



# **Vector Boson Scattering:**

## **A Phenomenological Perspective**

**HiggsTools Summer School**

**Valle d'Aosta – July 2015**

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**University of Tübingen**

# outline

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## vector boson scattering:

- theoretical concepts & techniques
- phenomenological results
- the quest for more realistic predictions

## Higgs production via vector boson fusion:

- motivation: a super-clean environment
- precise predictions and unexpected features
- omnipresent: backgrounds

# VBS: outline of the NLO-QCD Calculation

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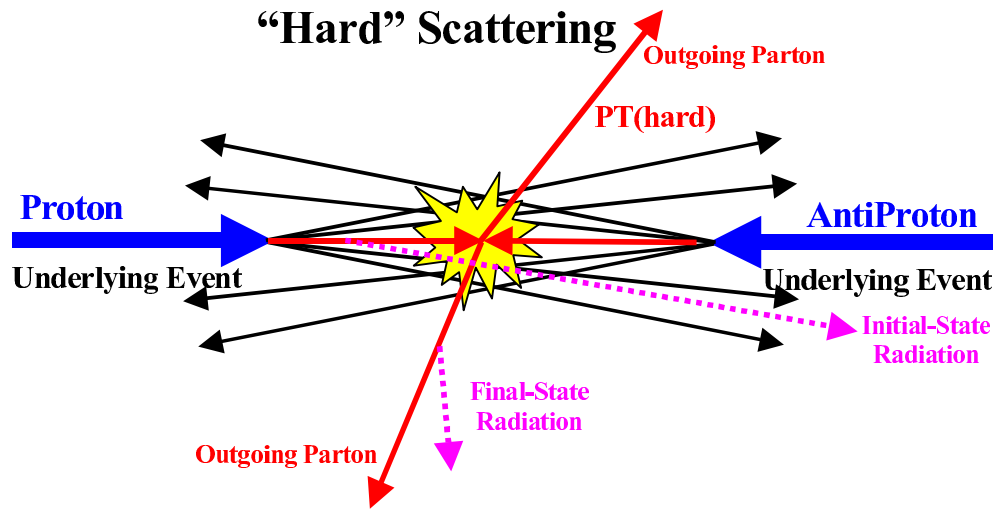
- ❖ calculation of  $d\hat{\sigma}$  at  $\mathcal{O}(\alpha^6\alpha_s)$  (NLO QCD)
  - dimensional reduction ( $d = 4 - 2\epsilon$ )
  - $\overline{\text{MS}}$ -renormalization
- ❖ handling of infrared singularities by dipole subtraction approach of *Catani & Seymour*
- ❖ need to compute
  - real emission contributions
  - counterterms
  - virtual corrections
- ❖ phase space integration and convolution with PDFs with Monte Carlo techniques in 4 dimensions

# VBS results: summary

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- ✓ obtained numerical results at NLO-QCD for various weak boson scattering processes  
(focusing on fully leptonic final states)
- ✓ all reactions **under excellent control perturbatively**  
(moderate  $K$ -factors and small scale dependencies at NLO)
- ✓ **shape** of some distributions **changes** noticeably at NLO  
(advantageous: dynamical scale choice)

# more realistic simulation



for realistic description of scattering processes at hadron colliders:

❖ combine matrix elements for hard scattering with programs for simulation of

underlying event, parton shower, and hadronization

(PYTHIA, HERWIG, SHERPA, ...)

# details on event simulation

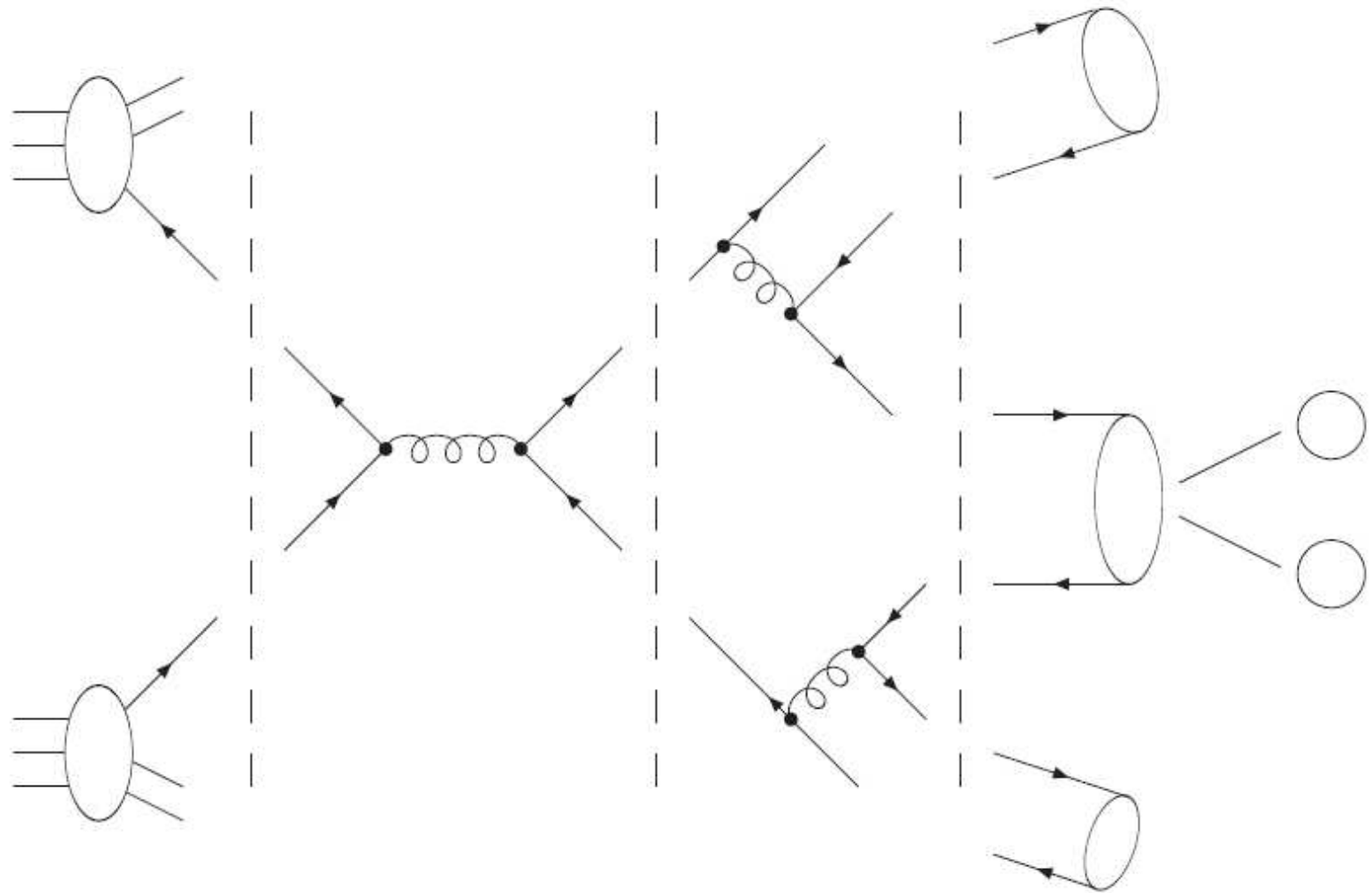
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for details:

Frank Krauss' lecture

# hadron-hadron collision



PDFs

hard partonic  
scattering

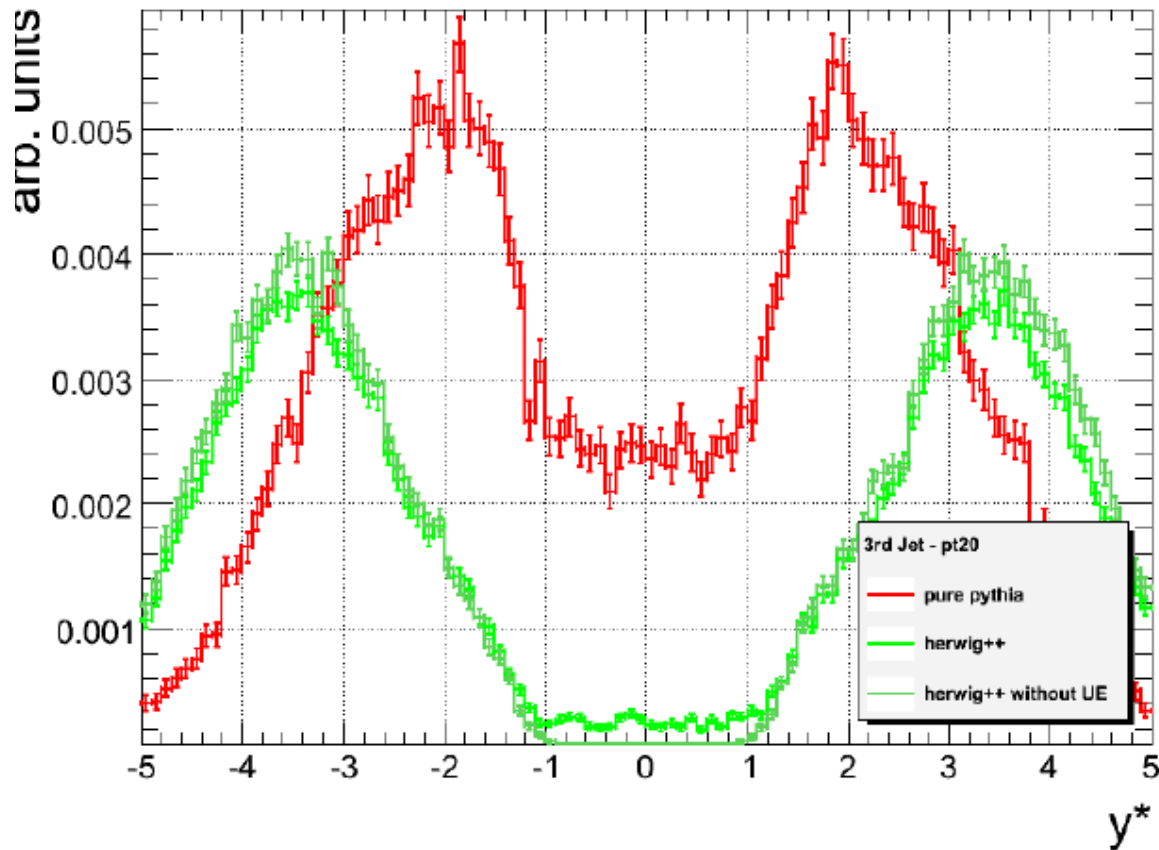
parton  
shower

hadronization  
and decay

# $pp \rightarrow Hjj$ via VBF and parton showers

rapidity separation of the third jet:  $y^* = y_3 - \frac{1}{2}(y_1 + y_2)$

*Hackstein et al. (2008)*



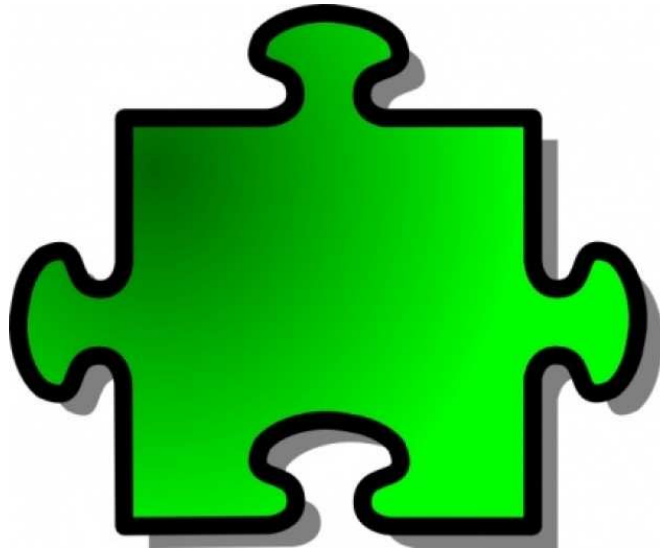
Pythia: rapidity gap filled by parton shower

→ better understanding and modeling needed



# realistic & precise predictions

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exploit merits of flexible  
Monte Carlo tools

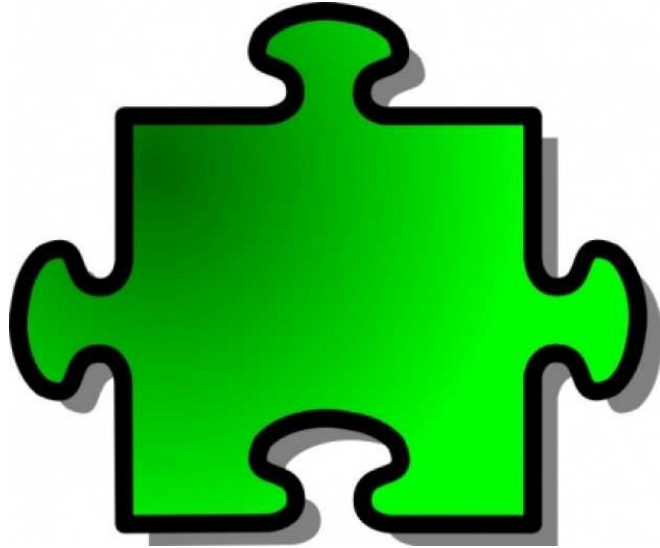


retain NLO accuracy  
for hard scattering



# realistic & precise predictions

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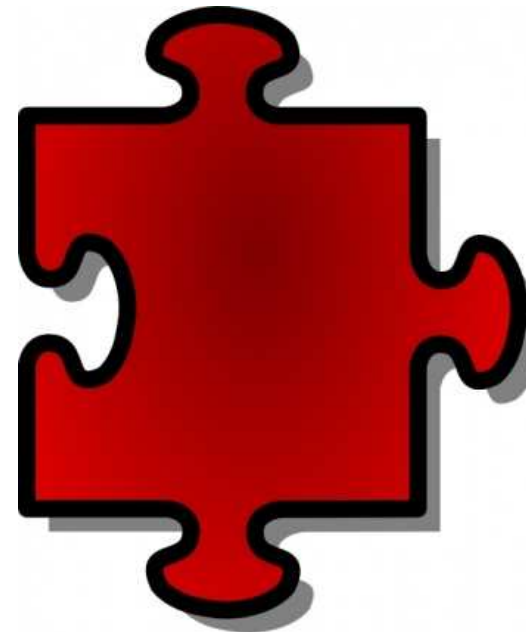


shower Monte Carlo:

- good description at low transverse momenta ( $p_T$ )
- events at hadron level

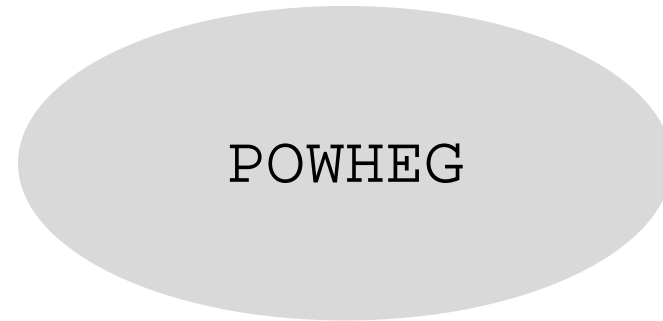
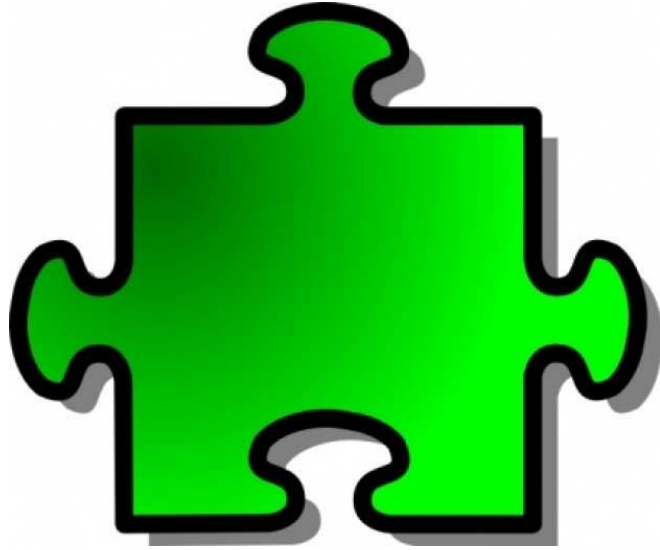
NLO-QCD calculation:

- accurate shapes at high  $p_T$
- normalization accurate at NLO
- reduced scale dependence



# realistic & precise predictions

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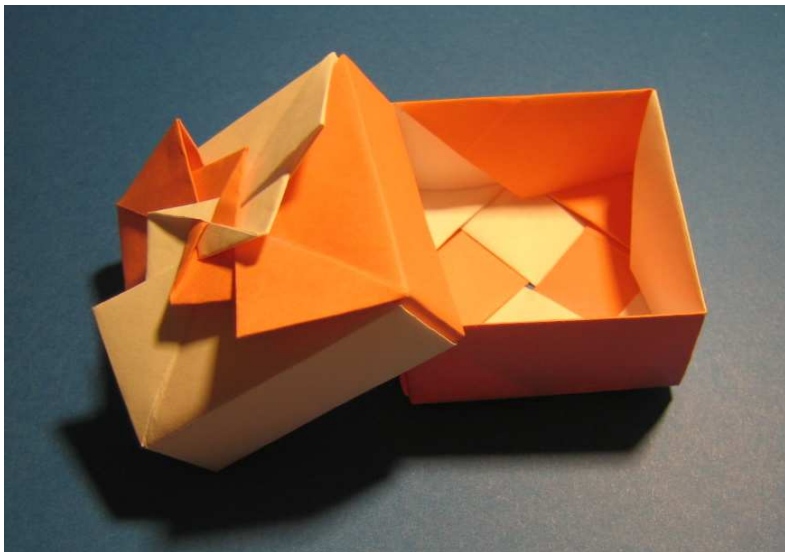
# realistic & precise predictions

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general prescription for **matching**  
parton-level **NLO-QCD** calculation  
with **parton-shower programs**

*[Frixione, Nason, Oleari]*

POWHEG



a public multi-purpose tool  
for “do-it-yourself” implementations:

the **POWHEG-BOX**

<http://powhegbox.mib.infn.it/>

*[Alioli, Nason, Oleari, Re]*

# parton showers & NLO-QCD: the POWHEG method

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POsitive Weight Hardest Emission Generator

general prescription for **matching** parton-level **NLO-QCD** calculations with **parton shower programs**

*[Frixione, Nason, Oleari]*

- ❖ generate partonic event with single emission at NLO-QCD
- ❖ all subsequent radiation must be softer than the first one
- ❖ event is written on a file in standard Les Houches format
  - can be processed by default parton shower program (HERWIG, PYTHIA, ...)

# parton showers & NLO-QCD: the POWHEG method

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POsitive Weight Hardest Emission Generator

general prescription for **matching** parton-level **NLO-QCD** calculations with **parton shower programs**

*[Frixione, Nason, Oleari]*

- ❖ applicable to any  $p_T$ -ordered parton shower program
- ❖ no double counting of real-emission contributions
- ❖ produces events with positive weights
- ❖ tools for “do-it-yourself” implementation  
publicly available (the POWHEG-BOX)

*[Alioli, Nason, Oleari, Re]*

# NLO cross sections

reminder: differential **NLO cross section**

$$d\sigma_{\text{NLO}} = d\Phi_n \left\{ B(\Phi_n) + V(\Phi_n) + \left[ R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] d\Phi_r \right\}$$

Born

real emission and counter-terms

finite virtuals:

$$V_b(\Phi_n) + \int d\phi_r C(\Phi_n, \Phi_r)$$

radiation phase space:

$$d\Phi_r = dt dz d\phi$$

# shower Monte Carlo cross sections

leading order **shower Monte Carlo** cross section

Born

first emission  
(governed by  
splitting function  $P$ )

$$d\sigma_{\text{LO-SMC}} = d\Phi_n B(\Phi_n) \left\{ \Delta_{t_0} + \Delta_t \frac{\alpha_s}{2\pi} P(z) \frac{1}{t} d\Phi_r \right\}$$

Sudakov factor:

$$\Delta_t = \exp \left[ - \int d\Phi'_r \frac{\alpha_s}{2\pi} P(z') \frac{1}{t'} \theta(t' - t) \right]$$

... probability for no emission at scale  $t' > t$



# POWHEG cross sections

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$$\bar{B} = \left\{ B(\Phi_n) + V(\Phi_n) + \int d\Phi_r \left[ R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] \right\}$$

$$d\sigma_{\text{POWHEG}} = d\Phi_n \bar{B}(\Phi_n) \left\{ \Delta(\Phi_n, p_T^{\min}) + \Delta(\Phi_n, p_T) \frac{R(\Phi_n, \Phi_r)}{B(\Phi_n, \Phi_r)} d\Phi_r \right\}$$

POWHEG “Sudakov” factor:

$$\Delta(\Phi_n, p_T) = \exp \left[ - \int d\Phi'_r \frac{R(\Phi_n, \Phi'_r)}{B(\Phi_n)} \theta(k_T(\Phi_n, \Phi'_r) - p_T) \right]$$

# the POWHEG cross section

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$$d\sigma_{\text{NLO}} = d\Phi_n \left\{ B(\Phi_n) + V(\Phi_n) + \left[ R(\Phi_n, \Phi_r) - C(\Phi_n, \Phi_r) \right] d\Phi_r \right\}$$

$$d\sigma_{\text{LO-SMC}} = d\Phi_n B(\Phi_n) \left\{ \Delta_{t_0} + \Delta_t \frac{\alpha_s}{2\pi} P(z) \frac{1}{t} d\Phi_r \right\}$$

$$d\sigma_{\text{POWHEG}} = d\Phi_n \bar{B}(\Phi_n) \left\{ \Delta(\Phi_n, p_T^{\min}) \right. \\ \left. + \Delta(\Phi_n, p_T) \frac{R(\Phi_n, \Phi_r)}{B(\Phi_n, \Phi_r)} d\Phi_r \right\}$$

# parton showers & NLO-QCD: the POWHEG-BOX

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up-to-date info on the POWHEG-BOX and code download:

`http://powhegbox.mib.infn.it/`

✗ **user** has to supply process-specific quantities:

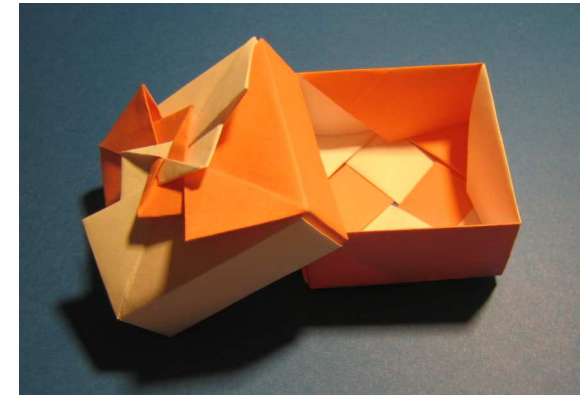
- ❖ lists of flavor structures for Born and real emission processes
- ❖ Born phase space
- ❖ Born amplitudes squared, color-and spin-correlated amplitudes
- ❖ real-emission amplitudes squared
- ❖ finite part of the virtual corrections
- ❖ Born color structure in the limit of a large number of colors

✓ all general, process-independent aspects of the matching  
are **provided by the POWHEG-BOX**

# $VVjj$ matched with parton showers & NLO-QCD

so far only implementation of EW- and QCD-induced  $VVjj$  production processes available in the POWHEG-BOX:

<http://powhegbox.mib.infn.it/>

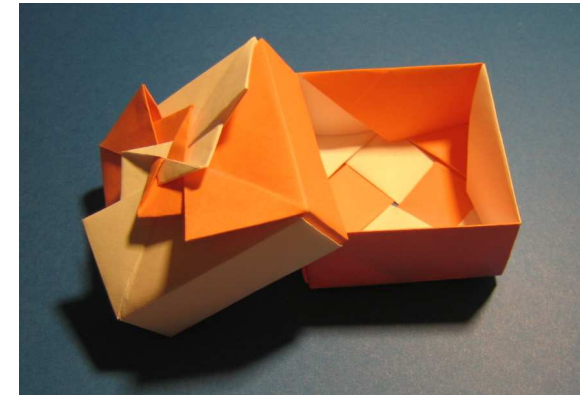


- ❖ QCD  $W^+W^+jj$  production [Melia, Nason, Rontsch, Zanderighi (2011)]
- ❖ EW  $W^+W^+jj$  production [Zanderighi, B.J. (2011)]
- ❖ EW  $W^+W^-jj$  production [Zanderighi, B.J. (2013)]
- ❖ EW  $ZZjj$  production [Karlberg, Zanderighi, B.J. (2013)]

# VBF in the POWHEG-BOX: getting started

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- ❖ get access to a computing farm
- ❖ download the POWHEG-BOX from:  
`http://powhegbox.mib.infn.it/`
- ❖ go to the directory of the process you are interested in, e.g.,  
`$ cd POWHEG-BOX/VBF_Wp_Wm`
- ❖ for instructions on running the code refer to  
the documentation in `POWHEG-BOX/VBF_Wp_Wm/Docs`
- ❖ use sample files for input and analysis,  
or replace them with your own files

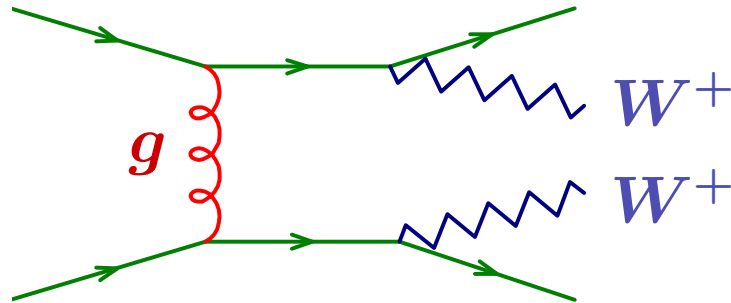


# $pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

## QCD-induced production

*Melia, Melnikov, Rontsch, Zanderighi (2010);*

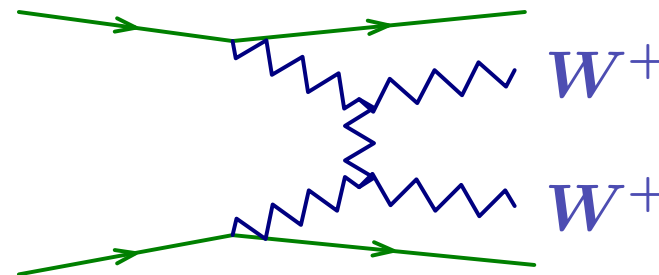
*Melia, Nason, Rontsch, Zanderighi (2011)*



## EW production

*Oleari, Zeppenfeld, B.J. (2009);*

*Zanderighi, B.J. (2011)*



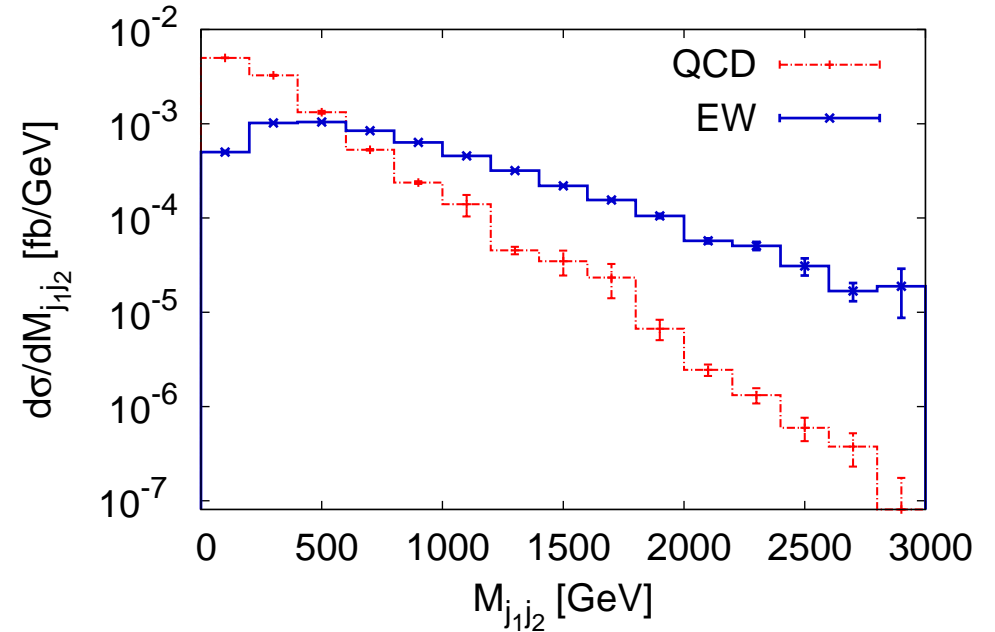
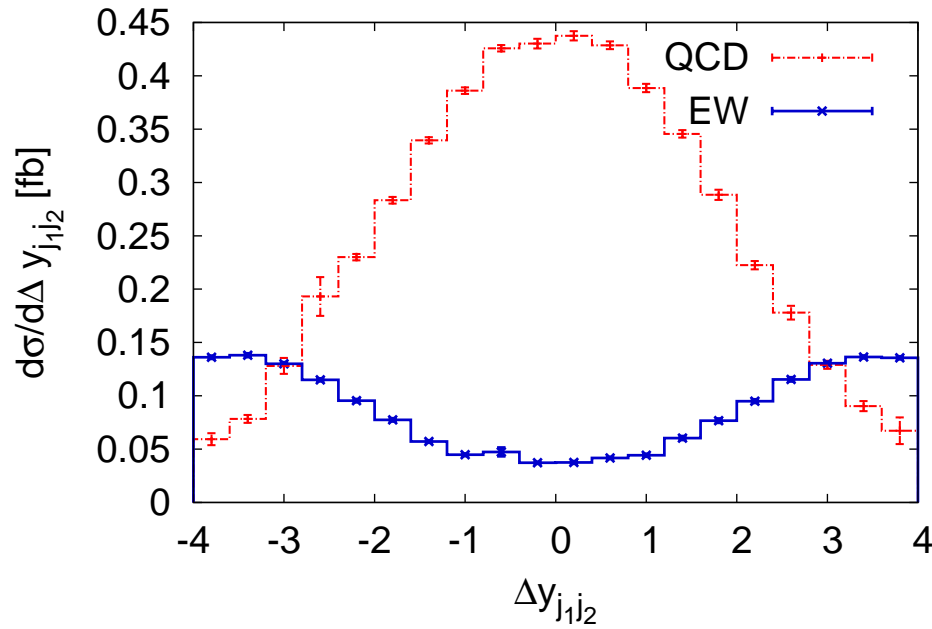
NLO-QCD results for  $\sqrt{s} = 7$  TeV with basic jet cuts only ( $p_T^{\text{tag}} > 20$  GeV):

$$\sigma_{\text{QCD}}^{\text{inc}} = 2.12 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{inc}} = 1.097 \text{ fb}$$

# $pp \rightarrow W^+W^+jj$ : QCD versus EW production

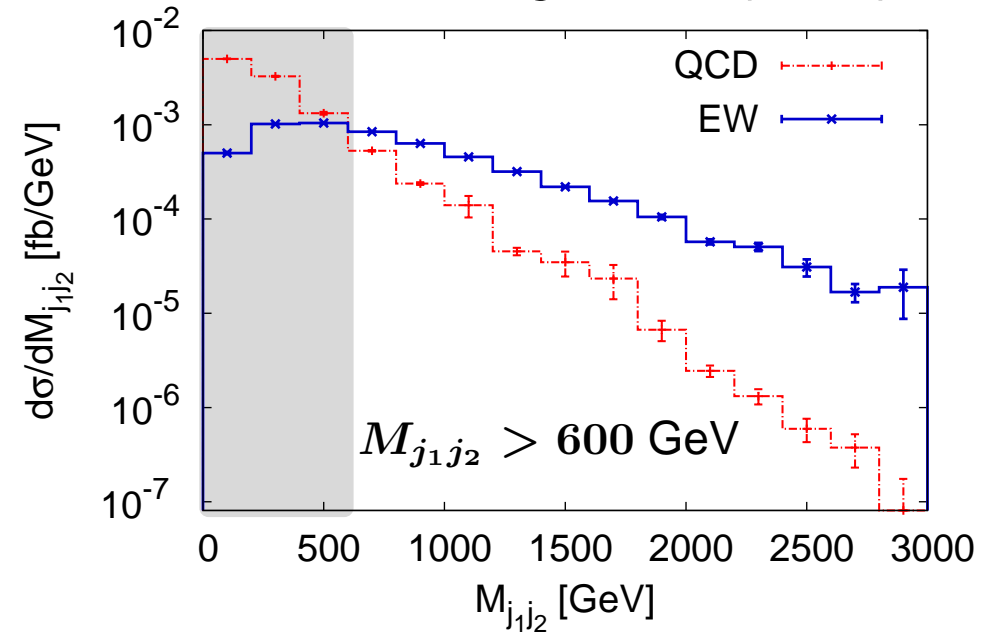
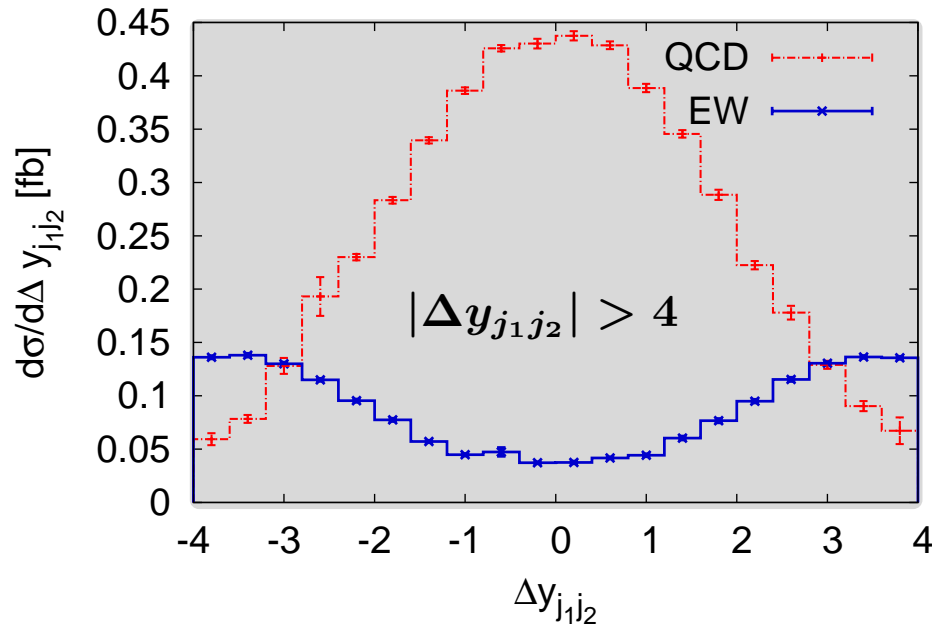
Zanderighi, B.J. (2011)



- $\sqrt{s} = 7$  TeV
- basic jet cuts only
- NLO-QCD accuracy

# $pp \rightarrow W^+W^+jj$ : QCD versus EW production

Zanderighi, B.J. (2011)



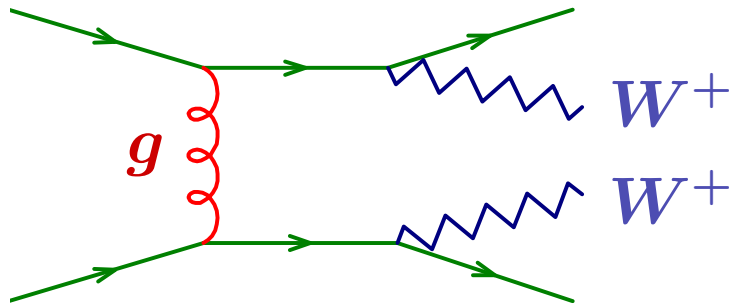
- $\sqrt{s} = 7 \text{ TeV}$
- basic jet cuts only
- NLO-QCD accuracy



# $pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

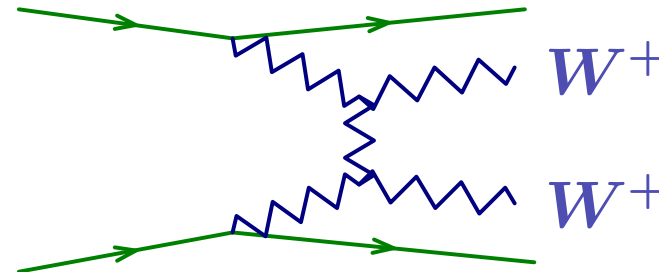
## QCD-induced production

*Melia, Melnikov, Rontsch, Zanderighi (2010);  
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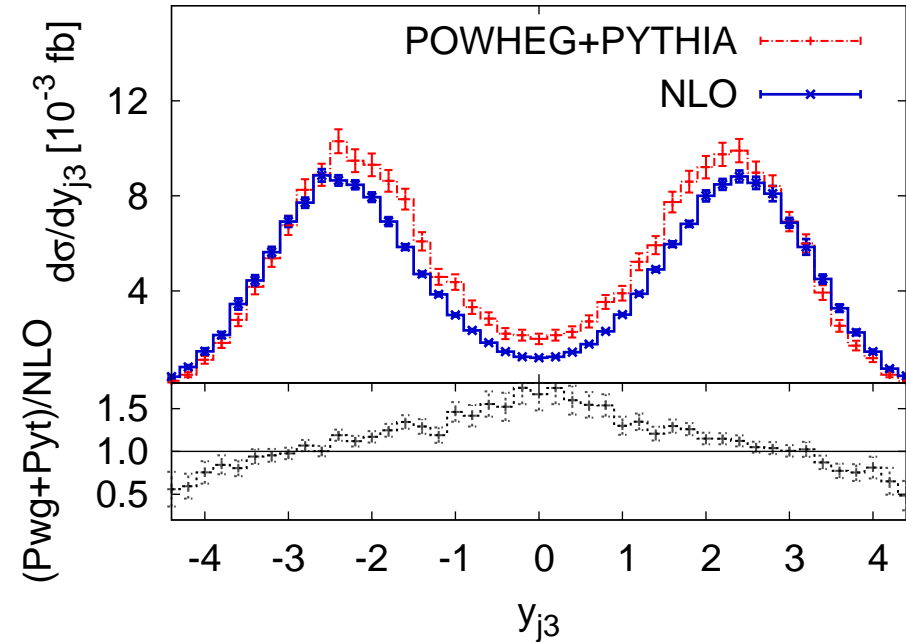
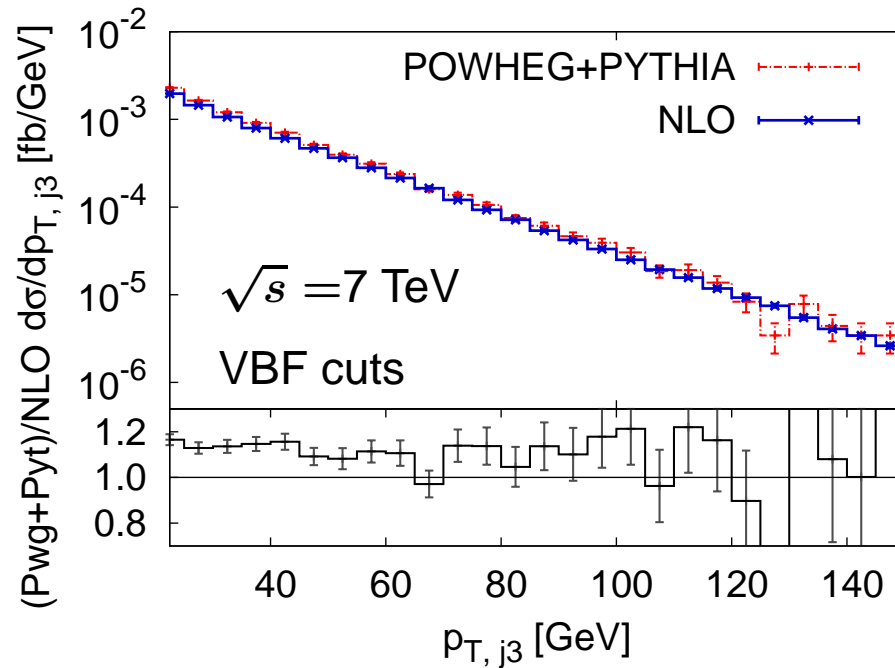
NLO results with VBF cuts:

$$\sigma_{\text{QCD}}^{\text{cuts}} = 0.0074 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{cuts}} = 0.201 \text{ fb}$$

# $pp \rightarrow W^+W^+jj$ via VBF in the POWHEG-BOX

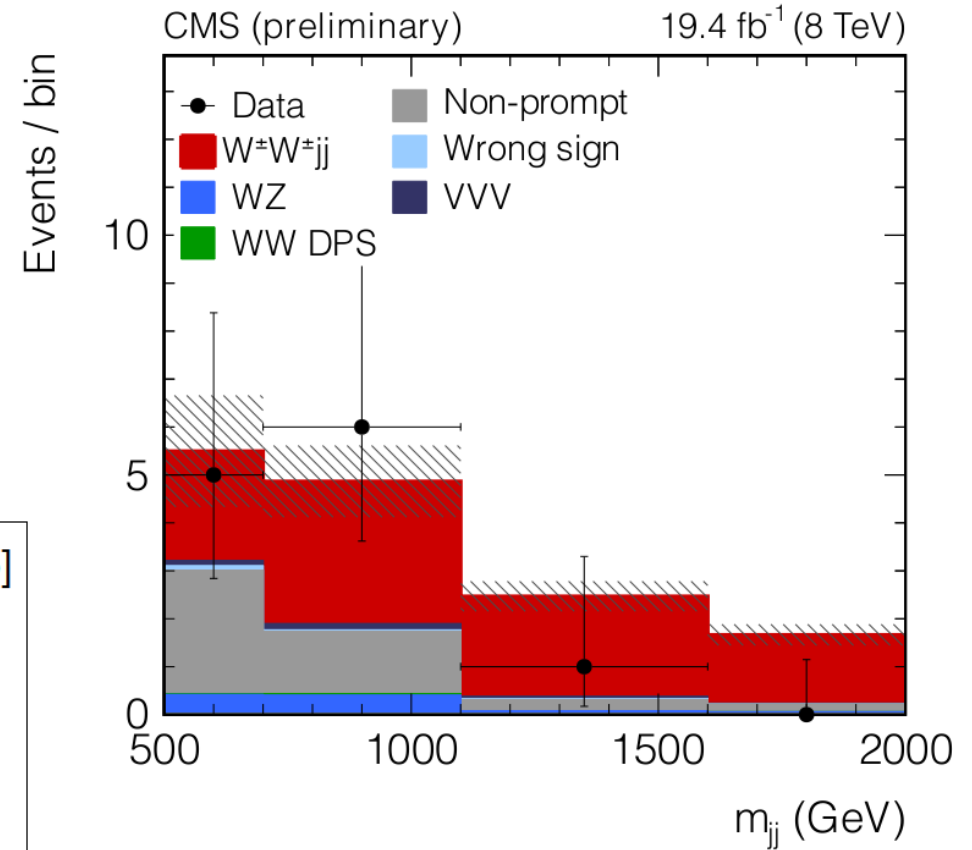
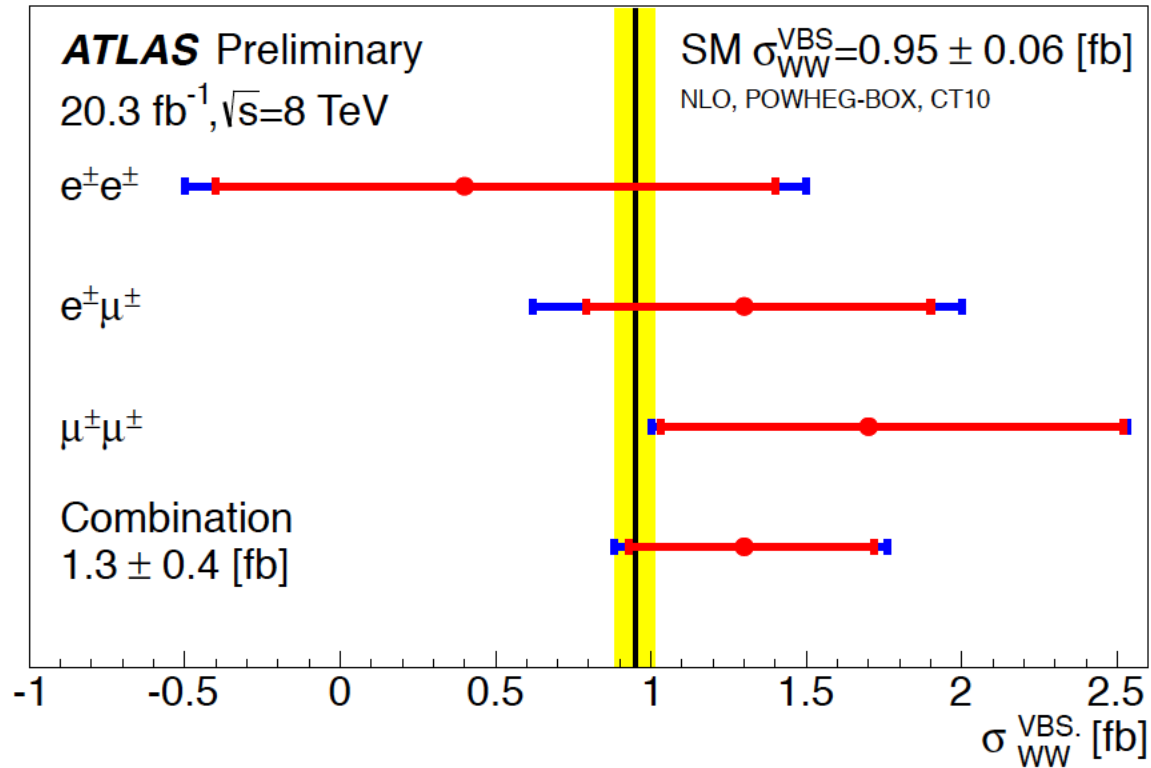
Zanderighi, B.J. (2011)



typical for VBF processes: little jet activity at central rapidities  
→ exploited by central-jet veto techniques

note: parton-shower effects slightly enhance central jet activity

# evidence for $W^\pm W^\pm jj$ from ATLAS and CMS



**the next step:  $pp \rightarrow W^+W^-jj$**

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# $pp \rightarrow W^+W^-jj$ via VBF in the POWHEG-BOX

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full description of EW process  $pp \rightarrow W^+W^-jj$ , including fully leptonic and semi-leptonic decays:

matching of hard matrix elements  
with parton shower at NLO QCD

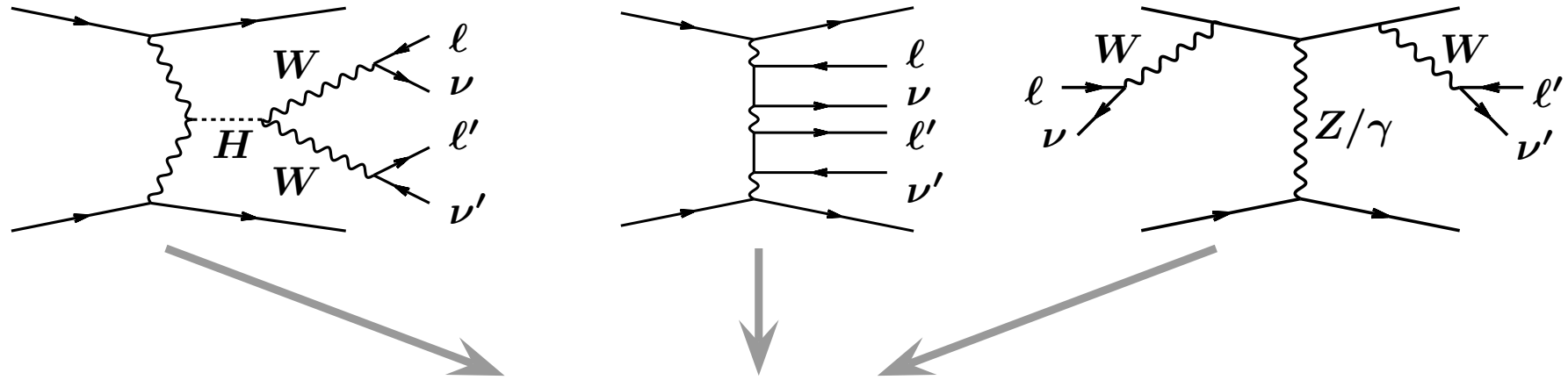
✓ provide implementation in versatile  
public program package POWHEG-BOX

✗ challenge: complex multi-leg process with  
involved resonance structure

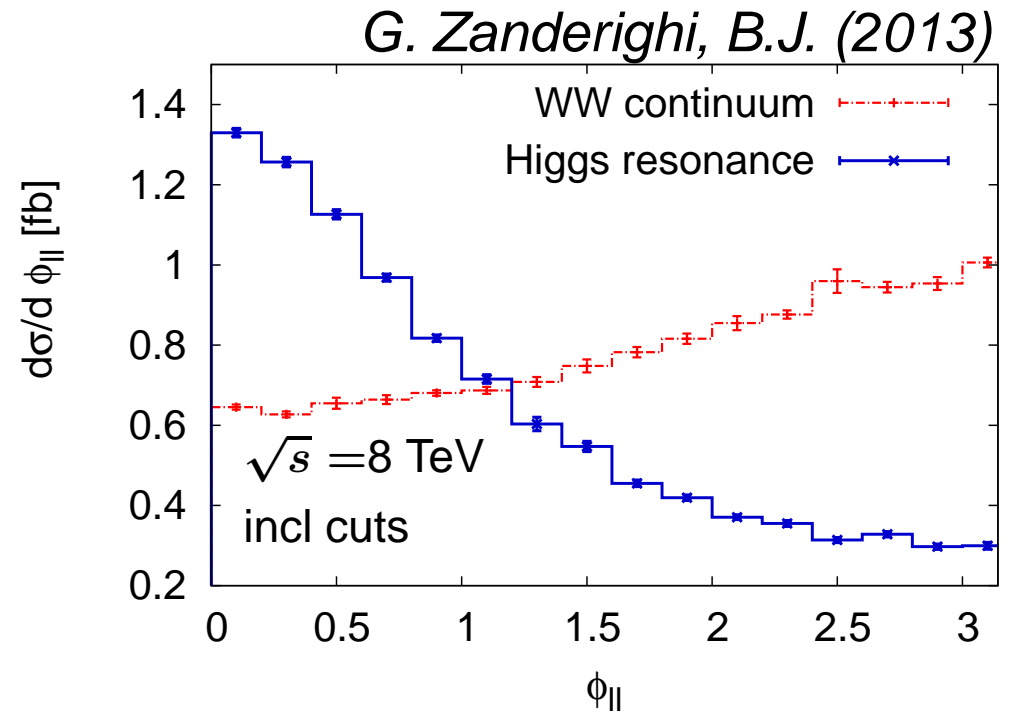
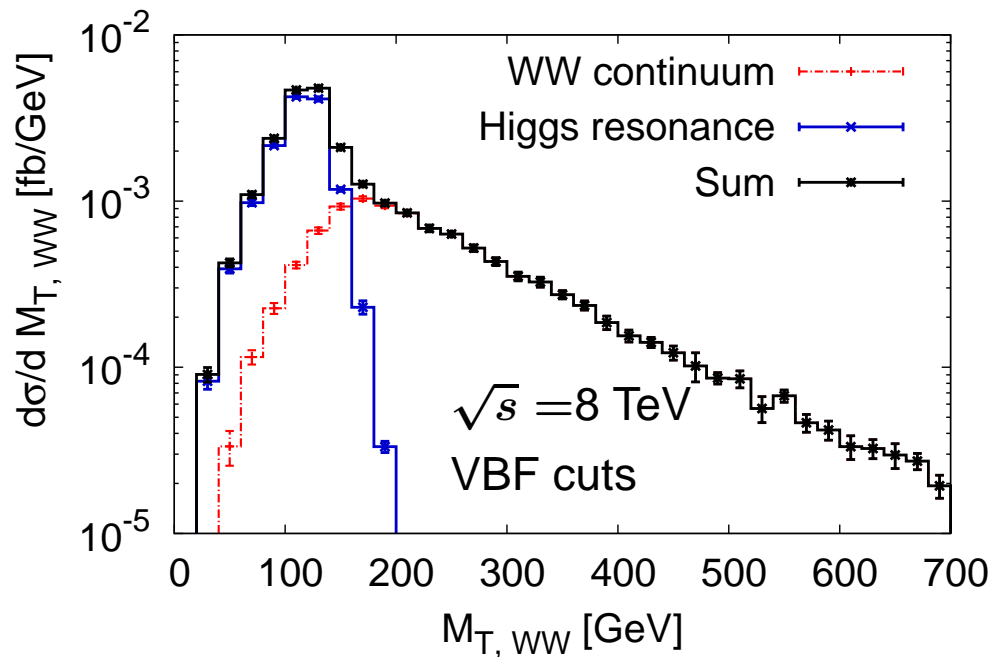
→ conceptually and computationally demanding\*

\* requires about 12 hours  $\times$  100 nodes on a HPC cluster

# $pp \rightarrow W^+W^-jj$ via VBF: technicalities

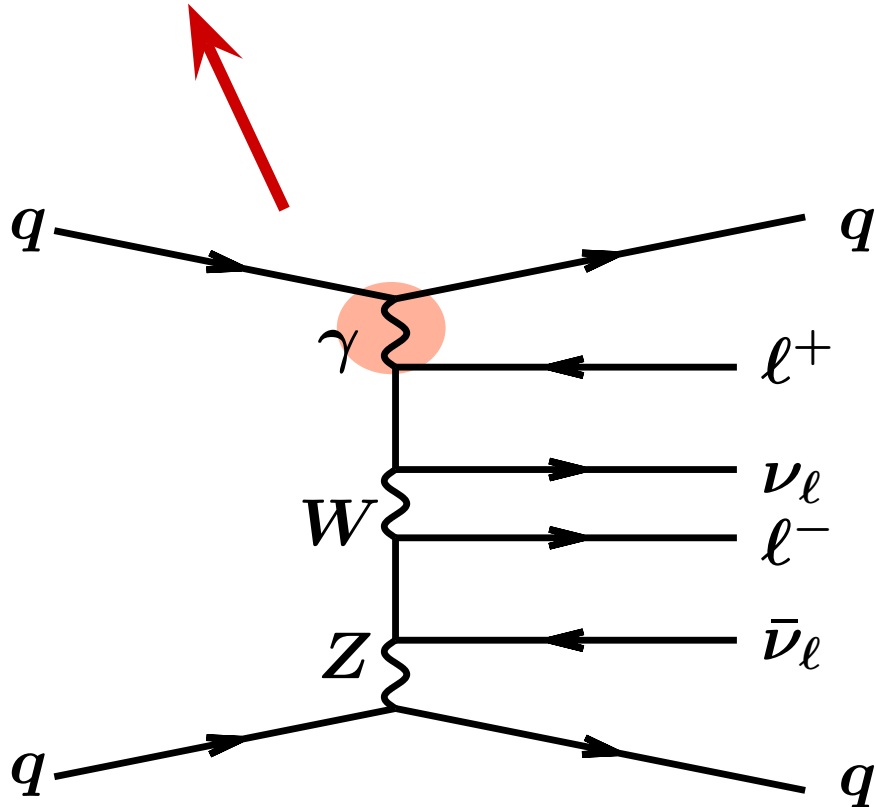


different topologies populate different regions in phase space:



# $pp \rightarrow W^+W^-jj$ : technicalities

photon propagator  $\sim 1/Q_\gamma^2$



need to handle

singularities for photons in  $t$ -channel

with  $Q_\gamma^2 \rightarrow 0$

(numerically irrelevant for meaningful observables)

(1) damping factor to effectively suppress matrix elements

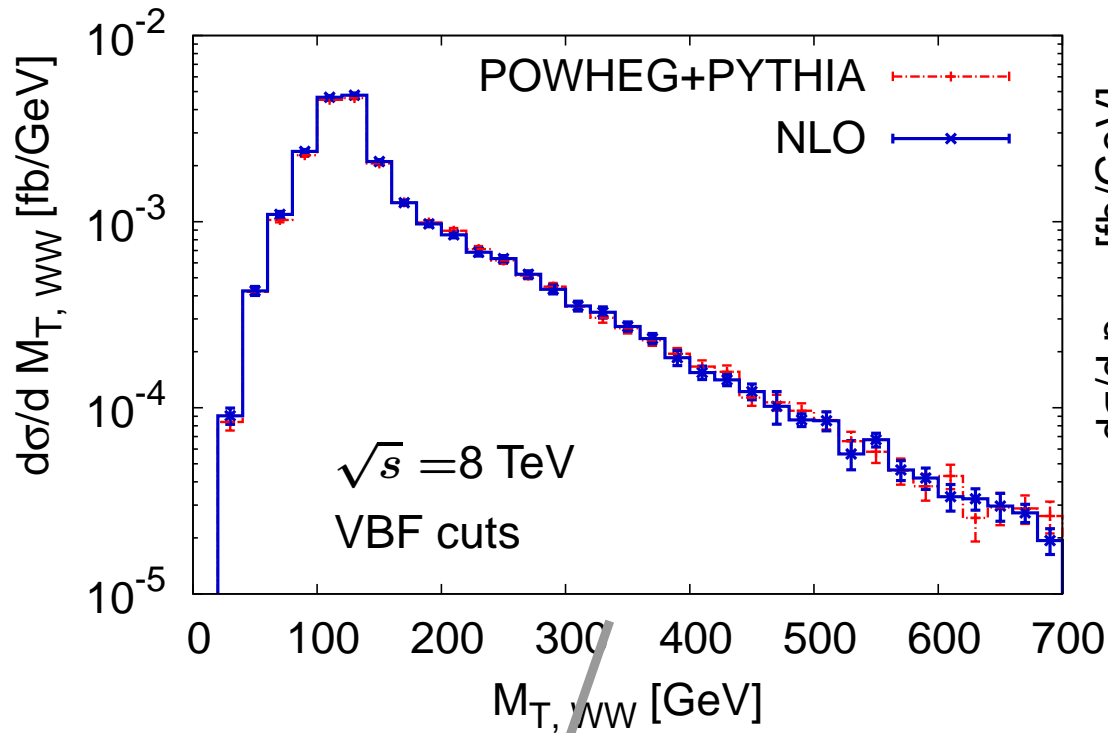
(2) Born-suppression factor to achieve efficient phase space integration

$$F \sim \left( \frac{p_{T,1}^2}{p_{T,1}^2 + \Lambda^2} \right)^2 \left( \frac{p_{T,2}^2}{p_{T,2}^2 + \Lambda^2} \right)^2$$

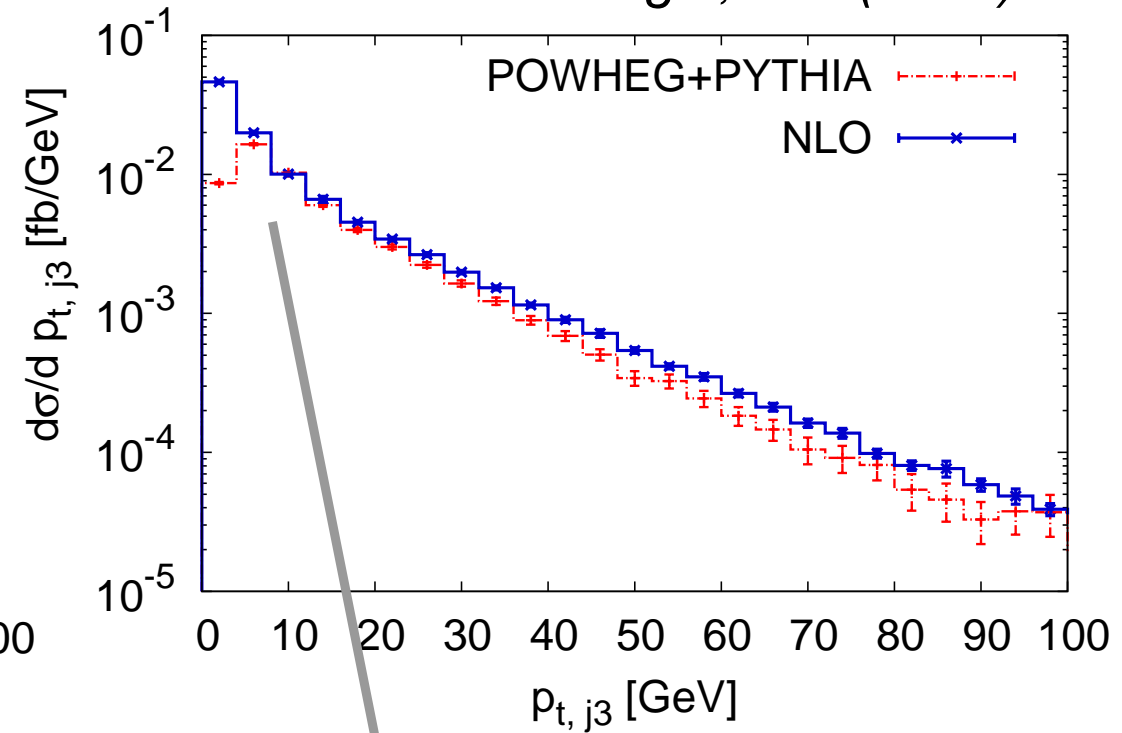
(alternative: explicit generation cuts)

# $pp \rightarrow W^+W^-jj$ via VBF with leptonic decays

G. Zanderighi, B.J. (2013)



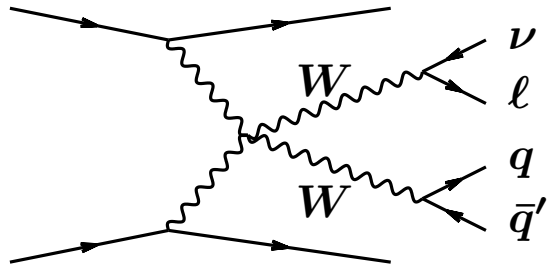
leptonic observables  
not very sensitive to  
parton shower



growth of jet distribution  
tamed by Sudakov factor



# $pp \rightarrow W^+W^-jj$ via VBF with semi-leptonic decays



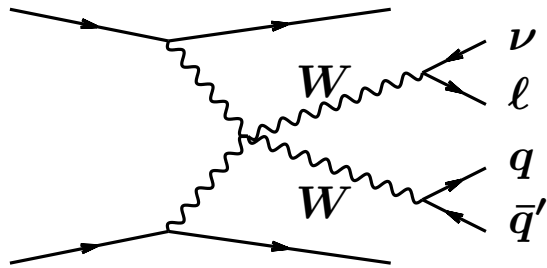
“semi-leptonic” final state:

$$W^+W^- \rightarrow \ell\nu + q\bar{q}'$$

different from fully leptonic modes:

- ✓ branching ratio  $\text{BR}_{W \rightarrow q\bar{q}'} \approx 3 \times \text{BR}_{W \rightarrow \ell\nu} \rightarrow$  larger x-sec
- ✓ only one neutrino  $\rightarrow$  on-shell:  $M_{WW}$  reconstruction possible
- ✗ sophisticated analysis techniques needed to isolate signal

# $pp \rightarrow W^+W^-jj$ via VBF with semi-leptonic decays



consider fictitious scenario with heavy Higgs

$$m_H = 400 \text{ GeV} > 2M_W$$

→  $W$  bosons are typically on-shell

❖ require VBF topology for tagging jets:

$$p_{T,j}^{\text{tag}} > 25 \text{ GeV}, \quad |y_j^{\text{tag}}| < 4.5$$
$$\Delta y_{jj}^{\text{tag}} > 3, \quad m_{jj}^{\text{tag}} > 600 \text{ GeV}$$

❖ two decay jets have to be compatible with  $W$  decay

$$M_W - 10 \text{ GeV} \leq m_{jj}^{\text{dec}} \leq M_W + 10 \text{ GeV}$$

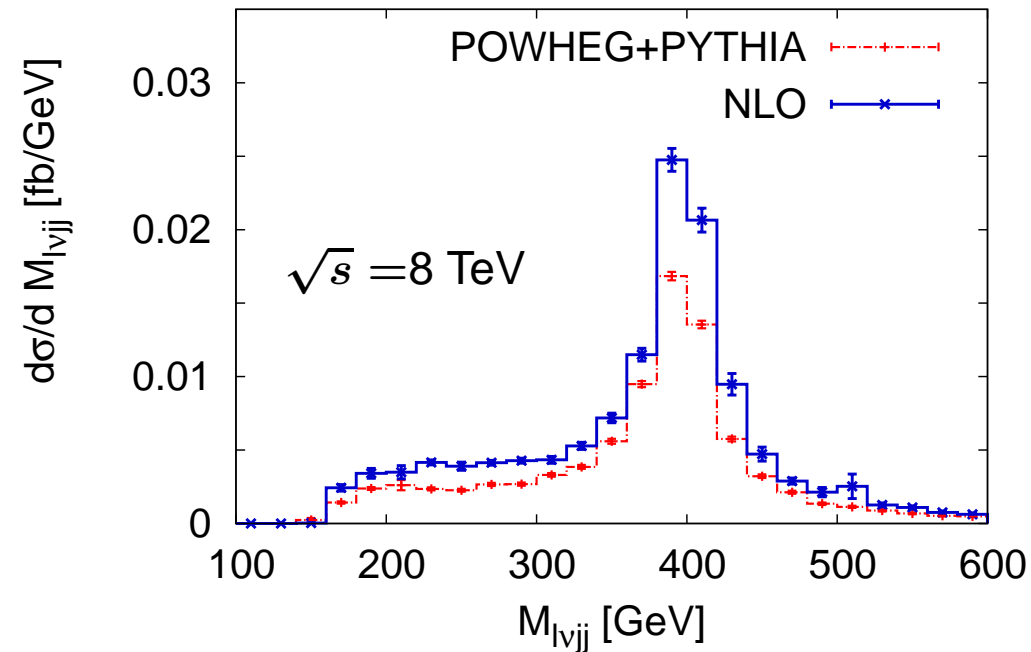
# $pp \rightarrow W^+W^-jj$ via VBF with semi-leptonic decays

- ◆ reconstruct  $M_{\ell\nu jj}$  using the assumption that

$$M_{\ell\nu} = M_W$$

( $\rightarrow$  neutrino momentum)

- ✗  $M_{\ell\nu jj}$  distribution very sensitive to parton-shower effects!

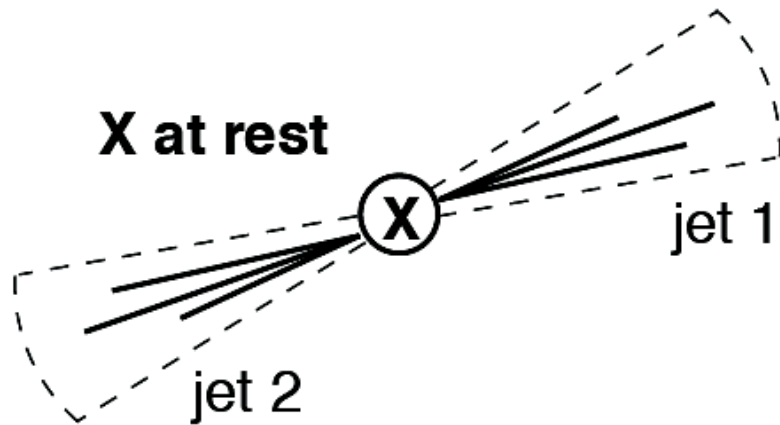


soft radiation smears distribution of  $W$  decay jets

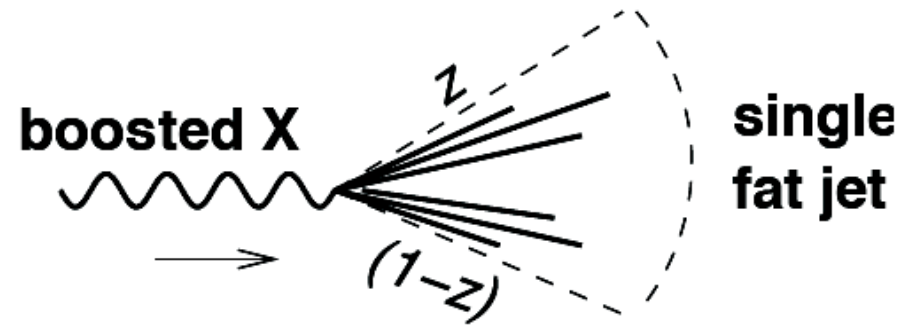
$\rightarrow m_{jj}^{\text{dec}} \sim M_W$  requirement no longer fulfilled

# boosted jet techniques

Normal analyses: two quarks from  $X \rightarrow q\bar{q}$  reconstructed as two jets



**High- $p_t$  regime: EW object X is boosted, decay is collimated,  $q\bar{q}$  both in same jet**



❖ pioneering work on  $WW$  scattering at the LHC

*Butterworth, Cox, Forshaw (2002)*

❖ break-through in  $pp \rightarrow VH$

*Butterworth, Davison, Rubin, Salam (2008)*

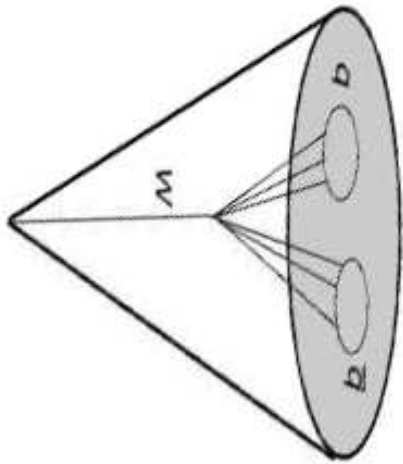
❖ today: established field in its own

# $pp \rightarrow W^+W^-jj$ via VBF with semi-leptonic decays

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$$pp \rightarrow W^+(q\bar{q}')W^-(\ell\nu)jj:$$

require a **highly boosted fat jet**  
with invariant mass close to  $M_W$



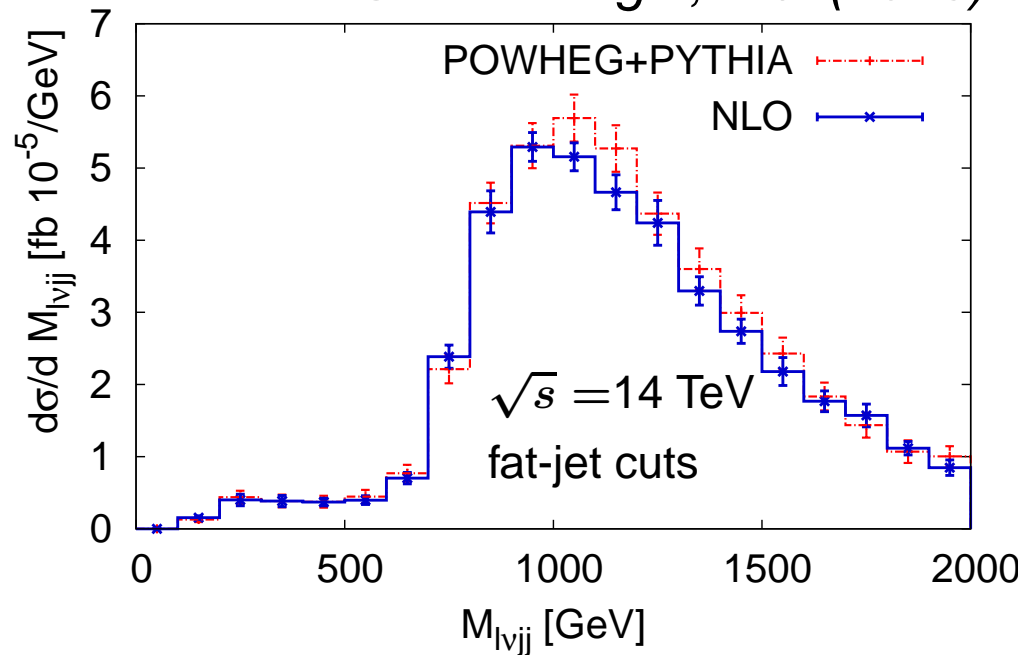
make use of jet properties / composition:

→ distinguish hadronically decaying  
heavy bosons  
from ordinary QCD jets

(stable against parton-shower effects)

# $pp \rightarrow W^+W^-jj$ via VBF with semi-leptonic decays

G. Zanderighi, B.J. (2013)



results stable against  
parton-shower effects

selection cuts  
specific for fat-jet analysis:

$$p_{T,J}^{\text{boosted}} > 300 \text{ GeV},$$
$$M_J \in (M_W \pm 10 \text{ GeV}),$$
$$p_{T,\ell} > 300 \text{ GeV}$$

cuts enforce highly energetic  
 $WW$  system  
(above light Higgs resonance)

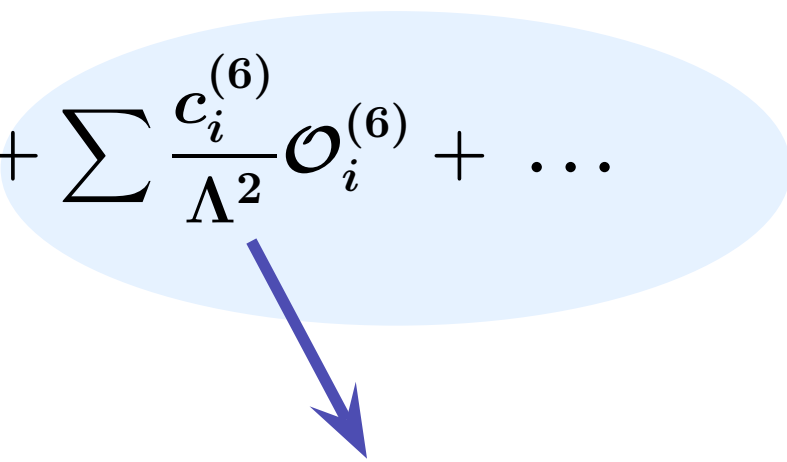
# BSM effects: effective operator approach

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parameterize deviations from Standard Model via  
**effective field theory** expansion  
(valid up to scale  $\Lambda$ ):

$$\mathcal{L}_{\text{eff}} = \sum \frac{c_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^{(d)} = \mathcal{L}_{\text{SM}} + \sum \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \dots$$

[ cf. Degrande et al. (2012) ]



modifications of triple and  
quartic gauge couplings

note: higher dim. operator coefficients severely constrained by data from LEP, Tevatron, LHC

# dimension six operators

CP conserving:

$$\mathcal{O}_{WWW} = \text{Tr}[W_{\mu\nu} W^{\nu\rho} W_{\rho}^{\mu}]$$

$$\mathcal{O}_W = (D_{\mu}\Phi)^{\dagger} W^{\mu\nu} (D_{\nu}\Phi)$$

$$\mathcal{O}_B = (D_{\mu}\Phi)^{\dagger} B^{\mu\nu} (D_{\nu}\Phi)$$

CP violating:

$$\mathcal{O}_{\tilde{W}WW} = \text{Tr}[\tilde{W}_{\mu\nu} W^{\nu\rho} W_{\rho}^{\mu}]$$

$$\mathcal{O}_{\tilde{W}} = (D_{\mu}\Phi)^{\dagger} \tilde{W}^{\mu\nu} (D_{\nu}\Phi)$$

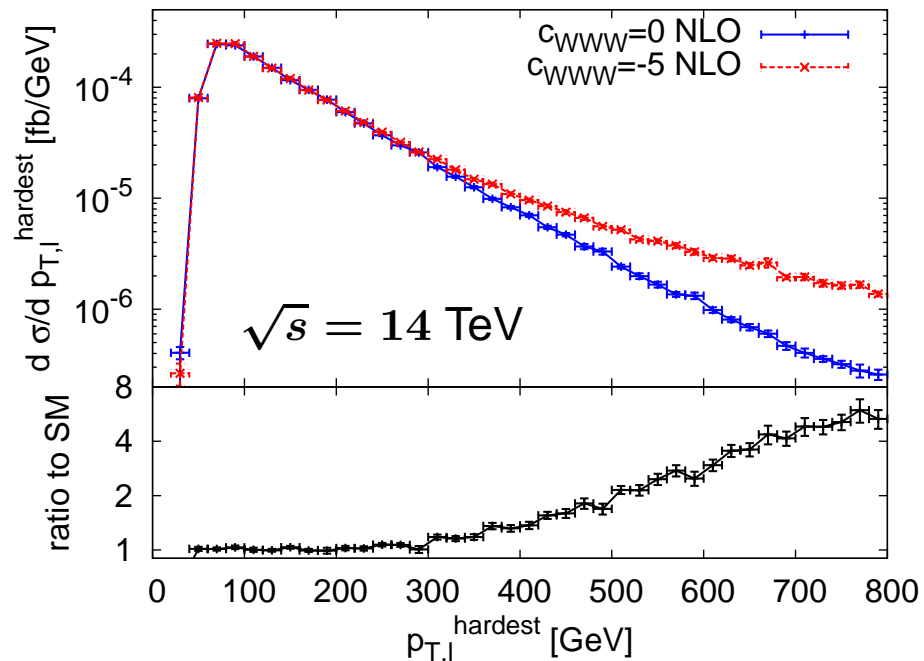
	$WWZ$	$WW\gamma$	$WWH$	$ZZH$	$\gamma ZH$	$WWWW$	$WWZZ$	$WWZ\gamma$	$WW\gamma\gamma$
$\mathcal{O}_{WWW}$	x	x	-	-	-	x	x	x	x
$\mathcal{O}_W$	x	x	x	x	x	x	x	x	-
$\mathcal{O}_B$	x	x	-	x	x	-	-	-	-
$\mathcal{O}_{\tilde{W}WW}$	x	x	-	-	-	x	x	x	x
$\mathcal{O}_{\tilde{W}}$	x	x	x	x	x	-	-	-	-

impact of dim-6 operators on triple and quartic gauge couplings



# new interactions in electroweak $ZZjj$ production

Karlberg, Zanderighi, B.J. (2013)



allow for non-zero dimension-six operator coefficients

(compatible with exp. limits)

→ tails of transverse momentum distributions enhanced

but:

very demanding at LHC14 because of small signal rates

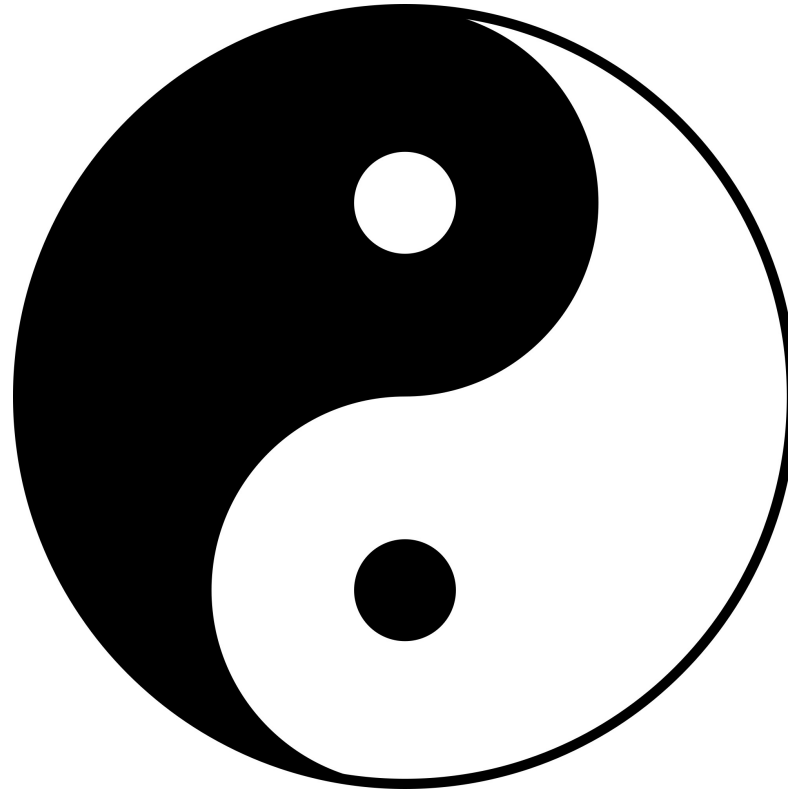
(much better limits possible with 33 or 100 TeV)

# two sides of the same picture

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Higgs sector

vector boson scattering



vector boson fusion

electroweak symmetry breaking

# Higgs as a tool

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Higgs boson is becoming **precision tool**  
for exploring the electro-weak sector



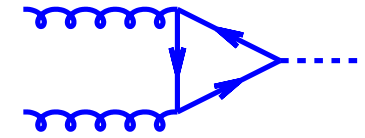
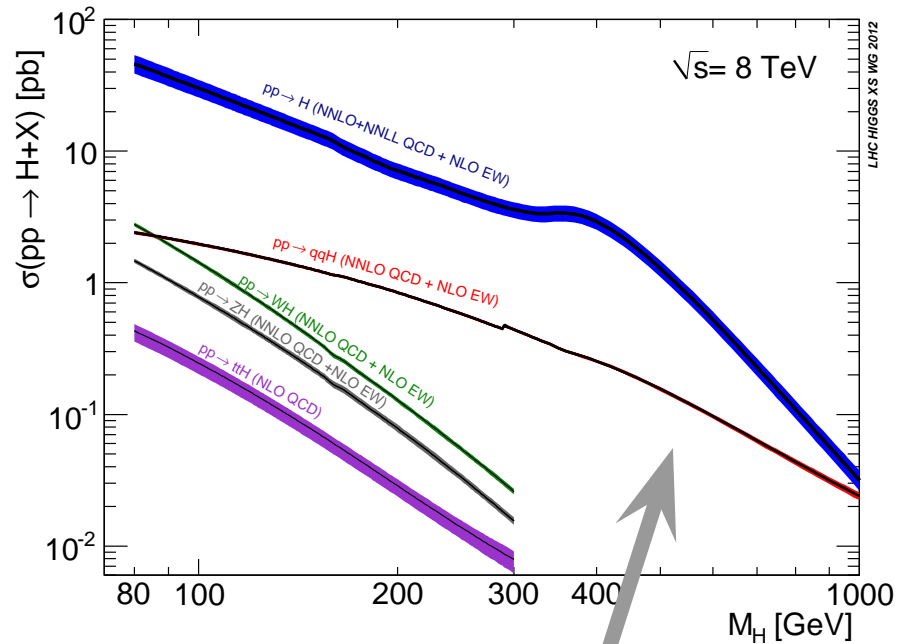
Higgs sector

electroweak symmetry breaking

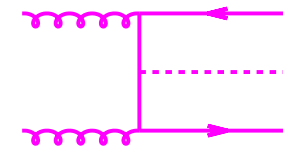
vector boson fusion

# why VBF Higgs production?

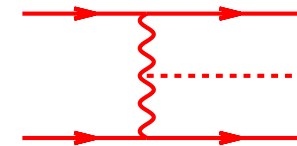
Higgs cross section WG



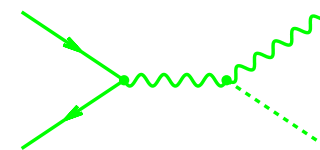
gluon fusion (GF)



$t\bar{t}H$  production



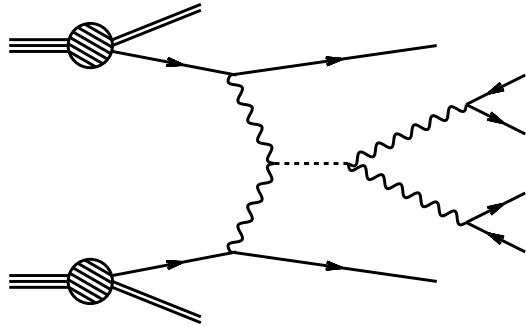
vector boson fusion (VBF)



$W, Z$  bremsstrahlung

- ❖ second-largest Higgs production cross section at the LHC
- ❖ largest cross section that involves only tree-level production

# why VBF Higgs production?

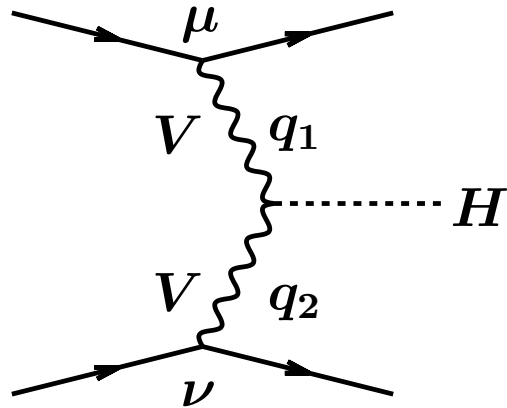


**distinctive signature** → very useful for  
signal extraction and  
background suppression

**suppressed color exchange** between quark lines gives rise to

- ❖ little jet activity in central rapidity region
  - ❖ scattered quarks → **two forward tagging jets**
  - ❖ Higgs **decay products** typically **between** tagging jets
- 👉 allows a **determination of couplings and CP-properties**  
of the Higgs boson

# tensor structure of the $HVV$ coupling



most general  $HVV$  vertex:

$$T^{\mu\nu} = a_1 g^{\mu\nu} + a_2 (q_1 \cdot q_2 g^{\mu\nu} - q_1^\nu q_2^\mu) + a_3 \epsilon^{\mu\nu\rho\sigma} q_{1\rho} q_{2\sigma}$$

physical interpretation:

SM Higgs scenario:  $\mathcal{L} \sim HV_\mu V^\mu \rightarrow a_1$

CP even scenario:  $\mathcal{L}_{eff} \sim HV_{\mu\nu} V^{\mu\nu} \rightarrow a_2$

CP odd scenario:  $\mathcal{L}_{eff} \sim HV_{\mu\nu} \tilde{V}^{\mu\nu} \rightarrow a_3$

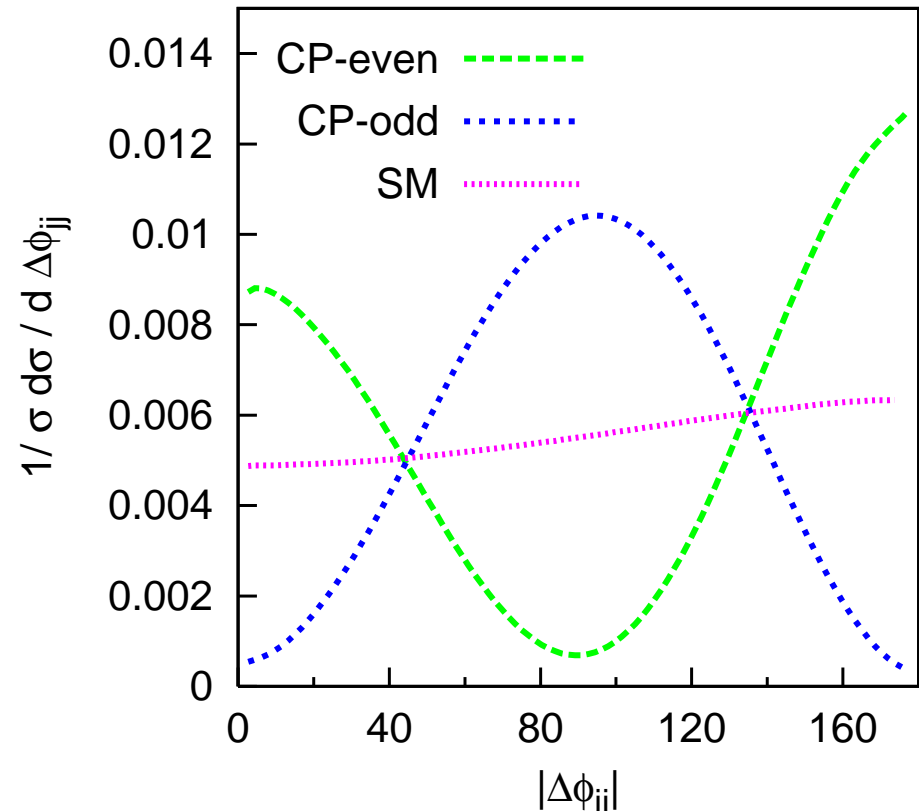
# $CP$ properties of the Higgs boson

azimuthal angle between  
tagging jets

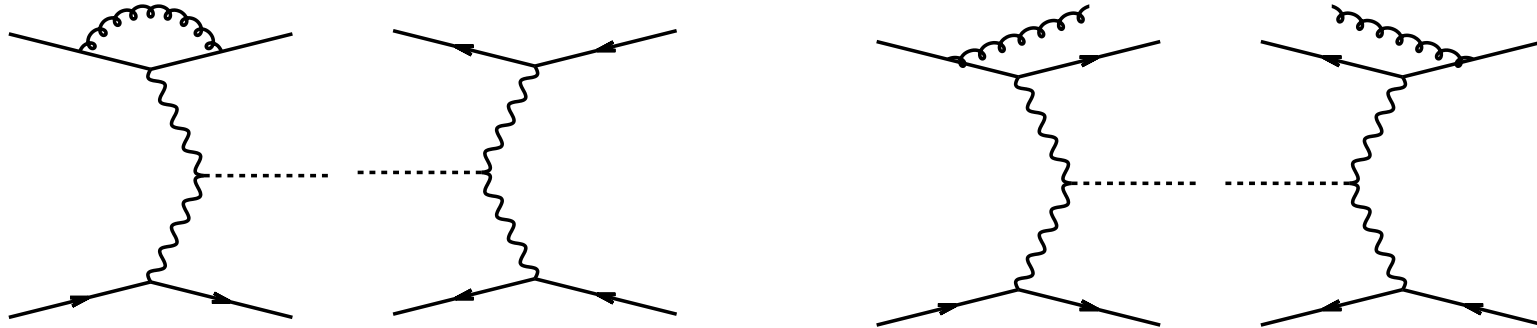


dip structure at  $90^\circ$  (CP even)  
or  $0/180^\circ$  (CP odd)  
only depends on **tensor  
structure of  $HVV$  vertex**  
(little dependence on actual  
size of form factor,  
QCD corrections,  
Higgs mass etc.)

*Figy et al. (2006)*



# Higgs production in VBF @ NLO QCD



NLO QCD:

inclusive cross section:

*Han, Valencia, Willenbrock (1992)*

distributions:

*Figy, Oleari, Zeppenfeld (2003)*

*Berger, Campbell (2004)*



NLO QCD corrections  
moderate

and well under control  
(order 10% or less)

publicly available  
parton-level Monte Carlos:

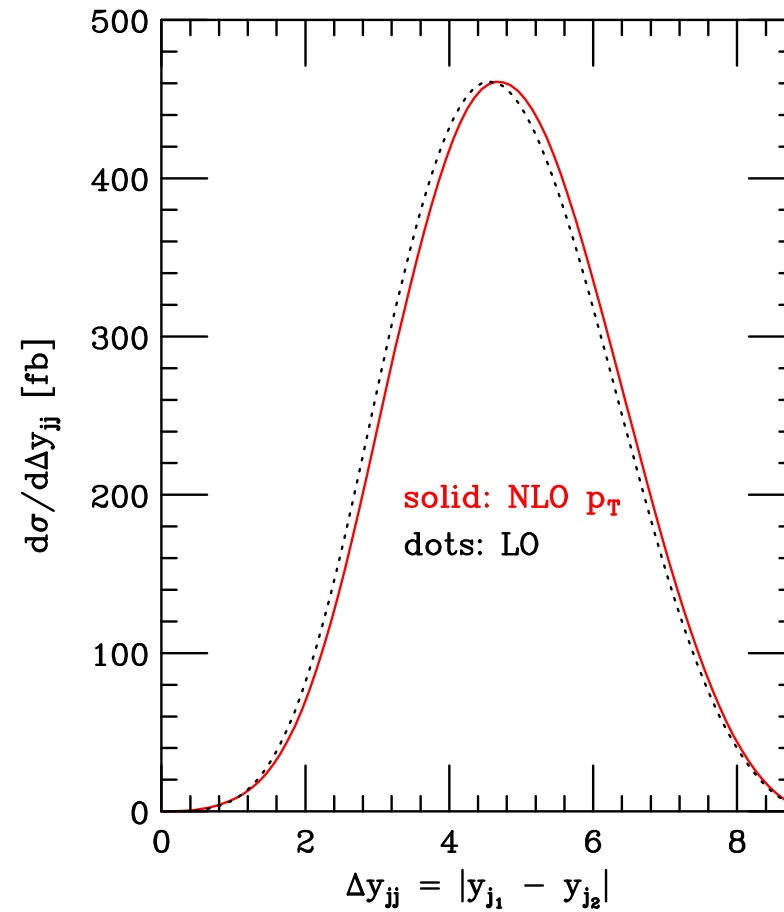
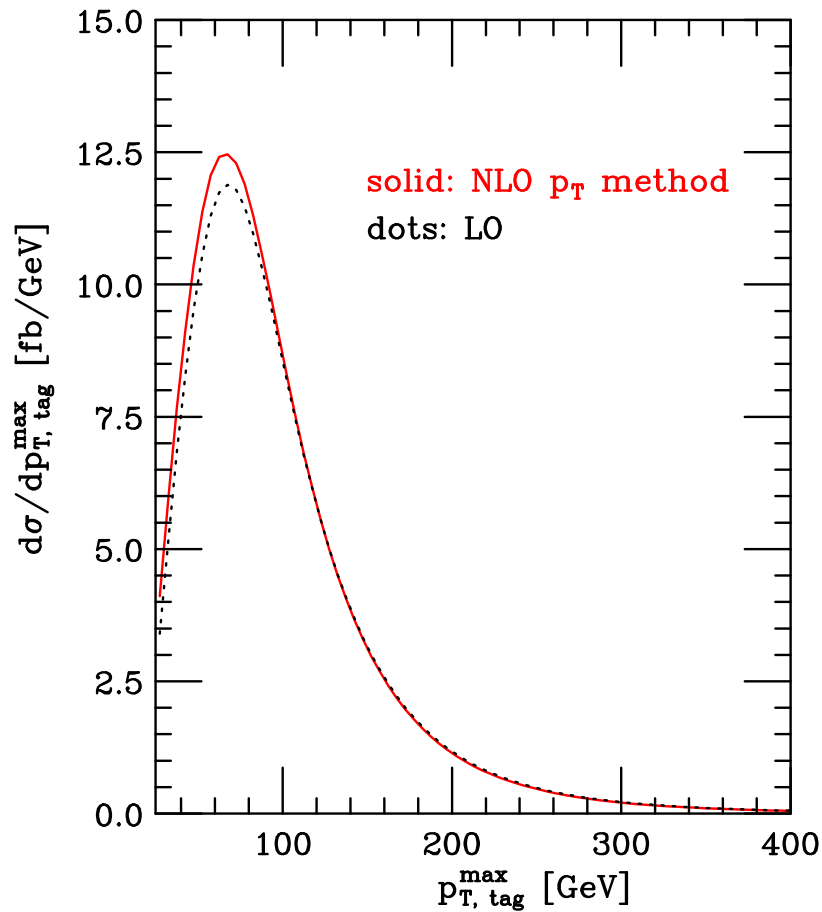
VBFNLO

MCFM



# Higgs production in VBF @ NLO QCD

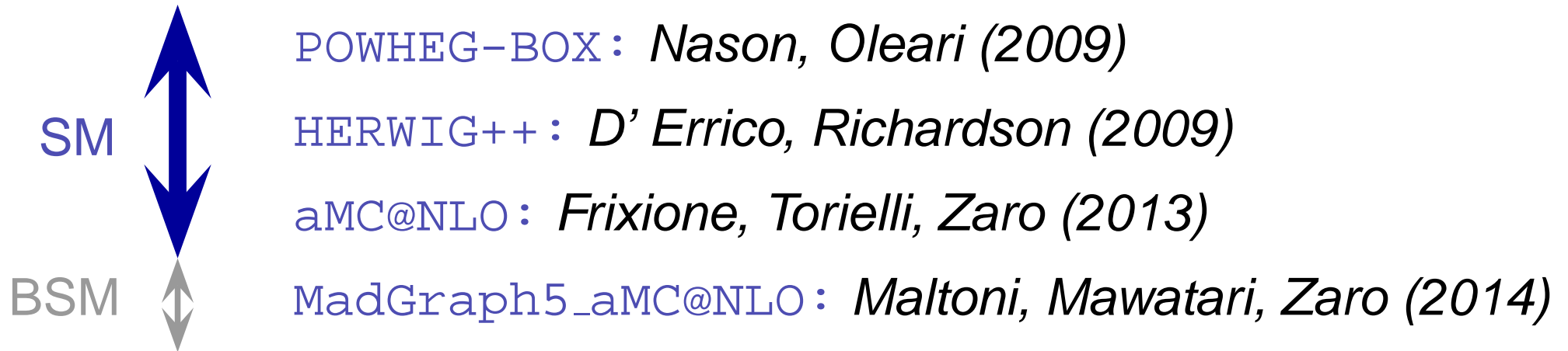
*Figy, Oleari, Zeppenfeld (2003)*



# $pp \rightarrow Hjj$ via VBF @ NLO QCD with parton shower

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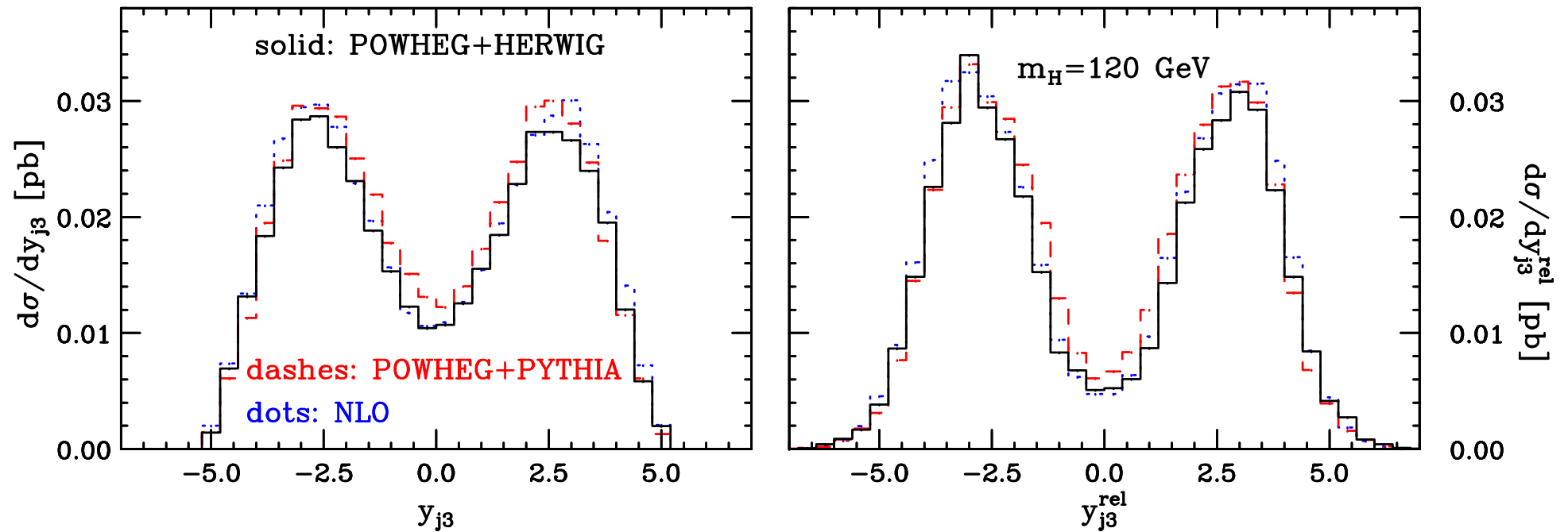
various implementations in different frameworks available:



generally **parton shower does not significantly modify**  
distributions related to **tagging jets**

# $pp \rightarrow Hjj$ via VBF @ NLO QCD with parton shower

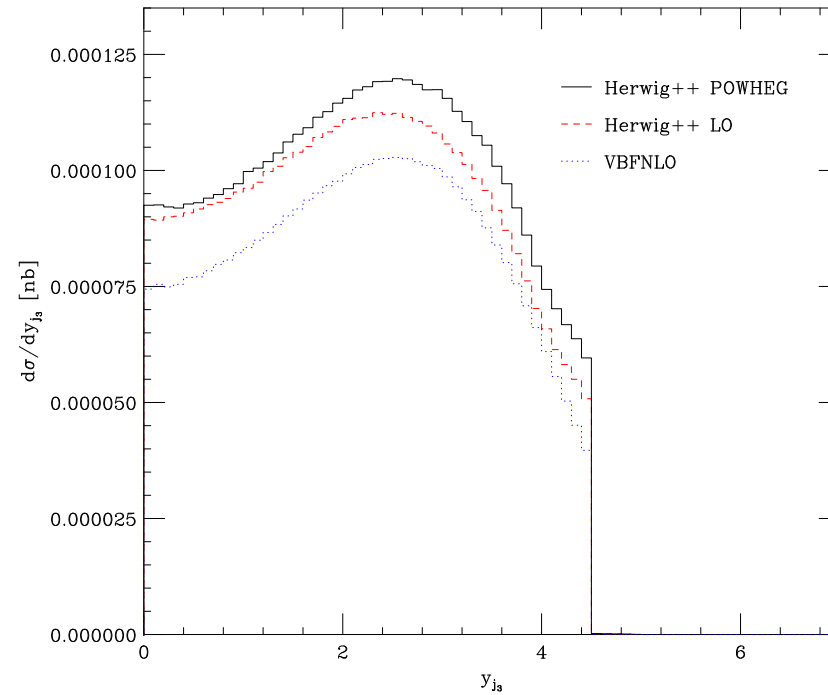
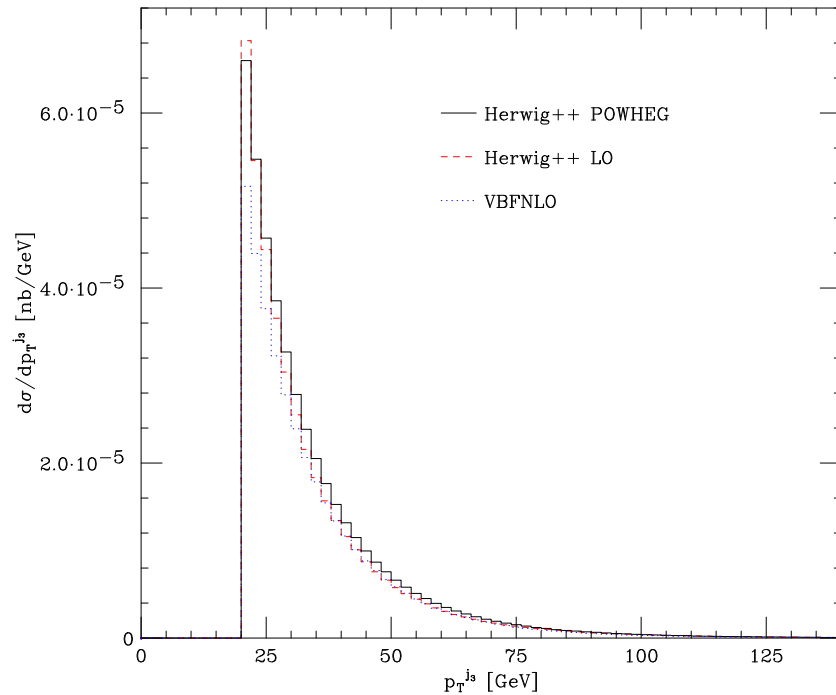
Nason, Oleari (2009)



distributions related to the **third jet** are more **sensitive to parton shower effects** and details of the **implementation**

# $pp \rightarrow Hjj$ via VBF and parton showers @ NLO

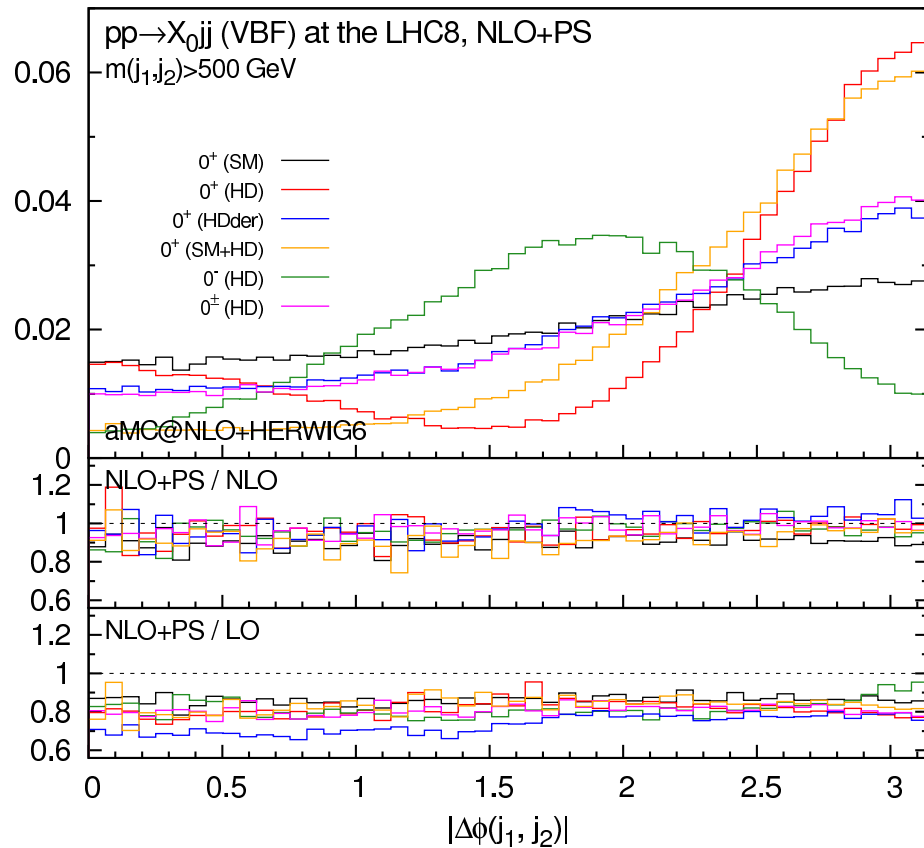
Richardson, De Luca (2011)



- ❖ parton-level NLO calculation matched via POWHEG with HERWIG++ including vetoed truncated shower ( $\leftrightarrow$  angular-ordered PS)
- ❖ HERWIG++ results differ from pure parton level at LO and NLO

# $pp \rightarrow Hjj$ via VBF: NLO+PS and BSM effects

Maltoni, Mawatari, Zaro (2013)

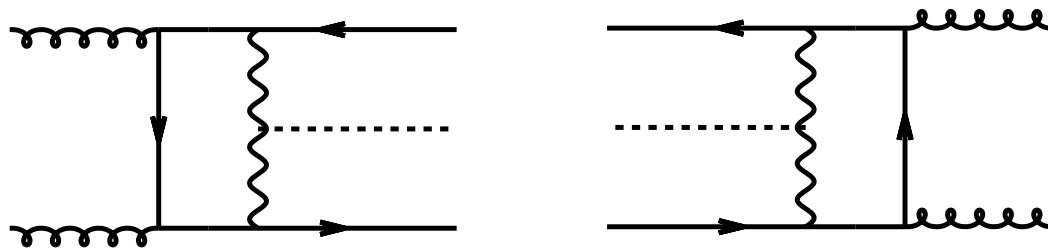


impact of higher-dimensional operators on azimuthal angle correlation of tag jets not depleted by parton shower

# higher orders of QCD in VBF

*Harlander, Vollinga, Weber (2007):*

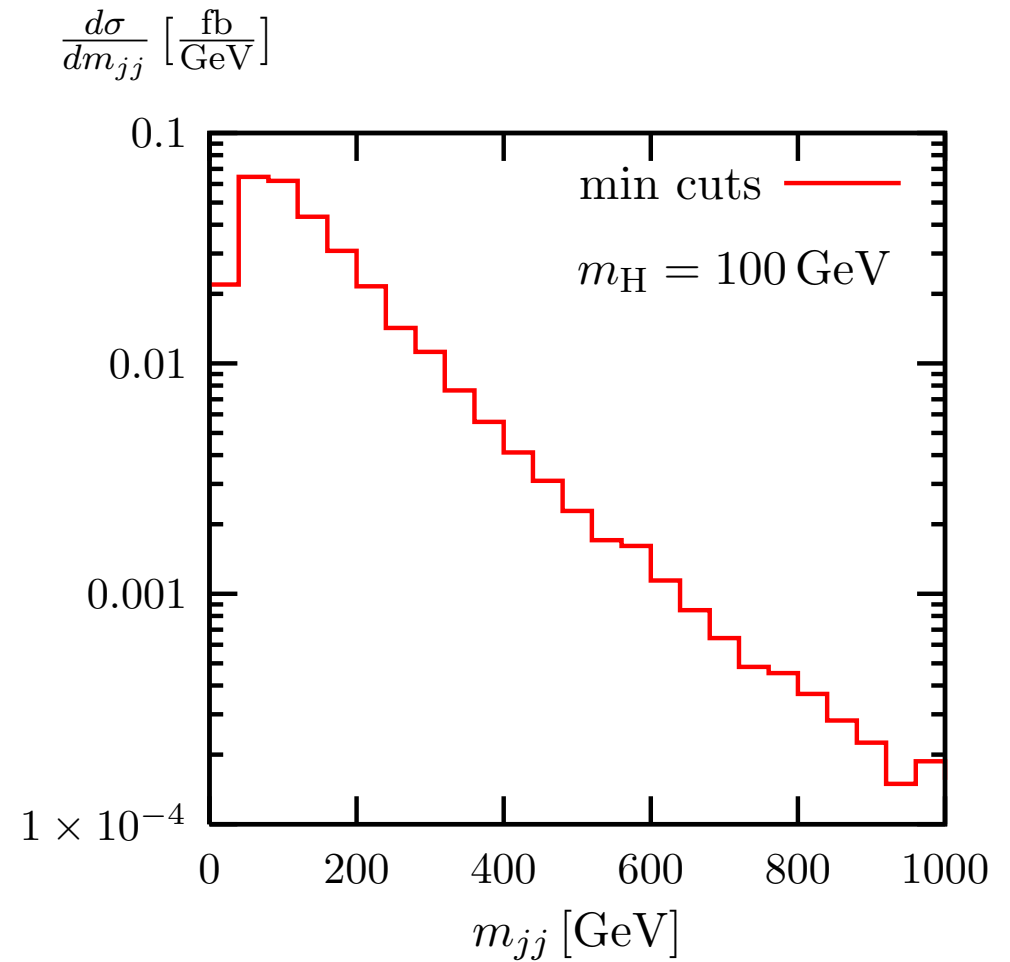
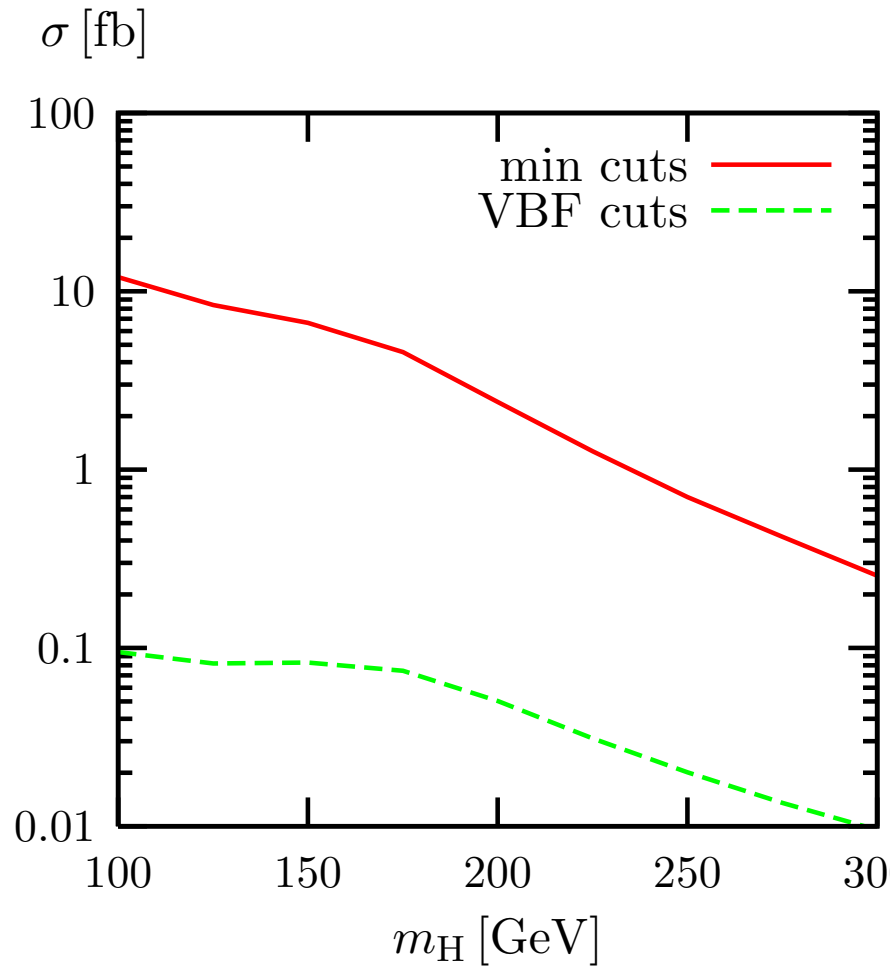
gauge invariant, finite sub-class of virtual  
**two-loop QCD corrections** to  $pp \rightarrow Hjj$  via VBF



important due to large  
gluon luminosity at LHC?

$$gg \rightarrow q\bar{q}H, q\bar{q} \rightarrow ggH,$$
$$qg \rightarrow qgH, \bar{q}g \rightarrow \bar{q}gH$$

# higher orders in VBF?



taken from *M. M. Weber, proceedings contributions to "Loops and Legs 2006"*

# higher orders in VBF?

---

- \* minimal set of cuts:

$$\sigma^{(2-loop)}(gg \rightarrow q\bar{q}H) \sim \mathbf{0.3\%} \text{ of } \sigma^{NLO}(q\bar{q} \rightarrow q\bar{q}H)$$

- \* VBF cuts: **strong suppression**

( $\sim 2$  orders of magnitude)

- rapidity gap  $\Delta\eta_{jj}$  smaller than in VBF
- $M_{jj}$  ... rapid decrease

*Harlander, Weber, Vollinga (2006)*

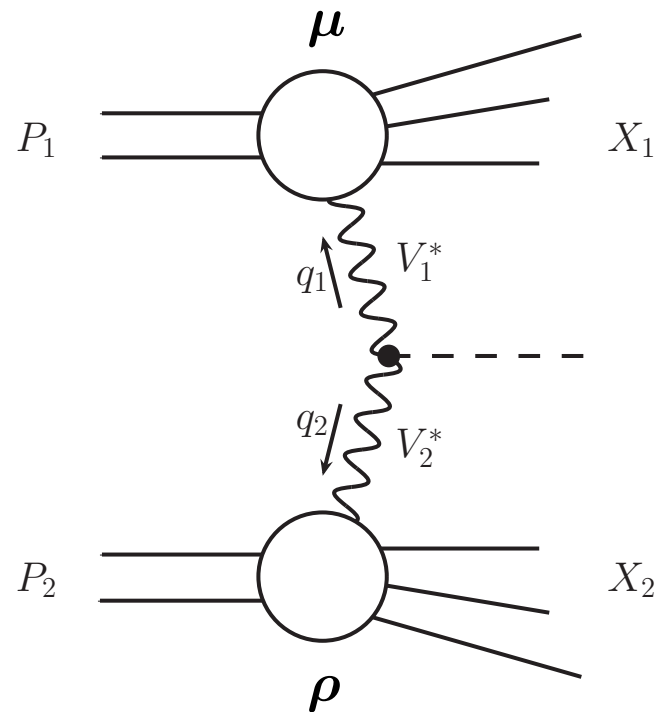


# higher orders of QCD in VBF

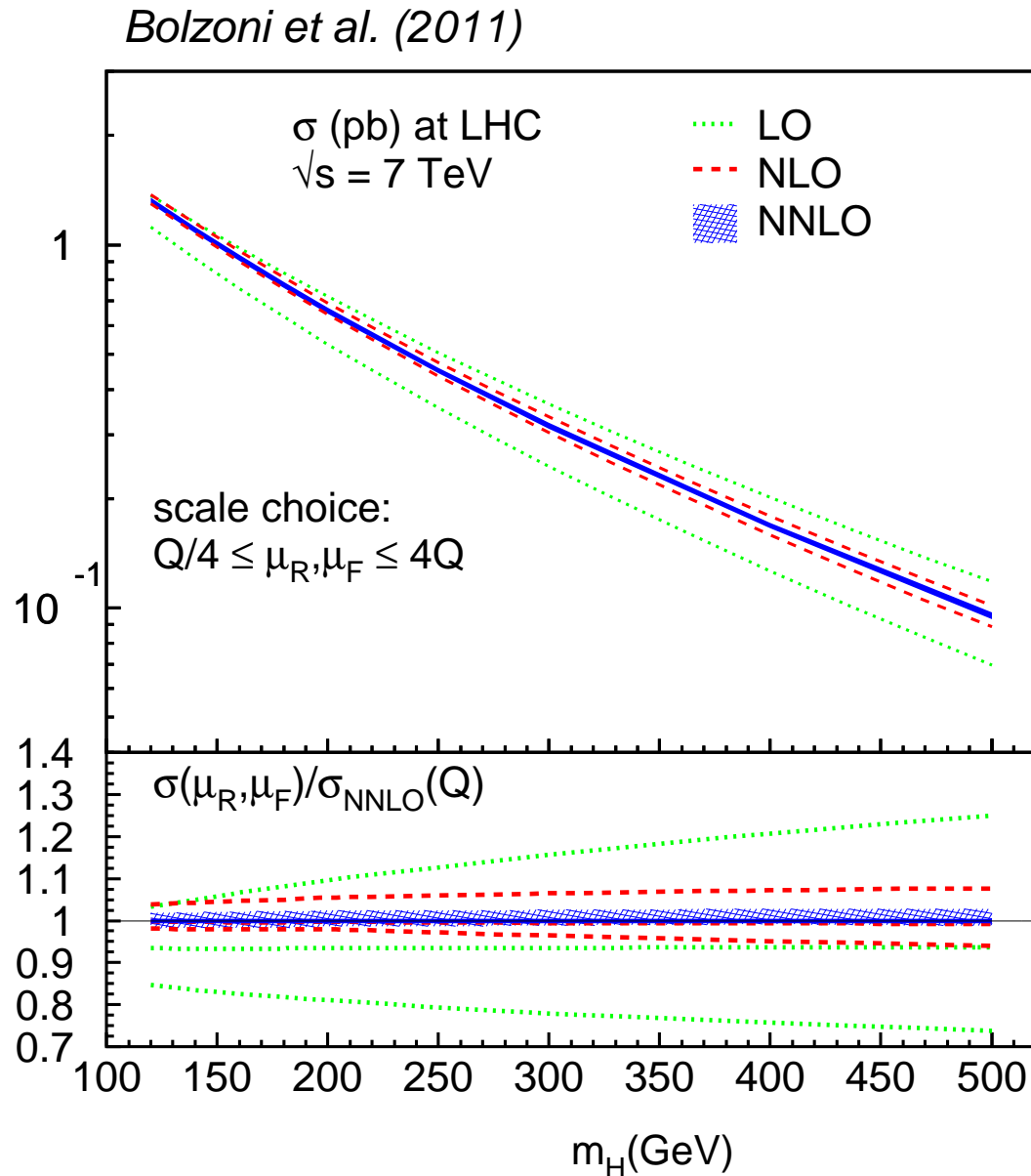
*Bolzoni, Maltoni, Moch, Zaro (2010):*

subset of the NNLO QCD contributions  
to the **total cross section** for  $pp \rightarrow Hjj$  via VBF  
in the **structure function approach**

1



# higher orders of QCD in VBF



- ◆ NNLO predictions are in full agreement with NLO results
- ◆ residual scale uncertainties are reduced from  $\sim 4\%$  to  $2\%$
- ◆ NNLO PDF uncertainties are at the  $2\%$  level

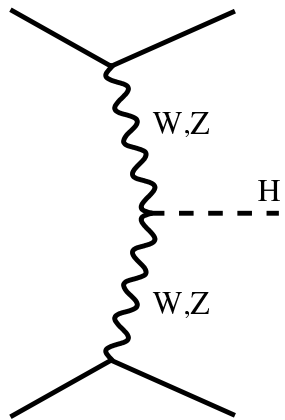
# VBF @ NNLO: exclusive results

brandnew (June 2015):

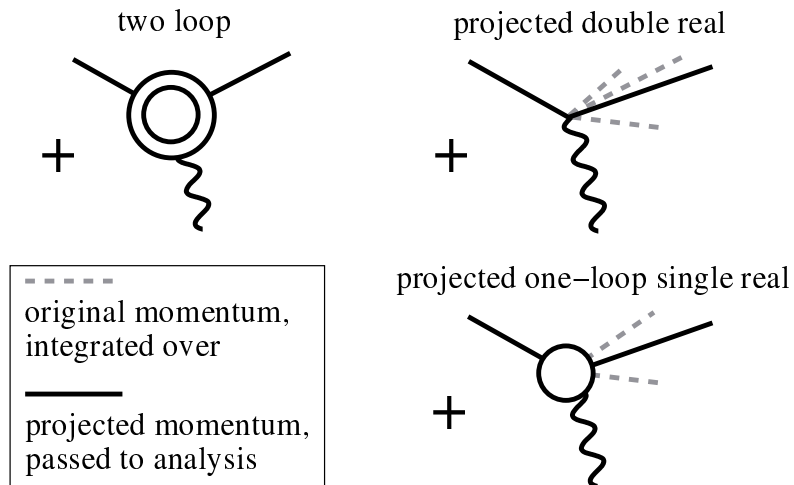
fully differential VBF Higgs production at NNLO QCD

*Cacciari, Dreyer, Karlberg, Salam, Zanderighi*

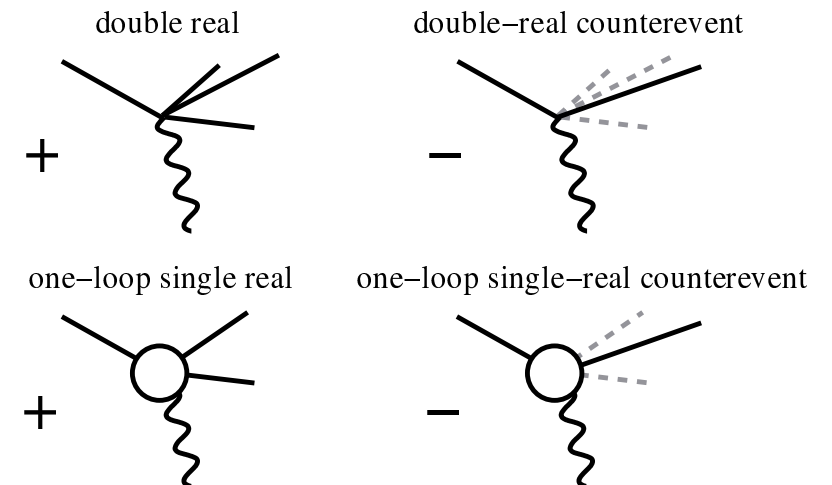
(a) Born VBF process



(b) NNLO "inclusive" part (from structure function method)



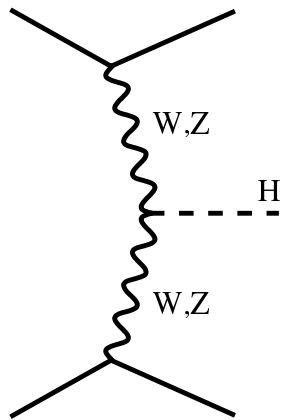
(c) NNLO "exclusive" part (from VBF H+3j@NLO)



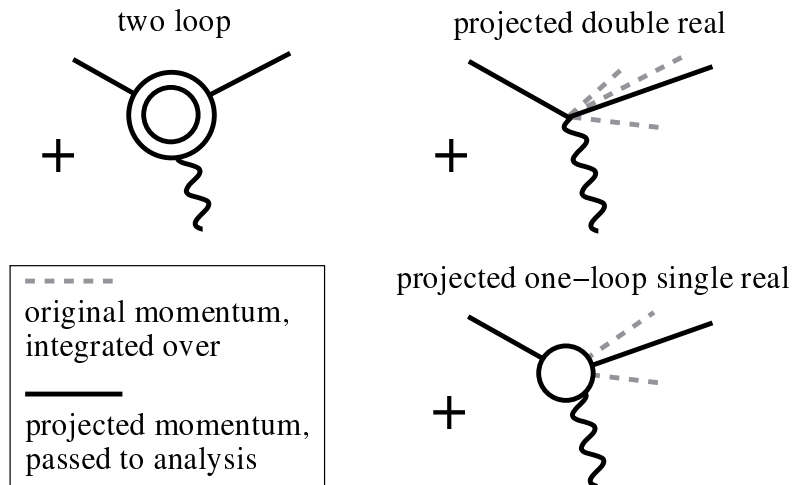
# VBF @ NNLO: exclusive results

- ◆ retain **NNLO accuracy** of structure function approach
- ◆ provide **fully differential information** on final-state kinematics

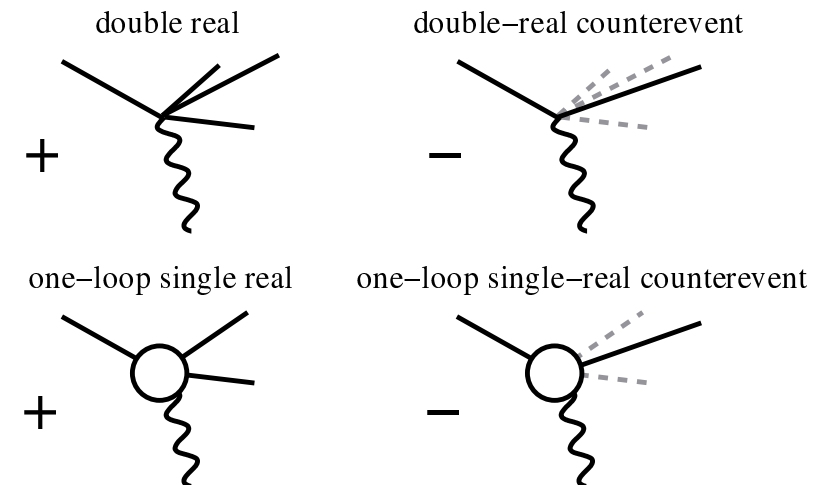
(a) Born VBF process



(b) NNLO "inclusive" part (from structure function method)



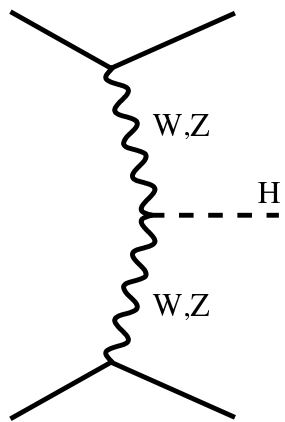
(c) NNLO "exclusive" part (from VBF H+3j@NLO)



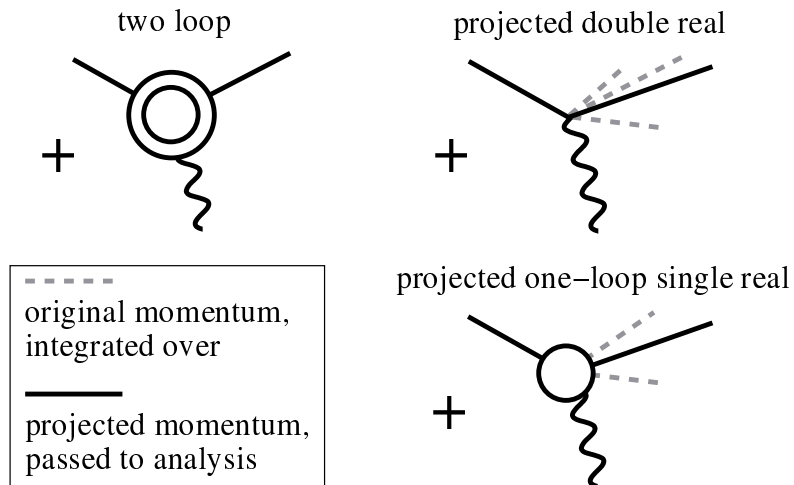
# VBF @ NNLO: exclusive results

$$\begin{aligned}
 \sigma &= \int d\Phi_B (B + V) + \int d\Phi_R R \\
 &= \underbrace{\int d\Phi_B (B + V) + \int d\Phi_R R_{\text{proj}}}_{\text{from inclusive contribution}} + \underbrace{\int d\Phi_R R - \int d\Phi_R R_{\text{proj}}}_{\text{finite, from exclusive contribution}}
 \end{aligned}$$

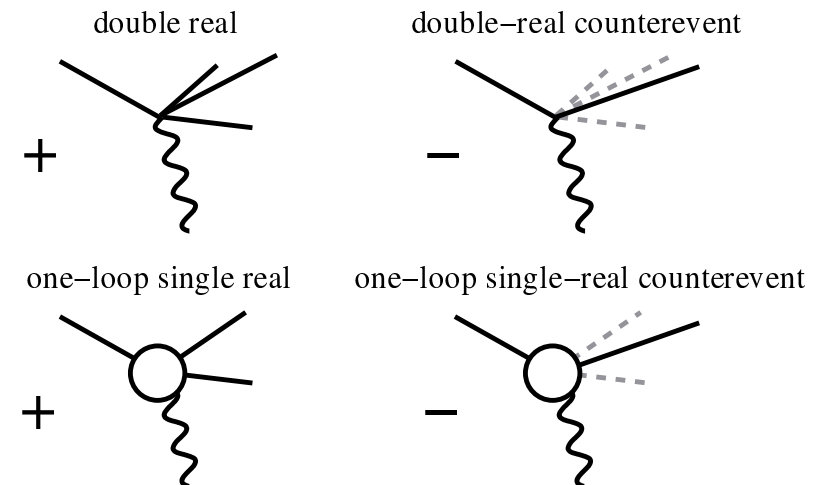
(a) Born VBF process



(b) NNLO "inclusive" part (from structure function method)



(c) NNLO "exclusive" part (from VBF H+3j@NLO)



# VBF @ NNLO: exclusive results

*Cacciari, Dreyer, Karlberg, Salam, Zanderighi (2015)*

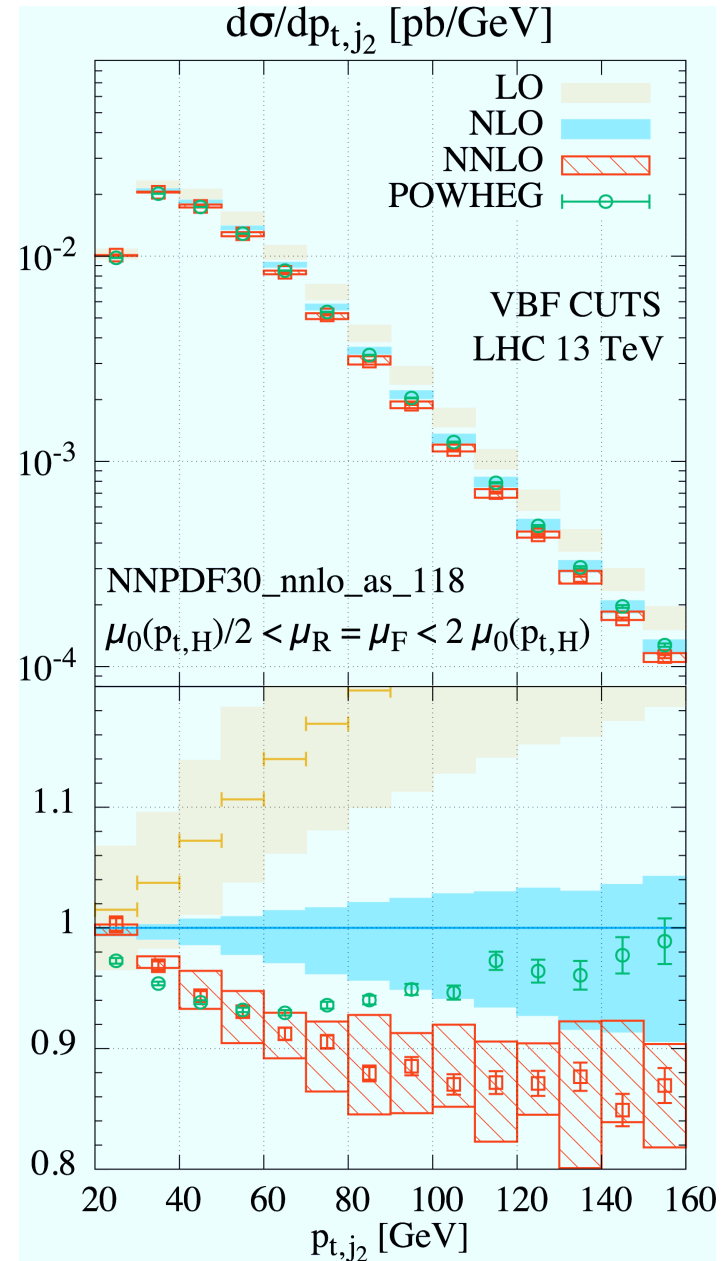
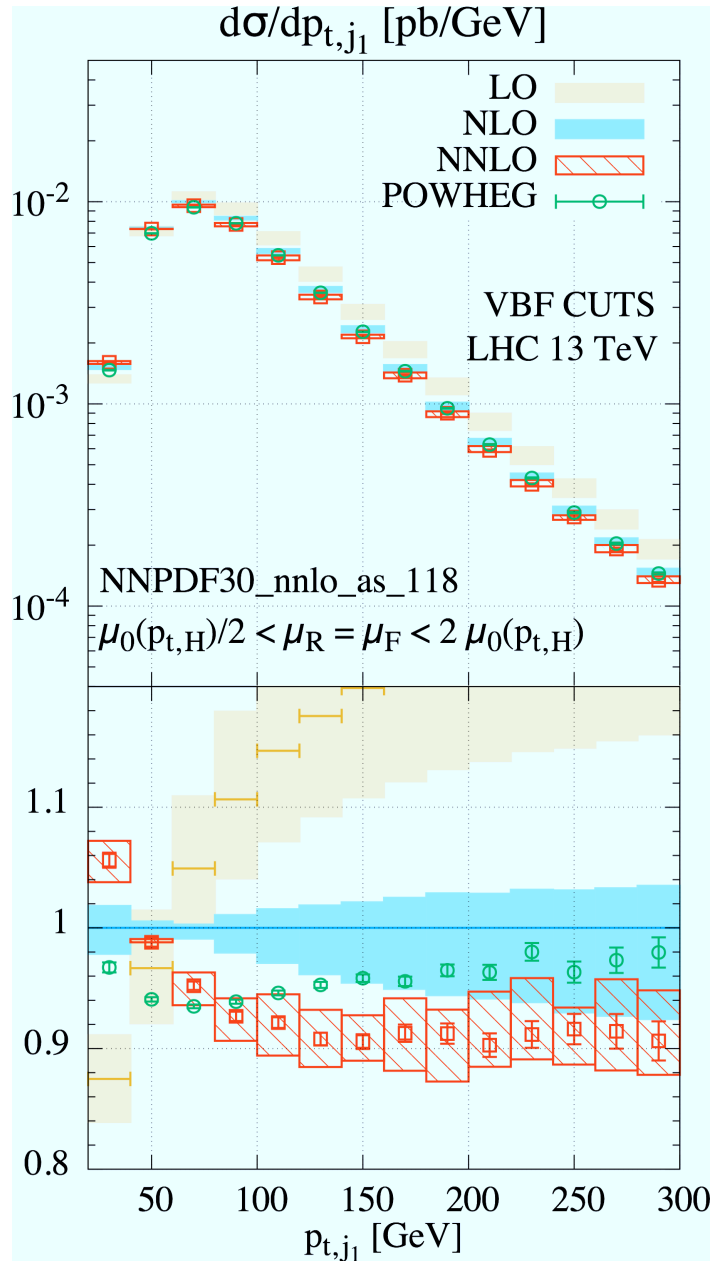
	$\sigma^{(\text{no cuts})}$ [pb]	$\sigma^{(\text{VBF cuts})}$ [pb]
LO	4.032 <sup>+0.057</sup> <sub>-0.069</sub>	0.957 <sup>+0.066</sup> <sub>-0.059</sub>
NLO	3.929 <sup>+0.024</sup> <sub>-0.023</sub>	0.876 <sup>+0.008</sup> <sub>-0.018</sub>
NNLO	3.888 <sup>+0.016</sup> <sub>-0.012</sub>	0.826 <sup>+0.013</sup> <sub>-0.014</sub>

relative NNLO  
corrections  $\sim 1\%$

relative NNLO  
corrections  $\sim 6\%$

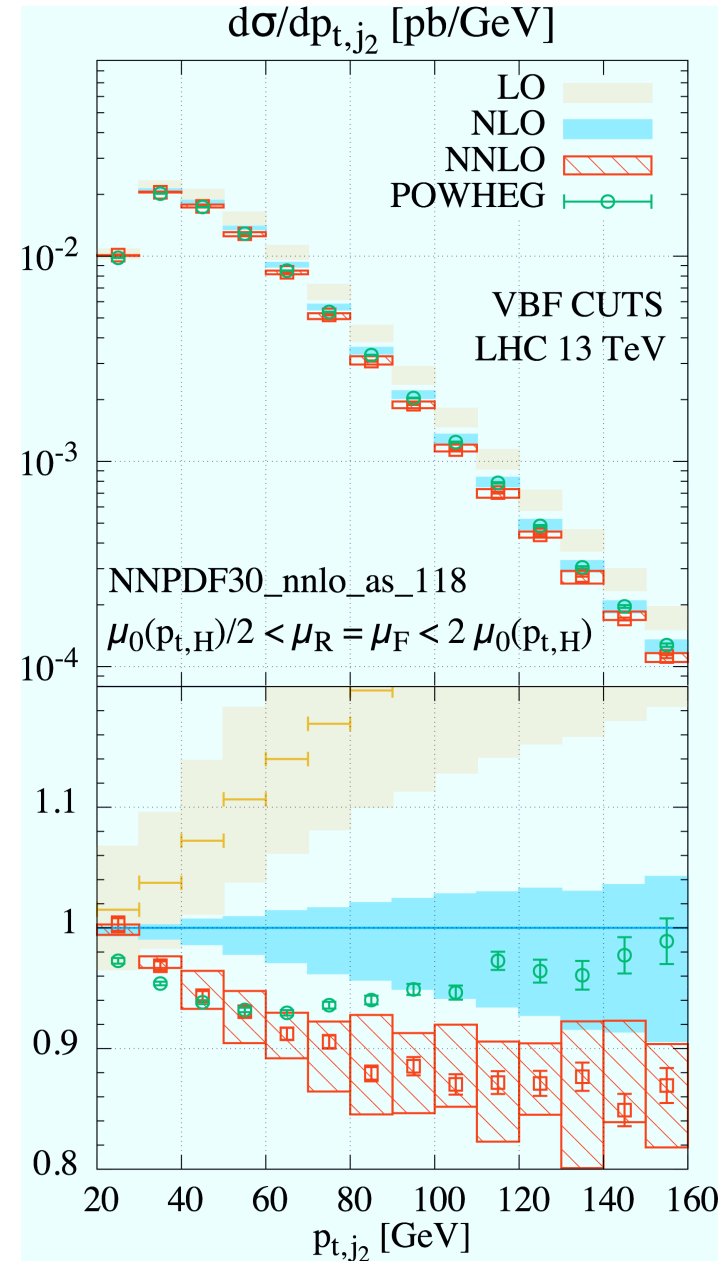
NNLO QCD corrections are much larger in VBF  
setup than for inclusive cuts

# VBF @ NNLO: exclusive results



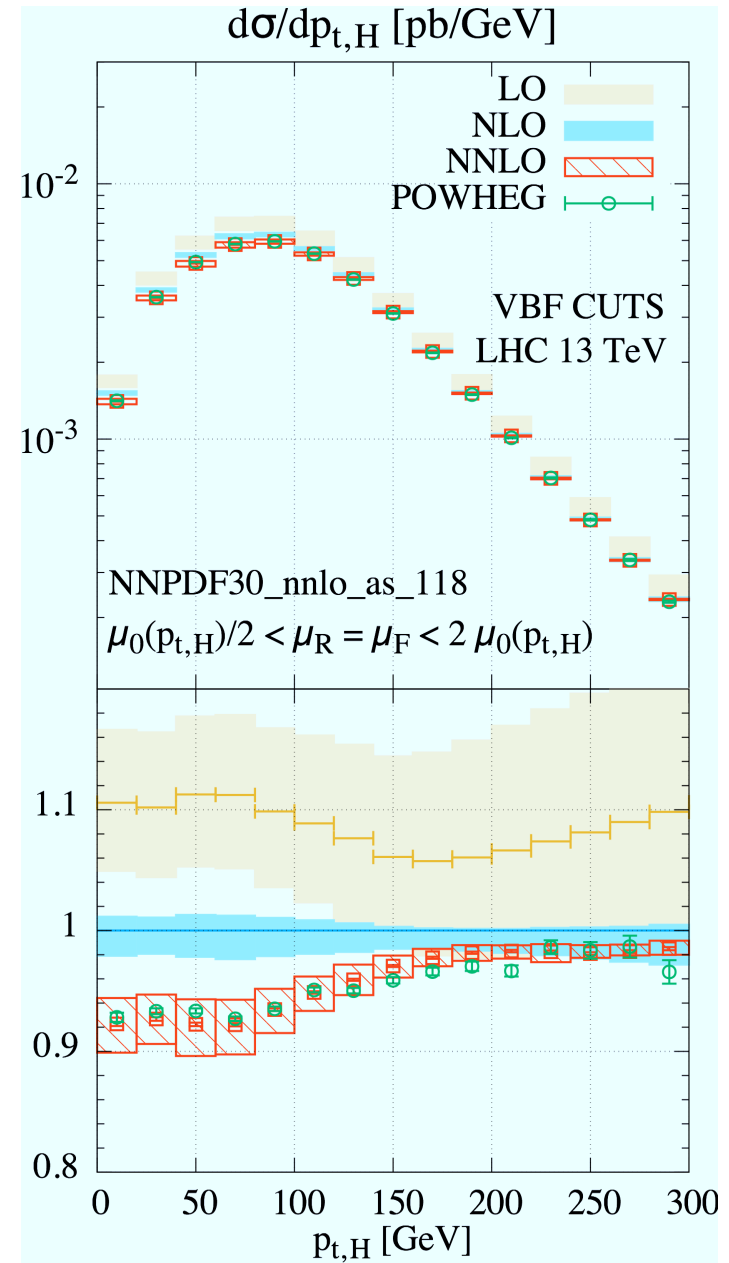
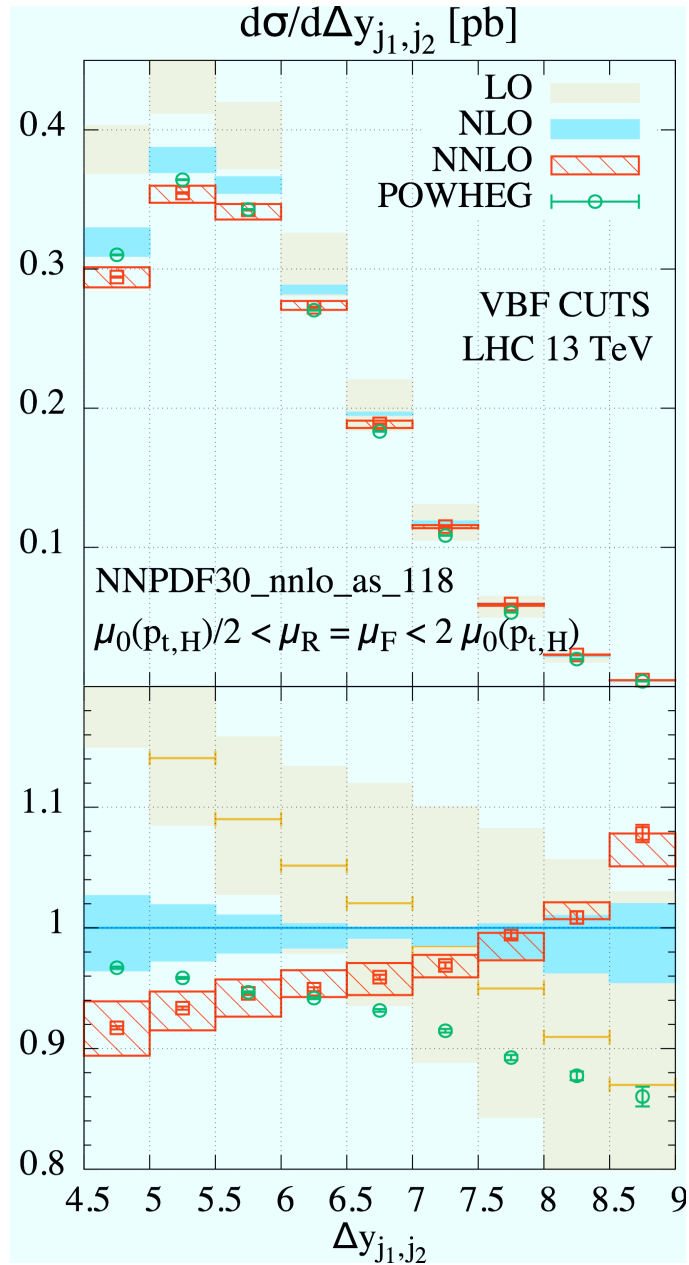
# VBF @ NNLO: exclusive results

NNLO corrections  
make jets softer  
→ fewer events pass VBF cuts





# VBF @ NNLO: exclusive results



# $pp \rightarrow Hjj$ via gluon fusion

VBF can be faked by double real corrections  
to  $gg \rightarrow H$  (“gluon fusion”)



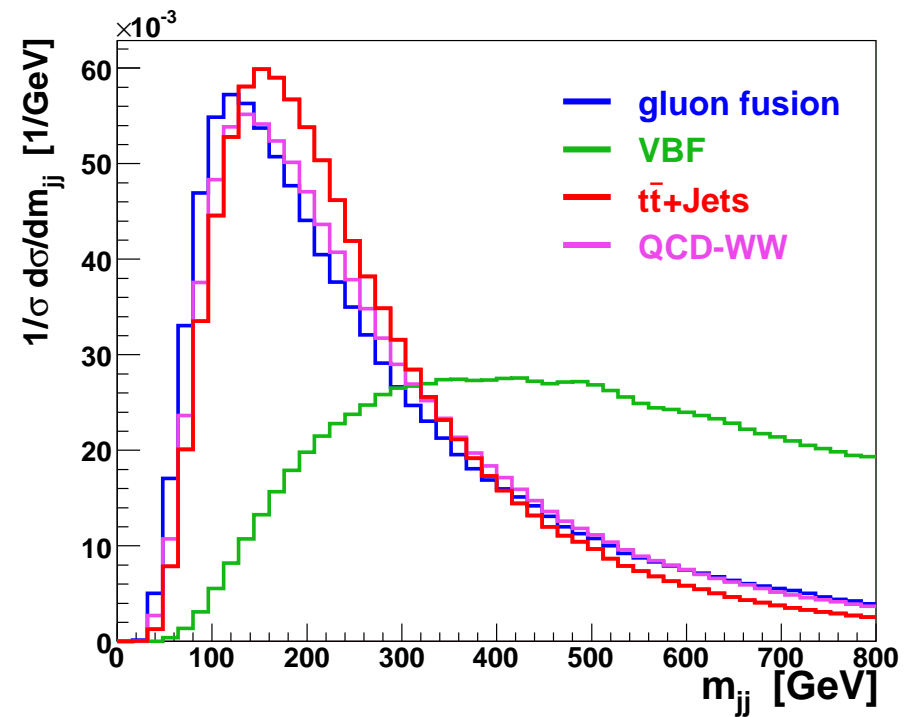
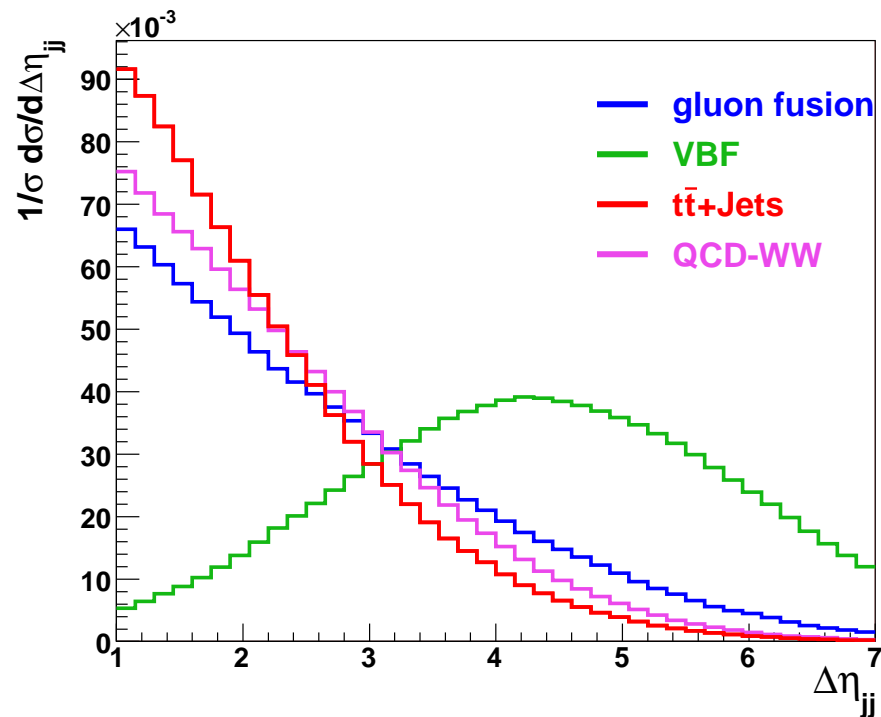
complete LO calculation (including pentagons):  
*Del Duca, Kilgore, Oleari, Schmidt, Zeppenfeld (2001)*

NLO QCD calculation in  $m_t \rightarrow \infty$  limit:  
*Campbell, Ellis, Zanderighi (2006); Greiner et al. (2013)*

need to understand **phenomenology** of both processes to  
distinguish between them

# $pp \rightarrow Hjj$ via gluon fusion

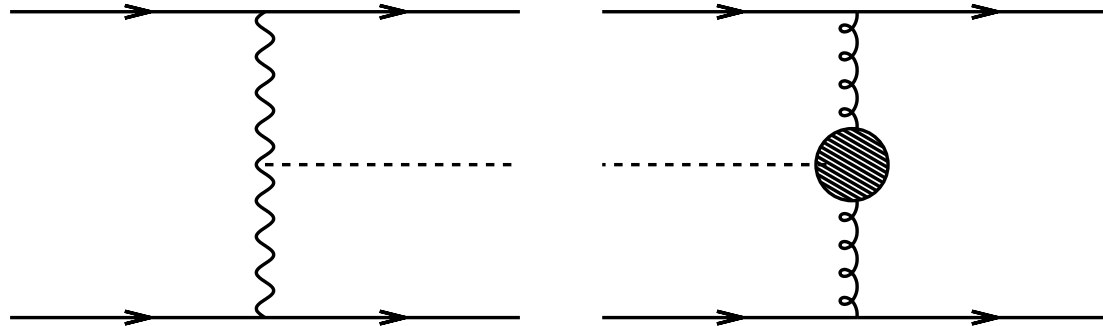
apply cuts to separate VBF from gluon fusion (GF)



*Klámke, Zeppenfeld (2007)*

# $pp \rightarrow Hjj$ via $VBF \times GF$ at tree level

can  $VBF \times GF$  interference pollute the clean VBF signature?



*Georg (2005) & Andersen, Smillie (2006):*

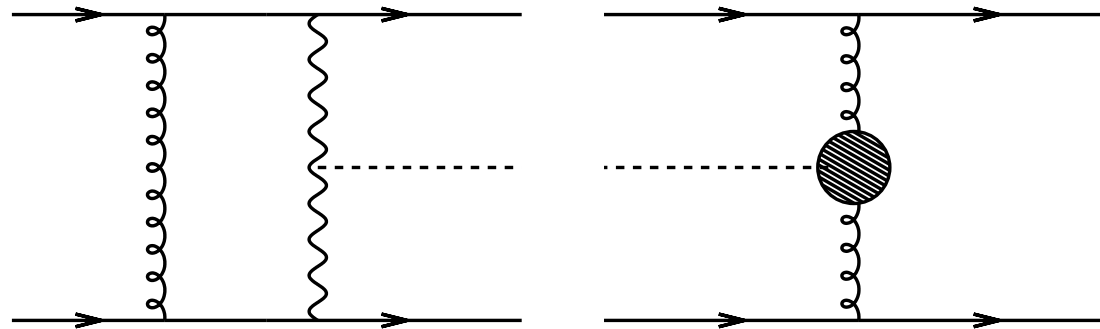
tree-level interference possible only for

- neutral current graphs (no charged current interference)
- identical quark contributions with  $t \leftrightarrow u$  crossing (kinematically suppressed)

☞ completely negligible

# $pp \rightarrow Hjj$ via $\text{VBF} \times \text{GF}$ beyond tree level

additional gluon  $\rightarrow$   $\text{VBF} \times \text{GF}$  interference for  $qq' \rightarrow qq'H$  ✓  
(no  $t \leftrightarrow u$  crossing necessary)

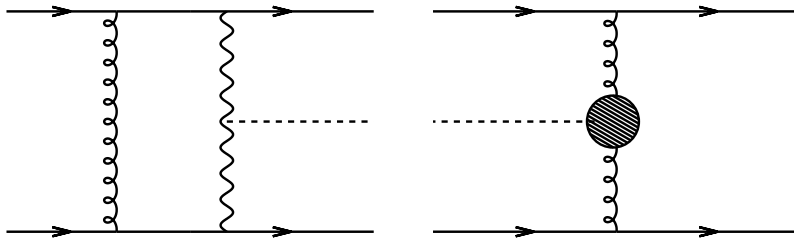


☞ speculations that the size of the **one-loop interference** could be **comparable** to the size of the one-loop **NLO-QCD corrections** to the **VBF** and the **GF** processes

# virtual contributions

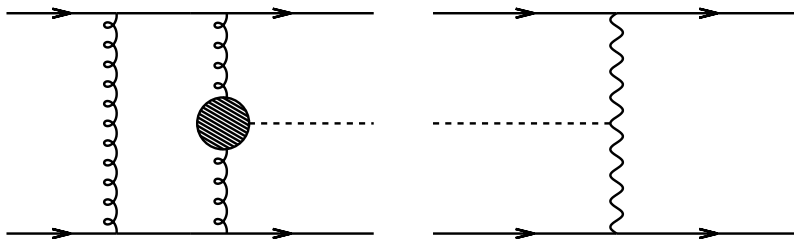
within VBF approximation need two types of loop contributions:

❖ interference of **VBF@1-loop** with GF at LO



$$\mathcal{M}_{\text{VBF}}^{(1\text{-loop})} \cdot \mathcal{M}_{\text{GF}}^{(0)\star}$$

❖ interference of **GF@1-loop** with VBF at LO



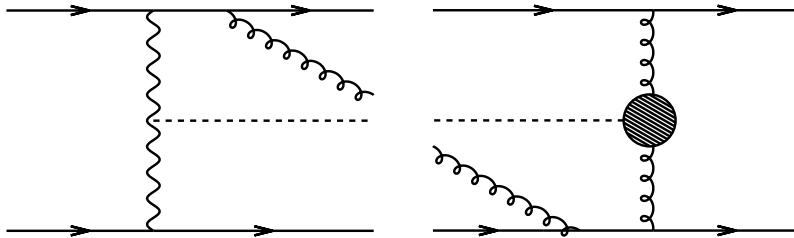
$$\mathcal{M}_{\text{GF}}^{(1\text{-loop})} \cdot \mathcal{M}_{\text{VBF}}^{(0)\star}$$

all **bubble, triangle, and box corrections vanish**

due to color conservation  $\implies$  **pentagon diagrams only!**

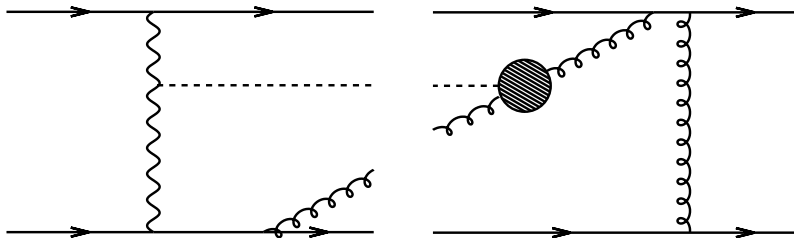
# real emission contributions

- ◆ gluons emitted from different fermion lines, Higgs in  $t$ -channel



$$\mathcal{M}_{\text{VBF}}^{(\text{real})} \cdot \mathcal{M}_{\text{GF}}^{(\text{real},t)\star}$$

- ◆ gluon (VBF) / gluon-plus-Higgs (GF) from different fermion lines

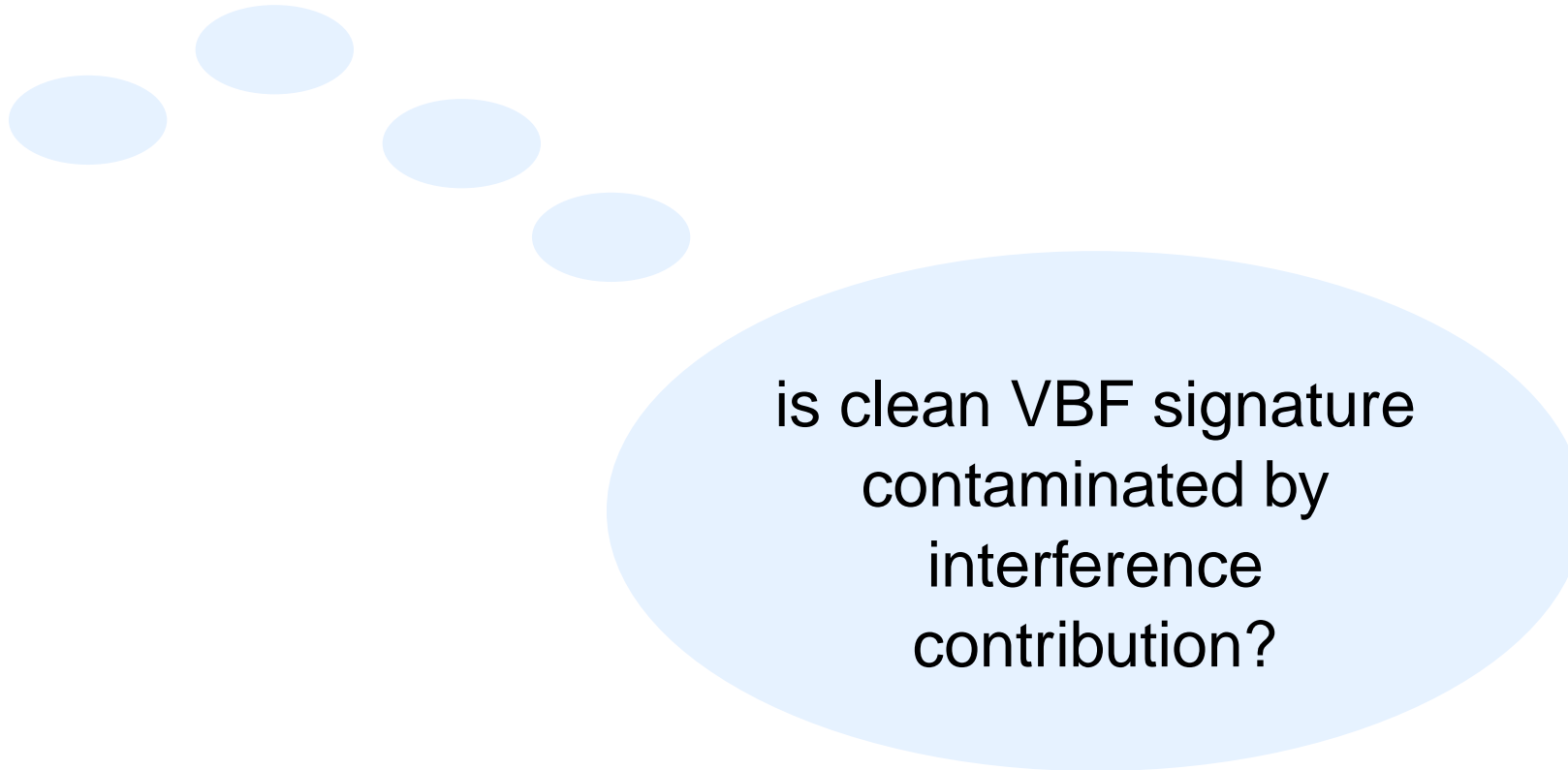


$$\mathcal{M}_{\text{VBF}}^{(\text{real})} \cdot \mathcal{M}_{\text{GF}}^{(\text{real},f)\star}$$

- ◆ no contributions from:
  - $gq$ -scattering diagrams
  - interference of graphs with gluon emission from the same fermion line in VBF and GF

... numbers ...

---



is clean VBF signature  
contaminated by  
interference  
contribution?

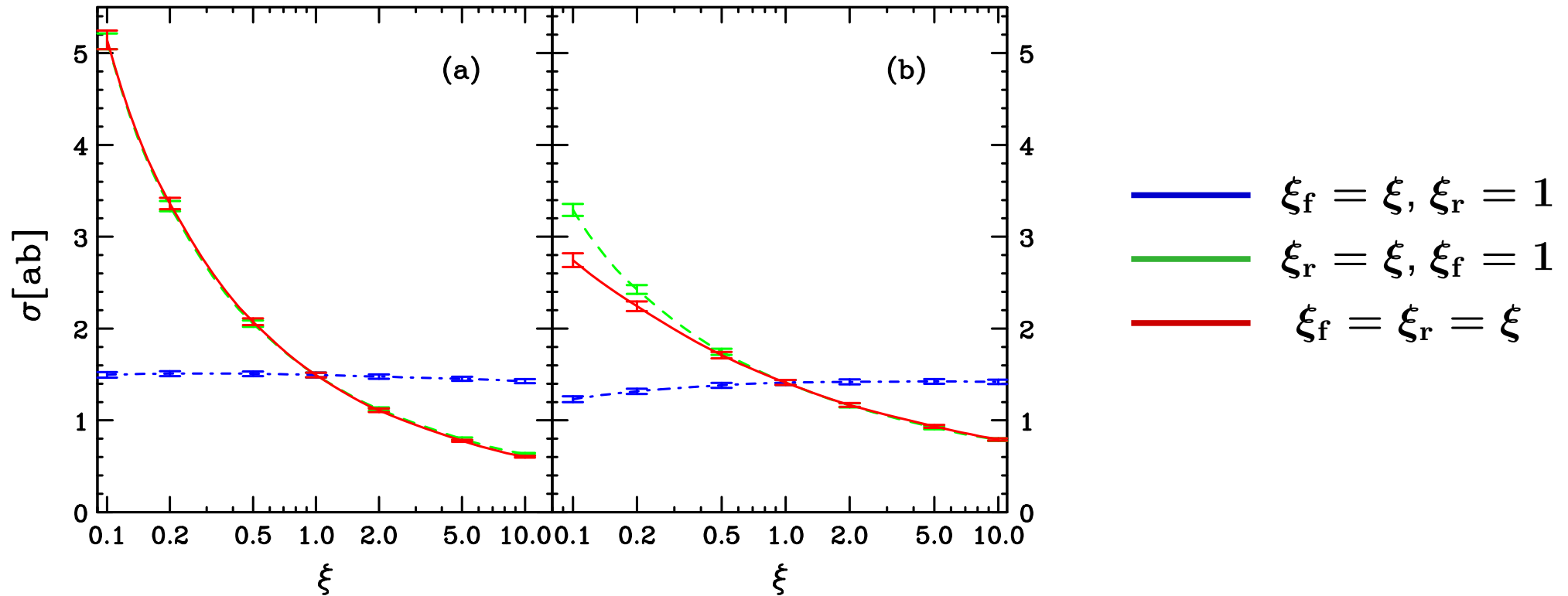


# cuts and settings

apply  $k_T$  algorithm, CTEQ6 parton distributions,  
and typical VBF cuts:

tagging jets	$p_{Tj} \geq 20 \text{ GeV}, \quad  y_j  \leq 4.5,$ $\Delta y_{jj} =  y_{j_1} - y_{j_2}  > 4,$ $M_{jj} > 600 \text{ GeV}$ <p>jets located in opposite hemispheres</p>
for $H \rightarrow \ell\ell'$ ( $\ell = \gamma, b \dots$ )	$p_{T\ell} \geq 20 \text{ GeV}, \quad  \eta_\ell  \leq 2.5, \quad \Delta R_{j\ell} \geq 0.6,$ $y_{j,\min} < \eta_\ell < y_{j,\max}$ $m_H = 120 \text{ GeV}$

# scale uncertainty



study dependence of interference x-sec on choice  
and value of scale  $\rightarrow$  two settings:

$$(a) \mu_f = \xi_f m_H, \alpha_s^3(\mu_r) = \alpha_s^3(\xi_r m_H)$$

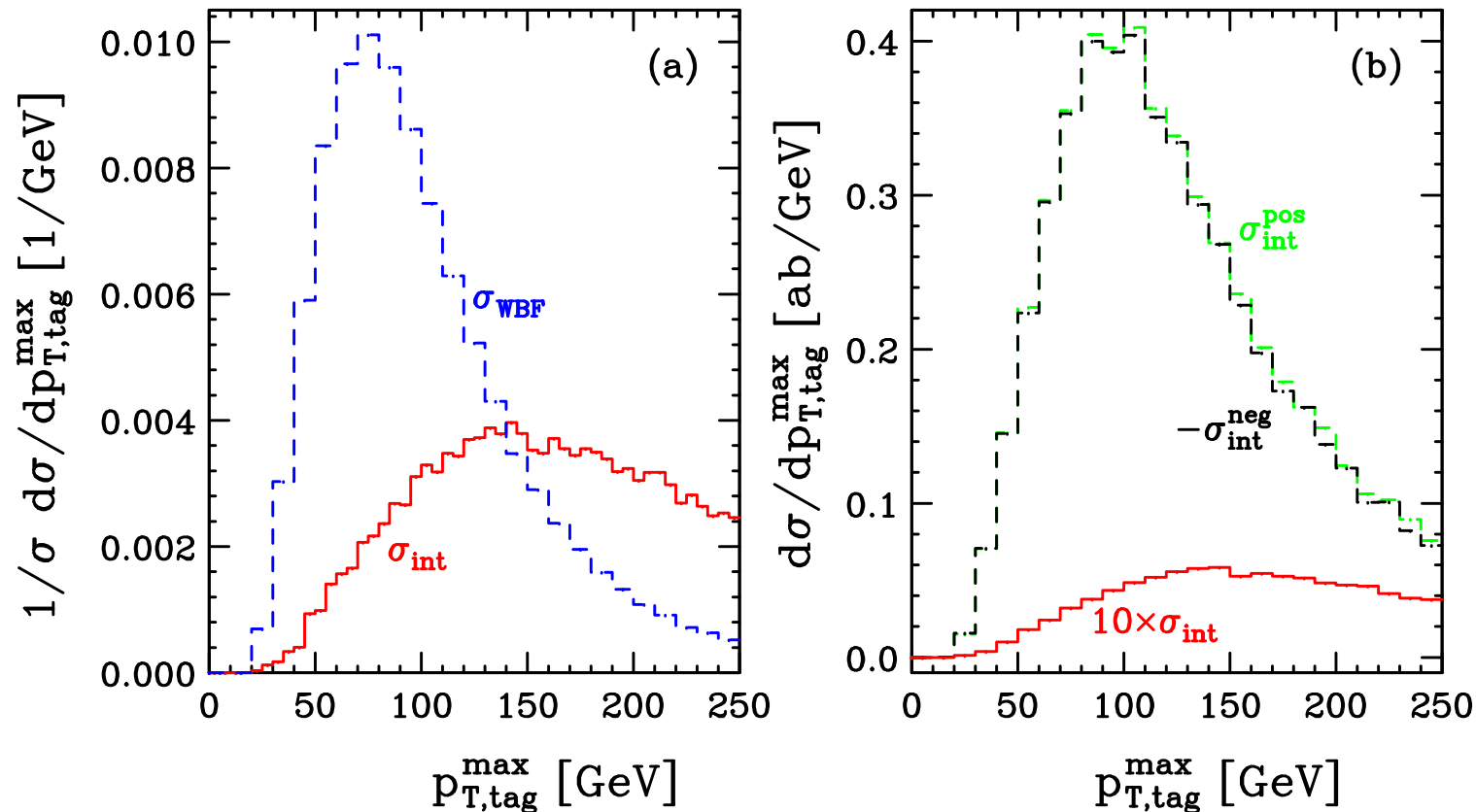
$$(b) \mu_f = \xi_f p_{Tj}, \alpha_s^3(\mu_r) = \alpha_s(\xi_r p_{T1}) \cdot \alpha_s(\xi_r p_{T2}) \cdot \alpha_s(\xi_r m_H)$$

# ... numbers ...

explicit calculation reveals **strong cancelation effects**  
in the total interference cross section

initial state	interaction	isospin	$\sigma_{\text{int}}^{\text{cuts}}$ [ab]	$\sigma_{\text{VBF}}^{\text{cuts}}$ [fb]
$qq$	NC	+ + or - -	51.4	72.3
	NC	+ - or - +	-49.8	70.8
	CC	+ - or - +	-	405.7
$q\bar{q}$	NC	+ - or - +	-3.1	39.3
	NC	+ + or - -	2.2	43.0
	CC	+ + or - -	-	230.7
$\bar{q}\bar{q}$	NC	- - or + +	4.0	5.1
	NC	- + or + -	-3.2	4.3
	CC	- + or + -	-	25.7
sum	NC+CC	all	1.5	896.9

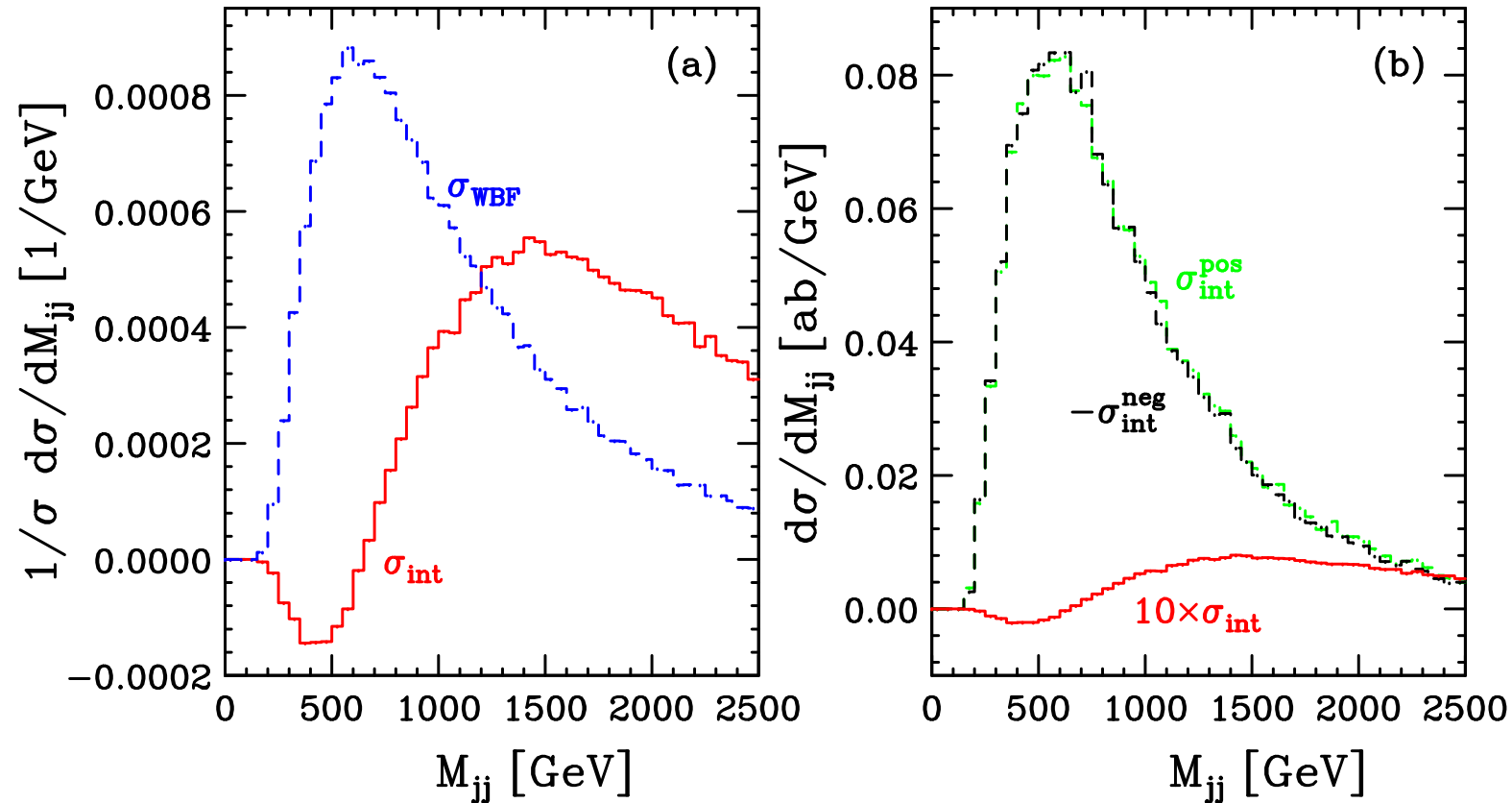
# distributions: $p_T$ of tagging jet



cancelations lead to **unexpected shapes** of distributions

but:  $\sigma_{\text{int}}$  tiny  $\rightarrow$  no effect on VBF signal

# distributions: dijet invariant mass



reminder: pure GF ... softer  $M_{jj}$  distribution than pure VBF!

# distributions: rapidity separation

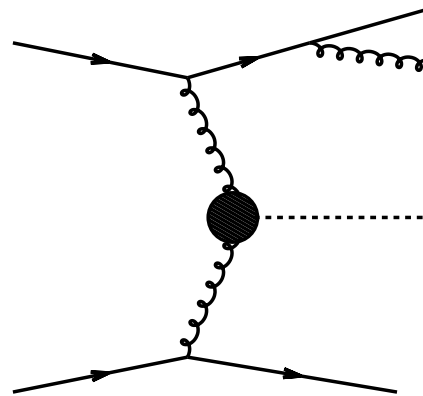
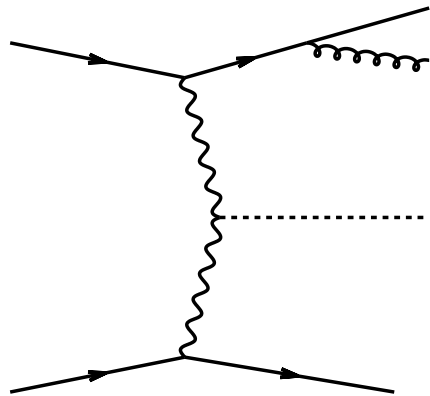
---

what about rapidity distribution of  
third, non-tagged jet in  $Hjjj$  events?

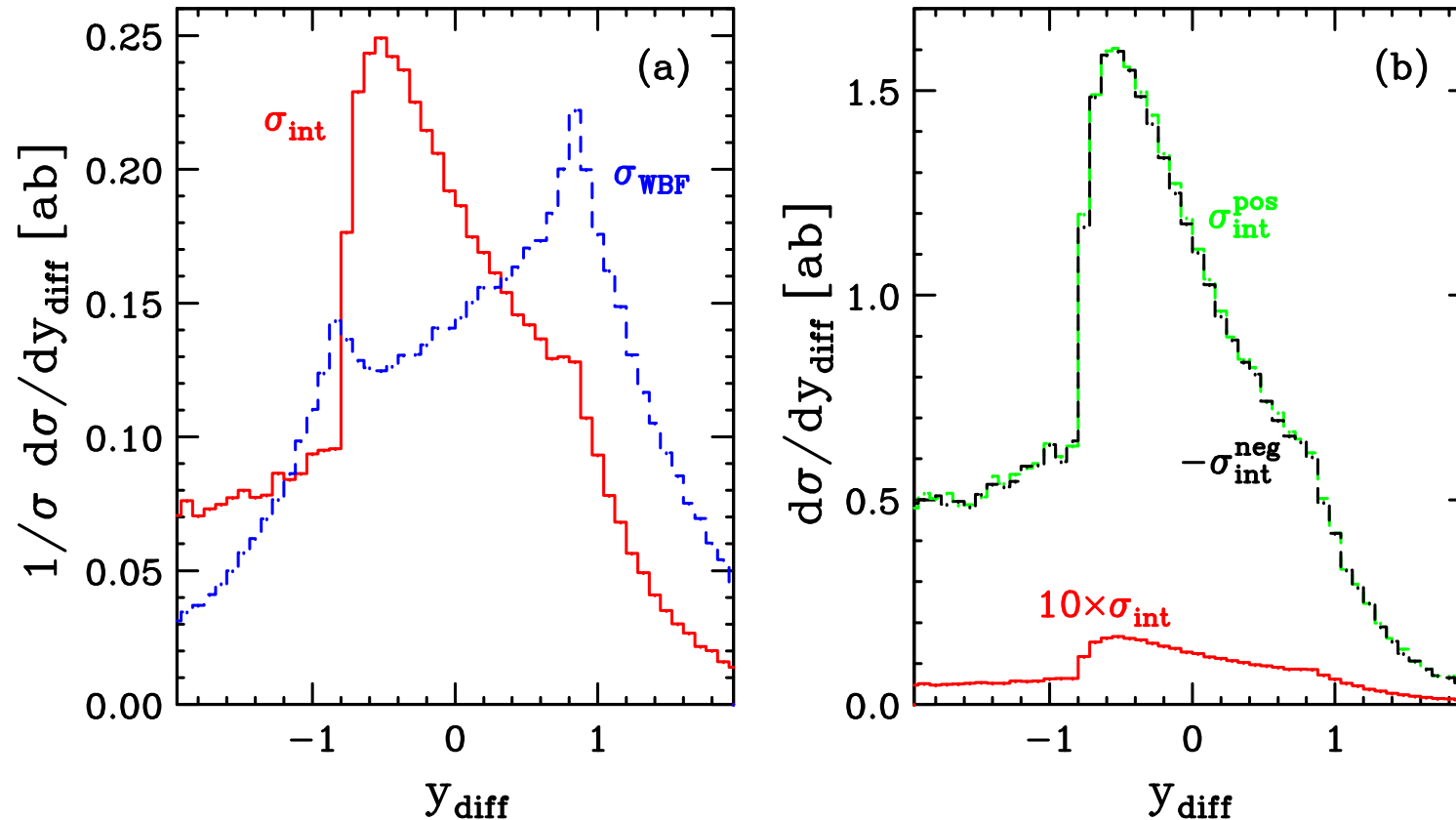


consider separation of third jet from positive-rapidity jet:

$$y_{\text{diff}} = y_3 - \max(y_1, y_2)$$

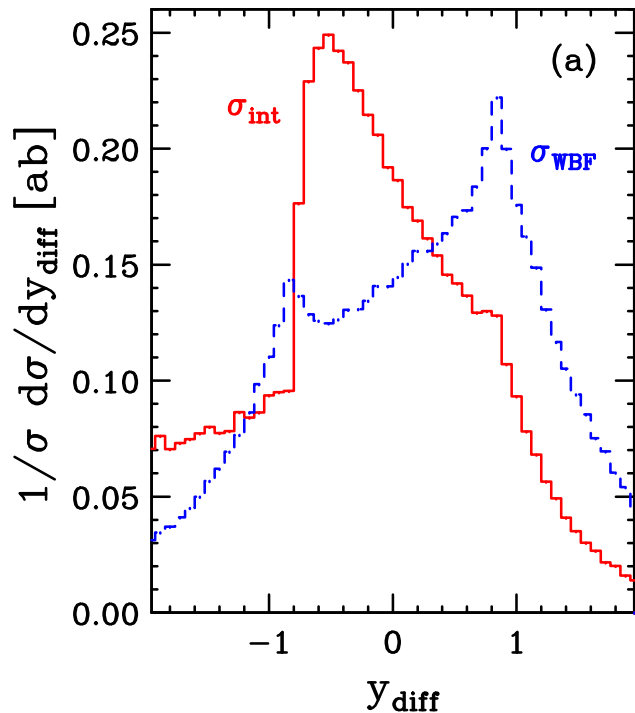


# distributions: rapidity separation



cancelations do not affect shape of  $y_{\text{diff}} = y_3 - \max(y_1, y_2)$   
as strongly as  $M_{jj}$  and  $p_{Tj}$  distributions

# distributions: rapidity separation



◆  $|\text{VBF}|^2$  and  $\text{VBF} \times \text{GF}$  peak at small values of  $|y_{\text{diff}}| \lesssim 1$

▢ soft jet close to considered hard jet

◆  $|\text{VBF}|^2$ :  $y_{\text{soft}} > y_{\text{hard}}$

▢ soft jet located “outside” tag jets

◆  $\text{VBF} \times \text{GF}$ :  $y_{\text{soft}} < y_{\text{hard}}$

▢ soft jet located between tag jets

☞ rapidity gap for color singlet weak boson exchange can be filled by QCD-EW interference contribution

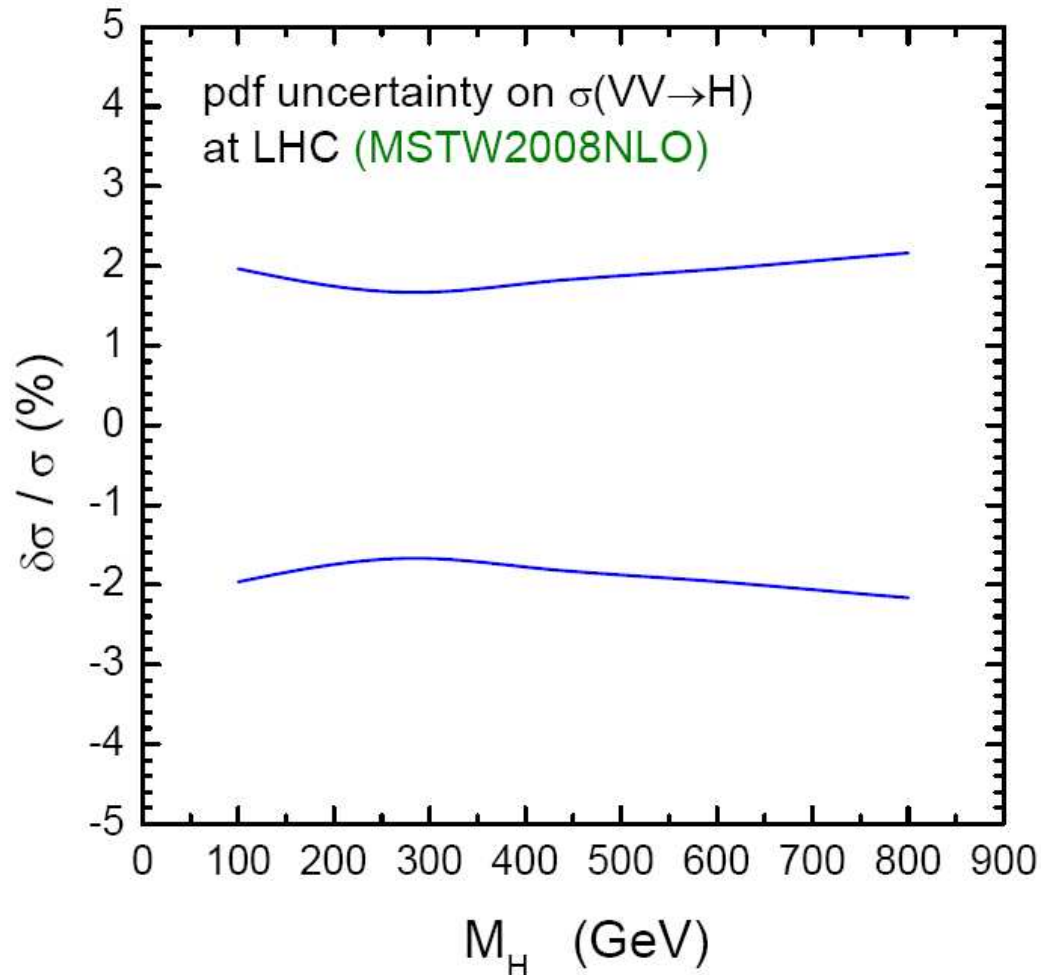


# wrap up: interference contributions

---

- ❖  $GF \times$  VBF loop-interference contributions for  $Hjj$  production at the LHC exhibit interesting **features different from VBF** (unexpected shapes of distributions due to cancellation effects)
  - ❖ but: **numerical effects** on the signal are **tiny**
  - ❖ predicting size and shape of higher order corrections by plausibility considerations can be dangerous
  - ❖ confirming the small impact of higher order contributions and interference effects by explicit calculations strengthens VBF as a promising Higgs boson search channel at the LHC

# PDF uncertainties in VBF



CTEQ:

difference between sets

$$\sigma_{6.1} / \sigma_{6.6} \lesssim 4\%$$

PDF uncertainty

$$\Delta_{\text{PDF}} \lesssim 3.5\%$$

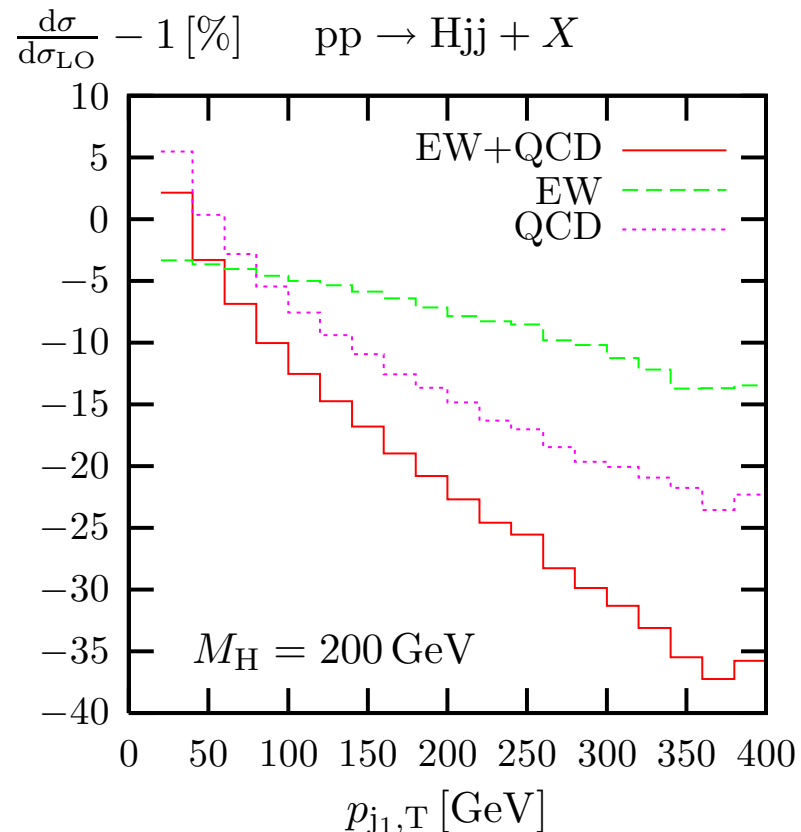
for  $100 \text{ GeV} \leq M_H \leq 800 \text{ GeV}$

# Higgs production in VBF @ NLO EW

*Ciccolini, Denner, Dittmaier (2007):*

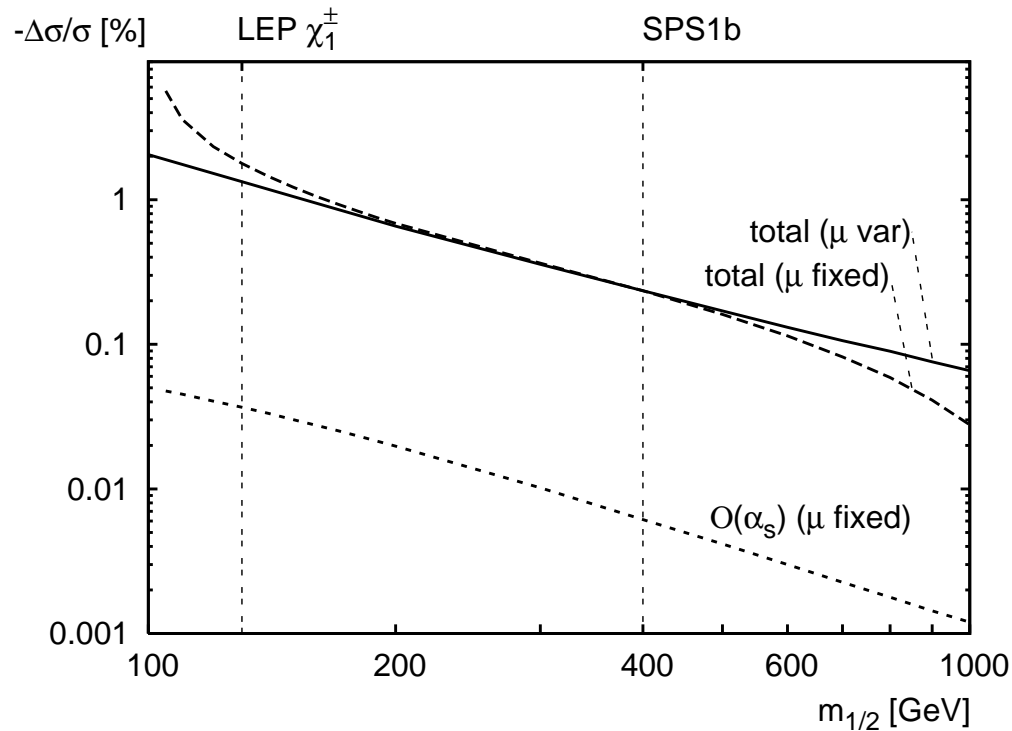
NLO EW corrections to inclusive cross sections and distributions

- ➔ **NLO EW corrections non-negligible**, modify  $K$  factors and distort distributions by up to 10%



publicly available  
parton-level Monte Carlo:  
HAWK  
*[Denner, Dittmaier, Mück]*

# SUSY QCD+EW corrections to VBF



*Hollik, Plehn, Rauch, Rzehak (2008):*

**SUSY QCD & EW corrections  $\lesssim 1\%$**   
for inclusive cross sections

in typical regions of the MSSM parameter space

# review perturbative corrections

---

- ❖ **NLO QCD and EW corrections:**
  - modify  $K$  factors and distort distributions by up to 10%
- ❖ **interference** with  $Hjj$  production via gluon fusion: negligible
- ❖ **SUSY corrections:**  $\lesssim 1\%$  for representative parameter points
- ❖ gluon-induced virtual **NNLO-QCD corrections** (one-loop squared):
  - numerically irrelevant in all considered regions
- ❖ DIS-type **NNLO-QCD corrections** (structure function approach):
  - further reduce scale uncertainties of total cross sections;
  - effects on differential distributions non-negligible

# Higgs production in VBF: more corrections

- ❖ **NLO QCD and EW corrections:**
  - modify  $K$  factors and distort distributions by up to 10%
- ❖ **interference** with  $Hjj$  production via gluon fusion: negligible
- ❖ **SUSY corrections:**  $\lesssim 1\%$  for representative parameter points
- ❖ **gluon-induced virtual NNLO-QCD corrections** (one-loop squared):
  - numerically irrelevant in all considered regions
- ❖ **DIS-type NNLO-QCD corrections** (structure function approach):
  - further reduce scale uncertainties of total cross sections;
  - effects on differential distributions non-negligible

**PERTURBATIVE CORRECTIONS ARE SMALL**

but:

establishing a signal requires also  
sufficient knowledge of ...

**...background contributions**



# VBF: signal & backgrounds

---

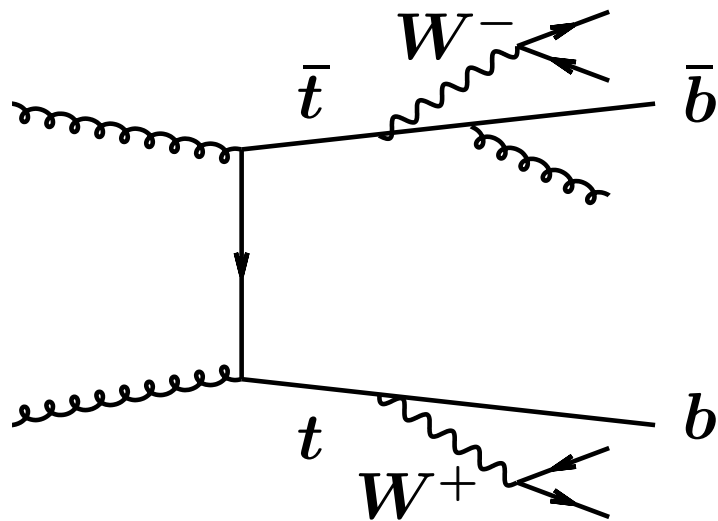
distinct event topology of the Higgs signal in

$$pp \rightarrow Hjj \text{ via VBF with}$$
$$H \rightarrow W^+W^- \rightarrow e^\pm \mu^\mp \cancel{p}_T$$

→ important for **suppression of backgrounds**

- ❖  $t\bar{t} + 0, 1, 2$  jets production  
(note:  $t\bar{t} \rightarrow W^+W^-b\bar{b}$ )
- ❖  $pp \rightarrow Hjj$  via gluon fusion  
(followed by  $H \rightarrow W^+W^-$ )
- ❖ QCD  $W^+W^-jj$  production
- ❖ EW  $W^+W^-jj$  production

# $t\bar{t}$ + jets backgrounds



- ❖ large top production cross section at the LHC
- ❖  $t \rightarrow Wb$  branching ratio  $\sim 100\%$
- ❖  $b$  quarks may be identified as tagging jets



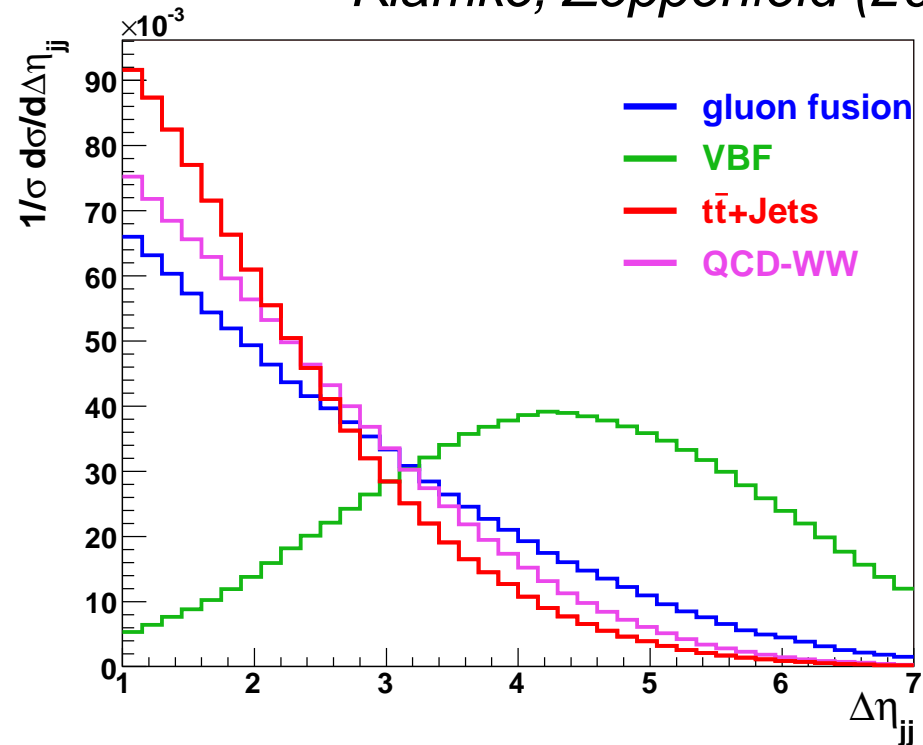
final-state configuration  
similar to Higgs signal in VBF

but distributions can be employed to suppress top backgrounds

# tagging jets: properties

rapidity separation of the tagging jets

*Klämke, Zeppenfeld (2007)*



**jets more central** in QCD- than in EW-induced production processes

# angular distribution of charged leptons

in  $H \rightarrow W^+W^-$ : spins anti-correlated



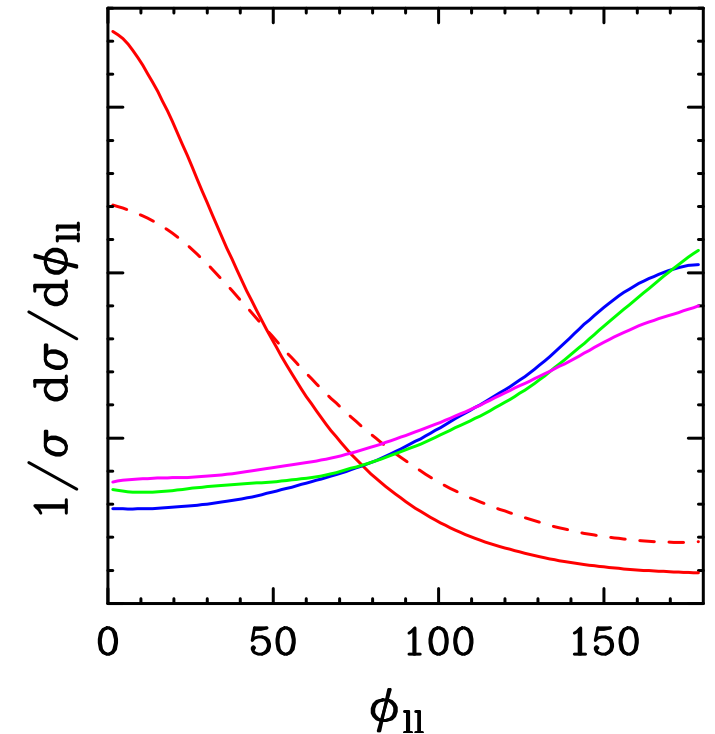
leptons emitted preferentially in same direction

no such correlation, if  $W$  bosons do not stem from the Higgs

*Dittmar, Dreiner (1996)*

distribution for EW  $W^+W^-$  production significantly different from Higgs signal

*Rainwater, Zeppenfeld (1999)*



- EW  $W^+W^-jj$
- QCD  $W^+W^-jj$
- $Hjj$  via VBF,  $H \rightarrow WW$
- $t\bar{t} + \text{jets}$

# VBF signal / background analysis

☞ selection of signal and background rates

for  $M_H = 160$  GeV (in [fb])

in the  $H \rightarrow e^+ \mu^- p_T$  decay mode at the LHC :

cuts	$Hjj$	$t\bar{t}+\text{jets}$	QCD $WWjj$	EW $WWjj$	...	S / B
forward tagging	17.1	1080	4.4	3.0	...	1/65
+ $b$ veto		64			...	1/5.1
+angular cuts	11.4	5.1	0.50	0.45	...	1.7/1
+central jet veto	10.1	1.48	0.15	0.34	...	4.6/1
all cuts	7.5	1.09	0.11	0.25	...	4.6/1

*Rainwater, Zeppenfeld (1999)*

# central jet veto

central jet veto (CJV):

remove events with extra jet(s) in central-rapidity region

$$p_T^{\text{veto}} > 20 \text{ GeV}, \eta_{\text{jet}}^{\text{min}} < \eta_{\text{jet}}^{\text{veto}} < \eta_{\text{jet}}^{\text{max}}$$

cuts	$Hjj$	$t\bar{t}+\text{jets}$	QCD $WWjj$	EW $WWjj$	...	S / B
forward tagging	17.1	1080	4.4	3.0	...	1/65
+ $b$ veto		64			...	1/5.1
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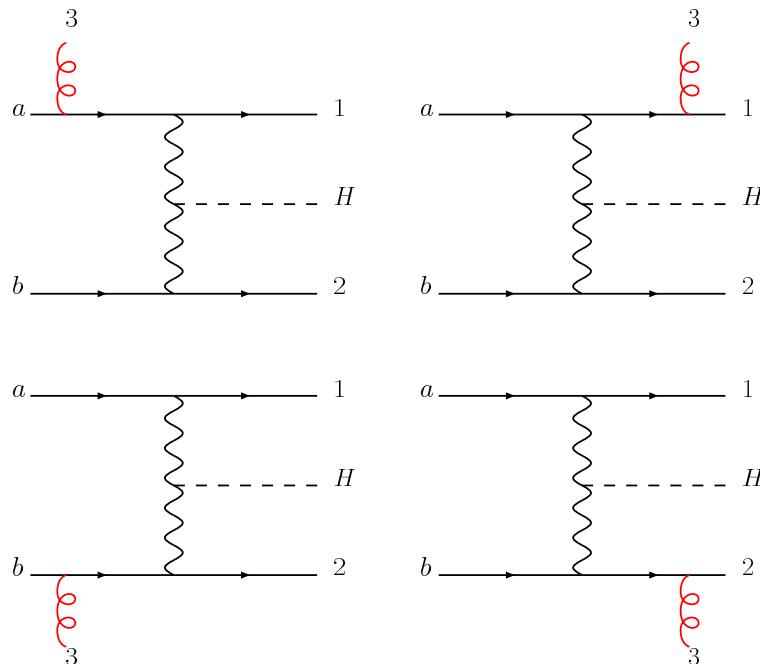
☞ precise knowledge of extra jet activity essential,  
requiring

❖  $pp \rightarrow Hjj$  interfaced to parton shower programs

❖  $pp \rightarrow Hjjj$  at NLO-QCD accuracy

# $pp \rightarrow Hjjj$ via VBF

$$\mathcal{M}_B(Hjjj) \leftrightarrow \mathcal{M}_R(Hjjj)$$



*Figy, Hankele, Zeppenfeld (2007):*

NLO-QCD in VBF approximation

(no color exchange between  
upper/lower quark lines,  
no  $VH$ -type contributions)

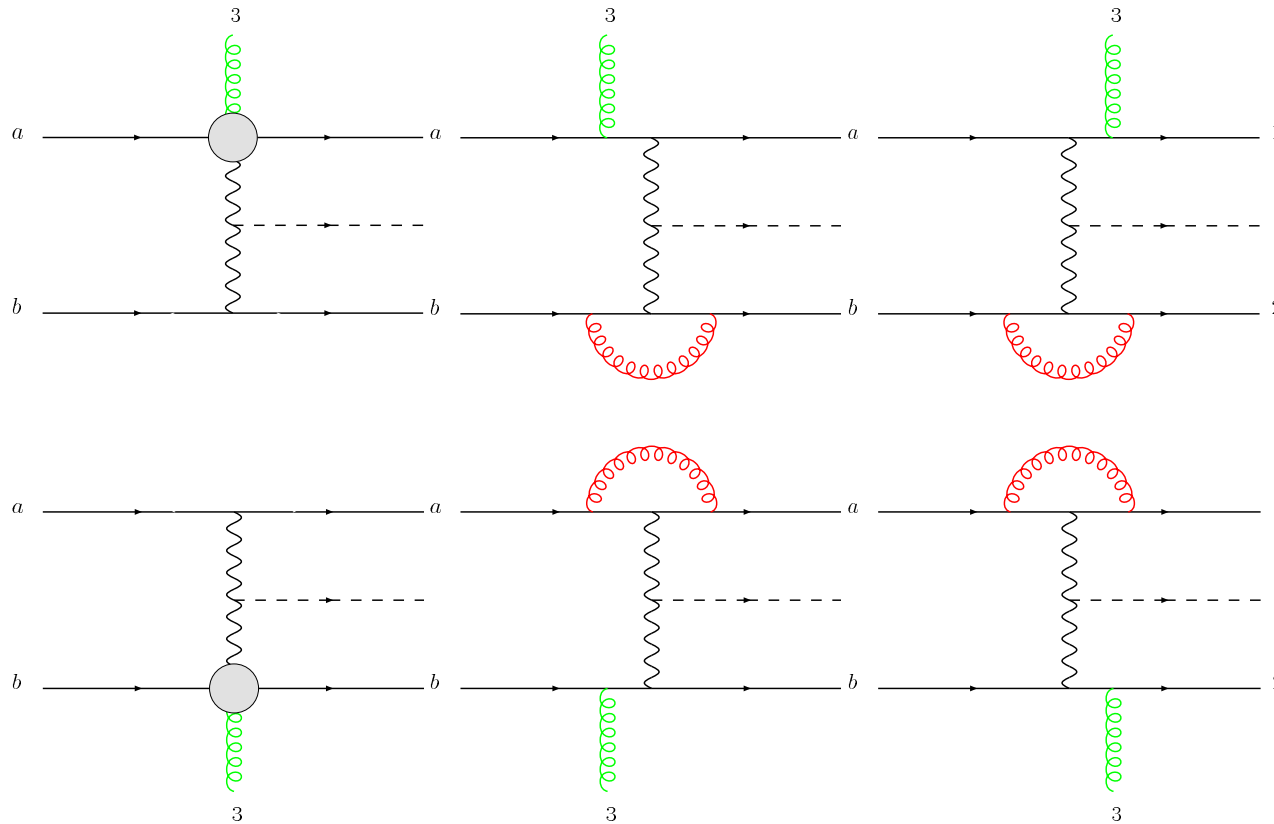
*Campanario, Figy, Plätzer, Sjö Dahl (2013):*

full NLO-QCD calculation

(good agreement with  
approximative calculation)

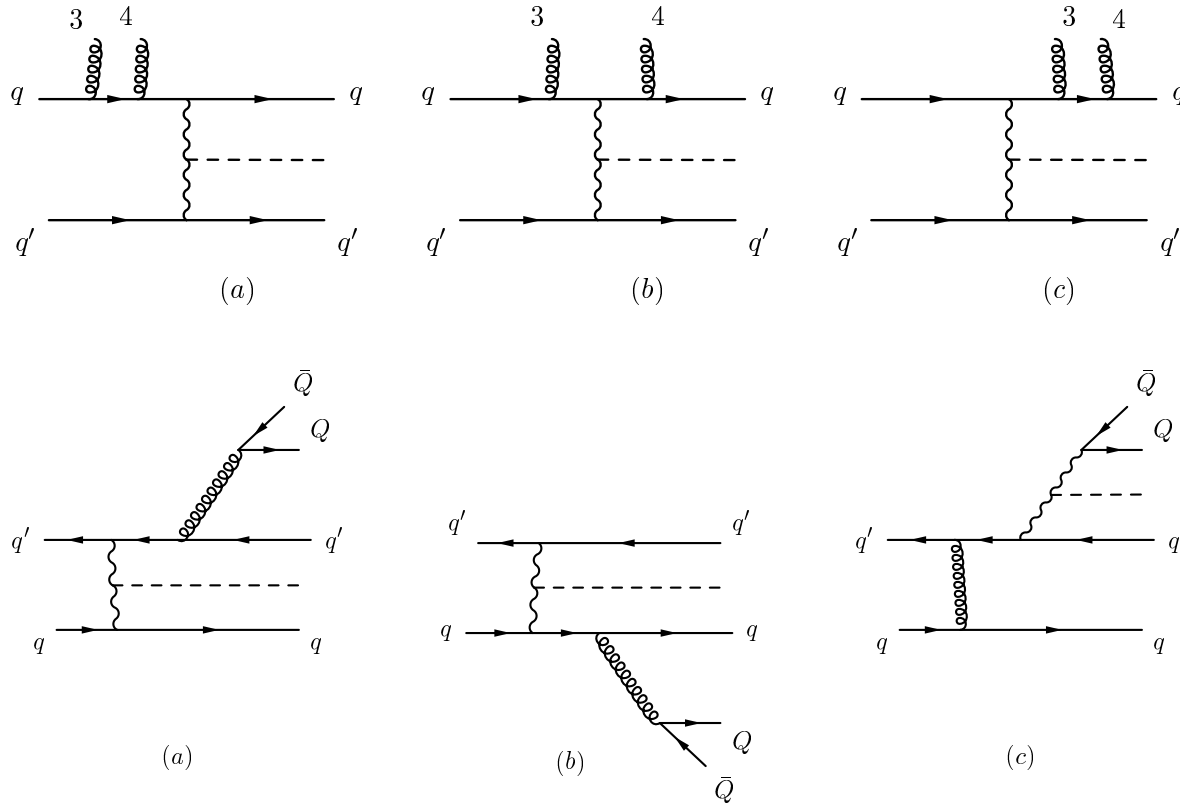


# $pp \rightarrow Hjjj$ via VBF @ NLO QCD



dominant virtual corrections require computation of  
triangle, box, and pentagon diagrams

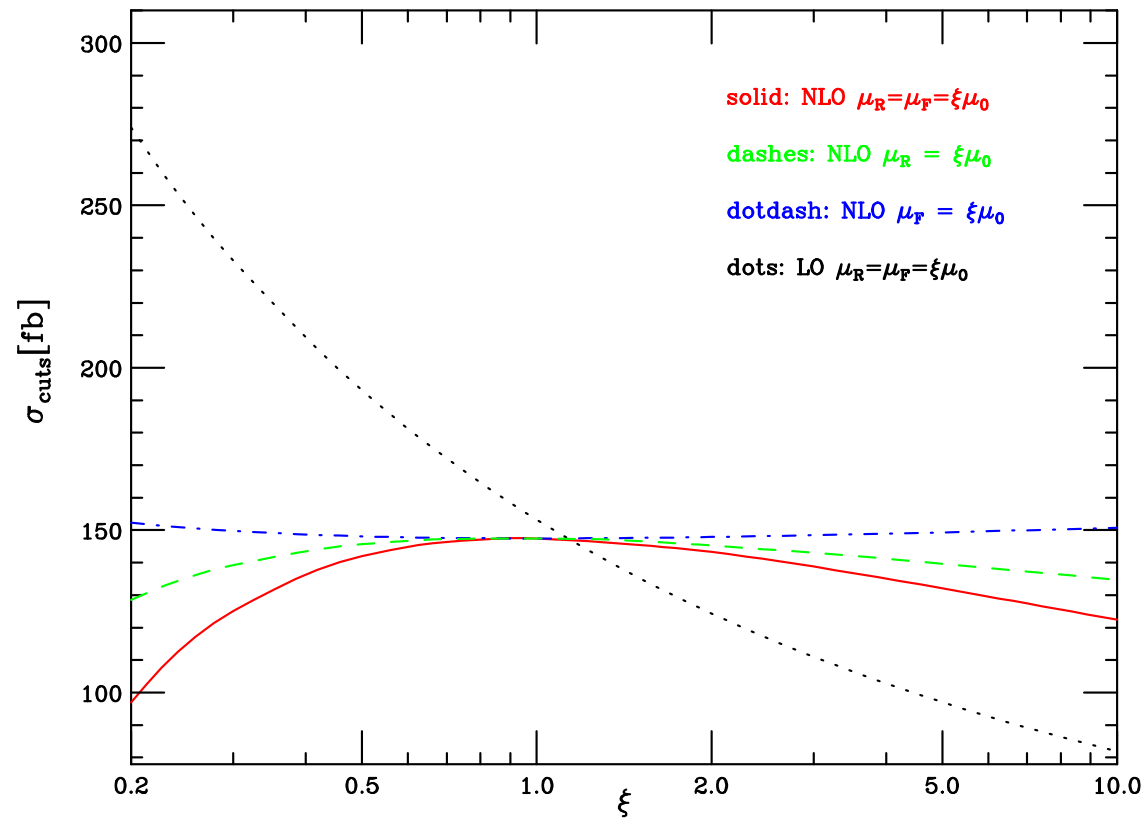
# $pp \rightarrow Hjjj$ via VBF @ NLO QCD



real emission contributions comprise processes with  
4 quarks+2 gluons and processes with 6 quarks

# $pp \rightarrow Hjjj$ via VBF @ NLO QCD

Figy, Hankele, Zeppenfeld (2007)



scale dependence moderate  
(comparable to other VBF processes)

# $pp \rightarrow Hjjj$ via VBF @ NLO QCD

central jet veto (CJV):

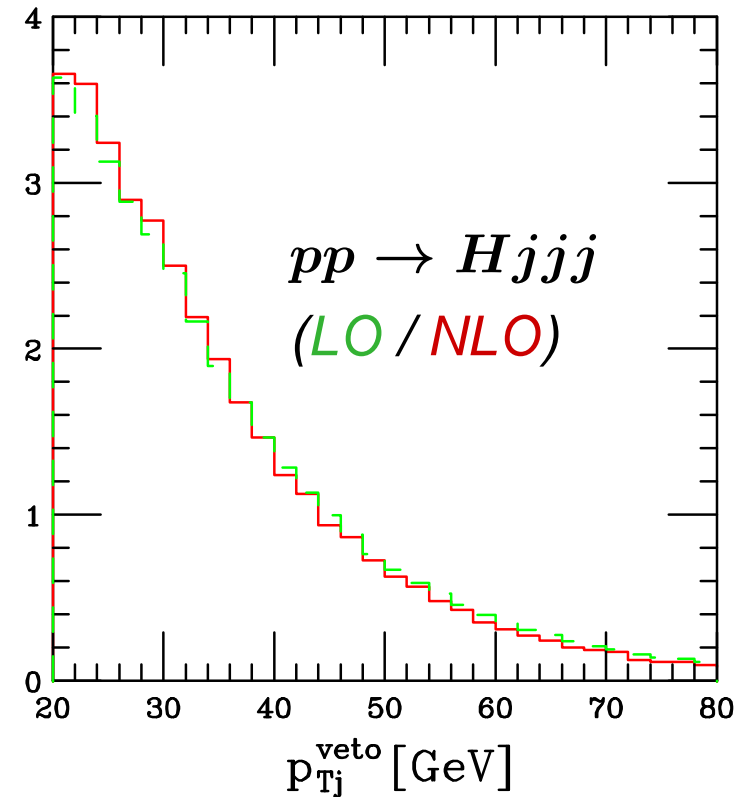
important tool for suppression  
of QCD backgrounds

remove events with extra jet(s)  
in central-rapidity region

$$p_T^{\text{veto}} > 20 \text{ GeV}, \eta_{\text{jet}}^{\text{min}} < \eta_{\text{jet}}^{\text{veto}} < \eta_{\text{jet}}^{\text{max}}$$

☞ need precise predictions for  
distributions of 3<sup>rd</sup> jet

Figy, Hankele, Zeppenfeld (2007)



❖ (dominant) NLO-QCD corrections modest

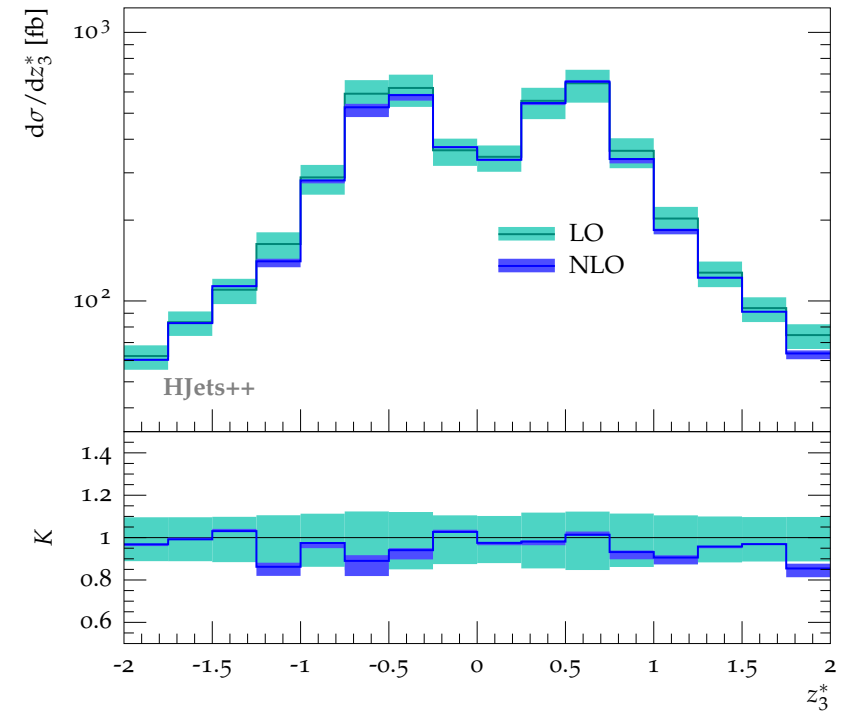
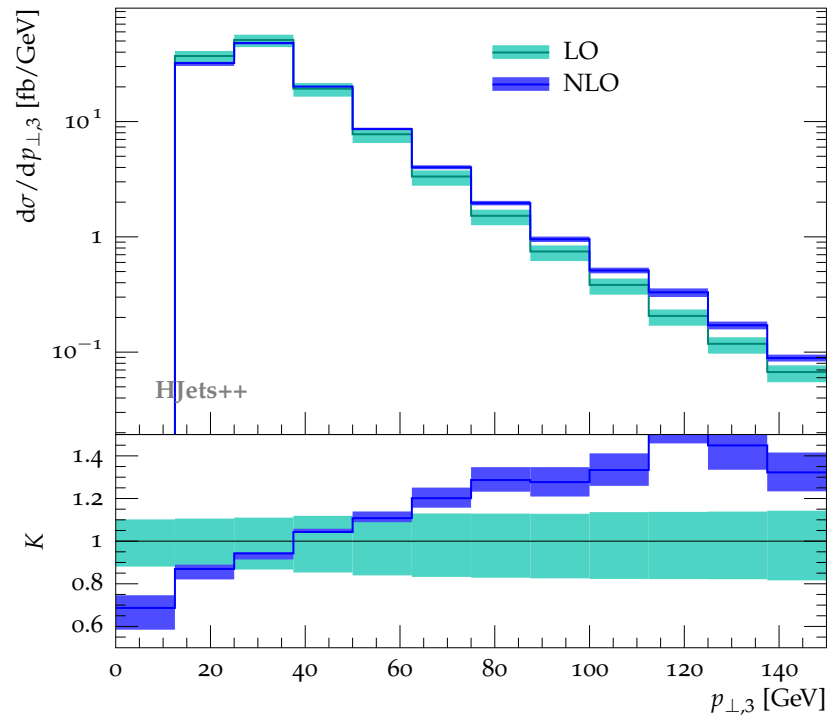
❖ scale uncertainties of CJV observables significantly reduced

# $pp \rightarrow Hjjj$ via VBF @ NLO QCD

Campanario et al. (2013)

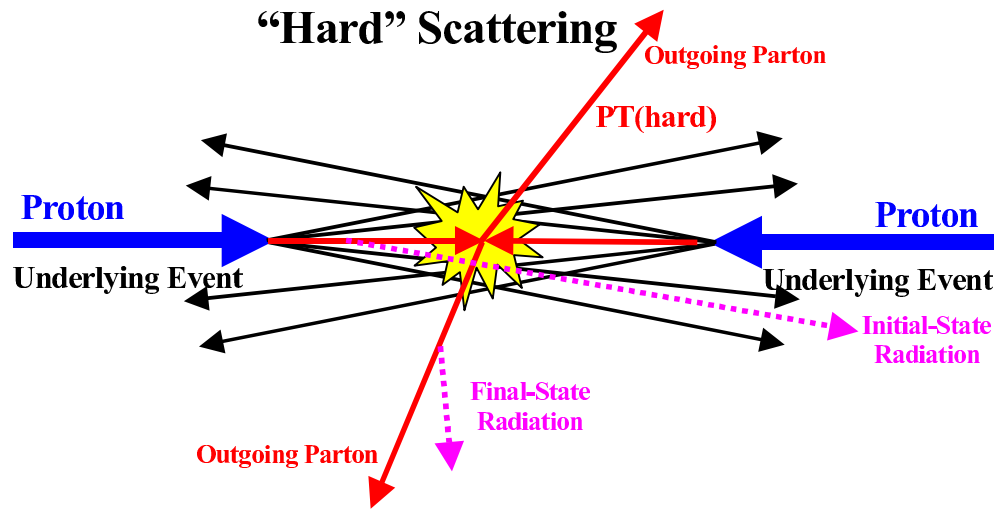
transverse momentum of 3<sup>rd</sup> jet

relative rapidity of 3<sup>rd</sup> jet



- ◆ (dominant) NLO-QCD corrections modest
- ◆ scale uncertainties of CJV observables significantly reduced

# more realistic simulation



for realistic description of scattering processes at hadron colliders:

- ❖ combine matrix elements for hard scattering with programs for simulation of underlying event, parton shower, and hadronization

(PYTHIA, HERWIG, SHERPA, ...)

# parton showers & NLO-QCD: the POWHEG method

---

POsitive Weight Hardest Emission Generator

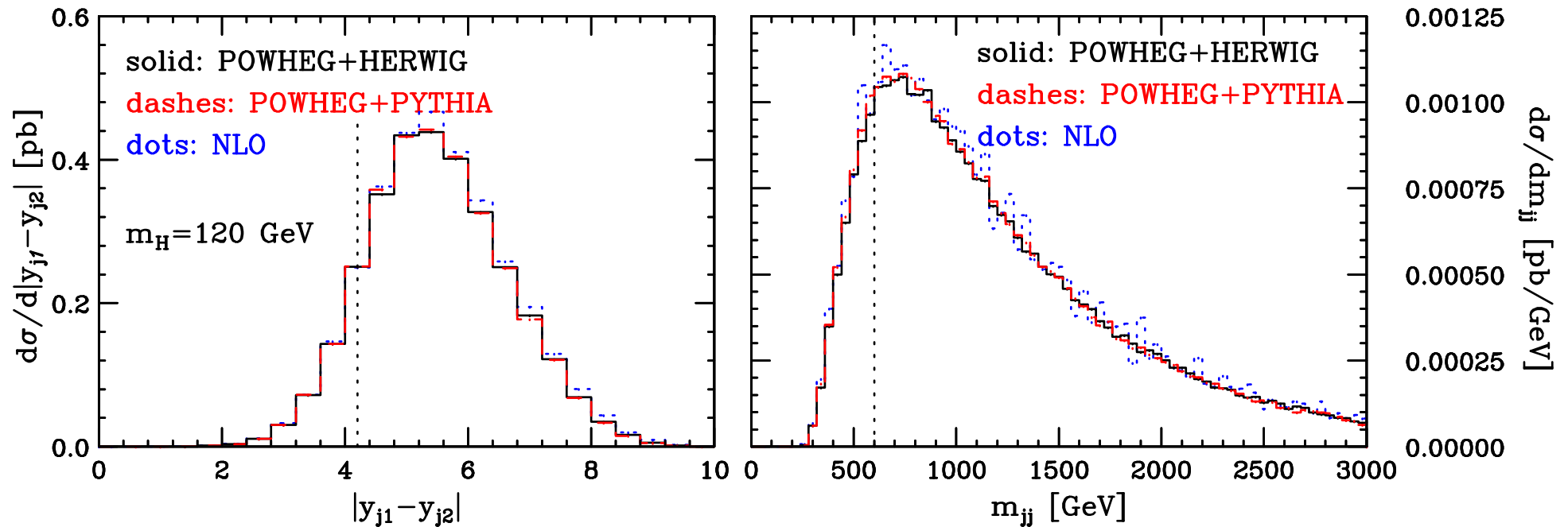
general prescription for **matching** parton-level **NLO-QCD** calculations with **parton shower programs**

*[Frixione, Nason, Oleari]*

- ❖ generate partonic event with single emission at NLO-QCD
- ❖ all subsequent radiation must be softer than the first one
- ❖ event is written on a file in standard Les Houches format
  - can be processed by default parton shower program (HERWIG, PYTHIA, ...)

# $pp \rightarrow Hjj$ via VBF and parton showers @ NLO

*Nason, Oleari (2009)*

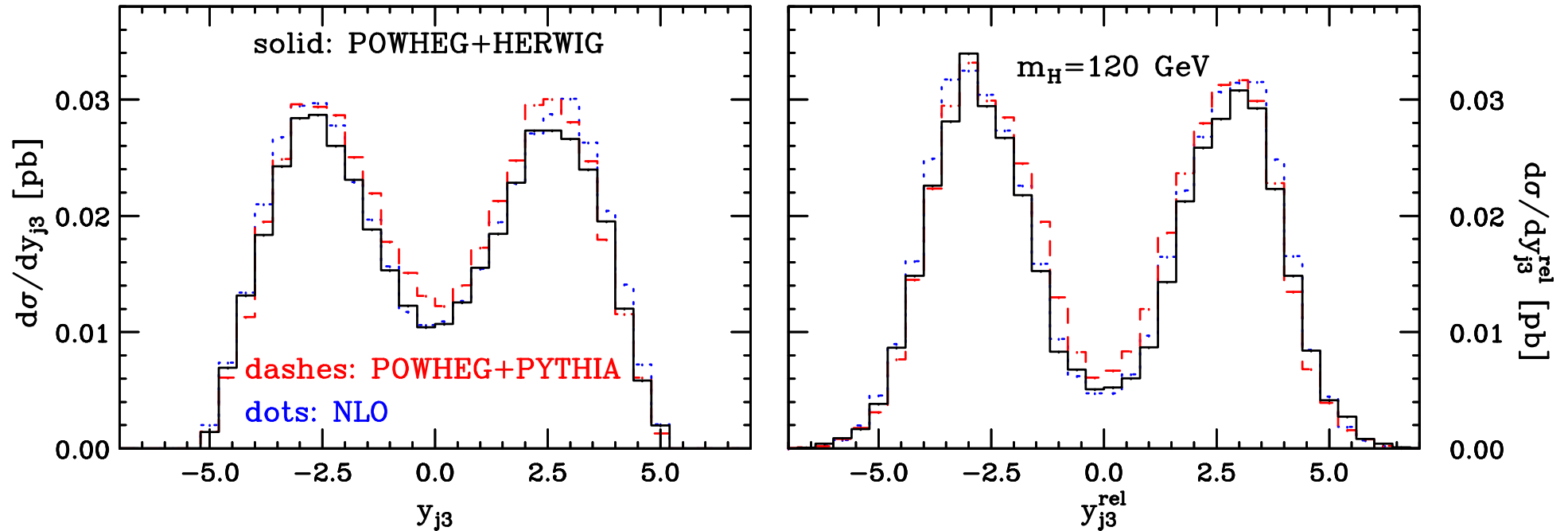


**good agreement** between parton-level NLO calculation and POWHEG matched with HERWIG or PYTHIA for many observables related to hard tagging jets



# $pp \rightarrow Hjj(j)$ via VBF and parton showers @ NLO

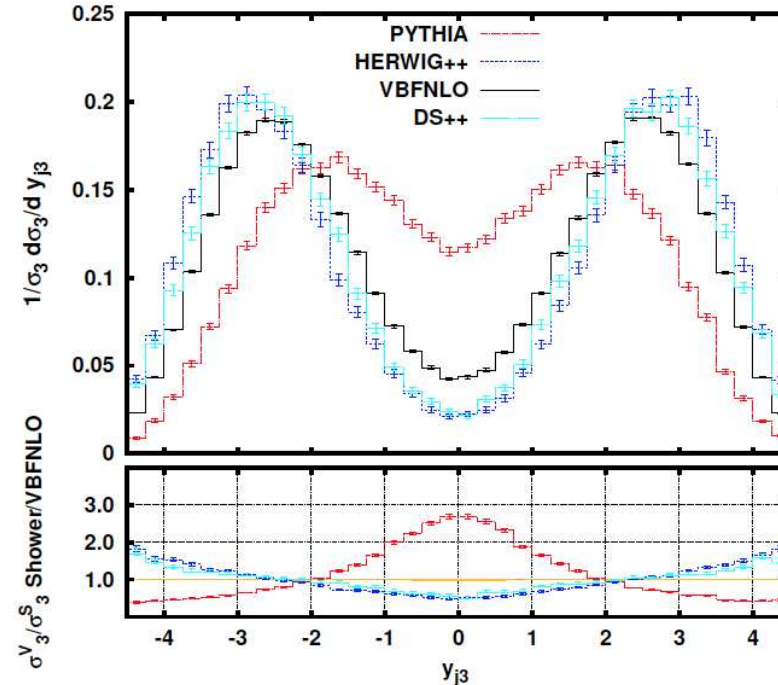
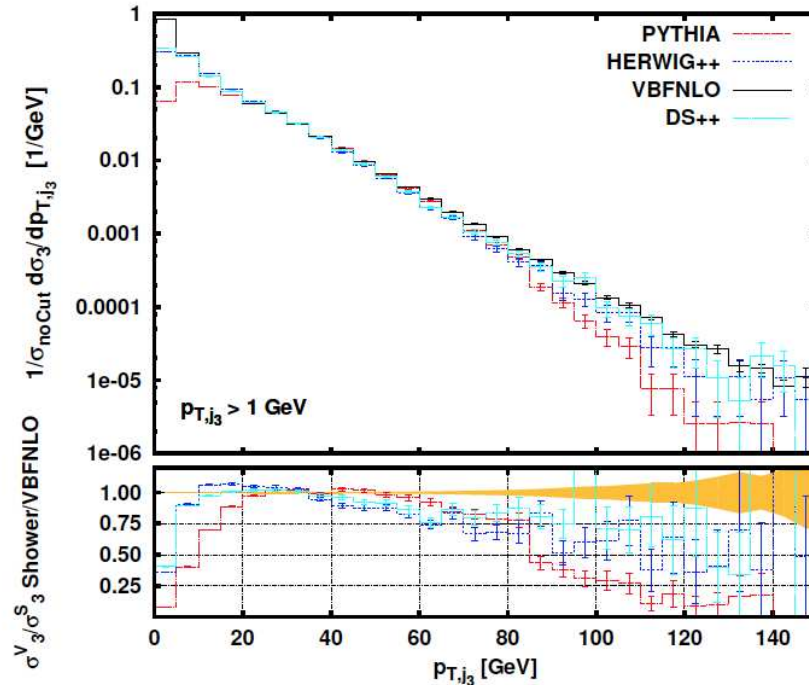
Nason, Oleari (2009)



VBF  $Hjj$  matrix elements at NLO combined with parton shower  
→ improvement w.r.t. LO simulation

# $pp \rightarrow Hjj(j)$ via VBF and parton shower @ LO

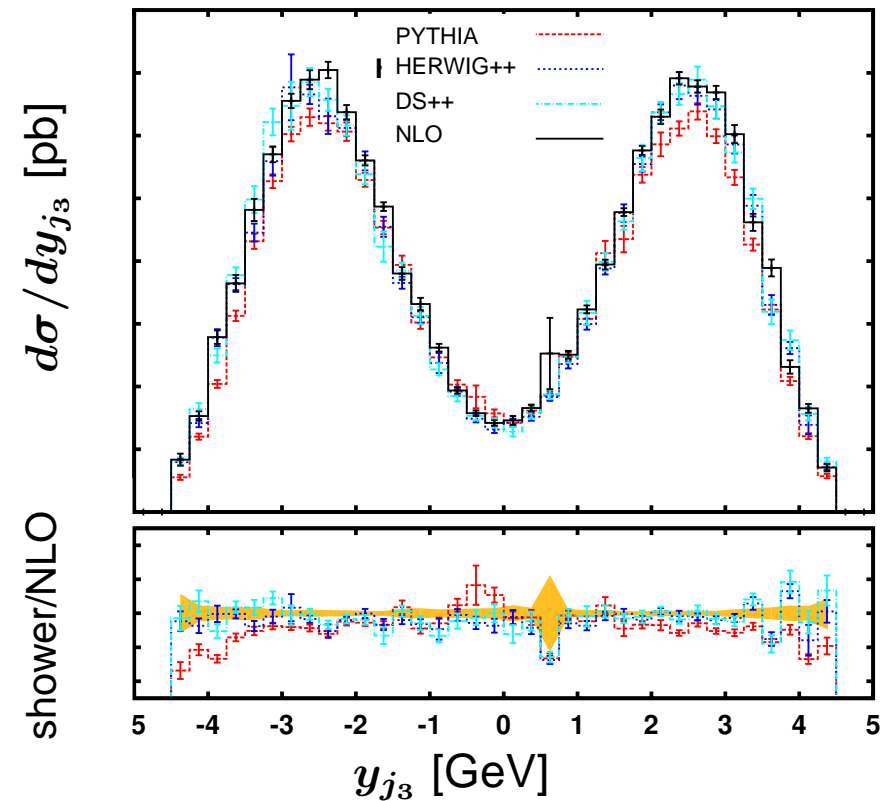
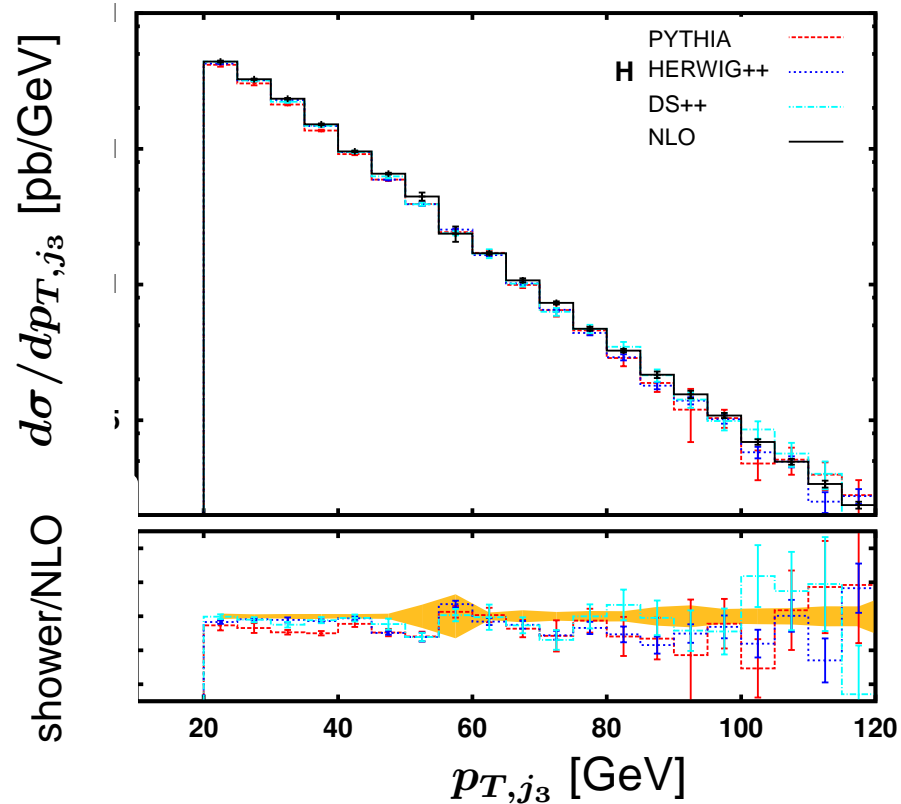
Schissler (2014)



VBF  $Hjj$  matrix elements at LO combined with parton shower  
→ large uncertainty on 3rd jet (problematic for CJV observables)

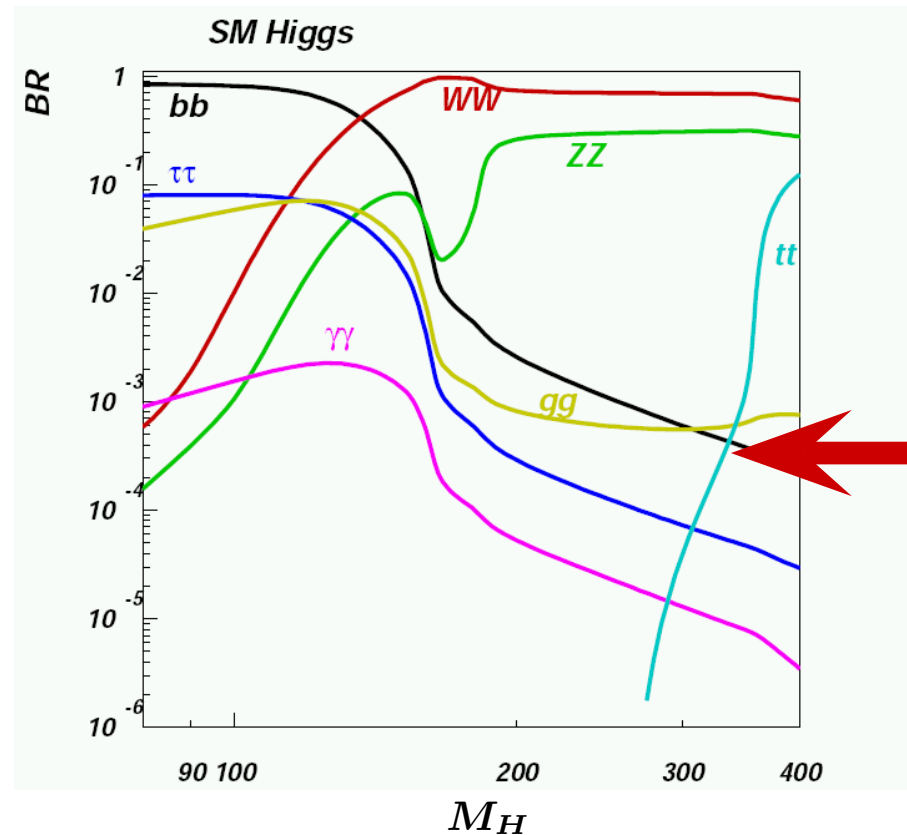
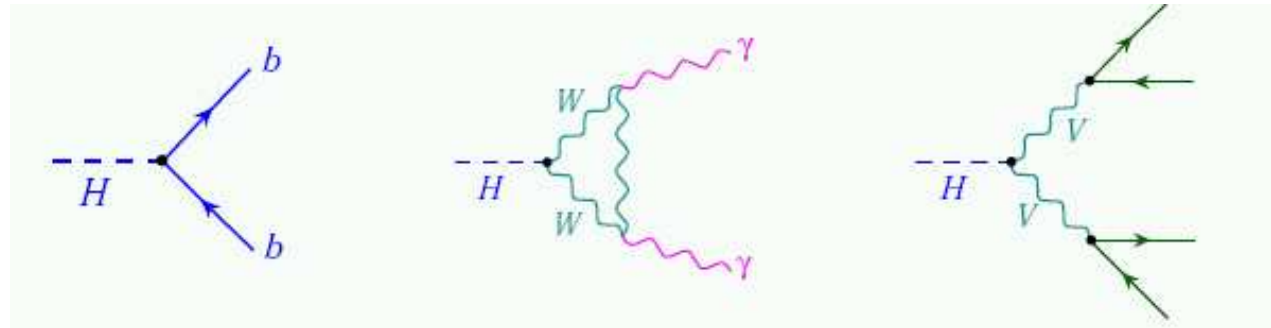
# $pp \rightarrow Hjjj$ via VBF and parton shower @ NLO QCD

Schissler, Zeppenfeld, B.J. (2014)



VBF  $Hjjj$  matrix elements at NLO combined with parton shower  
→ description of 3rd jet well under control

# Higgs decay



branching fractions

# determination of the $Hb\bar{b}$ coupling

---

$H \rightarrow b\bar{b}$  is dominant decay mode for  $m_H \lesssim 140$  GeV, but  
accessing the bottom-quark Yukawa coupling remains difficult

→ consider Higgs production at a future lepton-hadron collider

idea goes back to the 1980ies: *Hioki et al. (1983)*

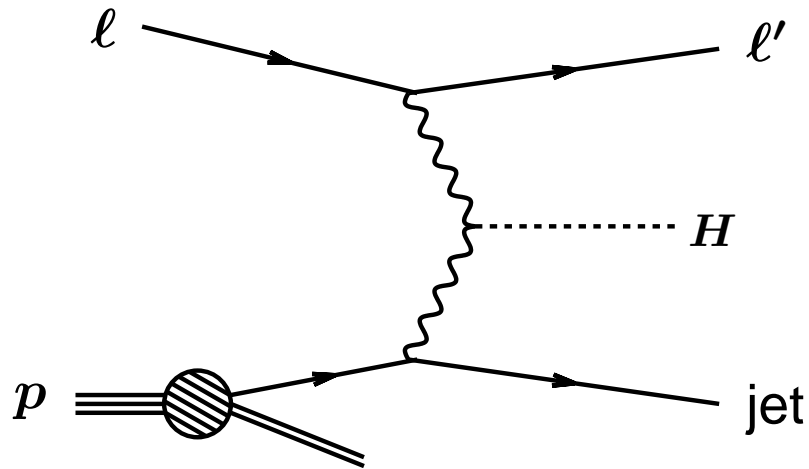
*Han et al. (1985), ...*

revived in the context of ep collider project at CERN:

**Large Hadron electron Collider (LHeC)**

LHC proton beam combined with electron beam

# Higgs production at the LHeC



sample scenario:

$$E_p = 7 \text{ TeV}$$

$$E_e = 140 \text{ GeV}$$

$$M_H = 120 \text{ GeV}$$

- ❖ production modes:  $ep \rightarrow ejH$  (NC) and  $ep \rightarrow \nu_e jH$  (CC)
- ❖ clean environment facilitates separation of signal from backgrounds
- ❖ extraction of **bottom Yukawa coupling** in  $H \rightarrow b\bar{b}$  decay mode feasible

[for details see, e.g., Han, Mellado (2009)]

# determination of the $Hb\bar{b}$ coupling

---

$H \rightarrow b\bar{b}$  is dominant decay mode for  $m_H \lesssim 140$  GeV, but accessing the bottom-quark Yukawa coupling remains difficult

→ consider **WBF  $H\gamma jj$**  production with  $H \rightarrow b\bar{b}$  decay:

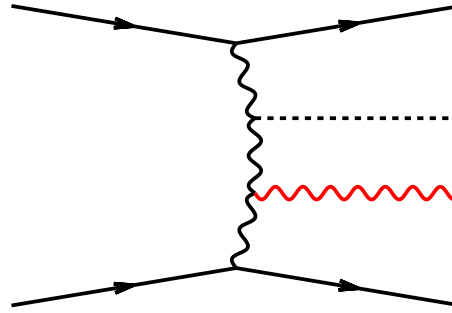
- detailed signal-background analysis:

*Gabrielli, Maltoni, Mele, Moretti, Piccinini, Pittau (2007)*

- NLO-QCD calculation of signal process:

*Arnold, Figy, B. J., Zeppenfeld (2010)*

# extra photon radiation in VBF: $pp \rightarrow H\gamma jj$



*Gabrielli et al. (2007):*

**extra hard, central photon** in  $pp \rightarrow Hjj$

powerful tool for suppression of  
(gluon-dominated) QCD backgrounds

➡ can the **WBF  $H \rightarrow b\bar{b}$  mode** be tackled that way?



# extra photon radiation in VBF: $pp \rightarrow H\gamma jj$

effects of hard central photon requirement:

✗ “naive expectation”: signal  $S$  and background  $B$   
suppressed by same factor  $\sim \mathcal{O}(\alpha)$

- $S/B$  not much affected:

$$\left(\frac{S}{B}\right)_{Hjj} \sim \left(\frac{S}{B}\right)_{H\gamma jj}$$

- signal significance decreases:

$$\left(\frac{S}{\sqrt{B}}\right)_{H\gamma jj} \sim \sqrt{\alpha} \left(\frac{S}{\sqrt{B}}\right)_{Hjj} \lesssim 1/10 \left(\frac{S}{\sqrt{B}}\right)_{Hjj}$$

👉 no advantage?

# extra photon radiation in VBF: $pp \rightarrow H\gamma jj$

---

effects of hard central photon requirement:

✗ “naive expectation”: signal  $S$  and background  $B$   
suppressed by same factor  $\sim \mathcal{O}(\alpha)$

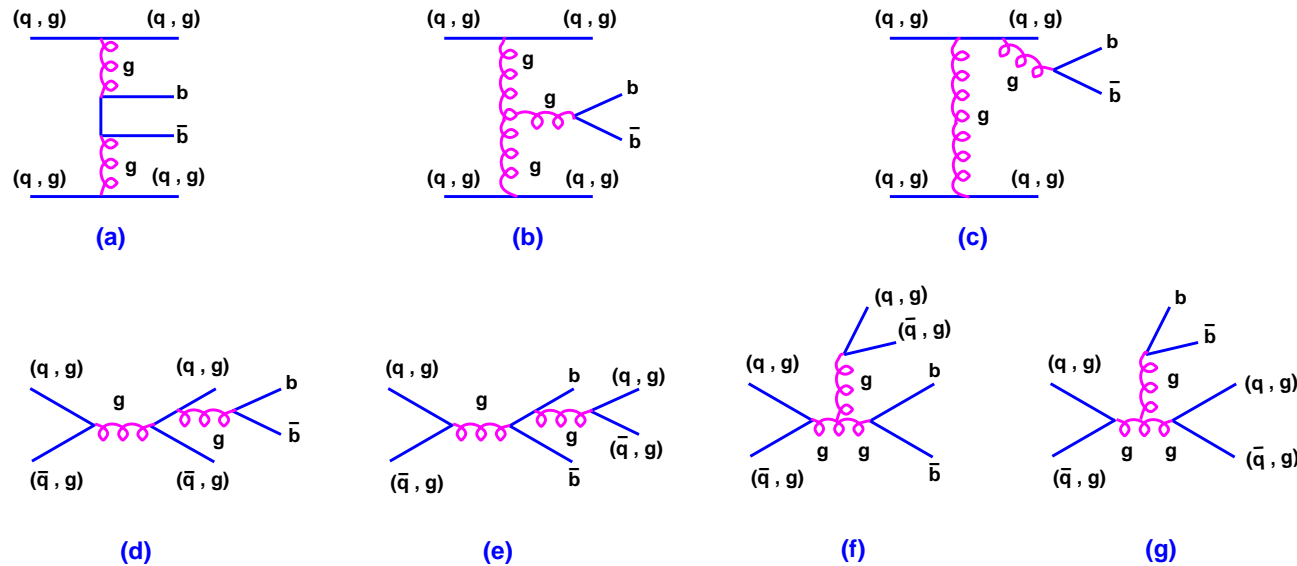
- $S/B$  not much affected
- signal significance decreases

☞ no advantage?

✓ decrease in rate for QCD multi-jet final states

☞ improvement on trigger efficiencies for  $b\bar{b}jj$  events

# extra photon radiation in VBF: $pp \rightarrow H\gamma jj$



- ✓ large gluonic component in  $b\bar{b}jj$  background ( $\sim 80\%$  of  $\sigma_{bbjj}$ )
  - QCD backgrounds less active in radiating photon than quark-dominated WBF signal
- ✓ WBF-specific selection cuts favor large values of  $x$ 
  - valence-quarks more relevant than gluons in initial state

# extra photon radiation in VBF: $pp \rightarrow H\gamma jj$

---

effects of hard central photon requirement:

- ✓ **destructive interference** between photon emission off initial-state and off final-state quarks that are linked by neutral  $t$ -channel-exchange boson
  - ☞ central photon emission in backgrounds further suppressed
- ✓ similar interference effects in WBF signal
  - suppress  $ZZ$  fusion, but **enhance  $WW$  fusion** contributions
    - ☞ relative contribution of  $ZZ$  fusion depleted w.r.t.  $WW$  fusion

# extra photon radiation in VBF: $pp \rightarrow H\gamma jj$

effects of hard central photon requirement:

✗ “naive expectation”: signal and background  
suppressed by same factor  $\sim \mathcal{O}(\alpha)$

✓ de facto: reduction factors different for  $S$  and  $B$

backgrounds:  $\sigma_\gamma/\sigma \sim 1/3000$

signal:  $\sigma_\gamma/\sigma \sim 1/100$

✓  $\left(S/\sqrt{B}\right)_{H\gamma jj} \lesssim 3$  for  $m_H = 120$  GeV,  $\mathcal{L} = 100$  fb $^{-1}$   
and optimized selection cuts

[Gabrielli et al. (2007)]

# photon isolation

---

problem: collinear photon-fermion configurations are singular

cure:

a) compute parton-to-photon fragmentation contributions;  
absorb singularities in non-perturbative functions

✓ theoretically well-defined

✗ introduces poorly known photon fragmentation functions

b) naive photon-jet separation criterion  $R_{j\gamma} \geq R_{min}$

✓ easy to implement

✗ theoretically ill-defined:

soft-gluon contributions in cone are also removed and  
can't fully cancel IR singularities of virtual contributions

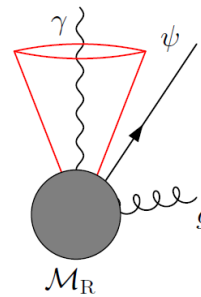
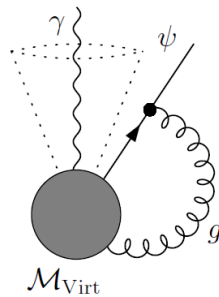
# photon isolation

our implementation: cone-isolation criterion of *Frixione (1998)*

idea: veto collinear photon-jet configurations, but  
allow soft QCD emission

in practice: limit hadronic energy deposited in a cone  
around the direction of the photon by

$$\sum_{i: R_{i\gamma} < R} p_{Ti} \leq \frac{1 - \cos R}{1 - \cos \delta_0} p_{T\gamma} \quad (\forall R \leq \delta_0 = 0.7)$$



# $pp \rightarrow H\gamma jj$ @ LHC: settings

apply  $k_T$  jet algorithm and use CTEQ6 parton distributions

inclusive cuts

$$p_{Ti} \geq 20 \text{ GeV},$$

$$|y_j| \leq 5, \quad |y_{\gamma,b}| \leq 2.5,$$

$$\Delta R_{ik} \geq 0.4,$$

$$M_{jj}^{\text{tag}} > 100 \text{ GeV}$$

$$y_j^{\min} < y_{\gamma}, y_b < y_j^{\max}$$

$$\Delta y_{jj} = |y_{j_1} - y_{j_2}| > 4,$$

$$\Delta R_{ik} \geq 0.7,$$

$$M_{jj}^{\text{tag}} > 600 \text{ GeV}$$

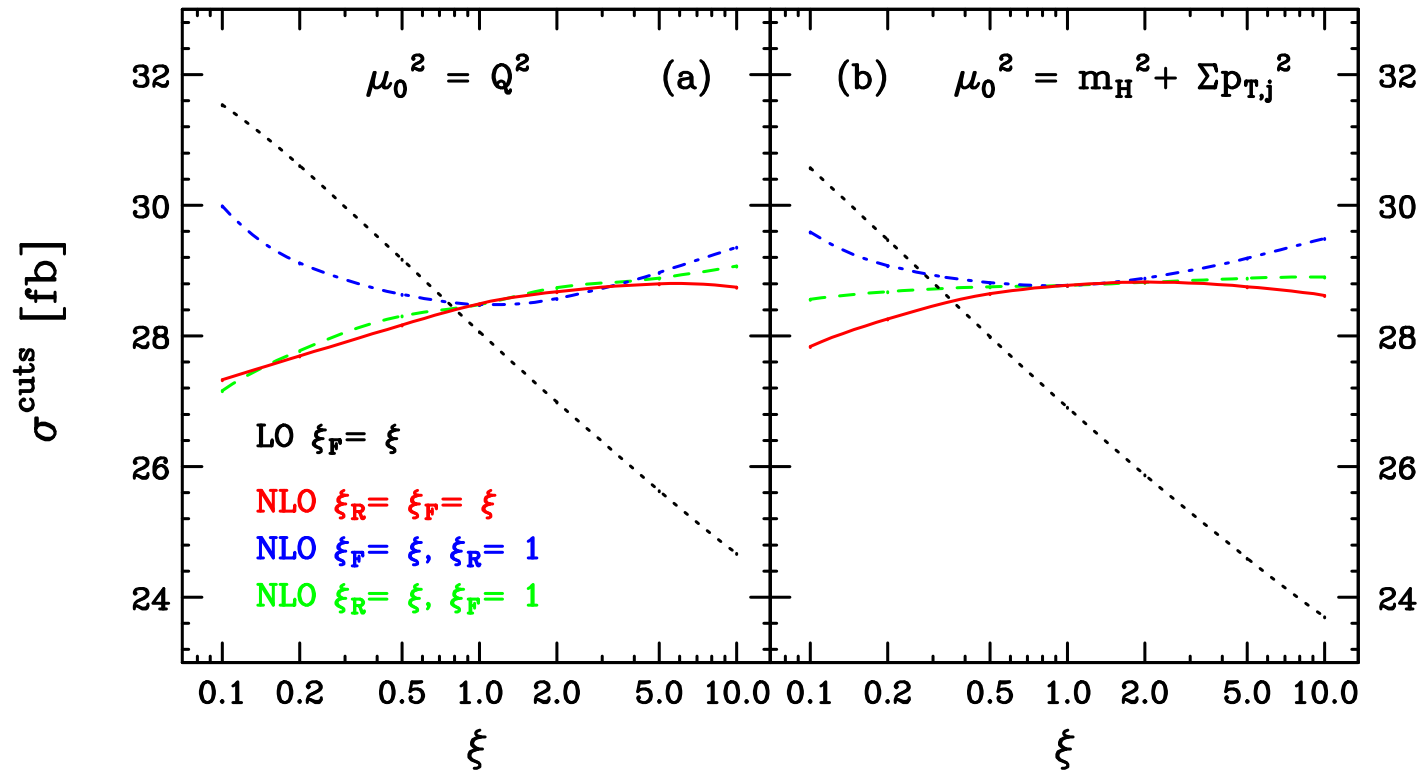
jets located in opposite hemispheres

WBF cuts



# scale uncertainty

choose default scale  $\mu_0^2 = Q_i^2$  or  $\mu_0^2 = m_H^2 + \sum p_{Tj}^2$   
set  $\mu_R = \xi_R \mu_0$  and  $\mu_F = \xi_F \mu_0$ , with variable  $\xi$



LO: no control on scale

NLO QCD: scale dependence strongly reduced

# impact of PDFs and scales

variation of cross section  $\sigma^{\text{WBF}}$  for  $Q^2/2 \leq \mu^2 \leq 2Q^2$ :

CTEQ6

$$\text{LO: } 14.65_{-0.95}^{+1.07} \text{ fb}$$

$$\text{NLO: } 14.79_{-0.19}^{+0.14} \text{ fb}$$

MSTW

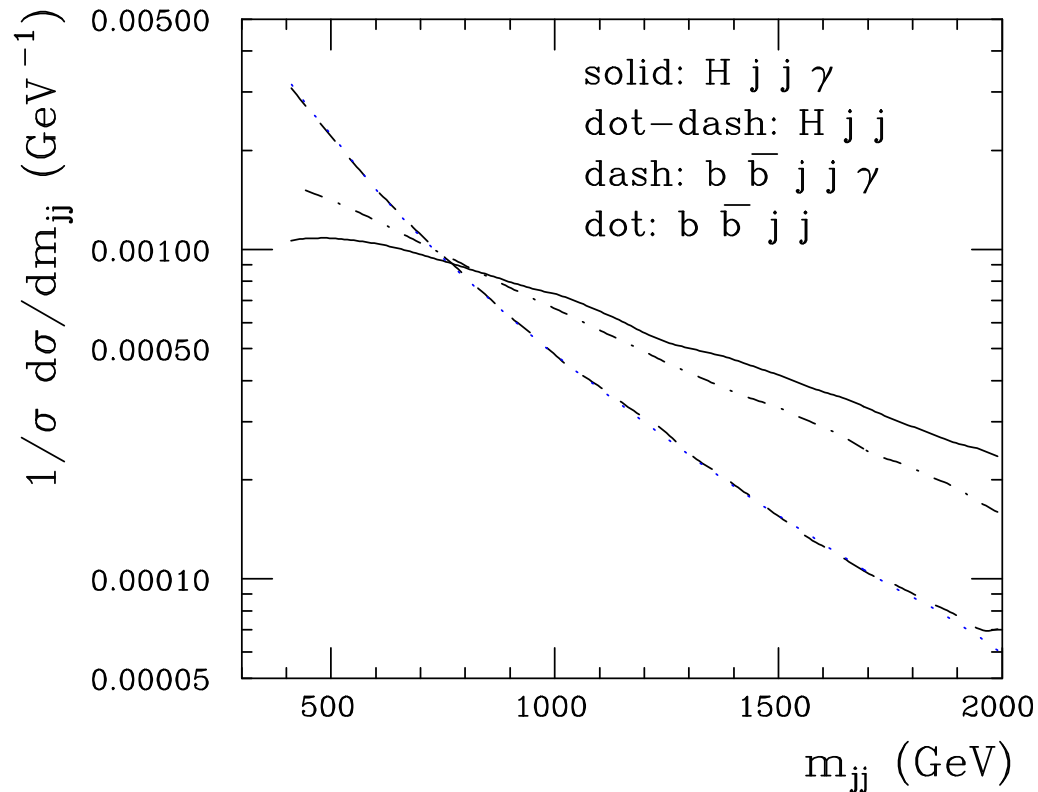
$$\text{LO: } 14.40_{-1.0}^{+1.13} \text{ fb}$$

$$\text{NLO: } 14.91_{-0.21}^{+0.03} \text{ fb}$$

$$\text{☞ } \Delta\sigma_{\text{LO}}^{\text{WBF}} \sim 14\% \quad \text{and} \quad \Delta\sigma_{\text{NLO}}^{\text{WBF}} \sim 2\%$$

# invariant mass of the tagging jets

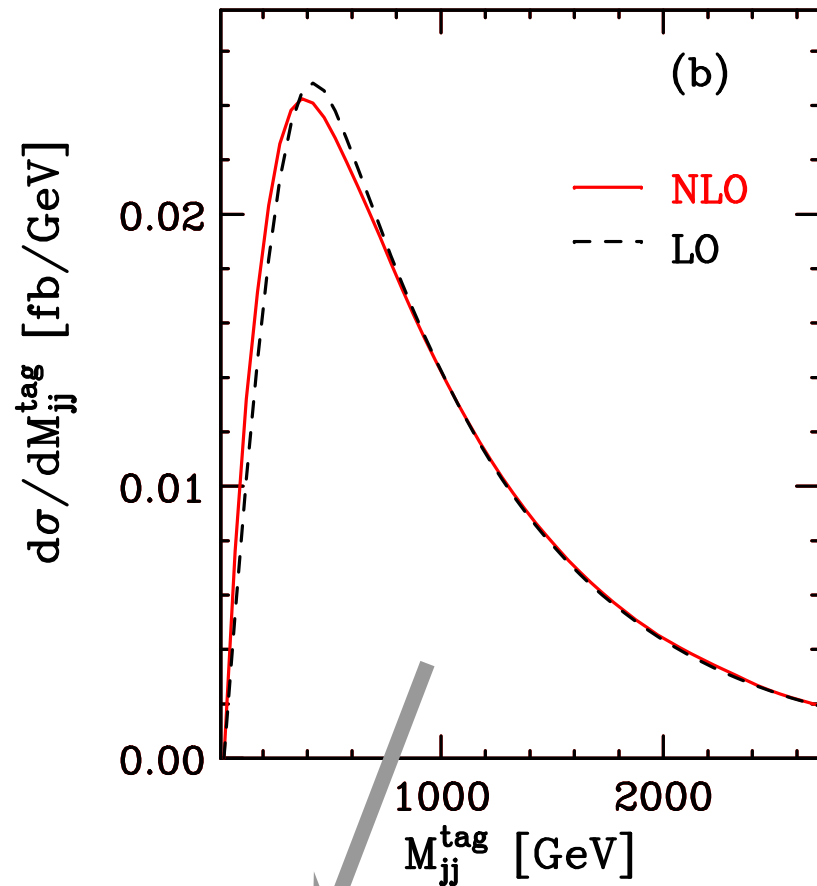
Gabrielli et al. (2007)



- ✦  $d\sigma/dm_{jj}$  slightly flatter for  $H\gamma jj$  signal than for  $Hjj$
- ✦  $b\bar{b}jj$  and  $b\bar{b}\gamma jj$  backgrounds have very similar shapes
- ✦ background distributions exhibit much steeper slope than signal
- ☞ stringent cut on  $m_{jj}$  is powerful tool for background suppression

# invariant mass of the tagging jets

Arnold, Figy, B. J., Zeppenfeld (2010)

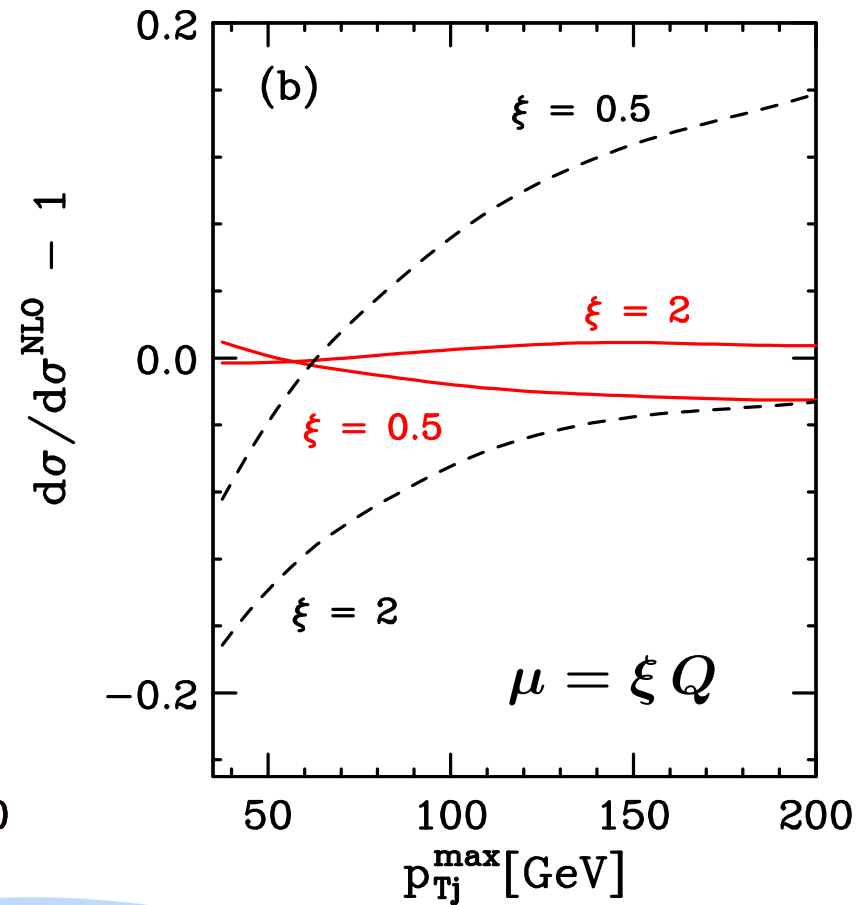
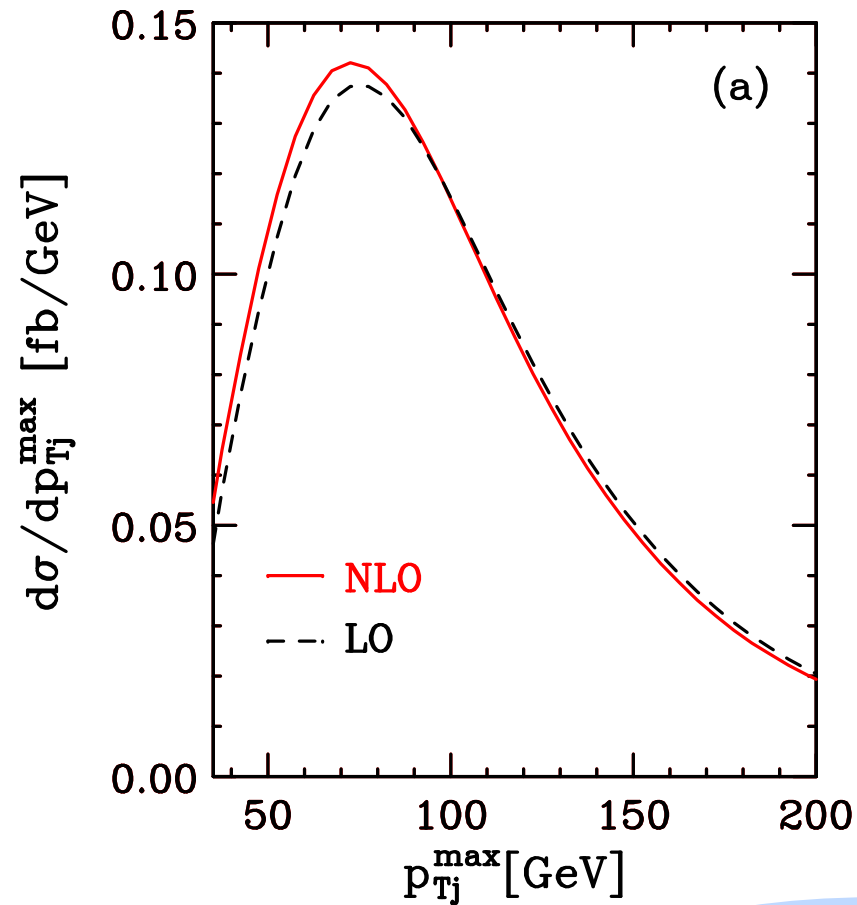


effect of NLO-QCD  
corrections small

- ❖  $d\sigma/dm_{jj}$  slightly flatter for  $H\gamma jj$  signal than for  $Hjj$
- ❖  $b\bar{b}jj$  and  $b\bar{b}\gamma jj$  backgrounds have very similar shapes
- ❖ background distributions exhibit much steeper slope than signal
- ☞ stringent cut on  $m_{jj}$  is powerful tool for background suppression

# transverse momentum of the hardest jet

Arnold, Figy, B. J., Zeppenfeld (2010)



$\sqrt{S} = 14 \text{ TeV}$

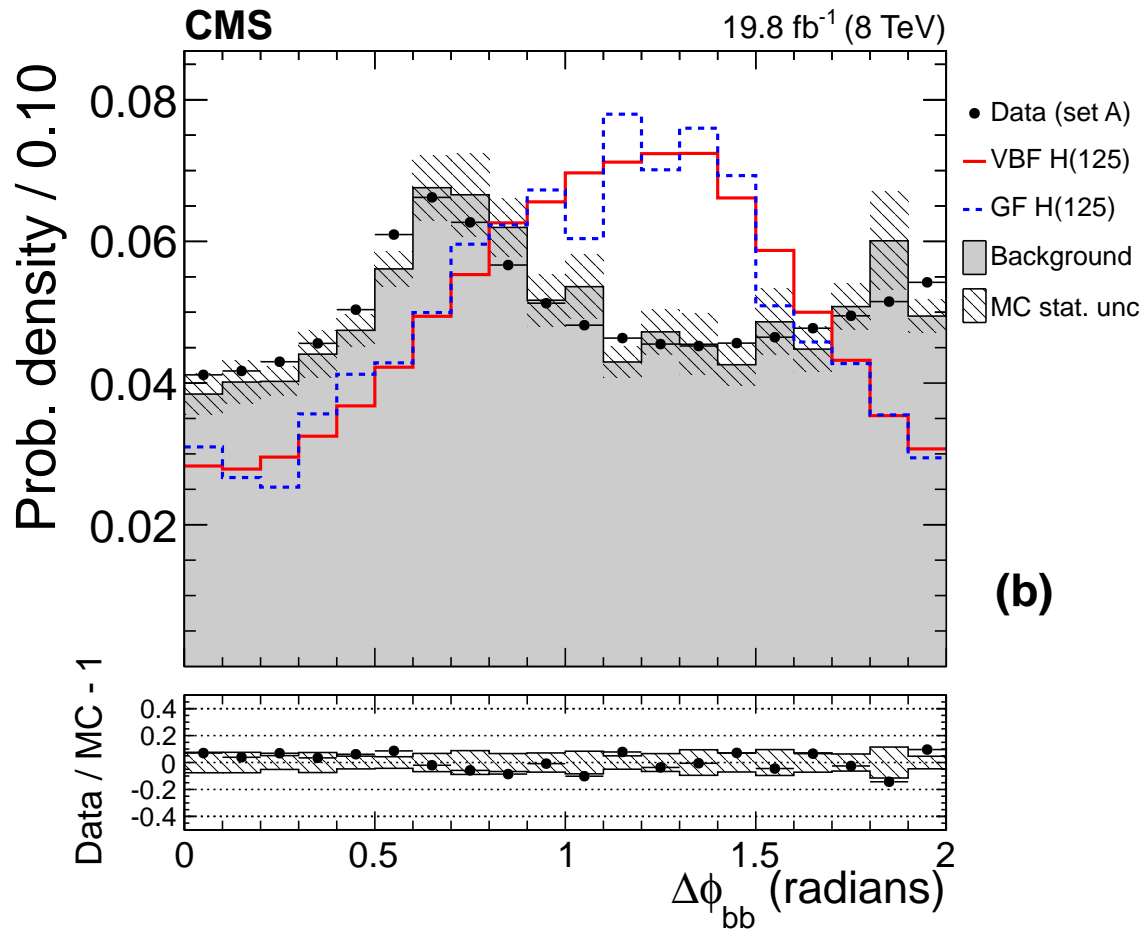
# $H\gamma jj$ : conclusions

---

- ❖ WBF offers promising prospects for Higgs boson search
- ❖  $H \rightarrow b\bar{b}$  mode profits from requirement of hard, central photon:
  - trigger efficiencies improved
  - QCD backgrounds suppressed significantly
  - signal significance  $S/\sqrt{B} \sim 3$  for  $100 \text{ fb}^{-1}$
- ❖ perturbative QCD corrections well under control  
(modest scale uncertainties &  $K$ -factors)
- ❖ shape of some distributions sensitive to radiative corrections

# news from CMS: $H \rightarrow b\bar{b}$ in VBF

arXiv: 1506.01010



search for Higgs production  
via VBF with decay  $H \rightarrow b\bar{b}$   
at  $\sqrt{s} = 8$  TeV

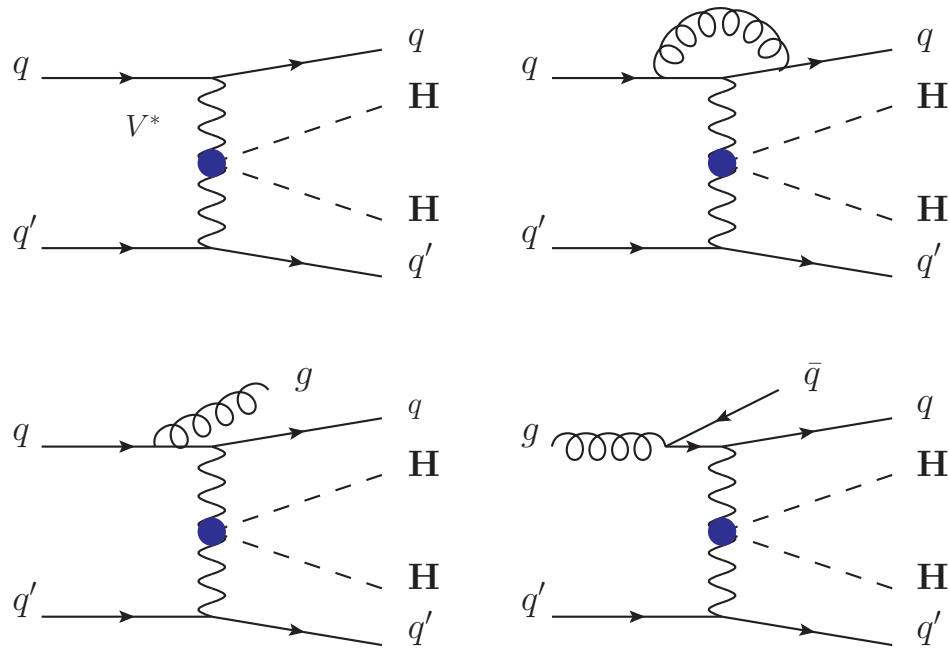
signal strength

$$\mu = \sigma / \sigma_{\text{SM}} = 2.8^{+1.6}_{-1.4}$$

compare to

$$\mu = 1.03^{+0.44}_{-0.42} (VH + ttH)$$

# Higgs pair production via VBF



sensitive to

❖  $VVHH$  coupling

❖ Higgs self coupling

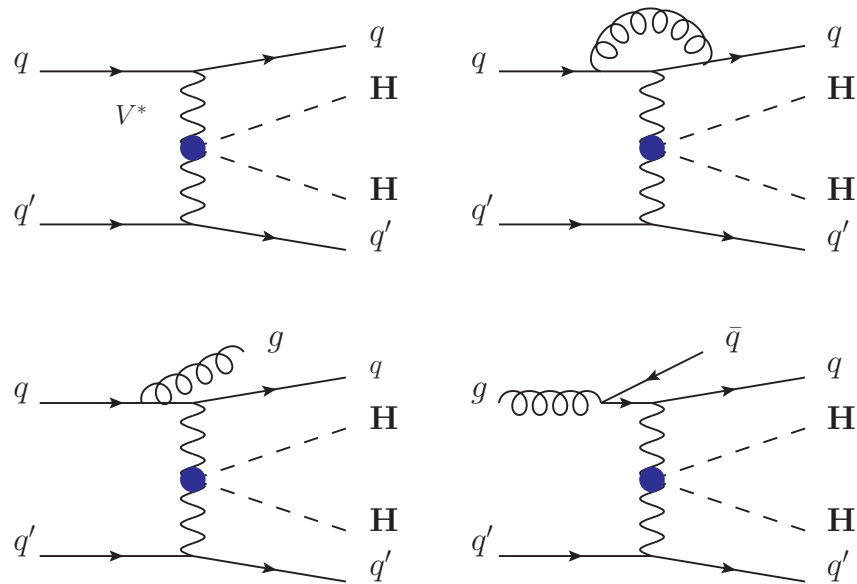
→ access Higgs potential

recall: Higgs potential

$$V(H^\dagger H) = -\mu^2 H^\dagger H + \frac{\lambda}{4} (H^\dagger H)^2$$



# Higgs pair production via VBF



✓ same (simple) QCD structure as single Higgs production via VBF

✗ cross sections very small

$\sqrt{s}$ [TeV]	$\sigma_{gg \rightarrow HH}^{\text{NLO}}$ [fb]	$\sigma_{qq' \rightarrow HHqq'}^{\text{NLO}}$ [fb]	$\sigma_{q\bar{q}' \rightarrow WHH}^{\text{NNLO}}$ [fb]	$\sigma_{q\bar{q} \rightarrow ZHH}^{\text{NNLO}}$ [fb]	$\sigma_{q\bar{q}/gg \rightarrow t\bar{t}HH}^{\text{LO}}$ [fb]
8	8.16	0.49	0.21	0.14	0.21
14	33.89	2.01	0.57	0.42	1.02
33	207.29	12.05	1.99	1.68	7.91
100	1417.83	79.55	8.00	8.27	77.82

taken from *Baglio et al. (2012)*

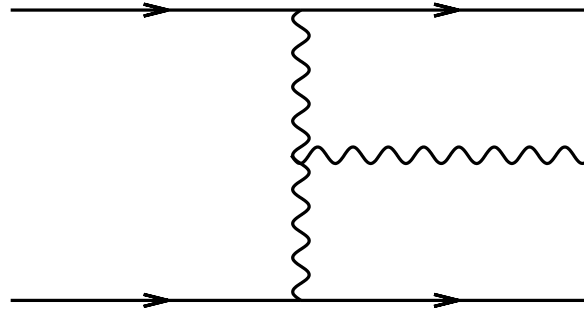
# the Higgs: only one part of the full picture

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# $pp \rightarrow Vjj$ via VBF

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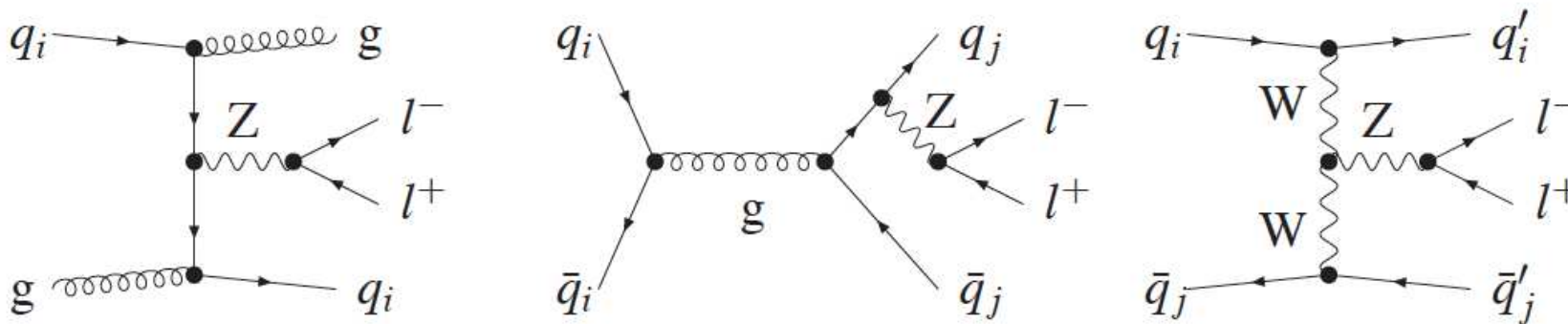


- ❖ sensitive to **triple gauge boson couplings**  
complementary to di-boson production  
(2 bosons spacelike, not timelike)
- ❖ similar signature as Higgs production via VBF  
→ explore systematics of  $Hjj$  final state

# Z boson production in association with two jets

$pp \rightarrow \ell^+ \ell^- jj$  proceeds via **different production modes**;

tree-level:  $\mathcal{O}(\alpha^2 \alpha_s^2)$ ,  $\mathcal{O}(\alpha^3 \alpha_s)$ ,  $\mathcal{O}(\alpha^4)$



NLO-QCD to QCD contributions [Campbell, Ellis, Rainwater (2002-03)]

NLO-QCD to VBF contributions [Oleari, Zeppenfeld (2003)]

NLO-EW at order  $\mathcal{O}(\alpha^2 \alpha_s^3)$  [Denner, Hofer, Scharf, Uccirati (2013-14)]

[ similar calculation for  $W + \leq 3$  jets by Kallweit et al. (2014) ]

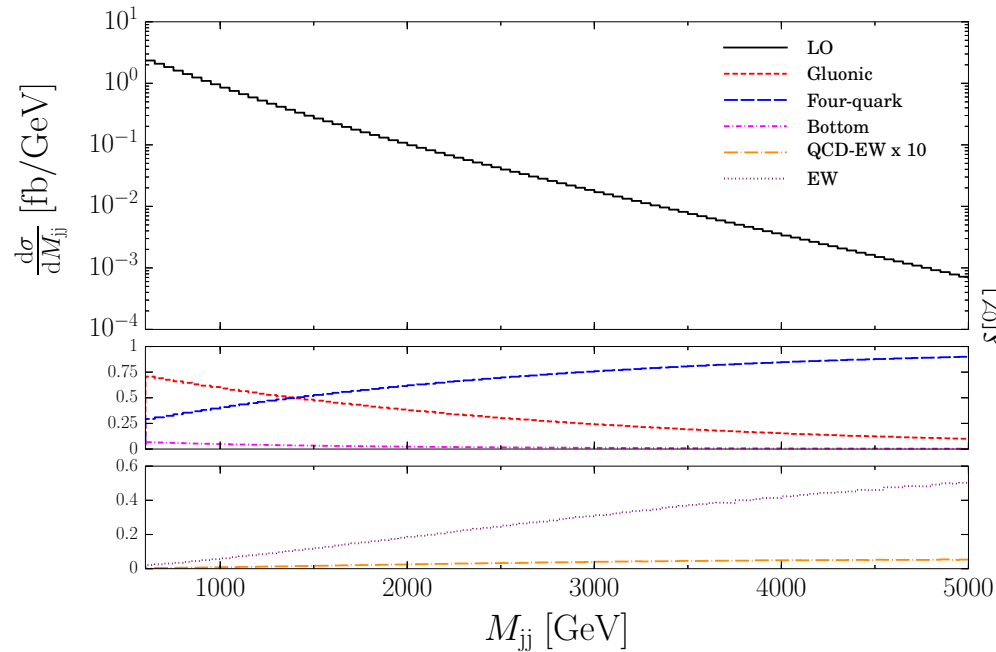
# $pp \rightarrow Zjj$ @ LO: basic and VBF cuts

process class	$\sigma$ [fb]	$\sigma/\sigma_{tot}$ [%]	$\sigma_{\alpha_s^2\alpha^2}/\sigma$ [%]	$\sigma_{\alpha_s\alpha^3}/\sigma$ [%]	$\sigma_{\alpha^4}/\sigma$ [%]
gluonic	40910(8)	79.9	100	—	—
four-quark	10299(1)	20.1	94.7	+0.4	4.8
bottom quarks	4376(3)	8.54	—	—	—
<b>sum (basic)</b>	<b>51209(8)</b>	<b>100</b>	<b>98.9</b>	<b>&lt; 0.1</b>	<b>1.0</b>
gluonic	617.8(4)	59.4	100	—	—
four-quark	421.7(1)	40.6	82.9	0.2	16.9
bottom quarks	51.82(2)	4.98	—	—	—
<b>sum (VBF)</b>	<b>1039.6(4)</b>	<b>100</b>	<b>93.1</b>	<b>0.01</b>	<b>6.9</b>

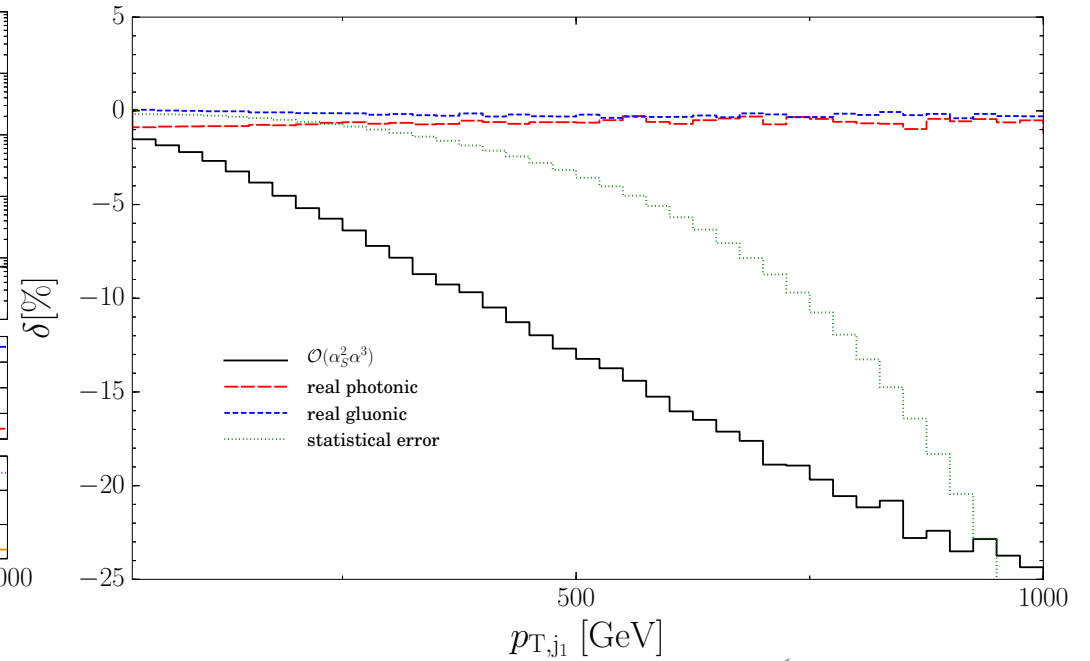
numbers taken from *Denner, Hofer, Scharf, Uccirati (2014)*

# $pp \rightarrow \ell^+ \ell^- jj$ with VBF cuts

[Denner, Hofer, Scharf, Uccirati (2014)]



gluonic channels  
dominant in bulk of x-sec



large EW Sudakov logs

# $pp \rightarrow Zjj$ via VBF in the POWHEG-BOX

Schneider, Zanderighi, B.J. (2012)

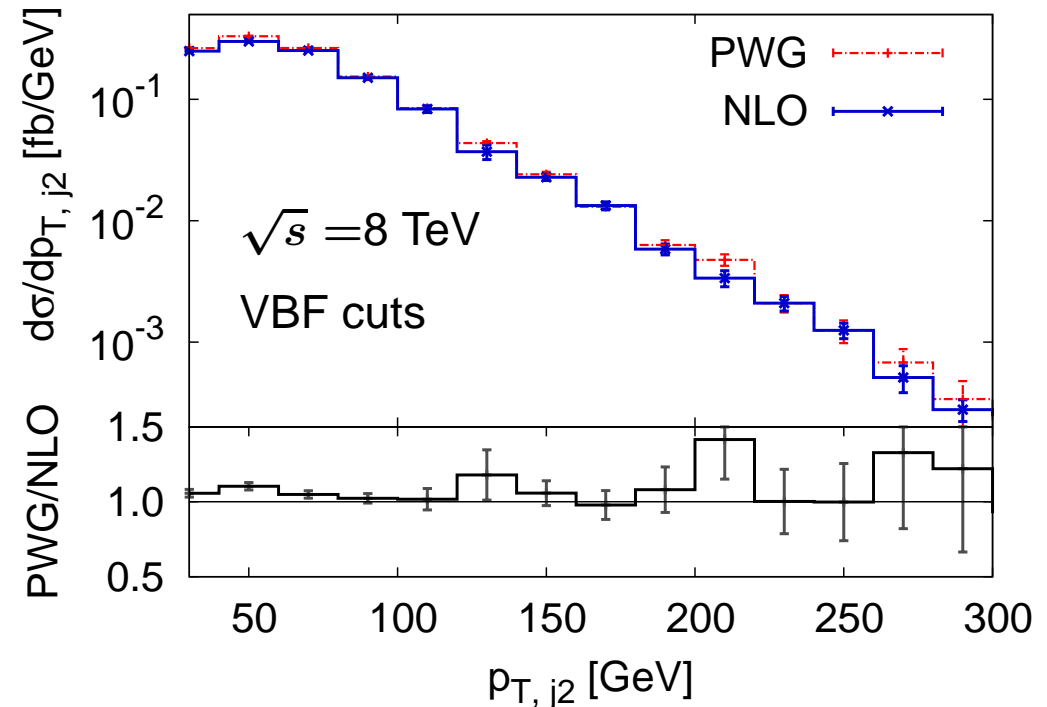
matching with parton shower programs in the POWHEG-BOX:

QCD production:

*Campbell, Ellis, Nason, Zanderighi; Re (2012-13)*

VBF production:

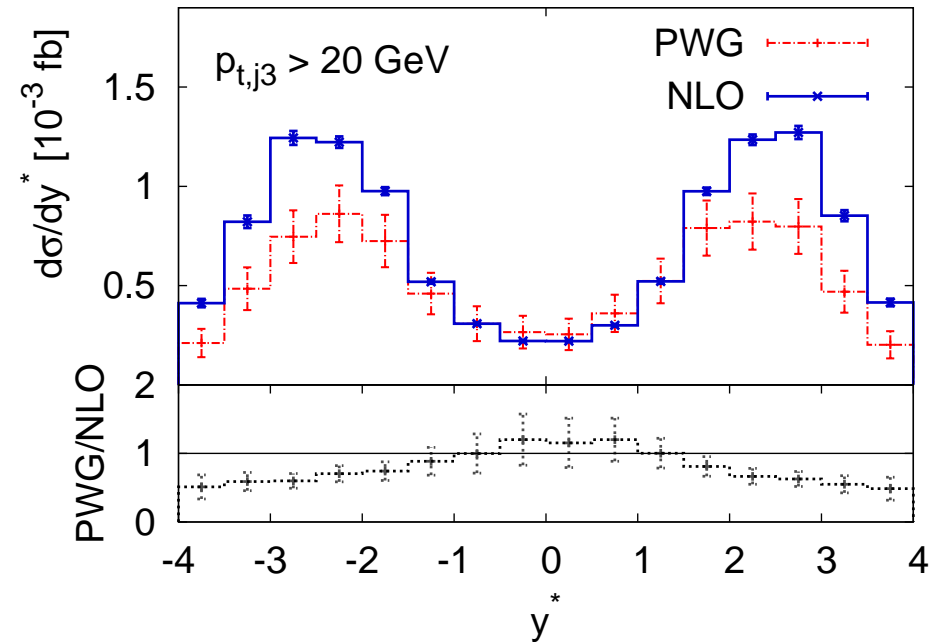
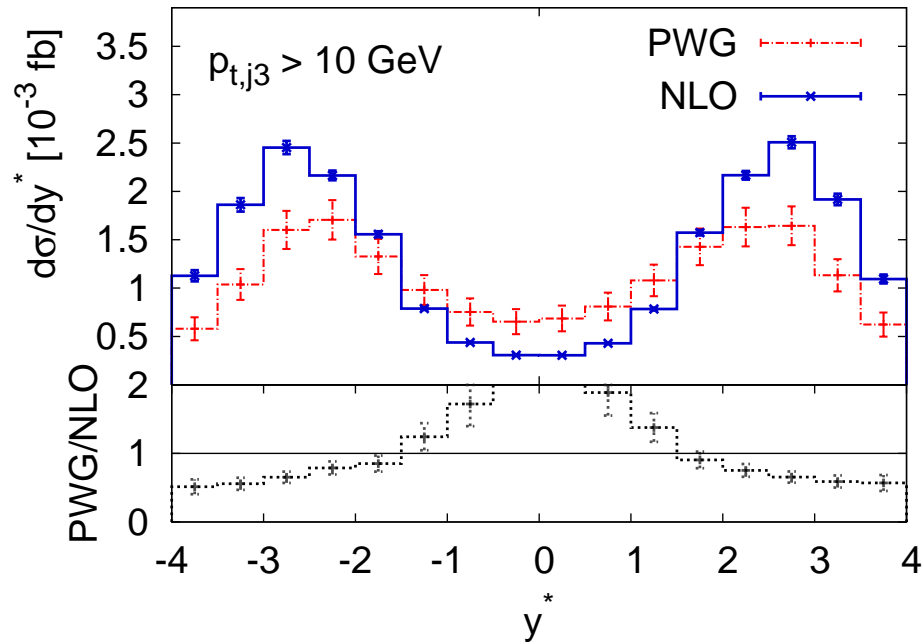
*Schneider, Zanderighi, BJ (2012); Schissler, Zeppenfeld (2013)*



parton shower effects are moderate for hard jets

# $pp \rightarrow Zjj$ via VBF in the POWHEG-BOX

Schneider, Zanderighi, B.J. (2012)



location of third jet relative to tagging jets

$$y^* = y_{j3} - \frac{y_{j1} - y_{j2}}{2}$$

note: transverse momentum cut on extra jets matters



# further developments in $pp \rightarrow V + n \text{ jets}$

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- ❖ NLO QCD for QCD production mode:

  - $Z + \leq 4 \text{ jets}$  in BlackHat [Ita et al. (2011)]

  - $W + \leq 5 \text{ jets}$  in BlackHat [Bern et al. (2013)]

- ❖ NLO QCD+EW for QCD production mode:

  - $W + \leq 3 \text{ jets}$  in OpenLoops+Sherpa/Munich

  - [Kallweit, Lindert, Maierhöfer, Pozzorini, Schönherr (2014)]

- ❖ room for improvements:

  - matching and merging for QCD-induced  $V + n \text{ jets}$  beyond LO QCD (including more than two jets)

  - NLO(+PS) for higher jet multiplicities in EW production mode

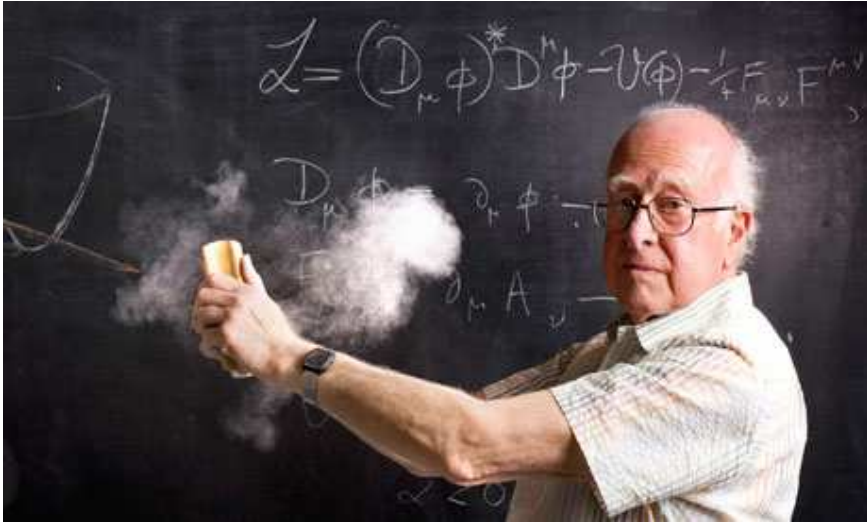
VBF crucial for understanding mechanism of electroweak symmetry breaking:

- \*  $Hjj$ : very clean Higgs production channel
- \*  $VVjj$ : sensitive to signatures of new physics in the gauge boson sector

important pre-requisites:

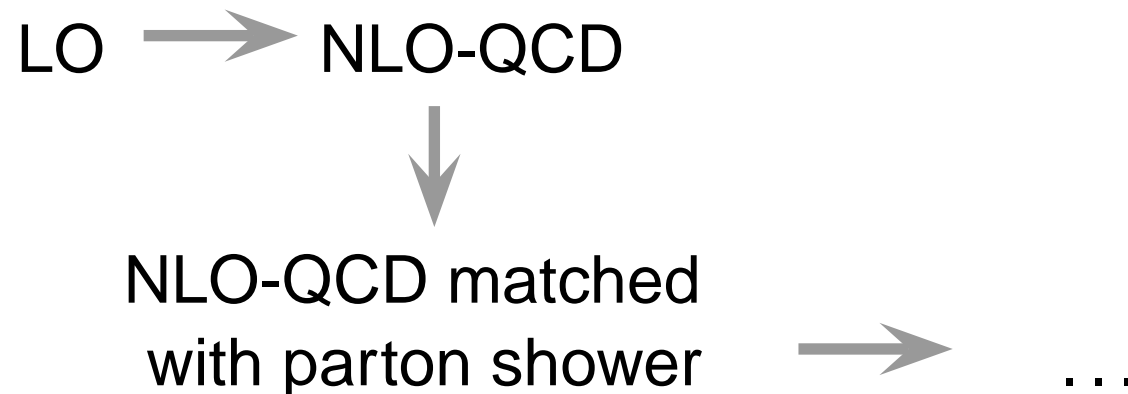
- ✓ explicit calculations revealed that VBF reactions are **perturbatively well-behaved** (NLO-QCD corrections and parton-shower effects moderate)

# summary



- ✓ exciting times as the Higgs boson is being discovered and explored
- \* crucial pre-requisite: modern methods in collider physics

we have seen how methods become more advanced and sophisticated as time goes by:



# conclusions

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for understanding and interpreting physics

at the LHC (and beyond . . . ) it is vital to provide:

- ❖ **precise predictions** for **signals and backgrounds**, including
  - NLO QCD corrections
  - interference effects, resummations, well-constrained PDFs, . . .
- ❖ **realistic predictions**, allowing for
  - calculation of distributions within experimental selection cuts
  - matching to parton-shower Monte Carlos at NLO-QCD accuracy
- ❖ **sophisticated analysis techniques**, requiring cross links between experimentalists and theorists / phenomenologists

# outlook

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- ❖ the future will ask for **more precise predictions**, including
  - NLO electroweak corrections
  - NNLO-QCD predictions for standard-candle processes
  - precision calculations beyond the Standard Model
  
- ❖ we'll need **more realistic predictions**, requiring
  - tools that are fast and easy-to-use
  - better parton-shower Monte Carlos
    - (new tunes, better modeling of non-perturbative effects, . . .)
  - matching beyond NLO in QCD
  - matching & merging
    - (combination of processes with different jet multiplicities)
  - matching NLO electroweak calculations to parton showers