



## $t\bar{t}$ production with N-jets and with jet vetoes at CMS

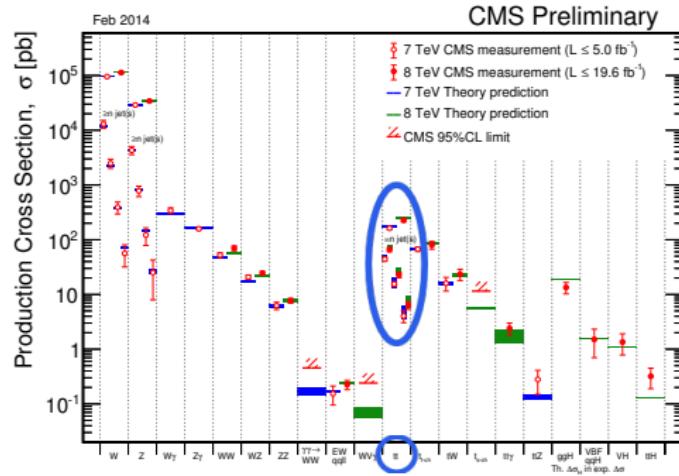
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for the CMS collaboration

DESY

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## Outline

- 1 Introduction
  - 2 Normalised differential  $\sigma_{t\bar{t}}$  as a function of N Jets
  - 3  $\sigma_{t\bar{t}}$  as a function of N additional jets
  - 4 Kinematic distributions for the leading  $p_T$  additional jets
  - 5 Veto on additional jets
  - 6 Summary

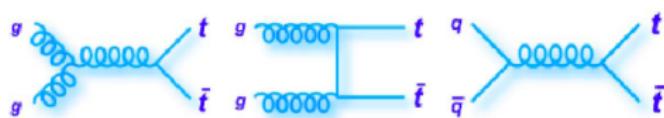


# Motivation

- At LHC energies, about half of  $t\bar{t}$  events are produced with additional hard jets (not coming from the  $t\bar{t}$  decay).
- Precise understanding of these events is important:
  - Test higher-order QCD predictions
  - Anomalous production of  $t\bar{t}$ (+jets) could reveal new physics
  - $t\bar{t}$ +jets is a background for many searches and for  $t\bar{t}H$
- In general, sizeable uncertainty from QCD radiation for many top quark analysis
  - Theory predictions and models need to be tuned and tested with new measurements
- Large samples of  $t\bar{t}$  events provide a great opportunity to study the details of the production mechanisms
  - Potential of constraining QCD radiation at the scale of the top quark mass

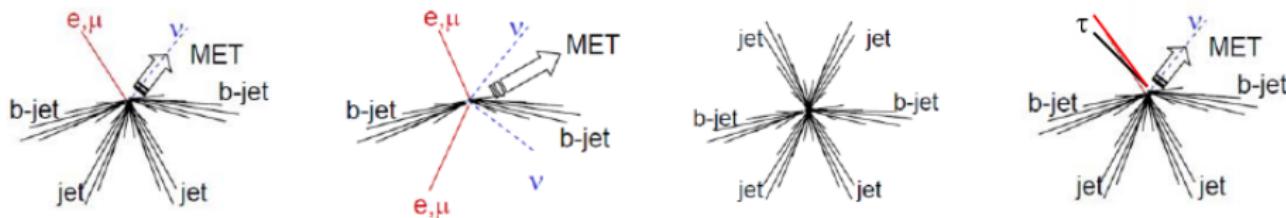
# Top quark production and decay

$t\bar{t}$  production mainly by gluon fusion at LHC ( $\sim 80\%$  at 7-8 TeV)



W decay defines final state:  
Top Pair Decay Channels

|              |               |              |               |                       |
|--------------|---------------|--------------|---------------|-----------------------|
| $t\bar{t}$   | electron+jets | muon+jets    | tau+jets      | all-hadronic          |
| $t^-\tau^+$  | $e\tau$       | $\mu\tau$    | $\tau\tau$    | tau+jets              |
| $t^-\mu^+$   | $e\mu$        | $\mu\mu$     | $\tau\mu$     | muon+jets             |
| $t^-\bar{e}$ | $e\bar{e}$    | $\mu\bar{e}$ | $\tau\bar{e}$ | electron+jets         |
| W decay      | $e^+$         | $\mu^+$      | $\tau^+$      | $u\bar{d}$ $c\bar{s}$ |



Semileptonic [e/ $\mu$ ]:  
BR $\sim 30\%$  and  
manageable BG (ie.  
 $W+jets$ )

Dileptonic [e/ $\mu$ ]:  
BR $\sim 5\%$  and small  
BG (ie. DY+jets)

All-jets: BR $\sim 46\%$   
but largest BG (ie.  
QCD multijet)

$\tau+jets$ : BR $\sim 15\%$

# Introduction

Present studies of  $t\bar{t}$ +jets with 7 TeV data, both in the dilepton and the lepton+jets channels, and 8 TeV data in the dilepton channels.

- Measurements performed:

- Differential cross-section measurement in the dilepton and l+jets channels as a function of jet multiplicity
- l+jets:  $t\bar{t}$  production as a function of the additional jet multiplicity.
- dilepton: properties of additional jets,  $t\bar{t}$  production with a veto on additional jet activity.

→ Measurements in visible phase space, corrected to particle level.

- 7 TeV results: [arXiv:1404.3171](https://arxiv.org/abs/1404.3171), submitted to EPJC (lepton+jets, dilepton channels)
- 8 TeV results: [CMS-PAS-TOP-12-041](#) (dilepton channel)

# Generator setups for $t\bar{t}$ at CMS

- Matrix Element + Parton Shower generators
  - Better description of high multiplicities
  - Initial and final state radiation (ISR/FSR) modelling via ME from assumed  $Q^2$  variation
  - Matching procedure to remove double counting between partons produced by ME and PS
  
- Next to Leading Order generators
  - More accurate in normalisation
  - Smaller uncertainty on  $Q^2$

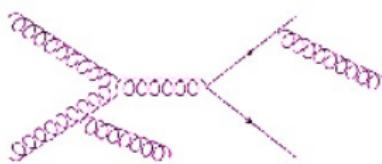
| Matrix element | Shower & Hadronization | PDF                            | Tune                      |
|----------------|------------------------|--------------------------------|---------------------------|
| MadGraph v5    | Pythia 6               | cteq6l                         | Z2 (7 TeV)<br>Z2* (8 TeV) |
| Powheg         | Pythia 6               | cteq6m (7 TeV)<br>CT10 (8 TeV) | Z2 (7 TeV)<br>Z2* (8 TeV) |
| MC@NLO v3.4    | Herwig 6 + Jimmy       | cteq6m                         | default tune              |

Top mass:  
 $m_t = 172.5 \text{ GeV}$

# Radiative corrections

- The  $Q^2$  scale variations address two aspects:
  - renormalisation and factorisation scale (ME)
  - amount of ISR/FSR
- For each event,  $Q^2$  is defined as:
  - MadGraph:  $Q^2 = m_t^2 + \sum p_T^2$
  - Powheg/MC@NLO:  $Q^2 = m_t^2$
- Parton showering:
  - shares  $Q^2$  factor  $\alpha_s$  with ME
  - implicitly: starting scale changes with  $\Delta Q^2$
- MadGraph(+Pythia), the default MC, uses:
  - tree-level diagrams for hard radiation and interferences (up to 3 final-state partons for  $t\bar{t}$ )
  - parton showering for soft and collinear region (with Pythia 6.42X)
  - matching with ktMLM (ensures smoothness of  $N \rightarrow N+1$  jet rates), thresholds varied by a factor 0.5 and 2.0 (nominal = 20 GeV)

→ Uncertainty on radiation covered by variations of  $Q^2$  and ME-PS matching



# Event selection

## Dilepton

- ➊ Dilepton triggers
- ➋ At least two isolated leptons ( $p_T > 20 \text{ GeV}$ ,  $|\eta| < 2.4$ ), opposite sign
- ➌  $\geq 2$  jets (anti- $kT$ ,  $R < 0.5$ ) with  $p_T > 30 \text{ GeV}$ ,  $|\eta| < 2.4$
- ➍ QCD veto:  
 $M_{II} > 12\text{-}20 \text{ GeV}$
- ➎ In  $ee$ ,  $\mu\mu$ : Z veto  
 $(76 < M_{II} < 106 \text{ GeV})$ ,  $E_T^{miss} > 30\text{-}40 \text{ GeV}$
- ➏ At least one b-tagged jet

## Lepton+jets

- ➊ Single muon or electron+jets trigger
- ➋ One isolated lepton ( $p_T > 30 \text{ GeV}$ ,  $e: |\eta| < 2.5$ ,  $\mu: |\eta| < 2.1$ )
- ➌  $\geq 3$  jets (anti- $kT$ ,  $R < 0.5$ ) with  $p_T > 35 \text{ GeV}$ ,  $|\eta| < 2.4$   
 $(\geq 4$  jets with  $p_T > 30 \text{ GeV}$  - additional jet measurement)
- ➍ Loose lepton veto in both channels
- ➎ At least two b-tagged jets

# Selection and analysis strategy

## Dilepton channels

- Event reconstruction: Kinematic reconstruction of the  $t\bar{t}$  system
- Background estimation:
  - ◊  $Z/\gamma^*$ +jets estimated from data
  - ◊ Other BGs (single top, dibosons, etc) estimated from MC

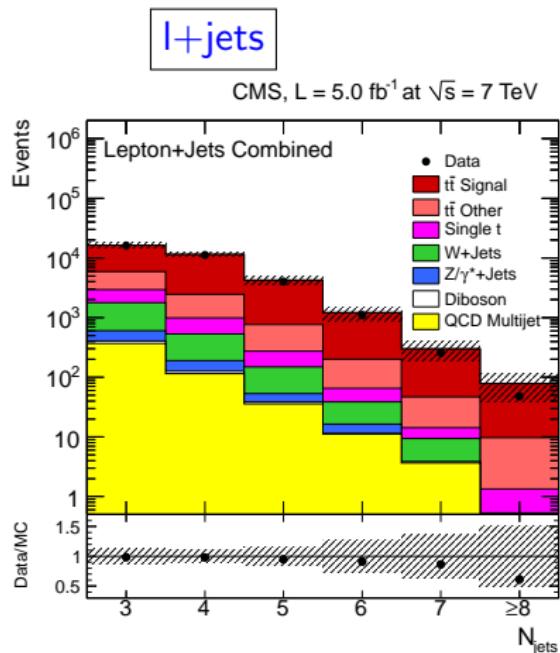
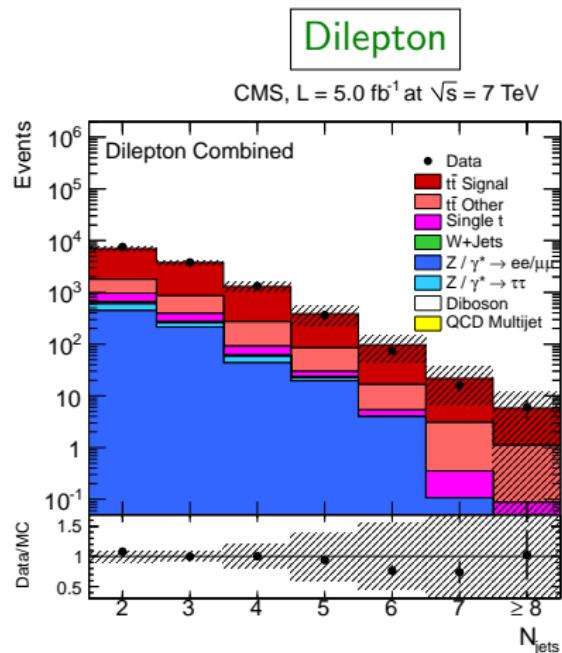
## Lepton+jets channels

- Background estimation
  - ◊ W+jets estimated from data
  - ◊ QCD: data driven
  - ◊ Single top,  $Z/\gamma^*$ +jets and diboson are from MC

→ **Signal:**  $t\bar{t}$  MadGraph+Pythia (normalised to NNLO+NNLL)

# Control Plots: Reconstructed jet multiplicity

7 TeV, dilepton:  $p_T > 30$  GeV, I+jets:  $p_T > 35$  GeV



Good description of data within uncertainties. (Similar description with 8 TeV data)

# Normalised differential cross sections

$$\frac{1}{\sigma_{t\bar{t}}} \frac{d\sigma^i}{dN_j} = \frac{1}{\sigma_{t\bar{t}}} \frac{x^i}{\Delta_X^i L}$$

- $x^i$  number of events after background subtraction, corrected for detector efficiencies, acceptances and migration to particle level (regularised unfolding).
- $\sigma_{t\bar{t}}$  inclusive  $t\bar{t}$  cross section in the same phase space (visible).
- $\Delta_X$ : bin width ( $=1$ )

Measurement done in the visible phase space:

- $p_T^l > 20(30)$  GeV,  $|\eta^\mu| < 2.4$  (2.1) dilepton (l+jets),  $|\eta^e| < 2.5$
- $p_T^{jet} > 30(35)$  GeV dilepton (l+jets),  $|\eta^{jet}| < 2.4$ , jets required  $\Delta R(j, l) > 0.4$ , b-jets identified by B-hadron

Comparing results to predictions from:

- Different generators (POWHEG+Pythia, MC@NLO+Herwig)
- MadGraph+Pythia with varied  $Q^2$  scale, matching threshold

# Systematic uncertainties

- Sources considered:
  - Jet energy scale and resolution
  - Background estimate
  - Model uncertainties:  $Q^2$  scale (using samples with  $2*Q$ ,  $0.5*Q$ ), jet-parton matching threshold (threshold halved/doubled), hadronisation model, the color reconnection modelling and PDF
  - Other sources: luminosity, pileup, b-tagging, lepton identification and trigger efficiencies
- Uncertainties determined individually for each bin.
- Normalised cross sections: bin-to-bin correlated uncertainties cancel (luminosity, flat SF, etc.), only shape uncertainties contribute (shape variation for b-tag, BG, scale, hadronisation etc.)

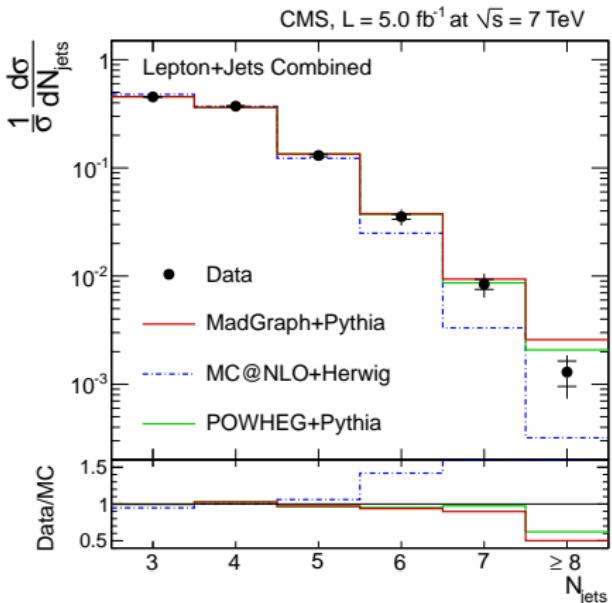
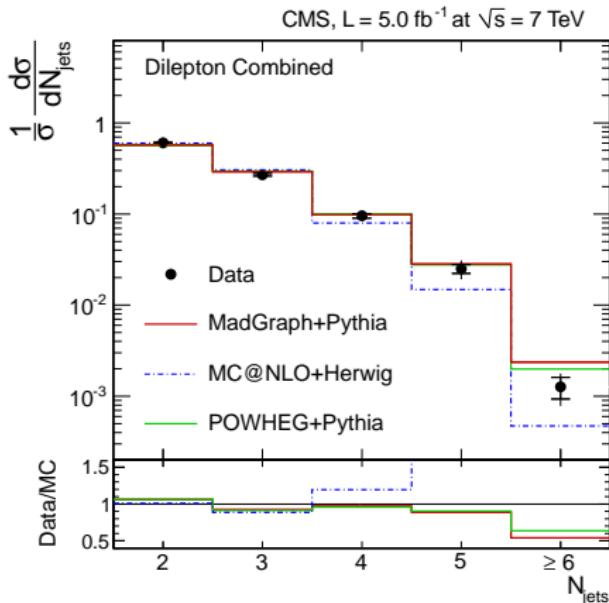
Total syst. uncertainty varies from 3-6% in the low multiplicity bins to 20-30% for the highest multiplicities.

Most important sources: JES and  $Q^2$  scale and ME/PS Matching

# Normalised diff. $\sigma_{t\bar{t}}$ as a function of NJets

Results 7 TeV: dilepton and l+jets channels

- ◊ MadGraph+Pythia, POWHEG+Pythia provide a reasonable description
- ◊ MC@NLO+Herwig doesn't describe large jet multiplicities

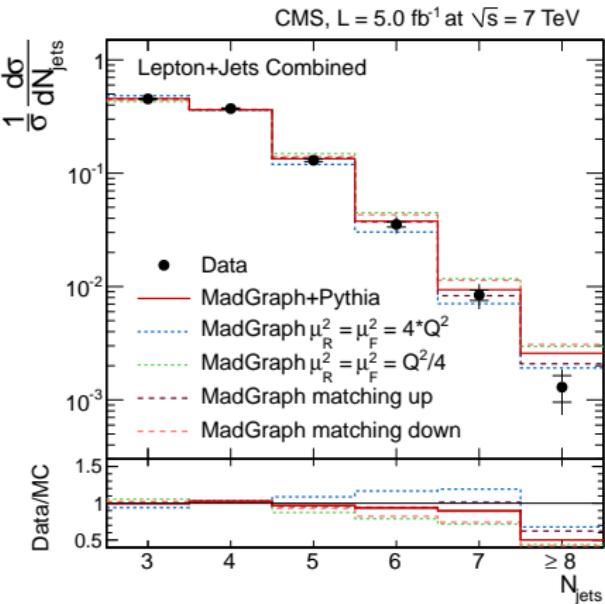
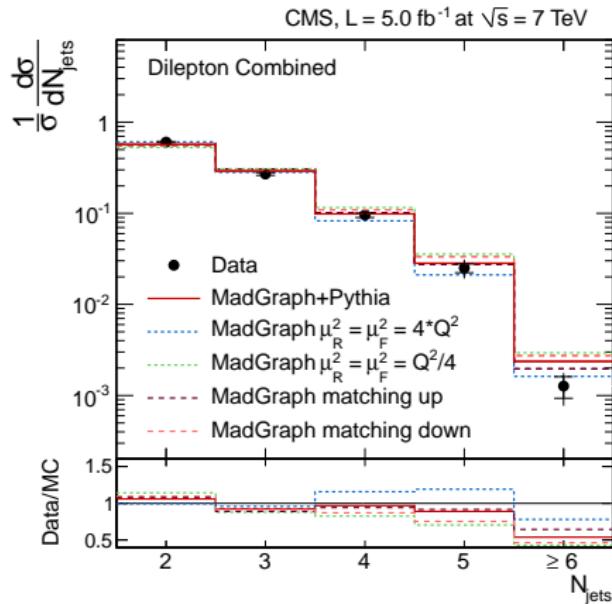


Results are consistent among channels (dilepton, l+jets)

# Normalised diff. $\sigma_{t\bar{t}}$ as a function of NJets

Results 7 TeV: dilepton and l+jets channels

- Comparison with MadGraph, varying  $Q^2$  scale and jet/parton matching threshold up and down

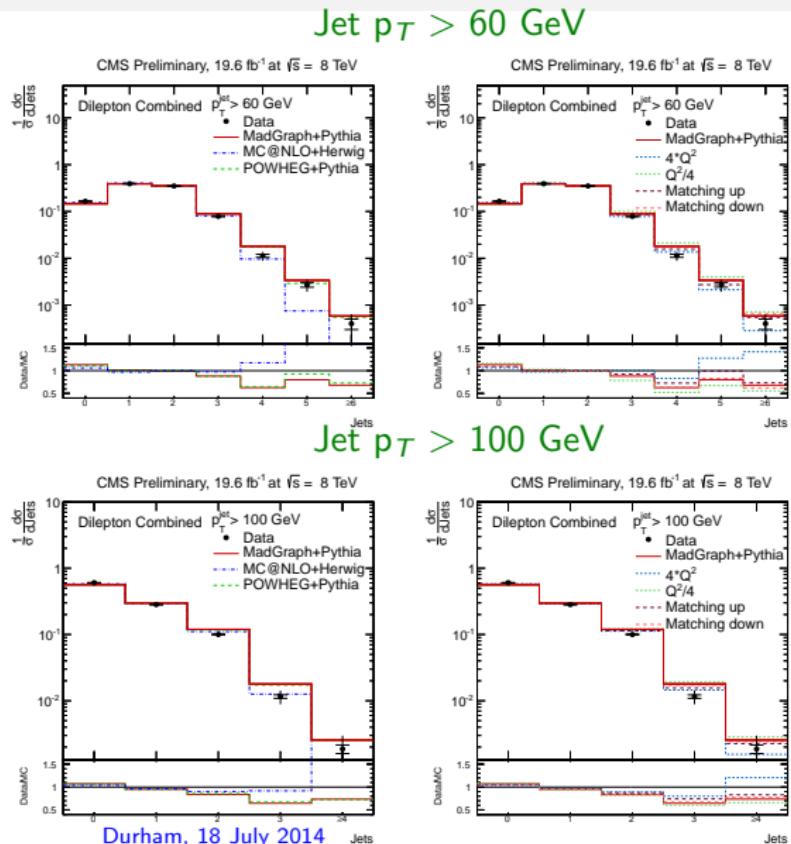


- Choice of lower scale gives slightly worse description of the data.

# Normalised diff. $\sigma_{t\bar{t}}$ as a function of NJets

Results 8 TeV: dilepton for jets  $p_T > 60$  GeV,  $p_T > 100$  GeV

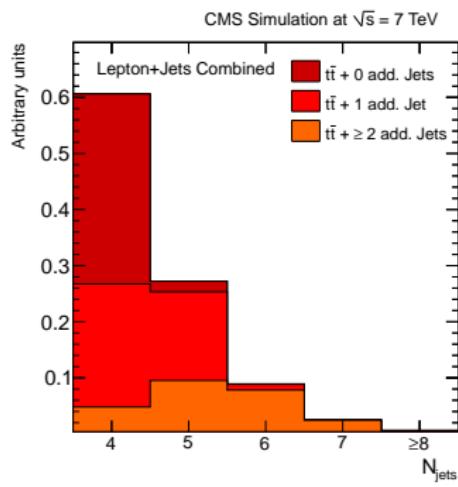
- Larger data samples allow to measure higher  $p_T$
- MadGraph+Pythia, POWHEG+Pythia provide a reasonable description, MC@NLO+Herwig describes data better for high jet- $p_T$ .
- Choice of lower  $Q^2$  scale gives slightly worse description of the data.
- Results consistent with 7 TeV measurement.



# Cross section as a function of the additional jet number

7 TeV: Lepton+jets channel

- Categorise every  $t\bar{t}$  MC event as a function of the number of generated jets NOT matching any of top decay products (b quarks, light quarks and prompt lepton)
- Jets with  $\Delta R > 0.5$ : additional radiated jets  
→ classification of events in  $t\bar{t}+0,1,\geq 2$  additional jets
- Extracting rates of these  $t\bar{t}$  classes from data via a template fit
- **Selection:** similar to previous section, but selection events with at least 4 jets with  $p_T > 30$  GeV.



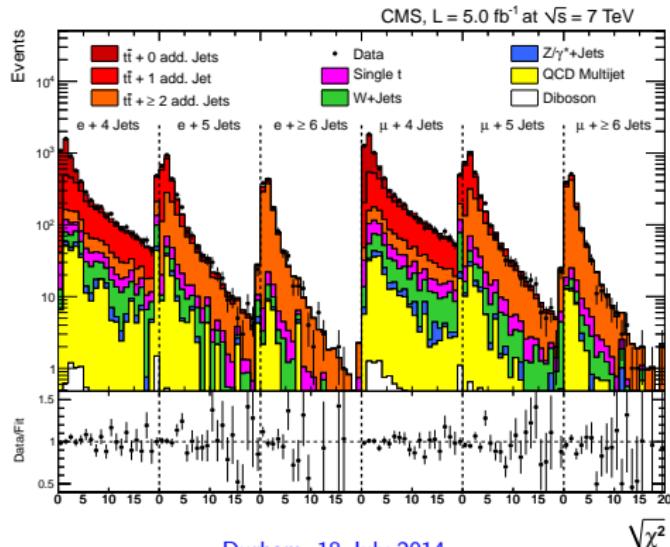
# Template fit results

- Simultaneous fit to data in three jet multiplicity bins in  $e/\mu + \text{jets}$  channels
- Templates built from smallest  $\chi$  of any jet combination (using b-tag info)

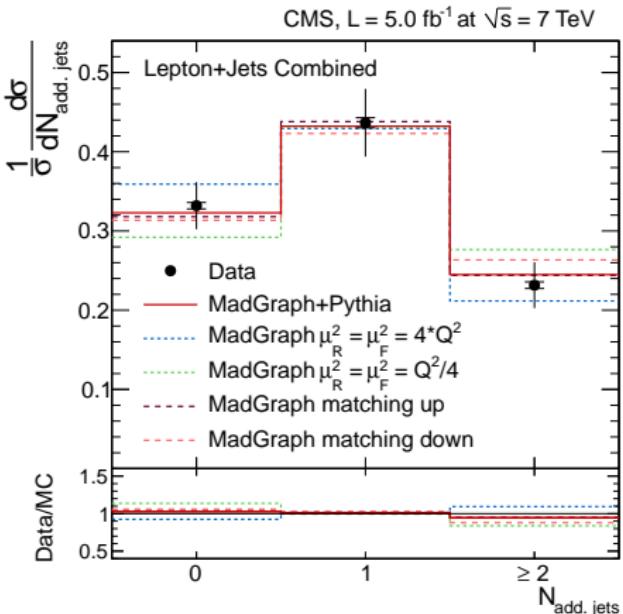
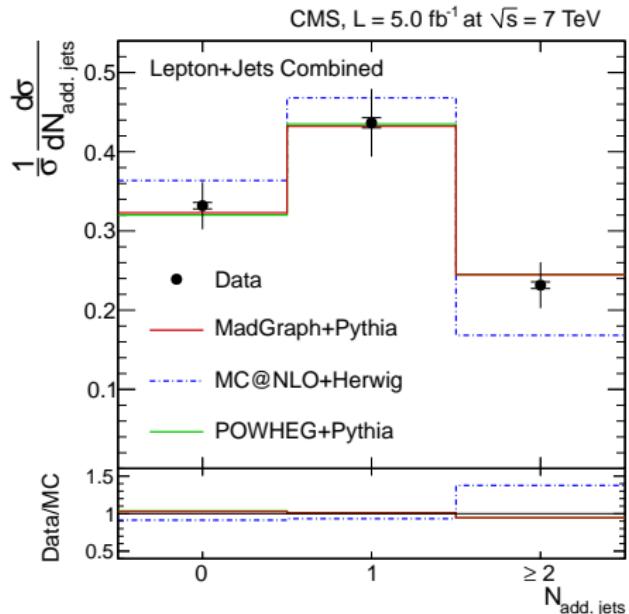
$$\chi = \sqrt{\left( \frac{m_{W\text{had}}^{\text{rec}} - m_{W\text{had}}^{\text{true}}}{\sigma_{W\text{had}}} \right)^2 + \left( \frac{m_{t\text{had}}^{\text{rec}} - m_{t\text{had}}^{\text{true}}}{\sigma_{t\text{had}}} \right)^2 + \left( \frac{m_{t\text{lep}}^{\text{rec}} - m_{t\text{lep}}^{\text{true}}}{\sigma_{t\text{lep}}} \right)^2}$$

from full event reconstruction

- $\chi$  lower if all jets from the  $t\bar{t}$  decay are reconstructed



# Diff. cross section: additional jet multiplicity

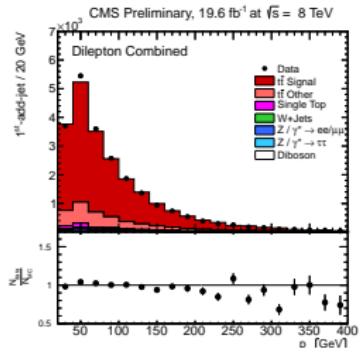
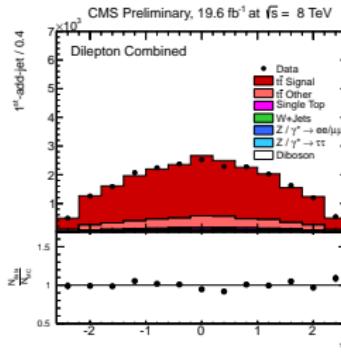


- Systematic uncertainties evaluated with pseudoexperiments
- Best agreement with **MadGraph+Pythia** and **POWHEG+Pythia**, **MC@NLO+Herwig** shows discrepancies

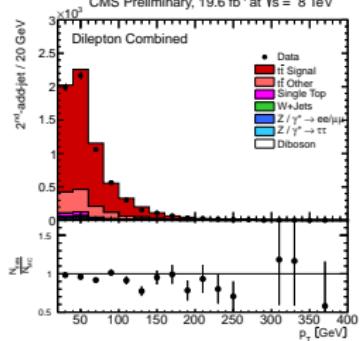
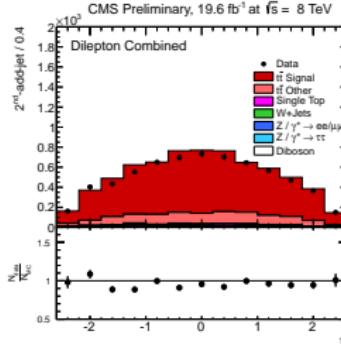
# Kinematic distributions for the leading $p_T$ additional jets

- Additional jets defined as the jets in visible phase space NOT selected by the kinematic reconstruction

$1^{st}$  leading add. jet



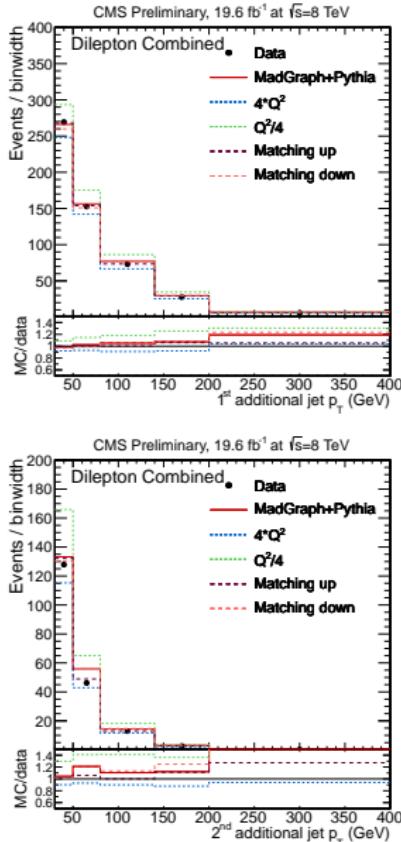
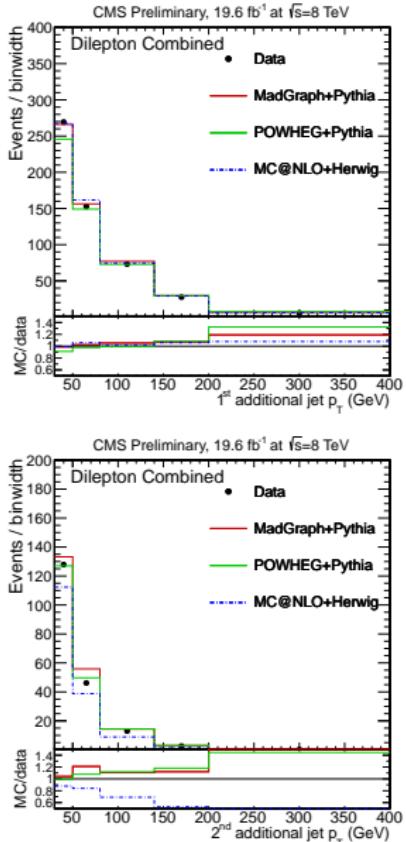
$2^{nd}$  leading add. jet



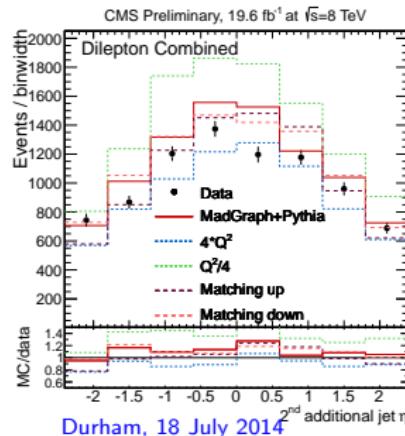
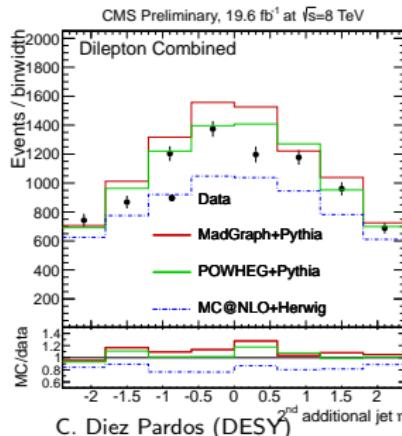
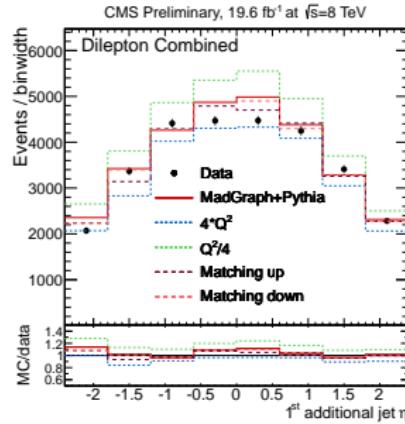
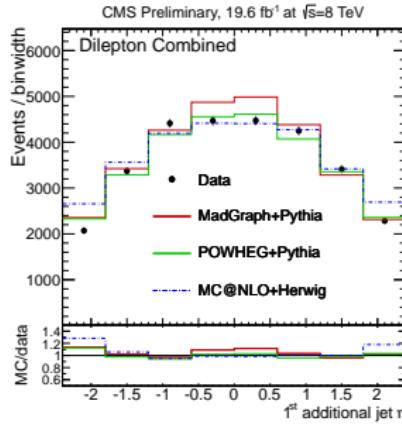
Good agreement between data and MC (similar to 7 TeV results)

# $p_T$ of 1<sup>st</sup> and 2<sup>nd</sup> leading additional jets (8 TeV)

- Comparison with various theory predictions
- Distributions at reconstructed level (no unfolding applied!), background is subtracted using MC predictions
- All predictions normalised to in situ measured cross-section (with MadGraph)



# $\eta$ of 1<sup>st</sup> and 2<sup>nd</sup> leading additional jets (8 TeV)



- ◊ MadGraph+Pythia, Powheg+Pythia provide a reasonable description
- ◊ MC@NLO+Herwig fails to describe 2<sup>nd</sup> add. jet distributions
- ◊ Lower scale ( $Q^2$ ) sample predicts lower yields than data

# $t\bar{t}$ production with a veto on additional jet activity

*gap fraction - dilepton channel*

- Jet activity arising from quark and gluon radiation produced with the  $t\bar{t}$  system is quantified with a jet veto

$$f(p_T) = \frac{N(p_T)}{N_{total}}$$

$$f(H_T) = \frac{N(H_T)}{N_{total}}$$

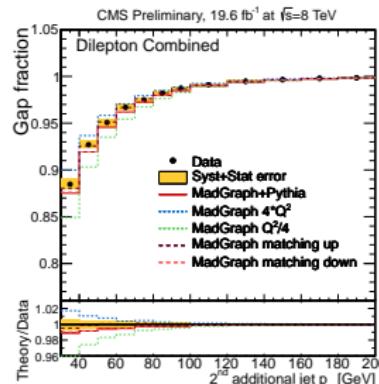
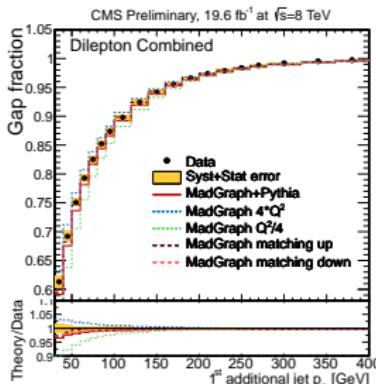
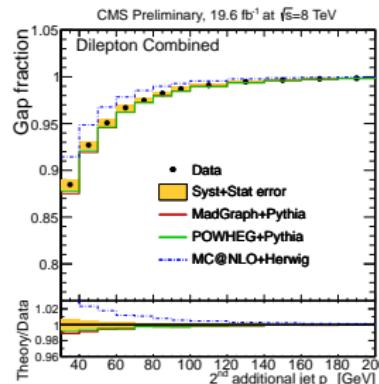
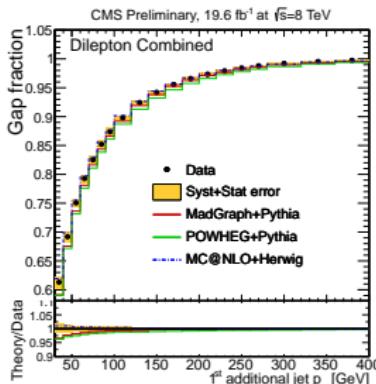
- $N(p_T)$  are the events without 1 (2) additional jets with  $p_T$  above a threshold
- Sensitive to the (2<sup>nd</sup>) leading- $p_T$  emission.

- $N(H_T)$  is the number of events in which the scalar sum of the  $p_T$  of the additional jets is less than a certain threshold,  $H_T = \sum p_T^{add.jets}$
- Sensitive to all hard emission accompanying  $t\bar{t}$  system

Gap fraction in data corrected for detector effects to particle level using MadGraph: for each value of the threshold the ratio of the “true” and “reconstructed” simulated gap fraction is computed and applied to data.

# Gap fraction ( $1^{st}$ add. jet, $2^{nd}$ add. jet $p_T$ )

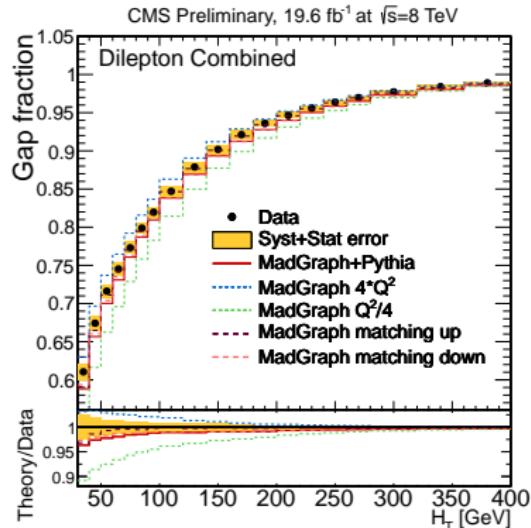
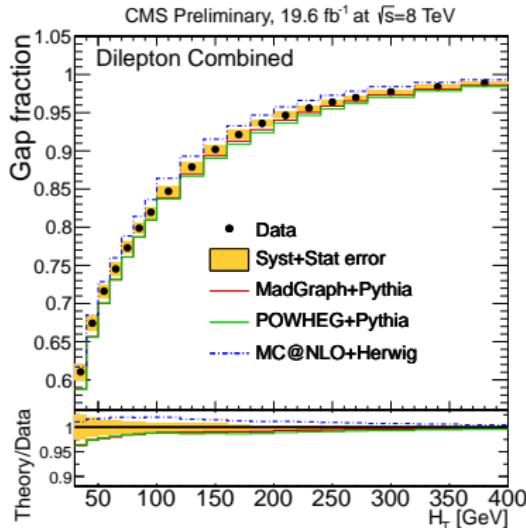
## Full pseudorapidity range



- ◊ MadGraph+Pythia, Powheg+Pythia provide a reasonable description for both jet- $p_T$  threshold.
- ◊ Gap fraction as a function of  $1^{st}$  add. jet  $p_T$  better described with MC@NLO+Herwig.
- MadGraph with decreased  $Q^2$  scale predicts lower gap fraction values than the measured ones.

# Gap fraction as a function of $H_T$

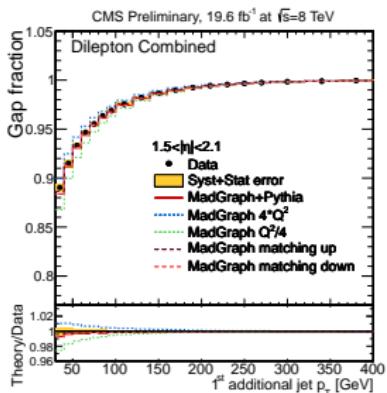
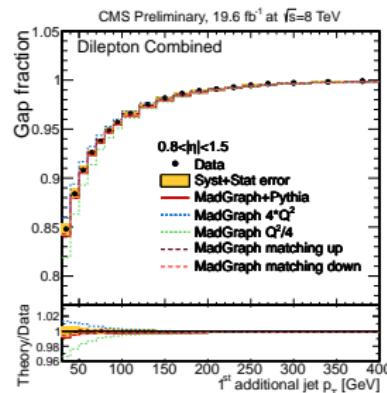
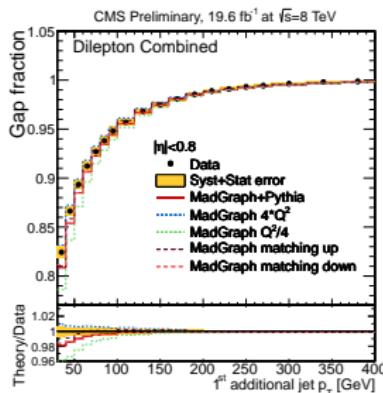
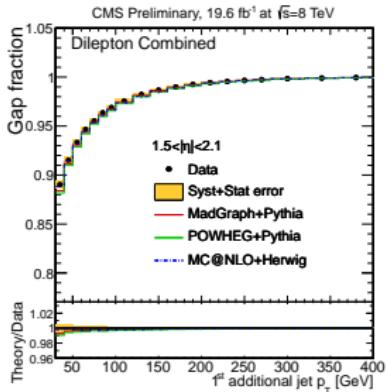
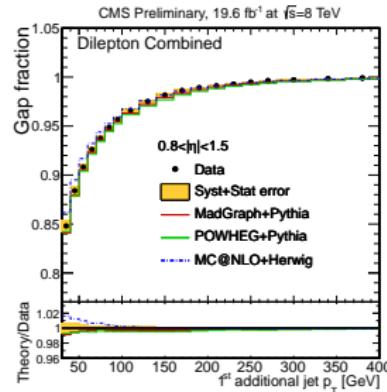
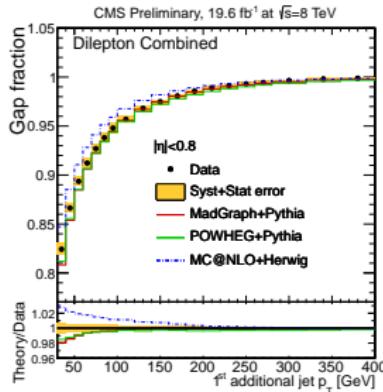
$$H_T = \sum p_T^{\text{add. jets}}$$



- ◊ Reasonable agreement between **MadGraph+Pythia**, **Powheg+Pythia** and data.
- ◊ Gap fraction slightly better described by MadGraph with increased matching threshold.

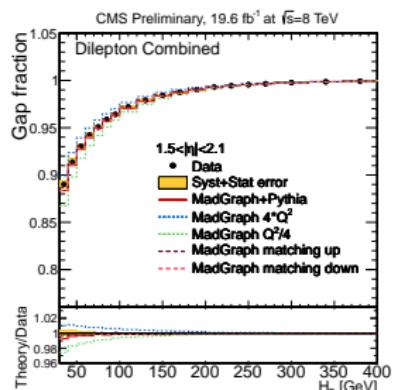
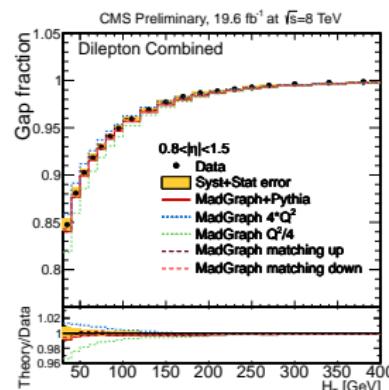
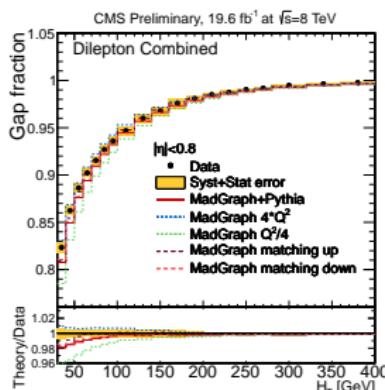
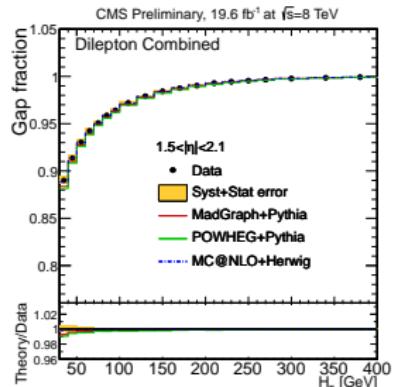
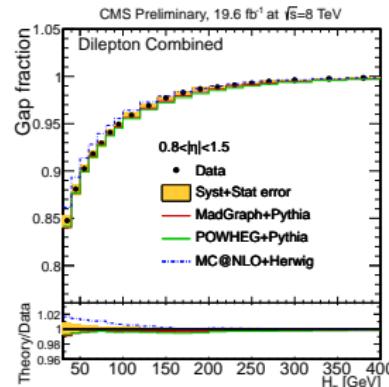
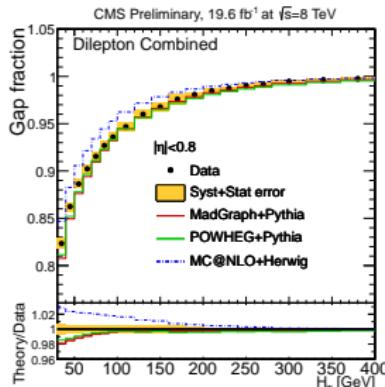
# Gap fraction: $p_T$ first additional jet

## Different rapidity ranges



# Gap fraction as a function of $H_T$

## Different rapidity ranges



# Summary and Outlook

- Presented  $t\bar{t}$  production with additional jet activity in the 1+jets and in the dilepton channels.
  - ◊ Normalised  $t\bar{t}$  production cross section as a function of jet multiplicity and additional jet multiplicity
  - ◊ Kinematics of the additional jets
  - ◊ Gap fraction
- Compared to different MCs and parameter variations from Madgraph.
- In general, good agreement between data-MC observed with different predictions.
- Consistent result among channels and measurements.
- Often, experimental precision smaller than spread due to parameter variation. → Variations could be reduced
- Working towards comparisons with other predictions (Powheg+Herwig) and NLO+Parton Showering multileg generators like aMC@NLO.

# Questions

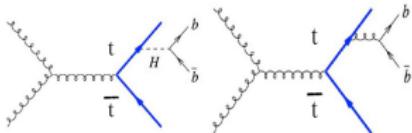
- Is it actually feasible/meaningful to constrain the MC radiation parameters ( $Q^2$ , matching) with measurements?
- Which other measurements would be useful?
  - Additional jets: diff. xsec as a function of kin. variables,  $H_T$
  - ratio  $N_{\text{jets}} \geq 2 / N_{\text{jets}} \geq 1$  as function of  $p_T^{tt}$ ,  $\langle N_{\text{Jet}} \rangle$  vs  $p_T^{tt}$  ?
  - ???

# BACK UP

# $t\bar{t} + b\bar{b}$ : ratio of b- to light-flavour jets

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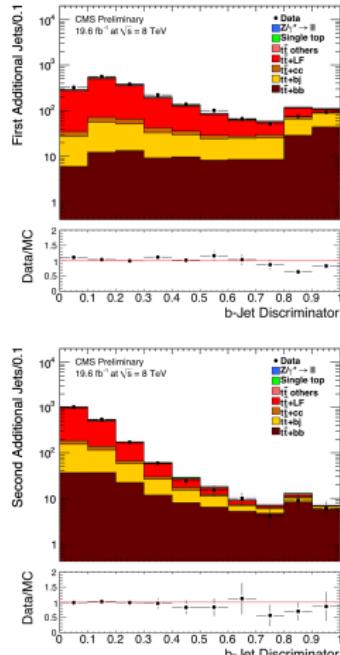
- Comparison with NLO QCD calculations
- Irreducible BG for  $t\bar{t} + H(b\bar{b})$



- Measure ratio  $\sigma(t\bar{t}b\bar{b})/\sigma(t\bar{t}jj)$ : large cancellation of uncertainties

- Selection: dilepton events with  $\geq 4$  jets with  $p_T > 20$  (40) GeV,  $\geq 2$  b-tagged jets
- Signal extraction by fit to the measured b-tagging algorithm discriminators
- Corrected to particle level
- Dominant systematic: mistag efficiency

$R = 0.023 \pm 0.003(\text{stat.}) \pm 0.005(\text{sys.})$  for 20 GeV [MadGraph (Powheg): 0.016 (0.017)]  
 $R = 0.022 \pm 0.004(\text{stat.}) \pm 0.005(\text{sys.})$  for 40 GeV [MadGraph (Powheg): 0.013 (0.014)]



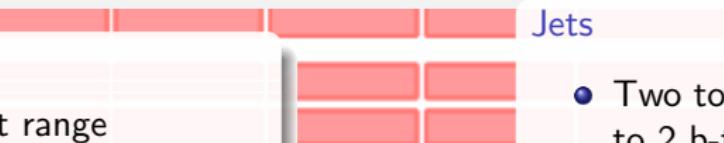
# Top quarks

## MET

- Typical cut range 20-40 GeV, not applied for all analysis (lept+jets, dilepton)

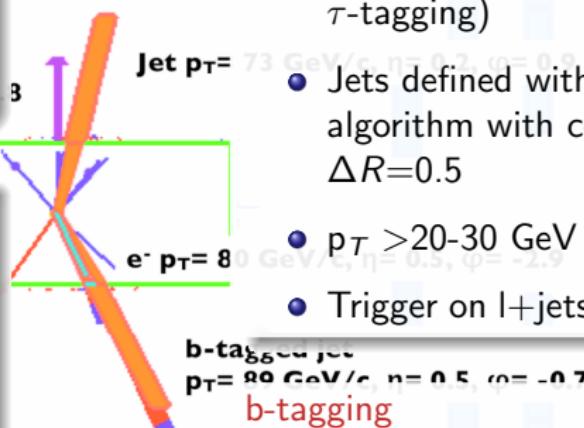
## Leptons

- Up to two high  $p_T$  leptons
  - Isolated, high  $p_T$  from W, soft leptons in b-jets
- With  $p_T > 20 \text{ GeV}$   $|\eta| < 2.5$
- Trigger largely based on leptons (Single/double (isolated) lepton)



## Jets

- Two to six high  $p_T$  jets (up to 2 b-tags, might use  $\tau$ -tagging)
- Jets defined with anti-kT algorithm with cone  $\Delta R=0.5$
- $p_T > 20-30 \text{ GeV}$   $|\eta| < 2.5$
- Trigger on l+jets signatures
- Uses secondary vertices and/or IP information
- Efficiencies and fake rates are calibrated by using data



# Selection and analysis strategy

- Full 2011 data (7 TeV,  $5.0 \pm 0.1 \text{ fb}^{-1}$ ) and 2012 data (8 TeV,  $19.7 \pm 0.1 \text{ fb}^{-1}$ )
- ◊ Signal:  $t\bar{t}$  MadGraph+Pythia (normalised to NNLO+NNLL)
  - For comparison:  
POWHEG+Pythia and MC@NLO+Herwig  
MadGraph+Pythia with varied hadronisation/renormalization scale ( $Q^2$ ) and jet-parton matching threshold.
- ◊ Backgrounds:
  - $Z/\gamma^* + \text{jets}$ : MadGraph+Pythia (dominant BG ee,  $\mu\mu$  channels)
  - $W + \text{jets}$ : MadGraph+Pythia (dominant BG  $l+\text{jets}$ )
  - Single top (s-, tW-channel): POWHEG+Pythia
  - Diboson (WW,WZ,ZZ): Pythia
  - QCD: Pythia (data driven for  $l+\text{jets}$ )

# Selection and analysis strategy

## Dilepton channels

- Event reconstruction: Kinematic reco. underconstrained ( $2\nu$ )
  - ◊  $m_W \equiv 80.4 \text{ GeV}$ ,  $m_t \equiv m_{\bar{t}}$  fixed
  - ◊  $p_T^{\nu_1} + p_T^{\nu_2} = E_T^{miss}$
  - ◊ vary  $m_T$  between 100-300 GeV (1 GeV steps)
  - ◊ prefer solutions with b-tagged jets
  - ◊ choose solution with best reco. neutrino energy w.r.t MC spectrum
- Background estimation:
  - ◊  $Z/\gamma^* + \text{jets}$  estimated from data: The normalisation is determined using the events inside the  $Z$ -peak region, after subtracting the contamination from non- $Z/\gamma^* + \text{jets}$ , derived with  $e\mu$  events.
  - ◊ Other BGs (single top, dibosons, etc) estimated from MC
- Scale Factors: PU, Lepton selection, trigger SF, b-tag SF and kinematic reconstruction

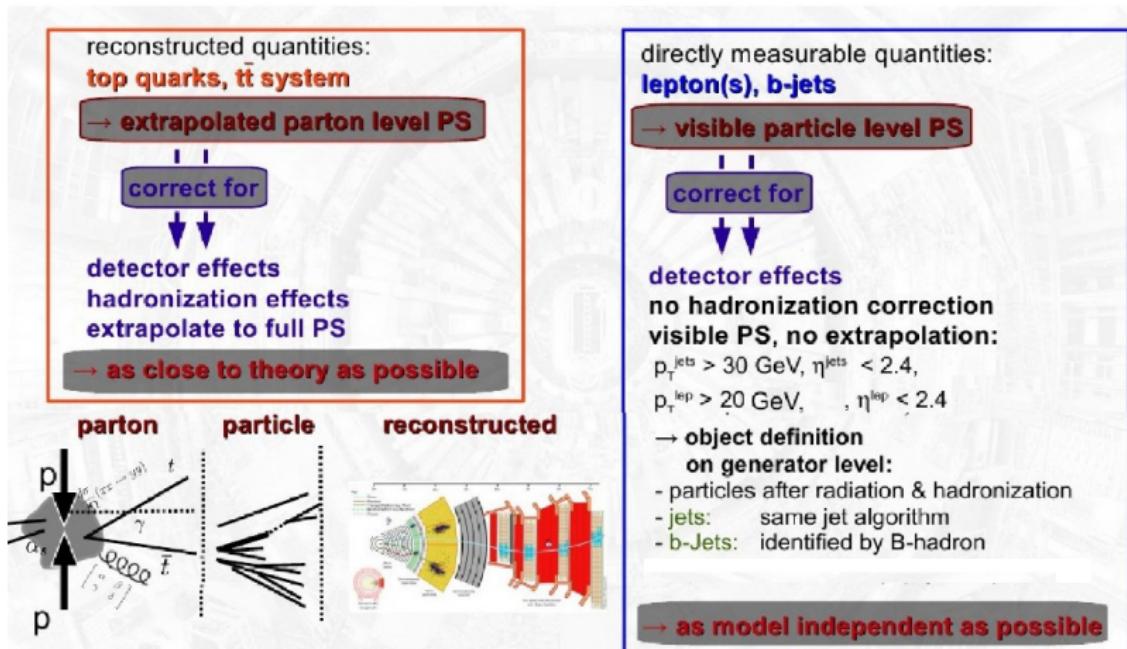
# Selection and analysis strategy

## lepton+jets channels

- Background estimation
  - ◊ W+jets estimated from data:
    - Normalization is from data using charge asymmetry property of W+jets events.
    - Jet multiplicity shape is from MC
    - Additional correction of heavy flavour fraction
  - ◊ QCD: data driven
    - Define sideband (1 b-tag) and signal ( $\geq 2$  b-tag) regions with events with inverted lepton isolation
    - Fit MET from sideband to obtain the QCD normalization parameter
    - Multiply the QCD shape in the signal region by the QCD normalization parameter
  - ◊ Single top,  $Z/\gamma^*$ +jets and diboson are from MC
- Scale Factors: PU, Lepton selection, trigger SF, b-tag SF

# Phase space definitions

- Measurements are presented at particle level in the visible phase space.  
Additionally GenJets must fullfill:  $\Delta R(\text{genJet}, \text{selected leptons}) > 0.4$

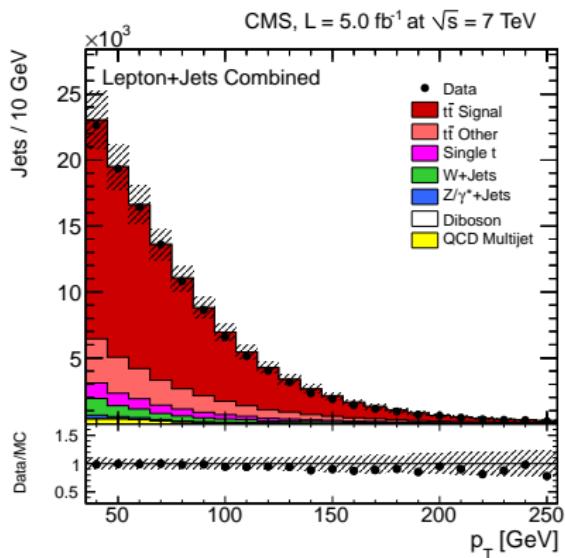
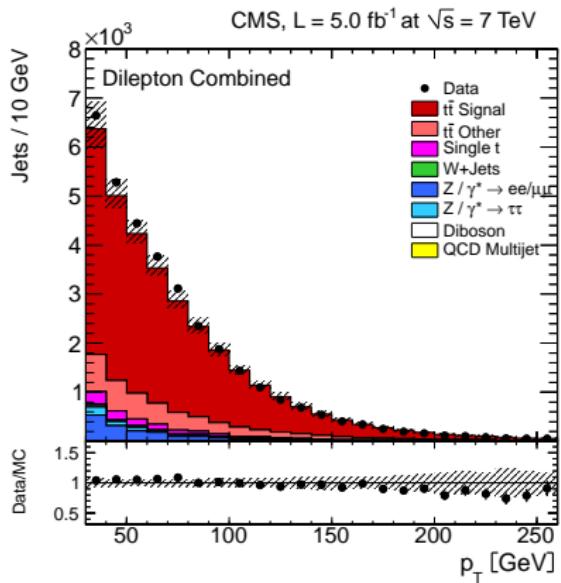


# Control Plots: Jet $p_T$

Dilepton:  $p_T > 30$  GeV, I+jets:  $p_T > 35$  GeV

Dilepton

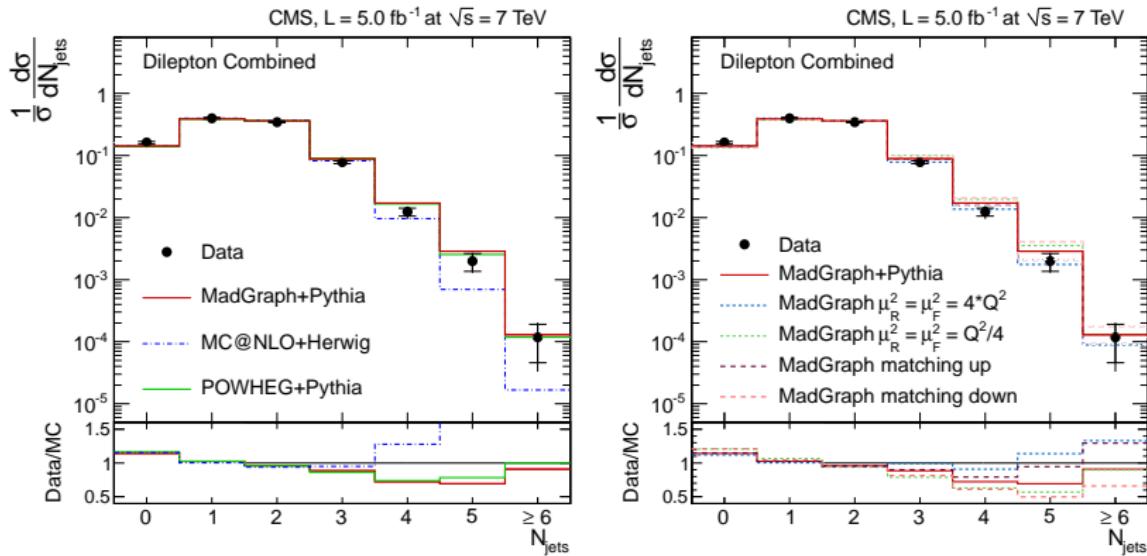
I+jets



Good description of data within uncertainties.

# Results: dilepton channel

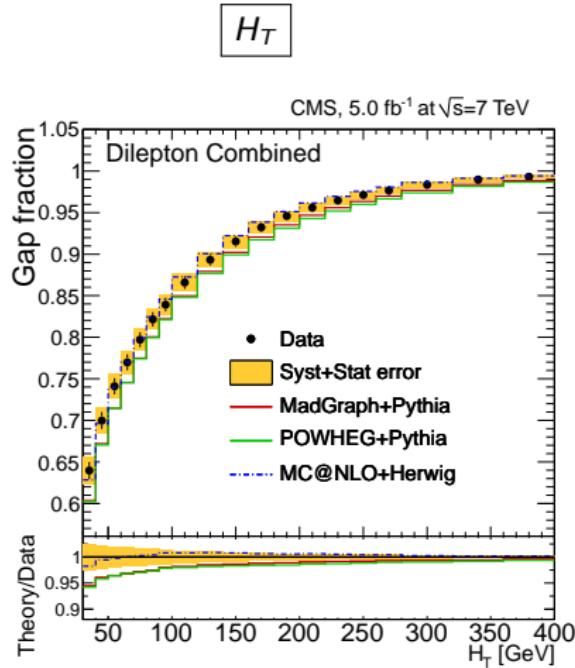
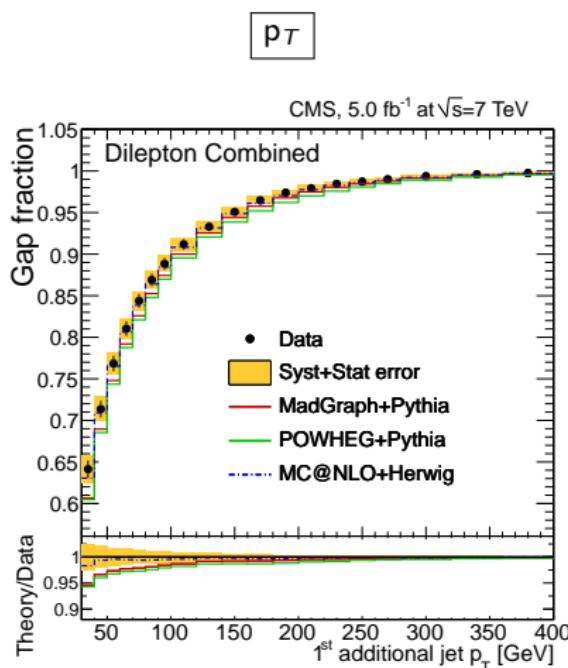
Jet  $p_T > 60$  GeV



- ◊ MadGraph+Pythia, POWHEG+PYTHIA provide a reasonable description
- ◊ MC@NLO+HERWIG doesn't generate large jet multiplicities.
- ◊ Choice of lower scale gives slightly worse description of the data.

# Gap fraction: results 7 TeV

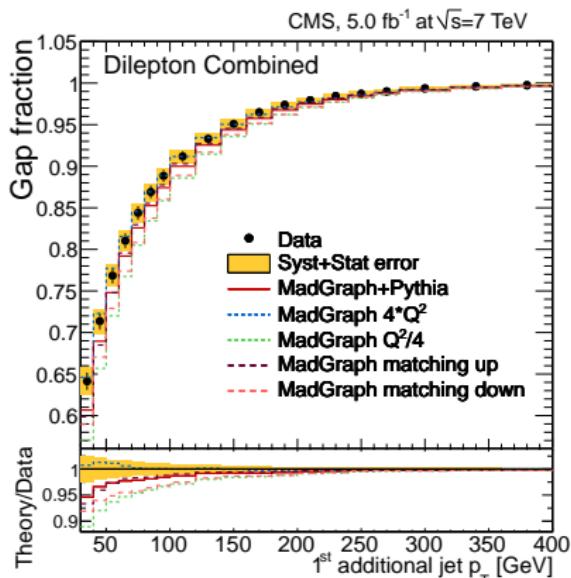
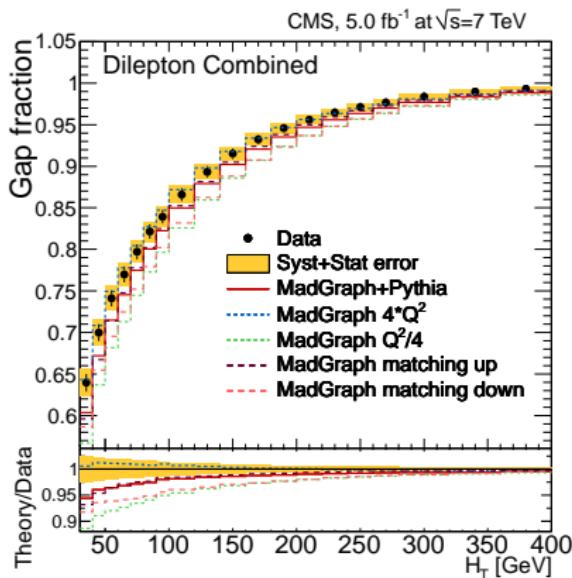
Gap fraction in data corrected for detector effects to particle level using MadGraph



Gap fraction better described by MC@NLO+HERWIG

Dominant systematic uncertainties: JES uncertainty, BG contamination

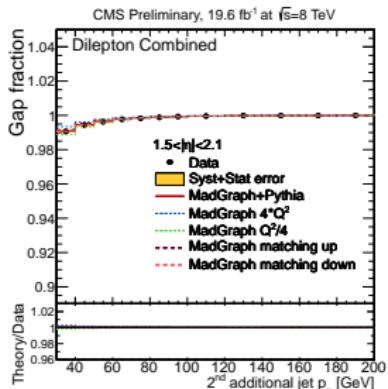
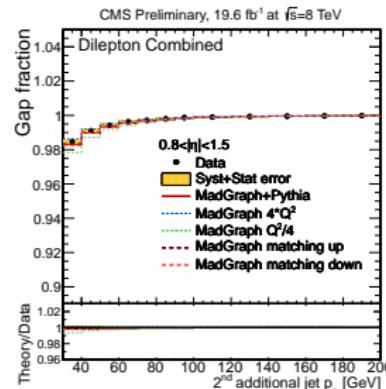
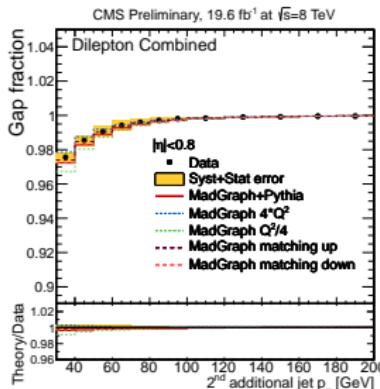
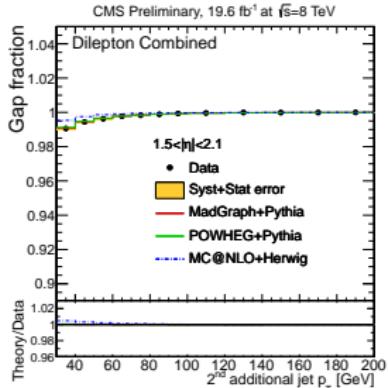
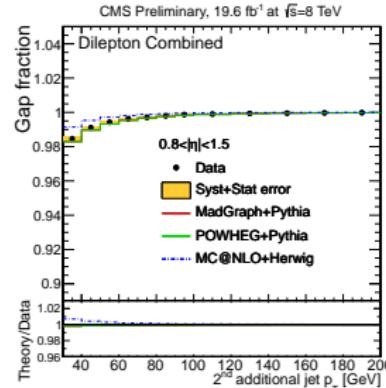
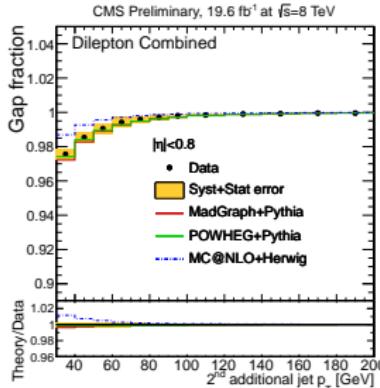
# Gap fraction: results 7 TeV

 $p_T$  $H_T$ 

Decreasing the  $Q^2$  scale, jet-parton matching threshold worsens the agreement with data

# $p_T$ second additional jet

- Gap fraction for different pseudorapidity ranges.

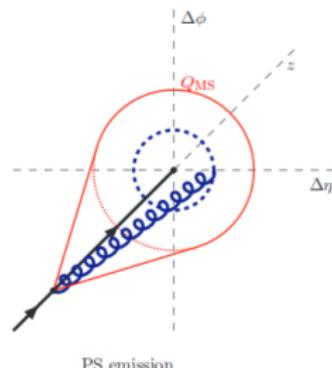
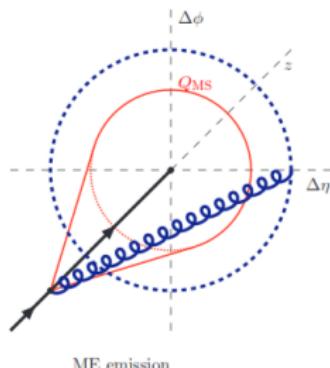


# Matching scale (MadGraph only)

MadGraph uses

- ▶ tree-level diagrams for **hard radiation & interferences** (up to 3 final state partons)
- ▶ parton-showering for **soft & collinear** region (with Pythia 6.42x)
- ▶ matching via **ktMLM** ( $k_T$  instead of cone algorithm)

The idea:



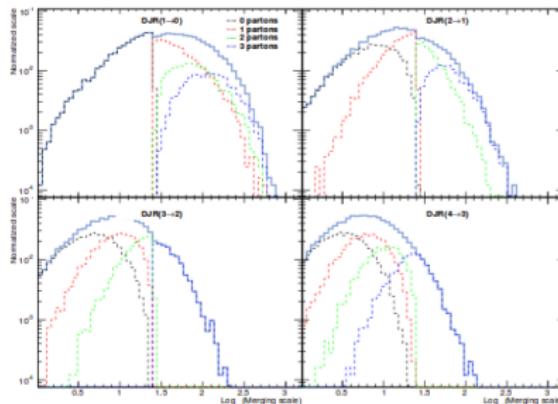
(for illustrative purposes only)



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- ▶ study **smoothness** N-jet vs N+1-jet transitions (y-axis) as function of scale
- ▶ matching **thresholds** ( $xqcut$ ) drives the optimal matching **scale** ( $qcut$ )

- ▶ default  $xqcut = 20$  ( $qcut = 40$ ) for  $t\bar{t} + \text{jets}$
- ▶ thresholds are varied by factor **0.5 to 2.0**

