Rare B decays: SM and/or beyond

Sebastian Jäger (University of Sussex)

UK Flavour 2017 Durham, IPPP, 05 September 2017

05/09/2017

Sebastian Jaeger - Durham, 05 Sep 2017

Is the SM in trouble?



SM

20

15

10

- Global analysis of rare semileptonic decays (pre-RK*)
 - several branching ratios seem low compared to SM expectation (orange)
 - angular analysis in B->K* II seems to disagree with SM expectations
 - if SM Wilson coefficients are allowed to float, negative shift to C9 favoured

Altmannshofer et al 2017



Evidence for a leptonflavour-dependent effect in branching fractions (RK, RK*)

• PRL 113 (2014) 151601

PRD 86 (2012) 032012

PRL 103 (2009) 171801

What makes a B decay rare?

- small CKM elements
- loop suppression in SM (typically of the dominant contribution)
- 'partonic phase space' in exclusive decays



In certain observables also helicity suppression
 e.g. A(B_s→µµ) proportional m_µ/m_B
 angular observables S₃, A₉ in B→K* I I

General logic: small SM -> BSM might compete. BSM might lift CKM, loop, or helicity suppression

Rare semileptonic B decays

many new results on LHCb, ATLAS, CMS, Belle. Some anomalies

Branching ratios (differential in dilepton mass): $B \rightarrow K^{(*)}\mu\mu$, $B \rightarrow K^{(*)}ee$, $B_s \rightarrow \phi\mu\mu$ $R_{K^{(*)}}[a,b] = \frac{\int_{a}^{b} \frac{d\Gamma}{dq^{2}} (B \to K^{(*)} \mu^{+} \mu^{-}) dq^{2}}{\int_{a}^{b} \frac{d\Gamma}{dq^{2}} (B \to K^{(*)} e^{+} e^{-}) dq^{2}}$ Lepton universality ratios differential angular distribution for B->VII : 3 angles, dilepton mass q² θ_{K^*} -> angular differential observables P_i Sensitive to effective couplings $\begin{array}{ccc} & (\bar{s}\sigma^{\mu\nu}P_Rb)F_{\mu\nu} & \mathbf{C_7} \\ & (\bar{s}\gamma_{\mu}P_Lb)(\bar{l}\gamma^{\mu}l) & \mathbf{C_9} \\ & (\bar{s}\gamma_{\mu}P_Lb)(\bar{l}\gamma^{\mu}\gamma^5l) & \mathbf{C_{10}} \end{array}$ (BSM constrained by inclusive) + BSM? + BSM?

Theory uncertainties: C_i multiplied by nonperturbative form factors C_9 degenerate with virtual-charm contributions

& right-handed currents C_i'

Weak Hamiltonian for rare semileptonic decay:

 C_9 : dilepton from vector current (L=1)

$$Q_{9V} = \frac{\alpha_{\rm em}}{4\pi} (\bar{s}\gamma_{\mu}P_L b)(\bar{l}\gamma^{\mu}l)$$

 C_{10} : dilepton from axial current (L=1 or 0)

$$Q_{10A} = \frac{\alpha_{\rm em}}{4\pi} (\bar{s}\gamma_{\mu}P_L b) (\bar{l}\gamma^{\mu}\gamma^5 l)_A$$

- both can be obtained from Z' exchanges
- or leptoquarks

rks Descotes-Genon et al; Altmannshofer et : Alonso-Grinstein-Martin Camalich; Hiller-Schmaltz; Allanach et al; Gripajos et al; ...

C₇ : dilepton produced through photon (virtuality q², pole at q²=0)

$$Q_{7\gamma} = \frac{e}{16\pi^2} m_b \left(\bar{s}\sigma_{\mu\nu} P_R b\right) F^{\mu\nu}$$

- strongly constrained from inclusive b->s decay

BSM: also parity-transformed operators (C₉', C₁₀', C₇')
C₉, C₁₀ can depend on the lepton flavour.
Universal BSM effects in C₉ mimicked by a range of SM effects
C10 effects or lepton-specific effects distinguishable from SM effects

Weak Hamiltonian 2/2

Also purely hadronic operators are important, primarily:



Induces strong scale dependence of C_9 – must cancel in observables.

-> also means BSM bscc operators can induce sizable ΔC_9 (Talk by K. Leslie) At $\mu = 4.6$ GeV: $C_9(\mu) \sim 4$ $C_{10}(\mu) \sim -4$ $C_7^{eff}(\mu) \sim -0.3$ Chiral combinations: $C_L = (C_9 - C_{10})/2 \sim 4$ $C_R = (C_9 + C_{10})/2 \sim 0$ The near-vanishing of $C_R(4.6$ GeV) is a complete numerical accident.



Form factors

In helicity basis (makes for simple expressions in HQ limit):

$$-im_B \tilde{V}_{L(R)\lambda}(q^2) = \langle M(\lambda) | \bar{s} \epsilon^*(\lambda) P_{L(R)} b | \bar{B} \rangle,$$

$$m_B^2 \tilde{T}_{L(R)\lambda}(q^2) = \epsilon^{*\mu}(\lambda) q^{\nu} \langle M(\lambda) | \bar{s} \sigma_{\mu\nu} P_{R(L)} b | \bar{B} \rangle$$

$$im_B \tilde{S}_{L(R)}(q^2) = \langle M(\lambda = 0) | \bar{s} P_{R(L)} b | \bar{B} \rangle.$$

SJ, Martin Camalich 2012 (Bharucha, Feldmann, Wick 2010)

Close to q²_{max}: determinations from lattice QCD (B -> pi; K; stable V) Low q²: no first-principles determinations

- heavy-quark limit: calculable relations, eg 7 FF -> 2 FF for B->V uncontrolled systematic: power corrections ($\Lambda/m_b = 10\%$? 20% ?)
- light-cone sum rules (LCSR)

correlation function
$$G_{F\lambda}(q^2; p^2) = i \int d^4y e^{-ip \cdot y} \langle K^*(k) | T\{\epsilon^*_\mu(q;\lambda)(\bar{s}\Gamma^\mu_F b)[0] j^\dagger_B(y)\} | 0 \rangle$$

$$G_{F\lambda} = \underbrace{\begin{array}{c} \text{hadronic representation} \\ p^2 - m_B^2 \end{array}}_{p^2 - m_B^2} \underbrace{\begin{array}{c} \text{Form factor} \\ \text{(output)} \\ m_b \end{array}}_{F_{B}m_B^2} + \dots, \\ F_{B}m_B^2 + \dots,$$

model omitted higher states: Borel transform & continuum threshold ("semilocal parton-hadron duality")

Main uncontrolled systematic: continuum threshold (not parametrically suppressed)

Nonlocal term and scale dependence

$$\begin{split} H_{V}(\lambda) \propto \tilde{V}_{\lambda}(q^{2})C_{9} - V_{-\lambda}(q^{2})C'_{9} + \frac{2 m_{b}m_{B}}{q^{2}} \left(\tilde{T}_{\lambda}(q^{2})C_{7} - \tilde{T}_{-\lambda}(q^{2})C'_{7}\right) \underbrace{\left[\frac{16 \pi^{2}m_{B}^{2}}{q^{2}}h_{\lambda}(q^{2})\right]}_{q^{2}} + \text{strong interactions!} \\ \\ \text{more properly:} \quad \frac{e^{2}}{q^{2}}L_{V}^{\mu}a_{\mu}^{\text{had}} = -i\frac{e^{2}}{q^{2}}\int d^{4}xe^{-iq\cdot x} \langle \ell^{+}\ell^{-}|j_{\mu}^{\text{em,lept}}(x)|0\rangle \underbrace{\int d^{4}y \, e^{iq\cdot y} \langle M|j^{\text{em,had},\mu}(y)\mathcal{H}_{\text{eff}}^{\text{had}}(0)|\bar{B}\rangle}_{\text{nonlocal, nonperturbative, large normalisation (V_{\text{cb}}^{*} \text{V}_{\text{cs}} \text{C}_{2})} \end{split}$$

traditional "ad hoc fix" : $C_9 \rightarrow C_9 + Y(q^2) = C_9^{eff}(q^2)$ $C_7 \rightarrow C_7^{eff}$

Systematic justification in QCD factorisation (low q2, heavy quark limit) scale dependence cancels order by order in PT

Beneke, Feldmann, Seidel 2001,2004

power corrections ? But subdominant to FF (S\$, JMAattin Camaditbh 20022, 20034)



High q2: OPE in 1/q2

duality violation ? Grinstein, Pirjol 2004; Beylich/Buchalla/Feldmann 2008, Lyon & Zwicky 2014

Data-driven determination?

Bobeth, Chrzaszcz, Van Dyk, Virto 2017

Basic idea: reduce theory dependence of h_{λ} by using data & analyticity

- Ignoring CKM-suppressed terms, h_{λ} is complex-analytic in q2 except for a cut from 4 m_D^2 to infinity, and poles at the J/psi and psi²

- Use QCDF (+LCSR pc estimate) only at q2 <~ 0
- And experimental data to fix/constrain the residues at the poles
- Conformal mapping to increase separation of the input data from the cut in hope of a fast-converging Taylor series (truncate after 3 terms)

k	0	1	2
$\operatorname{Re}[\alpha_k^{(\perp)}]$	-0.06 ± 0.21	-6.77 ± 0.27	18.96 ± 0.59
$\mathrm{Re}[\alpha_k^{(\parallel)}]$	-0.35 ± 0.62	-3.13 ± 0.41	12.20 ± 1.34
$\operatorname{Re}[\alpha_k^{(0)}]$	0.05 ± 1.52	17.26 ± 1.64	_
$\mathrm{Im}[\alpha_k^{(\perp)}]$	-0.21 ± 2.25	1.17 ± 3.58	-0.08 ± 2.24
$\mathrm{Im}[\alpha_k^{(\parallel)}]$	-0.04 ± 3.67	-2.14 ± 2.46	6.03 ± 2.50
$\operatorname{Im}[\alpha_k^{(0)}]$	-0.05 ± 4.99	4.29 ± 3.14	-



Used with LCSR form factors gives BSM C9 consistent with when HQE computation is used with LCSR FF form factors

If the convergence/stability of this method can be established, it may eliminate the charm loop as a source of concern for interpreting low-q2 data.

No new information on form factors

05/09/2017

Scalar branching ratio

In this case only helicity zero, no photon pole, mild dilepton mass dependence Schematically (neglecting some normalisations and small imaginary parts),

$$H_V = C_7 T + C_9 V + h \qquad H_A = C_{10} V$$

BR \propto (|H_V|^2 + |H_A|^2) = $\frac{1}{2} (C_7 T + h_0 + 2C_R V)^2 + \frac{1}{2} (C_7 T + h_0 + 2C_L V)^2$

Because C_7 and C_R are small in the SM, BR essentially is determined by the product $C_L \cdot V$. Weak sensitivity to C_R (as long as small) or C_7 .



Explains the shape of the BR band: part of a circle around (-4, +4) (centre far outside plot region)

Suggests 20-25% suppression of C_L w.r.t SM

But perfectly degenerate with form factor V ! To interpret this as evidence of BSM physics need precision on V much better than 25%. Form factor estimates from light-cone sum rules

Angular observables

For zero mass there are the following independent observables:

Forward-backward asymmetry / P₂

The zero-crossing of $I_6^s = F\beta \operatorname{Re} \left[H_V^- (H_A^-)^* - H_V^+ (H_A^+)^* \right]$ (or of A_{FB}, or P2)

approximately coincides with that of HV-, because HV+ HA+ is doubly suppressed in the heavy-quark limit (and constrained by non-signal in I3, I9).

Have

 $H_V^- \propto \frac{2m_b^2}{q^2} C_7 T_- + C_9 V_- + h_-$

Zero depends on form factor ratio T-/V- (besides on nonlocal term h-). This ratio is calculable in the heavy-quark limit (in terms of meson LCDA's). Charles et al 1999 Beneke, Feldmann 2000

Forms the basis for the 'optimised observables' (P2, P5', etc) Descotes-Genon, Hofer, Matias, Virto

HQ limit: T-(0)/V-(0) ~ 1.05 > 1

compare to: T_(0)/V_(0) = 0.94 +/- 0.04[D Straub, priv comm based on
Bharucha, Straub, Zwicky 1503.05534]LCSR computation with correlated parameter variations.Size consistent with a power correction; 5% uncertainty estimate.

05/09/2017

P2 – theory vs data



Boxes – predictions from SJ, Martin Camalich 2014

(pure heavy-quark limit, general power correction parameterisation, varying in 10% range, Gaussian error combination)

Good agreement with data, even for pure heavy-quark limit with no power corrections (red lines)

P5'



As a result, the C10 (as well as form factor) dependence largely cancels, and the observable is strongly dependent on C9 (very roughly proportional)

However, the number of independent hadronic inputs (for which power corrections must be estimated, LCSRs used, etc) is larger, because both transverse and longitudinal helicities enter.

Emphatic claims in literature that this does not matter Descotes-Genon et al; Capdevila et al

P5'



Simone Bifani, seminar at CERN (overlaid predictions from SJ&Martin Camalich 2014)

Modest discrepancy around 4-6 GeV, consistent with reduced C9

05/09/2017

C9 sensitivity w/o light-cone sum rules

Most general parameterisation of power correction to the heavy-quark limit; varying each parameter at 10% of 'natural' leading-power effect; profile likelihood



Preference for C9<C9SM, with modest significance

Lepton universality measurements vs theory





Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446

Theory uncertainties completely negligible relative to experimental ones.

 $p(SM) = 2.1 \times 10^{-4} (3.7)$

Suggests nonzero C10(BSM)

Dastian Jaeger - Durham, 05 Sep 2017

Pure LUV fit

Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446 Also Capdevila et al, Ciuchini et al, Altmannshofer et al, D'Amico et al, Hiller & Nisandzic

Obs.	Expt.	SM	$\delta C_L^\mu = -0.5$	$\delta C_9^\mu = -1$	$\delta C_{10}^{\mu} = 1$	$\delta C_9^{\prime \mu} = -1$
$R_K [1, 6] \mathrm{GeV}^2$	0.745 ± 0.090	$1.0004^{+0.0008}_{-0.0007}$	$0.773_{-0.003}^{+0.003}$	$0.797^{+0.002}_{-0.002}$	$0.778^{+0.007}_{-0.007}$	$0.796^{+0.002}_{-0.002}$
R_{K^*} [0.045, 1.1] GeV ²	0.66 ± 0.12	$0.920^{+0.007}_{-0.006}$	$0.88^{+0.01}_{-0.02}$	$0.91^{+0.01}_{-0.02}$	$0.862^{+0.016}_{-0.011}$	$0.98^{+0.03}_{-0.03}$
R_{K^*} [1.1, 6] GeV ²	0.685 ± 0.120	$0.996\substack{+0.002\\-0.002}$	$0.78^{+0.02}_{-0.01}$	$0.87^{+0.04}_{-0.03}$	$0.73_{-0.04}^{+0.03}$	$1.20^{+0.02}_{-0.03}$
R_{K^*} [15, 19] GeV ²	—	$0.998\substack{+0.001\\-0.001}$	$0.776_{-0.002}^{+0.002}$	$0.793\substack{+0.001 \\ -0.001}$	$0.787^{+0.004}_{-0.004}$	$1.204_{-0.008}^{+0.007}$



Theory uncertainties negligible. 1sigma and 3sigma confidence regions

C10(BSM)>0 favoured

p = 0.158

SM pull 3.78 sigma

Considerable degeneracy (flat direction in chi2)

Adding Bs->mu mu



Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446

Selective probe of C10 (and C10')

Theory error negligible relative to exp (will hold till the end of HL-LHC !)

Considerably narrows the allowed fit region

p = 0.191

SM point excl. at 3.76 sigma

Fit prefers nonzero CL = (C9-C10)/2

CR = (C9+C10)/2 not well constrained and consistent with zero

1-parameter CL fit: besf fit -0.61. 1sigma [-0.78, -0.46], p = 0.339 SM point (origin) excluded at 4.16 sigma 05/09/2017 Sebastian Jaeger - Durham, 05 Sep 2017

Adding B->K*µµ,ee angular data

Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446



Serves to determine best-fit region even better.

SM pull 4.17 sigma

p = 0.572 [63 dof]

(but p(SM) now up to to 0.086)

Wilson coefficient value CL=0 again excluded at high confidence.

Determining CR (break C9/C10 degeneracy)

Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446

Propose to measure observable



Remains very clean in presence of new physics. Probes a LUV C10 precisely, irrespective of values of C9e, C9mu

Prospective fit with LUV obs. only

Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446

Consider a hypothetical experimental result R6' = 0.80(5)



BSM models?

Assuming the effect is real, many authors have constructed models (no space to review here). They fall in two classes:

- Z' (=neutral vector) mediator (tree, loop-level, or composite)
- Leptoquark mediators (tree, loop-level, or composite)

None of these particles (so far as I know) address the naturalness problem, or any other theoretical puzzle (although they could be part of a more elaborate structure that does).

Given that the naturalness problem is the main reason to expect new flavour physics at the TeV scale, it would be desirable to have a models where RK, RK* (and perhaps RD, RD* - not discussed here) are more directly connected to naturalness.

Summary

observable	Anomaly?	Dominant theory error	comment
Branching ratios (differential)	Lowish in muonic final states	Form factor values	
Angular (muonic)	P5' off; significance unclear (1-3σ?)	Form factor ratios, long-distance charm	
Angular (electronic)	None (but low statistics)	Similar to muonic	Best theoretical sensitivity to C ₇ '
Lepton-universality ratios (RK, RK*)	Each of 3 bins off by >2σ; 3.7σ combined	no known issue (dominant is QED radiation – tiny)	clean NP discovery with more data Belle2 confirmation?

Possible BSM explanations

to explain all anomalies: require BSM $\bar{s}_L b_L \bar{\mu}_L \mu_L$ coupling to explain only RK, RK*: BSM $\bar{s}_L b_L \bar{\mu}_L \mu_L$ or various $\bar{s}b\bar{e}e$ possibilities

Eagerly anticipating LHCb updates of RK, RK* with more data; ratios for ${\sf B}_s {\to} \phi {\sf II};$ angular lepton-universality tests

Experimental uncertainties in RK, RK*, ... at LHC dominated by electronic modes: Belle2 powerful, with different systematic

Must C9 show LUV ?

Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446

Modified C10 needed to suppress RK* (both bins)



Preference for modified C9 (over C10) is due to angular observables in B->K* mu mu

This means a model with (for example) nonzero CLmu and in addition an ordinary, **leptonflavour-universal**, **C9**, can describe the data similarly well or better

Eg. 'charming BSM' scenario

SJ, Kirk, Lenz, Leslie arXiv:1701.09183

b→c т v(т)

For some time B-factories and LHCb have consistently shown semileptonic B ->D (D*) τv decay rates larger than expected

$$R(D^{(*)}) = \frac{BR(B \to D^{(*)}\tau\nu_{\tau})}{BR(B \to D^{(*)}\ell\nu_{\ell})}$$



3.9 sigma effect

SM tree-level effect



Theory error negligible relative to experiment

 $b \rightarrow C T V(T)$

Can be interpreted as BSM effect

Including differential decay distribution, data favour modification of SM effective coupling (operator with all fermions left-handed)

Eg Ligeti et al 2015,16

Possible mediation by W' or leptoquarks,



Isidori et al, Ligeti et al, Becirevic et al, Crivellin et al, ...

In principle R(D(*)) could also be affected by suppressing the couplings to light leptons; disvafoured by B-factory data