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Steps beyond the Standard Model: searching for simplicity

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For 125 GeV Higgs mass the Standard Model is a self-consistent weakly coupled effective field theory for all energies up to the quantum gravity scale $M_P \sim 10^{19}$ GeV The LHC results must be reconciled with experimental evidence for new physics beyond the Standard Model:

- Observations of neutrino oscillations (in the SM neutrinos are massless and do not oscillate)
- Evidence for Dark Matter (SM does not have particle physics candidate for DM).
- No antimatter in the Universe in amounts comparable with matter (baryon asymmetry of the Universe is too small in the SM)
- Cosmological inflation is absent in canonical variant of the SM
- Accelerated expansion of the Universe (?) though can be "explained" by a cosmological constant.

Marginal evidence (less than 2σ) for the SM vacuum metastability given uncertainties in relation between Monte-Carlo top mass and the top quark Yukawa coupling



Bednyakov et al, '15

Vacuum is unstable at 1.3σ



Where is new physics?

Energy scale of new physics:

- Neutrino masses and oscillations: the masses of right-handed see-saw neutrinos can vary from $\mathcal{O}(1) \text{ eV to } \mathcal{O}(10^{15}) \text{ GeV}$
- Dark matter, absent in the SM: the masses of DM particles can be as small as $\mathcal{O}(10^{-22}) \text{ eV}$ (super-light scalar fields) or as large as $\mathcal{O}(10^{20}) \text{ GeV}$ (wimpzillas, Q-balls).
- Baryogenesis, absent in the SM: the masses of new particles, responsible for baryogenesis (e.g. right-handed neutrinos), can be as small as $\mathcal{O}(10)$ MeV or as large as $\mathcal{O}(10^{15})$ GeV
- Higgs mass hierarchy : models related to SUSY, composite Higgs, large extra dimensions require the presence of new physics right above the Fermi scale , whereas the models based on scale invariance (quantum or classical) may require the absence of new physics between the Fermi and Planck scales

Searching for simplicity:

New Physics without new energy scale

Quantum scale invariance and naturalness

If the mass of the Higgs boson is put to zero in the SM, the Lagrangian has a wider symmetry: it is scale and conformally invariant: Dilatations - global scale transformations ($\sigma = const$)

 $\Psi(x) \rightarrow \sigma^n \Psi(\sigma x) ,$

n = 1 for scalars and vectors and n = 3/2 for fermions.

It is tempting to use this symmetry for solution of the hierarchy problem

Common lore: quantum scale invariance does not exist, divergence of dilatation current is not-zero due to quantum corrections:

 $\partial_\mu J^\mu \propto eta(g) G^a_{lphaeta} G^{lphaeta\ a} \ ,$

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The way out: scale independent subtraction of divergences

Toy model

Classically scale-invariant Lagrangian

$$\mathcal{L} = rac{1}{2} (\partial_\mu h)^2 + rac{1}{2} (\partial_\mu \chi)^2 - V(arphi,\chi)$$

Potential (χ - "dilaton", φ - "Higgs"):

$$V(arphi,\chi) = rac{\lambda}{4} \left(h^2 - rac{lpha}{\lambda}\chi^2
ight)^2 + eta\chi^4,$$

 $\beta < 0$: vacuum is unstable

eta = 0: flat direction, $h^2 = \frac{\alpha}{\lambda} \chi^2$. Choice of parameters: $lpha \sim \left(\frac{M_W}{M_P}\right)^2 \sim 10^{-32}$, to get the Higgs-Planck hierarchy correctly.

Standard reasoning

Dimensional regularisation $d = 4 - 2\epsilon$, \overline{MS} subtraction scheme: mass dimension of the scalar fields: $1 - \epsilon$,

mass dimension of the coupling constant: 2ϵ

Counter-terms:

$$\lambda = \mu^{2\epsilon} \left[\lambda_R + \sum_{k=1}^\infty rac{a_n}{\epsilon^n}
ight] \; ,$$

 μ is a dimensionful parameter!!

One-loop effective potential along the flat direction:

$$V_1(\chi) = rac{m_H^4(\chi)}{64\pi^2} \left[\log rac{m_H^2(\chi)}{\mu^2} - rac{3}{2}
ight] \; ,$$

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Idea: Replace $\mu^{2\epsilon}$ by combinations of fields χ and h, which have the correct mass dimension:

$$\mu^{2\epsilon} o \chi^{rac{2\epsilon}{1-\epsilon}} F_\epsilon(x) \ ,$$

where $x = h/\chi$. $F_{\epsilon}(x)$ is a function depending on the parameter ϵ with the property $F_0(x) = 1$.

Englert, Truffin, Gastmans '76; Zenhäusern, M.S '09 two loop analysis: Ghilencea et al, '16 Almost trivial statement - by construction: Quantum effective action is scale invariant in all orders of perturbation theory.

Less trivial statement Gretsch, Monin '15: Quantum effective action is conformally invariant in all orders of perturbation theory.

The main problem with this construction: theory is not renormalisable, one needs to add infinite number of counter-terms.

However:

- For $\alpha \ll 1$ all counter-terms are suppressed by the dimensionful parameter $\langle \chi \rangle$
- We get an effective field theory valid up to the energy scale fixed
 by $\langle \chi \rangle$
- Gravity is non-renormalisable anyway, and making <a> χ $\sim M_P$ does not make a theory worse

Hierarchy problem

For $\alpha = \beta = 0$ the classical Lagrangian has an extra symmetry : $\chi \rightarrow \chi + const$. Therefore, there are no large perturbative corrections to the Higgs mass: those proportional to χ contain necessarily α or β , those proportional to λ contain only logs of χ . This construction leads to "natural" hierarchy $\chi \gg h$. However, no explanation of why $\alpha \ll 1$.

$$V(arphi,\chi) = rac{\lambda}{4} \left(h^2 - rac{lpha}{\lambda}\chi^2
ight)^2 + eta\chi^4,$$

Important ingredient for naturalness: almost exact shift symmetry. Requirement of the shift symmetry \equiv requirement of absence of heavy particles with sufficiently strong interaction with the Higgs field and the dilaton, e.g.

$\lambda_h h^2 \phi^2 + \lambda_\chi \chi^2 \phi^2$

 $\lambda_h \sim \lambda_\chi \sim 1$ spoils the argument! Also: C. Tamarit

Conjecture: natural theory should not have heavy particles between the Fermi and Planck scales

Inclusion of gravity

Planck scale: through non-minimal coupling of the dilaton to the Ricci scalar.

Gravity part

$$\mathcal{L}_G = -\left(\xi_\chi \chi^2 + \xi_h h^2
ight) rac{R}{2} \, ,$$

This term, for $\xi_{\chi} \sim 1$, does break the shift symmetry. However, this is a coefficient in front of graviton kinetic term. Since the graviton stays massless in any constant scalar background, the perturbative computations of gravitational corrections to the Higgs mass in scale-invariant regularisation are suppressed by M_P . There are no corrections proportional to M_P !



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Consequences

- Theory is "natural" in perturbative sense: Higgs mass is stable against radiative corrections
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- Since it is a Goldstone boson of spontaneously broken symmetry it has only derivative couplings to matter (inclusion of gravity is essential: it makes scale transformations to be internal symmetry!)

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- The dilaton is massless in all orders of perturbation theory
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- Fifth force or Brans-Dicke constraints are not applicable to it

Problems

- What happens beyond perturbation theory?
- What leads to selection of parameter β = 0 ≡ existence of flat direction ≡ absence of the cosmological constant ?
- Unitarity and high-energy behaviour: What is the high-energy behaviour ($E > M_{Pl}$) of the scattering amplitudes? Is the theory unitary? Can it have a scale-invariant UV completion?

The minimal model - scale invariant ν MSM

Requirements: no heavy particles with sufficiently strong interaction with the Higgs field and the dilaton + simplicity Similar in spirit studies: SMASH by Ballesteros et al; V. Khoze et al

Particle content

Particles of the SM ╋ graviton dilaton 3 Majorana leptons

Scale-invariant Lagrangian

$$egin{split} \mathcal{L}_{
u\mathrm{MSM}} &= \mathcal{L}_{\mathrm{SM}[\mathrm{M}
ightarrow 0]} + \mathcal{L}_{G} + rac{1}{2} (\partial_{\mu}\chi)^{2} - V(arphi,\chi) \ &+ ig(ar{N}_{I}i\gamma^{\mu}\partial_{\mu}N_{I} - h_{lpha I}\,ar{L}_{lpha}N_{I} ilde{arphi} - f_{I}ar{N}_{I}ar{arphi} - h_{lpha I}\,ar{\chi} + \mathrm{h.c.}ig) \;, \end{split}$$

Potential (χ - dilaton, φ - Higgs, $\varphi^{\dagger}\varphi = 2h^2$):

$$V(arphi,\chi) = \lambda \left(arphi^\dagger arphi - rac{lpha}{2\lambda}\chi^2
ight)^2 + eta\chi^4,$$

Gravity part

$${\cal L}_G = - \left(\xi_\chi \chi^2 + 2 \xi_h arphi^\dagger arphi
ight) {R \over 2} \, ,$$

Roles of different particles

The roles of dilaton:

- determine the Planck mass
- give mass to the Higgs
- give masses to 3 Majorana leptons

Roles of the Higgs boson:

- give masses to fermions and vector bosons of the SM
- provide inflation

New physics below the Fermi scale: the ν MSM



Role of N_1 with mass in keV region: dark matter.

Role of N_2 , N_3 with mass in 100 MeV – GeV region: "give" masses to neutrinos and produce baryon asymmetry of the Universe.

The couplings of the νMSM

Particle physics part, accessible to low energy experiments: the ν MSM. Mass scales of the ν MSM:

 $M_I < M_W$ (No see-saw)

Consequence: small Yukawa couplings,

$$F_{lpha I} \sim rac{\sqrt{m_{atm} M_I}}{v} \sim (10^{-6} - 10^{-13}),$$

here $v \simeq 174$ GeV is the VEV of the Higgs field, $m_{atm} \simeq 0.05$ eV is the atmospheric neutrino mass difference. Small Yukawas are also necessary for stability of dark matter and baryogenesis (out of equilibrium at the EW temperature). Cosmology and phenomenology of a minimal model
Inflation: Higgs boson

Potential in Einstein frame for non-minimally coupled Higgs, ξRh^2



 χ - canonically normalised scalar field in Einstein frame.





- Makes the Universe flat, homogeneous and isotropic
- Produces fluctuations leading to structure formation: clusters of galaxies, etc

CMB parameters - spectrum and tensor modes, $\xi \gtrsim 1000$









- All particles of the Standard Model are produced
- Coherent Higgs field disappears
- The Universe is heated up to $T \propto M_P / \xi \sim 10^{14} \text{ GeV}$

DM: sterile neutrino N_1



3.5 keV line: E. Bulbul et al, Boyarsky et al

Akhmedov, Rubakov, Smirnov; Asaka, MS

 $N_{2,3}$ HNL dynamics as a source of baryon asymmetry. Qualitatively:

- HNL are created in the early universe and oscillate in a coherent way with CP-breaking.
- Lepton number from HNL can go to active neutrinos and back.
- The lepton number of active left-handed neutrinos is transferred to baryons due to equilibrium sphaleron processes.

Constraints on BAU HNL $N_{2,3}$



Constraints on U^2 coming from the baryon asymmetry of the Universe, from the see-saw formula, from the big bang nucleosynthesis and experimental searches. Left panel - normal hierarchy, right panel inverted hierarchy (Canetti, Drewes, Frossard, MS). Other studies: Drewes et al., Hernandez et al

Summary of predictions, 2005-2009

Prediction	assumptions	status
No deviations from SM at LHC	structure of ν MSM	ОК
SM Higgs boson with $M_H > 127 \pm 2~{ m GeV}$	Higgs inflation	OK within 2σ
SM Higgs boson with $M_H = 127 \pm 2~{ m GeV}$	asymptotic safety	OK within 2σ
No WIMPS	structure of ν MSM	ОК
DM is a keV scale HNL , $N o u \gamma$	structure of ν MSM	3.5 keV X-ray line?
New particles - HNL	structure of ν MSM	constraints only
Unitarity of PMNS matrix	structure of ν MSM	ОК
no light sterile $ u$	structure of ν MSM	ОК
neutrino mass $m_1 \lesssim 10^{-5}$ eV	dark matter	constraints only
No visible $\mu ightarrow e\gamma, \ \mu ightarrow 3e, etc$	BAU	ОК
$N_ u = 3$	structure of ν MSM	OK, Planck
spectral index $n_s = 0.967$	Higgs inflation	OK, Planck
small tensor to scalar ratio $r = 0.003$	Higgs inflation	Planck, constraints only
no non-Gaussianities	Higgs inflation	Planck, constraints only

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Theoretical challenges, similar to the Standard Model:

- UV completion, unification with gravity
- Why the Higgs and HNL masses are so much smaller than the Planck scale?
- Why the cosmological constant (or dark energy) is so tiny?
- Origin and magnitude of Yukawa couplings

Experimental challenges:

- HNL production and decays are highly suppressed dedicated experiments or analyses are needed:
 - Mass below $\sim 2~{
 m GeV}$ Intensity frontier, CERN SPS.
 - Mass above ~ 2 GeV FCC in e^+e^- mode in Z-peak, LHC
 - HNL's in beauty and charm decays: Belle, LHCb

Proposal to Search for Heavy Neutral Leptons at the SPS arXiv:1310.1762

W. Bonivento, A. Boyarsky, H. Dijkstra, U. Egede, M. Ferro-Luzzi, B. Goddard, A. Golutvin, D. Gorbunov, R. Jacobsson, J. Panman, M. Patel, O. Ruchayskiy, T. Ruf, N. Serra, M. Shaposhnikov, D. Treille

General beam dump facility: Search for Hidden Particles



Hidden sector: very weakly interacting relatively light particles: HNL, dark photon, scalars, ALPS, etc



Energy Scale

SHiP is currently a collaboration of 46 institutes from 15 countries

web-site: http://ship.web.cern.ch/ship/



Survey of constraints, $N_{2,3}$



- HNL (N₁) dark matter searches in X-rays, future after Astro-H failure
 - Micro-calorimeter on sounding rocket (2017): instrument with large field-of-view and very high spectral resolution
 - Large ESA X-ray mission (2028) Athena + , X-ray spectrometer (X-IFU) with unprecedented spectral resolution



Conclusions

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 - inflation Higgs boson
 - neutrino masses, dark matter and baryogenesis 3 HNLs

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- High energy limit?
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