

# Excited and exotic Charmonium, $D_s$ and $D$ meson spectra for two light quark masses

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# Outline of talk

- Why charmed mesons?
- Method and Lattice Details
- Results from  $M_\pi \sim 240\text{MeV}$
- Comparison with  $M_\pi \sim 400\text{MeV}$

# Why mesons with charm quarks?

- Open-charm mesons and Charmonium contain a number of experimentally well-established states.
- However, there are a plethora of unexpected charmonium-like states discovered (X, Y, Z's) and they are subject to many theoretical interpretations.
- Possibilities: hybrid states, tetra-quarks, molecular mesons, hadro-quarkonium.

- Measured masses and widths of the low-lying  $D_{s0}^*(2317)^\pm$  and  $D_{s1}(2460)^\pm$  states are significantly lighter and narrower than expected from phenomenological models. [\[arXiv:hep-ph/0505206v2\]](https://arxiv.org/abs/hep-ph/0505206v2)
- Complete understanding of these states can in principle be achieved using lattice QCD.

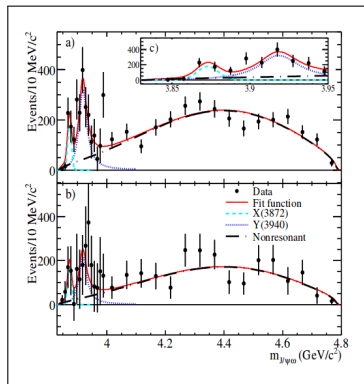


Figure: BaBar  $B^+ \rightarrow J/\psi\omega K$ ,  $B^0 J/\psi\omega K_S^0$  decays [\[arXiv:1012.0074\]](https://arxiv.org/abs/1012.0074)

# Lattice details and Method

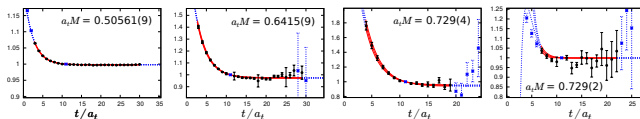
- Goal: Determine spectrum of open and hidden charmed meson states, including excitations and any states with an intrinsic gluonic component at pion mass  $M_\pi \sim 240\text{MeV}$ . Compare with previous study with  $M_\pi \sim 400\text{MeV}$ .  
[arXiv:1301.7670]
- We use the setup of the Hadron Spectrum Collaboration; dynamical 2+1 anisotropic lattices [arXiv:1004.4930v1]
- We use distillation to compute correlation functions for a large basis of interpolating operators
- Employing this we solve a GEVP:

$$C_{ij}(t)v_j^n = \lambda(t, t_0)^n C_{ij}(t_0)v_j^n \quad (1)$$

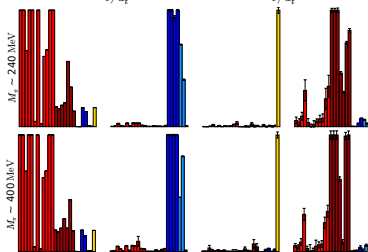
- $\lambda \propto e^{-E_n(t-t_0)}$ ,  $v_j^n$  related to  $Z_i^n = \langle n | O_i^\dagger | 0 \rangle$

| Lattice Volume    | $M_\pi$ (MeV) | $N_{\text{cfgs}}$ | $N_{\text{tsrcs}}$ for $c\bar{c}$ , $c\bar{s}$ , $c\bar{l}$ | $N_{\text{vecs}}$ |
|-------------------|---------------|-------------------|-------------------------------------------------------------|-------------------|
| $24^3 \times 128$ | 391           | 553               | 32, 16, 16                                                  | 162               |
| $32^3 \times 256$ | 236           | 484               | 1, 1, 2                                                     | 384               |

# Operator Overlaps



$M_\pi \sim 240 \text{ MeV}$



$M_\pi \sim 400 \text{ MeV}$

**Figure:** **Top row:** principal correlators for a selection of low-lying charmonium states in the  $T_1^-$  irrep. **Middle row:** the operator-state overlaps,  $Z$ , for the state above. **Bottom row:** overlaps for the corresponding state on the  $M_\pi \sim 400$  MeV ensemble.

# Charmonium Spectrum $M_{\pi} \sim 240\text{MeV}$

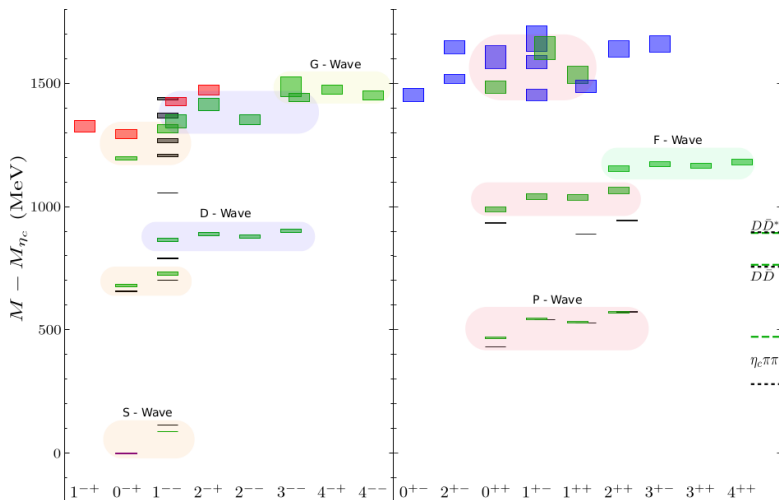
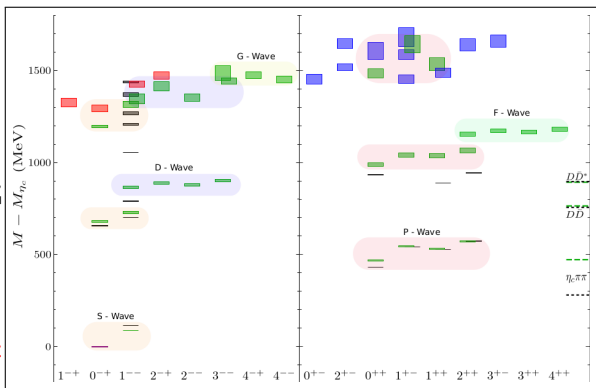


Figure: Charmonium spectrum up to around 4.5 GeV.

# Charmonium Spectrum $M_{\pi} \sim 240\text{MeV}$

- States labeled by  $J^{PC}$
- Masses presented with  $M_{\eta_c}$  subtracted
- Most states follow  $n^{2S+1}L_J$  pattern, grouped into S,P,D,F,G wave multiplets using  $Z_i$
- Red + Blue 'hybrids', some states with **exotic quantum numbers**  
 $1^{-+}, 0^{+-}, 2^{+-}$
- Group hybrids into multiplets, pattern consistent with  $q\bar{q}$  coupled to  $1^{+-}$  gluonic excitation



# $D_s$ spectrum $M_\pi \sim 240\text{MeV}$

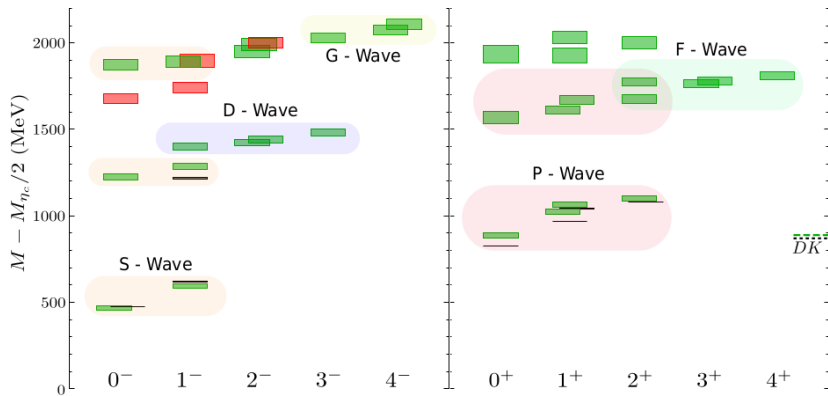
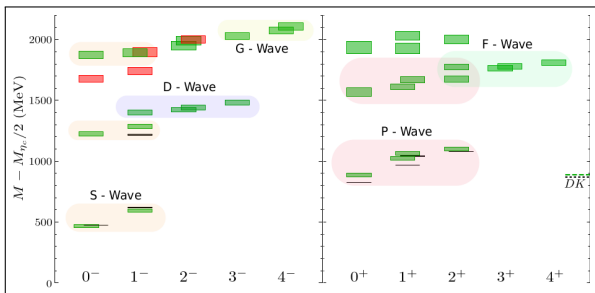


Figure:  $D_s$  meson spectrum.



# $D_s$ spectrum $M_{\pi} \sim 240\text{MeV}$

- Identify complete S,P,D and F wave multiplets
- Four states highlighted in red that do not fit  $n^{2S+1}L_J$  pattern
- Again: Identified as lightest hybrid meson multiplet, consistent with  $q\bar{q}$  (in S-wave) coupled to  $1^{+-}$  gluonic excitation
  - Not able to identify first excited hybrid multiplet



# D meson spectrum $M_{\pi} \sim 240\text{MeV}$

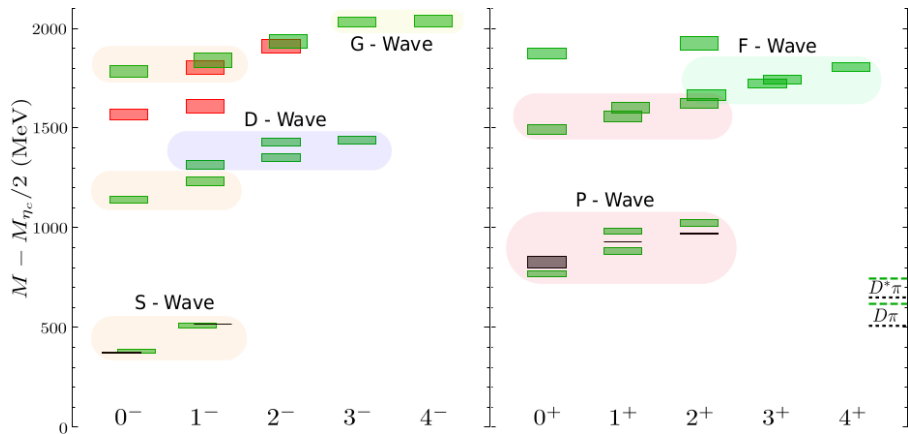


Figure:  $D$  meson spectrum.

# Charmonium comparison

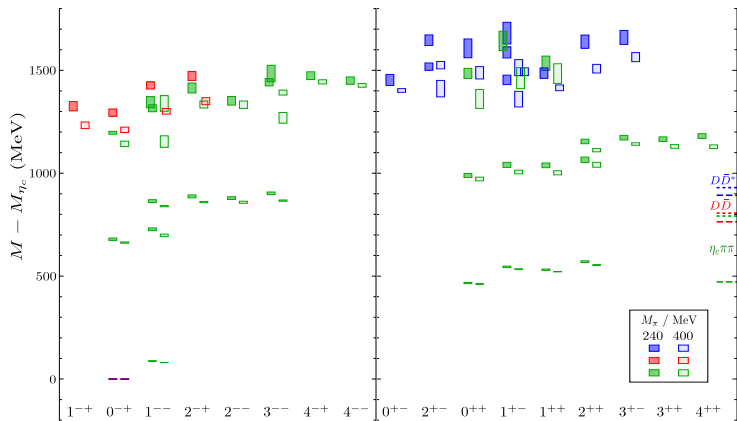
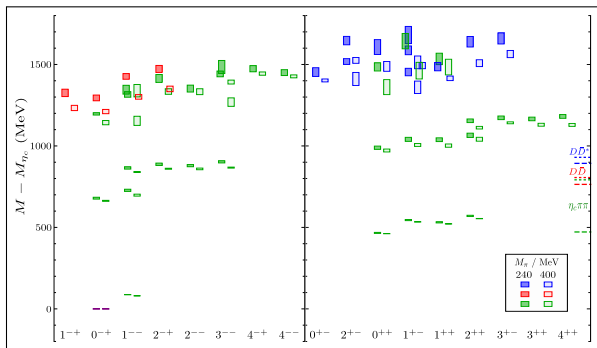


Figure: Charmonium spectrum, with  $M_{\pi} \sim 240$  MeV (left column for each  $J^{PC}$ ) compared to the spectrum with  $M_{\pi} \sim 400$  MeV (right column for each  $J^{PC}$ ).

# Charmonium comparison

- Light quark dep. enters through sea quarks
- Mild light quark dependence, **no change in overall pattern of states**
- $J/\psi$ : statistically significant increase in mass  
 $\sim 80\text{MeV} \rightarrow \sim 87\text{MeV}$
- Checked for possible systematic effects arising from scale setting, no effects found!



# $D_s$ comparison

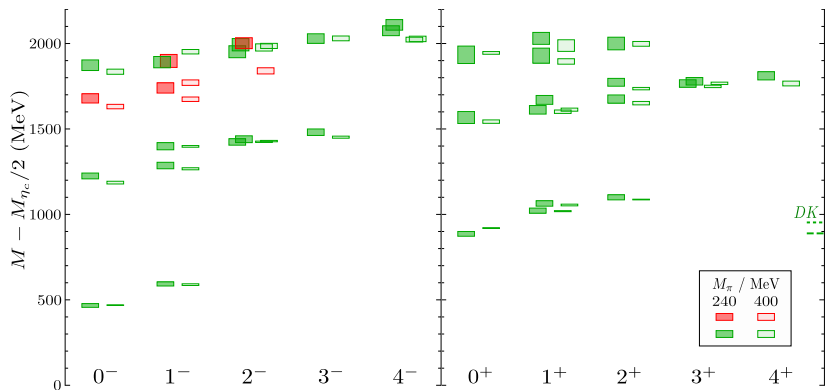
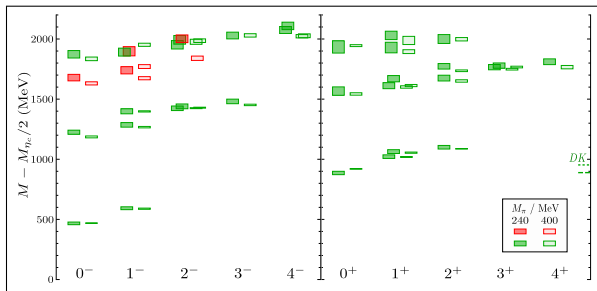


Figure:  $D_s$  meson spectrum labelled by  $J^P$ .

## $D_s$ comparison

- Again, mild light quark dependence, **no change in overall pattern of states**
- Largest change:  $0^+$  corresponding to  $D_{s0}^*(2317)$ , expected influence by  $DK$  threshold
- Tendency for hybrids to increase in mass as  $M_\pi$  is reduced (however pattern unchanged)



# D comparison

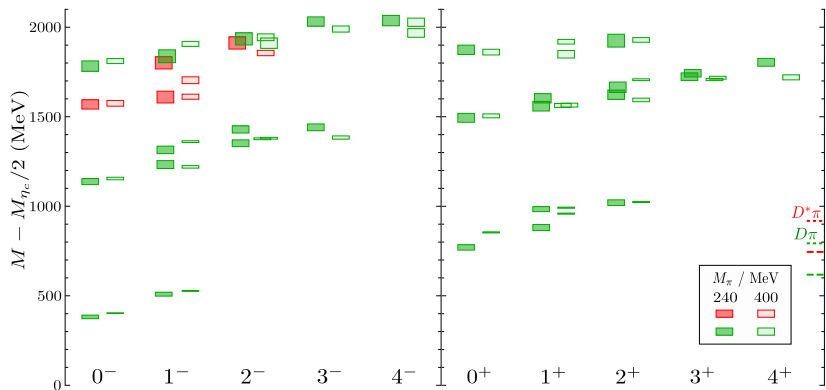
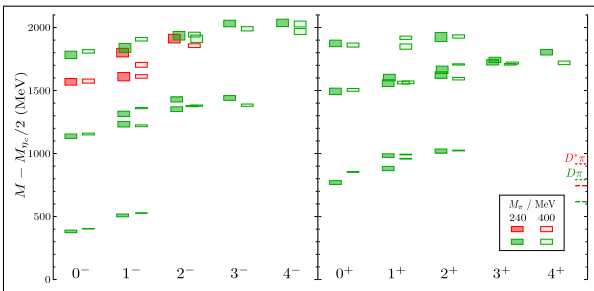


Figure:  $D$  meson spectrum labelled by  $J^P$ .

# D comparison

- D mesons contain light quarks
- Again, we see mild light quark dependence



- Largest change: Lowest  $0^+$  and  $1^+$  states, possibly due to coupling to  $D\pi$  and  $D^*\pi$



# Summary

- Distillation and variational method allow us to extract highly excited spectra and robustly identify the continuum  $J^{P(C)}$  of states up to  $J = 4$
- States with intrinsic gluonic excitations and states with exotic quantum numbers identified
- Many states follow the  $n^{2S+1}L_J$  pattern, also find states which we identify as hybrid mesons that fall into hybrid supermultiplets, pattern consistent with a quark-antiquark combination coupled to a  $1^{+-}$  gluonic excitation
- Only mild differences between the spectra calculated on an ensemble where  $M_\pi \sim 240$  MeV to our previously determined spectra on an ensemble with  $M_\pi \sim 400$  MeV
- Even in the case of the  $D$  meson we find only minor quantitative changes
- At least between  $240 \text{ MeV} \lesssim M_\pi \lesssim 400 \text{ MeV}$ , the mass of the light quarks play very little role in the overall pattern of structure of our hidden and open-charm spectra

# Thank You

- Thank You for listening!