

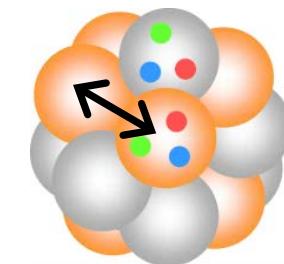
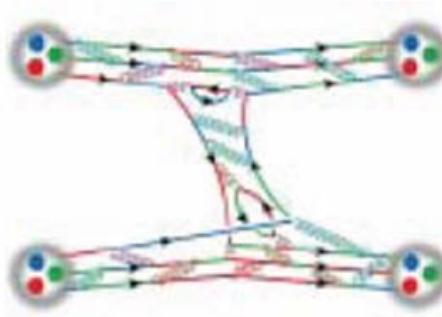
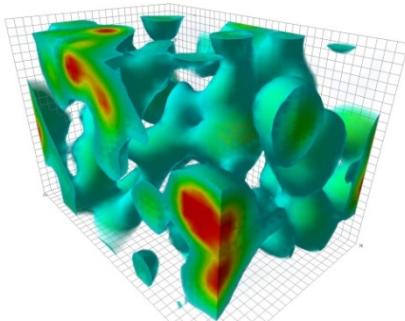
Baryon interactions from lattice QCD with physical masses

– Overview and $S = 0, -4$ sectors –

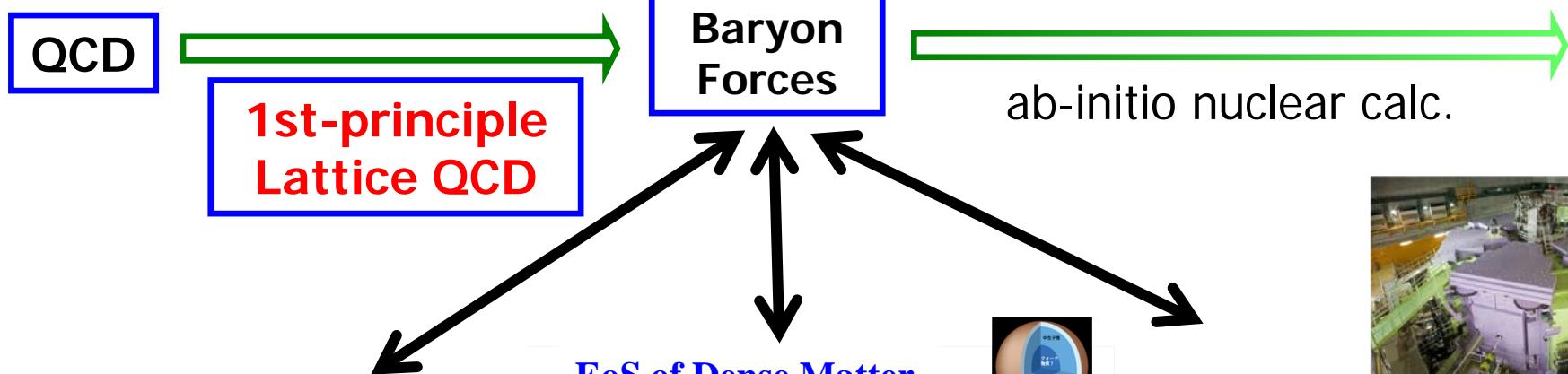
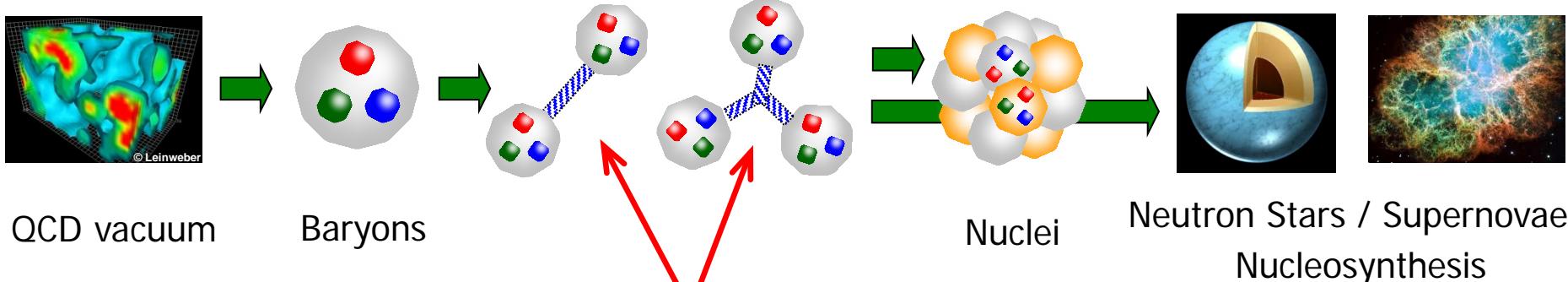
$S = -6$

Takumi Doi
(Nishina Center, RIKEN)

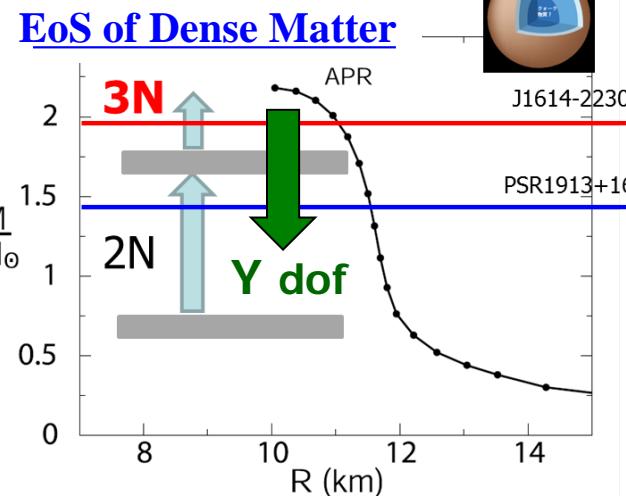
for HAL QCD Collaboration



The Odyssey from Quarks to Universe



Nuclear Forces / Hyperon Forces



aLIGO/KAGRA

NS-NS merger



The Odyssey from unphysical to physical quark masses

~2010



→ lighter m_q

We were here

$M_\pi=800$ MeV
 $L=2$ fm



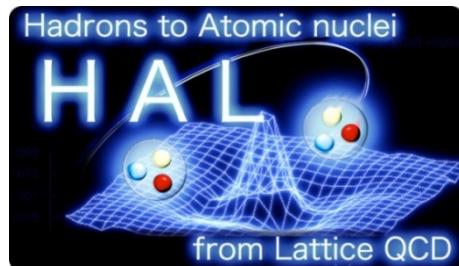
K-computer [10PFlops]

HPCI Program Field 5 (FY2010-15)

Priority Issue 9 (FY2015-19)



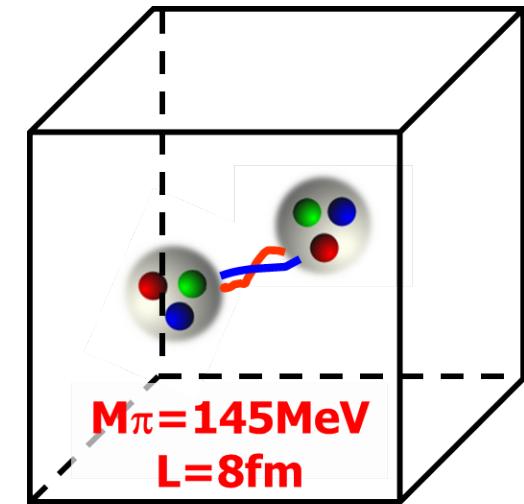
Staple Wilson-line
@ ~2000 BC



S. Aoki, T. Doi, F. Etminan, S. Gongyo,
T. Hatsuda, Y. Ikeda, T. Inoue, T. Iritani,
N. Ishii, D. Kawai, T. Miyamoto,
K. Murano, H. Nemura, K. Sasaki



Phys. point



[HAL QCD method]

- Nambu-Bethe-Salpeter (NBS) wave function

$$\psi(\vec{r}) = \langle 0 | N(\vec{r}) N(\vec{0}) | N(\vec{k}) N(-\vec{k}); \text{in} \rangle$$

$$(\nabla^2 + k^2)\psi(\vec{r}) = 0, \quad r > R$$

- phase shift at asymptotic region

$$\psi(r) \simeq A \frac{\sin(kr - l\pi/2 + \delta(k))}{kr}$$

Extended to multi-particle systems

M.Luscher, NPB354(1991)531

C.-J.Lin et al., NPB619(2001)467

N.Ishizuka, PoS LAT2009 (2009) 119

CP-PACS Coll., PRD71(2005)094504

S. Aoki et al., PRD88(2013)014036

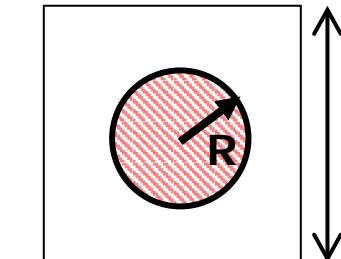
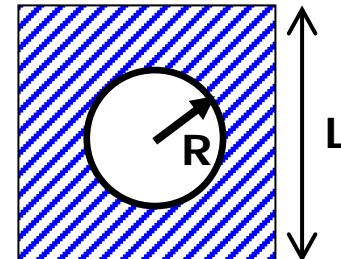
- Consider the wave function at “interacting region”

$$(\nabla^2 + k^2)\psi(\vec{r}) = m \int d\vec{r}' U(\vec{r}, \vec{r}') \psi(\vec{r}'), \quad r < R$$

- $U(\vec{r}, \vec{r}')$: faithful to the phase shift by construction

- $U(\vec{r}, \vec{r}')$: E-independent, while non-local in general

- Non-locality → derivative expansion



Aoki-Hatsuda-Ishii PTP123(2010)89

Crucial Theoretical Development

- **Time-dependent HAL method**

N.Ishii et al. (HAL Coll.) PLB712(2012)437

- Multi-baryon systems on large box w/ light mass → **~ gapless (continuum)**
- [**Luscher's method**] → G.S. saturation required → the S/N problem
- [**HAL method**] → G.S. saturation NOT required w/ E-indep pot

→ **“exponential” S/N Improvement**

$$S/N \sim \exp[-A \times (m_N - 3/2m_\pi) \times t]$$

→ Talks by T. Iritani, S. Aoki (Thur.)

T. Iritani et al. (HAL Coll.) arXiv:1607.06371

- **Coupled Channel systems**

S. Aoki et al. (HAL Coll.) Proc.Jpn.Acad.B87(2011)509

- Extension above inelastic threshold by **Coupled channel potentials**
→ Essential for YN/YY-forces

- **Unified Contraction Algorithm (UCA)**

TD, M.Endres, CPC184(2013)117

- Drastically faster algorithm by unifying Wick and color/spinor contractions

Speedup: **×192** for $^3\text{H}/^3\text{He}$, **×20736** for ^4He , **×10¹¹** for ^8Be

See also subsequent works:

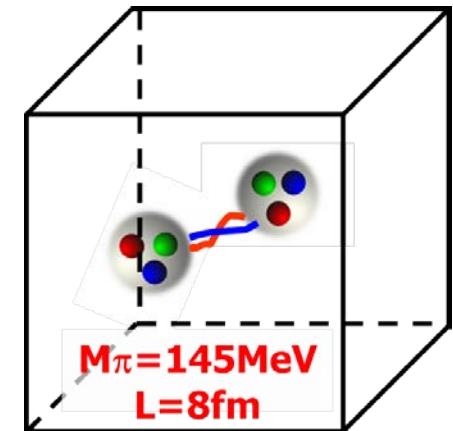
Detmold et al., PRD87(2013)114512

Gunther et al., PRD87(2013)094513

Setup of Lattice QCD

- **Nf = 2+1 full QCD**
 - Clover fermion + Iwasaki gauge action
 - Non-perturbatively O(a)-improved
 - APE-Stout smearing ($\alpha=0.1$, $n_{\text{stout}}=6$)
 - $m(\pi) \sim 145 \text{ MeV}$, $m(K) \sim 525 \text{ MeV}$
 - #traj ~ 2000 generated

K.I. Ishikawa et al., PoS LAT2015, 075



96^4 box
($a \sim 0.085 \text{ fm}$)

- **Measurement**
 - Wall source w/ Coulomb gauge
 - K @ RIKEN/AICS, FX100 @ RIKEN/Wako, HA-PACS @ Tsukuba are used
 - Efficient UCA code + block solver → ~25% efficiency on K @ 2048node
 - #stat = 200 confs x 4 rot x 44 (or 88) src → x 4 (or 2) in FY2016
 - All results preliminary

Target of Lattice QCD

- All of NN/YN/YY for central/tensor forces in $P=(+)$ (S, D-waves)

Central Tensor

$$U(\vec{r}, \vec{r}') = V_c(r) + S_{12}V_T(r) + \vec{L} \cdot \vec{S} V_{LS}(r) + \mathcal{O}(\nabla^2)$$

LO

LO

NLO

NNLO

(derivative expansion)

S=0

NN

S=-1

NΛ, NΣ

S=-2

ΛΛ, ΛΣ, ΣΣ, NΞ

S=-3

ΛΞ, ΣΞ

S=-4

ΞΞ

S=-5

ΞΩ

S=-6

ΩΩ

LQCD

better S/N

EXP

rich data



T. Doi



H. Nemura



K. Sasaki



N. Ishii



T. Doi



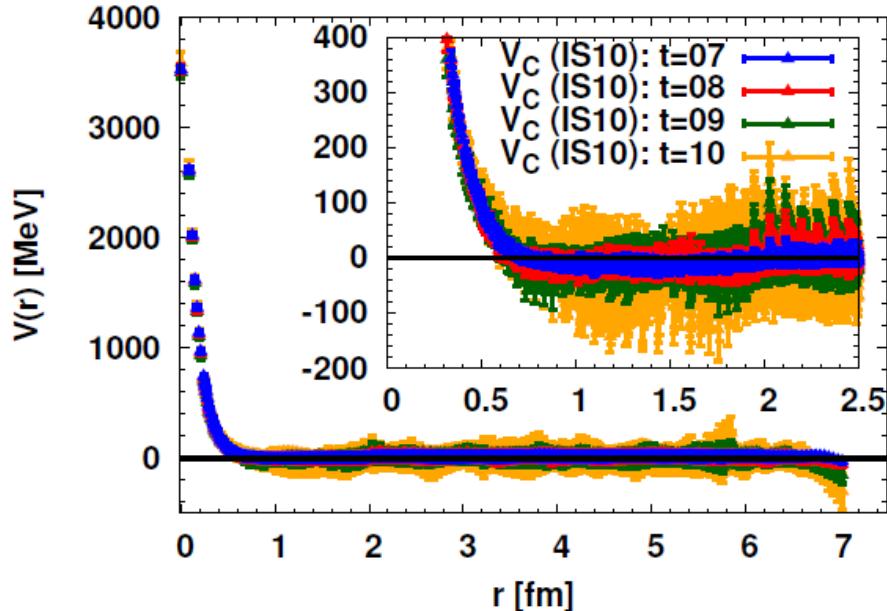
S. Gongyo
(→ T. Doi)

Hyperon forces provide precious predictions

NN system ($S=0$)

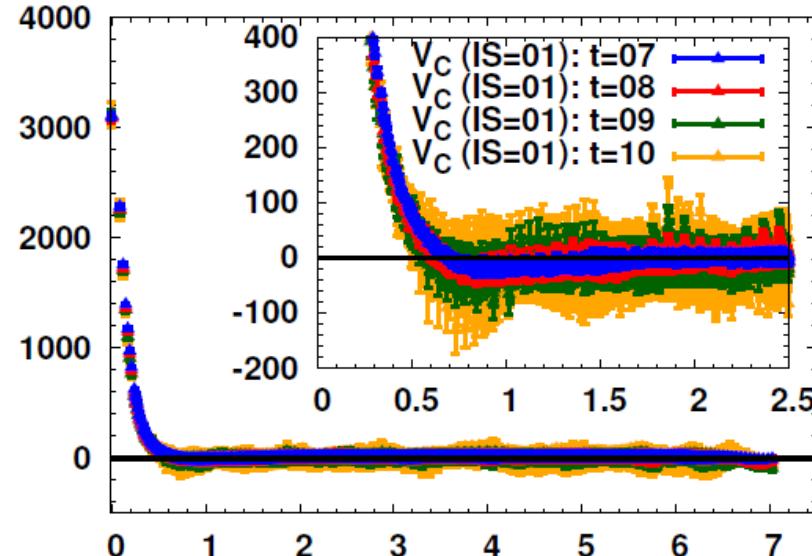
NN-Potentials

1S_0

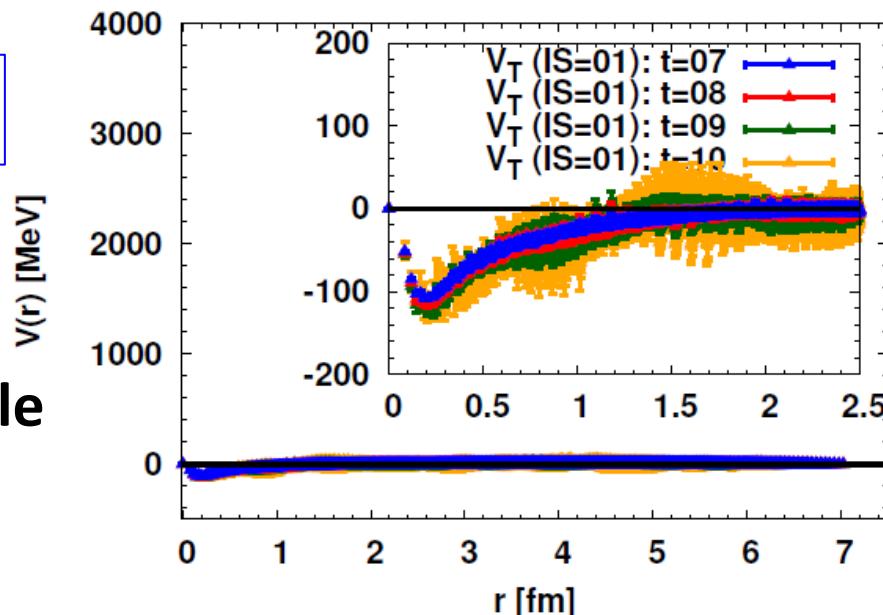


Preliminary

$^3S_1 - ^3D_1$



Central



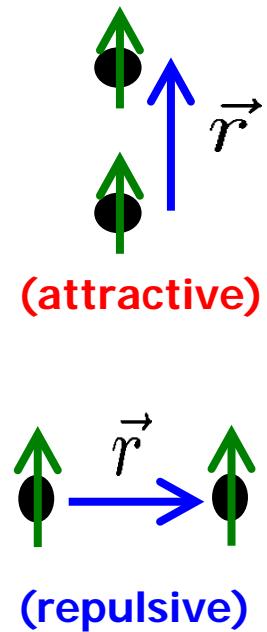
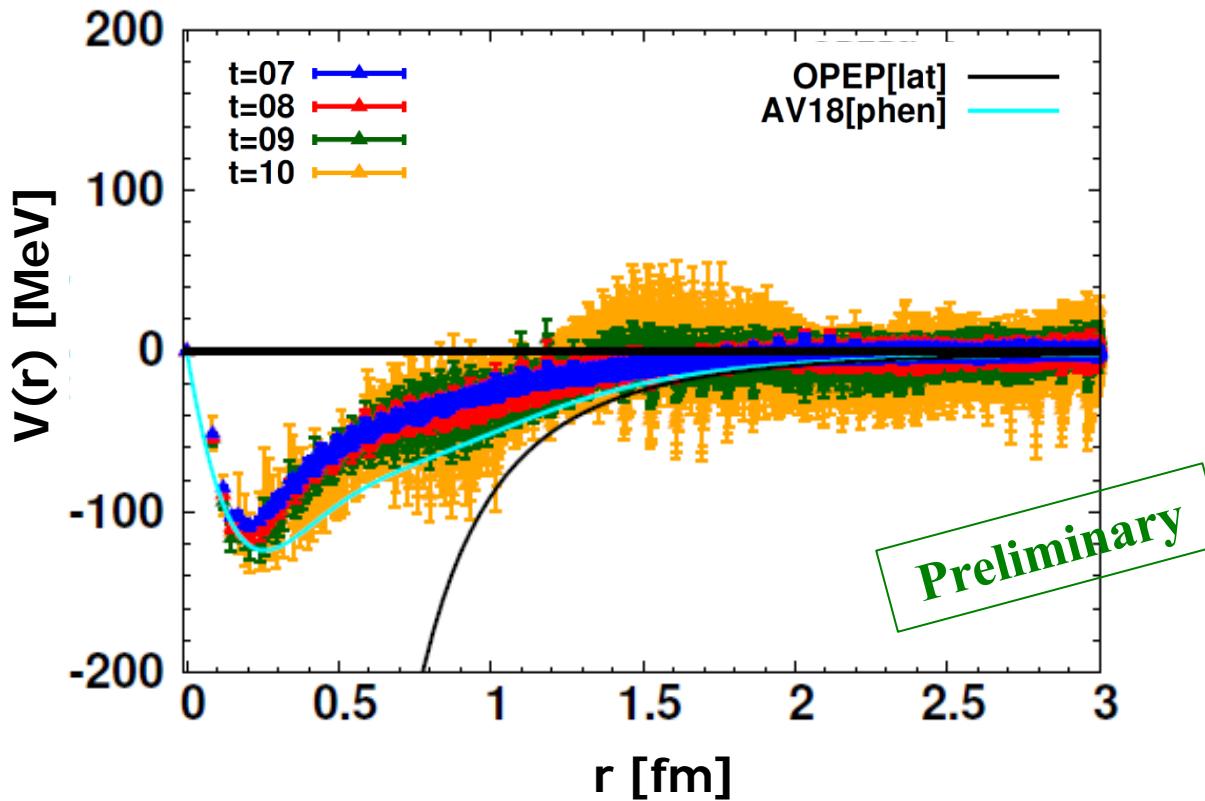
Tensor

- V_c : repulsive core
+ long-range attraction
- V_t : tensor force clearly visible

(200conf x 4rot x 44src)

NN system (3S_1 - 3D_1)

Tensor Force

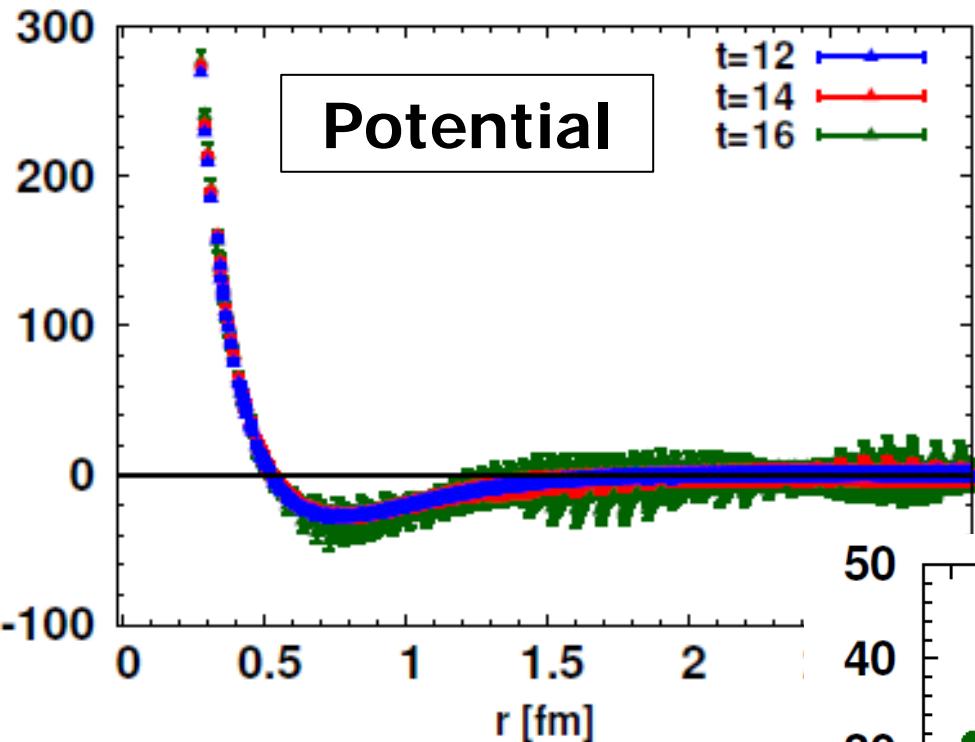


- Qualitatively similar tail as OPEP force
- Larger t w/ larger #stat is desirable

$m(\text{eff})$ for single N: ~2-4% sys err for $t = 8-10$

EE system ($S = -4$)

$\Xi\Xi$ system (1S_0)



Strong Attraction

yet Unbound

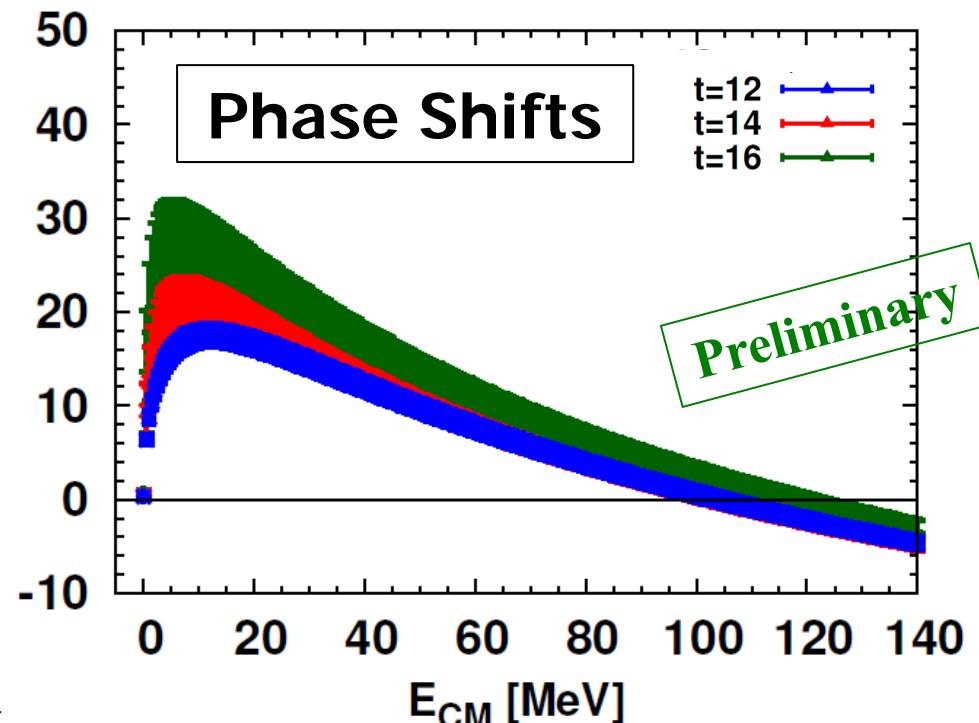
\Longleftrightarrow $\Xi\Xi$ correlation in HIC

$m(\text{eff})$ for single Ξ : ~0.3-1% sys err for $t=14-18$

t -dependence will be checked again w/ larger #stat

Flavor SU(3)-partner of dineutron

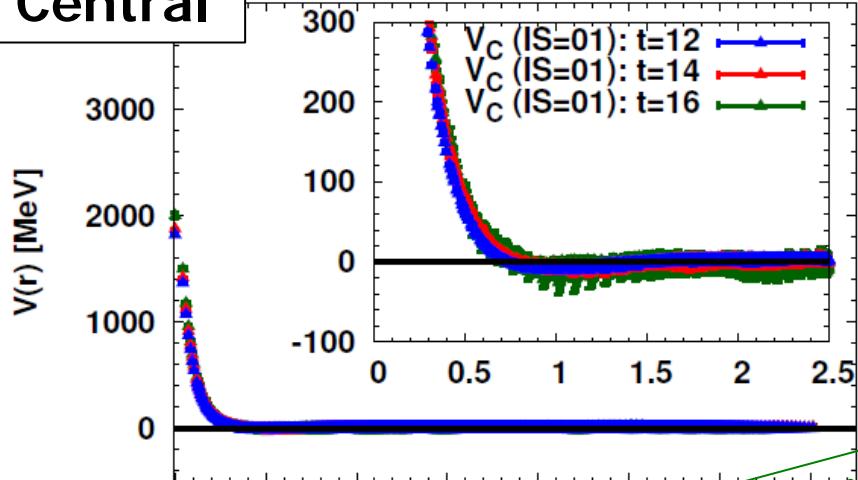
- ➡ • “Doorway” to NN-forces
- Bound by SU(3) breaking ?



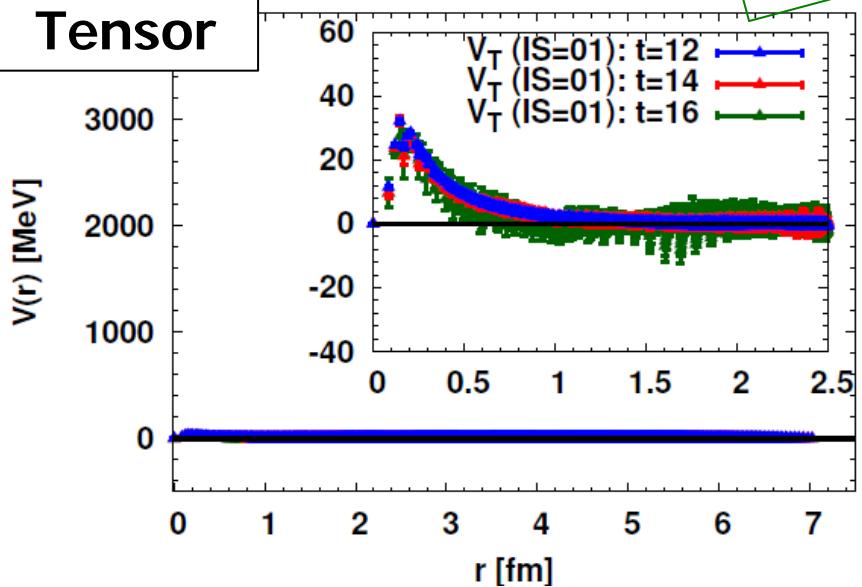
$\Xi\Xi$ system (3S_1 - 3D_1)

Potentials

Central



Tensor



10plet \Leftrightarrow unique w/ hyperon DoF

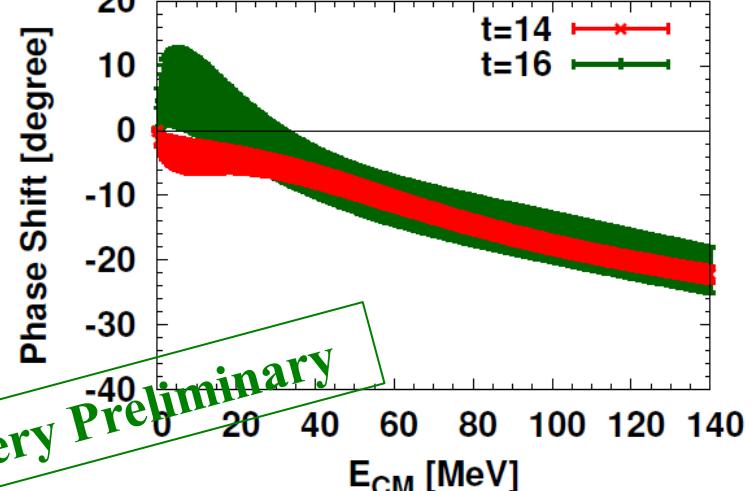
Flavor SU(3)-partner of Σ^- n

→ • Σ^- in neutron star ?

Central: Strong Repulsion
Tensor: Weak

Phase Shifts

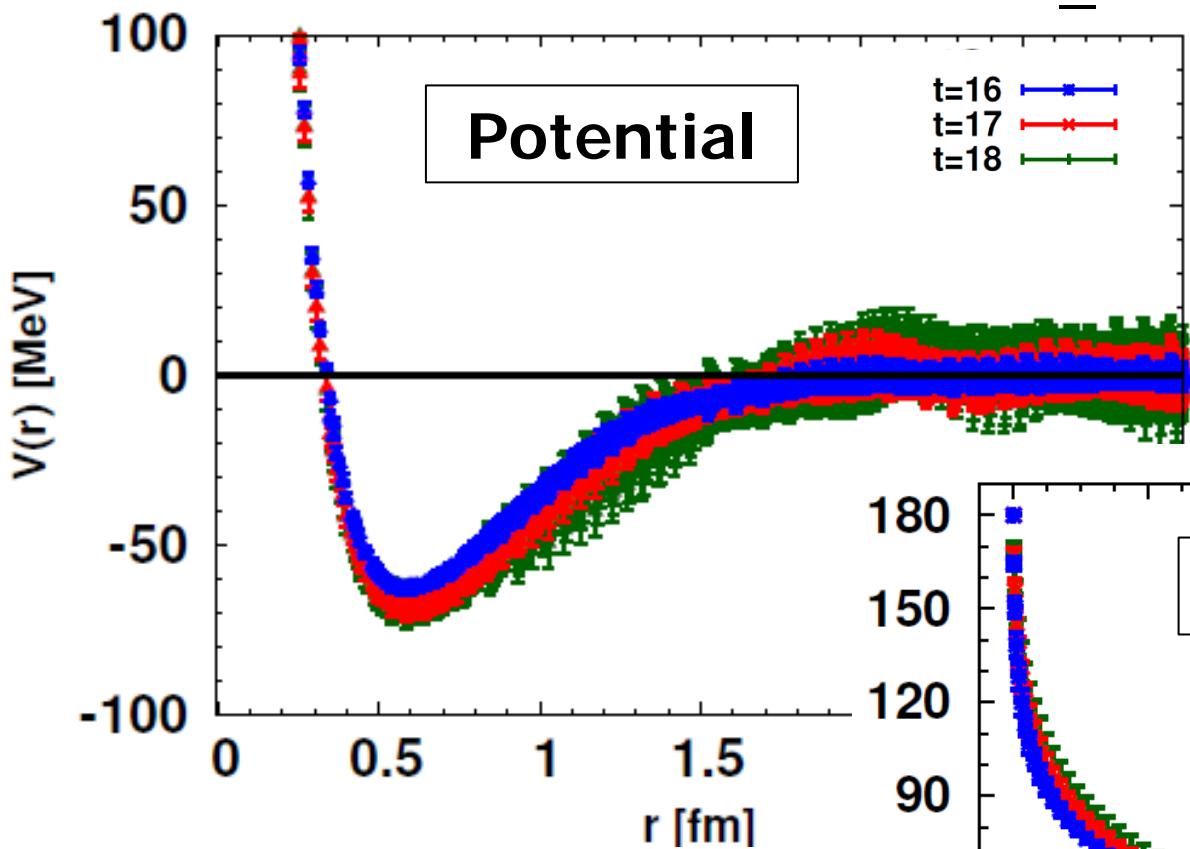
(effective 3S_1)



Very Preliminary

$\Omega\Omega$ system (1S_0)

The “most strange”
dibaryon system

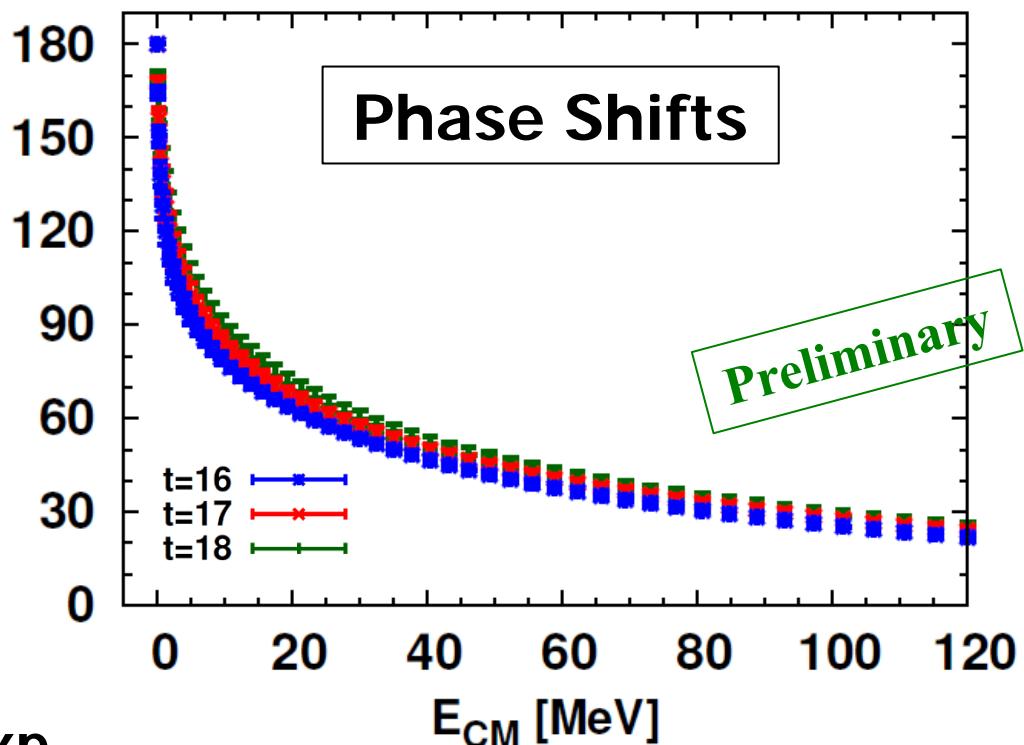


[S. Gongyo / K. Sasaki]

Strong Attraction

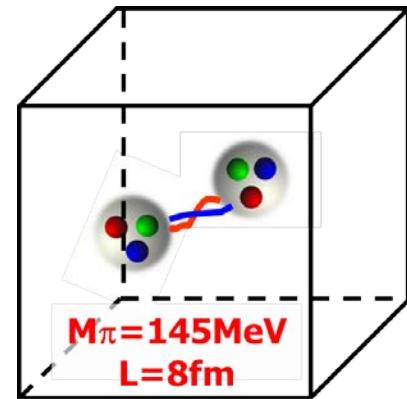
→ Vicinity of bound/unbound
[~ Unitary limit]

↔ $\Omega\Omega$ correlation in HIC exp.



Summary

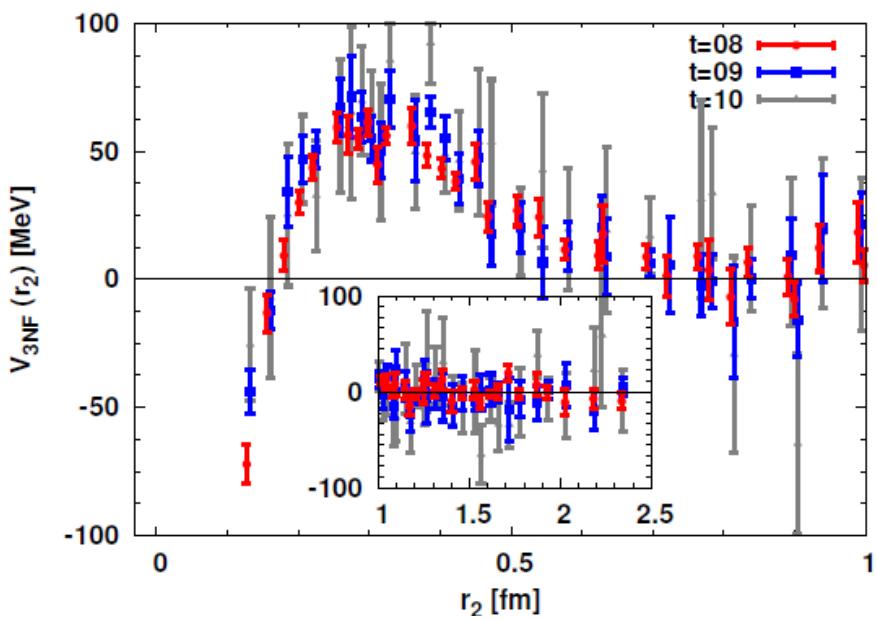
- The 1st LQCD for Baryon Forces at \sim phys. point
 - $m(\pi) \sim= 145$ MeV, $L \sim= 8$ fm, $1/a \sim= 2.3$ GeV
 - [Predictions](#) in particular for [Hyperon Forces](#)
- NN systems
 - Tensor forces clearly visible
- $\Xi\Xi$ systems
 - 1S_0 : strong attraction but unbound
 - 3S_1 : strong repulsion $\Leftrightarrow \Sigma^-$ in neutron stars unlikely
- $\Omega\Omega$ system
 - 1S_0 : strong attraction; \sim unitary limit system
- Prospects
 - #stat will be $\sim x2$ -4 in FY2016
 - Exascale computing Era ~ 2020
 - LS-forces, Parity-odd channel, Three-body forces → LQCD EoS



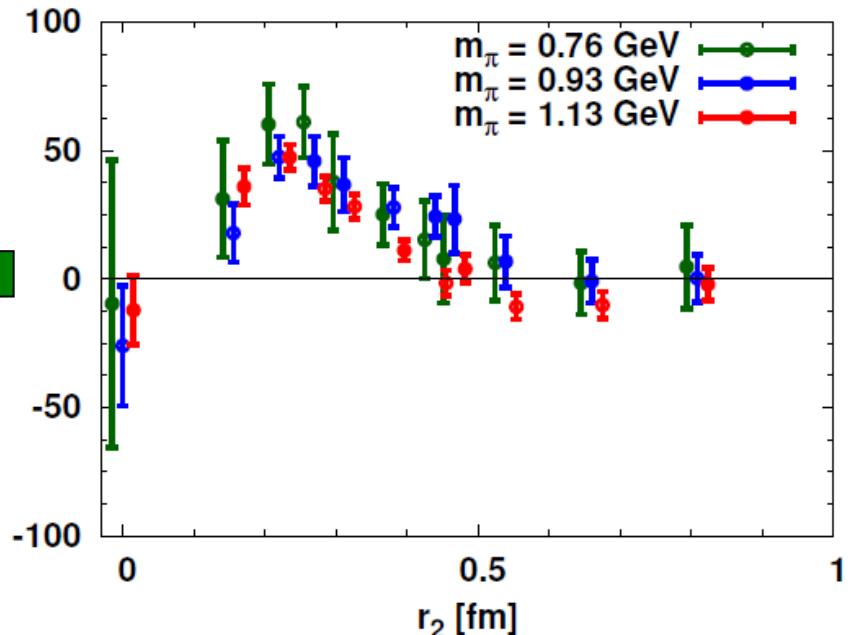
3N-forces (3NF)

Preliminary

Nf=2+1, $m_\pi=0.51$ GeV



Nf=2, $m_\pi=0.76-1.1$ GeV

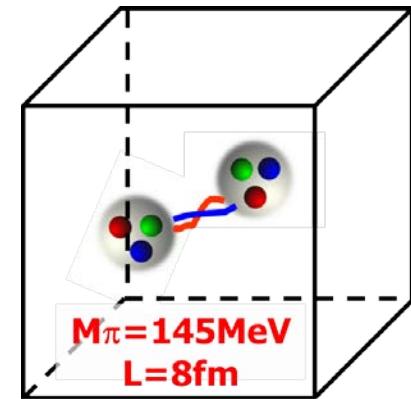


Short-range repulsive 3NF

Kernel (B/F ~ = 4): ~50% efficiency achieved !

Summary

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Nuclear Physics from LQCD
New Era is dawning !