

Tools for Spectroscopy



Michael Pennington
Durham, September 2017



ρ, η, π, \dots

K, D, B, \dots

$\Lambda, \psi, \chi, \dots$

X, Y, Z, \dots

Window on confinement

Resonances in QCD

$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b,t} \bar{q} (i \gamma_{\mu} D^{\mu} - m_q) q - \frac{1}{4} \mathcal{G}^{\mu\nu} \mathcal{G}_{\mu\nu}$$

Resonances in QCD

Hadrons: effective degrees of freedom

$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b,t} \bar{q} (i \gamma_{\mu} D^{\mu} - m_q) q - \frac{1}{4} \mathcal{G}^{\mu\nu} \mathcal{G}_{\mu\nu}$$

Resonances in QCD

Hadrons: effective degrees of freedom

how do these depend on flavour, b, c, s, d, u

$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b,t} \bar{q} (i \gamma_{\mu} D^{\mu} - m_q) q - \frac{1}{4} \mathcal{G}^{\mu\nu} \mathcal{G}_{\mu\nu}$$

Resonances in QCD

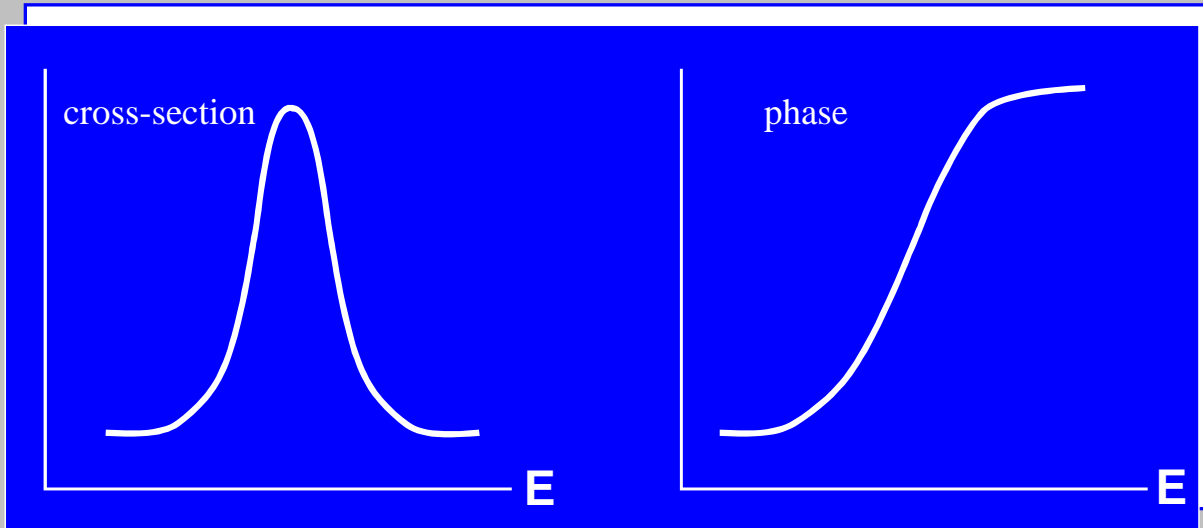
Hadrons: effective degrees of freedom

how do these depend on flavour, b, c, s, d, u

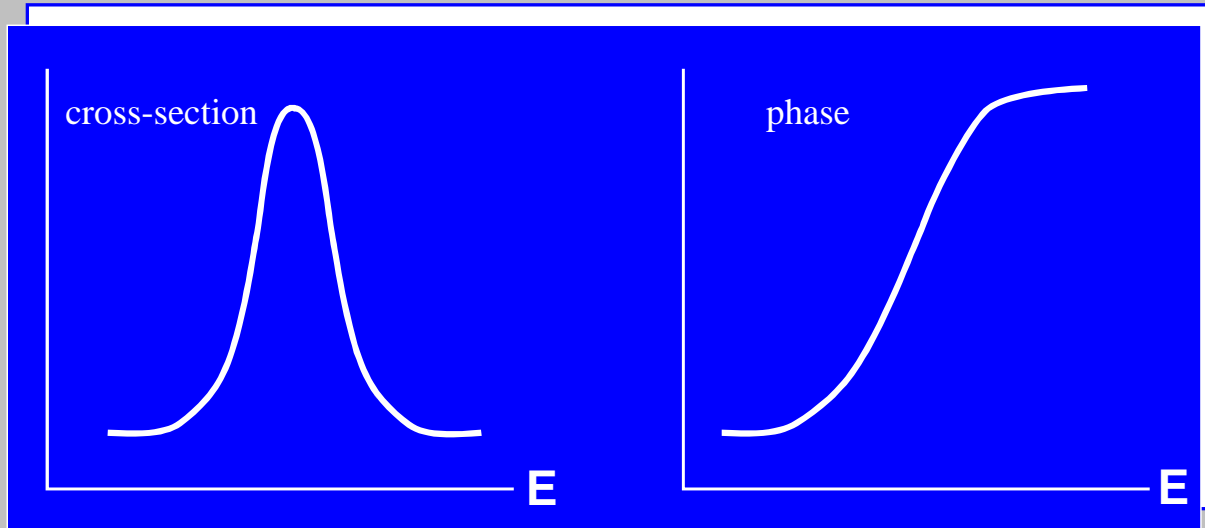
Hadron interactions: universality

$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b,t} \bar{q} (i \gamma_{\mu} D^{\mu} - m_q) q - \frac{1}{4} \mathcal{G}^{\mu\nu} \mathcal{G}_{\mu\nu}$$

Hadron States



Hadron States

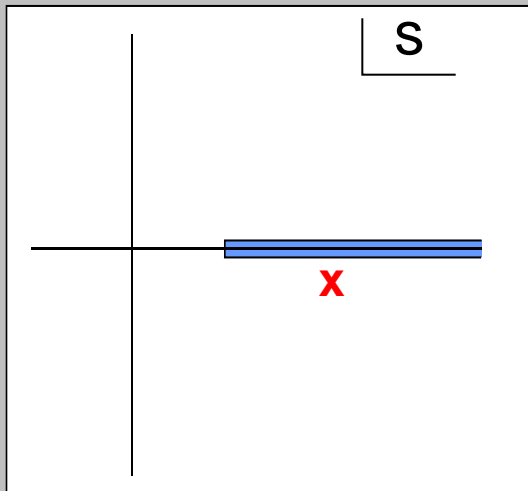
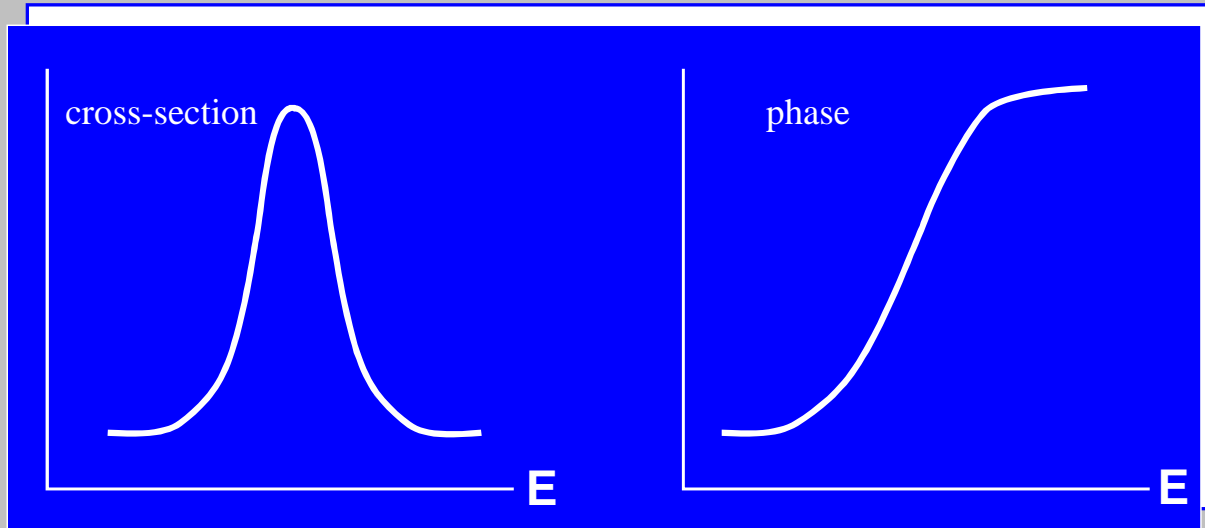


$$s = E^2$$

Breit-Wigner

$$\frac{1}{M^2 - s - iM\Gamma}$$

Hadron States

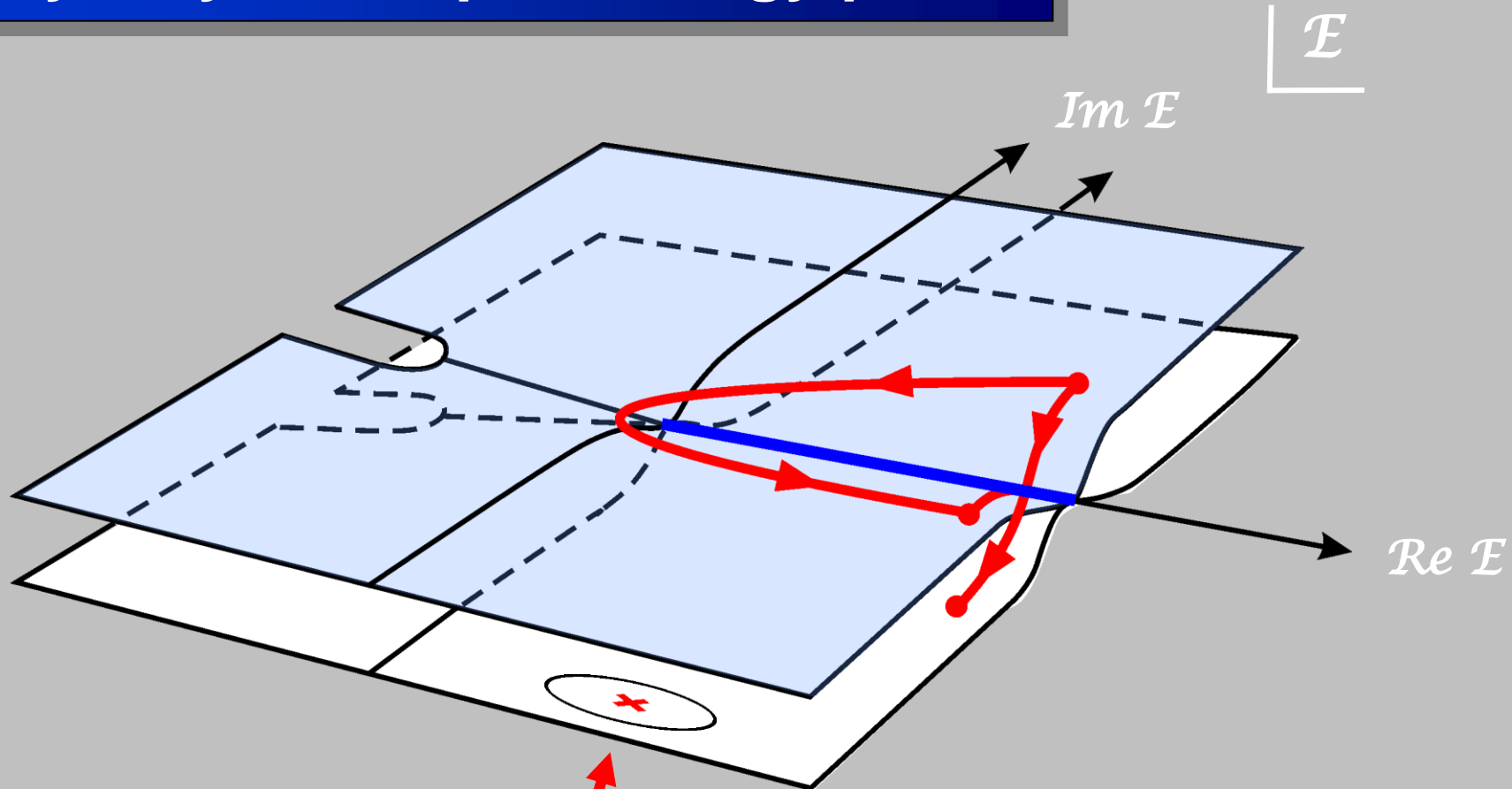


$$s = E^2$$

Breit-Wigner

$$\frac{1}{M^2 - s - iM\Gamma}$$

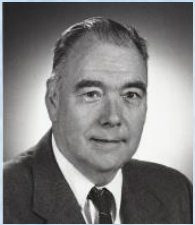
analyticity & complex energy plane



resonance pole

Landscape to be explored





Res Jost

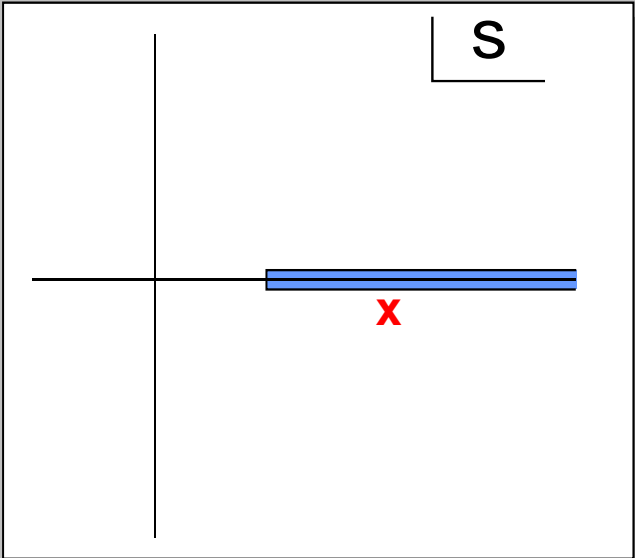
A world with cuts



and overlapping peaks

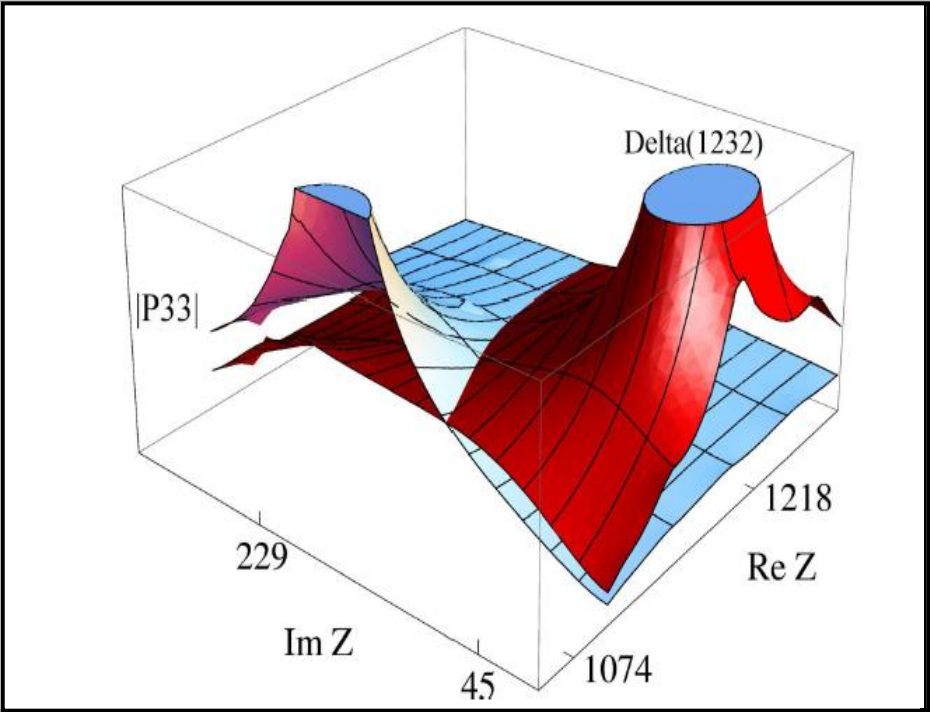


$$s = E^2$$

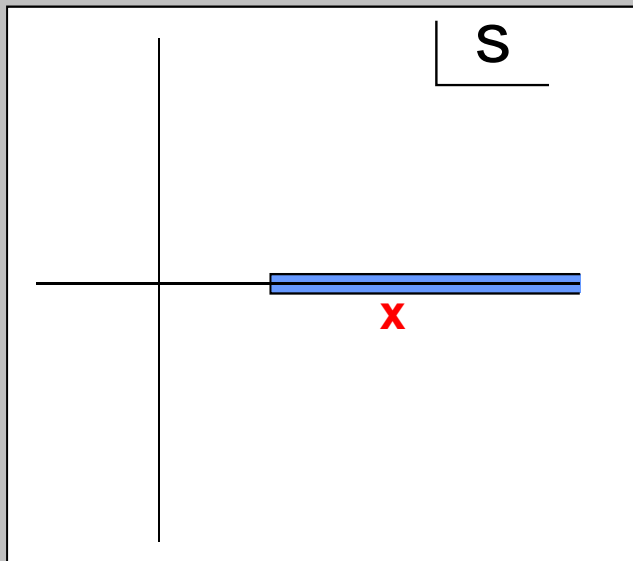


Breit-Wigner

$$\frac{1}{M^2 - s - iM\Gamma}$$



$$s = E^2$$

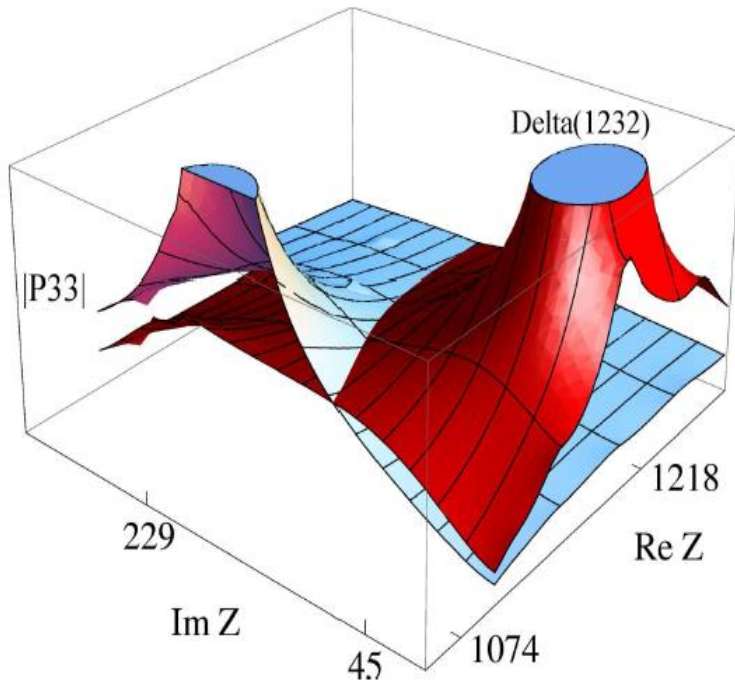


Breit-Wigner

$$\frac{1}{M^2 - s - iM\Gamma}$$

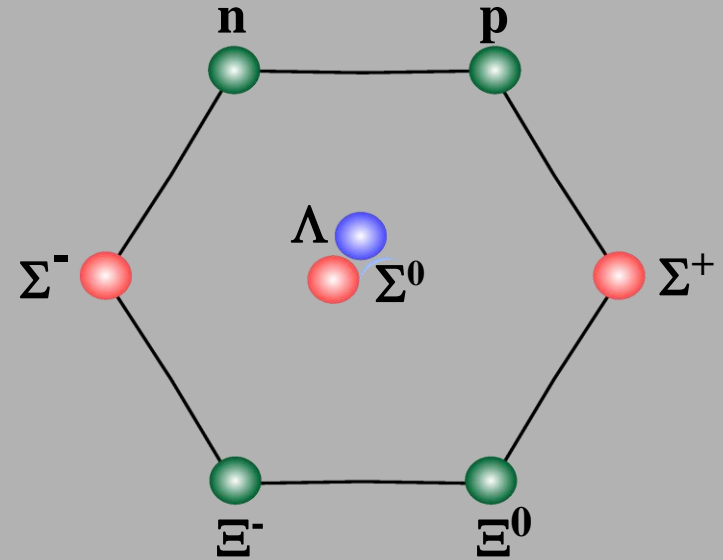
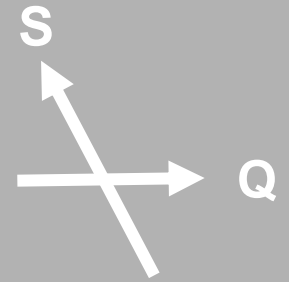
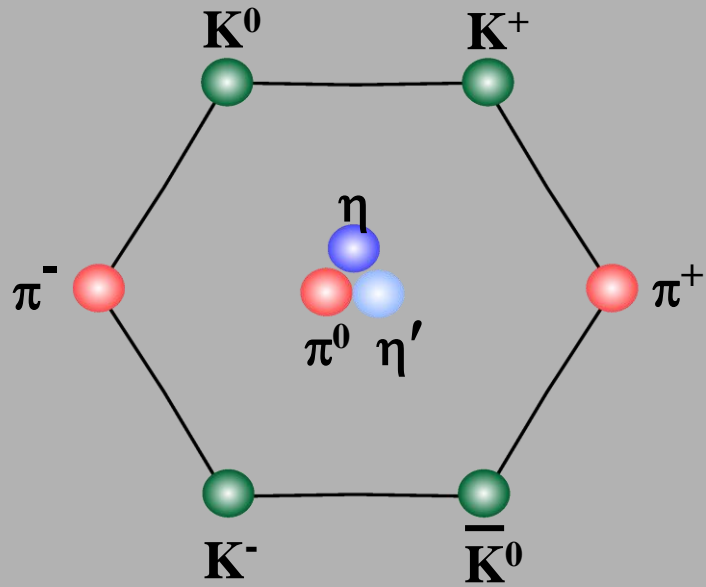
merely an approximation
valid in the region of the pole

$$\frac{1}{M^2(s) - s}$$

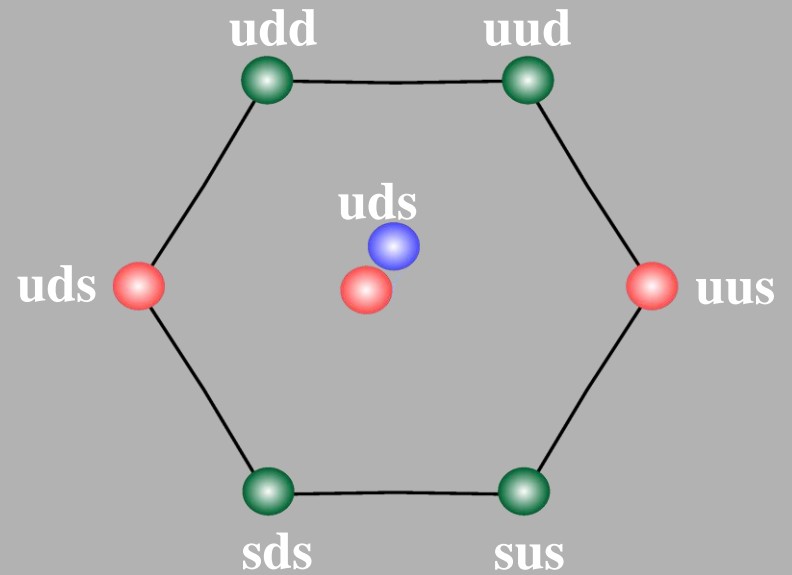
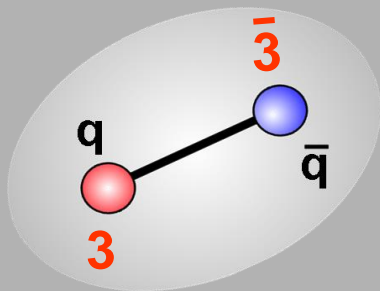
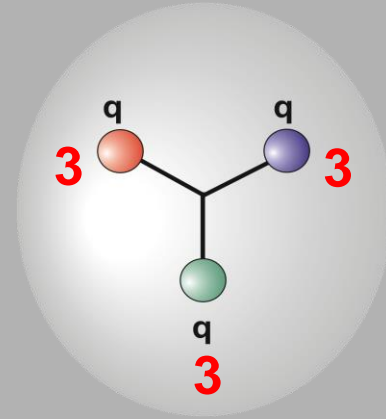
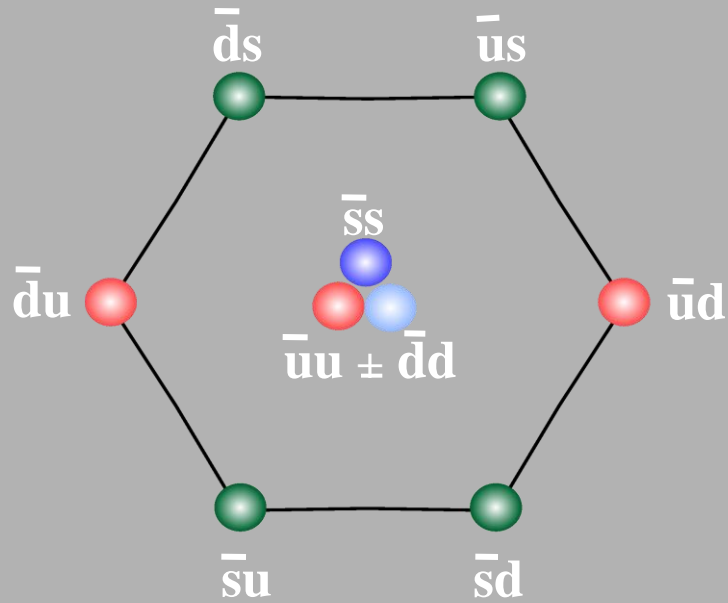


Quark model spectrum

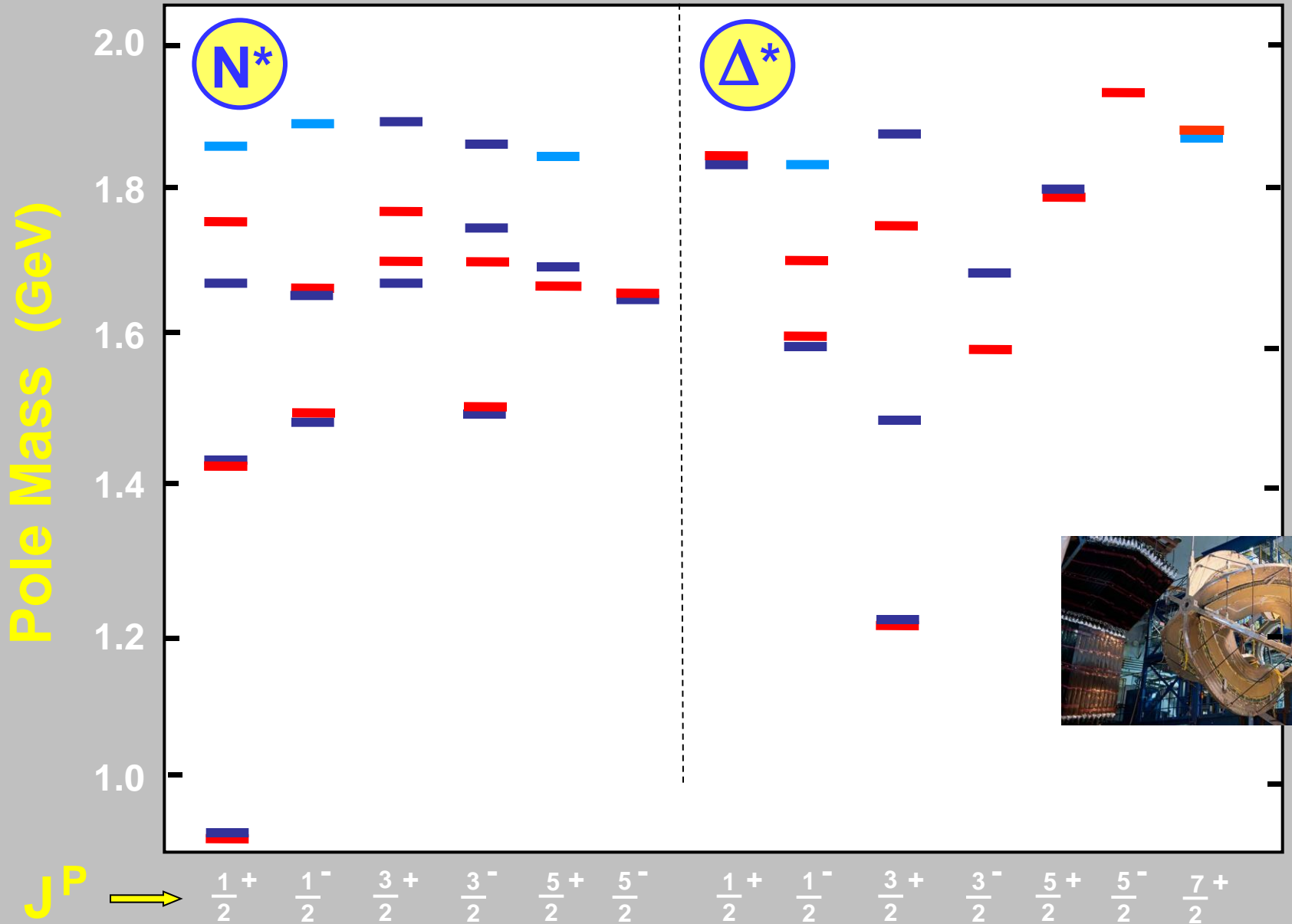
ground states



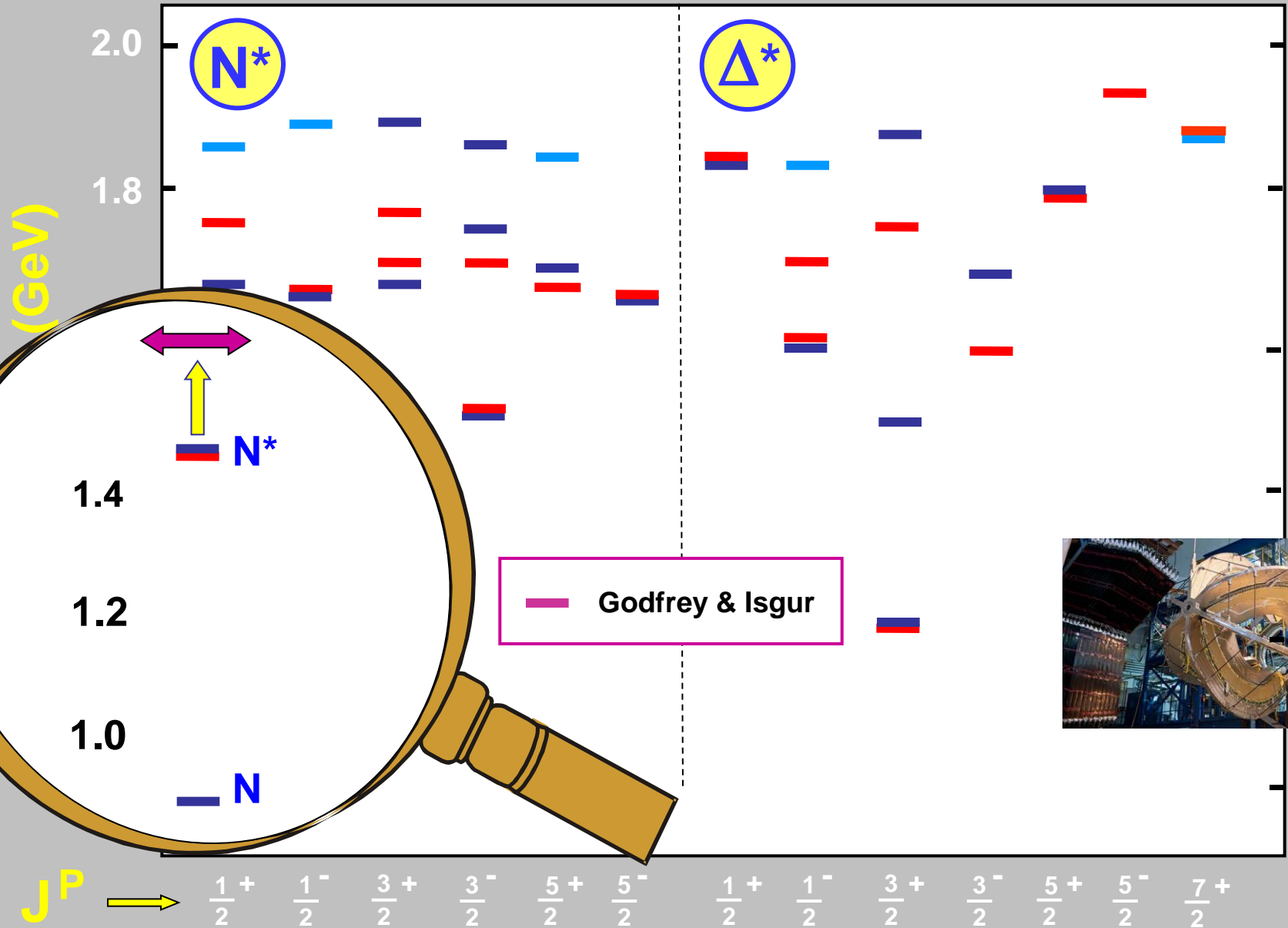
Quark model spectrum



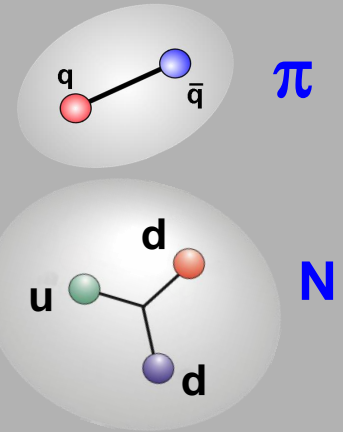
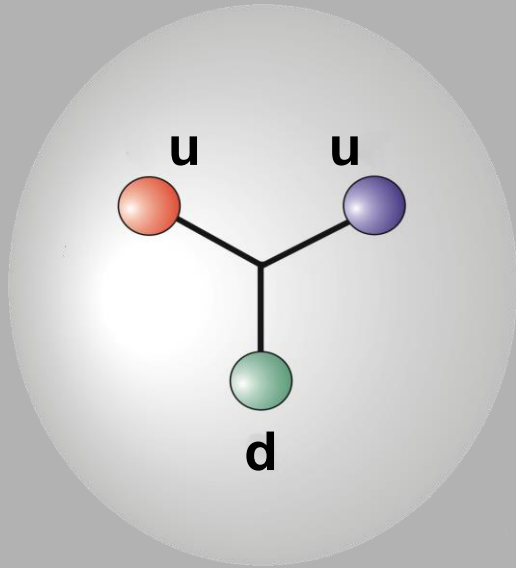
Baryon spectrum from ANL-Osaka & Bonn-Ga



Baryon spectrum from ANL-Osaka & Bonn-Ga



$N^*(1440)$ colour wave-function

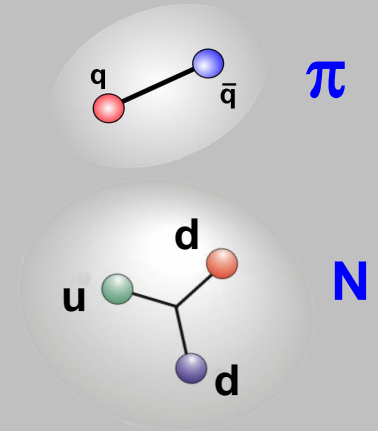
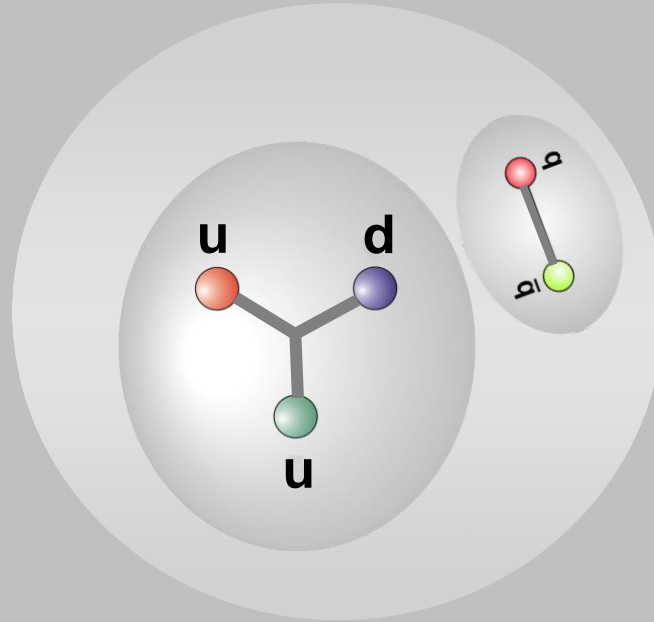
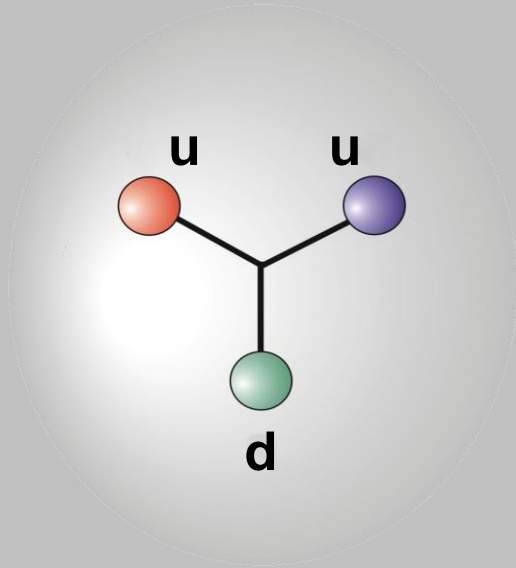


Roper

$$N^{*+} = \frac{1}{\sqrt{6}} [\text{uud} + \text{uud} + \text{uud} - \text{uud} - \text{uud} - \text{uud}]$$

$$N_c = 3$$

$N^*(1440)$ colour wave-function

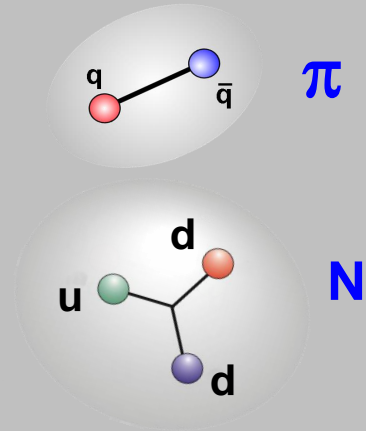
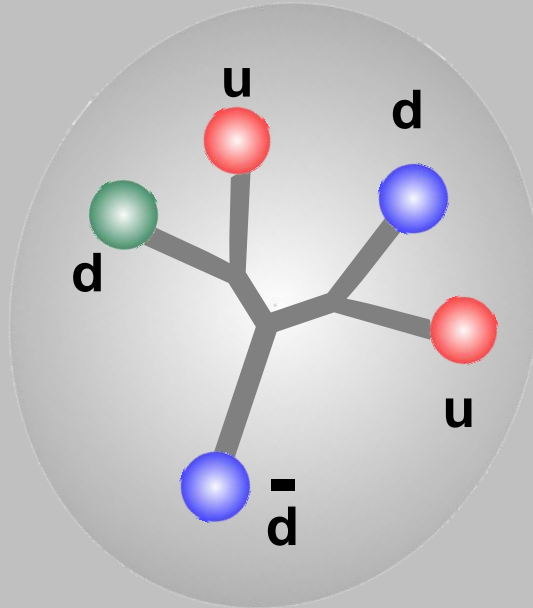
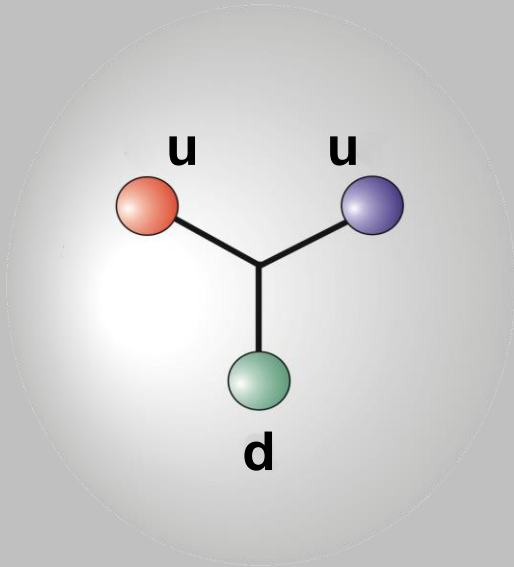


Roper

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N*(1440) colour wave-function

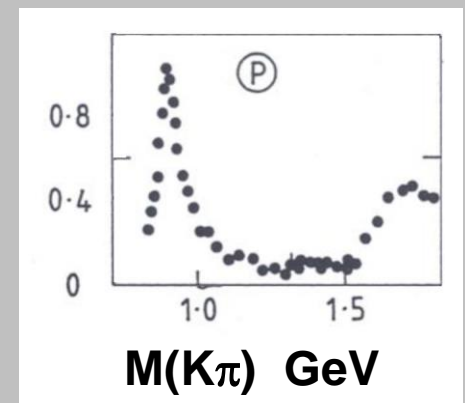
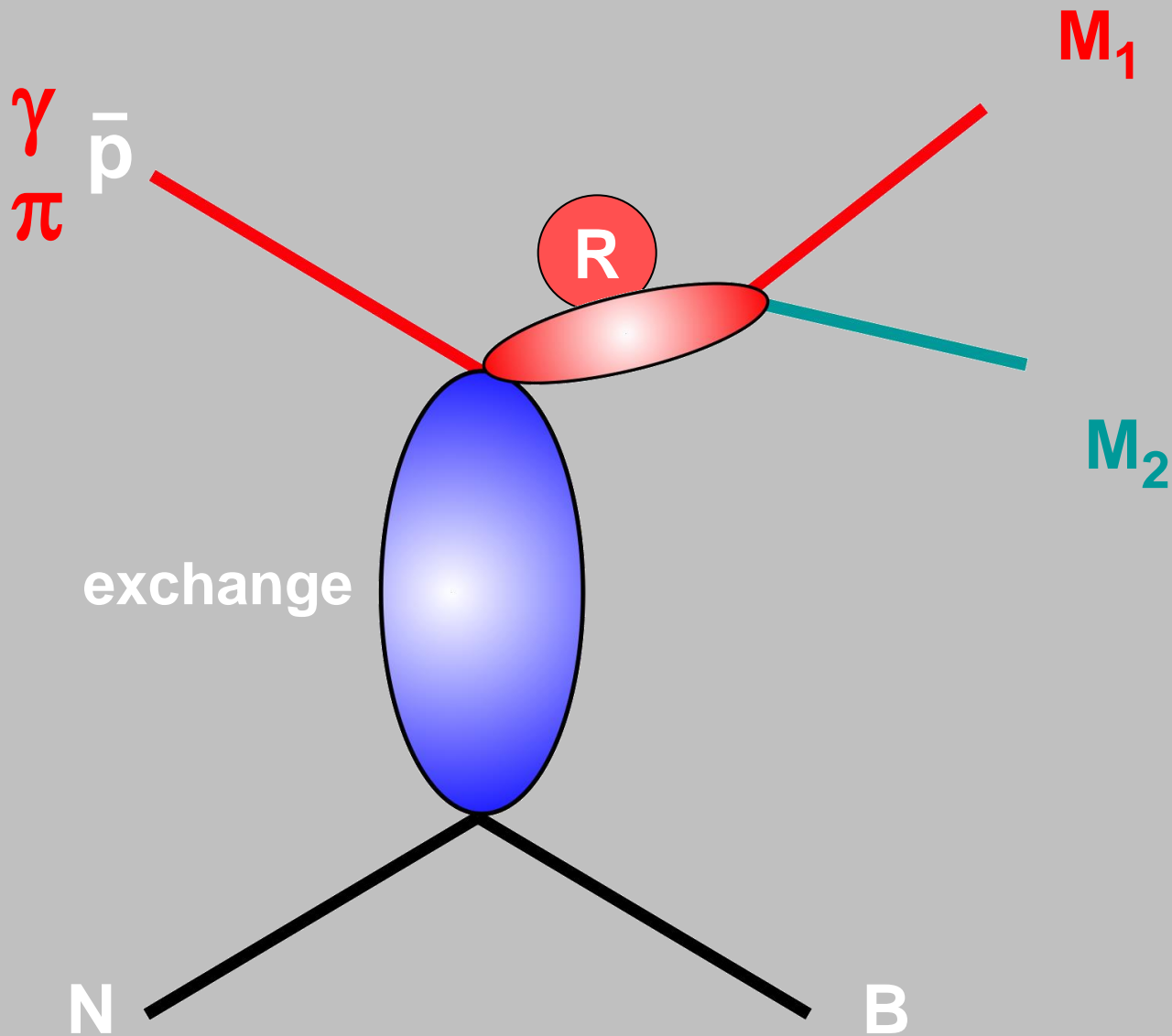


Roper

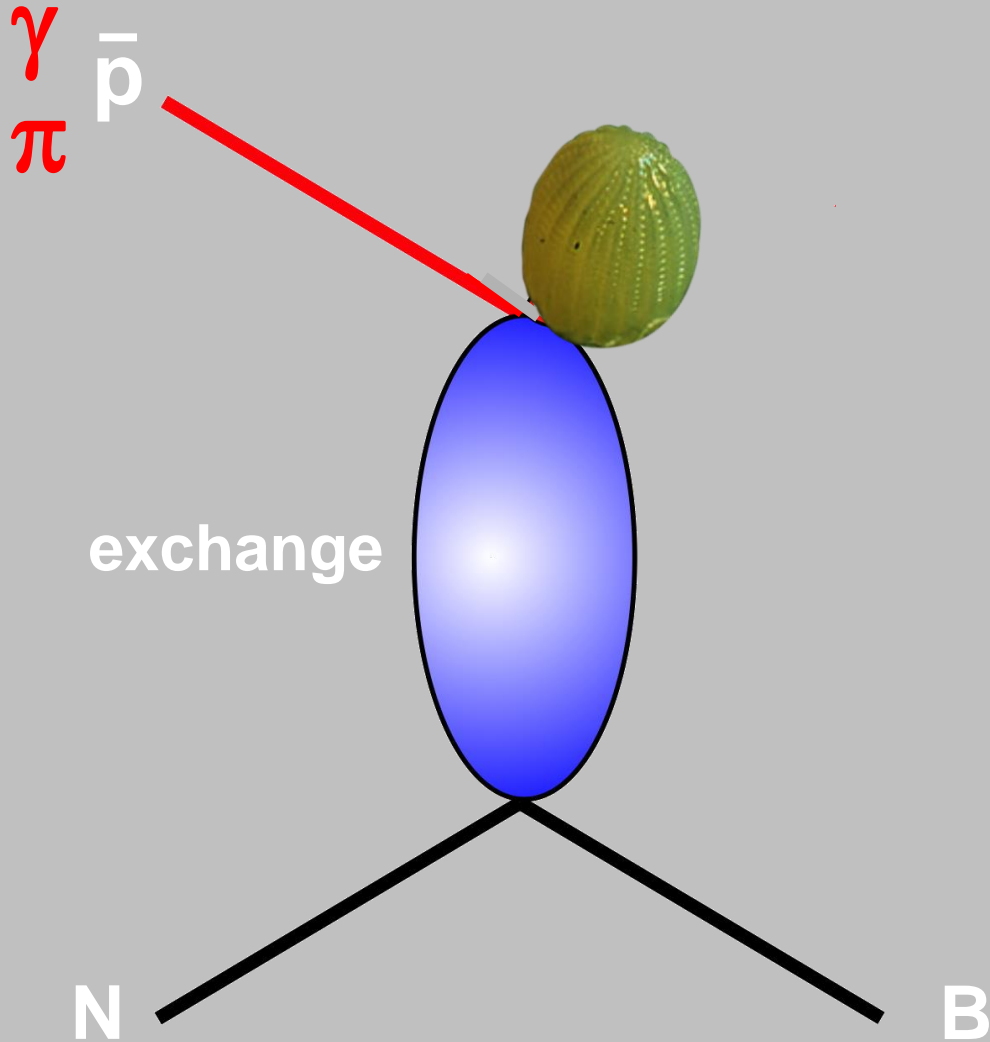
$N_c = 3$

$$N^{*+} = \frac{1}{\sqrt{6}} [\text{uud} + \text{uud} + \text{uud} - \text{uud} - \text{uud} - \text{uud}]$$

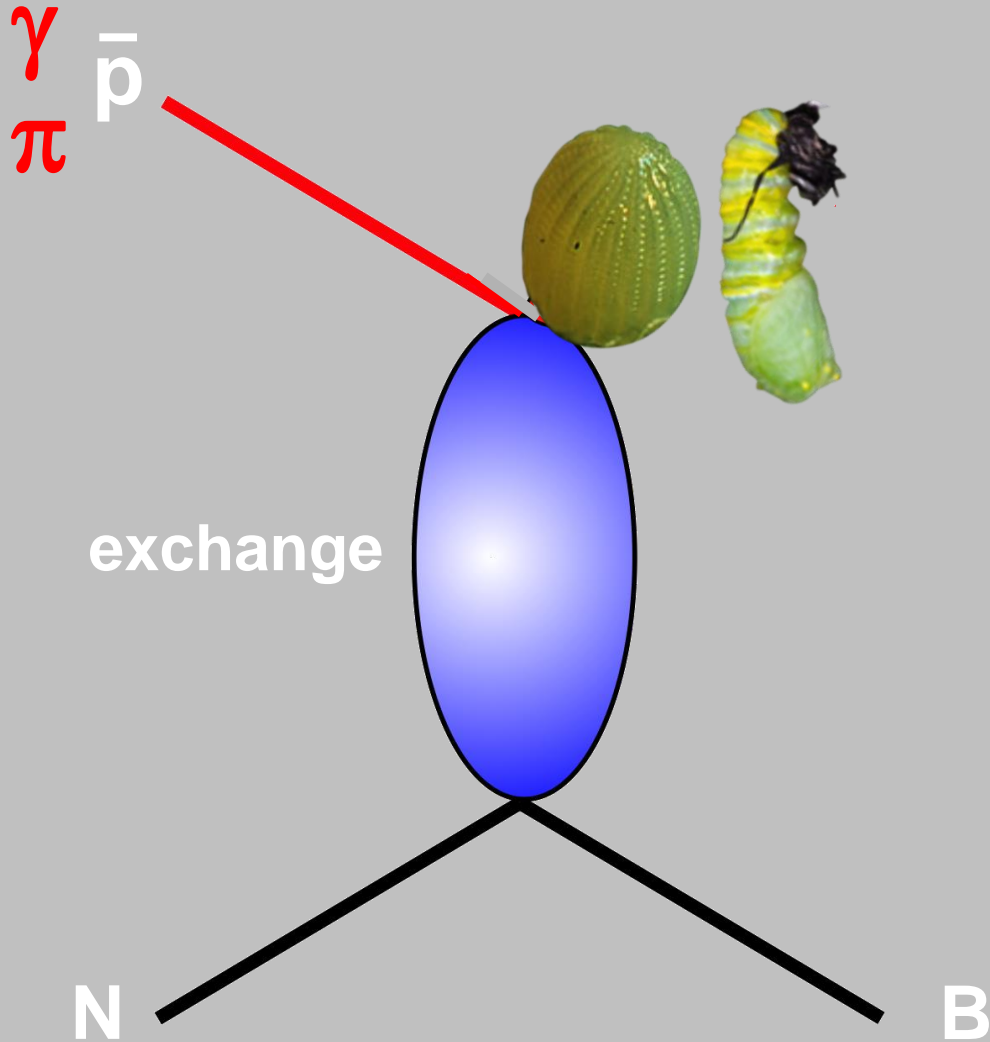
Hadroproduction



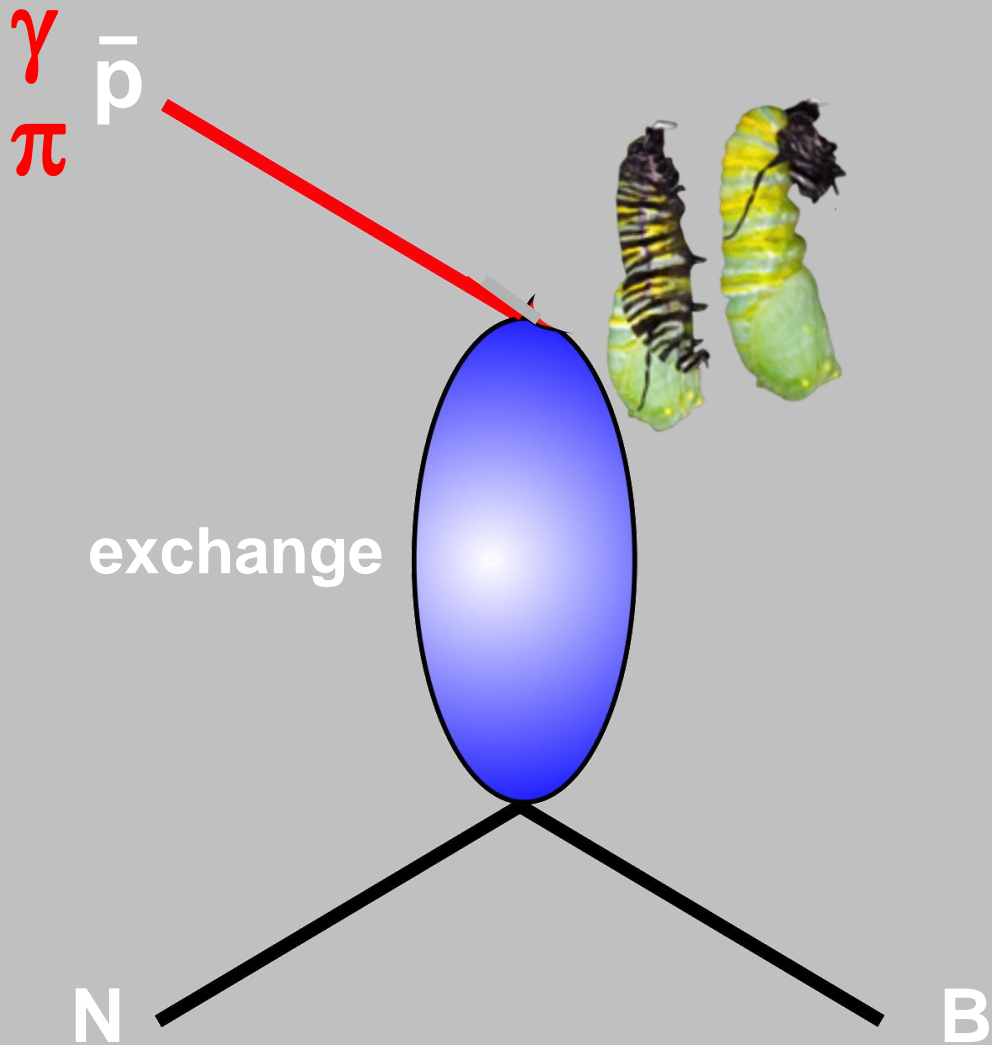
Hadroproduction



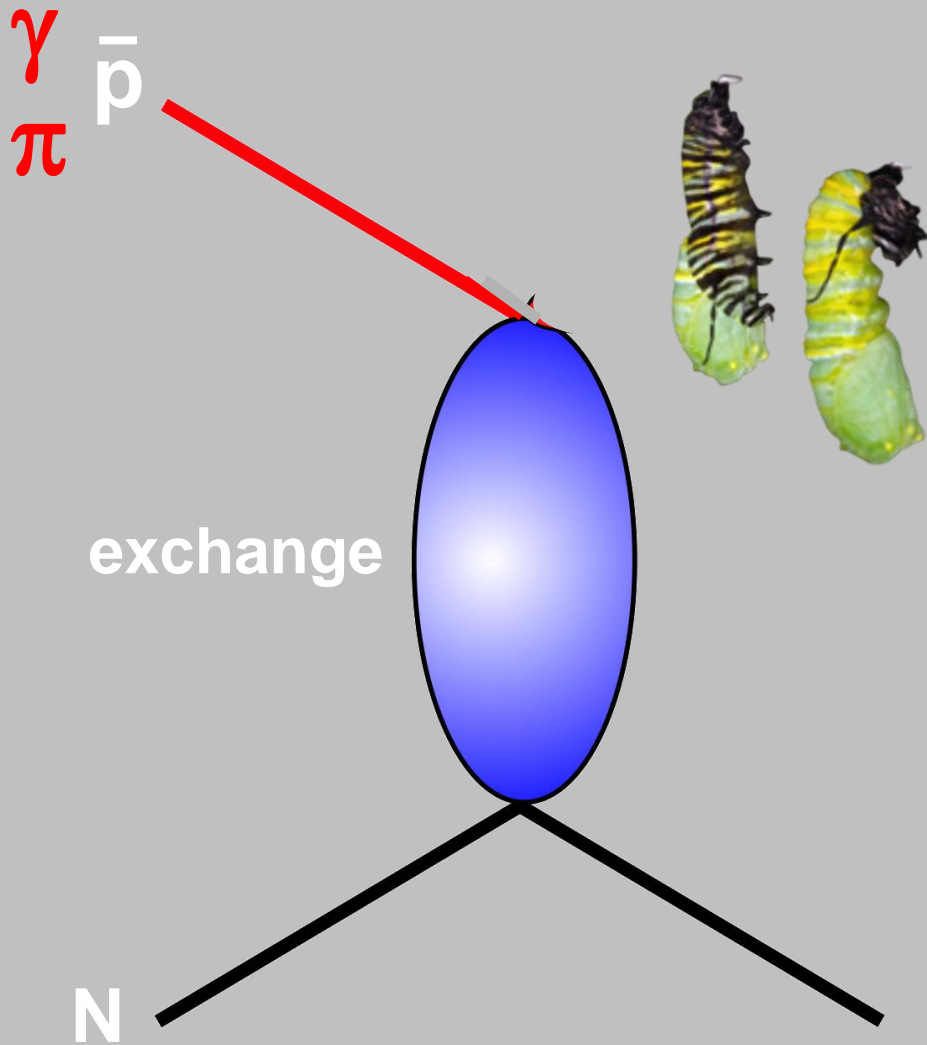
Hadroproduction



Hadroproduction



Hadroproduction



Hadroproduction

γ
 π

\bar{p}

exchange

N

B



Hadroproduction

γ
 π \bar{p}

exchange

N

B



Hadroproduction

γ
 π \bar{p}

exchange

N

B



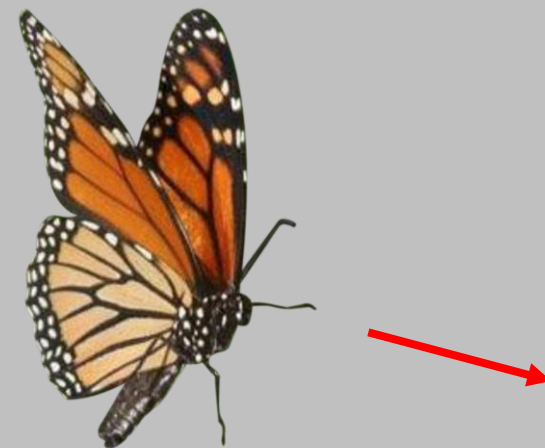
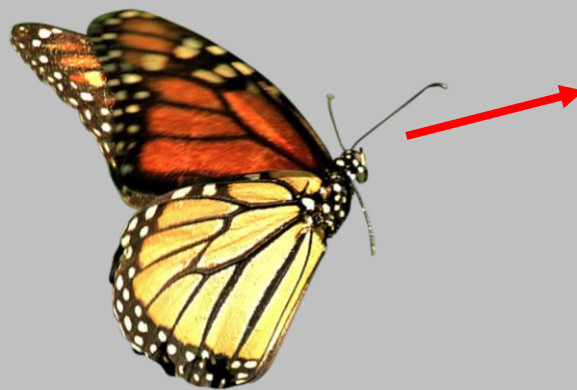
Hadroproduction

γ
 π \bar{p}

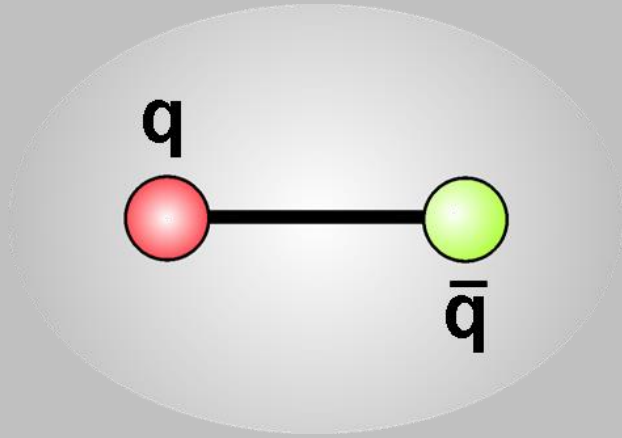
exchange

N

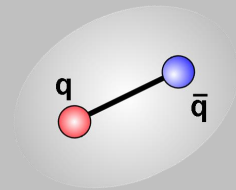
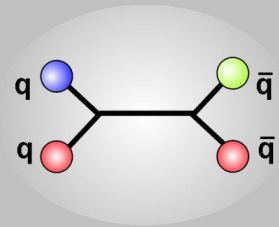
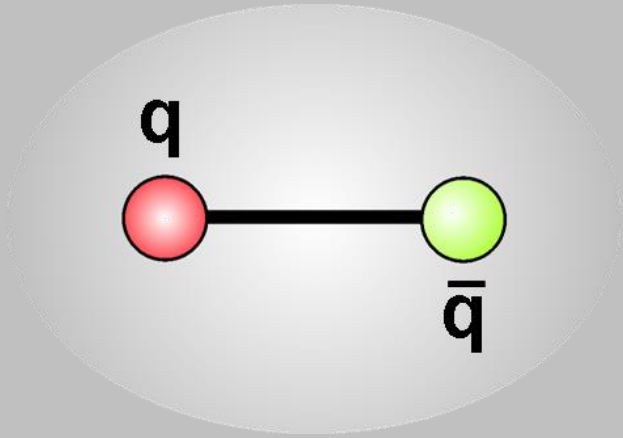
B



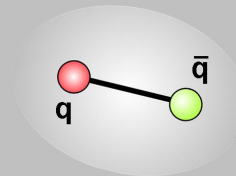
$\rho(770)$



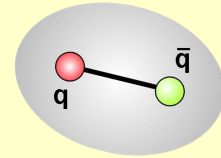
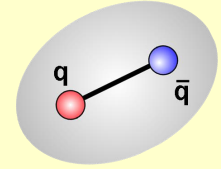
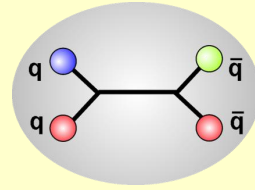
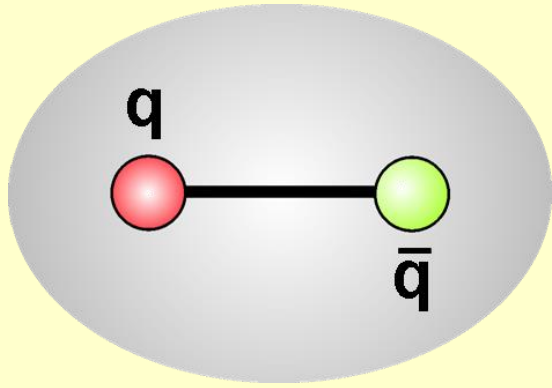
$\rho(770)$

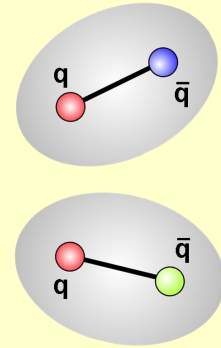
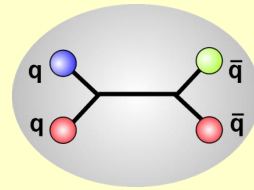
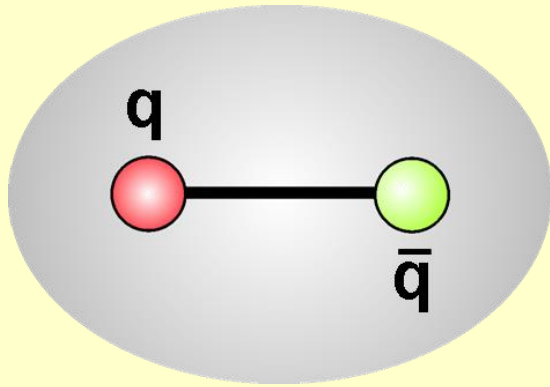


π^+

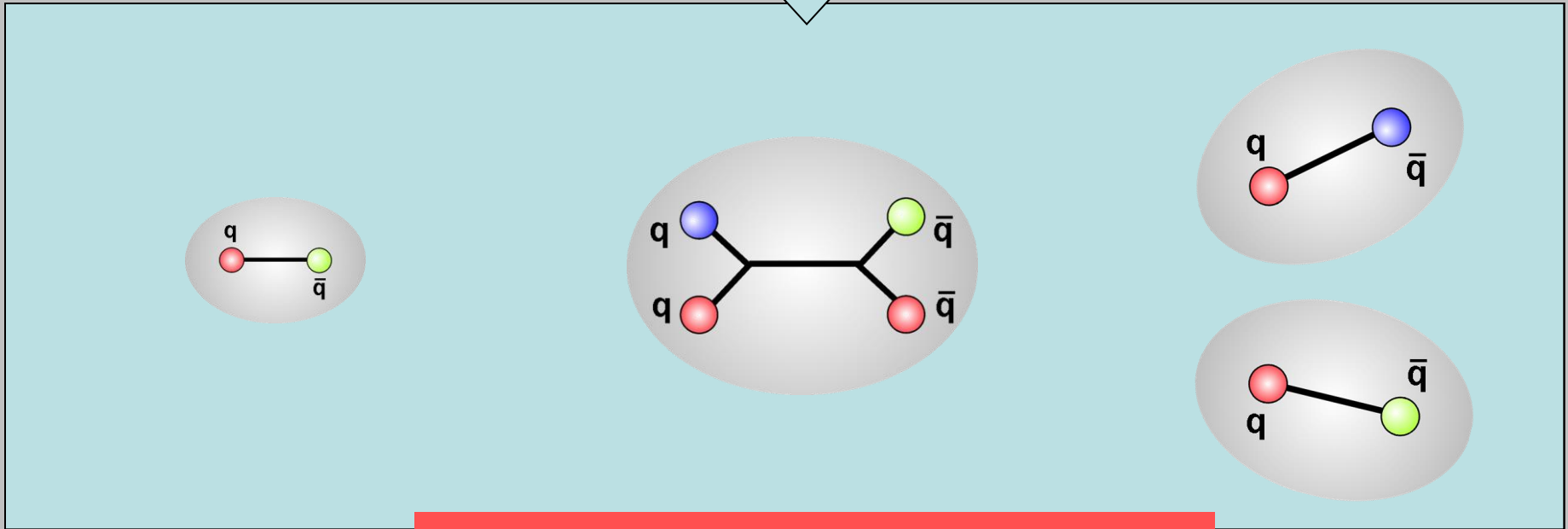
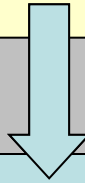
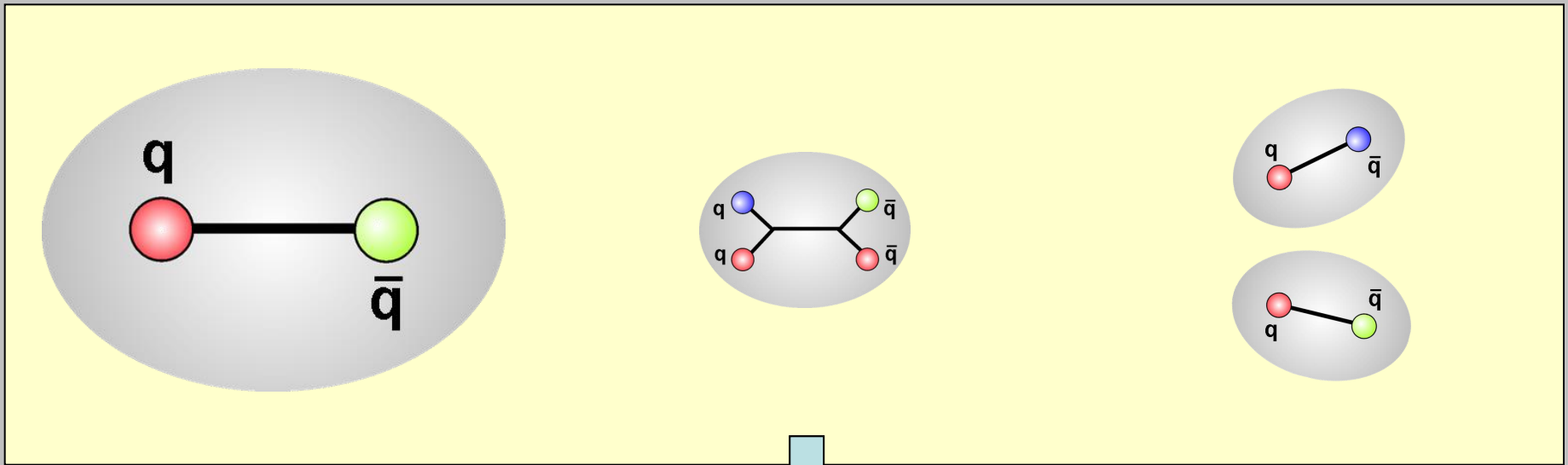


π^-

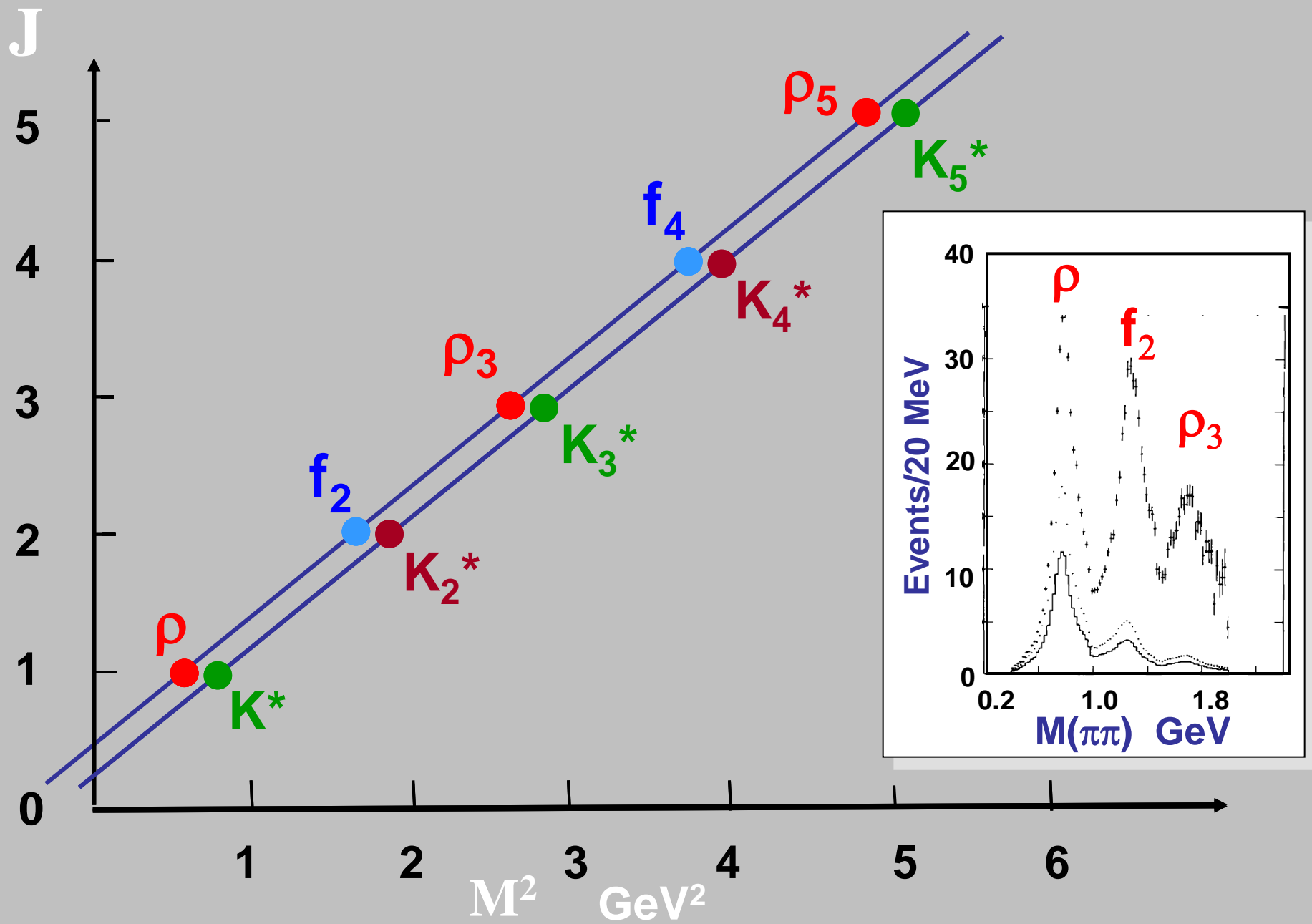


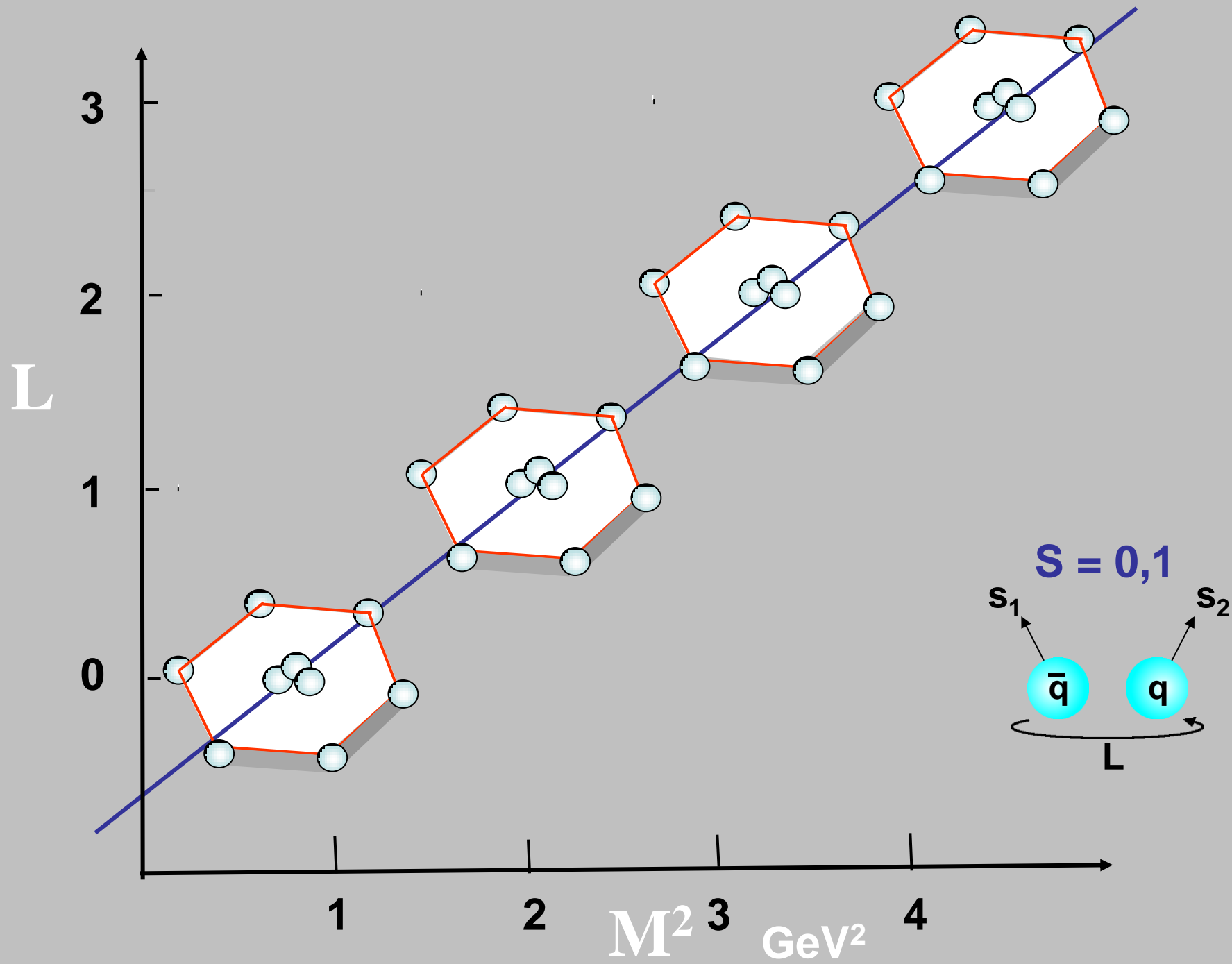


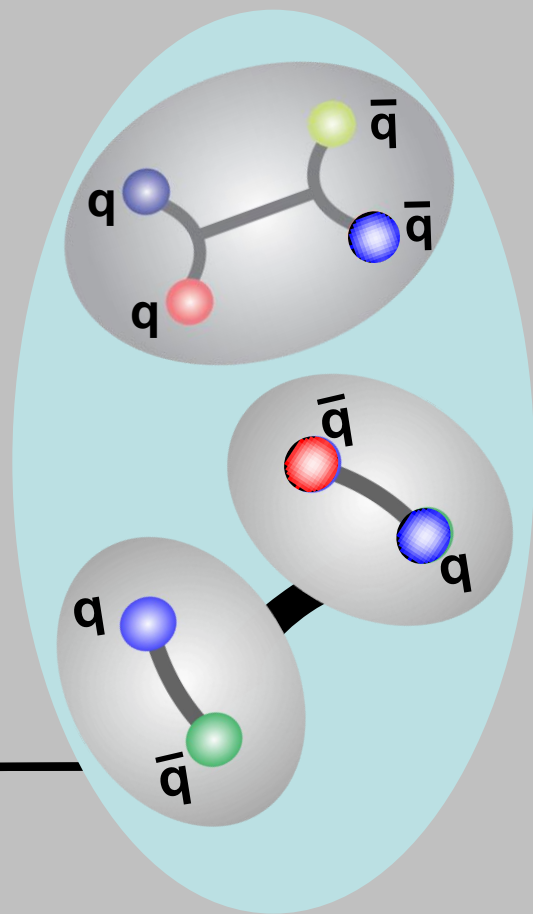
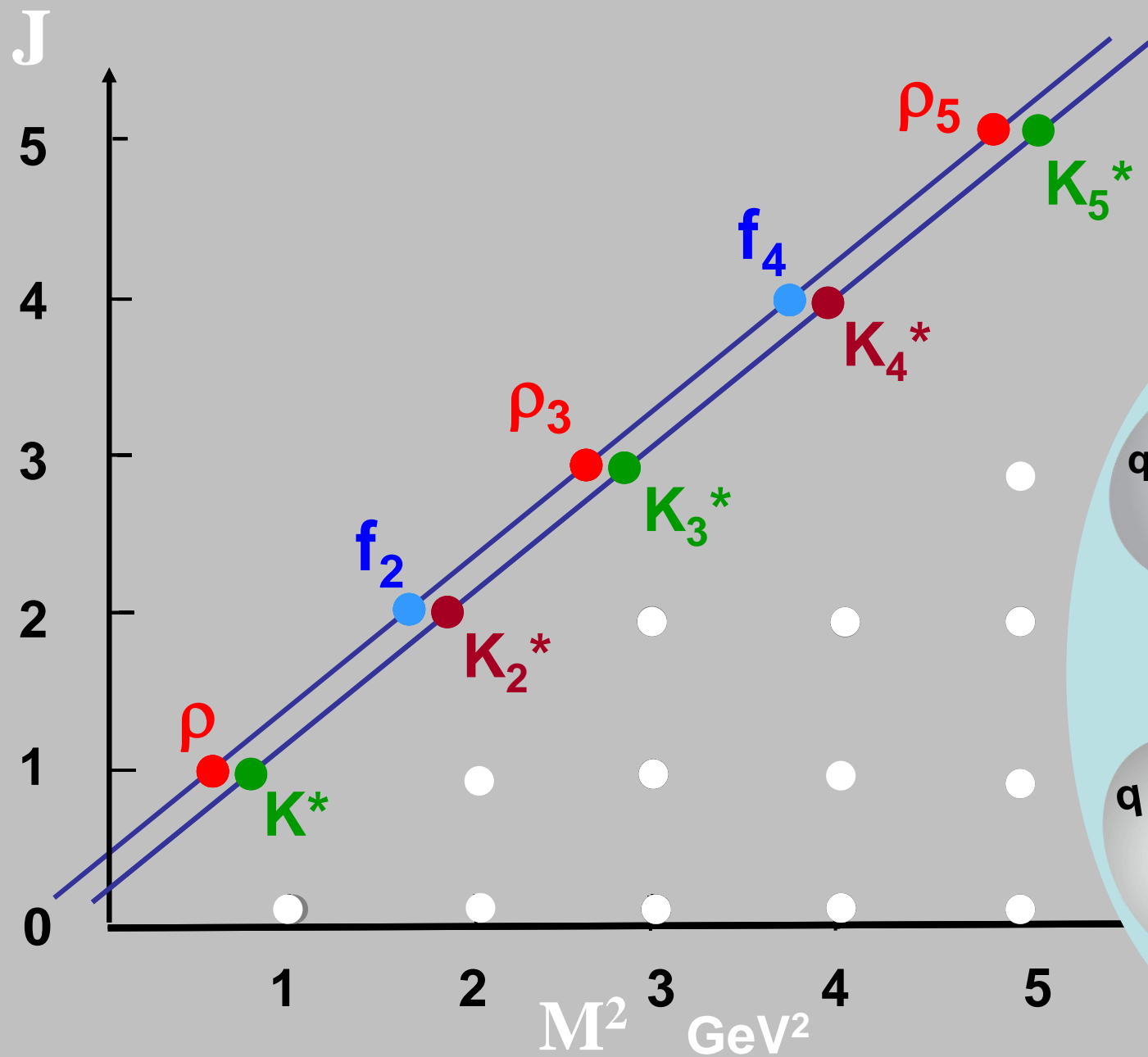
Degrees of freedom

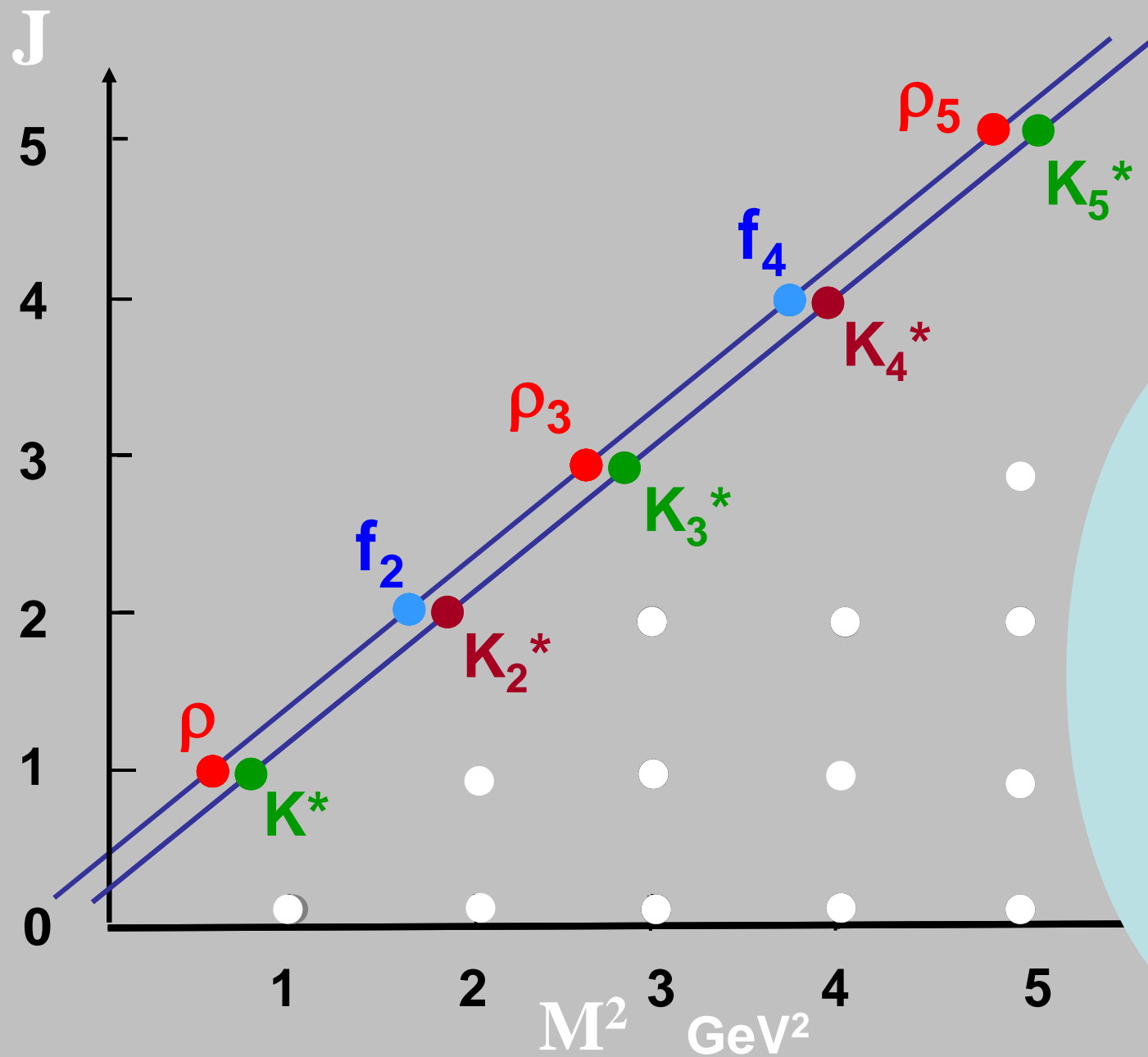


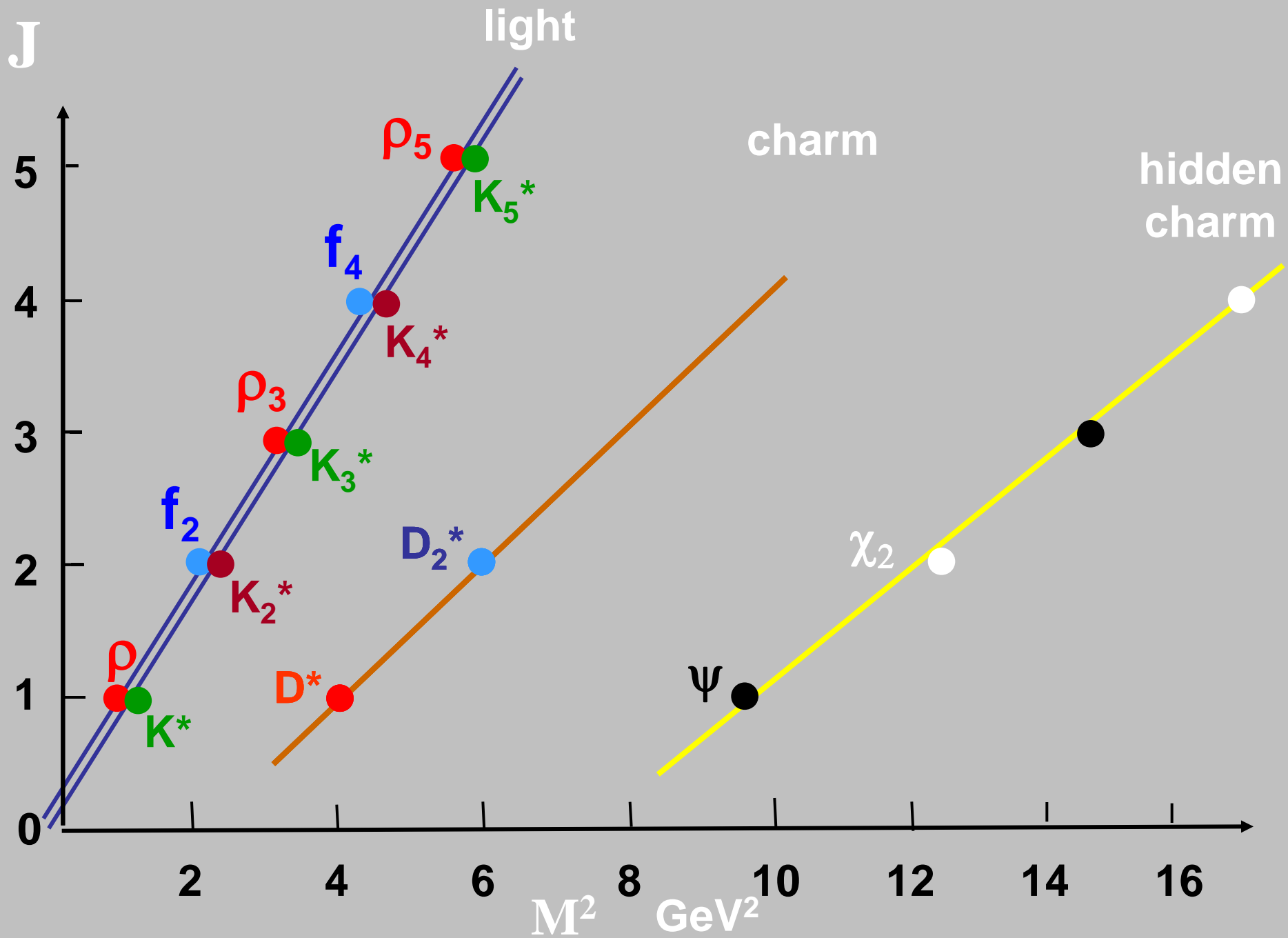
Dynamically generated states





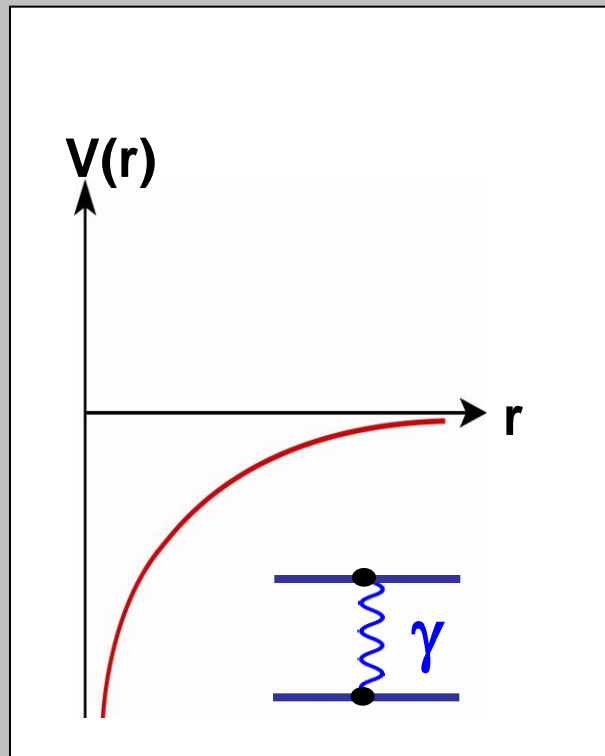
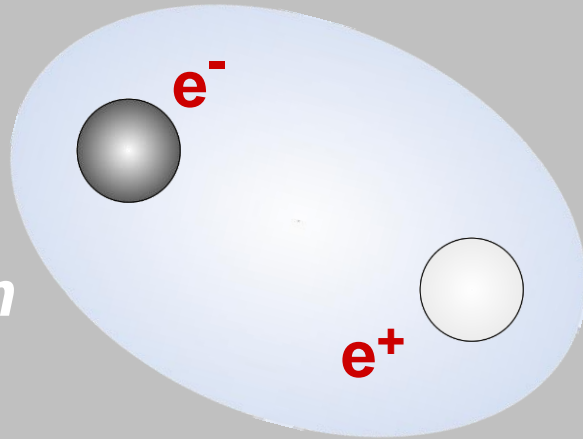






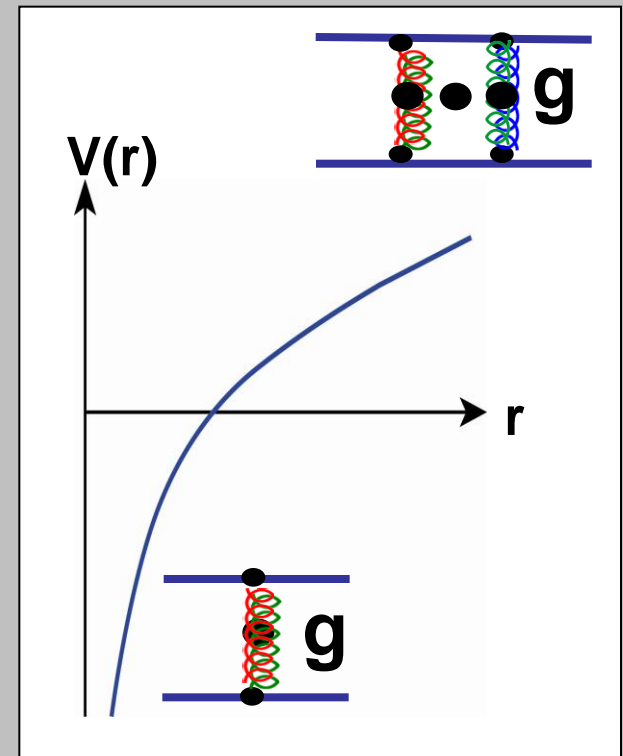
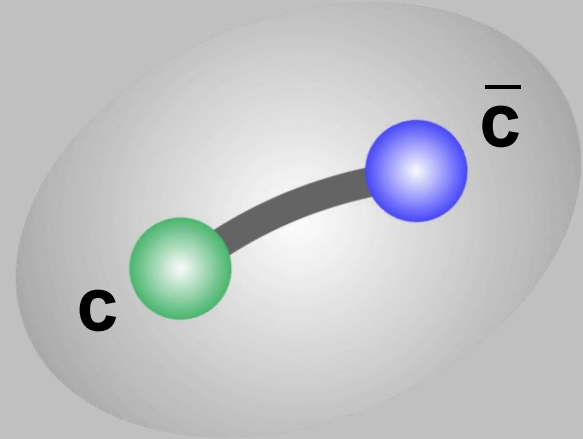
positronium

0.1 nm



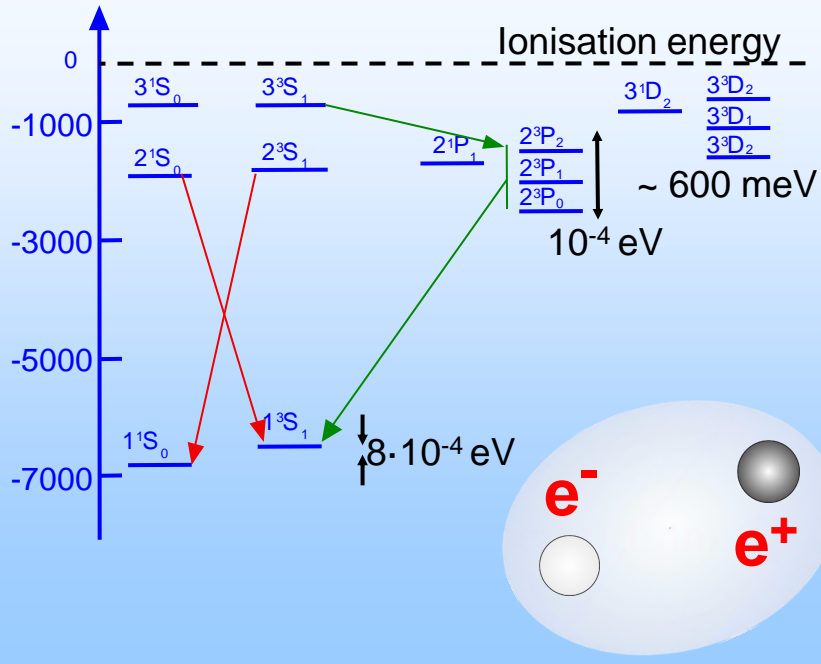
charmonium

1 fm



positronium

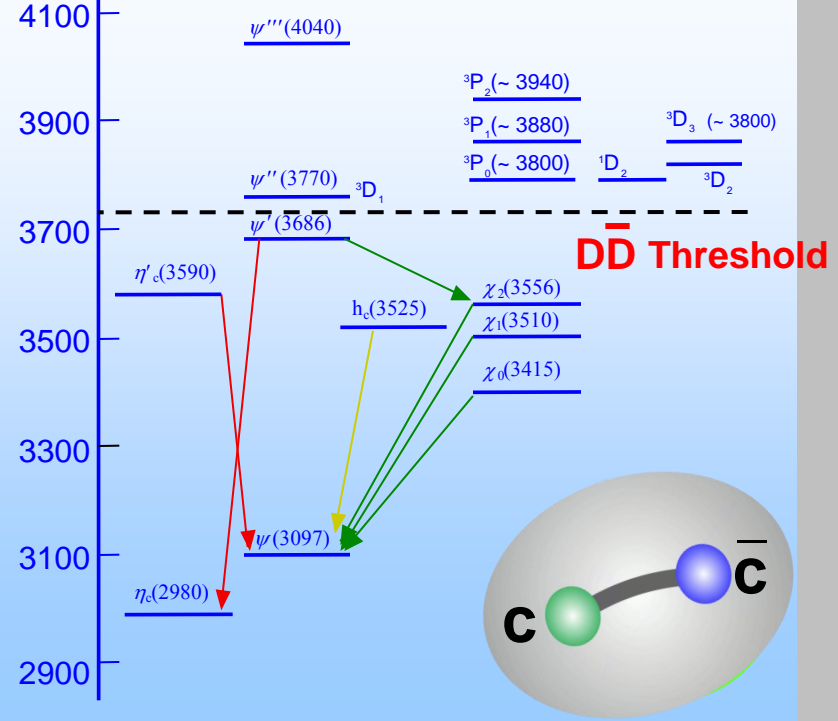
Binding energy [meV]



0.1 nm

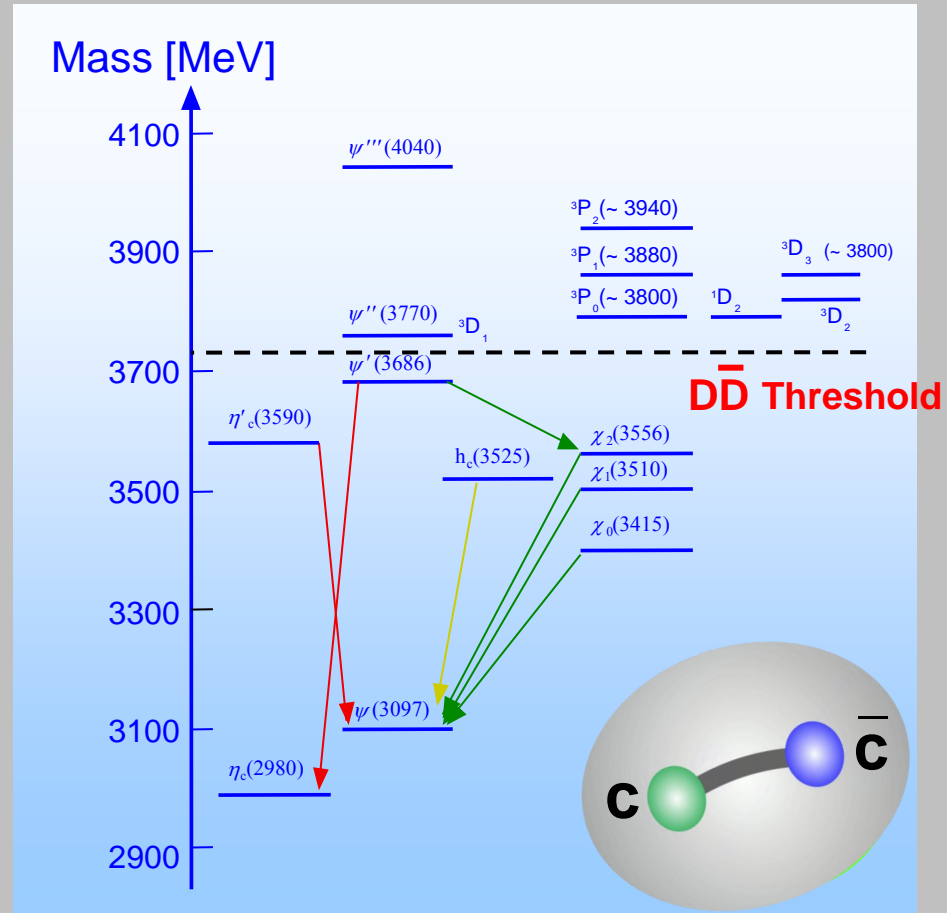
charmonium

Mass [MeV]

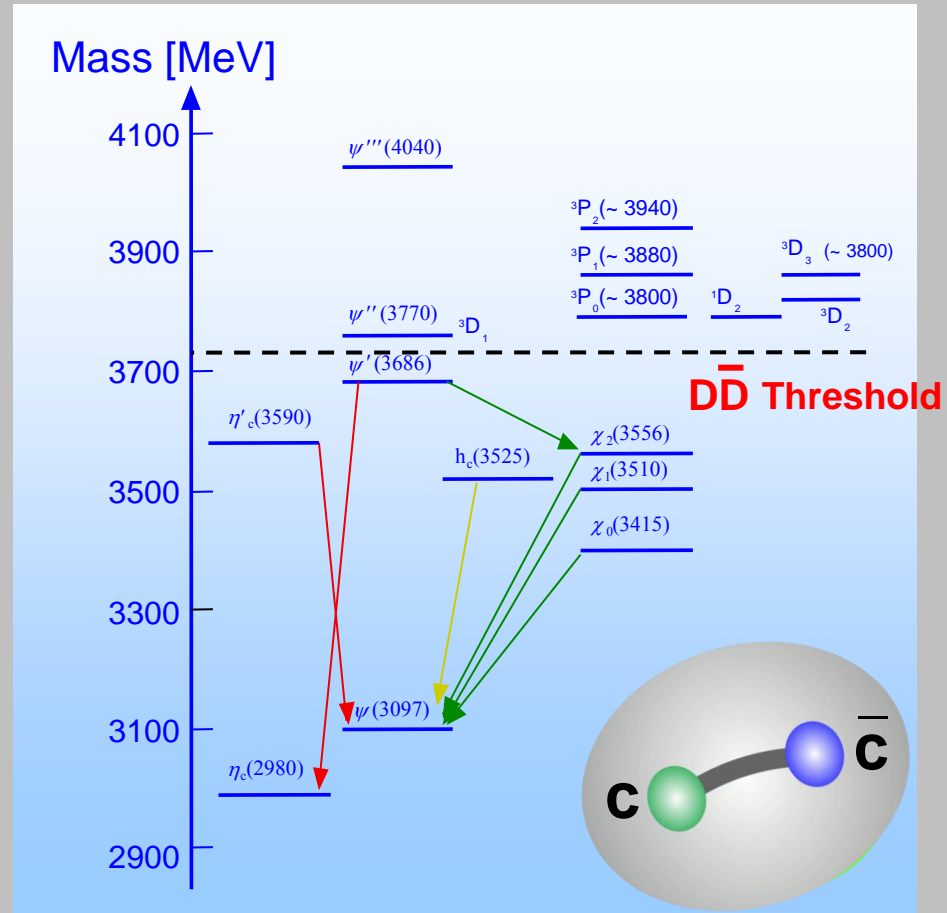
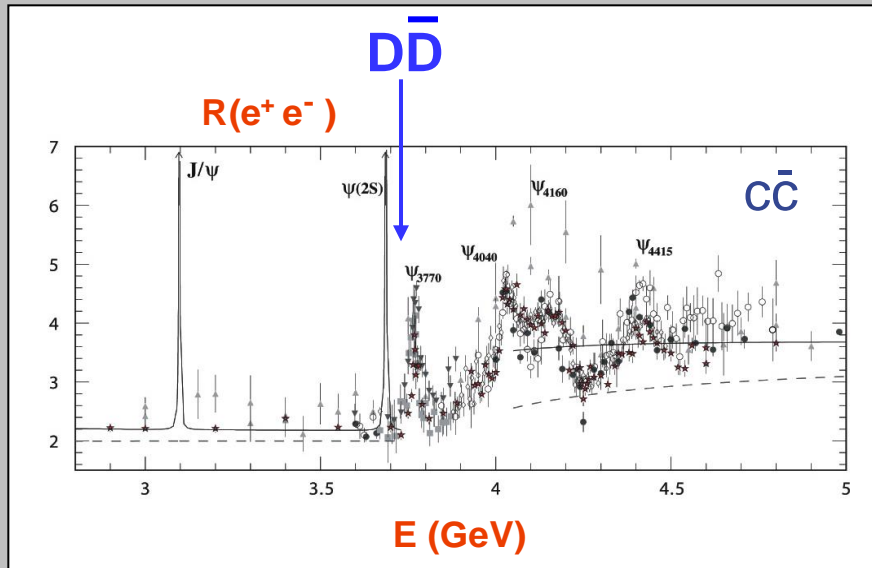


1 fm

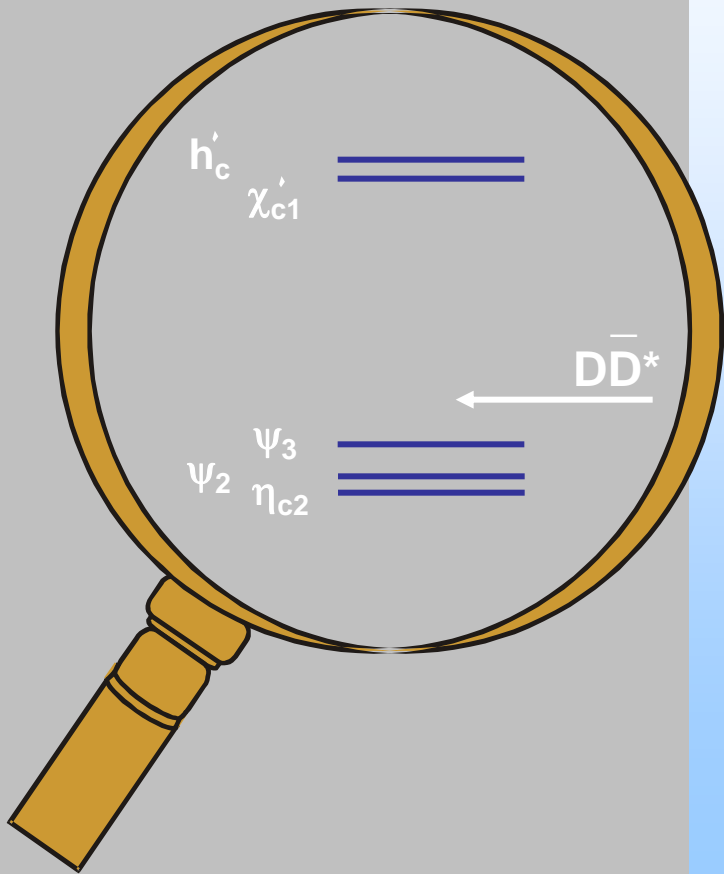
charmonium



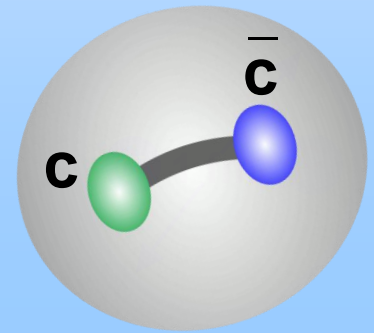
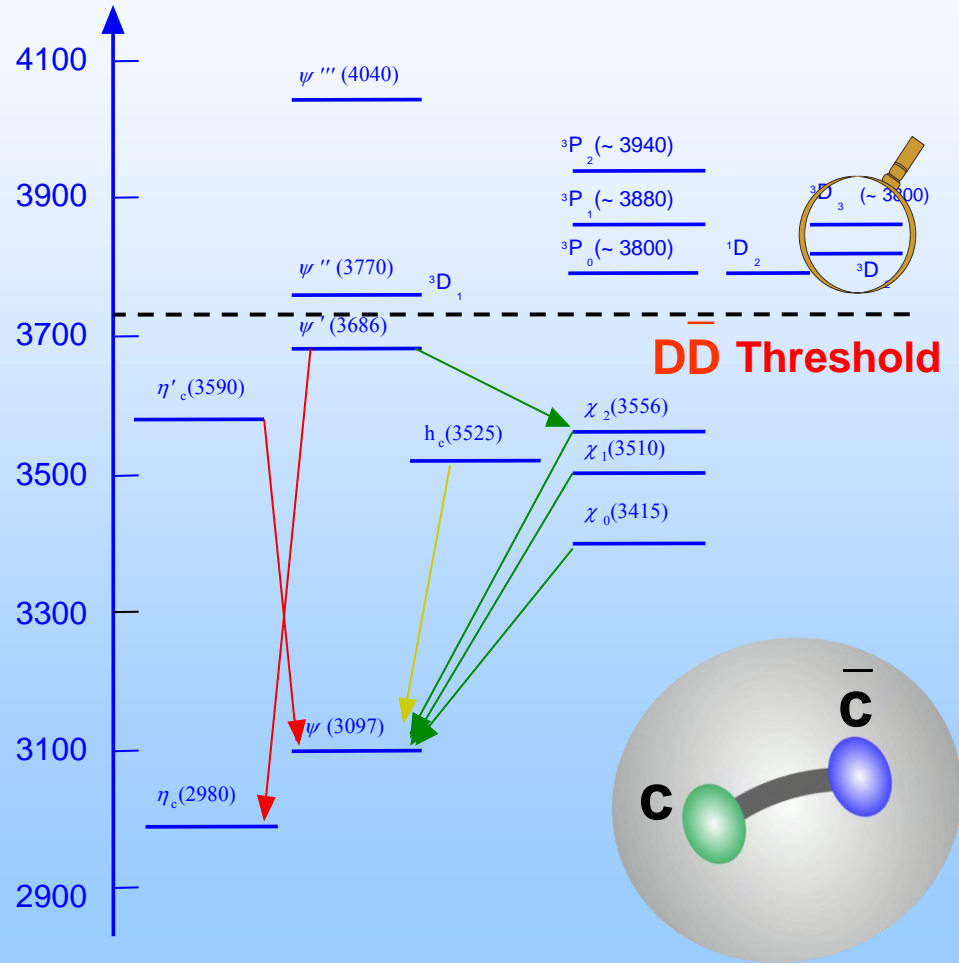
charmonium



charmonium

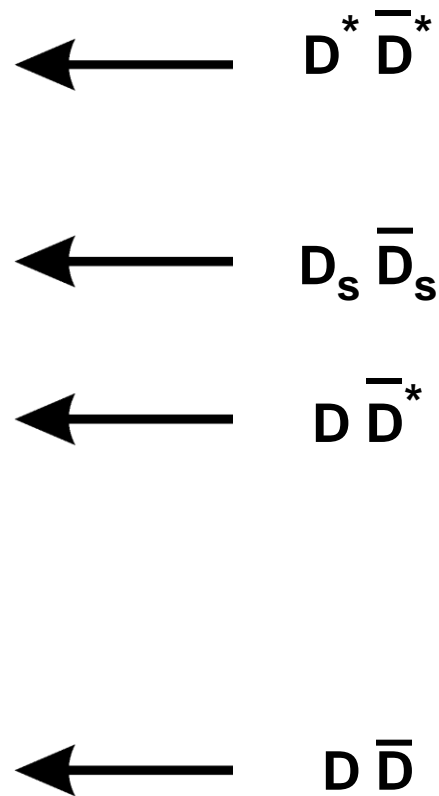
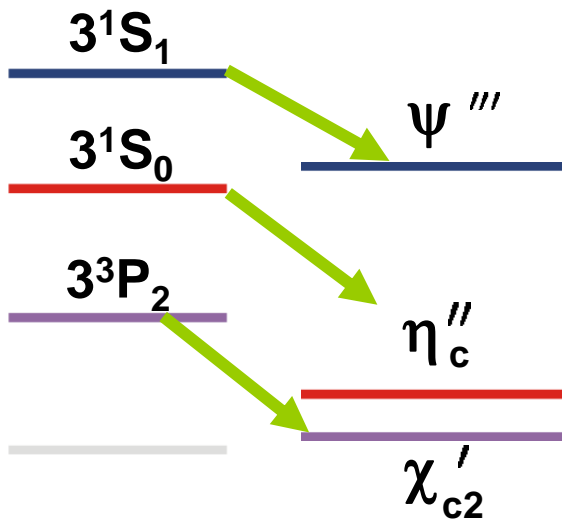
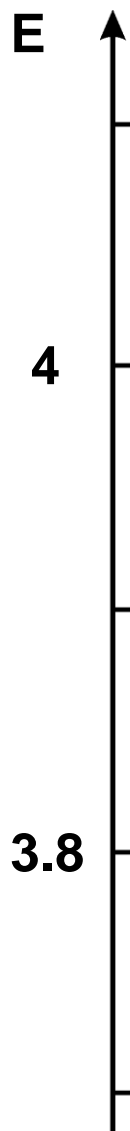


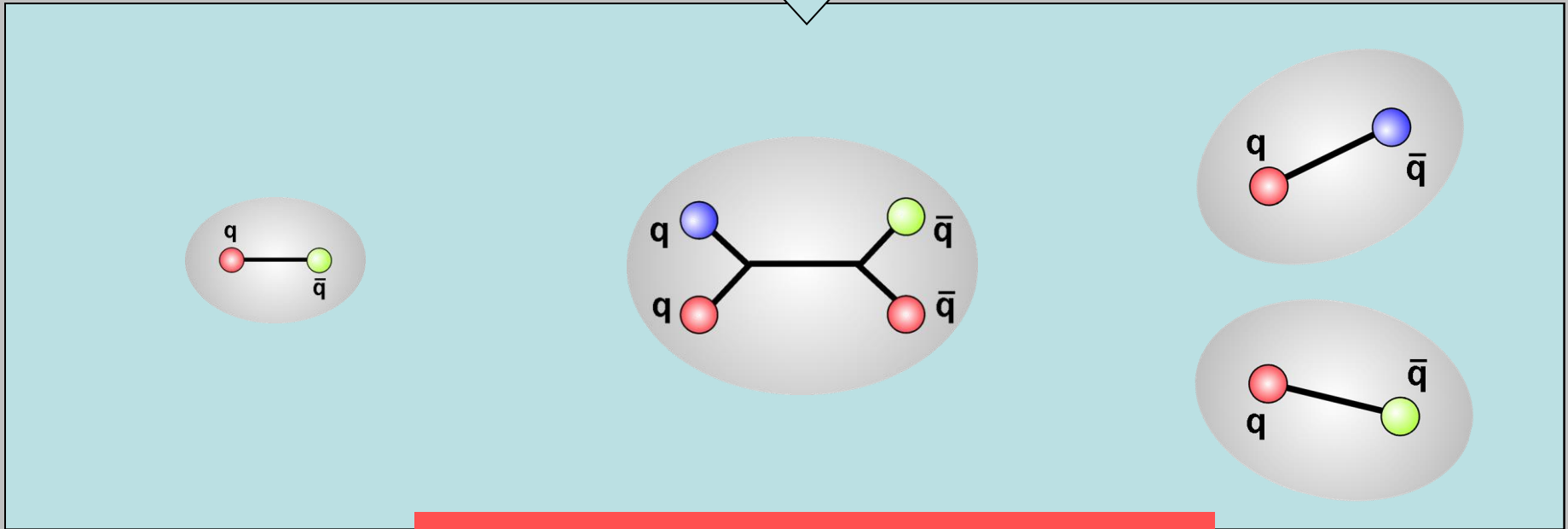
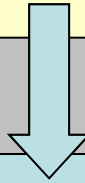
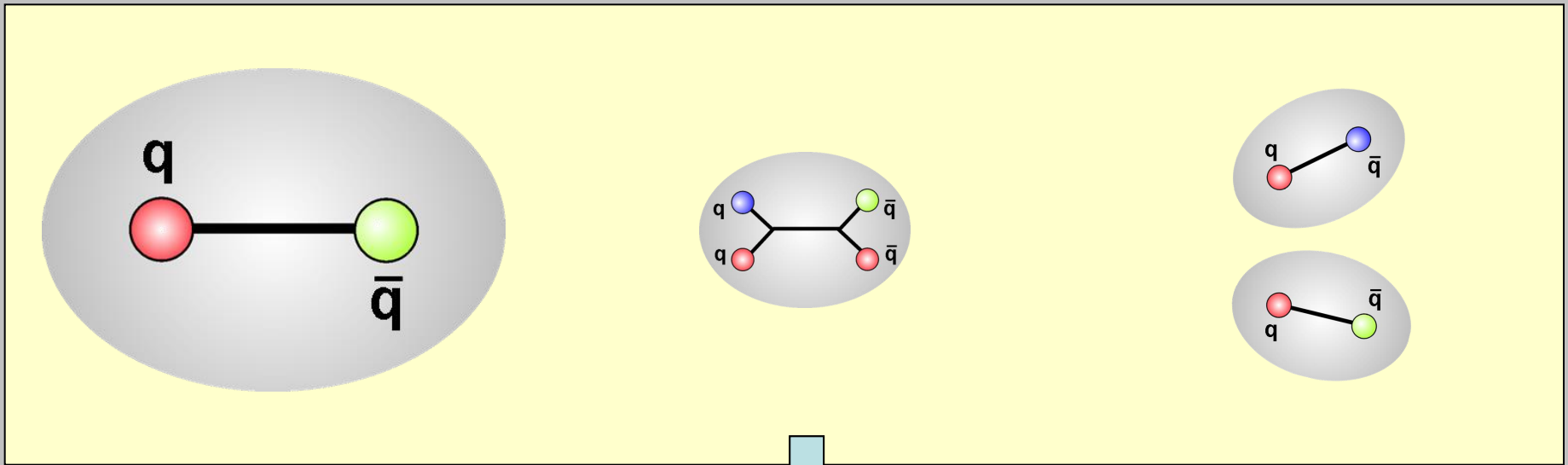
Mass [MeV]



$c\bar{c}$

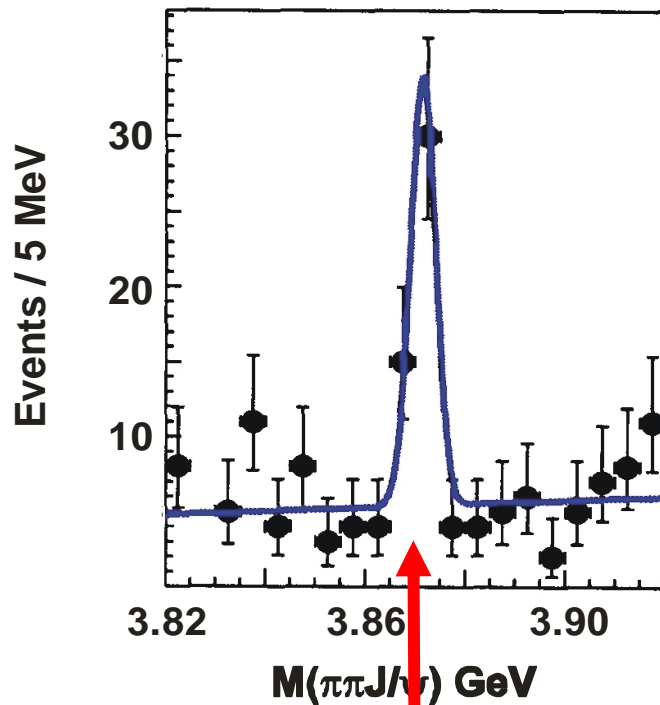
experiment





Dynamically generated states

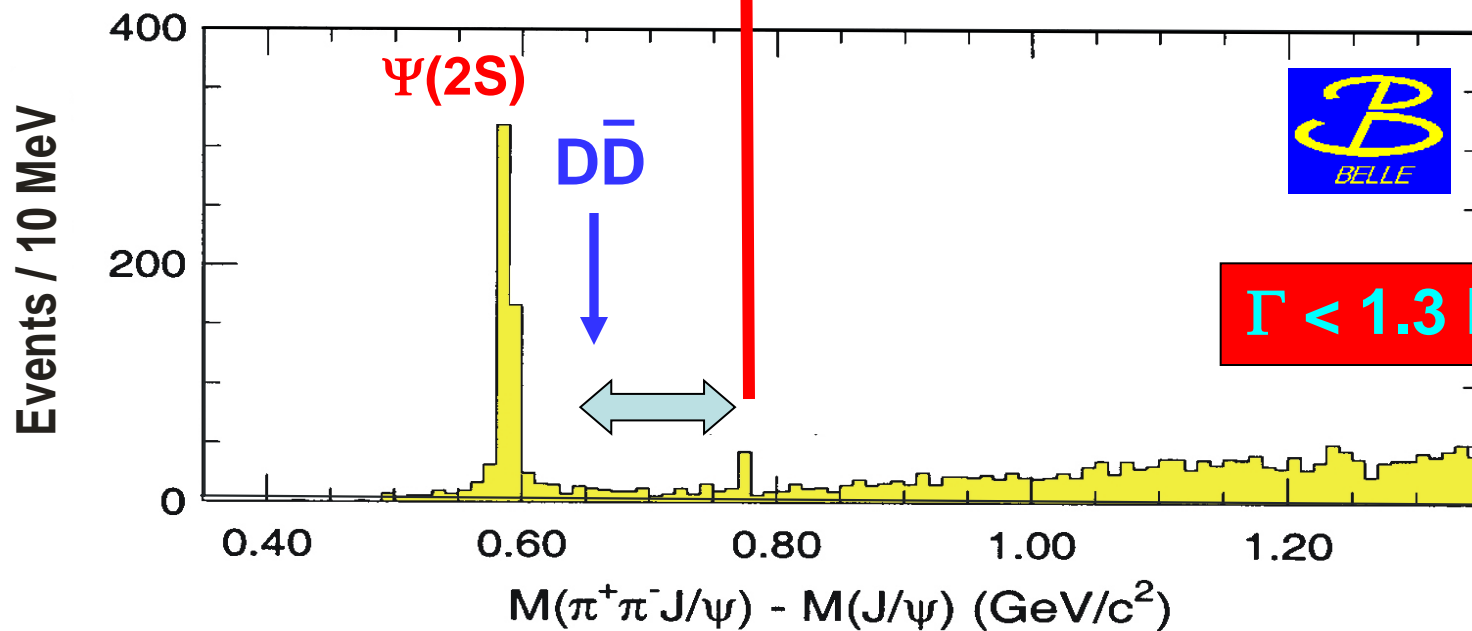
X(3872)



304M B's

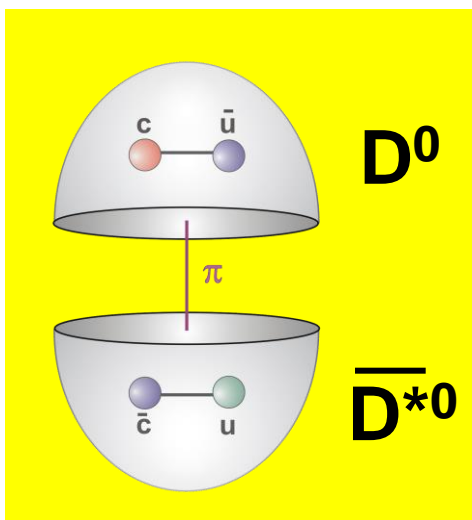
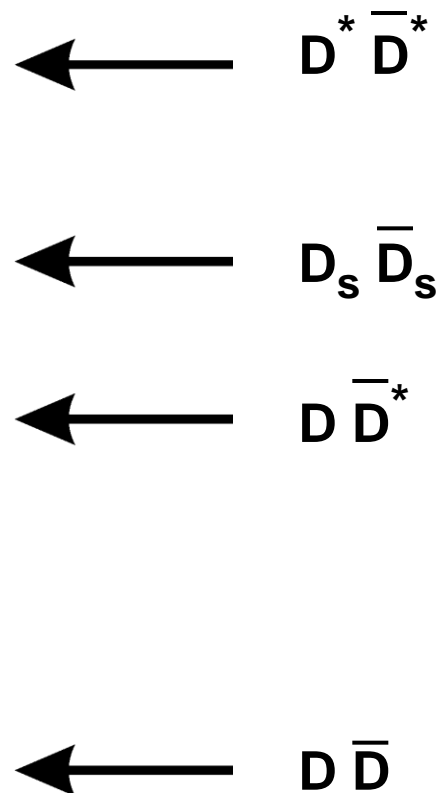
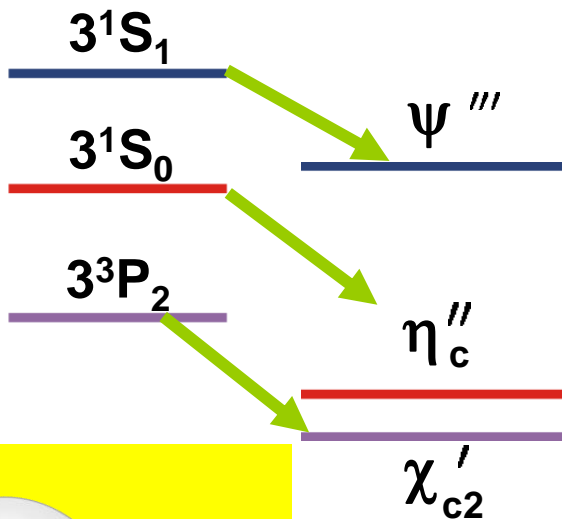
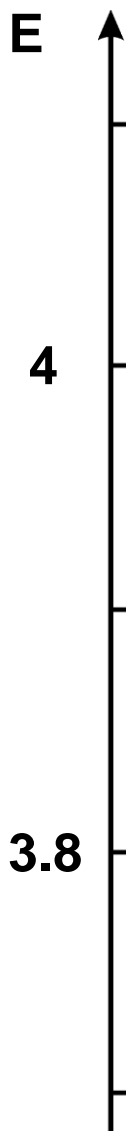
$B \rightarrow KX$

$X \rightarrow \pi^+\pi^- J/\psi$



$c\bar{c}$

experiment



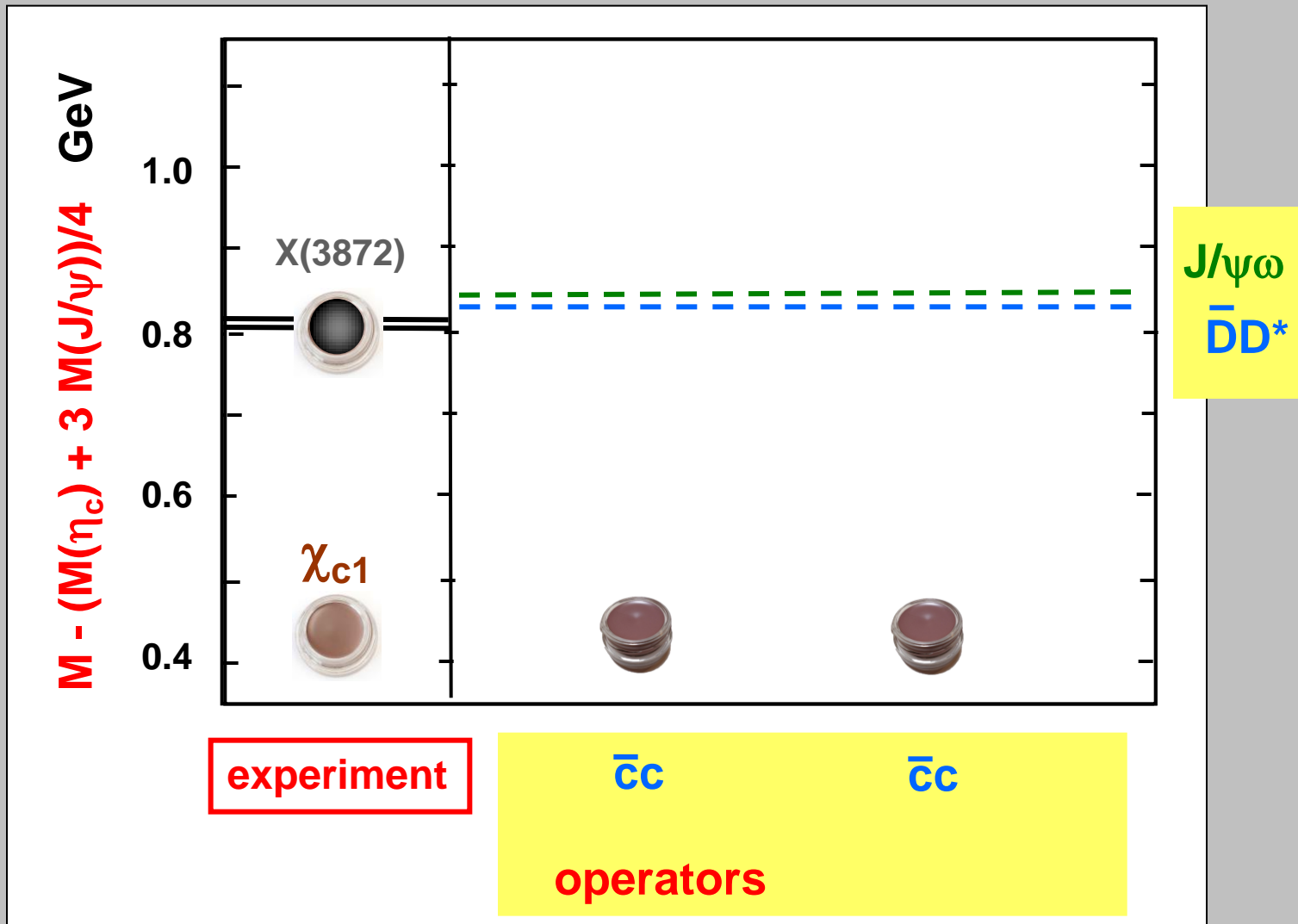
Tornqvist, ...

Barnes & Swanson

Wilson & P

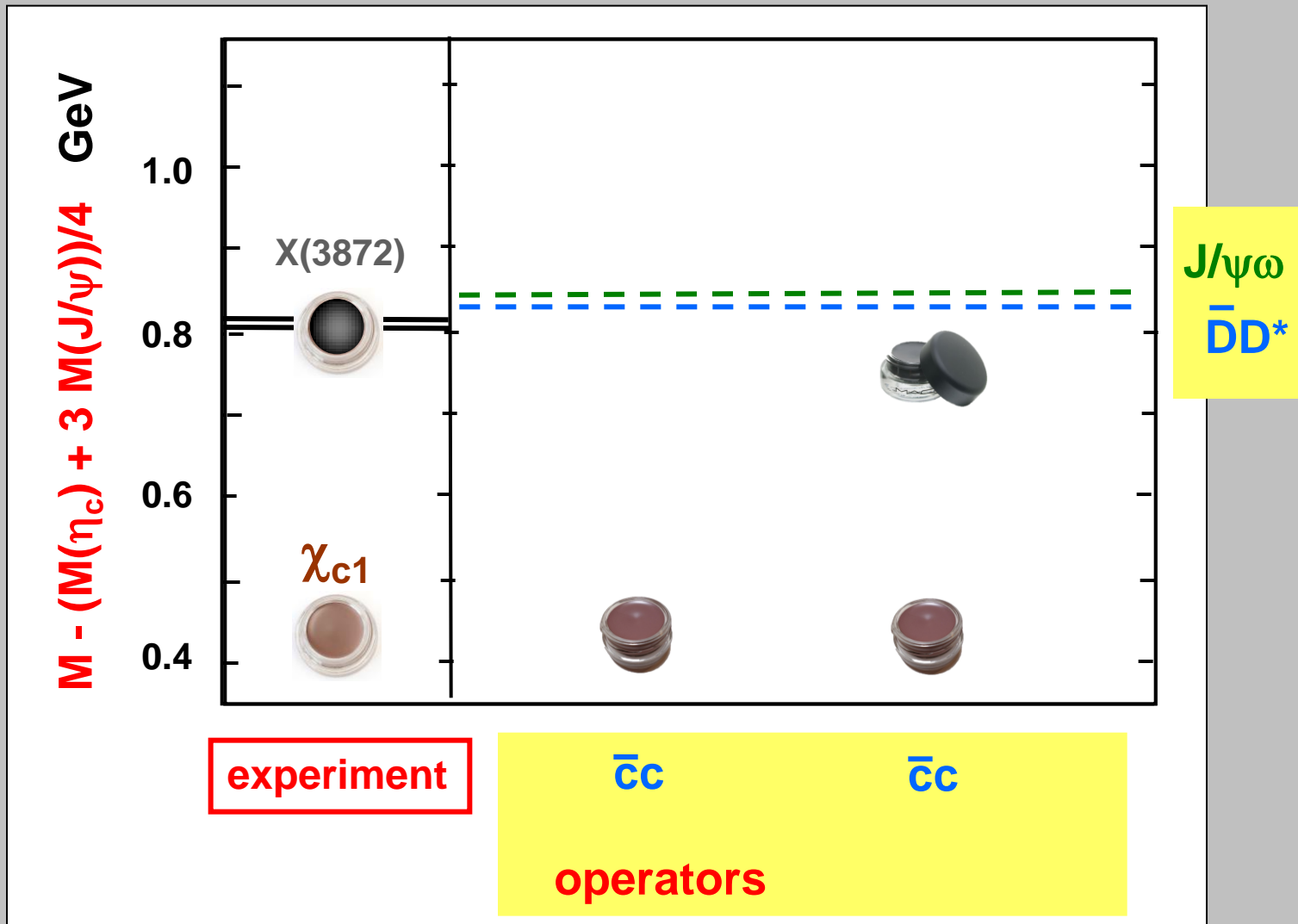
X(3872) & 1^{++} charmonium

m_π 296 MeV

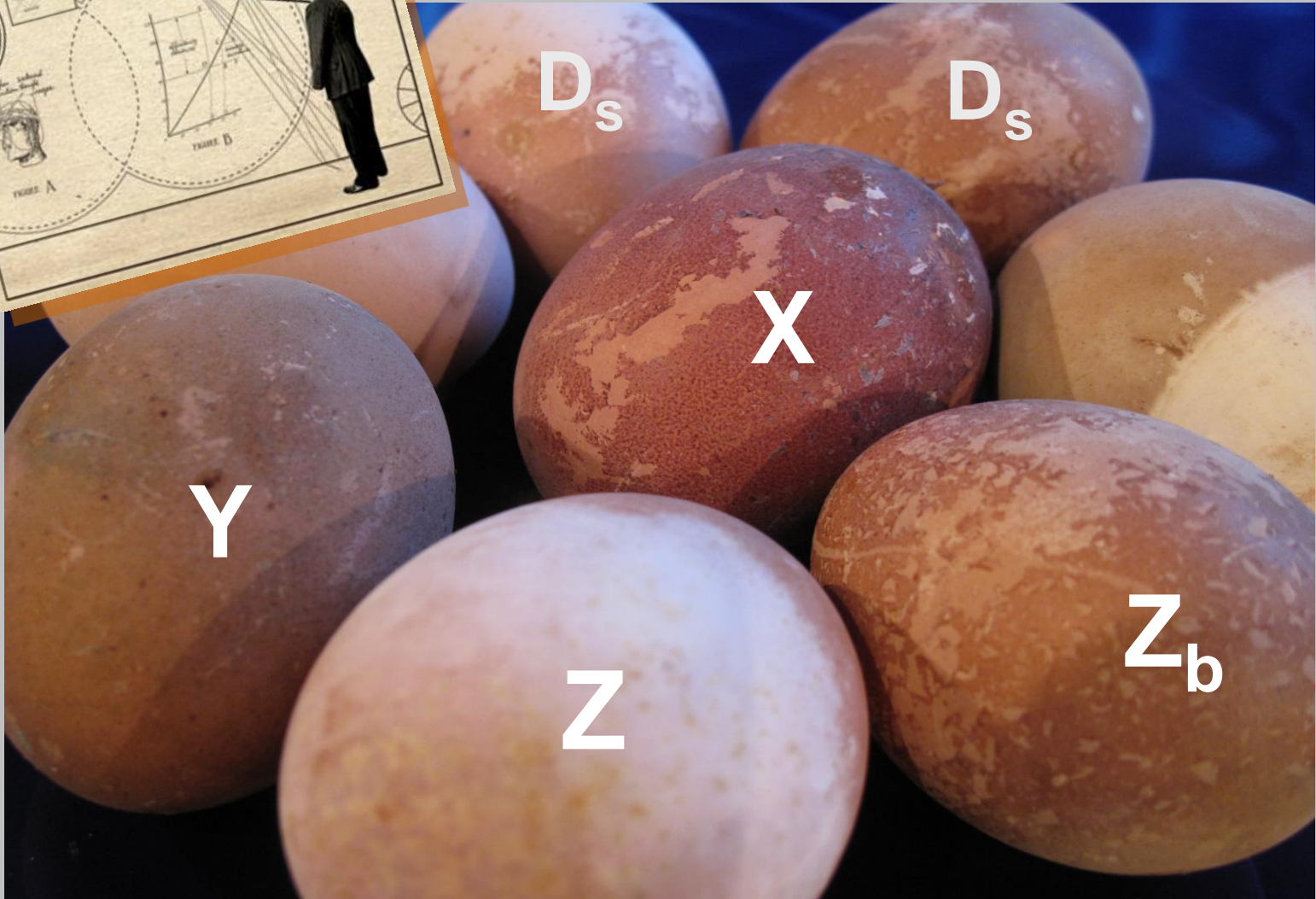
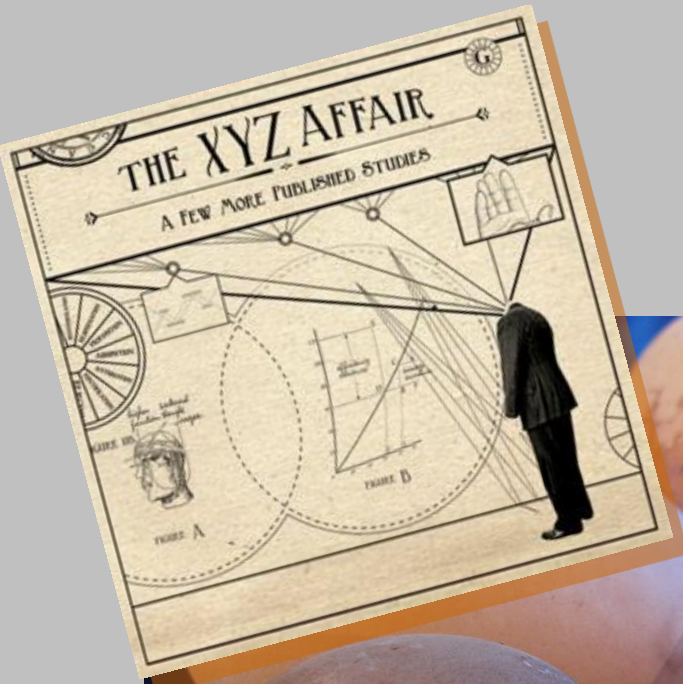


X(3872) & 1^{++} charmonium

m_π 296 MeV

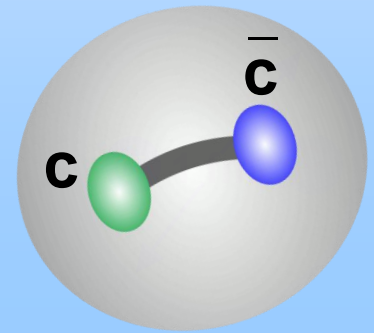
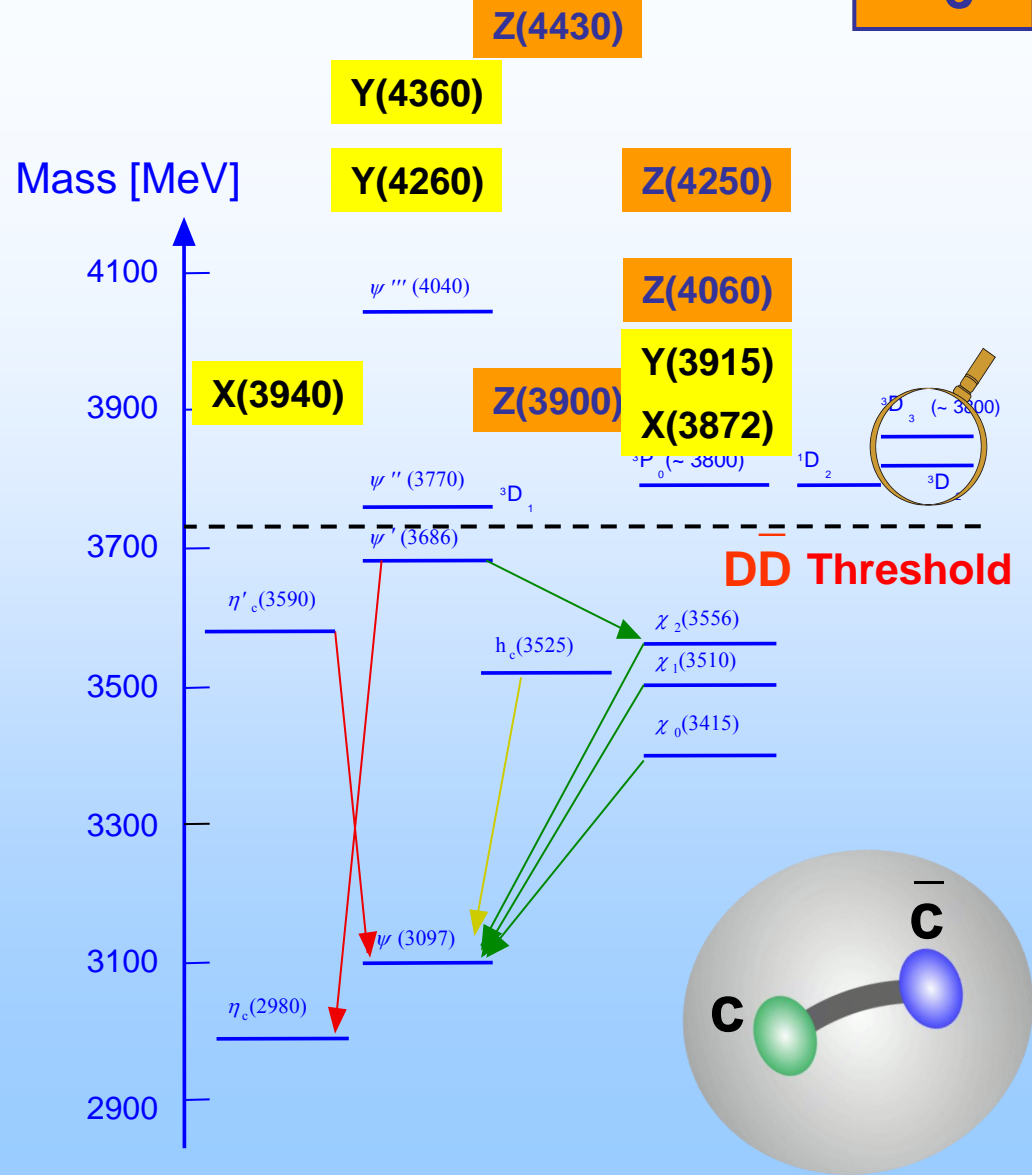
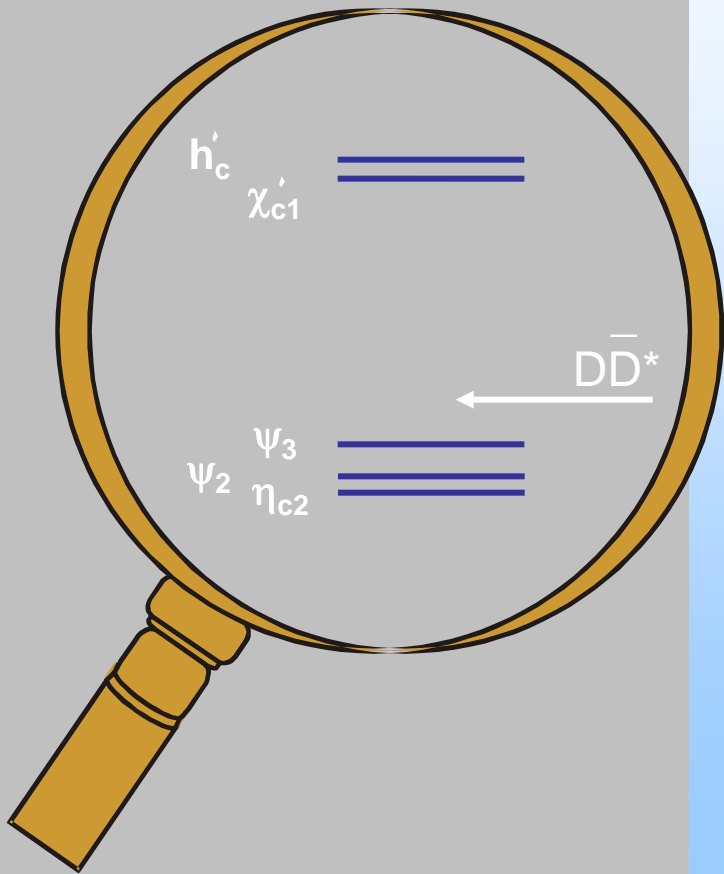


THE XYZ AFFAIR



charmonium

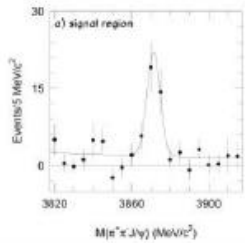
Z_c^\pm



XYZ states

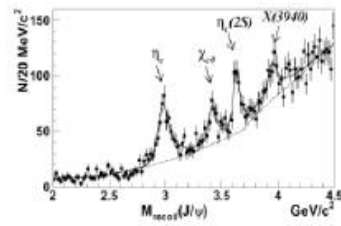
X(3872)

PRL 91,262001 (2003)



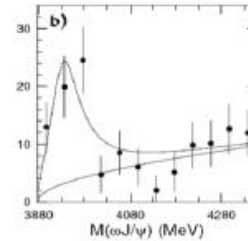
X(3940)

PRL 98,082001 (2007)



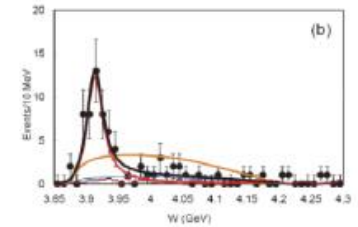
Y(3940)

PRL 94,182002 (2005)



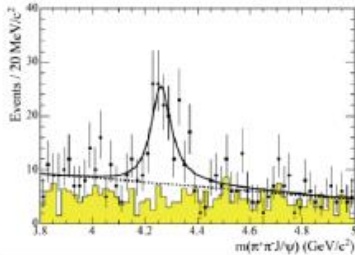
X(3915)

PRL 104,092001 (2010)



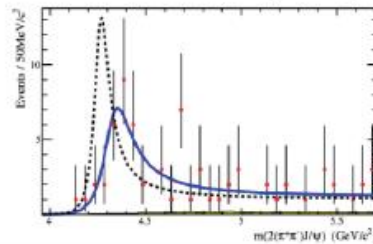
Y(4260)

PRL 95,142001 (2005)



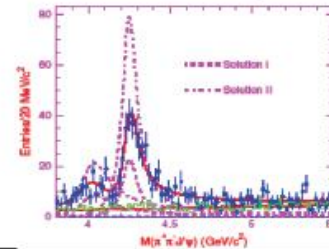
Y(4350)

PRL 98,212001 (2007)



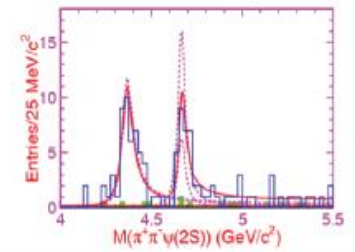
Y(4008)

PRL 99,182004 (2007)



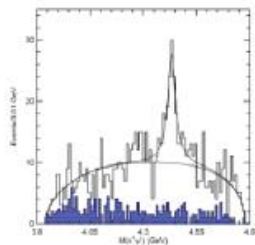
Y(4660)

PRL 99,142002 (2007)



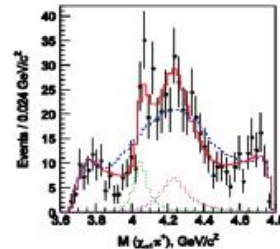
Z⁻(4430)

PRL 100,142001 (2008)



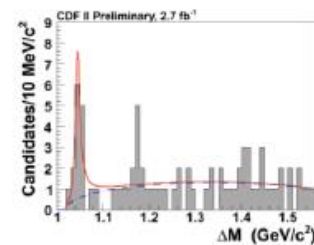
Z₁⁻/Z₂⁻

PRD 78,072004 (2008)



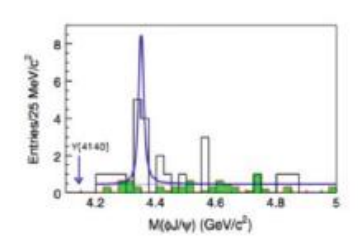
Y(4140)

PRL 102,242002 (2009)



X(4350)

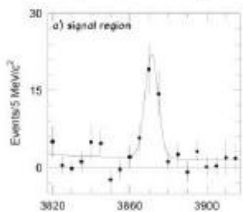
PRL 104,112004 (2010)



XYZ states

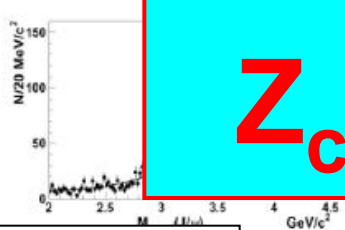
X(3872)

PRL 91,262001 (2003)



X(3940)

PRL 98,082001 (2007)



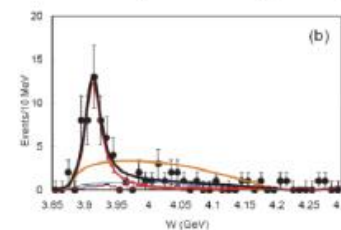
Y(3940)

PRL 94,182002 (2005)



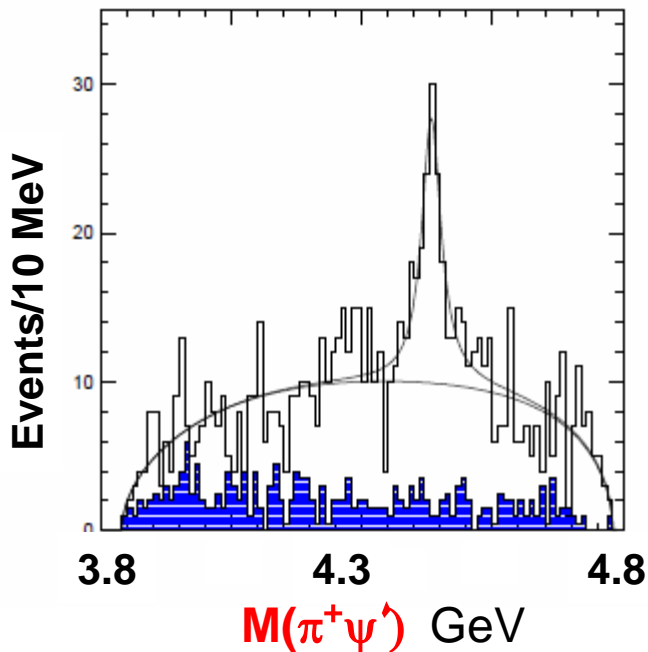
X(3915)

PRL 104,092001 (2010)



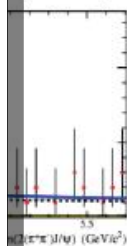
Z_c^\pm (4430)

$B \rightarrow K\pi^+\psi'$



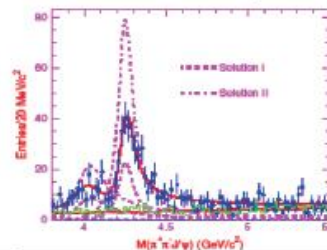
0)

(2007)



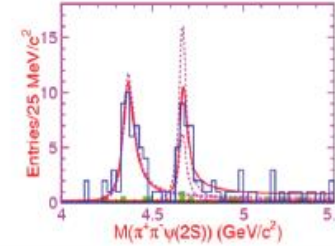
Y(4008)

PRL 99,182004 (2007)



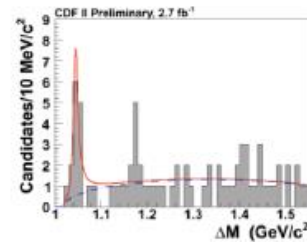
Y(4660)

PRL 99,142002 (2007)



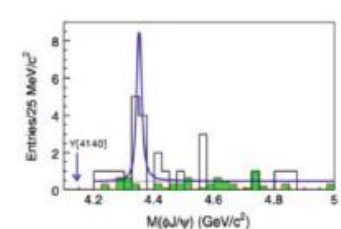
Y(4140)

PRL 102,242002 (2009)

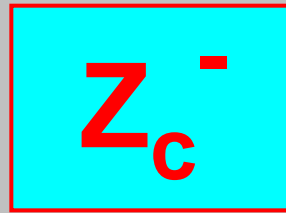
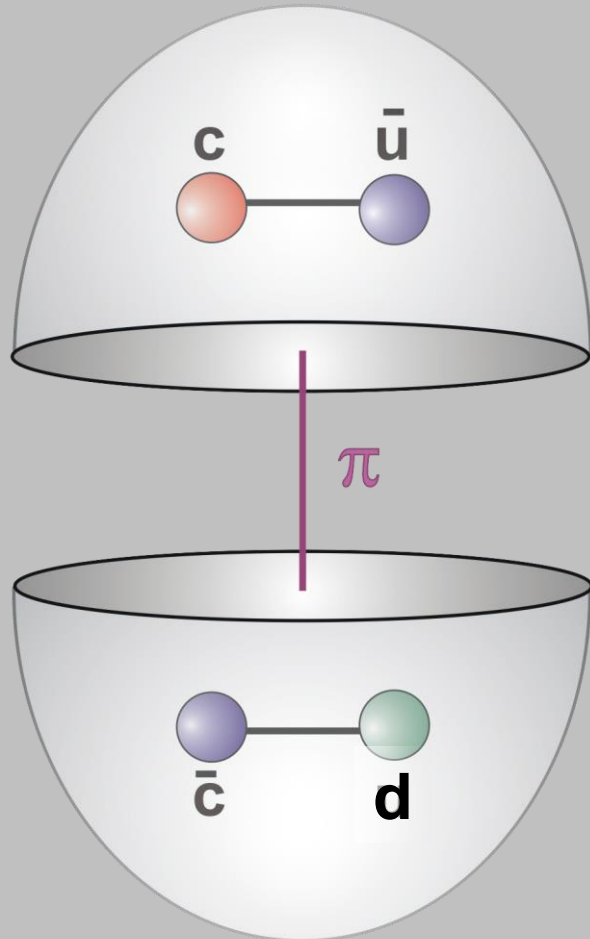


X(4350)

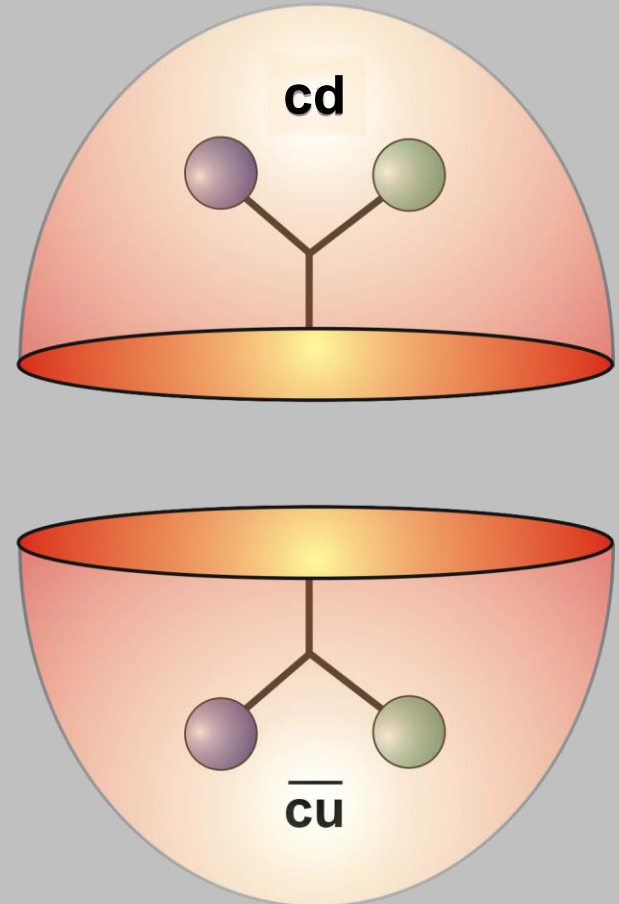
PRL 104,112004 (2010)



molecule



tetraquark



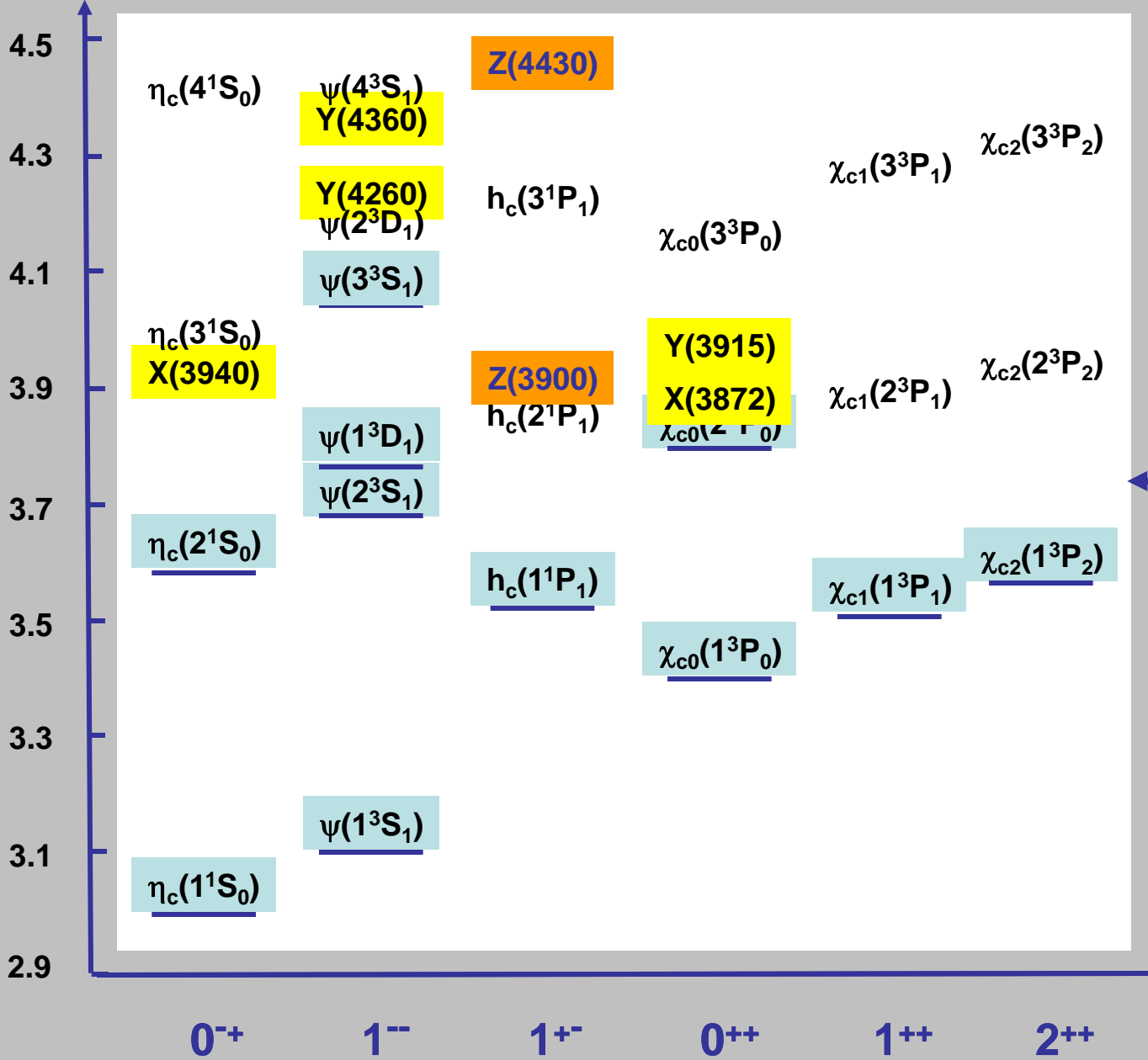


$\bar{D}D$

threshold



Mass (GeV)



Z(4250)

Z(4060)

J^{PC}

0^{-+}

1^{-}

1^{+-}

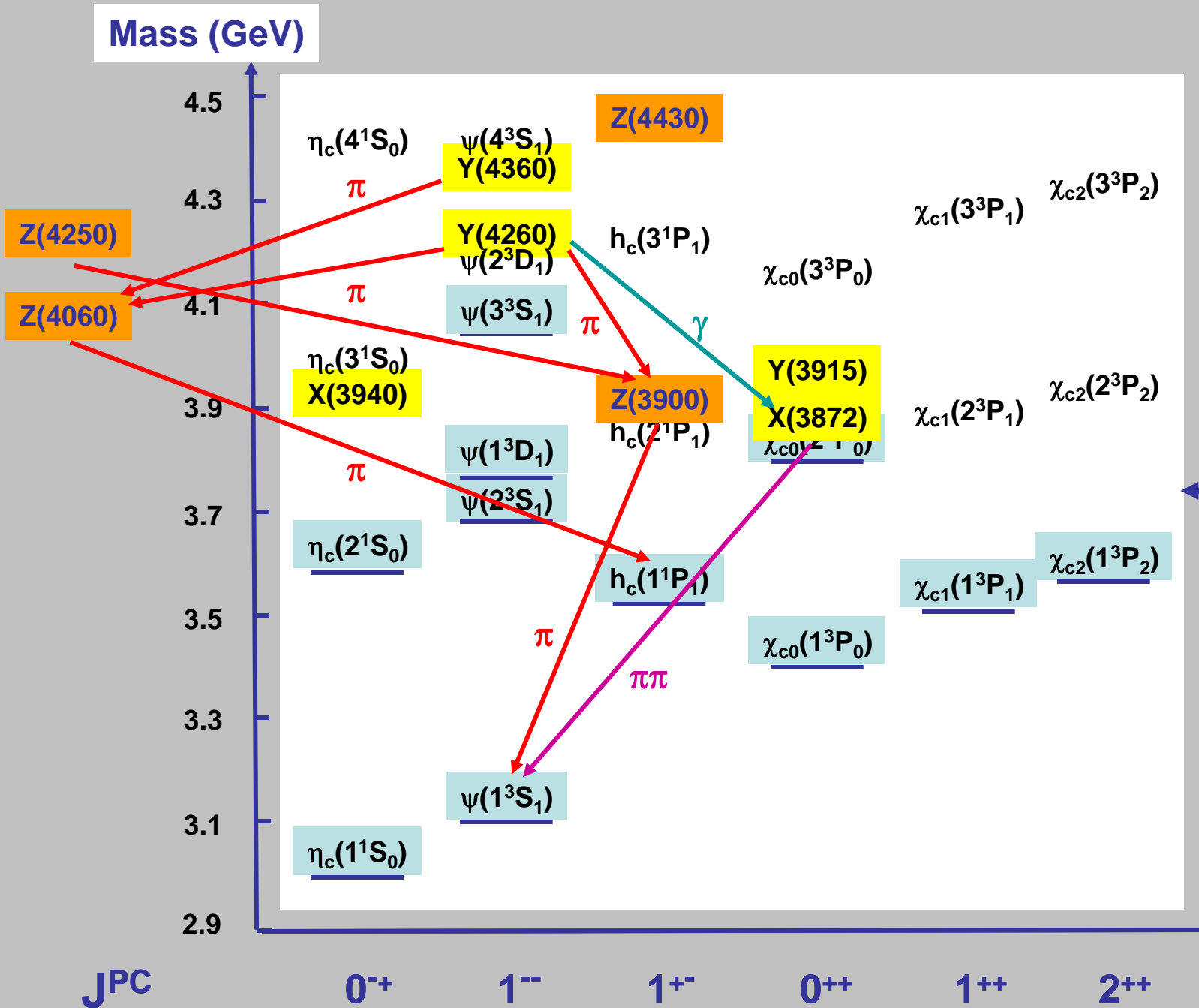
0^{++}

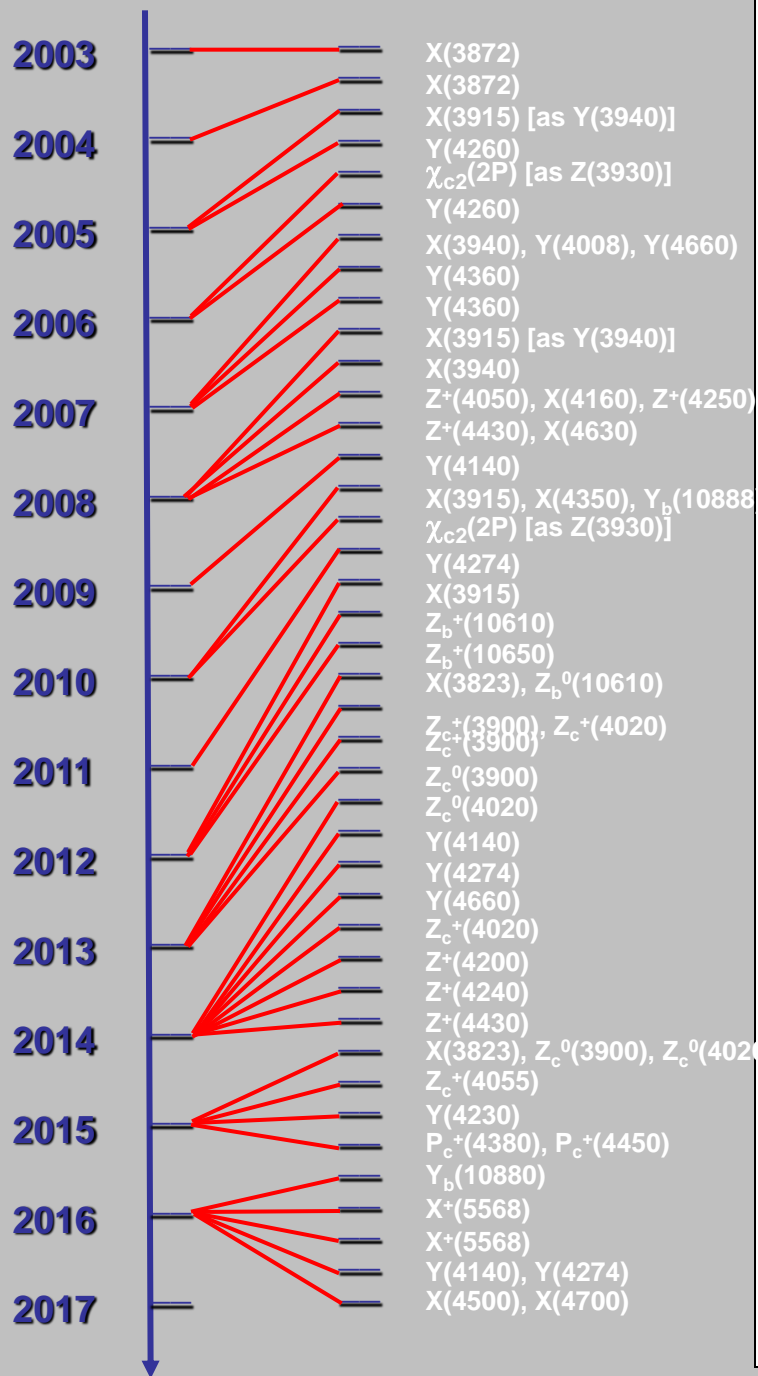
1^{++}

2^{++}



$\bar{D}D$
threshold





Observed	Confirmed
Belle	CDF, D0 Belle BaBar
Belle	CLEO-c
Belle BaBar	Belle BaBar Belle
Belle	CDF
Belle	BaBar
CDF	BaBar Belle Belle
Belle	Belle
BESIII	Belle
CLEO-c BESIII	D0, CMS CMS BaBar
BESIII	Belle LHCb LHCb BESIII
Belle BESIII LHCb	NOT Belle
D0	NOT LHCb LHCb
LHCb	

2003



X(3872)

Observed

Belle

Confirmed

2004



X(3872)
X(3915) [as Y(3940)]

Belle

CDF, D0
Belle
BaBar

2005



Y(4260)
 $\chi_{c2}(2P)$ [as Z(3930)]

CLEO-c

2006



Y(4260)
X(3940), Y(4008), Y(4360)

Essential to confirm all such states and their connections with robust analyses

2007



Y(4360)
X(3915) [as Y(3940)]

X(3940)
Z⁺(4050), X(4160)

Z⁺(4430), X(4630)

Y(4140)

2008



X(3915), X(4350), Y_b(10888)

Belle

BaBar

$\chi_{c2}(2P)$ [as Z(3930)]

CDF

2009



Y(4274)
X(3915)
Z_b⁺(10610)

BaBar
Belle
Belle

2010



Z_b⁺(10650)
X(3823), Z_b⁰(10610)

Belle

Z_c⁺(3900), Z_c⁺(4020)

BESIII

Belle

2011



Z_c⁰(3900)
Z_c⁰(4020)

CLEO-c
BESIII

2012



Y(4140)
Y(4274)
Y(4660)

D0, CMS
CMS
BaBar

2013



Z_c⁺(4020)
Z⁺(4200)

BESIII

Belle
LHCb
LHCb
BESIII

2014



Z⁺(4240)
Z⁺(4430)

X(3823), Z_c⁰(3900), Z_c⁰(4020)

Belle

BESIII
LHCb

2015



Z_c⁺(4055)
Y(4230)
P_c⁺(4380), P_c⁺(4450)

NOT Belle

2016



Y_b(10880)
X⁺(5568)

D0

NOT LHCb
LHCb

2017



X⁺(5568)
Y(4140), Y(4274)

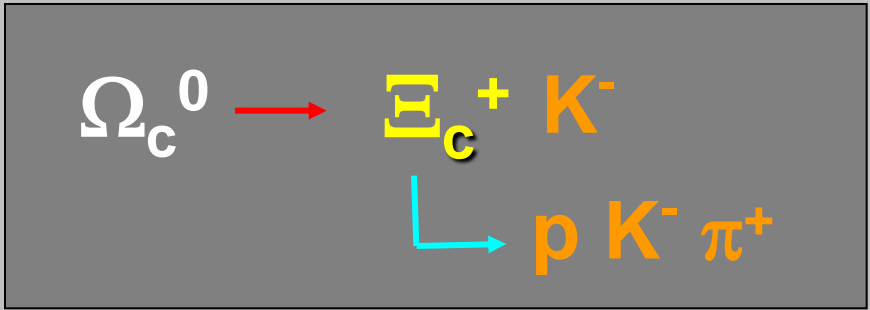
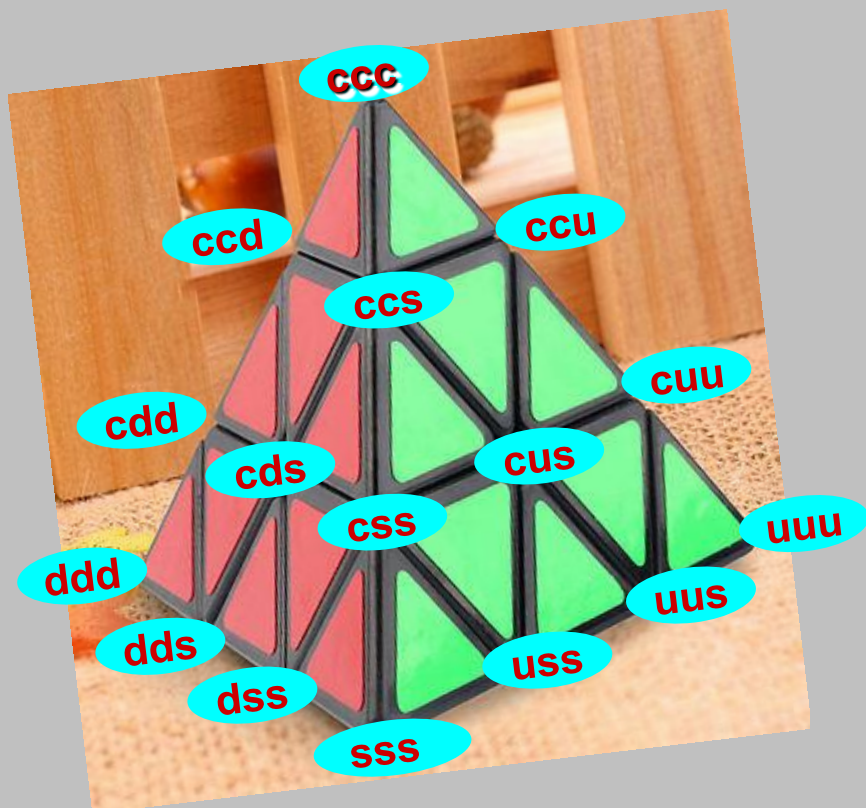
LHCb

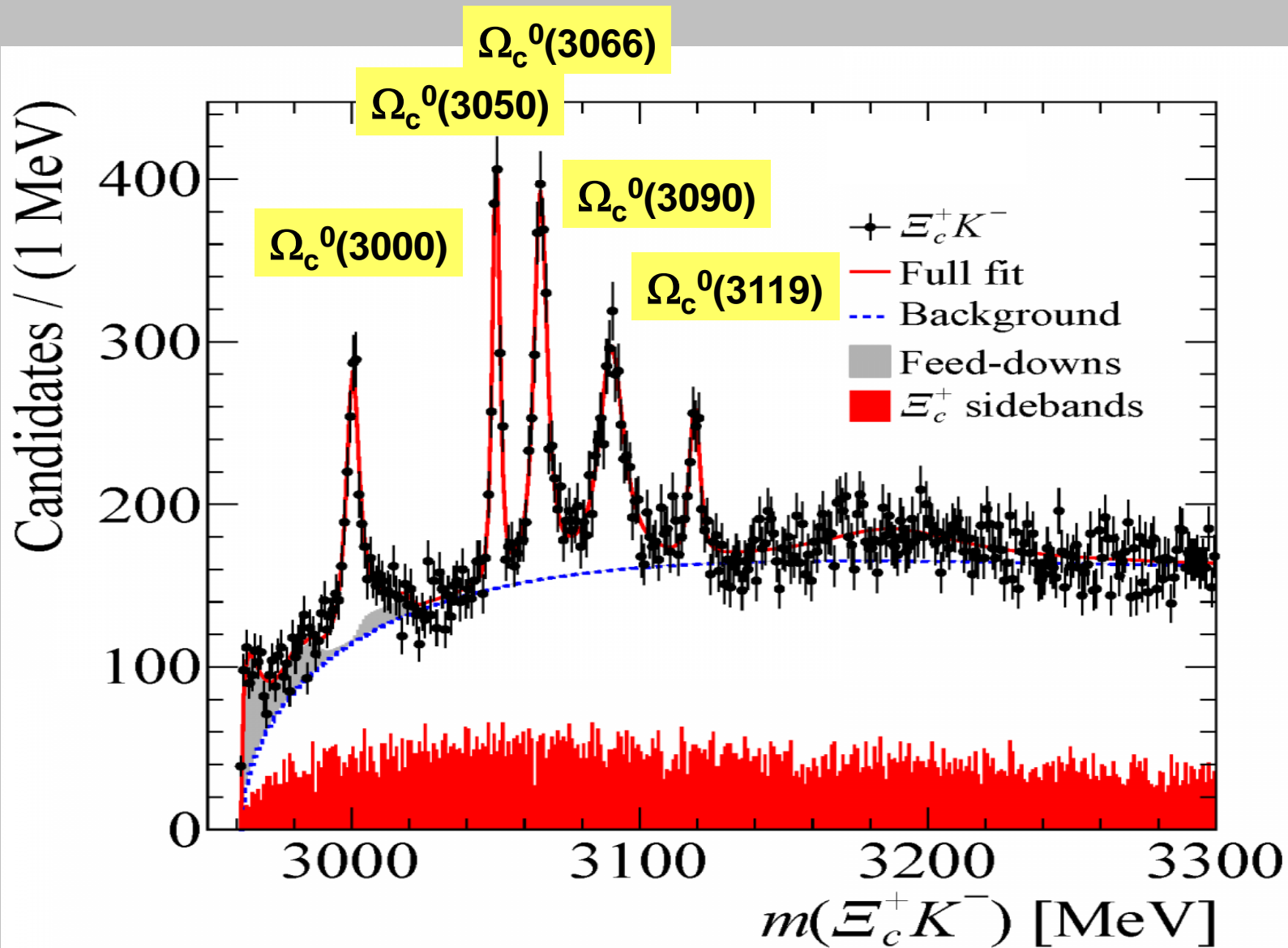
X(4500), X(4700)



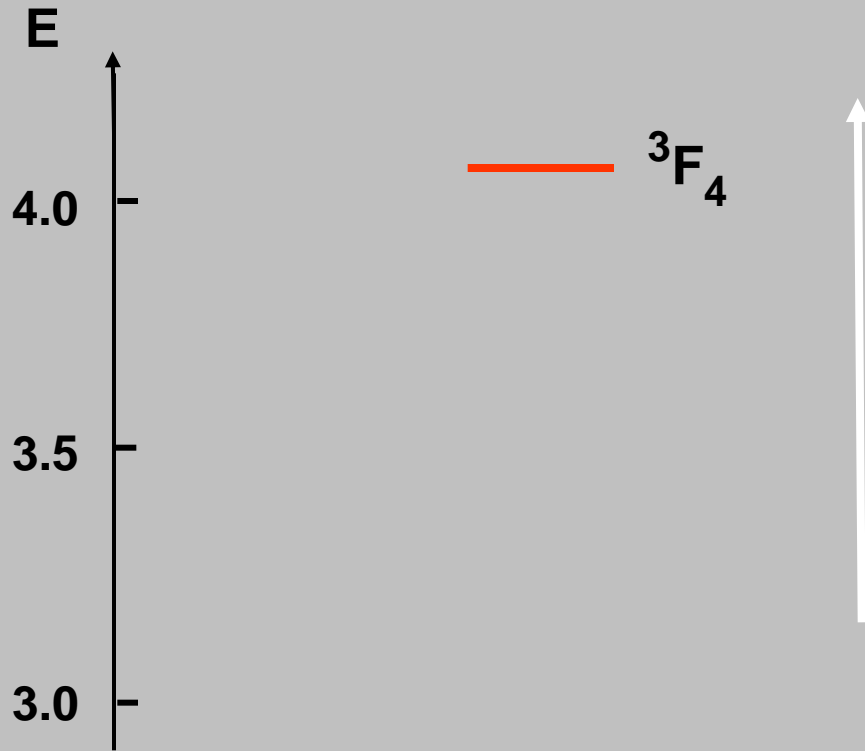
Discovering New Worlds

LHCb discoveries 2017

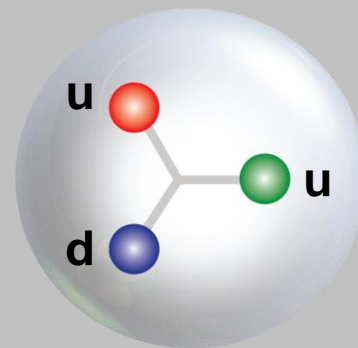
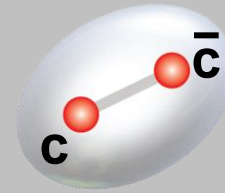




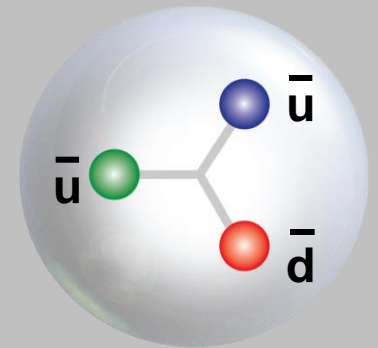
1^3F_4	1^3D_3	χ_{c2}	J/ψ
$J^{PC}=4^{++}$	$J^{PC}=3^{--}$	$J^{PC}=2^{++}$	$J^{PC}=1^{--}$
4095 MeV	3849 MeV	3556 MeV	3097 MeV
$\Gamma=8.3$ MeV	$\Gamma=0.5$ MeV	$\Gamma=2.0$ MeV	$\Gamma=0.3$ MeV
$E_\gamma=246$ MeV	$E_\gamma=338$ MeV	$E_\gamma=413$ MeV	-



Lange, Prencipe *et al.*

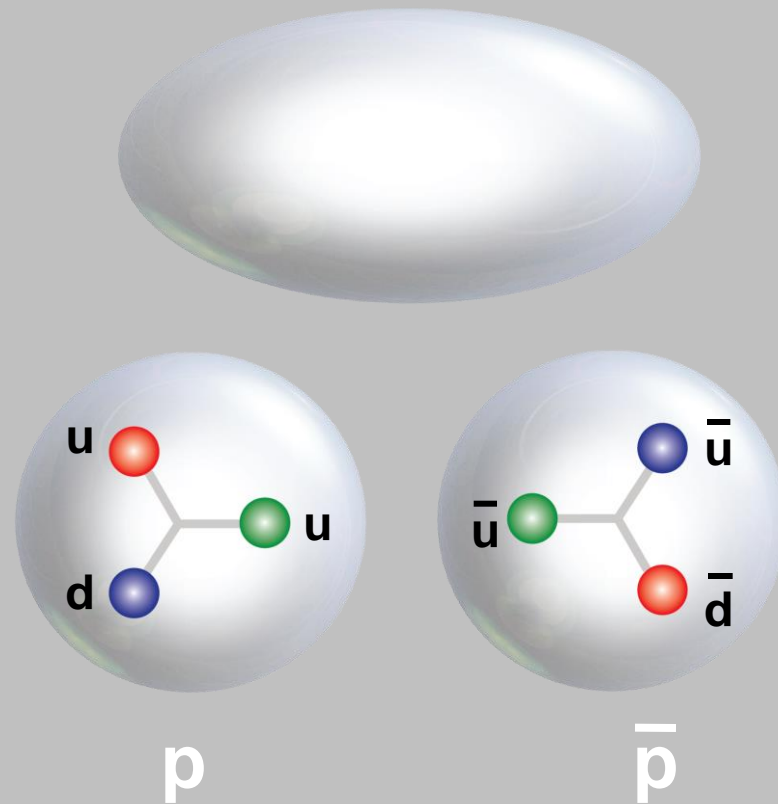
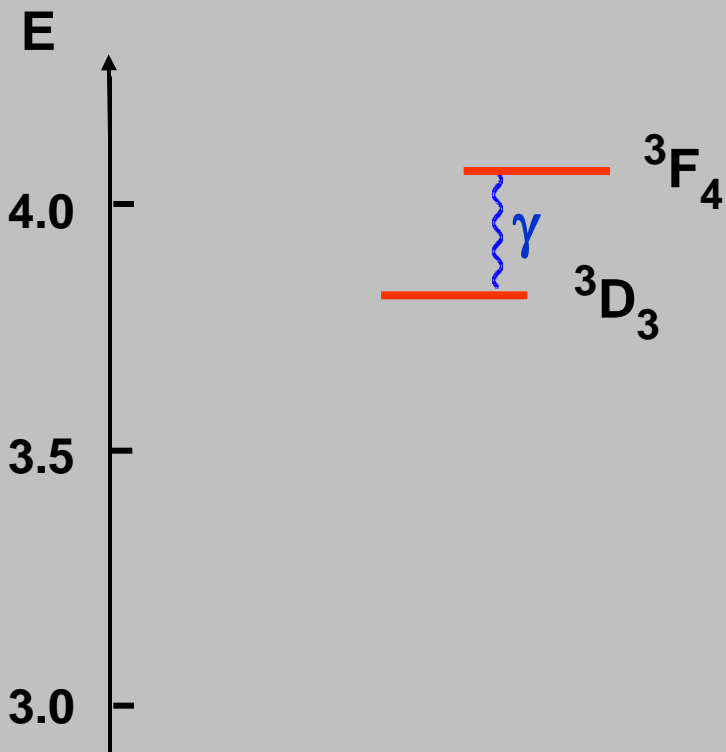
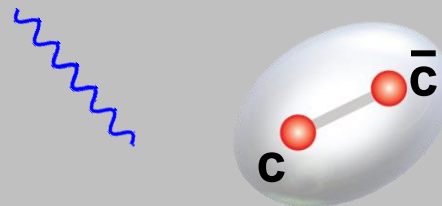


p



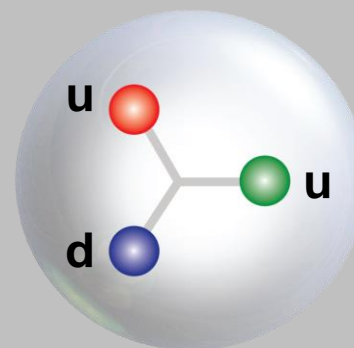
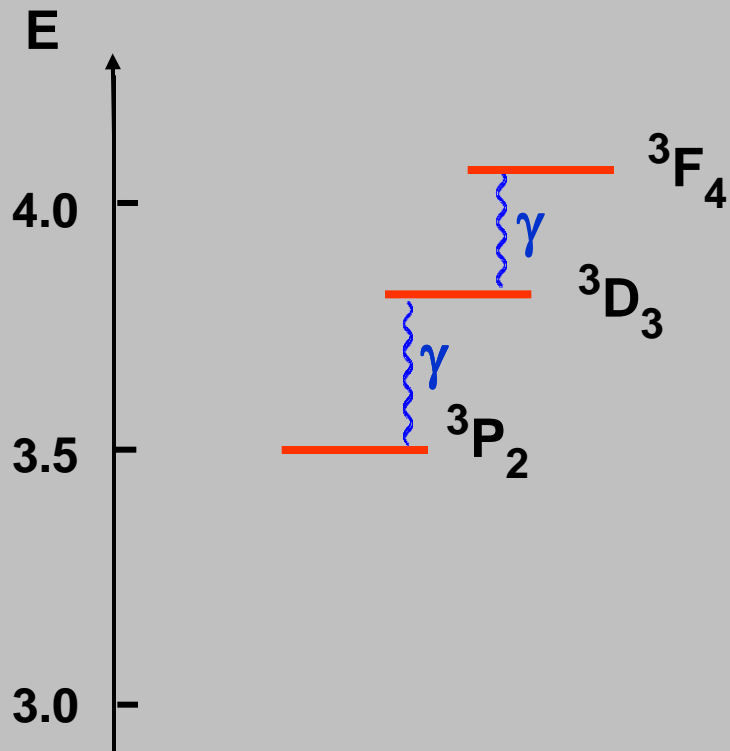
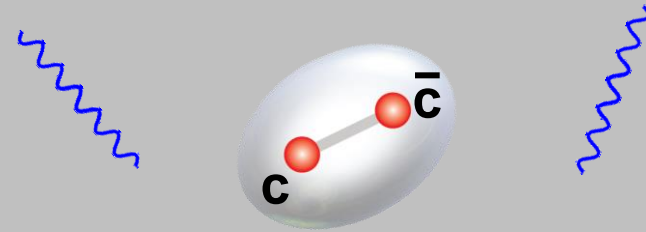
\bar{p}

1^3F_4	1^3D_3	χ_{c2}	J/ψ
$J^{PC}=4^{++}$	$J^{PC}=3^{--}$	$J^{PC}=2^{++}$	$J^{PC}=1^{--}$
4095 MeV	3849 MeV	3556 MeV	3097 MeV
$\Gamma=8.3$ MeV	$\Gamma=0.5$ MeV	$\Gamma=2.0$ MeV	$\Gamma=0.3$ MeV
$E_\gamma=246$ MeV	$E_\gamma=338$ MeV	$E_\gamma=413$ MeV	-

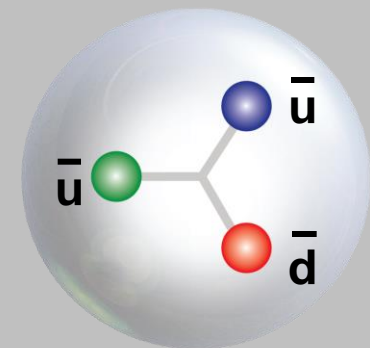


Lange, Prencipe *et al.*

1^3F_4	1^3D_3	χ_{c2}	J/ψ
$J^{PC}=4^{++}$	$J^{PC}=3^{--}$	$J^{PC}=2^{++}$	$J^{PC}=1^{--}$
4095 MeV	3849 MeV	3556 MeV	3097 MeV
$\Gamma=8.3$ MeV	$\Gamma=0.5$ MeV	$\Gamma=2.0$ MeV	$\Gamma=0.3$ MeV
$E_\gamma=246$ MeV	$E_\gamma=338$ MeV	$E_\gamma=413$ MeV	-



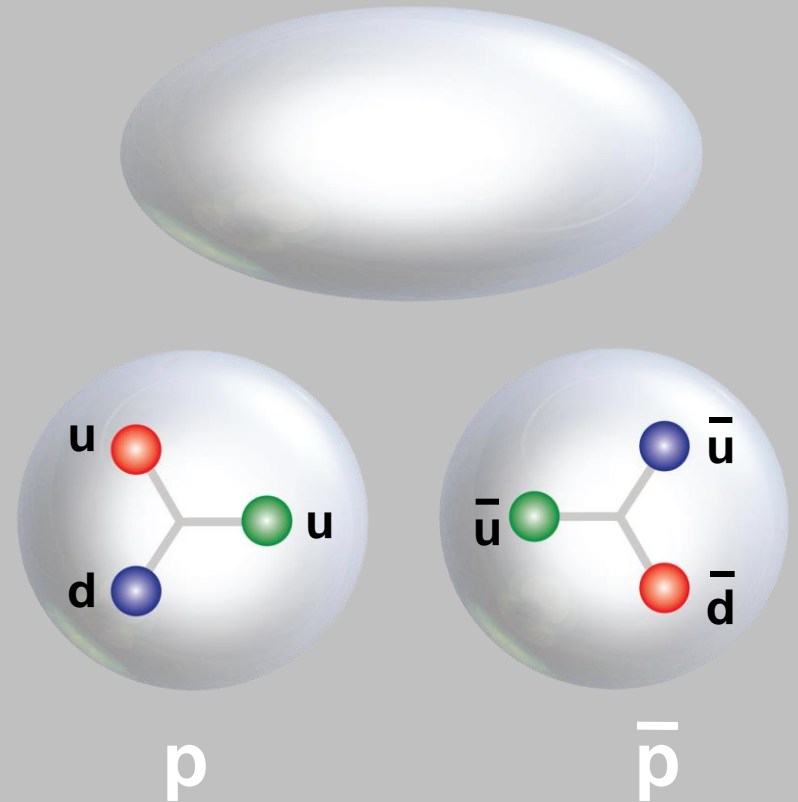
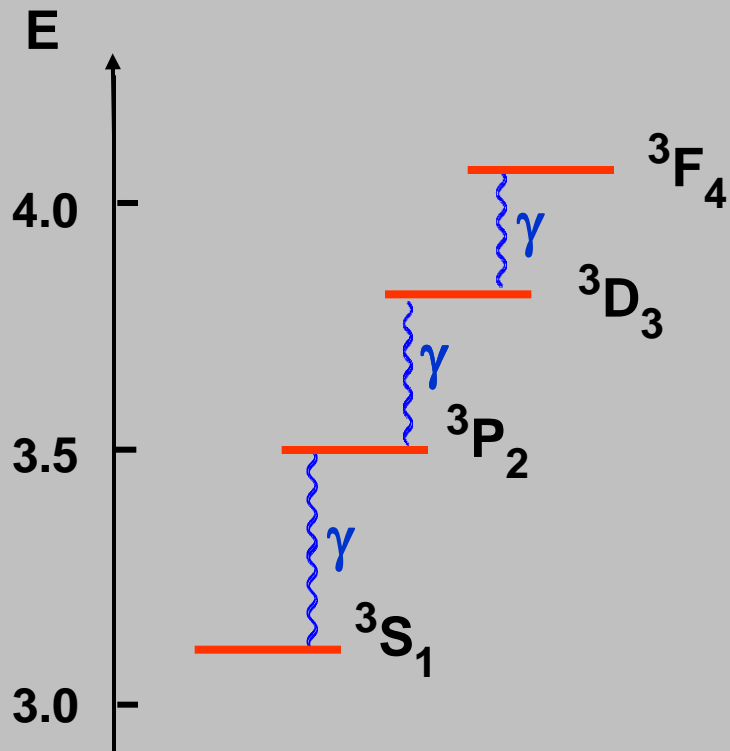
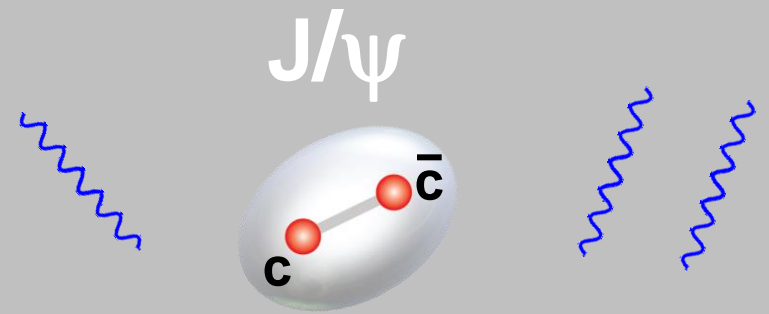
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\bar{p}

Lange, Prencipe *et al.*

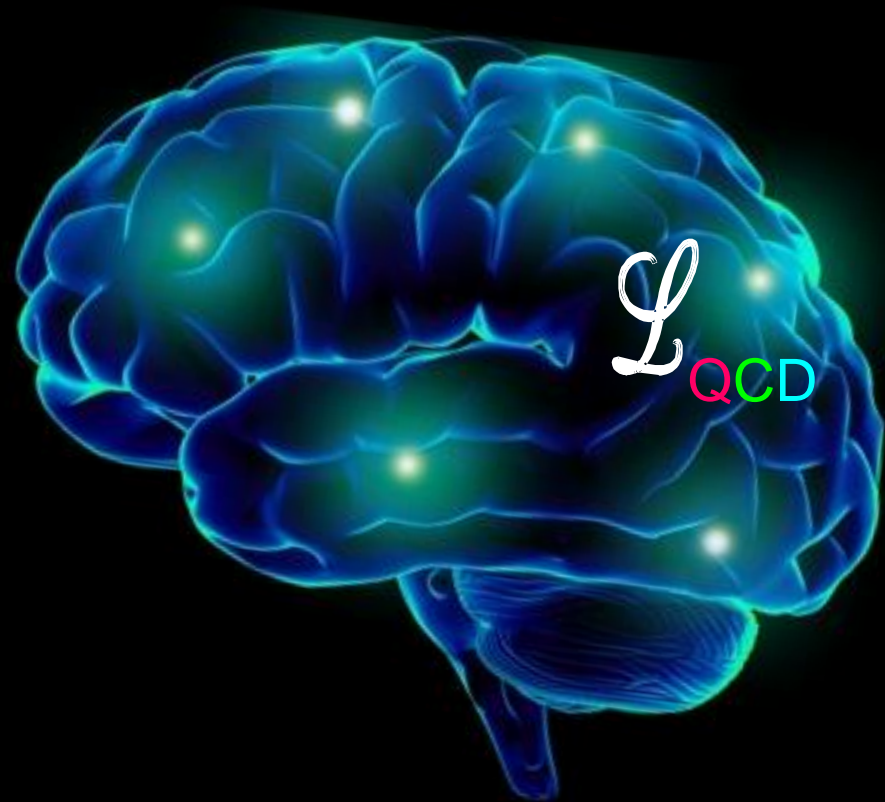
1^3F_4	1^3D_3	χ_{c2}	J/ψ
$J^{PC}=4^{++}$	$J^{PC}=3^{--}$	$J^{PC}=2^{++}$	$J^{PC}=1^{--}$
4095 MeV	3849 MeV	3556 MeV	3097 MeV
$\Gamma=8.3$ MeV	$\Gamma=0.5$ MeV	$\Gamma=2.0$ MeV	$\Gamma=0.3$ MeV
$E_\gamma=246$ MeV	$E_\gamma=338$ MeV	$E_\gamma=413$ MeV	-



Lange, Prencipe *et al.*



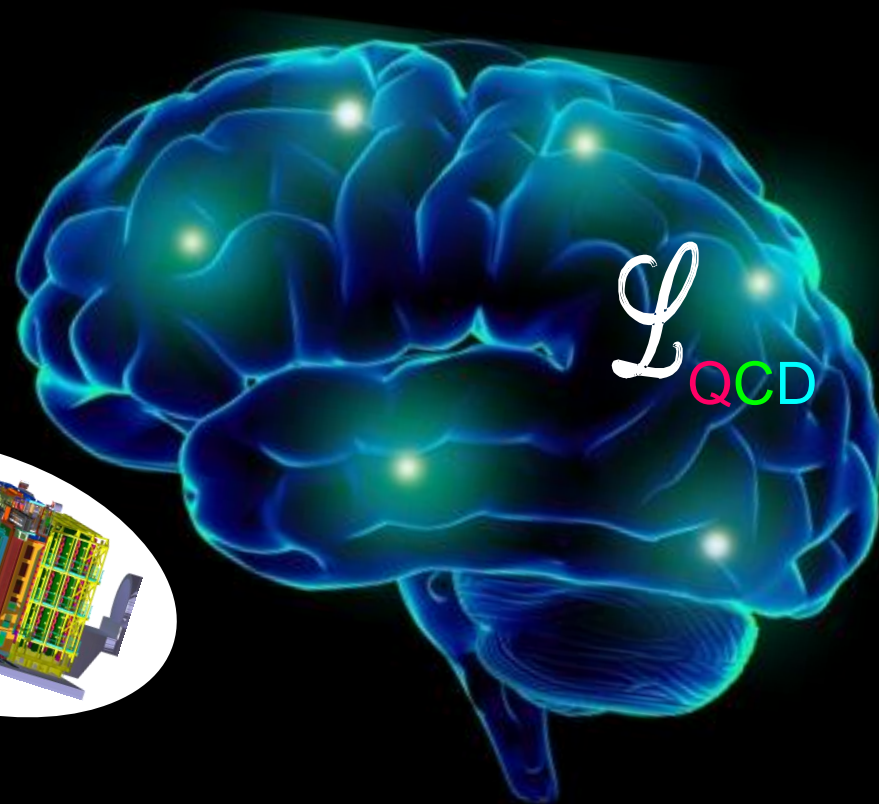
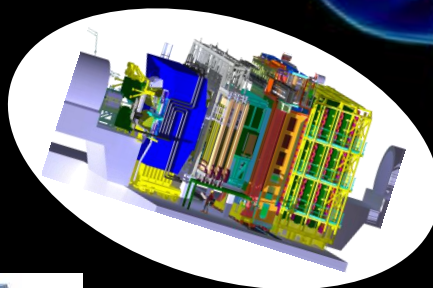
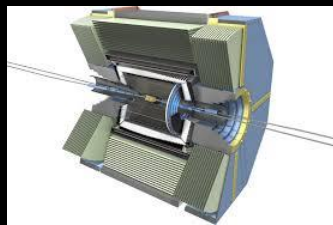
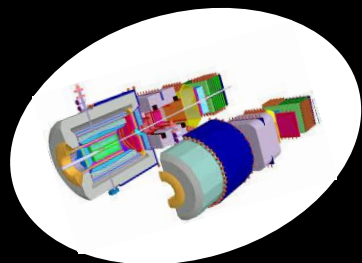
precision research



precision research



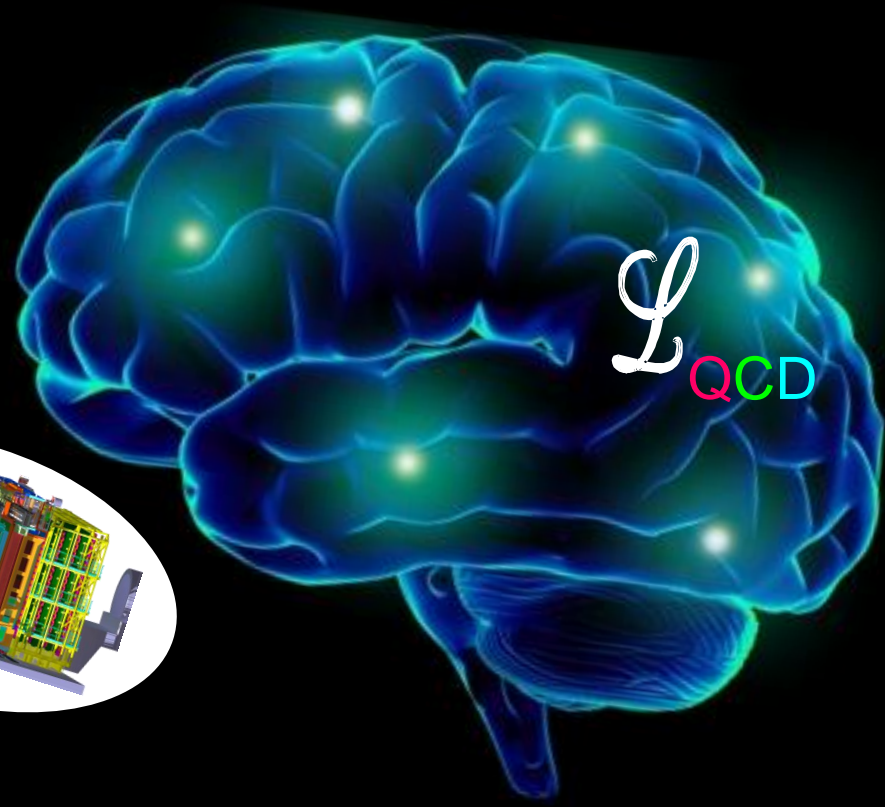
precision tools



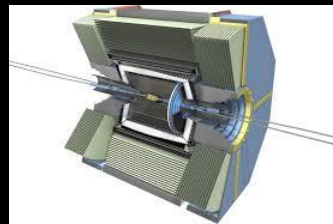
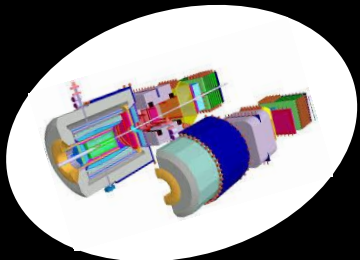
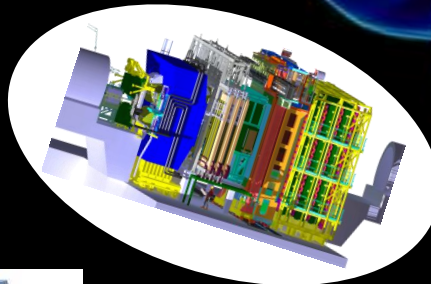
precision research



accurate modelling

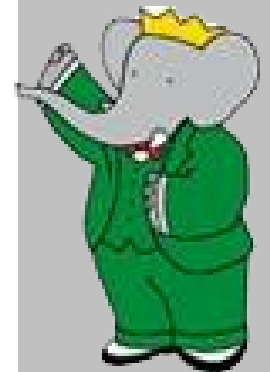
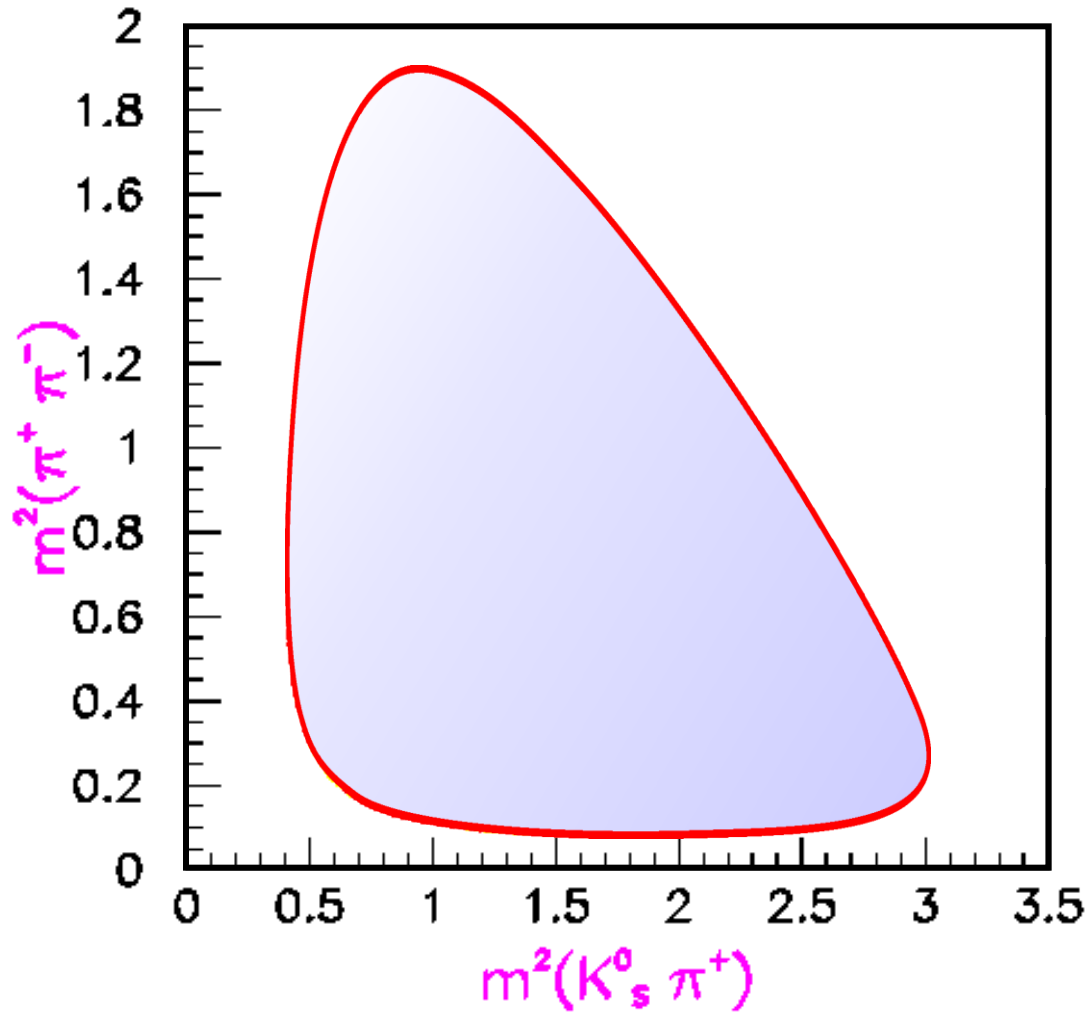
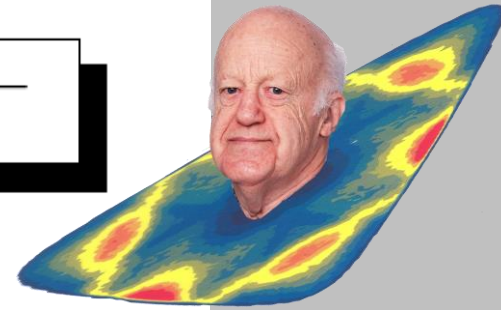


precision tools

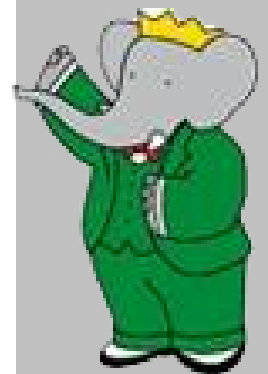
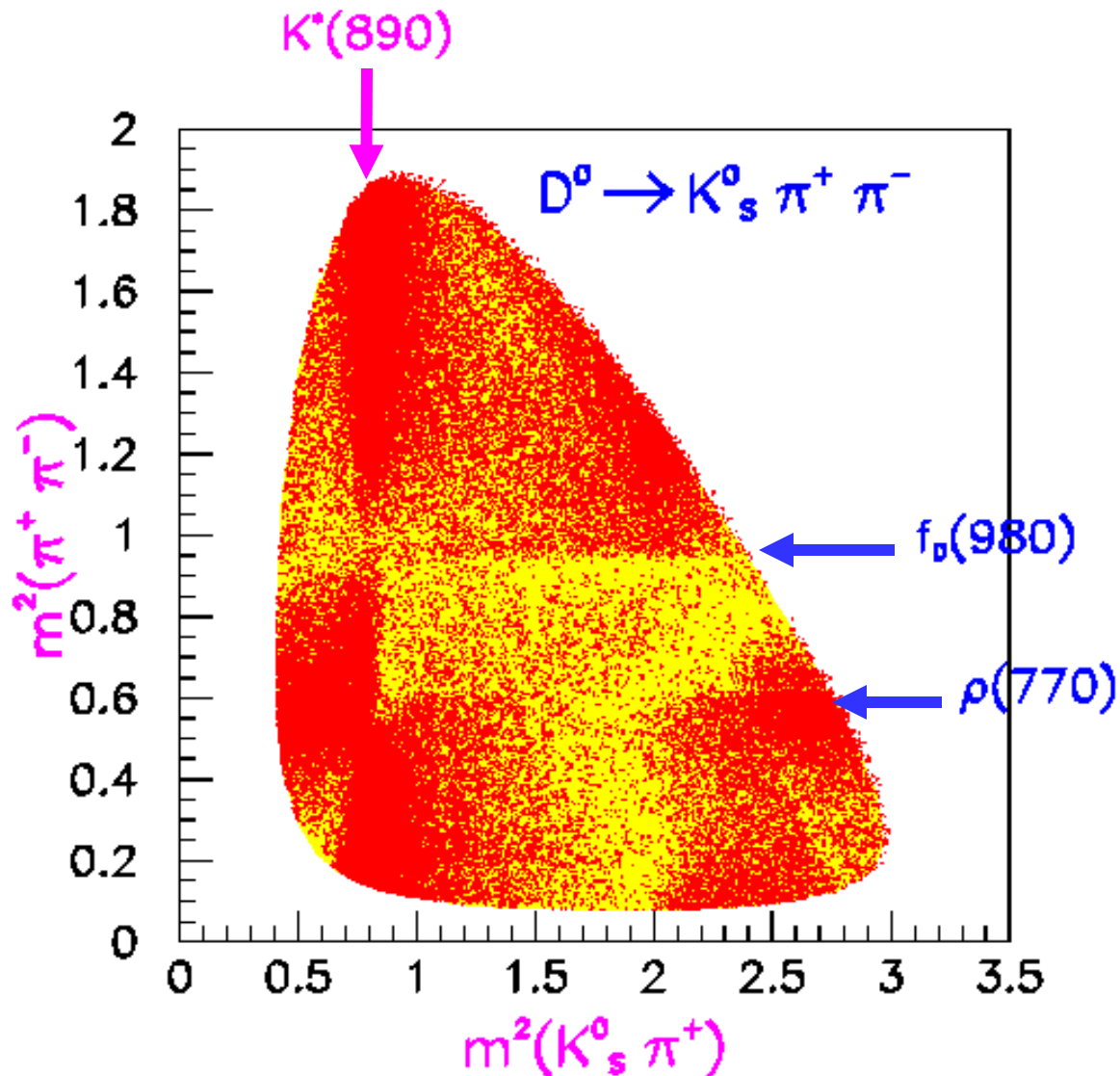




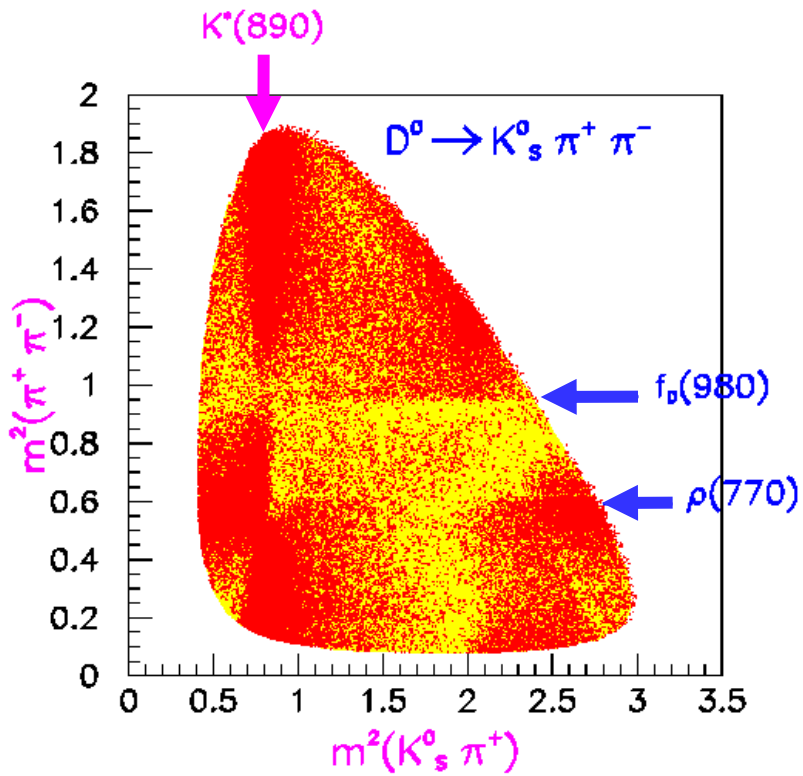
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$



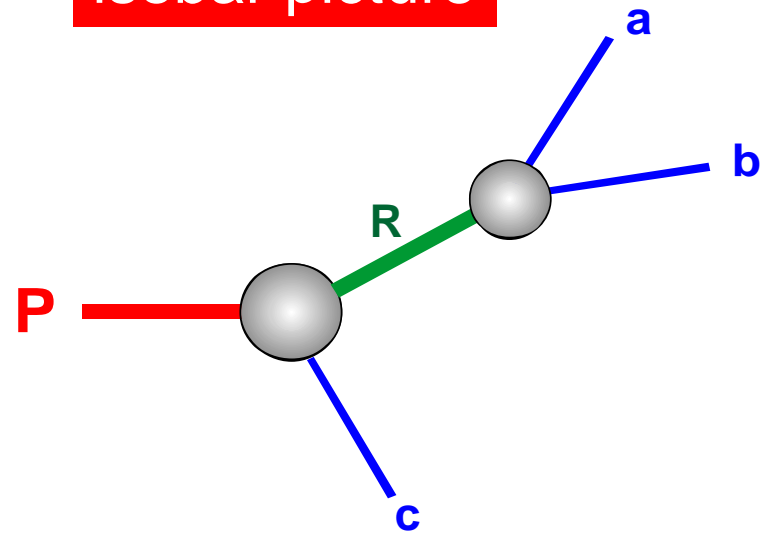
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$



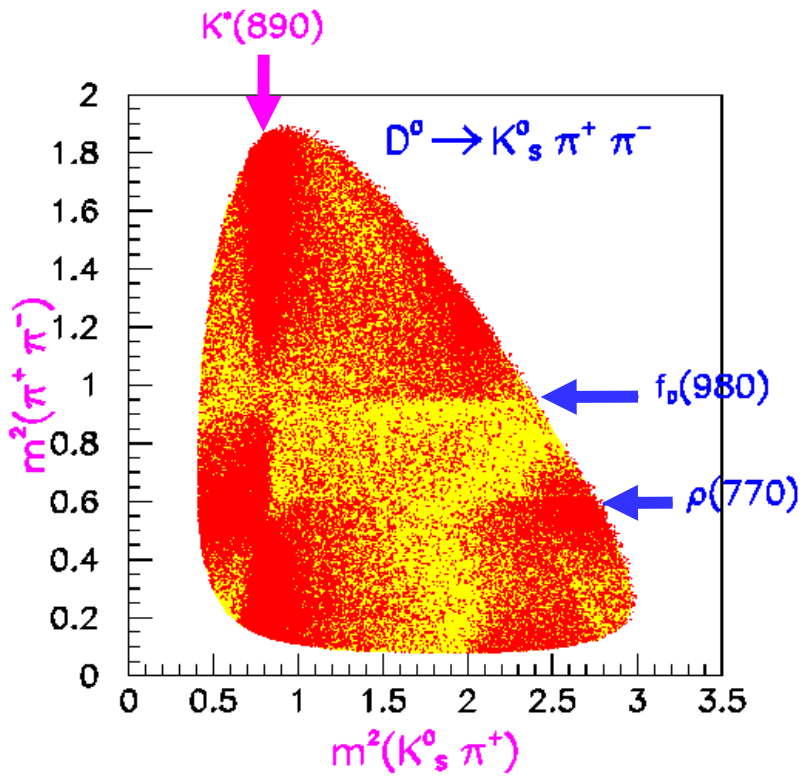
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$



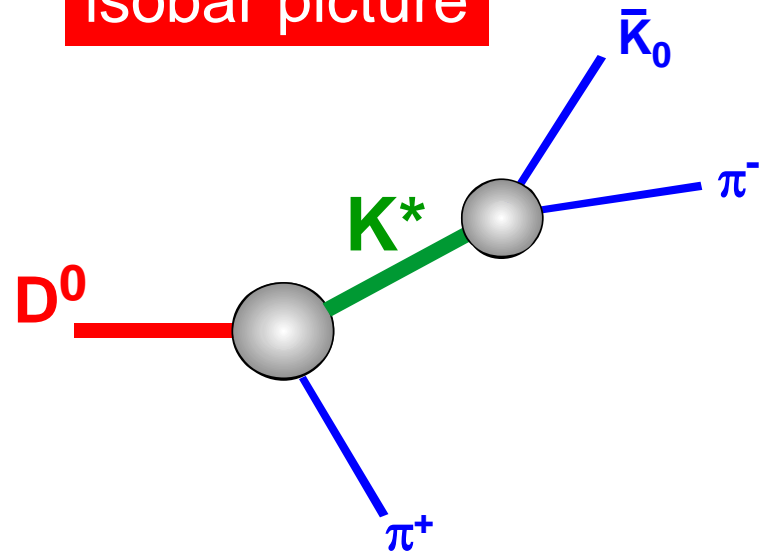
isobar picture



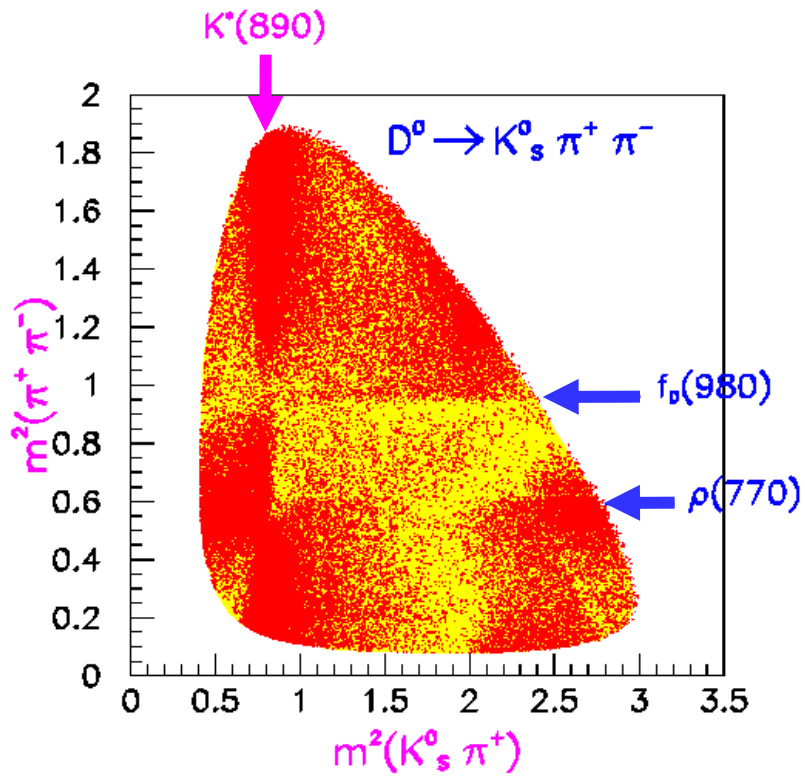
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$



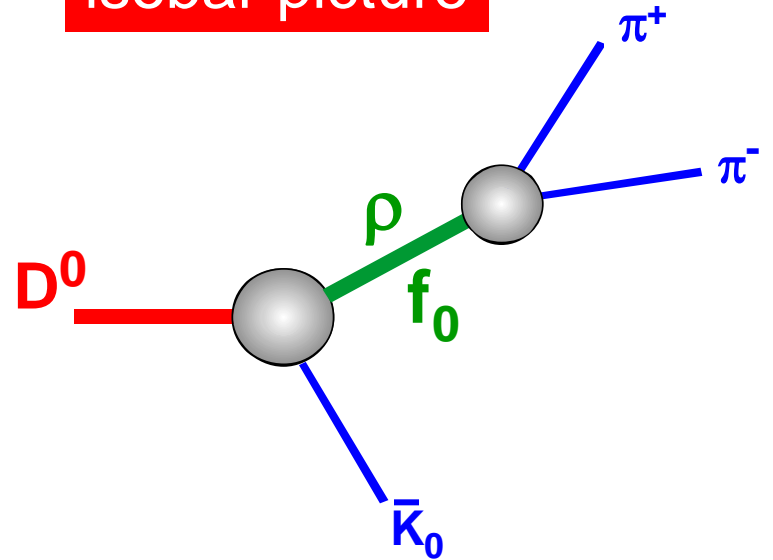
isobar picture

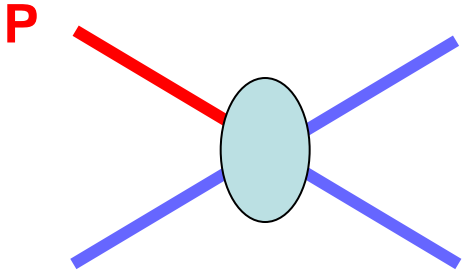


Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$

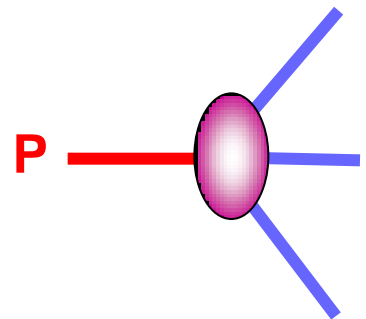
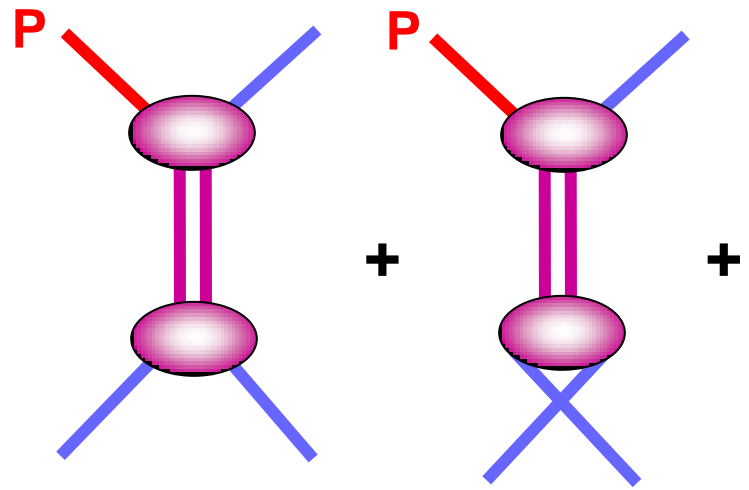
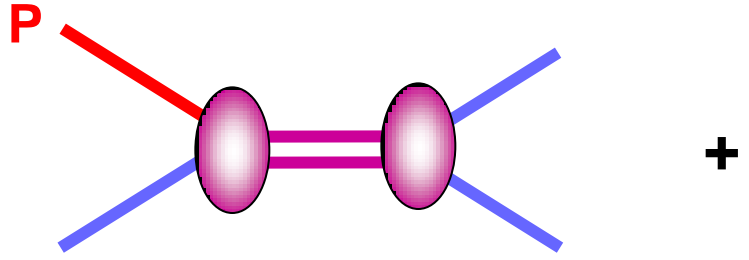


isobar picture

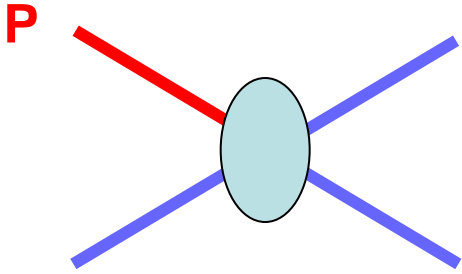




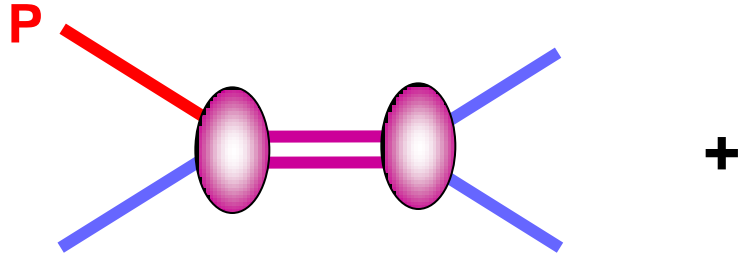
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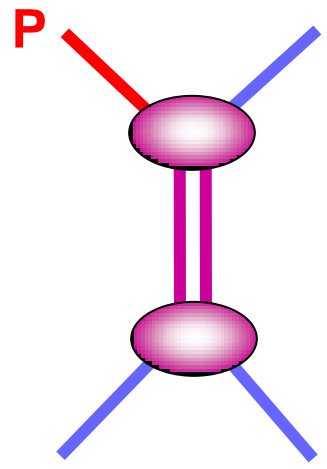
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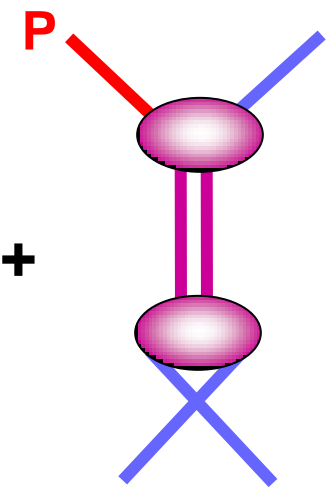
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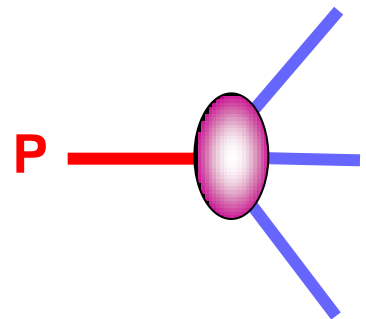
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isobar picture



Szczepaniak et al

S-MATRIX RELOADED

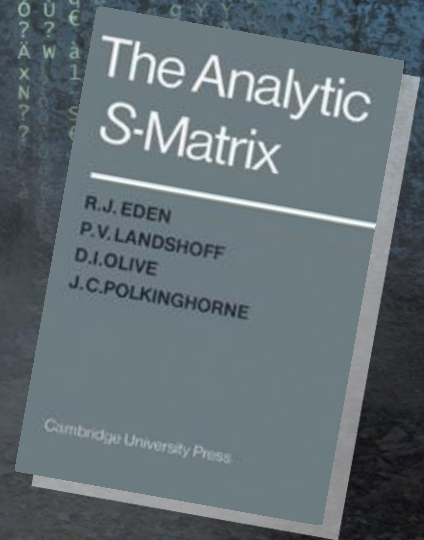
The Analytic
S-Matrix

R.J. EDEN
P.V. LANDSHOFF
D.I. OLIVE
J.C. POLKINGHORNE

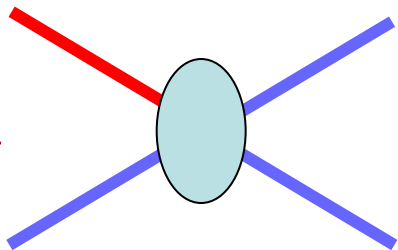
Cambridge University Press

**Weapons:
analyticity
unitarity**

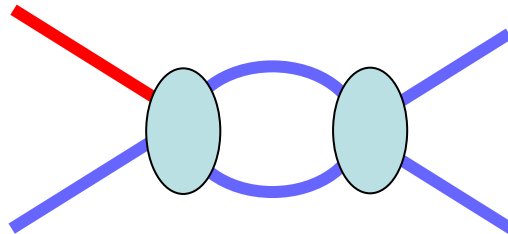
S-MATRIX RELOADED



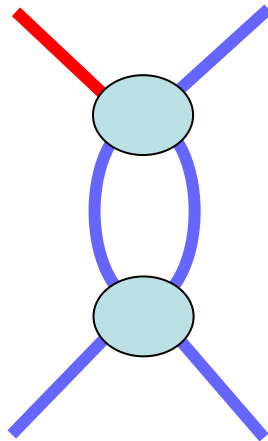
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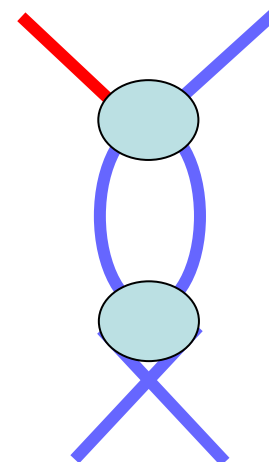
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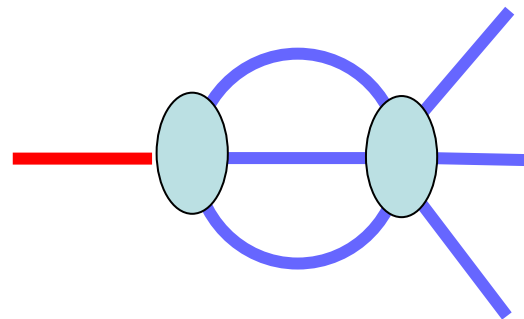
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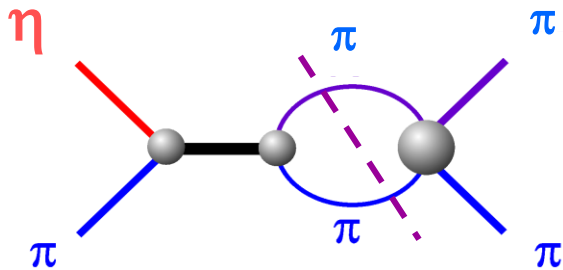
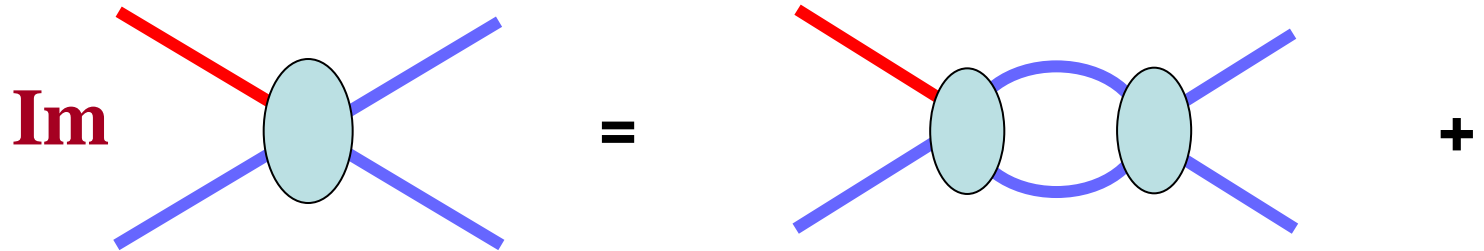
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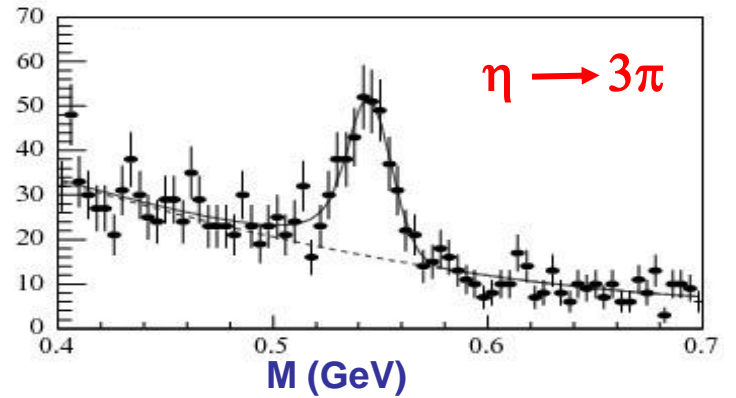
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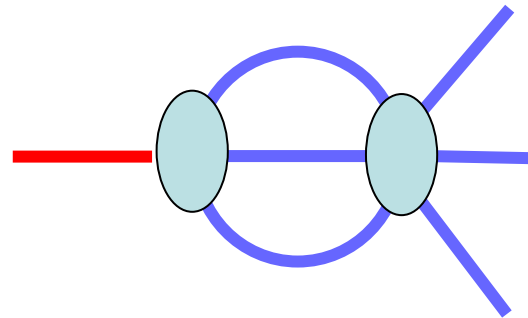
2-body unitarity



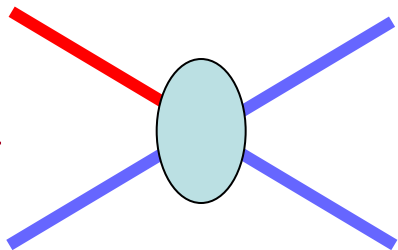
Khuri-Treiman relations



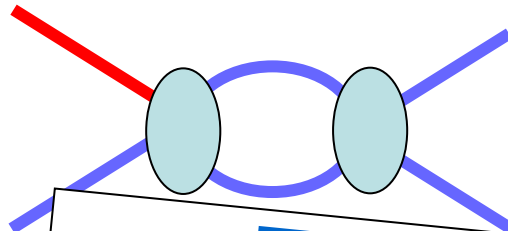
2-body unitarity



Im

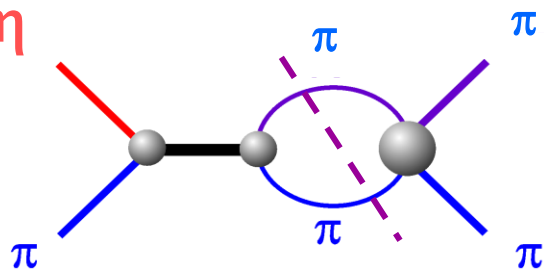


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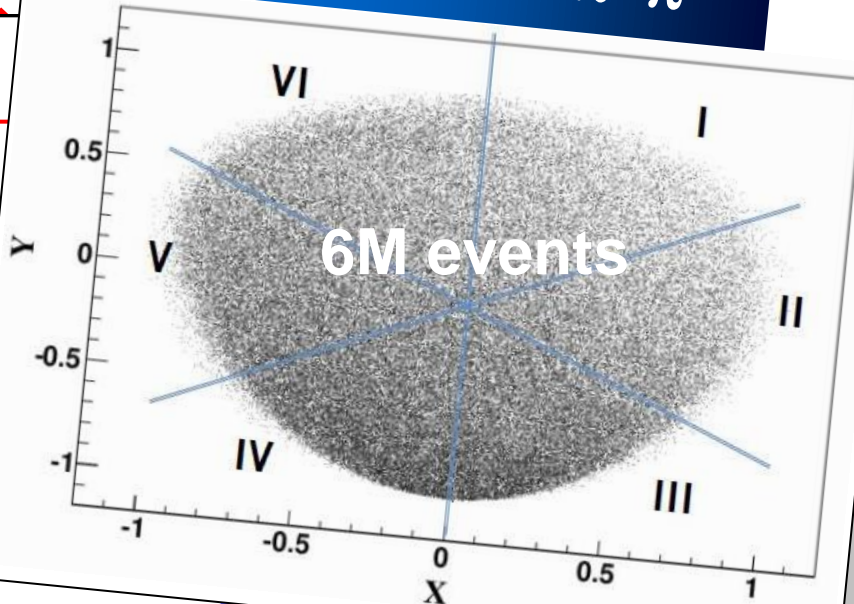
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η

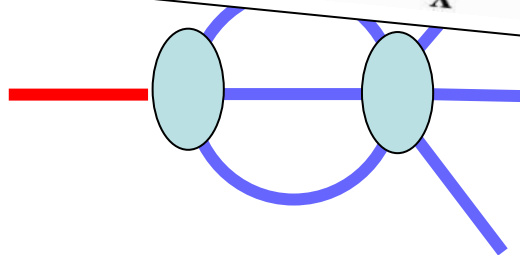


Khuri-Treiman relations

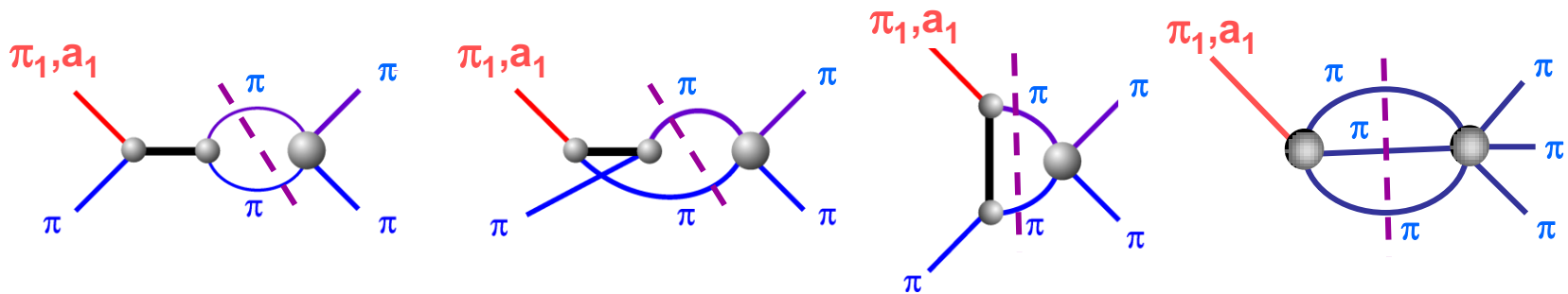
$\eta \rightarrow \pi^+ \pi^- \pi^0$



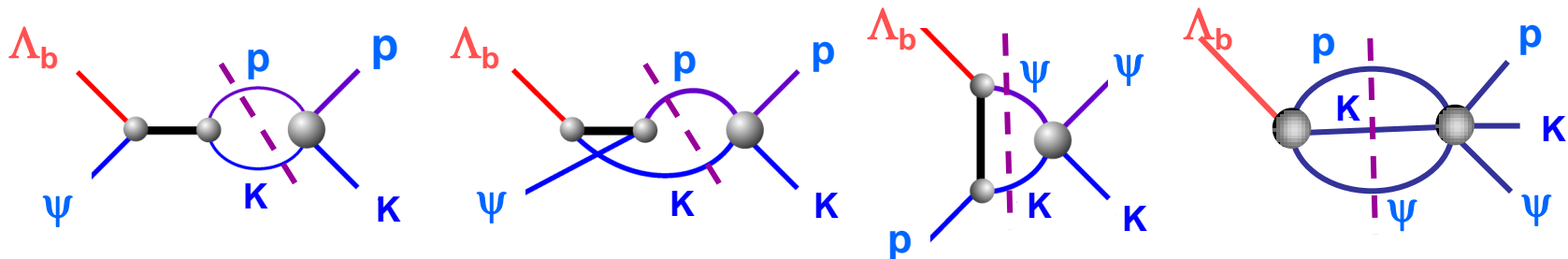
2-body unitarity



$$\pi_1/a_1 \rightarrow \pi\pi\pi$$

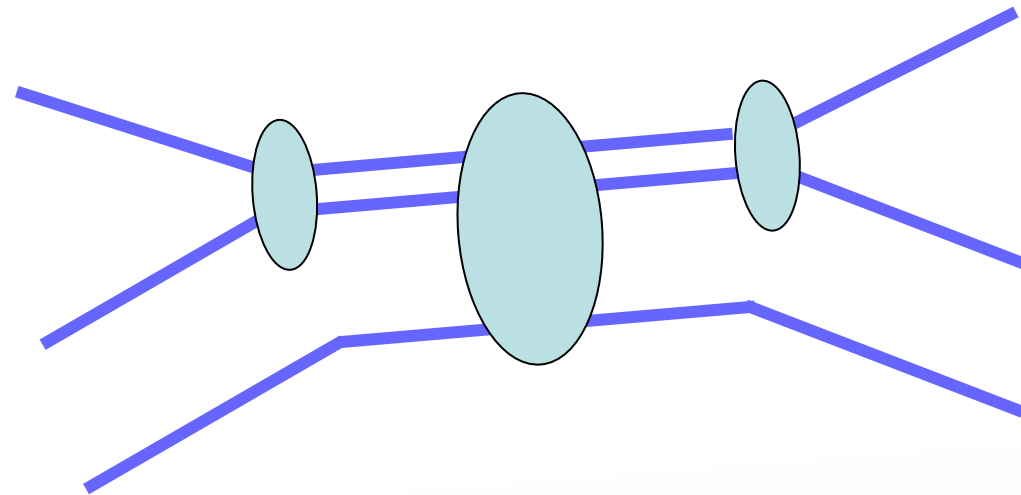
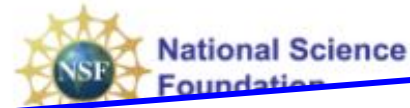


$$\Lambda_b \rightarrow K^- J/\psi p$$



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Three-body Unitarity with Isobars Revisited
M. Mai,^{1,*} B. Hu,¹ M. Döring,^{1,2} A. Pilloni,² and A. Szczepaniak^{2,3,4}

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JPAC acknowledges support from DOE and NSF

NEWS

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- High energy model for η' beam asymmetry photoproduction: [\$\gamma p \rightarrow \eta' p\$](#)
- High energy model for η photoproduction: [\$\gamma p \rightarrow \eta p\$](#)
- High energy model for π^0 photoproduction: [\$\gamma p \rightarrow \pi^0 p\$](#)
- High energy model for J/ψ photoproduction: [\$\gamma p \rightarrow J/\psi p\$](#)

Hadroproduction:

- Pion-nucleon scattering: [\$\pi N \rightarrow \pi N\$ amplitude](#)
- Finite energy sum rules [\$\pi N \rightarrow \pi N\$ FESR page](#)
- Kaon-nucleon scattering: [\$K N \rightarrow K N\$](#)

Light meson Decay:

- η meson into three pions: [\$\eta \rightarrow 3\pi\$](#)
- vector meson into three pions: $\omega, \phi \rightarrow 3\pi$

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- **Geoffrey Fox** Professor
- **Emilie Passemar** Professor
- **Tim Londergan** Professor
- **Vincent Mathieu** Postdoctoral researcher
- **Ina Lorenz** Postdoctoral researcher
- **Andrew Jackura** PhD student



Jefferson Lab

- **Michael R. Pennington** Professor
- **Viktor Mokeev** Professor
- **Vladislav Pauk** Postdoctoral researcher
- **Alessandro Pilloni** Postdoctoral researcher



George Washington University

- **Ron Workman** Professor
- **Michael Doring** Professor



Universidad Nacional Autonoma de Mexico

- **Cesar Fernandez-Ramirez** Professor

Johannes Gutenberg University, Mainz

- **Igor Danilkin** Postdoctoral researcher

Bonn University

- **Misha Mikhasenko** PhD student

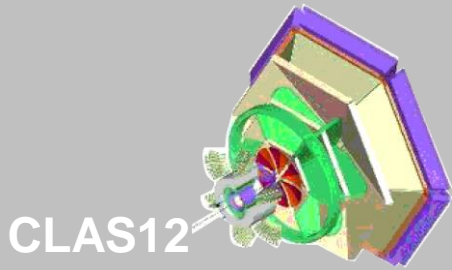
University of Valencia

- **Astrid Hiller Blin** PhD student

Ghent University

- **Jannes Nys** PhD student

φ Phase



CLAS12

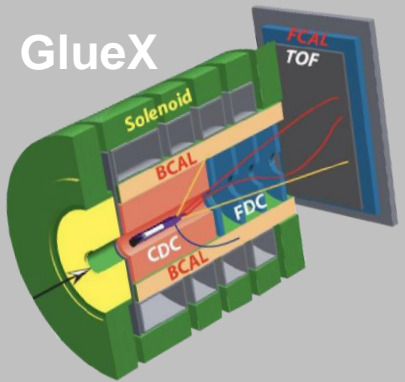
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Exposing QCD

- what are the relevant degrees of freedom?



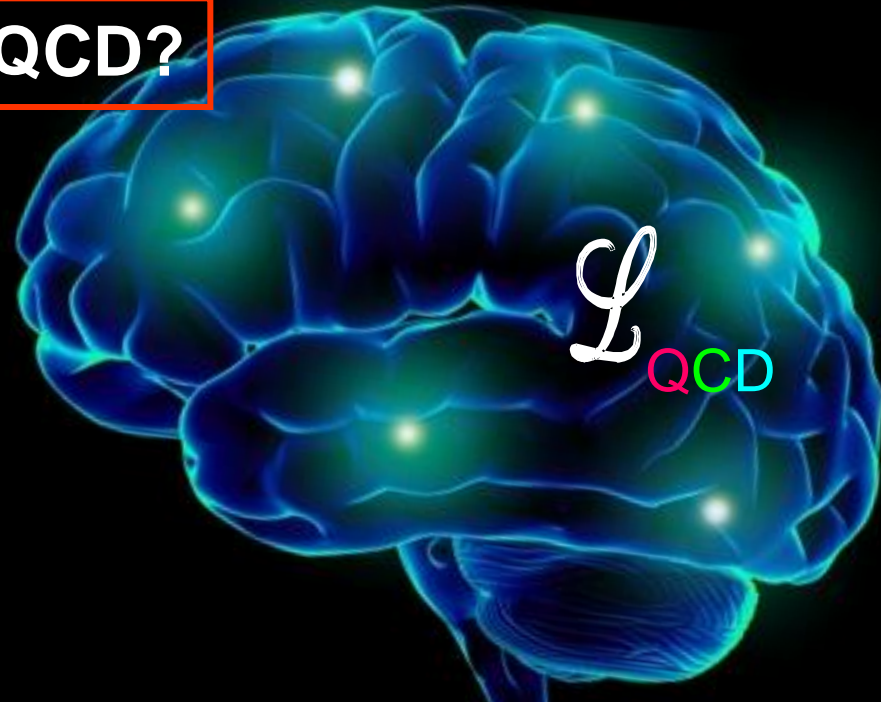
Exposing QCD

- what are the relevant degrees of freedom?
- what is the Fock space decomposition of each hadron
what are their patterns -- flavour, spin, ...?
what does this reveal about the internal dynamics?



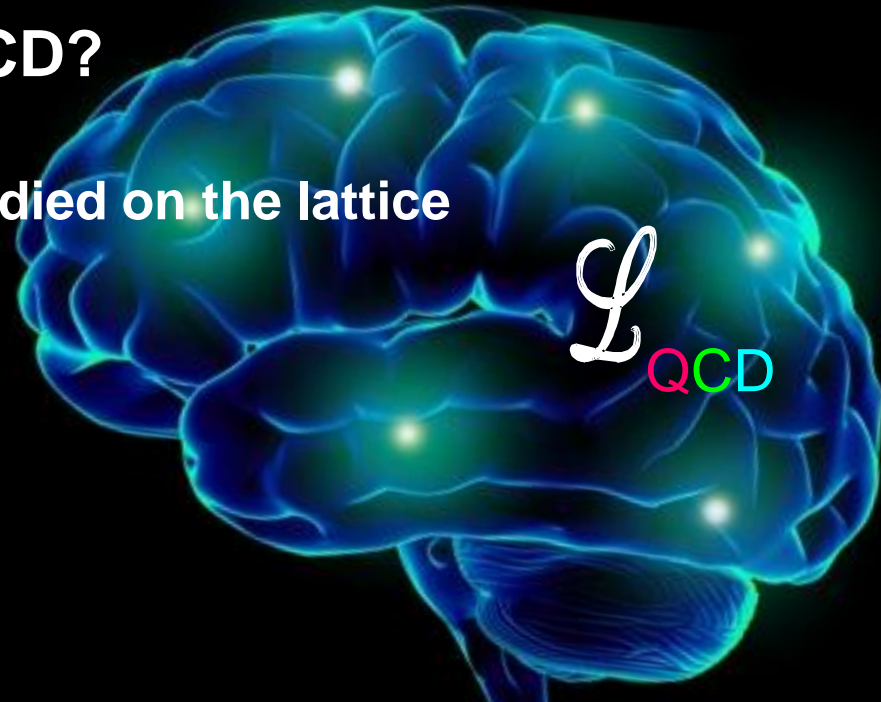
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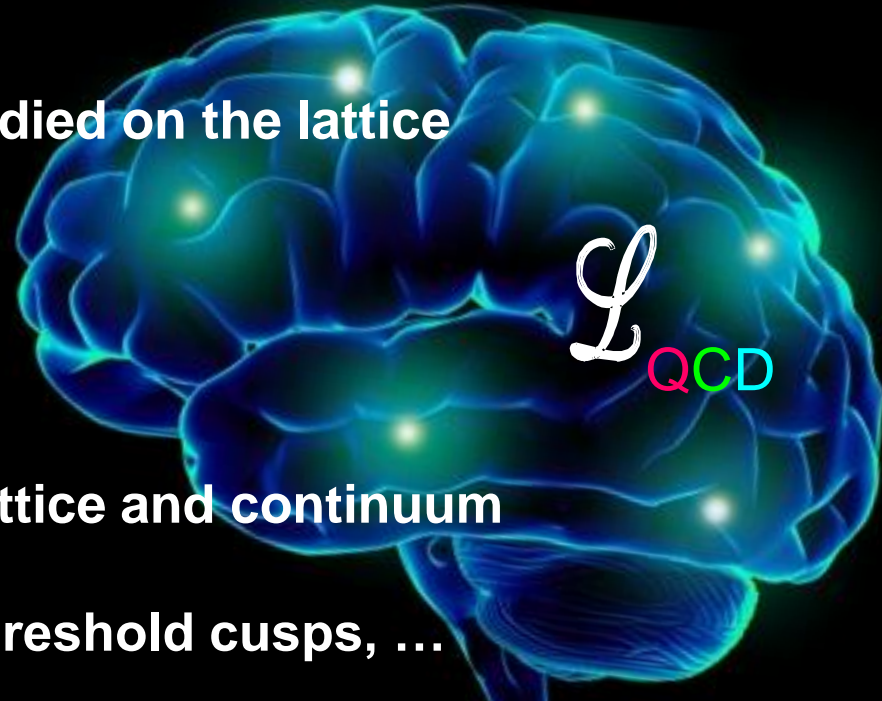
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- are the appropriate operators studied on the lattice
(or continuum)?
- multi-particle scattering on the lattice and continuum
- methods of S-matrix theory
poles, triangle singularities, threshold cusps, ...



Exposing QCD

- what are the relevant degrees of freedom?

- how are hadrons *really* connected to QCD?

