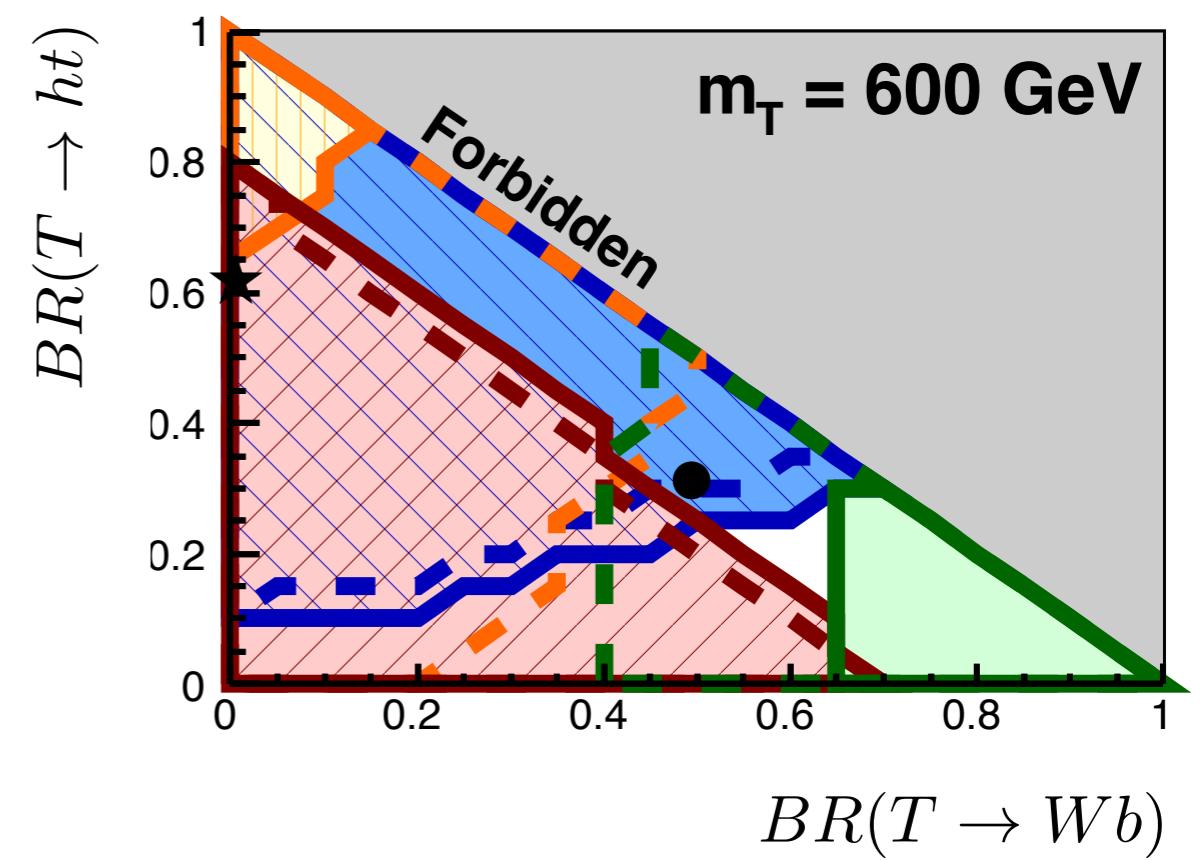


Current limits  
 $> 700 - 800 \text{ GeV}$

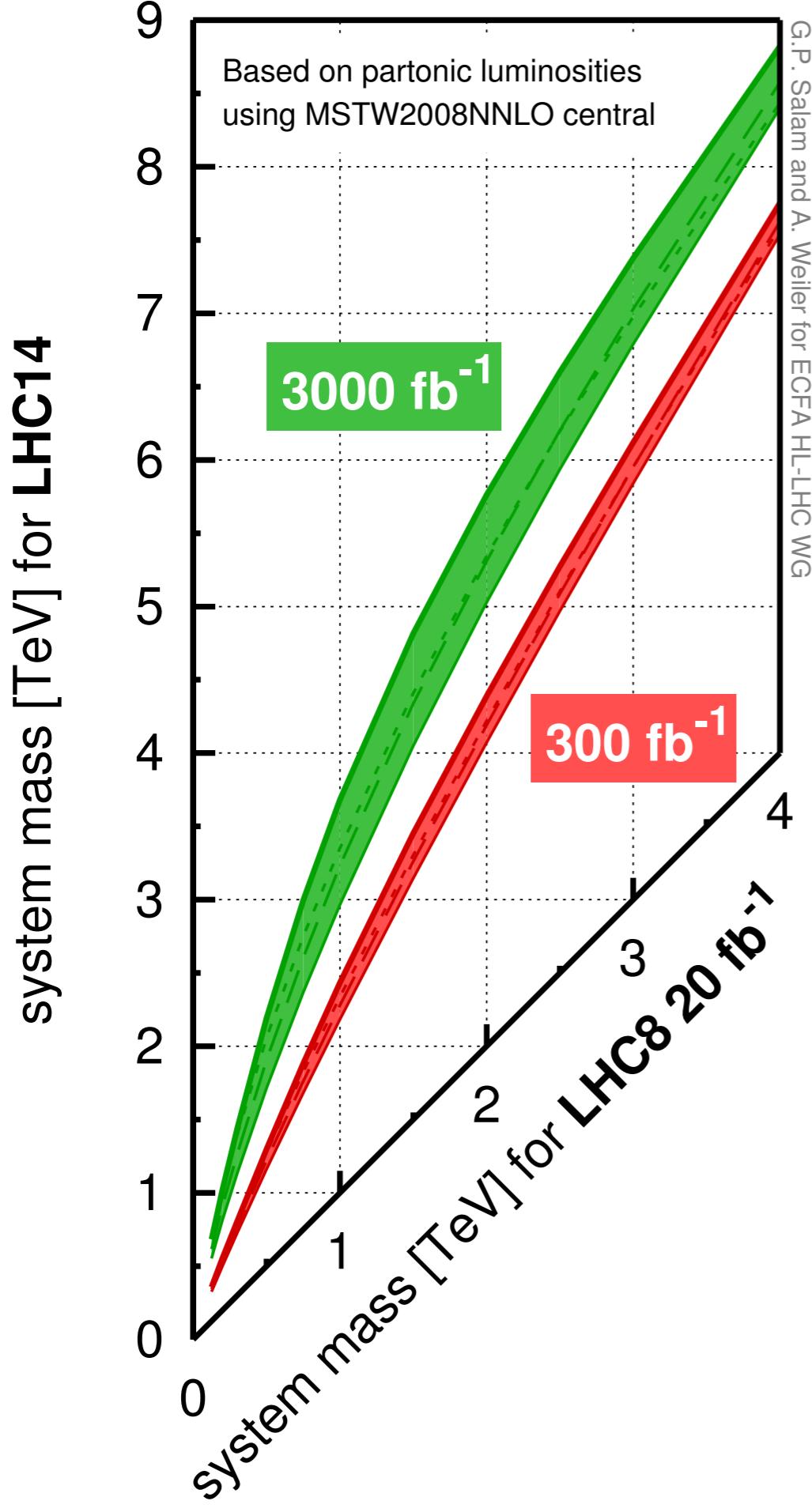
# Decay modes



**Current limits**  
 $> 700 - 800 \text{ GeV}$



# Outlook



—  $\Sigma\Sigma$   
- - -  $\Sigma g$   
- · -  $\Sigma_i q_i \bar{q}_i$   
—  $gg$

A lot of juice  
left in the LHC!

# Conclusions

The battle for a natural resolution of the hierarchy problem goes on, **top partner searches are at the frontier**

LHC<sub>I4</sub> will be decisive:  
2 × energy, sensitive to 4 × tuning

“Absence of evidence is not evidence of absence”,  
still: some experimental guidance would be nice.