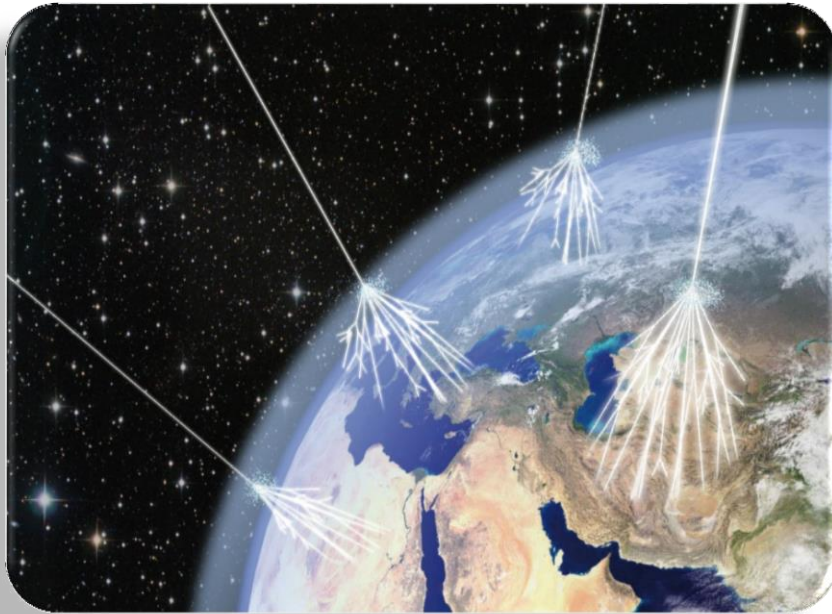


How can we get cosmic-rays from dark matter?

D. Kim & JCP [[arXiv:1507.07922](#)] & [[arXiv:1508.06640](#)],
K. Boddy, K. Dienes, D. Kim, J. Kumar, JCP & B. Thomas
[[arXiv:1606.07440](#)] & [[arXiv:1609.09104](#)]



Jong-Chul Park

CNU 충남대학교
CHUNGNAM NATIONAL UNIVERSITY

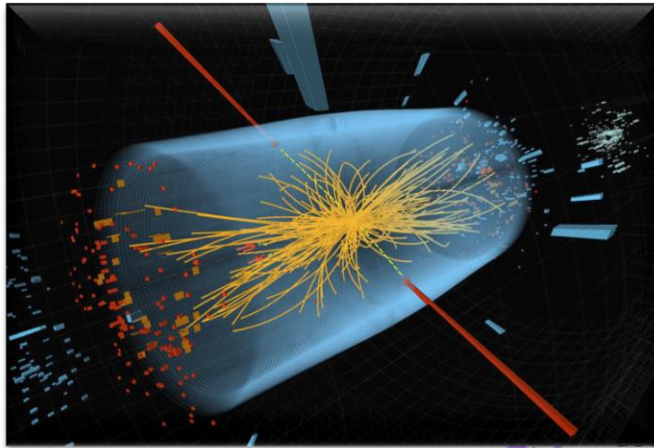
DM from aeV to ZeV: IBS-MultiDark-IPPP Workshop

November 24 (2016)

Standard Model (SM)

	<p>mass → $\approx 2.3 \text{ MeV}/c^2$</p> <p>charge → $2/3$</p> <p>spin → $1/2$</p> <p>u</p> <p>up</p>	<p>mass → $\approx 1.275 \text{ GeV}/c^2$</p> <p>charge → $2/3$</p> <p>spin → $1/2$</p> <p>c</p> <p>charm</p>	<p>mass → $\approx 173.07 \text{ GeV}/c^2$</p> <p>charge → $2/3$</p> <p>spin → $1/2$</p> <p>t</p> <p>top</p>	<p>mass → 0</p> <p>charge → 0</p> <p>spin → 1</p> <p>g</p> <p>gluon</p>
QUARKS	<p>mass → $\approx 4.8 \text{ MeV}/c^2$</p> <p>charge → $-1/3$</p> <p>spin → $1/2$</p> <p>d</p> <p>down</p>	<p>mass → $\approx 95 \text{ MeV}/c^2$</p> <p>charge → $-1/3$</p> <p>spin → $1/2$</p> <p>s</p> <p>strange</p>	<p>mass → $\approx 4.18 \text{ GeV}/c^2$</p> <p>charge → $-1/3$</p> <p>spin → $1/2$</p> <p>b</p> <p>bottom</p>	<p>mass → 0</p> <p>charge → 0</p> <p>spin → 1</p> <p>γ</p> <p>photon</p>
LEPTONS	<p>mass → $0.511 \text{ MeV}/c^2$</p> <p>charge → -1</p> <p>spin → $1/2$</p> <p>e</p> <p>electron</p>	<p>mass → $105.7 \text{ MeV}/c^2$</p> <p>charge → -1</p> <p>spin → $1/2$</p> <p>μ</p> <p>muon</p>	<p>mass → $1.777 \text{ GeV}/c^2$</p> <p>charge → -1</p> <p>spin → $1/2$</p> <p>τ</p> <p>tau</p>	<p>mass → $91.2 \text{ GeV}/c^2$</p> <p>charge → 0</p> <p>spin → 1</p> <p>Z</p> <p>Z boson</p>
		<p>mass → $< 2.2 \text{ eV}/c^2$</p> <p>charge → 0</p> <p>spin → $1/2$</p> <p>ν_e</p> <p>electron neutrino</p>	<p>mass → $< 0.17 \text{ MeV}/c^2$</p> <p>charge → 0</p> <p>spin → $1/2$</p> <p>ν_μ</p> <p>muon neutrino</p>	<p>mass → $< 15.5 \text{ MeV}/c^2$</p> <p>charge → 0</p> <p>spin → $1/2$</p> <p>ν_τ</p> <p>tau neutrino</p>
				GAUGE BOSONS

Standard Model (SM)



$\approx 1.275 \text{ GeV}/c^2$ 2/3 1/2 C charm	$\approx 173.07 \text{ GeV}/c^2$ 2/3 1/2 t top	0 0 1 g gluon	$\approx 126 \text{ GeV}/c^2$ 0 0 H Higgs boson
$\approx 95 \text{ MeV}/c^2$ -1/3 1/2 s strange	$\approx 4.18 \text{ GeV}/c^2$ -1/3 1/2 b bottom	0 0 1 γ photon	
$1.777 \text{ GeV}/c^2$ -1 1/2 τ tau	$91.2 \text{ GeV}/c^2$ 0 1 Z Z boson	GAUGE BOSONS	
$< 15.5 \text{ MeV}/c^2$ 0 1/2 ν_τ tau neutrino	$80.4 \text{ GeV}/c^2$ ± 1 1 W W boson		



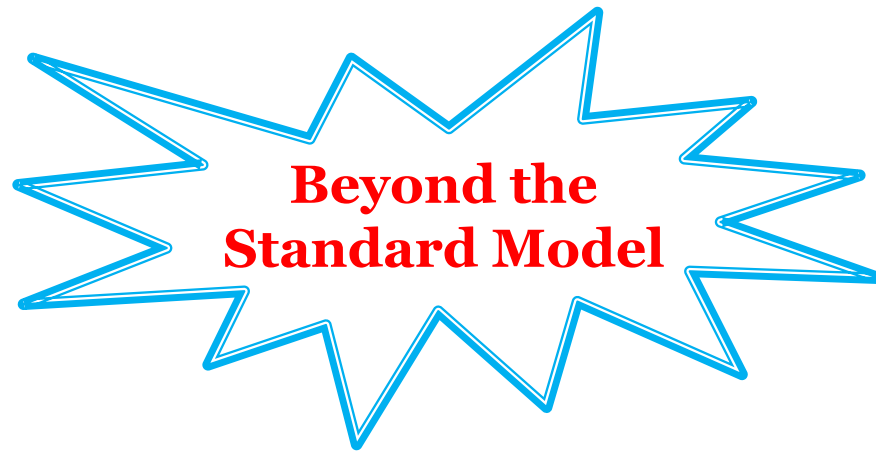


SM is not the end of the story



Need for New Physics

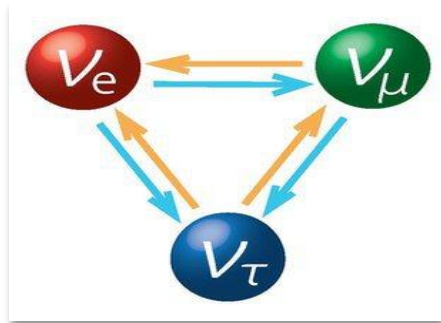
- ❖ On top of theory motivation, there are **real** & **hopefully-real** motivations for new physics.



Need for New Physics

- ❖ On top of theory motivation, there are **real** & **hopefully-real** motivations for new physics.

Neutrino

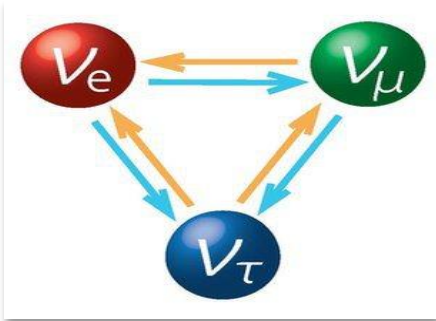


**Beyond the
Standard Model**

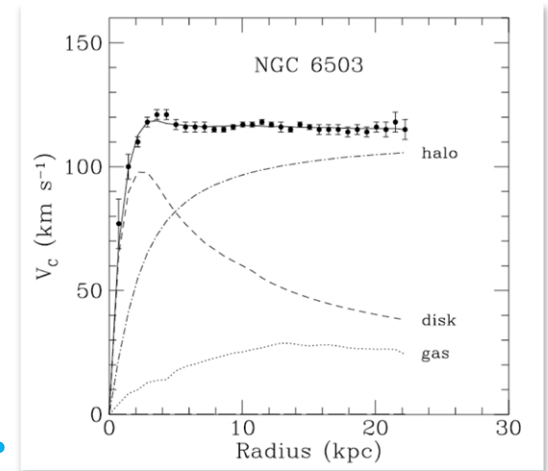
Need for New Physics

- ❖ On top of theory motivation, there are **real** & **hopefully-real** motivations for new physics.

Neutrino, Dark Matter



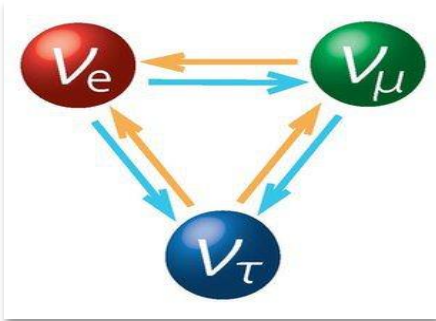
**Beyond the
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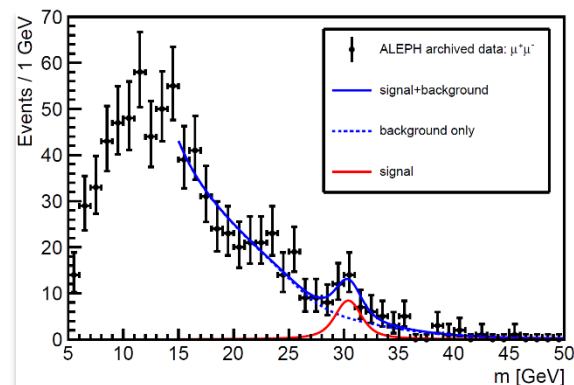
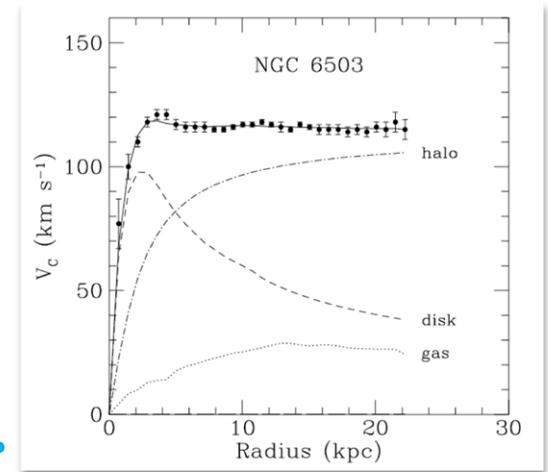
Need for New Physics

- ❖ On top of theory motivation, there are **real** & **hopefully-real** motivations for new physics.

Neutrino, Dark Matter, Collider



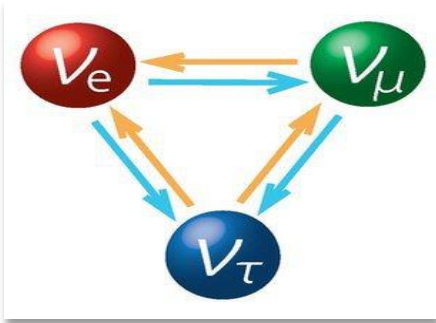
**Beyond the
Standard Model**



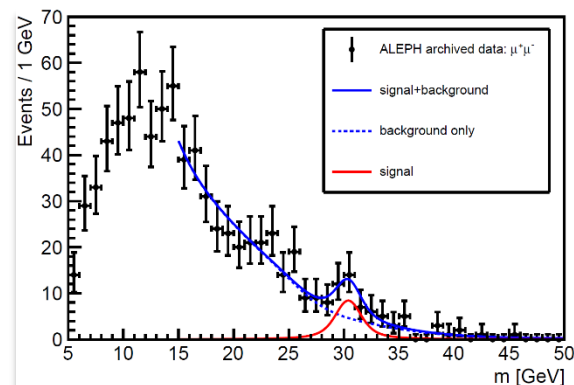
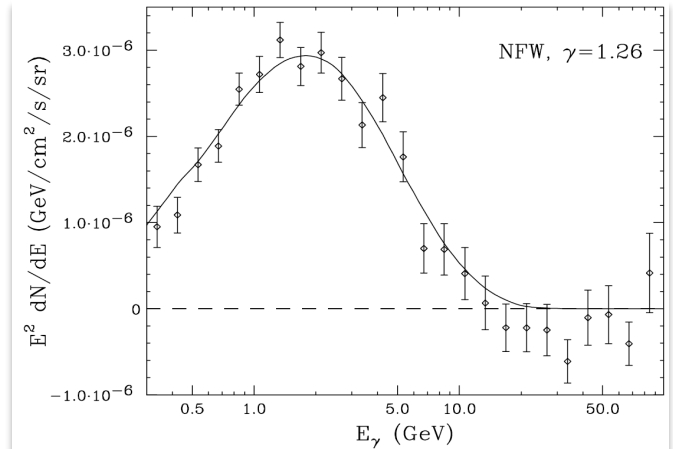
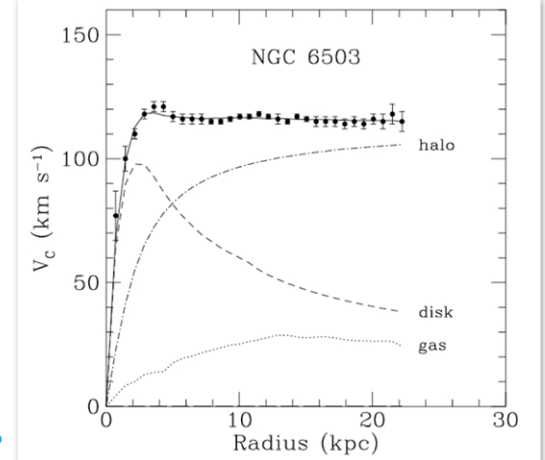
Need for New Physics

- ❖ On top of theory motivation, there are **real** & **hopefully-real** motivations for new physics.

Neutrino, Dark Matter, Collider, Cosmic-Ray



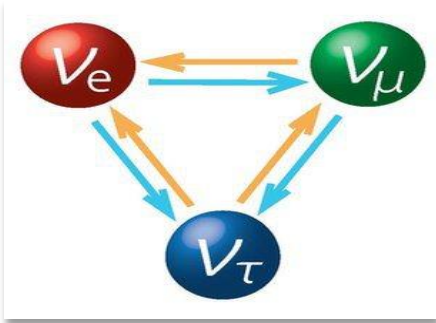
**Beyond the
Standard Model**



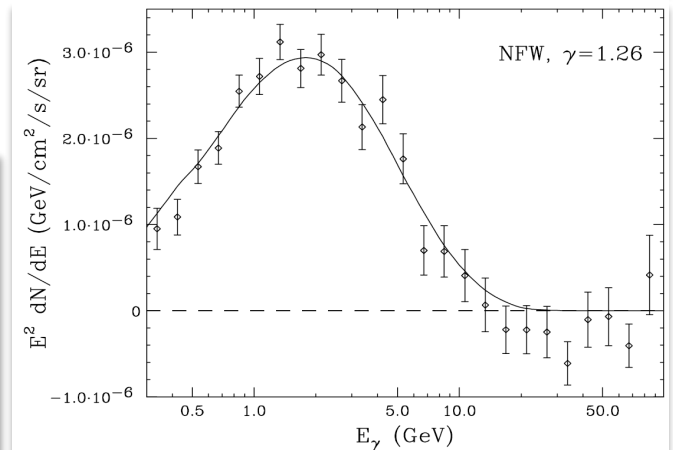
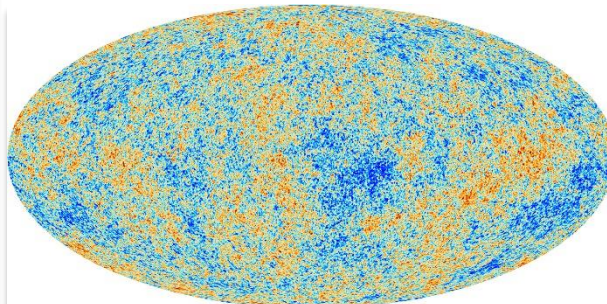
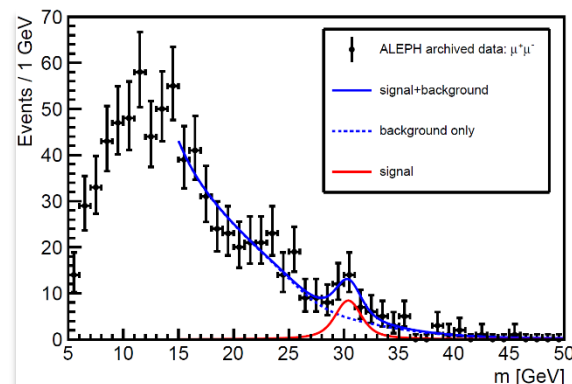
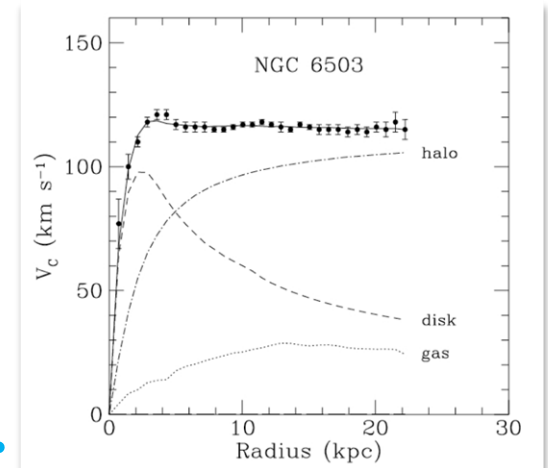
Need for New Physics

- ❖ On top of theory motivation, there are **real** & **hopefully-real** motivations for new physics.

Neutrino, Dark Matter, Collider, Cosmic-Ray, Cosmology, ...



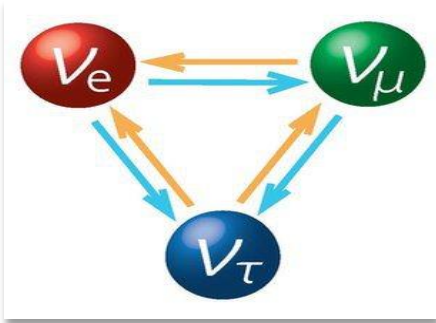
**Beyond the
Standard Model**



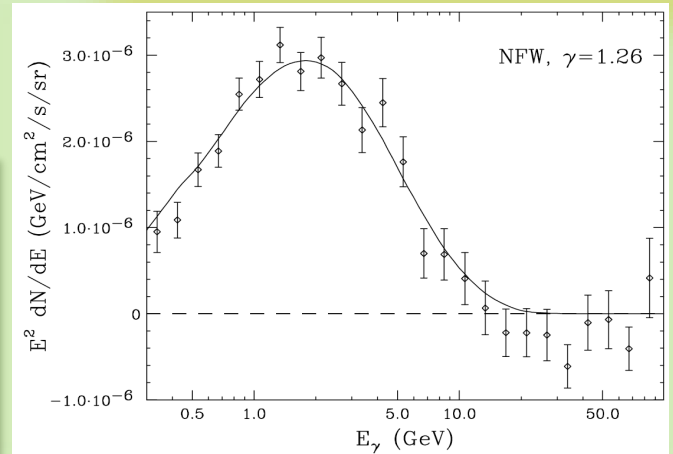
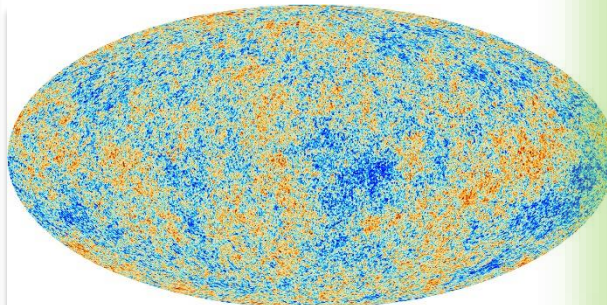
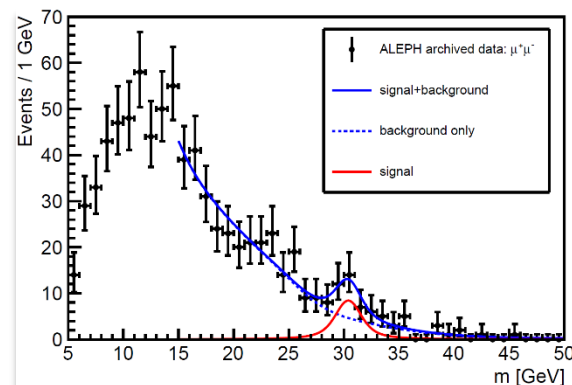
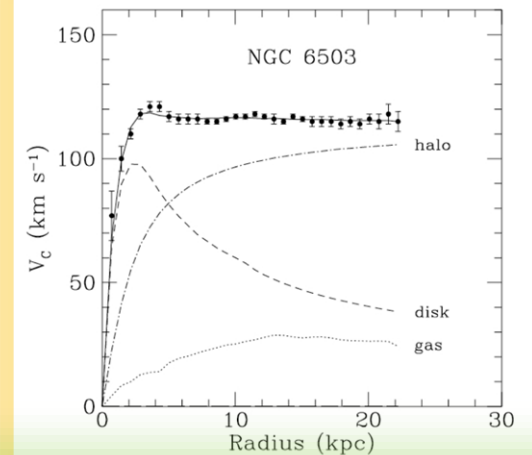
Need for New Physics

- ❖ On top of theory motivation, there are **real** & **hopefully-real** motivations for new physics.

Neutrino, **Dark Matter**, **Collider**, **Cosmic-Ray**, **Cosmology**, ...

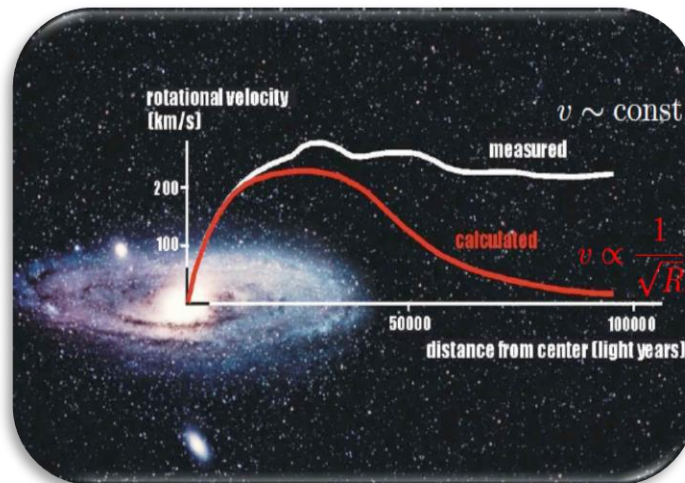


**Beyond the
Standard Model**

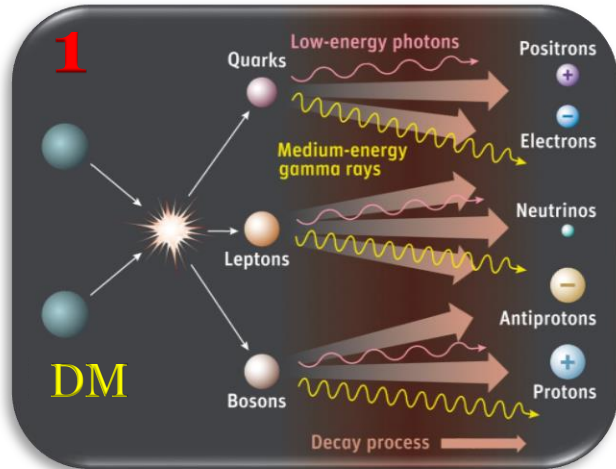


Dark Matter (DM)

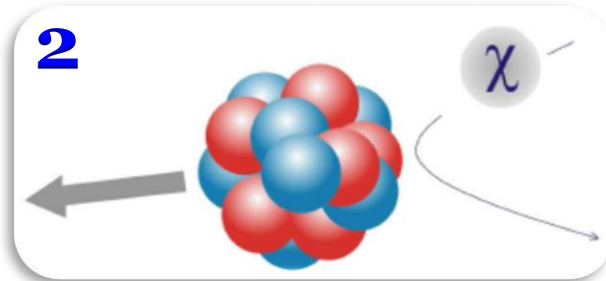
- ❖ **DM**: ~25% of our Universe
- ❖ **Compelling paradigm**:
massive, non-luminous & stable particles
- ❖ **Evidence**
 - ✓ Galaxy rotation curve
 - ✓ Bullet cluster
 - ✓ Gravitational lensing
 - ✓ Structure formation
 - ✓ CMB
 - ✓ Coma Cluster
 - ✓ Sky surveys
 - ✓ ...



DM Search Strategies



Today!

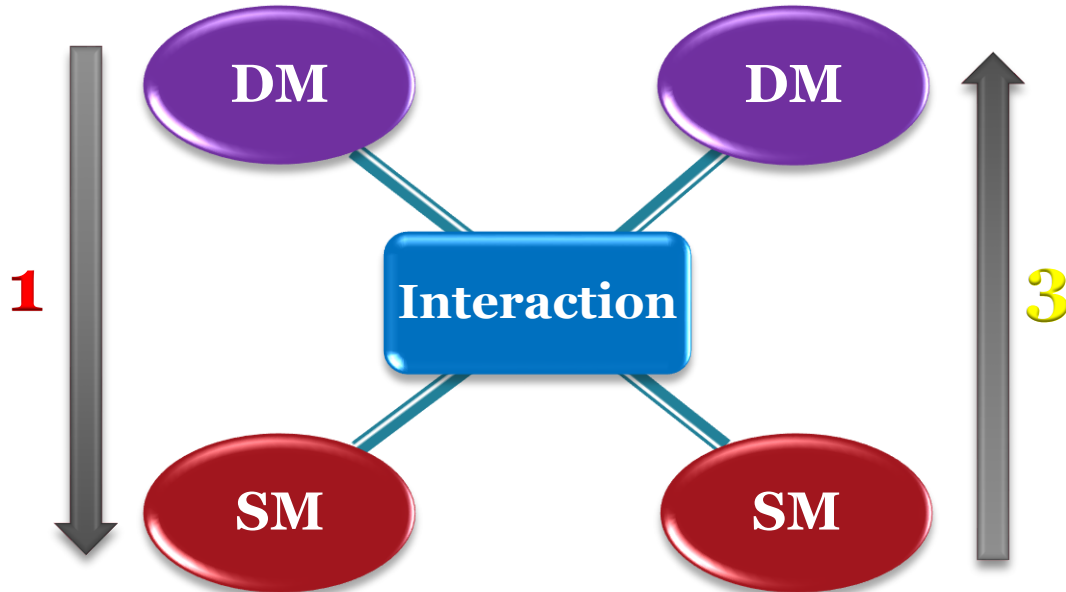


Wednesday

2



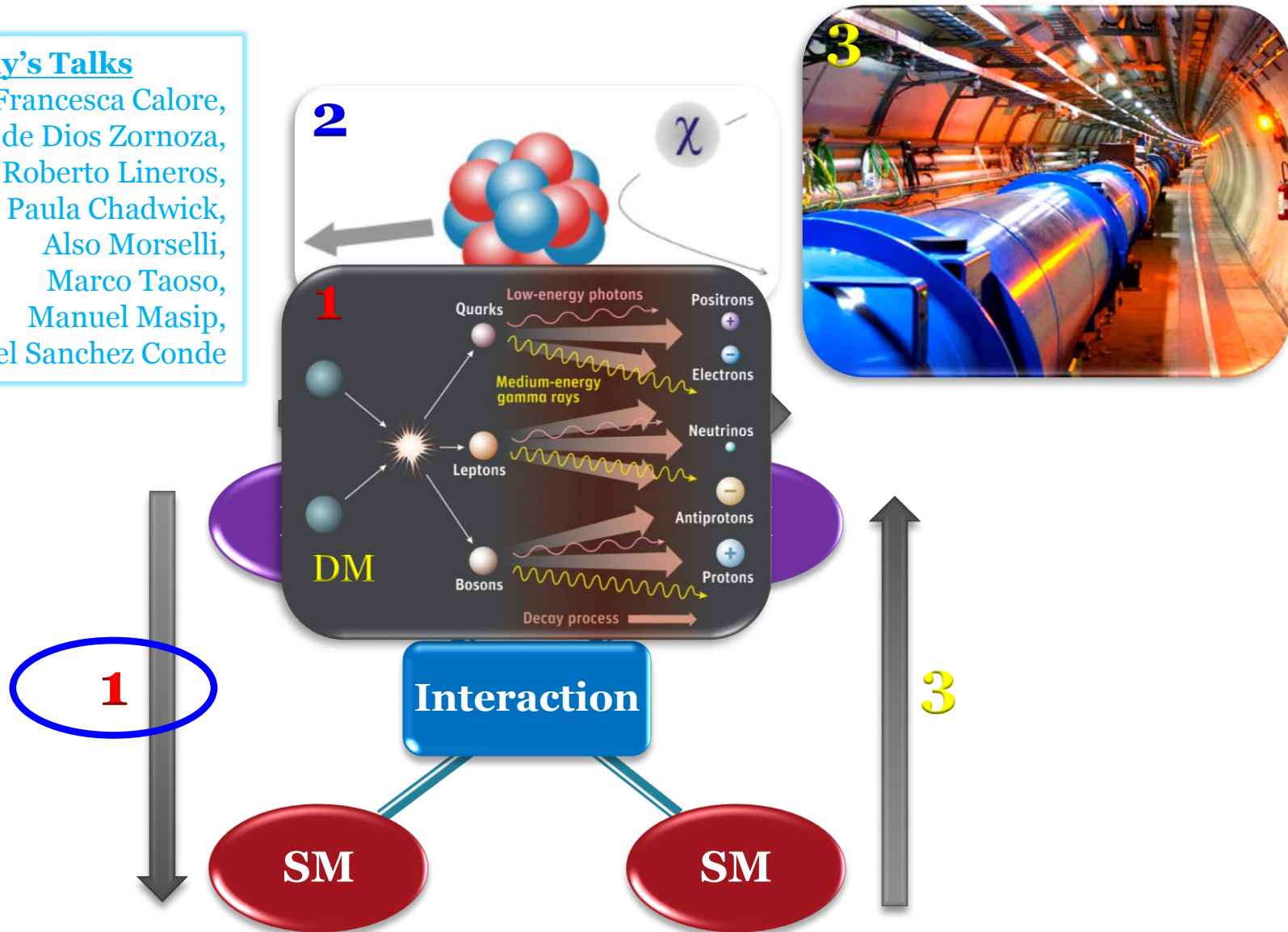
Tuesday



Indirect Detection: Cosmic-Rays

Today's Talks

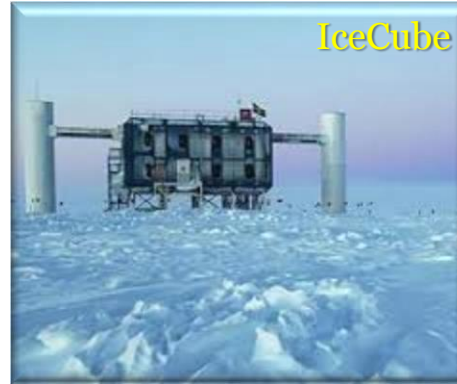
Francesca Calore,
Juan de Dios Zornoza,
Roberto Lineros,
Paula Chadwick,
Also Morselli,
Marco Taoso,
Manuel Masip,
Miguel Angel Sanchez Conde



Cosmic-Ray Experiments

❖ Ground-based

MAGIC, HESS, CTA, IceCube, Super-K, Hyper-K, ...

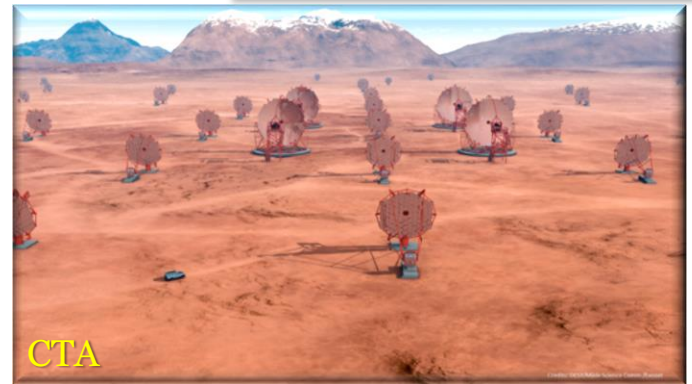


❖ Balloon-based:

ATIC, PPB-BETS, ...

❖ Satellite-based:

AMS, Chandra, Fermi-LAT, PAMELA, XMM-Newton, Hitomi, ASTROGAM, ...



✓ **Great sensitivity** to cosmic-ray signals

✓ Better chance to have the information for

extracting DM properties



Hints from Cosmic-Rays?

❖ **Anomalies** in cosmic-ray measurements \Leftrightarrow **DM signature** ?

- SPI/INTEGRAL ($\gamma \rightarrow e^+$): 511 keV line
- PAMELA (e^\pm, p^\pm, \dots): e^+ excess
- ATIC (e^-e^+): e^-e^+ excess
- Fermi-LAT (e^-e^+, γ): e^-e^+ excess, 130 GeV line, GeV excess
- AMS-02 (e^\pm, p^\pm, \dots): e^+ excess
- XMM-Newton (X-ray): 3.5 keV line
- IceCube (ν): PeV events
- ...

Today's Talks

Francesca Calore,
Juan de Dios Zornoza,
Roberto Lineros,
Paula Chadwick,
Also Morselli,
Marco Taoso,
Manuel Masip,
Miguel Angel Sanchez Conde

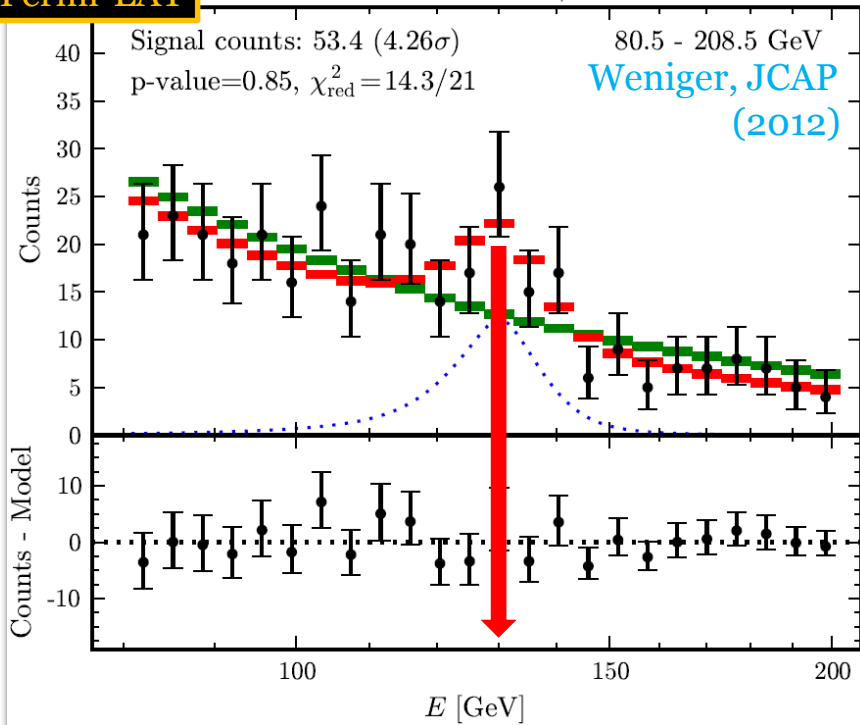
Conventional Approaches



Line-like Excesses

Fermi-LAT

Reg3 (ULTRACLEAN), $E_\gamma = 129.6$ GeV



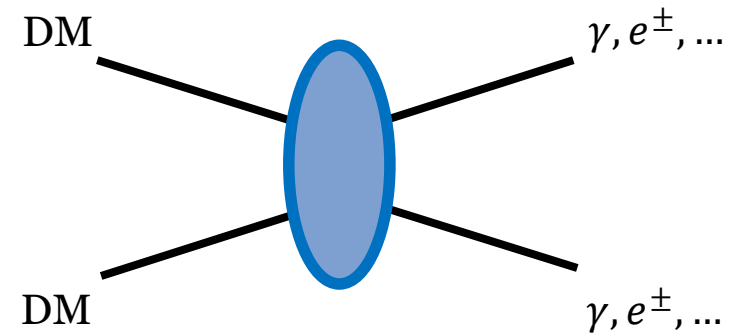
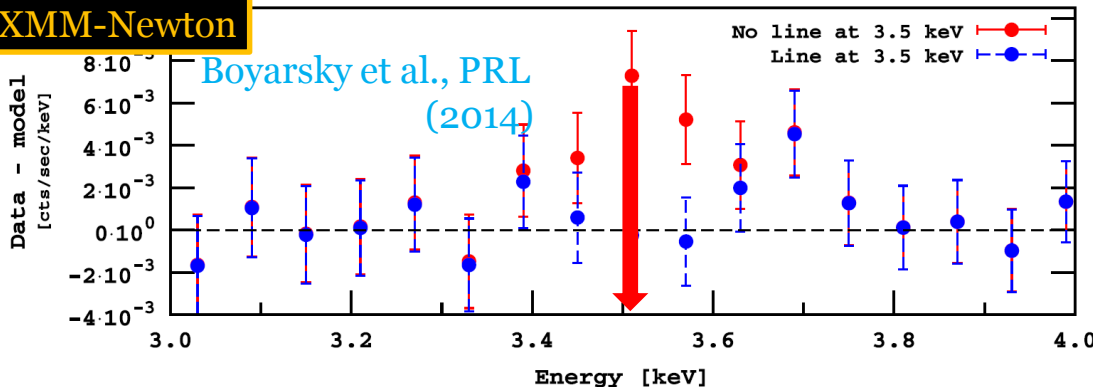
❖ 3.5 keV line, 511 keV line, 130 GeV line, ...

❖ Typical DM interpretation

- ✓ DM: **directly** annihilates/decays into **2 (stable) SM particles**, $\gamma + X$
- ✓ **The location of the line** is identified as **the (double) mass of DM**
- ✓ Width of the line is instrumental

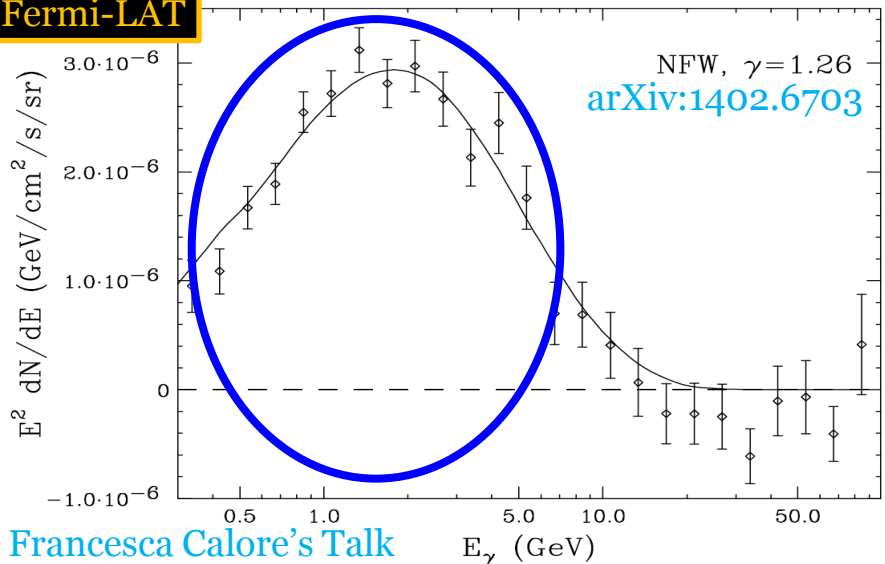
XMM-Newton

Boyarsky et al., PRL (2014)



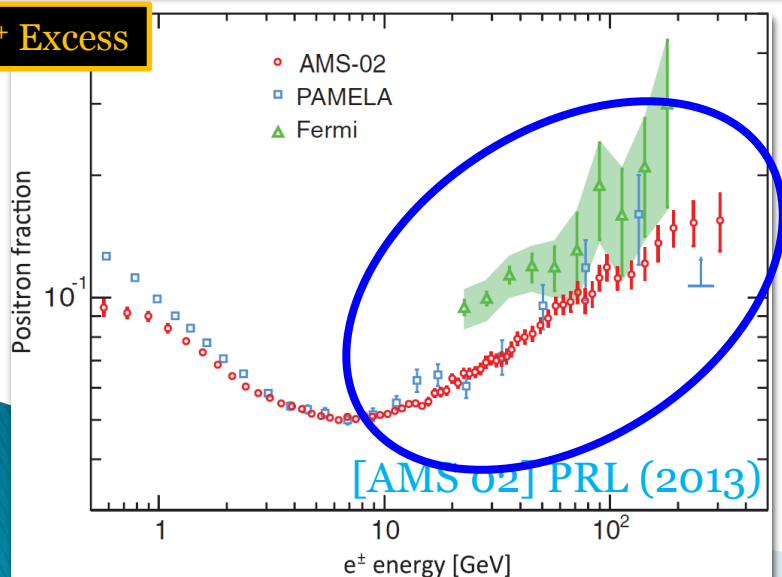
Bump-Like Excesses

Fermi-LAT



Francesca Calore's Talk

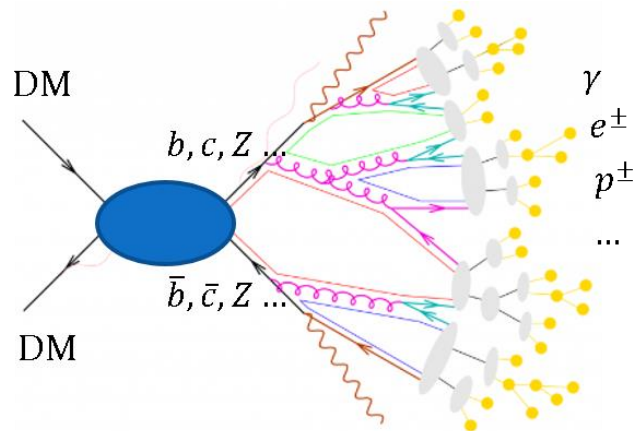
e^\pm Excess



❖ GC GeV γ -ray excess, e^\pm excess, ...

❖ Typical DM interpretation

- ✓ DM: **directly** annihilates/decays into **2 (unstable) SM particles** which further goes to stable SM particles through secondary processes
- ✓ **Diffusion mechanism** for **charged particles**
- ✓ **Shape information** (including the peak position): **highly model-dependent**



Minimal vs Non-minimal

❖ Scenario with a single DM species

- ✓ **Simplest** & **well-motivated** scenario
- ✓ Stability of DM ensured (typically) by a discrete symmetry
- ✓ **Popular models** having a single type of DM candidate:
 - SUSY models with R-parity
 - Extra-D models with KK-parity
 - Little Higgs models with T-parity

Minimal vs Non-minimal

- ❖ Scenario with multiple DM species
 - ✓ Nothing stops from having more stable particles
 - Visible sector (SM) has many stable particles
 - Rising interest in non-minimal scenarios

Minimal vs Non-minimal

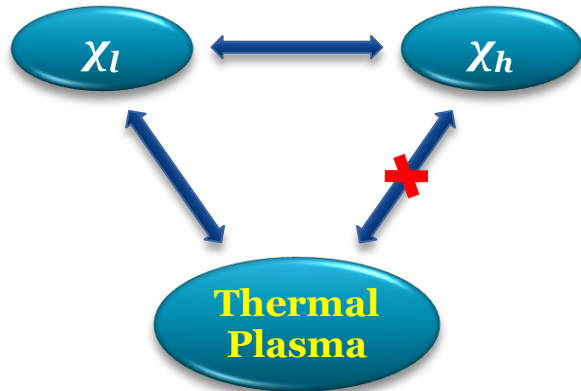
❖ Scenario with multiple DM species

✓ **Nothing stops** from **having more stable particles**

- Visible sector (SM) has many stable particles

- **Rising interest** in non-minimal scenarios

✓ Assisted freeze-out



E. J. Chun & JCP (2011)

G. Belanger & JCP (2011)

Minimal vs Non-minimal

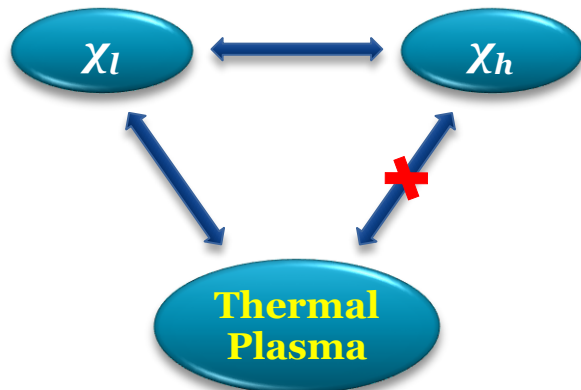
❖ Scenario with multiple DM species

✓ **Nothing stops** from **having more stable particles**

- **Visible sector (SM)** has many stable particles

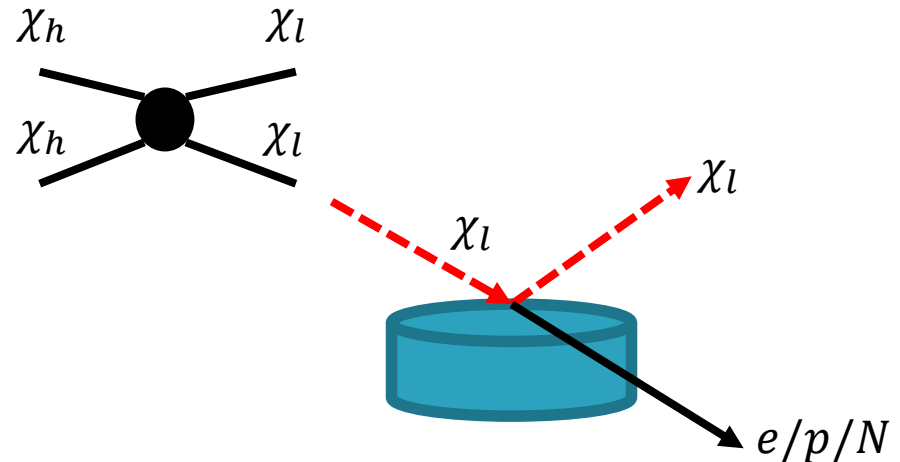
- **Rising interest** in non-minimal scenarios

✓ Assisted freeze-out



E. J. Chun & **JCP** (2011)
G. Belanger & **JCP** (2011)

✓ Boosted DM



K. Agashe, Y. Cui, L. Necib, J. Thaler (2014)
KC Kong, G. Mohlabeng & **JCP** (2014)
H. Alhazmi, KC Kong, G. Mohlabeng & **JCP** (2016)

Minimal vs Non-minimal

❖ Scenario with multiple DM species: Dynamical DM framework

- ✓ DDM framework: the dark sector comprises a potentially vast **ensemble of individual particle species** χ_n whose cosmological abundances Ω_n are balanced against their decay width Γ_n in such a way as to ensure consistency with observational data.

K. Dienes & B. Thomas (2011)

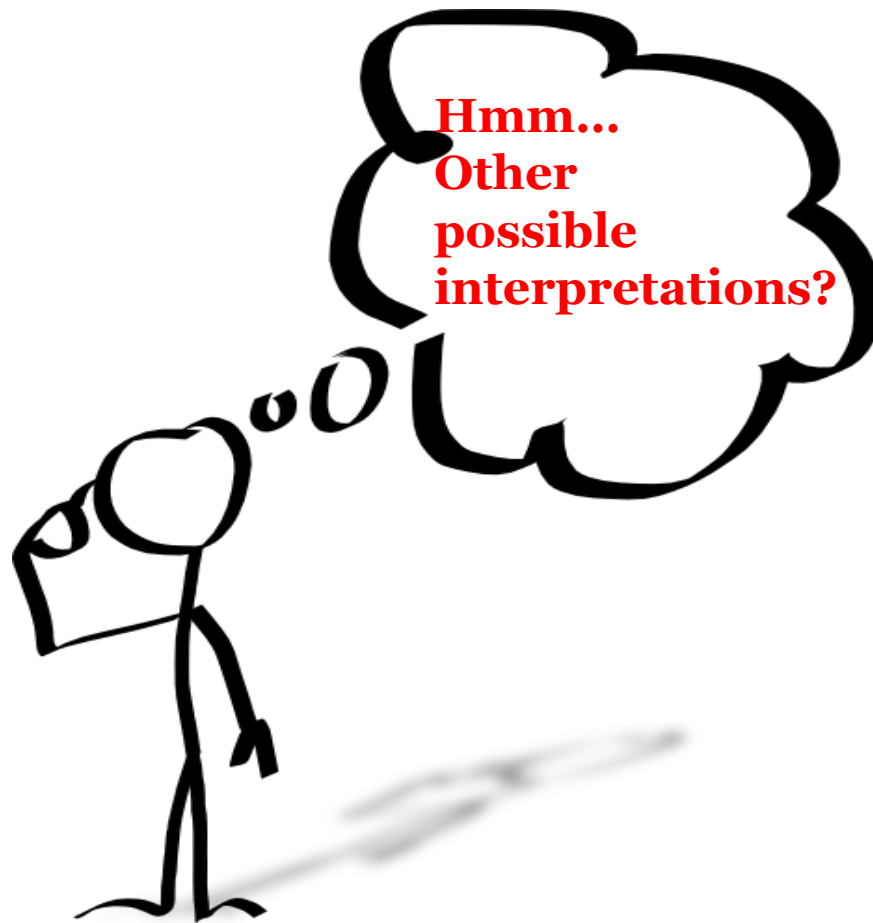
- ✓ Mass parameters (generic parameterization)

$$m_n = m_0 + n^\delta \Delta m$$

δ : mass scaling parameter, Δm : mass splitting/gap

- ✓ Parameterizing the fluxes Φ_n by a single power law with a scaling parameter ξ

$$\Phi_n = \Phi_0 \left(\frac{m_n}{m_0} \right)^\xi = \Phi_0 \left(\frac{\sqrt{s_n}}{\sqrt{s_0}} \right)^\xi$$



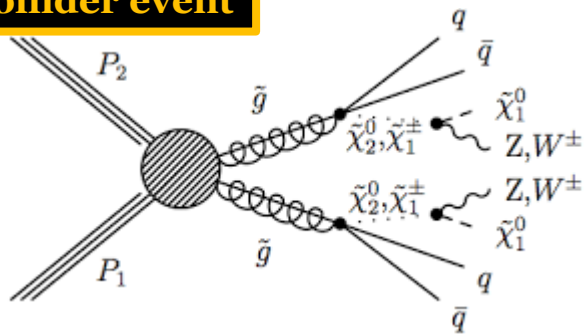
**Hmm...
Other
possible
interpretations?**

Energy Peak in Cosmic-Rays

❖ With **DM interpretation** in mind, we propose **alternative mechanisms** based on the observation of the “**Energy-Peak**” in **collider physics** to explain **cosmic-ray excesses**.

❖ Why E-Peak?

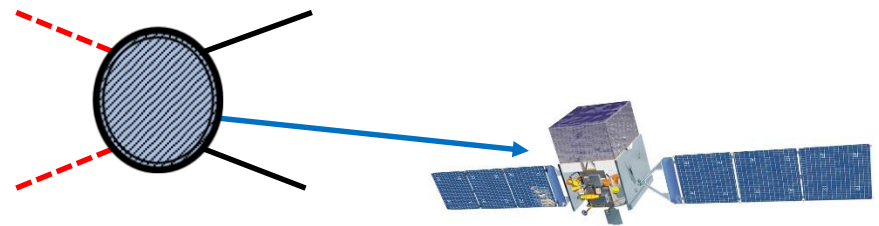
A collider event



- Large multiplicity
- Momentum w.r.t. the beam line

✓ **Unique spectral features** from 1st principle irrespective of underlying DM model details
(vs. **highly model-dependent** in the conventional interpretation)

A DM indirect detection event



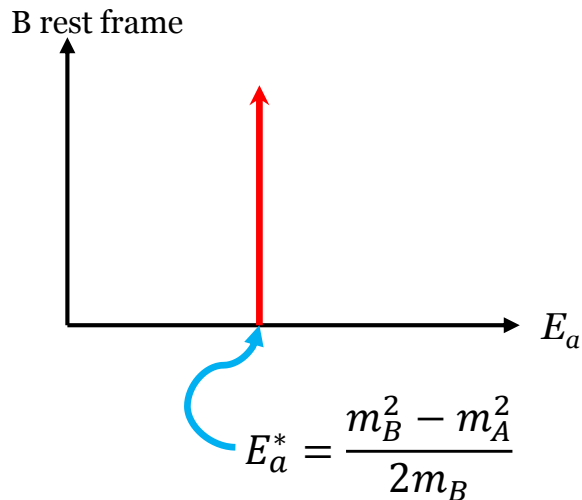
- **Energy** is the **only** available quantity

E-Peak: a Quick Review

● Two-body decay kinematics

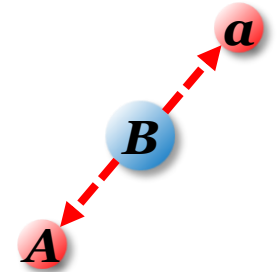
A simple 2-body decay of a heavy resonance B into A and massless visible a

- Energy of visible particle a is
monochromatic & simple
function of masses



- E_a^* measured & m_A known,
→ m_B determined, vice versa

Rest frame of B

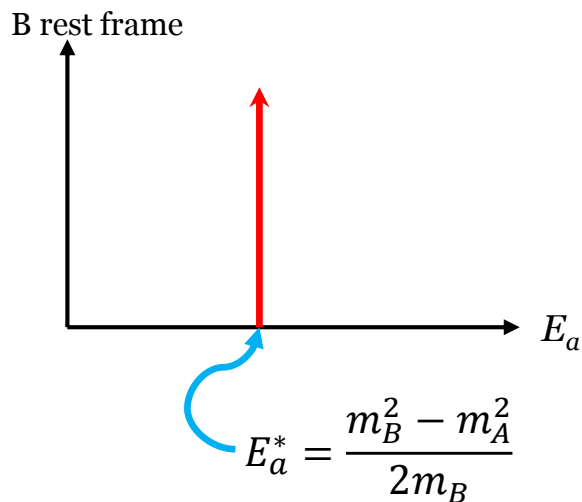
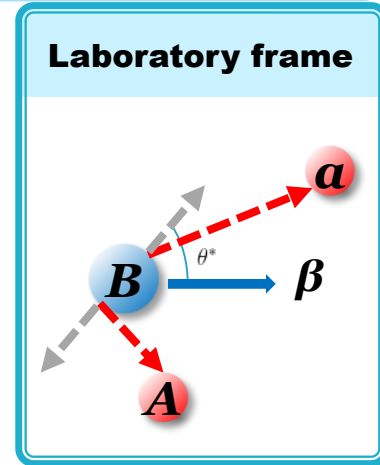


E-Peak: a Quick Review

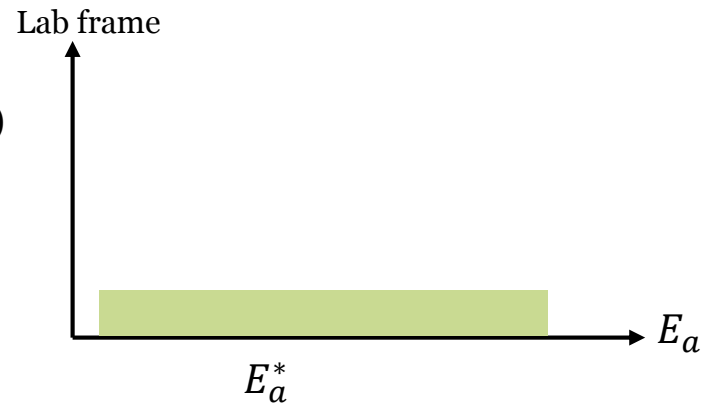
● Two-body decay kinematics

A simple 2-body decay of a heavy resonance B into A and massless visible a

- Energy of visible particle a is **monochromatic & simple** function of masses



$$E_a = E_a^* \gamma (1 + \beta \cos \theta^*)$$



- E_a^* measured & m_A known,
→ m_B determined, vice versa

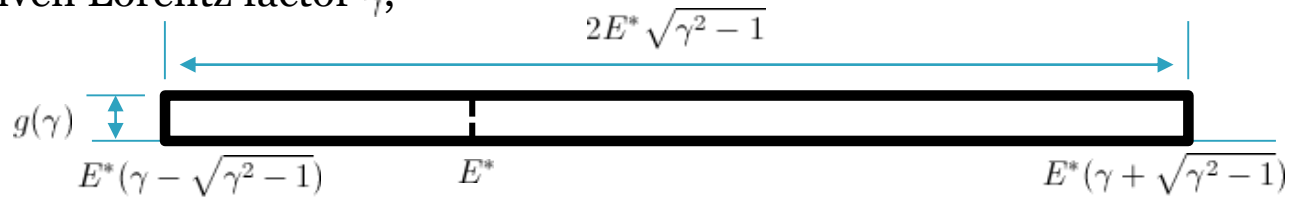
- Rectangular spectrum containing E_a^* for any B boost γ

E-Peak: a Quick Review

● “stacking up” rectangles

$$E = E^* \gamma (1 + \beta \cos \theta^*) = E^* (\gamma + \sqrt{\gamma^2 - 1} \cos \theta^*)$$

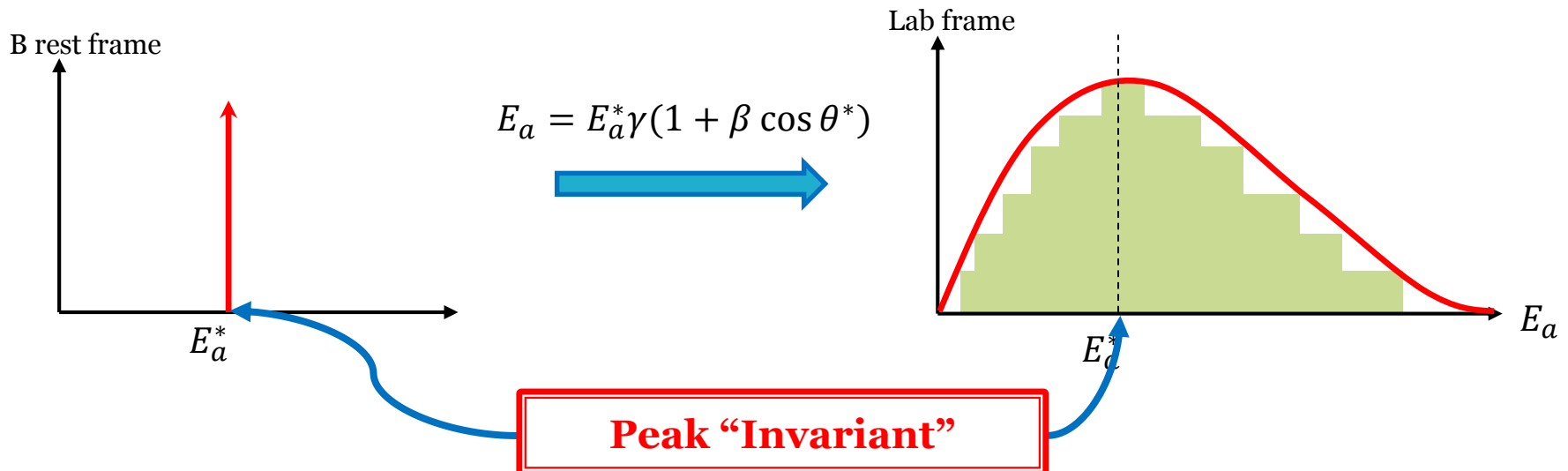
- For any given Lorentz factor γ ,



- Distribution in $E \rightarrow$ summing up the contributions from all relevant boost factors

\rightarrow “**Stacking up**” rectangles weighted by boost distribution of particle B

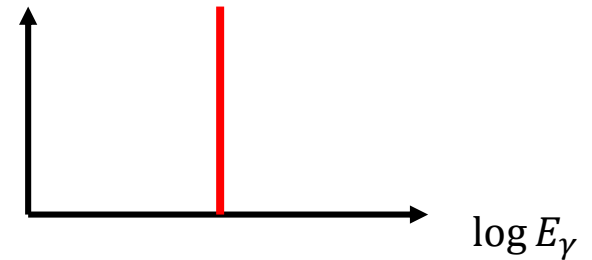
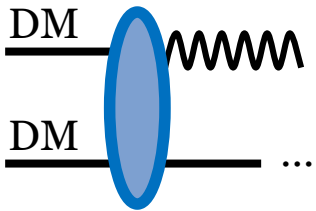
- Energy distribution has a unique **peak** at $E=E^*$



Applications

Dark Sector Cascade

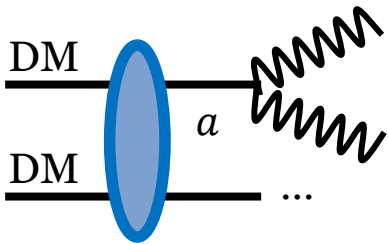
● o-step cascade



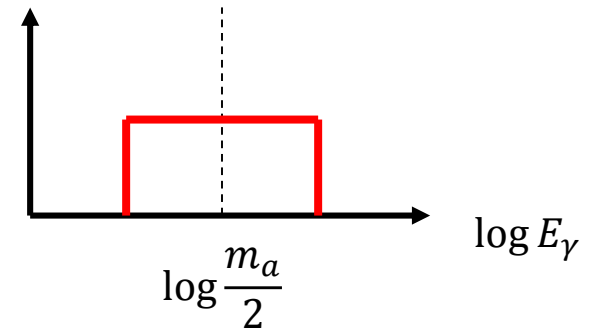
- ❑ Simplest and conventional model
- ❑ Featured by a sharp peak

Dark Sector Cascade

● 1-step cascade

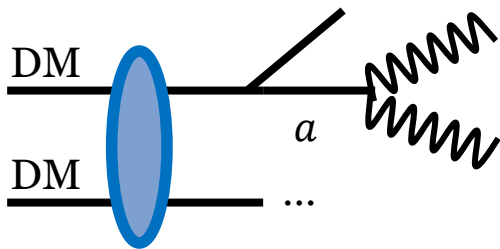


- ❑ Introducing an **on-shell intermediary state** directly decaying into two photons (e.g. dark pion, ALP)
- ❑ Featured by a **box-like** distribution

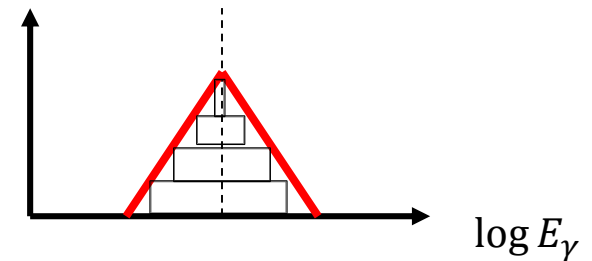
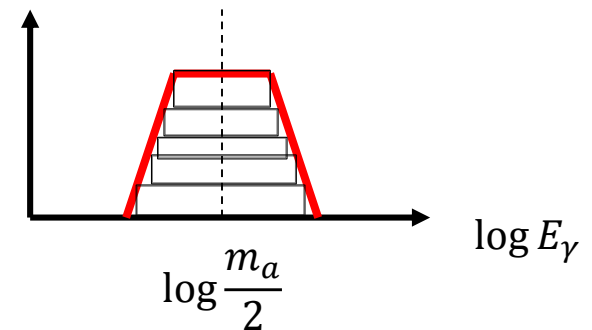


Dark Sector Cascade

2-step cascade



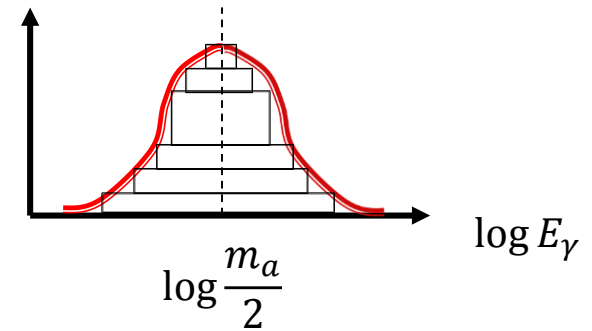
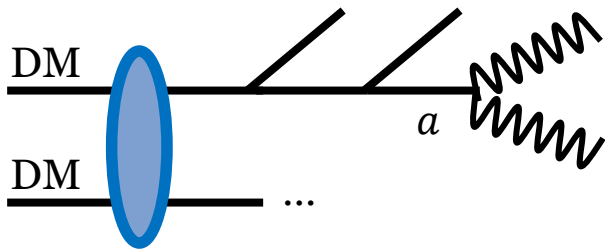
- ❑ Introducing an **on-shell intermediary** state before the state decaying into two photons
- ❑ Developing a **plateau** or a **peak** depending on model details
- ❑ Morphologically constrained: **analytic expression** for the shape available
- ❑ **Alternative mechanism** for **cosmic-ray peaks**
e.g. 130 GeV/3.5 keV lines
D. Kim & **JCP** [PLB (2015)]



Later

Dark Sector Cascade

● 3-step cascade

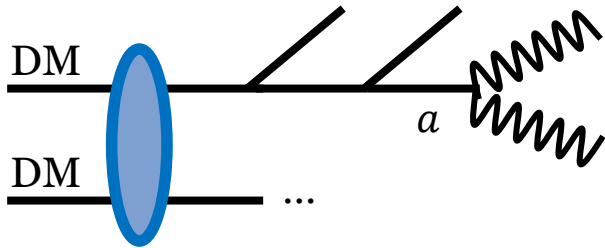


- ❑ Introducing **one more on-shell intermediary** state before the state decaying into two photons
- ❑ Developing a **smoothly rising-and-falling shape**
- ❑ Generic distribution function:

$$f(E_\gamma) \propto \exp\left[-\frac{w}{2} \left(\frac{E_\gamma}{E_\gamma^*} + \frac{E_\gamma^*}{E_\gamma}\right)^p\right]$$

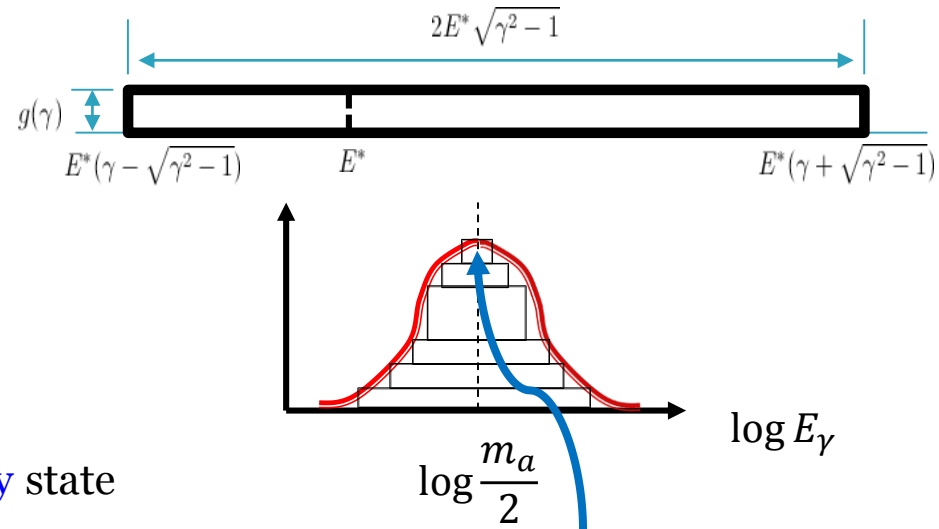
Dark Sector Cascade

3-step cascade



- ❑ Introducing **one more on-shell intermediary** state before the state decaying into two photons
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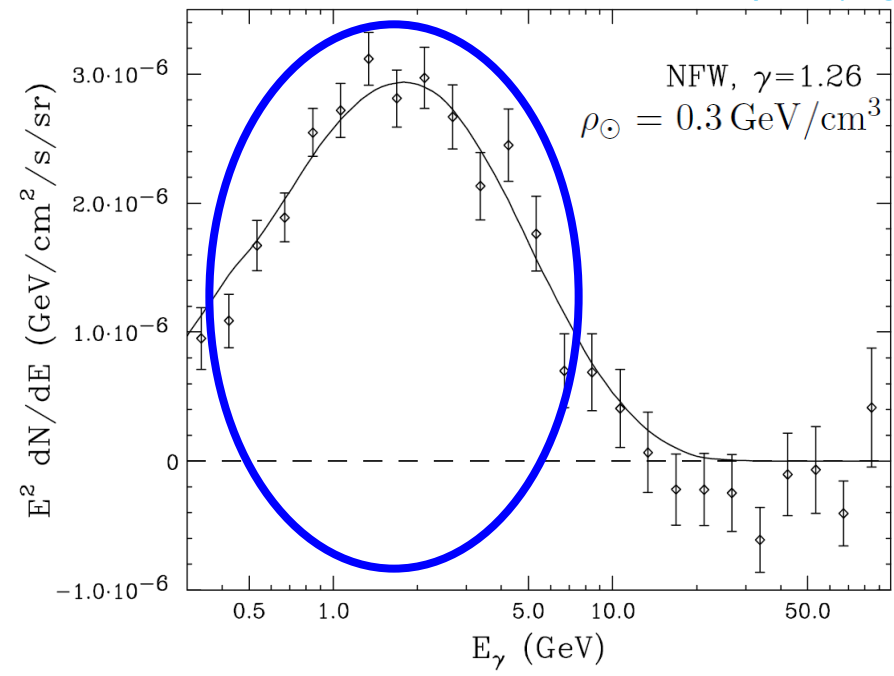
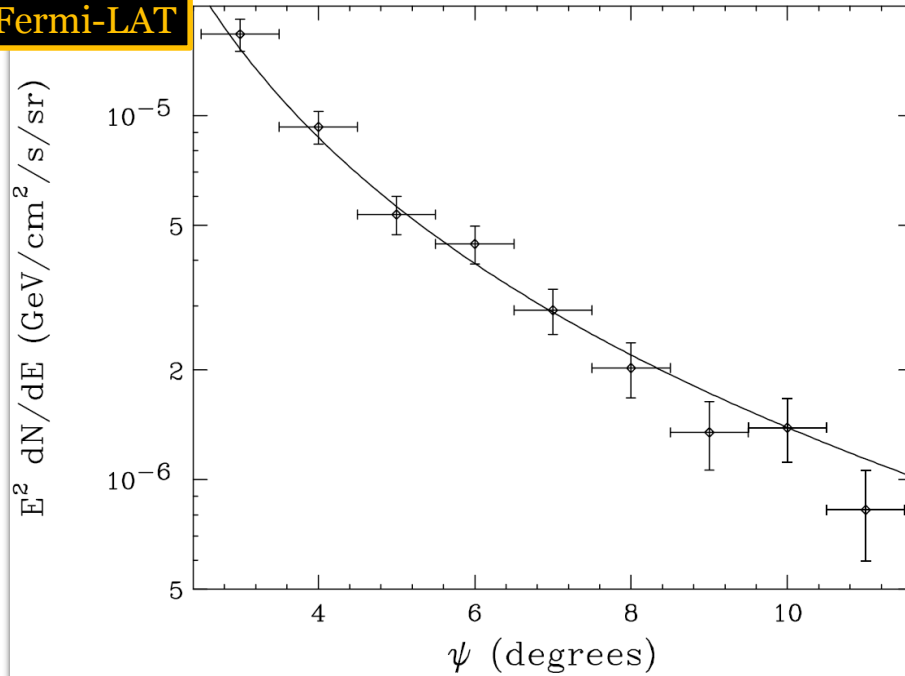
**Symmetric w.r.t the peak
in logarithmic E_γ**

$$(E^*)^2 = E_\gamma^+ E_\gamma^-$$

Bump: Features of GeV Excess

arXiv:1402.6703

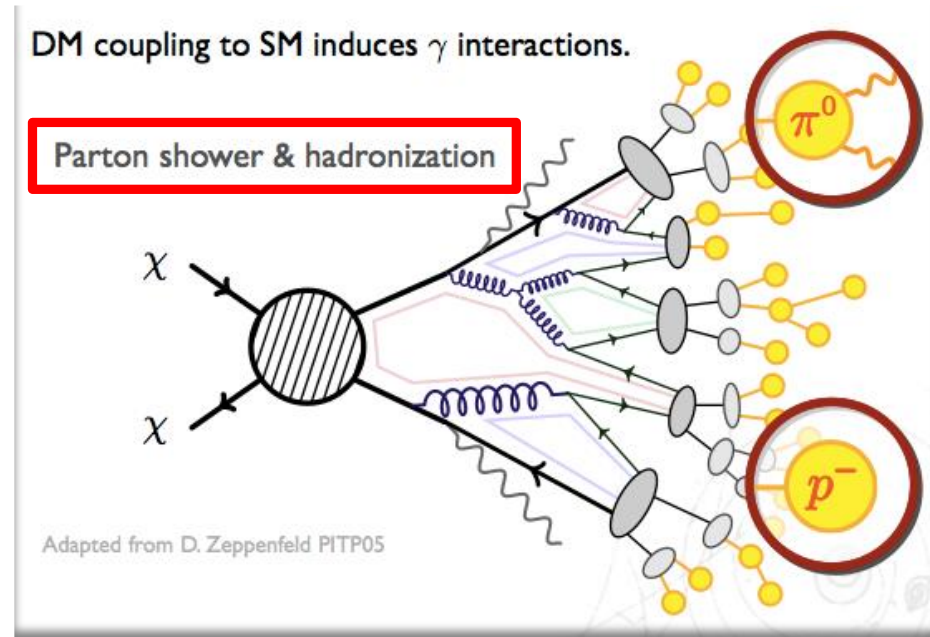
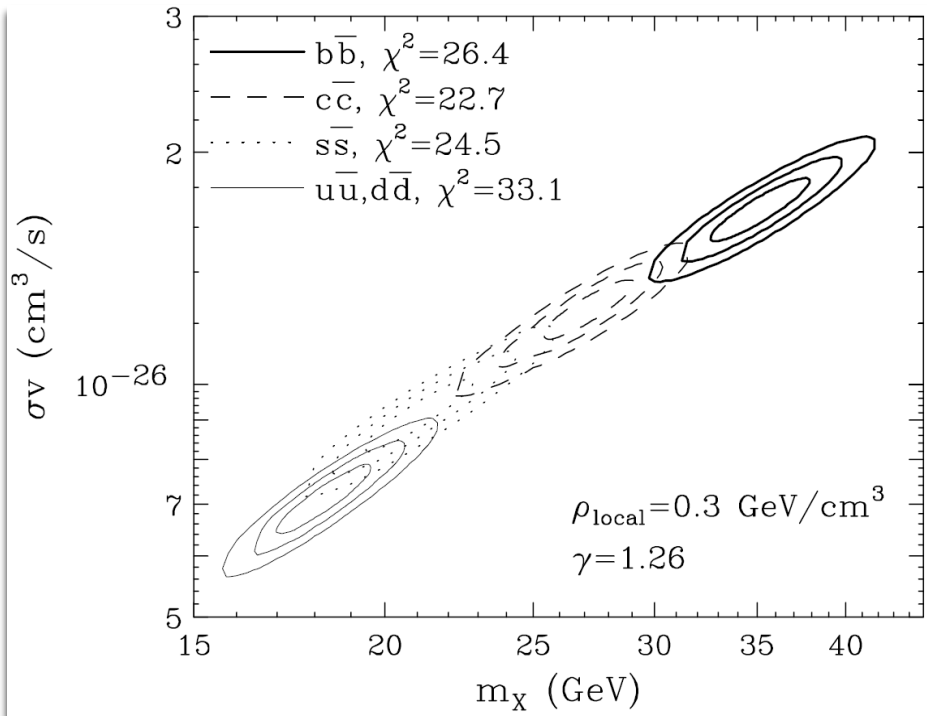
Fermi-LAT



- ❖ **Signal: extended to $> 10^\circ$** from the GC
- ❖ Consistent with the **dynamical center** of the **Milky Way ($< 0.05^\circ$)**
- ❖ The spectrum of the excess **peaks at 1-3 GeV**.

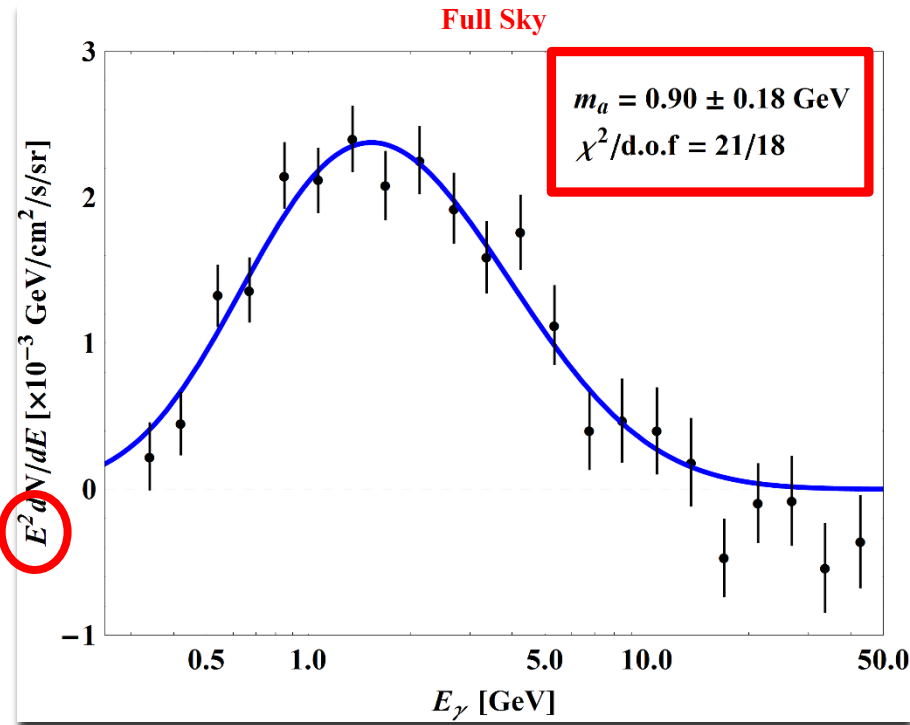
Bump: Conventional Approach

arXiv:1402.6703

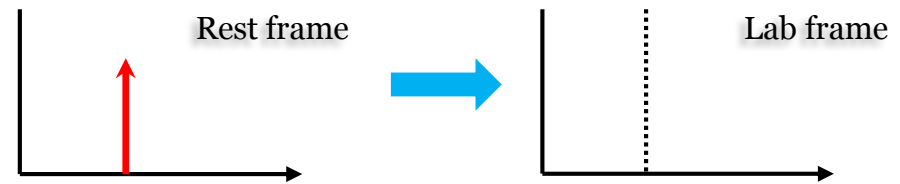
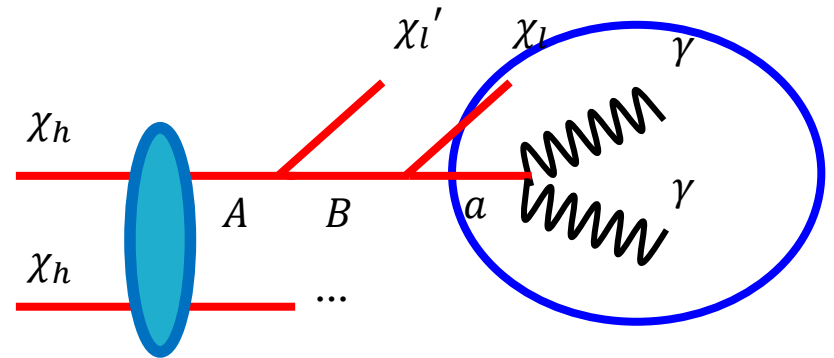


- ❖ The spectrum is in **good agreement** with the predictions from **20-40 GeV DM mostly annihilating to quarks** (fragmentation, IC, bremsstrahlung, ...).
- ❖ Required cross section is $\sim 0.7-2.1 \cdot 10^{-26} \text{ cm}^3/\text{s}$

Dark Cascade: GeV γ -ray Bump



➤ Multi-step cascade decay!



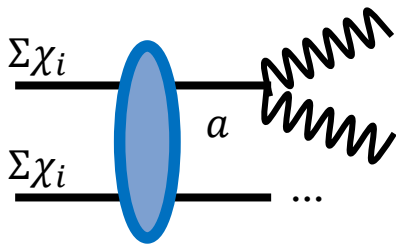
➤ Fitting function: $f_M(E_\gamma) = N \exp \left[-\frac{w}{2} \left(\frac{E_\gamma}{E_\gamma^*} + \frac{E_\gamma^*}{E_\gamma} \right)^p \right]$ with $E_\gamma^* = m_a/2$

➤ cf. [arXiv:1402.6703](https://arxiv.org/abs/1402.6703) (bb) $\rightarrow \chi^2/\text{d.o.f.} = 44/20$ with $m_{\text{DM}} = 36.6 \text{ GeV}$

Multi-Component DM Models

● Mechanism

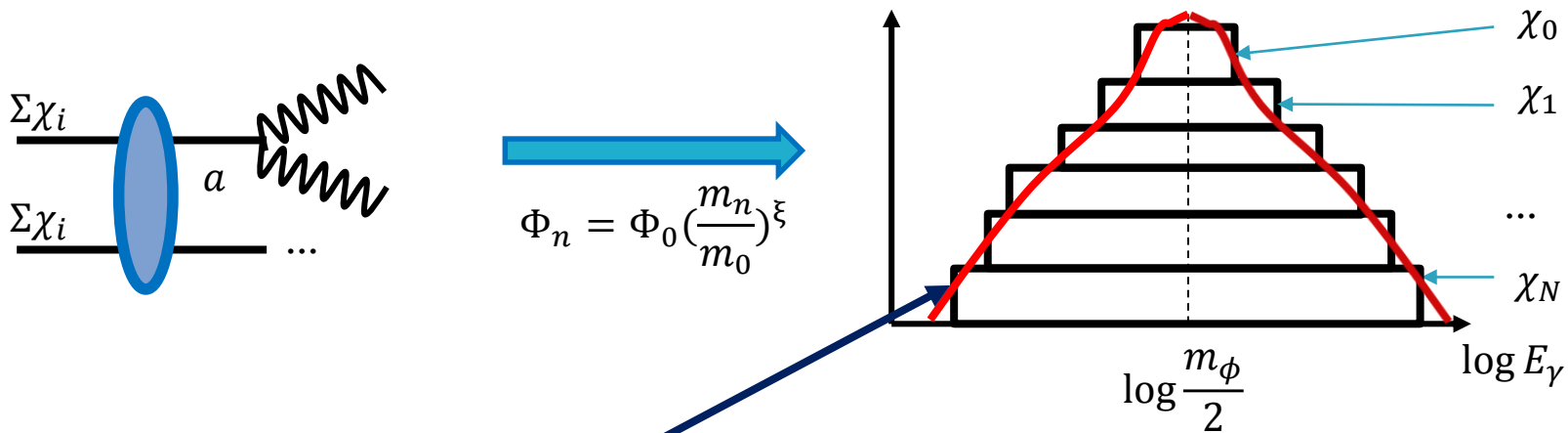
- What if there exist **multiple DM species**? What if the **collection of DM particles** have sufficiently small mass gaps (smaller than relevant energy resolution)?



Multi-Component DM Models

● Mechanism

- ❑ What if there exist **multiple DM species**? What if the **collection of DM particles** have sufficiently small mass gaps (smaller than relevant energy resolution)?
- ❑ Obtaining continuum energy spectra not by cascade decays, but by **increasing the number of DM species**

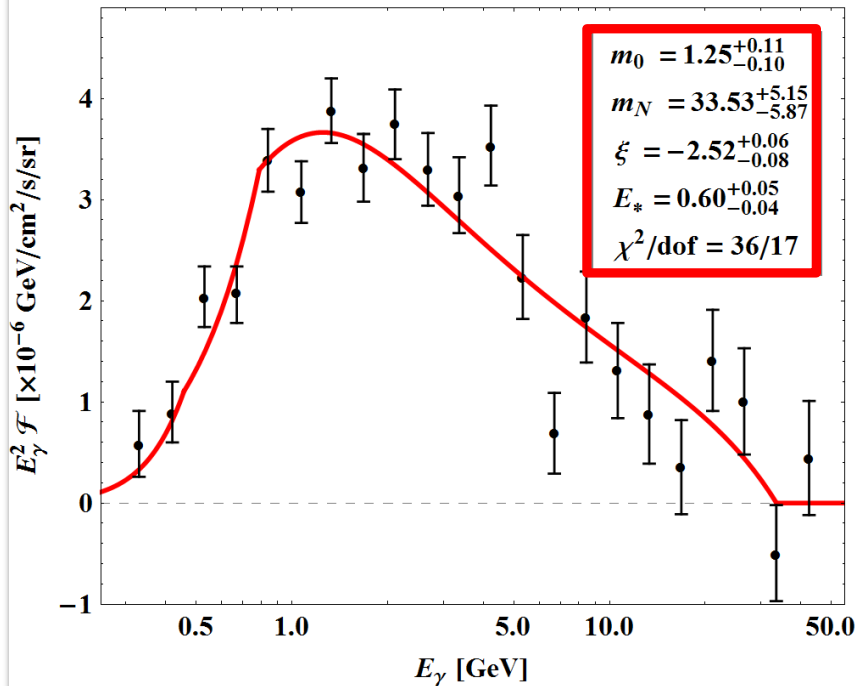


mass gap \ll energy resolution

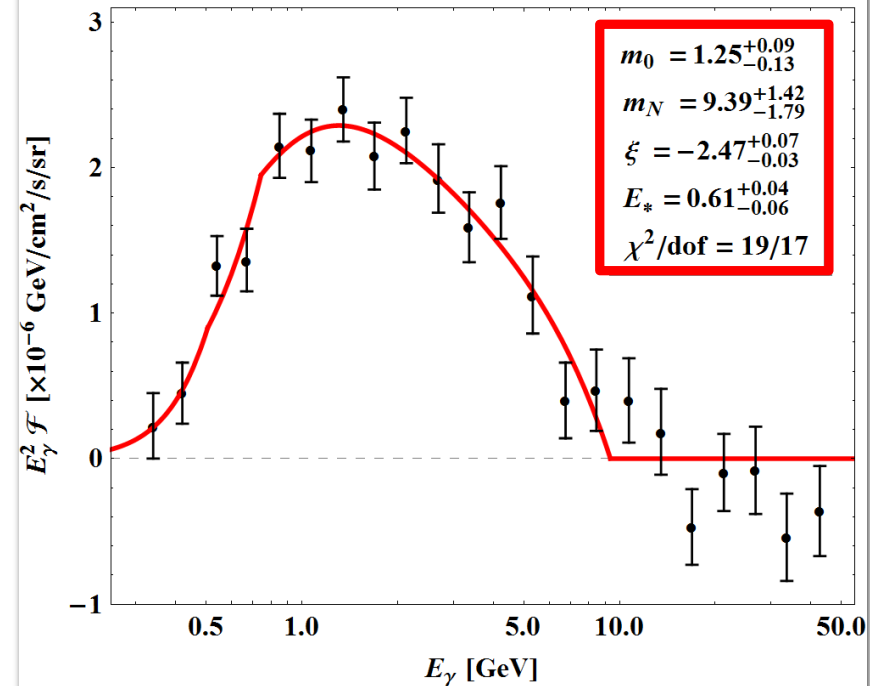
K. Boddy, K. Dienes, D. Kim, J. Kumar, **JCP**, and B. Thomas (2016)

Fit Results to GeV γ -ray Bump

40°×40°



Full Sky

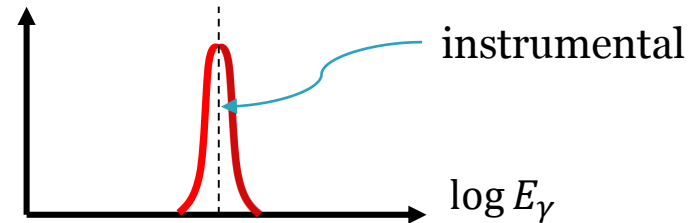
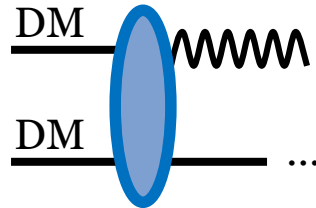


- Data reproduced well enough (see χ^2 values)
- cf. [arXiv:1402.6703](https://arxiv.org/abs/1402.6703) (bb) $\rightarrow \chi^2/\text{d.o.f.} = 64/20$ (44/20) with $m_{\text{DM}} = 43.0$ (36.6) GeV

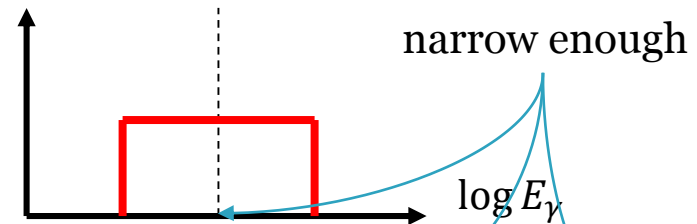
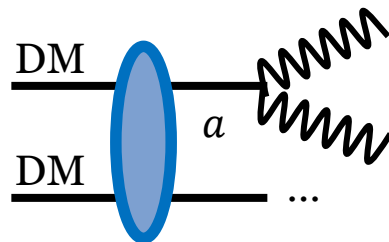
Line-like Excesses

Models explaining line-like signals

Scenario I

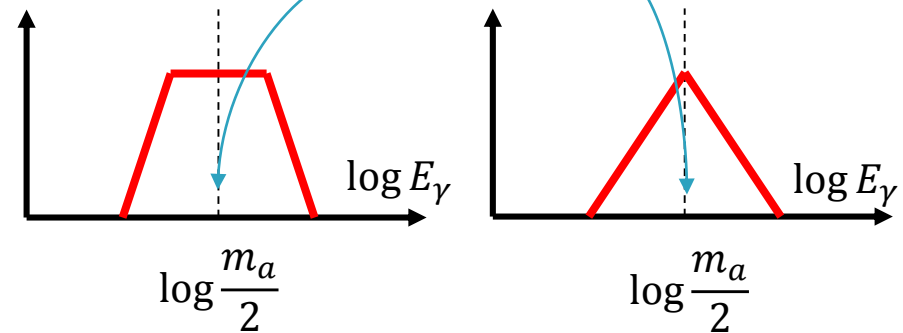
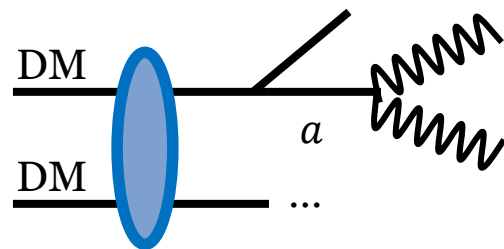


Scenario II



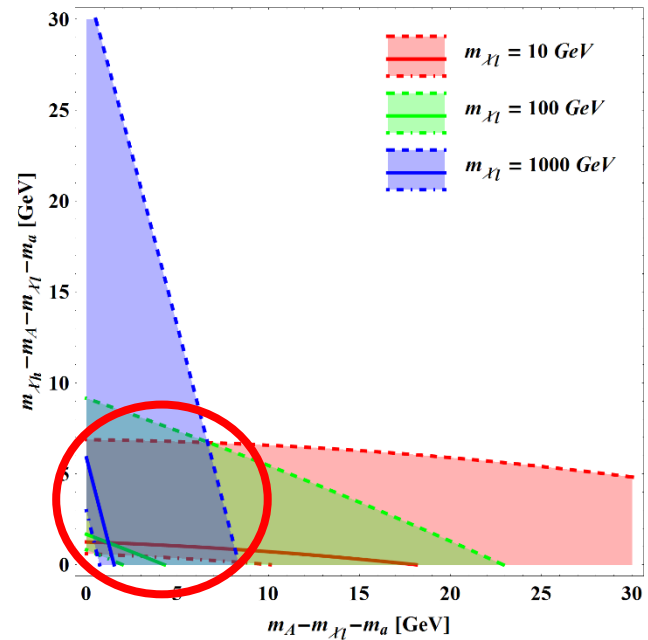
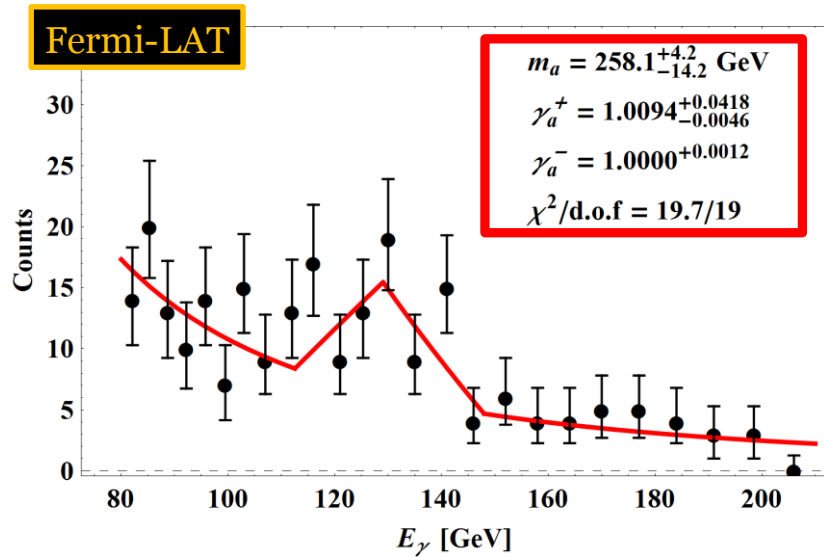
Scenario III

[D. Kim & JCP, PLB
(2015)]



Line-like Excesses

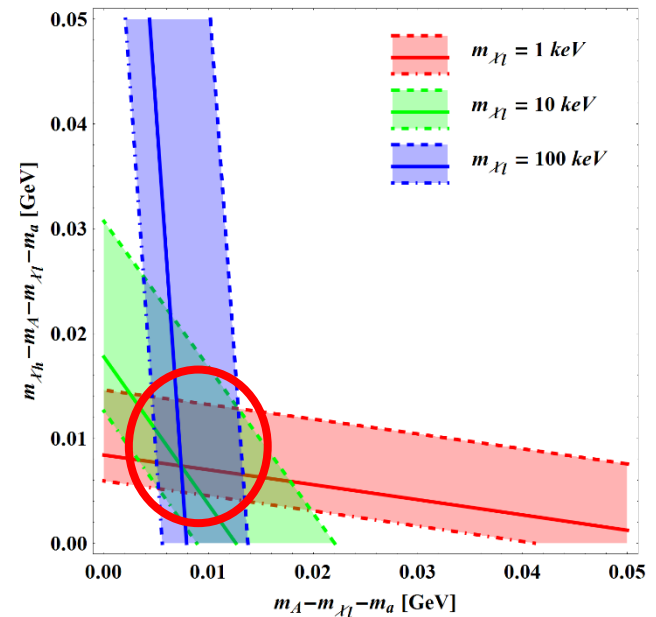
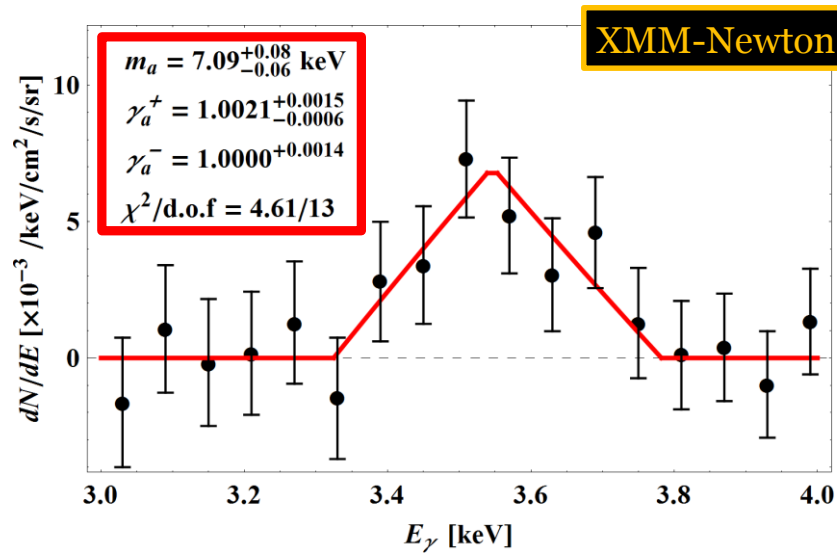
● Application to 130 GeV line



- ❑ Data extracted from the ULTRACLEAN event class in arXiv:1204.2797
- ❑ Power-law background template considered simultaneously

Line-like Excesses

● Application to 3.5 keV line

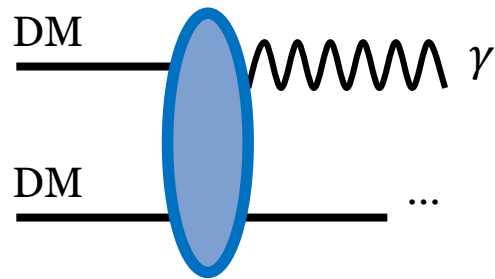


- ❑ Data extracted from the MOS spectrum of the central region of the galaxy M31 in arXiv:1402.4119
- ❑ Signal template only considered

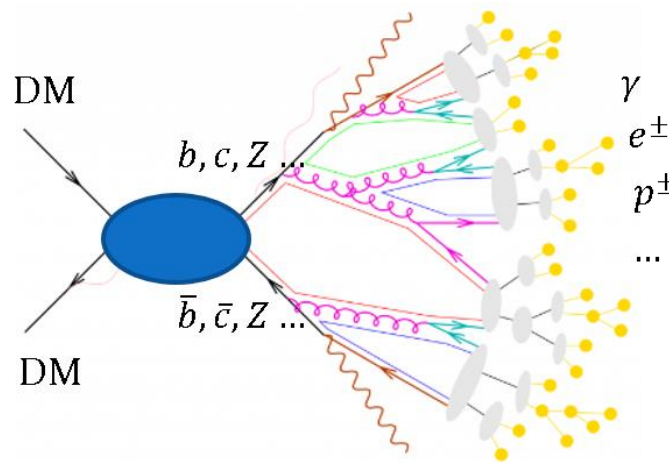
Conclusions

➤ Conventional DM interpretations on γ /cosmic-ray excesses:

1. **Line**: directly into $\gamma + X$



2. **Bump**: into SM particle pairs $\rightarrow \gamma$'s, e 's, ...



Conclusions

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➤ **Alternative mechanisms** using **E-peak idea**:

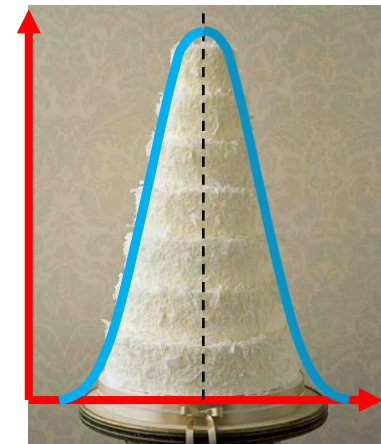
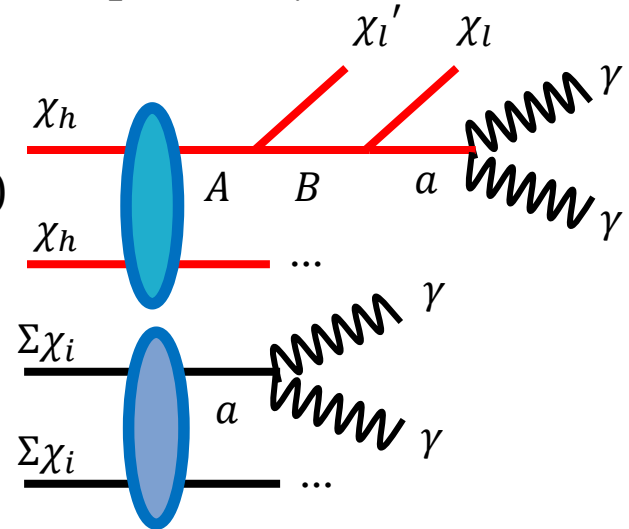
Non-minimal DM sector (e.g., Assisted FO, DDM, ...)

1. χ_h finally into $\chi_l + a (\rightarrow 2\gamma)$ via $\geq 1(2)$ step cascade
2. $\Sigma\chi_i$ into $X + a (\rightarrow 2\gamma)$

➤ **Reasonable χ^2 fits** ($\chi^2/\text{d.o.f.} \sim 1$)

➤ **Symmetric** w.r.t the peak in logarithmic E_γ

\rightarrow prediction: m_a



Conclusions

➤ Conventional DM interpretations on γ /cosmic-ray excesses:

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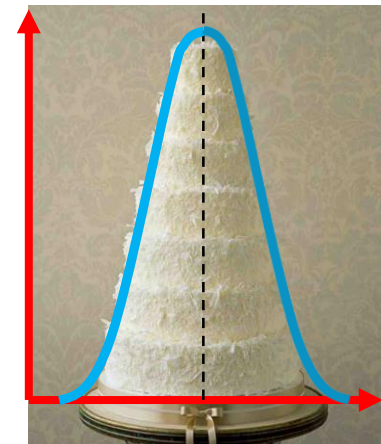
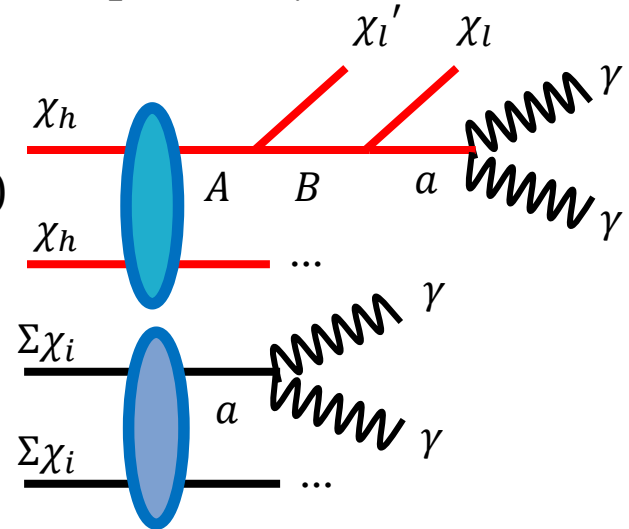
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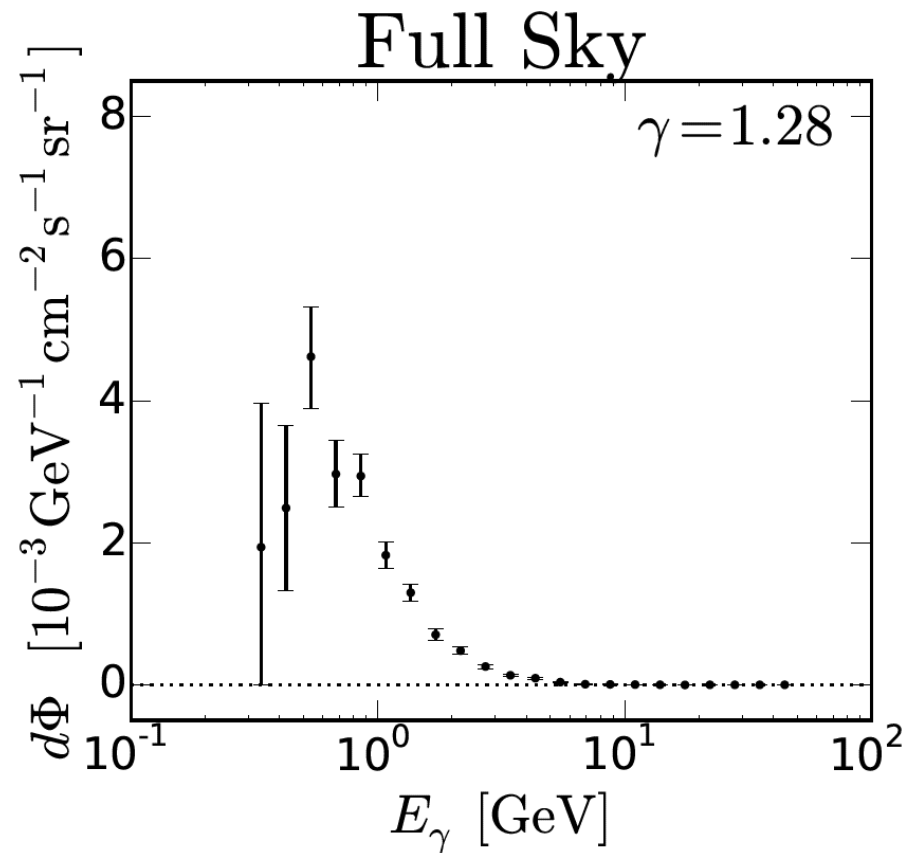
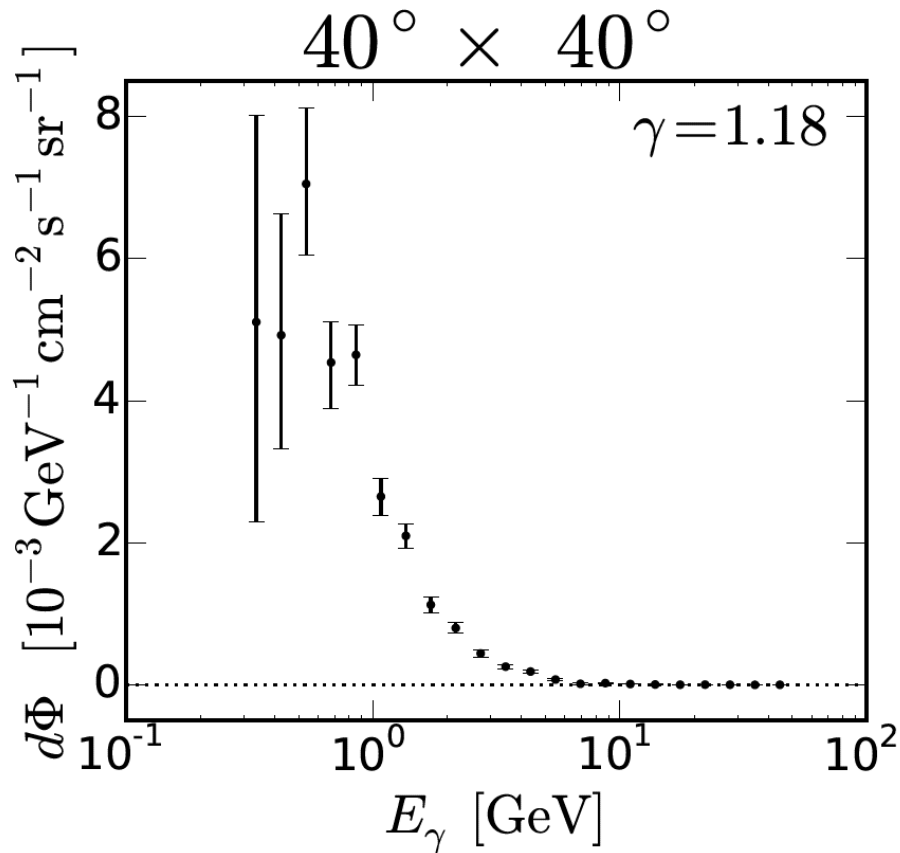
\rightarrow prediction: m_a



Thank you

Back-Up

Unweighted E Spectrum



Hitomi Perseus

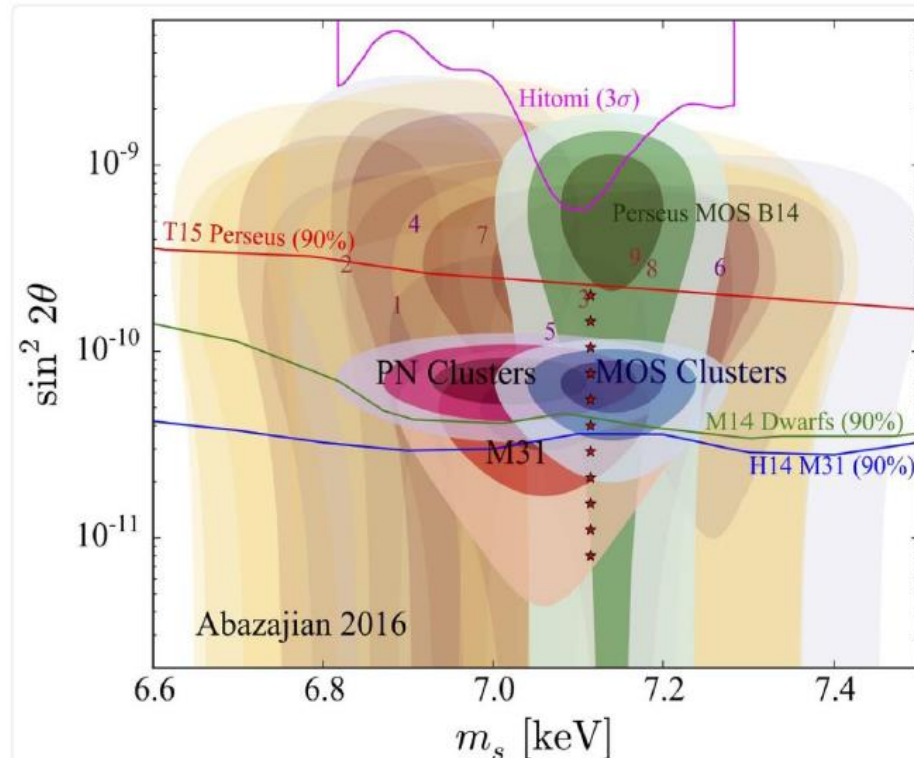


Kevork Abazajian
@kevaba



Following

#Hitomi constraints on 3.5 keV dark matter relative to previous constraints & signals. Significantly weaker...



Line-like Excesses

● Scenario III

- **Analytic expression** for E spectrum available

$$f(E_\gamma) = \int_{\gamma_a^{\min}}^{\gamma_a^{\max}} d\gamma_a \frac{g(\gamma_a)}{2E_\gamma^* \sqrt{\gamma_a^2 - 1}} \quad (11)$$

$$= \frac{m_a}{4E_\gamma^* p_a^* \sqrt{\gamma_A^2 - 1}} \left\{ \log \left[\sqrt{(\gamma_a^{\max})^2 - 1} + \gamma_a^{\max} \right] - \log \left[\sqrt{(\gamma_a^{\min})^2 - 1} + \gamma_a^{\min} \right] \right\}, \quad (12)$$

where γ_a^{\min} and γ_a^{\max} are defined as

$$\gamma_a^{\min} \equiv \max \left[\gamma_a^-, \frac{1}{2} \left(\frac{E_\gamma}{E_\gamma^*} + \frac{E_\gamma^*}{E_\gamma} \right) \right], \quad \gamma_a^{\max} \equiv \gamma_a^+. \quad (13)$$

$$\gamma_a^\pm \equiv \frac{E_a^*}{m_a} \gamma_A \pm \frac{p_a^*}{m_a} \sqrt{\gamma_A^2 - 1}.$$

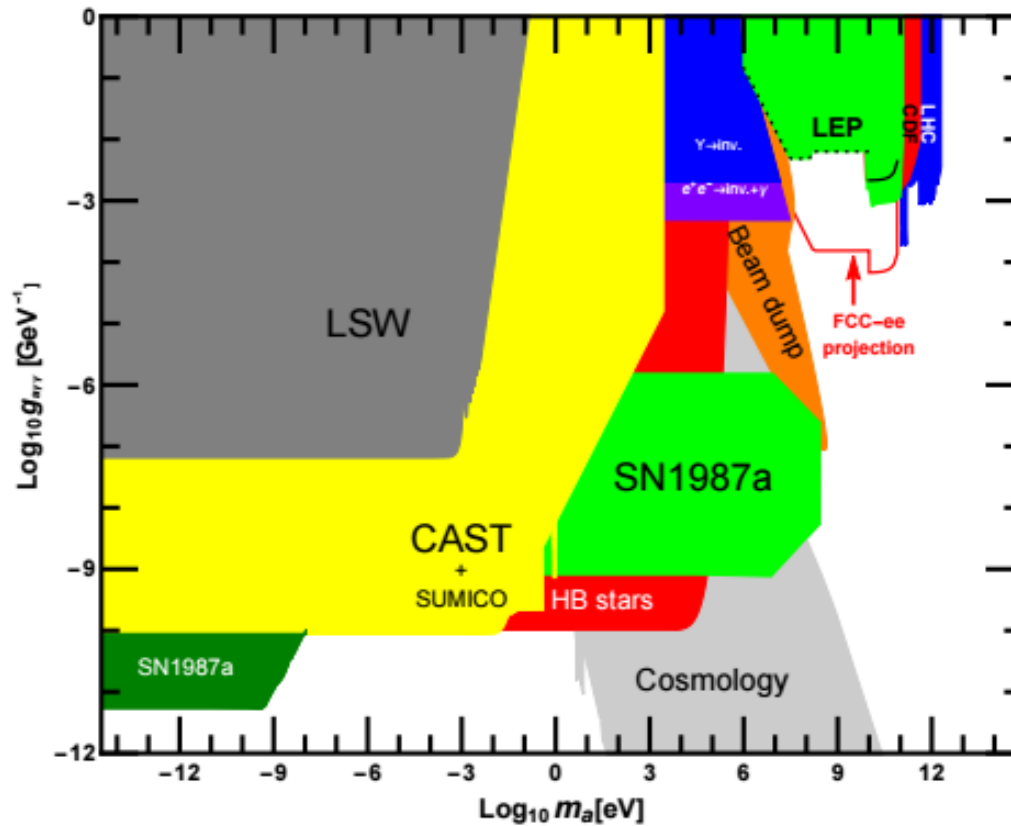
- Fit parameters: $E_\gamma^*, \gamma_a^+, \gamma_a^-$

- Possible to **distinguish DM models** to give a line-like signature using morphological features

	Scenario i)	Scenario ii)	Scenario iii)
Peak existence	Always	Absent	Sometimes
Plateau existence	Absent	Always	Sometimes
Width	Instrumental	Physical	Physical
Symmetry in E	Symmetric	Not available	Asymmetric
Symmetry in $\log E$	Asymmetric	Not available	Symmetric
Shape in E	Curved	Rectangular	Curved
Shape in $\log E$	Curved	Rectangular	Oblique

Bounds of Axion-Like Particles

● Limits from current experiments



Energy Peak

● Advertisement

Available on the CERN CDS information server

CMS PAS TOP-15-002

CMS Physics Analysis Summary

Contact: cms-pag-conveners-top@cern.ch

2015/09/16

Measurement of the top-quark mass from the b jet energy spectrum

The CMS Collaboration



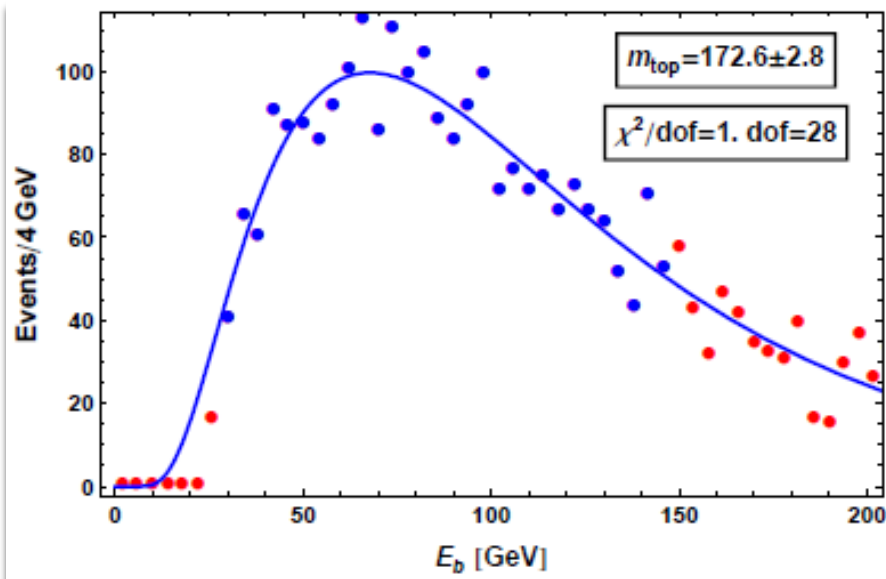
Example: M_{top} Measurement

arXiv: 1209.0772

● Detector level test

□ (Assuming W mass is well-known,) the result is quite good.

$$\langle m_{\text{top}} \rangle = 173.1 \pm 2.5 \text{ GeV}$$



□ Compared with the traditional method, ours is simpler.:

purely based on the kinematics and not rely at all on the detailed knowledge of underlying dynamics of top decay such as matrix element of the process.

Energy Peak

arXiv: 1209.0772

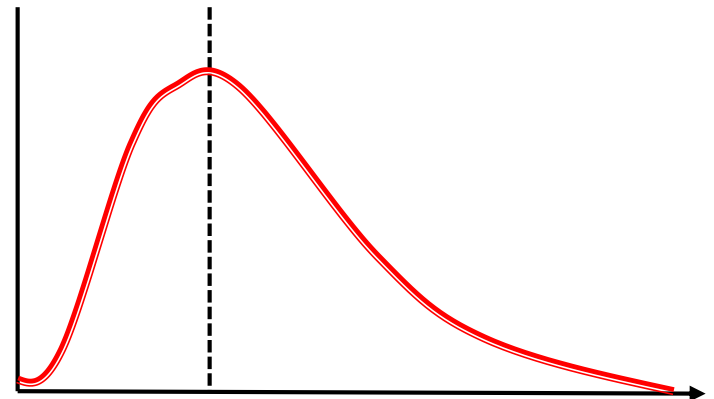
● Analysis: introduction of an ansatz

□ Generic distributions are obtained by an integration over the boost factor with **unknown** boost distribution $g(\gamma)$, generally, not doable

□ Nevertheless, there are common features of $f(E)$

- ❖ Even under $E/E^* \leftrightarrow E^*/E$
- ❖ Maximized at $E = E^*$
- ❖ Vanishing as E goes to $0/\infty$
- ❖ Returning a δ -function for some limiting parameter choice

$$f(E) = \int_{\frac{1}{2}(\frac{E}{E^*} + \frac{E^*}{E})}^{\infty} d\gamma \frac{g(\gamma)}{2E^* \sqrt{\gamma^2 - 1}}$$



□ Proposal of an ansatz:

$$f(E) = \frac{1}{K_1(w)} \exp\left[-\frac{w}{2} \left(\frac{E}{E^*} + \frac{E^*}{E}\right)\right]$$

Energy Peak

arXiv: 1209.0772

● Proposal of a “simple” *ansatz*

$$f(E) = \frac{1}{K_1(p)} \exp \left[-\frac{p}{2} \left(\frac{E}{E^*} + \frac{E^*}{E} \right) \right]$$

- $K_1(p)$: modified Bessel function of the second kind of order 1
- p : fitting parameter which encodes the width of the peak
- E^* as a **fitting parameter** can be extracted by fitting!
- All four properties are satisfied. → for the last property, use the asymptotic behavior of $K_1(p)$

$$K_1(p) \xrightarrow{p \rightarrow \infty} \sim \frac{e^{-p}}{\sqrt{p}} \left(1 + \mathcal{O} \left(\frac{1}{p} \right) \right)$$

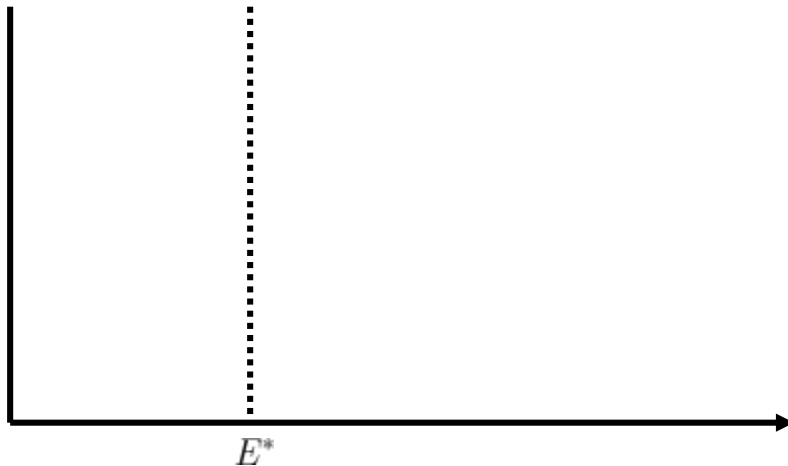
- Proposed ansatz does not develop a cusp so that it is more suitable for the case of $g(1)=0$, e.g., pair-production of mothers

Fitting Function

arXiv: 1209.0772

● Functional properties of generic $f(E)$

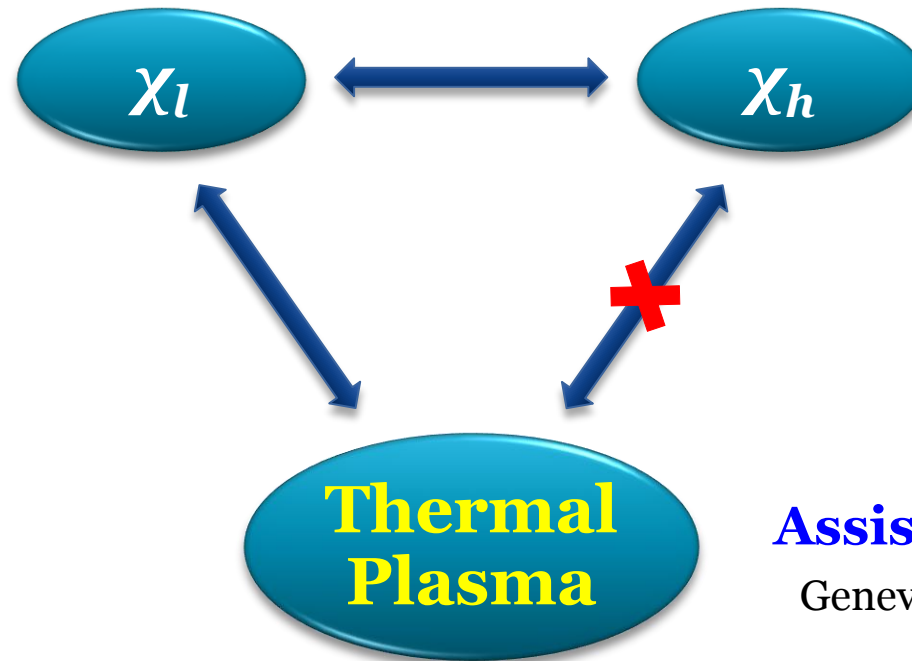
$$f(E) = \int_{\frac{1}{2}(\frac{E}{E^*} + \frac{E^*}{E})}^{\infty} d\gamma \frac{g(\gamma)}{2E^* \sqrt{\gamma^2 - 1}}$$



- 1) Even under $\frac{E}{E^*} \leftrightarrow \frac{E^*}{E}$ or $E \rightarrow \frac{E^{*2}}{E}$
- 2) Maximized at $E=E^*$
- 3) Vanishing as E goes to zero or infinity
- 4) Returning a δ -function for some limiting parameter choice

Multi-DM Set-up: Assisted FO

- ❖ Two species of DM: χ_h, χ_l with $m_h > m_l$ (e.g. $U(1)' \otimes U(1)''$, $Z_2' \otimes Z_2''$)
- ❖ χ_h : **dominant** DM component, **no direct coupling** to the SM
 - Assisted Freeze-Out
- ❖ χ_l : sub-dominant, **direct coupling** to the SM ($\mathcal{L} \supset -\frac{1}{2} \sin \epsilon X_{\mu\nu} F^{\mu\nu}$)



Assisted Freeze-Out

Genevieve Belanger & JCP,
JCAP (2012)