

VECTOR BOSON SCATTERING AND VH-ASSOCIATED PRODUCTION IN THE VBFNLO MC

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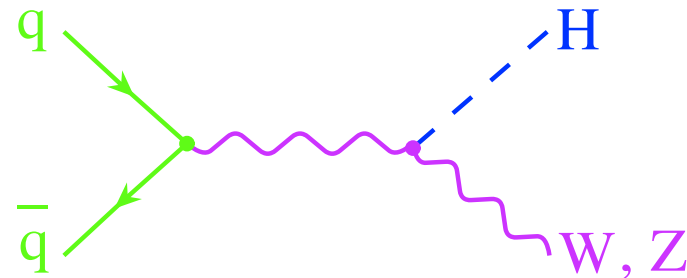
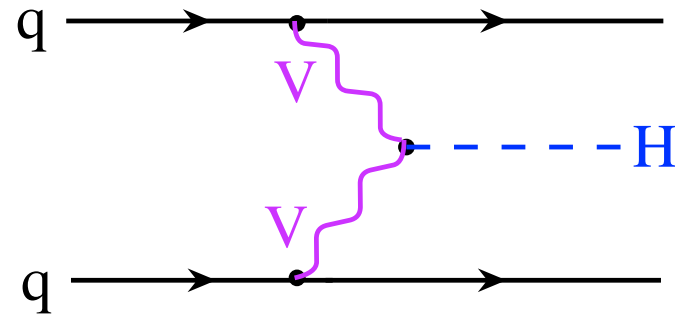
- NLO QCD corrections to VBF and VBS
- Central Jet Veto
- Anomalous couplings in $VV \rightarrow VV$ scattering
- Interface to Parton Shower



Introduction/Motivation

Vector boson fusion ($qq \rightarrow qqH, qq \rightarrow qqV$) and vector boson scattering ($qq \rightarrow qqVV$) are expected to provide prime information on the dynamics of electroweak symmetry breaking at the LHC

Information on hVV and hff couplings is augmented by study of VH production

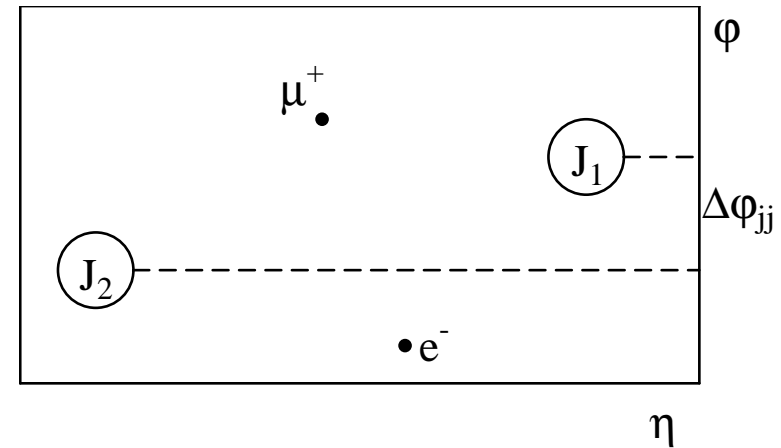
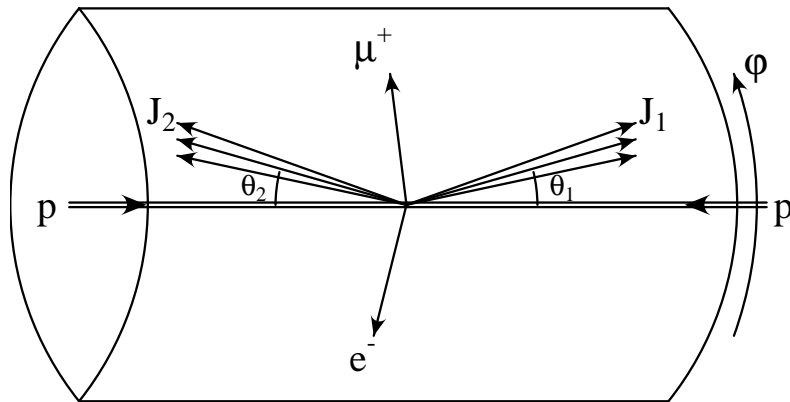


- We have calculated NLO QCD corrections for these and a variety of other processes with vector bosons in the final state.

Calculations are publicly available within the VBFNLO program package.

Code can be downloaded from <http://www.itp.kit.edu/~vbfnlweb/>

VBF and VBS signature



Characteristics:

- energetic jets in the **forward** and **backward** directions ($p_T > 20$ GeV)
- large **rapidity separation** and large **invariant mass** of the two tagging jets
 \implies Enhance signal contributions by “VBF cuts”, e.g.

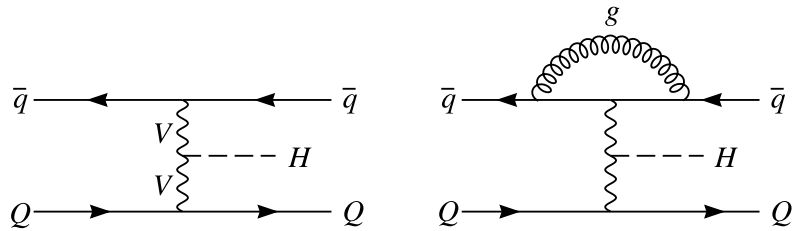
$$m_{jj} > 600 \text{ GeV} \quad |y_{j_1} - y_{j_2}| > 4$$

- Higgs/V/VV decay products **between** tagging jets

Generic features of NLO QCD corrections to VBF and VBS

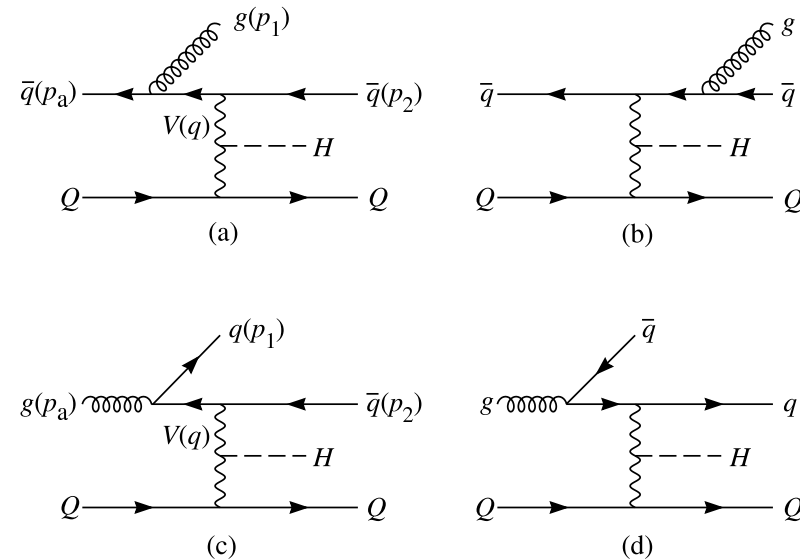
t -channel color singlet exchange \Rightarrow QCD corrections to different quark lines are independent

Born and vertex corrections to upper line



No t -channel gluon exchange at NLO

real emission contributions: upper line



Treat s -channel contributions (here VH production with $V \rightarrow jj$ decay)

and QCD processes (e.g. $VVjj$ production at order $\alpha_s^2 \alpha^2$) as separate processes.

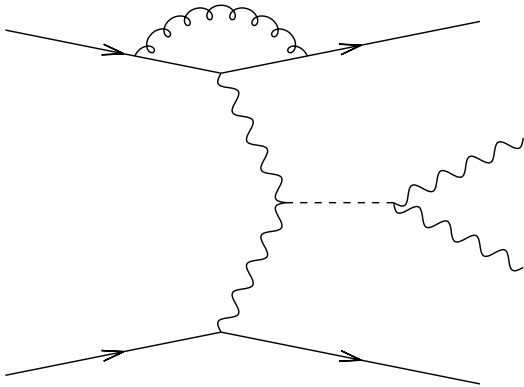
Neglect interference for identical fermions: small effects in phase space where VBF/VBS is visible

Features are generic for all VBF/VBS processes

Virtual corrections: Higgs production

Most trivial case: Higgs production

Virtual correction is vertex correction only



virtual amplitude proportional to Born

$$\mathcal{M}_V = \mathcal{M}_{\text{Born}} \frac{\alpha_s(\mu_R)}{4\pi} C_F \left(\frac{4\pi\mu_R^2}{Q^2} \right)^\epsilon \Gamma(1+\epsilon) \left[-\frac{2}{\epsilon^2} - \frac{3}{\epsilon} + \frac{\pi^2}{3} - 7 \right] + \mathcal{O}(\epsilon)$$

- Divergent piece canceled via Catani Seymour algorithm

Remaining virtual corrections are accounted for by trivial factor multiplying Born cross section

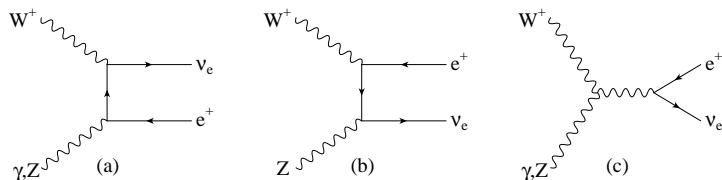
$$|\mathcal{M}_{\text{Born}}|^2 \left(1 + 2\alpha_s \frac{C_F}{2\pi} c_{\text{virt}} \right)$$

- Factor 2 for corrections to upper and lower quark line
- Same factor to Born cross section absorbs most of the virtual corrections for other VBF processes

3 weak bosons on a quark line: $qq \rightarrow qqWW, qqZZ, qqWZ$ at NLO

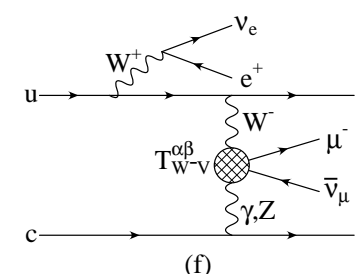
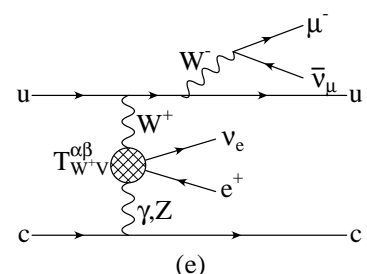
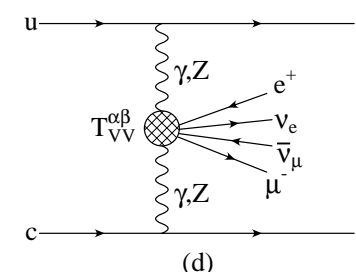
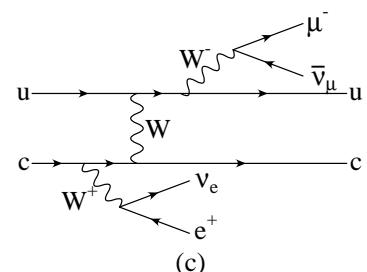
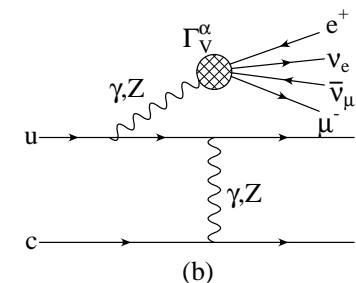
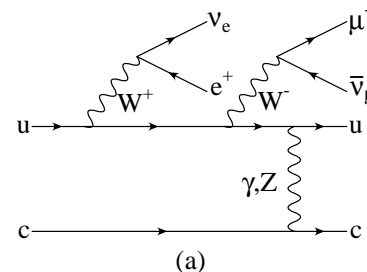
- example: WW production via VBF with leptonic decays: $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu + 2j$
- Spin correlations of the final state leptons
- All resonant and non-resonant Feynman diagrams included
- NC \Rightarrow 181 Feynman diagrams at LO
- CC \Rightarrow 92 Feynman diagrams at LO

Use modular structure, e.g. leptonic tensor



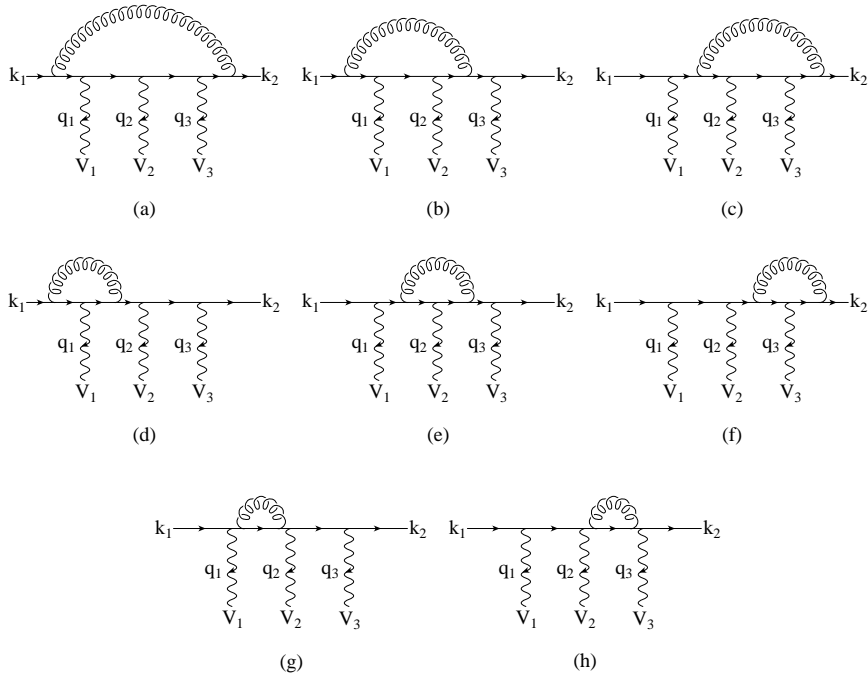
Calculate once, reuse in different processes

Speedup factor ≈ 70 compared to 2005 version of MadGraph for real emission corrections



Most complex for virtual: penline corrections

Virtual corrections involve up to pentagons



The external vector bosons correspond to $V \rightarrow l_1 \bar{l}_2$ decay currents or quark currents

The sum of all QCD corrections to a single quark line is simple

$$\mathcal{M}_V^{(i)} = \mathcal{M}_B^{(i)} \frac{\alpha_s(\mu_R)}{4\pi} C_F \left(\frac{4\pi\mu_R^2}{Q^2} \right)^\epsilon \Gamma(1+\epsilon) \left[-\frac{2}{\epsilon^2} - \frac{3}{\epsilon} + c_{\text{virt}} \right] + \widetilde{\mathcal{M}}_{V_1 V_2 V_3, \tau}^{(i)}(q_1, q_2, q_3) + \mathcal{O}(\epsilon)$$

- Divergent pieces sum to Born amplitude: canceled via Catani Seymour algorithm
- Use amplitude techniques to calculate finite remainder of virtual amplitudes

Pentagon tensor reduction with Denner-Dittmaier is stable at 0.1% level

Some Phenomenology

Study LHC cross sections within typical VBF cuts

- Identify two or more jets with k_T -algorithm ($D = 0.8$)

$$p_{Tj} \geq 20 \text{ GeV}, \quad |y_j| \leq 4.5$$

- Identify two highest p_T jets as tagging jets with wide rapidity separation and large dijet invariant mass

$$\Delta y_{jj} = |y_{j1} - y_{j2}| > 4, \quad M_{jj} > 600 \text{ GeV}$$

- Charged decay leptons ($\ell = e, \mu$) of W and/or Z must satisfy

$$\begin{aligned} p_{T\ell} &\geq 20 \text{ GeV}, & |\eta_\ell| &\leq 2.5, & \Delta R_{j\ell} &\geq 0.4, \\ m_{\ell\ell} &\geq 15 \text{ GeV}, & \Delta R_{\ell\ell} &\geq 0.2 \end{aligned}$$

and leptons must lie between the tagging jets

$$y_{j,min} < \eta_\ell < y_{j,max}$$

For scale dependence studies we have considered

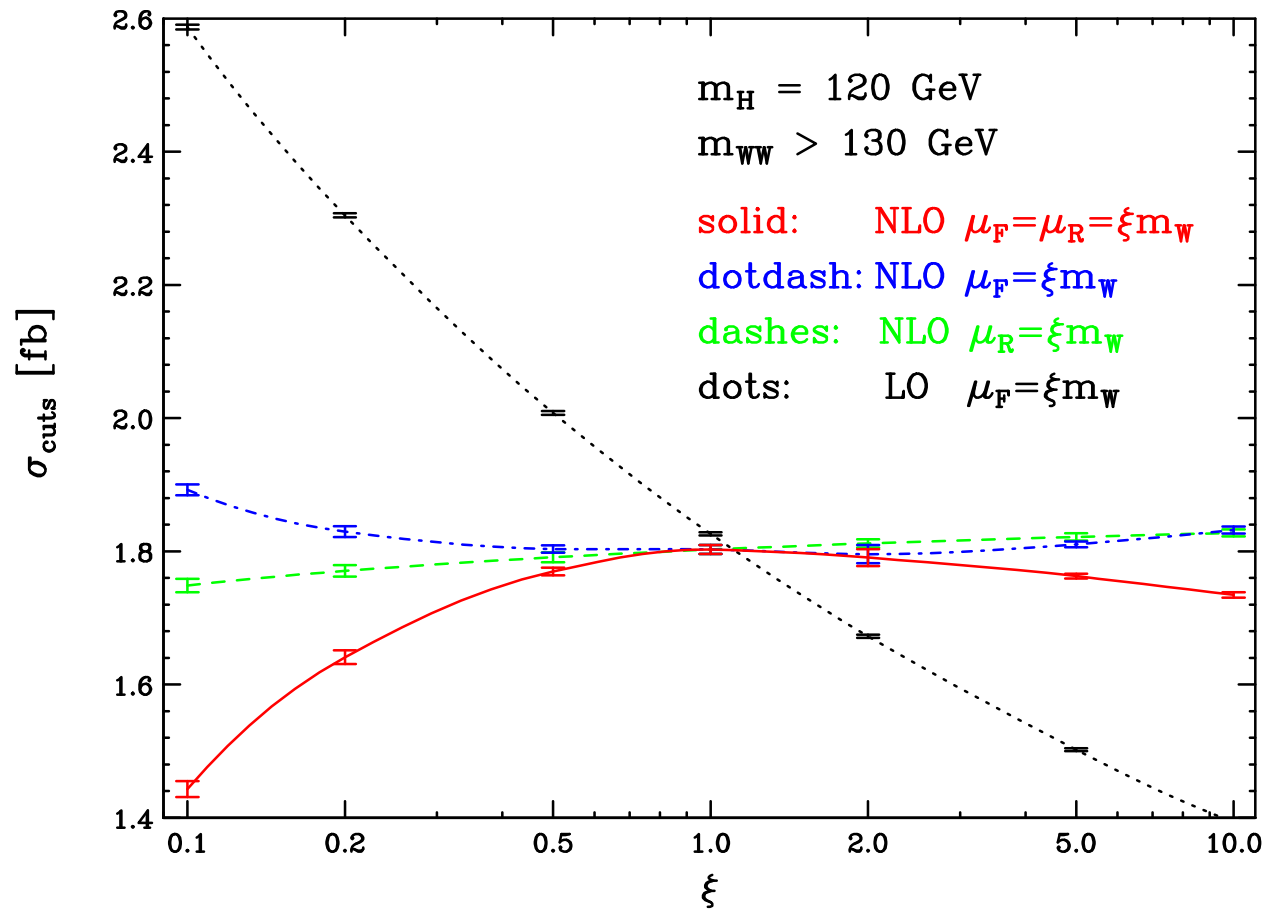
$$\mu = \xi m_V \quad \text{fixed scale}$$

$$\mu = \xi Q_i \quad \text{weak boson virtuality : } Q_i^2 = 2k_{q1} \cdot k_{q2}$$

WW production: $pp \rightarrow jje^+ \nu_e \mu^- \bar{\nu}_\mu X$ @ LHC

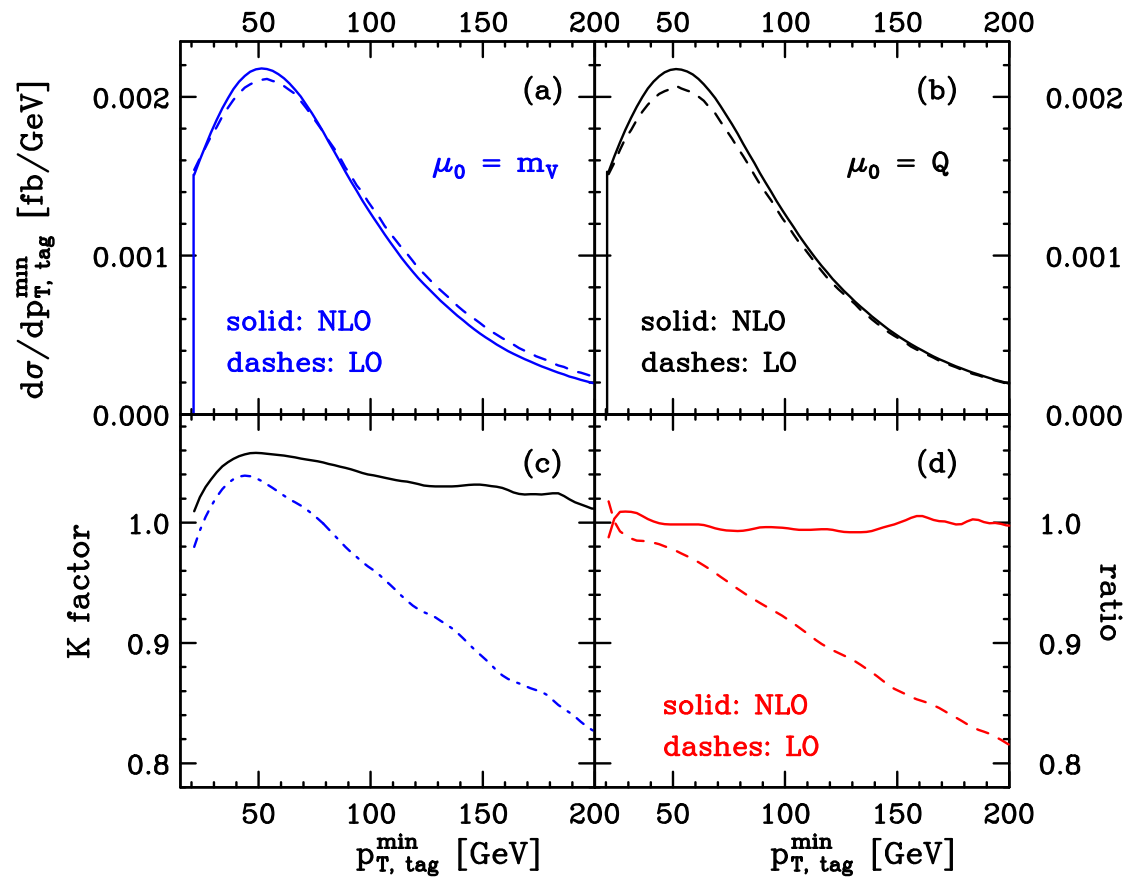
Stabilization of scale dependence at NLO

Jäger, Oleari, DZ hep-ph/0603177



WZ production in VBF, $WZ \rightarrow e^+ \nu_e \mu^+ \mu^-$

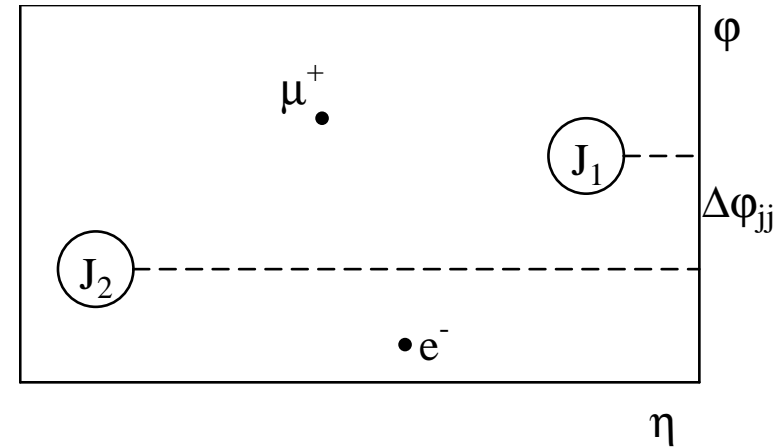
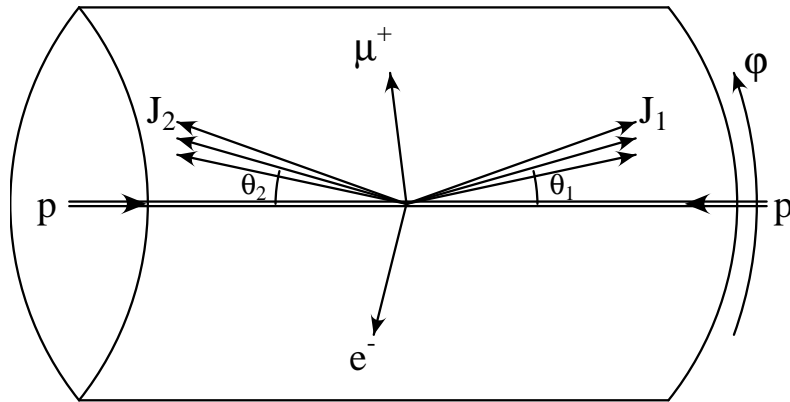
Transverse momentum distribution of the softer tagging jet



- Shape comparison LO vs. NLO depends on scale
- Scale choice $\mu = Q$ produces approximately constant K -factor
- Ratio of NLO curves for different scales is unity to better than 2%: scale choice matters very little at NLO

Use $\mu_F = Q$ at LO to best approximate the NLO results

VBF signature



Characteristics:

- energetic jets in the **forward** and **backward** directions ($p_T > 20$ GeV)
- large **rapidity separation** and large **invariant mass** of the two tagging jets
- **Higgs decay products between** tagging jets
- Little gluon radiation in the central-rapidity region, due to **colorless** W/Z exchange (**central jet veto**: no extra jets with $p_T > 20$ GeV between tagging jets)

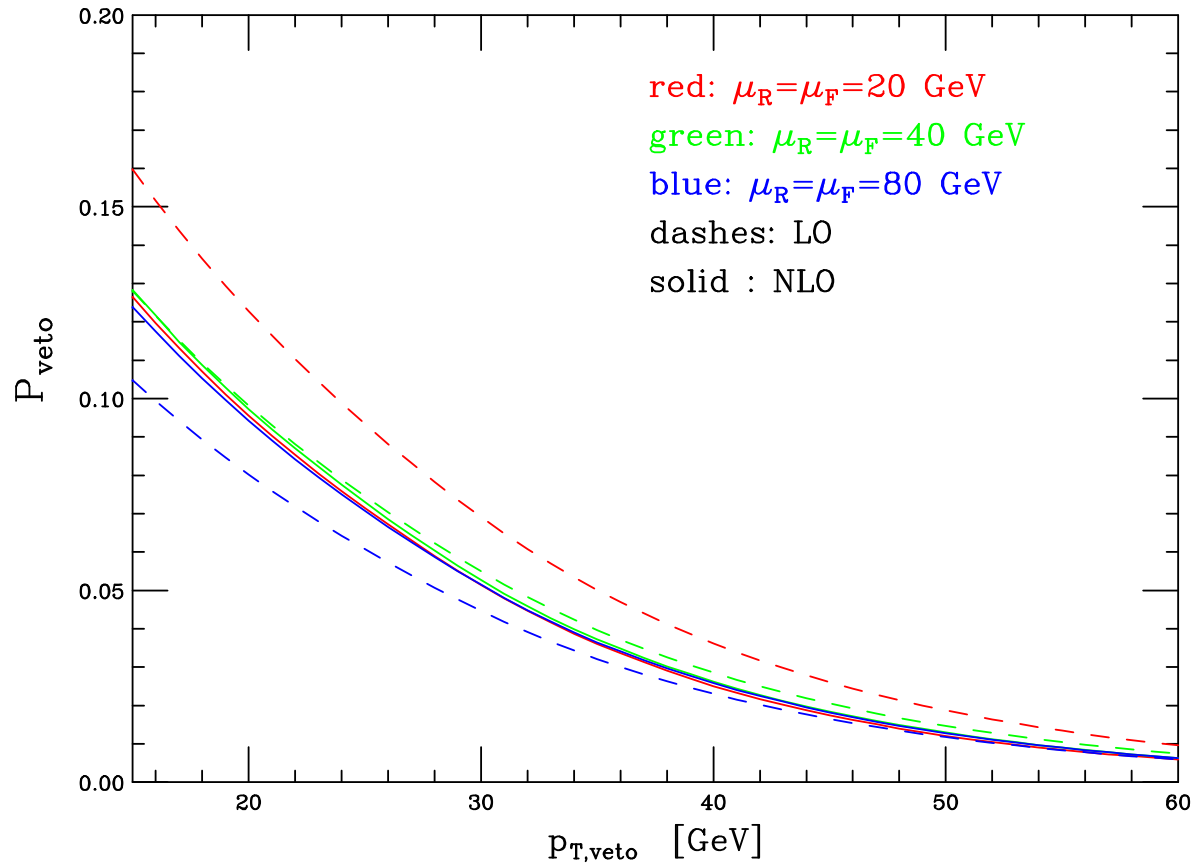
VBF $hjjj$ production and NLO corrections

- Born: 3 final state partons + Higgs via VBF

$$\begin{aligned}
 \mathcal{M}_B = & \delta_{i_2 i_b} t_{i_1 i_a}^{a_3} \left[\begin{array}{c} \mathcal{M}_{B,1a} : \end{array} \right. \\
 & \left. \begin{array}{c} \mathcal{M}_{B,2b} : \end{array} \right] \\
 & + \delta_{i_1 i_a} t_{i_2 i_b}^{a_3} \left[\begin{array}{c} \mathcal{M}_{B,1a} : \end{array} \right. \\
 & \left. \mathcal{M}_{B,2b} : \end{array} \right]
 \end{aligned}$$

- Catani, Seymour subtraction method
- Real: 4 final state partons + Higgs via VBF
- Virtual: Two classes of gauge invariant subsets
 - Box + Vertex + Propagator
 - Pentagon + Hexagon **are small and can be neglected**
(consistent with full NLO calculation by Campanario, Figy, Plätzer, Sjö Dahl)

Veto Probability for the VBF Signal



$$P_{\text{veto}} = \frac{1}{\sigma_2^{\text{NLO}}} \int_{p_{T,\text{veto}}}^{\infty} dp_{Tj}^{\text{veto}} \frac{d\sigma_3}{dp_{Tj}^{\text{veto}}}$$

Scale variations, $p_{T,\text{veto}} = 15$ GeV:

- LO: +33% to -17%
- NLO: -1.4% to -3.4%

Reliable prediction for **perturbative** part of veto probability at NLO

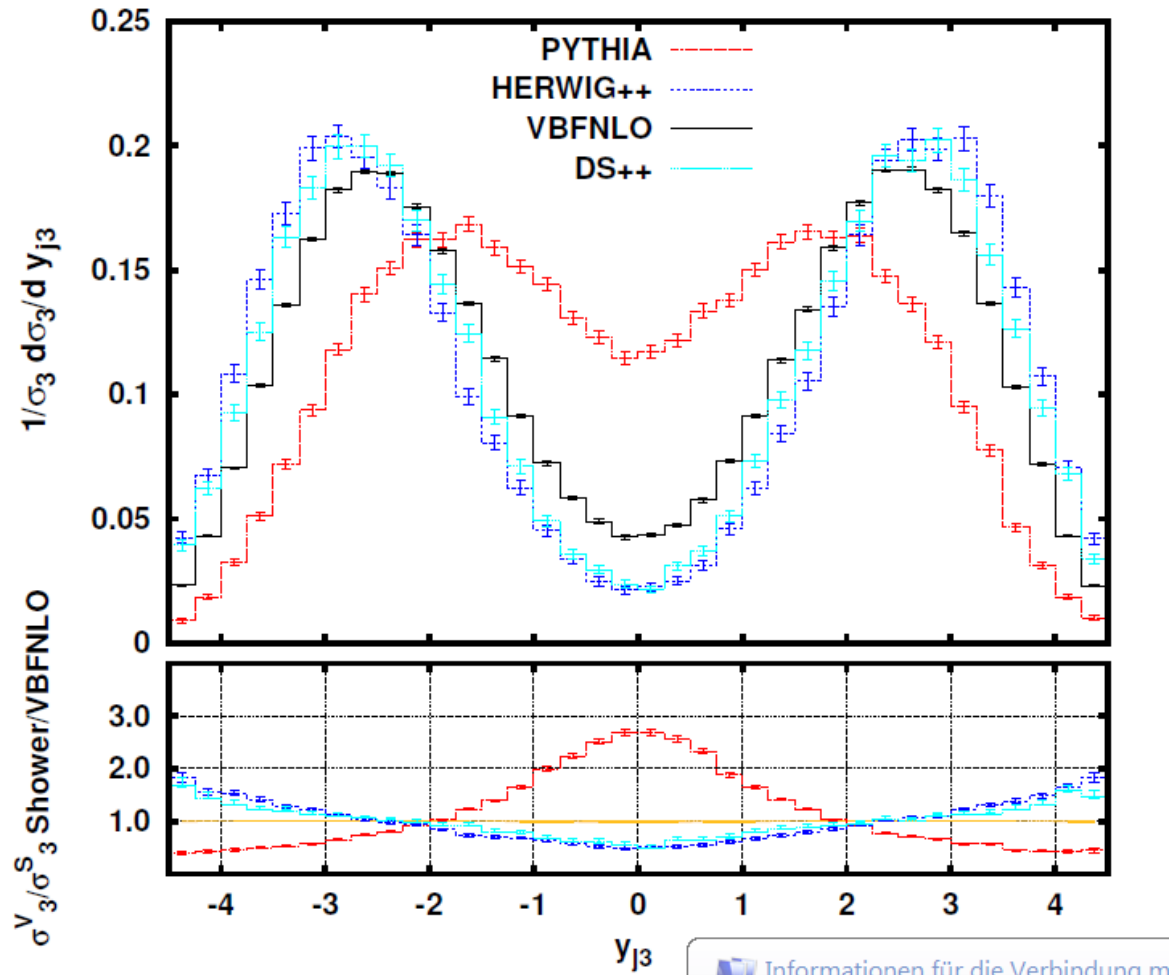
Veto jets beyond fixed order

Interface of NLO calculations with Herwig and PYTHIA via Powheg Box has been implemented by Franziska Schissler

- How well can “veto jets” be modeled directly by parton shower approach?
- Differences between basic shower models
(PYTHIA vs. default Herwig shower vs. dipole shower)
- Improvements when adding true NLO corrections

Veto jet distribution: LO $qq \rightarrow qqh$ matrix elements

Schissler thesis, 2014



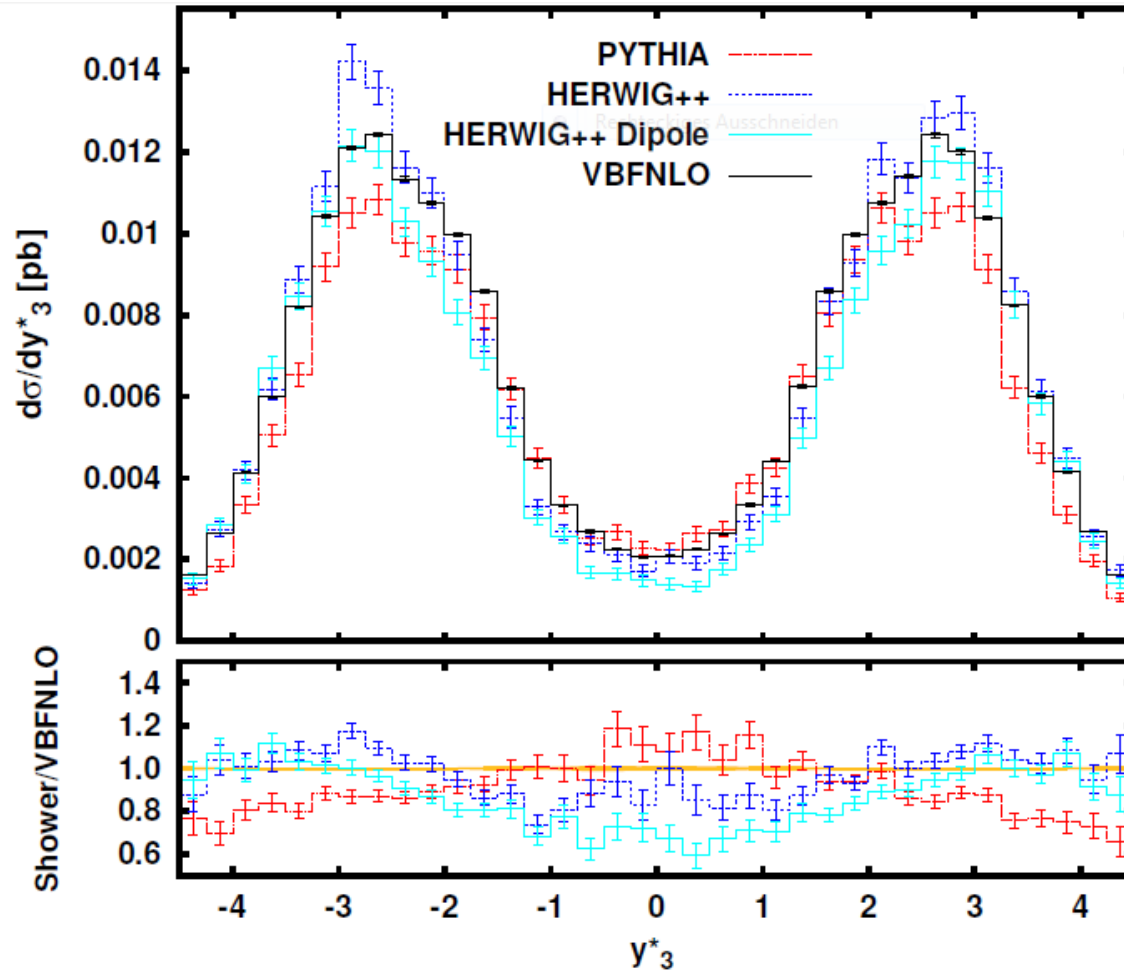
Pure parton-shower generation of central jets does not produce reliable results

Collinear approximation inherent in PS approach is not valid in veto region for VBF events

Extra parton must be included in hard matrix element

Veto jet distribution: VBF $Wjjj$ production at LO

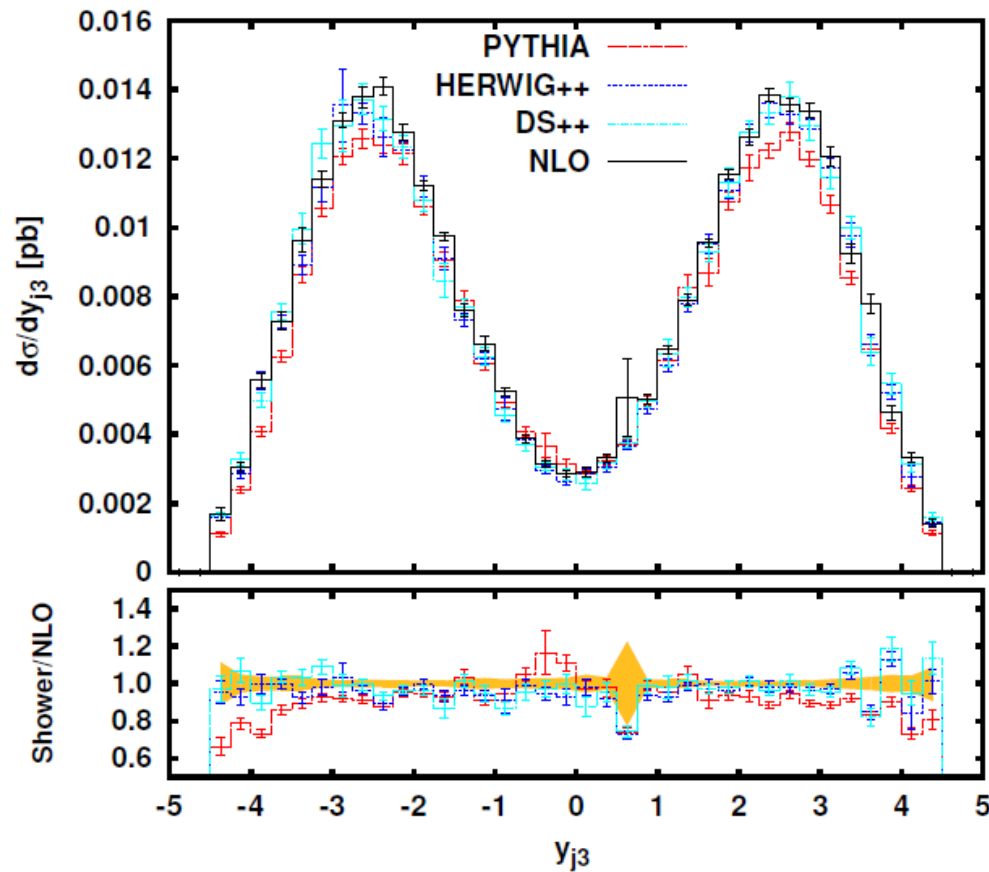
Schissler,DZ arXiv:1302.2884



Inclusion of third parton at ME level produces reasonable agreement between NLO Vjj calculations and parton shower programs

Veto jet distribution: VBF $hjjj$ production at NLO

Jäger, Schissler, DZ arXiv:1405.6950

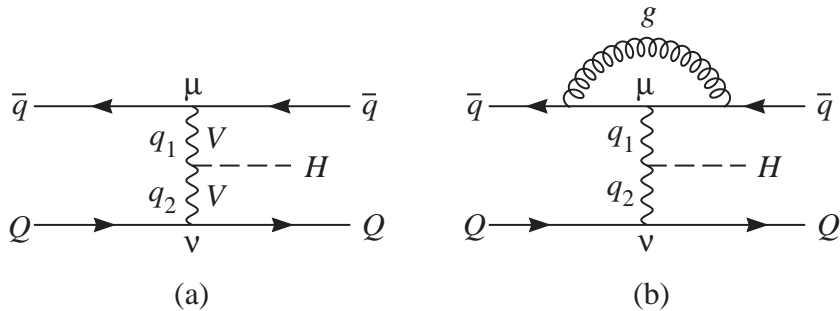


Further improvement with NLO $hjjj$ calculation matched to PS programs

Reliable simulation of veto jet candidates is possible but requires matrix elements with sufficiently high parton multiplicity

Tensor structure of the HVV coupling

Most general HVV vertex $T^{\mu\nu}(q_1, q_2)$



Physical interpretation of terms:

SM Higgs $\mathcal{L}_I \sim HV_\mu V^\mu \longrightarrow a_1$

loop induced couplings for neutral scalar

CP even $\mathcal{L}_{eff} \sim HV_{\mu\nu} V^{\mu\nu} \longrightarrow a_2$

CP odd $\mathcal{L}_{eff} \sim HV_{\mu\nu} \tilde{V}^{\mu\nu} \longrightarrow a_3$

Must distinguish a_1, a_2, a_3 experimentally

$$T^{\mu\nu} = a_1 g^{\mu\nu} + a_2 (q_1 \cdot q_2 g^{\mu\nu} - q_1^\nu q_2^\mu) + a_3 \varepsilon^{\mu\nu\rho\sigma} q_{1\rho} q_{2\sigma}$$

The $a_i = a_i(q_1, q_2)$ are scalar form factors

Connection to effective Lagrangian

We need model of the underlying UV physics to determine the form factors $a_i(q_1, q_2)$

Approximate its low-energy effects by an effective Lagrangian

$$\mathcal{L}_{\text{eff}} = \frac{f_{WW}}{\Lambda^2} \phi^\dagger \hat{W}_{\mu\nu} \hat{W}^{\mu\nu} \phi + \frac{f_\phi}{\Lambda^2} \left(\phi^\dagger \phi - \frac{v^2}{2} \right) (D_\mu \phi)^\dagger D^\mu \phi + \dots + \sum_i \frac{f_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$

Gives leading terms for form factors, e.g. for hWW coupling

$$a_1 = \frac{2m_W^2}{v} \left(1 + \frac{f_\phi}{\Lambda^2} \frac{v^2}{2} \right) + \sum_i c_i^{(1)} \frac{f_i^{(8)}}{\Lambda^4} v^2 q^2 + \dots$$

$$a_2 = c^{(2)} \frac{f_{WW}}{\Lambda^2} v + \sum_i c_i^{(2)} \frac{f_i^{(8)}}{\Lambda^4} v q^2 + \dots$$

$$a_3 = c^{(3)} \frac{\tilde{f}_{WW}}{\Lambda^2} v + \sum_i c_i^{(3)} \frac{\tilde{f}_i^{(8)}}{\Lambda^4} v q^2 + \dots$$

Describe same physics (for a particular vertex) by taking some minimal set of effective Lagrangian coefficients f_i as form factors

Implementation in VBFNLO

Start from effective Lagrangians (set PARAMETR1=.true. in anom_HVV.dat)

$$\begin{aligned} \mathcal{L} = & \frac{g_{5e}^{HZZ}}{2\Lambda_5} H Z_{\mu\nu} Z^{\mu\nu} + \frac{g_{5o}^{HZZ}}{2\Lambda_5} H \tilde{Z}_{\mu\nu} Z^{\mu\nu} + \frac{g_{5e}^{HWW}}{\Lambda_5} H W_{\mu\nu}^+ W^{\mu\nu}_- + \frac{g_{5o}^{HWW}}{\Lambda_5} H \tilde{W}_{\mu\nu}^+ W^{\mu\nu}_- + \\ & \frac{g_{5e}^{HZ\gamma}}{\Lambda_5} H Z_{\mu\nu} A^{\mu\nu} + \frac{g_{5o}^{HZ\gamma}}{\Lambda_5} H \tilde{Z}_{\mu\nu} A^{\mu\nu} + \frac{g_{5e}^{H\gamma\gamma}}{2\Lambda_5} H A_{\mu\nu} A^{\mu\nu} + \frac{g_{5o}^{H\gamma\gamma}}{2\Lambda_5} H \tilde{A}_{\mu\nu} A^{\mu\nu} \end{aligned}$$

or , alternatively, (set PARAMETR3=.true. in anom_HVV.dat)

$$\mathcal{L}_{\text{eff}} = \frac{f_{WW}}{\Lambda_6^2} \phi^\dagger \hat{W}_{\mu\nu} \hat{W}^{\mu\nu} \phi + \frac{f_{BB}}{\Lambda_6^2} \phi^\dagger \hat{B}_{\mu\nu} \hat{B}^{\mu\nu} \phi + \text{CP-odd part} + \dots$$

see VBFNLO manual for details on how to set the anomalous coupling choices

Remember to choose form factors in anom_HVV.dat

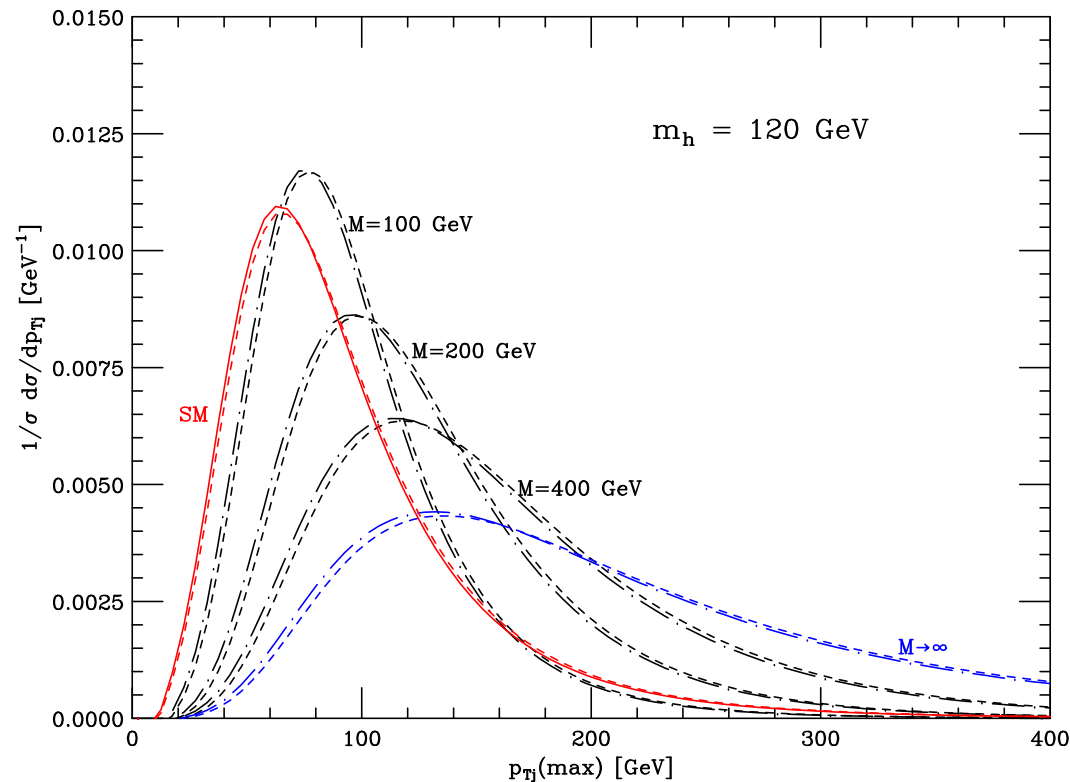
$$F_1 = \frac{M^2}{q_1^2 - M^2} \frac{M^2}{q_2^2 - M^2} \quad \text{or} \quad F_2 = -2 M^2 C_0(q_1^2, q_2^2, (q_1 + q_2)^2, M^2)$$

- Anomalous couplings implemented in VBFNLO for VBF, for WH , WHj and other production processes

$qq \rightarrow qqH$: jet transverse momentum

Form factors affect momentum transfer and thus jet transverse momenta (Here: a_2 only)

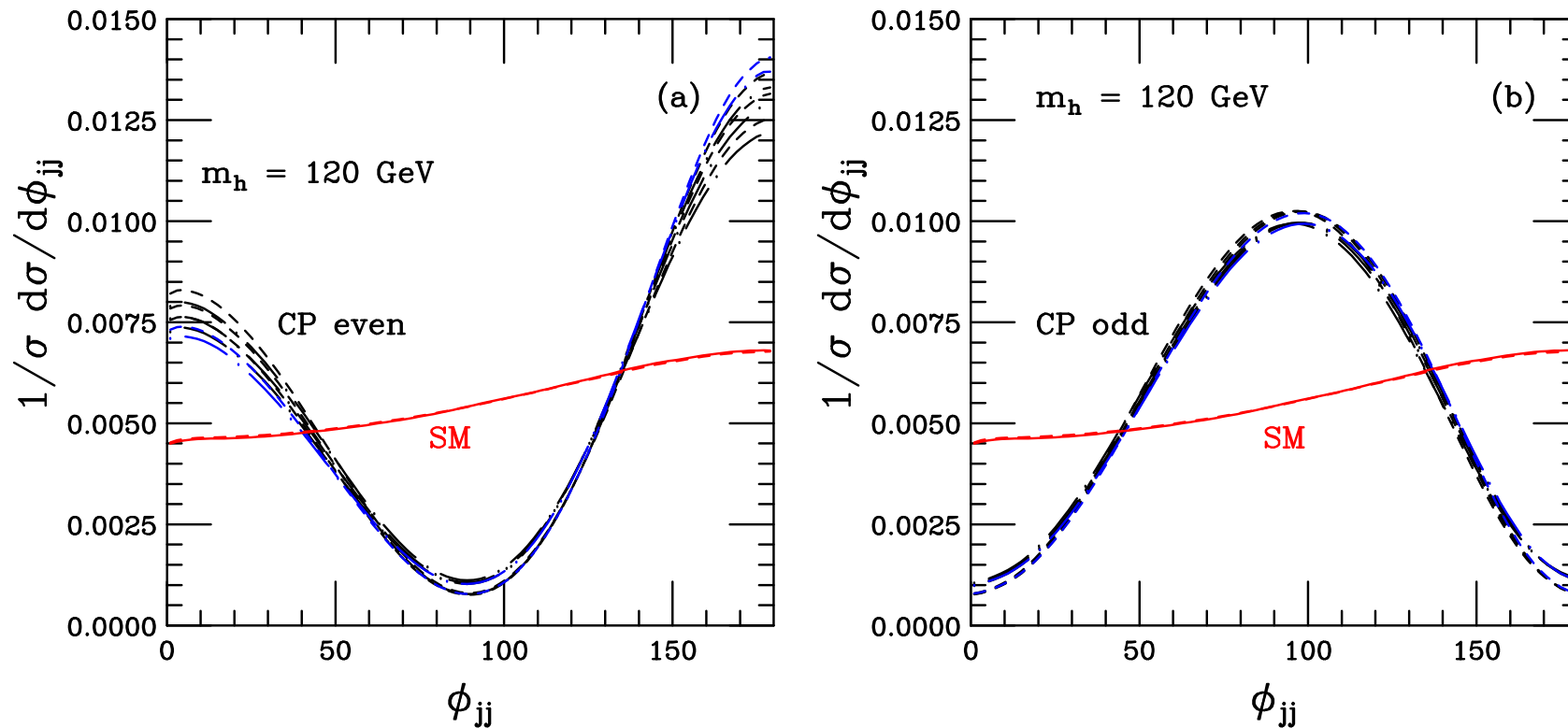
Figy, DZ hep-ph/0403297



- Change in tagging jet p_T distributions is sensitive indicator of anomalous couplings
- Can choose form-factor such as to approximate SM p_T distributions of the two tagging jets

Azimuthal angle correlations

Tell-tale signal for non-SM coupling is azimuthal angle between tagging jets



Dip structure at 90° (CP even) or $0/180^\circ$ (CP odd) only depends on tensor structure of hVV vertex. Very little dependence on form factor, LO vs. NLO, Higgs mass etc.

Same physics in decay plane correlations for $h \rightarrow ZZ^* \rightarrow 4\text{ leptons}$

Some extensions in 2014 and 2015 updates of VBFNLO

Additional NLO QCD corrected processes

- $W\gamma jj$ production from VBF and order $\alpha^2\alpha_s^3$ QCD sources
- $Z\gamma jj$ production from VBF and order $\alpha^2\alpha_s^3$ QCD sources
- Same sign QCD $WWjj$ production
- WH and WHj associated production (with anomalous couplings)
- Inclusion of hadronic decay of one W or Z for all VVV triple vector boson production and $VVjj$ vector boson scattering processes

Hadronic decay simulated at LO only, but K factor is $1 + \alpha_s/\pi \approx 1.04$

Code is stable when one jet only is produced from Z, γ^* decay

- Anomalous couplings for $VV \rightarrow VV$ scattering processes.
- BLHA interface of VBS processes with parton shower in VBFNLO 3.0.0 β

Vector boson scattering

The $m_h = 125$ GeV Higgs will unitarize $VV \rightarrow VV$ scattering **provided** it has SM hVV couplings

\Rightarrow Check this by either

- precise measurements of the hVV couplings at the light Higgs resonance
- measurement of $VV \rightarrow VV$ differential cross sections at high p_T and invariant mass

Full $qq \rightarrow qqVV$ with VV leptonic and semileptonic decay is implemented in VBFNLO with NLO QCD corrections and large set of dimension 6 and 8 terms in the effective Lagrangian

Going beyond dimension 6

Reason for dimension 8 operators like

$$\begin{aligned}\mathcal{L}_{S,0} &= \left[(D_\mu \Phi)^\dagger D_\nu \Phi \right] \times \left[(D^\mu \Phi)^\dagger D^\nu \Phi \right] \\ \mathcal{L}_{M,1} &= \text{Tr} \left[\hat{W}_{\mu\nu} \hat{W}^{\nu\beta} \right] \times \left[(D_\beta \Phi)^\dagger D^\mu \Phi \right] \\ \mathcal{L}_{T,1} &= \text{Tr} \left[\hat{W}_{\alpha\nu} \hat{W}^{\mu\beta} \right] \times \text{Tr} \left[\hat{W}_{\mu\beta} \hat{W}^{\alpha\nu} \right]\end{aligned}$$

- Dimension 6 operators only do not allow to parameterize $VVVV$ vertex with arbitrary helicities of the four gauge bosons

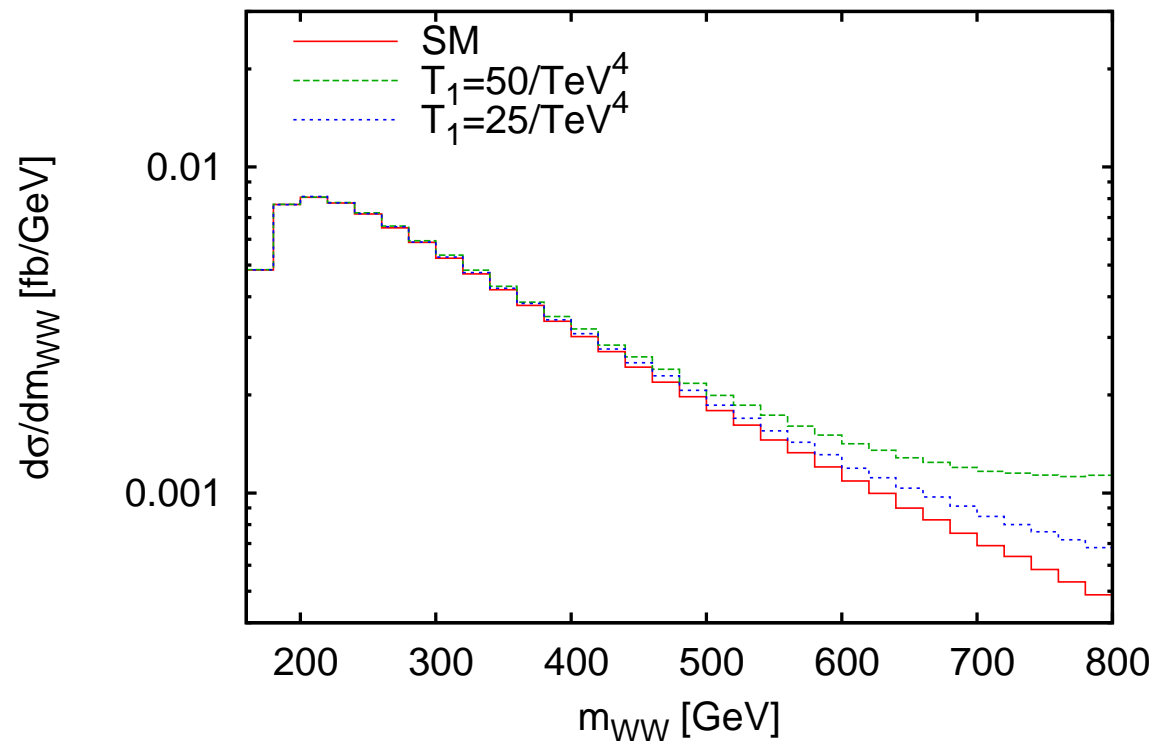
For example: $\mathcal{L}_{S,0}$ is needed to describe $V_L V_L \rightarrow V_L V_L$ scattering

- New physics may appear at 1-loop level for dimension 6 operators but at tree level for some dimension 8 operators

$VV \rightarrow W^+ W^-$ with dimension 8 operators

Effect of $\mathcal{L}_{eff} = \frac{f_{M,1}}{\Lambda^4} \text{Tr} [\hat{W}_{\alpha\gamma} \hat{W}^{\mu\beta}] \times \text{Tr} [\hat{W}_{\mu\beta} \hat{W}^{\alpha\gamma}]$

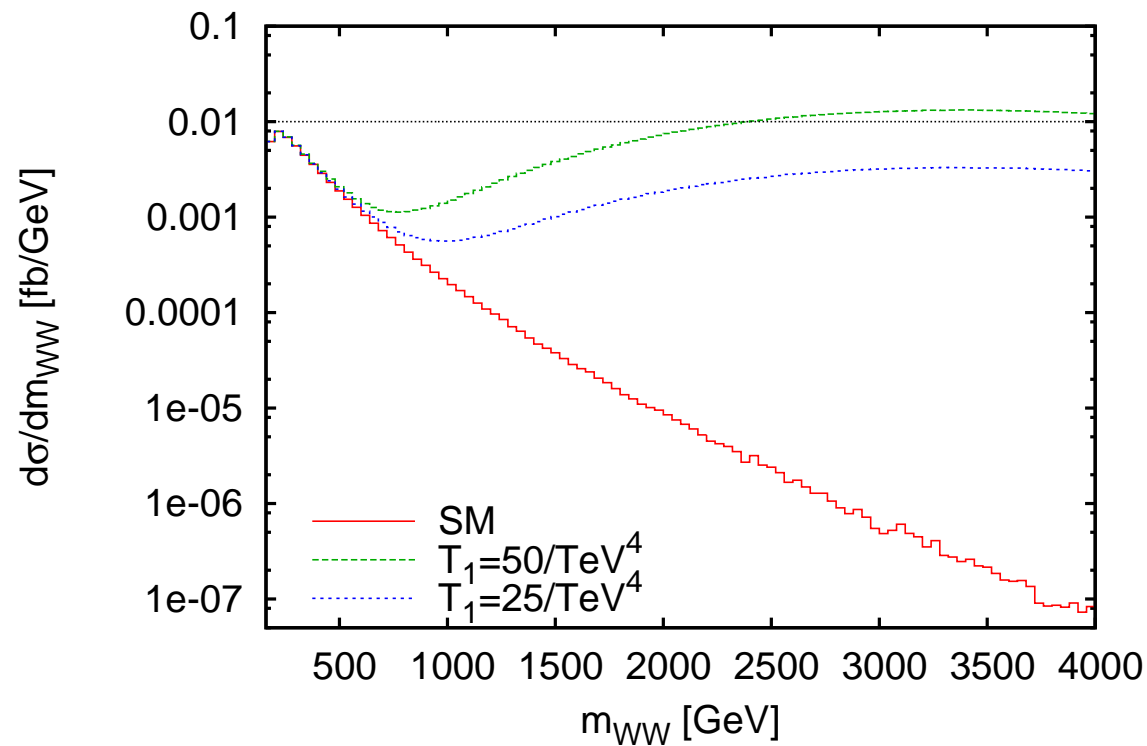
with $T_1 = \frac{f_{M,1}}{\Lambda^4}$ constant on $pp \rightarrow W^+ W^- jj \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu jj$



- Small increase in cross section at high WW invariant mass??

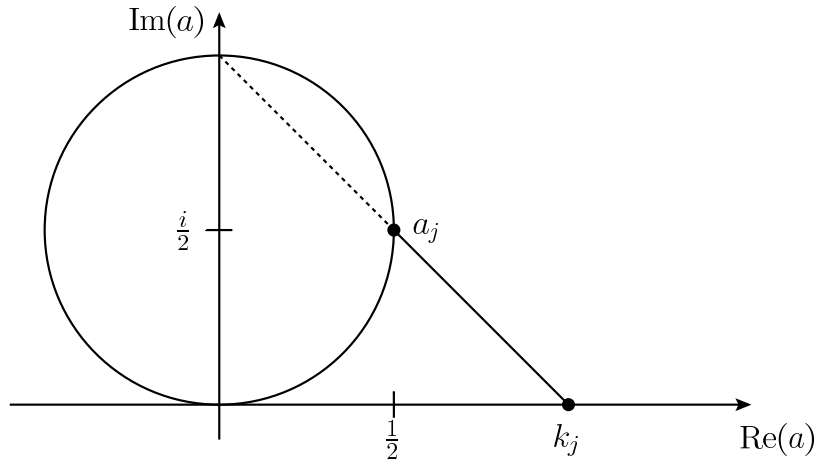
$VV \rightarrow W^+ W^-$ with dimension 8 operators

Effect of constant $T_1 = \frac{f_{M,1}}{\Lambda^4}$ on $pp \rightarrow W^+ W^- jj \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu jj$



- Huge increase in cross section at high m_{WW} is completely unphysical
 - Need form factor for analysis or some other unitarization procedure
- K-matrix unitarization for $V_L V_L \rightarrow V_L V_L$ scattering in VBFNLO 3.0.0 β (Max Löschner)

K matrix unitarization

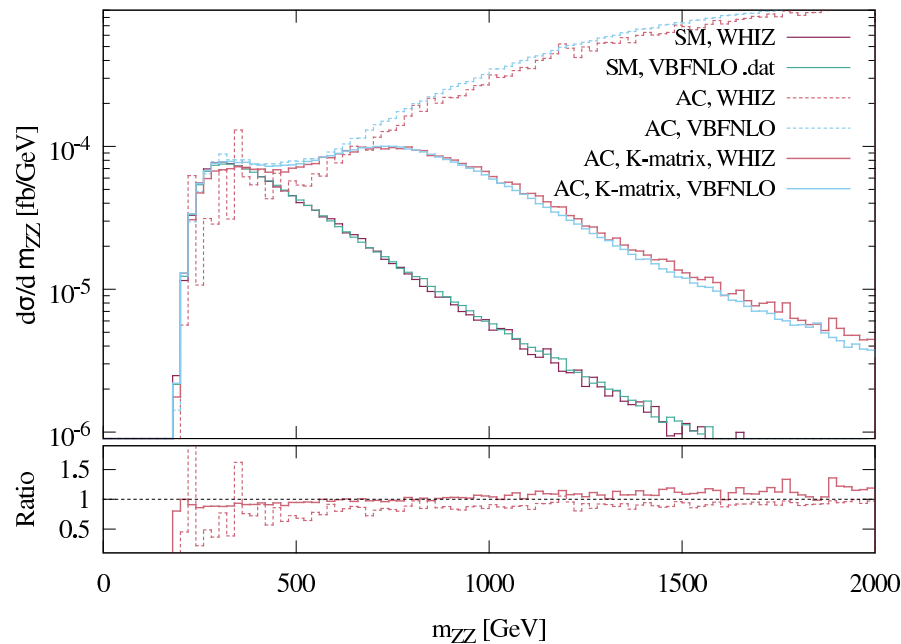


Project amplitude k_j , which exceeds (tree-level) unitarity, back onto Argand circle
 → K matrix unitarized amplitude a_j

[VBFNLO implementation: Löschner, Perez;

following: Alboteanu, Kilian, Reuter]

Comparison with Whizard, which has this method already implemented: [Kilian, Ohl, Reuter, Sekulla, et al.]



Example: VBF-ZZ ($e^+e^- \mu^+ \mu^-$)

good agreement between both codes
 for longitudinal ops. at LO

→ can now generate distributions
 also at NLO via VBFNLO

Extension to mixed and transverse operators not straight-forward

→ work ongoing

BLHA Interface

Interface NLO program with parton-shower MC
well-defined standard: Binoth Les Houches Accord (BLHA)

[Arnold, Plätzer, Rauch et al.]

Motivation: Combine advantages of NLO calculations and parton shower

NLO calculation

Parton shower

- | | |
|--|--------------------------------------|
| • normalization correct to NLO | • Sudakov suppression at small p_T |
| • additional jet at high- p_T accurately described | • events at hadron level possible |
| • theoretical uncertainty reduced | |

⇒ Interface VBFNLO with parton shower → BLHA interface

(work by Michael Rauch)

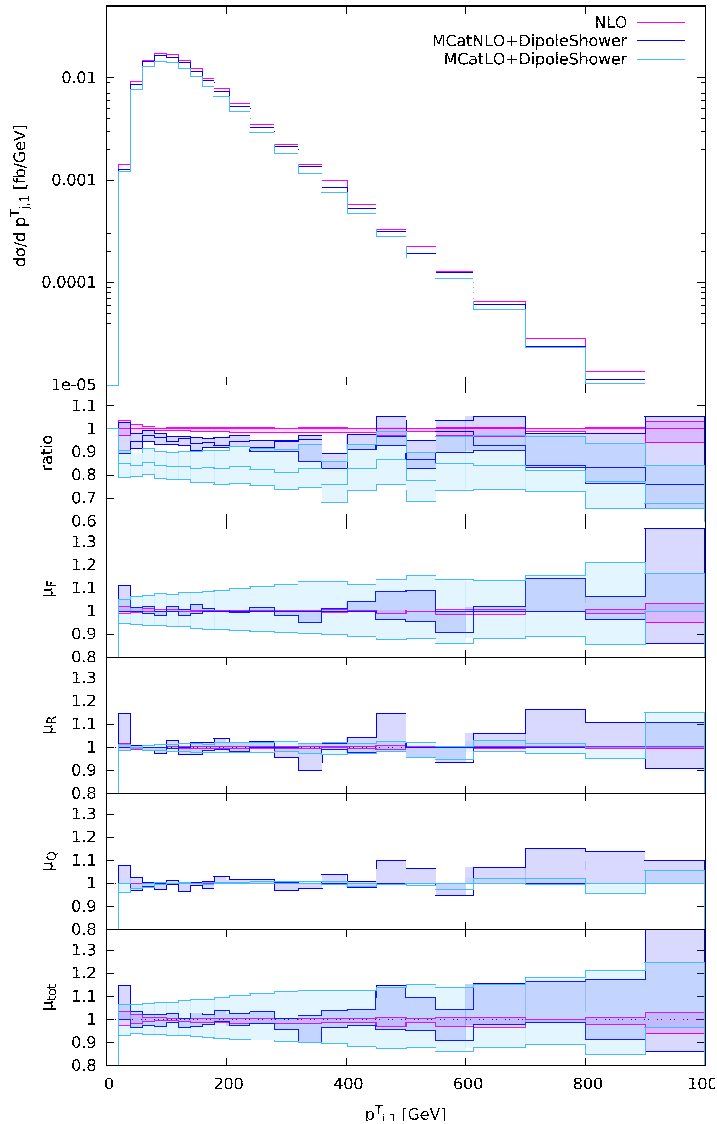
→ First tests: Herwig 7 package Matchbox as MC program

[Gieseke, Plätzer]

Two parton showers: angular-ordered and Catani-Seymour dipoles

Matching methods: MC@NLO and POWHEG

VBF- W^+W^- + parton shower



For $p_{T,j1}$, comparison of:

- pure NLO
- NLO+PS (MC@NLO+dipole shower)
- LO+PS (dipole shower)

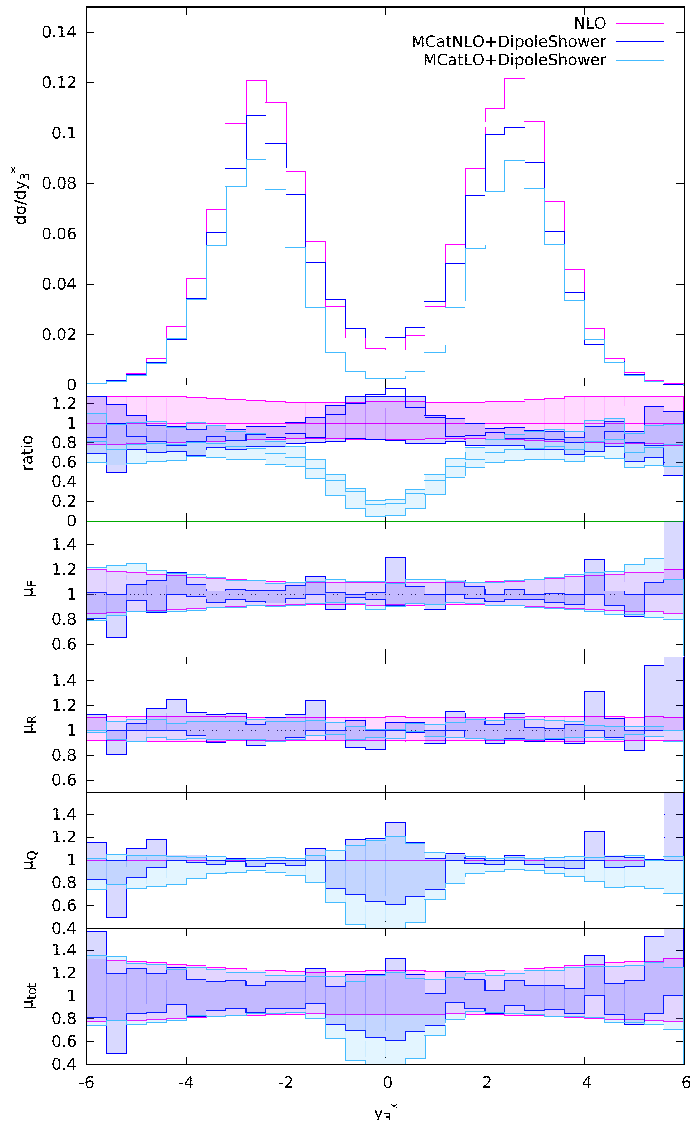
Panels:

- differential c.s.
- ratio of c.s. and total scale variation ($\mu_0 = p_{T,j1}^T$)
- individual variation of μ_F, μ_R, μ_Q (shower scale)
- total variation $\mu_i/\mu_0 \in [\frac{1}{2}; 2]$

Inclusion of parton shower:

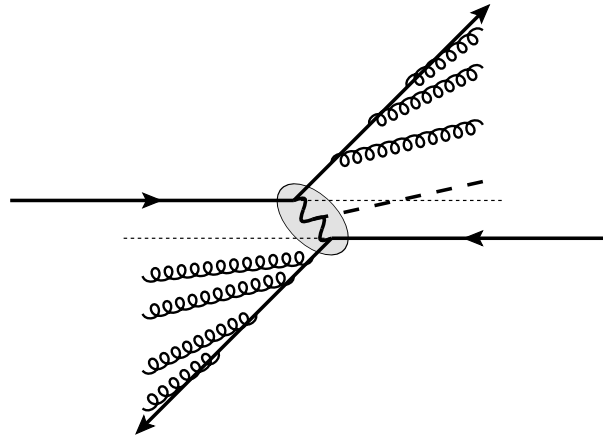
- smaller c.s. (additional splittings)
- larger uncertainties (add. shower scale)

VBF- W^+W^- + parton shower



$$y_3^* = y_3 - \frac{y_1 + y_2}{2}$$

- almost no radiation generated in central region by LO+PS
- additional radiation by shower created mainly between jets and beam axis (color connections)



- \rightarrow central region corrected at NLO by LO W^+W^-jjj ME
- dipole shower “interpolates” between NLO behavior in central region and shower behavior at small angles

NLO Event Output

Additional features:

- events at NLO

```
HepMC::Version 2.06.08
HepMC::IO_GenEvent-START_EVENT_LISTING
E 1 -1 1.0000000000000000e+02 1.1426144356896106e-01 8.0545791941901580e-03 0 -1 5 10003 10006 0 1 9.6574119350375395e-05
N 1 "0"
U GEV MM
C 1.2003526218804084e+00 1.2429340593057579e+04
F 2 -2 1.9944966561722052e-01 5.4752809081600089e-03 1.0000000000000000e+02 4.8837107666330770e-01 7.0773553098927189e-01 0 0
V -1 0 0 0 0 0 0 2 0
P 10001 24 -4.5106124574613865e+01 2.1914561871288999e+01 4.8707785224913533e+02 4.8305712963914090e+02 -8.0096530215583300e+01 11 0 0 -5 0
[...]
```

- anomalous couplings including available unitarization schemes
- BLHA interface completely following Les Houches standard
→ also working with other MC generators (e.g. Sherpa)
↔ when using BLHA v1 with VBF processes, care needs to be taken to use the VBF approximation also in the MC generator
- other process classes will follow (e.g. QCD-VVjj)

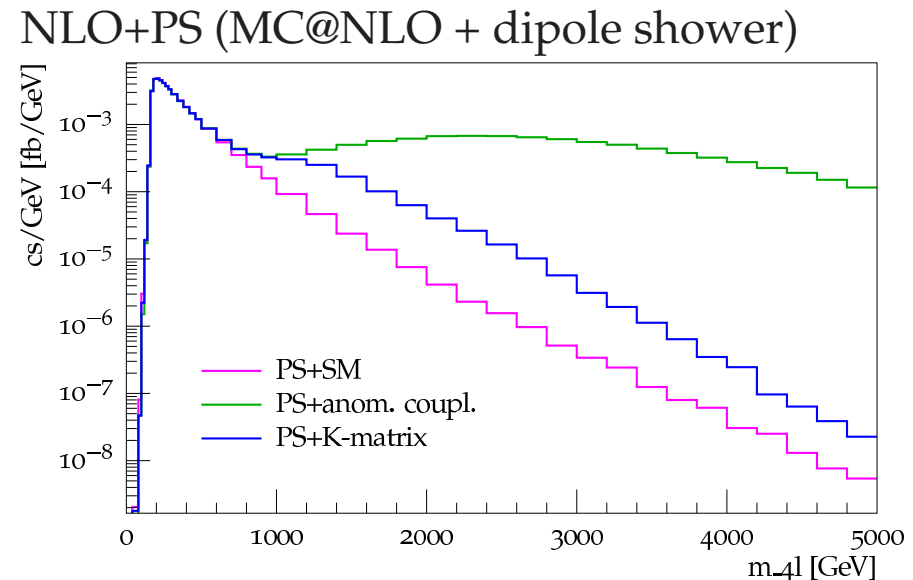
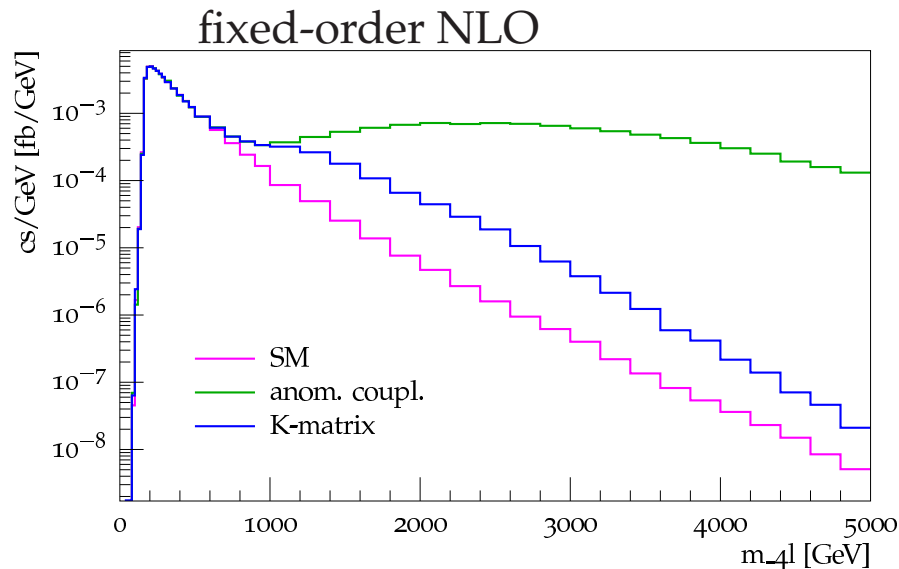
Combination with Parton Shower

Can also combine K-matrix in setup with parton shower

[VBFNLO3&Herwig7]

Example: VBF- W^+W^+ ($pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$)

anom. coupl.: $f_{S,1}/\Lambda^4 = 100 \text{ TeV}^{-4}$



No significant shape changes in $d\sigma/dm_{4\ell}$ when switching on PS

(integrated c.s. PS/NLO: -3.0% (SM) / -3.8% (K-matrix))

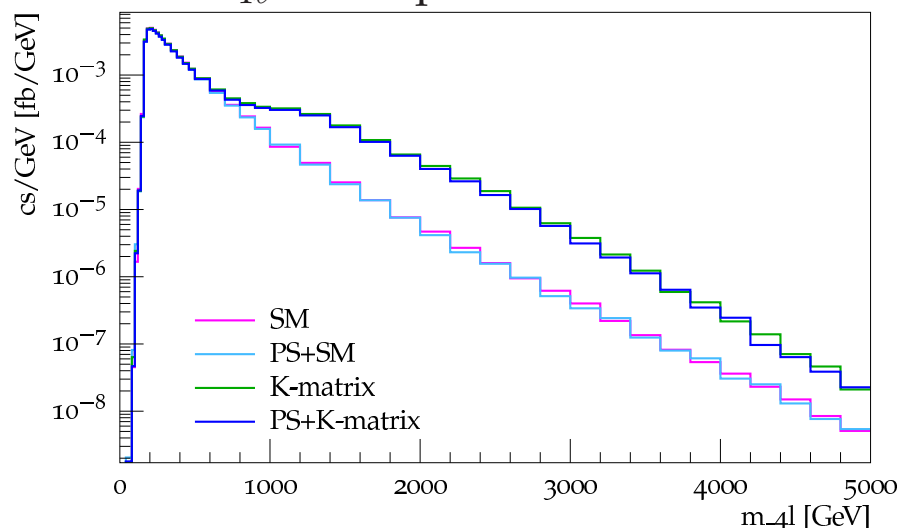
W^+W^+ : Combination with Parton Shower

Can also combine K-matrix in setup with parton shower

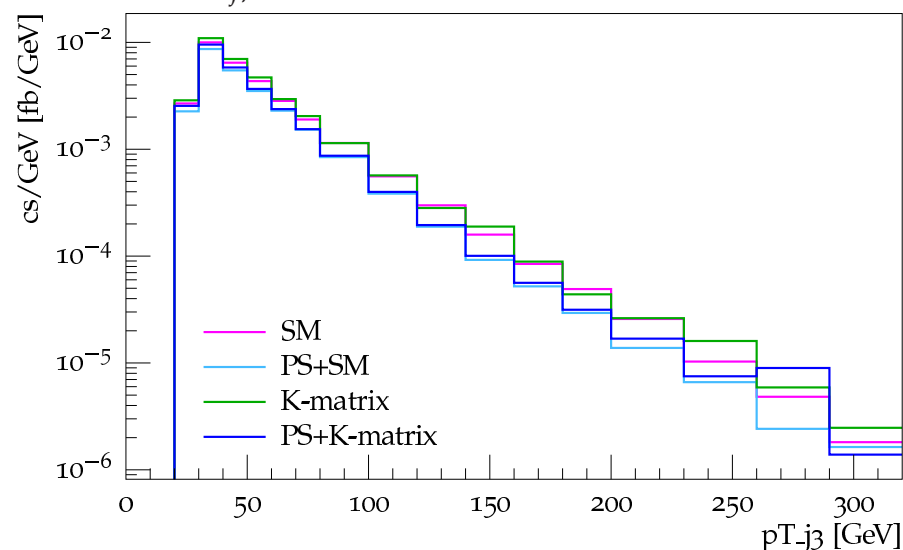
[VBFNLO3&Herwig7]

anom. coupl.: $f_{S,1}/\Lambda^4 = 100 \text{ TeV}^{-4}$

$m_{4\ell}$ – Comparison



$p_{j,3}^T$ – Comparison



No significant shape changes in $m_{4\ell}$ when switching on PS

(integrated c.s. PS/NLO: -3.0% (SM) / -3.8% (K-matrix))

$\leftrightarrow p_{j,3}^T$ more sensitive to parton-shower effects since it is LO distribution

Conclusions

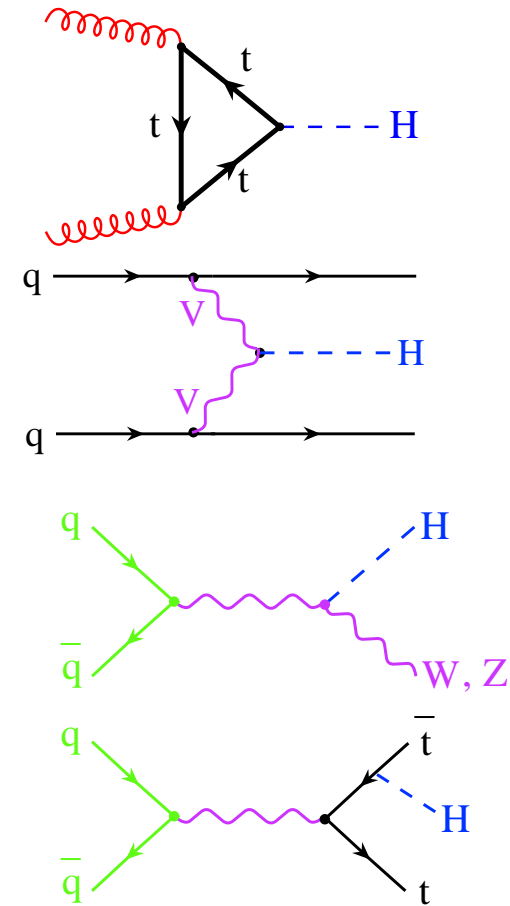
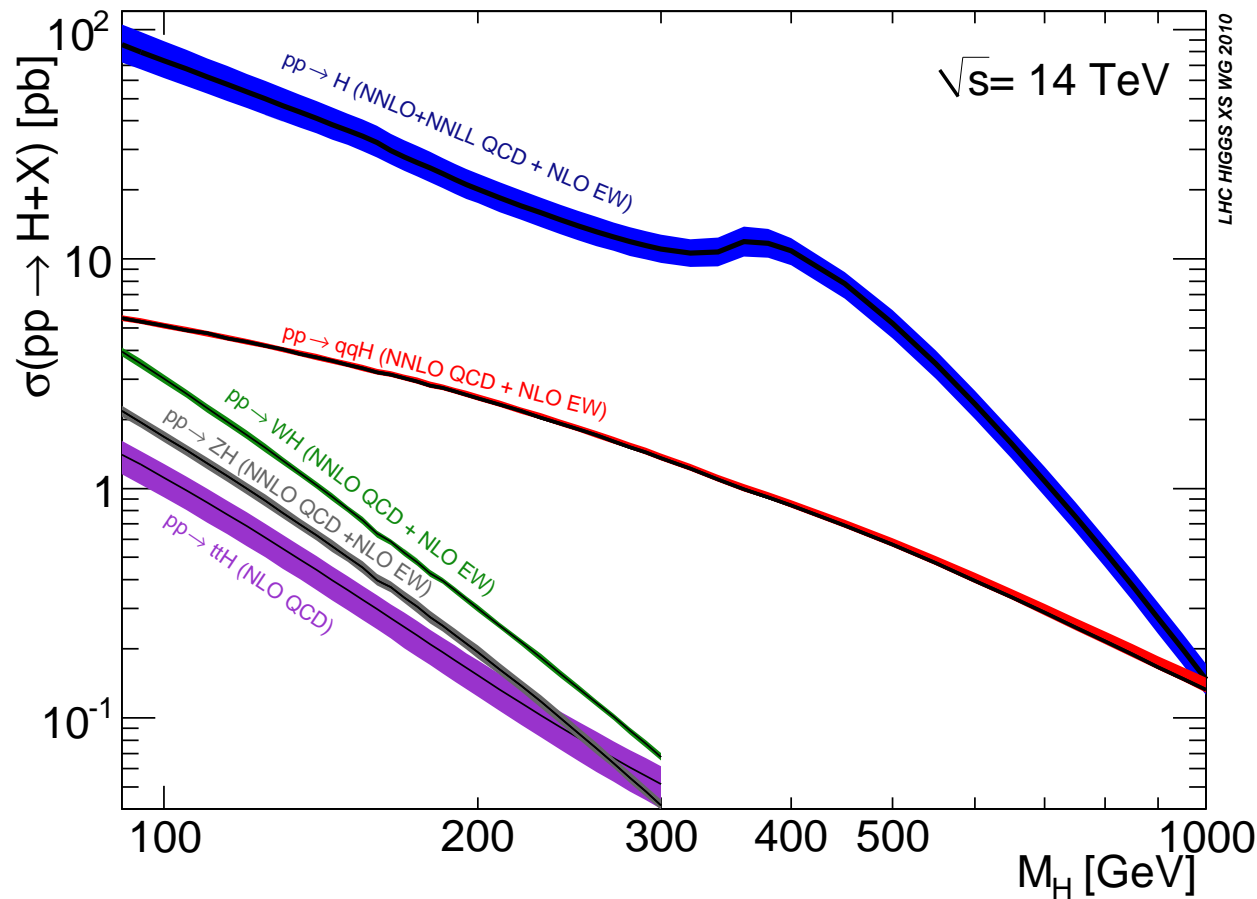
- VBF production of the light Higgs provides for important information on Higgs properties, i.e. coupling measurements. VBS at high VV invariant mass and high p_T of the weak bosons complements these measurements
- NLO QCD corrections are available for VBF and all VBS processes. VBFNLO now also provides interface to event generators for VBF/VBS.
- Model independent parameterizations of deviations from the SM are provided in VBFNLO
- Form factors or some other unitarization procedure cannot be avoided when using effective Lagrangians for VV scattering at the LHC
- NLO corrections and their implementation have been a collaborative effort!

Thanks to

V. Hankele, B. Jäger, M. Worek, S. Palmer, F. Campanario, M. Rauch, C. Oleari, K. Arnold, J. Bellm, G. Bozzi, C. Englert, B. Feigl, T. Figy, J. Frank, M. Kerner, G. Klämke, M. Kubocz, M. Löschner, G. Perez, S. Plätzer, S. Prestel, H. Rzehak, F. Schissler, M. Spannowsky, Ninh Duc Le, R. Roth, N. Kaiser, O. Schlimpert

Backup

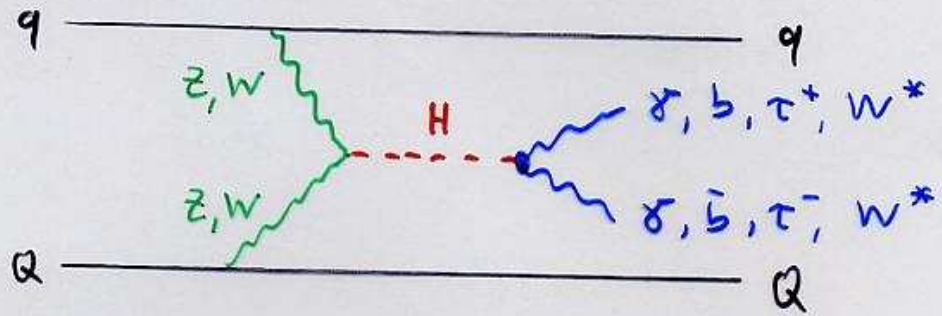
Total cross sections at the LHC



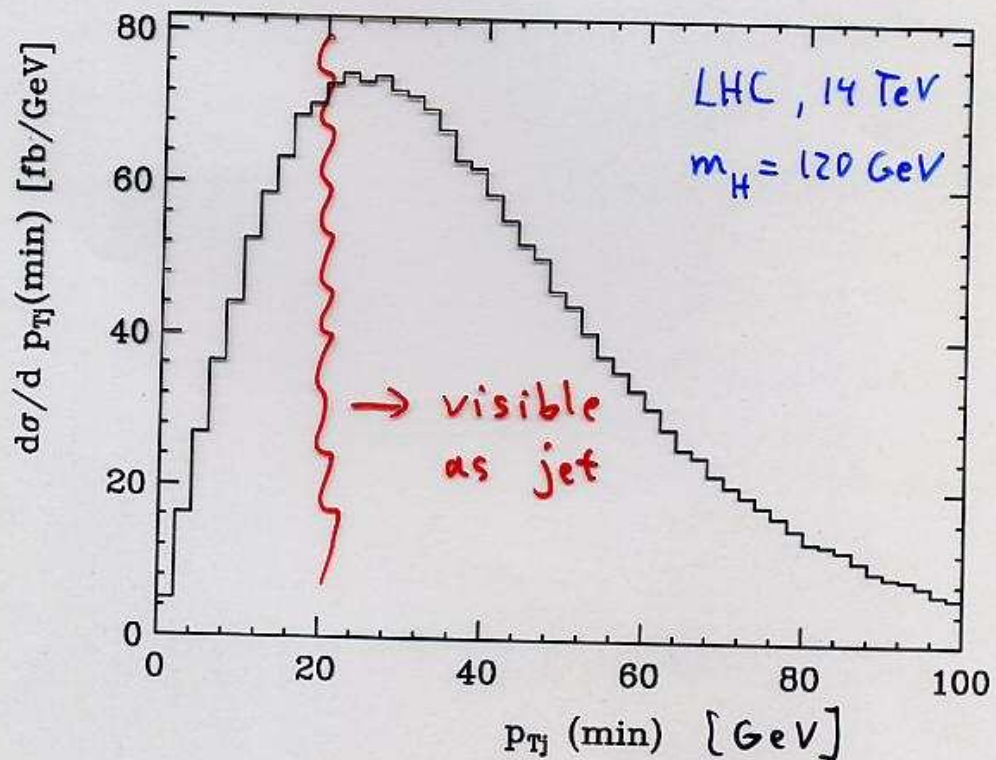
Vector boson fusion cross section for $m_h = 125 \text{ GeV}$ at 13 TeV: $\sigma(qq \rightarrow qqh) = 3.75 \text{ pb}$

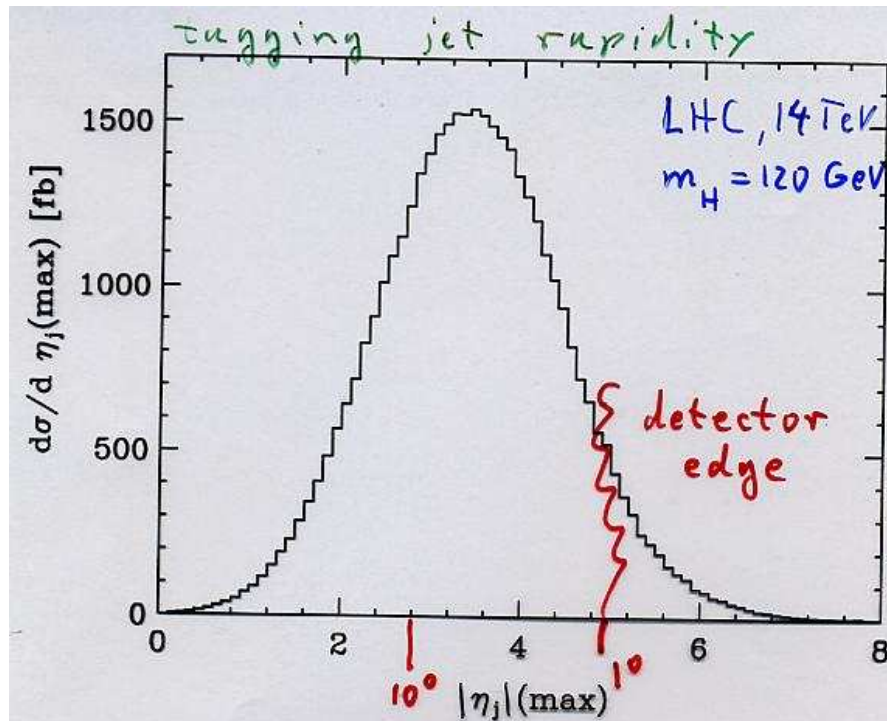
Vector boson fusion cross section for $m_h = 125 \text{ GeV}$ at 14 TeV: $\sigma(qq \rightarrow qqh) = 4.23 \text{ pb}$

Characteristics of weak boson fusion



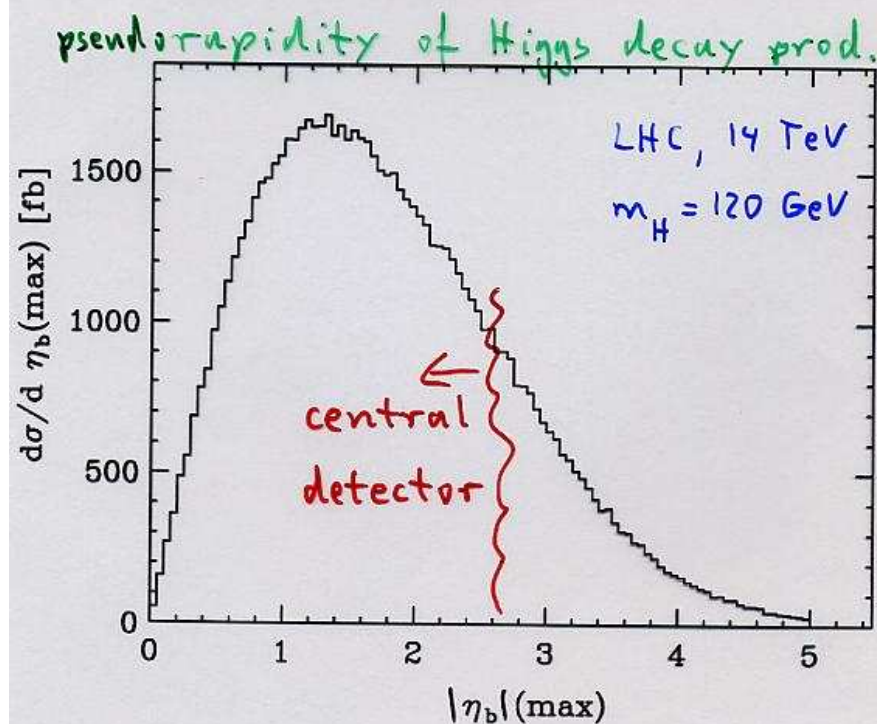
- scattered quarks lead to 2 forward tagging jets [Cahn, Kleiss, Stirling]





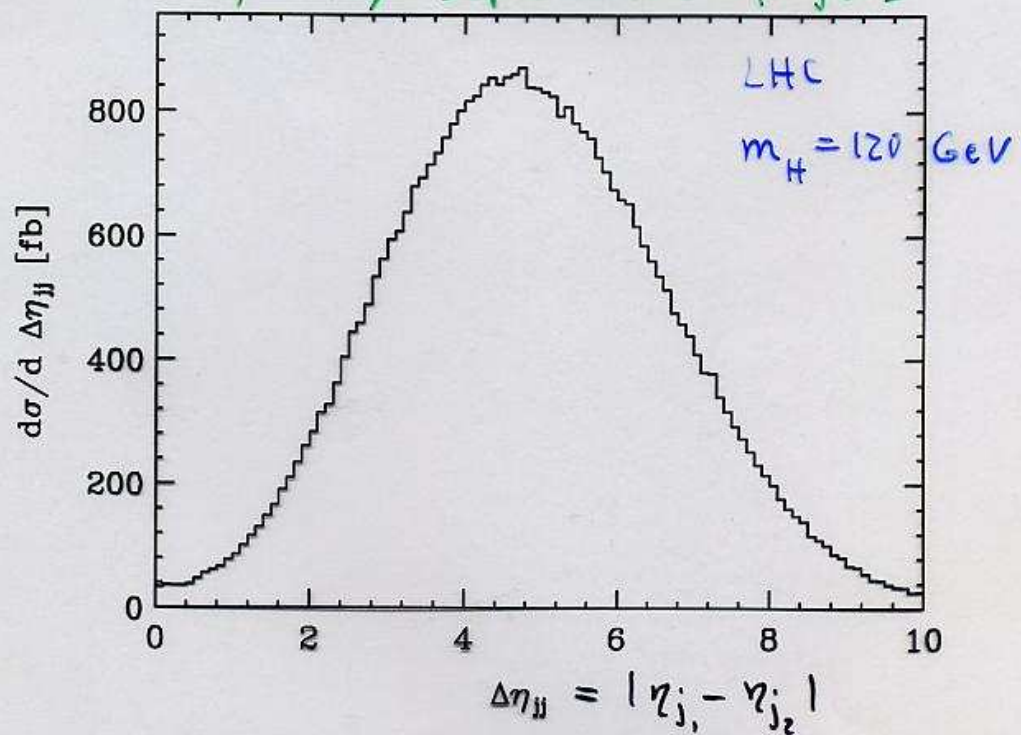
tagging jet
 forward but
 well inside
 detector

$$\eta = \frac{1}{2} \ln \frac{1 + \cos \theta}{1 - \cos \theta}$$



Higgs decay
 products
 are quite
 central

rapidity separation of jets



Tagging jets are typically far apart. Higgs decay products usually between 2 tagging jets

Real emission

Calculation is done using **Catani-Seymour** subtraction method

Consider $q(p_a)Q \rightarrow g(p_1)q(p_2)QH$. Subtracted real emission term

$$|\mathcal{M}_{\text{emit}}|^2 - 8\pi\alpha_s \frac{C_F}{Q^2} \frac{x^2 + z^2}{(1-x)(1-z)} |\mathcal{M}_{\text{Born}}|^2 \quad \text{with } 1-x = \frac{p_1 \cdot p_2}{(p_1 + p_2) \cdot p_a}, \quad 1-z = \frac{p_1 \cdot p_a}{(p_1 + p_2) \cdot p_a}$$

is integrable \Rightarrow **do by Monte Carlo**

Integral of subtracted term over $d^{3-2\epsilon}\mathbf{p}_1$ can be done analytically and gives

$$\frac{\alpha_s}{2\pi} C_F \left(\frac{4\pi\mu_R^2}{Q^2} \right)^\epsilon \Gamma(1+\epsilon) |\mathcal{M}_{\text{Born}}|^2 \left[\frac{2}{\epsilon^2} + \frac{3}{\epsilon} + 9 - \frac{4}{3}\pi^2 \right] \delta(1-x)$$

after factorization of splitting function terms (yielding additional “finite collinear terms”)

The divergence must be canceled by virtual corrections for all VBF processes

only variation: meaning of Born amplitude $\mathcal{M}_{\text{Born}}$

Gauge invariance tests

Numerical problems flagged by gauge invariance test: use Ward identities for penline and boxline contributions

$$q_2^{\mu_2} \tilde{\mathcal{E}}_{\mu_1 \mu_2 \mu_3}(k_1, q_1, q_2, q_3) = \tilde{\mathcal{D}}_{\mu_1 \mu_3}(k_1, q_1, q_2 + q_3) - \tilde{\mathcal{D}}_{\mu_1 \mu_3}(k_1, q_1 + q_2, q_3)$$

With Denner-Dittmaier recursion relations for E_{ij} functions the ratios of the two expressions agree with unity (to 10% or better) at more than 99.8% of all phase space points.

Ward identities reduce importance of computationally slow pentagon contributions when contracting with W^\pm polarization vectors

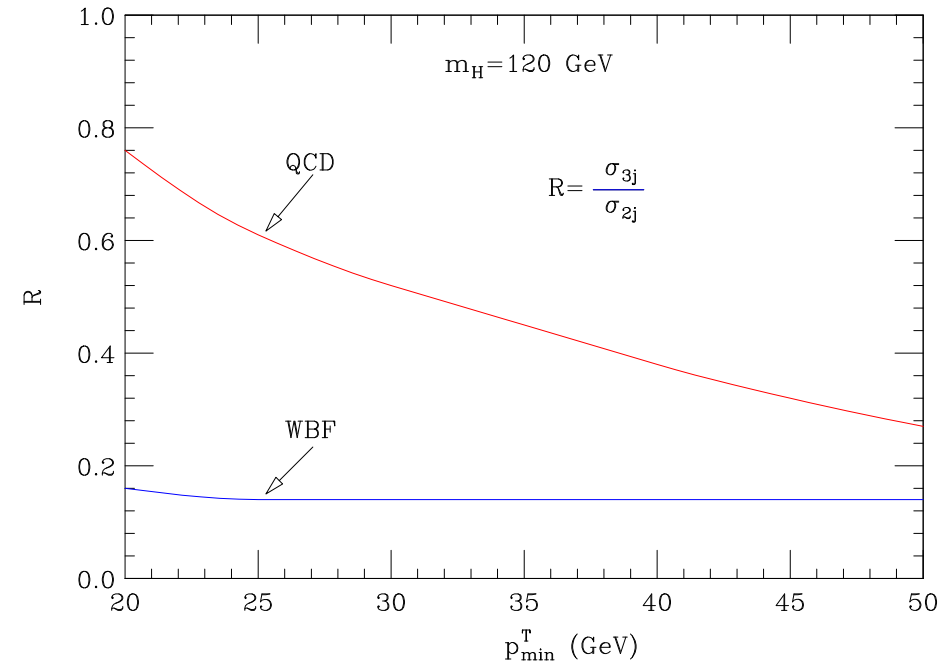
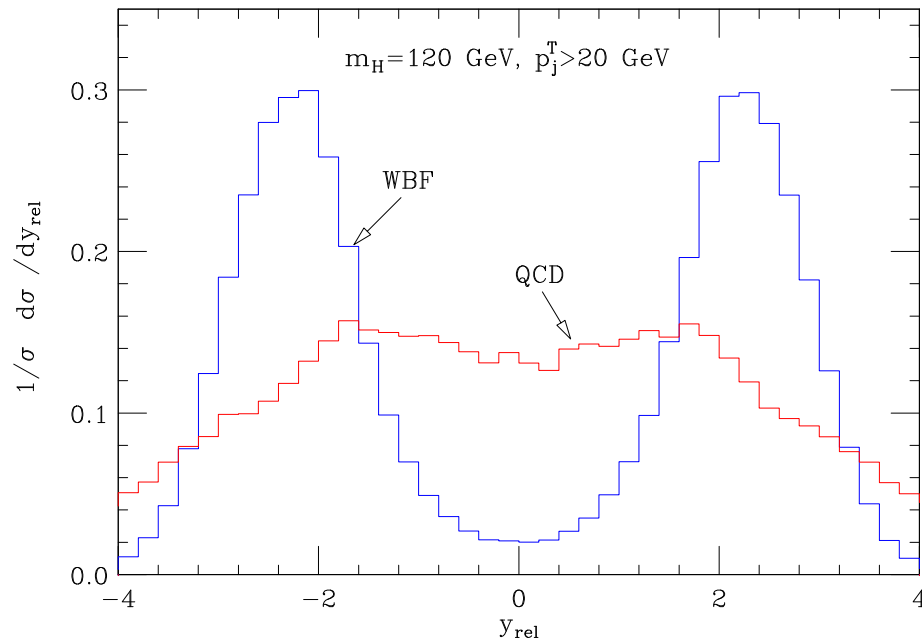
$$J_\pm^\mu = x_\pm q_\pm^\mu + r_\pm^\mu$$

choose x_\pm such as to minimize pentagon contribution from remainders r_\pm in all terms like

$$J_+^{\mu_1} J_-^{\mu_2} \tilde{\mathcal{E}}_{\mu_1 \mu_2 \mu_3}(k_1, q_+, q_-, q_0) = r_+^{\mu_1} r_-^{\mu_2} \tilde{\mathcal{E}}_{\mu_1 \mu_2 \mu_3}(k_1, q_+, q_-, q_0) + \text{box contributions}$$

Resulting true pentagon piece contributes to the cross section at permille level \Rightarrow totally negligible for phenomenology

Central Jet Veto: $Hjjj$ from VBF vs. gluon fusion

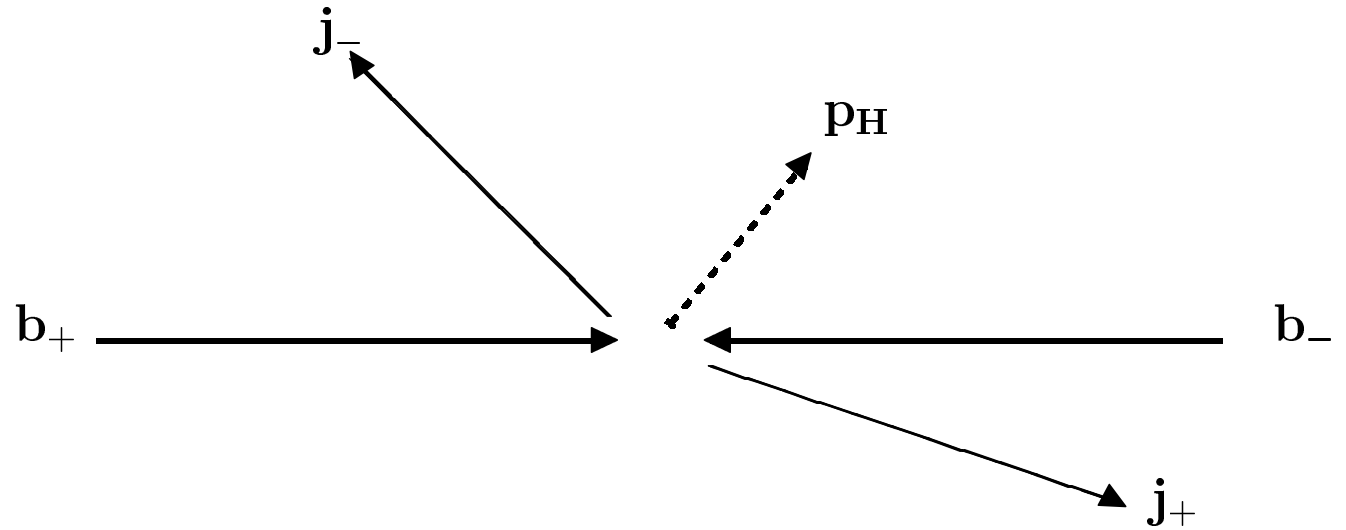


[Del Duca, Frizzo, Maltoni, JHEP 05 (2004) 064]

- Angular distribution of third (softest) jet follows classically expected radiation pattern
- QCD events have higher effective scale and thus produce harder radiation than VBF (larger three jet to two jet ratio for QCD events)
- Central jet veto can be used to distinguish Higgs production via GF from VBF

Azimuthal angle distribution and Higgs CP properties

Kinematics of Hjj event:



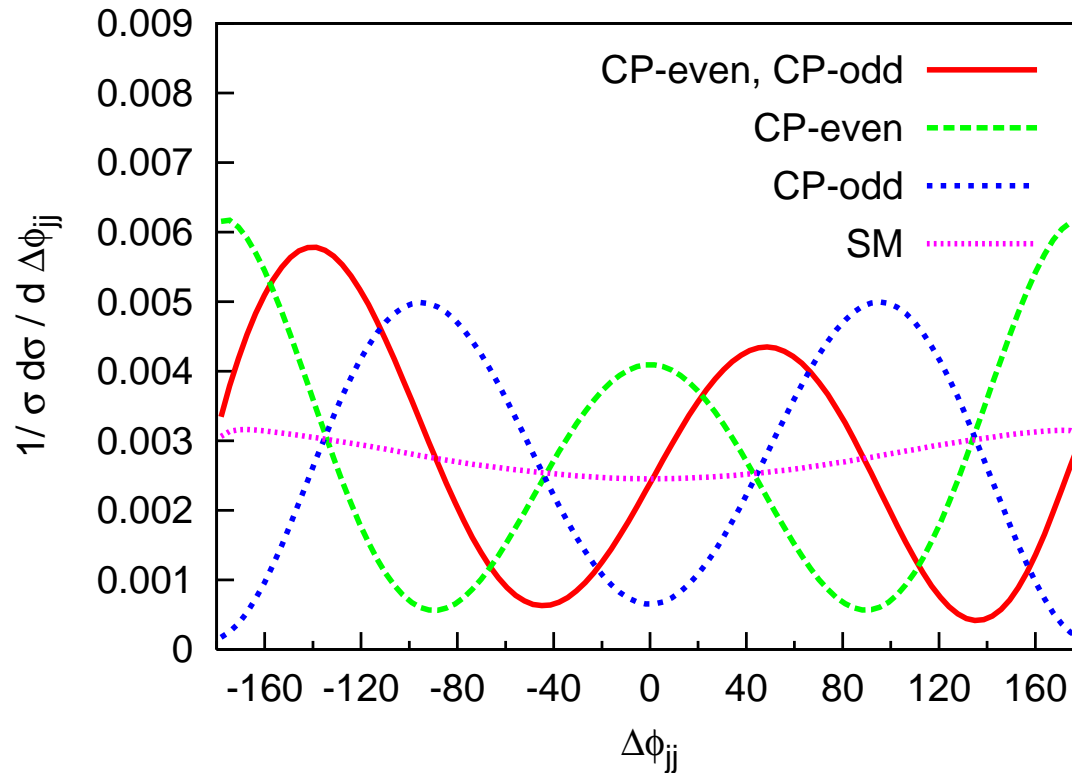
Define azimuthal angle between jet momenta j_+ and j_- via

$$\epsilon_{\mu\nu\rho\sigma} b_+^\mu j_+^\nu b_-^\rho j_-^\sigma = 2p_{T,+} p_{T,-} \sin(\phi_+ - \phi_-) = 2 p_{T,+} p_{T,-} \sin \Delta\phi_{jj}$$

- $\Delta\phi_{jj}$ is a parity odd observable
- $\Delta\phi_{jj}$ is invariant under interchange of beam directions $(b_+, j_+) \leftrightarrow (b_-, j_-)$

Work with Vera Hankele, Gunnar Klmke and Terrance Figy: [hep-ph/0609075](https://arxiv.org/abs/hep-ph/0609075)

Signals for CP violation in the Higgs Sector



mixed CP case:

$$a_2 = a_3, a_1 = 0$$

pure CP-even case:

a_2 only

pure CP odd case:

a_3 only

Position of **minimum of $\Delta\phi_{jj}$ distribution** measures relative size of CP-even and CP-odd couplings. For

$$a_1 = 0,$$

$$a_2 = d \sin \alpha,$$

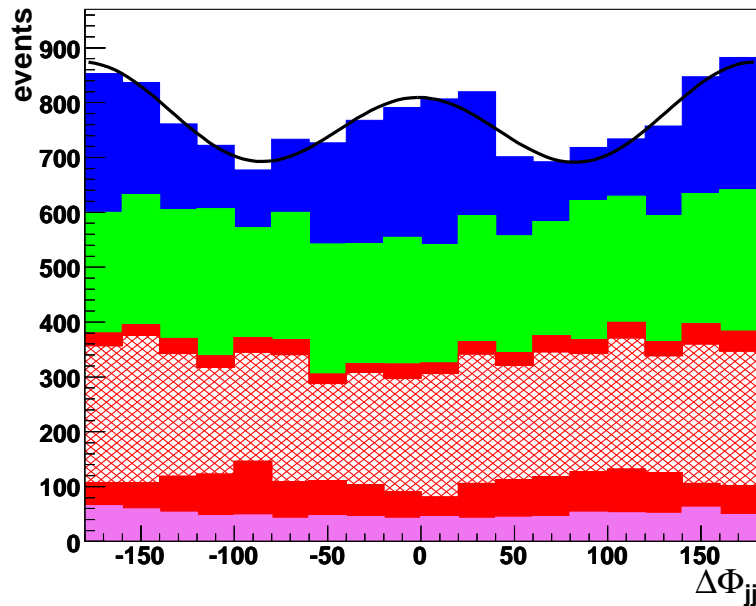
$$a_3 = d \cos \alpha,$$

\Rightarrow Minimum at $-\alpha$ and $\pi - \alpha$

$\Delta\Phi_{jj}$ -Distribution in gluon fusion

Fit to Φ_{jj} -distribution with function $f(\Delta\Phi) = N(1 + A \cos[2(\Delta\Phi - \Delta\Phi_{max})] - B \cos(\Delta\Phi))$

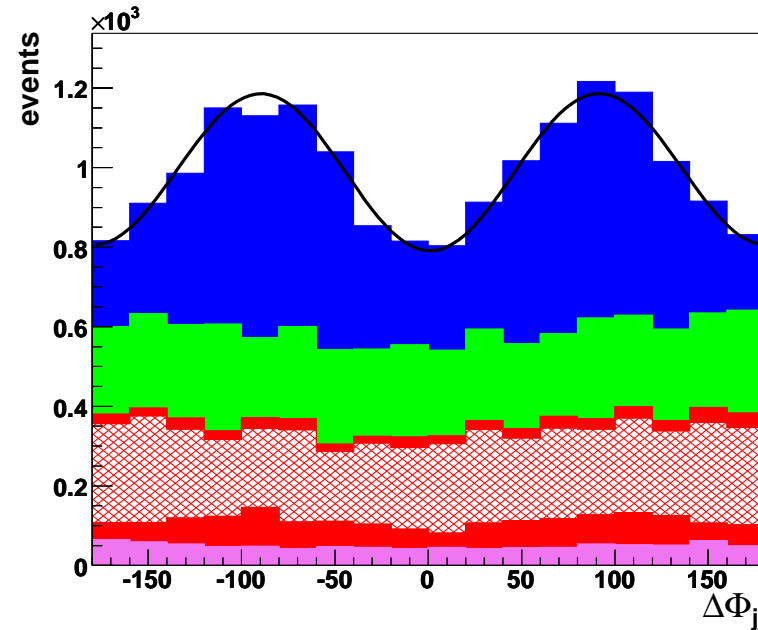
Klámke, DZ hep-ph/0703202



CP-even

$$A = 0.100 \pm 0.039$$

$$\Delta\Phi_{max} = 5.8 \pm 15.3$$



CP-odd

$$A = 0.199 \pm 0.034$$

$$\Delta\Phi_{max} = 93.7 \pm 5.1$$

Signal

VBF

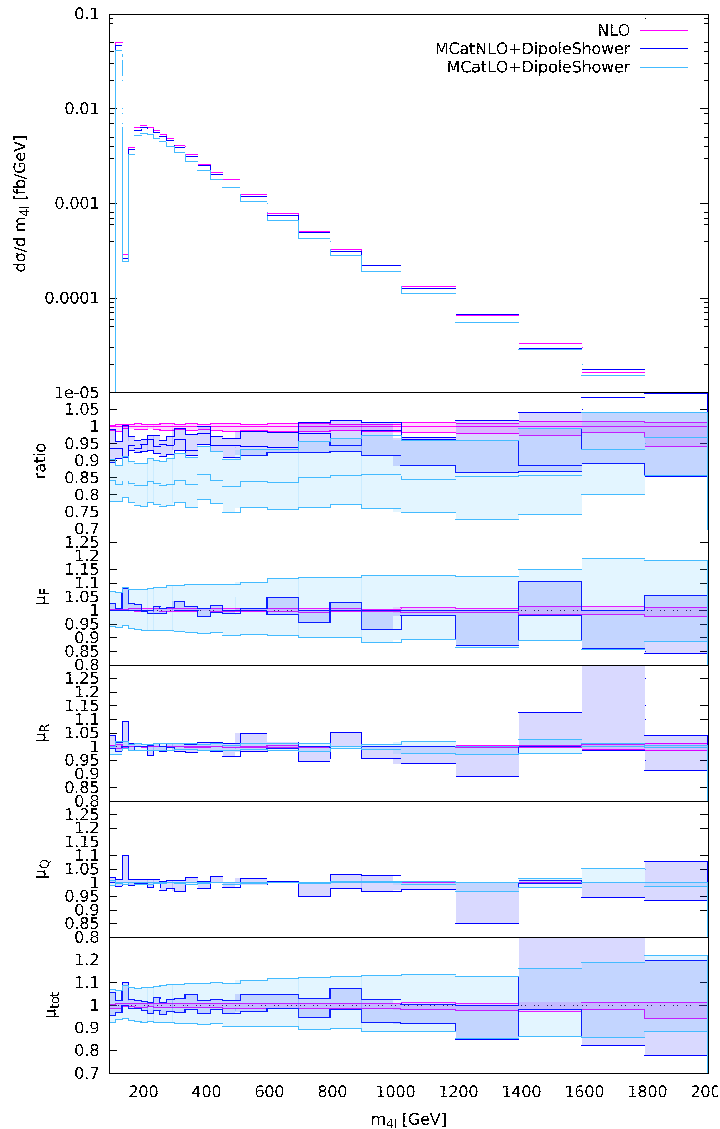
$t\bar{t}$ +Jets

QCD-WW

$L = 300 \text{ fb}^{-1}$

$(\Delta\eta_{jj} > 3.0)$

VBF- W^+W^- + parton shower



Comparison of:

- pure NLO
- NLO+PS (MC@NLO+dipole shower)
- LO+PS (dipole shower)

Panels:

- differential c.s.
- ratio of c.s. and total scale variation ($\mu_0 = p_{j,1}^T$)
- individual variation of μ_F, μ_R, μ_Q (shower scale)
- total variation $\mu_i/\mu_0 \in [\frac{1}{2}; 2]$

Inclusion of parton shower:

- smaller c.s. (additional splittings)
- larger uncertainties (add. shower scale)

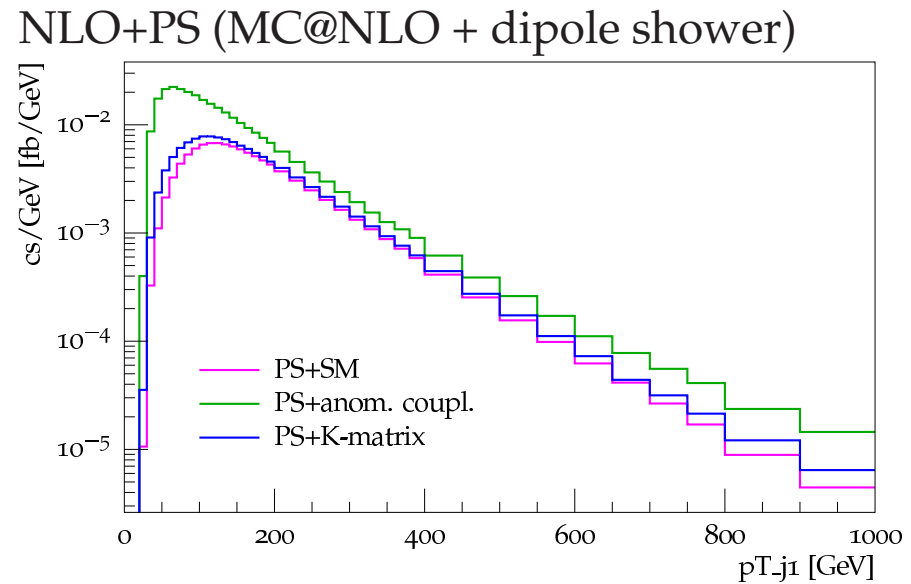
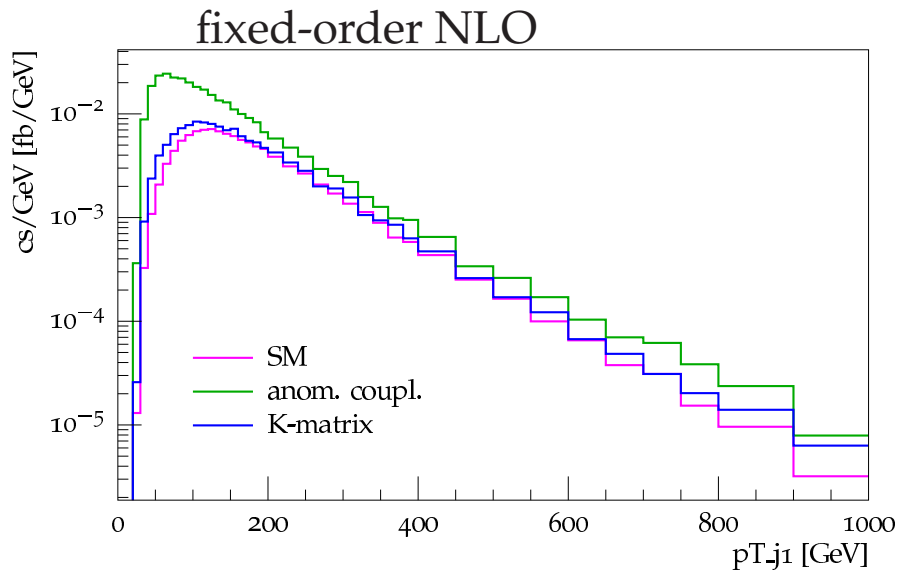
K-matrix + Parton Shower

Combine K-matrix setup with parton shower

[VBFNLO3&Herwig7]

Example: VBF- W^+W^+ ($pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$)

anom. coupl.: $f_{S,1}/\Lambda^4 = 100 \text{ TeV}^{-4}$



Strong enhancement of leading jet at low transverse momentum without unitarization is caused by huge excess of high m_{VV} events

small dependence on parton-shower effects

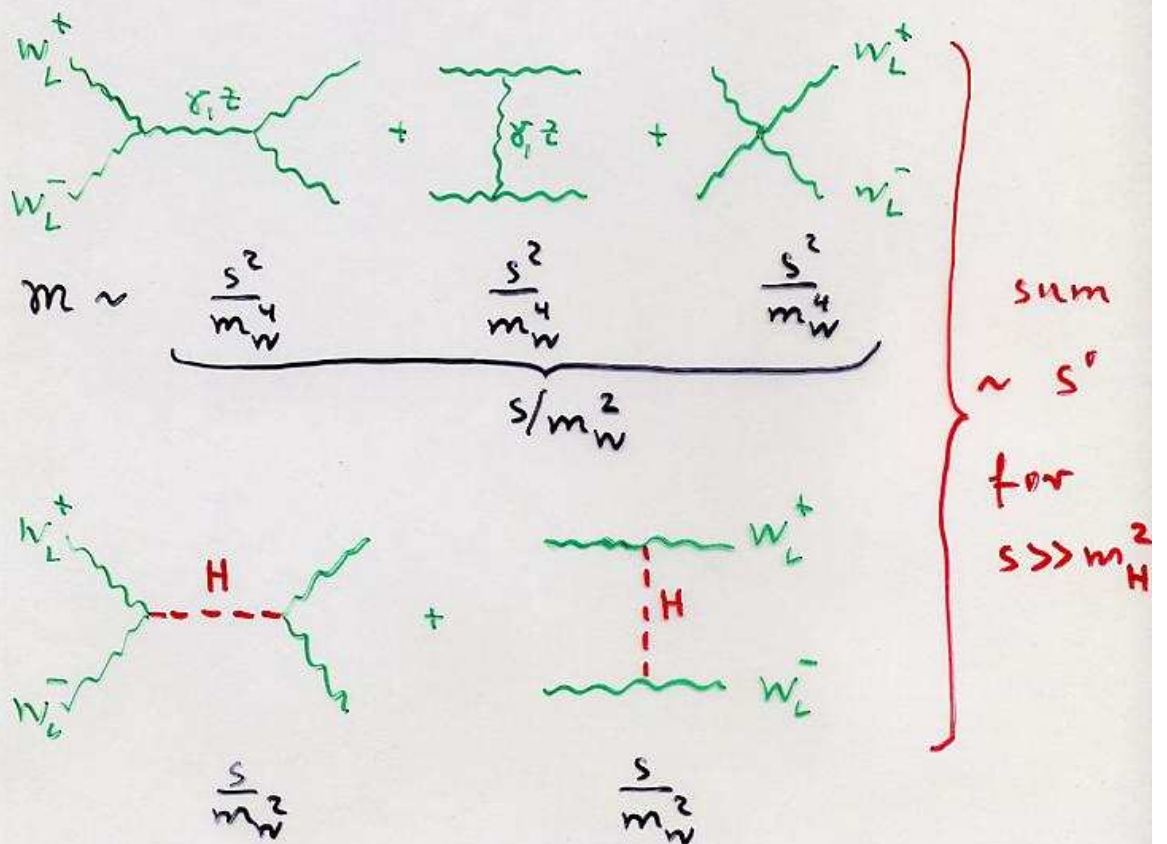
WW scattering and unitarity

Consider longitudinal W's

$$W_L^+ W_L^- \rightarrow W_L^+ W_L^-$$

Polarisation vector

$$\epsilon_L^\mu = \frac{p^\mu}{m_W} + \mathcal{O}\left(\frac{m_W}{E}\right) \sim \frac{\sqrt{s}}{m_W}$$



Signal definition in VV scattering

Problem: heavy Higgs or technirho or interferes with continuum electroweak background
How do we take **interference** into account in our definition of the signal?

Notation:

$\mathcal{M}_X = \mathcal{M}_X(m_X) \sim \frac{s}{v^2}$ Signal amplitude for s-, t- and u-channel exchange of new particle X

$\mathcal{M}_B \sim \frac{-s}{v^2}$ continuum electroweak background amplitude

$\Rightarrow B = \int d\Phi |\mathcal{M}_B|^2$ or $S = \int d\Phi [|\mathcal{M}_X|^2 + 2\text{Re}\mathcal{M}_X\mathcal{M}_B^*]$ violate unitarity at large s

Compare to SM light Higgs scenario with $m_h = 125$ GeV, i.e. define

electroweak background: $B = \int d\Phi |\mathcal{M}_B + \mathcal{M}_h(m_h)|^2$ and

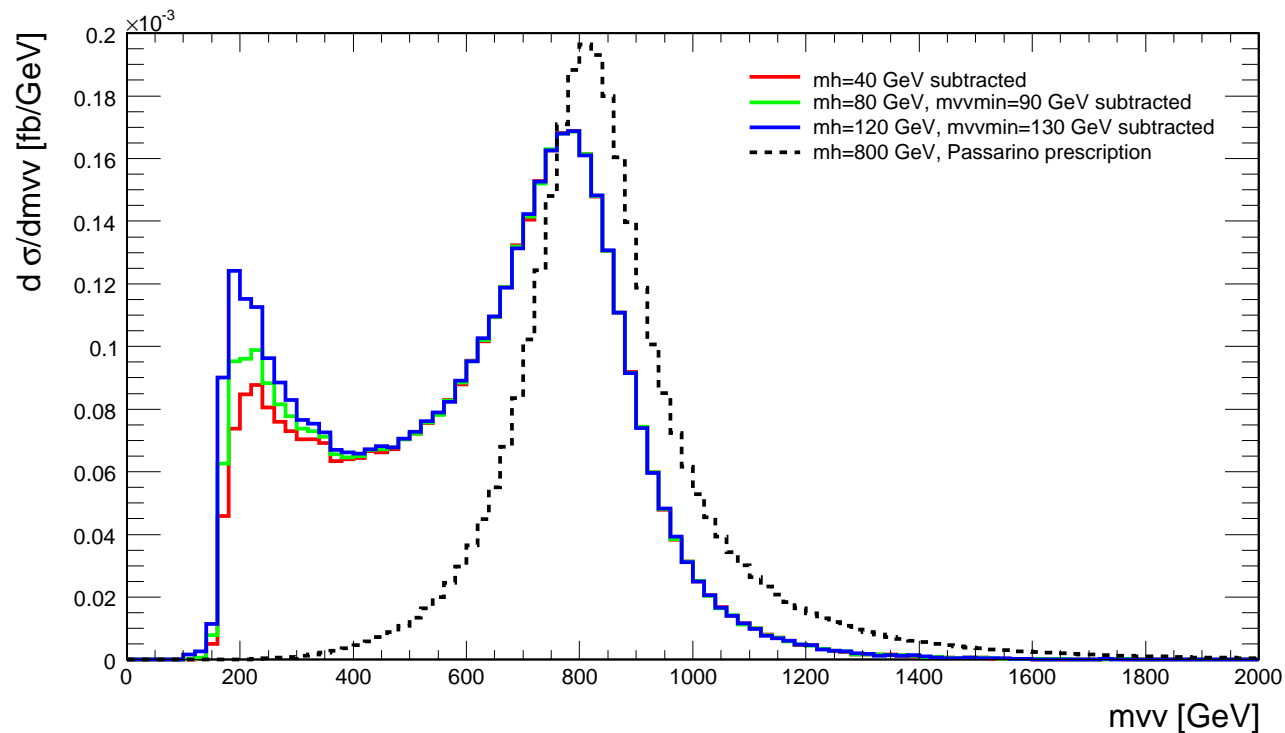
signal: $S = \int d\Phi |\mathcal{M}_B + \mathcal{M}_X(m_X)|^2 - B$

Integrate over suitable mass range $[m_X - \Gamma_1, m_X + \Gamma_2]$

Advantages:

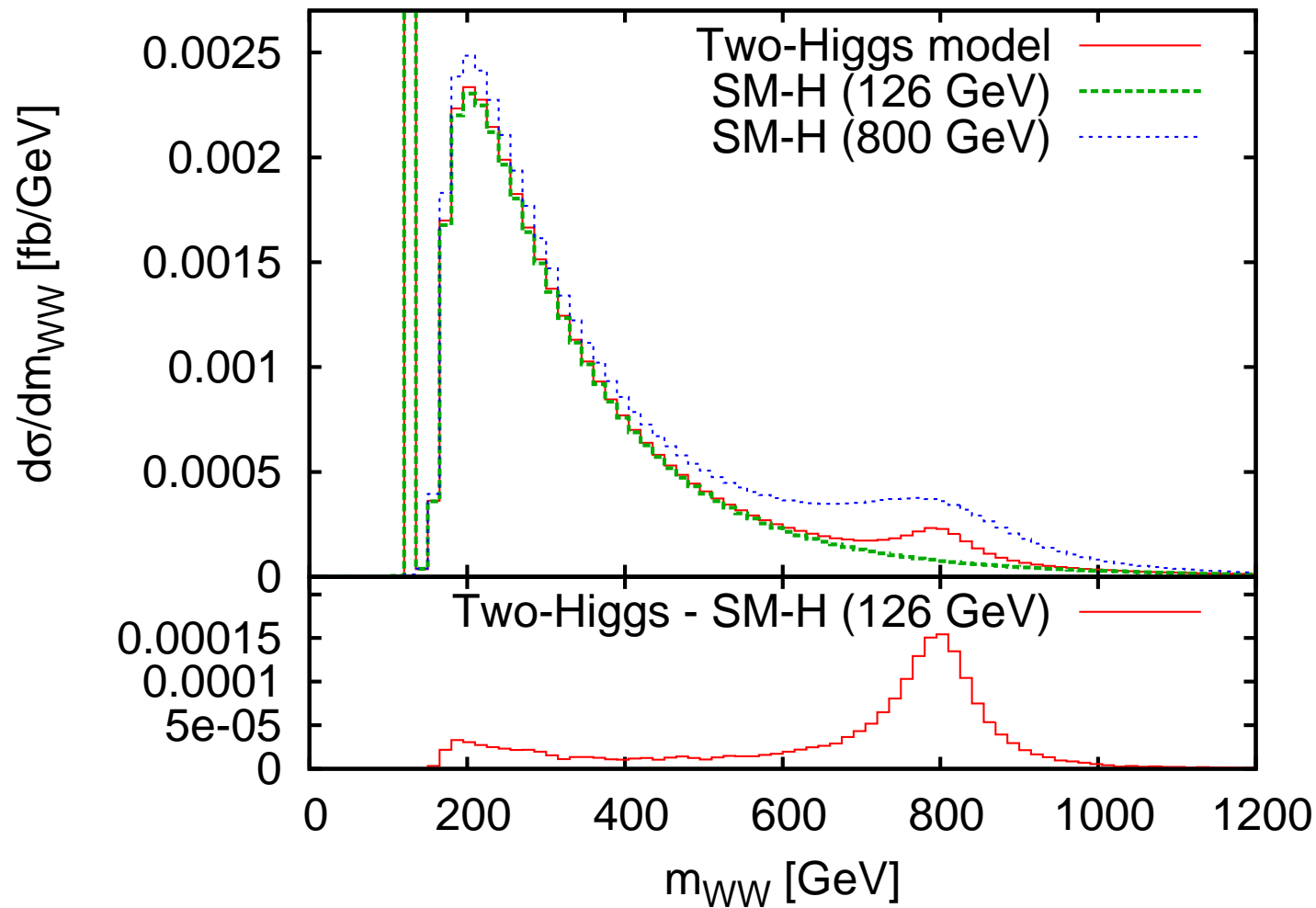
- S and B are well defined and do not violate unitarity
- B is minimized since early onset of cancellations for light SM Higgs are taken into account
- Avoid potentially negative signal cross section due to dominance of (negative) interference terms

Resonance shape for heavy Higgs: LO WW_{jj} case



- Resonance peak is independent of light Higgs mass used in subtraction of continuum background
- True resonance shape is not reproduced by modified Breit Wigner distribution

More realistic: additional heavy Higgs



- Light Higgs at 126 GeV with reduced coupling (here $g_{hWW}^2 = 0.7 \times \text{SM value}$)
- Heavy Higgs is narrower than SM case due to reduction of $g_{HWW}^2 = 0.3 \times \text{SM value}$