

# Charming new physics in rare $B$ decays and mixing

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**Kirsty Leslie**  
**With S.Jäger, M.Kirk, A.Lenz**

University of Sussex

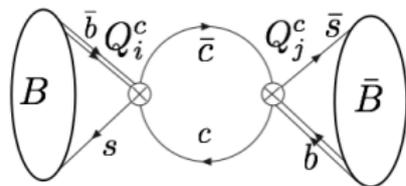
September 5, 2017

# Outline

- Motivation
- Methodology
- Results
- Conclusions

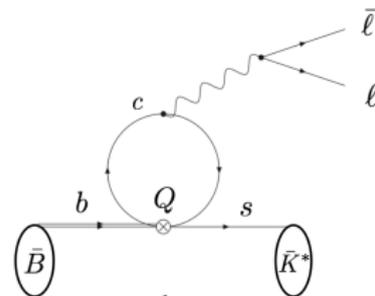
# Central idea

$B_s$  meson mixing, lifetimes and rare  $B$  decays all receive contributions from charmed 4 quark operators at 1-loop



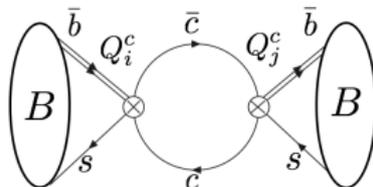
$B_s$ - $B_d$  Lifetime ratio

$$r = \left( \frac{\tau_{B_s}}{\tau_{B_d}} \right)$$



Width difference

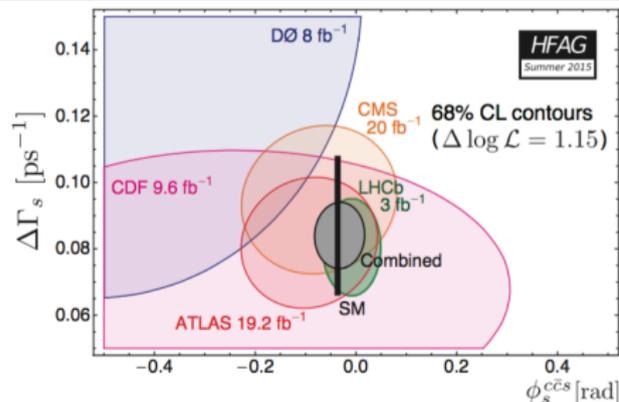
$$\Delta\Gamma_s$$



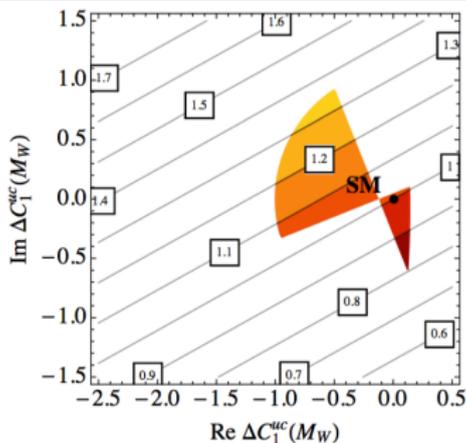
Rare  $B$  decay observables

$$A_{FB}, P'_5$$

# Motivation: Mixing observables



[http://www.slac.stanford.edu/xorg/hfag/osc/spring\\_2016](http://www.slac.stanford.edu/xorg/hfag/osc/spring_2016)

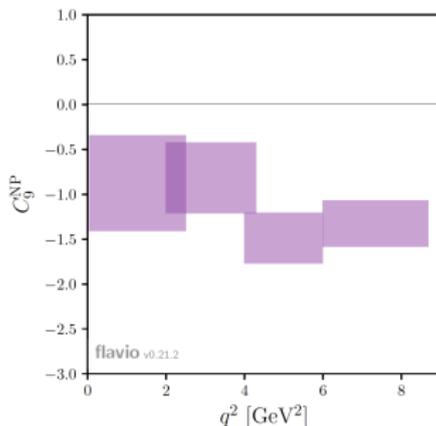
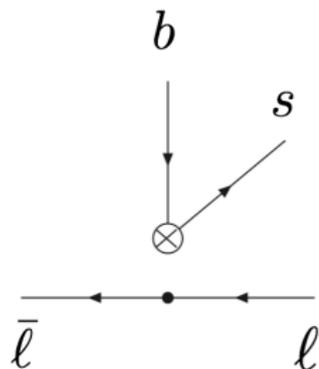


Bobeth, Haisch, Pecjack, Tetlalmatzi-Xolocotzi, 1404.2531

- Mixing observables such as the decay rate difference and semileptonic asymmetry show consistency with the SM
- Another important observable to consider is the  $B_s - B_d$  lifetime ratio

If sizable NP contributions to  $b \rightarrow c\bar{c}s$  couplings are present in mixing, they could also effect and constrain  $b \rightarrow s\ell\bar{\ell}$

# Motivation: Rare decay anomalies



Altmannshofer, Niehoff, Stangl, Straub, 1703.09189, and others

$$Q_9^l = \frac{\alpha}{4\pi} (\bar{s} \gamma^\mu P_L b) (\bar{l} \gamma_\mu l)$$

- Recent analysis of LHCb data suggests a negative contribution to the Wilson coefficient  $C_9$
- Possible explanation for tensions in rare decays such as  $B \rightarrow K^* \mu \mu$

Assume a negative shift to  $C_9$  - Ask if there are viable charming BSM scenarios which reproduce this effect?

# Operator Basis

## Effective Hamiltonian

$$\mathcal{H}_{eff}^{c\bar{c}} = \frac{4G_F}{\sqrt{2}} V_{cb} V_{cs}^* \left[ \sum_{i=1}^{10} (C_i^c Q_i^c + C_i^{c'} Q_i^{c'}) + h.c \right]$$

## SM

$$Q_1^c = (\bar{c}_L^i \gamma_\mu b_L^j) (\bar{s}_L^j \gamma^\mu c_L^i),$$

$$Q_2^c = (\bar{c}_L^i \gamma_\mu b_L^i) (\bar{s}_L^j \gamma^\mu c_L^j),$$

## BSM

$$Q_3^c = (\bar{c}_R^i b_L^j) (\bar{s}_L^j c_R^i),$$

$$Q_4^c = (\bar{c}_R^i b_L^i) (\bar{s}_L^j c_R^j),$$

$$Q_5^c = (\bar{c}_R^i \gamma_\mu b_R^j) (\bar{s}_L^j \gamma^\mu c_L^i),$$

$$Q_6^c = (\bar{c}_R^i \gamma_\mu b_R^i) (\bar{s}_L^j \gamma^\mu c_L^j),$$

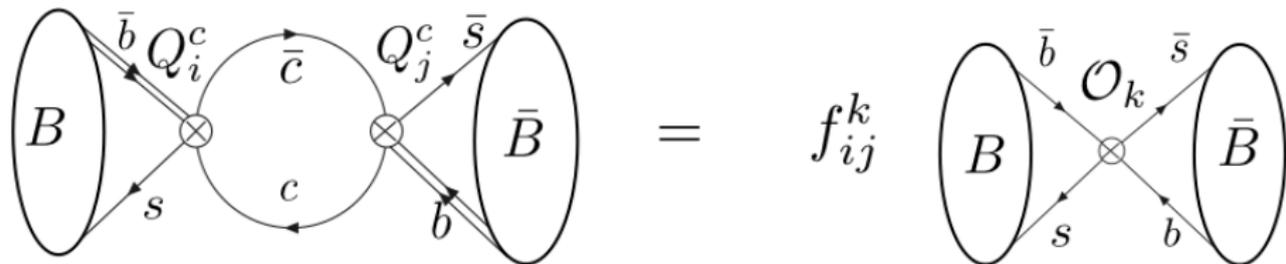
$$Q_7^c = (\bar{c}_L^i b_R^j) (\bar{s}_L^j c_R^i),$$

$$Q_8^c = (\bar{c}_L^i b_R^i) (\bar{s}_L^j c_R^j),$$

$$Q_9^c = (\bar{c}_L^i \sigma_{\mu\nu} b_R^j) (\bar{s}_L^j \sigma^{\mu\nu} c_R^i),$$

$$Q_{10}^c = (\bar{c}_L^i \sigma_{\mu\nu} b_R^i) (\bar{s}_L^j \sigma^{\mu\nu} c_R^j),$$

# $B_s - \bar{B}_s$ mixing: $\Gamma_{12}^{cc}$



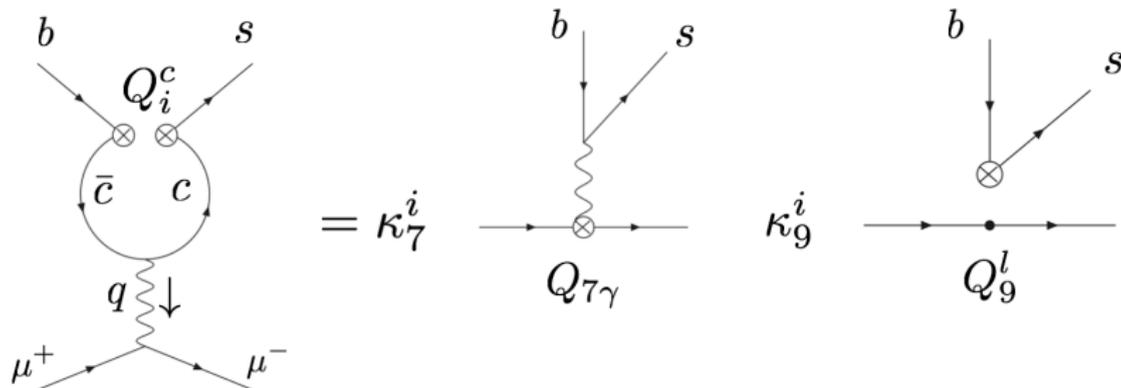
- Heavy Quark Expansion reduces original  $\Delta B = 1$  basis to standard  $\Delta B = 2$  basis

$$\Gamma_{12}^{cc} \sim \sum_{ijk} C_i^c C_j^c f_{ij}^k \frac{\langle B_s^0 | \mathcal{O}_k | \bar{B}_s^0 \rangle}{2M_B}$$

## Width difference

$$\Delta\Gamma_s = 2|\Gamma_{12}| \cos \phi_{12}^s$$

# Rare Decay: Short distance effects



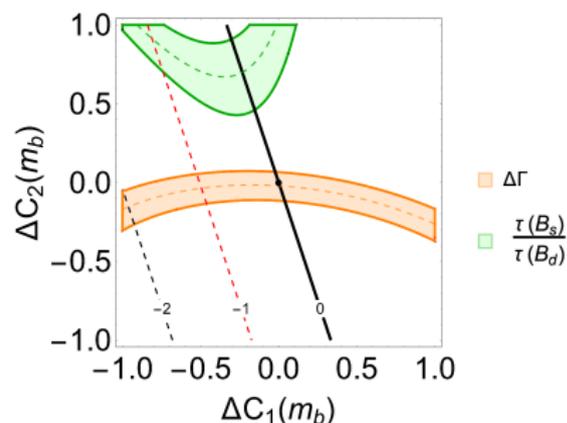
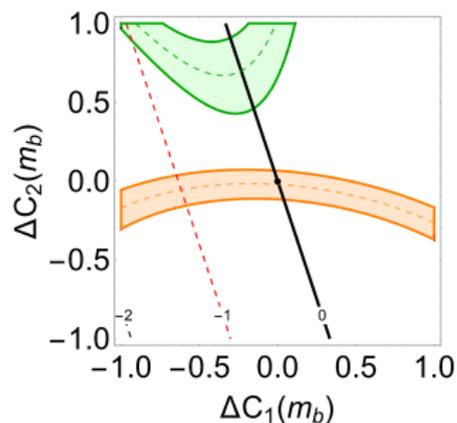
$$\Delta C_9^{eff}(q^2) = \sum_{i=1}^{10} C_i \kappa_9^i$$

$$\Delta C_7^{eff}(q^2) = \sum_{i=1}^{10} C_i \kappa_7^i$$

$$\Delta C_{\text{eff}}^9 = \left[ ((3\Delta C_1 + \Delta C_2) - \frac{1}{2}(3\Delta C_3 + \Delta C_4)) h(q^2) - \frac{2}{9}(3\Delta C_3 + \Delta C_4) \right]$$

- $h(q^2)$  is a loop function

# Results I: Low Scale Constraints on $\Delta C_{eff}^9(q^2)$



$$\Delta C_{eff}^9(q^2 = 2 \text{ GeV}^2)$$

$$\Delta C_{eff}^9(q^2 = 5 \text{ GeV}^2)$$

- $q^2$  dependence of  $\Delta C_{eff}^9$  is more sensitive to NP at higher values of  $q^2$
- Negative shift of  $\Delta C_{eff}^9 = -1$  can be accommodated by  $\Delta\Gamma_s$

# Renormalization Group Evolution

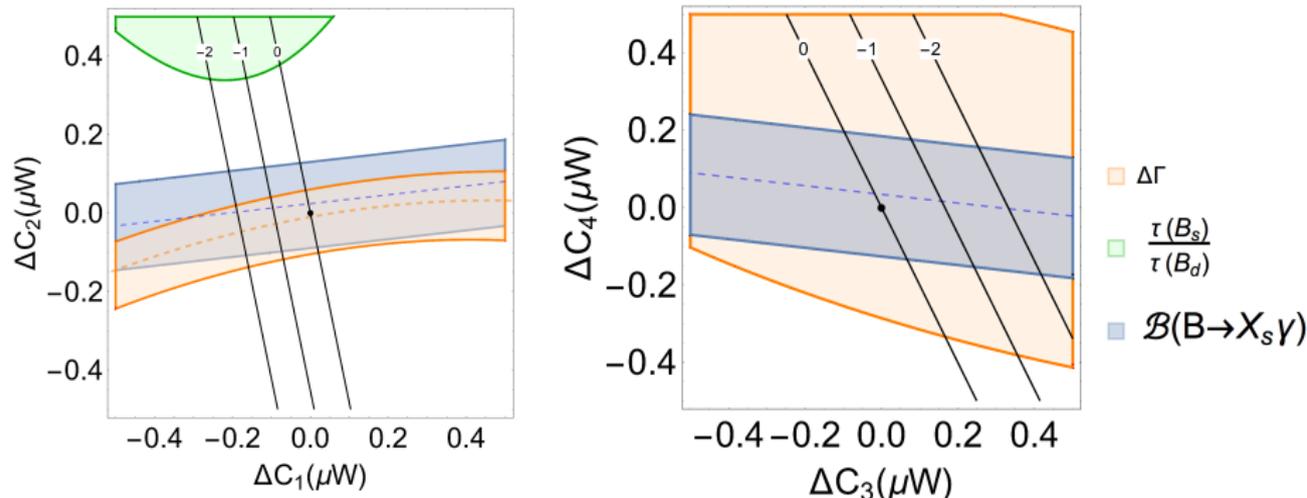
- When NP enters at the high scale  $\mu \approx M_W$  Renormalization Group effects become important

$$\Delta C_{eff}^7(\mu_b) = 0.02C_1^c(M_W) - 0.19C_2^c(M_W) - 0.01C_3^c(M_W) - 0.13C_4^c(M_W)$$

$$\Delta C_{eff}^9(\mu_b) = 8.65C_1^c(M_W) + 2.00C_2^c(M_W) - 4.33C_3^c(M_W) - 1.95C_4^c(M_W)$$

- $\Delta C_{eff}^7$  generates  $B \rightarrow X_s \gamma$  constraint
- $C_3^c(M_W)$  and  $C_4^c(M_W)$  are new in  $\Delta C_{eff}^7$  and only appear at 2-loop

# Results II: High Scale Constraints on $\Delta C_{eff}^9(5GeV^2)$

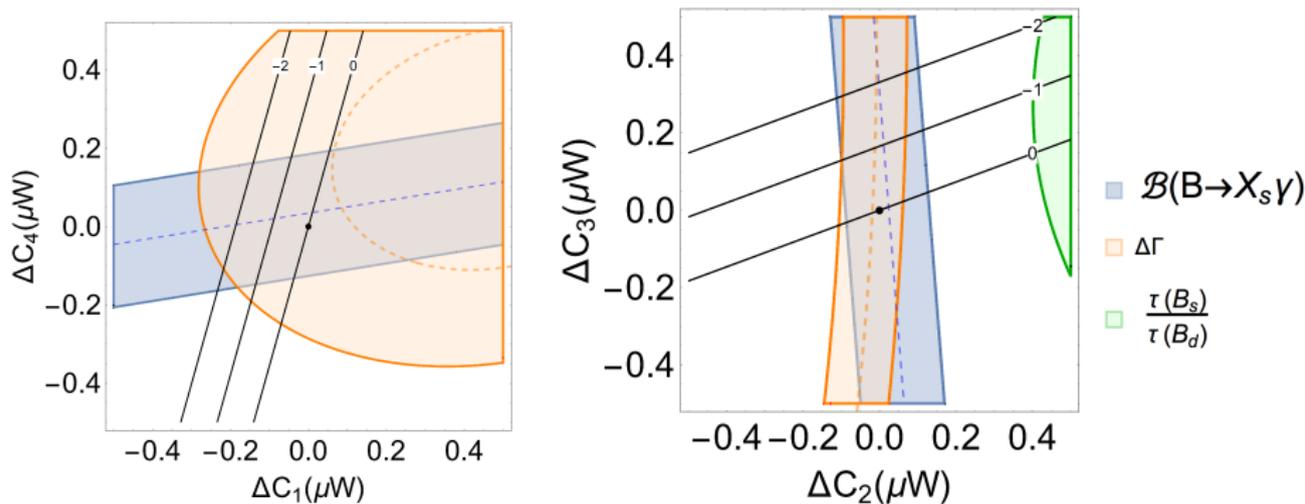


NP in  $C_1$ - $C_2$  scenario

NP in  $C_3$ - $C_4$  scenario

- In the  $C_1$ - $C_4$  and  $C_3$ - $C_4$  scenario,  $B \rightarrow X_s \gamma$  and mixing constraints allows a negative shift to  $C_9^{eff}$

## Results III: Constraints on $\Delta C_{eff}^9(5GeV^2)$



NP in  $C_1$ - $C_4$  scenario

NP in  $C_2$ - $C_3$  scenario

- Lifetime ratio  $r = \left( \frac{\tau_{B_s}}{\tau_{B_d}} \right)$  could discriminate between different scenarios - all 6 combinations of Wilson coefficients under investigation

# $B_s - B_d$ Lifetime Ratio - Outlook

- **New Dirac structures** emerge in  $\Delta B = 0$  operator basis  $\Rightarrow$  New matrix elements

$$\mathcal{O}_{V-A}^s = (\bar{b}_L \gamma^\mu s_L)(\bar{s}_L \gamma_\mu b_L)$$

$$\mathcal{O}_{S-P}^s = (\bar{b}_R s_L)(\bar{s}_L b_R)$$

$$T_{V-A}^s = (\bar{b}_L \gamma^\mu T^a s_L)(\bar{s}_L \gamma_\mu T^a b_L)$$

$$T_{S-P}^s = (\bar{b}_R T^a s_L)(\bar{s}_L T^a b_R)$$

M. Neubert and C. Sachrajda,  
[hep-ph/9709386](https://arxiv.org/abs/hep-ph/9709386)

## New Operators

$$\mathcal{O}_{LR}^s = (\bar{b}_L \gamma^\mu s_L)(\bar{s}_R \gamma_\mu b_R)$$

$$\mathcal{O}_{LL}^s = (\bar{b}_R s_L)(\bar{s}_R b_L)$$

$$T_{LR}^s = (\bar{b}_L \gamma^\mu T^a s_L)(\bar{s}_R \gamma_\mu T^a b_R)$$

$$T_{LL}^s = (\bar{b}_R T^a s_L)(\bar{s}_R T^a b_L)$$

- In Heavy Quark Limit Number of independent operators has been reduced
- Eliminate odd parity operator matrix elements  $\rightarrow$  Reduce number more
- Large  $N_c$  limit  $\rightarrow$  Some matrix new elements may be suppressed

# Conclusions

- Deviations of SM theory predictions from experimental data could be explained by a negative shift in  $C_9$
- Charmed new physics in  $b \rightarrow c\bar{c}s$  transitions could provide an explanation, but will affect mixing
- A feature of the low scale scenario where NP enters at  $\mu \approx 4.6$  is the  $q^2$  dependence of  $\Delta C_9^{eff}$
- Bounds from mixing observables  $\frac{\Delta\Gamma}{\Delta M}$  and from inclusive  $\mathcal{B}r(B \rightarrow X_s\gamma)$  allow a negative shift to  $C_9$  in NP high scales BSM scenarios for both SM and BSM Wilson coefficients
- Lifetime ratio  $r = \left(\frac{\tau_{B_s}}{\tau_{B_d}}\right)$  may be able to discriminate between different scenarios - currently under investigation
- New  $\Delta B = 0$  operators appear in Lifetime calculation - can be reduced in HQ limit

# Back up slides

# $\Delta C_7(q^2)$ and Loop functions

- The coefficients  $\Delta C_9$  and  $\Delta C_7$  are

$$\Delta C_{\text{eff}}^7 = \frac{m_c}{m_b} \left[ (4(3C_9 + C_{10}) - (3C_7 + C_8)) y + \frac{(4(3C_5 + C_6) - (3C_7 + C_8))}{6} \right]$$

$$\Delta C_{\text{eff}}^9 = \left[ ((3C_1 + C_2) - \frac{1}{2}(3C_3 + C_4)) h - \frac{2}{9}(3C_3 + C_4) \right]$$

- The loop functions are

$$h(q^2, m_c, \mu) = -\frac{4}{9} \left( \ln \left( \frac{m_c^2}{\mu^2} \right) - \frac{2}{3} - z + (z + 2) \sqrt{|z - 1|} \arctan \left( \frac{1}{\sqrt{z-1}} \right) \right)$$

$$y(q^2, m_c, \mu) = -\frac{1}{3} \left( \ln \left( \frac{m_c^2}{\mu^2} \right) - \frac{3}{2} + 2 \sqrt{|z - 1|} \arctan \left( \frac{1}{\sqrt{z-1}} \right) \right)$$

- $z = \frac{4m_c^2}{q^2}$ ,  $z < 1$