

The smallest of the Little Bangs – Thermalization and collective flow in proton-proton and proton-nucleus collisions (??!)

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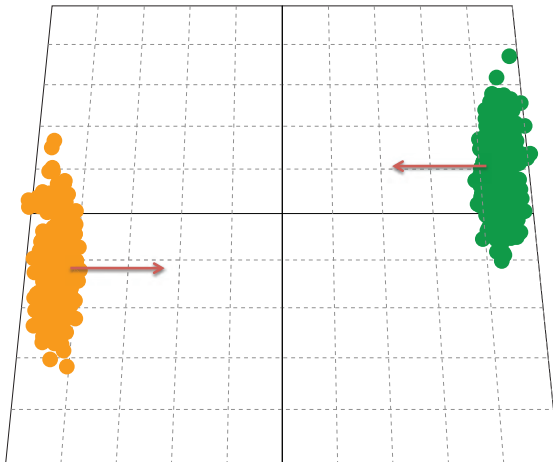
XQCD 2016, 8/1/2016

Overview

- 1 The big picture
- 2 Flow in small systems?
 - Flow in small systems?
 - Do small systems behave hydrodynamically?
 - Collectivity in small systems
 - Initial-state momentum correlations?
- 3 What is needed to resolve this ambiguity?
 - What is needed?
 - What is missing?
- 4 Proton substructure: what does a proton look like in position space?
 - CGC picture of the nucleon
 - Modeling quark substructure of the nucleon
 - Characteristics of initial entropy density distributions in pp and light-heavy collisions
- 5 Back to the big picture

Relativistic Nucleus-Nucleus Collisions

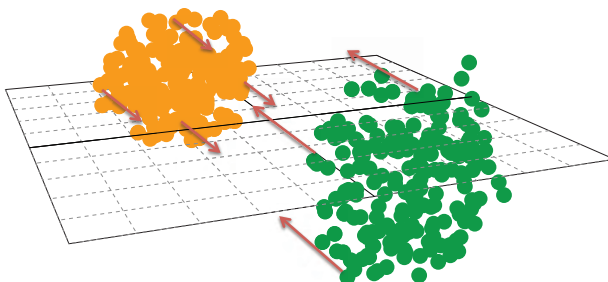
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

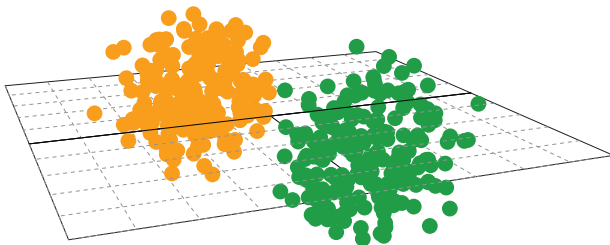
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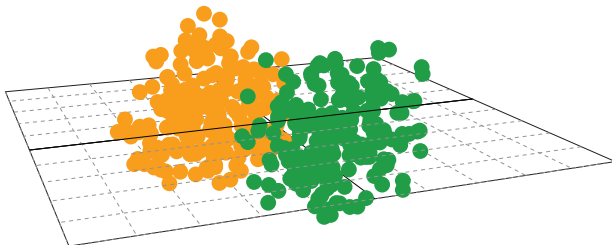
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

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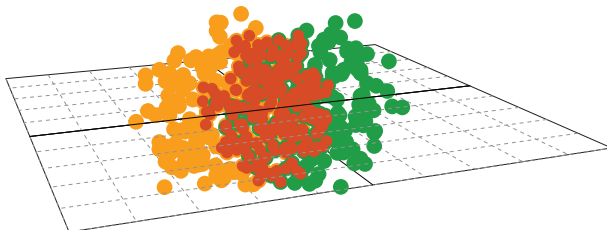
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Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

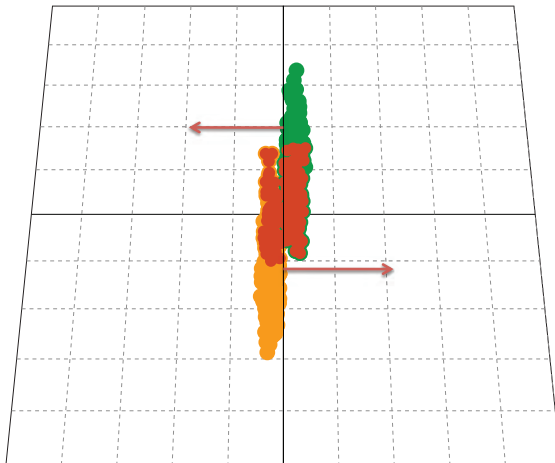
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

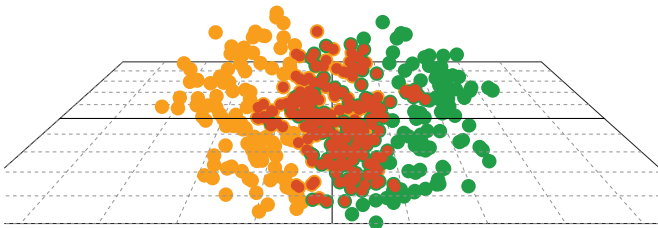
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

Animation: P. Sorensen

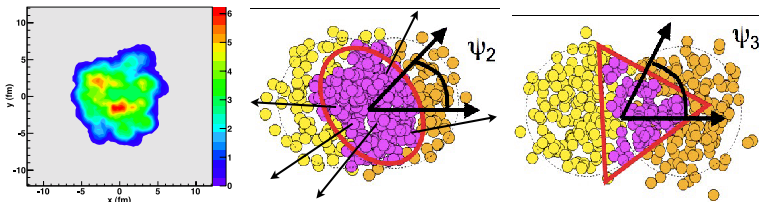


Produced fireball is $\sim 10^{-14}$ meters across
and lives for $\sim 5 \times 10^{-23}$ seconds

Collision of two Lorentz contracted gold nuclei

Event-by-event shape and flow fluctuations rule!

(Alver and Roland, PRC81 (2010) 054905)

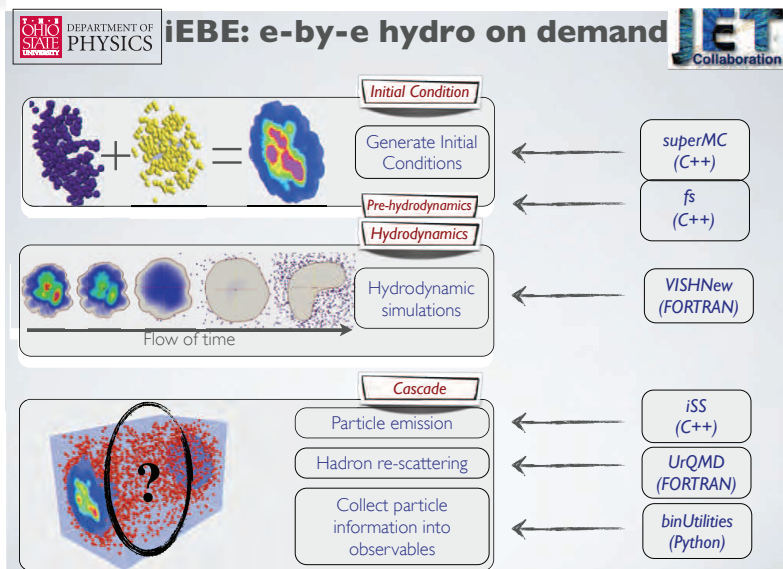


- Each event has a different initial shape and density distribution, characterized by different set of harmonic eccentricity coefficients ε_n
- Each event develops its individual hydrodynamic flow, characterized by a set of harmonic flow coefficients v_n and flow angles ψ_n
- At small impact parameters fluctuations (“hot spots”) dominate over geometric overlap effects
(Alver & Roland, PRC81 (2010) 054905; Qin, Petersen, Bass, Müller, PRC82 (2010) 064903)

Definition of flow coefficients:

$$\frac{dN^{(i)}}{dy p_T dp_T d\phi_p}(b) = \frac{dN^{(i)}}{dy p_T dp_T}(b) \left(1 + 2 \sum_{n=1}^{\infty} v_n^{(i)}(y, p_T; b) \cos(\phi_p - \Psi_n^{(i)}) \right).$$

<https://u.osu.edu/vishnu>: A product of the JET Collaboration



Viscous relativistic hydrodynamics (Israel & Stewart 1979)

Include shear viscosity η , neglect bulk viscosity (massless partons) and heat conduction ($\mu_B \approx 0$); solve

$$\partial_\mu T^{\mu\nu} = 0$$

with modified energy momentum tensor

$$T^{\mu\nu}(x) = (e(x) + p(x))u^\mu(x)u^\nu(x) - g^{\mu\nu}p(x) + \pi^{\mu\nu}.$$

$\pi^{\mu\nu}$ = traceless viscous pressure tensor which relaxes locally to 2η times the shear tensor $\nabla^{\langle\mu}u^{\nu\rangle}$ on a microscopic kinetic time scale τ_π :

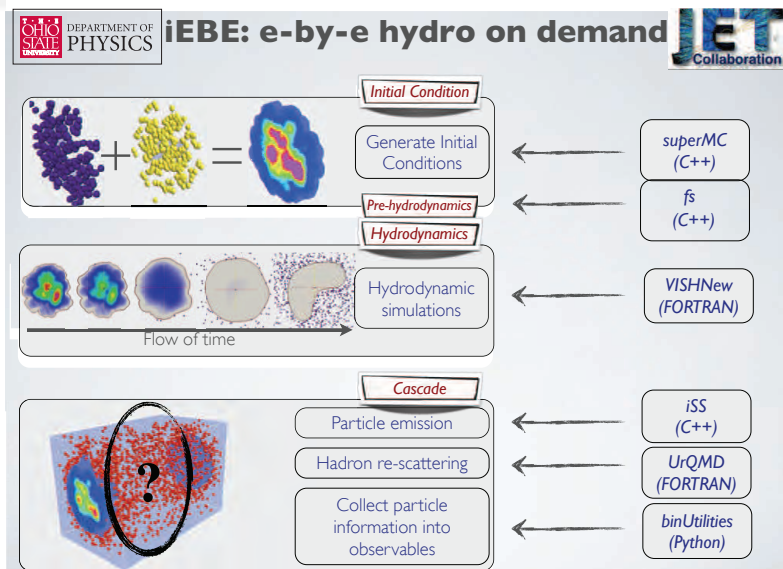
$$D\pi^{\mu\nu} = -\frac{1}{\tau_\pi}(\pi^{\mu\nu} - 2\eta\nabla^{\langle\mu}u^{\nu\rangle}) + \dots$$

where $D \equiv u^\mu \partial_\mu$ is the time derivative in the local rest frame.

Kinetic theory relates η and τ_π , but for a strongly coupled QGP neither η nor this relation are known \implies treat η and τ_π as independent phenomenological parameters.

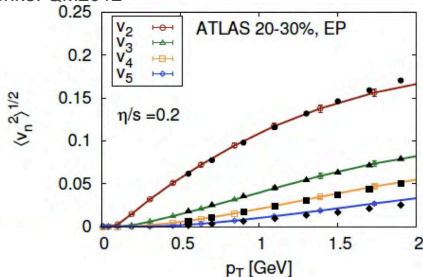
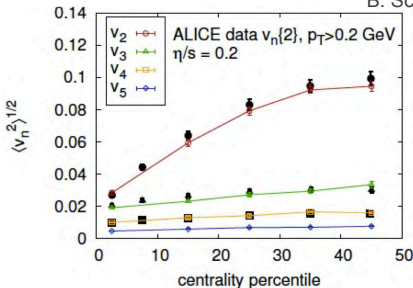
For consistency: $\tau_\pi \theta \ll 1$ ($\theta = \partial^\mu u_\mu$ = local expansion rate).

<https://u.osu.edu/vishnu>: A product of the JET Collaboration



Towards a Standard Model of the Little Bang

B. Schenke: QM2012



Schenke, Tribedy, Venugopalan,
Phys.Rev.Lett. 108:25231 (2012)

With inclusion of sub-nucleonic quantum fluctuations
and pre-equilibrium dynamics of gluon fields:

→ outstanding agreement between data and model

Rapid convergence on a standard model of the Little Bang!

Perfect liquidity reveals in the final state initial-state gluon field correlations
of size $1/Q_s$ (sub-hadronic)!

The big question

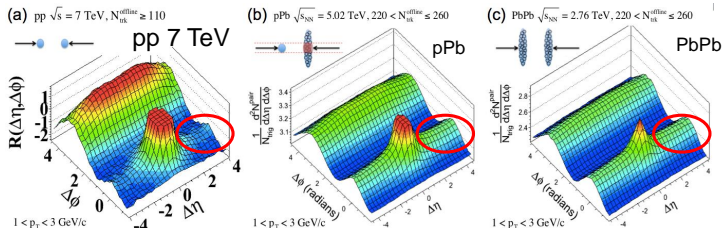
- Flow-like signatures of similar characteristics as those in AA collisions were also seen in pA and high-multiplicity pp.
- Seen in both single-particle observables (“radial flow”) and two-particle correlations (“anisotropic flow”).
- Initial-state momentum correlations can also manifest themselves as “anisotropic flow” in the final state, especially in small collision systems where they may survive final-state interactions.
- **What is the true origin of these flow-like signatures? How can we separate initial-state from final-state effects, in particular in small systems?**
- **What is the internal phase-space structure of a proton?**

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Flow in small systems?

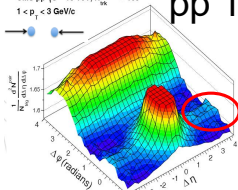
Ridge in pp, pPb and PbPb



NEW

CMS pp $\sqrt{s} = 13$ TeV, $N_{\text{ch}}^{\text{offline}} \geq 105$
 1 < p_T < 3 GeV/c

pp 13 TeV



Zhenyu Chen

CMS-FSQ-15-002

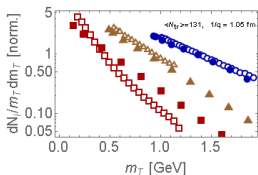
Ridge observed in high multiplicity
pp collisions at **13 TeV** !



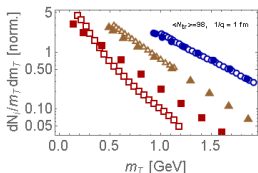
13 TeV vs. 7 TeV?

Flow in small systems?

Flow in small systems?

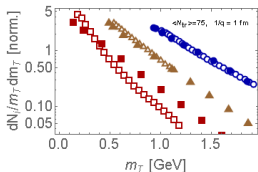


Kalaydzhyan & Shuryak PRC91 (2015) 054913



Open symbols: CMS data;
filled symbols: Glubser flow

K-*p* mass splitting of m_T -slopes increases
with *pp* multiplicity



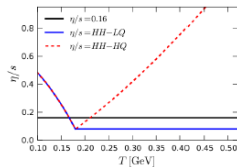
Radial flow in *pp*?

Flow in small systems?

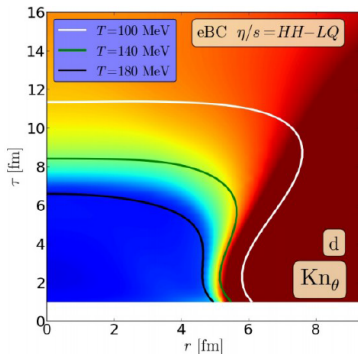
Validity of viscous hydro: Knudsen number check

Niemi & Denicol, arXiv:1404.7327

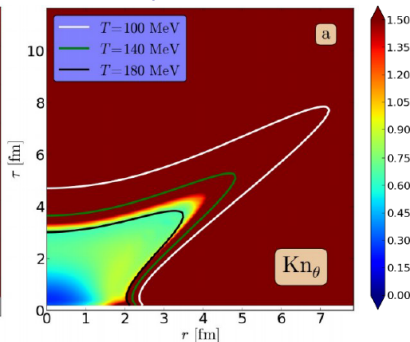
$$\text{Kn} = \tau_{\text{micro}} \theta = \tau_{\text{micro}} / \tau_{\text{macro}}$$



Pb+Pb



p+Pb



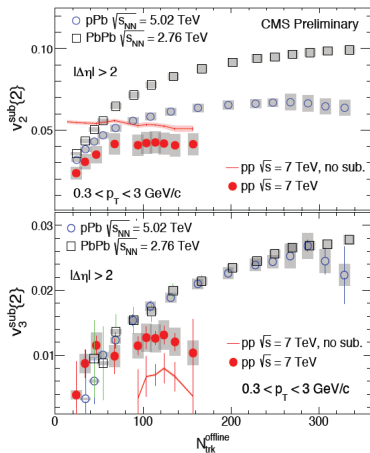
Predicts freeze-out at higher temperature in p+Pb than in Pb+Pb

Flow in small systems?

Flow in small systems?

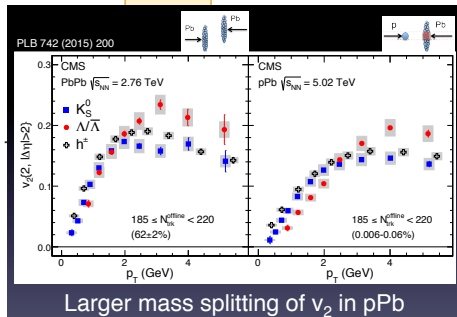
Long-range correlations in high-mult. pp

Flow parameter analysis



Z. Chen

CMS-HIN-15-009

Larger mass splitting of v_2 in pPb

- $v_2(pp) < v_2(pPb) < v_2(PbPb)$
- $v_3(pp) \approx v_3(pPb) \approx v_3(PbPb)$, but $v_3(pp)$ deviates for $N_{trk}^{offline} \gtrsim 90$
- Mass ordering for $v_2^{sub}\{2\}$ at low p_T

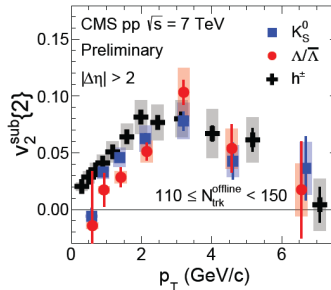
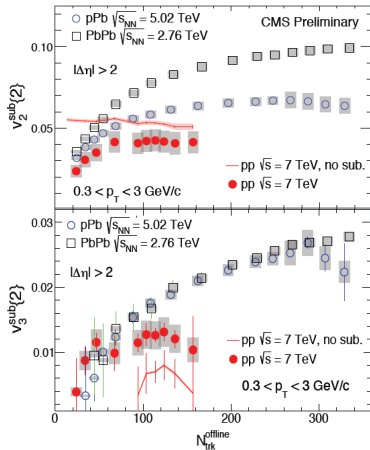
Flow in small systems?

Long-range correlations in high-mult. pp

Z. Chen

CMS-HIN-15-009

Flow parameter analysis



- $v_2(\text{pp}) < v_2(\text{pPb}) < v_2(\text{PbPb})$
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Byungsik Hong

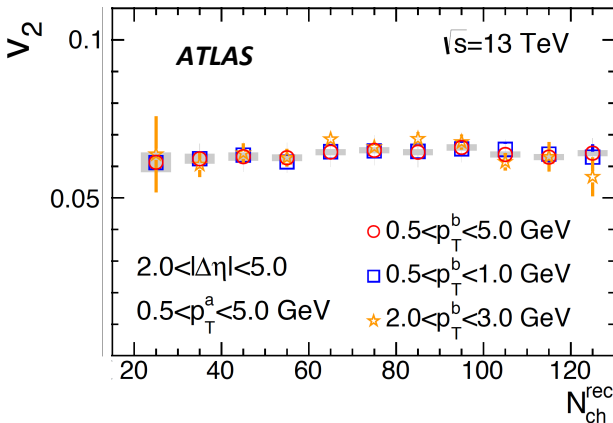
Quark Matter 2015, Kobe

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Flow in small systems?

Flow in small systems?



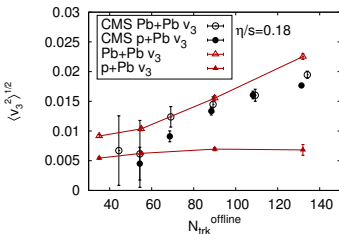
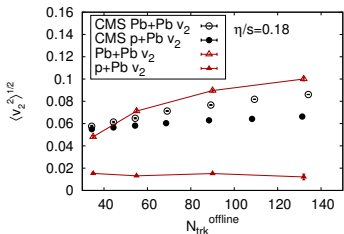
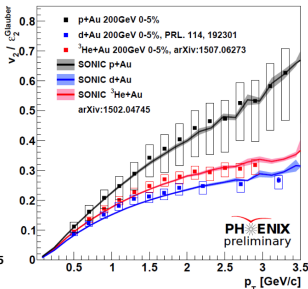
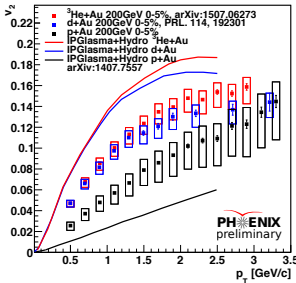
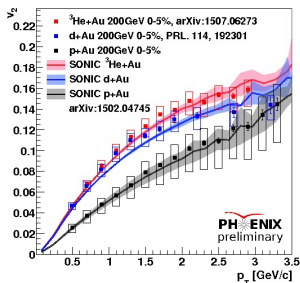
No centrality dependence of elliptic flow in pp?!

Flow not just in high-multiplicity pp?!

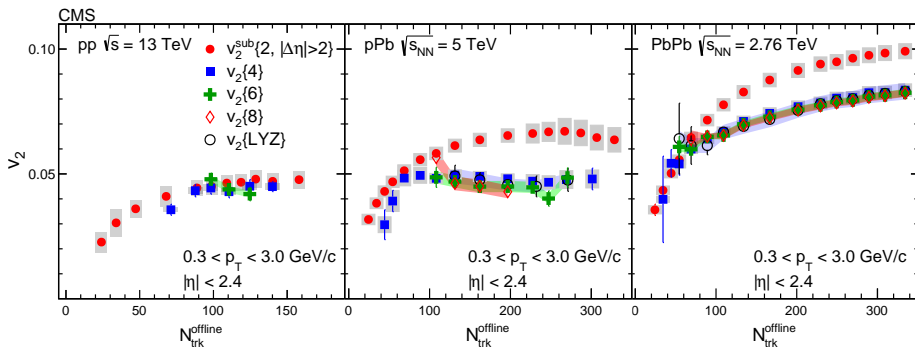
Not flow but something else?

Do small systems behave hydrodynamically?

Do small systems behave hydrodynamically?



Collectivity in small systems!

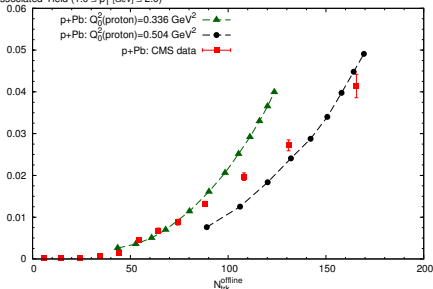


Whatever its origin, the “flow signal” represents a collective response (to what?) of all particles!

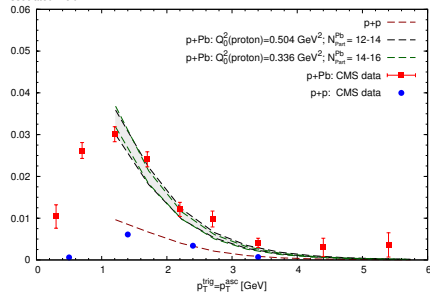
Initial-state momentum correlations?

Dusling and Venugopalan, PRD87 (2013) 054014

Associated Yield ($1.0 \leq p_T [\text{GeV}] \leq 2.0$)



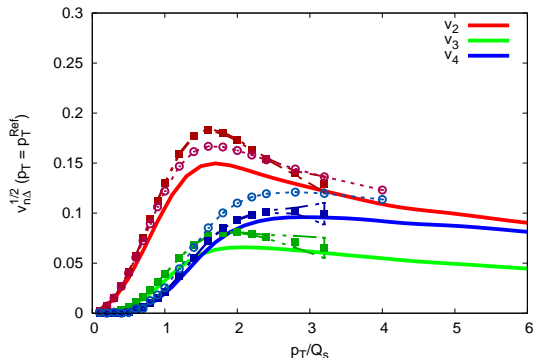
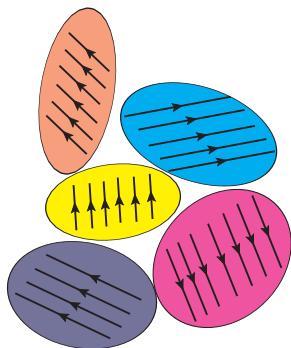
Associated Yield



Initial-state momentum (anti-)correlations from “Glasma graphs” qualitatively explain the multiplicity dependence and p_T -dependence at high p_T of the **ridge yields** in pPb and high-multiplicity pp collisions

Initial-state momentum correlations?

Lappi, Schenke, Schlichting, Venugopalan, JHEP 2016 (arXiv:1509.03499)



Spatial inhomogeneity of CGC and spatial deformation of CGC regions of homogeneity generate momentum anisotropies among the initially produced partons, corresponding to non-zero v_n for all n , with “reasonable-looking” p_T dependence.

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What is needed to resolve this ambiguity?

- Initial conditions for the phase-space distribution of the produced matter,

$$f_{\text{matter}}(x_{\perp}, \phi_s; p_{\perp}, \phi_p; y_p - \eta_s; \tau_0)$$

which depends on the

- phase-space (Wigner) distribution of the glue inside the nucleons bound into small nuclei:

$$f_{\text{glue}}(x_{\perp}, \phi_s; k_{\perp}, \phi_k; y_k - \eta_s; \tau_0)$$

- From f_{matter} we obtain the initial energy-momentum tensor

$$T^{\mu\nu}(x_{\perp}, \eta_s, \tau_0) = \frac{\nu_{\text{dof}}}{(2\pi)^3} \int dy_p d^2 p_{\perp} p^{\mu} p^{\nu} f_{\text{matter}}(x_{\perp}, \phi_s; p_{\perp}, \phi_p; y_p - \eta_s; \tau_0)$$

What is needed to resolve this ambiguity?

- Once the initial $T^{\mu\nu}(x)$ is known, we can evolve it for some time $\tau_{\text{eq}} - \tau_0$ with a pre-equilibrium model, match it to viscous hydrodynamic form,

$$T^{\mu\nu} = eu^\mu u^\nu - (P(e) + \Pi)\Delta^{\mu\nu} + \pi^{\mu\nu},$$

run it through viscous hydrodynamics plus hadronic afterburner, and compare its output with experiment.

- To account for event-by-event quantum fluctuations in the initial $T^{\mu\nu}(x)$, and for thermal noise during the evolution, the dynamical evolution must be performed many times before taking ensemble averages as done in experiment.

What is missing?

What is missing in present calculations?

Present modeling uses simplified assumptions for the initial phase-space distrib'n:

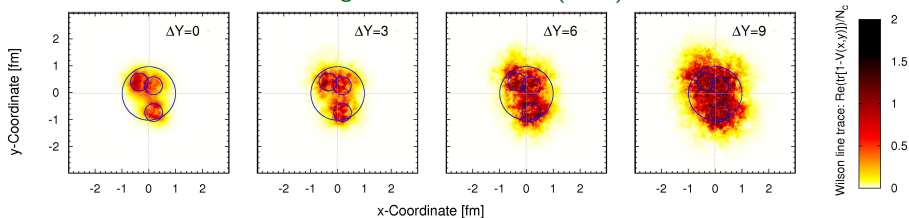
- Few models account for the initial momentum structure of the medium; most ignore it completely. \Rightarrow **incorrect/unreliable initial conditions for $\Pi, \pi^{\mu\nu}$**
- While granularity of the initial spatial density distribution **is accounted for at the nucleon length scale**, by Monte-Carlo sampling the nucleon positions from a smooth Woods-Saxon probability distribution before allowing them to collide and lose energy to create lower-rapidity secondary matter, **quantum fluctuations on sub-nucleonic length scales are poorly controlled and mostly ignored. IP-Glasma includes sub-nucleonic gluon field fluctuations, but appears to get them wrong**, yielding spatial gluon distributions inside protons that are too compact.
- Most approaches (e.g. PHOBOS Glauber Monte Carlo) use disk-like nucleons for computing the collision probability. More realistic collision detection using Gaussian nucleons is implemented in GLISSANDO and iEBE-VISHNU.
- Most approaches ignore quantum fluctuations in the amount of beam energy lost to lower rapidities in a NN collision. Without these, the measured KNO-like multiplicity distributions in pp collisions are not reproduced, and pp collisions produce zero ϵ_3 by symmetry. GLISSANDO and iEBE-VISHNU include pp multiplicity fluctuations, creating non-zero triangularity in pp, even without sub-nucleonic structure.

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“Three quarks for Muster Mark!”

Schlichting, Schenke, PLB739 (2014) 313



- 3 valence quarks act as large- x color sources of the low- x gluon fields.
- Spatial positions of quarks at the instant of collision fluctuate from event to event and generate a lumpy color distribution at large x .
- This lumpiness is tracked by the quarks' gluon clouds, becoming more diffuse at smaller $x \implies$ triune lumpiness of the gluon fields inside the nucleon when viewed through midrapidity particle production, with an intrinsic length scale (“gluonic radius of a quark”) that appears to grow with collision energy.
- \implies Protons have just as much intrinsic triangularity as ^3He nuclei, just on a shorter length scale. But in p+A *all* particle production occurs on a smaller length scale than in $^3\text{He}+A$! This affects mostly radial flow, though.

Modeling quark substructure of the nucleon I

K. Welsh, J. Singer, UH, PRC, in press (arXiv:1605.09418)

- The gluon field density inside the proton is the **sum of three 3-d Gaussians** of norm $\frac{1}{3}$ and width σ_g (representing the gluon clouds around the valence quarks). **Default value:** $\sigma_g = 0.3 \text{ fm}$ (best fit of pPb mult. dist. at LHC)
- The quark positions (centers of the gluon clouds) are sampled from a 3-d Gaussian with width σ_q around the center of the nucleon, requiring their center of mass to coincide with the nucleon center.
- The widths are constrained by $\sigma_g^2 + \frac{2}{3}\sigma_q^2 = B$ such that the average proton density is a normalized Gaussian

$$\langle \rho_p(\mathbf{r}) \rangle = \frac{e^{-\frac{r^2}{2B}}}{(2\pi B)^{2/3}}$$

with \sqrt{s} -dependent width $B(\sqrt{s}) = \frac{\sigma_{\text{NN}}^{\text{inel}}(\sqrt{s})}{8\pi}$, to reproduce the measured inelastic NN cross section.

Modeling quark substructure of the nucleon II

- Projecting ρ_p along z gives the nucleon thickness function $T_N(\mathbf{r}_\perp)$ in the transverse plane.
- Folding two nucleon thickness functions yields the nucleon-nucleon overlap function $T_{NN}(\mathbf{b})$ at impact parameter \mathbf{b} (which actually depends on all 6 quark positions), from which the probability for each of the two nucleons to get wounded in the collision is computed as

$$P_{ij}(\mathbf{r}_{\perp i} - \mathbf{r}_{\perp j}) = 1 - \exp[-\sigma_{gg} T_{NN}(\mathbf{r}_{\perp i} - \mathbf{r}_{\perp j})]$$

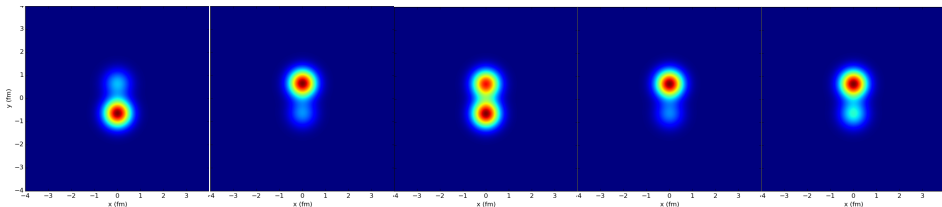
where i and j are from projectile and target, respectively. The gluon-gluon cross section σ_{gg} is determined by the normalization of P_{ij} to the inelastic NN cross section.

- For each wounded nucleon, all three quarks are assumed to contribute to energy production at midrapidity, with a Gaussian density profile of width σ_g and **independently fluctuating (Γ -distributed) normalization**, with variance adjusted to reproduce measured pp multiplicity distributions.

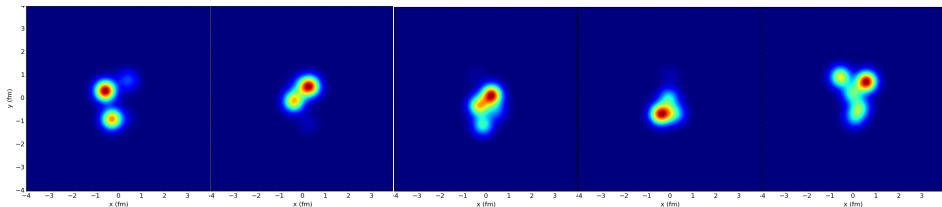
Characteristics of initial entropy density distributions in pp and light-heavy collisions

Initial entropy density in $b=1.3$ fm pp collisions

smooth Gaussian protons:



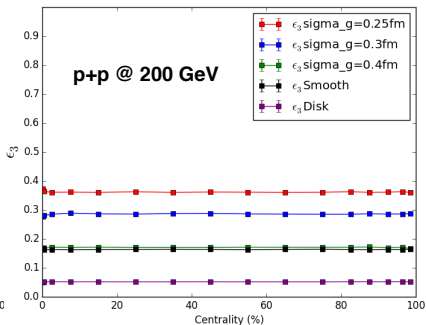
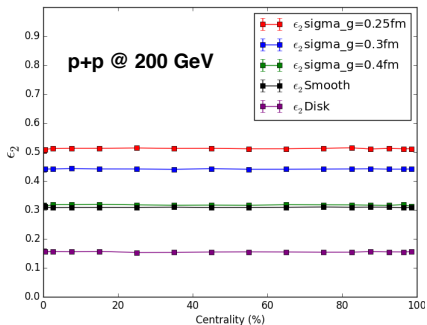
protons with fluctuating quark substructure ($\sigma_g = 0.3$ fm):



For protons with quark substructure the Gaussian collision criterium appears to favor somewhat more compact distributions of produced entropy density

Characteristics of initial entropy density distributions in pp and light-heavy collisions

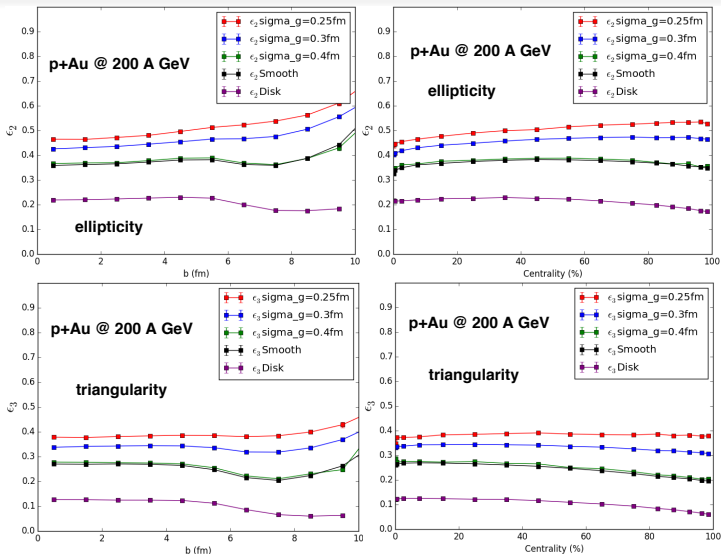
$\varepsilon_{2,3}$ vs. centrality: pp @ $\sqrt{s}=200$ A GeV



- Ellipticity and triangularity show strong sensitivity to σ_g .
- Since $\sqrt{B} = 0.408$ fm at $\sqrt{s} = 200$ GeV, quark subdivision with $\sigma_g = 0.4$ fm is almost indistinguishable from a smooth Gaussian proton.
- Disk-like collision detection gives smallest eccentricities.

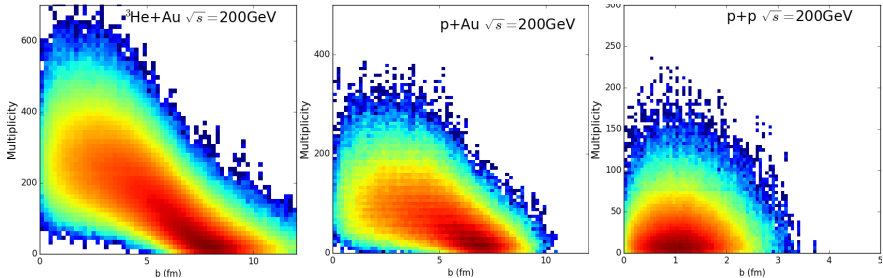
Characteristics of initial entropy density distributions in pp and light-heavy collisions

$\epsilon_{2,3}$ vs. centrality: p+Au @ $\sqrt{s}=200$ A GeV



Characteristics of initial entropy density distributions in pp and light-heavy collisions

In p+p and light+heavy “centrality” does not measure b!

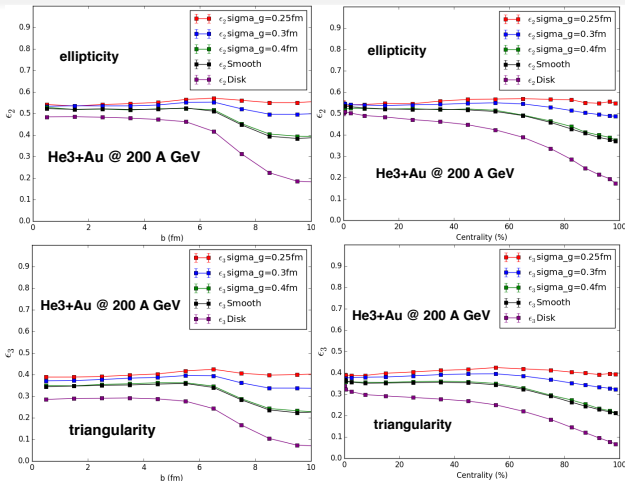


pp multiplicity fluctuations destroy strong anticorrelation between multiplicity and impact parameter seen in Au+Au and Pb+Pb

⇒ “centrality” measured by multiplicity is a misnomer in collisions involving light projectiles

Characteristics of initial entropy density distributions in pp and light-heavy collisions

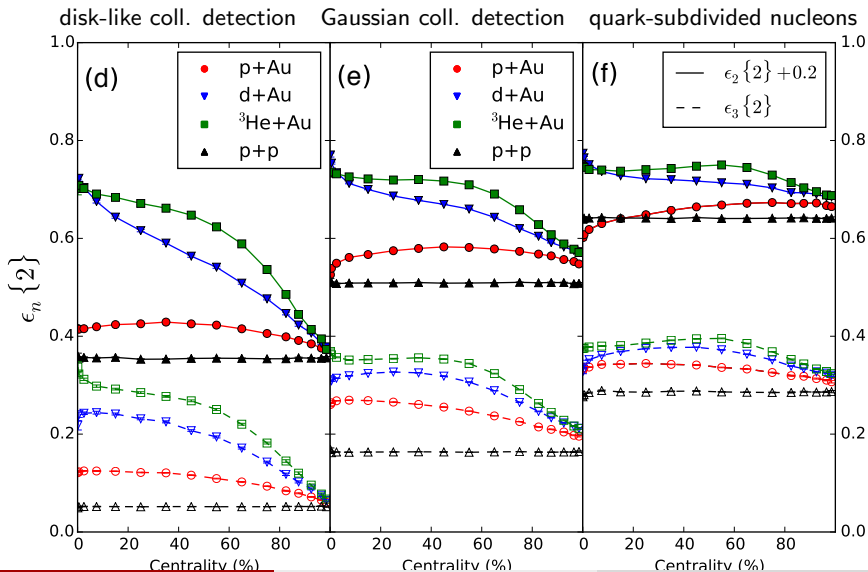
$\varepsilon_{2,3}$ vs. centrality: $^3\text{He}+\text{Au}$ @ $\sqrt{s}=200$ A GeV



Reduced sensitivity to p-substructure and σ_g for larger projectiles, except in peripheral events

Characteristics of initial entropy density distributions in pp and light-heavy collisions

$\epsilon_{2,3}$ vs. “centrality” for different collision systems



Overview

- 1 The big picture
- 2 Flow in small systems?
 - Flow in small systems?
 - Do small systems behave hydrodynamically?
 - Collectivity in small systems
 - Initial-state momentum correlations?
- 3 What is needed to resolve this ambiguity?
 - What is needed?
 - What is missing?
- 4 Proton substructure: what does a proton look like in position space?
 - CGC picture of the nucleon
 - Modeling quark substructure of the nucleon
 - Characteristics of initial entropy density distributions in pp and light-heavy collisions
- 5 Back to the big picture

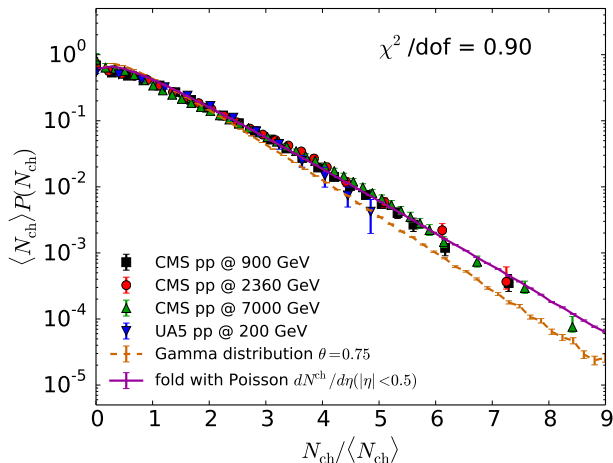
Back to the big question: do pp and pA collisions create droplets of flowing QGP?

- Hydrodynamics is an effective field theory that describes the macroscopic effects of the microscopic transport dynamics
- **Gerry Brown: “Some EFTs are more effective than others!”**
- Israel-Stewart theory cannot handle the rapid, very anisotropic expansion in pp and pA, and fails similarly during the earliest stages in AA collisions
- **Welcome the “more effective” anisotropic hydrodynamics framework (Strickland, Martinez, Florkowski, Bazow, UH, et al.)**
- vAHYDRO minimizes second-order viscous hydro effects by resumming large first-order corrections at leading order
- Stay tuned!

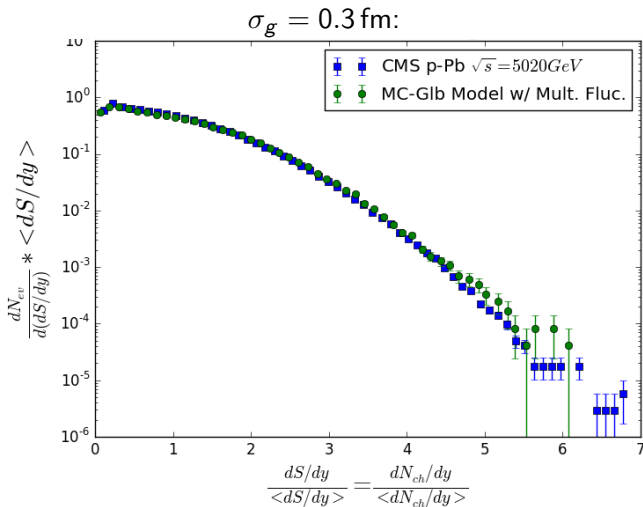
Thank You!

pp multiplicity distribution

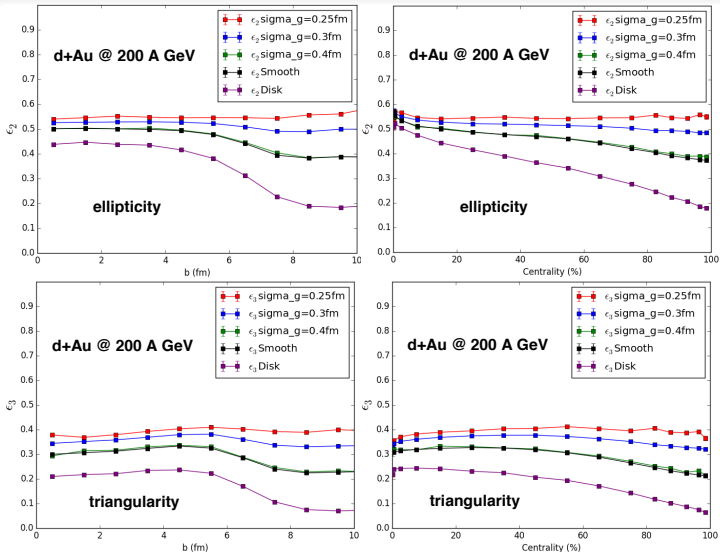
Same for smooth Gaussian and quark-subdivided protons, after rescaling of the Γ -distribution:



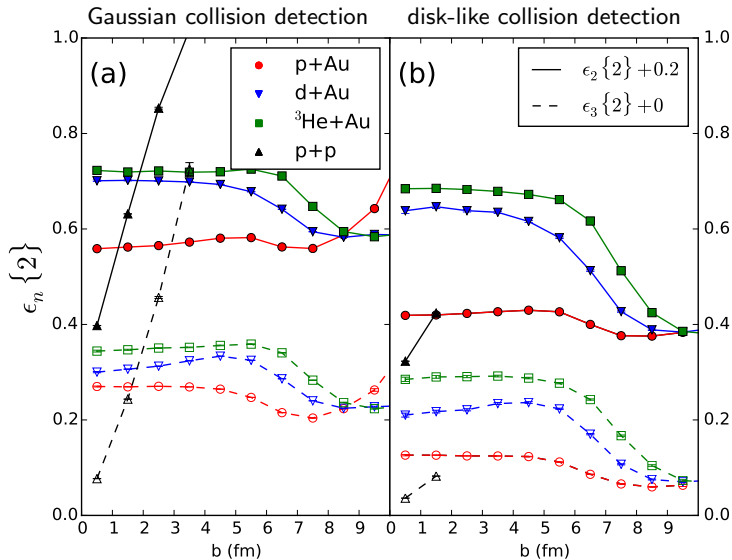
pPb multiplicity distribution



$\epsilon_{2,3}$ vs. centrality: d+Au @ $\sqrt{s}=200$ A GeV



$\epsilon_{2,3}$ vs. impact parameter for different collision systems



ϵ_2 - ϵ_3 correlations: pp & light-heavy collisions, $\sigma_g = 0.3$ fm

