

Precision predictions for $t\bar{t}$ production. Status and prospects.

David Heymes

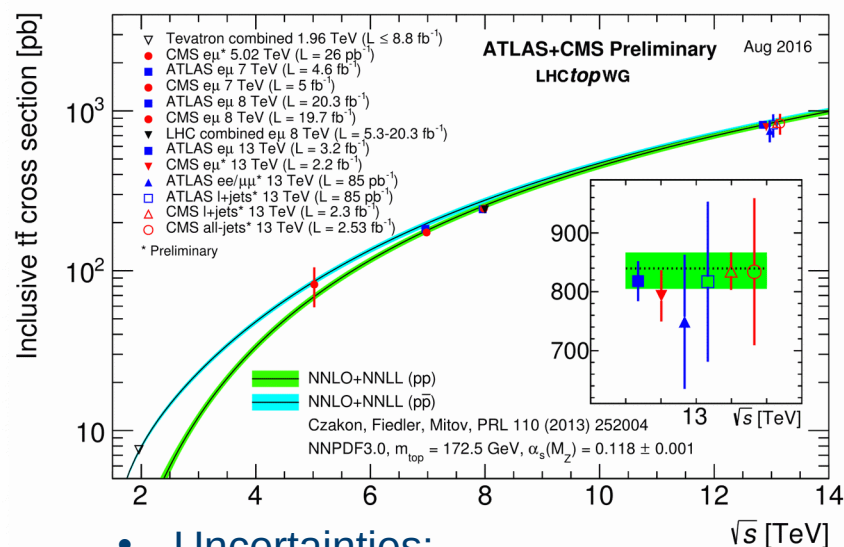
Future challenges for precision QCD 2016, Durham

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Cavendish Laboratory - HEP Group

Top-Quark pairs at the LHC (total cross section)

- Precision QCD predictions for the top-quark pair production cross section



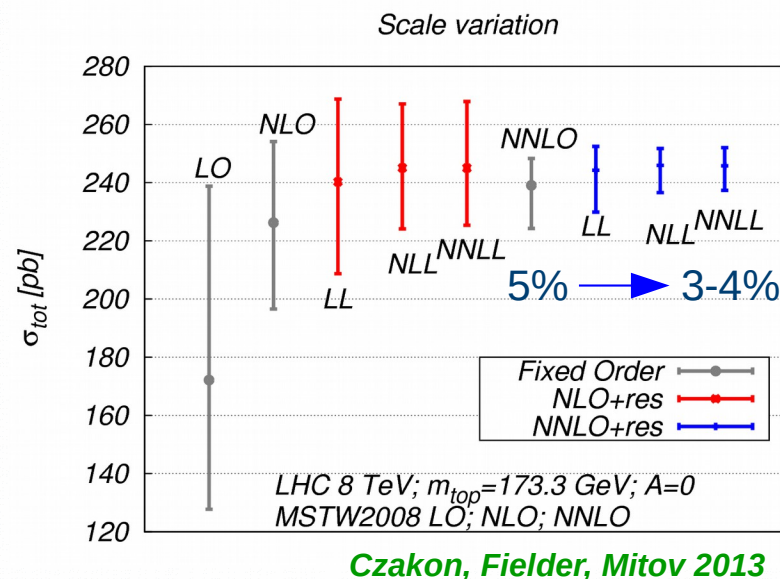
- Uncertainties:

Scales	~ 3-4%
pdf	~ 2-3%
α_s	~ 1.5%
m_{top}	~ 3%



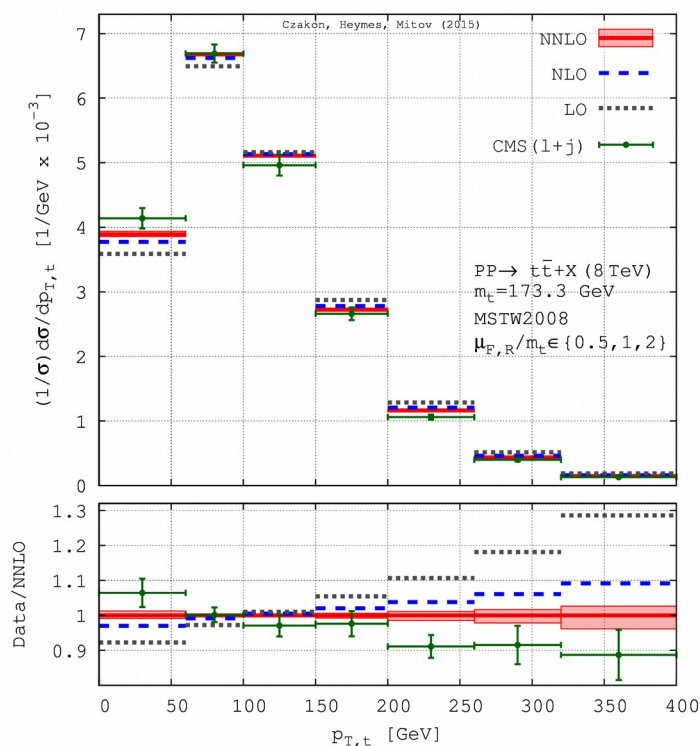
NNLO needed (at least)

Single measurements: < 4%



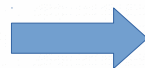
Top-Quark pairs at the LHC (differential)

- Precision (NNLO) for differential distributions → better description of data
- Example: transverse momentum distribution at 8 TeV



Czakon, DH, Mitov 2015

- Discrepancy between data and prediction is alleviated at NNLO
- Calculation with fixed scales (here: m_{top}) is limited to low p_T and invariant mass region
- Dynamical scales in extended kinematical regime required (→ probed at the LHC)



Precision predictions in a wide regime

Dynamical scales for top-quark pair production (1)

- Fixed order perturbative QCD
 - Only ambiguity is the choice of renormalization and factorization scale

$$\sigma_{h_1 h_2}(P_1, P_2) = \sum_{ab} \iint_0^1 dx_1 dx_2 f_{a/h_1}(x_1, \mu_F^2) f_{b/h_2}(x_2, \mu_F^2) \hat{\sigma}_{ab}(x_1 P_1, x_2 P_2; \alpha_s(\mu_R^2), \mu_R^2, \mu_F^2)$$

- Choose dynamical scale in order to maintain/improve perturbative convergence

$$\mu_0 \sim m_t,$$

$$\mu_0 \sim m_T = \sqrt{m_t^2 + p_{T,t}^2},$$

$$\mu_0 \sim H_T = \sqrt{m_t^2 + p_{T,t}^2} + \sqrt{m_t^2 + p_{T,\bar{t}}^2},$$

$$\mu_0 \sim H'_T = \sqrt{m_t^2 + p_{T,t}^2} + \sqrt{m_t^2 + p_{T,\bar{t}}^2} + \sum_i p_{T,i},$$

$$\mu_0 \sim E_T = \sqrt{\sqrt{m_t^2 + p_{T,t}^2} \sqrt{m_t^2 + p_{T,\bar{t}}^2}},$$

$$\mu_0 \sim H_{T,\text{int}} = \sqrt{(m_t/2)^2 + p_{T,t}^2} + \sqrt{(m_t/2)^2 + p_{T,\bar{t}}^2},$$

$$\mu_0 \sim m_{t\bar{t}},$$

← 1/2

← 1/4

Recommendation for p_T of the top

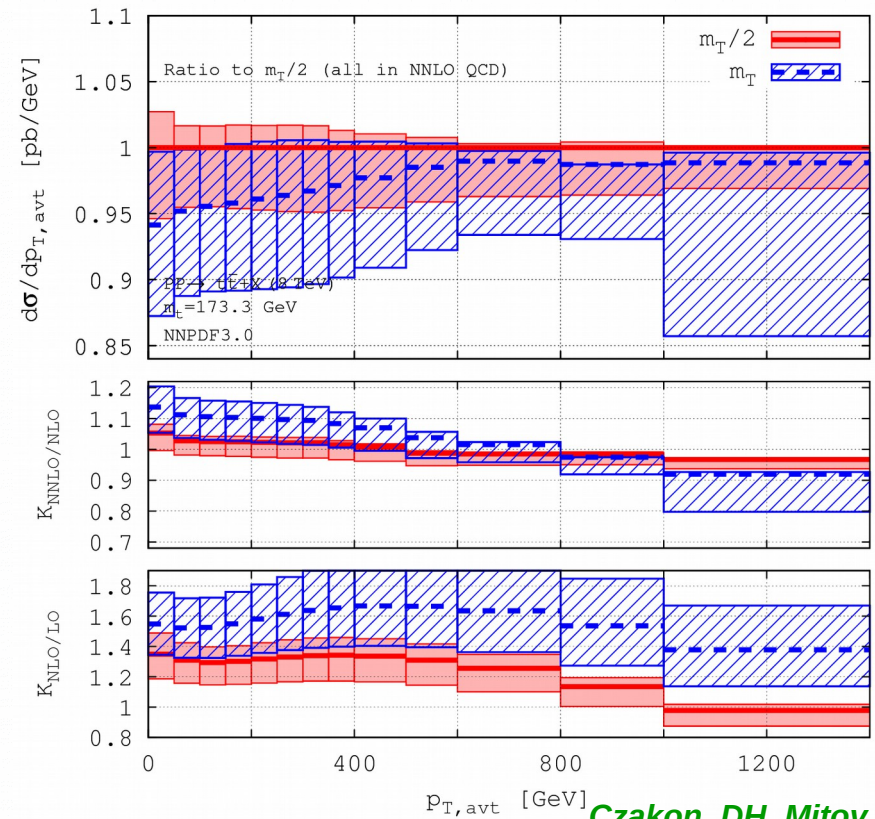
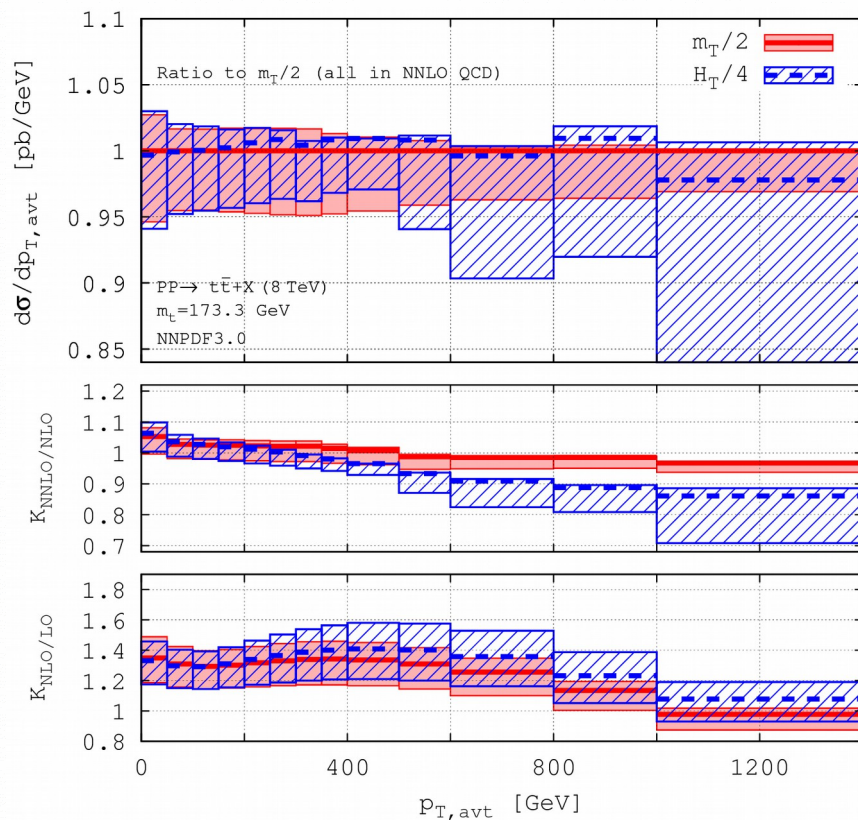
Recommendation for $m_{t\bar{t}}$ (and others)

Czakon, DH, Mitov 2016

Remark: Different observables/different processes require different scales.

Dynamical scales for top-quark pair production (2)

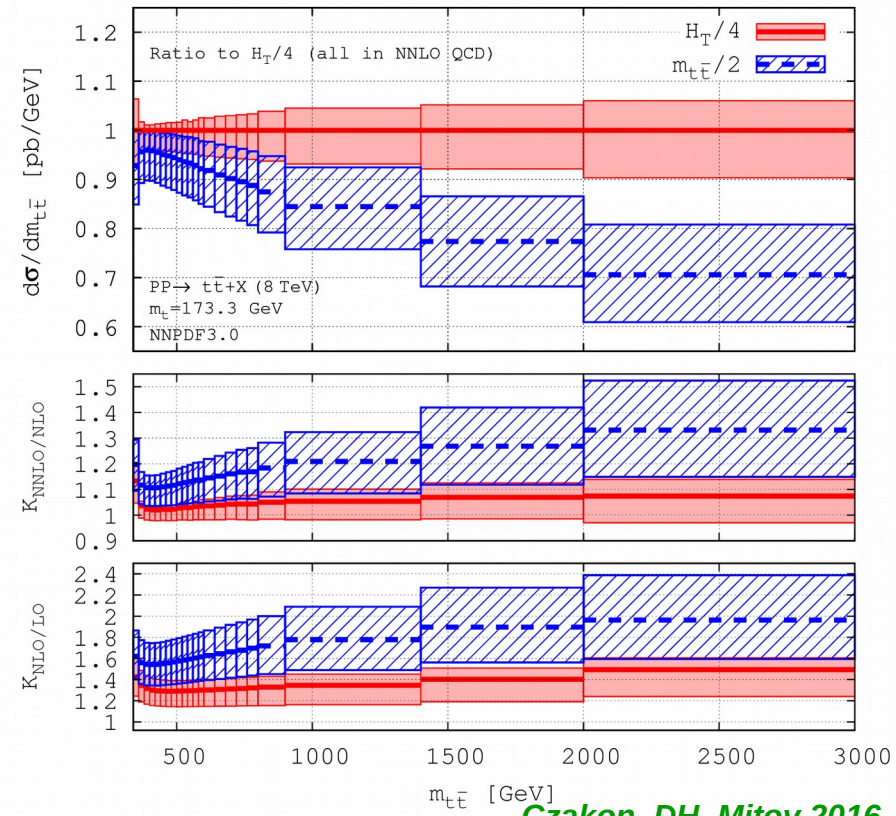
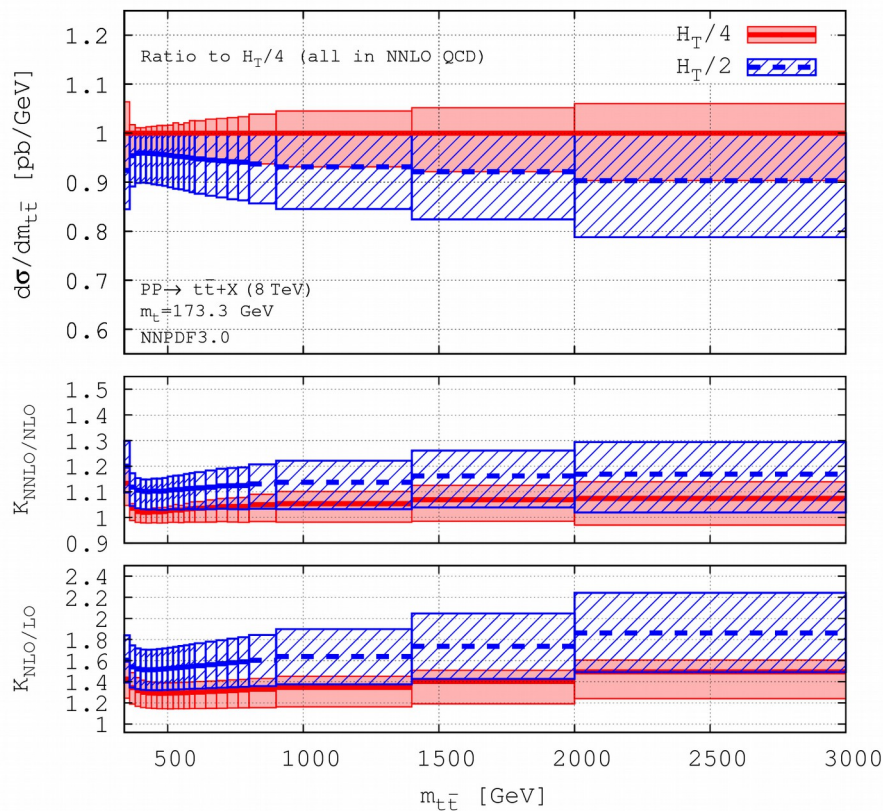
- Comparison of different scales (average top/antitop p_T) at 8 TeV
 - Main differences in k-factors and scale uncertainties



Czakon, DH, Mitov 2016

Dynamical scales for top-quark pair production (3)

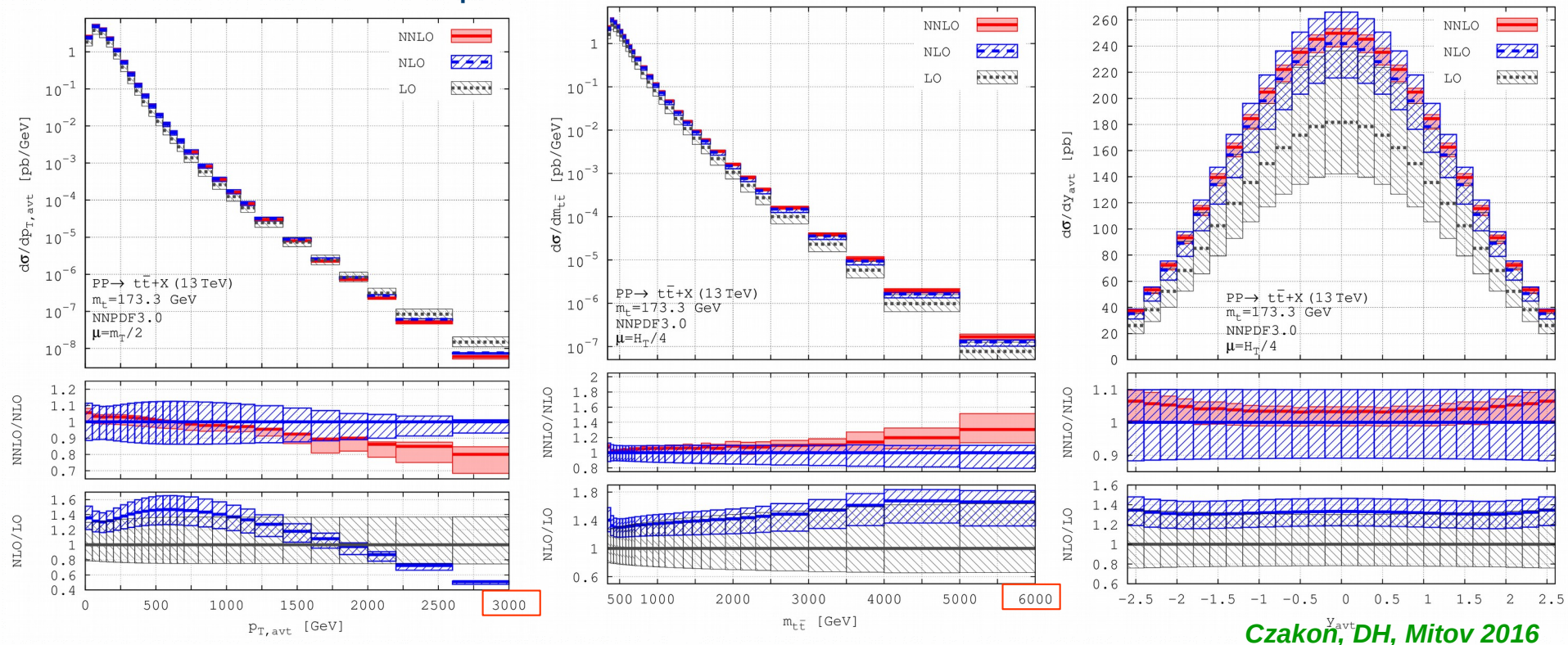
- Comparison of different scales ($m_{t\bar{t}}$ – distribution) at 8 TeV
- Scales based on invariant mass itself seem to behave worse



Czaron, DH, Mitov 2016

Differential NNLO QCD predictions for the LHC (1)

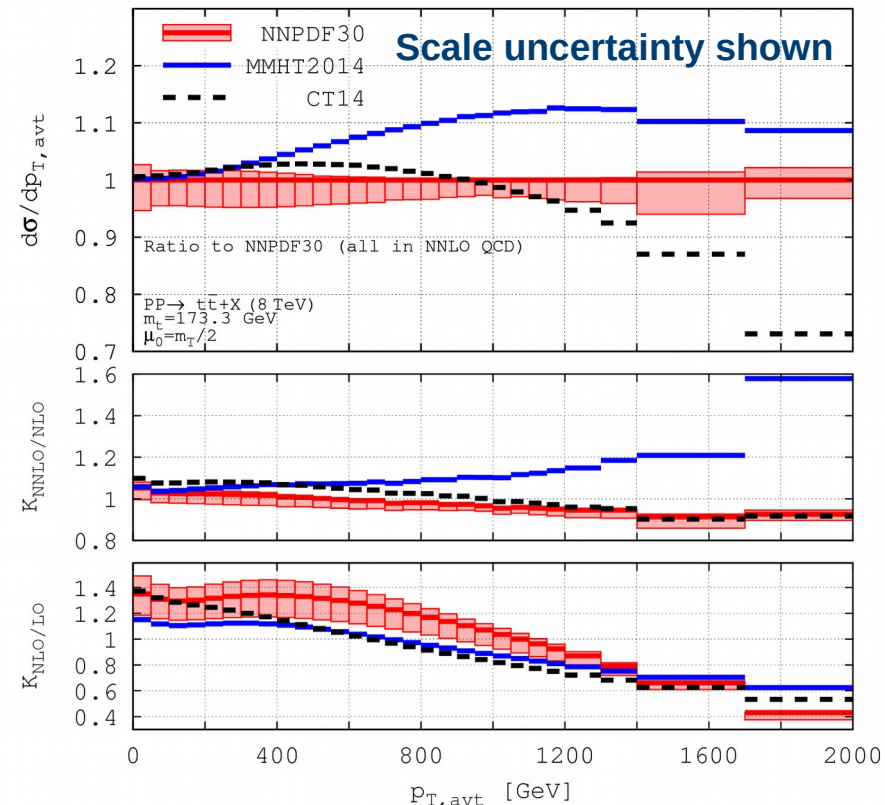
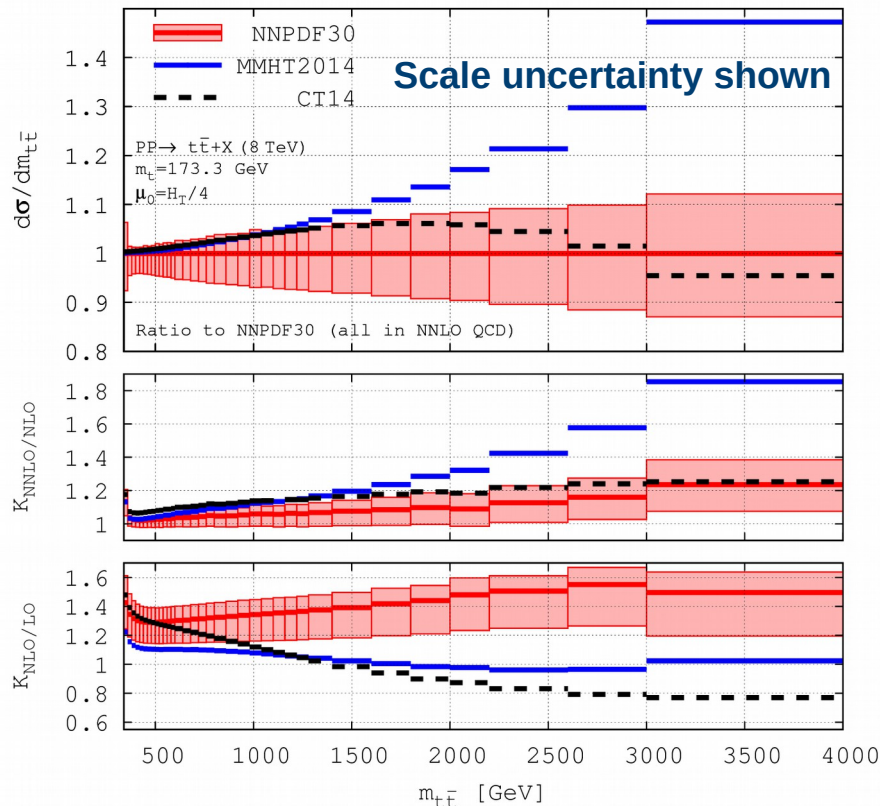
- LHC at 13 TeV
- Good perturbative convergence in a wide kinematical regime
- Scale choice is independent of the PDF set used



Differential NNLO QCD predictions for the LHC (2)

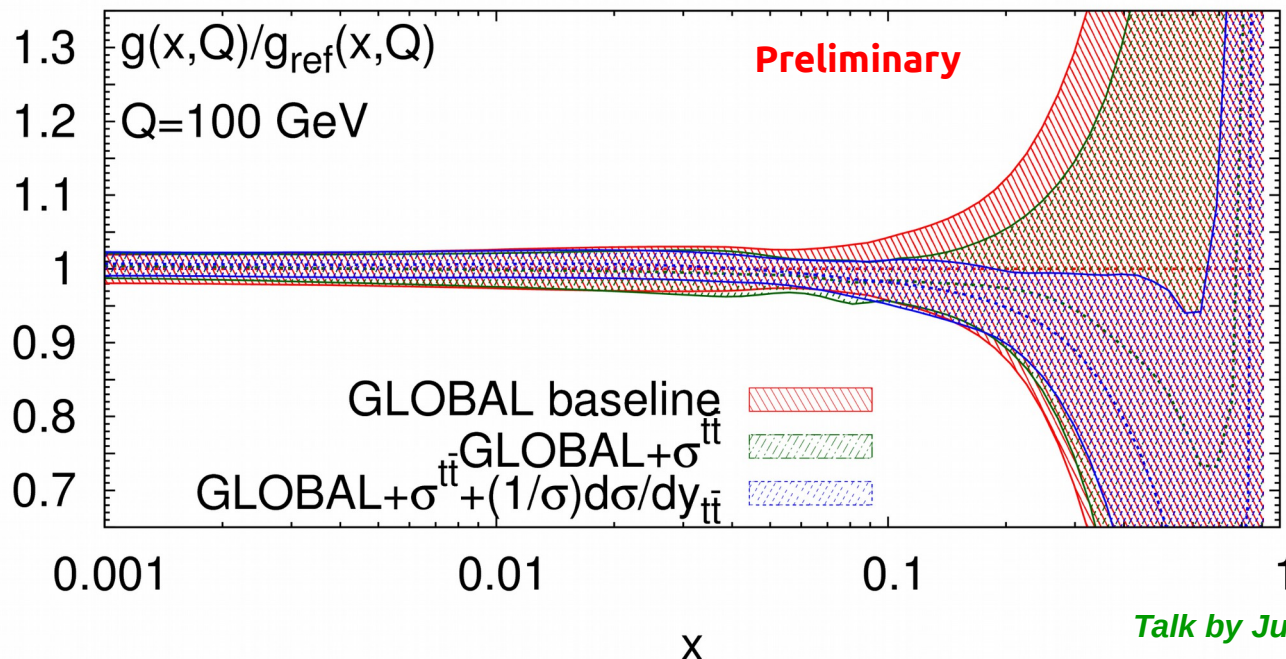
- Above a certain threshold ($m_{t\bar{t}}$ and $p_{T,\text{avt}}$) PDF sets have large uncertainties
- Main source of uncertainty at (very) large $p_{T,\text{avt}}/m_{t\bar{t}}$
- Use $t\bar{t}$ -distributions to constrain pdf sets?

Czakon, DH, Mitov 2016



Impact of differential distributions on gluon PDF

- Inclusion of total cross section already reduces gluon PDF uncertainty at $x > 0.1$ using Tevatron and LHC measurements (NNPDF30, MMHT14, ...) *Czakon, Mangano, Mitov, Rojo 2013*
 - Reduction of uncertainties of gluon initiated processes
- Include $t\bar{t}$ top quark differential distributions at 8TeV (ATLAS, CMS) into NNPDF *Czakon, Hartland, Mitov, Nocera, Rojo in preparation*



Talk by Juan Rojo at PDF4LHC meeting 2016

Adding NLO EW corrections

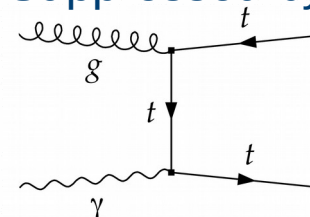
EW correction for tt production

- Naive power counting suggests that one should consider EW corrections at this level of accuracy ($\alpha_s \sim 0.1$, $\alpha \sim 0.01$)

		naive	reality(σ_{tot})
LO QCD	α_s^2	100%	100%
NLO QCD	α_s^3	10%	50%
NNLO QCD	α_s^4	1%	15%

		naive
LO EW	$\alpha_s \alpha$	10%
	α^2	1%
NLO EW	$\alpha_s^2 \alpha$	1%
	...	subleading

Suppressed by photon PDF



Sudakov enhanced negative corrections at regions $M_w \ll p_{T,} m_{tt}$

EW correction for tt production

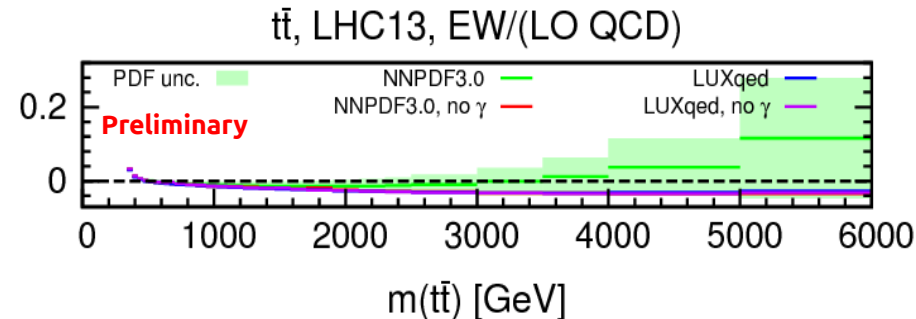
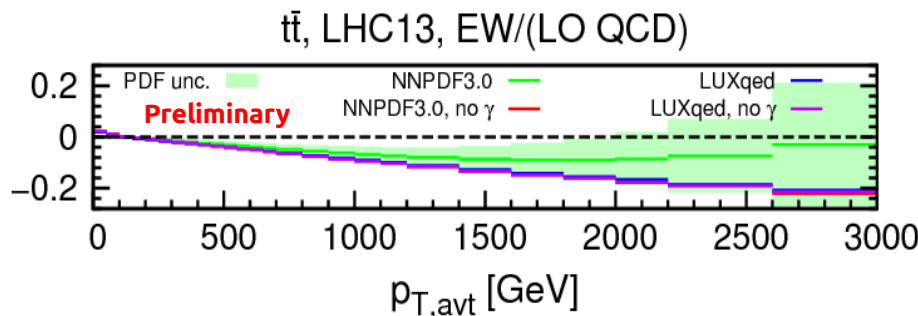
- History of EW corrections for on-shell $t\bar{t}$
 - Purely weak *Beenakker et al. 1994; Kühn et al. 2006-2013; Bernreuther et al. 2006; Campbell et al. 2016*
 - QED *Hollik, Kollar 2008*
 - Asymmetry A_{FB} *Hollik, Pagani 2011; Kühn, Rodrigo 2012; Manohar, Trott 2012; Bernreuther, Si 2012*
 - NLO+EW+decay(NWA) *Bernreuther, Si 2010*
- NLO QCD + EW (MadGraph5_aMC@NLO framework) *Pagani, Tsinikos, Zaro 2016*
 - Thorough study of photon induced contributions $\alpha_s\alpha$, $\alpha_s^2\alpha$, ... (subleading)
 - Pdf sets including photon pdf
 - MRSTW2004QED *Martin et al. 2004*
 - CT14QED *Schmidt et al. 2016*
 - NNPDF2.3QED, NNPDF3.0QED *Ball et al. 2013; Bertone Carraza 2016*
 - LUXqed *Manohar et al. 2016 Talk by P. Nason*
- Conclusion: Treatment of the photon pdf as in LUXqed (small photonic contribution)

Dependence on the Photon PDF

NNPDF30 vs. LUXqed

Czakon, DH, Mitov, Pagani, Tsinikos, Zaro in preparation

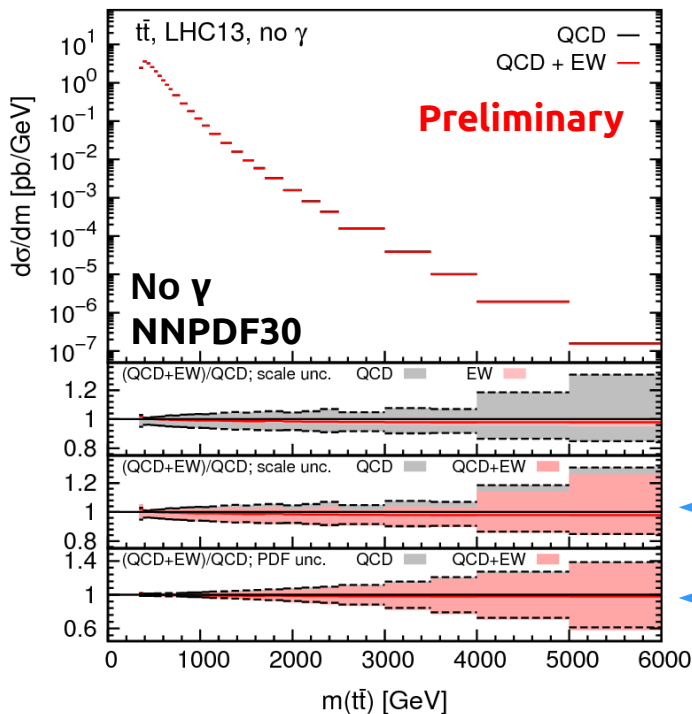
- Large differences for photon PDFs
- Photon contribution is much smaller in LUXqed (negligible ?)
- LUXqed at the lower edge of NNPDF30 uncertainty band
- NNPDF30 (no γ) at the same order as LUXqed
→ no compensation from photon induced channels expected



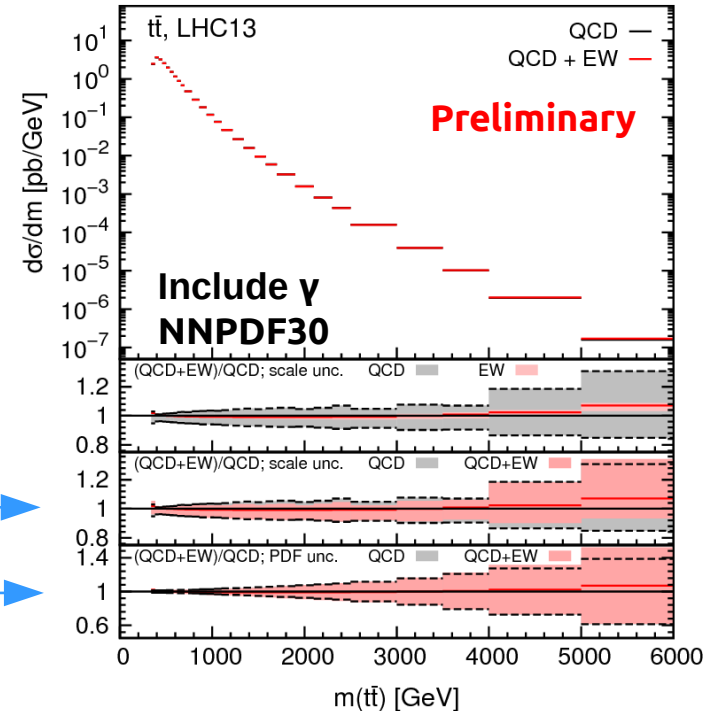
Combining NNLO QCD and EW for the invariant mass

Czakon, DH, Mitov, Pagani, Tsinikos, Zaro (in progress)

- Very small EW corrections in the whole energy range (1%)
- Large PDF uncertainties in the high energy range ($m_{t\bar{t}} > \sim 3$ TeV)
- Use NNLO for new physics searches (bump-hunting) *Czakon, DH, Mitov 2016*



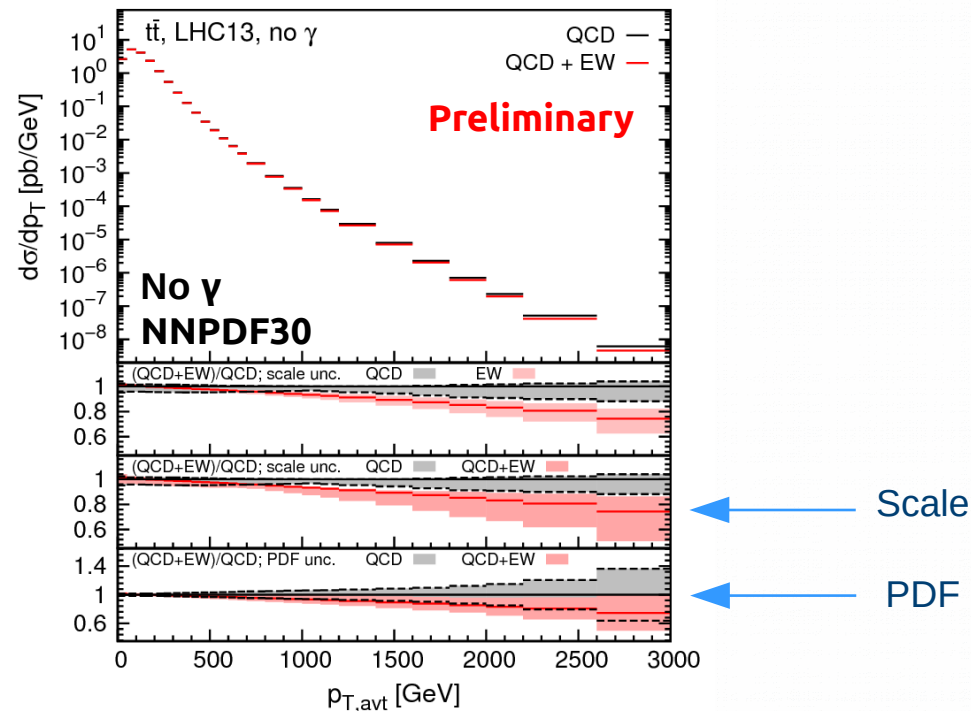
Scale
PDF



Combining NNLO QCD and EW for the p_T of the top

Czakon, DH, Mitov, Pagani, Tsinikos, Zaro (in progress)

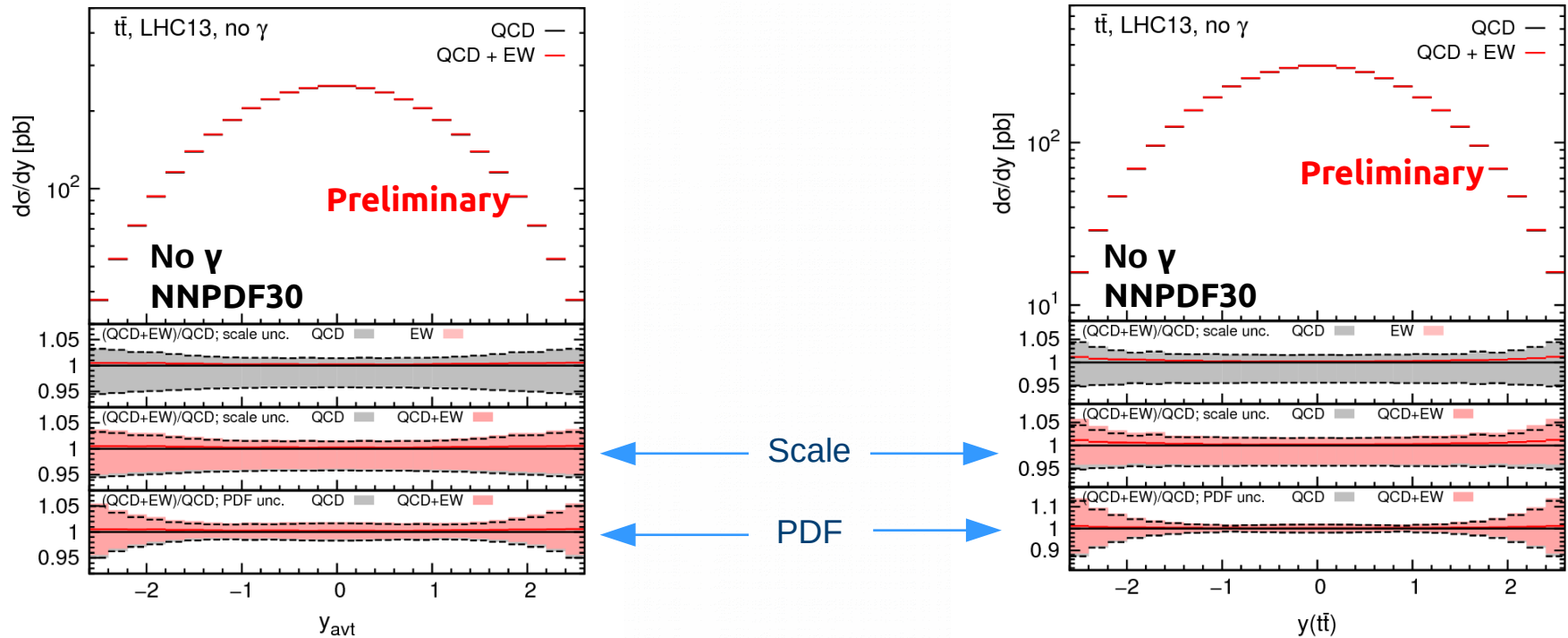
- Negative Sudakov contributions are sizeable (up to 20%) at very large p_T (> 2 TeV)
- They are outside the QCD scale uncertainty band, but inside the PDF uncertainty
- PDF uncertainty is large at high p_T



Combining NNLO QCD and EW for the rapidity

Czakon, DH, Mitov, Pagani, Tsinikos, Zaro (in progress)

- Very small EW corrections in the whole range (1%)
- PDF uncertainties large at high y_{tt}



Large logarithms in the boosted regime

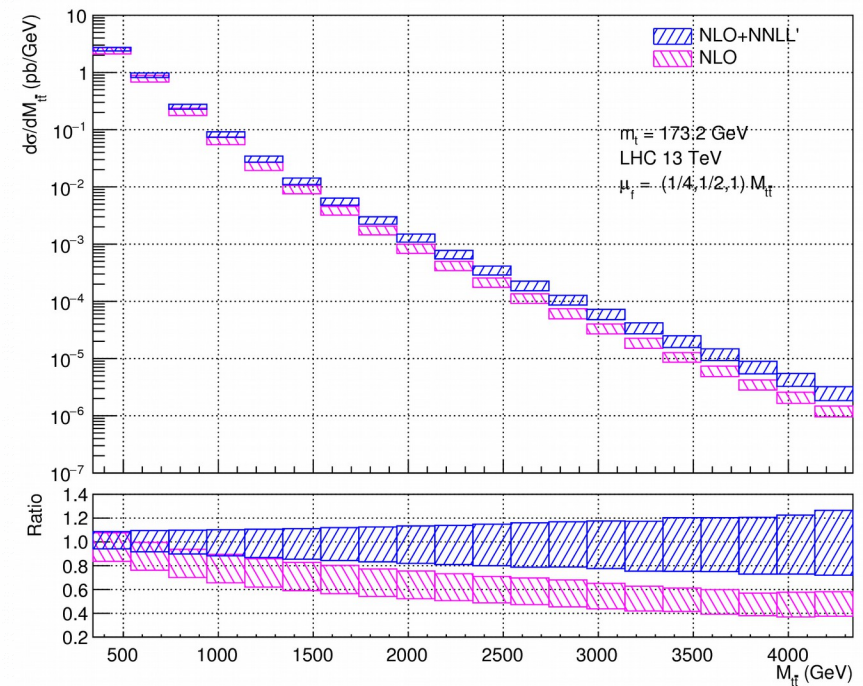
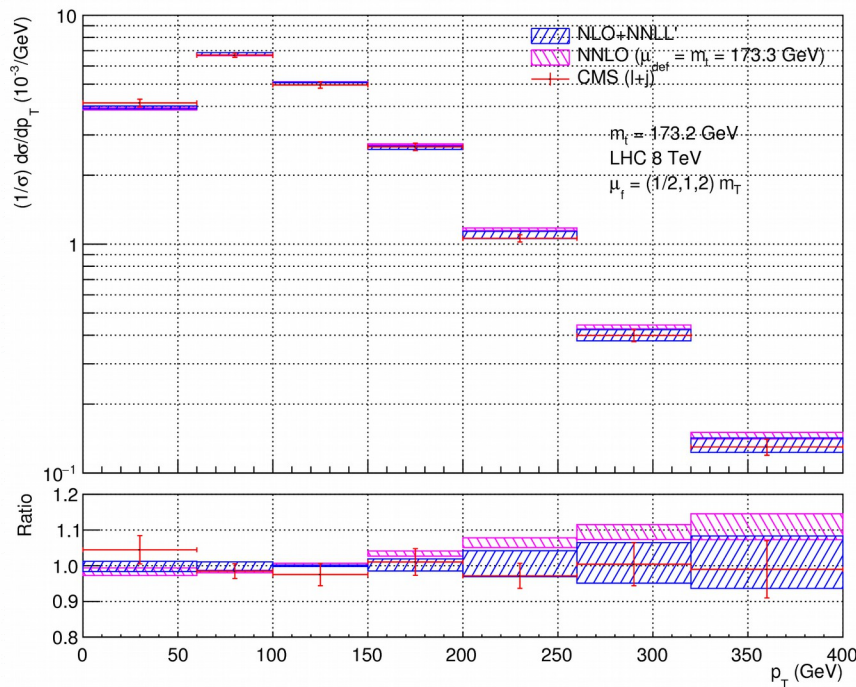
Large QCD logarithms in the boosted regime

- Large logarithms at $s > m_t$

e.g. : $\ln^n(m_t/m_T)$, where $m_T = \sqrt{m_t^2 + p_T^2}$

- Not captured by fixed order perturbation theory → Resummation NNLL'

Ferroglia, Pecjak, Scott, Wang, Yang 2015-2016



- At which scale do these contributions become important? *Work in progress at NNLO*

Application:

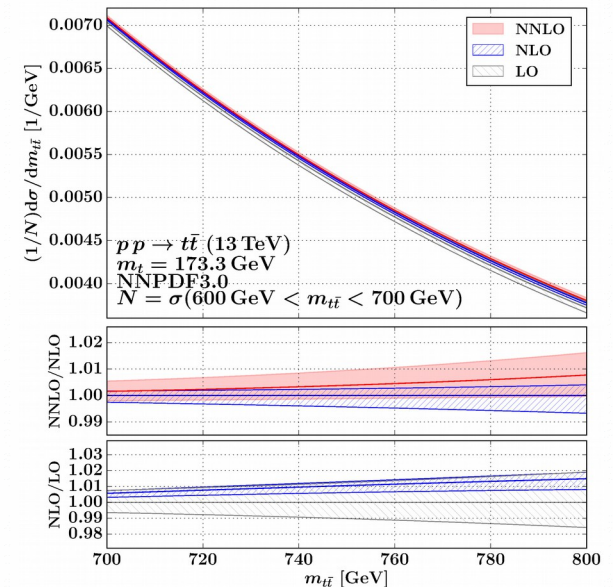
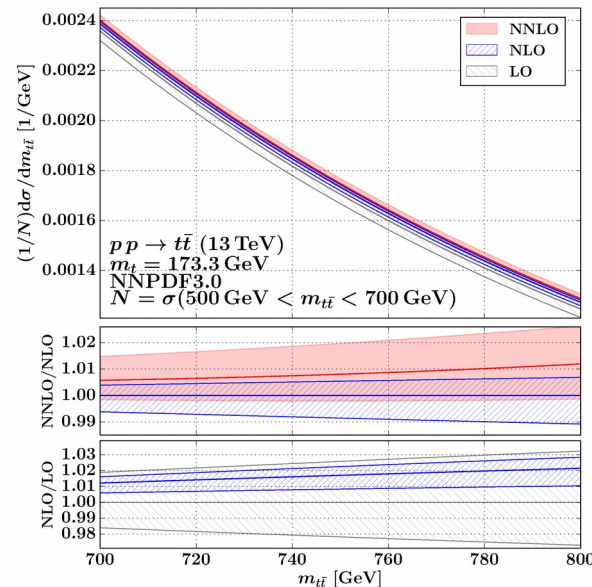
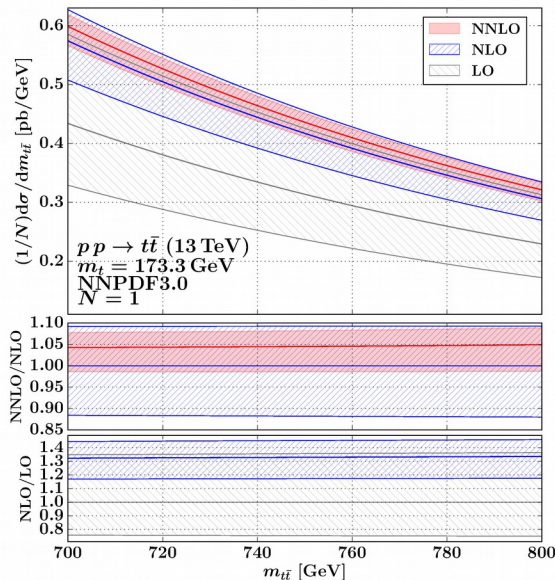
Bump-hunting using m_{tt} – distribution at NNLO

Bumps in top-pair invariant mass distribution

- Minimize theory uncertainty → choose appropriate normalization

NNLO scale + (approx.) PDF uncertainty added in quadrature

Czakon, DH, Mitov 2016



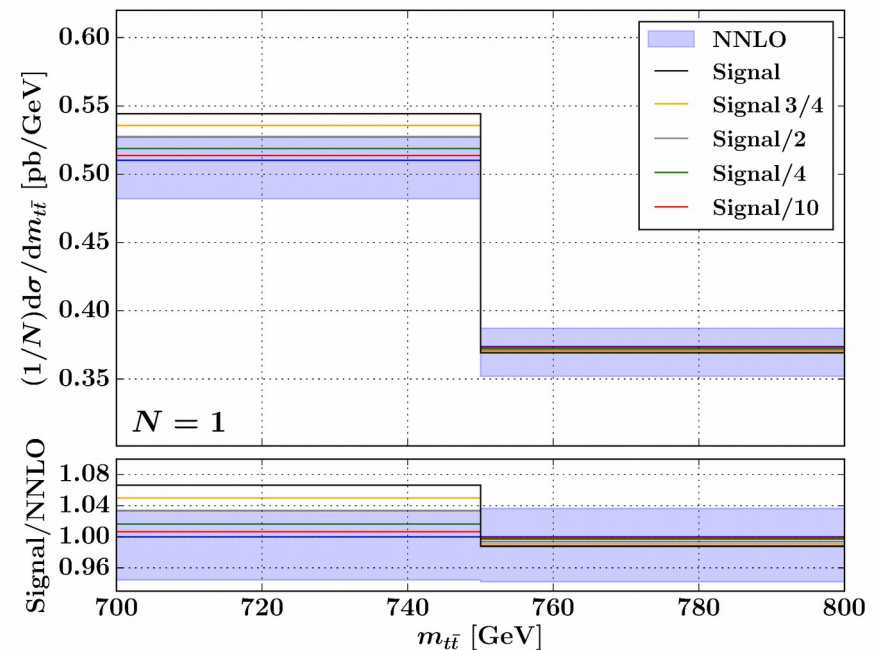
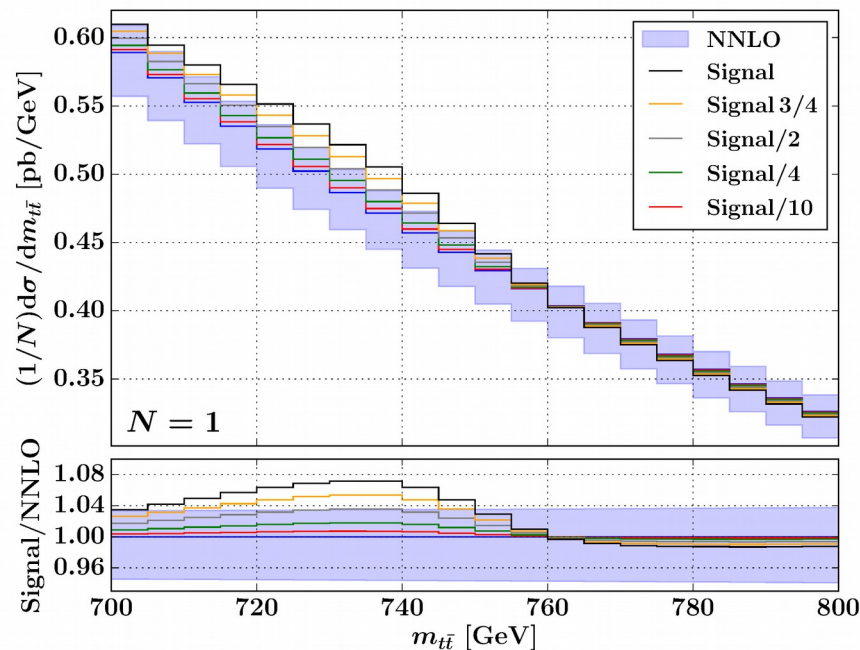
- Trade off between experimental uncertainty and theory uncertainty to choose N
 - Minimize dependence on the top-mass $\ll 1\%$, checked at NLO
- Analytic fit of the distribution allows flexible rebinning

Bump Hunting using $m_{t\bar{t}}$ – distribution at NNLO

- Minimize uncertainties → choose appropriate normalization
- Discriminate a possible BSM signal from background for different possible binnings

NNLO scale + (approx.) PDF uncertainty added in quadrature

Czakon, DH, Mitov 2016



Signal from: Hespel, Maltoni, Vryonidou 2016

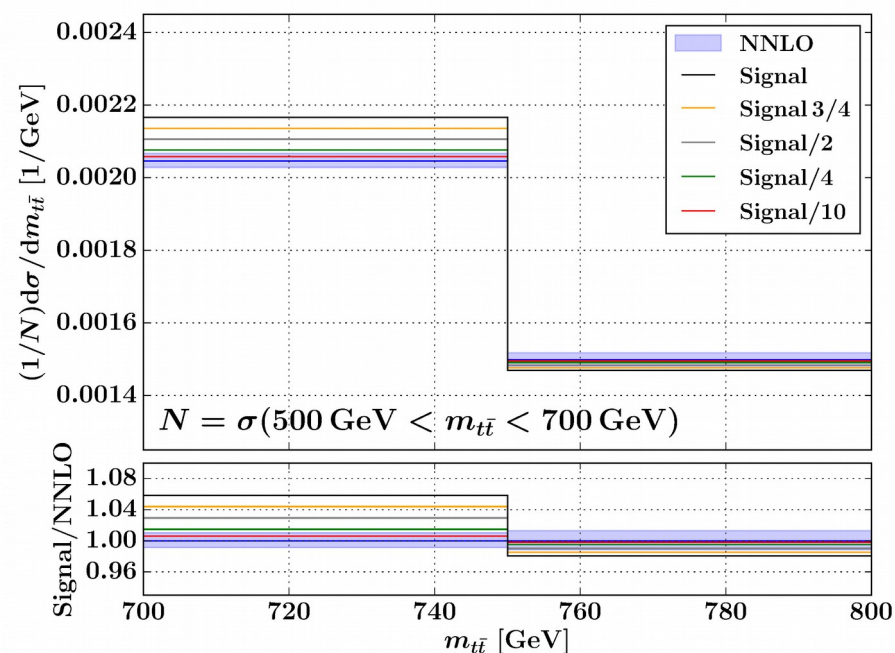
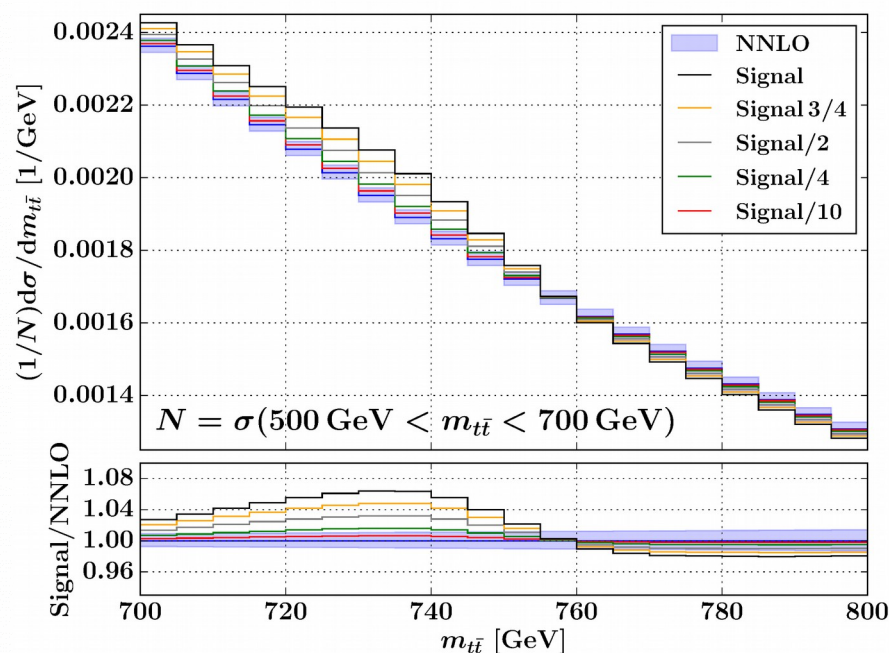
- Significance depends on bin-width and position of the bin

Bump Hunting using $m_{t\bar{t}}$ – distribution at NNLO

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Czakon, DH, Mitov 2016



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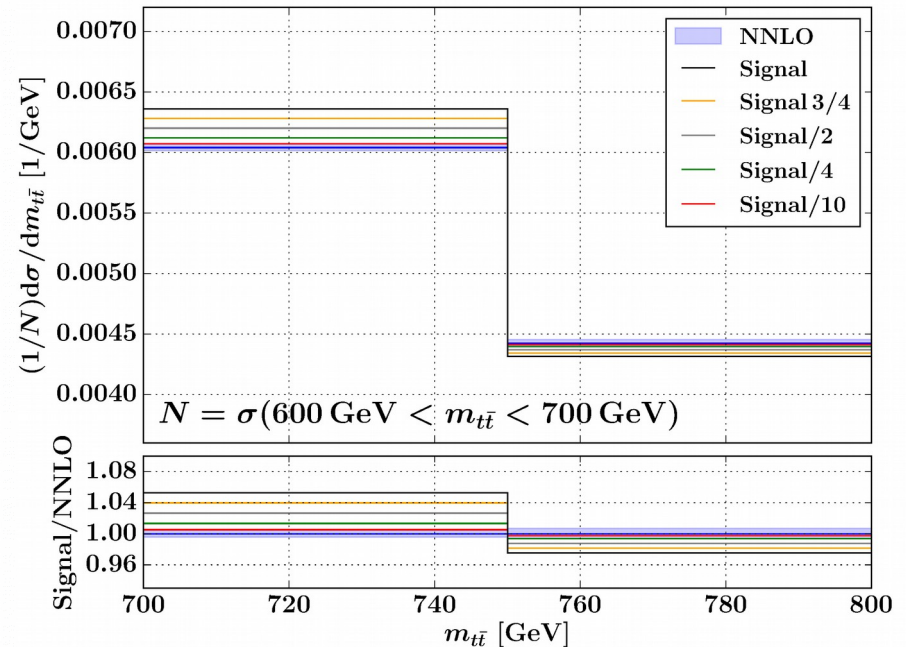
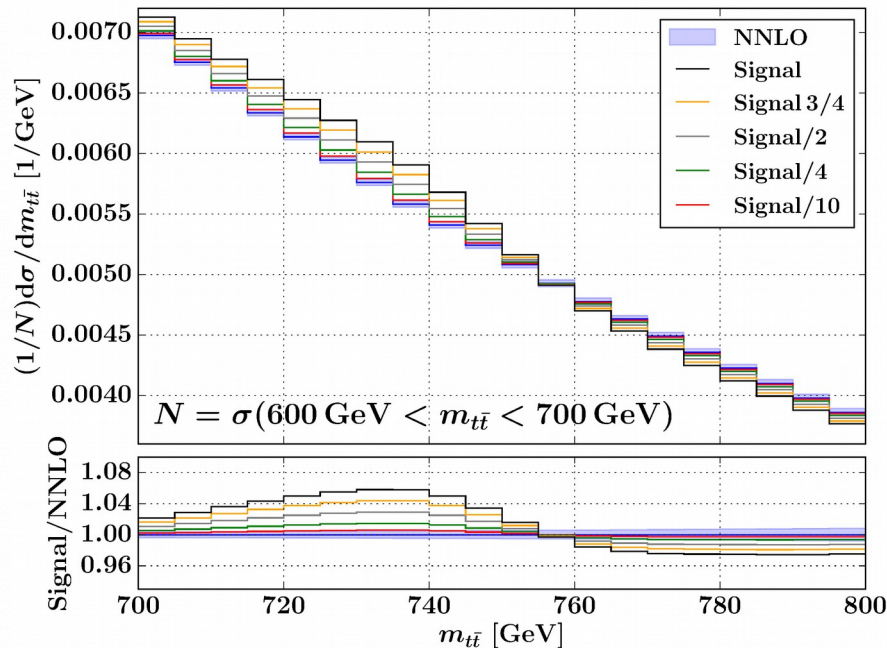
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Czakon, DH, Mitov 2016



Signal from: Hespel, Maltoni, Vryonidou 2016

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Conclusion

NNLO QCD

- High precision predictions \leftrightarrow fixed order results for top-quark pair production at NNLO QCD
- Precision at high $p_T/m_{t\bar{t}}/y$ currently limited by pdf uncertainty
- Use NNLO $t\bar{t}$ predictions to constrain PDF sets using LHC data
- FastNLO tables in preparation *Britzger, Rabbertz, Stober, Wobisch: fastNLO*

Combined NNLO QCD + EW

- EW corrections could be sizeable at large p_T
 - Negative Sudakov contribution up to -20 % (but: inside QCD PDF uncertainty)
 - Photon induced contributions are small (LUXqed, future pdf sets: MMHT)
- EW corrections are generally small for other distribution
 - Use precision for new physics searches

Outlook

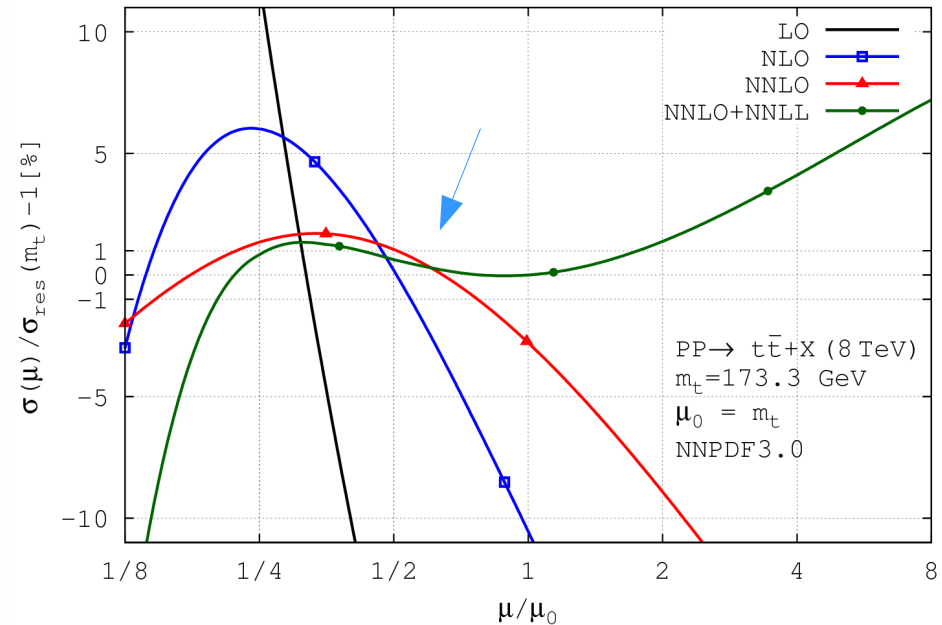
- Resummation effects
- Including top-decays in the NWA at NNLO in progress
- Top mass extraction using differential distributions at the LHC

*Brucherseifer, Caola, Melnikov 2013
Gao, Li, Zhu 2012*

Back Up

Scale dependance of the total cross section

- Look for convergence
 - Scale value which minimizes difference
 - $\text{NLO} \rightarrow \text{NNLO} \rightarrow (\text{NNLO} + \text{NNLL})$
 - Best convergence: $\mu_0 < m_{\text{top}}$
 - Little dependence on PDFset at NNLO



- Value of NNLO cross section at point of best convergence equals the NNLO+NNLL at the usual canonical scale $\mu_0 = m_{\text{top}}$
 - Therefore: Resummation has negligible impact on the total cross section at the point of fastest convergence

Czakon, DH, Mitov 2016