

NNLL RESUMMATION

A NOVEL APPROACH



ANDREA
BANFI



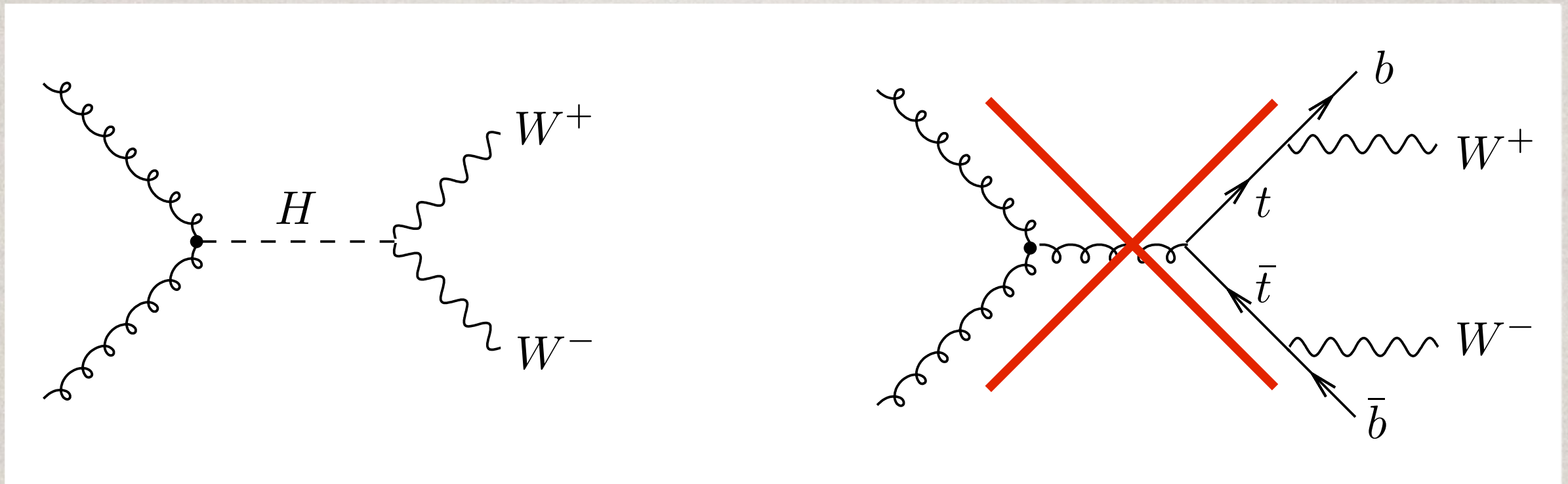
IN COLLABORATION WITH
H. MCASLAN, P.F. MONNI AND G. ZANDERIGHI

OUTLINE

- Motivations
- State of the art of QCD resummations
- General technique for QCD resummations
 - Observable's properties
 - Amplitudes
 - Relevant phase space regions
- Applications in e^+e^- annihilation
- Current work in progress and outlook

AN EXAMPLE: JET-VETO

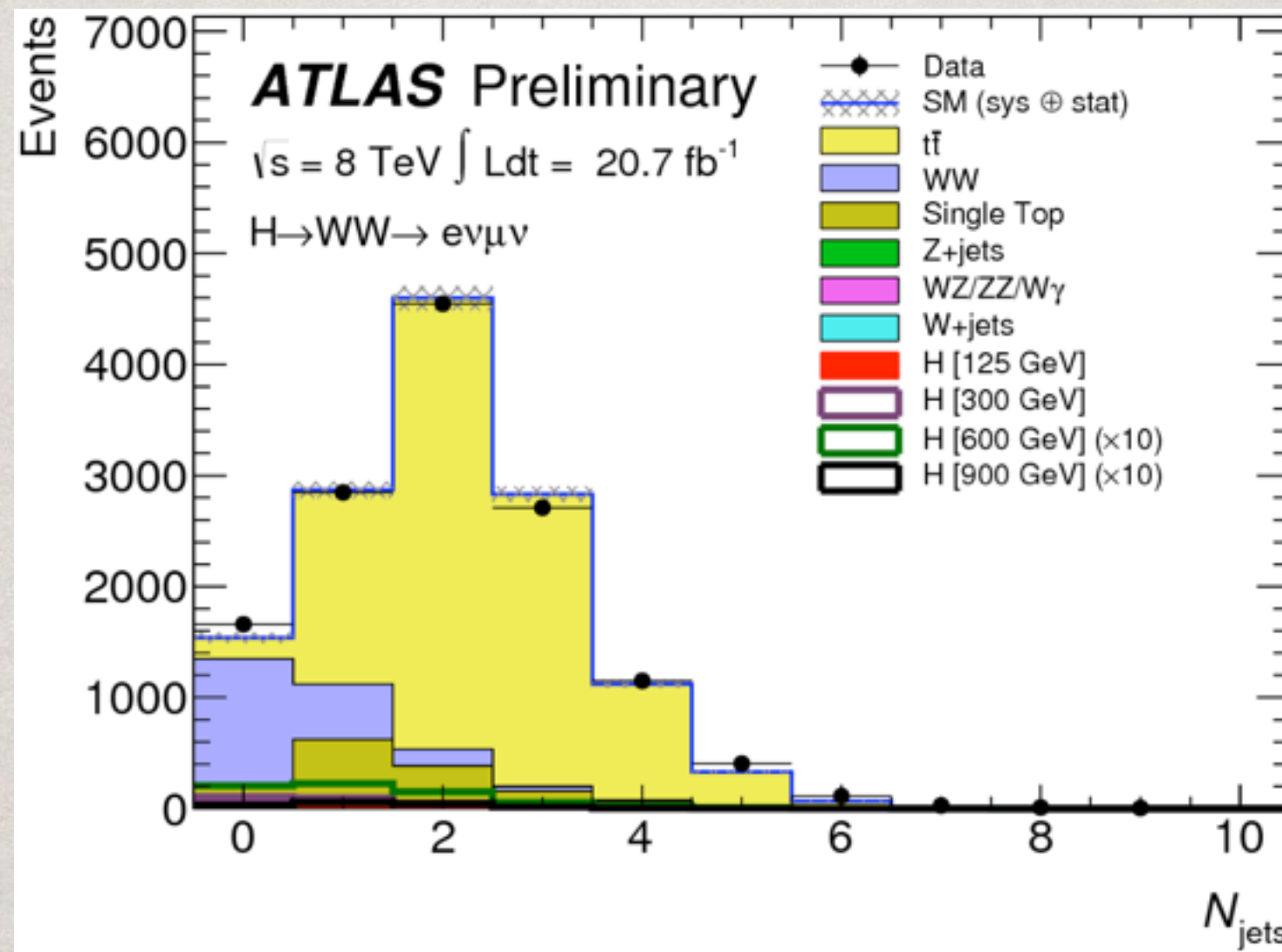
- Example: Higgs decaying into WW suffers from a large background from top-antitop production



- Each top quark decays into a b-jet \Rightarrow veto events with jets in the final state
- Jet-vetoes are employed in many LHC analyses (e.g. vector-boson cross sections, boosted Higgs searches, etc.)

HOW DO WE VETO JETS?

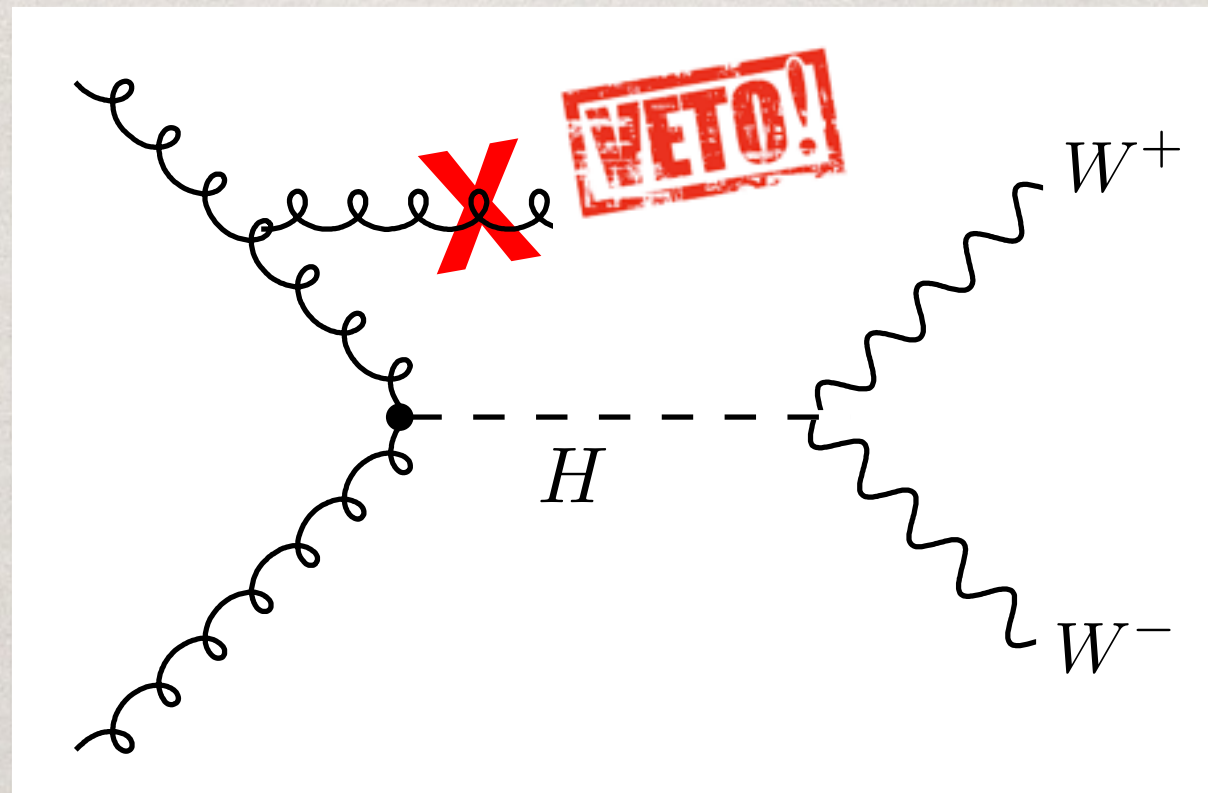
- We require that all jets with transverse momentum smaller than $p_{t,\text{veto}}$



- The zero-jet cross section $\sigma_{0\text{-jet}}$ is least contaminated by the huge (yellow) top-antitop background

INFRARED SENSITIVITY

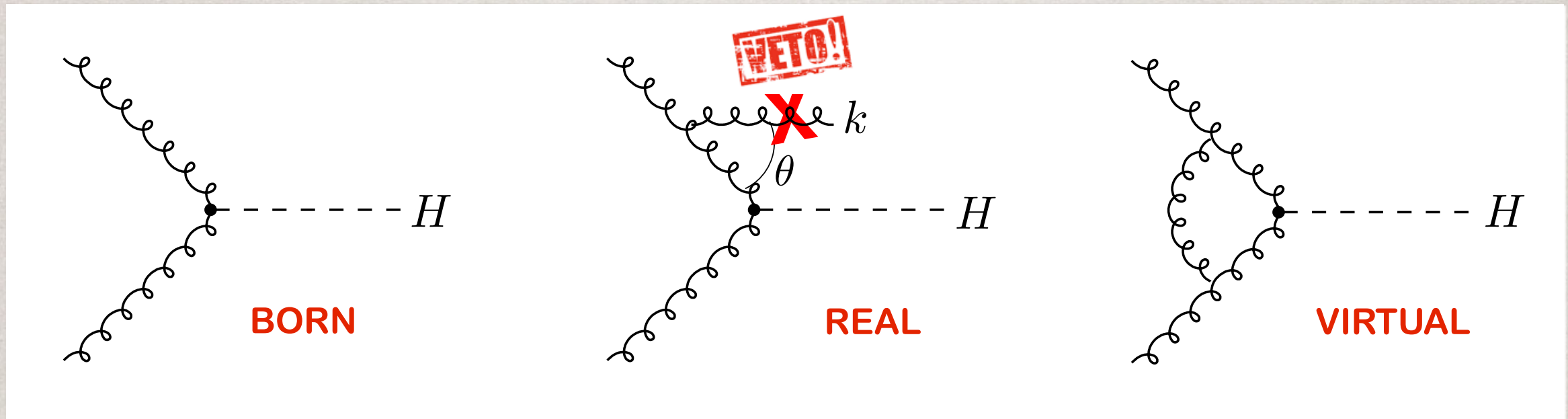
- The 0-jet cross section is characterised by two scales, the Higgs mass m_H and the jet resolution $p_{t,\text{veto}}$



- In QCD, logarithms $\ln(m_H/p_{t,\text{veto}})$ appear whenever the phase space for the emission of soft and/or collinear gluons is restricted

ONE GLUON EMISSION

- Example: veto one soft ($E \ll m_H$) and collinear ($\theta \ll 1$) gluon k



$$\sigma_0 \left[1 + C_A \frac{\alpha_s}{\pi} \int \overset{\text{soft}}{\frac{dE}{E}} \overset{\text{collinear}}{\frac{d\theta^2}{\theta^2}} \Theta(p_{t,\text{veto}} - E\theta) - C_A \frac{\alpha_s}{\pi} \int \frac{dE}{E} \frac{d\theta^2}{\theta^2} \right]$$

factorisation of
soft radiation

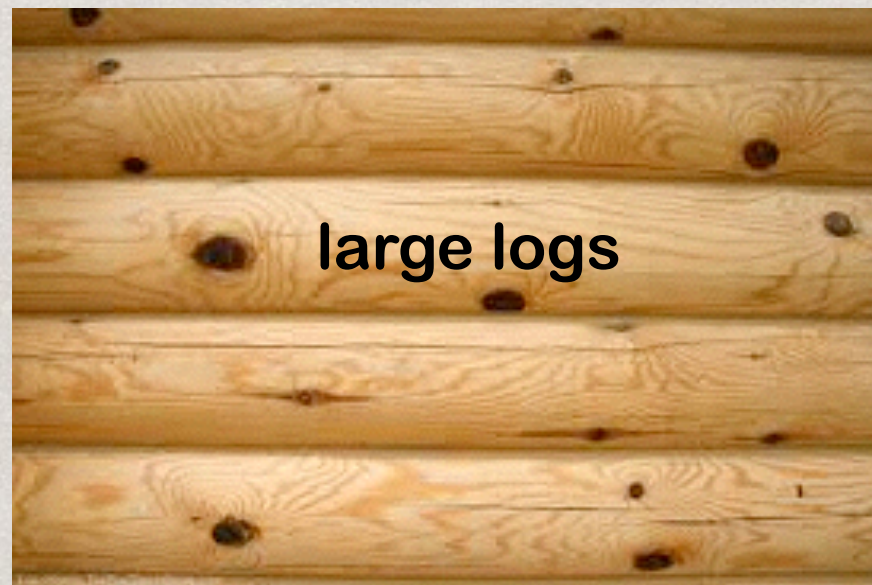
$$\sigma_{0-\text{jet}} = \sigma_0 \left[1 - C_A \frac{\alpha_s}{\pi} \ln^2 \left(\frac{m_H}{p_{t,\text{veto}}} \right) \right]$$

ALL-ORDER 0-JET CROSS SECTION

- The zero-jet cross section contains logarithmic contributions which can become large when $p_{t,\text{veto}} \ll m_H$

$$\sigma_{0\text{-jet}} \simeq \underbrace{\sigma_0}_{\text{LO}} \left(1 - \underbrace{2C_A \frac{\alpha_s(m_H)}{\pi}}_{\text{NLO}} \ln^2 \frac{m_H}{p_{t,\text{veto}}} + \dots \right)$$

breakdown of perturbation theory!



ALL-ORDER O-JET CROSS SECTION

- All-order resummation of large logarithms \Rightarrow reorganisation of the PT series in the region $\alpha_s L \sim 1$, with $L = \ln(m_H/p_{t,\text{veto}})$

$$\sigma_{0\text{-jet}} \sim \sigma_0 \exp \left[\underbrace{Lg_1(\alpha_s L)}_{\text{LL}} + \underbrace{g_2(\alpha_s L)}_{\text{NLL}} + \underbrace{\alpha_s g_3(\alpha_s L)}_{\text{NNLL}} + \dots \right]$$



ALL-ORDER O-JET CROSS SECTION

- All-order resummation of large logarithms \Rightarrow reorganisation of the PT series in the region $\alpha_s L \sim 1$, with $L = \ln(m_H/p_{t,\text{veto}})$

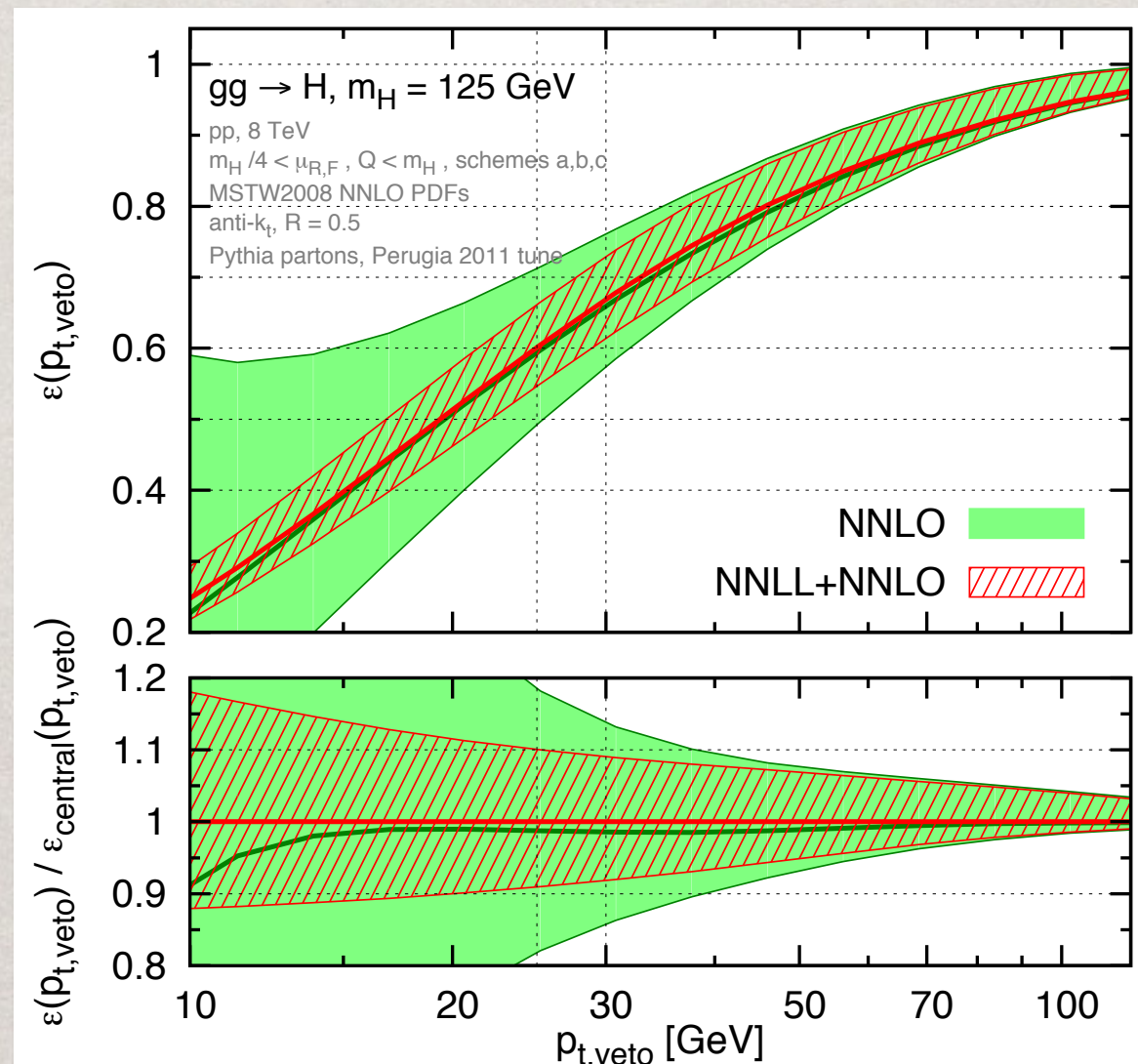
$$\sigma_{0\text{-jet}} \sim \sigma_0 e^{\underbrace{Lg_1(\alpha_s L)}_{\text{LL}}} \times \left(\underbrace{1}_{\text{NLL}} + \underbrace{\alpha_s G_2(\alpha_s L)}_{\text{NLL}} + \underbrace{\alpha_s G_3(\alpha_s L)}_{\text{NNLL}} + \dots \right)$$



PREDICTIONS FOR JET-VETO EFFICIENCY

- Jet-veto efficiency $\epsilon(p_{t,\text{veto}}) = \sigma_{0\text{-jet}} / \sigma_{\text{tot}}$

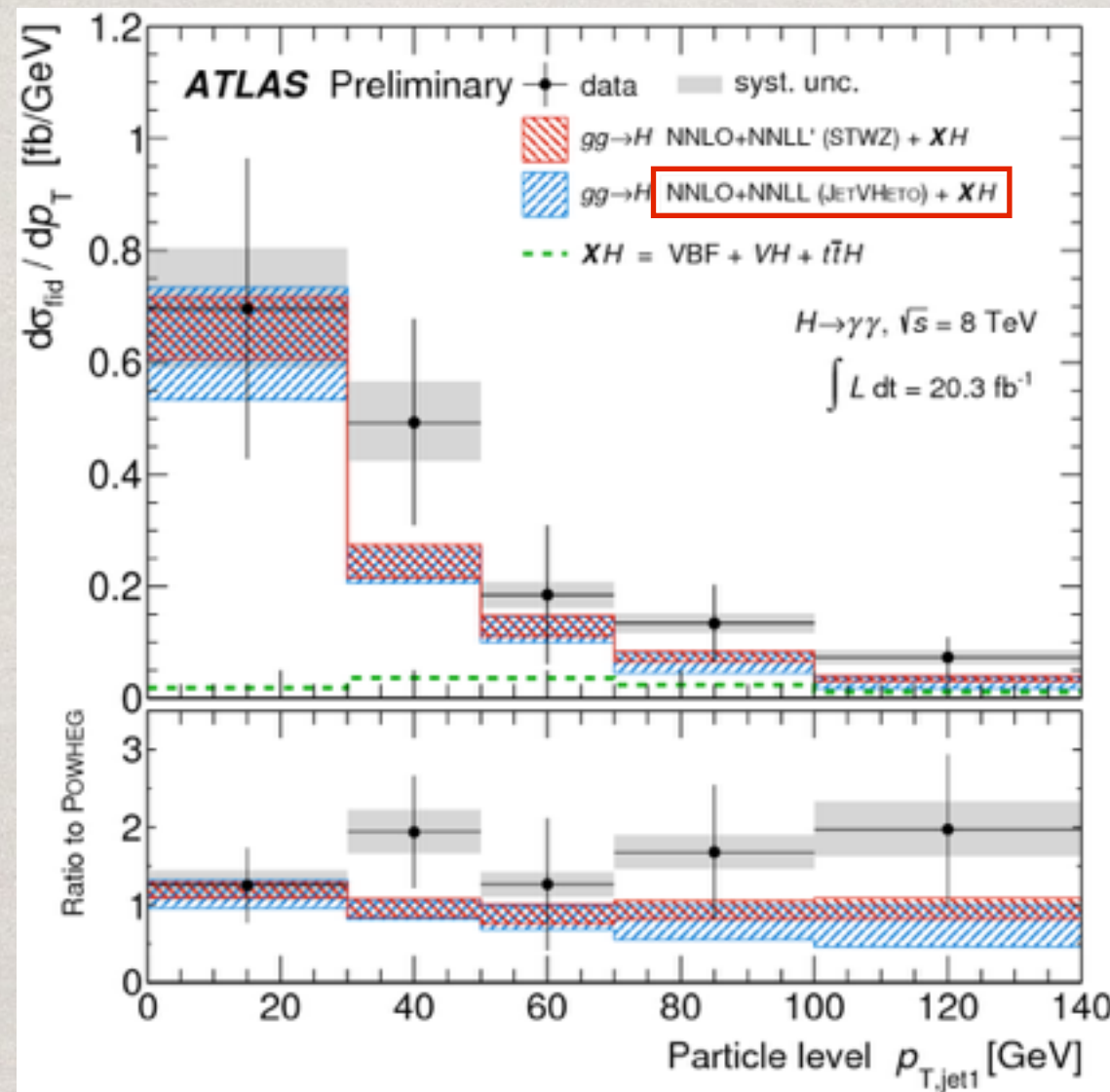
[AB Monni Salam Zanderighi]



- Reduction of theoretical uncertainty from NNLO to NNLL+NNLO

COMPARISON TO DATA

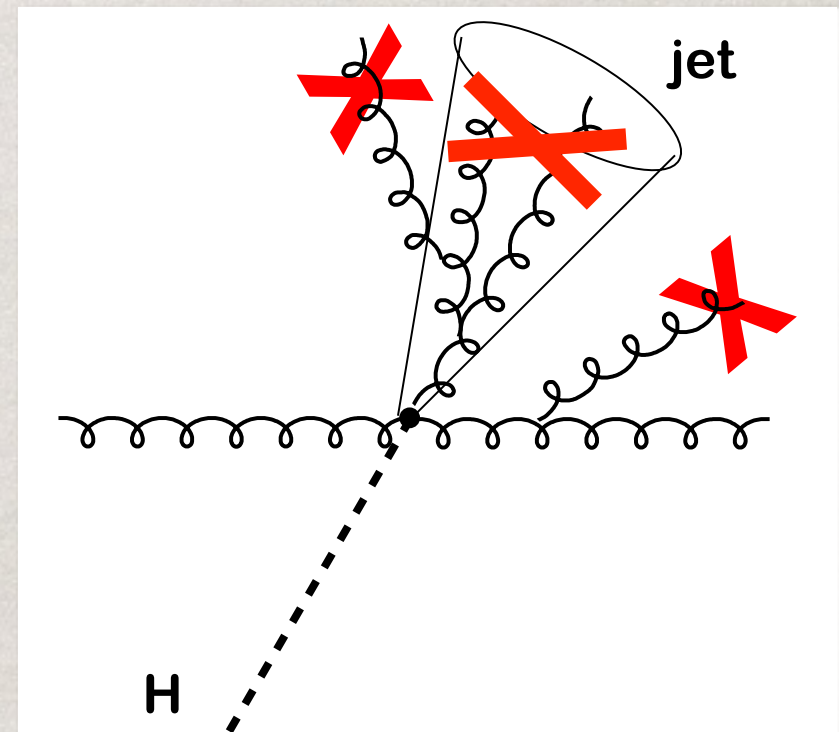
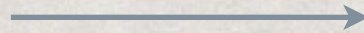
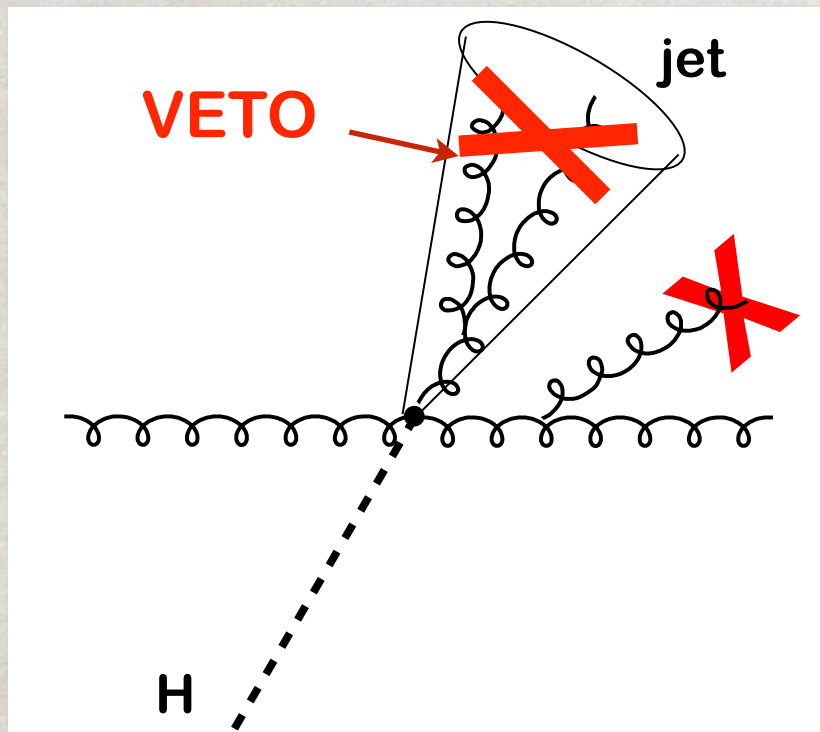
- With existing data it is already possible to have a measurement of $\sigma_{0\text{-jet}}$



- Good agreement with data in the zero-jet bin
- The leading-jet p_t spectrum is underestimated at high p_t , but there VBF and NNLO corrections to Higgs+1jet are missing

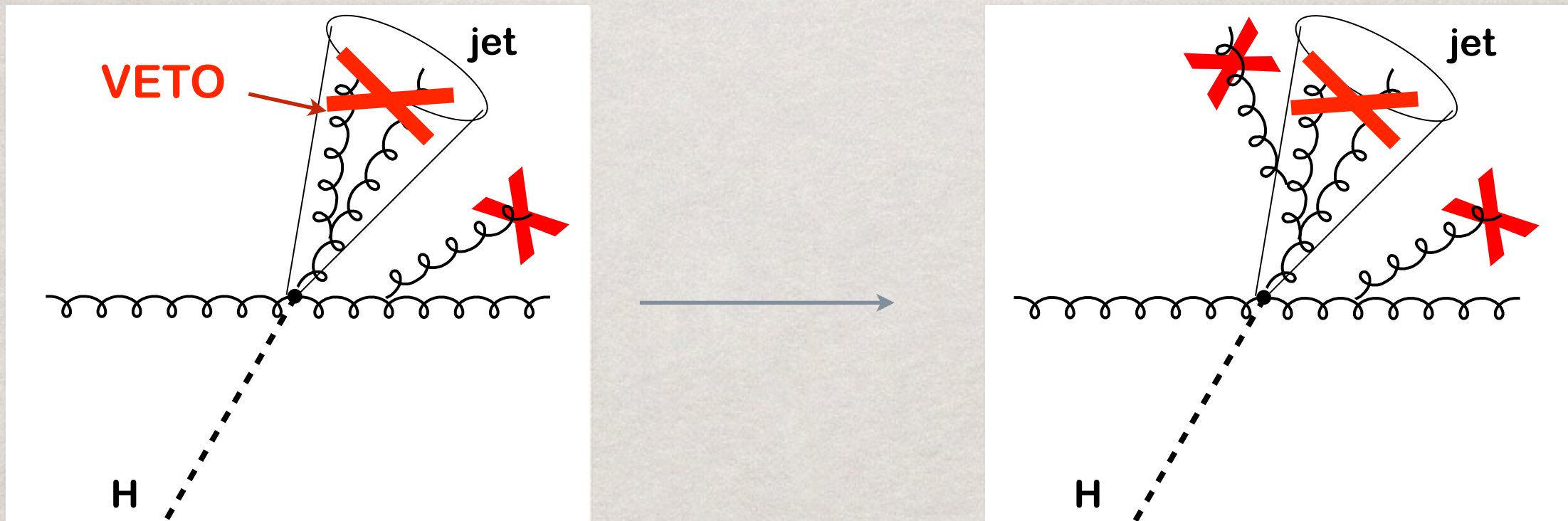
BEYOND ZERO JETS

- The 0-jet cross section has the special property that is sensitive to soft and collinear gluons everywhere in the phase space



BEYOND ZERO JETS

- The 0-jet cross section has the special property that is sensitive to soft and collinear gluons everywhere in the phase space

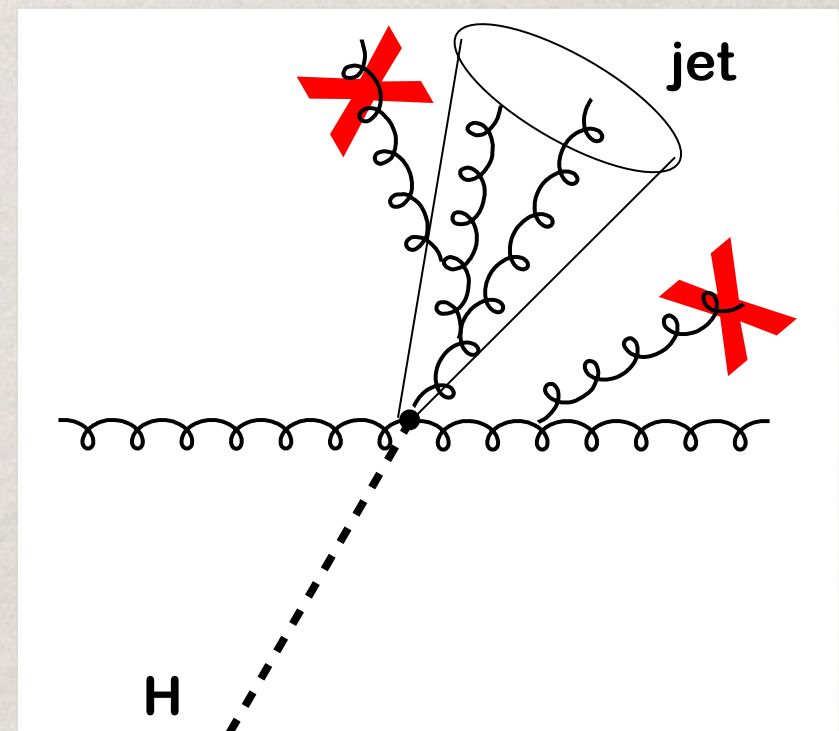
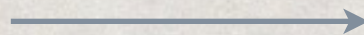
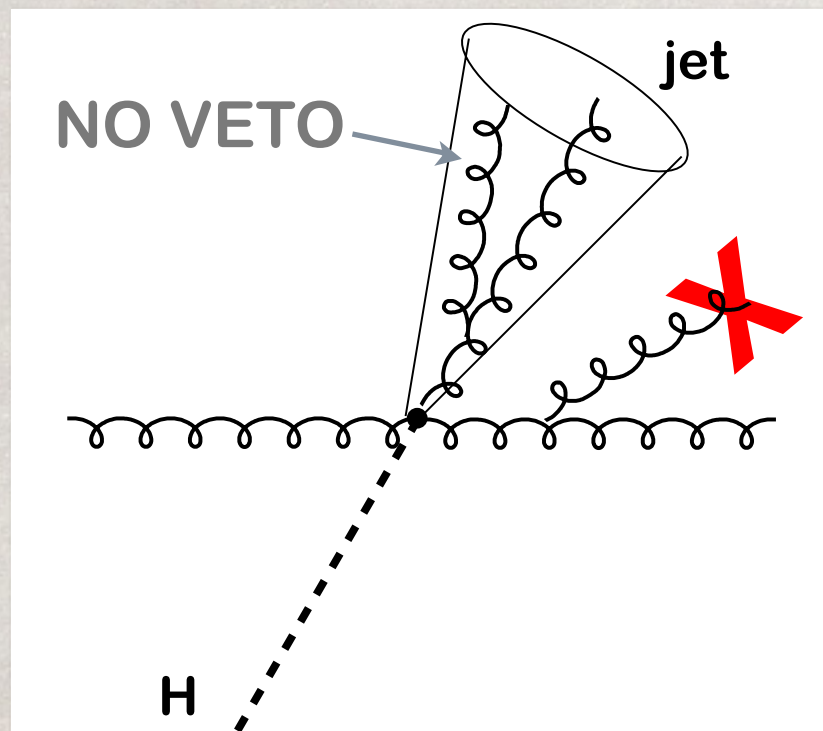


- Gluon splitting close to the jet boundary gives a small contribution, of relative order α_s , hence NNLL

[AB Salam Zanderighi]

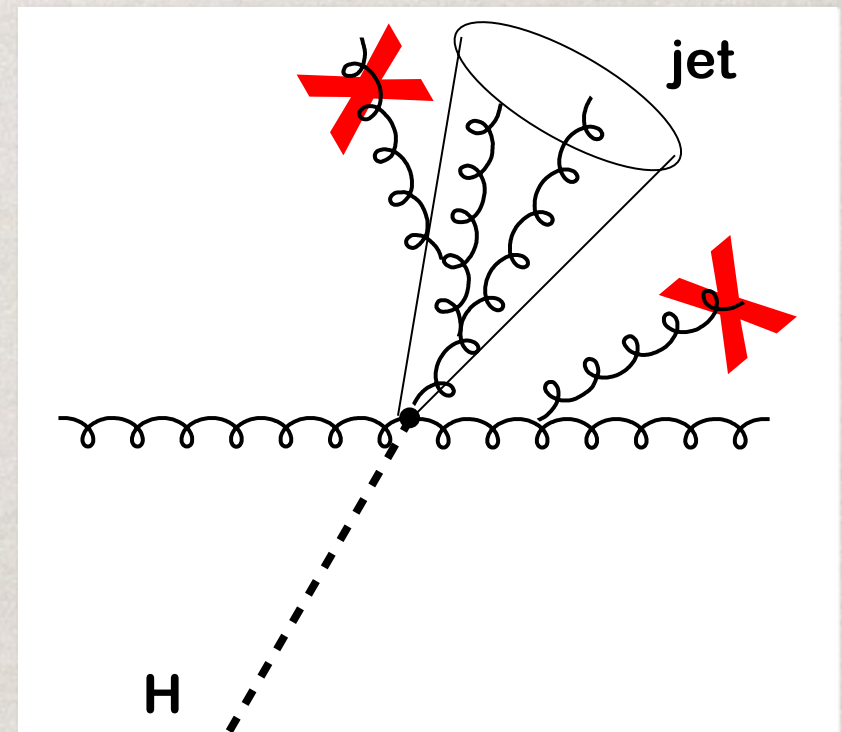
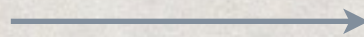
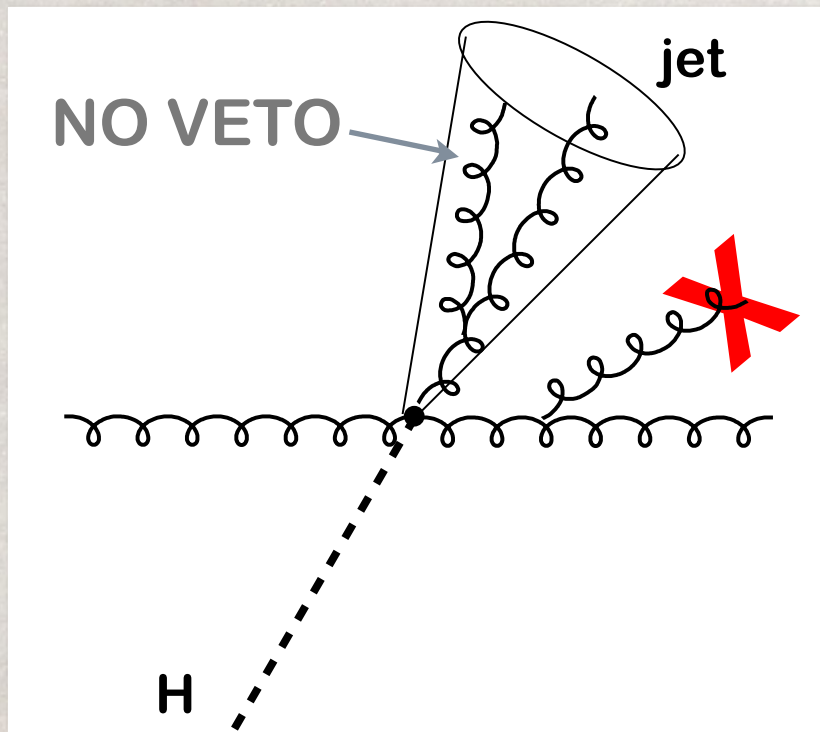
BEYOND ZERO JETS

- The one-jet exclusive cross section is insensitive to emissions inside the tagged jet \Rightarrow new logarithmic contributions for $p_{t,\text{veto}} \ll p_{t,\text{jet}}$



BEYOND ZERO JETS

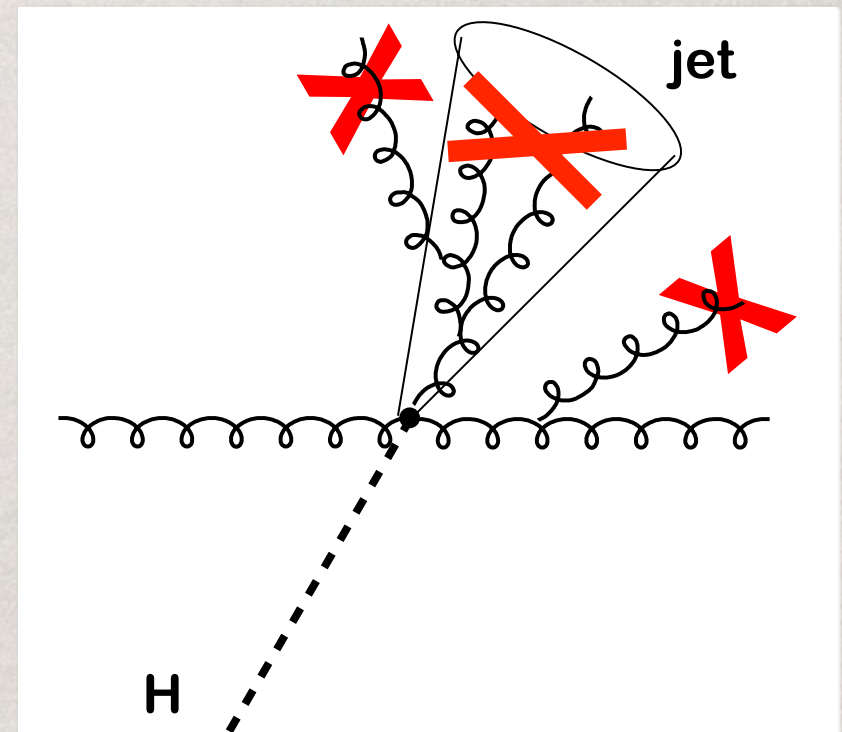
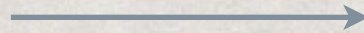
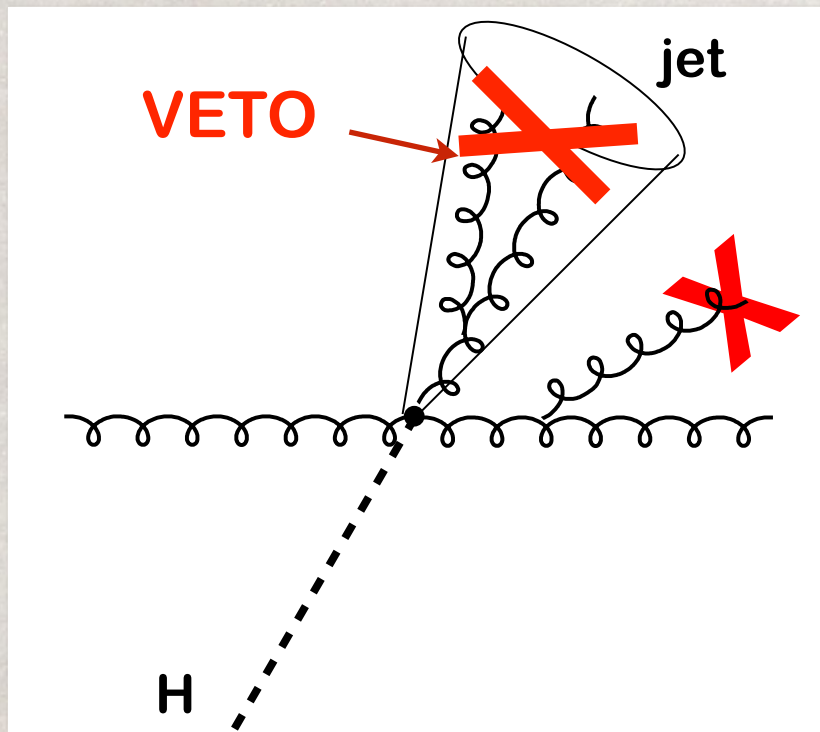
- The one-jet exclusive cross section is insensitive to emissions inside the tagged jet \Rightarrow new logarithmic contributions for $p_{t,\text{veto}} \ll p_{t,\text{jet}}$



- Gluon splitting close to the jet boundary gives contributions of order $\alpha_s L$, called non-global and clustering logarithms, large for $p_{t,\text{veto}} \ll p_{t,\text{jet}}$
[Dasgupta Salam; Appleby Seymour; AB Dasgupta]
- Non-global logarithms known only in the large- N_c limit \Rightarrow we restrict ourselves to global observables

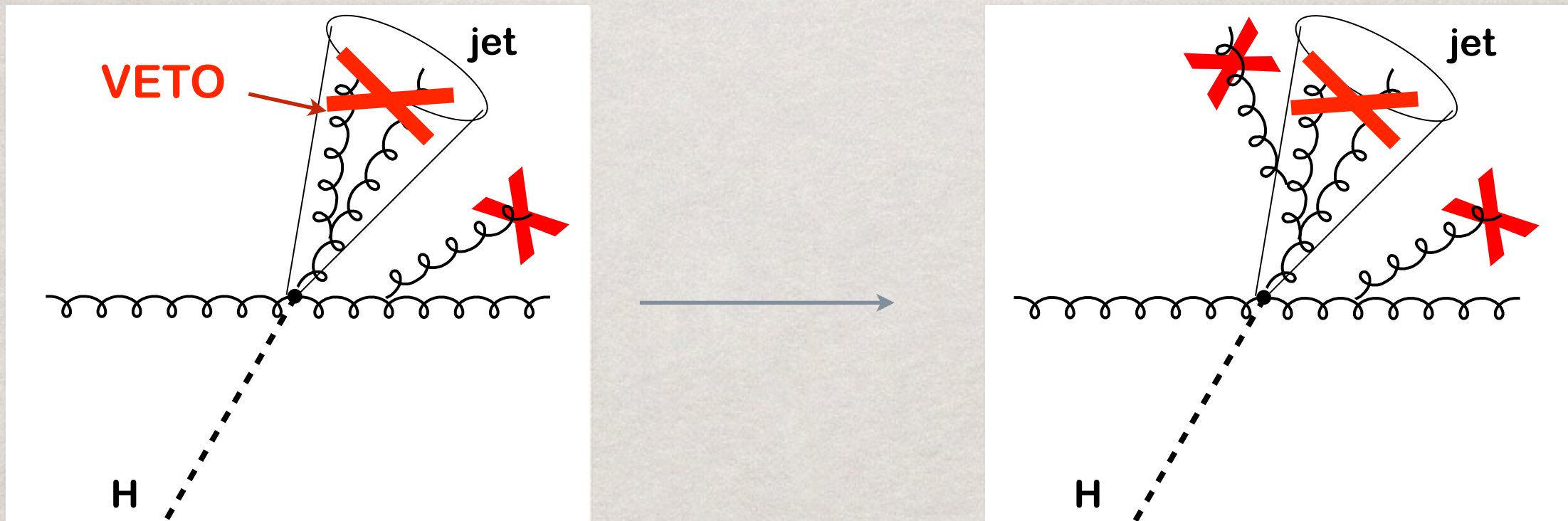
BEYOND ZERO JETS

- One can veto emissions inside the tagged jet as well, for instance imposing a cut on the resolution of sub-jets inside the leading jet



BEYOND ZERO JETS

- One can veto emissions inside the tagged jet as well, for instance imposing a cut on the resolution of sub-jets inside the leading jet



- Besides its theoretical interest, a NNLL resummation of a global one-jet exclusive cross section has important applications
 - measurements of the QCD coupling
 - matching of parton-shower event generators with exact NNLO

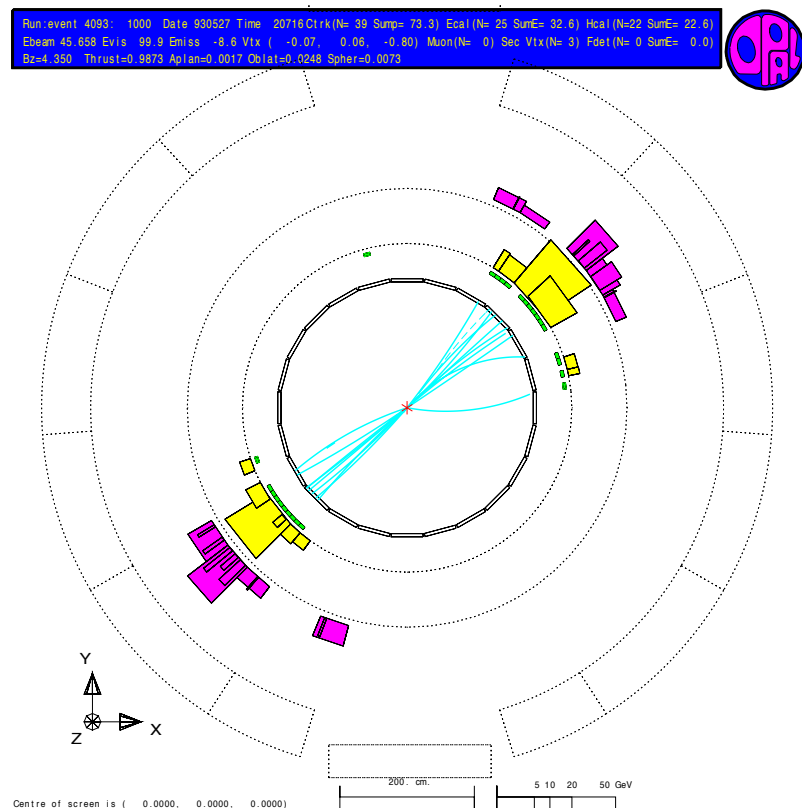
[Hamilton Nason Zanderighi; Hoeche et al]

FINAL-STATE OBSERVABLES

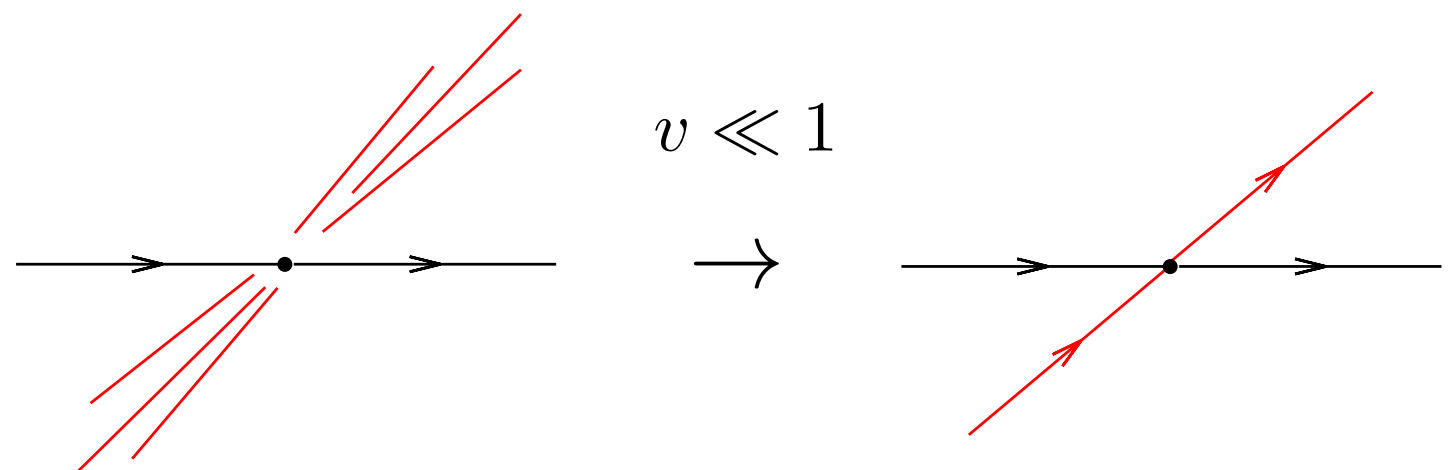
- We consider a generic final-state observable, a function $V(p_1, \dots, p_n)$ of all possible final-state momenta p_1, \dots, p_n
- Examples: leading jet transverse momentum in Higgs production or thrust in $e^+e^- \rightarrow \text{hadrons}$

$$\frac{p_{t,\max}}{m_H} = \max_{j \in \text{jets}} \frac{p_{t,j}}{m_H}$$

$$T \equiv \max_{\vec{n}} \frac{\sum_i |\vec{p}_i \cdot \vec{n}|}{\sum_i |\vec{p}_i|}$$



$$\Sigma(v) = \text{Prob}[V(p_1, \dots, p_n) < v]$$



NLL RESUMMATION

- Several NLL exist for a number of observables (extensive literature ~1 observable per article)
- (~) 4 approaches to Sudakov resummation are available
 - Branching algorithm
[Catani Marchesini Webber et al.]
Resummation achieved through factorisation of cross section into leading kinematic subprocesses and subsequent RGE evolution
 - Soft Collinear Effective Theory (SCET)
[Bauer Fleming Pirol Stewart Beneke Becher Neubert et al.]
 - Collins-Soper-Sterman factorisation theorems
[Collins Soper Sterman Kidanakis Laenen Magnea et al.]
 - CAESAR approach
[Banfi Salam Zanderighi]
Resummation achieved by simulating (numerically) the QCD radiation to all orders in perturbation theory
- From CAESAR onwards, NLL resummation is a solved problem (at least for rIRC safe observables)

RESUMMATION BEYOND NLL

- How many approaches to resummations survive beyond NLL?
 - Branching algorithm
[Catani Marchesini Webber et al.]
 - Soft Collinear Effective Theory (SCET)
[Bauer Fleming Pirol Stewart Beneke Becher Neubert et al.]
 - Collins-Soper-Sterman factorisation theorems
[Collins Soper Sterman Kidonakis Laenen Magnea et al.]
 - CAESAR approach
[Banfi Salam Zanderighi]
- Only SCET and CSS formalism are able to go beyond NLL accuracy, but with factorisation formulae that are observable dependent
- Is it possible to devise a synergy for a new, more powerful approach?

STATE OF THE ART

- NNLL corrections are often sizeable and important for precision physics
- Few results exist in e^+e^- annihilation, and even fewer in hadron collisions
- The most important limitation is the analytical treatment of the observable in some (smartly defined) conjugate space \Rightarrow resummation often leads to very tedious calculations (~ 14 - 16 years to go from NLL to NNLL)
- **GOAL:** devise a semi-numerical approach that:
 - does not rely on analytical properties of the observable
 - is NNLL accurate and extendable to higher orders
 - is fully general for a very broad category of observables (\sim all that can be possibly resummed at NNLL accuracy)
 - is flexible and automated (only input: observable's routine)

DEFINITION OF THE PROBLEM

- The problem consists in computing all-order logarithmic enhanced contributions to a generic final-state observable (e.g. event shape or jet resolution parameter)
- We need to control the behaviour of QCD matrix elements and the observable in the presence of an arbitrary number of soft and/or collinear emission
- We divide the problem (and its solution) in three parts
 - observable's properties
 - amplitudes in the soft/collinear limit
 - relevant phase space regions

OBSERVABLE'S PROPERTIES

- We consider an infrared and collinear (IRC) safe observable normalised as

$$v = V(\{\tilde{p}\}, k_1, \dots, k_n) \leq 1$$

- We study the limit $v \rightarrow 0$
- In this limit, radiative corrections are just virtual corrections and soft/and or collinear emissions \Rightarrow QCD amplitudes factorise

$$|\mathcal{M}(\{\tilde{p}\}, k_1, \dots, k_n)|^2 \simeq |M_{\text{Born}}(\{\tilde{p}\})|^2 |M(k_1, \dots, k_n)|^2 + \dots$$

- Standard approach: full factorisation is achievable only if the constrained phase space (including the observable's definition) factorises \Rightarrow resummation can be achieved once a factorisation theorem is available (and a lot of patience to carry out the calculations)

OBSERVABLE'S PROPERTIES

- Final-state observables (e.g. event shapes) do not trivially factorise in products of terms \Rightarrow integral transforms needed
- Successful for simple very inclusive observables (e.g. thrust in e^+e^-)

$$1 - T \simeq \sum_{i=1}^n \frac{k_{ti}}{Q} e^{-\eta_i} \quad \rightarrow \quad \Theta(1 - T < \tau) = \int \frac{d\nu}{2\pi i \nu} e^{\nu\tau} \prod_{i=1}^n e^{-\nu \frac{k_{ti}}{Q}} e^{-\eta_i}$$

- Cumbersome for more involved observables, like the jet broadening in e^+e^- or the vector boson transverse momentum in hadron collisions
- Impossible for observables in which all emissions cooperate in a non-trivial way (e.g. two-jet rate or thrust minor in e^+e^-)
- Factorisation is a unnecessary request for resummation, all is needed is some scaling properties of the observable

OBSERVABLE REQUIREMENTS

- Parametrisation for a single soft/collinear emission

$$V(\{\tilde{p}\}, k_i) = \zeta_i v$$

- Standard requirement of IRC safety

$$\lim_{\zeta_{n+1} \rightarrow 0} V(\tilde{p}, k_1(\zeta_1), \dots, k_n(\zeta_n), k_{n+1}(\zeta_{n+1})) = V(\tilde{p}, k_1(\zeta_1), \dots, k_n(\zeta_n))$$

soft and/or collinear

- An analogous condition holds for secondary collinear splittings

OBSERVABLE REQUIREMENTS

- Parametrisation for a single soft/collinear emission

$$V(\{\tilde{p}\}, k_i) = \zeta_i v$$

- Further requirements of **recursive IRC safety**

[Banfi Salam Zanderighi]

$$\lim_{v \rightarrow 0} \frac{V(\tilde{p}, k_1(\zeta_1), \dots, k_n(\zeta_n))}{v} = \text{finite (non-zero)}$$

 all emissions simultaneously soft and/or collinear

- This conditions means that the observable scales in the same fashion in the present of one or many emissions
- It is necessary for the exponentiation of double logarithms at all orders

OBSERVABLE REQUIREMENTS

- Parametrisation for a single soft/collinear emission

$$V(\{\tilde{p}\}, k_i) = \zeta_i v$$

- Further requirements of **recursive IRC safety**

[Banfi Salam Zanderighi]

$$\lim_{\zeta_{n+1}} \lim_{v \rightarrow 0} \frac{V(\tilde{p}, k_1(\zeta_1), \dots, k_n(\zeta_n), \underbrace{k_{n+1}(\zeta_{n+1})}_{\text{one emission softer or more collinear than the others}})}{v} = \lim_{v \rightarrow 0} \frac{V(\tilde{p}, k_1(\zeta_1), \dots, k_n(\zeta_n))}{v}$$

all emissions simultaneously
soft and/or collinear

one emission softer or more
collinear than the others

- This conditions ensures that there exists $\epsilon \gg v$ such that we can neglect all emissions with $V(\{\tilde{p}\}, k_i) < \epsilon v$
- An analogous condition holds for secondary collinear splittings

VIRTUAL AND (UNRESOLVED) REAL

- Virtual corrections to the underlying Born process (e.g. $e^+e^- \rightarrow q\bar{q}$) exponentiate
[Parisi; Magnea Sterman]
- We define a subset of (unresolved) emissions such that $V_{\text{sc}}(\{\tilde{p}\}, k_i) < \epsilon v$
 - The soft-collinear approximation for V is enough to ensure the cancellation of infrared singularities with virtual corrections (a different prescription can be used, leaving the final result unchanged)
 - By rIRC safety, these emissions do not generate new logarithms, and can be neglected

$$V(\{\tilde{p}\}, k_1, \dots, k_n, \dots, k_m) \simeq V(\{\tilde{p}\}, k_1, \dots, k_n) + \epsilon^p v$$

- Unresolved emissions are largely unconstrained \Rightarrow exponentiation
[Frenkel Gatheral Taylor; Altarelli Parisi]
- Using rIRC safety and renormalisation group it is possible to show that unresolved emissions and virtual corrections exponentiate at all orders
[known for simple observables + work in progress...]

VIRTUAL AND (UNRESOLVED) REAL

- Unresolved real and virtual corrections give rise to an exponential factor, interpreted as the no emission probability up to the scale ϵv

$$P(\text{no emissions}) \sim e^{-R(\epsilon v)}$$

- Different logarithmic contributions are isolated by expanding around v

$$P(\text{no emissions}) \sim e^{-\underbrace{R(v)}_{\text{LL}} - \underbrace{R'(v) \ln \frac{1}{\epsilon}}_{\text{NLL}} - \frac{1}{2} \underbrace{R''(v) \ln^2 \frac{1}{\epsilon}}_{\text{NNLL}} + \dots}$$

- Owing to the definition of unresolved emissions, the radiator $R(v)$ is the same for all observables that scale in the same way with respect to a single soft-collinear emission
- The remaining terms in the exponent cancel the ϵ -dependence of resolved real emissions

RESOLVED REAL EMISSIONS

- General expression of the cumulative distribution of $V(\{\tilde{p}\}, k_1, \dots, k_n)$

$$\Sigma(v) = \text{Prob}[V(\{\tilde{p}\}, k_1, \dots, k_n) < v] \sim e^{-R(v)} \mathcal{F}(v)$$

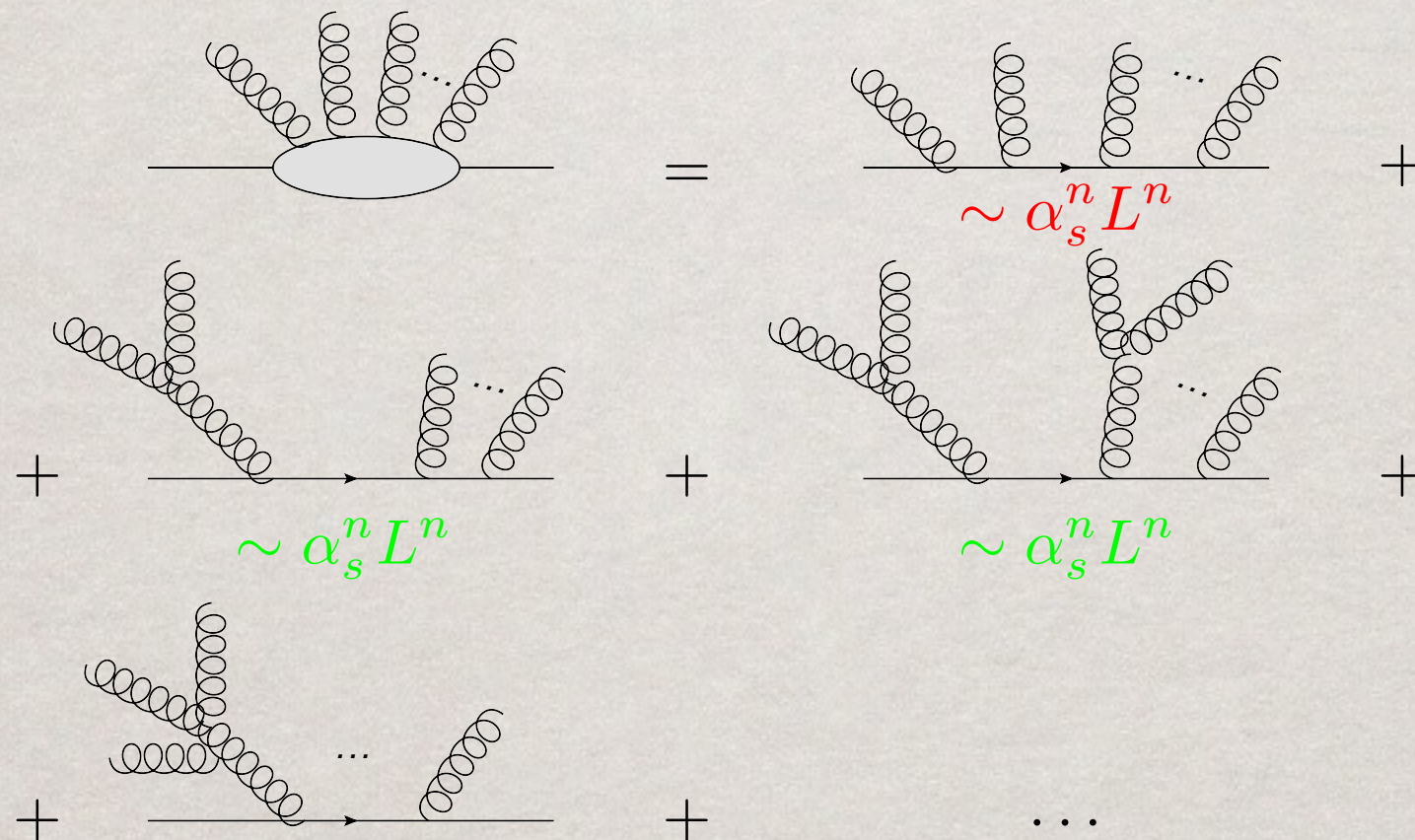
- rIRC safety ensures that
 - all double logarithms are contained in the radiator $R(v)$
 - resolved real emissions are constrained in the region $\epsilon v \lesssim V(\{\tilde{p}\}, k_i) \lesssim v$



resolved real emissions lose one logarithm $\Rightarrow \mathcal{F}(v)$ starts at NLL

SOFT MATRIX ELEMENT

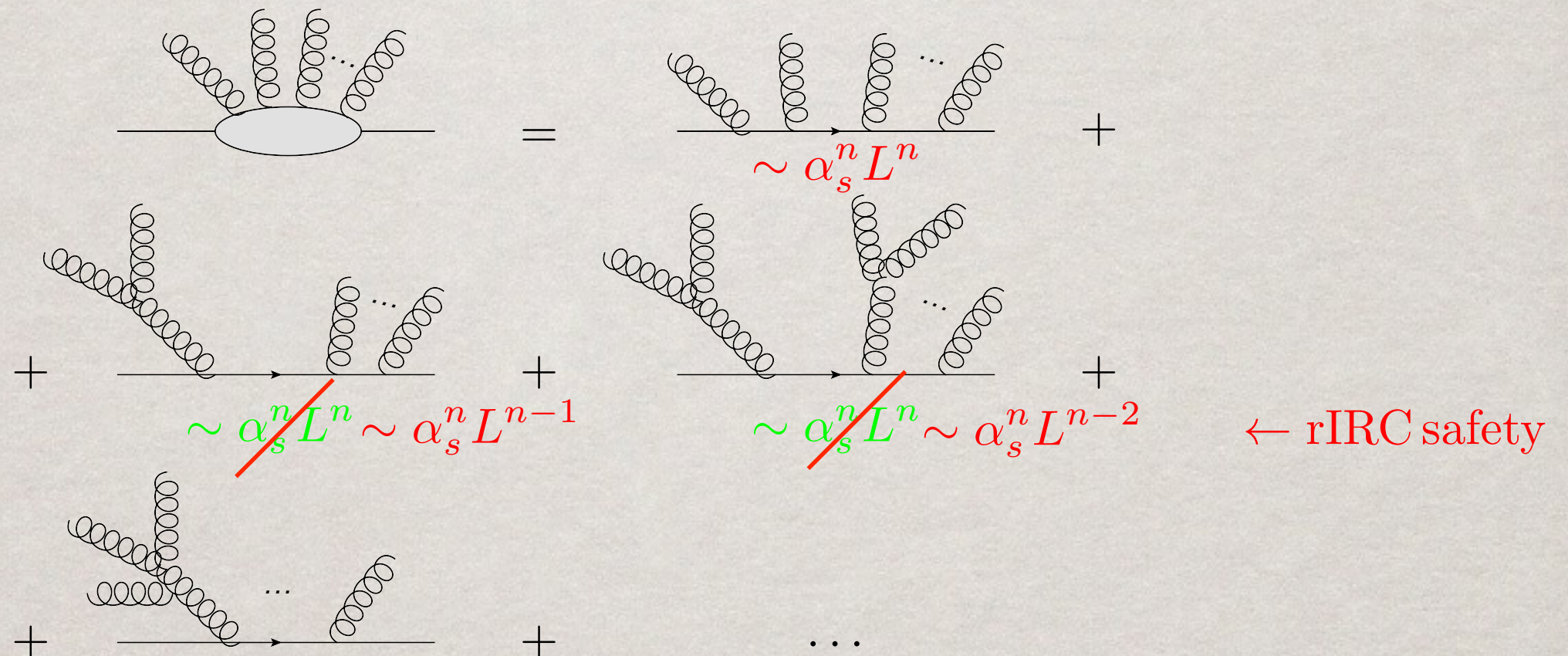
- Cluster decomposition of the matrix element for n soft emissions into terms with increasing number of colour correlations



- Which diagrams do we need to achieve NNLL accuracy (i.e. neglect terms of order $\alpha_s^n L^{n-2}$?)

SOFT (RESOLVED) MATRIX ELEMENT

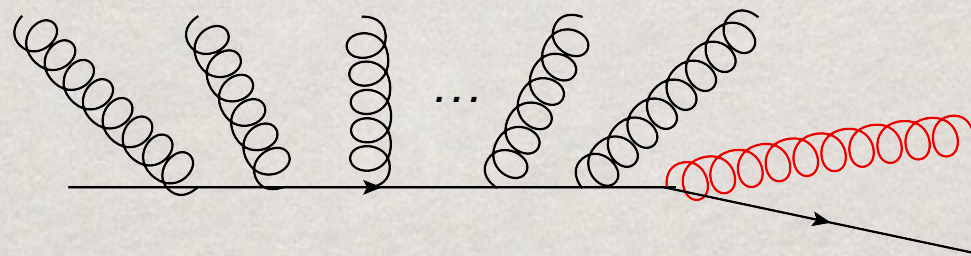
- Cluster decomposition of the matrix element for n soft emissions into terms with increasing number of colour correlations



- Which diagrams do we need to achieve NNLL accuracy (i.e. neglect terms of order $\alpha_s^n L^{n-2}$?)

COLLINEAR (RESOLVED) MATRIX ELEMENT

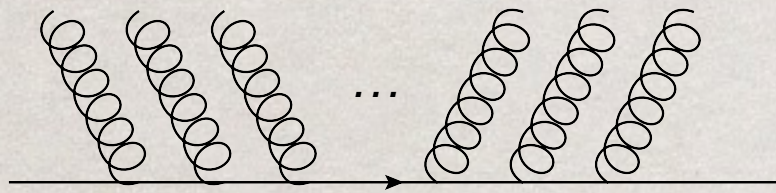
- From the previous analysis, at NNLL, we need to keep only configurations with an arbitrary number of independent soft-collinear emissions, and a single gluon branching
- Similarly, repeating the same analysis in the collinear limit, at NNLL only a single hard emission can be emitted collinear to any Born leg



- Further gluon branchings or more collinear emissions can be included for extensions to higher logarithmic orders

PHASE SPACE AT NLL

- At NLL the multiple emission function $\mathcal{F}(v)$ is given by an ensemble of soft and collinear gluons, widely separated in rapidity (angle)



Measure defined by the
soft-collinear ensemble

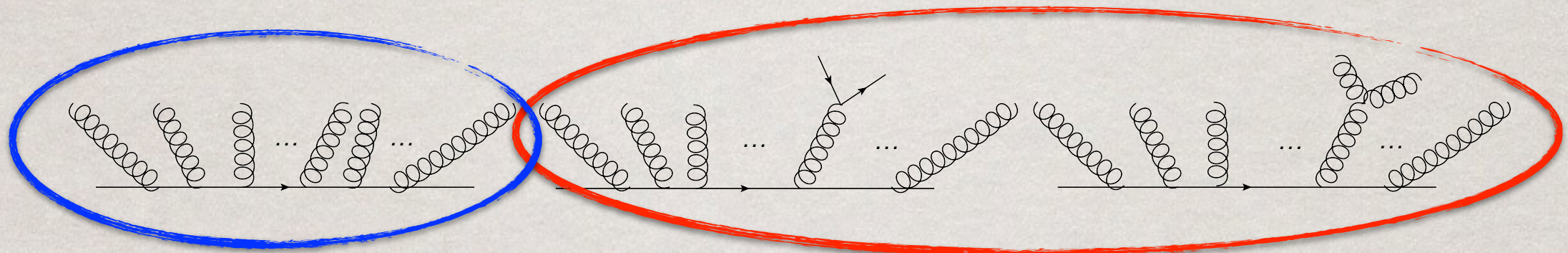
$$= \int \mathcal{Z}[\{R'_{\ell_i}, k_i\}] \Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{sc}}(\{\tilde{p}\}, \{k_i\})}{v} \right)$$

$$\mathcal{F}_{\text{NLL}}(v) = \langle \Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{sc}}(\{\tilde{p}\}, \{k_i\})}{v} \right) \rangle$$

- The exact rapidity bound for each emission can be neglected at this order (but does contribute at NNLL)

PHASE SPACE AT NNLL

- At most two soft-collinear emissions can get close in rapidity



Clustering correction
(jet algorithms only)

Correlated corrections

$$\delta F_{\text{correl}}(\lambda) = \int_0^\infty \frac{d\zeta_a}{\zeta_a} \int_0^{2\pi} \frac{d\phi_a}{2\pi} \sum_{\ell_a=1,2} \left(\frac{2C_{\ell_a} \lambda}{\beta_0} \frac{R''_{\ell_a}}{\alpha_s} \right) \int_0^\infty \frac{d\kappa}{\kappa} \int_{-\infty}^\infty \int_0^{2\pi} \frac{1}{2!} C_{ab}(\kappa, \eta, \phi) \times$$

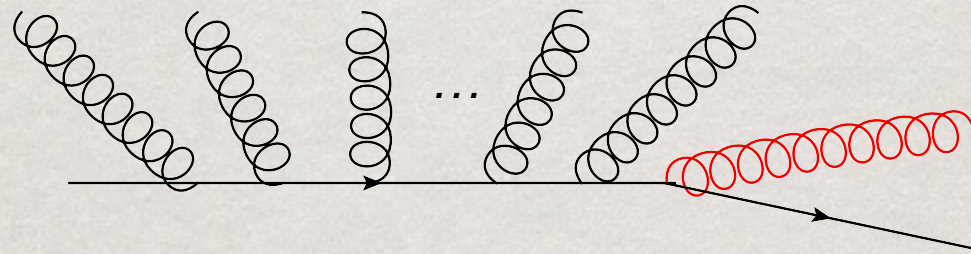
$$\times \int dZ[\{R'_{\ell_i}, k_i\}] [\Theta(v - V_{\text{sc}}(\{\tilde{p}\}, k_a, k_b, \{k_i\})) - \Theta(v - V_{\text{sc}}(\{\tilde{p}\}, k_a + k_b, \{k_i\}))]$$

$$C_{ab}(\kappa, \eta, \phi) = \frac{\tilde{M}^2(k_a, k_b)}{M_{\text{sc}}^2(k_a) M_{\text{sc}}^2(k_b)}$$

All corrections in terms of four-dimensional integrals

PHASE SPACE AT NNLL

- At most one collinear emission that carries a significant fraction of the energy of the emitter, which recoils against it



- We have split this contribution into a hard-collinear and recoil correction

$$\delta\mathcal{F}_{\text{hc}}(\lambda) = \sum_{\ell=1,2} \frac{\alpha_s(v^{1/(a+b_\ell)}Q)}{\alpha_s(Q)(a+b_\ell)} \int_0^\infty \frac{d\zeta}{\zeta} \int_0^{2\pi} \frac{d\phi}{2\pi} \int d\mathcal{Z}[\{R'_{\ell_i}, k_i\}] \times$$

$$\times \int_0^1 \frac{dz}{z} (z p_\ell(z) - 2C_\ell) \left[\Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{sc}}(\{\tilde{p}\}, k, \{k_i\})}{v} \right) - \Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{sc}}(\{\tilde{p}\}, \{k_i\})}{v} \right) \Theta(1 - \zeta) \right]$$

$$\delta\mathcal{F}_{\text{rec}}(\lambda) = \sum_{\ell=1,2} \frac{\alpha_s(v^{1/(a+b_\ell)}Q)}{\alpha_s(Q)(a+b_\ell)} \int_0^\infty \frac{d\zeta}{\zeta} \int_0^{2\pi} \frac{d\phi}{2\pi} \int d\mathcal{Z}[\{R'_{\ell_i}, k_i\}] \times$$

$$\times \int_0^1 dz p_\ell(z) \left[\Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{hc}}(\{\tilde{p}\}, k', \{k_i\})}{v} \right) - \Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{sc}}(\{\tilde{p}\}, k, \{k_i\})}{v} \right) \right]$$

PHASE SPACE AT NNLL

- At most one soft-collinear emission has exact phase space

$$\delta\mathcal{F}_{\text{sc}}(\lambda) = \frac{\pi}{\alpha_s} \int_0^\infty \frac{d\zeta}{\zeta} \int_0^{2\pi} \frac{d\phi}{2\pi} \sum_{\ell=1,2} \left(\delta R'_\ell + R''_\ell \ln \frac{d_\ell g_\ell(\phi)}{\zeta} \right) \int d\mathcal{Z}[\{R'_{\ell_i}, k_i\}] \times$$

$$\times \int_0^1 dz p_\ell(z) \left[\Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{sc}}(\{\tilde{p}\}, k, \{k_i\})}{v} \right) - \Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{sc}}(\{\tilde{p}\}, \{k_i\})}{v} \right) \Theta(1 - \zeta) \right]$$

- At most one soft emission can have small rapidity (large angle)

$$\delta\mathcal{F}_{\text{wa}}(\lambda) = \frac{2C_F}{a} \frac{\alpha_s(v^{1/a}Q)}{\alpha_s(Q)} \int_0^\infty \frac{d\zeta}{\zeta} \int_{-\infty}^\infty d\eta \int_0^{2\pi} \frac{d\phi}{2\pi} \int d\mathcal{Z}[\{R'_{\ell_i}, k_i\}] \times$$

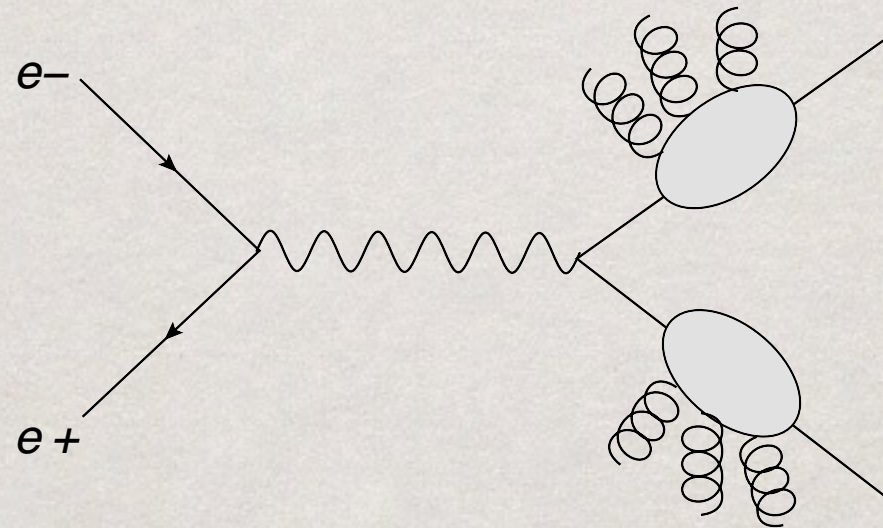
$$\times \left[\Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{wa}}(\{\tilde{p}\}, k, \{k_i\})}{v} \right) - \Theta \left(1 - \lim_{v \rightarrow 0} \frac{V_{\text{sc}}(\{\tilde{p}\}, k, \{k_i\})}{v} \right) \right]$$

- With more than two legs there are additional contributions due to colour correlations between hard legs

[Botts Sterman; Kidonakis Oderda Sterman]

APPLICATION TO 2-LEG PROCESS

- Event shapes in $e^+e^- \rightarrow 2 \text{ jets}$



- Relevant for precise determination of the strong coupling, through deviations from the 2-jet limit
- Toy model for final-state radiation (conceptually complete)
- Clean experimental environment to study non-perturbative corrections (hadronisation)

APPLICATION TO 2-LEG PROCESS

- Reproduced old results and presented new ones

- thrust and heavy-jet mass (known)

$$T \equiv \max_{\vec{n}} \frac{\sum_i |\vec{p}_i \cdot \vec{n}|}{\sum_i |\vec{p}_i|} \quad \rho_H \equiv \max_{i=1,2} \frac{M_i^2}{Q^2} \quad M_i^2 = \left(\sum_{j \in \mathcal{H}_i} p_j \right)^2$$

- total and wide-jet broadening(known)

$$B_L \equiv \sum_{i \in \mathcal{H}_1} \frac{|\vec{p}_i \times \vec{n}_T|}{2Q}, \quad B_R \equiv \sum_{i \in \mathcal{H}_2} \frac{|\vec{p}_i \times \vec{n}_T|}{2Q} \quad B_W \equiv \max\{B_L, B_R\}$$

$$B_T \equiv B_L + B_R$$

- C-parameter (new)

$$C \equiv 3 \left(1 - \frac{1}{2} \sum_{i,j} \frac{(p_i \cdot p_j)^2}{(p_i \cdot Q)(p_j \cdot Q)} \right)$$

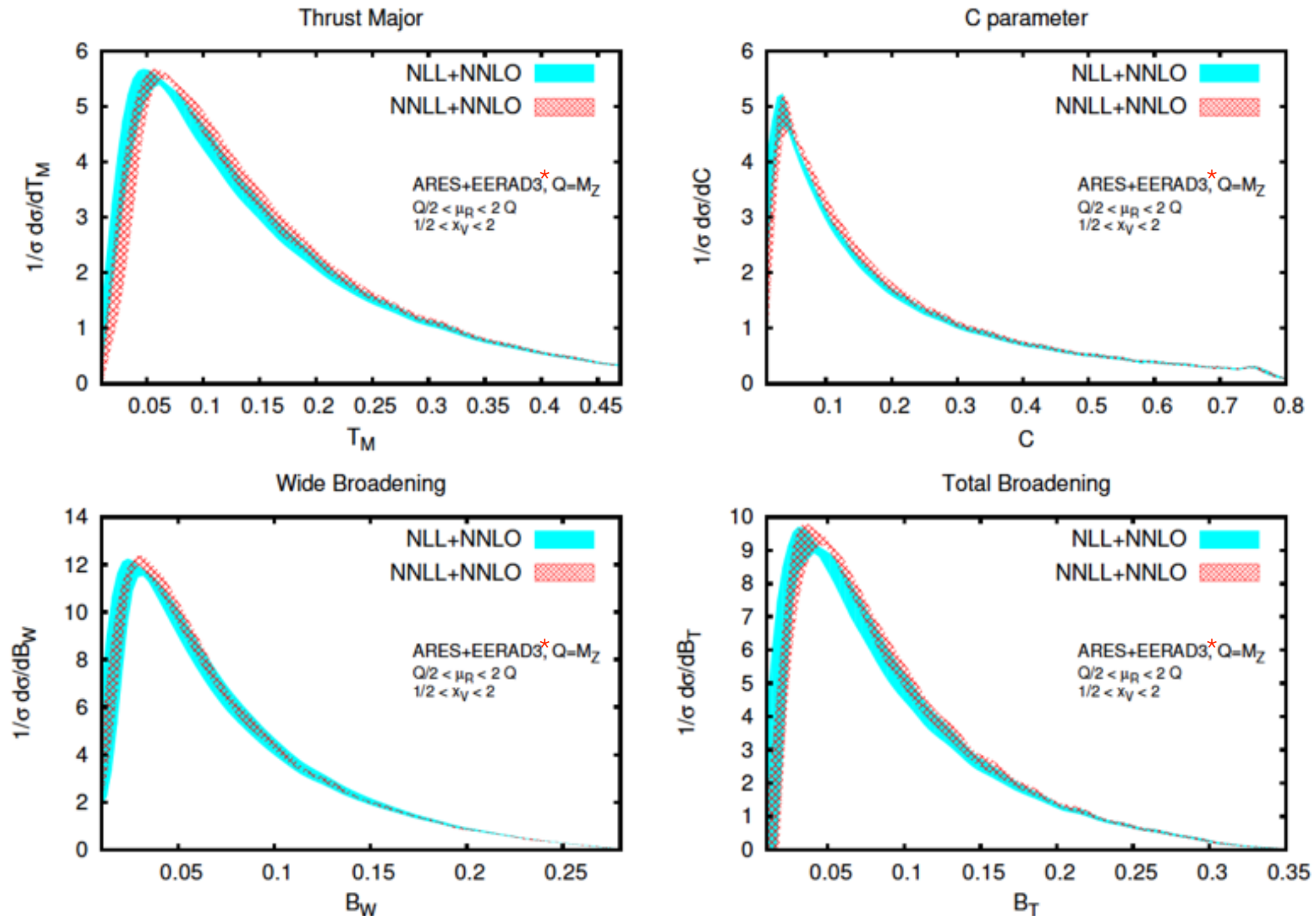
- thrust major and oblateness (new)

$$T_M \equiv \max_{\vec{n} \cdot \vec{n}_T} \frac{\sum_i |\vec{p}_i \cdot \vec{n}|}{\sum_i |\vec{p}_i|} \quad T_m \equiv \frac{\sum_i |\vec{p}_{x,i}|}{\sum_i |\vec{p}_i|} \quad O \equiv T_M - T_m$$

APPLICATION TO 2-LEG PROCESS

- Event-shapes distributions at NNLL matched to exact NNLO

[AB McAslan Monni Zanderighi]



[* Gehrmann-De Ridder Gehrmann Glover Heinrich]

APPLICATION TO 2-LEG PROCESS

- Observables with different logarithmic structures can be resummed with the same method (fully general)

correction type	$p_{t,\text{veto}}$	$1 - T$	B_T	B_W	C	ρ_H	T_M	O
\mathcal{F}_{NLL}	✓	✓	✓	✓	✓	✓	✓	✓
$\delta\mathcal{F}_{\text{rap}}$	X	✓	✓	✓	✓	✓	✓	✓
$\delta\mathcal{F}_{\text{wa}}$	X	X	X	X	✓	X	X	X
$\delta\mathcal{F}_{\text{hc}}$	X	✓	✓	✓	✓	✓	✓	✓
$\delta\mathcal{F}_{\text{rec}}$	X	✓	✓	✓	✓	✓	✓	✓
$\delta\mathcal{F}_{\text{clust}}$	✓	X	X	X	X	X	X	X
$\delta\mathcal{F}_{\text{correl}}$	✓	X	✓	✓	X	X	✓	✓

CONCLUSIONS

- Novel general method for the resummation of any rIRC safe (global) observable in the two-scale regime
 - weak applicability conditions
 - cancellation of poles between real and virtual corrections performed analytically in dimensional regularisation
 - contributions of resolved real emissions formulated in terms of four-dimensional integrals (suitable for Monte Carlo implementation)
- Modulo technical work the NNLL resummation for any rIRC safe observable in the two-scale regime is a theoretically solved problem
- Application to jet cross sections in e^+e^- (Durham and Cambridge 2-jet rate) and in hadron collisions (H+1jet) is under way

CONCLUSIONS

- Novel general method for the resummation of any rIRC safe (global) observable in the two-scale regime
 - weak applicability conditions
 - cancellation of poles between real and virtual corrections performed analytically in dimensional regularisation
 - contributions of resolved real emissions formulated in terms of four-dimensional integrals (suitable for Monte Carlo implementation)
- Modulo technical work the NNLL resummation for any rIRC safe observable in the two-scale regime is a theoretically solved problem
- Application to jet cross sections in e^+e^- (Durham and Cambridge 2-jet rate) and in hadron collisions (H+1jet) is under way

Thank you for your attention!