

BEYOND THE STANDARD MODEL

Michael Spira (PSI)

I Introduction

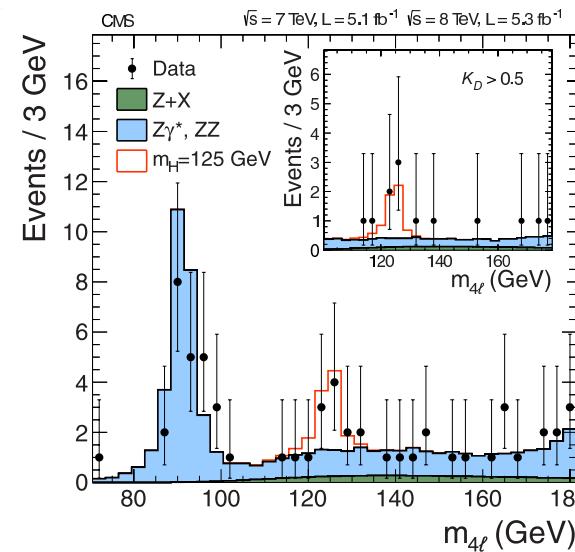
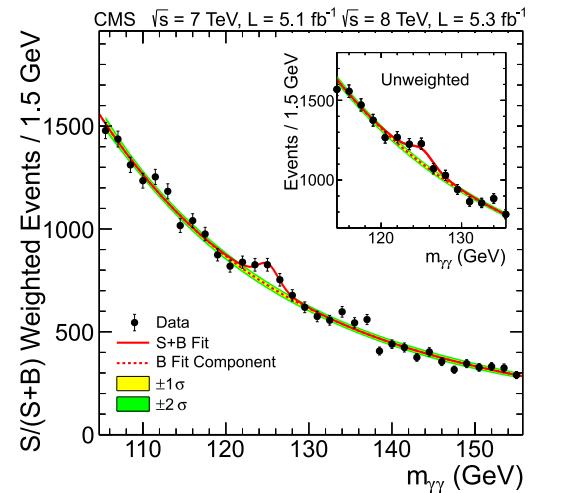
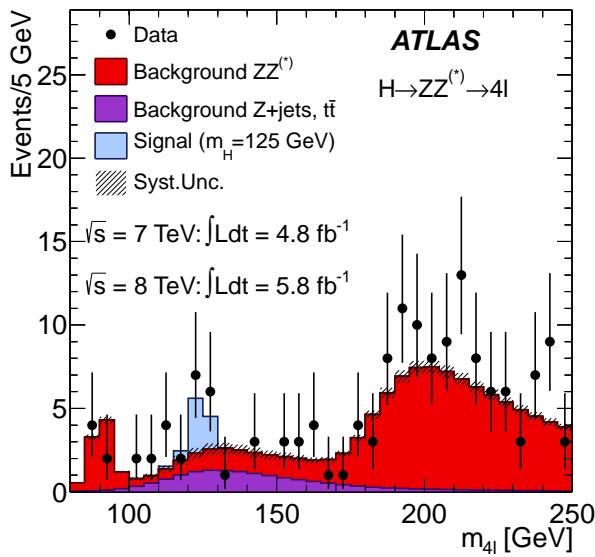
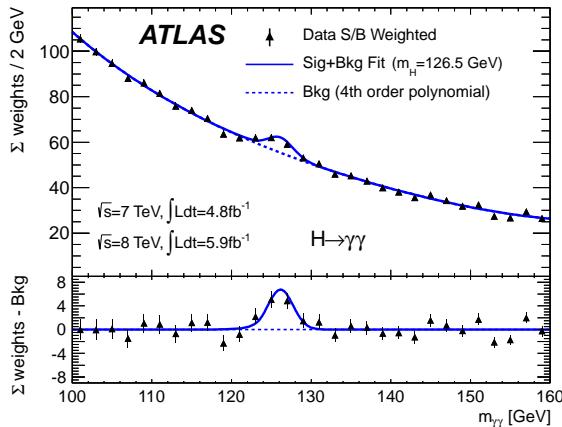
II Higgs Boson Production

III Conclusions

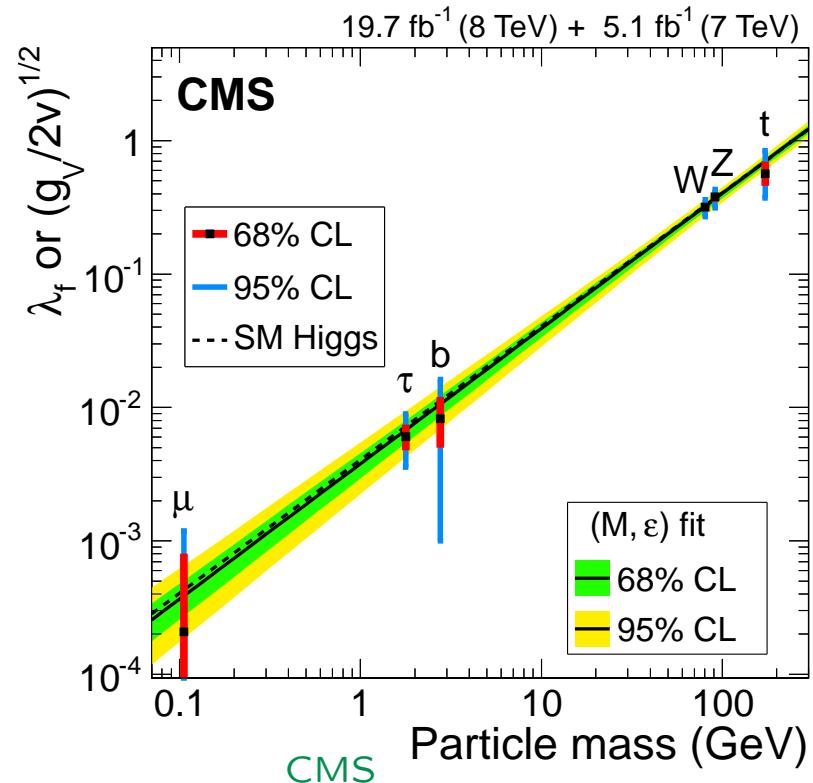
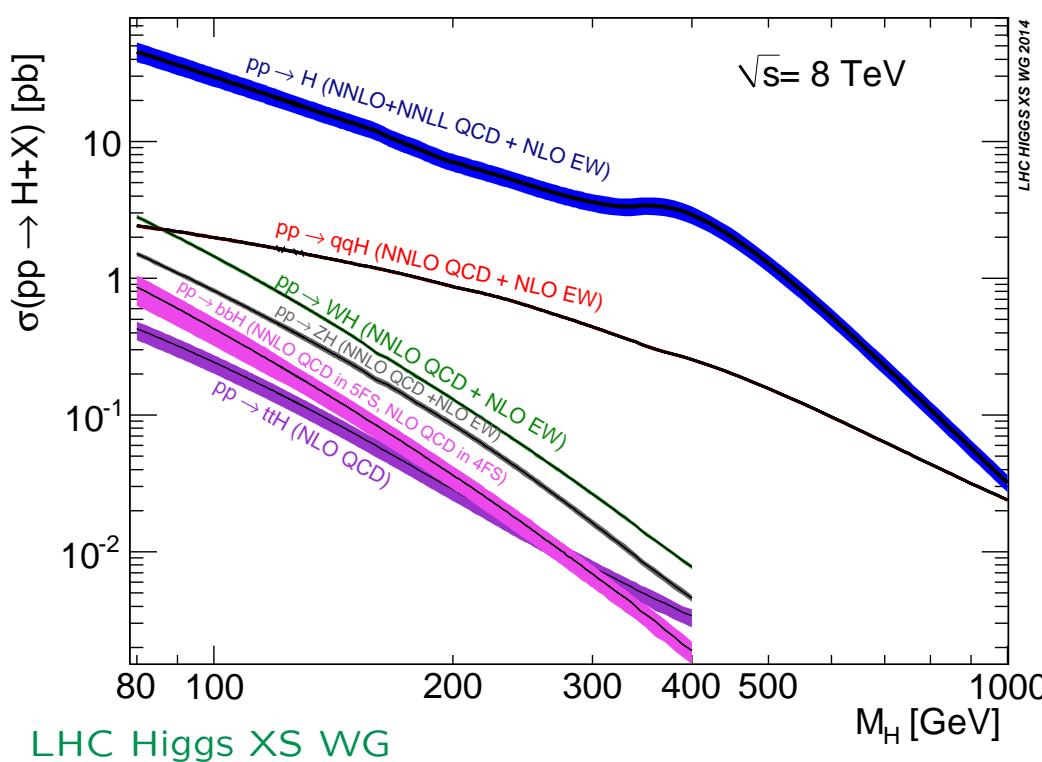
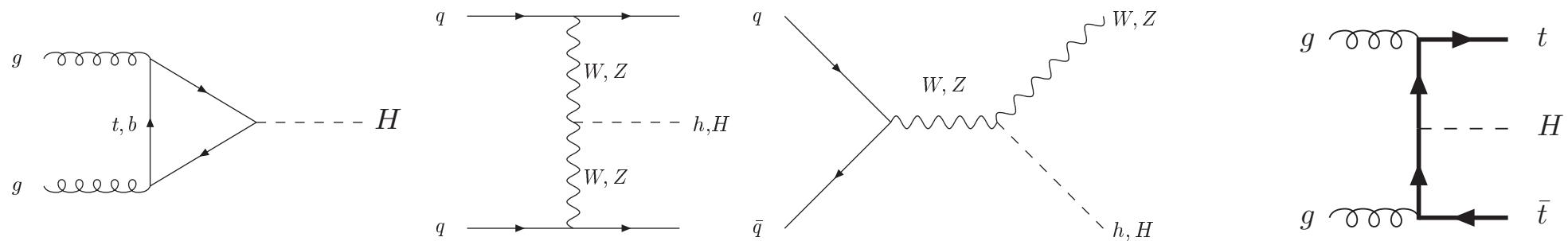
I INTRODUCTION

(i) Standard Model

- we have found the Higgs: $M_H \sim 125$ GeV
- $gg \rightarrow H$ dominant



- Higgs Boson Production

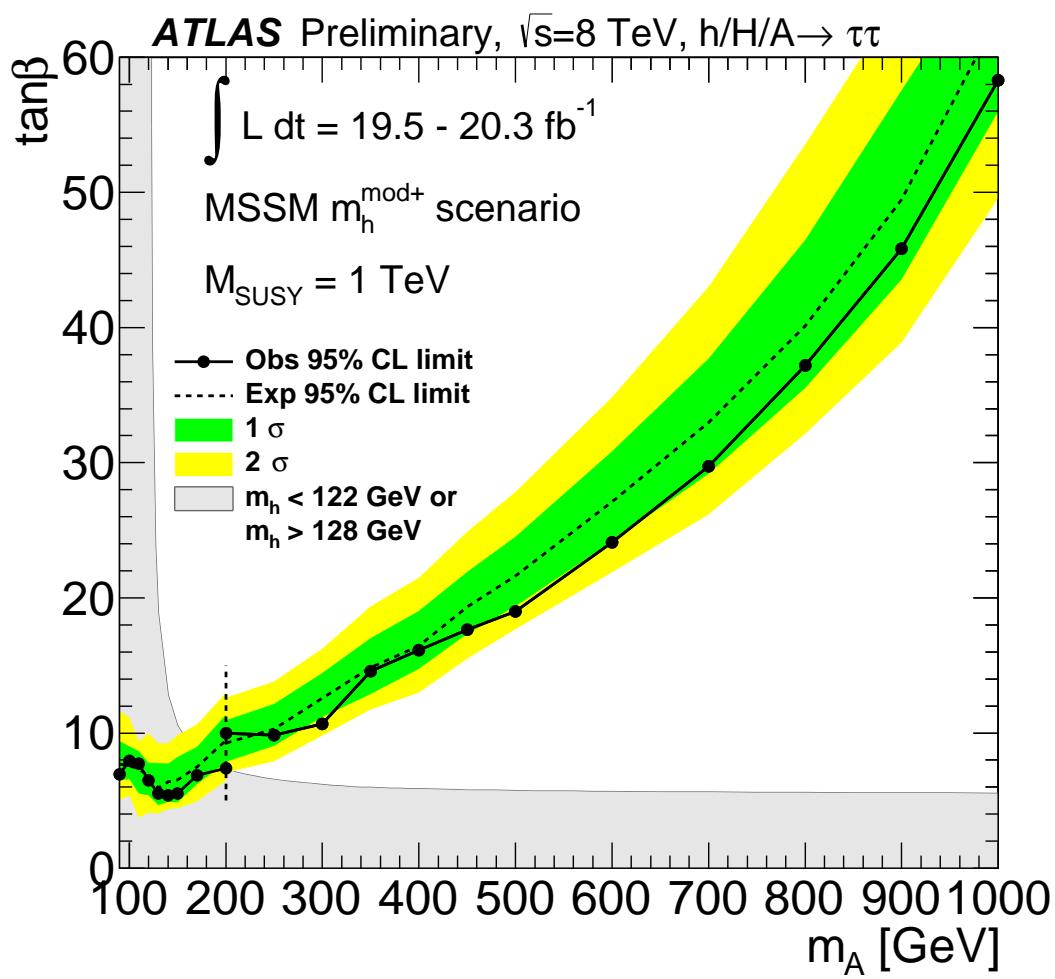


- modifications: (i) higher-dim. operators \rightarrow eff. Lagrangians
(ii) extended Higgs sectors (mixing, loop effects)

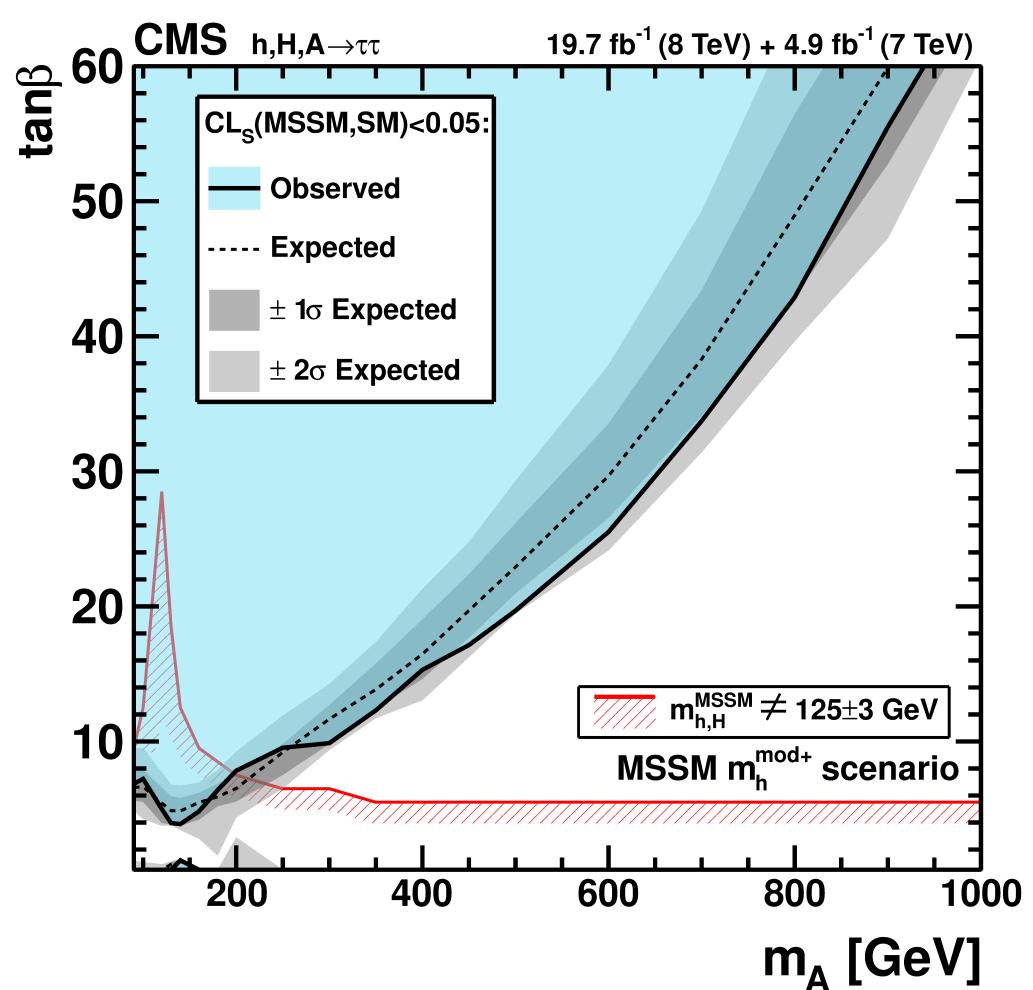
(ii) MSSM

- 2 Higgs doublets $\xrightarrow{\text{ESB}}$ 5 Higgs bosons: h, H, A, H^\pm
- LO: 2 input parameters: $M_A, \tan\beta = \frac{v_2}{v_1}$
- radiative corrections $\propto m_t^4 \log \frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2}$ $\rightarrow M_h \lesssim 135 \text{ GeV}$
 - Haber
 - Carena,...
 - Heinemeyer,...
 - Zhang
 - Slavich,...
 - ...
- Yukawa couplings: $\tan\beta \uparrow \Rightarrow g_u^\phi \downarrow \quad g_d^\phi \uparrow \quad g_V^\phi \downarrow$
- LHC: $gg \rightarrow \phi$ dominant for $\tan\beta \lesssim 10$
 $gg \rightarrow \phi b\bar{b}$ dominant for $\tan\beta \gtrsim 10$
- [NMSSM: additional Higgs singlet \rightarrow 7 Higgs bosons]

$gg \rightarrow b\bar{b}\phi^0, \quad gg \rightarrow \phi^0$

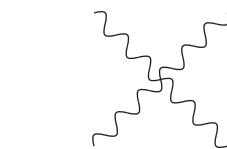
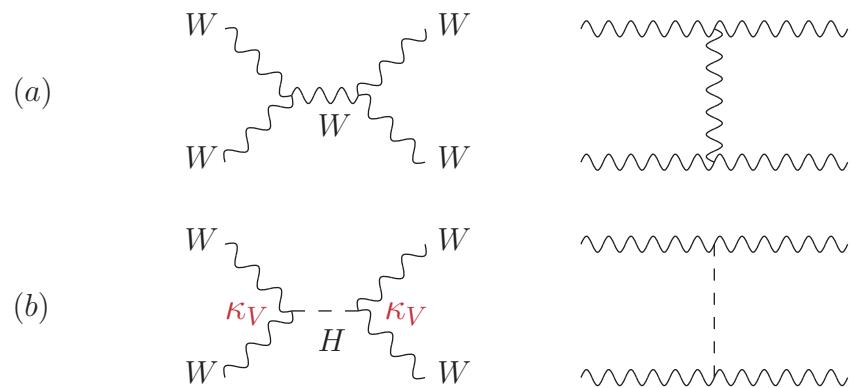


$\phi^0 \rightarrow \tau^+\tau^-$



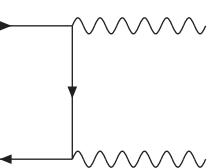
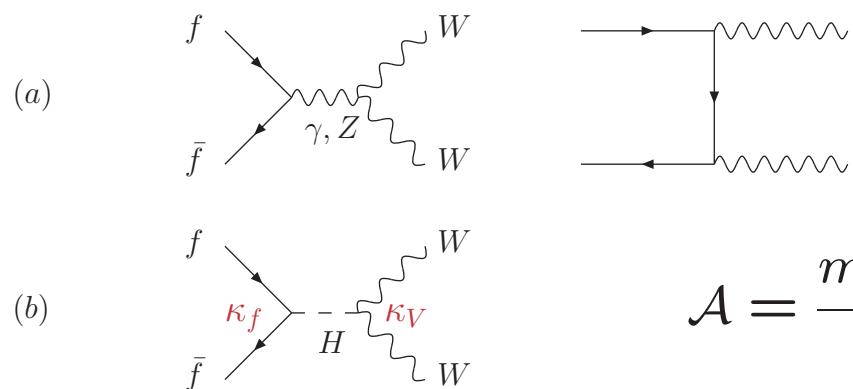
(iii) HEFT

- $WW \rightarrow WW$ @ high energies



$$\mathcal{A} = \frac{s}{v^2} \left\{ 1 - \frac{\kappa_V^2 s}{s - M_H^2} \right\} \Rightarrow \kappa_V = 1$$

- $f\bar{f} \rightarrow WW$ @ high energies



$$\mathcal{A} = \frac{m_f \sqrt{s}}{v^2} \left\{ 1 - \frac{\kappa_f \kappa_V s}{s - M_H^2} \right\} \Rightarrow \kappa_f = \kappa_V = 1$$

- analogous for κ_H

weakly interacting theories

- effective higher dimension operators up to dim 6

Buchmüller, Wyler
Grzadkowski, Iskrzynski, Misiak, Rosiek
Giudice, Grojean, Pomarol, Rattazzi

$$\begin{aligned}\mathcal{L} &= \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \sum_i \alpha_i O_i \\ &\equiv \mathcal{L}_{SM} + \sum_i \bar{c}_i O_i \\ &\equiv \mathcal{L}_{SM} + \Delta\mathcal{L}_{SILH} + \Delta\mathcal{L}_{F_1} + \Delta\mathcal{L}_{F_2} + \Delta\mathcal{L}_{bos} + \Delta\mathcal{L}_{4f} + \Delta\mathcal{L}_{CP}\end{aligned}$$

[assume Λ large]

- assume Higgs $SU(2)$ -doublet

$$H = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

$$\begin{aligned}
\Delta \mathcal{L}_{SILH} &= \frac{\bar{c}_H}{2v^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{\bar{c}_T}{2v^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) - \frac{\bar{c}_6 \lambda}{v^2} (H^\dagger H)^3 \\
&\quad + \left(\frac{\bar{c}_u}{v^2} y_u H^\dagger H \bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} y_d H^\dagger H \bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} y_l H^\dagger H \bar{L}_L H l_R + h.c. \right) \\
&\quad + \frac{i\bar{c}_W g}{2m_W^2} \left(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \right) (D^\nu W_{\mu\nu})^i + \frac{i\bar{c}_B g'}{2m_W^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) (\partial^\nu B_{\mu\nu}) \\
&\quad + \frac{i\bar{c}_{HW} g}{m_W^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{i\bar{c}_{HB} g'}{m_W^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\
&\quad + \frac{\bar{c}_\gamma g'^2}{m_W^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g g_S^2}{m_W^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu} \\
\Delta \mathcal{L}_{F_1} &= \frac{i\bar{c}_{Hq}}{v^2} (\bar{q}_L \gamma^\mu q_L) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) + \frac{i\bar{c}'_{Hq}}{v^2} (\bar{q}_L \gamma^\mu \sigma^i q_L) \left(H^\dagger \sigma^i \overleftrightarrow{D}_\mu H \right) \\
&\quad + \frac{i\bar{c}_{Hu}}{v^2} (\bar{u}_R \gamma^\mu u_R) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) + \frac{i\bar{c}_{Hd}}{v^2} (\bar{d}_R \gamma^\mu d_R) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) \\
&\quad + \left(\frac{i\bar{c}_{Hud}}{v^2} (\bar{u}_R \gamma^\mu d_R) \left(H^c \overleftrightarrow{D}_\mu H \right) + h.c. \right) \\
&\quad + \frac{i\bar{c}_{HL}}{v^2} (\bar{L}_L \gamma^\mu L_L) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) + \frac{i\bar{c}'_{HL}}{v^2} (\bar{L}_L \gamma^\mu \sigma^i L_L) \left(H^\dagger \sigma^i \overleftrightarrow{D}_\mu H \right) \\
&\quad + \frac{i\bar{c}_{Hl}}{v^2} (\bar{l}_R \gamma^\mu l_R) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) \\
\Delta \mathcal{L}_{F_2} &= \frac{\bar{c}_{uB} g'}{m_W^2} y_u \bar{q}_L H^c \sigma^{\mu\nu} u_R B_{\mu\nu} + \frac{\bar{c}_{uW} g}{m_W^2} y_u \bar{q}_L \sigma^i H^c \sigma^{\mu\nu} u_R W_{\mu\nu}^i + \frac{\bar{c}_{uG} g_S}{m_W^2} y_u \bar{q}_L H^c \sigma^{\mu\nu} \lambda^a u_R G_{\mu\nu}^a \\
&\quad + \frac{\bar{c}_{dB} g'}{m_W^2} y_d \bar{q}_L H \sigma^{\mu\nu} d_R B_{\mu\nu} + \frac{\bar{c}_{dW} g}{m_W^2} y_d \bar{q}_L \sigma^i H \sigma^{\mu\nu} d_R W_{\mu\nu}^i + \frac{\bar{c}_{dG} g_S}{m_W^2} y_d \bar{q}_L H \sigma^{\mu\nu} \lambda^a d_R G_{\mu\nu}^a \\
&\quad + \frac{\bar{c}_{lB} g'}{m_W^2} y_l \bar{L}_L H \sigma^{\mu\nu} l_R B_{\mu\nu} + \frac{\bar{c}_{lW} g}{m_W^2} y_l \bar{L}_L \sigma^i H \sigma^{\mu\nu} l_R W_{\mu\nu}^i + h.c.
\end{aligned}$$

$$\begin{aligned}\Delta\mathcal{L}_{bos} &= \frac{\bar{c}_{3W} g^3}{m_W^2} \epsilon^{ijk} W_\mu^{i\nu} W_\nu^{j\rho} W_\rho^{k\mu} + \frac{\bar{c}_{3G} g_S^3}{m_W^2} f^{abc} G_\mu^{a\nu} G_\nu^{b\rho} G_\rho^{c\mu} \\ &+ \frac{\bar{c}_{2W}}{m_W^2} (D^\mu W_{\mu\nu})^i (D_\rho W^{\rho\nu})^i + \frac{\bar{c}_{2B}}{m_W^2} (\partial^\mu B_{\mu\nu}) (\partial_\rho B^{\rho\nu}) + \frac{\bar{c}_{2G}}{m_W^2} (D^\mu G_{\mu\nu})^a (D_\rho G^{\rho\nu})^a\end{aligned}$$

$$\Delta\mathcal{L}_{4f} = \sum_{\psi, L/R, T^a} \bar{\psi}_i \gamma^\mu T^a \psi_j \bar{\psi}_k \gamma_\mu T^a \psi_l + \bar{\psi}_i T^a \psi_j \bar{\psi}_k T^a \psi_l$$

$$\Delta\mathcal{L}_{CP} = \frac{i\tilde{c}_{HW} g}{m_W^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) \tilde{W}_{\mu\nu}^i + \frac{i\tilde{c}_{HB} g'}{m_W^2} (D^\mu H)^\dagger (D^\nu H) \tilde{B}_{\mu\nu}$$

$$+ \frac{\tilde{c}_\gamma g'^2}{m_W^2} H^\dagger H B_{\mu\nu} \tilde{B}^{\mu\nu} + \frac{\tilde{c}_g g_S^2}{m_W^2} H^\dagger H G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

$$+ \frac{\tilde{c}_{3W} g^3}{m_W^2} \epsilon^{ijk} W_\mu^{i\nu} W_\nu^{j\rho} \tilde{W}_\rho^{k\mu} + \frac{\tilde{c}_{3G} g_S^3}{m_W^2} f^{abc} G_\mu^{a\nu} G_\nu^{b\rho} \tilde{G}_\rho^{c\mu}$$

$$\tilde{V}_{\mu\nu} = \frac{1}{2} \epsilon_{\mu\nu\alpha\beta} V^{\alpha\beta}$$

- after using EOM: 53 (59) independent dim6 operators

- power counting: $H \rightarrow \mathcal{O}(g_*/M = 1/f)$, $\partial_\mu \rightarrow \mathcal{O}(1/M)$

\Rightarrow expansion in H/f and E/M

$$\bar{c}_H, \bar{c}_T, \bar{c}_6, \bar{c}_\psi \sim O\left(\frac{v^2}{f^2}\right), \quad \bar{c}_W, \bar{c}_B \sim O\left(\frac{m_W^2}{M^2}\right), \quad \bar{c}_{HW}, \bar{c}_{HB}, \bar{c}_\gamma, \bar{c}_g \sim O\left(\frac{m_W^2}{16\pi^2 f^2}\right)$$

$$\bar{c}_{H\psi}, \bar{c}'_{H\psi} \sim O\left(\frac{\lambda_\psi^2 v^2}{g_*^2 f^2}\right), \quad \bar{c}_{Hud} \sim O\left(\frac{\lambda_u \lambda_d v^2}{g_*^2 f^2}\right), \quad \bar{c}_{\psi W}, \bar{c}_{\psi B}, \bar{c}_{\psi G} \sim O\left(\frac{m_W^2}{16\pi^2 f^2}\right)$$

Giudice, Grojean, Pomarol, Rattazzi

- canonical normalization, unitary gauge:

$$\begin{aligned} v^2 &= v_{SM}^2 \left(1 + \frac{3}{4} \bar{c}_6\right) \\ h_{SM} &= h \left[1 - \frac{\bar{c}_H}{2} - \frac{\bar{c}_T}{8}\right] - \frac{3}{8} \bar{c}_6 v \\ m_h^2 &= m_{h_{SM}}^2 \left[1 - \bar{c}_H + \frac{3}{2} \bar{c}_6 - \frac{1}{2} \bar{c}_T\right] \end{aligned}$$

etc.

$$\begin{aligned}
\mathcal{L} = & \frac{1}{2}\partial_\mu h \partial^\mu h - \frac{1}{2}m_h^2 h^2 - c_3 \frac{1}{6} \left(\frac{3m_h^2}{v} \right) h^3 - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \bar{\psi}^{(i)} \psi^{(i)} \left(1 + c_\psi \frac{h}{v} + \dots \right) \\
& + m_W^2 W_\mu W^\mu \left(1 + 2c_W \frac{h}{v} + \dots \right) + \frac{1}{2}m_Z^2 Z_\mu Z^\mu \left(1 + 2c_Z \frac{h}{v} + \dots \right) + \dots \\
& + \left(c_{WW} W_{\mu\nu}^+ W^{-\mu\nu} + \frac{c_{ZZ}}{2} Z_{\mu\nu} Z^{\mu\nu} + c_{Z\gamma} Z_{\mu\nu} \gamma^{\mu\nu} + \frac{c_{\gamma\gamma}}{2} \gamma_{\mu\nu} \gamma^{\mu\nu} + \frac{c_{gg}}{2} G_{\mu\nu}^a G^{a\mu\nu} \right) \frac{h}{v} \\
& + \left(c_{W\partial W} (W_\nu^- D_\mu W^{+\mu\nu} + h.c.) + c_{Z\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} + c_{Z\partial\gamma} Z_\nu \partial_\mu \gamma^{\mu\nu} \right) \frac{h}{v} + \dots
\end{aligned}$$

Higgs couplings	$\Delta\mathcal{L}_{SILH}$	MCHM4	MCHM5
c_W	$1 - \bar{c}_H/2$	$\sqrt{1-\xi}$	$\sqrt{1-\xi}$
c_Z	$1 - \bar{c}_H/2 - 2\bar{c}_T$	$\sqrt{1-\xi}$	$\sqrt{1-\xi}$
c_ψ ($\psi = u, d, l$)	$1 - (\bar{c}_H/2 + \bar{c}_\psi)$	$\sqrt{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$
c_3	$1 + \bar{c}_6 - 3\bar{c}_H/2$	$\sqrt{1-\xi}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$
c_{gg}	$8(\alpha_s/\alpha_2)\bar{c}_g$	0	0
$c_{\gamma\gamma}$	$8\sin^2\theta_W \bar{c}_\gamma$	0	0
$c_{Z\gamma}$	$(\bar{c}_{HB} - \bar{c}_{HW} - 8\bar{c}_\gamma \sin^2\theta_W) \tan\theta_W$	0	0
c_{WW}	$-2\bar{c}_{HW}$	0	0
c_{ZZ}	$-2(\bar{c}_{HW} + \bar{c}_{HB} \tan^2\theta_W - 4\bar{c}_\gamma \tan^2\theta_W \sin^2\theta_W)$	0	0
$c_{W\partial W}$	$-2(\bar{c}_W + \bar{c}_{HW})$	0	0
$c_{Z\partial Z}$	$-2(\bar{c}_W + \bar{c}_{HW}) - 2(\bar{c}_B + \bar{c}_{HB}) \tan^2\theta_W$	0	0
$c_{Z\partial\gamma}$	$2(\bar{c}_B + \bar{c}_{HB} - \bar{c}_W - \bar{c}_{HW}) \tan\theta_W$	0	0

strongly interacting theories

$$\begin{aligned}\mathcal{L} = & \frac{1}{2}\partial_\mu h \partial^\mu h - \frac{1}{2}m_h^2 h^2 - c_3 \frac{1}{6} \left(\frac{3m_h^2}{v} \right) h^3 - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \bar{\psi}^{(i)} \psi^{(i)} \left(1 + c_\psi \frac{h}{v} + \dots \right) \\ & + m_W^2 W_\mu W^\mu \left(1 + 2c_W \frac{h}{v} + \dots \right) + \frac{1}{2}m_Z^2 Z_\mu Z^\mu \left(1 + 2c_Z \frac{h}{v} + \dots \right) + \dots \\ & + \left(c_{WW} W_{\mu\nu}^+ W^{-\mu\nu} + \frac{c_{ZZ}}{2} Z_{\mu\nu} Z^{\mu\nu} + c_{Z\gamma} Z_{\mu\nu} \gamma^{\mu\nu} + \frac{c_{\gamma\gamma}}{2} \gamma_{\mu\nu} \gamma^{\mu\nu} + \frac{c_{gg}}{2} G_{\mu\nu}^a G^{a\mu\nu} \right) \frac{h}{v} \\ & + \left(c_{W\partial W} (W_\nu^- D_\mu W^{+\mu\nu} + h.c.) + c_{Z\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} + c_{Z\partial\gamma} Z_\nu \partial_\mu \gamma^{\mu\nu} \right) \frac{h}{v} + \dots\end{aligned}$$

- also valid in case of a non-linear Lagrangian for a light Higgs-like scalar [h generic \mathcal{CP} -even scalar]

⇒ expansion in E/M (derivatives) only, large deviations from SM couplings

SILH: expansion in $v^2/f^2, E^2/M^2, \alpha_s/\pi, \alpha/\pi$

non-lin.: expansion in $E^2/M^2, \alpha_s/\pi$

- $h \rightarrow f\bar{f}$:

$$\begin{aligned}\Gamma(\bar{\psi}\psi)|_{SILH} &= \Gamma_0^{SM}(\bar{\psi}\psi) \left[1 - \bar{c}_H - 2\bar{c}_\psi + \frac{2}{|A_0^{SM}|^2} \text{Re} (A_0^{*SM} A_{1,ew}^{SM}) \right] [1 + \delta_\psi \kappa^{QCD}] \\ &\quad + \mathcal{O}\left(\frac{v^4}{f^4}, \frac{v^2\alpha}{f^2\pi}, \frac{\alpha^2}{\pi^2}\right) \\ \Gamma(\bar{\psi}\psi)|_{NL} &= c_\psi^2 \Gamma_0^{SM}(\bar{\psi}\psi) [1 + \delta_\psi \kappa^{QCD}] + \mathcal{O}\left(\frac{m_h^2}{M^2}, \frac{\alpha}{\pi}\right)\end{aligned}$$

A_0^{SM} : SM tree-level amplitude

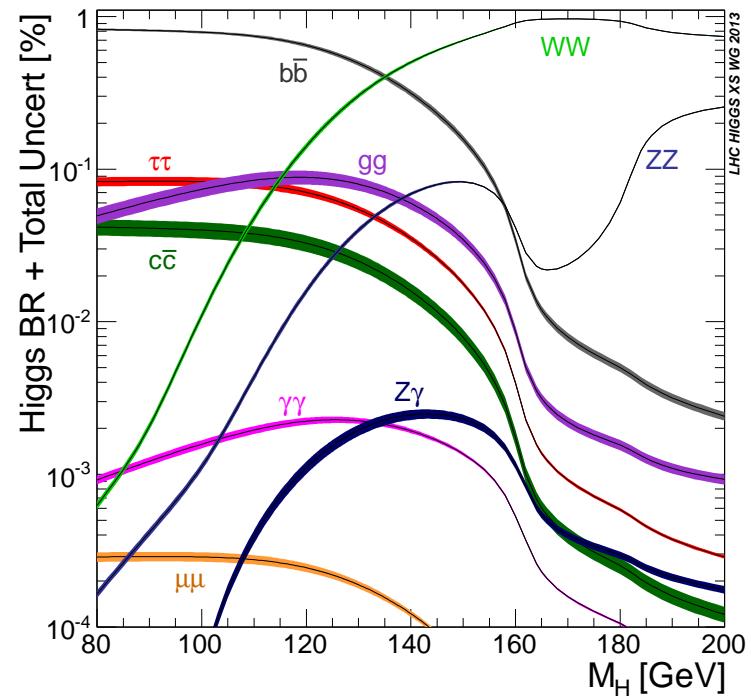
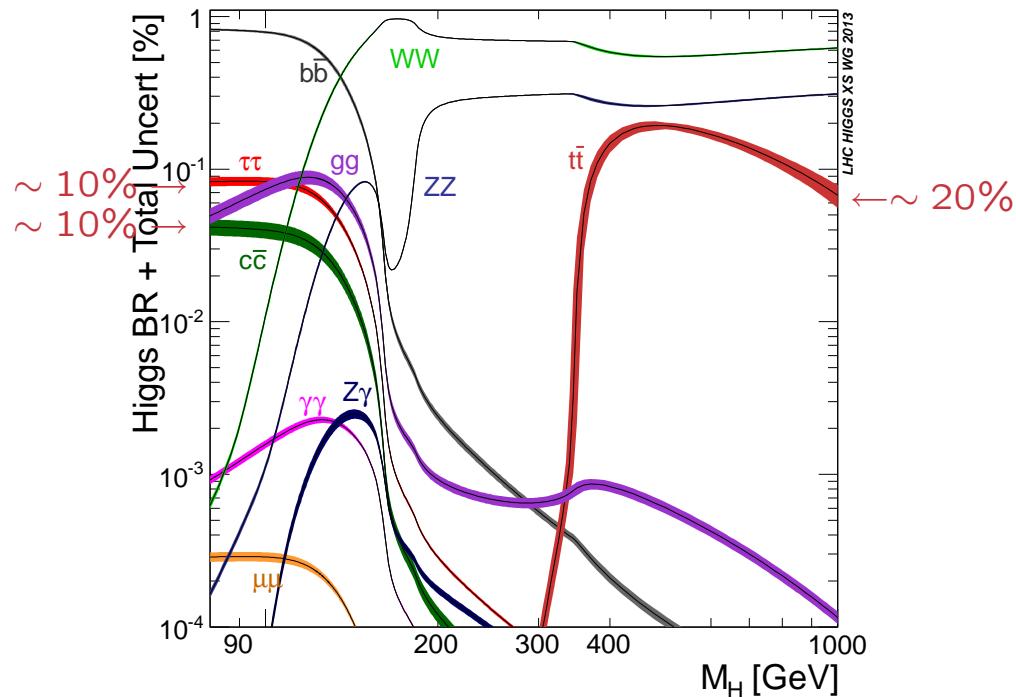
$A_{1,ew}^{SM}$: SM elw. amplitude [real corrections treated analogously]

- factorization of QCD \leftrightarrow elw. [limit small m_h]
- NL: no elw. corrections!

Partial Width	QCD	Electroweak	Total	
$H \rightarrow b\bar{b}/c\bar{c}$	$\sim 0.1\%$	$\sim 1\text{--}2\%$ for $M_H \lesssim 135\text{GeV}$	$\sim 2\%$	NNNNLO / NLO
$H \rightarrow \tau^+\tau^-/\mu^+\mu^-$		$\sim 1\text{--}2\%$ for $M_H \lesssim 135\text{GeV}$	$\sim 2\%$	NLO
$H \rightarrow t\bar{t}$	$\lesssim 5\%$	$\lesssim 2\text{--}5\%$ for $M_H < 500\text{GeV}$ $\sim 0.1(\frac{M_H}{1\text{TeV}})^4$ for $M_H > 500\text{GeV}$	$\sim 5\%$ $\sim 5\text{--}10\%$	(NNN)NLO / LO
$H \rightarrow gg$	$\sim 3\%$	$\sim 1\%$	$\sim 3\%$	NNNLO approx. / NLO
$H \rightarrow \gamma\gamma$	$< 1\%$	$< 1\%$	$\sim 1\%$	NLO / NLO
$H \rightarrow Z\gamma$	$< 1\%$	$\sim 5\%$	$\sim 5\%$	(N)LO / LO
$H \rightarrow WW/ZZ \rightarrow 4f$	$< 0.5\%$	$\sim 0.5\%$ for $M_H < 500\text{GeV}$ $\sim 0.17(\frac{M_H}{1\text{TeV}})^4$ for $M_H > 500\text{GeV}$	$\sim 0.5\%$ $\sim 0.5\text{--}15\%$	(N)NLO

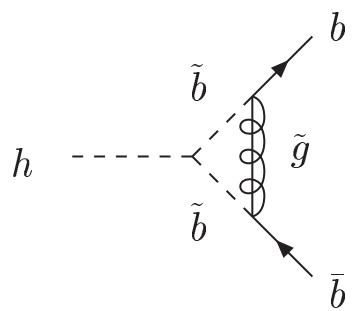
- QCD: variation of Higgs widths for scale by factor 2 and 1/2
elw: missing HO estimated from known structure at NLO
 $M_H \gtrsim 500$ GeV: Higgs self-interactions dominate error
different uncertainties added linearly for each channel
- parametric uncertainties:
 $m_t = 172.5 \pm 2.5$ GeV $\alpha_s(M_Z) = 0.119 \pm 0.002$
 $m_b(m_b) = 4.16 \pm 0.06$ GeV $m_c(m_c) = 1.28 \pm 0.03$ GeV
 different uncertainties added quadratically for each channel
- total uncertainties: parametric & theor. uncertainties added linearly

HDECAY & Prophecy4f



Denner, Heinemeyer, Puljak, Rebuzzi, S.

- MSSM: large SUSY–QCD corrections to $\phi^0 \rightarrow b\bar{b}$



$$\propto \frac{\alpha_s}{\pi} \frac{m_{\tilde{g}} \mu \operatorname{tg}\beta}{M_{SUSY}^2} \sim \Delta_b$$

Hall, ...
Carena, ...
Nierste, ...
Häfliger, ...
Noth, S.
Mihaila, Reisser
etc.

SUSY-QCD Corrections to $b\bar{b}\phi^0$

$[\Delta \lesssim 1\%]$

$$\begin{aligned} \mathcal{L}_{eff} &= -\lambda_b \bar{b}_R \left[\phi_1^0 + \frac{\Delta_b}{\text{tg}\beta} \phi_2^{0*} \right] b_L + h.c. \quad \text{valid to all orders in } \Delta_b \\ &= -m_b \bar{b} \left[1 + i\gamma_5 \frac{G^0}{v} \right] b - \frac{m_b/v}{1 + \Delta_b} \bar{b} \left[g_b^h \left(1 - \frac{\Delta_b}{\text{tg}\alpha \text{tg}\beta} \right) h \right. \\ &\quad \left. + g_b^H \left(1 + \Delta_b \frac{\text{tg}\alpha}{\text{tg}\beta} \right) H - g_b^A \left(1 - \frac{\Delta_b}{\text{tg}^2\beta} \right) i\gamma_5 A \right] b \end{aligned}$$

$$\begin{aligned} \Delta_b &= \Delta_b^{QCD(1)} + \Delta_b^{elw(1)} \\ \Delta_b^{QCD(1)} &= \frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} \mu \text{tg}\beta I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, M_{\tilde{g}}^2) \end{aligned}$$

$$\Delta_b^{elw(1)} = \frac{\lambda_t^2(\mu_R)}{(4\pi)^2} \mu A_t \text{tg}\beta I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, \mu^2)$$

$$I(a, b, c) = -\frac{ab \log \frac{a}{b} + bc \log \frac{b}{c} + ca \log \frac{c}{a}}{(a-b)(b-c)(c-a)}$$

Carena, Garcia, Nierste, Wagner
Guasch, Häfliger, S.

\Rightarrow resummed Yukawa couplings \tilde{g}_b^Φ
[analogous for NMSSM]

small α_{eff} scenario [modified]

$$\tan\beta = 30$$

$$M_{\tilde{Q}} = 800 \text{ GeV}$$

$$M_{\tilde{g}} = 1000 \text{ GeV} \quad \leftarrow$$

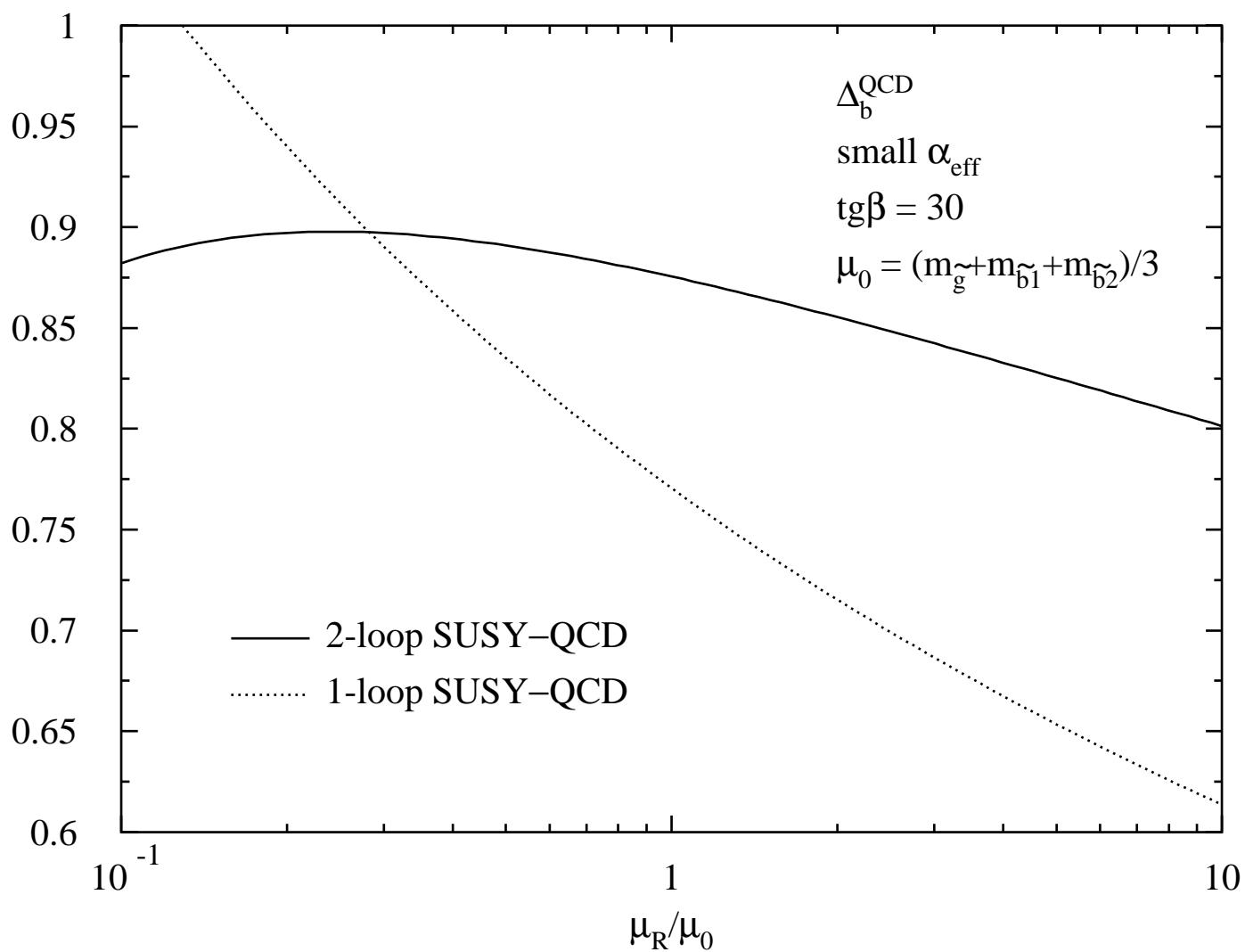
$$M_2 = 500 \text{ GeV}$$

$$A_b = A_t = -1.133 \text{ TeV}$$

$$\mu = 2 \text{ TeV}$$

$$m_{\tilde{t}_1} = 679 \text{ GeV} \quad m_{\tilde{t}_2} = 935 \text{ GeV}$$

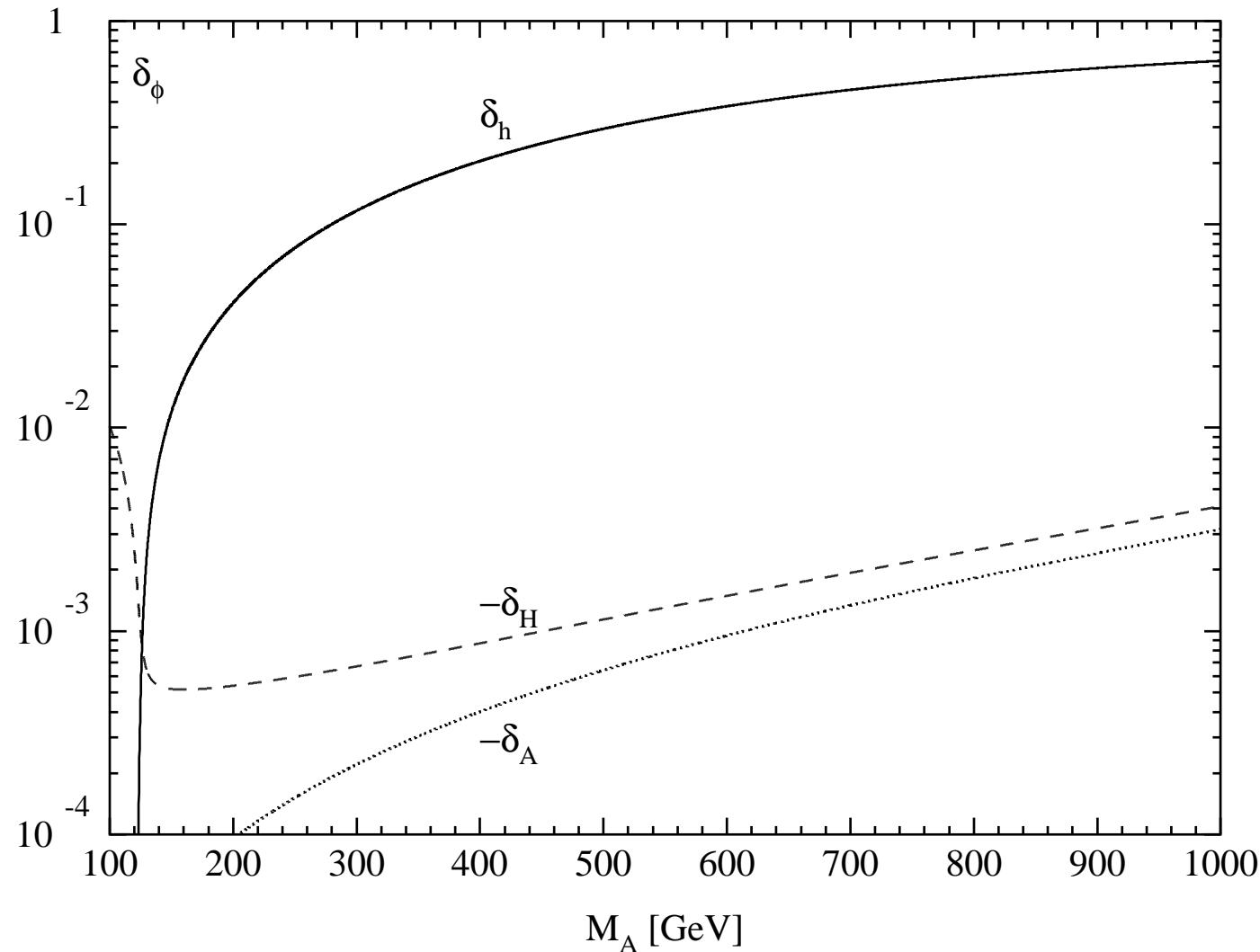
$$m_{\tilde{b}_1} = 601 \text{ GeV} \quad m_{\tilde{b}_2} = 961 \text{ GeV}$$



Noth, S.
(Mihaila, Reisser)

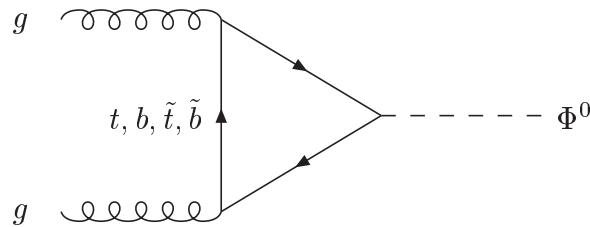
$$\Gamma[\Phi \rightarrow b\bar{b}] = \frac{3G_F M_\Phi}{4\sqrt{2}\pi} \overline{m}_b^2(M_\Phi) \Delta_{\text{QCD}} \tilde{g}_b^{\Phi 2} [1 + \delta_\Phi]$$

$$M_A^2 \gg M_Z^2 : \operatorname{tg}\alpha \rightarrow -\frac{1}{\operatorname{tg}\beta} \quad \Rightarrow \quad \tilde{g}_b^h \rightarrow \frac{1}{1 + \Delta_b} \left(1 - \frac{\Delta_b}{\operatorname{tg}\alpha \operatorname{tg}\beta} \right) \rightarrow 1$$



II HIGGS BOSON PRODUCTION

(i) $gg \rightarrow h/H/A$



Georgi, ...
Gamberini, ...
S., Djouadi, Graudenz, Zerwas
Dawson, Kauffman
Harlander, Kilgore
Anastasiou, Melnikov
Ravindran, Smith, van Neerven

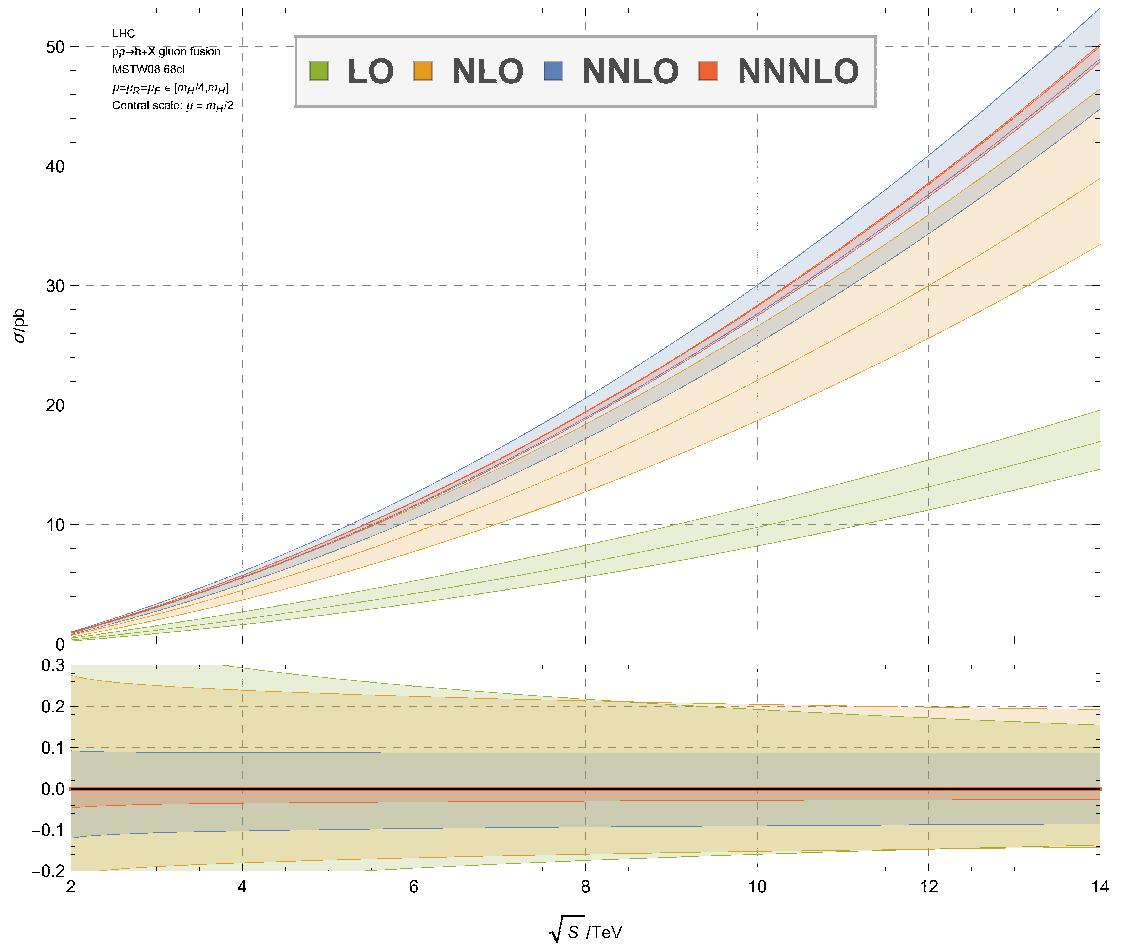
- NLO QCD corrections: $\sim 10 \dots 100\%$

- NNLO calculated for $m_t \gg M_\phi \Rightarrow$ further increase by 20–30%
[mass effects small]

Marzani, Ball, Del Duca, Forte, Vicini
Harlander, Ozeren
Pak, Rogal, Steinhauser

- N^3LO for $m_t \gg M_\phi \Rightarrow$ scale stabilization
scale dependence: $\Delta \lesssim 5\%$

Moch, Vogt
Ravindran
de Florian, Mazzitelli, Moch, Vogt
Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Mistlberger
Ball, Bonvini, Forte, Marzani, Ridolfi
Anastasiou, Duhr, Dulat, Herzog, Mistlberger

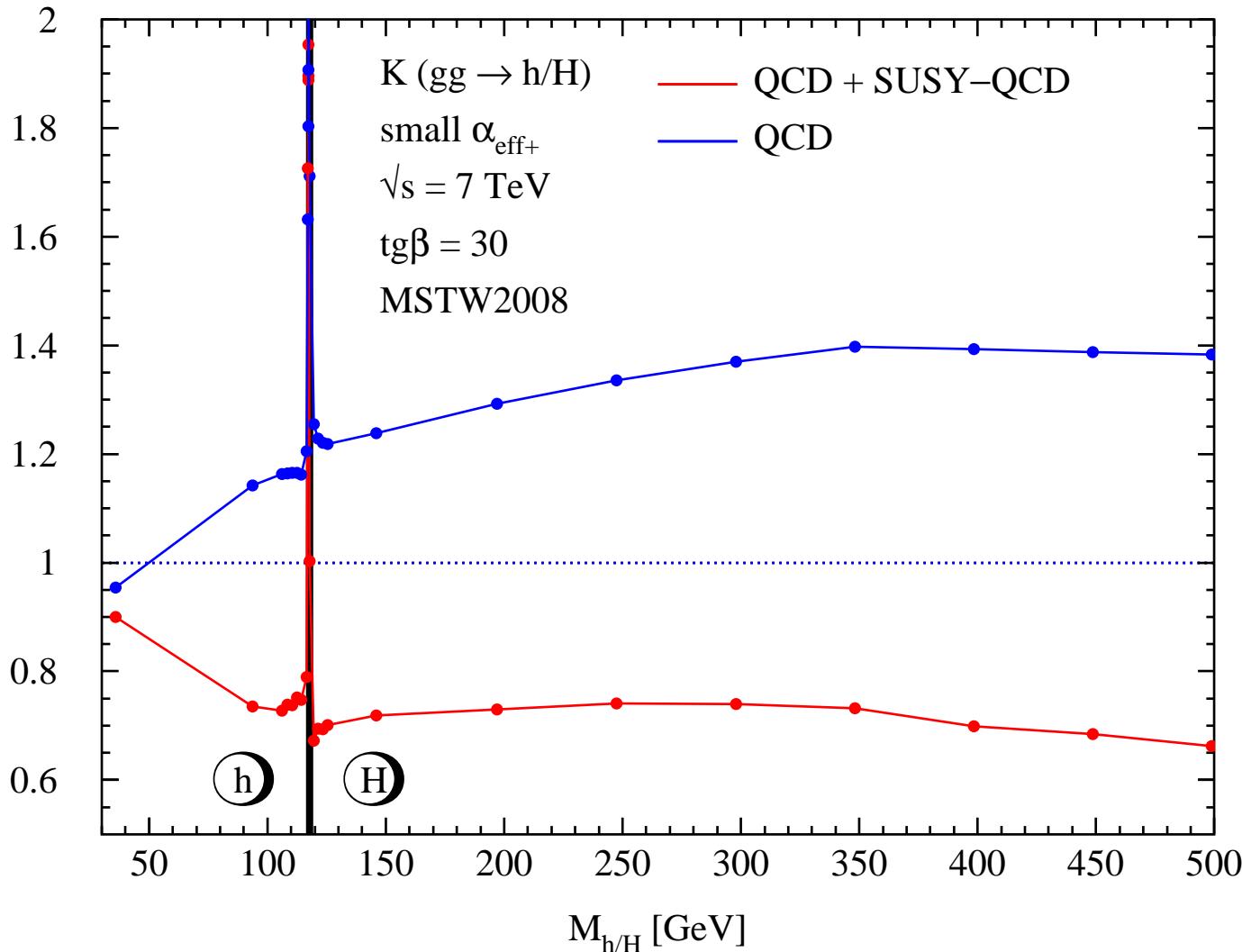


Anastasiou, Duhr, Dulat, Herzog, Mistlberger

- N³LL soft gluon resummation [$m_t \gg M_\phi$]: $\lesssim 5\%$
Catani, de Florian, Grazzini, Nason
Ahrens, Becher, Neubert, Yang
Ball, Bonvini, Forte, Marzani, Ridolfi
Schmidt, S.
- elw. corrections: $\sim 5\%$
Aglietti,...
Degrassi, Maltoni
Actis, Passarino, Sturm, Uccirati
- QCD corrections to squark loops: 10–100%
Mühlleitner, S.
Bonciani, Degrassi, Vicini
- impl. of $gg \rightarrow \phi$ in POWHEG including mass effects @ NLO
Bagnaschi, Degrassi, Slavich, Vicini
- genuine SUSY–QCD corrections: 10–100%
[$\leftarrow \Delta_b$ @ large $\tan\beta$]
Harlander, Steinhauser, Hofmann
Degrassi, Slavich
Anastasiou, Beerli, Daleo
Mühlleitner, Rzehak, S.
- SUSY-elw. corrections unknown

$$\sigma(gg \rightarrow \Phi) = \sigma_{LO}(g_t^\Phi, \tilde{g}_b^\Phi) [1 + \delta_{QCD} + \delta_{SQCD}]$$

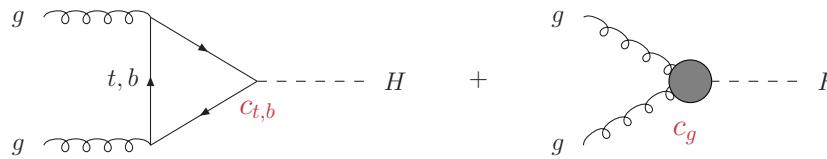
PRELIMINARY



Mühlleitner, Rzehak, S.

Dim 6

$$\mathcal{L} = - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \bar{\psi}^{(i)} \psi^{(i)} \left(1 + c_{\psi} \frac{h}{v} + \dots \right) + \frac{\alpha_s}{\pi} c_g G_{\mu\nu}^a G^{a\mu\nu} \frac{h}{v} + \dots$$



$$\sigma_{LO} \sim |c_t F_t + 12 c_g|^2 \rightarrow |c_t + 12 c_g|^2 \quad (m_t^2 \gg M_H^2)$$

$$\begin{aligned} \mathcal{L}_{eff} &= \frac{\alpha_s}{12\pi} \{c_t(1 + \delta_t) + 12c_g\} G_{\mu\nu}^a G^{a\mu\nu} \frac{h}{v} \\ \delta_t &= \frac{11\alpha_s}{4\pi} + \left[\frac{2777}{288} - \frac{67}{96} N_F + \left(\frac{19}{16} + \frac{N_F}{3} \right) \log \frac{\mu^2}{\overline{m}_t^2(\mu^2)} \right] \left(\frac{\alpha_s}{\pi} \right)^2 + \dots \end{aligned}$$

$$\frac{\partial c_g(\mu^2)}{\partial \log \mu^2} = \left(\alpha_s \frac{\partial}{\partial \alpha_s} \frac{\beta(\alpha_s)}{\alpha_s} - \frac{\beta(\alpha_s)}{\alpha_s} \right) c_g = - \left(\frac{\alpha_s}{\pi} \right)^2 \left(\beta_1 + 2\beta_2 \frac{\alpha_s}{\pi} + \dots \right) c_g \quad (\leftarrow \text{trace anomaly})$$

$$\beta(\alpha_s) = -\frac{\alpha_s^2}{\pi} \left(\beta_0 + \beta_1 \frac{\alpha_s}{\pi} + \beta_2 \left(\frac{\alpha_s}{\pi} \right)^2 + \dots \right)$$

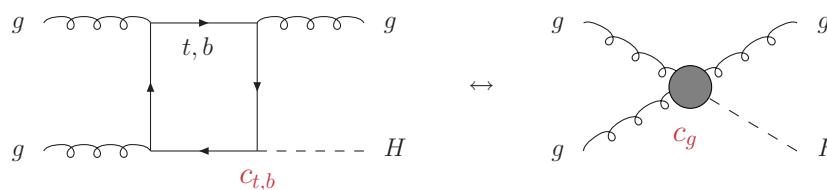
$$\beta_0 = \frac{33 - 2N_F}{12} \quad \beta_1 = \frac{153 - 19N_F}{24} \quad \beta_2 = \frac{1}{128} \left[2857 - \frac{5033}{9} N_F + \frac{325}{27} N_F^2 \right]$$

$\Rightarrow c_g$ renormalized @ NNLO, scale dependent @ NLL

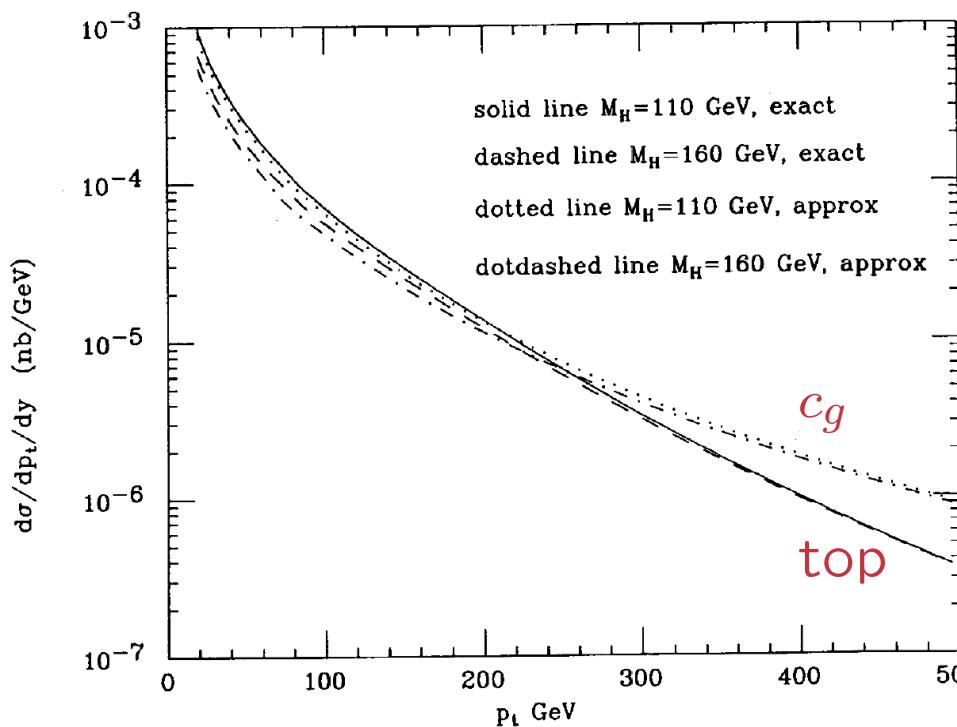
$$\Theta_\mu^\mu = [1 + \gamma_m(\alpha_s)] m_t \bar{t}t + \frac{\beta(\alpha_s)}{2\alpha_s} G_{\mu\nu}^a G_{\mu\nu}^a$$

Higgs p_T (or how to prove that ggF is loop-mediated)

$$\mathcal{L} = - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \bar{\psi}^{(i)} \psi^{(i)} \left(1 + c_\psi \frac{h}{v} + \dots \right) + \frac{\alpha_s}{\pi} c_g G_{\mu\nu}^a G^{a\mu\nu} \frac{h}{v} + \dots$$



- distinction dim4 \leftrightarrow dim5: shape of p_T distribution

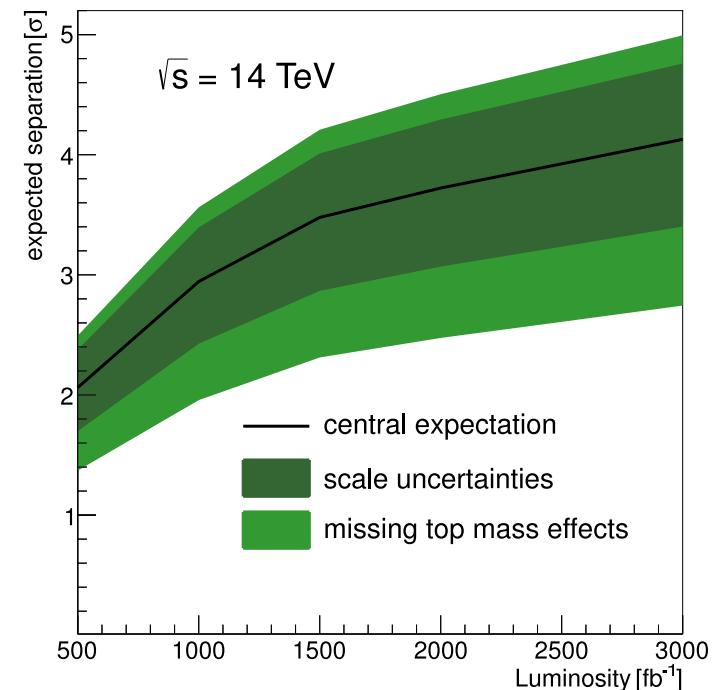
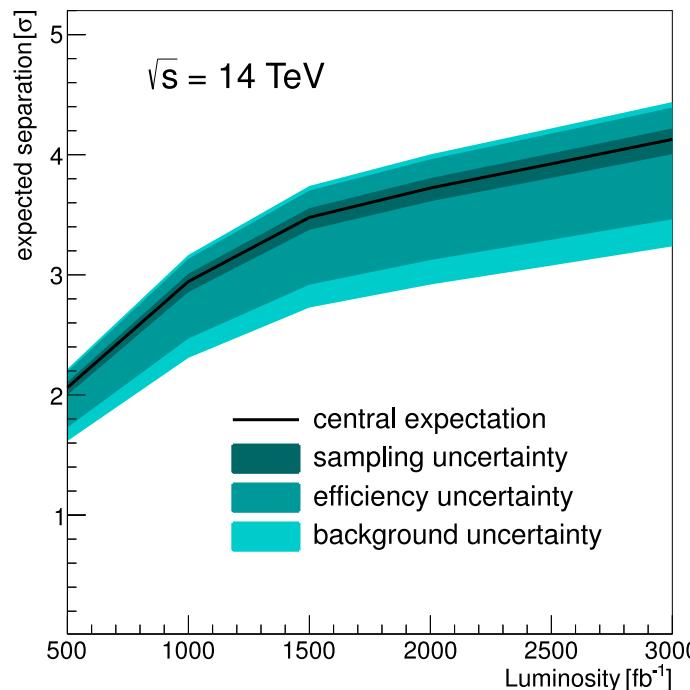


$m_t = 160$ GeV

Ellis, Hinchliffe, Soldate, van der Bij (1987!)

- QCD corrections only known for $m_t \gg M_H, p_{TH}$

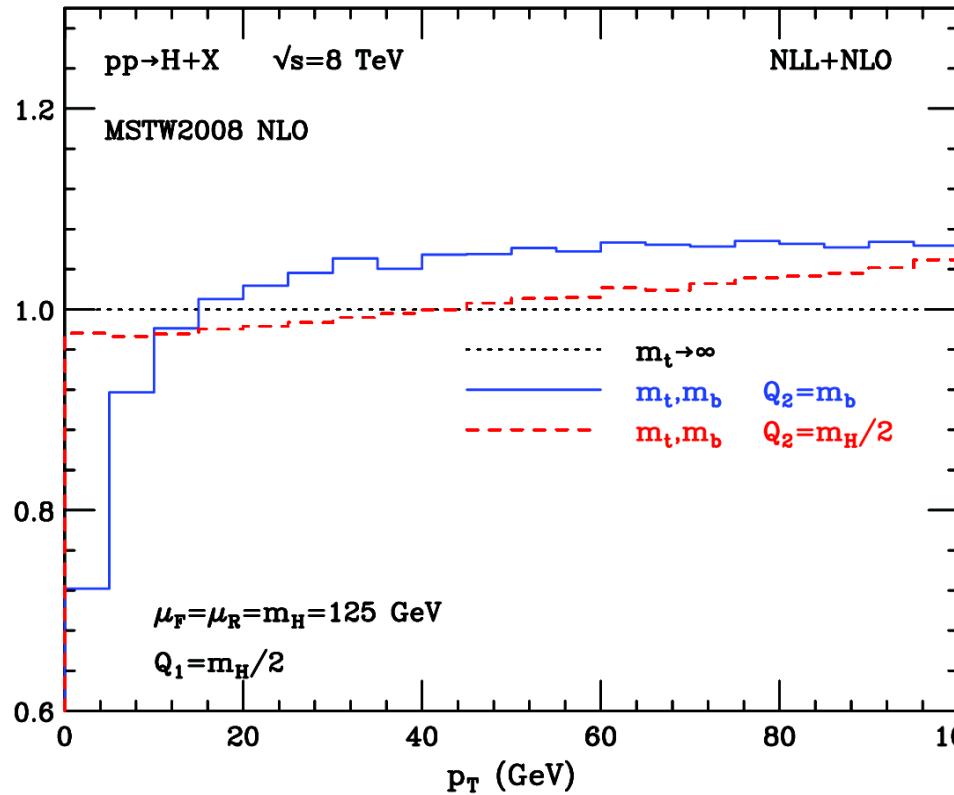
Glosser, Schmidt
 de Florian, Grazzini, Kunszt
 Anastasiou, Melnikov, Petriello
 Boughezal, Caola, Melnikov, Petriello, Schulze
 Chen, Gehrmann, Glover, Jaquier
 Boughezal, Focke, Giele, Liu, Petriello
 Harlander, Neumann, Ozeren, Wiesemann



Langenegger, S., Strebler

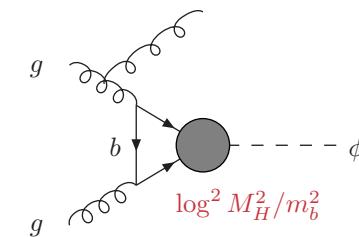
- large p_{TH} : elw. Sudakov logs $\sim \log^2 M_{W/Z}^2 / p_{TH}^2$

- factorization: $p_T \ll 2m_b \rightarrow Q \sim m_b$ [\leftarrow POWHEG, MC@NLO]

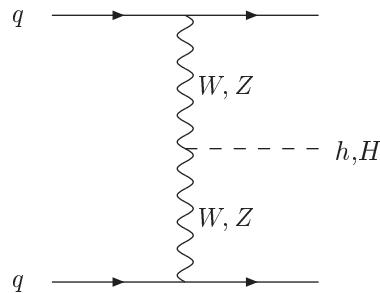


Grazzini, Sargsyan

- Sudakov form factor \rightarrow unresummed logs



(ii) W/Z fusion: $pp \rightarrow W^*W^*/Z^*Z^* \rightarrow h/H$



- QCD corrections \leftarrow DIS: $\sim 10\%$

Cahn, Dawson
Hikasa
Atarelli, Mele, Pitolli

2-loop: $\lesssim 1\%$ [approx]

Han, Valencia,
Willenbrock
Figy, Oleari, Zeppenfeld
Berger, Campbell

Bolzano, Maltoni, Moch, Zaro

- elw. corrections: $\sim 10\% \rightarrow$ HAWK

Ciccolini, Denner, Dittmaier

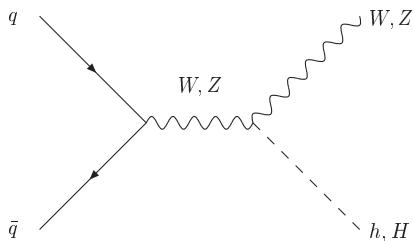
- full NLO SUSY-elw. corrections

Hollik, Rzehak, Plehn, Rauch
Figy, Palmer, Weiglein

- implemented in VBFNLO

- Dim 6: new tensor structures \leftarrow implemented @ LO

(iii) Higgs-strahlung: $pp \rightarrow W^*/Z^* \rightarrow W/Z + h/H$



- QCD corrections ← DY: $\sim 30\%$
2-loop: $\lesssim 5\%$
- SUSY-QCD corrections small
- electroweak corrections: $\sim -10\%$ → HAWK
- WH/ZH : fully exclusive @ NNLO QCD

Glashow,...
Kunszt,...

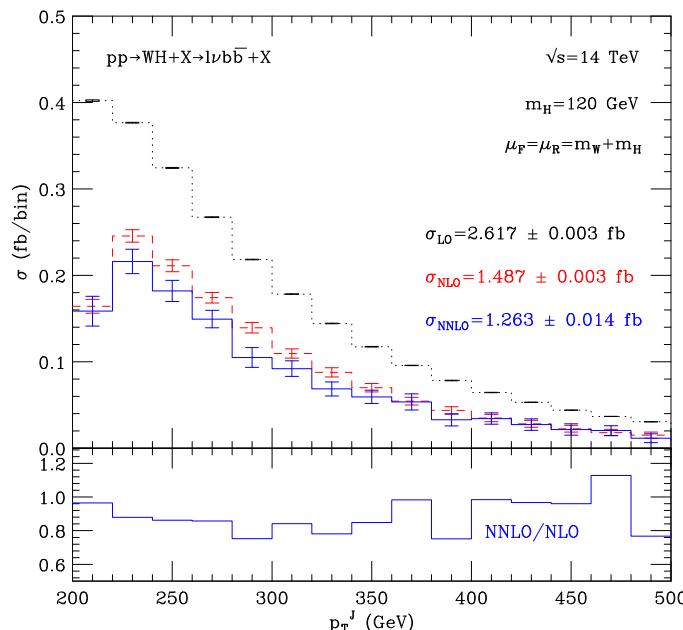
Han, Willenbrock

Brein, Djouadi, Harlander

Djouadi, S.

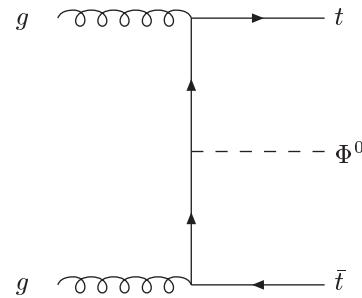
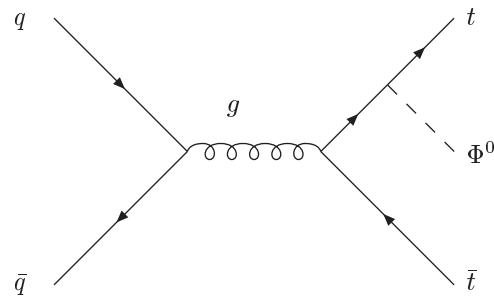
Ciccolini, Dittmaier, Krämer

Ferrera, Grazzini, Tramantano



- Dim 6: new tensor structures ← implemented @ LO

(iv) Bremsstrahlung: $pp \rightarrow t\bar{t} + h/H/A$



Kunszt
Gunion
Marciano, Paige

dominant

- $t\bar{t}h \rightarrow t\bar{t}b\bar{b}$ important @ LHC \rightarrow top Yukawa cplg.

Beenakker,...
Dawson, ...

Broggio, Ferroglia, Pecjak, Signer, Yang
Kulesza, Motyka, Stebel, Theeuwes

- link to parton showers: aMC@NLO, PowHe

Garzelli, Kardos, Papadopoulos, Trócsányi

Frederix et al.

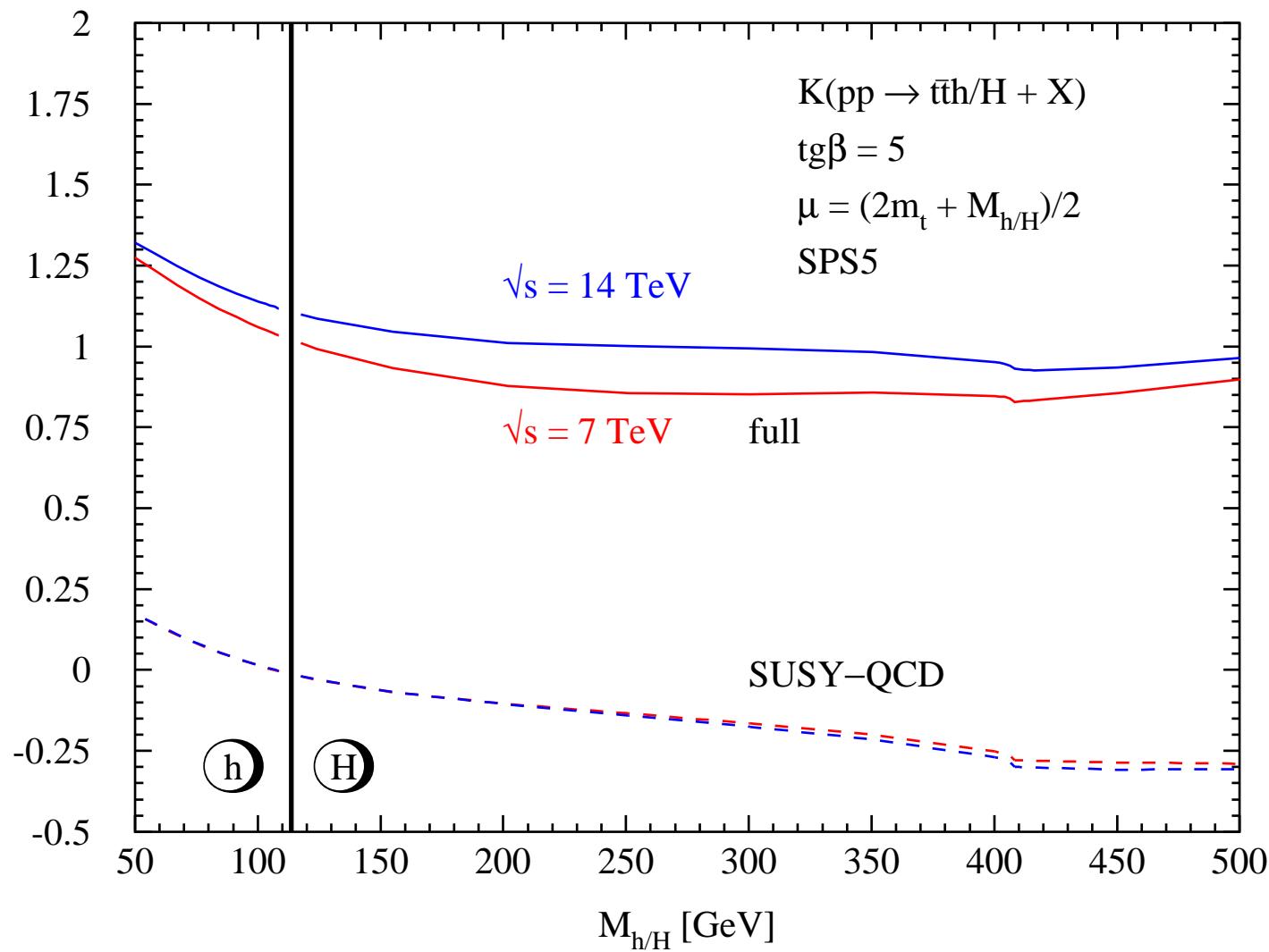
- elw. corrections: $\sim 1 - 2\%$

Yu, Wen-Gan, Ren-You, Chong, Lei
Frixione, Hirschi, Pagani, Shao, Zaro
Denner, Feger

- dim 6: $c_t, c_g \rightarrow c_t$ dominant

- SUSY-QCD corrections: moderate

Dittmaier, Häfliger, Krämer, S., Walser



Dittmaier, Häfliger, Krämer, S., Walser

SPS 5

$$\operatorname{tg}\beta = 5$$

$$\mu = 639.8 \text{ GeV}$$

$$A_t = -1671.4 \text{ GeV}$$

$$A_b = -905.6 \text{ GeV}$$

$$m_{\tilde{g}} = 710.3 \text{ GeV}$$

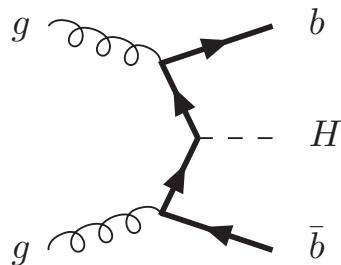
$$m_{\tilde{q}_L} = 535.2 \text{ GeV}$$

$$m_{\tilde{b}_R} = 620.5 \text{ GeV}$$

$$m_{\tilde{t}_R} = 360.5 \text{ GeV}$$

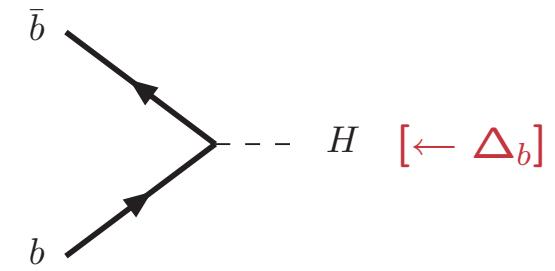
$$\longrightarrow m_{\tilde{t}_1} = 204.1 \text{ GeV}, m_{\tilde{t}_2} = 656.1 \text{ GeV}, m_{\tilde{b}_1} = 533.3 \text{ GeV}, m_{\tilde{b}_2} = 625.2 \text{ GeV}$$

(v) $b\bar{b}$ +Higgs production



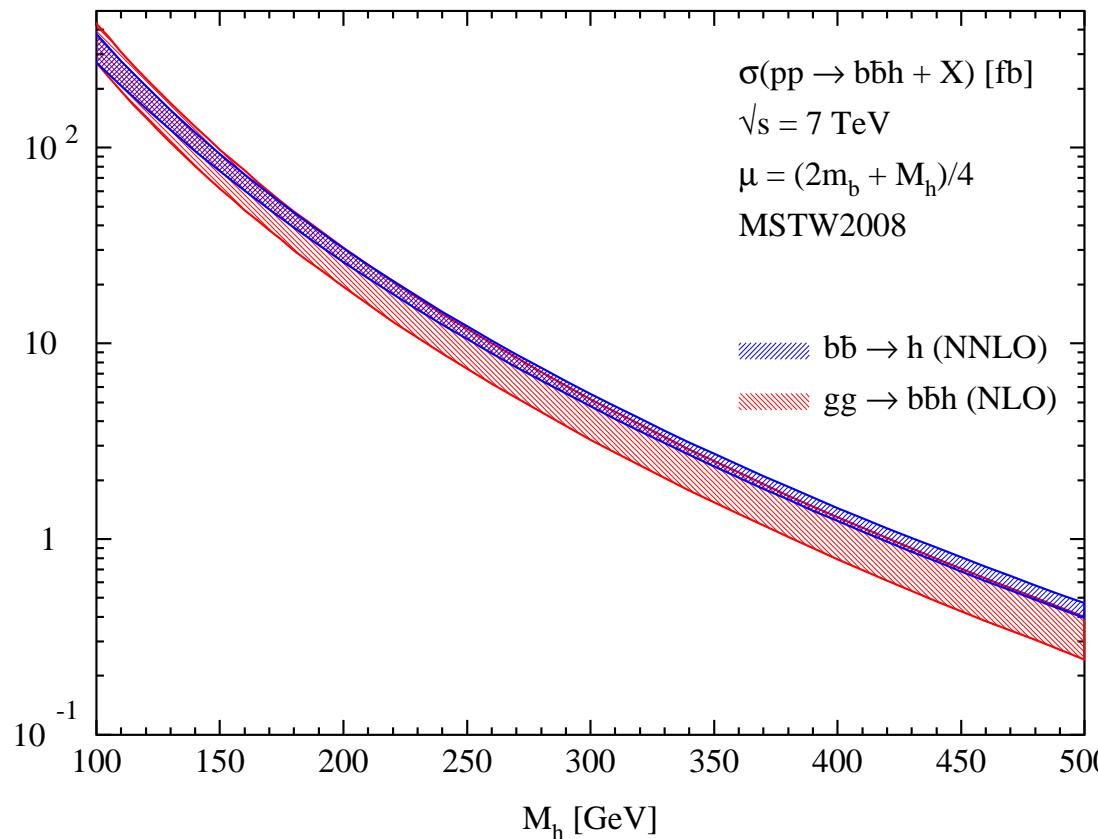
NLO

exact $g \rightarrow b\bar{b}$ splitting & mass/off-shell effects
no resummation of $\log M_H^2/m_b^2$ terms



NNLO

massless/on-shell b 's, no p_{Tb}
resummation of $\log M_H^2/m_b^2$ terms



Santander matching:

$$\sigma = \frac{\sigma^{4FS} + w\sigma^{5FS}}{1+w}$$

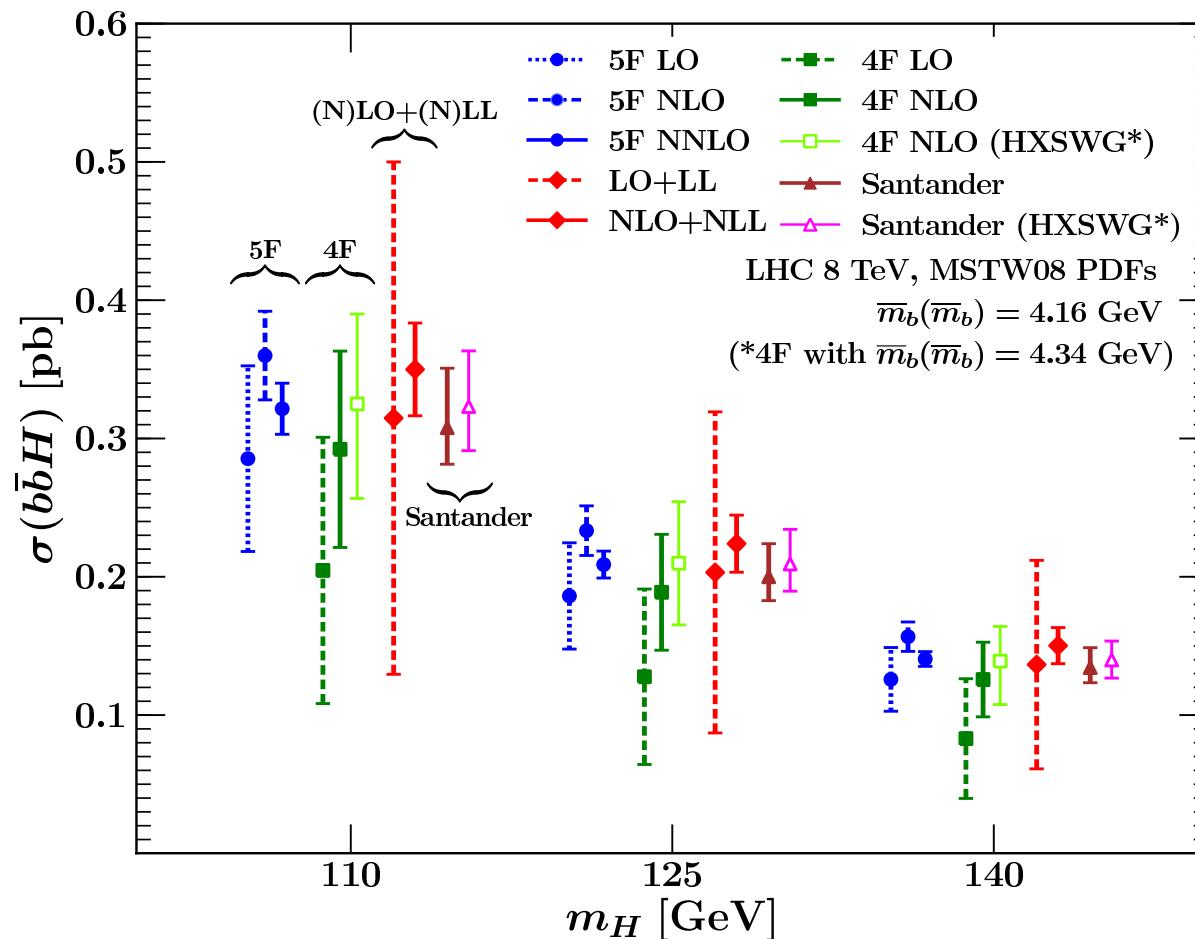
$$w = \log \frac{M_H}{m_b} - 2$$

Harlander, Krämer, Schumacher

Dittmaier, Krämer, S.
Dawson, Jackson, Reina, Wackerlo
Harlander, Kilgore

- two approaches for proper matching 4FS + 5FS

Bonvini, Papanastasiou, Tackmann
Forte, Napoletano, Ubiali



Bonvini, Papanastasiou, Tackmann

	M_A	M_H [GeV]	δ_{QCD}^A	δ_{SUSY}^A	$\delta_{SUSYrem}^A$	δ_{QCD}^H	δ_{SUSY}^H	$\delta_{SUSYrem}^H$
7 TeV	100	113.9	0.23	-0.30	0.4×10^{-4}	0.27	-0.38	0.3×10^{-4}
	200	200	0.38	-0.30	2.9×10^{-4}	0.39	-0.30	5.8×10^{-4}
	300	300	0.46	-0.30	6.7×10^{-4}	0.47	-0.30	9.3×10^{-4}
	400	400	0.53	-0.30	1.3×10^{-3}	0.53	-0.30	1.5×10^{-3}
	500	500	0.57	-0.30	2.0×10^{-3}	0.59	-0.30	2.2×10^{-3}
14 TeV	100	113.9	0.14	-0.30	0.4×10^{-4}	0.17	-0.38	0.5×10^{-4}
	200	200	0.28	-0.30	2.7×10^{-4}	0.29	-0.30	5.7×10^{-4}
	300	300	0.37	-0.30	6.5×10^{-4}	0.39	-0.30	9.3×10^{-4}
	400	400	0.45	-0.30	1.2×10^{-3}	0.45	-0.30	1.5×10^{-3}
	500	500	0.50	-0.30	2.1×10^{-3}	0.49	-0.30	2.3×10^{-3}

	$\text{tg}\beta$	M_A	M_H [GeV]	δ_{SUSY}^A	$\delta_{SUSYrem}^A$	δ_{SUSY}^H	$\delta_{SUSYrem}^H$
7 TeV	3	200	209.7	-0.04	2.1×10^{-4}	-0.04	5.7×10^{-4}
	5	200	204.0	-0.06	2.4×10^{-4}	-0.06	5.3×10^{-4}
	7	200	202.1	-0.08	2.5×10^{-4}	-0.09	3.9×10^{-4}
	10	200	200.9	-0.12	2.5×10^{-4}	-0.12	3.8×10^{-4}
	20	200	200.1	-0.21	2.6×10^{-4}	-0.21	4.4×10^{-4}
	30	200	200.0	-0.30	2.9×10^{-4}	-0.30	5.8×10^{-4}
14 TeV	3	200	209.7	-0.04	2.0×10^{-4}	-0.04	7.2×10^{-4}
	5	200	204.0	-0.06	2.2×10^{-4}	-0.06	5.0×10^{-4}
	7	200	202.1	-0.08	2.4×10^{-4}	-0.09	4.4×10^{-4}
	10	200	200.9	-0.12	2.5×10^{-4}	-0.12	4.1×10^{-4}
	20	200	200.1	-0.21	2.7×10^{-4}	-0.21	4.4×10^{-4}
	30	200	200.0	-0.30	2.7×10^{-4}	-0.30	5.7×10^{-4}

SPS 1b

$$\tan\beta = 30$$

$$\mu = 495.6 \text{ GeV}$$

$$A_t = -729.3 \text{ GeV}$$

$$A_b = -987.4 \text{ GeV}$$

$$m_{\tilde{g}} = 916.1 \text{ GeV}$$

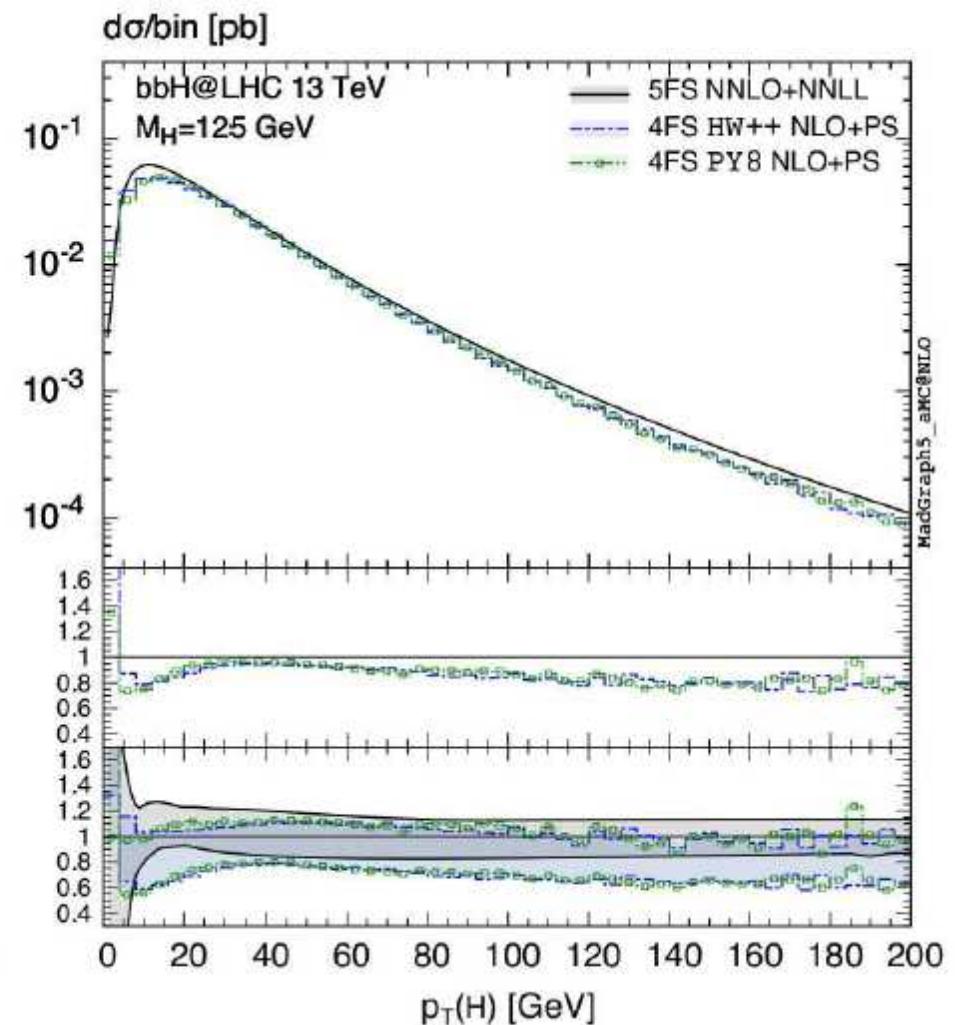
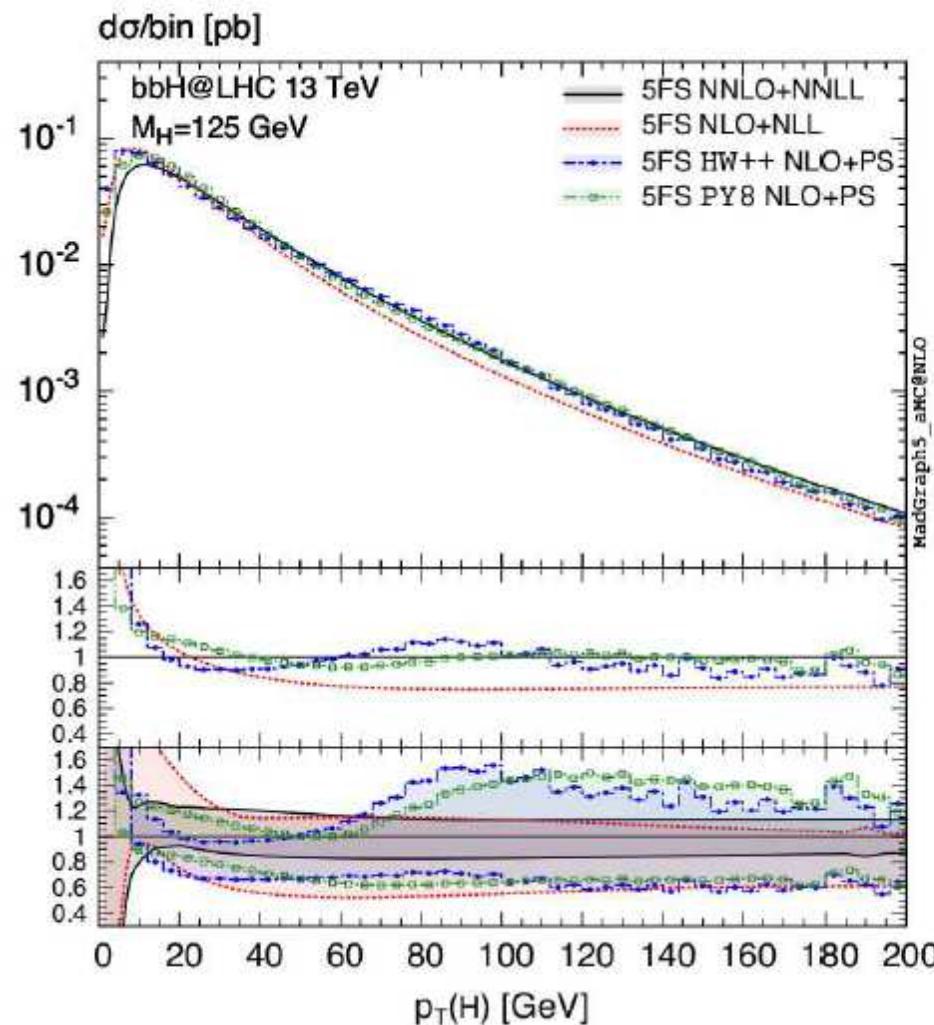
$$m_{\tilde{q}_L} = 762.5 \text{ GeV}$$

$$m_{\tilde{b}_R} = 780.3 \text{ GeV}$$

$$m_{\tilde{t}_R} = 670.7 \text{ GeV}$$

$$\longrightarrow m_{\tilde{t}_1} = 631.8 \text{ GeV}, m_{\tilde{t}_2} = 829.1 \text{ GeV}, m_{\tilde{b}_1} = 721.8 \text{ GeV}, m_{\tilde{b}_2} = 820.7 \text{ GeV}$$

distributions



Wiesemann, Frederix, Frixione, Hirschi, Maltoni, Torrielli

MG5_aMC@NLO

[POWHEG Jäger, Reina, Wackerlo]

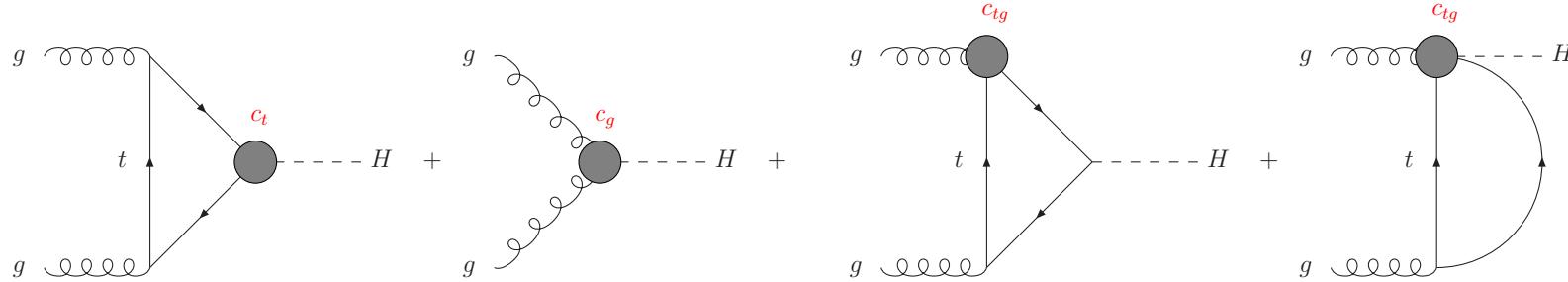
III *CONCLUSIONS*

- Higgs boson searches/studies at LHC belong to major endeavours
- most QCD and elw. corrections known in SM & MSSM
→ $\Delta \lesssim 10 - 15\% @ \text{LHC}$
- QCD & elw. corrections to dim 6 contributions in the making
(→ Ghezzi, Gomez-Ambrosio, Passarino, Uccirati
Berthier, Hartmann, Trott)
- important to develop NLO event generators [\leftarrow backgrounds]

BACKUP SLIDES

$gg \rightarrow H$

- chromomagnetic dipole operator



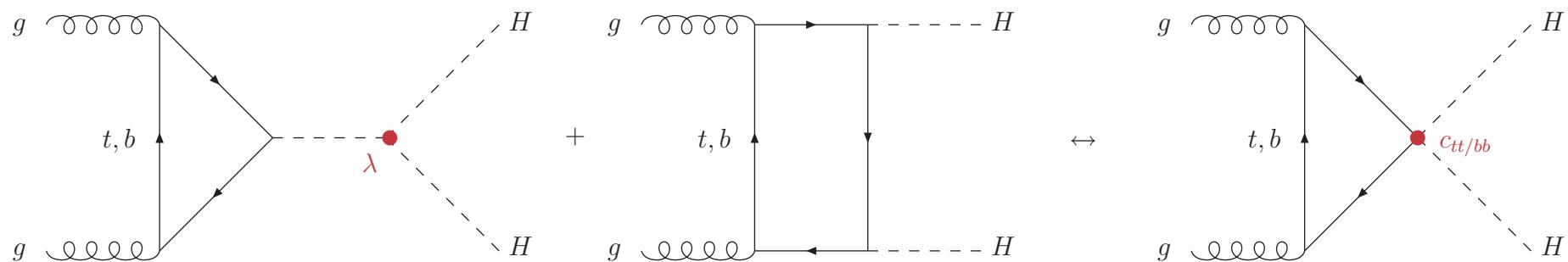
$$\mathcal{L}_{eff} = -\mathbf{c}_t m_t \bar{t} t \frac{H}{v} + \mathbf{c}_g \frac{g_s^2}{4\pi^2} G^{a\mu\nu} G_{\mu\nu}^a \frac{H}{v} + \mathbf{c}_{tg} \frac{g_s m_t}{2v^3} (v + H) G_{\mu\nu}^a [\bar{t}_L \sigma^{\mu\nu} T^a t_R + h.c.]$$

→ mixing of operators, renormalization @ 'LO':

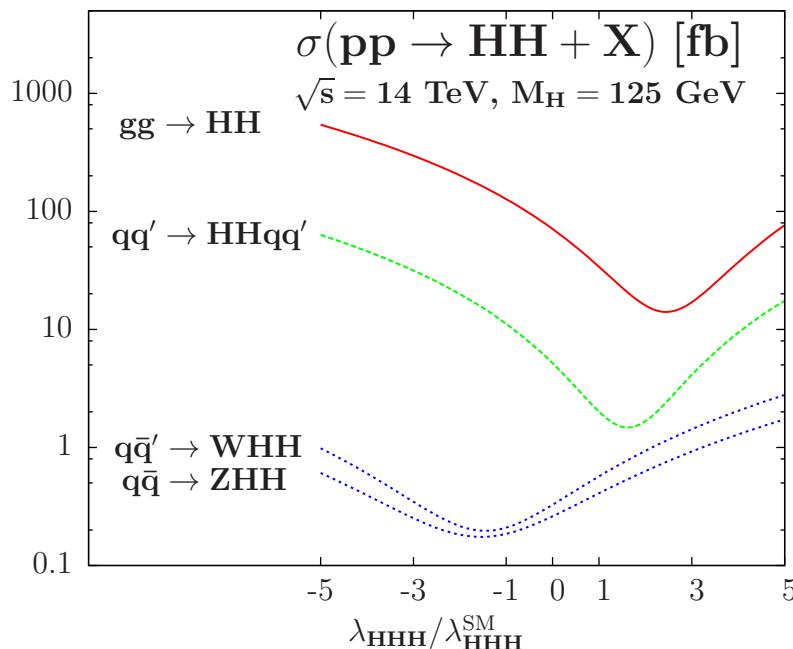
$$\delta c_g = \frac{\alpha_t}{2\pi} \Re e(c_{tg}) \Gamma(1 + \epsilon) \left(\frac{4\pi\mu^2}{\mu_R^2} \right)^\epsilon \frac{1}{\epsilon} \quad \left(\alpha_t = \frac{y_t^2}{4\pi} = \frac{m_t^2}{2\pi v^2} \right)$$

Degrade, Gérard, Grojean, Maltoni, Servant

$gg \rightarrow HH$



- threshold region: sensitive to λ
- large M_{HH} : sensitive to $c_{tt/bb}$ [e.g. boosted Higgs pairs]

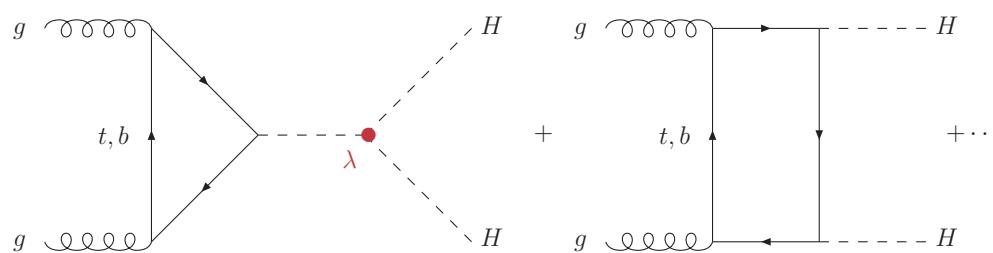


$$gg \rightarrow HH : \frac{\Delta\sigma}{\sigma} \sim -\frac{\Delta\lambda}{\lambda}$$

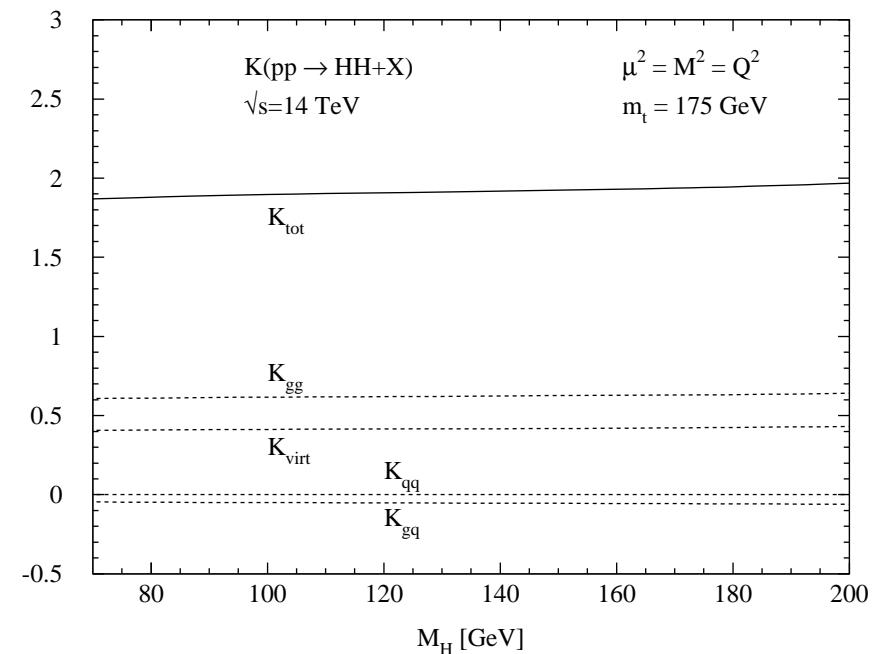
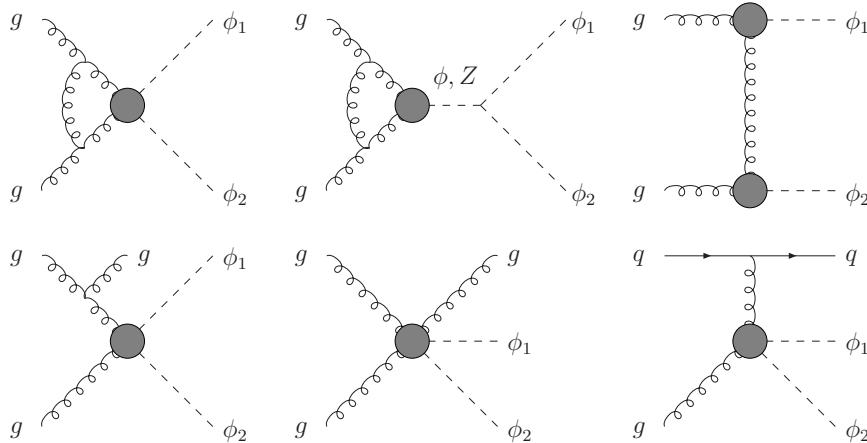
[decreasing with M_{HH}^2]

$gg \rightarrow HH$

SM

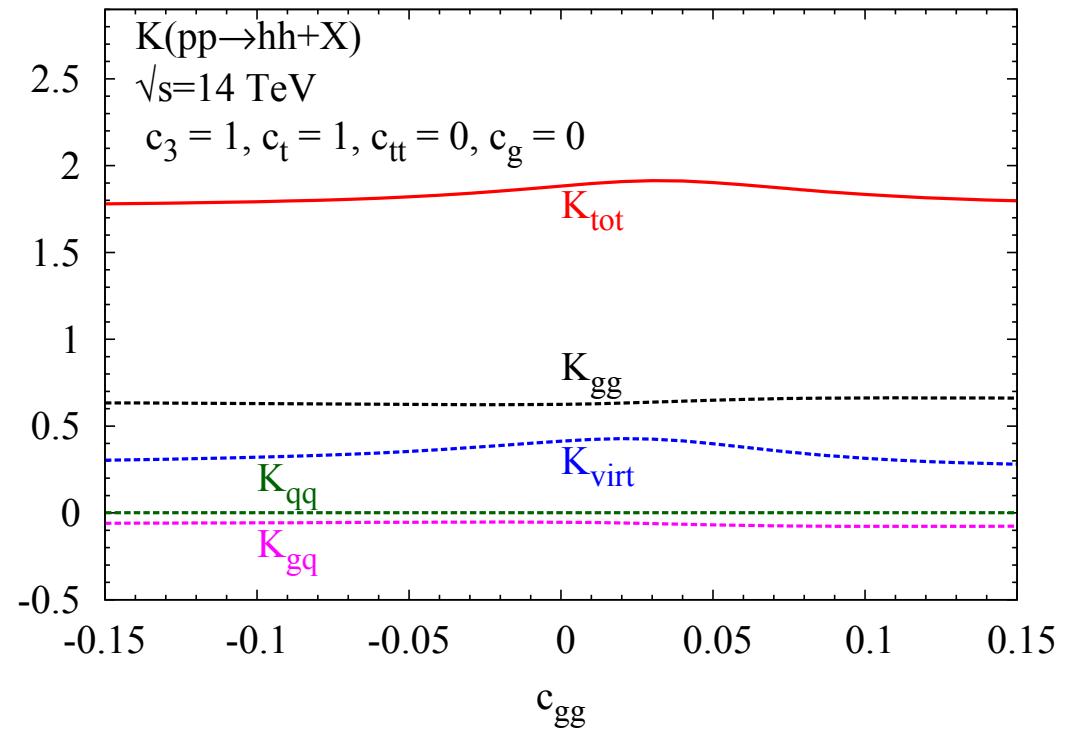
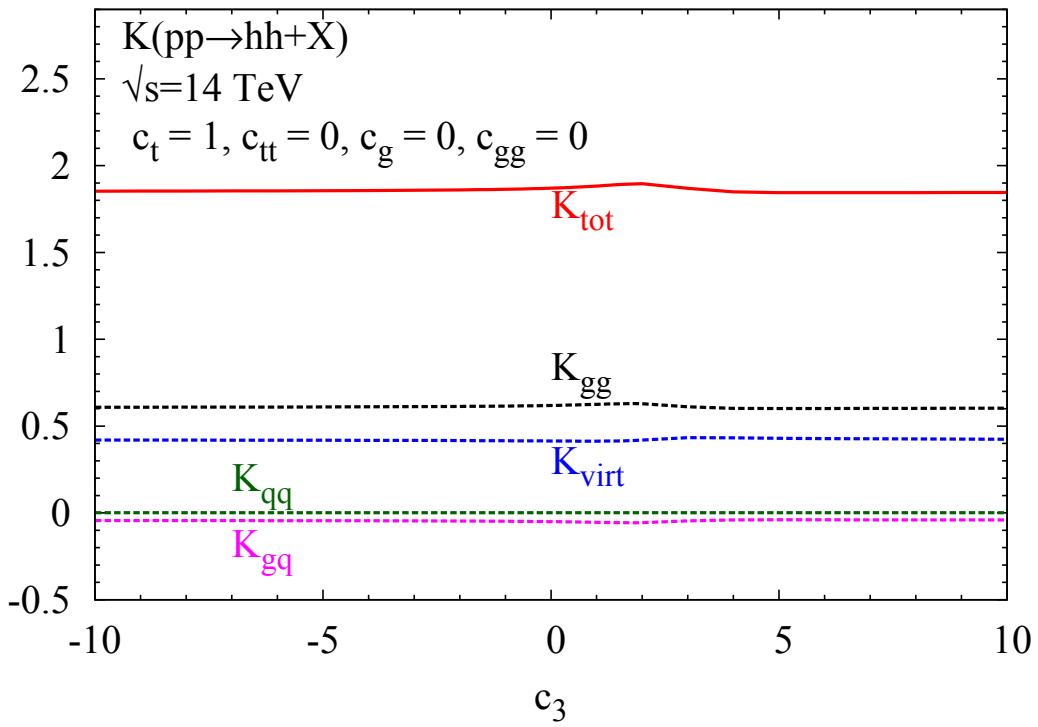


- third generation dominant $\rightarrow t, b$
- 2-loop QCD corrections: $\sim 90 - 100\%$
 $[M_H^2 \ll 4m_t^2, \mu = M_{HH}]$



- extended to dim6 → large impact on cxn
small impact on K-factor

$$\mathcal{L}_{eff} = -m_t \bar{t}t \left(\textcolor{red}{c_t} \frac{h}{v} + \textcolor{red}{c_{tt}} \frac{h^2}{2v^2} \right) - \textcolor{red}{c_3} \frac{1}{6} \left(\frac{3M_h^2}{v} \right) h^3 + \frac{\alpha_s}{\pi} G^{a\mu\nu} G_{\mu\nu}^a \left(\textcolor{red}{c_g} \frac{h}{v} + \textcolor{red}{c_{gg}} \frac{h^2}{2v^2} \right)$$



Gröber, Mühlleitner, S., Streicher

- 2-loop QCD corrections:

$$\sigma = \sigma_0 + \frac{\sigma_1}{m_t^2} + \cdots + \frac{\sigma_4}{m_t^8}$$

Grigo, Hoff, Melnikov, Steinhauser

- NLO mass effects @ NLO in real corrections: $\sim -10\%$

Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Torrielli, Vryonidou, Zaro

→ large virtual mass effects

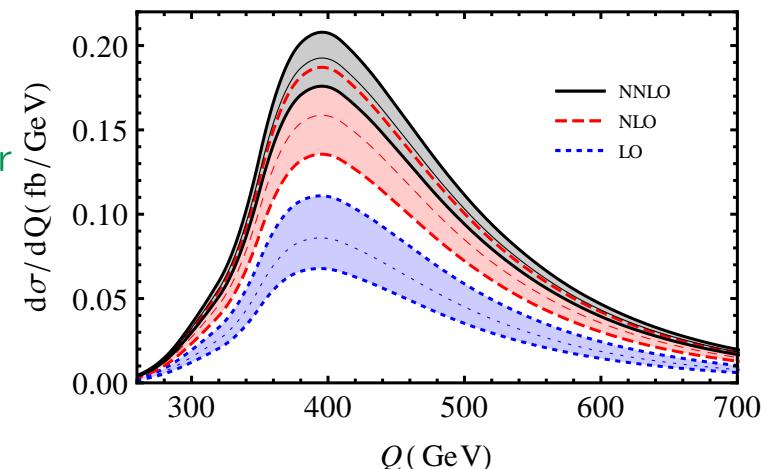
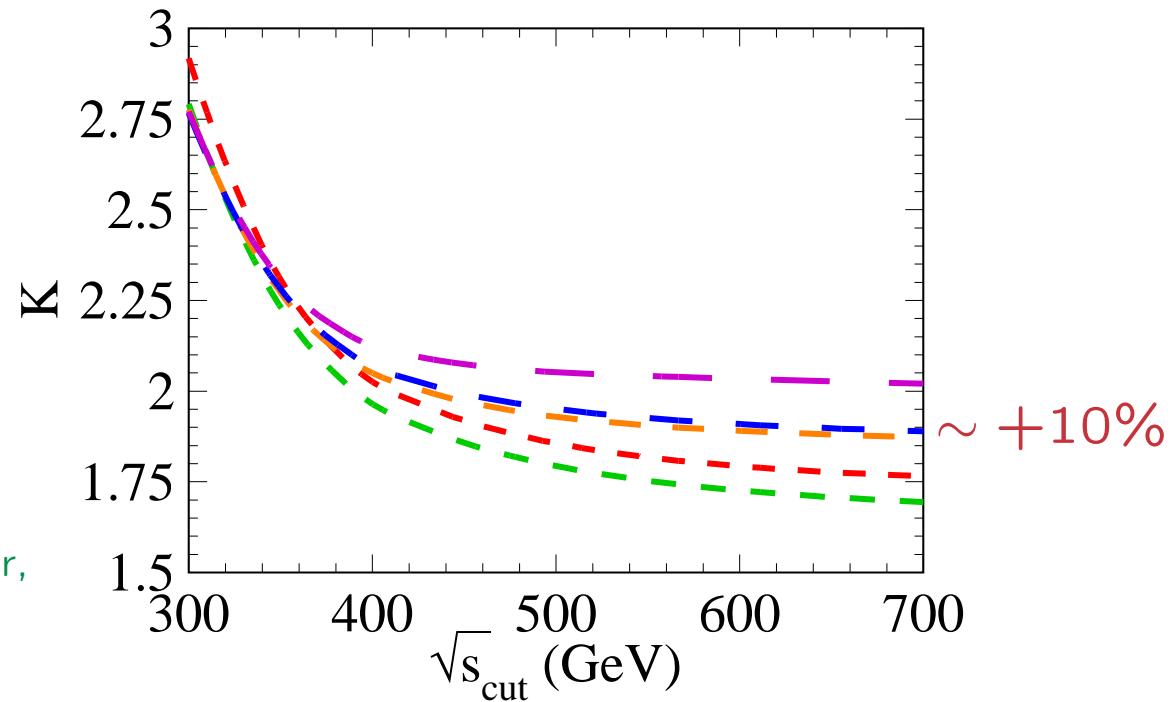
- NNLO QCD corrections: $\sim 20\%$

$$[M_H^2 \ll 4m_t^2]$$

de Florian, Mazzitelli
Grigo, Melnikov, Steinhauser

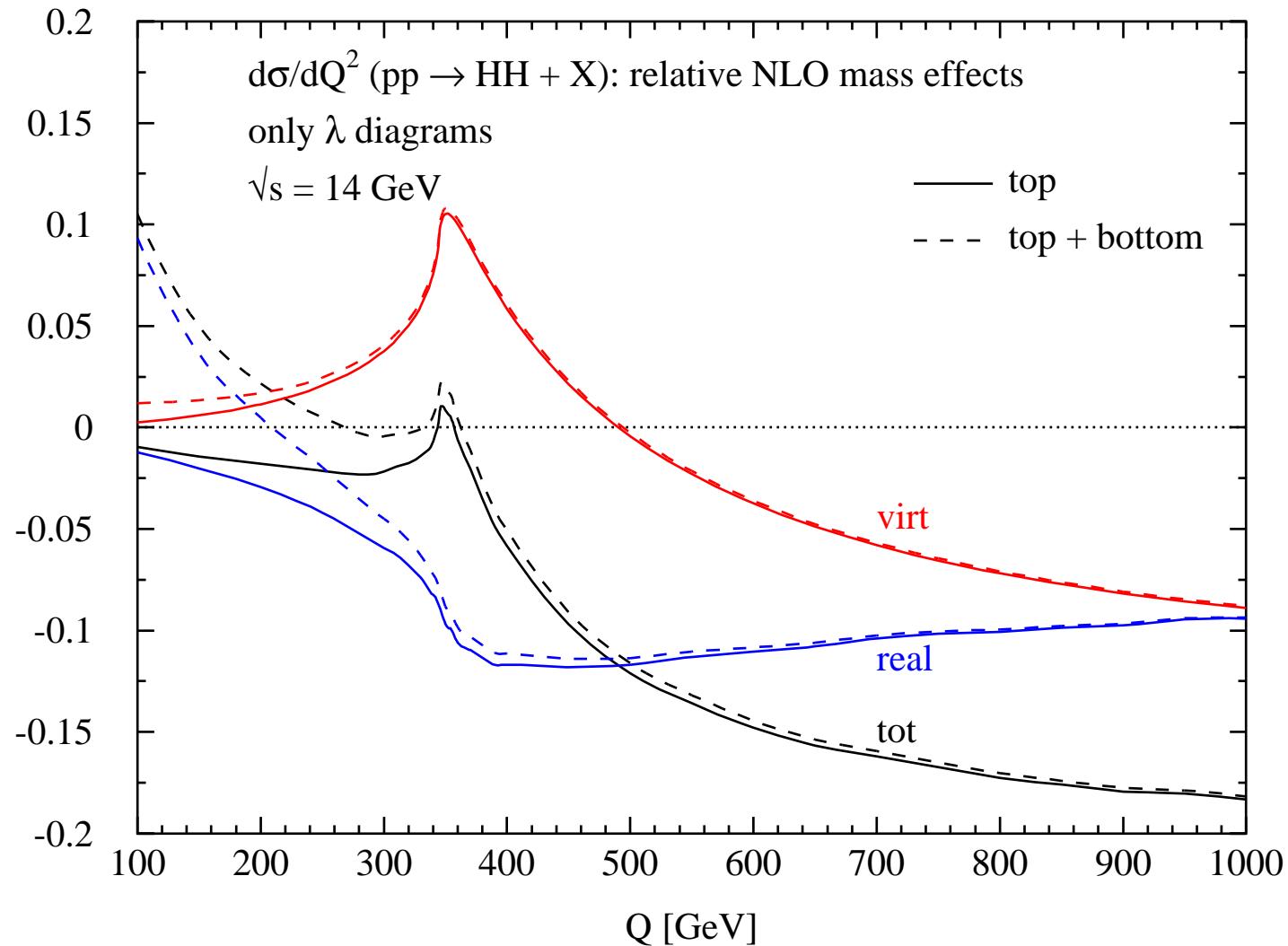
- soft gluon resummation: $\sim 10\%$

$$[M_H^2 \ll 4m_t^2]$$



Shao, Li, Li, Wang
de Florian, Mazzitelli

Diagrams with λ only:



- situation unclear \leftarrow boxes different?