The resummed Higgs qt spectrum

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Outline

Why transverse momentum resummation? The qT resummation formalism The resummed Higgs qT spectrum Ş The resummed gT spectrum for yy production Ş Ş Summary

Why transverse momentum resummation?

- The effects of the QCD radiation are encoded in the qT spectrum.
- Transverse momentum (qT) and rapidity identify the Higgs kinematics
- The fixed order can't describe the small qT region (qT<<M)</p>
- Solution In the small-qT region, where the bulk of events is produced, the convergence of the fixed-order expansion is spoiled, since the coefficients of the perturbative series in α_s are enhanced by powers of large logarithmic terms, $\ln^m(M^2/qT^2)$.

We have to distinguish two regions of transverse momenta

₽ qT ~ M_H

To have $qT \neq 0$ the Higgs boson has to recoil against at least one parton

NLO corrections are known only in the large m_{top} approximation (part of inclusive NNLO cross section !)



D. de Florian, Z.Kunszt, MG (1999) V.Ravindran, J.Smith, V.Van Neerven (2002) C.Glosser, C.Schmidt (2002)

We have to distinguish two regions of transverse momenta

ĕ qT ~ M_H

To have $qT \neq 0$ the Higgs boson has to recoil against at least one parton



(see also Boughezal, Caola, Petriello, Melnikov, Schulze (2013))

We have to distinguish two regions of transverse momenta

₽ qT << M_H

In this region large logarithmic corrections of the form $\alpha_s^{m}\ln^{2m}(M^2/qT^2)$ appear that originate from soft and collinear emission $\widehat{}$ the perturbative expansion becomes not reliable



LO:
$$\frac{d\sigma}{dp_T} \to +\infty$$
 as $p_T \to 0$
NLO: $\frac{d\sigma}{dp_T} \to -\infty$ as $p_T \to 0$

Resummation Needed (effectively performed at leading log level by standard MC generators)

Signal and background



The qT resummation formalism

The qT resummation formalism for colorless final states

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- Resummation in b-space was fully formalized by Collins, Soper and Sterman for the DY process by $q\bar{q}$ anihilation
- Process-independent universal generalization to generic
 colorless high-mass systems
 Catani, de Florian, Grazzini (2000)
 Bozzi, Catani, de Florian, Grazzini (2003)
 - Universal resummation coefficients explicitly known at NLO/NLL level Kodaira, Trentadue (1981) Catani, d'Emilio, Trentadue (1988)
 - And NNLO/NNLL

Davies, Stirling, Webber (1985) De Florian, Grazzini (2000) Becher, Neubert (2010) Catani, Grazzini (2011) \rightarrow H² (Higgs) Catani, LC, de Florian, Ferrera, Grazzini (2012) \rightarrow H² (Higgs) Catani, LC, de Florian, Ferrera, Grazzini (2013) \rightarrow H² (Univ) Gehrman, Lubbert, Yang (2012)

Catani-Grazzini (2010) (gg fusion sub-process)

Catani, de Florian, Grazzini (2000) Bozzi, Catani, de Florian, Grazzini (2005) Catani, LC, de Florian, Ferrera, Grazzini (2013)

PDFs

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Resummation performed in b-space \rightarrow constraint of qT conservation

$$\frac{d\sigma_F}{dq_T^2}(q_T, M, s) = \frac{M^2}{s} \int_0^\infty db \, \frac{b}{2} \, J_0(bq_T) \, W^F(b, M, s) + \dots$$

$$W_N^F(b,M) = \sum_{a,b} \mathcal{W}_{ab,N}^F(b,M;\alpha_S(\mu_R^2),\mu_R^2,\mu_F^2) f_{a/h_1,N}(\mu_F^2) f_{b/h_2,N}(\mu_F^2)$$

$$\frac{d\hat{\sigma}_{F\,ab}^{(\text{res.})}}{dq_T^2}(q_T, M, \hat{s}; \alpha_{\rm S}(\mu_R^2), \mu_R^2, \mu_F^2) = \frac{M^2}{\hat{s}} \int_0^\infty db \, \frac{b}{2} \, J_0(bq_T) \, \mathcal{W}_{ab}^F(b, M, \hat{s}; \alpha_{\rm S}(\mu_R^2), \mu_R^2, \mu_F^2)$$



Catani, de Florian, Grazzini (2000) Bozzi, Catani, de Florian, Grazzini (2005) Catani, LC, de Florian, Ferrera, Grazzini (2013)

$$\begin{aligned} \mathcal{G}_{N}(\alpha_{\rm S},L;M^{2}/\mu_{R}^{2},M^{2}/Q^{2}) &= L \, g^{(1)}(\alpha_{\rm S}L) + g^{(2)}_{N}(\alpha_{\rm S}L;M^{2}/\mu_{R}^{2},M^{2}/Q^{2}) \\ &+ \frac{\alpha_{\rm S}}{\pi} g^{(3)}_{N}(\alpha_{\rm S}L;M^{2}/\mu_{R}^{2},M^{2}/Q^{2}) \rightarrow \text{NNLL} \\ &+ \sum_{n=4}^{+\infty} \left(\frac{\alpha_{\rm S}}{\pi}\right)^{n-2} \, g^{(n)}_{N}(\alpha_{\rm S}L;M^{2}/\mu_{R}^{2},M^{2}/Q^{2}) \end{aligned}$$

With L= ln(1+ Q²b²/b²₀) and $\alpha_s = \alpha_s(\mu_R)$; $\mu_R \sim O(M)$

Resummation scale Q ~ O(M)

 $\stackrel{\checkmark}{\Rightarrow} O(\alpha_{s}L) \sim 1 \rightarrow LL \sim \alpha_{s}^{n} L^{n+1}$ and NLL $\sim \alpha_{s}^{n} L^{n} \rightarrow NLL/LL \sim O(\alpha_{s})$ $\stackrel{\backsim}{\Rightarrow}$ The form factor takes the same form as in threshold resummation $\stackrel{\backsim}{\Rightarrow}$ Unitarity constraint enforces correct total cross section

Catani, de Florian, Grazzini (2000) Bozzi, Catani, de Florian, Grazzini (2005) Catani, LC, de Florian, Ferrera, Grazzini (2013)

- L ~ $ln(Q^2b^2/b_0^2)$; b Q >> 1 (large log) L << 1 ; b Q << 1 (small corrections) In particular : L \rightarrow 0 if b \rightarrow 0 (total cross section)
 - Unitarity constraint \rightarrow the integral over qT of the transverse momentum distribution gives the total Xsection





Catani, de Florian, Grazzini (2000) Bozzi, Catani, de Florian, Grazzini (2005) Catani, LC, de Florian, Ferrera, Grazzini (2013)

Unitarity constraint \rightarrow the integral over qT of the transverse momentum distribution gives the total Xsection

$$\int_0^\infty dq_T^2 \; \frac{d\hat{\sigma}_F^{(\text{res.})}}{dq_T^2} (q_T, M, \hat{s}; \alpha_{\rm S}(\mu_R^2), \mu_R^2, \mu_F^2, Q^2) = \frac{M^2}{\hat{s}} \; \mathcal{H}^F \big(M, \hat{s}, \alpha_{\rm S}(\mu_R^2); M^2/\mu_R^2, M^2/\mu_F^2, M^2/Q^2 \big) \; ,$$

$$\frac{d\hat{\sigma}_{F\,ab}}{dq_T^2} = \frac{d\hat{\sigma}_{F\,ab}^{(\text{res.})}}{dq_T^2} + \frac{d\hat{\sigma}_{F\,ab}^{(\text{fin.})}}{dq_T^2}$$



The calculation can be done:

• NLL+NLO: we need the functions $g^{(1)}$, $g^{(2)}_N$ and the coefficient $\mathcal{H}^{(1)}_N$ plus the matching at relative order α_S

NNLL+NNLO: we also need the function $g_N^{(3)}$ and the coefficient $\mathcal{H}_N^{(2)}$ plus the matching at relative order $\alpha_{\rm S}^2$

Catani, de Florian, Grazzini (2000) Bozzi, Catani, de Florian, Grazzini (2005) Catani, LC, de Florian, Ferrera, Grazzini (2013)

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The formalism was applied at NNLL+NNLO to:

ZZ, WW, YY, H, DY

Catani, de Florian, Ferrera, Grazzini (2015); Bozzi, Catani, de Florian, Ferrera Grazzini (2011); LC, Coradeschi, de Florian (2015); de Florian, Ferrera, Tommasini, Grazzini (2011); Grazzini, Kallweit, Rathlev, Wiesemann (2015).

Catani, de Florian, Grazzini (2000) Bozzi, Catani, de Florian, Grazzini (2005) Catani, LC, de Florian, Ferrera, Grazzini (2013)

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Recently all-order extension of the formalism for tt First all-order formulation of qT resummation for final states with color

Zhu, Li, Li, Shao; Yang (2012) Zhu, Li, Li, Shao; Yang (2013) Catani, Grazzini, Torre (2013)

The resummed Higgs qT spectrum

Higgs boson → HRes

D. de Florian, G.Ferrera, D. Tommasini, M.Grazzini (2011)

HRes combines the NNLO calculation in HNNLO with the small-qT resummation as implemented in HqT → "Higgs event generator" Bozzi, Catani, de Florian, Grazzini (2003)(2005)

It includes the decay $H \rightarrow \gamma\gamma$, $H \rightarrow WW \rightarrow l\nu l\nu$, $H \rightarrow ZZ \rightarrow 4l$



Higgs boson → HRes

D. de Florian, G.Ferrera, D. Tommasini, M.Grazzini (2011) Bozzi, Catani, de Florian, Grazzini (2003)(2005)



The upper (lower) curve at small q_T is obtained with $g_{NP} = 1.67 \text{ GeV}^2 (g_{NP} = 5.64 \text{ GeV}^2)$

Higgs boson → HRes

D. de Florian, G.Ferrera, D. Tommasini, M.Grazzini (2011) Bozzi, Catani, de Florian, Grazzini (2003)(2005)



The first data



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ATLAS-CONF-2014-044

ATLAS data seem to suggest a harder spectrum (but still very large uncertainties !)

Sketchy form of contributions





The resummed qT spectrum for yy production

Resummation \rightarrow ATLAS $\gamma\gamma$ – (2 γ Res) First results!

LC, Coradeschi, de Florian



$$S_{NP}^{a} = \exp(-C_{a} g_{NP} b^{2})$$

$$a = F \text{ for } q\bar{q} \text{ and } a = A \text{ for } gg$$

$$C_{F} = (N_{c}^{2} - 1)/(2N_{c}) \text{ and } C_{A} = N_{c}$$

$$p_T^{\text{harder}} \ge 25 \text{ GeV}, \quad p_T^{\text{softer}} \ge 22 \text{ GeV},$$
$$|y_\gamma| < 1.37 \lor 1.52 < |y_\gamma| \le 2.37,$$
$$E_T \max = 4 \text{ GeV}, \quad n = 1, \quad R = 0.4,$$
$$R_{\gamma\gamma} = 0.4$$

Resummation → ATLAS yy - (2yRes)

LC, Coradeschi, de Florian



qT resummation "spreads" the uncertainties of the gg channel over the whole qT range

$$p_T^{\text{harder}} \ge 25 \text{ GeV}, \ p_T^{\text{softer}} \ge 22 \text{ GeV}, \ |y_{\gamma}| < 1.37 \lor 1.52 < |y_{\gamma}| \le 2.37, \ E_T \ max} = 4 \text{ GeV}, \ n = 1, \ R = 0.4, \ R_{\gamma\gamma} = 0.4$$

First results!

Resummation → ATLAS yy - (2yRes)



Resummation → ATLAS yy - (2yRes)



Resummation \rightarrow ATLAS $\gamma\gamma$ – (2 γ Res)

First results!

LC, Coradeschi, de Florian



Resummation \rightarrow ATLAS $\gamma\gamma$ – (2 γ Res) First results!

LC, Coradeschi, de Florian

dơ/d∆∲_{YY} [pb/rad] ATLAS NNLL+NLO (µF=2*Myy µR=0.5*Mvv) 10² √s = 7 TeV NNLL+NLO (µF=0.5*Myy; $\mu R=2*Myy)$ 100 — Data 2011, Ldt = 4.9 fb⁻¹ Data HIH DIPHOX+GAMMA2MC (CT10 dơ/dΔΦ_W [pb/rad] ///// 2γNNLO (MSTW2008) $pp \rightarrow yy + X$ ATLAS √s=7TeV 10 E data/DIPHOX 2.5 2.5 0.5 1.5 2 3 0 1.5 $\Delta \Phi_{\rm W}$ [rad] 0.5 Uncertainties \rightarrow 6% - 8% due to the opening of the gg channel which is data/2γNNLO "effectively" LO at NNLO 2.5 qT resummation "spreads" the uncertainties of the gg channel over the ⁰ठे 0.5 1.5 2.5 2 whole $\Delta \phi$ range ∆¢ ,, [rad]

Summary

- The qT resummation is necessary (and essential) in order to reproduce the phenomenology of the measured qT spectrum
- First ATLAS data show a spectrum which is significantly harder than the SM prediction, though still with very large uncertainties
- HRes includes the finite top and bottom quark masses at full NLL+NLO accuracy. NNLL+NNLO effects are included in the large-mtop limit
- HRes allows us to retain the full kinematical information on the Higgs boson and its decay products in $H \rightarrow \gamma \gamma$, $H \rightarrow WW \rightarrow |v|v$ and $H \rightarrow ZZ \rightarrow 4|$
- Among the various kinematical distributions in $gg \rightarrow H$ the qT spectrum plays an important role: embodies main effects of QCD radiation
- First results of diphoton production at NNLL+NNLO (2γRes) show an improved agreement (respect NNLO) with the LHC data over the whole qT range.

Thank you!!!

Backup slides

Higgs p_T and BSM

Modifications of the Higgs couplings to gluons and the top quark can be parametrised as

$$\mathcal{L} = -c_t \frac{m_{top}}{v} \bar{\psi} \psi + \frac{\alpha_S}{12\pi} c_g \frac{h}{v} G_{\mu\nu} G^{\mu\nu} \qquad \text{SM:} \quad c_t = 1 \qquad c_g = 0$$

neglecting CP violation

 $\sigma_H \sim |c_t + c_g|^2 \, \sigma_H^{SM}$

 $\rightarrow not possible to disentangle c_t and c_g in the inclusive rate$

Direct access to top Yukawa coupling is offered by tth production but low sensitivity

Looking at high-pT events allows us to break this degeneracy

Relative effect of top partners on high-pT cross section can be very large



Mass effects at fixed order

Let us look at the mass effects in the NLO pT spectrum



When only the top contribution is considered the shape of the spectrum in the small and intermediate p_T region is similar to the $m_t \rightarrow \infty$ result

The bottom contribution significantly distorts the spectrum in the low $p_{\rm T}$ region

Mass effects at fixed order

In order to understand what happens let us focus on the qg channel

We may expect that when p_T << m_H the diagram should factorize naively independently on the mass of the heavy quark running in the loop

but this is not the case





Also in this channel the bottom contribution modifies the shape at small pT

The resummation formalism

The resummation formalism has been developed in the eighties Y.Dokshitzer, D.Diakonov, S.I.Troian (197

Y.Dokshitzer, D.Diakonov, S.I.Troian (1978) G. Parisi, R. Petronzio (1979) G. Curci, M.Greco, Y.Srivastava(1979) J. Collins, D.E. Soper, G. Sterman (1985)

- As it is customary in QCD resummations one has to work in a conjugate space in order to allow the kinematics of multiple gluon emission to factorize
- Many phenomenological studies performed at different levels of theoretical accuracy I.Hinchliffe, S.F.Novaes (1988)

I.Hinchliffe, S.F.Novaes (1988) R.P. Kauffmann (1991) C.P.Yuan (1992) C.Balazs, C.P.Yuan (2000) E. Berger, J. Qiu (2003) A.Kulezsa, J.Stirling (2003)



Recent studies also in the context of SCET

S.Mantry, F.Petriello (2009,2010)

T. Becher, M.Neubert (2010)

Process

dependent

Xsection

Catani, de Florian, Grazzini (2000) Bozzi, Catani, de Florian, Grazzini (2005) Catani, LC, de Florian, Ferrera, Grazzini (2013)

functions \rightarrow Universal

Resummation performed in b-space \rightarrow constraints of qT conservation

$$\frac{d\sigma_F}{dq_T^2}(q_T, M, s) = \frac{M^2}{s} \int_0^\infty db \frac{b}{2} J_0(bq_T) W^F(b, M, s) + \dots$$
PDFs
$$W_N^F(b, M) = \sum_{a,b} \mathcal{W}_{ab,N}^F(b, M; \alpha_S(\mu_R^2), \mu_R^2, \mu_F^2, f_{a/h_1,N}(\mu_F^2) f_{b/h_2,N}(\mu_F^2)$$

$$W_N^F(b, M) = \sum_{a,b} \mathcal{O}_{c\bar{c},F}(\alpha_S(M^2), M) H_c^F(\alpha_S(M^2)) S_c(M, b)$$

$$\times \sum_{a,b} \mathcal{O}_{c\bar{c},N}(\alpha_S(b_0^2/b^2)) C_{c\bar{c},N}(\alpha_S(b_0^2/b^2)) f_{a/h_1,N}(b_0^2/b^2) f_{b/h_2,N}(b_0^2/b^2)$$
Hard coefficient

H.Sargsyan, M. Grazzini (2013)

- It is not difficult to extend the fully exclusive calculation in HNNLO to include the exact dependence on the masses of the heavy quarks up to NLO
- Two loop virtual corrections available

M.Spira et al. (1991,1995) R.Harlander , P.Kant (2005) U.Aglietti, R.Bonciani, G. Degrassi, A.Vicini (2006)

One loop real corrections available

R.K.Ellis,I.Hinchliffe,M.Soldate, J. van der Bij (1988)



Top and bottom quark contributions exactly taken into account up to NLO. At NNLO we consider only the top-quark contribution and we rescale it with the ratio $\sigma_{LO}(mt)/\sigma_{LO}(mt \rightarrow \infty)$

HNNLO now includes \rightarrow NLO mass effects

H.Sargsyan, M. Grazzini (2013)

- Studying the analytic behavior of the QCD matrix elements we find that collinear factorization is a good approximation only when qT << 2m b</p>
- The standard resummation procedure cannot be straightforwardly applied to the bottom quark contribution

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How to deal with different scales:

- the top quark gives the dominant contribution to the qT cross section and we treat it as usual with a resummation scale Q1
- the bottom contributions (and the top-bottom interference) are controlled by an additional resummation scale Q2 that we choose of the order of the b-mass

In this way we limit the resummation for the bottom contribution only to the region in which it is really justified (and needed)

H.Sargsyan, M. Grazzini (2013)



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- We see that for Q2 =mb/2, mb, 2mb the fixed order is nicely reproduced in the region qT > 10 GeV. For Q2 =4mb instead the resummation deviates from the NLO result. We thus choose Q2 =mb as central scale and proceed with the full calculation

H.Sargsyan, M. Grazzini (2013)

Numerical results



Comparison of the results obtained with $Q_2=m_b$ and $Q_2=m_H/2$

Significant differences in the low-p_T region

The result with Q₂=m_H/2 is in agreement with independent calculation by Mantler-Wiesemann (and with MC@NLO)

Our result for $Q_2\text{=}m_b$ somewhat more similar to POWHEG though the distortion is at smaller $p_{\rm T}$

But in order to judge the relevance of this effect we should compare with the perturbative uncertainties affecting the NLL+NLO calculation (which are large)

H.Sargsyan, M. Grazzini (2013)

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H.Sargsyan, M. Grazzini (2013)

- Recently the choice of the central value and range of the second resummation scale has been the subject of discussion
- It has been argued that the factorisation breaking terms are small and could be treated as a finite remainder A.Banfi, P.F.Monni, G.Zanderighi (2013)
- This point of view has been recently taken by Harlander et al. who suggest to choose Q2 so as to let the resummed spectrum agree (with 100%) with the fixed order at $qT \sim m H$

R.Harlander, R.Mantler, M.Wiesemann (2014)

In this way one is lead to consider values of the second resummation scale Q2 larger than what suggested in the analysis of Sargsyan and Grazzini (but still smaller than Q1)

QT resummation and Higgs couplings

- The transverse momentum spectrum of the Higgs boson can be used to extract information about the couplings
- It has been argued that the most important region for this task is the large qT region and the total Xsection

Azatov, Paul (2014); Langenegger, Spira, Strebel (2015); Englert,McCullough, Spannowsky (2013); Langenegger , Spira, Starodumov, Trüb (2006); Spira, Grazzini, Ilnicka, Wiesemann (to be published)

Resummation → ATLAS yy



Resummation → ATLAS yy



DYRes



Vector boson production at the LHC with lepton selection cuts. The NLL+NLO (red) and NNLL+NNLO (blue) normalized q_T spectra for Z/γ^* production

The inset plot shows the ratio of the data and of the scale dependent NNLL+NNLO result with respect to the NNLL+NNLO result at central values of the scales.

DYRes



(a) The q_T spectrum at NNLL+NNLO accuracy for Z boson production at the LHC with $\sqrt{s} = 14$ TeV. Comparison of scale dependence (blue solid) and PDF (red crossed solid) uncertainties. The possible impact of NP effects is also shown (black crossed dashed). (b) The same results are normalized to the central NNLL+NNLO prediction at $\sqrt{s} = 14$ TeV (upper panel), and corresponding results are shown at $\sqrt{s} = 8$ TeV (lower panel).

2yRes

