

Mass effects in $gg \rightarrow H + \text{jet}(s)$ (fixed order)

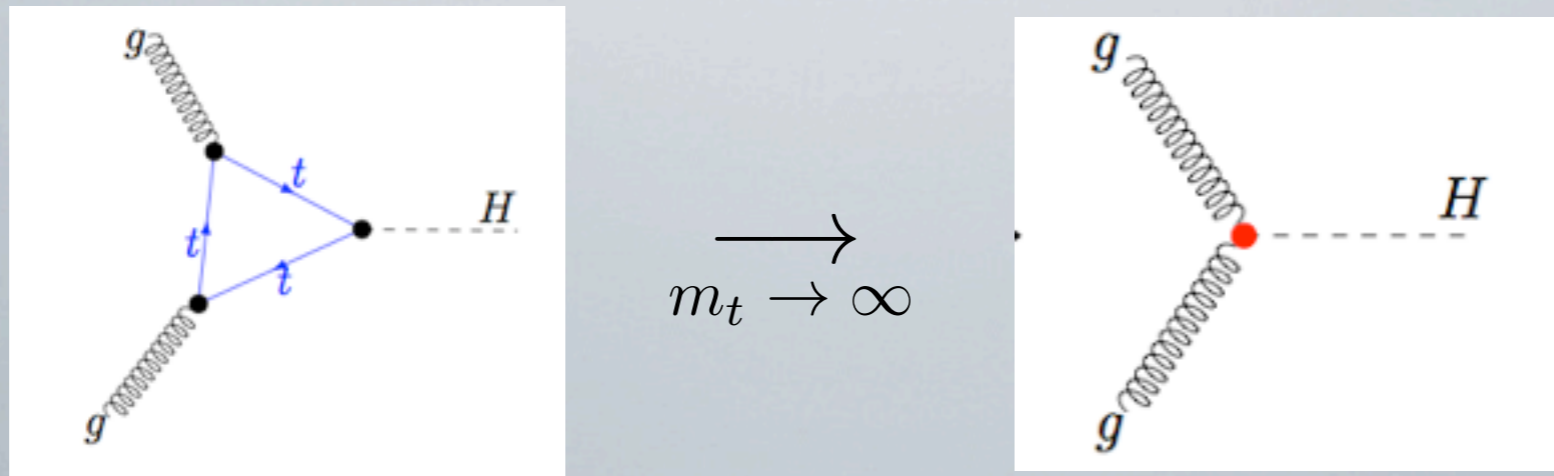
Gudrun Heinrich

Max Planck Institute for Physics, Munich

Higgs+jets workshop, IPPP Durham

December 9, 2014

Higgs Effective Theory (HEFT)



$$\mathcal{L}_{eff} = c_1 G^{\mu\nu,a} G_{\mu\nu,a} H$$

$$c_1(\mu)^{\overline{MS}} = \frac{\alpha_s(\mu)}{12\pi v} \left\{ 1 + \frac{\alpha_s(\mu)}{4\pi} (5C_A - 3C_F) + \mathcal{O}(\alpha_s^2) \right\}$$

- works very well for inclusive Higgs production

(at NLO in HEFT: deviations to full theory below 1% for total cross section)

- fails for observables which are related to large momentum scales

(e.g. Higgs p_T at large transverse momenta, $m_T(H)$ in far off-shell region, ...)

p_T/m_t not small, top loop “resolved”

how to obtain “Wilson coefficient” c_1 ?

$$\mathcal{L}_{ggH} = \frac{g_{ggH}}{v} G^{\mu\nu,a} G_{\mu\nu,a} H$$

$$\frac{g_{ggH}}{v} = \frac{\alpha_s}{8\pi} \frac{1}{v} \tau [1 + (1 - \tau)f(\tau)] \quad \tau = 4m_t^2/m_H^2$$

$f(\tau)$: full top mass dependence from (one-)loop calculation

$$m_t \rightarrow \infty : f(\tau) \rightarrow \frac{1}{\tau} + \frac{1}{3\tau^2} + \mathcal{O}\left(\frac{1}{\tau^3}\right) \quad \Longrightarrow \quad g_{ggH} \rightarrow \frac{\alpha_s}{8\pi} \frac{2}{3} + \mathcal{O}(1/\tau)$$

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valid for on-shell Higgs, $2 \rightarrow 1$ kinematics

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corrections within the HEFT take into account higher orders in $1/m_t^2$ expansion

but this will not help for kinematic effects e.g. due to Higgs pT

Higgs+jet(s): logarithmic m_{top} dependence at large pT, $\mathcal{M} \sim m_t^2 \log^2 \frac{p_{T,H}^2}{m_t^2}$

incomplete list of available results

- inclusive Higgs production:

NLO (2 loops) with full top mass dependence:

mt dep. through one-dim integral representation: Spira, Djouadi, Graudenz, Zerwas '93-95

analytic representation: Harlander, Kant '05;

Anastasiou, Beerli, Bucherer, Daleo, Kunstz '06; Aglietti, Bonciani, Degrandi, Vicini '06

NNLO within HEFT: (inclusive cross section)

Harlander, Kilgore '02; Anastasiou, Melnikov '02; Ravindran, Smith, van Neerven '03;

differential: Anastasiou, Melnikov, Petriello '05; Catani, Grazzini '07

mass effects in resummed jet veto efficiency: Mantler, Wiesemann '12;

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top mass effects on inclusive H cross section:

see e.g. Spira et al; Harlander et al; Steinhauser et al; Anastasiou et al, ...

Neumann, Wiesemann '14;

HEFT accurate to about 1% for $p_{T,veto}^j < \sim 100$ GeV

even better for more inclusive observables

can go up to 20-30% for larger values of $p_{T,veto}^j$

- Higgs plus one jet production:

LO (1 loop) with full top mass dependence:

R.K. Ellis, Hinchliffe, Soldate, van der Bij '88; Baur, Glover '89

NLO within HEFT:

DeFlorian, Grazzini, Kunszt '99; Ravindran, Smith, van Neerven '02; Glosser, Schmidt '02;

NNLO within HEFT: (gg channel)

Boughezal, Caola, Melnikov, Petriello, Schulze '13

Chen, Gehrmann, Glover, Jaquier '14 see Matthieu Jaquier's talk this afternoon

EW corrections within HEFT: Petriello, Keung '09

threshold expansion: Becher, Bell, Lorentzen, Marti '14 ; Huang, Li, Li, Wang '14

H to 4 leptons + 0,1 jet merged: Cascioli, Höche, Krauss, Maierhöfer, Pozzorini, Siegert '13

some recent studies of top mass effects:

Dawson, Lewis, Zeng '14; Neumann, Wiesemann '14; Grazzini, Sargsyan '13; Banfi, Monni, Zanderighi '13;

Harlander, Neumann, Ozeren, Wiesemann '12; Bagnaschi, Degrassi, Slavich, Vicini '12

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upshot: difficult to assess as full m_{top} dependence at NLO is not known

for inclusive 1-jet rate better than $\sim 2\%$

for more exclusive observables: very dependent on cuts, energy/pT range

for scales (e.g. p_T^H) $\leq \sim 2m_t$ HEFT accurate to about 1- 3% (see later)

- Higgs plus 2 jets (**gluon fusion**):

note: H+1jet and H+2 jet Higgs pT distributions have similar rates at large pT

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NLO within HEFT: Campbell, Ellis, Zanderighi '06;

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matched NLO+shower predictions for H+0,1,2 jets:

MC@NLO: Alwall, Li, Maltoni '11;

MCFM+POWHEG/MG4: Campbell, Ellis, Frederix, Nason, Oleari, Williams '12

MCFM/OpenLoops/VBFNLO+Sherpa:

Buschmann, Goncalves-Netto, Krauss, Kuttimalai, Plehn, Schönherr '14

towards NNLO within HEFT: see James Currie's talk this afternoon

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- Higgs plus 3 jets (gluon fusion):

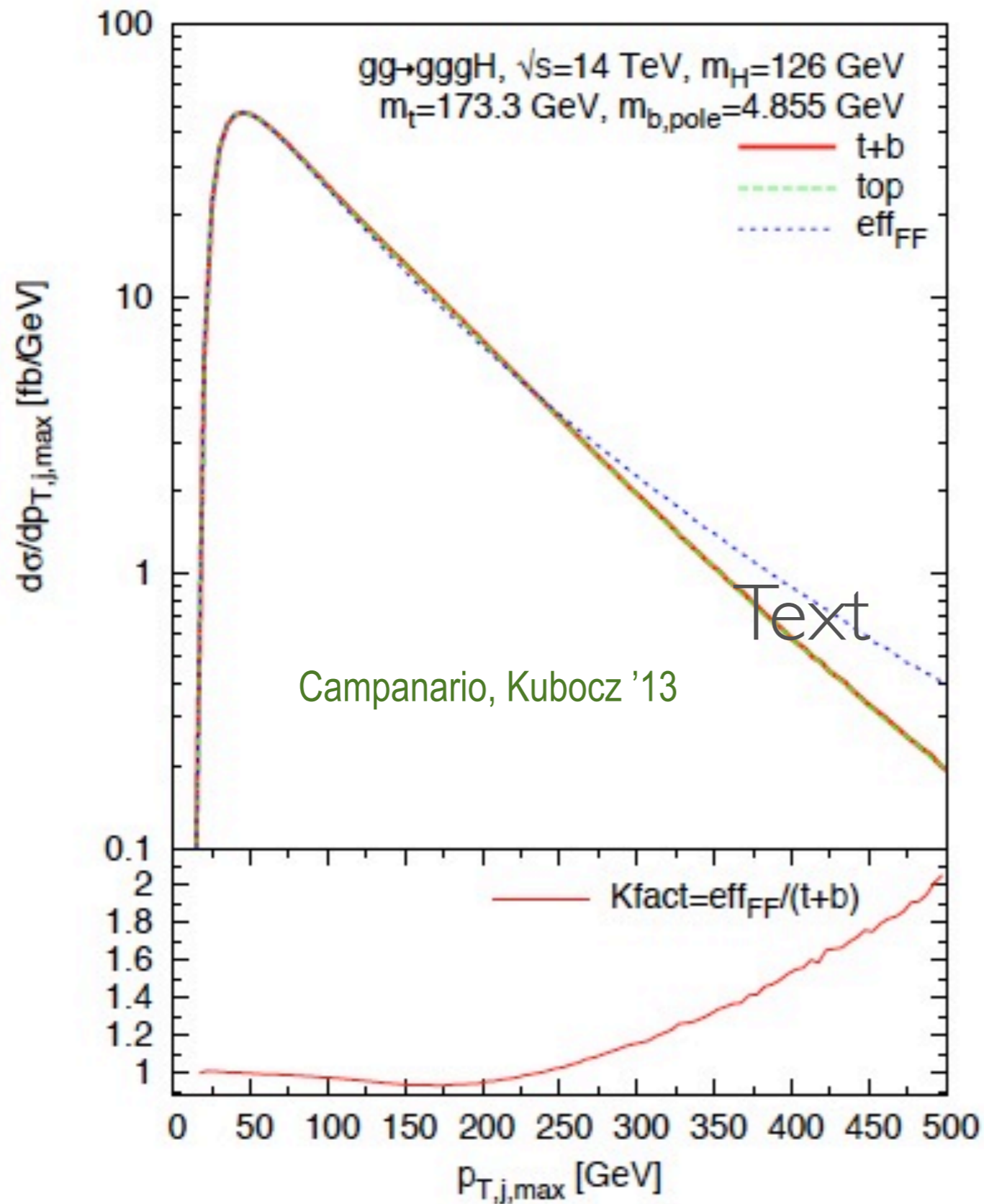
NLO within HEFT:

Cullen, van Deurzen, Greiner, Luisoni, Mastrolia, Mirabella, Ossola, Peraro, Tramontano '13

pheno studies, Ntuples, etc: Greiner, Höche, Luisoni, Schönherr, Winter, Yundin

see Gionata Luisoni's talk this afternoon

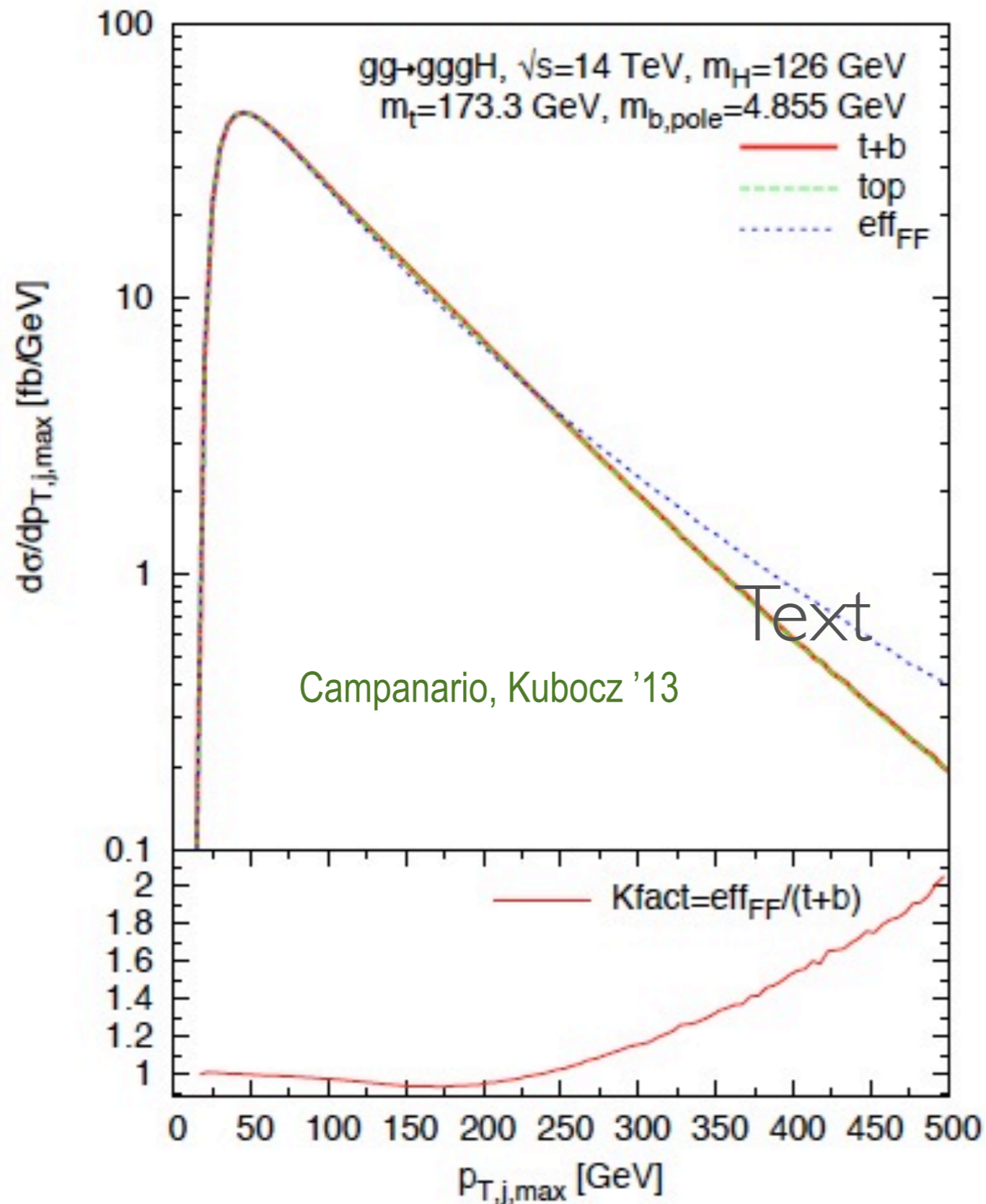
LO (one loop) with quark mass dependence for gg to H ggg: Campanario, Kubocz '13



HEFT very good approximation up to

$$p_t^j \sim 250 \text{ GeV}$$

for $p_t^j \sim 500$ GeV
 corrections up to 100%



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for $p_t^j \sim 500$ GeV
 corrections up to 100%

note that gg to H $qqbar$ g
 and all quark initiated channels are missing

study fixed order perturbative and $1/m_t^2$ expansion, with jet veto

Neumann, Wiesemann 1408.6836

$$[d\sigma^X]_{1/m_t^k}, \quad X \in \{\text{LO, NLO, NNLO}\}, \quad k \in \{0, 2, 4, \dots\}$$

within HEFT

all cross sections are reweighted by exact top mass dependence at LO

$$[d\sigma^X]_{1/m_t^k} = \sigma^{LO}(m_t) [d\bar{\sigma}^X]_{1/m_t^k} / [d\sigma^{LO}]_{1/m_t^k}$$

0-jet bin: $\sigma_{\text{veto}}^X = \sigma_{\text{tot}}^X - \sigma_{\geq 1\text{jet}}^{X'}$ ← if $X=\text{NNLO}$: $X' = \text{NLO}$ with NNLO pdfs

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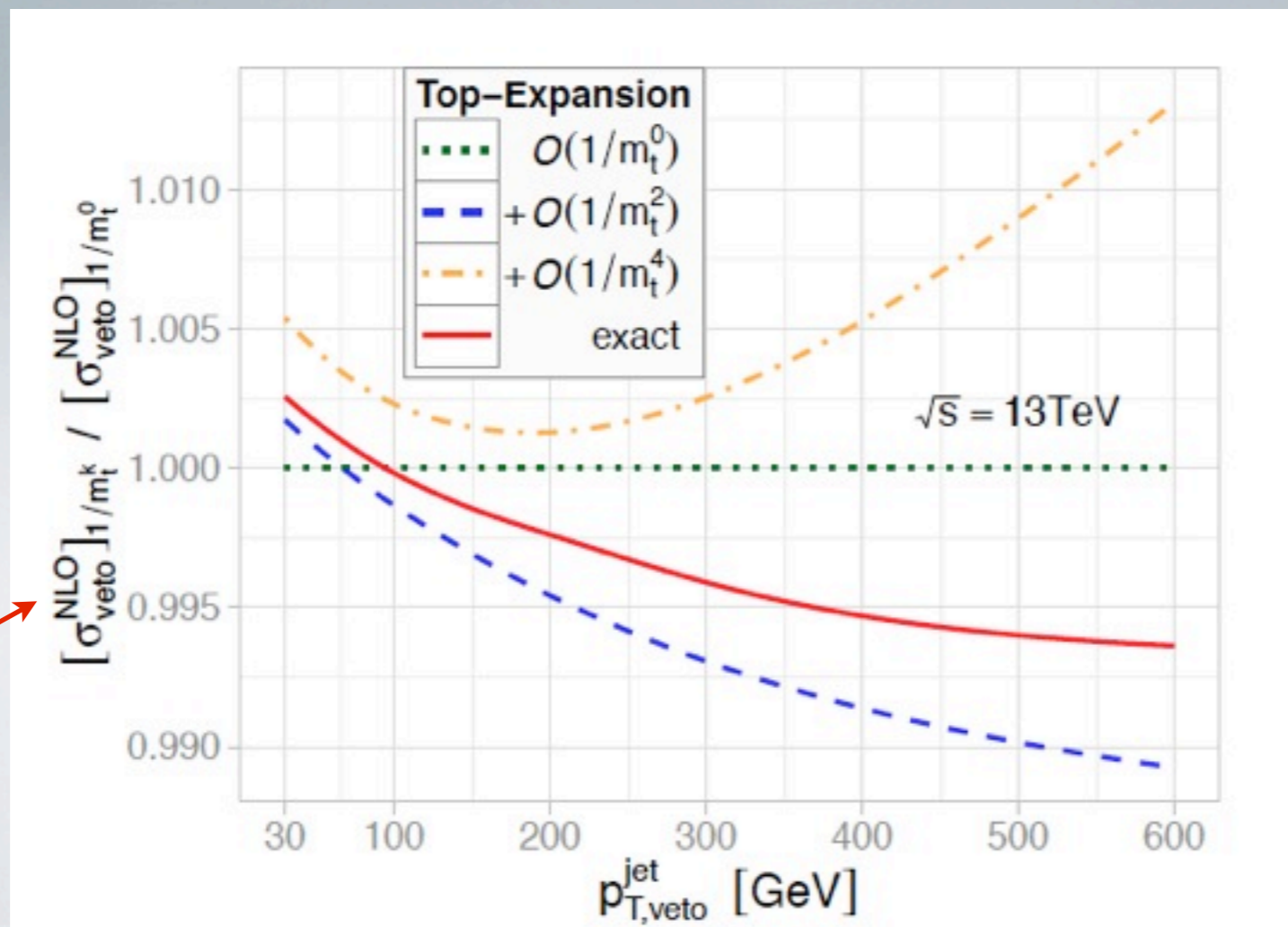
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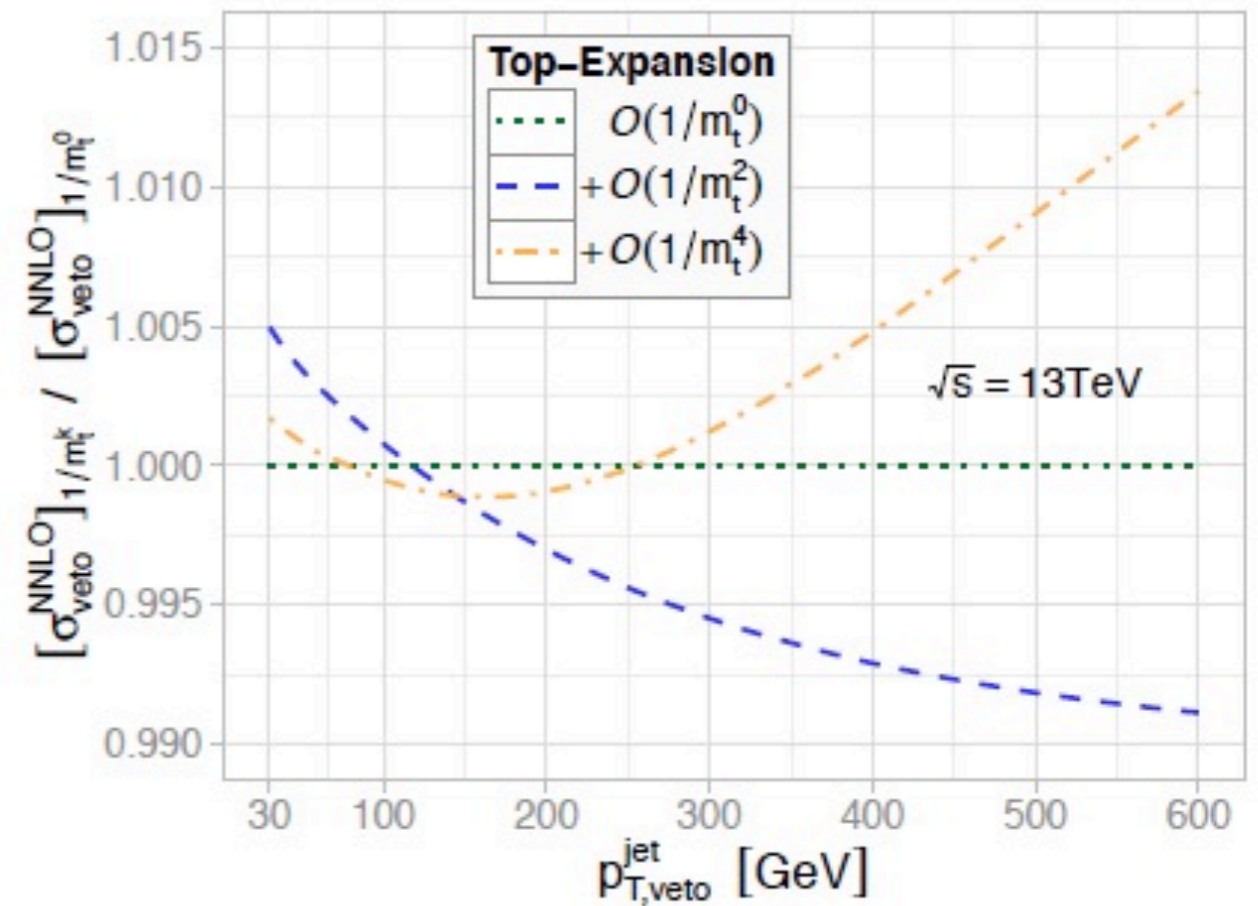
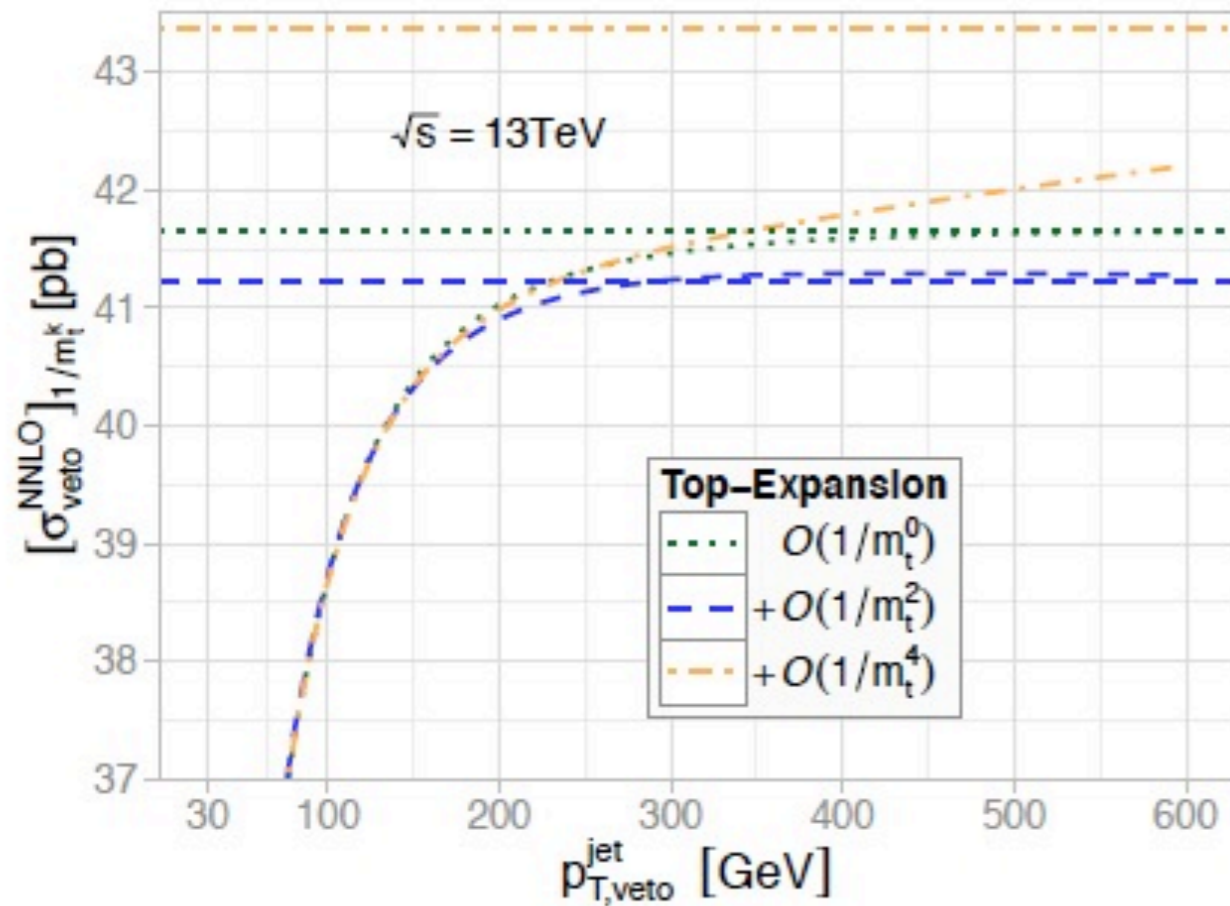
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NLO

envelope below 2.5%

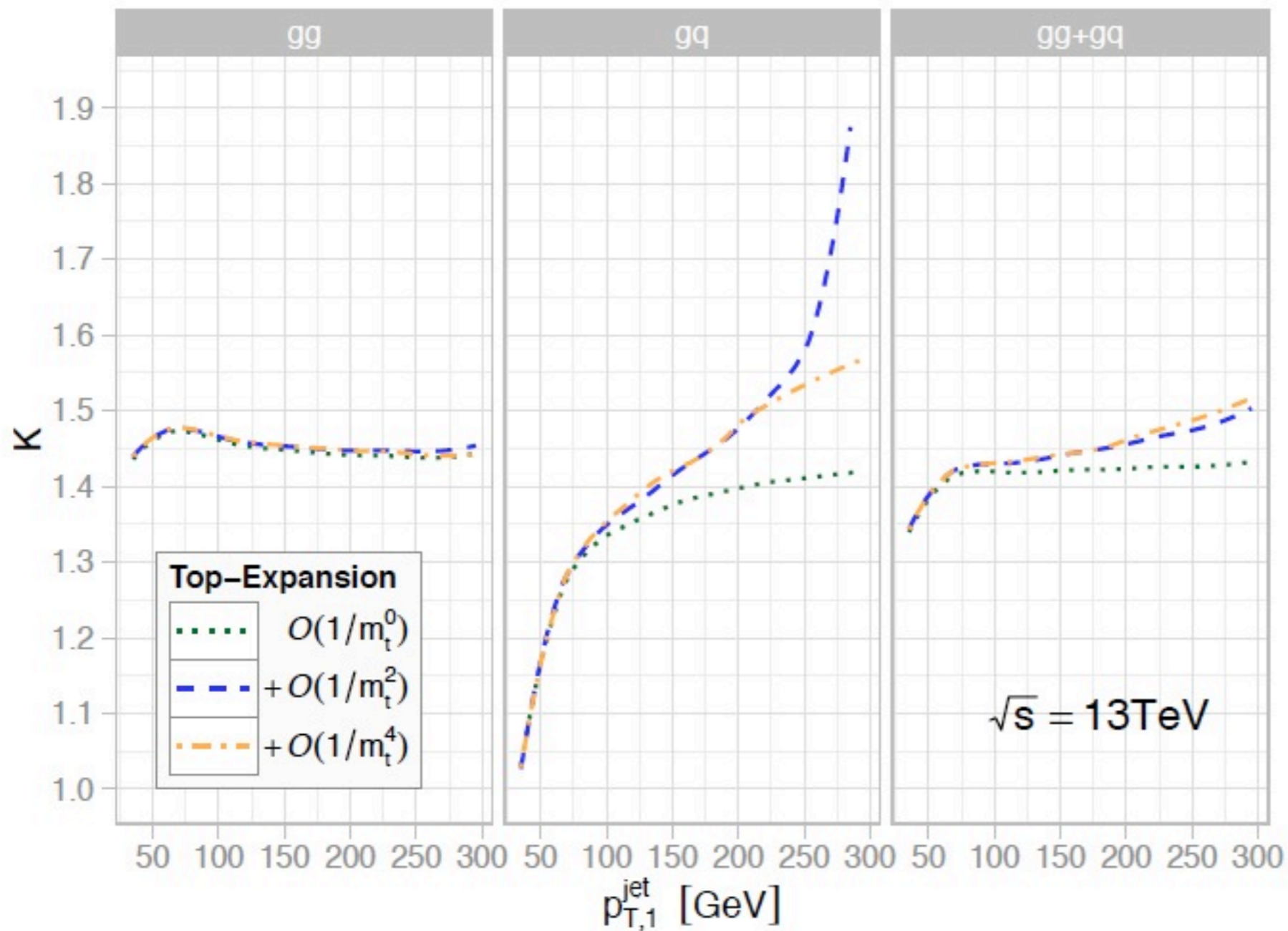
NNLO: ($\mu = m_H$)



rather small effects (below 3%) because contributions from large- p_T jets are suppressed by phase space (jet veto)

K-factor for $p_{T,1}^{\text{jet}}, p_T^H$

$$K_k^X(b) = \frac{[d\bar{\sigma}^X(b)]_{1/m_t^k}}{[d\bar{\sigma}^{LO}(b)]_{1/m_t^k}} \quad \text{e.g. } b = p_{T,1}^{\text{jet}}$$

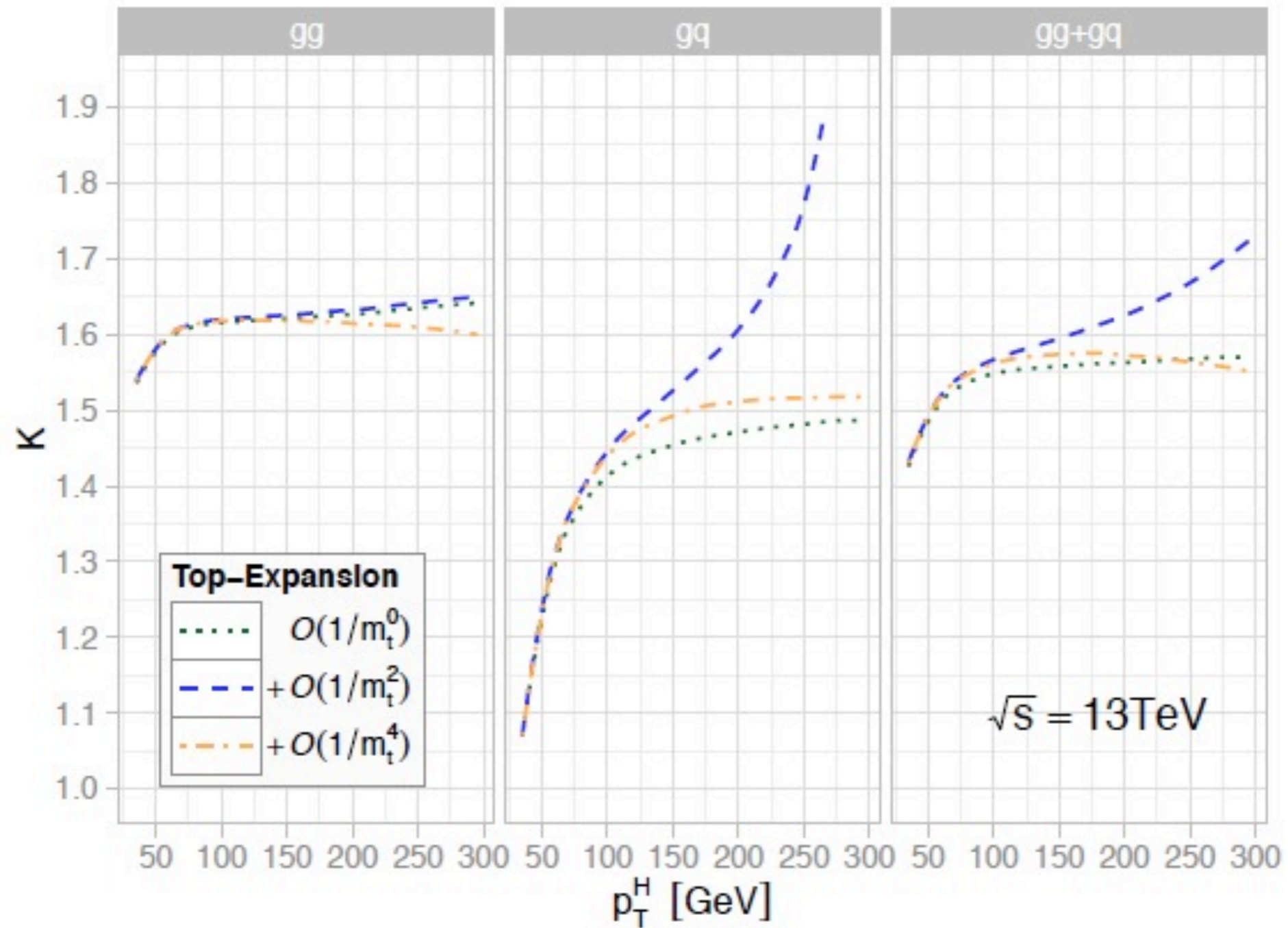


$$\mu^2 = m_H^2 + (p_{T,1}^{\text{jet}})^2$$

X=NLO

difference in gg+gq $\sim 7\%$ at $p_{T,1}^{\text{jet}} \sim 300\text{ GeV}$

Higgs p_T :



what is meant by “NLO including top mass effects” for H+jet(s) ?

Alwall, Li, Maltoni 1110.1728

Buschmann, Goncalves-Netto, Krauss, Kuttimalai, Plehn, Schönherr 1410.5806 ★

reweighting: $r^{(n)} = |\mathcal{M}^{(n)}(m_t)|^2 / |\mathcal{M}_{HEFT}^{(n)}|^2$

for each event (**jet multiplicity n**) the HEFT (NLO) matrix elements are rescaled with the mass dependent loop (LO!) counterparts

findings: top mass effects seem to factorize as a constant factor in each pT bin

→ top mass effects are fully associated with the hard process, therefore reweighting procedure is justified

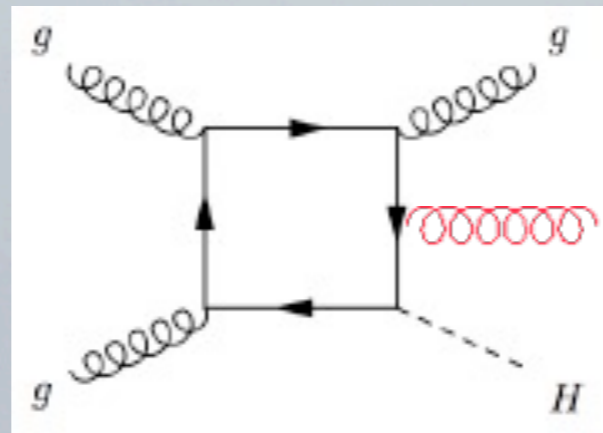
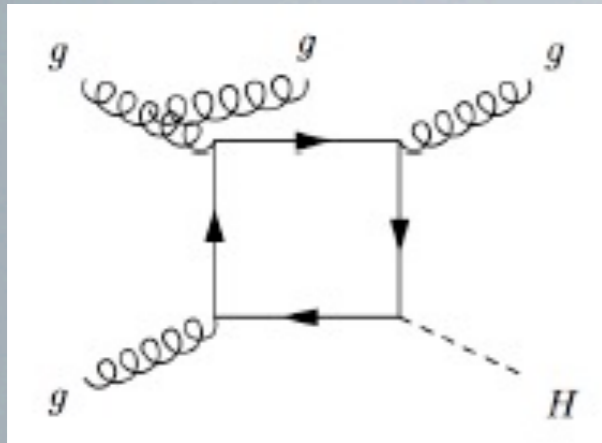
mass effects can lead to a factor ~ 4 at pT=600 GeV

★ refer to Maltoni, Vryonidou, Zaro 1408.6542 for HH production for this procedure

Maltoni, Vryonidou, Zaro 1408.6542:

full m_{top} dependence also in real radiation

transferred to H+jet means 1-loop diagrams combined with single real radiation, up to pentagon diagrams for H+1jet, hexagons for H+2jets

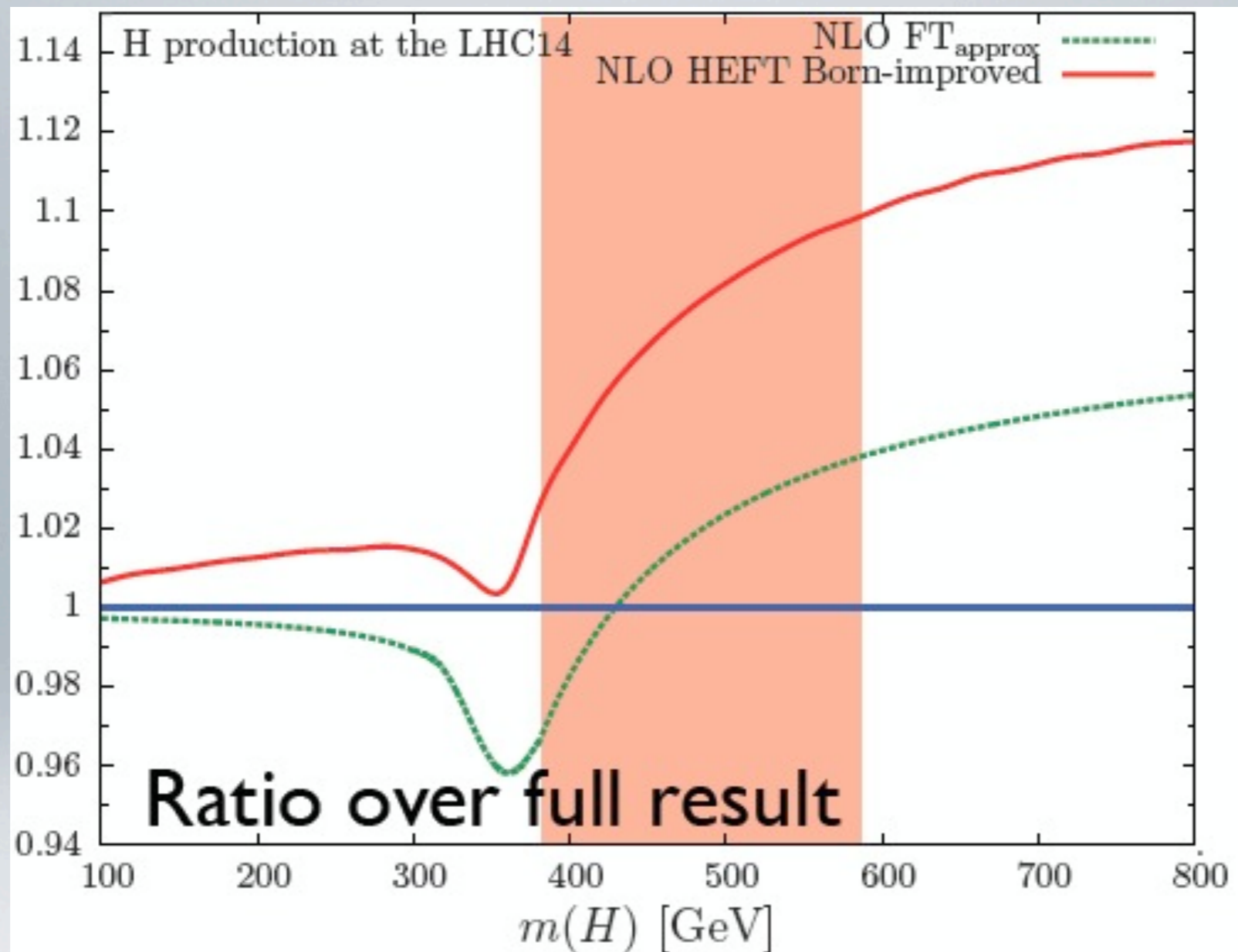


example diagrams for real radiation corrections to H+1jet

only missing ingredient for full NLO would be 2-loop virtual diagrams \longrightarrow “FT_approx”

compare to “Born improved HEFT” reweighting with $r = |\mathcal{M}_{loop}|^2 / |\mathcal{M}_{HEFT}|^2$
LO (“Born”)

comparison “FT_{approx}” and “Born improved HEFT” for single Higgs case:

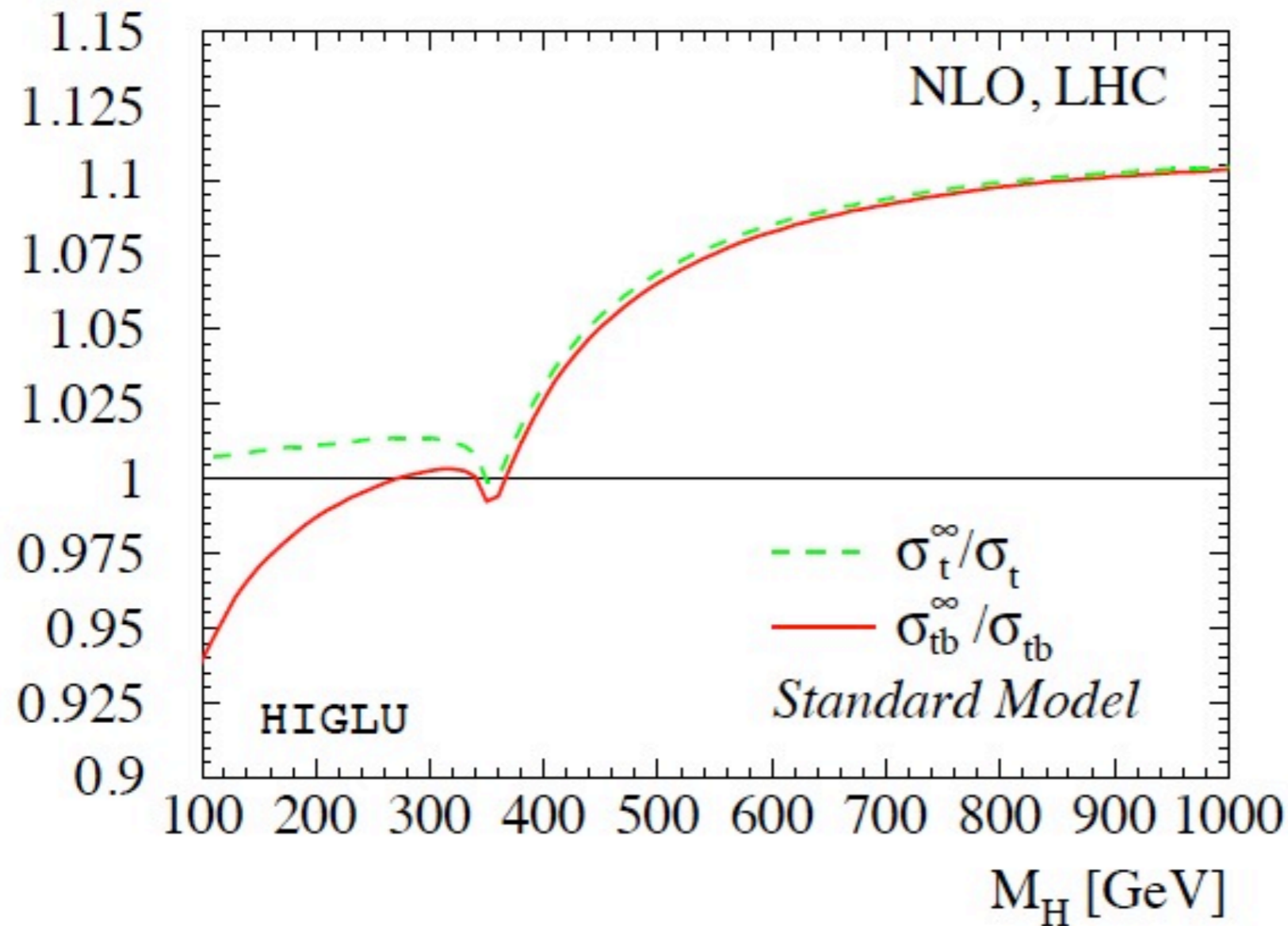


[M.Zaro, LHC XS WG meeting Nov '14]

inclusion of full mass dependence in real radiation
→ cancellations real-virtual spoiled or better approximation?

inclusive Higgs production: compare “Born improved HEFT” with full NLO

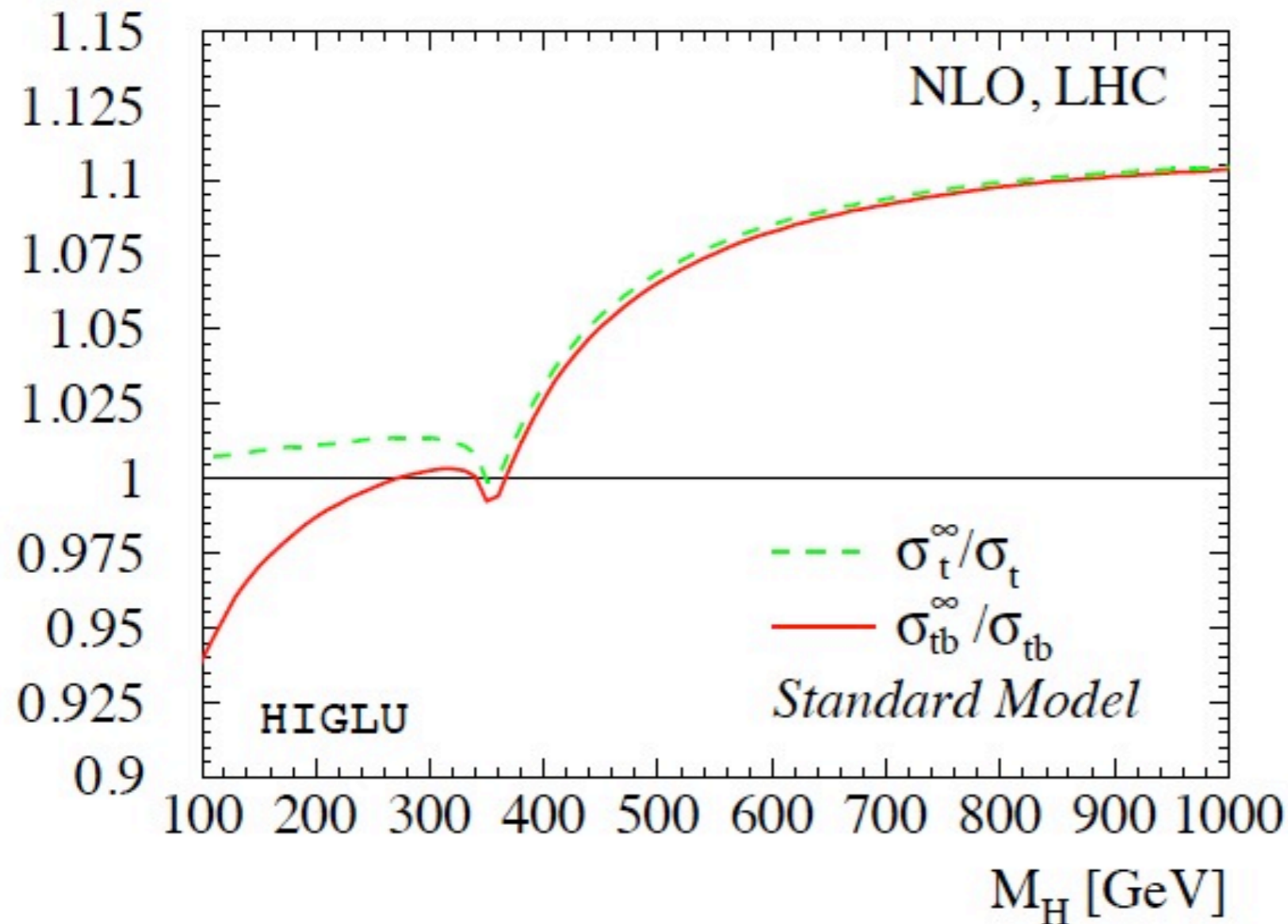
Harlander '03
based on HIGLU [Spira et al]



obvious cancellations between real and virtual contributions around the $2 m_{top}$ threshold because in this region “Born improved HEFT” is very close to full theory

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beyond the threshold region it is unclear which is the better approximation for **H+jet(s)** until full mass dependence in virtual corrections (2 loops) is available

Conclusions

- H+jet: HEFT does rather well for observables which are sufficiently inclusive in p_T (H, jet)
- less inclusive observables: top mass effects are important at large p_T

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- less inclusive observables: top mass effects are important at large p_T
- studying only the gg channel, does not always capture the leading effects
- different approximations towards full NLO can lead to substantial differences in the predictions, not only at high p_T