

# Vector Boson Fusion and Scattering: Parton-Shower Effects

Michael Rauch | Workshop "Future of VBF Measurements", 22 Sep 2016

INSTITUTE FOR THEORETICAL PHYSICS



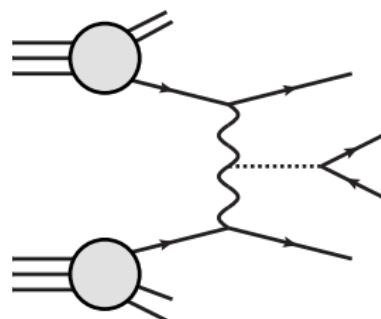
# VBF event topology

VBF (vector-boson fusion) topology shows distinct signature

- two tagging jets in forward region
  - reduced jet activity in central region
  - leptonic decay products typically between tagging jets
- two-sided deep-inelastic scattering

First studied in context of Higgs searches [Han, Valencia, Willenbrock; Figy, Oleari, Zeppenfeld; ...]

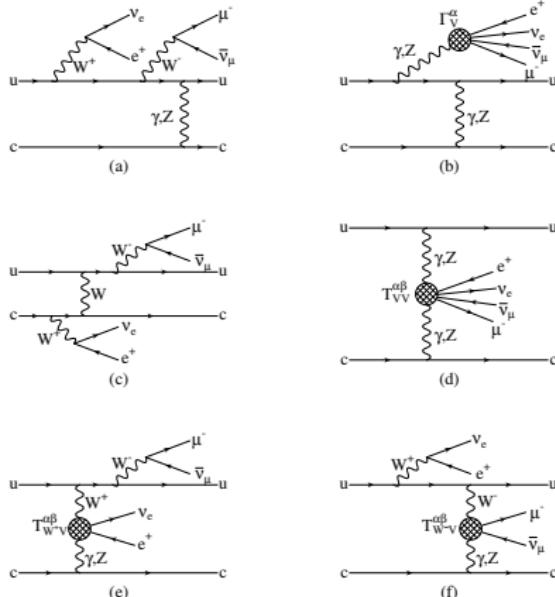
- $\sim 10\%$  compared to main production mode gluon fusion
- NLO QCD corrections moderate ( $\mathcal{O}(\lesssim 10\%)$ )
- NLO EW same size [Ciccolini *et al.*, Figy *et al.*]
- NNLO QCD known for subsets:  
no significant contributions for integrated c.s.  
[Harlander *et al.*, Bolzoni *et al.*]  
corrections up to 10% in distributions  
[Cacciari *et al.*]
- incl. NNNLO QCD: tiny effects [Dreyer, Karlberg]
- advantageous scale choice:  
momentum transfer  $q^2$  of intermediate vector bosons



# Diboson-VBF production

[Bozzi, Jäger, Oleari, Zeppenfeld (VV); Campanario, Kaiser, Zeppenfeld ( $W^\pm \gamma$ )  
[Denner, Hosekova, Kallweit ( $W^+ W^+$ )]

- Important process for LHC run-II
  - Part of the NLO wish list
    - [Les Houches 2005]
  - background to Higgs searches
  - access to anomalous triple and quartic gauge couplings
  - NLO QCD implementation of
    - all boson combinations
    - leptonic and semi-leptonic decays
    - including off-shell and non-resonant contributions
    - VBF approximation
- **VBFNLO**      [MR, Zeppenfeld et al.]



# NLO plus Parton Shower

Combine advantages of NLO calculations and parton shower

## NLO calculation

- normalization correct to NLO
- additional jet at high- $p_T$  accurately described
- theoretical uncertainty reduced

## Parton shower

- Sudakov suppression at small  $p_T$
- events at hadron level possible

## State of the Art

Implementations for specific VBF processes

- POWHEG-BOX

[Alioli, Hamilton, Nason, Oleari, Re]

currently available VBF implementations:

$Z$

[Jäger, Schneider, Zanderighi]

$W^\pm, Z$

[Schissler, Zeppenfeld]

$W^\pm W^\pm, W^\pm W^\mp$

[Jäger, Zanderighi]

$ZZ$

[Jäger, Karlberg, Zanderighi]

$H+3\text{jets}$

[Jäger, Schissler, Zeppenfeld]

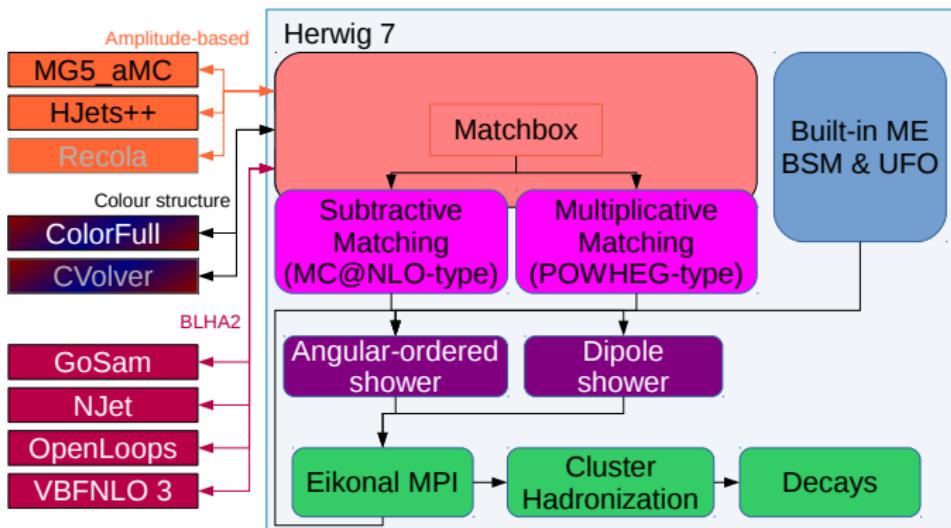
- VBF- $H$  with POWHEG method

[D'Errico, Richardson]

- HJets++

[Campanario, Figy, Plätzer, Sjödahl]

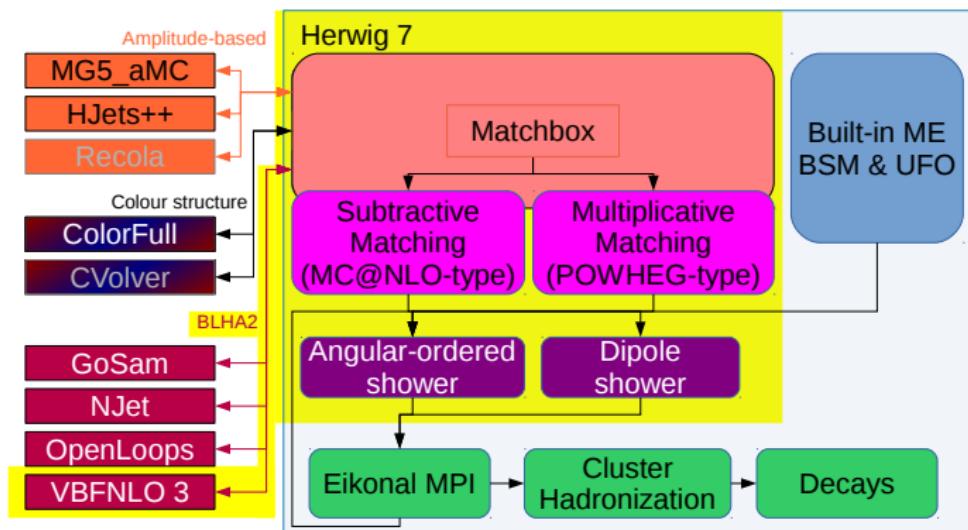
- fully automated matching of NLO to parton showers through Matchbox module  
[work led by S. Plätzer with substantial contributions by J. Bellm, A. Wilcock, MR, C. Reuschle]
- subtractive (MC@NLO-type,  $\oplus$ ) and multiplicative (POWHEG-type,  $\otimes$ ) matching
- angular-ordered (QTilde, PS) and dipole (Dipoles) shower
- matrix elements through binary interface, no event files



# VBFNLO 3 & Herwig 7 – this talk

- matrix elements from VBFNLO via **BLHA2** interface
- extensions to make accessible
  - phase-space sampling
  - (electroweak) random helicity summation
  - anomalous couplings

[Binoth et al., Alioli et al.]



# Setup

Process:

$$pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj \text{ via VBF}$$

Cuts:

$$\begin{array}{ll} p_{T,j} > 30 \text{ GeV}, & |y_j| < 4.5, \\ \text{anti-}k_T \text{ jets with } R = 0.4, & b\text{-quark veto} \\ \\ p_{T,\ell} > 20 \text{ GeV}, & |y_\ell| < 2.5, \\ m_{e^+, \mu^-} > 15 \text{ GeV}, & \\ \\ m_{j1, j2} > 600 \text{ GeV}, & |y_{j1} - y_{j2}| > 3.6 \end{array}$$

(inspired from ATLAS VBF category in  $H \rightarrow WW$ , CMS similar)

PDF: MMHT2014

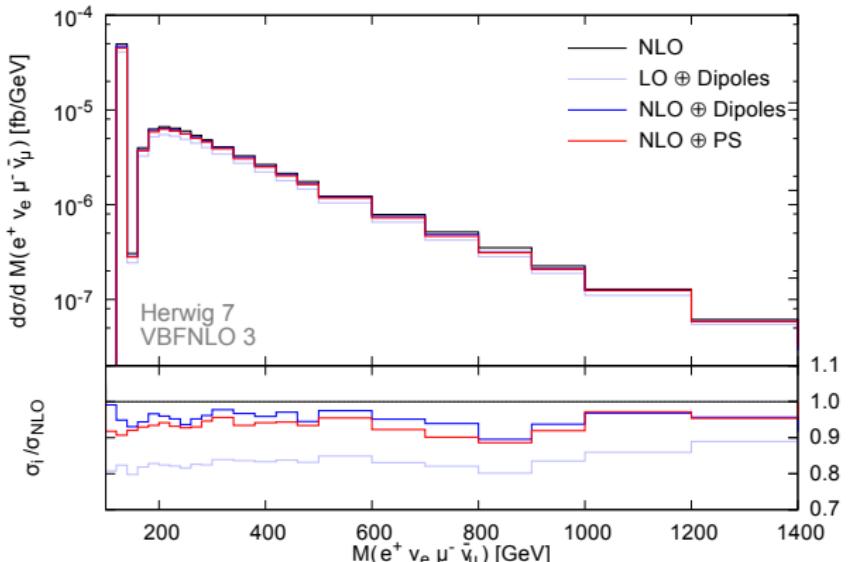
central scale choice: transverse momentum of the leading jet

$$\mu_0 = p_{T,j1}$$

(close to momentum transfer  $|q^2|$  in VBF region)

# Distributions

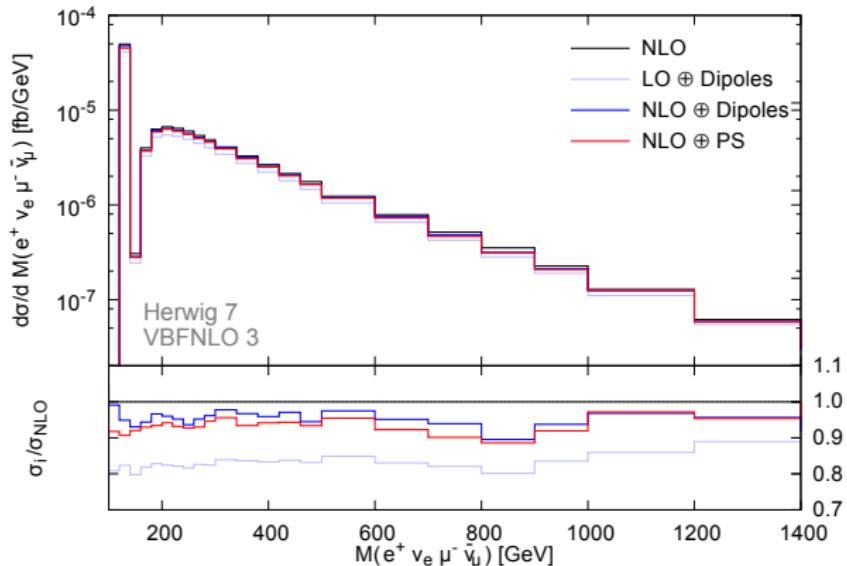
Process as example:  $pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj$  via VBF  
Four-lepton invariant mass



- Higgs peak at 125 GeV
- $WW$  continuum production above 180 GeV
- significant cancellation between diagrams at high invariant masses
- ⇒ ideal test for anomalous couplings

# Distributions

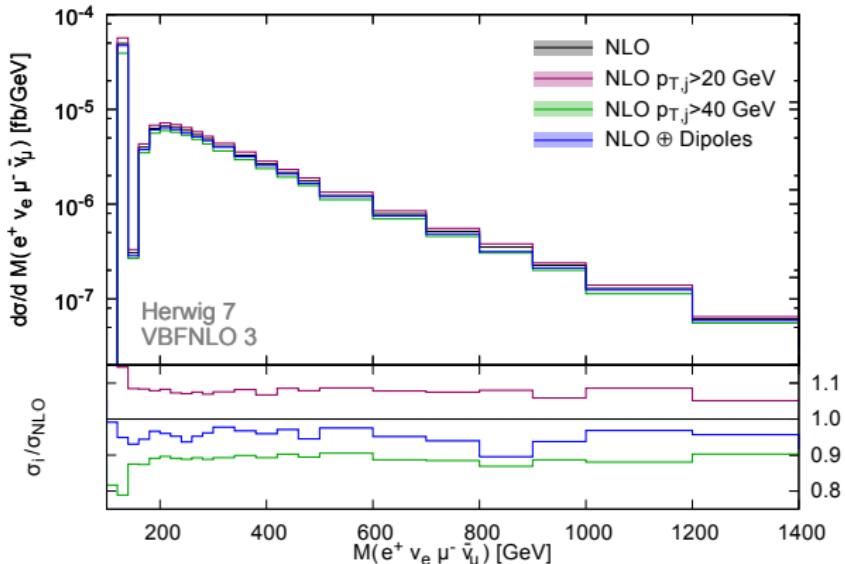
Process as example:  $pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj$  via VBF  
Four-lepton invariant mass



- all parton-shower results smaller than NLO cross section
- additional  $K$ -factor effect for LO  $\oplus$  Dipoles result ( $K = 1.077$ )
- no relevant shape changes  
(as expected: insensitive to QCD effects)

# Migration Effects

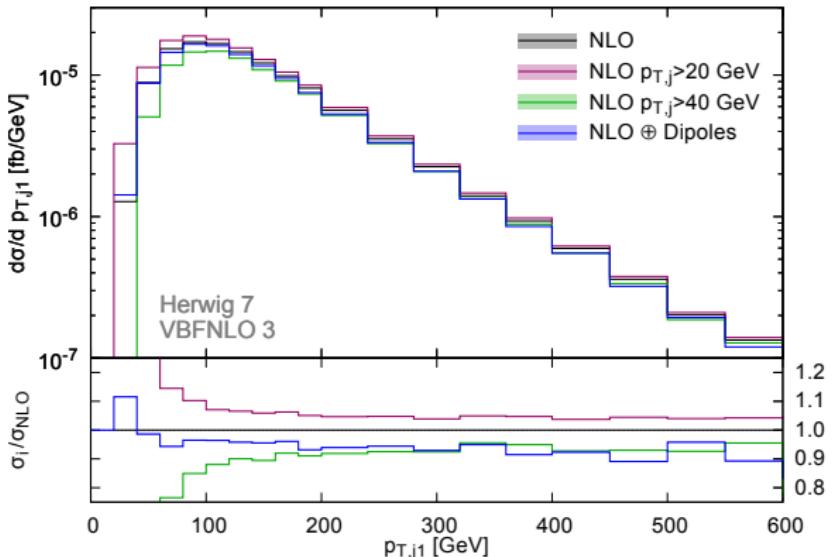
Vary transverse momentum cut of jets (default:  $p_{T,j} > 30 \text{ GeV}$ )



- same effect when slightly raising  $p_{T,j}$  cut
- additional parton splittings: if hard & wide-angle emission → separate jet
- reduces energy and transverse momentum of emitting parton
- ↔  $p_{T,j}$  cut, VBF cut  $m_{jj} > 600 \text{ GeV}$

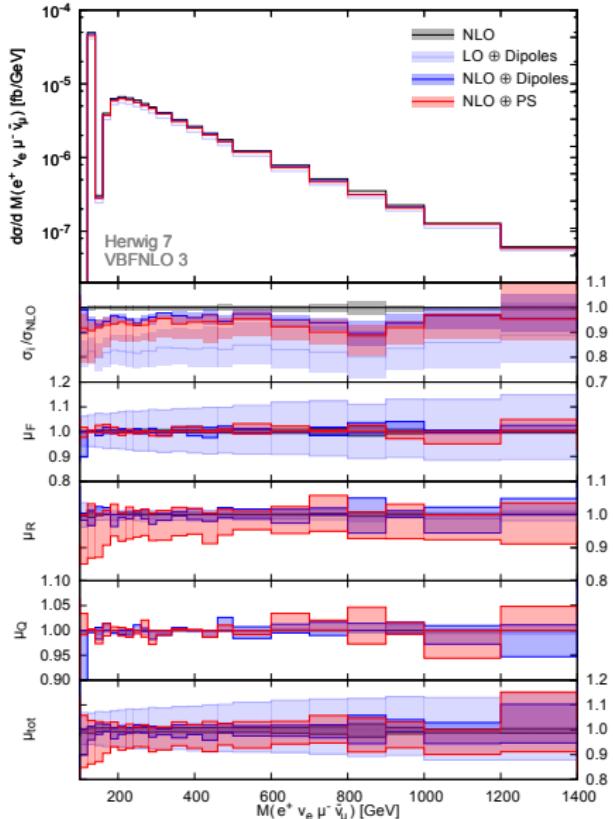
# Migration Effects

Vary transverse momentum cut of jets (default:  $p_{T,j} > 30 \text{ GeV}$ )



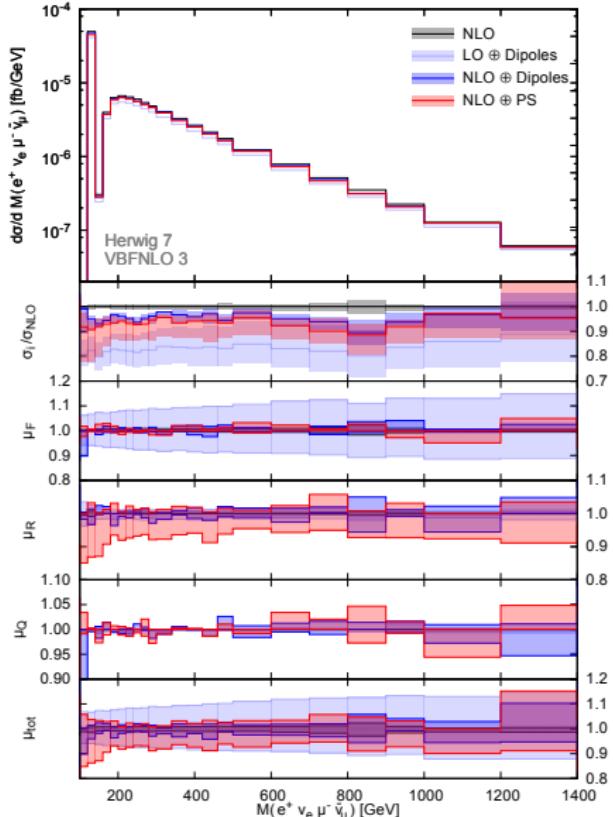
- less pronounced for small  $p_{T,j1}$   
→ VBF cut main source
- migration of events across cut boundary
- ↔ generation-level vs. analysis-level cuts
- ⇒ no tuning of acceptance criteria required
- generation-level cuts nevertheless chosen weaker

# Four-lepton Invariant Mass



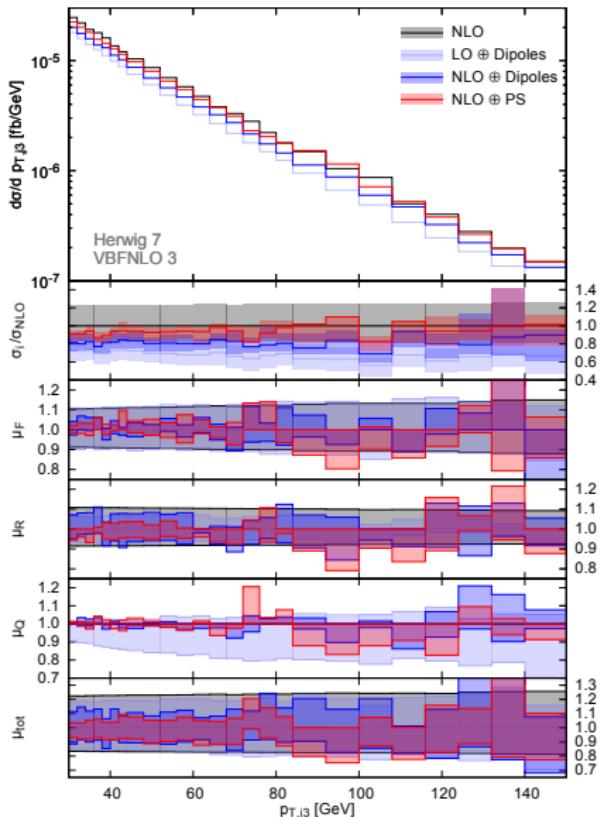
- ← ■ central scale  $\mu_0 = p_{T,j1}$   
transverse momentum of leading jet
- ← ■ band: scale variation  
 $\{\mu_F, \mu_R, \mu_Q\} / \mu_0 \in [\frac{1}{2}; 2]$   
 $\mu_i / \mu_j \in [\frac{1}{2}; 2]$
- ← ■ factorization scale  
 $\mu_F / \mu_0 \in [\frac{1}{2}; 2]$
- ← ■ renormalization scale  
 $\mu_R / \mu_0 \in [\frac{1}{2}; 2]$
- ← ■ shower scale  
 $\mu_Q / \mu_0 \in [\frac{1}{2}; 2]$
- ← ■ all three scales

# Four-lepton Invariant Mass



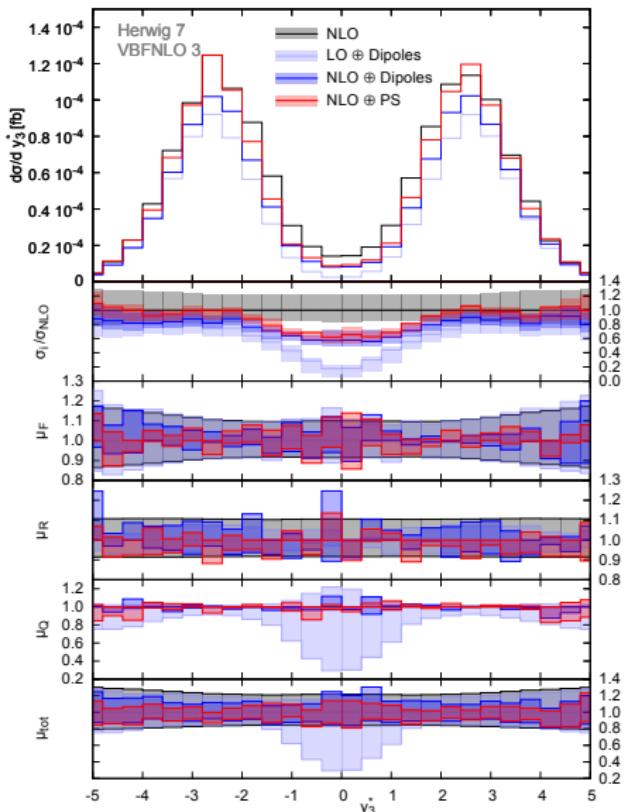
- consistent variation of scales between hard process and parton shower
- large factorization scale dependence for LO result
- larger dependence for down variation of renormalization scale in angular-ordered shower:  
 $\alpha_s \rightarrow$  more splittings  
 $\rightarrow$  bigger migration effects
- small variations from shower-scale changes
- modest remaining overall uncertainty

# Transverse Momentum Third Jet



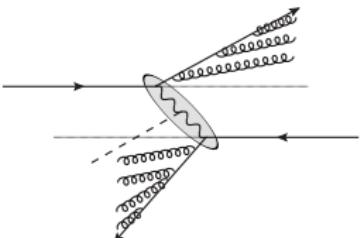
- large scale variation bands for
  - shower scale in LO+Dipoles  
→ pure parton-shower effect
  - fact./ren. scale in “NLO”  
→ LO accuracy of observable
- reduced for both NLO + parton-shower curves
- still significant remaining uncertainty  $\mathcal{O}(10 - 20\%)$
- call for multi-jet merging

# Rapidity of third jet



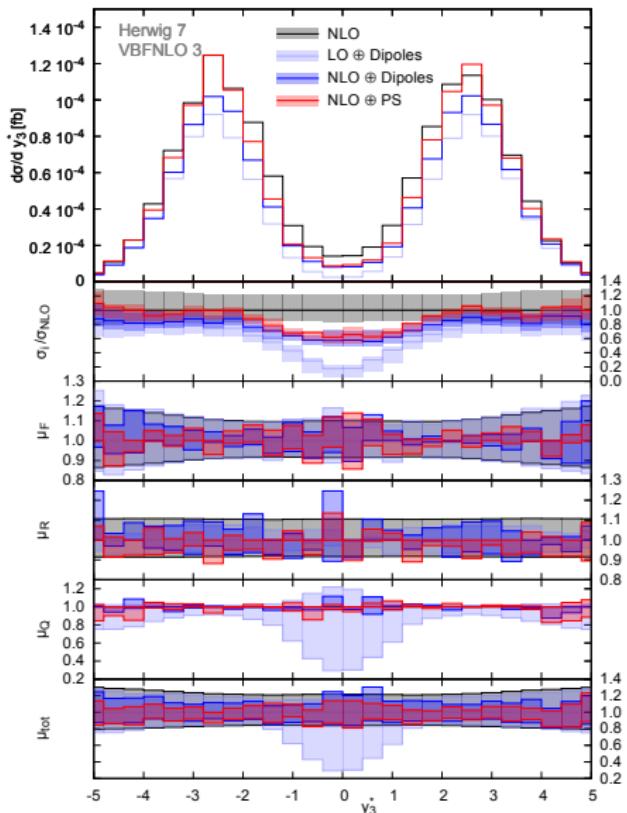
Rapidity of third jet  
relative to two tagging jets

$$y_3^* = y_3 - \frac{y_1 + y_2}{2}$$



- VBF colour structure suppresses additional central jet radiation
- colour connection between tagging jet and remnant
- ↔ distinction from QCD-induced production

# Rapidity of third jet

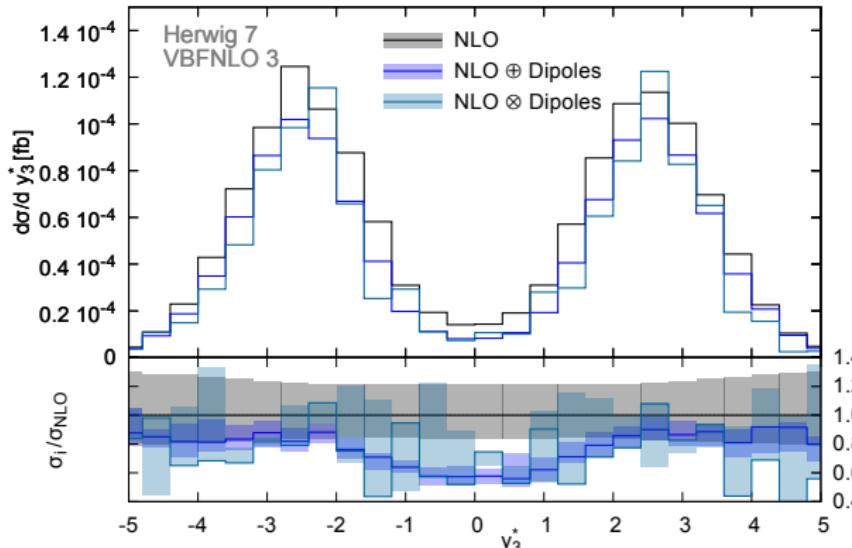


Rapidity of third jet  
relative to two tagging jets

$$y_3^* = y_3 - \frac{y_1 + y_2}{2}$$

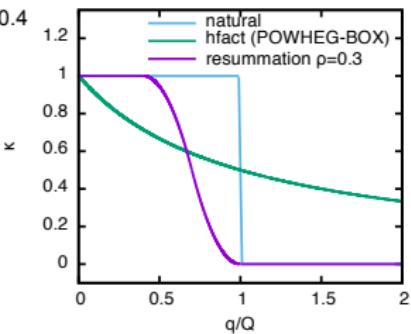
- impact of parton showers (+LO) long unclear
- Herwig predicts very low radiation in central region
- large shower-scale unc.
- stabilised when combining with NLO
- still reduction present
- scale variation bands not overlapping
- only small effects in forward region (mostly global normalization)

# Rapidity of third jet – POWHEG

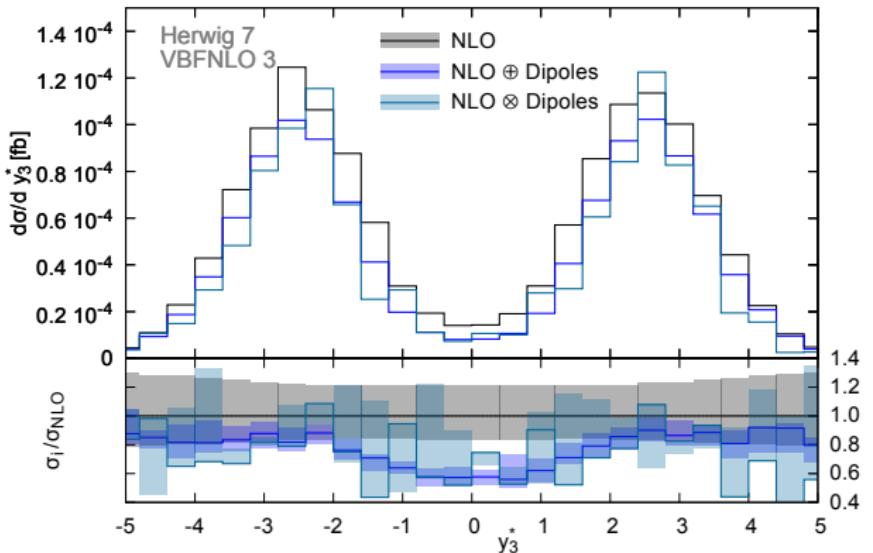


- POWHEG-like ( $\otimes$ ) using resummation scheme [Plätzer]:

$$\kappa(Q, q; \rho) = \begin{cases} 1 & \text{for } q < (1 - 2\rho)Q \\ 1 - \frac{(1-2\rho-\frac{q}{Q})^2}{2\rho^2} & \text{for } (1 - 2\rho)Q < q < (1 - \rho)Q \\ \frac{(1-\frac{q}{Q})^2}{2\rho^2} & \text{for } (1 - \rho)Q < q < Q \\ 0 & \text{for } q > Q \end{cases}$$



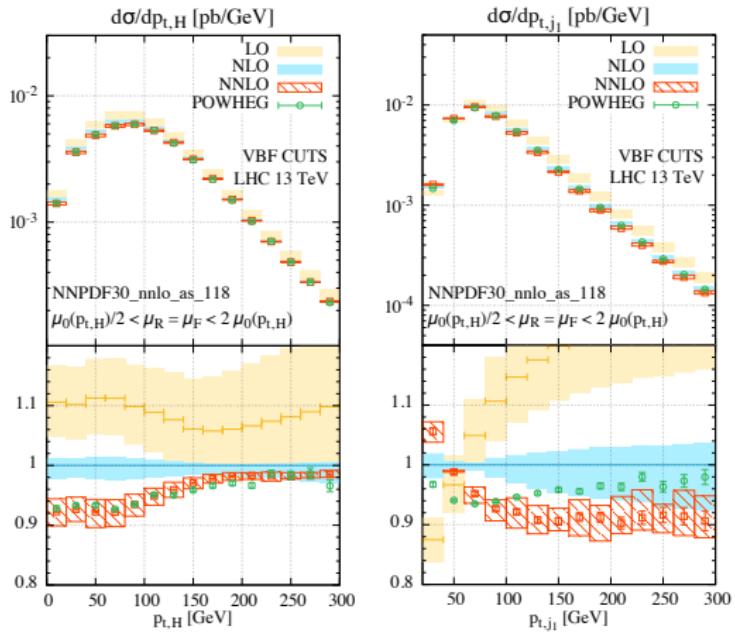
# Rapidity of third jet – POWHEG



- band: joint variation  $\mu_F = \mu_R = \mu_Q \in [\frac{1}{2}, 2] \mu_0$
- similar predictions from MC@NLO-like ( $\oplus$ ) and POWHEG-like ( $\otimes$ ) matching
- also holds for other distributions

# NNLO QCD vs. Parton Shower for VBF-H

[Cacciari, Dreyer, Karlberg, Salam, Zanderighi]



	$\sigma^{(\text{no cuts})}$ [pb]	$\sigma/\sigma^{\text{NLO}}$
LO	$4.032^{+0.057}_{-0.069}$	1.026
NLO	$3.929^{+0.024}_{-0.023}$	1
NNLO	$3.888^{+0.016}_{-0.012}$	0.990

	$\sigma^{(\text{VBF cuts})}$ [pb]	$\sigma/\sigma^{\text{NLO}}$
LO	$0.957^{+0.066}_{-0.059}$	1.092
NLO	$0.876^{+0.008}_{-0.018}$	1
NNLO	$0.826^{+0.013}_{-0.014}$	0.943

central scale:

$$\mu_0^2(p_{T,H}) = \frac{M_H}{2} \sqrt{\left(\frac{M_H}{2}\right)^2 + p_{T,H}^2}$$

jets: anti- $k_T$ ,  $R = 0.4$ ,

$$p_{T,j} > 25 \text{ GeV}, |y_j| < 4.5$$

VBF cuts:  $m_{jj} > 600 \text{ GeV}$ ,

$$\Delta y_{jj} > 4.5, y_{j1} \cdot y_{j2} < 0$$

- NNLO effects well approximated by NLO plus parton-shower results for some distributions, remaining differences for others

# Conclusions

Parton-shower and scale variation effects in  
 $W^+ W^-$  production via vector-boson-fusion

- important process for the LHC
  - Higgs properties – unitarity in WW scattering
  - testing anomalous (triple and) quartic gauge couplings
- study performed with Herwig 7 & VBFNLO 3
- compatible behavior of both parton showers and matching schemes
- small parton-shower effects for distributions of variables already present at LO
  - mostly reduction of inclusive cross section due to additional jet radiation
- presence of central rapidity gap stabilised

Defined standardized interface between Monte Carlo tools and one-loop programs

→ [Binoth Les Houches Accord \(BLHA\)](#)

[arXiv:1001.1307, arXiv:1308.3462]

- tree-level evaluation of matrix elements well under control
- modular structure of NLO calculations
- algorithms for treatment of infrared singularities (Catani-Seymour, FKS, ...)
- → incorporate one-loop matrix element information into MC tools

Distribution of tasks:

- MC tool:
  - cuts, histograms, parameters
  - Monte Carlo integration
  - phasespace (→ [VBFNLO](#))
  - IR subtraction
  - Born, colour- and spin-correlated Born ([only BLHA1](#))
- One-loop provider (OLP):
  - one-loop matrix elements  $2\Re(\mathcal{M}_{\text{LO}}^\dagger \mathcal{M}_{\text{virt}})$  (coefficients of  $\epsilon^{-2}, \epsilon^{-1}, \epsilon^0; |\mathcal{M}_{\text{LO}}|^2$ )
  - Born, colour- and spin-correlated Born ([only BLHA2](#))

Setup stage via “contract” file

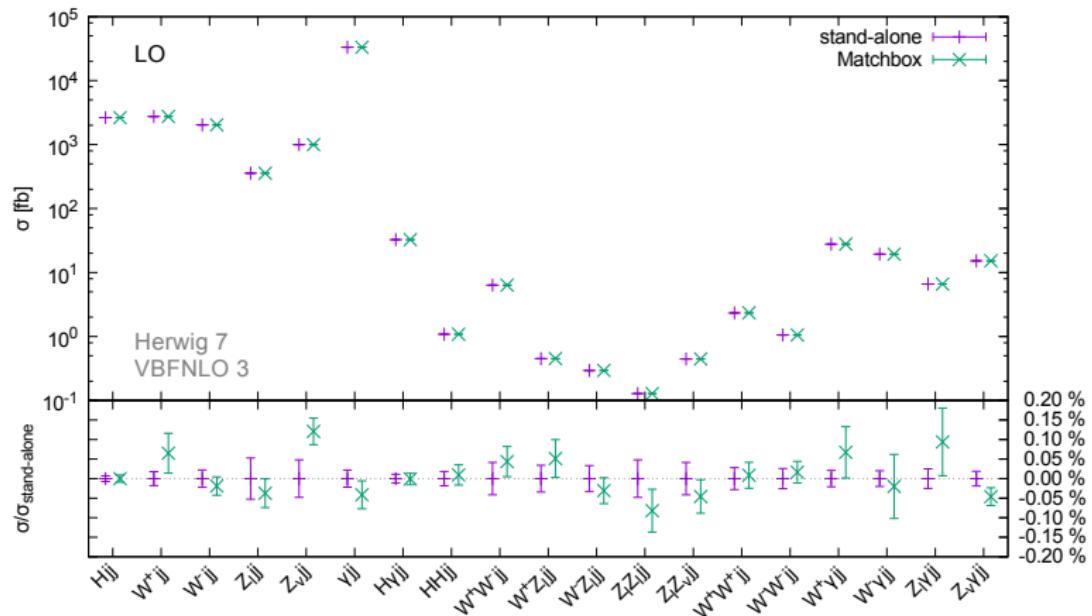
(needed for tools which generate code on the fly)

Run-time stage via binary interface (function calls) → fast

# Validation

Compare LO results between VBFNLO stand-alone run and interfaced to Herwig 7 via Matchbox

(inclusive cuts, with leptonic gauge boson decays into single different-flavour combination, Higgs non-decaying)

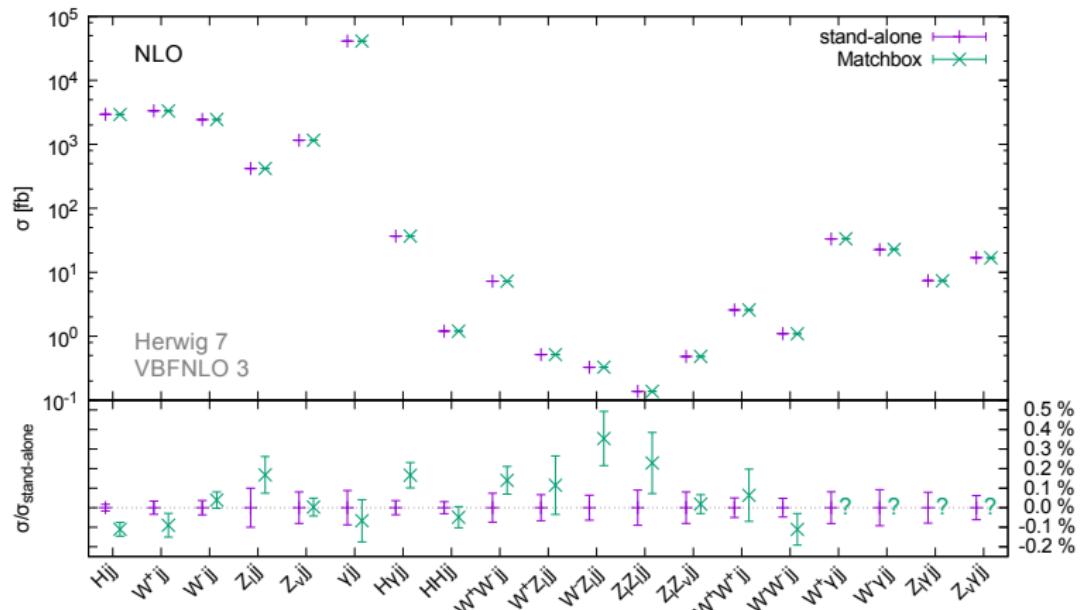


→ good agreement at or below permill level

# Validation

Compare NLO results between VBFNLO stand-alone run and  
interfaced to Herwig 7 via Matchbox

(inclusive cuts, with leptonic gauge boson decays into single different-flavour combination, Higgs non-decaying)



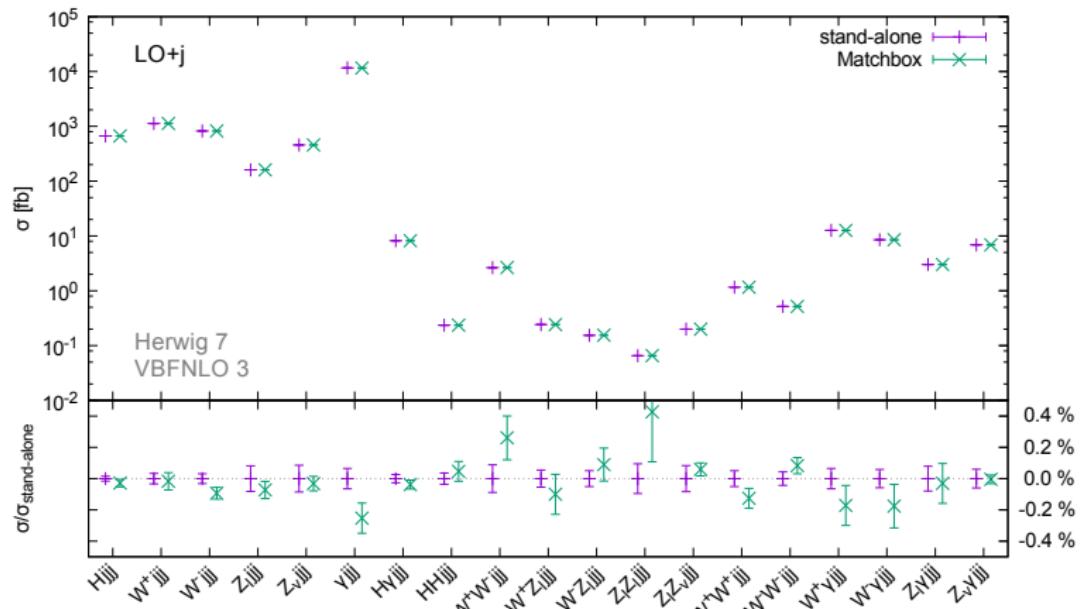
→ good agreement

$V\gamma$  processes:  $\pm 0.7\%$  deviation  $\leftrightarrow$  beyond errors → under investigation

# Validation

Compare LO+j results between VBFNLO stand-alone run and interfaced to Herwig 7 via Matchbox

(inclusive cuts, with leptonic gauge boson decays into single different-flavour combination, Higgs non-decaying)



→ good agreement

# Setup

Generation-level cuts:

$$\begin{aligned} p_{T,j} &> 20 \text{ GeV}, \\ \text{anti-}k_T \text{ jets with } R &= 0.4, \end{aligned}$$

$$\begin{aligned} |y_j| &< 5.0, \\ b\text{-quark veto} \end{aligned}$$

$$\begin{aligned} p_{T,\ell} &> 15 \text{ GeV}, \\ m_{e^+, \mu^-} &> 15 \text{ GeV}, \end{aligned}$$

$$|y_\ell| < 3.0,$$

$$m_{j1, j2} > 400 \text{ GeV},$$

$$|y_{j1} - y_{j2}| > 3.0$$

Analysis-level cuts:

$$\begin{aligned} p_{T,j} &> 30 \text{ GeV}, \\ \text{anti-}k_T \text{ jets with } R &= 0.4, \end{aligned}$$

$$\begin{aligned} |y_j| &< 4.5, \\ b\text{-quark veto} \end{aligned}$$

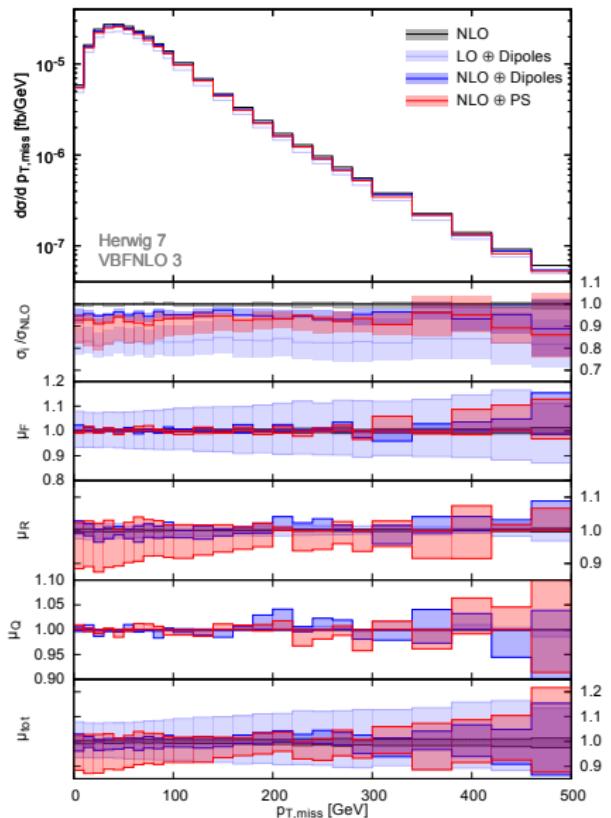
$$\begin{aligned} p_{T,\ell} &> 20 \text{ GeV}, \\ m_{e^+, \mu^-} &> 15 \text{ GeV}, \end{aligned}$$

$$|y_\ell| < 2.5,$$

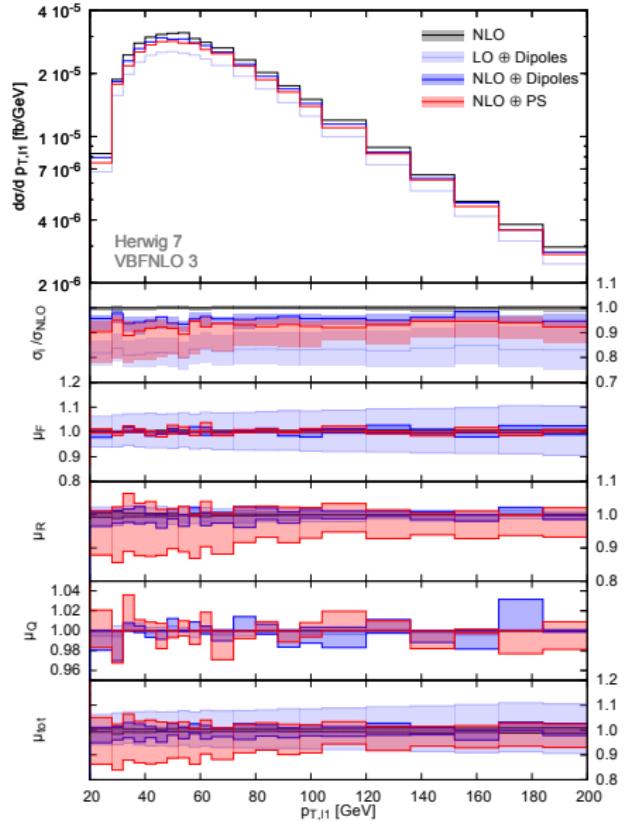
$$m_{j1, j2} > 600 \text{ GeV},$$

$$|y_{j1} - y_{j2}| > 3.6$$

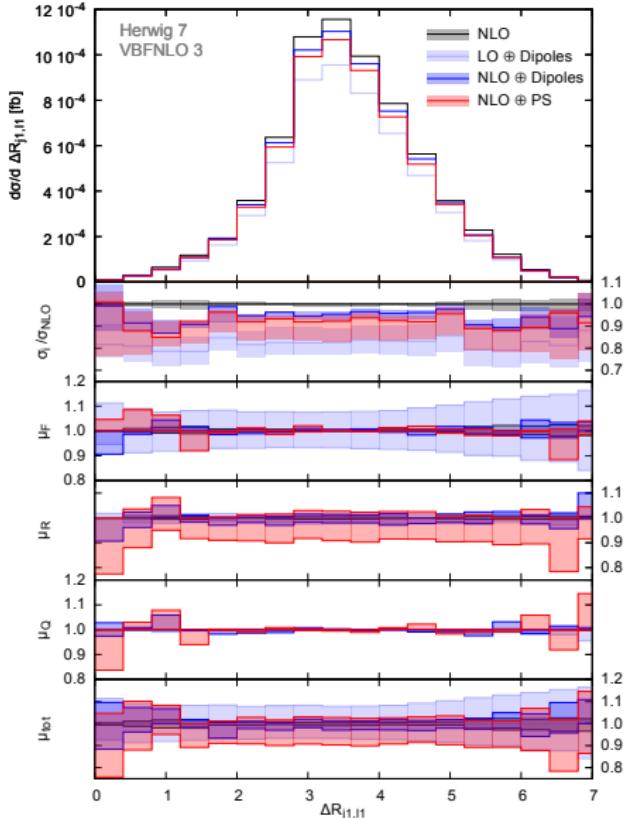
# Missing Transverse Momentum



# Transverse Momentum of Leading Lepton



# $R$ Separation of Leading Jet and Leading Lepton



$$\Delta R = \sqrt{\Delta y^2 + \Delta \phi^2}$$

Jacobian peak at  $\Delta R_{j1\ell 1} = \pi$