Southampton, UK

Lattice 2016

Composite Dark Matter

and insights from the Lattice

Enrico Rinaldi



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Computing support comes from the LLNL Institutional Computing Grand Challenge program.





Visible Matter 4.9%

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Dark Matter 26.8%

Dark Energy 68.3% Visible Matter 4.9%

 $\rho_{\text{DM}} \approx 5 \rho_{\text{SM}}$ 26.8%

Dark Energy 68.3%



Direct Detection



Indirect Detection



DM DM

Production at Colliders





Production at Colliders



Indirect Detection







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What is Dark Matter?



[Planning the Future of U.S. Particle Physics (Snowmass 2013), 1401.6085]



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Dark Matter is a composite object



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e.g. technibaryon or hidden glueball



- Dark Matter is a composite object
- Interesting and complicated internal structure
- Properties dictated by strong dynamics
- Self-interactions are natural

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Chance to observe them in experiments and give the correct relic abundance

















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Small **interactions** with SM particles arise from form factor **suppression** (higher dim. operators)

Self-interactions are included due to strongly coupled dynamics



★ Pion-like (dark quark-antiquark)

- ♦ pNGB DM [Hietanen et al., 1308.4130]
- ◆ Quirky DM [Kribs et al.,0909.2034]
- Ectocolor DM [Buckley&Neil, 1209.6054]
- ◆ SIMP [Hochberg et al.,1411.3727]
- Minimal SU(2) [Lewis, Wed.@11:50]

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★ Baryon-like (multiple quarks)

- "Technibaryons" [LSD, 1301.1693]
- Stealth DM [LSD, 1503.04203-1503.04205]
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[Wikipedia]








Lattice results for Composite Dark Matter

Template Models	Spectrum	Higgs	Mag. Dip.	Charge r.	Polariz.			
SU(2) N _f =1	\star	[Talk by Lewis, Wed.@11.50, new simulations are in progress]						
SU(2) N _f =2	\bigstar	\star			\star			
SU(3) N _f =2,6	\star		\star					
SU(3) N _f =8	\bigstar	\star						
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SU(4) N _f =4	\bigstar	\star			\star			
SO(4) N _f =2 (V)	\star							
SU(N) Nf=0		[Talk by Soni, W	ed.@11.30, interested in c	alculating self-interactions	s on the lattice]			



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Computing Higgs exchange



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$$\mathcal{M}_a = \frac{y_f y_q}{2m_h^2} \sum_f \langle B|\bar{f}f|B\rangle \sum_q \langle a|\bar{q}q|a\rangle$$

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- 2. dark baryon scalar form factor: need lattice input for generic DM models!
- 3. nucleon scalar form factor: ChPT and lattice input [Plenary talk by Collins, Tue@10:15]



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$$\begin{aligned} y_f B|\bar{f}f|B\rangle &= \frac{m_B}{v} \sum_f \frac{v}{m_f} \frac{\partial m_f(h)}{\partial h} \Big|_{h=v} f_f^{(B)} \\ m_f(h) &= m + \frac{y_f h}{\sqrt{2}} \\ \alpha &\equiv \frac{v}{m_f} \frac{\partial m_f(h)}{\partial h} \Big|_{h=v} = \frac{yv}{\sqrt{2}m + yv} \end{aligned}$$



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Computing Higgs exchange

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- Lattice input is necessary: compute mass and form factor

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Bounds from Higgs exchange

- Lattice results for the cross-section are compared to experimental bounds
- Coupling space in specific models can be vastly constrained

$SU(4) N_f=4$ Stealth DM



SU(3) Nf=8 "technibaryon"



- Some candidates can be excluded as dominant sources of dark matter
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Mesonic and Baryonic EM form factors directly from lattice simulations

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M_B >~ 10 TeV pushed to ~100 TeV with new LUX



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- \bigstar dm is "mesonic" pNGB
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 $M_B \sim < 13 \text{ GeV}$ depends on d_B

[Pospelov & Veldhuis, hep-ph/0003010] [Ovanesyan & Vecchi, 1410.0601] [Weiner & Yavin,1206.2910] [Frandsen et al., 1207.3971] [Detmold et al., 0904.1586-1001.1131]



Computing polarizability



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Computing polarizability























★QCD ideas and lattice QCD techniques can be borrowed when exploring the DM landscape (BSM)

Composite dark matter is a viable interesting possibility with rich phenomenology

★Lattice methods can help in calculating direct detection cross sections, production rates at colliders, and selfinteraction cross sections of phenomenological relevance.

★Dark matter constituents can carry electroweak charges and still the stable composites are currently undetectable. Stealth cross section.

extra

Open questions and future projects

- Structure formation in galaxies → influenced by DM scattering cross-section: hadron-hadron interactions are hard to model, but can be studied directly with lattice methods
- Colliders could produce the (lightest) dark mesons, but need to know their form factors: lattice methods can be used
- New dark sector → deconfinement phase transition: if first order, gravitational wave signals could be soon observed [Schwaller, 1504.07263]

A very familiar picture



The Standard Model of particles

[Wikipedia]

A very familiar picture



[Peccei & Quinn: PRL 38 (1977) 1440, PR D16 (1977) 1791] [Preskill, Wise & Wilczek, Phys. Lett. B 120 (1983) 127-132]

Axion dark matter

- Axions were originally proposed to deal with the Strong-CP problem
 - They also form a plausible DM candidate
 - The axion energy density requires nonperturbative QCD input
- Being sought in ADMX (LLNL, UW) & CAST-IAXO (CERN) with large discovery potential in the next few years
- Requiring $\Omega_a \leq \Omega_{CDM}$ yields a lower bound on the axion mass today





PDG 2014

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Constraints from lattice simulations



Non-perturbative calculation of QCD topology at finite temperature

Pure gauge SU(3) topological susceptibility
compatible with model predictions, but
large non-perturbative effects

[Kitano&Yamada, 1506.00370][Borsanyi et al., 1508.06917][Frison et al.,1606.07175]

 is QCD topological susceptibility at high-T well described by models? ⇒ light fermions importantly affect the vacuum
[Trunin et al., 1510.02265][Petreczky et al., 1606.03145][Borsanyi et al., 1606.07494]



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Great effort to control all systematic lattice effects in order to impact experiments. This direction has started only 1 year ago!



[Berkowitz, Buchoff, ER., 1505.07455]





Axion mass lower bound





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Composite DM signatures at colliders



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- Signatures are not dominated by missing energy: DM is not the lightest particle! The interactions are suppressed (form factors)
- Light meson production and decay give interesting signatures: the model can be constrained by collider limits

Photon interactions

 $\langle \chi(p') | j^{\mu}_{\rm EM} | \chi(p) \rangle = F(q^2) q^{\mu}$

Expansion at low momentum through effective operators

✦dimension 5 ➡ magnetic dipole

 \bullet dimension 6 \blacktriangleright charge radius

 \bullet dimension 7 \blacktriangleright polarizability

