

# Precision Constraints on Higgs and Z couplings

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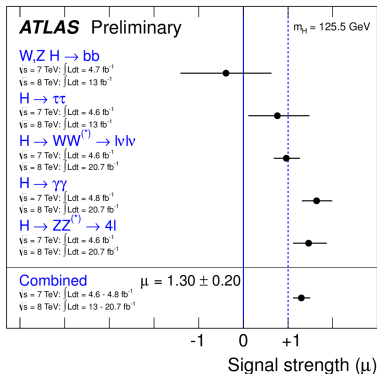


Seminar talk, IPPP  
Durham, November 20, 2014

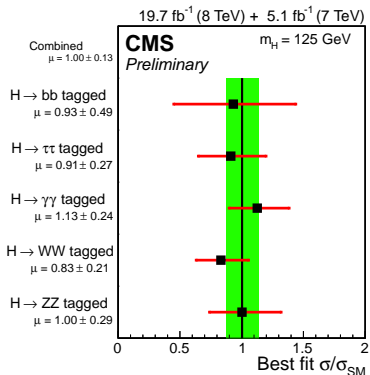
With Ulrich Haisch, Jure Zupan – [JHEP 1311 \(2013\) 180](#) [[arXiv:1310.1385](#)]

With Admir Greljo, Emmanuel Stamou, Patipan Uttayarat – [arXiv:1408.0792](#)

# What do we know about the Higgs couplings?



[ATLAS-CONF-2013-034]



[CMS-PAS-HIG-14-009]

# Outline

- Anomalous Higgs couplings
  - $ttH$
  - $bbH$
  - $\tau\tau H$
- Anomalous  $ttZ$  couplings
- Conclusion

# SM EFT

- No BSM particles at LHC  $\Rightarrow$  use EFT with only SM fields  
[See, e.g., Buchmüller et al. 1986, Grzadkowski et al. 2010]

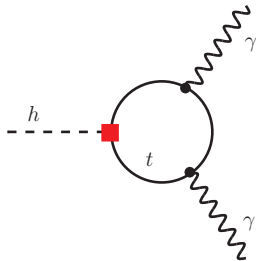
$$\mathcal{L}^{\text{eff}} = \mathcal{L}^{\text{SM}} + \mathcal{L}^{\text{dim.6}} + \dots$$

For instance,

$$y_f(\bar{Q}_L t_R H) + \text{h.c.} \xrightarrow{\text{EWSB}} m_t = \frac{y_t v}{\sqrt{2}}$$
$$\frac{H^\dagger H}{\Lambda^2}(\bar{Q}_L t_R H) + \text{h.c.} \xrightarrow{\text{EWSB}} \delta m_t \propto \frac{(v/\sqrt{2})^3}{\Lambda^2}, \quad \delta y_t \propto 3 \frac{(v/\sqrt{2})^2}{\Lambda^2}$$

- If both terms are present, mass and Yukawa terms are independent

## From $h \rightarrow \gamma\gamma \dots$



- In the SM, Yukawa coupling to fermion  $f$  is

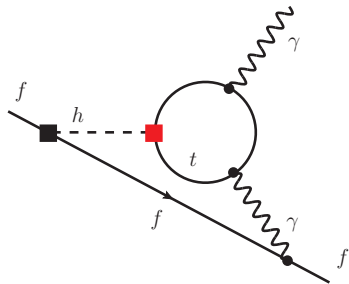
$$\mathcal{L}_Y = -\frac{y_f}{\sqrt{2}} \bar{f} f h$$

- We will look at modification

$$\mathcal{L}'_Y = -\frac{y_f}{\sqrt{2}} (\kappa_f \bar{f} f + i\tilde{\kappa}_f \bar{f} \gamma_5 f) h$$

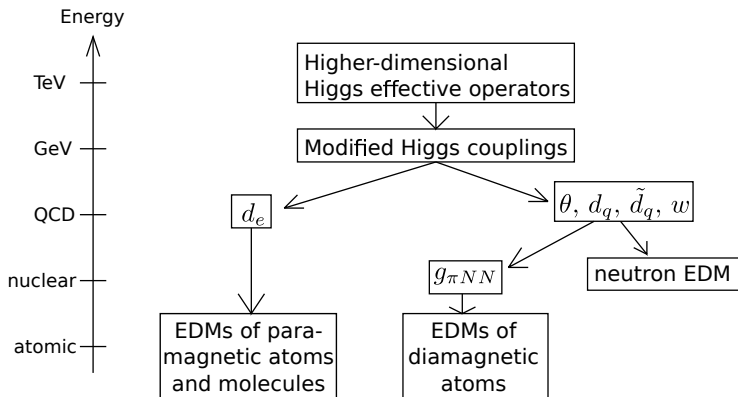
- New contributions will modify Higgs production cross section and decay rates

## ... to electric dipole moments



- Attaching a light fermion line leads to EDM
- Indirect constraint on  $CP$ -violating Higgs coupling
- SM “background” enters at three- and four-loop level
- Complementary to collider measurements
- Constraints depend on additional assumptions

# Electric Dipole Moments (EDMs) – Generalities



[Adapted from Pospelov and Ritz, hep-ph/0504231]

# ACME result on electron EDM

## Order of Magnitude Smaller Limit on the Electric Dipole Moment of the Electron

The ACME Collaboration\*: J. Baron<sup>1</sup>, W. C. Campbell<sup>2</sup>, D. DeMille<sup>3</sup>, J. M. Doyle<sup>1</sup>, G. Gabrielse<sup>1</sup>, Y. V. Gurevich<sup>1,4\*</sup>, P. W. Hess<sup>2</sup>, N. R. Hutzler<sup>1</sup>, E. Kirilov<sup>3,5</sup>, I. Kozyryev<sup>3,1</sup>, B. R. O'Leary<sup>3</sup>, C. D. Panda<sup>1</sup>, M. F. Parsons<sup>1</sup>, E. S. Petrik<sup>1</sup>, B. Spaun<sup>1</sup>, A. C. Vutha<sup>4</sup>, and A. D. West<sup>3</sup>

The Standard Model (SM) of particle physics fails to explain dark matter and why matter survived annihilation with antimatter following the Big Bang. Extensions to the SM, such as weak-scale Supersymmetry, may explain one or both of these phenomena by positing the existence of new particles and interactions that are asymmetric under time-reversal (T). These theories nearly always predict a small, yet potentially measurable ( $10^{-27}$ - $10^{-30}$  e cm) electron electric dipole moment (EDM,  $d_e$ ), which is an asymmetric charge distribution along the spin ( $\vec{S}$ ). The EDM is also asymmetric under T. Using the polar molecule thorium monoxide (ThO), we measure  $d_e = (-2.1 \pm 3.7_{\text{stat}} \pm 2.5_{\text{sys}}) \times 10^{-29}$  e cm. This corresponds to an upper limit of  $|d_e| < 8.7 \times 10^{-29}$  e cm with 90 percent confidence, an order of magnitude improvement in sensitivity compared to the previous best limits. Our result constrains T-violating physics at the TeV energy scale.

The exceptionally high internal effective electric field ( $\vec{E}_{\text{eff}}$ ) of heavy neutral atoms and molecules can be used to precisely probe for  $d_e$  via the energy shift  $U = -\vec{d}_e \cdot \vec{E}_{\text{eff}}$ , where  $\vec{d}_e = d_e \vec{S}/(\hbar/2)$ . Valence electrons travel relativistically near the heavy nucleus,

is prepared using optical pumping and state preparation lasers. Parallel electric ( $\vec{E}$ ) and magnetic ( $\vec{B}$ ) fields exert torques on the electric and magnetic dipole moments, causing the spin vector to precess in the  $xy$  plane. The precession angle is measured with a readout laser and fluorescence detection. A change in this angle as  $\vec{E}_{\text{eff}}$  is reversed is proportional to  $d_e$ .

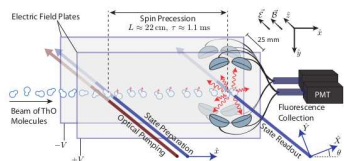


FIG. 1. Schematic of the apparatus (not to scale). A collimated pulse of ThO molecules enters a magnetically shielded region. An aligned spin

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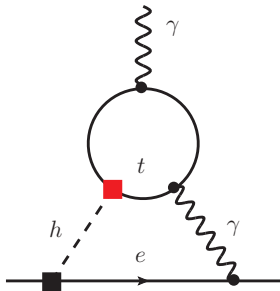
- Expect order-of-magnitude improvements!



# Anomalous $ttH$ couplings

# Electron EDM

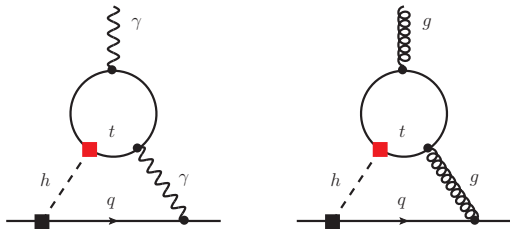
$$\mathcal{L}_{\text{eff}} = -d_e \frac{i}{2} \bar{e} \sigma^{\mu\nu} \gamma_5 e F_{\mu\nu}$$



- EDM induced via “Barr-Zee” diagrams [Weinberg 1989, Barr & Zee 1990]
- $\frac{d_e}{e} = \frac{16}{3} \frac{\alpha}{(4\pi)^3} \sqrt{2} G_F m_e \kappa_e \tilde{\kappa}_t f_1 \left( \frac{m_t^2}{M_h^2} \right)$
- $|d_e/e| < 8.7 \times 10^{-29}$  cm (90% CL) [ACME 2013] with ThO molecules
- Constraint on  $\tilde{\kappa}_t$  vanishes if Higgs does not couple to electron

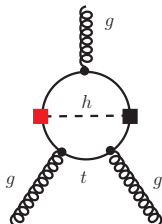
# Neutron EDM – EDM and CEDM

$$\mathcal{L}_{\text{eff}} \supset -d_q \frac{i}{2} \bar{q} \sigma^{\mu\nu} \gamma_5 q F_{\mu\nu} - \tilde{d}_q \frac{ig_s}{2} \bar{q} \sigma^{\mu\nu} T^a \gamma_5 q G_{\mu\nu}^a$$



- $d_q(\mu_W) = -\frac{16}{3} e Q_q \frac{\alpha}{(4\pi)^3} \sqrt{2} G_F m_q \kappa_q \tilde{\kappa}_t f_1 \left( \frac{m_t^2}{M_h^2} \right)$
- $\tilde{d}_q(\mu_W) = -2 \frac{\alpha_s}{(4\pi)^3} \sqrt{2} G_F m_q \kappa_q \tilde{\kappa}_t f_1 \left( \frac{m_t^2}{M_h^2} \right)$

# Neutron EDM – The Weinberg Operator



- Here the Higgs couples only to the top quark
- Get bound even if light-quark couplings are zero

$$\bullet w(\mu_W) = \frac{g_s}{4} \frac{\alpha_s}{(4\pi)^3} \sqrt{2} G_F \kappa_t \tilde{\kappa}_t f_3 \left( \frac{m_t^2}{M_h^2} \right)$$

# Neutron EDM – RG Running

- Need to run from  $\mu_W \sim M_W$  to hadronic scale  $\mu_H \sim 1 \text{ GeV}$
- Operators will mix:  $\mu \frac{d}{d\mu} \mathcal{C}(\mu) = \gamma^T \mathcal{C}(\mu)$

$$\gamma = \frac{\alpha_s}{4\pi} \begin{pmatrix} \frac{32}{3} & 0 & 0 \\ \frac{32}{3} & \frac{28}{3} & 0 \\ 0 & -6 & 14 + \frac{4N_f}{3} \end{pmatrix}$$

- At hadronic scale  $\mu_H$  need to evaluate hadronic matrix elements
- Use QCD sum rule techniques [Pospelov, Ritz, hep-ph/0504231]
- There are large  $\mathcal{O}(100\%)$  uncertainties
  - E.g. excited states, higher terms in OPE, ambiguity in nuclear current. . .
- In the future, lattice might provide more reliable estimates

# Neutron EDM – Bounds

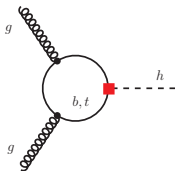
$$\frac{d_n}{e} = \left\{ (1.0 \pm 0.5) \left[ -5.3 \kappa_q \tilde{\kappa}_t + 5.1 \cdot 10^{-2} \kappa_t \tilde{\kappa}_t \right] \right. \\ \left. + (22 \pm 10) 1.8 \cdot 10^{-2} \kappa_t \tilde{\kappa}_t \right\} \cdot 10^{-25} \text{ cm}.$$

- $w \propto \kappa_t \tilde{\kappa}_t$  subdominant, but involves **only top Yukawa**
- $|d_n/e| < 2.9 \times 10^{-26} \text{ cm}$  (90% CL) [Baker et al., 2006]

# Constraints from $gg \rightarrow h$

- $gg \rightarrow h$  generated at one loop
- Have effective potential

$$V_{\text{eff}} = -c_g \frac{\alpha_s}{12\pi} \frac{h}{v} G_{\mu\nu}^a G^{\mu\nu,a} - \tilde{c}_g \frac{\alpha_s}{8\pi} \frac{h}{v} G_{\mu\nu}^a \tilde{G}^{\mu\nu,a}$$



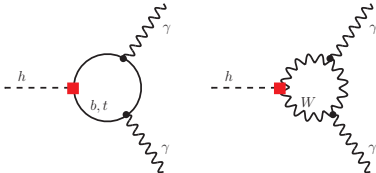
- $c_g, \tilde{c}_g$  given in terms of loop functions
- $\kappa_g \equiv c_g/c_{g,\text{SM}}, \tilde{\kappa}_g \equiv 3\tilde{c}_g/2c_{g,\text{SM}}$

$$\frac{\sigma(gg \rightarrow h)}{\sigma(gg \rightarrow h)_{\text{SM}}} = |\kappa_g|^2 + |\tilde{\kappa}_g|^2 = \kappa_t^2 + 2.6 \tilde{\kappa}_t^2 + 0.11 \kappa_t (\kappa_t - 1)$$

# Constraints from $h \rightarrow \gamma\gamma$

- $h \rightarrow \gamma\gamma$  generated at one loop
- Have effective potential

$$V_{\text{eff}} = -c_\gamma \frac{\alpha}{\pi} \frac{h}{v} F_{\mu\nu} F^{\mu\nu} - \tilde{c}_\gamma \frac{3\alpha}{2\pi} \frac{h}{v} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



- $c_\gamma, \tilde{c}_\gamma$  given in terms of loop functions

- $\kappa_\gamma \equiv c_\gamma/c_{\gamma,\text{SM}}, \tilde{\kappa}_\gamma \equiv 3\tilde{c}_\gamma/2c_{\gamma,\text{SM}}$

$$\frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{\text{SM}}} = |\kappa_\gamma|^2 + |\tilde{\kappa}_\gamma|^2 = (1.28 - 0.28 \kappa_t)^2 + (0.43 \tilde{\kappa}_t)^2$$

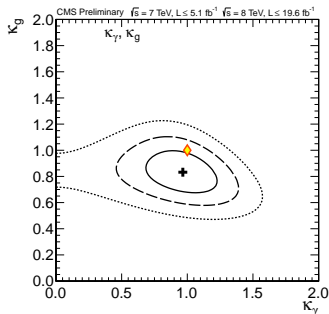


# LHC input

- Naive weighted average of ATLAS, CMS

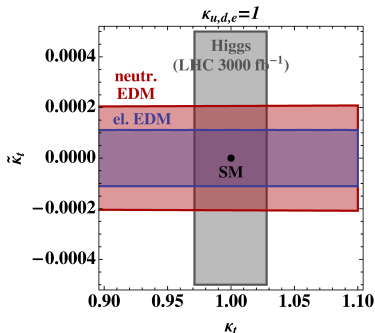
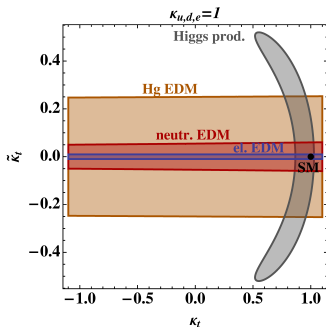
$$\kappa_{g,WA} = 0.91 \pm 0.08, \quad \kappa_{\gamma,WA} = 1.10 \pm 0.11$$

- We set  $\kappa_{g/\gamma,WA}^2 = |\kappa_{g/\gamma}|^2 + |\tilde{\kappa}_{g/\gamma}|^2$



[CMS-PAS-HIG-13-005]

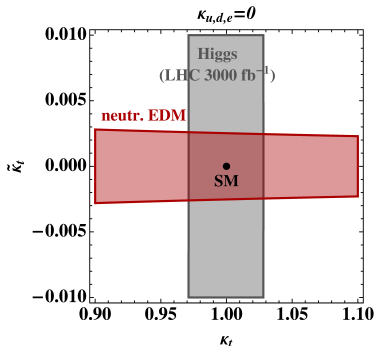
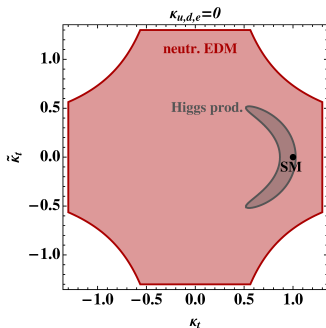
# Combined constraints on top coupling



- Assume SM couplings to electron and light quarks
- Future projection for 3000fb<sup>-1</sup> @ high-luminosity LHC  
[J. Olsen, talk at Snowmass Energy Frontier workshop]
- Factor 90 (300) improvement on electron (neutron) EDM  
[Fundamental Physics at the Energy Frontier, arXiv:1205.2671]

# Combined constraints on top couplings

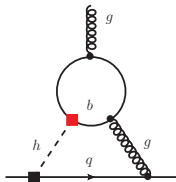
- Set couplings to electron and light quarks to zero
- Contribution of Weinberg operator will lead to strong constraints in the future scenario



# Anomalous $bbH$ couplings

# Constraints from EDMs

- Contributions to EDMs suppressed by small Yukawas; still get meaningful constraints in future scenario
- For electron EDM, simply replace charges and couplings
- For neutron EDM, extra scale  $m_b \ll M_h$  important



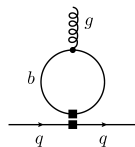
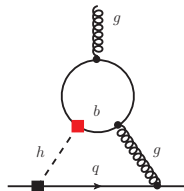
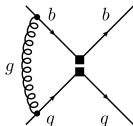
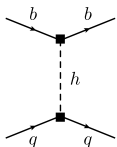
$$d_q(\mu_W) \simeq -4eQ_q N_c Q_b^2 \frac{\alpha}{(4\pi)^3} \sqrt{2} G_F m_q \kappa_q \tilde{\kappa}_b \frac{m_b^2}{M_h^2} \left( \log^2 \frac{m_b^2}{M_h^2} + \frac{\pi^2}{3} \right),$$

$$\tilde{d}_q(\mu_W) \simeq -2 \frac{\alpha_s}{(4\pi)^3} \sqrt{2} G_F m_q \kappa_q \tilde{\kappa}_b \frac{m_b^2}{M_h^2} \left( \log^2 \frac{m_b^2}{M_h^2} + \frac{\pi^2}{3} \right),$$

$$w(\mu_W) \simeq -g_s \frac{\alpha_s}{(4\pi)^3} \sqrt{2} G_F \kappa_b \tilde{\kappa}_b \frac{m_b^2}{M_h^2} \left( \log \frac{m_b^2}{M_h^2} + \frac{3}{2} \right).$$

# RGE analysis of the $b$ -quark contribution to EDMs

- $\approx 3$  scale uncertainty in CEDM Wilson coefficient
- Two-step matching at  $M_h$  and  $m_b$ :



- Integrate out Higgs

- Mixing into

- Matching onto

- $\mathcal{O}_1^q = \bar{q}q \bar{b}i\gamma_5 b$

- $\mathcal{O}_4^q = \bar{q}\sigma_{\mu\nu} T^a q \bar{b}i\sigma^{\mu\nu} \gamma_5 T^a b$

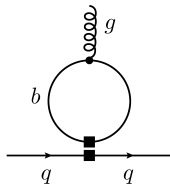
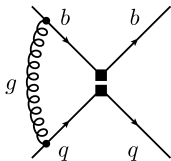
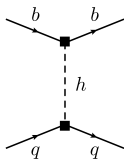
- $\mathcal{O}_6^q = -\frac{i}{2} \frac{m_b}{g_s} \bar{q}\sigma^{\mu\nu} T^a \gamma_5 q G_{\mu\nu}^a$

# RG Running

- Above  $\mu_b \sim m_b$  have 10 operators which mix:

$$\gamma^{(0)} = \begin{pmatrix} -16 & 0 & 0 & -2 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 2 & -\frac{4}{9} & -\frac{5}{6} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -96 & \frac{16}{3} & 0 & 0 & 0 & -48 & 0 & 0 & 0 & 0 \\ -\frac{64}{3} & -40 & 0 & -\frac{38}{3} & 0 & 0 & 0 & -8 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -10 & -\frac{1}{6} & 0 & 0 & 4 & 4 & 0 \\ 0 & 0 & 0 & 0 & 40 & \frac{34}{3} & 0 & 0 & -112 & -16 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\frac{14}{3} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{32}{3} & -6 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -\frac{14}{3} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{32}{3} & -6 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -6 & 0 & -6 & \frac{16}{3} \end{pmatrix}.$$

# CEDM operator



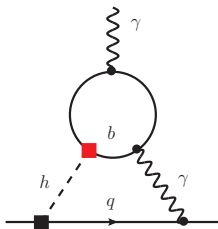
- $$C_{\tilde{d}_q}(\mu_b) = \frac{432}{2773 \eta_5^{9/23}} + \frac{0.07501}{\eta_5^{1.414}} + 9.921 \cdot 10^{-4} \eta_5^{0.7184} - \frac{0.2670}{\eta_5^{0.6315}} + \frac{0.03516}{\eta_5^{0.06417}}$$

- $$\bullet \eta_5 \equiv \alpha_s(\mu_W)/\alpha_s(\mu_b)$$

- $$\bullet \text{Expand: } C_{\tilde{d}_q}(\mu_b) \simeq \left(\frac{\alpha_s}{4\pi}\right)^2 \frac{\gamma_{14}^{(0)} \gamma_{48}^{(0)}}{8} \log^2 \frac{m_b^2}{M_h^2} + \mathcal{O}(\alpha_s^3)$$

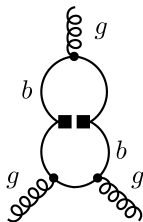


# EDM operator



- $C_{dq}(\mu_b) = -4 \frac{\alpha \alpha_s}{(4\pi)^2} Q_q \log^2 \frac{m_b^2}{M_h^2} + \left(\frac{\alpha_s}{4\pi}\right)^3 \frac{\gamma_{14}^{(0)} \gamma_{48}^{(0)} \gamma_{87}^{(0)}}{48} \log^3 \frac{m_b^2}{M_h^2} + \mathcal{O}(\alpha_s^4)$
- QCD mixing term dominates by a factor of  $\approx 4.5(-9.0)$ !

# Weinberg operator



- $C_w(\mu_b) = \left(\frac{\alpha_s}{4\pi}\right)^2 \frac{\gamma_{5,11}^{(1)}}{2} \log \frac{m_b^2}{M_h^2} + \mathcal{O}(\alpha_s^3)$
- Linear log requires two-loop running

# Neutron EDM at the hadronic scale

- Below  $\mu_b \sim m_b$ , analysis is analogous to case of top quarks

$$\frac{d_n}{e} = \left\{ (1.0 \pm 0.5) [-18.1 \tilde{\kappa}_b + 0.15 \kappa_b \tilde{\kappa}_b] + (22 \pm 10) 0.48 \kappa_b \tilde{\kappa}_b \right\} \cdot 10^{-27} \text{ cm}.$$

# Collider constraints

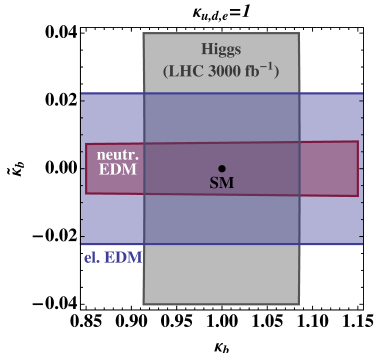
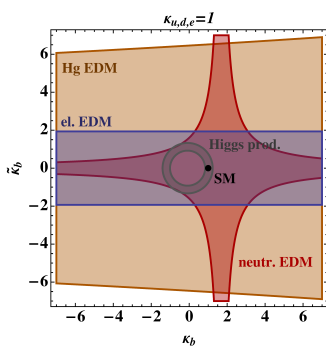
- Modifications of  $gg \rightarrow h$ ,  $h \rightarrow \gamma\gamma$  due to  $\kappa_b \neq 1$ ,  $\tilde{\kappa}_b \neq 0$  are subleading
- $\Rightarrow$  Main effect: modifications of branching ratios / total decay rate

$$\text{Br}(h \rightarrow b\bar{b}) = \frac{(\kappa_b^2 + \tilde{\kappa}_b^2)\text{Br}(h \rightarrow b\bar{b})_{\text{SM}}}{1 + (\kappa_b^2 + \tilde{\kappa}_b^2 - 1)\text{Br}(h \rightarrow b\bar{b})_{\text{SM}}}$$

$$\text{Br}(h \rightarrow X) = \frac{\text{Br}(h \rightarrow X)_{\text{SM}}}{1 + (\kappa_b^2 + \tilde{\kappa}_b^2 - 1)\text{Br}(h \rightarrow b\bar{b})_{\text{SM}}}$$

- Use naive averages of ATLAS / CMS signal strengths  $\hat{\mu}_X$  for  $X = b\bar{b}$ ,  $\tau^+\tau^-$ ,  $\gamma\gamma$ ,  $WW$ ,  $ZZ$
- $\hat{\mu}_X = \text{Br}(h \rightarrow X)/\text{Br}(h \rightarrow X)_{\text{SM}}$  up to subleading corrections of production cross section

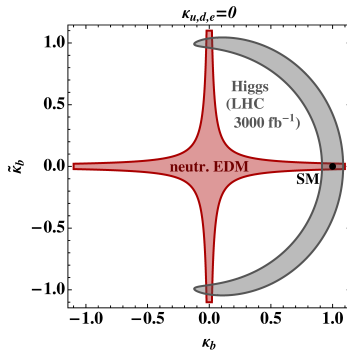
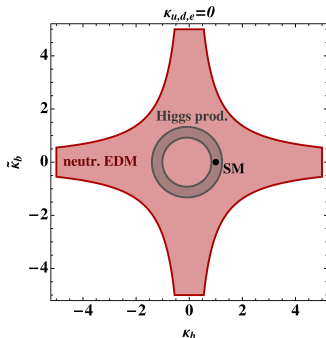
# Combined constraints on bottom couplings



- Assume SM couplings to electron and light quarks
- Future projection for 3000fb<sup>-1</sup> @ high-luminosity LHC
- Factor 90 (300) improvement on electron (neutron) EDM

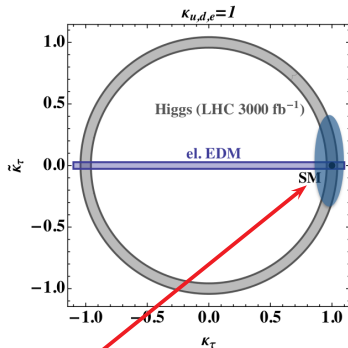
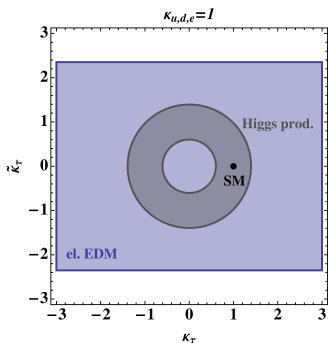
# Combined constraints on bottom couplings

- Set couplings to electron and light quarks to zero
- Contribution of Weinberg operator will lead to competitive constraints in the future scenario



# Combined constraints on $\tau$ couplings

- Effect of modified  $hT\tau$  coupling on  $\kappa_\gamma$ ,  $\tilde{\kappa}_\gamma$  again subleading
- Get simple constraint from modification of branching ratios



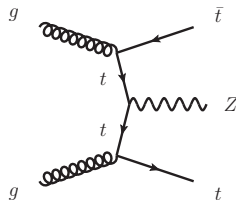
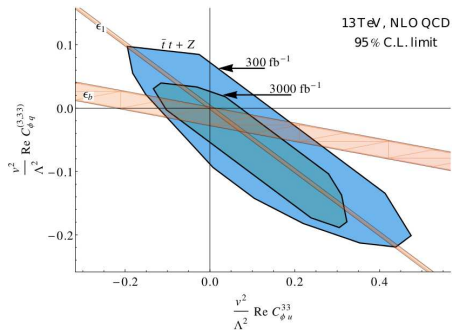
- Shaded region shows reach for direct searches

[Harnik et al., Phys.Rev. D88 (2013) 7, 076009 [arXiv:1308.1094[hep-ph]]]

# Anomalous $ttZ$ couplings



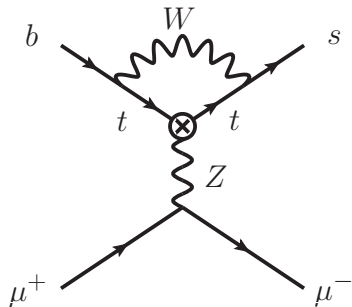
# Direct bounds on anomalous $t\bar{t}Z$ couplings



- $t\bar{t}Z$  production at NLO  
[Röntsch, Schulze, arXiv:1404.1005]
- $\approx 20\% - 30\%$  deviation from SM still allowed even with  $3000 \text{ fb}^{-1}$

# Basic idea

- Can we constrain anomalous  $t\bar{t}Z$  couplings by precision observables?
- Yes – using mixing via electroweak loops
- Need to make (only a few) assumptions



# Assumption I: Operators in the UV

- At NP scale  $\Lambda$ , only the following operators have nonzero coefficients:

$$Q_{Hq}^{(3)} \equiv (H^\dagger i \overleftrightarrow{D}_\mu^a H)(\bar{Q}_{L,3} \gamma^\mu \sigma^a Q_{L,3}),$$

$$Q_{Hq}^{(1)} \equiv (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{Q}_{L,3} \gamma^\mu Q_{L,3}),$$

$$Q_{Hu} \equiv (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{t}_R \gamma^\mu t_R).$$

- Here,  $Q_{L,3}^T = (t_L, V_{ti} d_{L,i})$
- Only these operators induce tree-level  $t\bar{t}Z$  couplings

## Assumption II: LEP bounds

- After EWSB these operators induce

$$\mathcal{L}' = g'_R \bar{t}_R \not{Z} t_R + g'_L \bar{t}_L \not{Z} t_L + g''_L V_{3i}^* V_{3j} \bar{d}_{L,i} \not{Z} d_{L,j} + (k_L \bar{t}_L W^+ b_L + \text{h.c.})$$

$$g'_R \propto C_{Hu}, \quad g'_L \propto C_{Hq}^{(3)} - C_{Hq}^{(1)}, \quad g''_L \propto C_{Hq}^{(3)} + C_{Hq}^{(1)}, \quad k_L \propto C_{Hq}^{(3)}$$

- LEP data on  $Z \rightarrow b\bar{b}$  constrain  $g''_L = 0$  within permil precision
- $C_{Hq}^{(3)}(\Lambda) + C_{Hq}^{(1)}(\Lambda) = 0$
- This scenario could be realized with vector-like quarks  
[del Aguila et al., hep-ph/0007316]

# Assumption III: Only top Yukawa

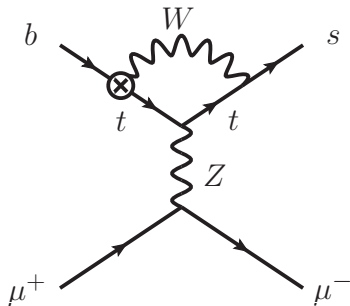
- Only the top-quark Yukawa is nonvanishing
- Neglect other Yukawas in RGE
- Our basis then comprises the leading operators in MFV counting
  - E.g.  $\bar{Q}_L Y_u Y_u^\dagger Q_L$
- Comment later on deviations from that assumption

# A Comment on the Literature

- In [arxiv:1112.2674, arxiv:1301.7535, arxiv:1109.2357] indirect bounds on  $qtZ$ ,  $tbW$  couplings have been derived using a similar approach
- They calculated the diagrams, with  $\Lambda \sim M_W$ :

$$\mathcal{A} = \frac{g^2}{16\pi^2} \left( A + B \log \frac{\mu_W}{\Lambda} \right)$$

- Note that the finite part  $A$  is **scheme dependent!**



# Getting the bounds: RG Mixing

- The RG induces mixing into [Jenkins et al., 2013; see also Brod et al. 2014]
  - $Q_{\phi q,ii}^{(3)} \equiv (\phi^\dagger i \overleftrightarrow{D}_\mu^a \phi)(\bar{Q}_{L,i} \gamma^\mu \sigma^a Q_{L,i}) \rightarrow b\bar{b}Z$
  - $Q_{\phi q,ii}^{(1)} \equiv (\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{Q}_{L,i} \gamma^\mu Q_{L,i}) \rightarrow b\bar{b}Z$
  - $Q_{lq,33jj}^{(3)} \equiv (\bar{Q}_{L,3} \gamma_\mu \sigma^a Q_{L,3})(\bar{L}_{L,j} \gamma^\mu \sigma^a L_{L,j}) \rightarrow \text{rare K / B}$
  - $Q_{lq,33jj}^{(1)} \equiv (\bar{Q}_{L,3} \gamma_\mu Q_{L,3})(\bar{L}_{L,j} \gamma^\mu L_{L,j}) \rightarrow \text{rare K / B}$
  - $Q_{\phi D} \equiv |\phi^\dagger D_\mu \phi|^2 \rightarrow \text{T parameter}$

## Results – Useless Form

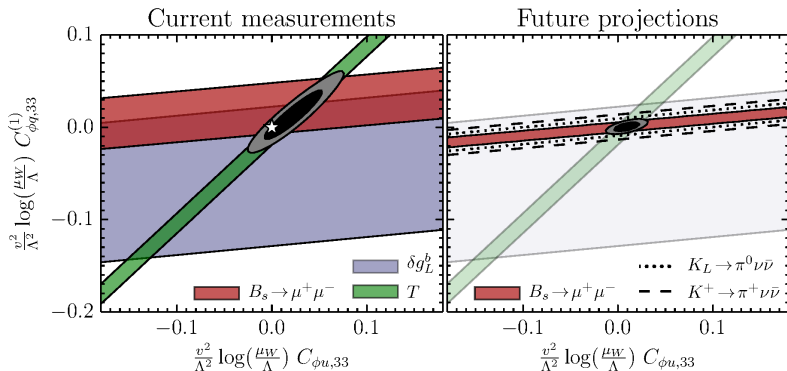
$$\delta g_L^b = -\frac{e}{2s_w c_w} \frac{v^2}{\Lambda^2} \frac{\alpha}{4\pi} \left\{ V_{33}^* V_{33} \left[ \frac{x_t}{2s_w^2} \left( 8C_{\phi q,33}^{(1)} - C_{\phi u} \right) + \frac{17c_w^2 + s_w^2}{3s_w^2 c_w^2} C_{\phi q,33}^{(1)} \right] \right. \\ \left. + \left[ \frac{2s_w^2 - 18c_w^2}{9s_w^2 c_w^2} C_{\phi q,33}^{(1)} + \frac{4}{9c_w^2} C_{\phi u} \right] \right\} \log \frac{\mu_W}{\Lambda}.$$

$$\delta T = -\frac{v^2}{\Lambda^2} \left[ \frac{1}{3\pi c_w^2} \left( C_{\phi q,33}^{(1)} + 2C_{\phi u,33} \right) + \frac{3x_t}{2\pi s_w^2} \left( C_{\phi q,33}^{(1)} - C_{\phi u,33} \right) \right] \log \frac{\mu_W}{\Lambda}.$$

$$\delta Y^{\text{NP}} = \delta X^{\text{NP}} = \frac{x_t}{8} \left( C_{\phi u} - \frac{12 + 8x_t}{x_t} C_{\phi q,33}^{(1)} \right) \frac{v^2}{\Lambda^2} \log \frac{\mu_W}{\Lambda},$$



# Results – Useful Form



$T$	$0.08 \pm 0.07$	[Ciuchini et al., arxiv:1306.4644]
$\delta g_L^b$	$0.0016 \pm 0.0015$	[Ciuchini et al., arxiv:1306.4644]
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ [CMS]	$(3.0_{-0.9}^{+1.0}) \times 10^{-9}$	[CMS, arxiv:1307.5025]
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ [LHCb]	$(2.9_{-1.0}^{+1.1}) \times 10^{-9}$	[LHCb, arxiv:1307.5024]
$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$(1.73_{-1.05}^{+1.15}) \times 10^{-10}$	[E949, arxiv:0808.2459]

## How general are our results?

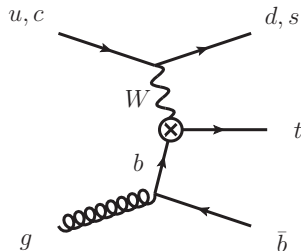
- A generic NP model can generate FCNC transitions in the up sector
- Consider models with large enhancement of the bottom Yukawa (2HDM. . .)
- Assume MFV – e.g., now, have  $\bar{Q}_L(Y_u Y_u^\dagger + Y_d Y_d^\dagger)Q_L$
- Large bottom Yukawa induces flavor off-diagonal operators in the up sector
- They will contribute to FCNC top decays and  $D - \bar{D}$  mixing
- These effects are suppressed by powers of  $\lambda \equiv |V_{us}|$
- $D - \bar{D}$  mixing is suppressed by  $\lambda^{10} \approx 10^{-7}$
- top-FCNC decays:

$$\text{Br}(t \rightarrow cZ) \simeq \frac{\lambda^4 v^4}{\Lambda^4} \left[ \left( C_{\phi q,33}^{(3)} - C_{\phi q,33}^{(1)} \right)^2 + C_{\phi u,33}^2 \right].$$

- $\text{Br}(t \rightarrow cZ) < 0.05\%$  [CMS, arxiv:1312.4194]  $\Rightarrow$  not competitive

# $t$ -channel single top production

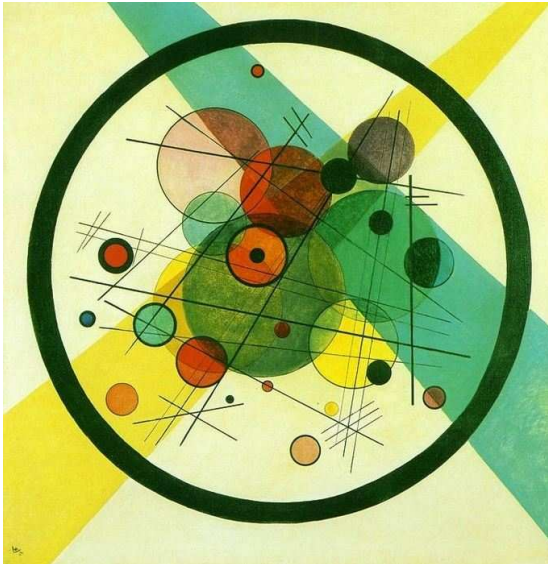
- $\sqrt{\sigma(t)/\sigma_{\text{SM}}(t)} = 0.97(10)$   
[ATLAS-CONF-2014-007]
- $\sqrt{\sigma(t)/\sigma_{\text{SM}}(t)} = 0.998(41)$  [CMS, arxiv:1403.7366]
- $t$ -channel single top production constrains  
 $v^2 C_{Hq}^{(3)}/\Lambda^2 = -0.006 \pm 0.038$  [arxiv:1408.0792]



# Summary

- LHC experiments and precision observables put complementary constraints on anomalous Higgs and Z couplings
- EMDs yield strong constraints on CP-violating Yukawa couplings
- FCNC down-sector transitions yield strong constraints on up-sector diagonal couplings
- Most bounds will improve in the future
- What about the small (e, u, d, ...) Yukawa couplings? [work in progress]

# Outlook



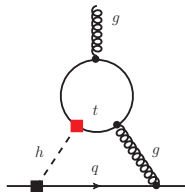
# Appendix

# Mercury EDM

- Diamagnetic atoms also provide constraints
- $|d_{\text{Hg}}/e| < 3.1 \times 10^{-29} \text{ cm}$  (95% CL) [Griffith et al., 2009]
- Dominant contribution from CP-odd isovector pion-nucleon interaction

$$\frac{d_{\text{Hg}}}{e} = - \left( 4_{-2}^{+8} \right) \left[ 3.1 \tilde{\kappa}_t - 3.2 \cdot 10^{-2} \kappa_t \tilde{\kappa}_t \right] \cdot 10^{-29} \text{ cm}$$

- Again,  $w \propto \kappa_t \tilde{\kappa}_t$  subdominant, but does not vanish if Higgs does not couple to light quarks

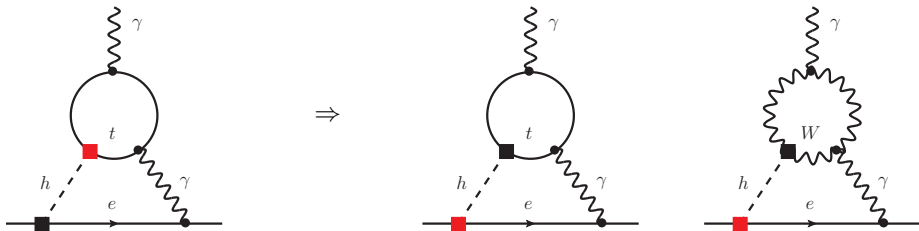


# What do we know about the electron Yukawa?



# Indirect bounds: electron EDM

- A different look at Barr & Zee:



- $|d_e/e| < 8.7 \times 10^{-29}$  cm (90% CL) [ACME 2013]
- leads to  $|\tilde{\kappa}_e| < 0.0013$  (for  $\kappa_t = 1$ )

# Indirect bounds: electron $g - 2$

- Usually, measurement of  $a_e \equiv (g - 2)_e/2$  used to extract  $\alpha$
- Using independent  $\alpha$  measurement, can make a prediction for  $a_e$   
[Giudice et al., arXiv:1208.6583]
- With
  - $\alpha = 1/137.035999037(91)$  [Bouchendira et al., arXiv:1012.3627]
  - $a_e = 11596521807.3(2.8) \times 10^{-13}$  [Gabrielse et al. 2011]
- ... I find  $|\kappa_e| \lesssim 3000$
- Bound expected to improve by a factor of 10

# Direct collider bounds

$$\text{Br}(h \rightarrow e^+e^-) = \frac{(\kappa_e^2 + \tilde{\kappa}_e^2) \text{Br}(h \rightarrow e^+e^-)_{\text{SM}}}{1 + (\kappa_e^2 + \tilde{\kappa}_e^2 - 1) \text{Br}(h \rightarrow e^+e^-)_{\text{SM}}}$$

- CMS limit  $\text{Br}(h \rightarrow e^+e^-) < 0.0019$  [CMS, arxiv:1410.6679]  
leads to  $\sqrt{\kappa_e^2 + \tilde{\kappa}_e^2} < 611$
- LEP bound (via radiative return) probably not competitive
- A future  $e^+e^-$  machine...
  - collecting  $100 \text{ fb}^{-1}$  on the Higgs resonance
  - assuming 25 MeV beam energy spread
- ... can push the limit to  $\sqrt{\kappa_e^2 + \tilde{\kappa}_e^2} \lesssim 10$