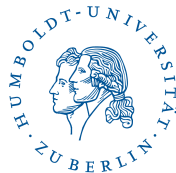


Future challenges for precision QCD

Exploring the top quark
electroweak interactions

Markus Schulze

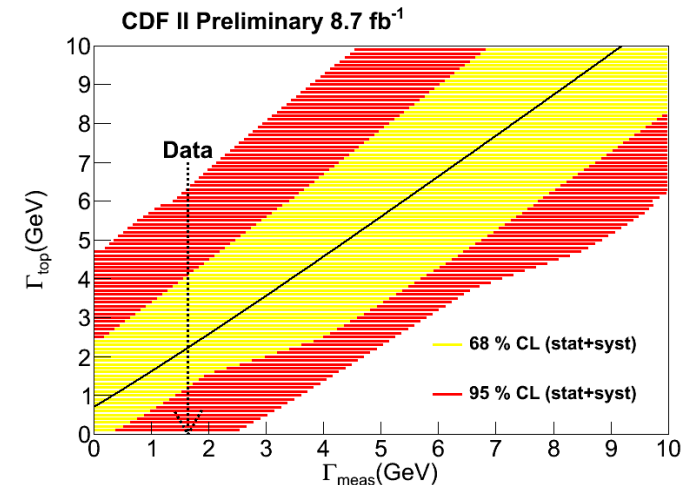
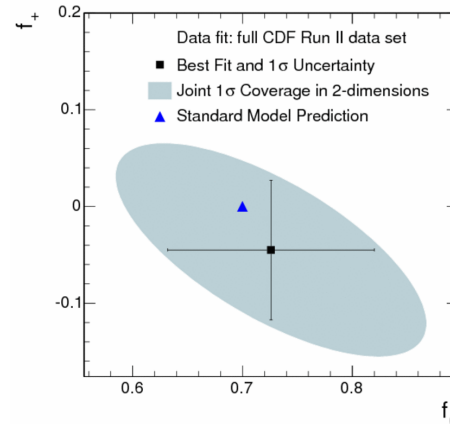
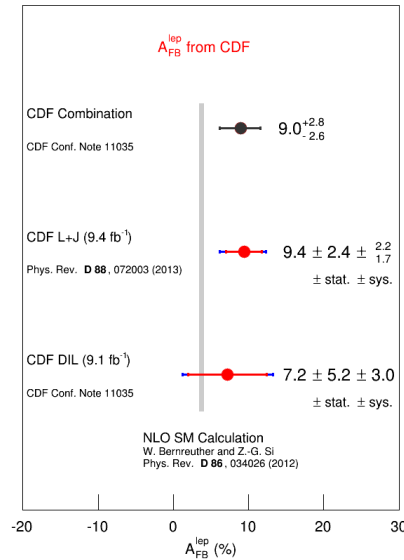
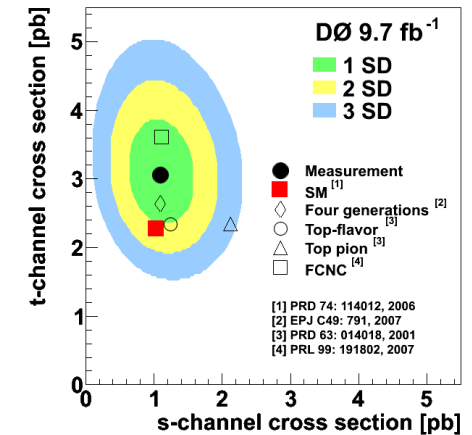
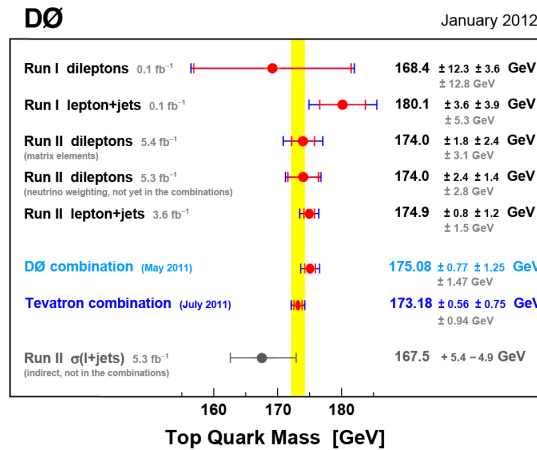
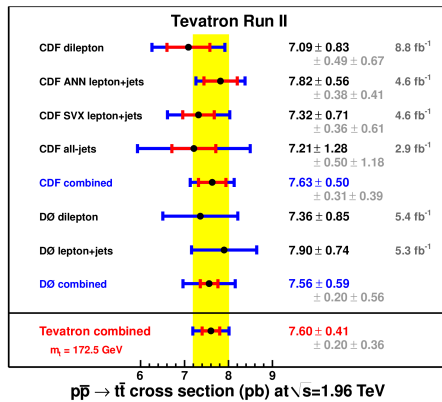
Humboldt-Universität zu Berlin



*work with R.Röntsch, Y.Soreq;
A.Gritsan, M.Xiao (CMS)*

The Tevatron Legacy

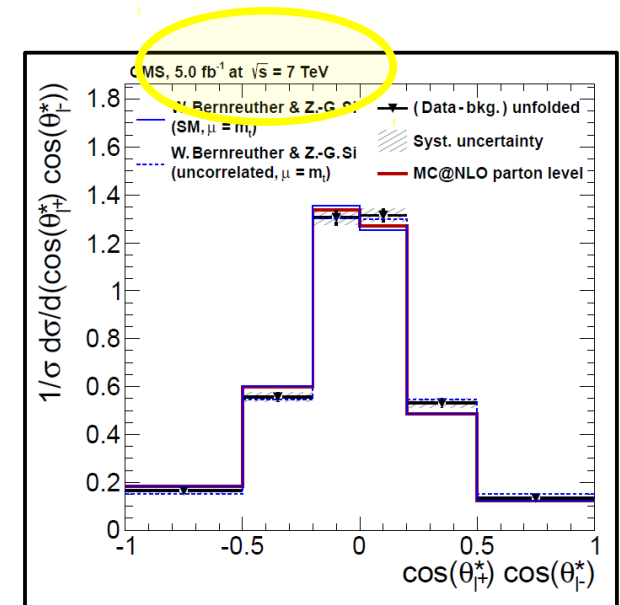
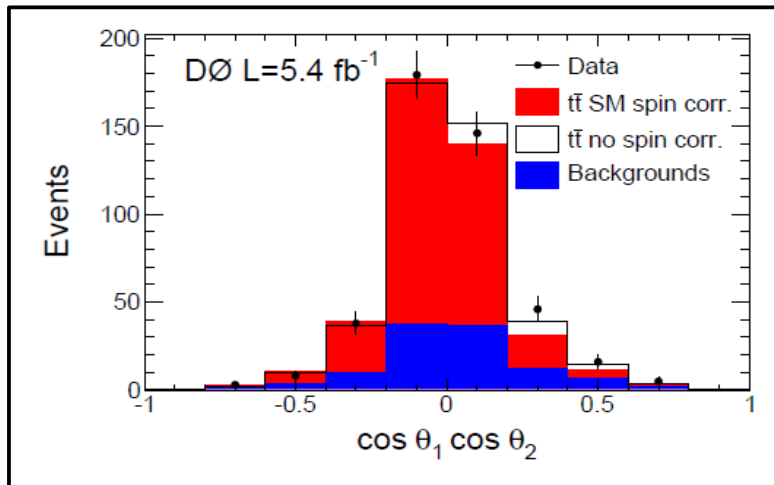
- Our understanding of the top quark as an elementary particle and its dynamics in QCD is very solid.
- Many of its properties were established at the Tevatron.



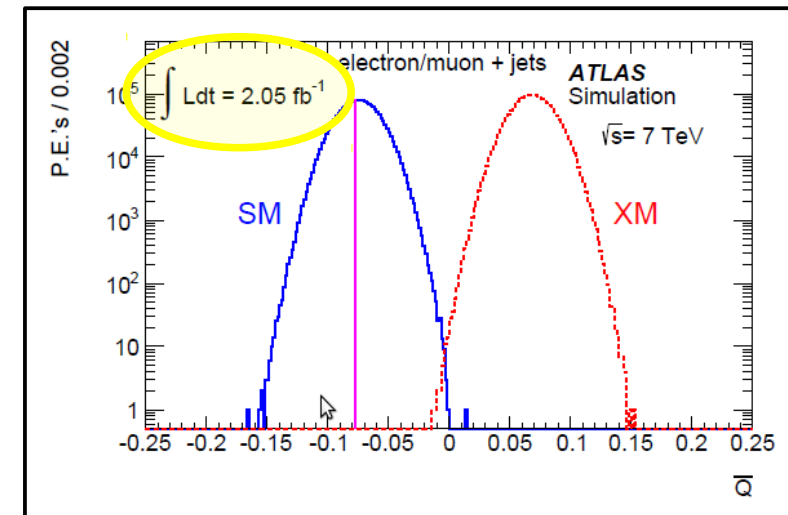
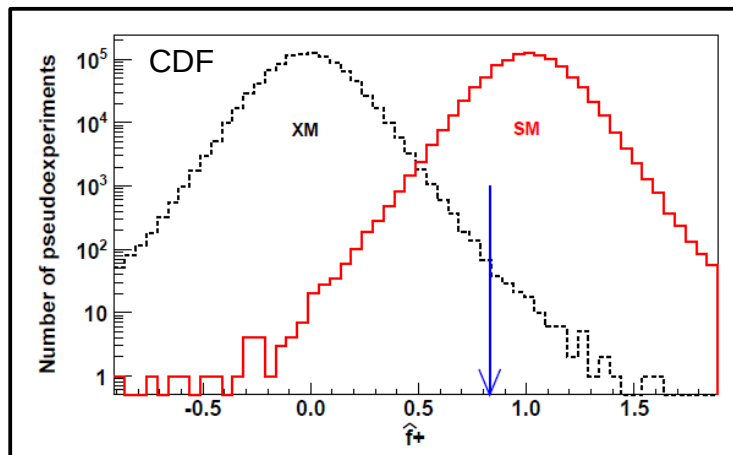
Early days of LHC experiments

- Results were confirmed and superseded by LHC experiments at impressive pace

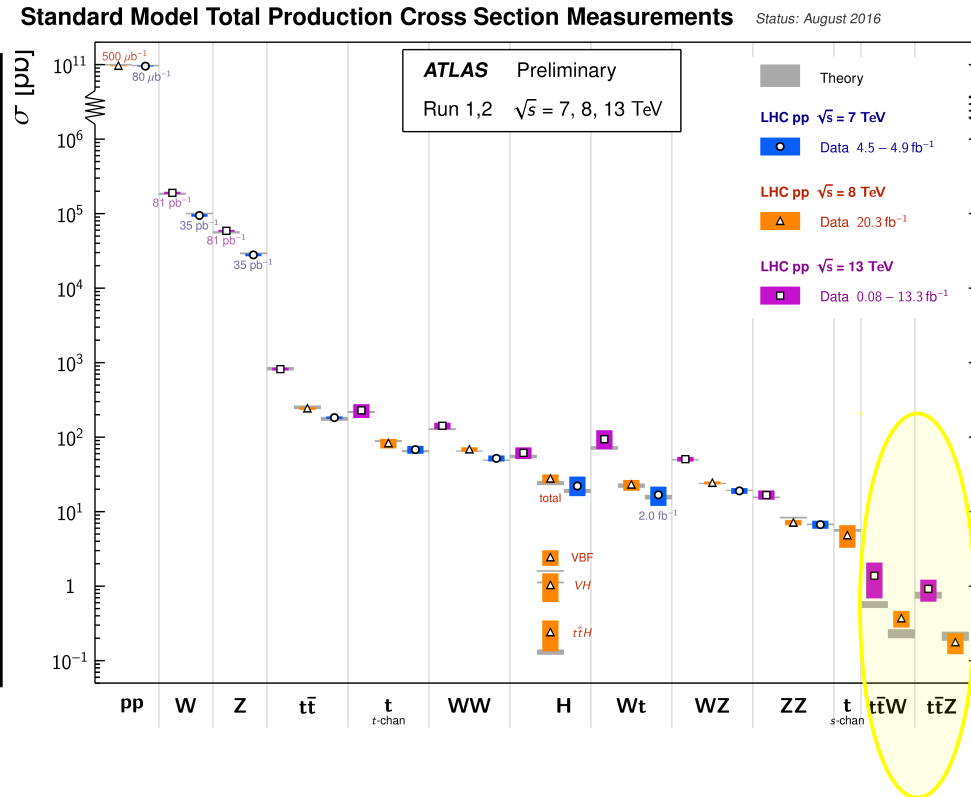
top spin-
correlations



top electric
charge



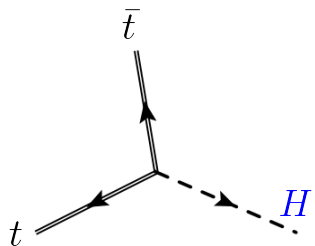
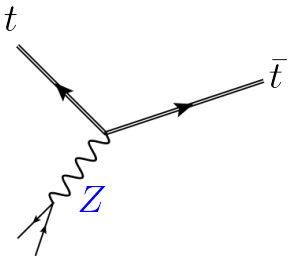
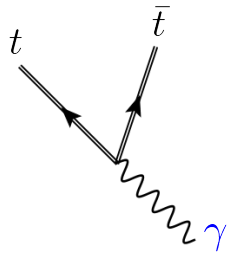
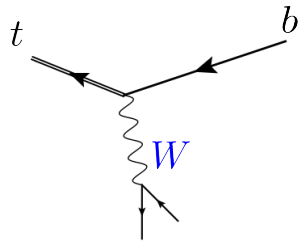
- The LHC is not only a *top quark factory*, but it is opening the door to a whole new process class: $t\bar{t} + \gamma, t\bar{t} + Z, t\bar{t} + W^\pm, t\bar{t} + H$ which was *never* observed at the Tevatron.



3 / 14

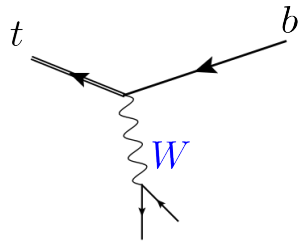
Top quark electroweak couplings

- $t\bar{t} + \gamma/Z/H$ yield *direct* sensitivity to anomalous couplings + dipole moments
- Largely unconstrained from hadron experiments. Indirect: LEP, B -factories

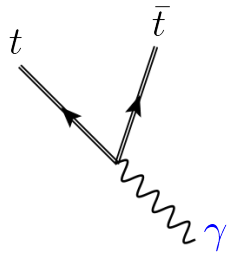


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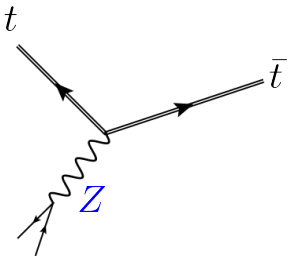
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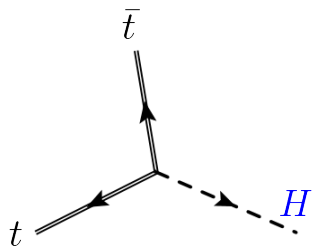
$$\mathcal{L}_{Wtb} = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^- + \text{H.c.}$$



$$\mathcal{L}_{\gamma tt} = -e Q_t \bar{t} \gamma^\mu t A_\mu - e \bar{t} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (d_V^\gamma + i d_A^\gamma \gamma_5) t A_\mu.$$



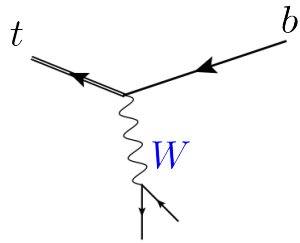
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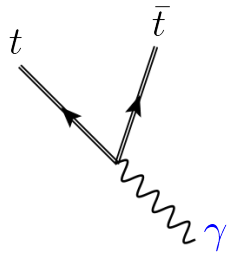
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Top quark electroweak couplings

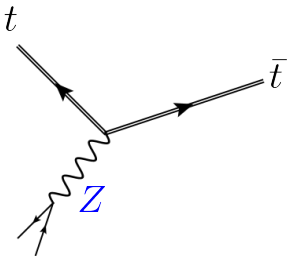
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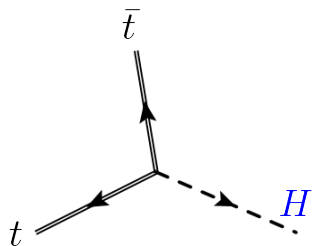
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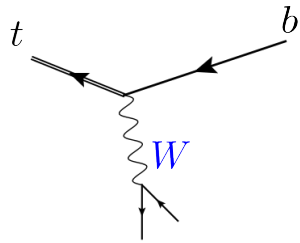
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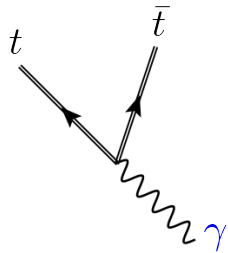
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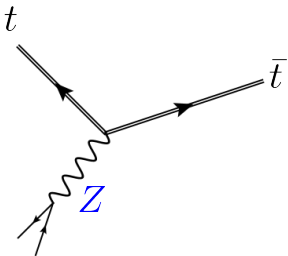
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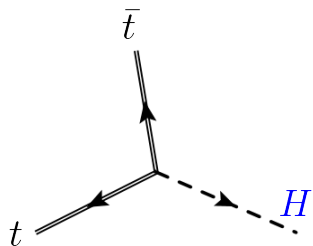
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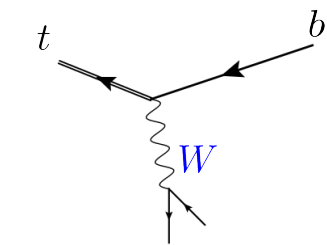
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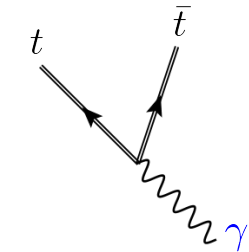
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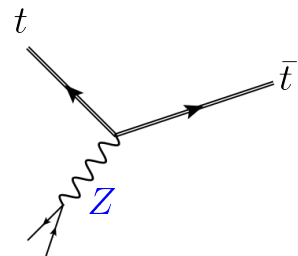
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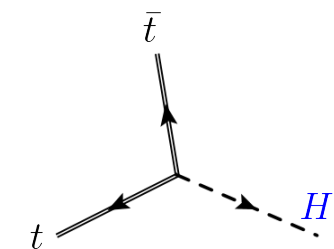
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Top dipole moments

Top dipole moments

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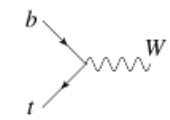
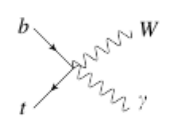
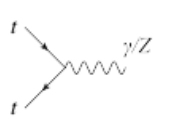
Eur.Phys.J. C76 (2016), 466; arXiv: 1603.08911

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C_{uW}^{33}	\otimes	\otimes	\otimes
C_{dW}^{33}	\otimes	\otimes	
$C_{uB\phi}^{33}$			\otimes

$$g_L^{W^-} = g_R^{W^{+*}} = -\frac{e m_t}{s_W M_W} \frac{v^2}{\Lambda^2} C_{dW}^{33*},$$

$$g_R^{W^-} = g_L^{W^{+*}} = -\frac{e m_t}{s_W M_W} \frac{v^2}{\Lambda^2} C_{uW}^{33},$$

$$g_L^\gamma = g_R^{\gamma*} = -\frac{\sqrt{2} m_t v}{\Lambda^2} (c_W C_{uB\phi}^{33*} + s_W C_{uW}^{33*}),$$

$$g_L^Z = g_R^{Z*} = -\frac{e m_t v^2}{\sqrt{2} s_W c_W M_Z \Lambda^2} (c_W C_{uW}^{33*} - s_W C_{uB\phi}^{33*}),$$

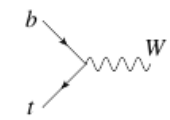
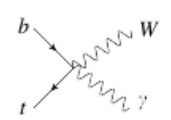
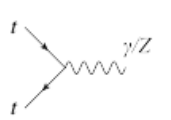
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→ Construct **ratios of cross sections** to cancel uncertainties and enhance sensitivity:

$$\mathcal{R}_\gamma = \frac{\sigma_{t\bar{t}\gamma}}{\sigma_{t\bar{t}}}, \quad \mathcal{R}_Z = \frac{\sigma_{t\bar{t}Z}}{\sigma_{t\bar{t}}}$$

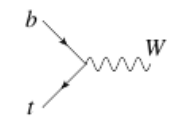
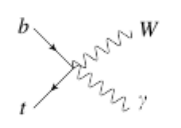
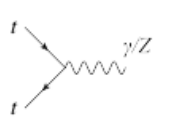
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$\langle E_{\text{CMS}} \rangle \approx 525 \text{ GeV}$ → \mathcal{R}_γ
 $\langle E_{\text{CMS}} \rangle \approx 630 \text{ GeV}$ → \mathcal{R}_Z
 $\langle E_{\text{CMS}} \rangle \approx 860 \text{ GeV}$ → \mathcal{R}_Z

Top dipole moments

$$\mathcal{R}_\gamma = \frac{\sigma_{t\bar{t}\gamma}}{\sigma_{t\bar{t}}}, \quad \mathcal{R}_Z = \frac{\sigma_{t\bar{t}Z}}{\sigma_{t\bar{t}}}$$

Properly cancel q^2 -dependent uncertainties (pdfs, α_s):

enhance $\sigma_{t\bar{t}}$ threshold: $m_{t\bar{t}} \geq 470 \text{ GeV}$ in \mathcal{R}_γ , $m_{t\bar{t}} \geq 700 \text{ GeV}$ in \mathcal{R}_Z .

Top dipole moments

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$$\mathcal{R}_\gamma^{\text{LO}} \times 10^{-3} = \begin{cases} 11.5 & \text{with NNPDF3.0,} \\ 11.4 & \text{with CTEQ6L1,} \\ 11.5 & \text{with MSTW08,} \end{cases}$$

$$\mathcal{R}_Z^{\text{LO}} \times 10^{-4} = \begin{cases} 2.29 & \text{with NNPDF3.0,} \\ 2.27 & \text{with CTEQ6L1,} \\ 2.27 & \text{with MSTW08.} \end{cases}$$

$$\mathcal{R}_\gamma^{\text{SM}} \times 10^{-3} = \begin{cases} 11.4_{+0.7\%}^{-0.7\%} & \text{at LO,} \\ 12.6_{-1.8\%}^{+3.1\%} & \text{at NLO QCD,} \end{cases}$$

$$\mathcal{R}_Z^{\text{SM}} \times 10^{-4} = \begin{cases} 2.27_{+2.0\%}^{-1.7\%} & \text{at LO,} \\ 1.99_{+2.8\%}^{-1.9\%} & \text{at NLO QCD,} \end{cases}$$

→ *pdf variation*:

ratio: **$\pm 1\%$**

cross sections: **$\pm 10\%$**

→ *scale variation (NLO)*:

ratio: **$\pm 2\text{-}3\%$**

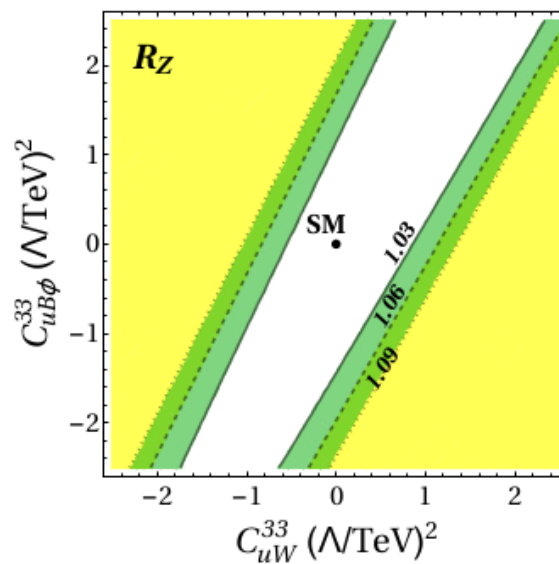
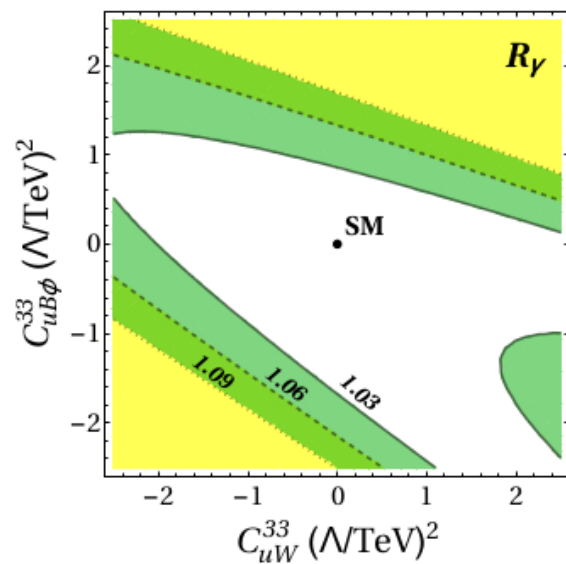
cross sections: **$\pm 20\%$**

In the following we assume a theoretical uncertainty of **$\pm 3\%$** .

First measurement by CMS: $\mathcal{R}_\gamma(8 \text{ TeV}) = 10.7 \times 10^{-3} \pm 6.5\%(\text{stat.}) \pm 25\%(\text{syst.})$

stat.: sub-dominant after 250 fb^{-1} , syst.: $\pm 23\%$ from backgr. modeling

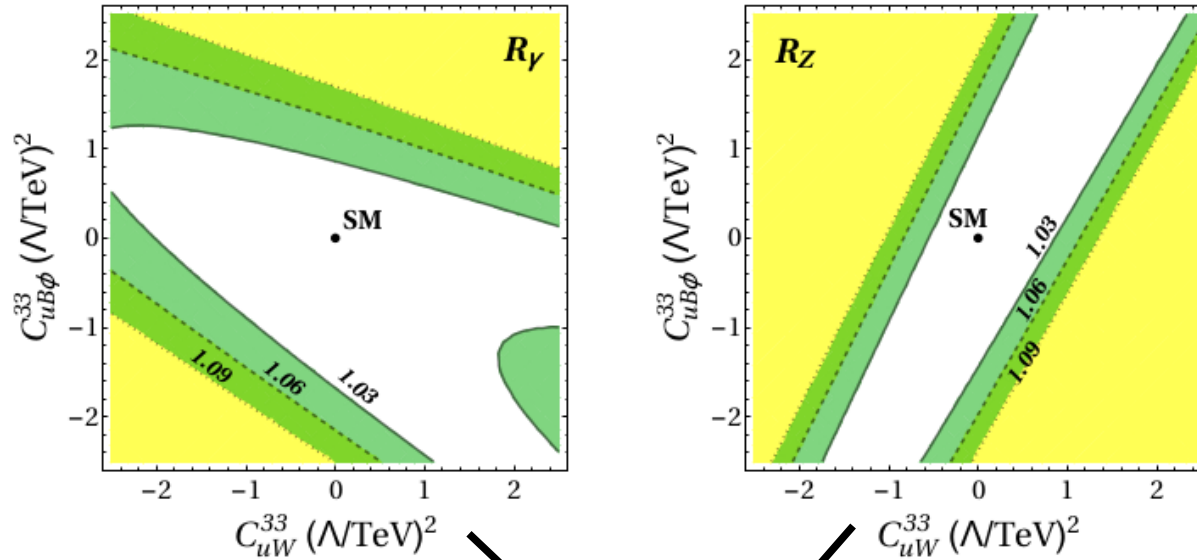
Top dipole moments



$$g_L^\gamma = g_R^{\gamma*} = -\frac{\sqrt{2} m_t v}{\Lambda^2} (c_W C_{uB\phi}^{33*} + s_W C_{uW}^{33*}),$$

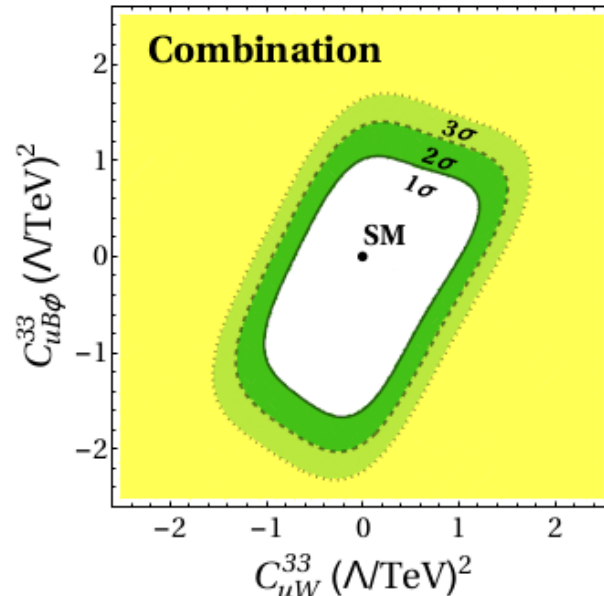
$$g_L^Z = g_R^{Z*} = -\frac{e m_t v^2}{\sqrt{2} s_W c_W M_Z \Lambda^2} (c_W C_{uW}^{33*} - s_W C_{uB\phi}^{33*}),$$

Top dipole moments



$$g_L^\gamma = g_R^{\gamma*} = -\frac{\sqrt{2} m_t v}{\Lambda^2} (c_W C_{uB\phi}^{33*} + s_W C_{uW}^{33*}),$$

$$g_L^Z = g_R^{Z*} = -\frac{e m_t v^2}{\sqrt{2} s_W c_W M_Z \Lambda^2} (c_W C_{uW}^{33*} - s_W C_{uB\phi}^{33*}),$$



$$C_{uW}^{33} = [-1.2, +1.4] (\Lambda/\text{TeV})^2$$

$$C_{uB\phi}^{33} = [-1.9, +1.2] (\Lambda/\text{TeV})^2$$

→ additional analysis of decay angles in $t\bar{t}$ to constrain remaining operator

Top-Z vector/axial couplings

Top-Z vector/axial couplings

“Constraining couplings of the top quark to the Z boson

in $t\bar{t}b+Z$ production at the LHC”

[R.Röntsch, M.S.]

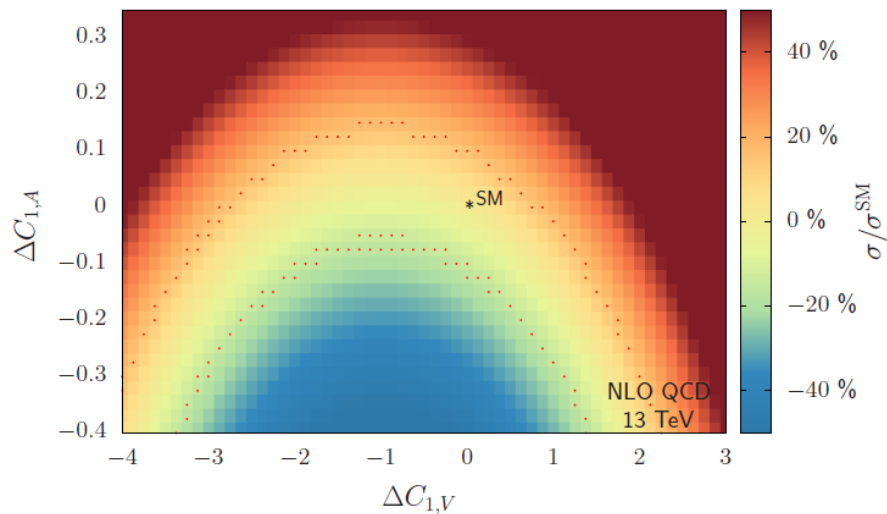
JHEP 1508(2015) 044; arXiv: 1501.05939

$$\mathcal{L}_{t\bar{t}Z} = ie\bar{u}(p_t) \left[\gamma^\mu (C_{1,V} + \gamma_5 C_{1,A}) + \frac{i\sigma_{\mu\nu} q_\nu}{M_Z} (C_{2,V} + i\gamma_5 C_{2,A}) \right] v(p_{\bar{t}}) Z_\mu,$$

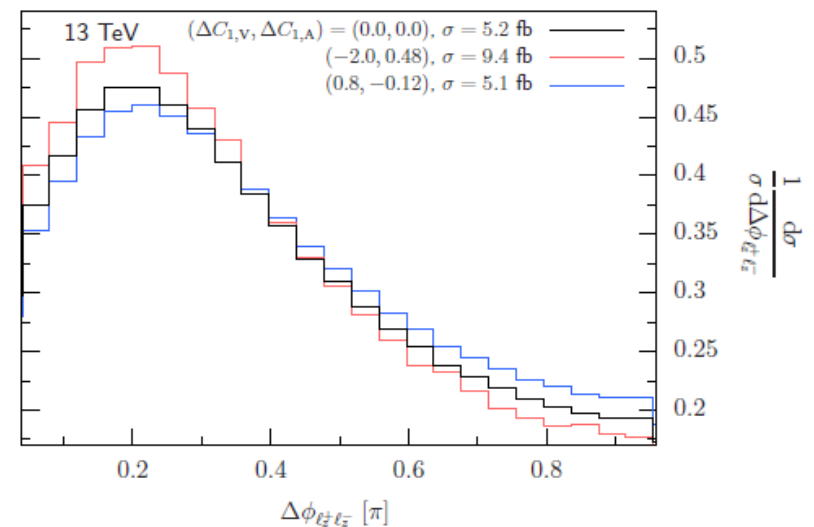
$$C_{1,V} = C_{1,V}^{\text{SM}} + \left(\frac{v^2}{\Lambda^2} \right) \text{Re} \left[C_{\phi q}^{(3,33)} - C_{\phi q}^{(1,33)} - C_{\phi u}^{33} \right],$$

$$C_{1,A} = C_{1,A}^{\text{SM}} + \left(\frac{v^2}{\Lambda^2} \right) \text{Re} \left[C_{\phi q}^{(3,33)} - C_{\phi q}^{(1,33)} + C_{\phi u}^{33} \right],$$

Degeneracy: cross section dominantly $\sim C_{1,V}^2 + C_{1,A}^2$



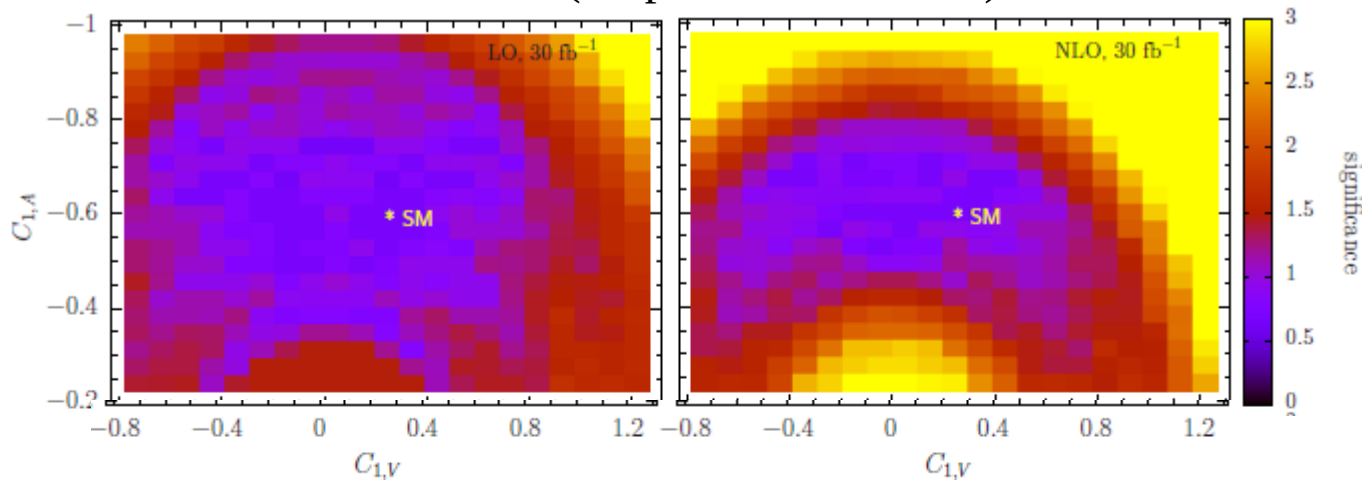
Differential observables resolve degeneracies



Top-Z vector/axial couplings

LHC 13 TeV (shape+normalization)

LO 30 fb⁻¹

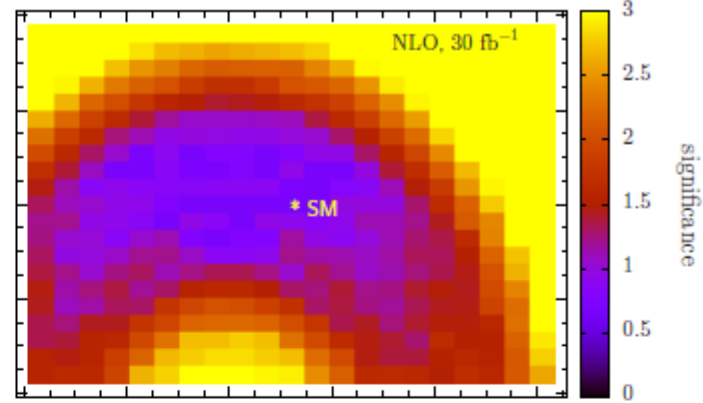
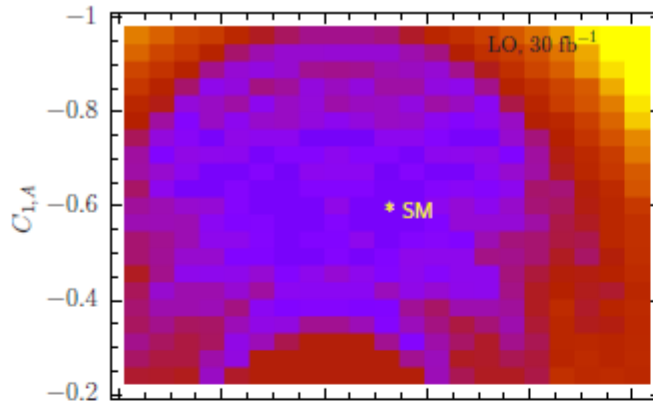


NLO 30 fb⁻¹

Top-Z vector/axial couplings

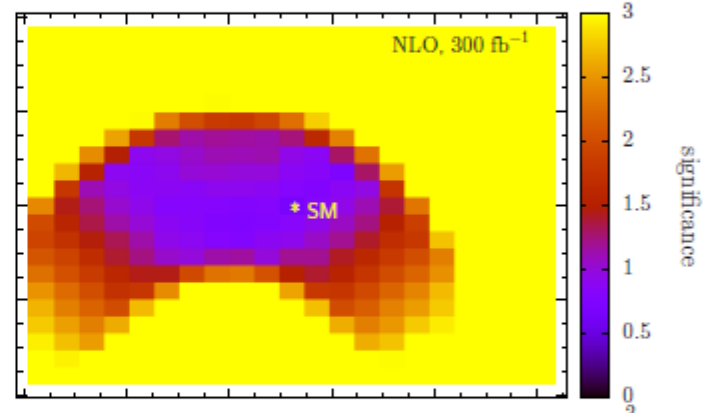
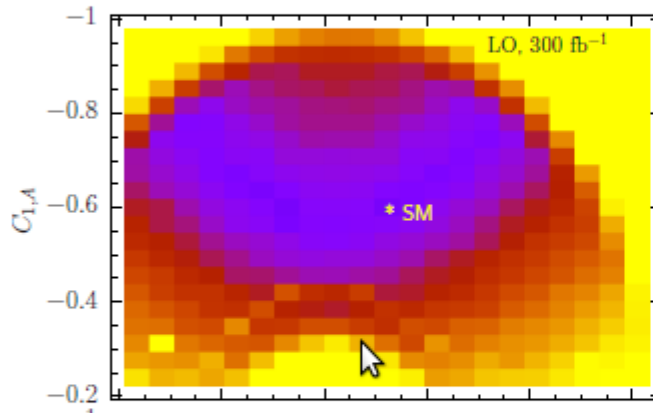
LHC 13 TeV (shape+normalization)

LO 30 fb⁻¹



NLO 30 fb⁻¹

LO 300 fb⁻¹

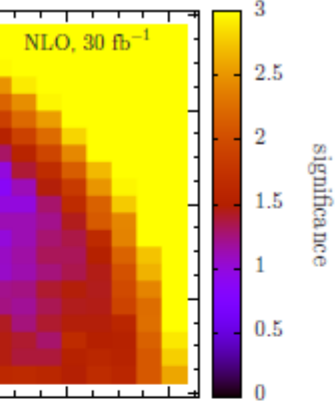
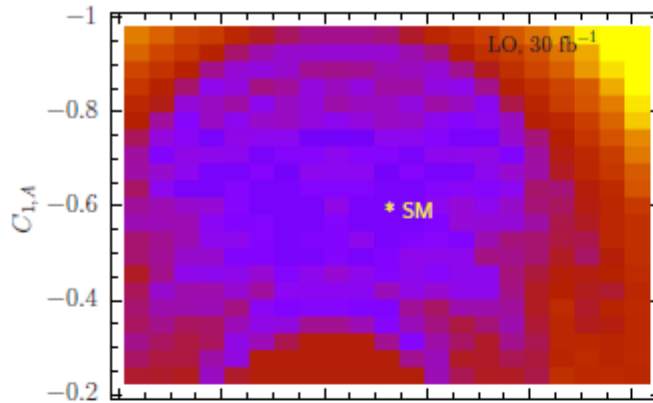


NLO 300 fb⁻¹

Top-Z vector/axial couplings

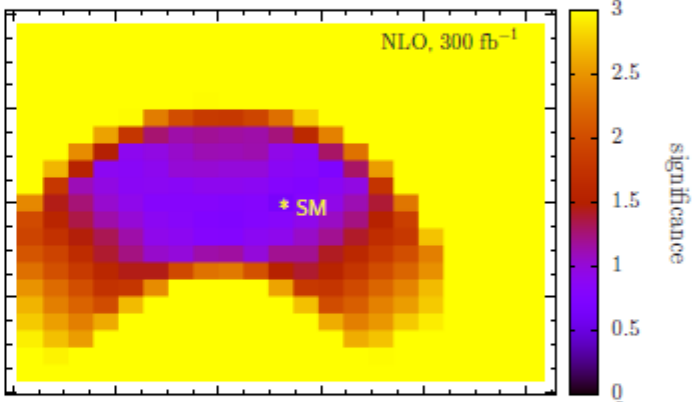
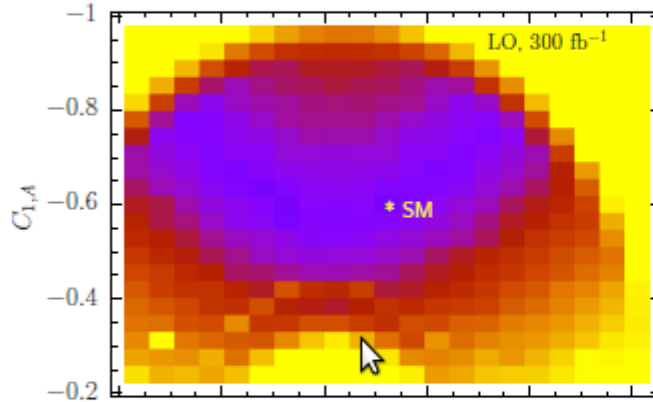
LHC 13 TeV (shape+normalization)

LO 30 fb⁻¹



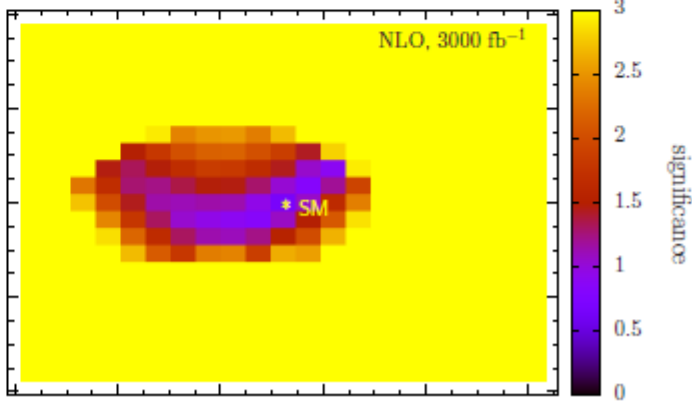
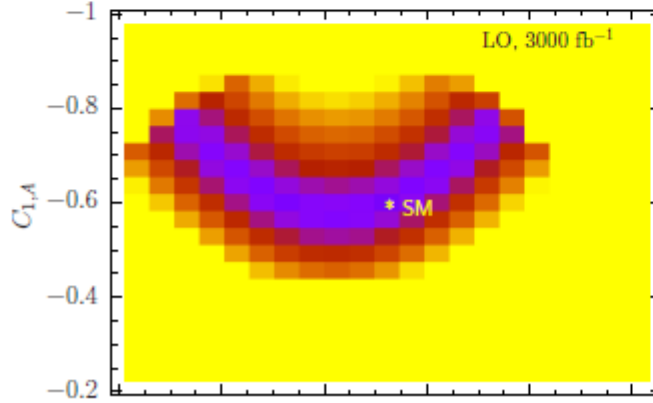
NLO 30 fb⁻¹

LO 300 fb⁻¹



NLO 300 fb⁻¹

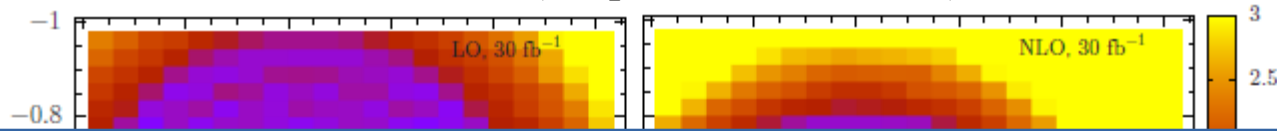
LO 3000 fb⁻¹



NLO 3000 fb⁻¹

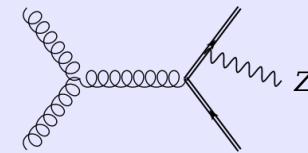
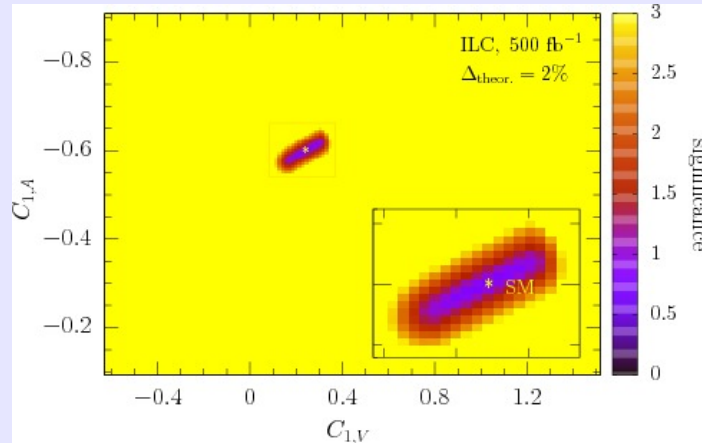
Top-Z vector/axial couplings

LHC 13 TeV (shape+normalization)

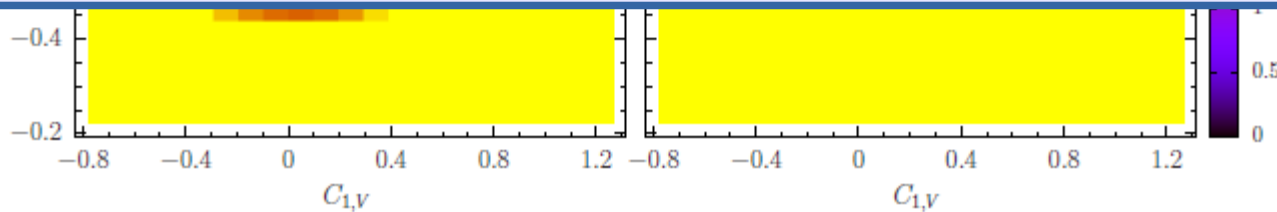
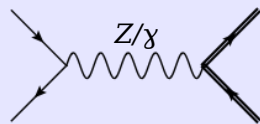
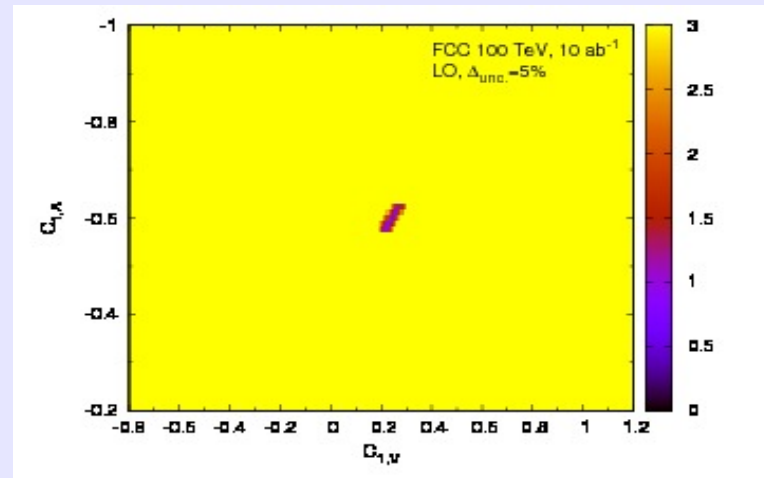


Future collider bounds

ILC 500 GeV

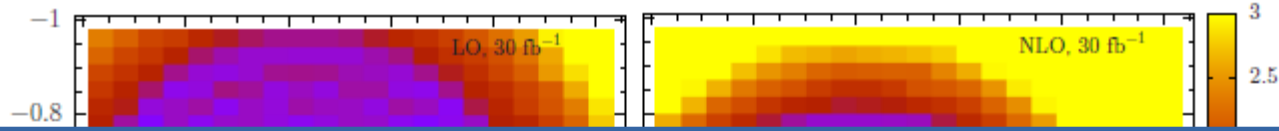


FCC 100 TeV



Top-Z vector/axial couplings

LHC 13 TeV (shape+normalization)

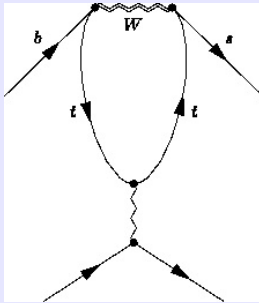


LO 30 fb⁻¹

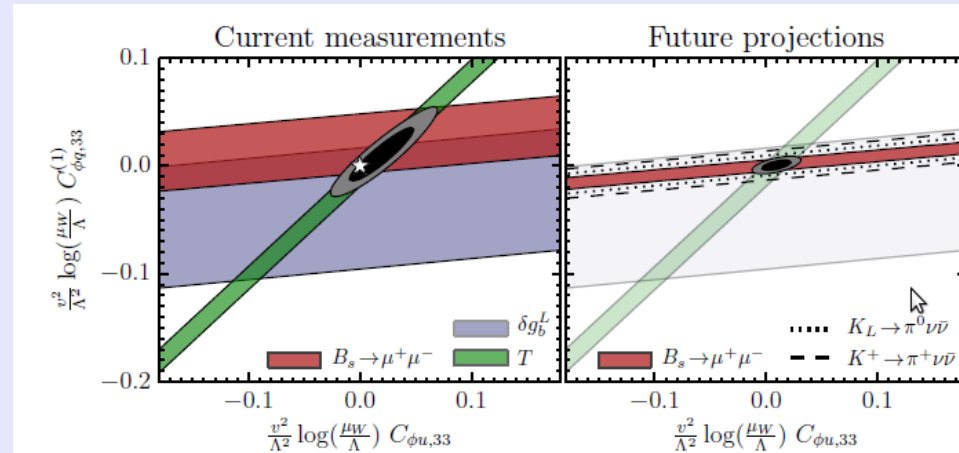
LO 30 fb⁻¹

Future collider bounds

[Brod,Greljo,Stamou,Uttayarath]



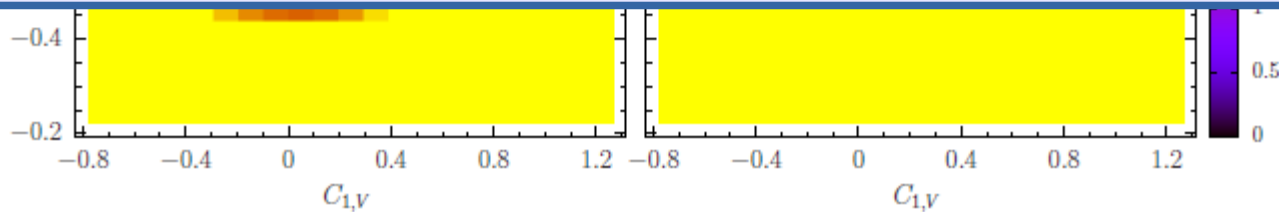
LO 300 fb⁻¹



Order of magnitude stronger bounds than direct reach with 3000/fb!

T	0.08 ± 0.07	[Ciuchini et al., arxiv:1306.4644]
δg_L^b	0.0016 ± 0.0015	[Ciuchini et al., arxiv:1306.4644]
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ [CMS]	$(3.0^{+1.0}_{-0.9}) \times 10^{-9}$	[CMS, arxiv:1307.5025]
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ [LHCb]	$(2.9^{+1.1}_{-1.0}) \times 10^{-9}$	[LHCb, arxiv:1307.5024]
$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$(1.73^{+1.15}_{-1.05}) \times 10^{-10}$	[E949, arxiv:0808.2459]

LO 3000 fb⁻¹



Top-Higgs interactions

Top-Higgs interactions

“Constraining anomalous Higgs boson couplings to the heavy flavor fermions using matrix element techniques”

[Gritsan,Röntschi,Xiao,M.S.]

Phys.Rev. D94 (2016) 055023

arXiv:1606.03107

$$\mathcal{L}(H f \bar{f}) = -\frac{m_f}{v} \bar{\psi}_f (\kappa_f + i\tilde{\kappa}_f \gamma_5) \psi_f H,$$

$$f_{\text{CP}} = \frac{|\tilde{\kappa}_f|^2}{|\kappa_f|^2 + |\tilde{\kappa}_f|^2}, \quad \phi_{\text{CP}} = \arg(\tilde{\kappa}_f / \kappa_f)$$

Top-Higgs interactions

“Constraining anomalous Higgs boson couplings to the heavy flavor fermions using matrix element techniques”

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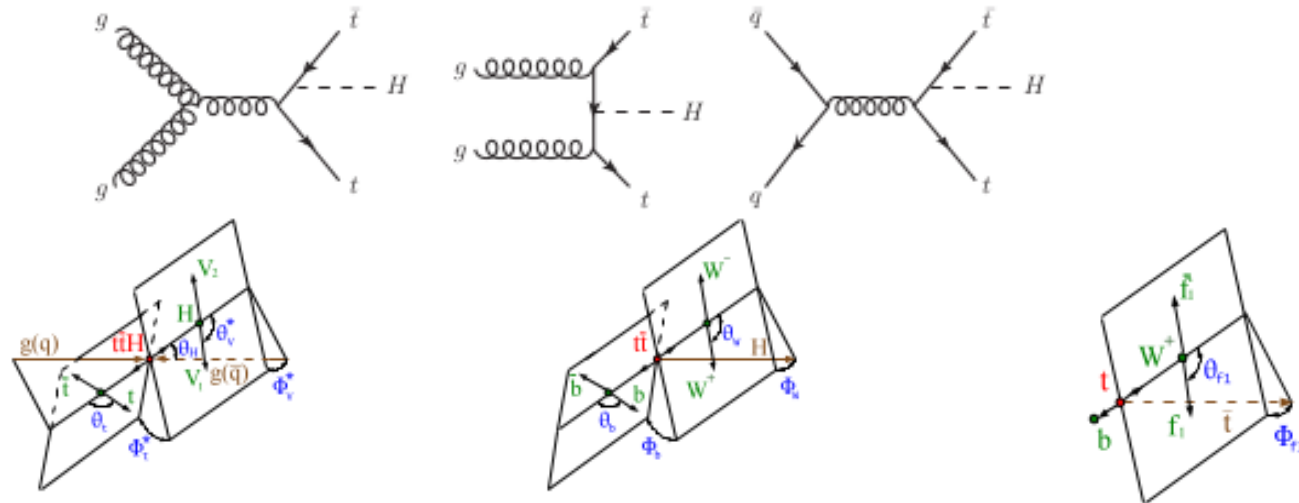
Phys.Rev. D94 (2016) 055023

arXiv:1606.03107

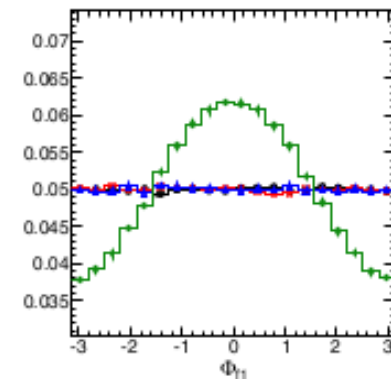
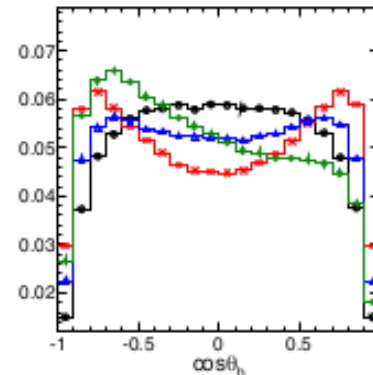
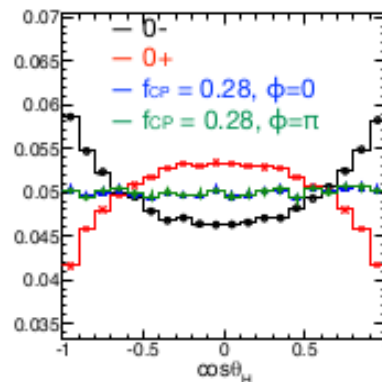
$$\mathcal{L}(H f \bar{f}) = -\frac{m_f}{v} \bar{\psi}_f (\kappa_f + i \tilde{\kappa}_f \gamma_5) \psi_f H,$$

$$f_{\text{CP}} = \frac{|\tilde{\kappa}_f|^2}{|\kappa_f|^2 + |\tilde{\kappa}_f|^2}, \quad \phi_{\text{CP}} = \arg(\tilde{\kappa}_f / \kappa_f)$$

$pp \rightarrow t\bar{t} + H$:



Fully describe the system through angles, decay planes, inv. masses:



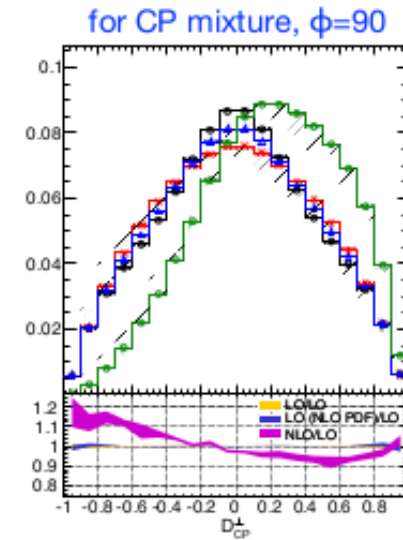
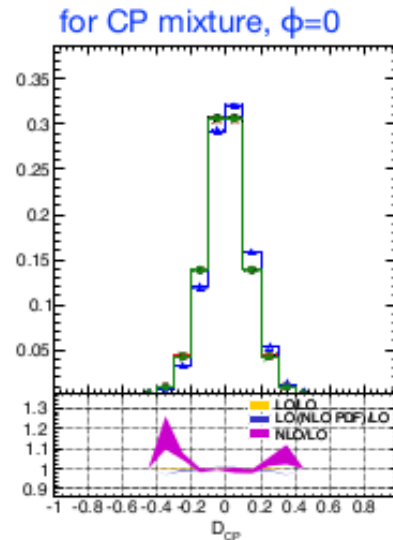
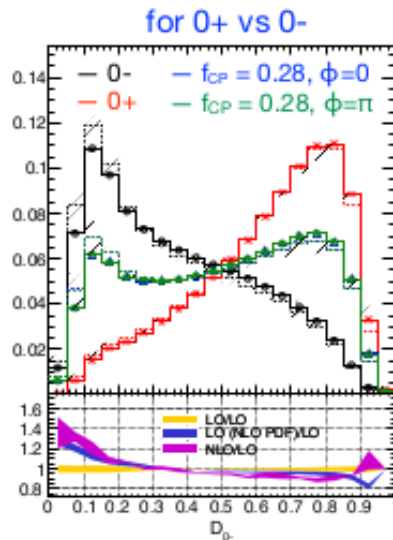
Top-Higgs interactions

MELA: Use matrix element likelihood analysis to gain optimal sensitivity.

Input: 4-momenta of $t\bar{t}H$ system in its rest frame.

$$\mathcal{P}(\{p\}_{t\bar{t}H}) = \frac{1}{2\hat{s}} \int dx_1 dx_2 f_i(x_1) f_2(x_2) |\mathcal{M}_{t\bar{t}H}|^2$$

$$\mathcal{D}_{0-} = \frac{\mathcal{P}_{0+}}{\mathcal{P}_{0+} + \mathcal{P}_{0-}}, \quad \mathcal{D}_{0-} = \frac{\mathcal{P}_{\text{int}}}{\mathcal{P}_{0+} + \mathcal{P}_{0-}}, \quad \mathcal{D}_{0-} = \frac{\mathcal{P}_{\text{int}}^{\perp}}{\mathcal{P}_{0+} + \mathcal{P}_{0-}}$$

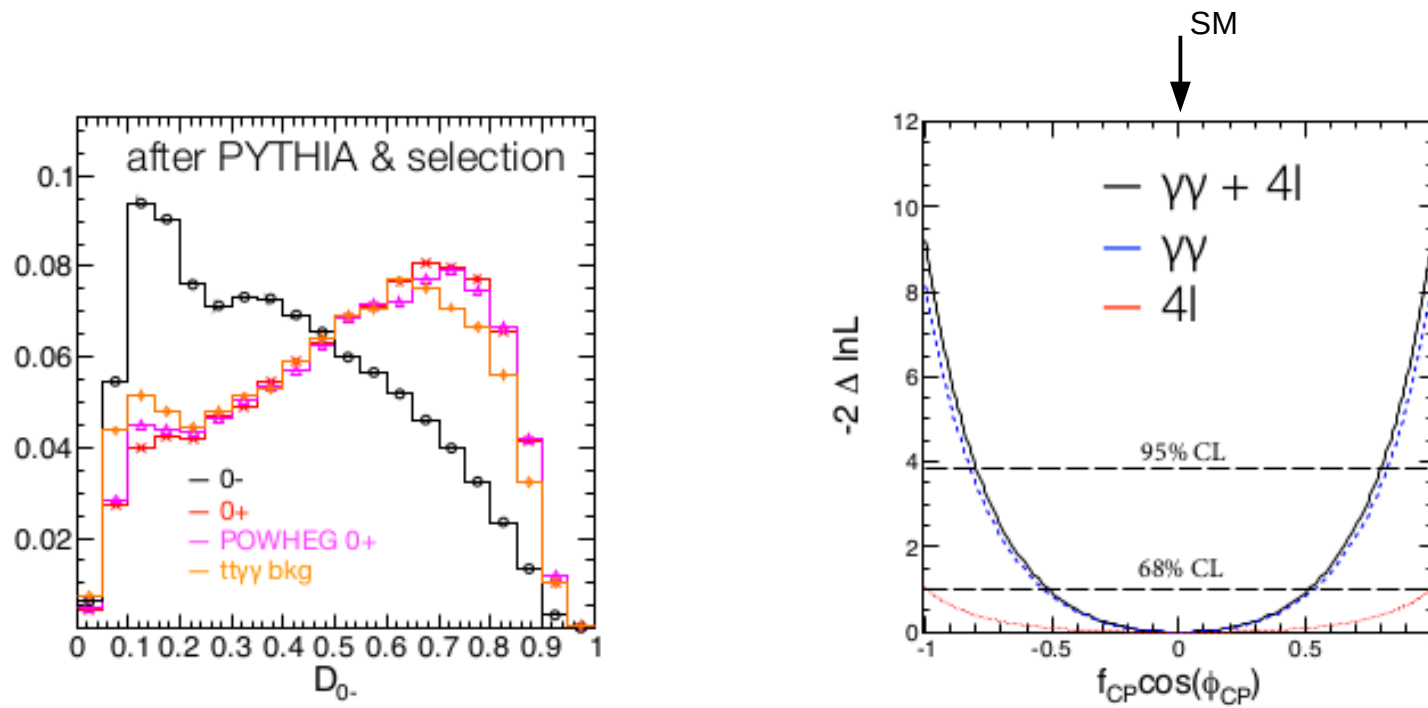


Study robustness of MELA (LO ME) with events at NLO QCD.

→ Discrimination power almost unaltered by virtual corrections and additional jet emissions.

Top-Higgs interactions

Realistic simulation of $H \rightarrow 4l$ and $H \rightarrow \gamma\gamma$, including backgrounds for 300 fb⁻¹:

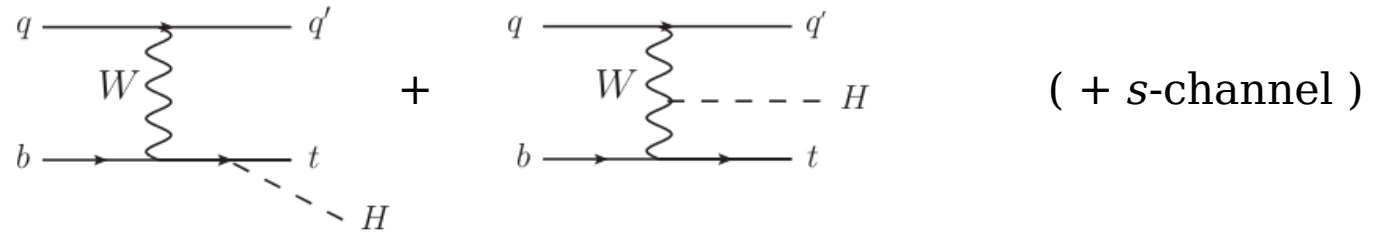


→ pure CP-odd Higgs can be excluded at 99.5% C.L.

50% CP-odd admixture can be excluded at the 68% C.L.

Top-Higgs interactions

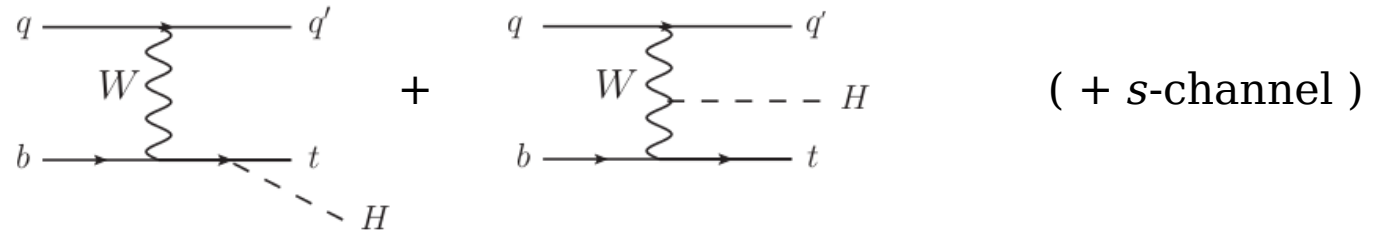
$pp \rightarrow t j + H$:



- Strong destr. interference between t - H and W - H diagrams
- Sensitive to the sign of the t - H coupling
- Simultaneous measurement of t - H and W - H possible

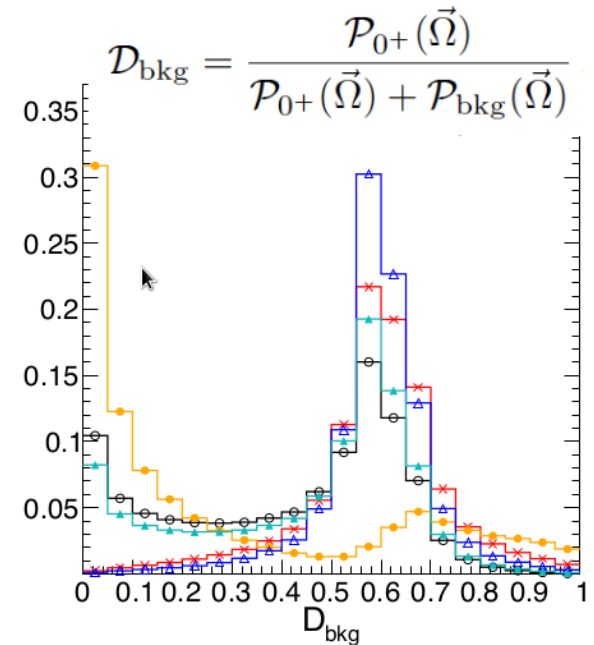
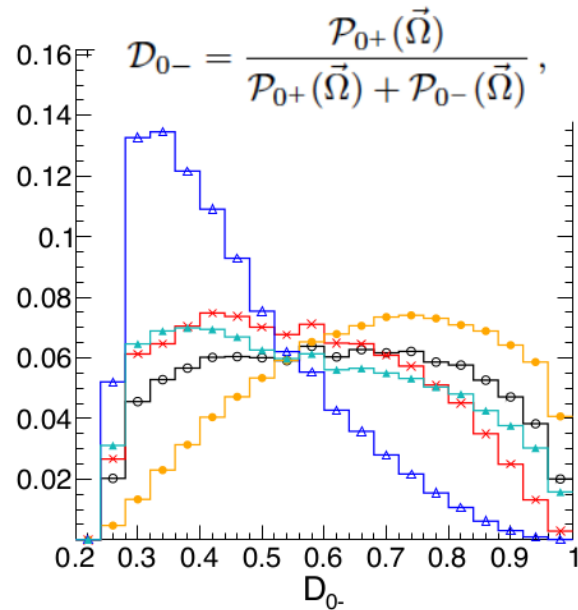
Top-Higgs interactions

$pp \rightarrow t j + H$:



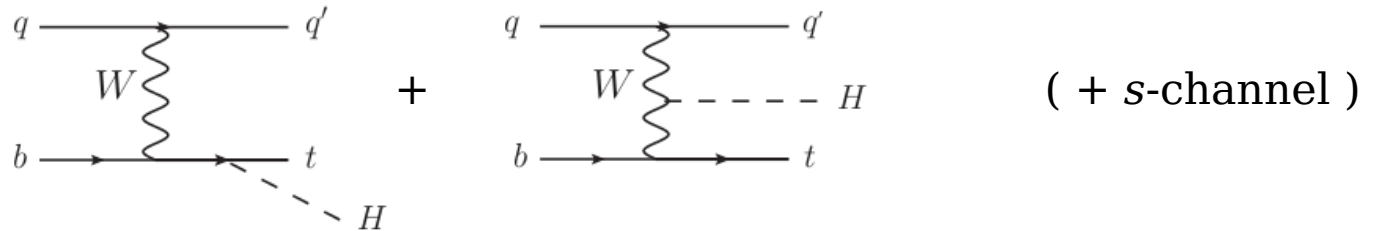
- Strong destr. interference between t - H and W - H diagrams
- Sensitive to the sign of the t - H coupling
- Simultaneous measurement of t - H and W - H possible

MELA discriminants:

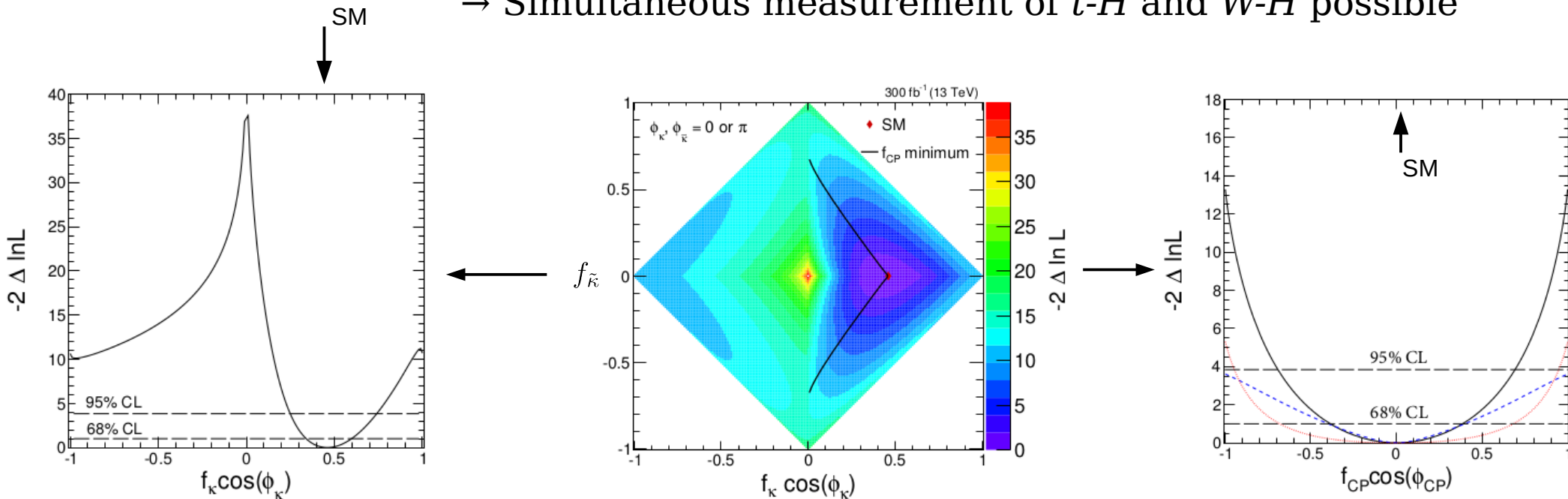


Top-Higgs interactions

$$pp \rightarrow t j + H:$$



- Strong destr. interference between t - H and W - H diagrams
- Sensitive to the sign of the t - H coupling
- Simultaneous measurement of t - H and W - H possible

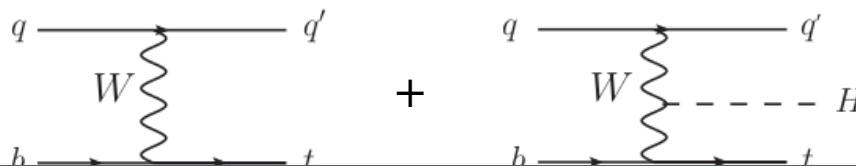


ttH is “background”, precision is driven by both $tt+H$ and $tj+H$.

99.5% C.L. exclusion of pure CP-odd and negative t - H coupling possible.

Top-Higgs interactions

$pp \rightarrow t j + H$:



(+ s-channel)

First 13 TeV constraints

[CMS PAS HIG-16-019]

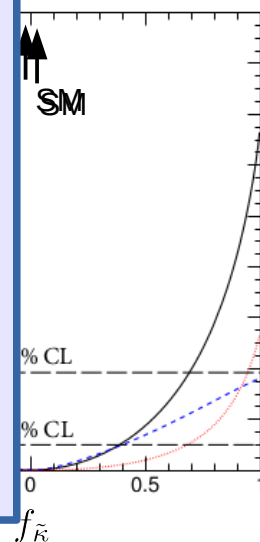
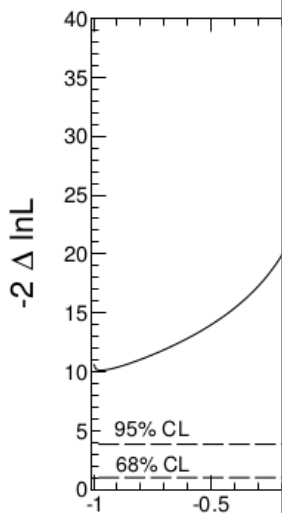
diagrams

ible

upper limit on
 $y_t = + y_{SM}$

upper limit on
 $y_t = - y_{SM}$

	Region	Observed Limit	Expected Limit		
			Median	$\pm 1\sigma$	$\pm 2\sigma$
SM scenario	3 tag	124.0	114.3	[73.6, 184.4]	[52.0, 295.2]
	4 tag	195.8	174.6	[112.9, 287.4]	[78.8, 464.4]
	Combination	113.7	98.6	[64.0, 159.2]	[45.3, 254.8]
ITC scenario	3 tag	7.4	7.4	[4.9, 11.6]	[3.5, 17.8]
	4 tag	9.2	10.0	[6.5, 16.3]	[4.5, 26.3]
	Combination	6.0	6.4	[4.2, 10.1]	[3.0, 15.7]



ttH is “background”, precision is driven by both $tt+H$ and $tj+H$.

99.5% C.L. exclusion of pure CP-odd and negative t - H coupling possible.

Summary

- For the first time, the LHC allows the study of $t\bar{t} + \gamma/Z/H$ final states which are *direct* probes of the top quark electroweak interactions.
- There is a rich interplay of anomalous terms between the associated top pair production processes and the top decay dynamics. + *B*-physics.
- NLO precision significantly improves the sensitivity to anomalous interactions. NLO QCD for production+decay dynamics is available for almost all processes.
- We studied a variety of approaches to boost sensitivity:
 - Cross section ratios
 - Differential analysis
 - Matrix element methods
 - $t\bar{t}$ vs. single top
- Towards the end of the 13 TeV run, these studies will fill empty gaps in our understanding of the top quark electroweak couplings and dipole moments, and provide a clear picture of the role tops in the electroweak model.

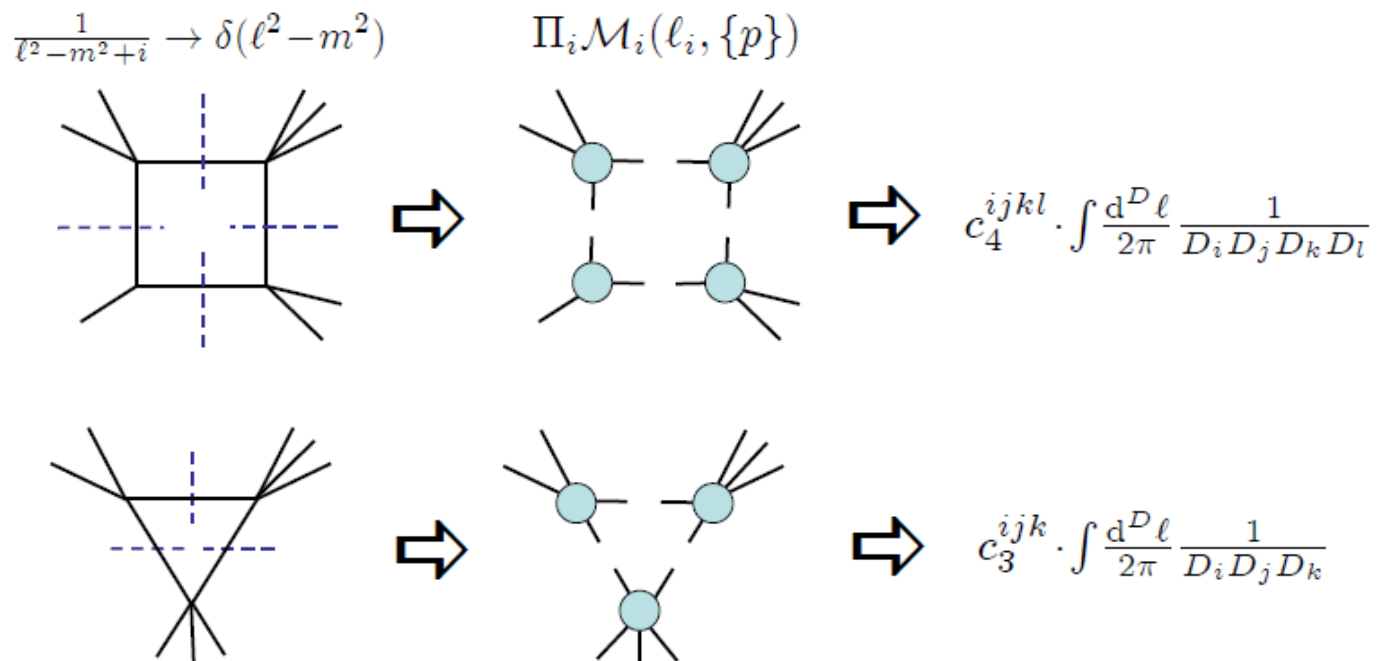
Extras

$$f_{\kappa} = \frac{\kappa^2 \sigma_{0+}^{tqH}}{(a_1^2 \sigma_{\text{bkg}}^{tqH} + \kappa^2 \sigma_{0+}^{tqH} + \tilde{\kappa}^2 \sigma_{0-}^{tqH})} , \quad \phi_{\kappa} = \arg(\kappa/a_1) = 0 \text{ or } \pi ,$$

$$f_{\tilde{\kappa}} = \frac{\tilde{\kappa}^2 \sigma_{0-}^{tqH}}{(a_1^2 \sigma_{\text{bkg}}^{tqH} + \kappa^2 \sigma_{0+}^{tqH} + \tilde{\kappa}^2 \sigma_{0-}^{tqH})} , \quad \phi_{\tilde{\kappa}} = \arg(\tilde{\kappa}/a_1) = 0 \text{ or } \pi .$$

Technology

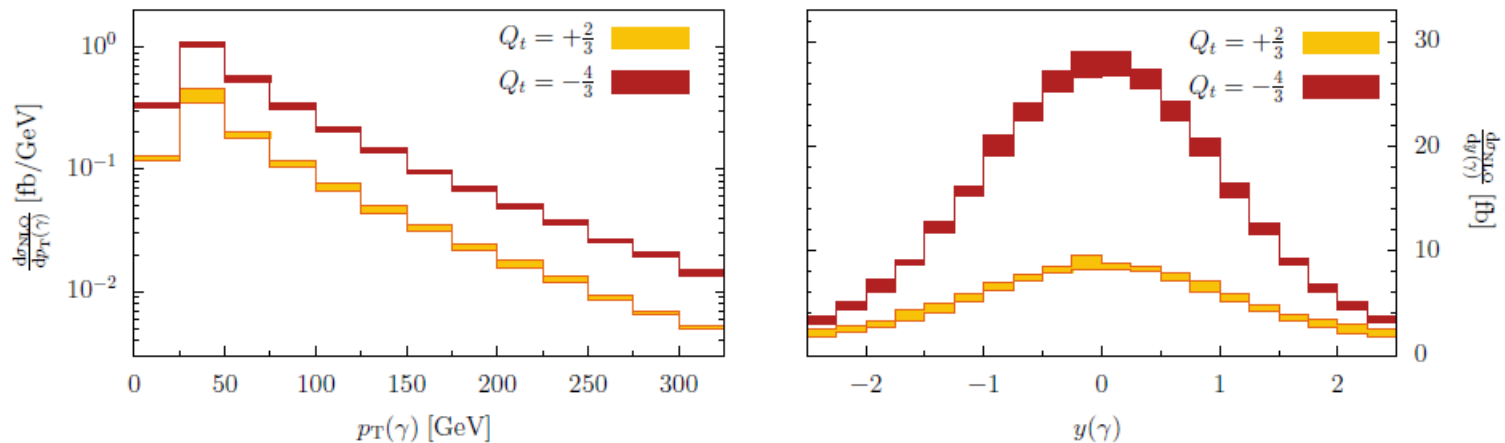
- Numerical OPP integrand reduction
 - Generalized D-dimensional unitarity
- Basic ingredients are tree level amplitudes
- Rational part obtained from calculation in $D=6$, $D=8 \rightarrow D=4-2\epsilon$



Sensitivity to Q_t at the LHC

- Apply cuts to suppress radiative top quark decays

$$m_T(bl\gamma; E_T^{\text{miss}}) > 180 \text{ GeV}, \quad m_T(\ell\gamma; E_T^{\text{miss}}) > 90 \text{ GeV}, \\ 160 \text{ GeV} < m(bjj) < 180 \text{ GeV}, \quad 70 \text{ GeV} < m(j, j) < 90 \text{ GeV}$$



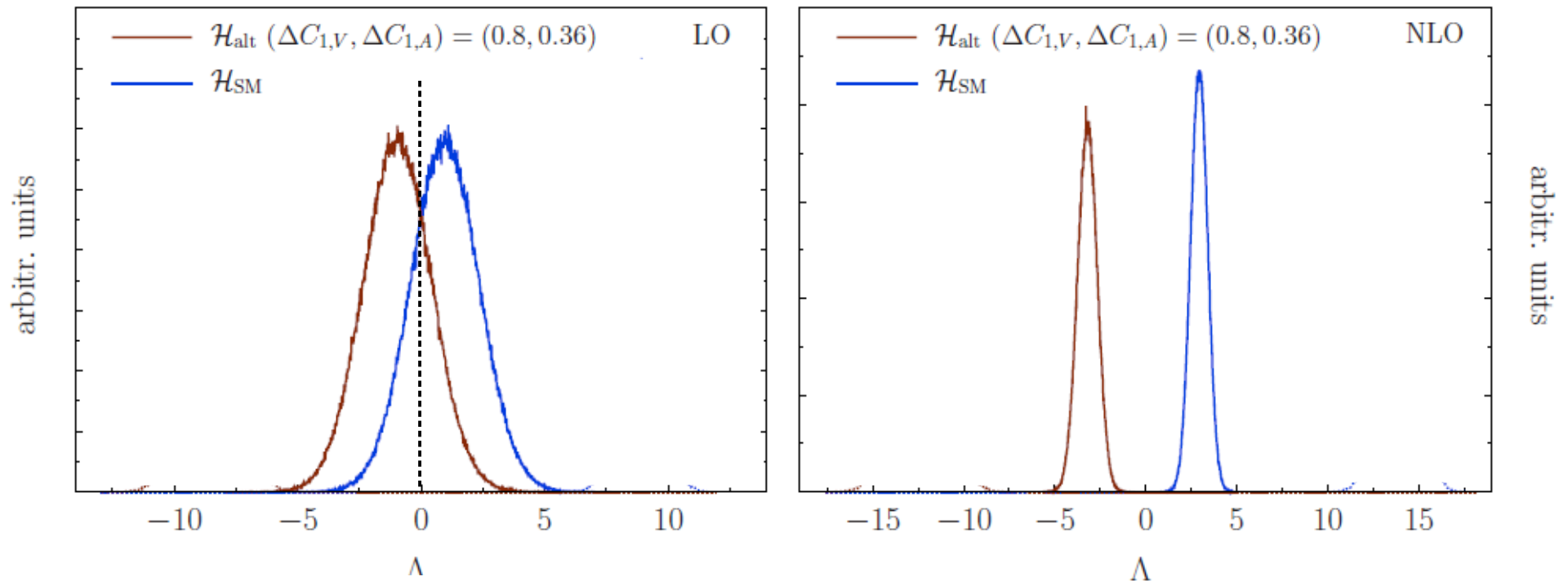
→ Significantly stronger separation power:

$$\mathcal{R}_{\text{RDS}}^{\text{NLO}} = \frac{\sigma_{\text{NLO}}^{Q_t=-4/3}}{\sigma_{\text{NLO}}^{Q_t=2/3}} = 2.88^{+0.05}_{-0.12}$$

But total cross section is reduced by x5.

Statistical Analysis

- LL ratio distributions evaluated with SM and alternative hypothesis



$$\alpha = \int_{-\infty}^{\hat{\Lambda}} d\Lambda P(\Lambda|\mathcal{H}_{\text{SM}}).$$

Type-I error: prob. accepting H_{alt}
even though H_{SM} is correct

$$\beta = \int_{\hat{\Lambda}}^{\infty} d\Lambda P(\Lambda|\mathcal{H}_{\text{alt}}).$$

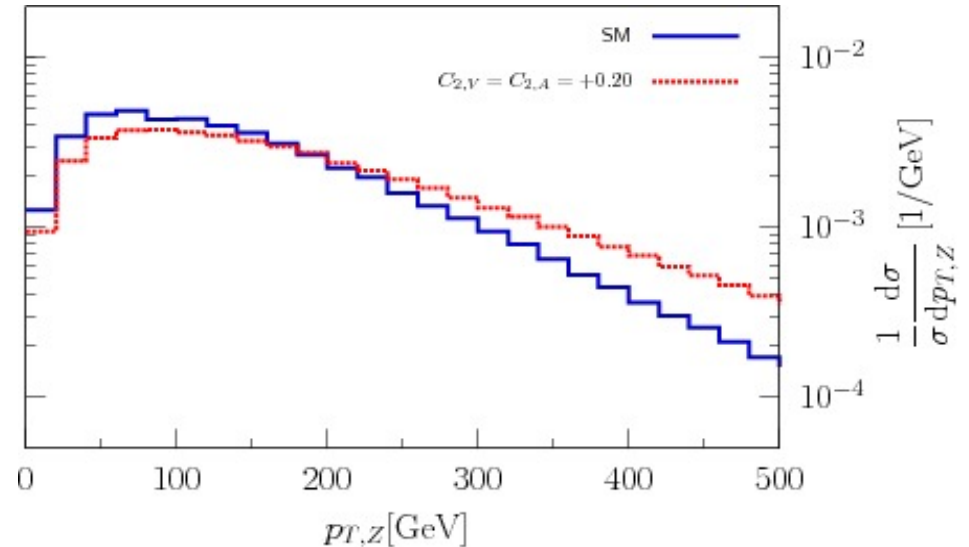
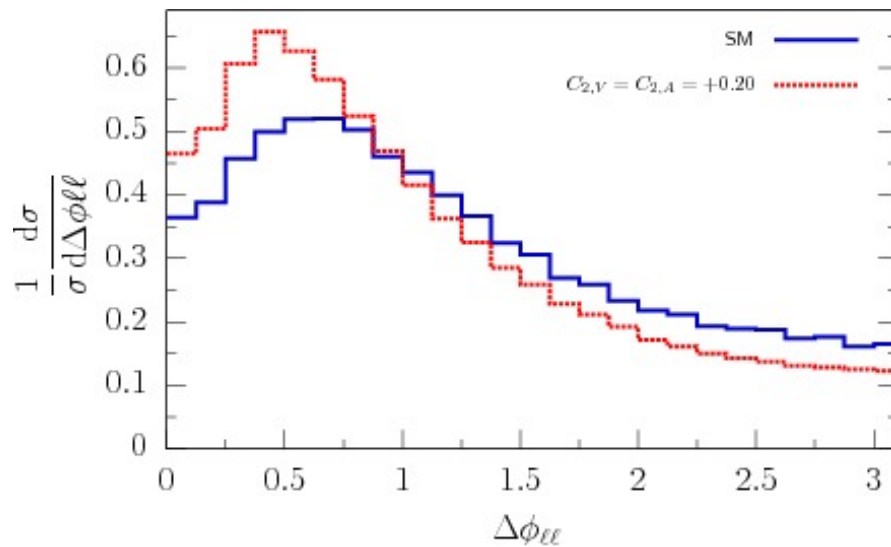
Type-II error: prob. accepting H_{SM}
even though H_{alt} is correct

- Study projected limits from future LHC run
- Consider $E_{\text{cm}}=13$ TeV and luminosities $L=30, 300, 3000 \text{ fb}^{-1}$
- Null Hypothesis = SM couplings
Alternative Hyp. = non-SM couplings
- Flat uncertainties, $\pm 30\%$ at LO and $\pm 15\%$ at NLO

Constraints from LHC run-II

Weak dipole moments

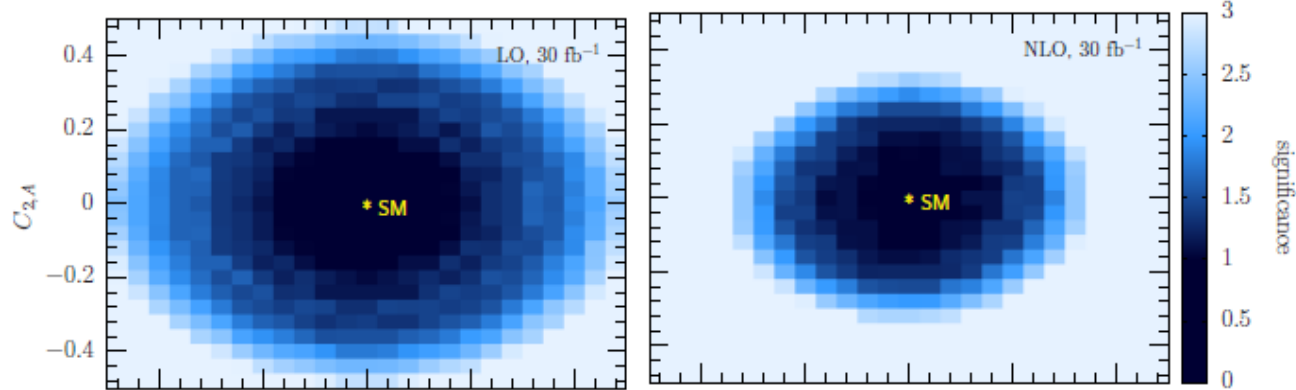
$$\mathcal{L}_{t\bar{t}Z} = ie\bar{u}(p_t) \left[\gamma^\mu (C_{1,V} + \gamma_5 C_{1,A}) + \frac{i\sigma_{\mu\nu}q_\nu}{M_Z} (C_{2,V} + i\gamma_5 C_{2,A}) \right] v(p_{\bar{t}}) Z_\mu,$$



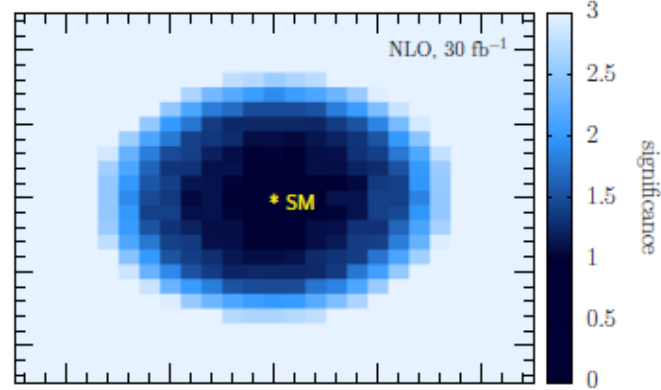
Constraints from LHC run-II

Weak dipole moments

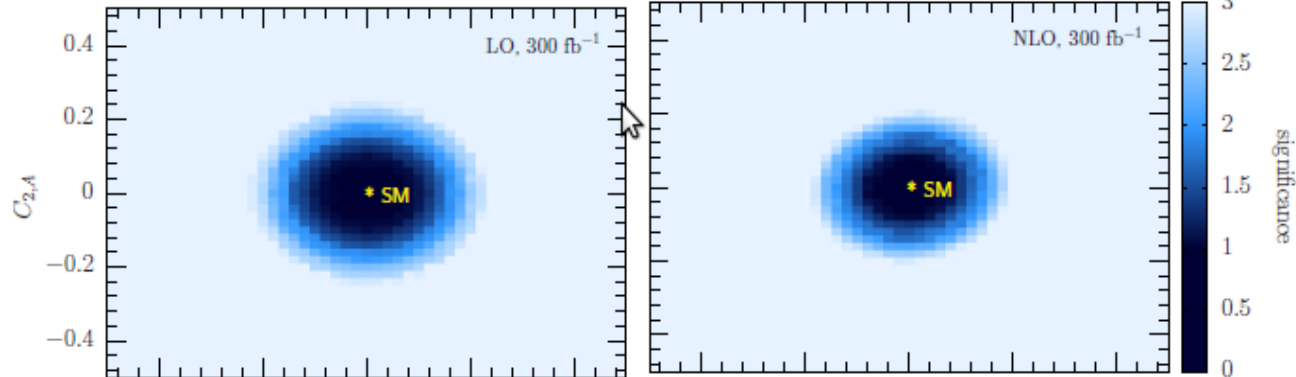
LO 30 fb⁻¹



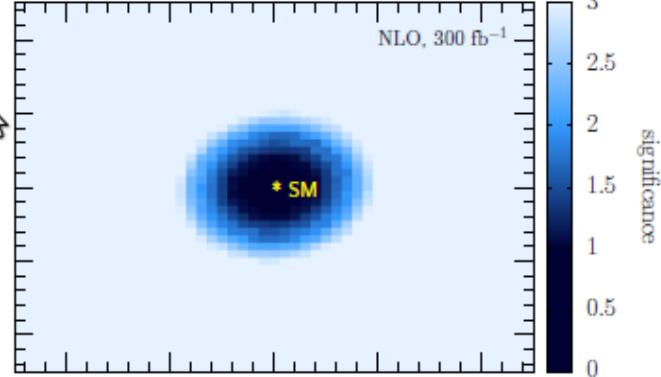
NLO 30 fb⁻¹



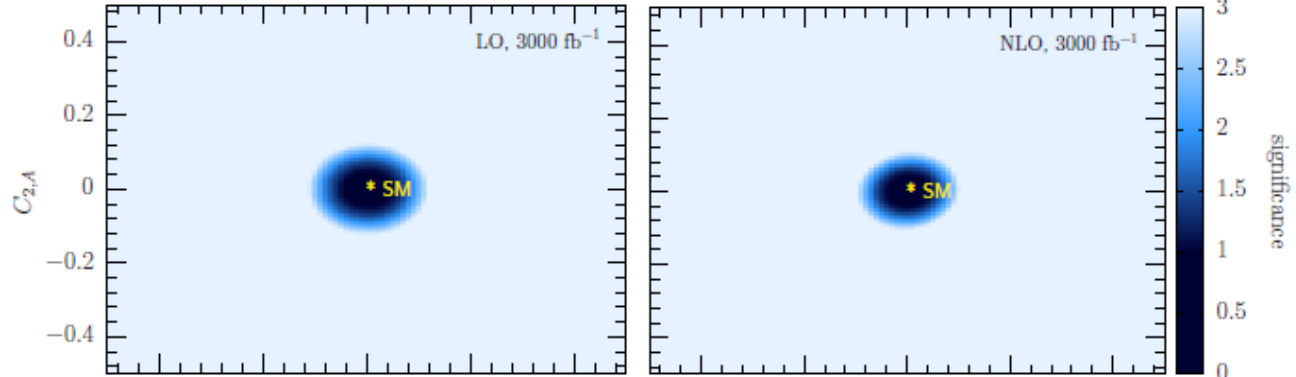
LO 300 fb⁻¹



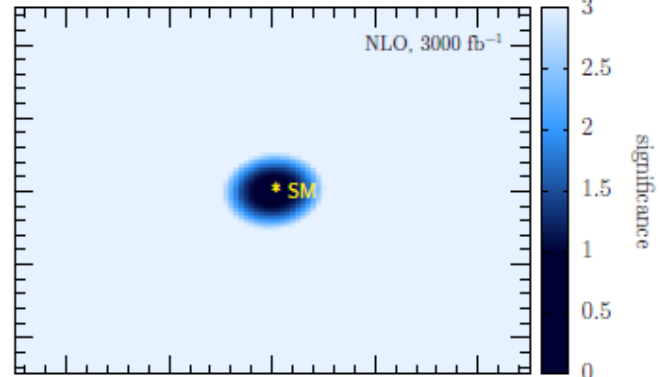
NLO 300 fb⁻¹



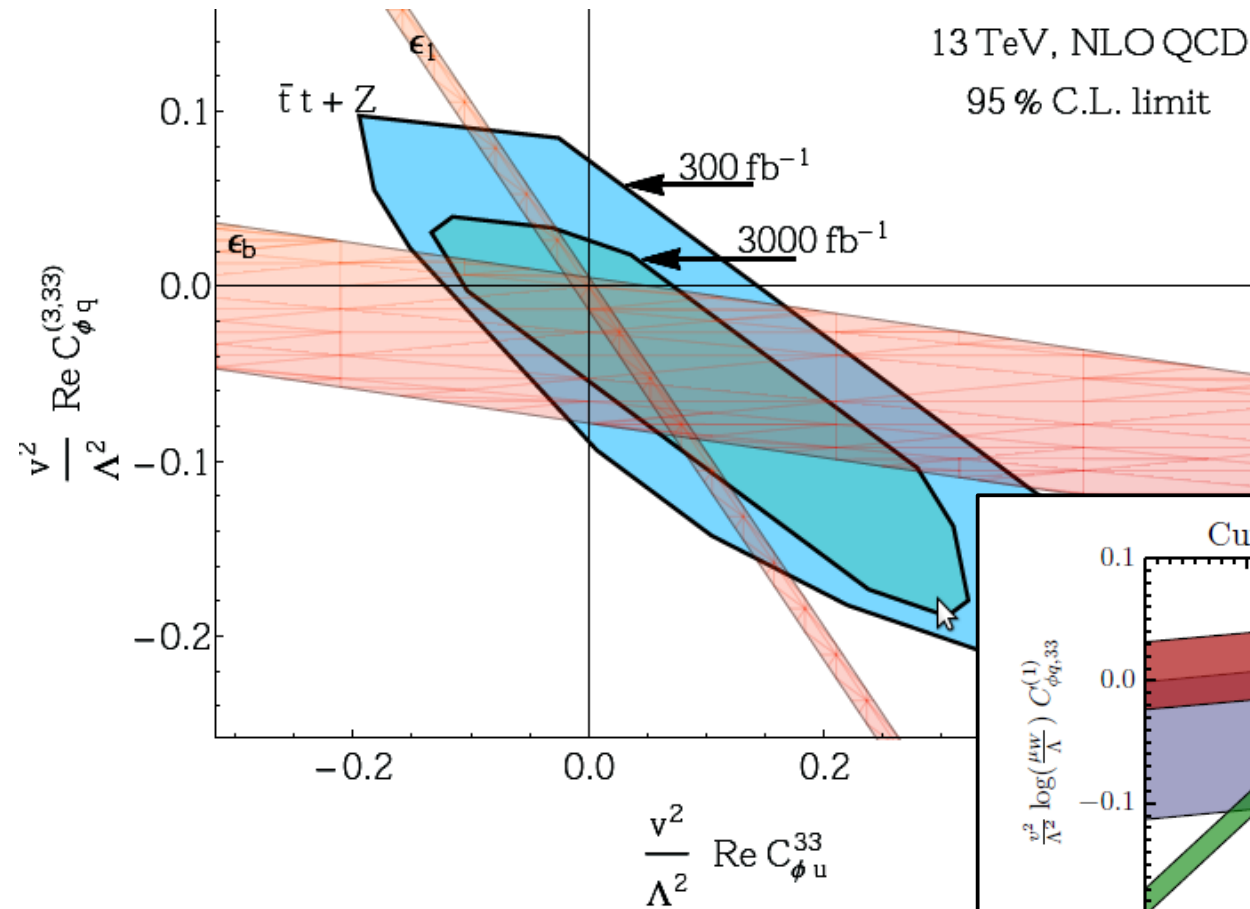
LO 3000 fb⁻¹



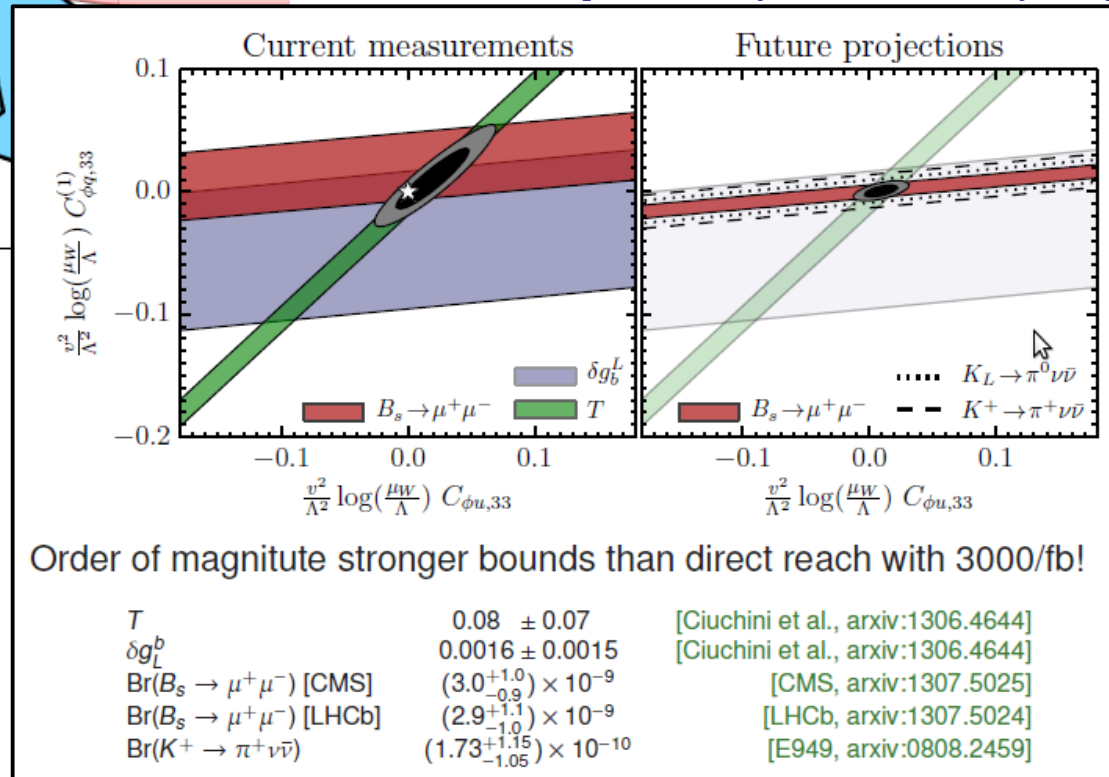
NLO 3000 fb⁻¹



Constraints on dim-six operators

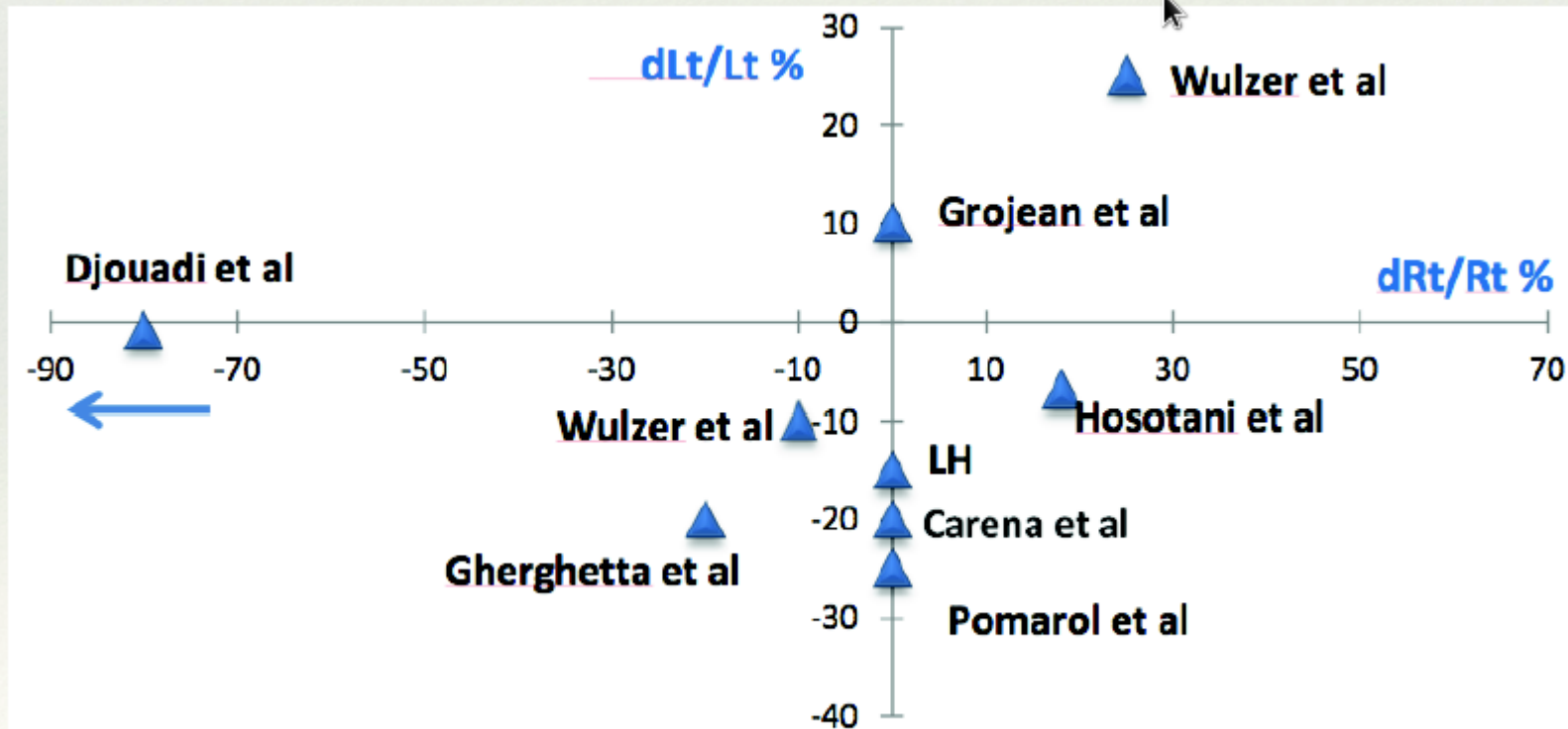


[Brod, Greljo, Stamou, Uttayarat]



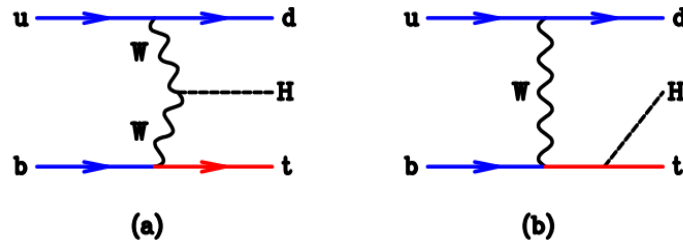
le Higgs models, ...

[Richard, 2014]

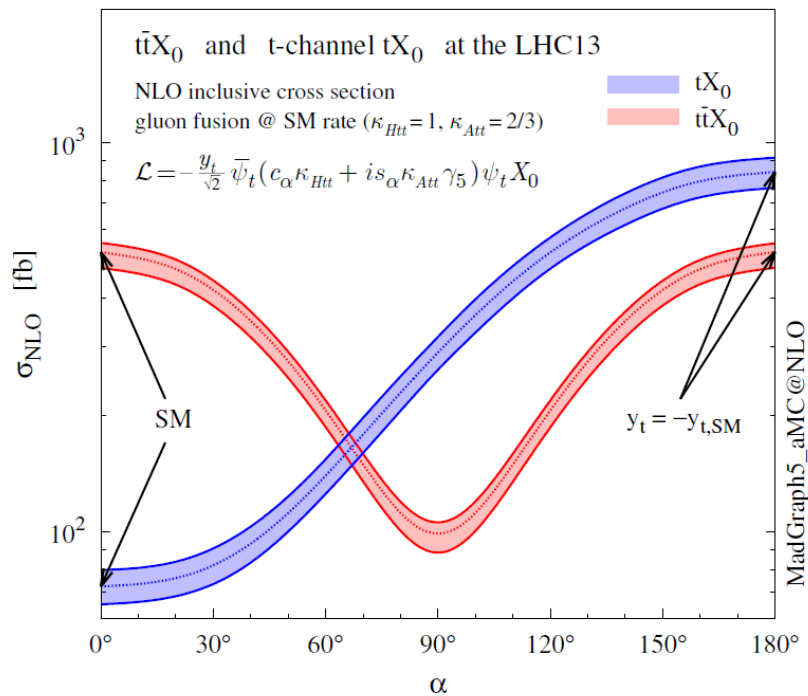


Top quark properties

single top + H :
NLO QCD



$$\mathcal{L}_0^t = -\bar{\psi}_t (c_\alpha \kappa_{Htt} g_{Htt} + i s_\alpha \kappa_{Att} g_{Att} \gamma_5) \psi_t X_0,$$



- $t\bar{t}b+H$ cannot resolve the sign of y_t
- $t+qH$ anomalous cross section grows large

Top quark properties

- Top quark pair production yields sensitivity to *chromo-magnetic/electric dipole moments*

$$H = -\mu \vec{B} \cdot \frac{\vec{S}}{S} - d \vec{E} \cdot \frac{\vec{S}}{S}$$

EDM violate CP:

$$P(\vec{E} \cdot \vec{S}) = -\vec{E} \cdot \vec{S}$$

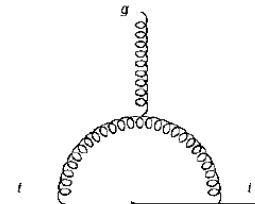
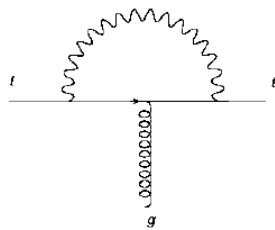
$$T(\vec{E} \cdot \vec{S}) = -\vec{E} \cdot \vec{S}$$

$$\mathcal{L}_{tg} = -g_s \bar{t} \gamma^\mu \frac{\lambda_a}{2} t G_\mu^a + \frac{g_s}{m_t} \bar{t} \sigma^{\mu\nu} (d_V + i d_A \gamma_5) \frac{\lambda_a}{2} t G_{\mu\nu}^a,$$

complex coupling

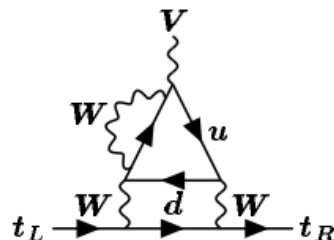
- In the SM, dipole moments are generated *radiatively*

MDM:



$$\sim d_V \approx -0.007$$

EDM:



$$\sim d_A \approx \text{tiny}$$

[Shabalin, Khriplovich, Czarnecki, Krause]
(1980-90)

Top quark properties

- Top quark pair production yields sensitivity to *chromo-magnetic/electric dipole moments*

$$H = -\mu \vec{B} \cdot \frac{\vec{S}}{S} - d \vec{E} \cdot \frac{\vec{S}}{S}$$

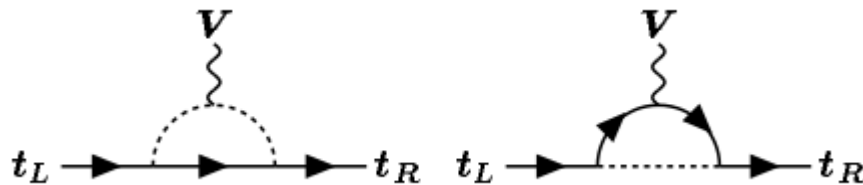
EDM violate CP:

$$\begin{aligned} P(\vec{E} \cdot \vec{S}) &= -\vec{E} \cdot \vec{S} \\ T(\vec{E} \cdot \vec{S}) &= -\vec{E} \cdot \vec{S} \end{aligned}$$

$$\mathcal{L}_{\text{tg}} = -g_s \bar{t} \gamma^\mu \frac{\lambda_a}{2} t G_\mu^a + \frac{g_s}{m_t} \bar{t} \sigma^{\mu\nu} (d_V + i d_A \gamma_5) \frac{\lambda_a}{2} t G_{\mu\nu}^a,$$

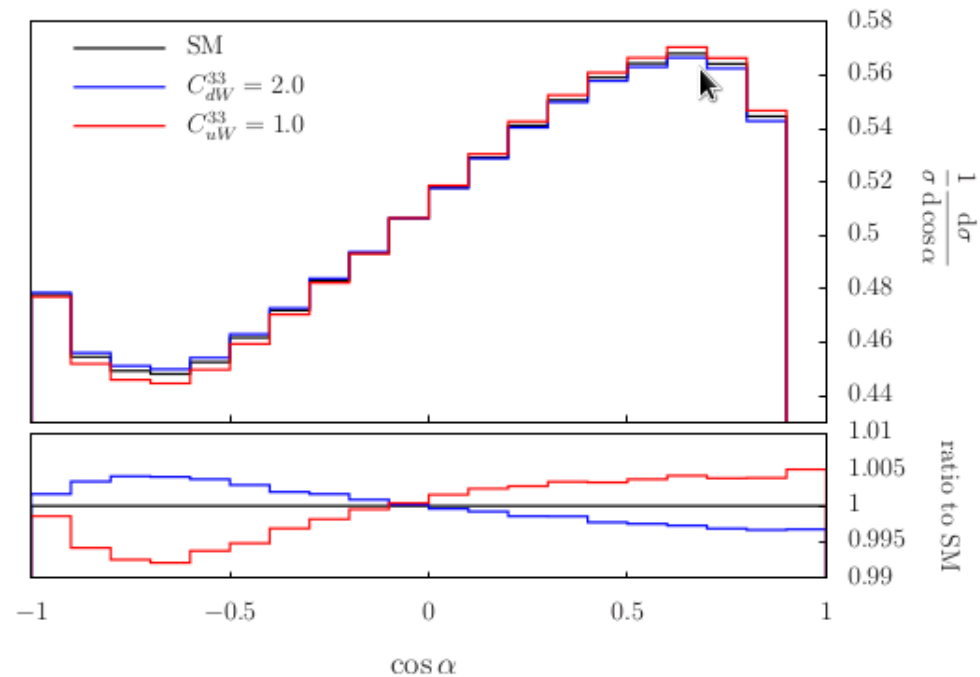
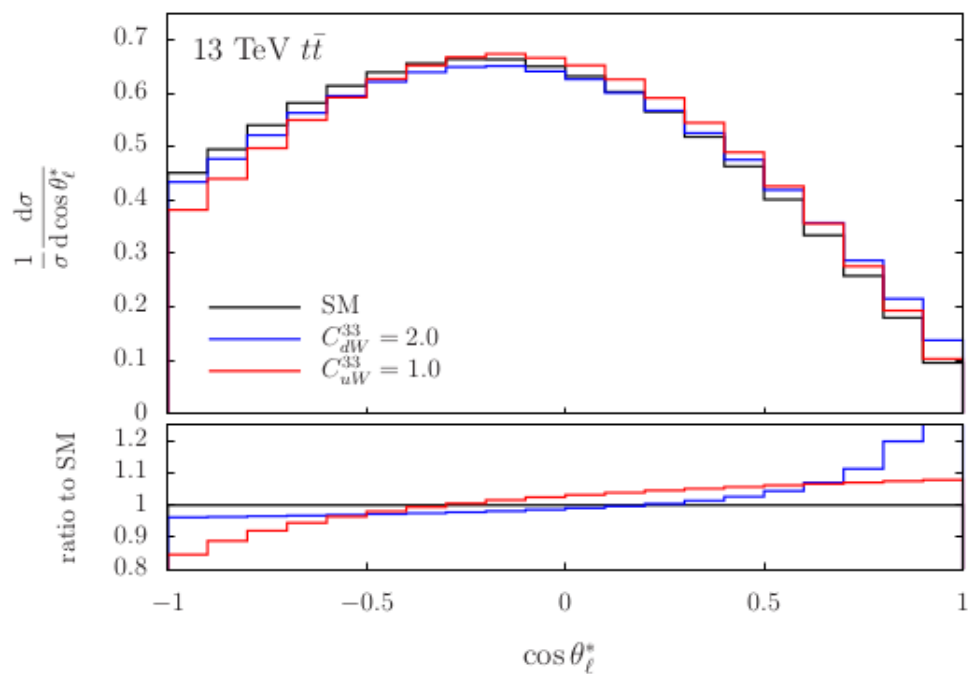
complex coupling

- Beyond the SM, dipole moment couplings can arise already at tree level



$$O_{uG\phi}^{33} = (\bar{q}_{L3} \lambda_a \sigma^{\mu\nu} t_R) \tilde{\phi} G_{\mu\nu}^a, \quad d_V = \frac{\sqrt{2} v m_t}{g_s \Lambda^2} \text{Re } C_{uG\phi}^{33}, \quad d_A = \frac{\sqrt{2} v m_t}{g_s \Lambda^2} \text{Im } C_{uG\phi}^{33}$$

For $\Lambda \approx 1 \text{ TeV}$: $d_{V,A} \approx 0.05 = \text{big!}$



$$\cos \theta_\ell^* = \frac{\vec{p}_\ell \cdot \vec{p}_W}{|\vec{p}_\ell| |\vec{p}_W|}, \quad \cos \alpha = \frac{\vec{p}_t \cdot \vec{p}_W}{|\vec{p}_t| |\vec{p}_W|},$$

$$A_\phi(c_0) = \frac{\sigma(\cos \phi < c_0) - \sigma(\cos \phi > c_0)}{\sigma(\cos \phi < c_0) + \sigma(\cos \phi > c_0)},$$

