

CP violation in charmless hadronic B decays

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UK Flavour 2017, Durham

Charmless b decays

mass→	2.4 MeV	1.27 GeV	171.2 GeV
charge→	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
spin→	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
name→	u up	c charm	t top
Quarks	4.8 MeV	104 MeV	4.2 GeV
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	d down	s strange	b bottom

No charm quark in final state particles

~ 1% of b decay

Large CPV from mixing and decay or with other diagrams from different resonant structures over Dalitz plot

$$b \rightarrow s\bar{u}u$$

P + T

$$b \rightarrow d\bar{u}u$$

$$b \rightarrow s\bar{d}d$$

P

$$b \rightarrow d\bar{s}s$$

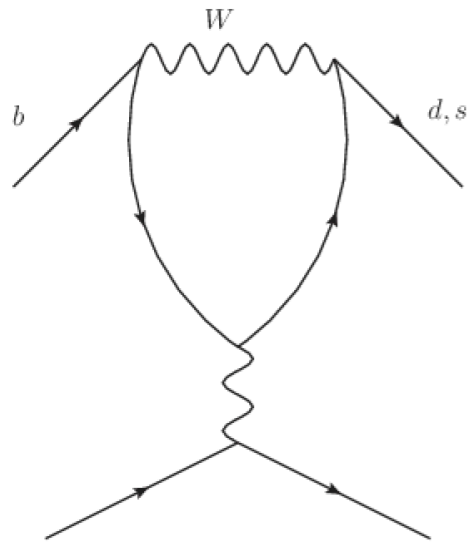
$$b \rightarrow s\bar{s}s$$

P

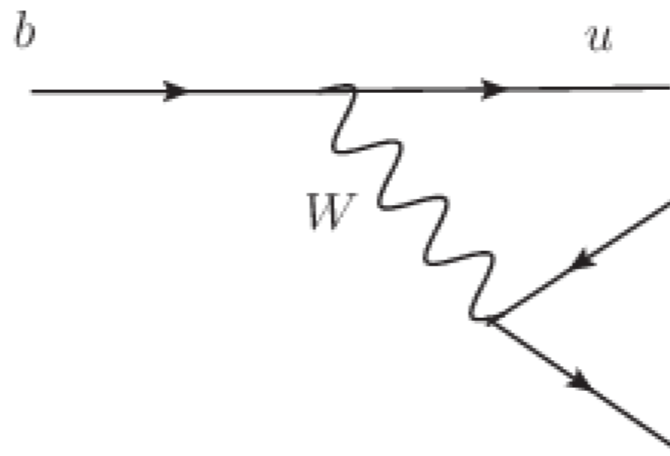
$$b \rightarrow d\bar{d}d$$

U-spin related

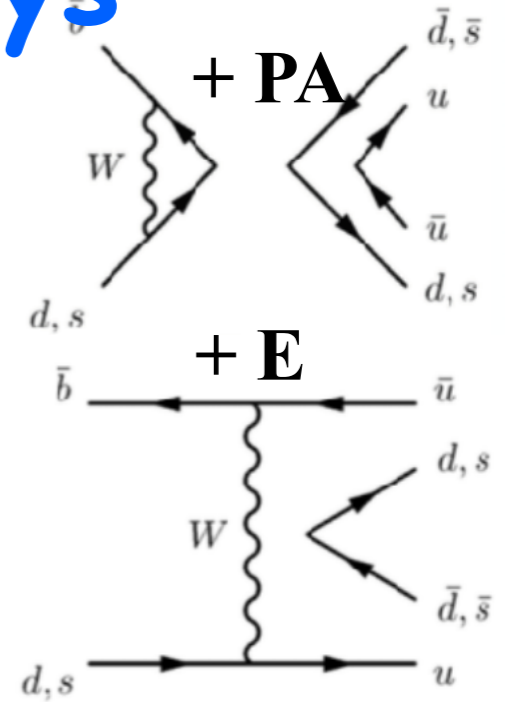
CPV in charmless B decays



$$|V_{td}|e^{i\beta} \quad \text{or} \quad -|V_{ts}|e^{-i\beta_s}$$



$$|V_{ub}|e^{-i\gamma}$$



+ **New Physics**

➤ **CPV appears when there are two competitive contributions:**

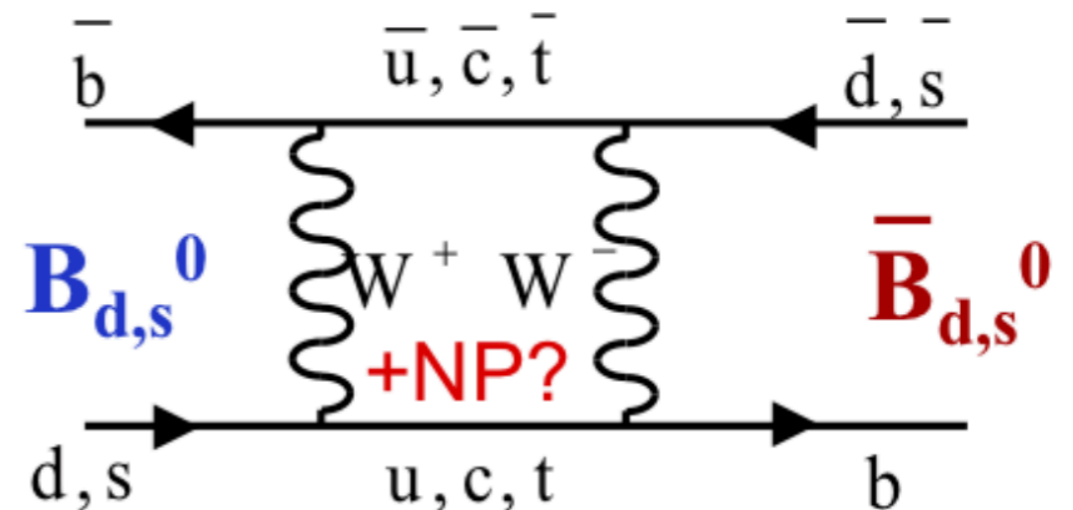
$$A = a_1 e^{i(\delta_1 + \phi_1)} + a_2 e^{i(\delta_2 + \phi_2)}$$

$$\bar{A} = a_1 e^{i(\delta_1 - \phi_1)} + a_2 e^{i(\delta_2 - \phi_2)}$$

$$A_{CP} = \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} \propto \sin(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)$$

➤ **Additional weak phase through mixing**

➤ **QCD plays an important role in the game**



$$|V_{td}|^2 e^{-2i\beta} \quad \text{or} \quad |V_{ts}|^2 e^{2i\beta_s}$$

Two body charmless B decays

➤ **Main contributions for $B^0 \rightarrow K^+K^-$ and $B_s \rightarrow \pi^+\pi^-, \pi^0\pi^0$: PA/E processes, very rare decay; two charged modes have been found by LHCb recently**

[PRL 118 \(2017\) 081801, JHEP 10 \(2012\) 037](#)

➤ **While $B_s \rightarrow K_s\pi^0, \pi^0\pi^0$ not observed yet, other decay modes are extensively studied by B factories and LHCb**

➤ **$B \rightarrow \pi\pi$ system: extract CKM angle α through Isospin relationship**

[arXiv:1705.02981](#)

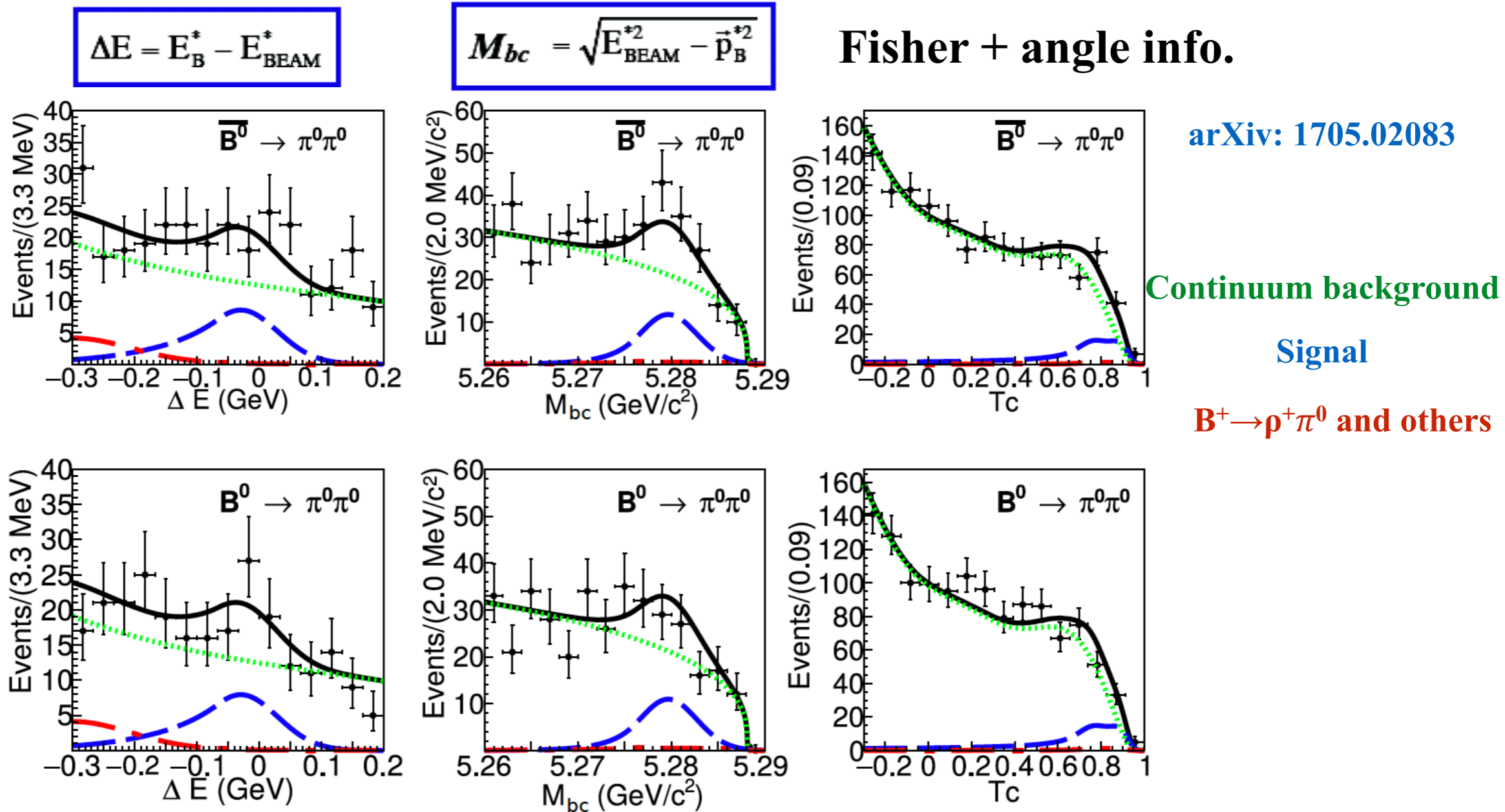
➤ **$B \rightarrow \pi\pi, B_s \rightarrow K^+K^-$ system: extract CKM angle γ and $2\beta_s$ through U-spin and U-spin + Isospin analyses**

[PLB 741 \(2015\) 1 and references therein](#)

➤ **Recently, Belle has updated the Branching fraction and A_{CP} measurements on $B^0 \rightarrow \pi^0\pi^0$ and LHCb on $B^0 \rightarrow \pi^+\pi^-$ and $B_s \rightarrow K^+K^-$**

Measurements on $B^0 \rightarrow \pi^0 \pi^0$ from Belle

➤ Measurements with $752 \times 10^6 \text{ B}\bar{\text{B}}$ (693 fb^{-1}) to replace previous results;
Time-integrated measurements; initial flavor from the other B



Projections in signal enhanced areas of other two variables

Results from $B^0 \rightarrow \pi^0 \pi^0$

$$\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0) = (1.31 \pm 0.19 \pm 0.18) \times 10^{-6}$$

arXiv: 1705.02083

$$\mathcal{A}_{CP} = +0.14 \pm 0.36 \pm 0.12$$

Some recent Predictions:

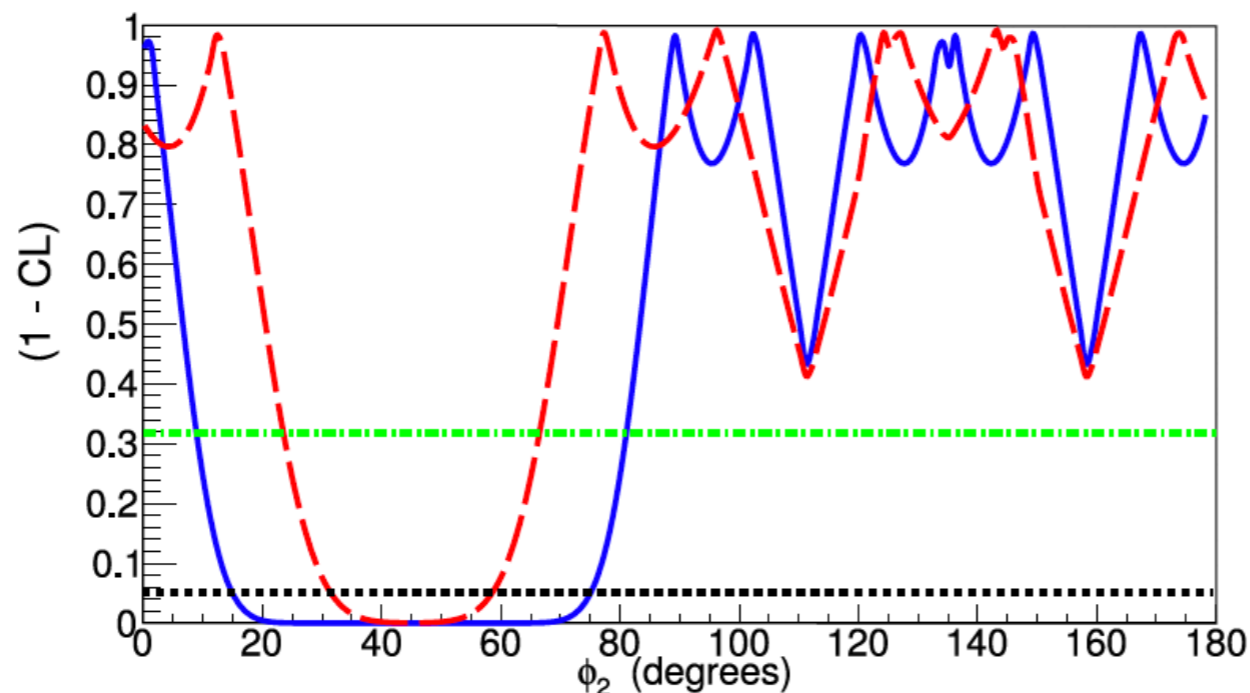
$$Br(B^0 \rightarrow \pi^0 \pi^0) = [0.23_{-0.05}^{+0.08} (\omega_b)_{-0.04}^{+0.05} (f_B)_{-0.03}^{+0.04} (a_2^\pi)] \times 10^{-6}, \quad \text{PRD 90 (2014) 014029}$$

$$\mathcal{B}(B_d \rightarrow \pi^0 \pi^0)|_{\text{PMC}} = \left(0.98_{-0.31}^{+0.44}\right) \times 10^{-6}, \quad \text{PLB 749 (2015) 422}$$

$$\text{Br}(\bar{B}^0(B^0) \rightarrow \pi^0 \pi^0) = (1.17_{-0.12}^{+0.11}) \times 10^{-6}. \quad \text{PRD 95 (2017) 034023}$$

Measured values lower and predicted values higher, though still have tensions

α excluded at 95% for $[15.5^\circ, 75^\circ]$



+ Belle results on $B^0 \rightarrow \pi^+ \pi^-$
and $B^+ \rightarrow \pi^+ \pi^0$

Previous from Belle

PRD 88 (2013) 092003

PRL 94 (2005) 181803 (253 fb⁻¹)

PRD 87 (2013) 031103(R)

Including new results

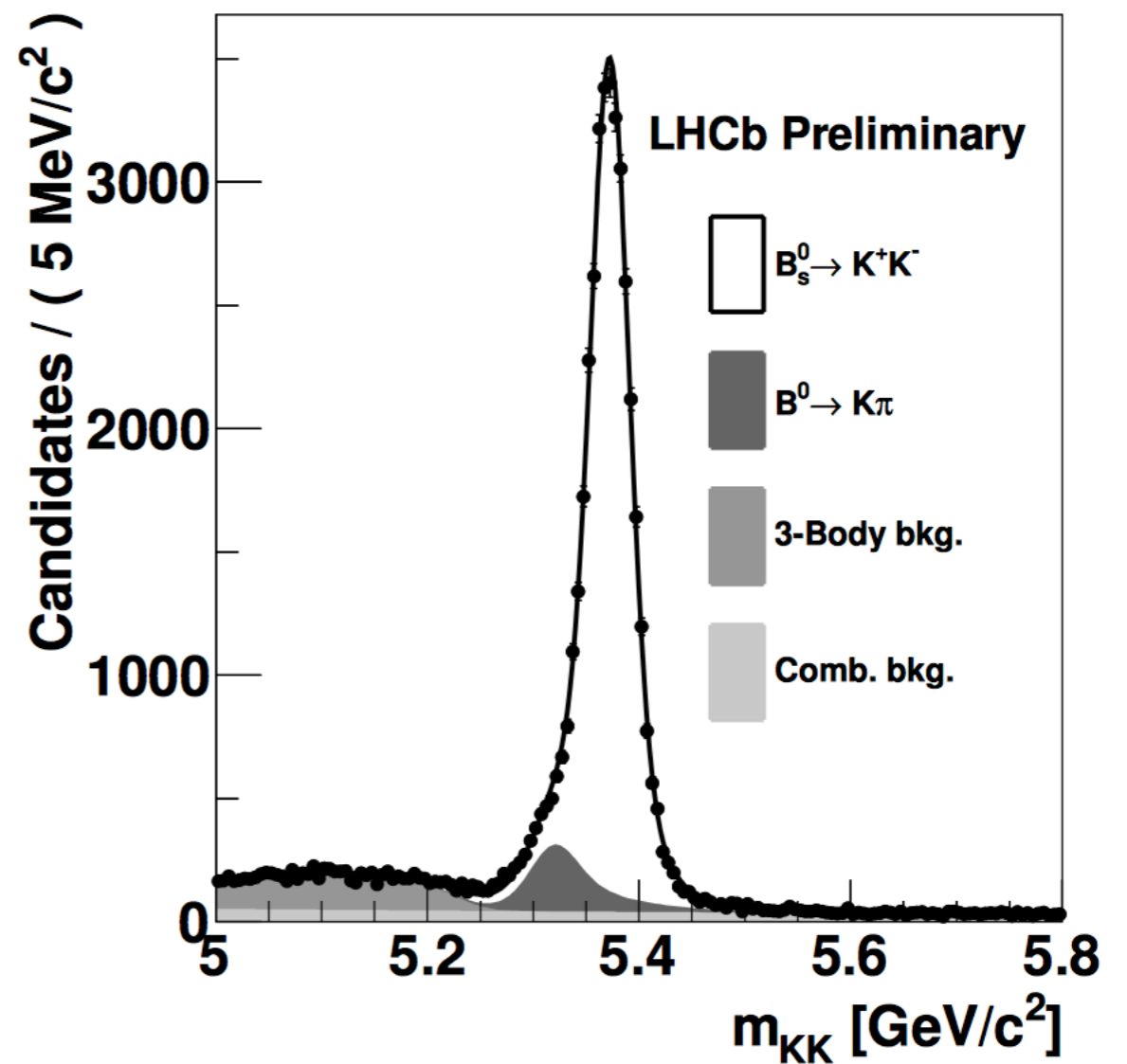
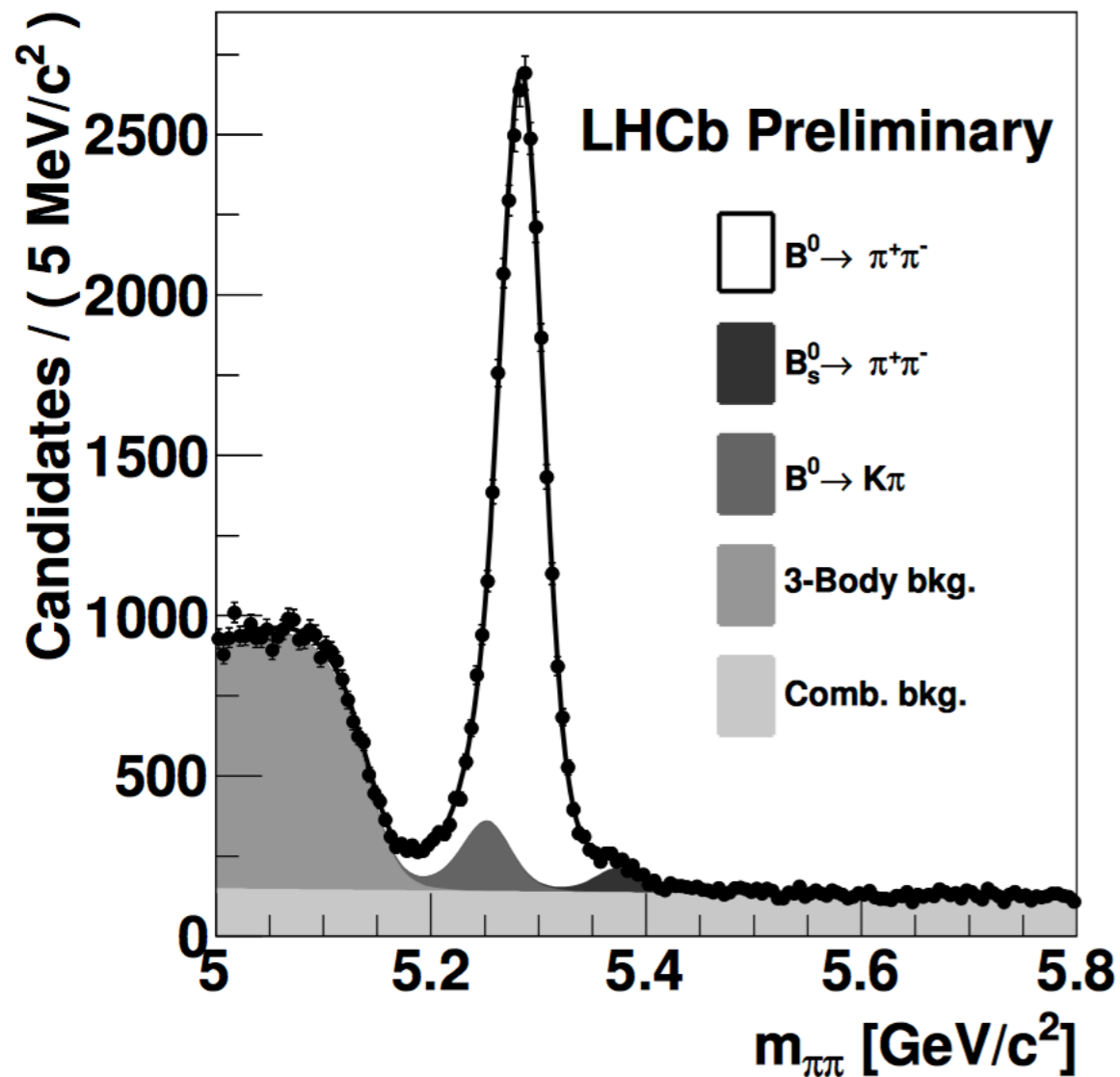
$B^0 \rightarrow \pi\pi$ and $B_s \rightarrow KK$ measurements from LHCb

LHCb-CONF-2016-018

➤ Time-dependent analysis with 3 fb^{-1} data;

$B^0 \rightarrow \pi^+\pi^-$ 28652 ± 226

$B_s \rightarrow K^+K^-$ 36840 ± 222



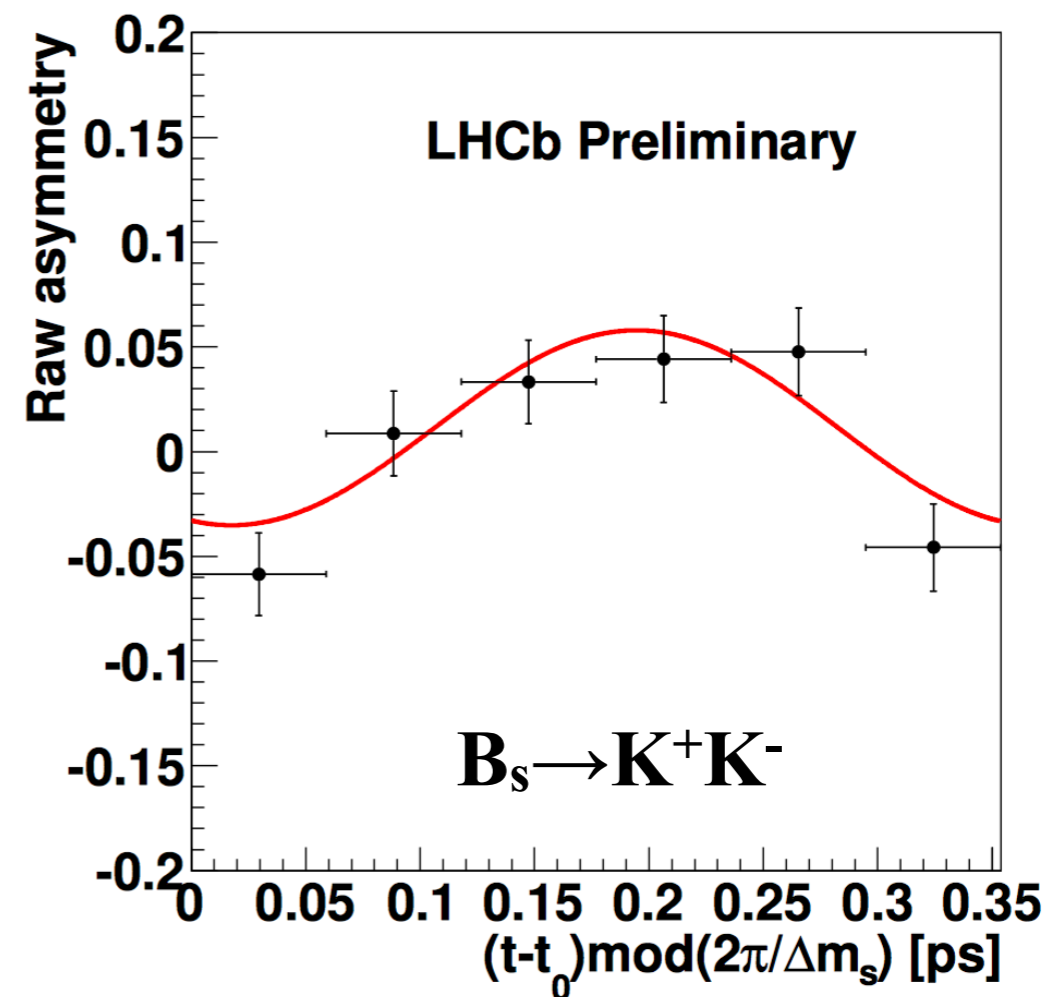
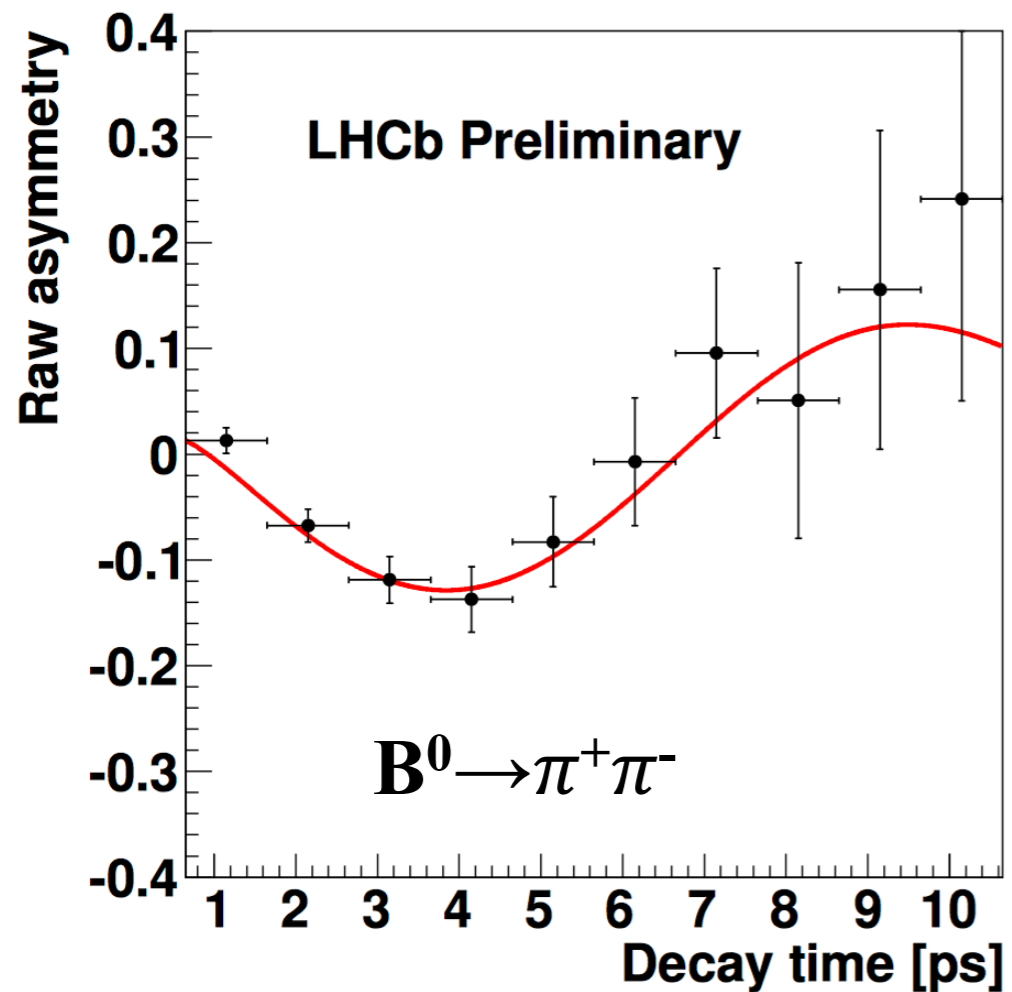
➤ Production asymmetries of $B_{d(s)}$ determined from $B_{d(s)} \rightarrow K\pi$

Time dependent asymmetries

LHCb-CONF-2016-018

➤ $\Delta m_{d(s)}$, $\Delta\Gamma_{d(s)}$ and $\Gamma_{d(s)}$ fixed from measured values

$$\mathcal{A}(t) = \frac{\Gamma_{\bar{B}_{(s)}^0 \rightarrow f}(t) - \Gamma_{B_{(s)}^0 \rightarrow f}(t)}{\Gamma_{\bar{B}_{(s)}^0 \rightarrow f}(t) + \Gamma_{B_{(s)}^0 \rightarrow f}(t)} = \frac{-C_f \cos(\Delta m_{d,s}t) + S_f \sin(\Delta m_{d,s}t)}{\cosh\left(\frac{\Delta\Gamma_{d,s}}{2}t\right) + A_f^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_{d,s}}{2}t\right)},$$



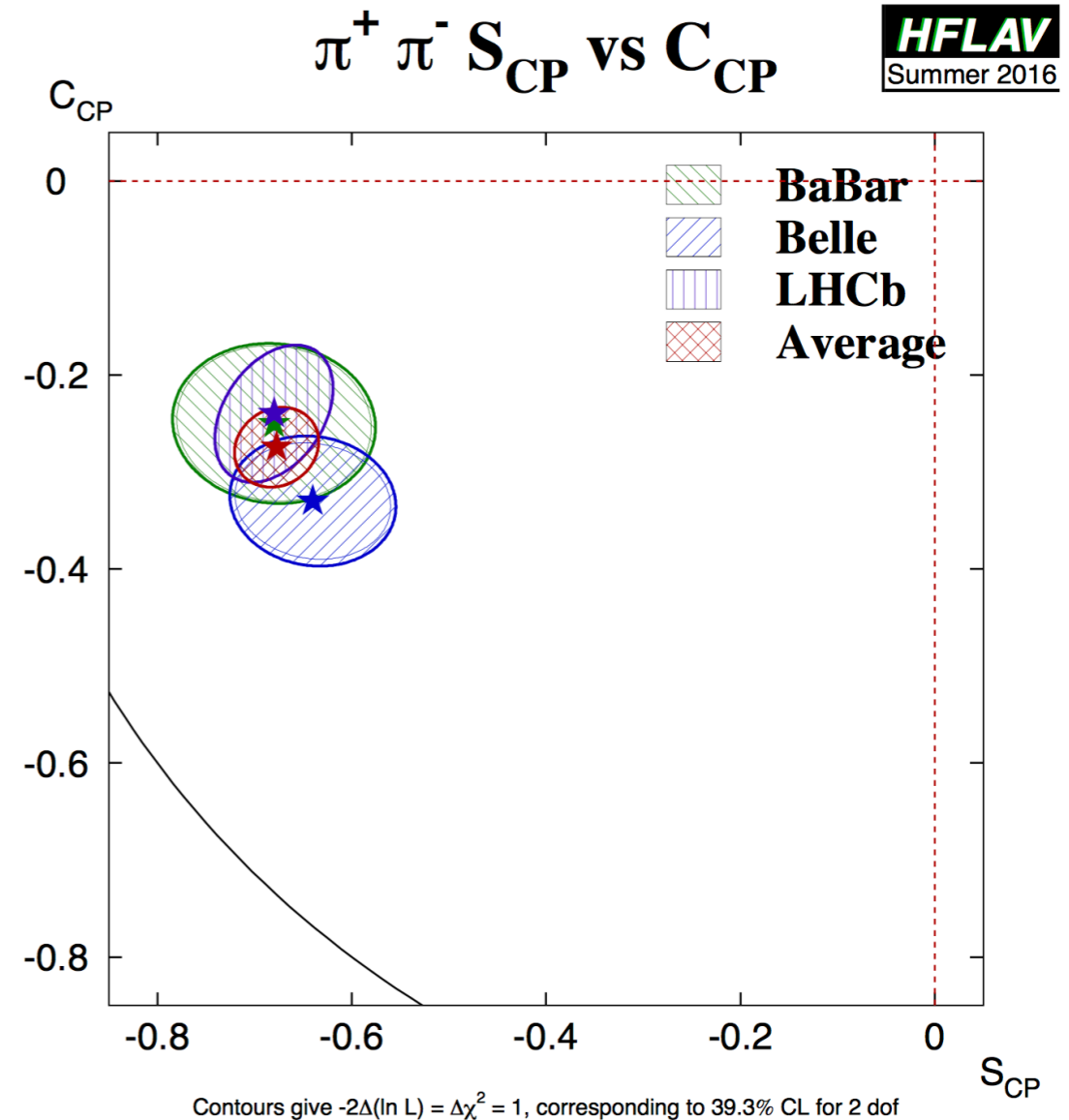
➤ $B_{(s)} \rightarrow K\pi$ used for calibration channels of flavor tagging

Results from $B^0 \rightarrow \pi\pi$ and $B_s \rightarrow KK$ measurements

LHCb-CONF-2016-018

$$\begin{aligned}
 C_{\pi^+\pi^-} &= -0.24 \pm 0.07 \pm 0.01, \\
 S_{\pi^+\pi^-} &= -0.68 \pm 0.06 \pm 0.01, \\
 C_{K^+K^-} &= 0.24 \pm 0.06 \pm 0.02, \quad 3.6\sigma \\
 S_{K^+K^-} &= 0.22 \pm 0.06 \pm 0.02, \quad 3.3\sigma \\
 A_{K^+K^-}^{\Delta\Gamma} &= -0.75 \pm 0.07 \pm 0.11,
 \end{aligned}$$

Evidence of CPV for B_s mode at 4.6σ



[arXiv:1612.07233](https://arxiv.org/abs/1612.07233)

➤ Recent updates into paper ongoing (3 fb^{-1}):

BDT selections re-optimized to gain more statistic power

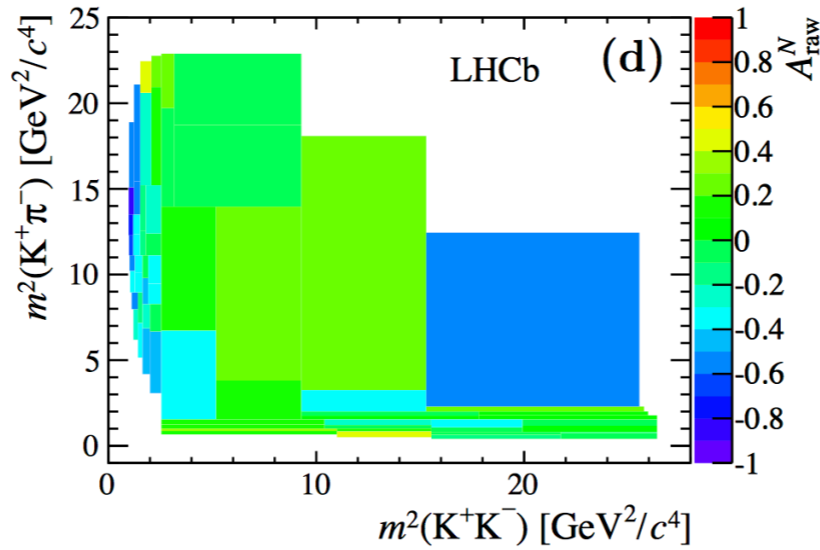
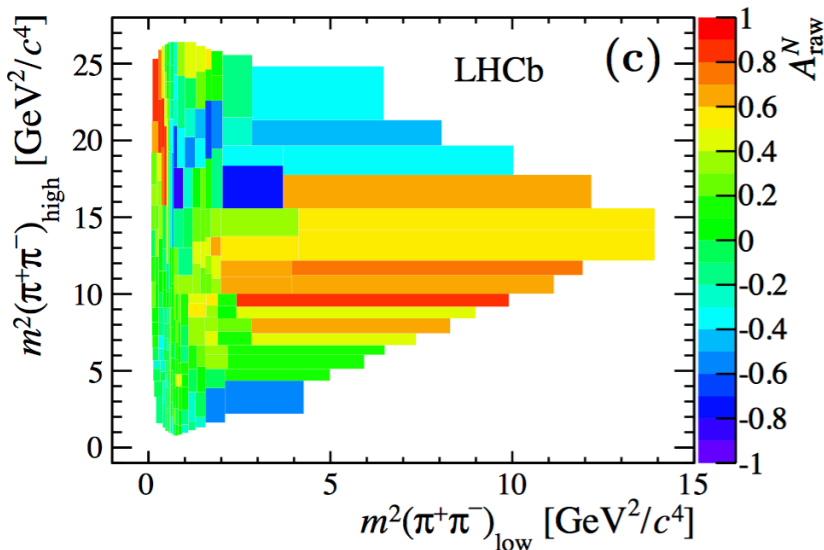
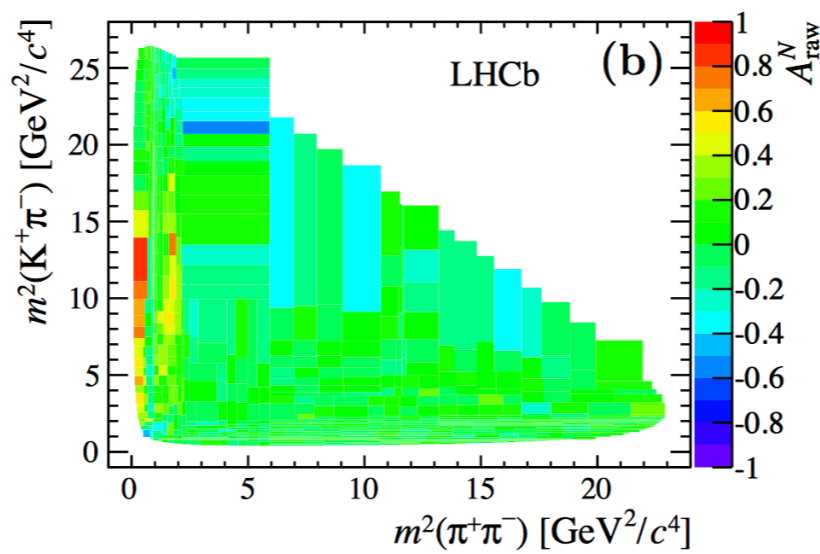
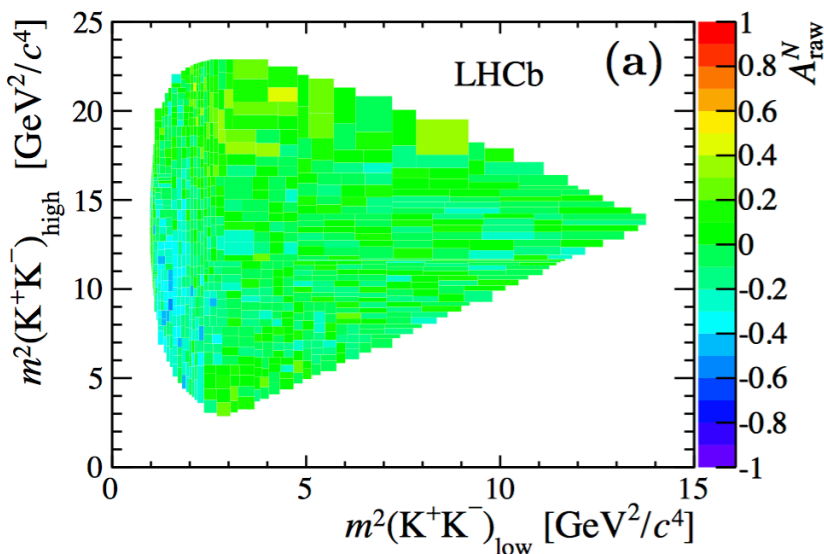
Adding SS flavor taggers

Three body charmless B decays

➤ Three body $B_{d(s)}$ charmless decays involve one or more neutral final state (π^0 or K_S): extensively studied by B factories with limited statistics; π^0 mode hard for LHCb but not fully impossible

➤ Three body B^- charmless decays with charged final states much easier experimentally; increasing interests after LHCb's CPV measurements over Dalitz plot

PRD 90, 112004 (2014)



➤ Amplitude analyses needed to extract CPV information; $B \rightarrow \pi\pi\pi$, $K\pi\pi$ and KKK have been performed by B factories

➤ Large data set collected by LHCb will show more interesting results

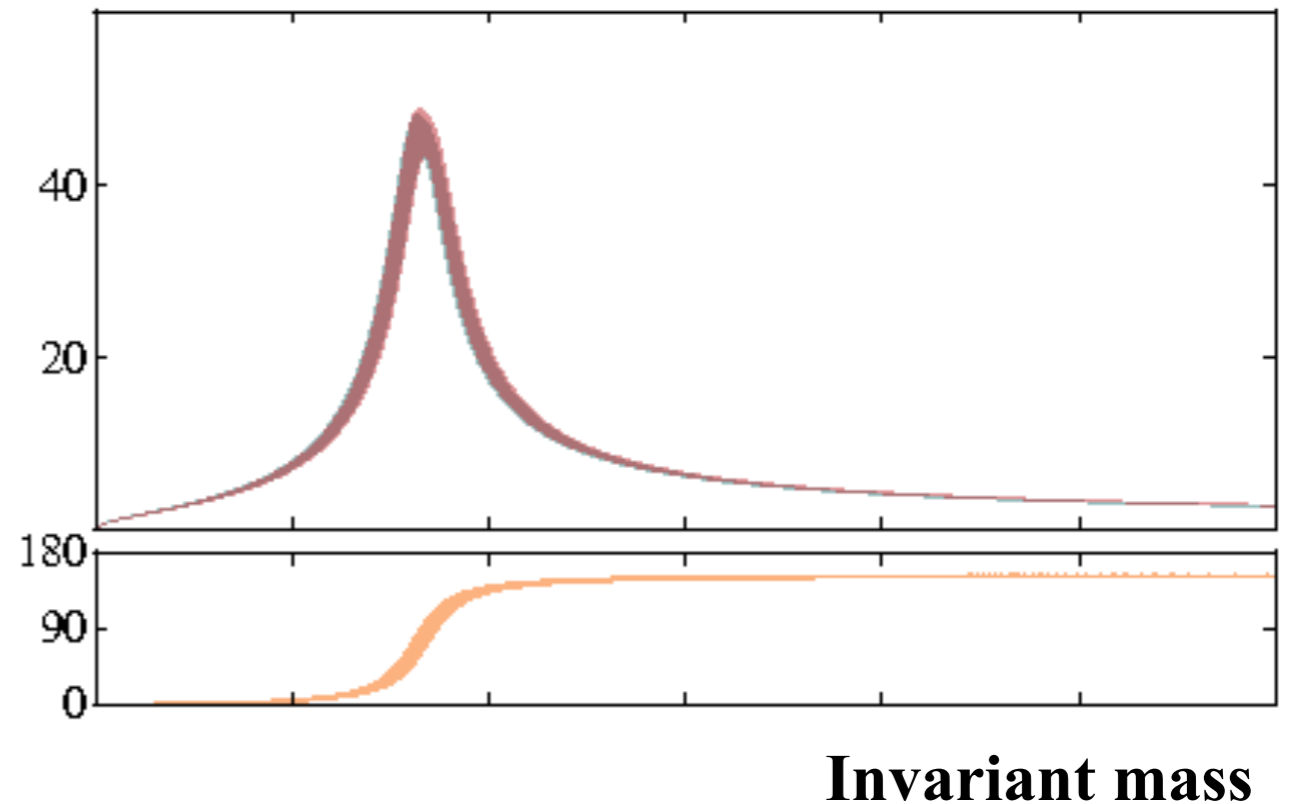
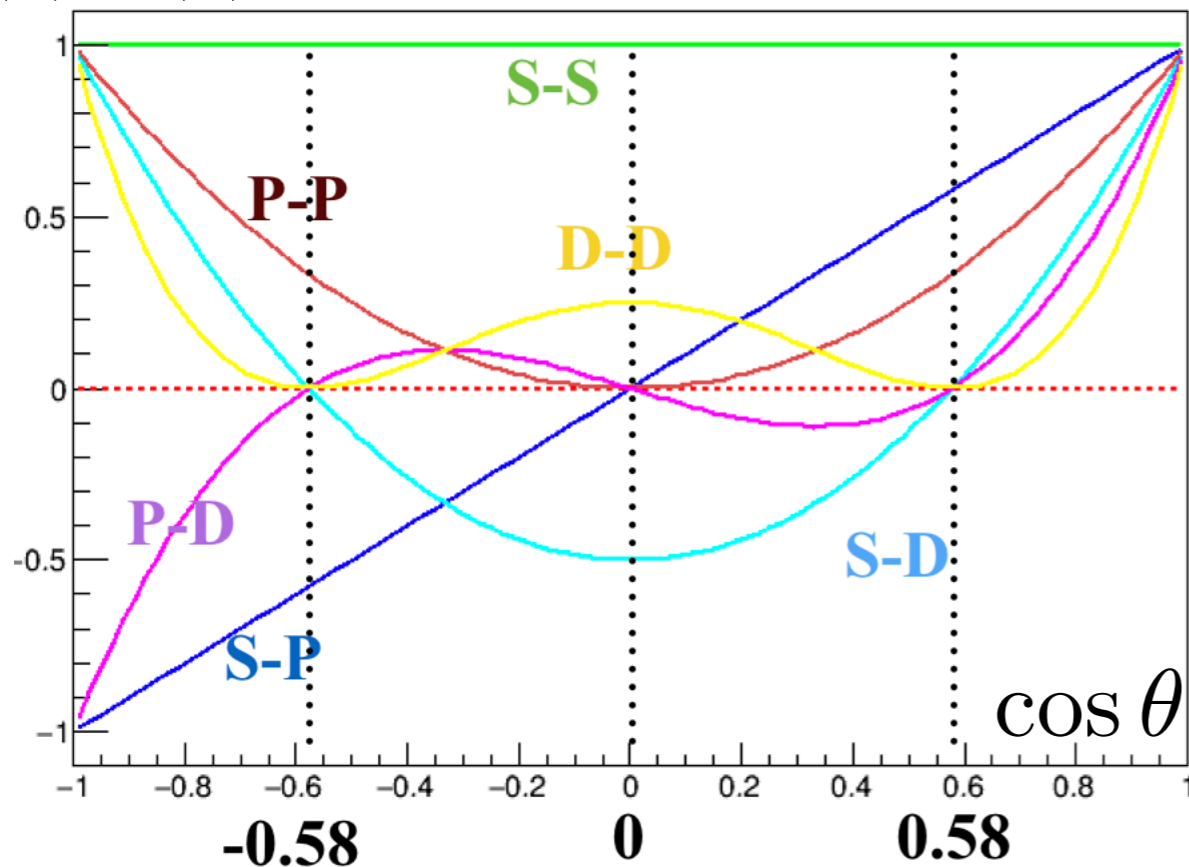
Resonant effect over Dalitz plot

➤ Full version of A_{CP} in slide 3 (also including angular distributions)

$$A_{CP} = \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} = \frac{2a_1 a_2 h_1(\theta) h_2(\theta) \sin(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)}{a_1^2 h_1^2(\theta) + a_2^2 h_2^2(\theta) + 2a_1 a_2 h_1(\theta) h_2(\theta) \cos(\delta_1 - \delta_2) \cos(\phi_1 - \phi_2)}$$

θ : helicity angle $h(\theta)$: angular distribution of resonance

$h_1(\theta)h_2(\theta)$



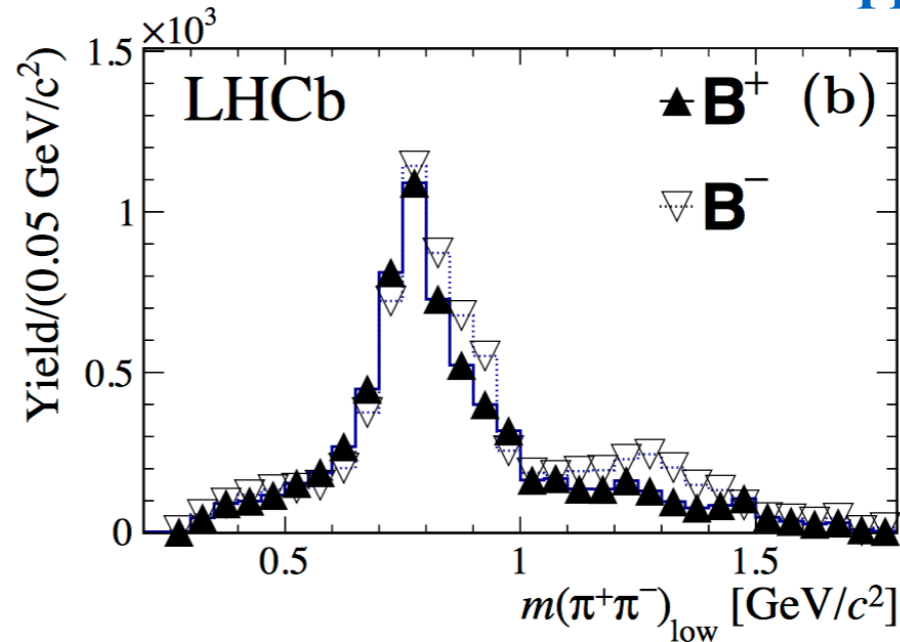
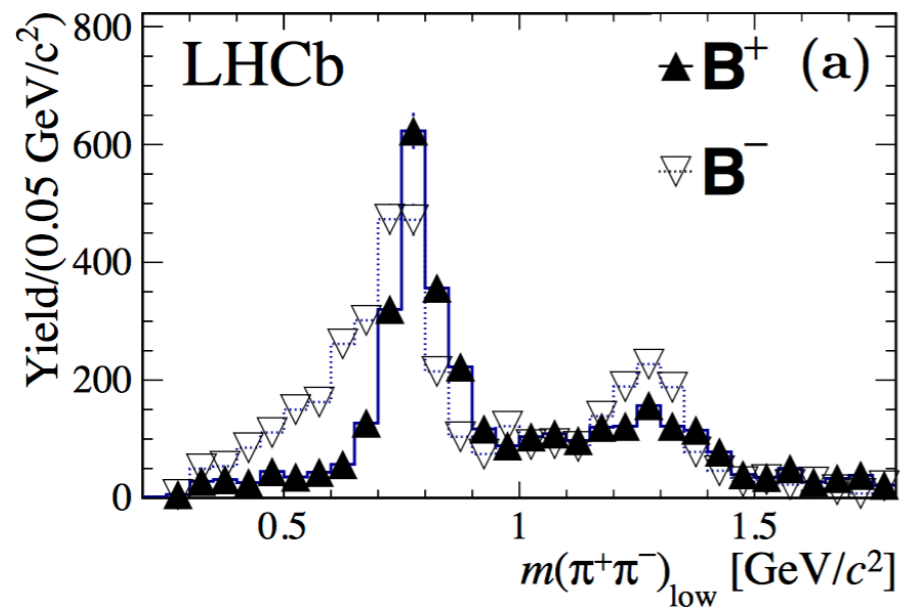
➤ 180° phase changing for Breit-Wigner \rightarrow CPV sign flip

➤ CPV sign flip when different wave (S-P, S-D, P-D etc) components interference

An Example: P-S interference

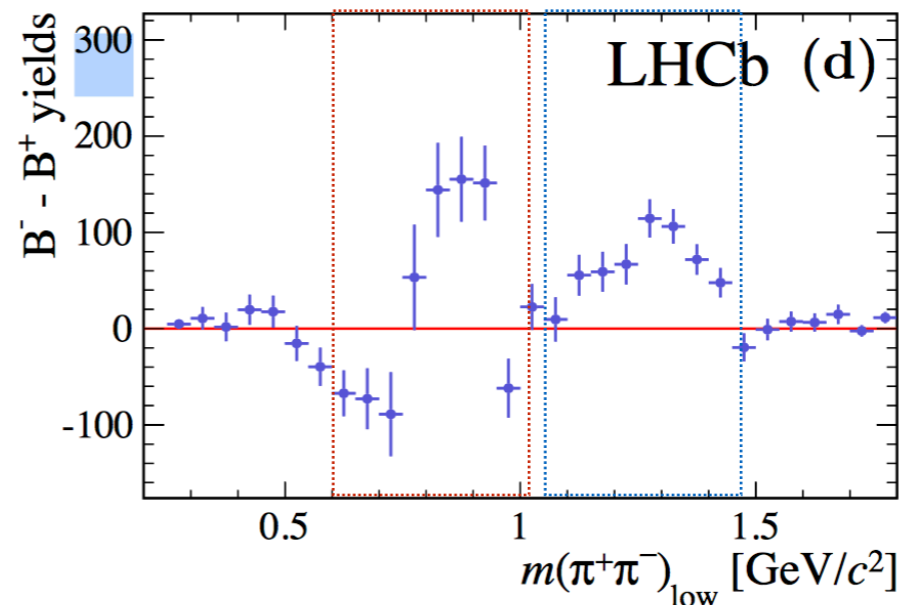
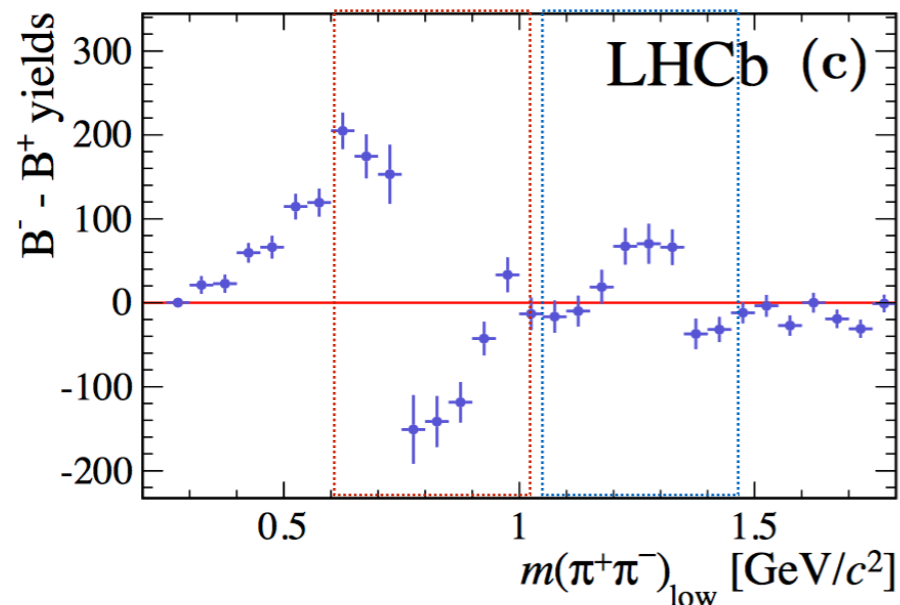
$$A_{CP} = \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} = \frac{2a_1 a_2 h_1(\theta) h_2(\theta) \sin(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)}{a_1^2 h_1^2(\theta) + a_2^2 h_2^2(\theta) + 2a_1 a_2 h_1(\theta) h_2(\theta) \cos(\delta_1 - \delta_2) \cos(\phi_1 - \phi_2)}$$

PRD 90, 112004 (2014)



RBW phase shift

RBW phase shift



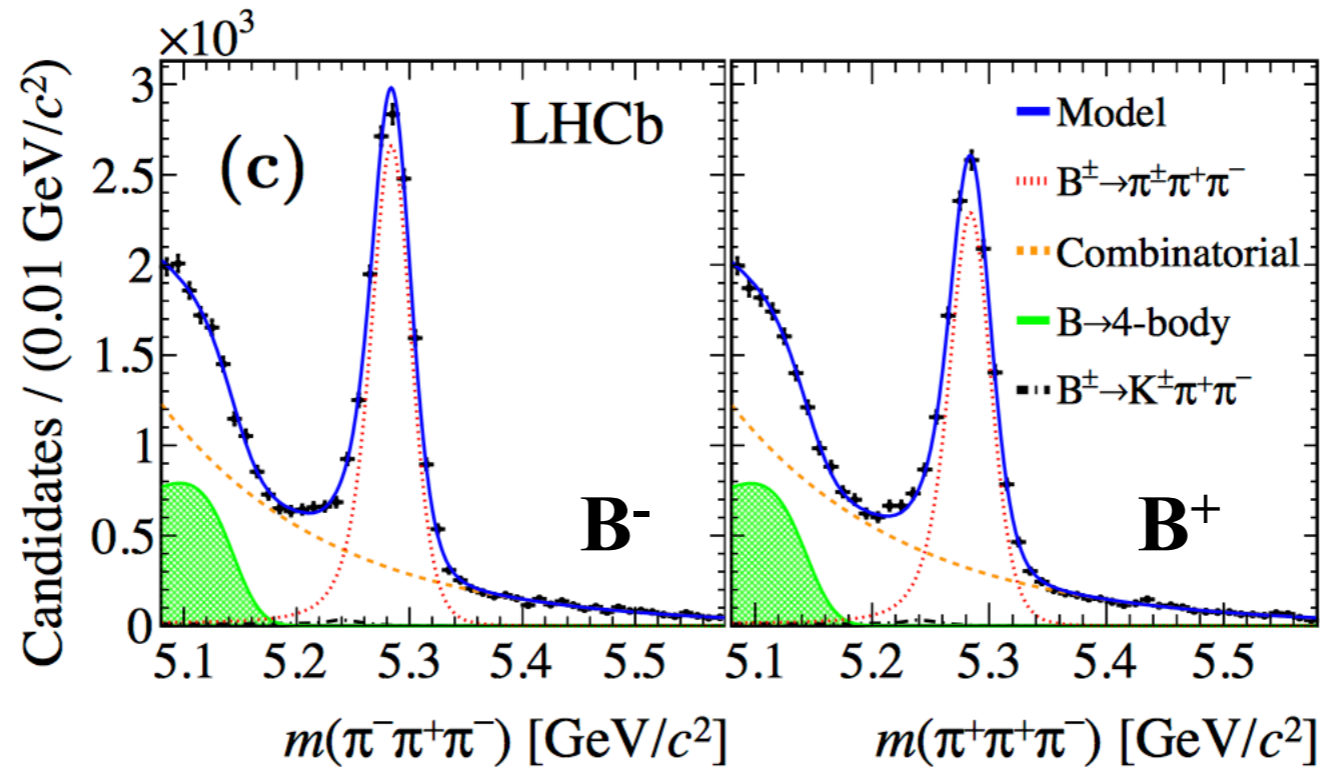
Large CP in $f_2(1270)$, but dividing w.r.t $\cos\theta = 0$ may not be ideal as shown in previous slide

$\text{Cos}\theta < 0$

$\text{Cos}\theta > 0$

θ : helicity angle

Amplitude analysis of $B \rightarrow \pi\pi\pi$ from LHCb



Plots from PRD 90, 112004 (2014) for instruction

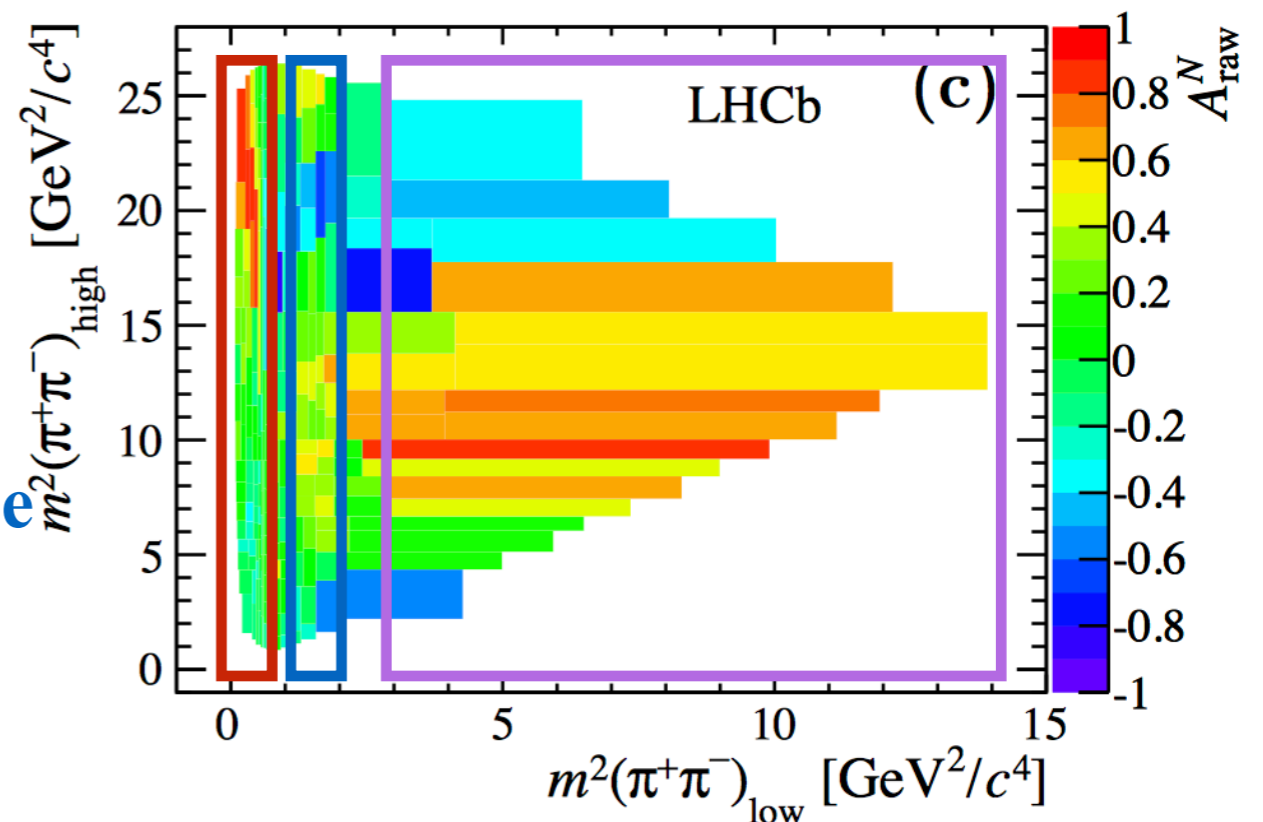
➤ RUN 1 LHCb data: ~21K signals with 4.4K background vs Babar: 1219 signals with 2.3K background

➤ Resonant contributions:

ρ - ω , $f_0(500)$, $f_0(980)$ region: S-P wave interference

$f_2(1270)$ region: D-S, P wave interference

High mass: KK - $\pi\pi$ rescattering



$\pi\pi$ S-wave description

- General agreed descriptions (RBW, GS) for $\pi\pi$ P- and D-waves;
- More complicated $\pi\pi$ S-wave, modeled in three different approaches:

- Isobar model: different S-wave contributions are explicitly modeled:

$f_0(500)$: RBW, **complex pole parameterization**

$f_0(980)$: Flatte parametrization

non-resonant: flat, **Belle model**, **re-scattering model** etc

$$T_{\sigma}(m_{13}) = \frac{1}{m_{\sigma}^2 - m_{13}^2},$$

PRD 71 (2005) 054030

$$T_{nr}(m_{13}, m_{23}) = c_{nr} (e^{-\alpha_{nr} m_{13}^2} e^{i\delta_1^{nr}} + e^{-\alpha_{nr} m_{23}^2} e^{i\delta_2^{nr}}),$$

PRL 96 (2006) 251803

$$T_{nr}(m_{13}) = \frac{a^{nr}}{1 + \frac{m_{13}^2}{\Lambda^2}} e^{i\delta^{nr}}$$

arXiv:hep-ph/1506.08332

- K-Matrix approach: 5 poles and 5 decay channels; parameters from global fit to previous data while production vector parameters from fit to data

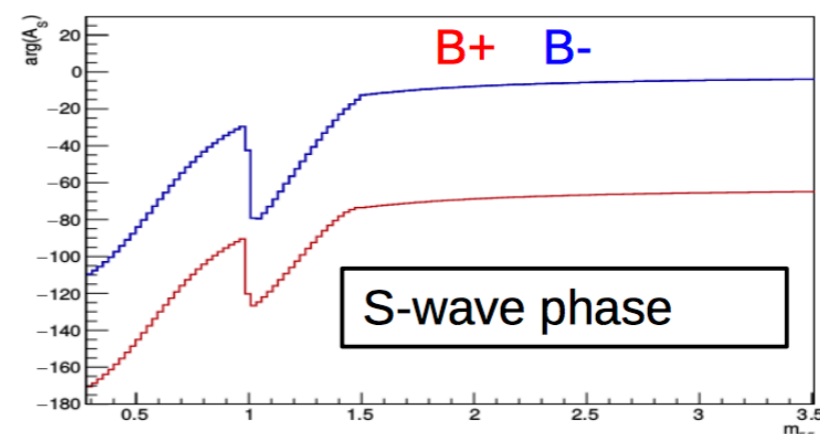
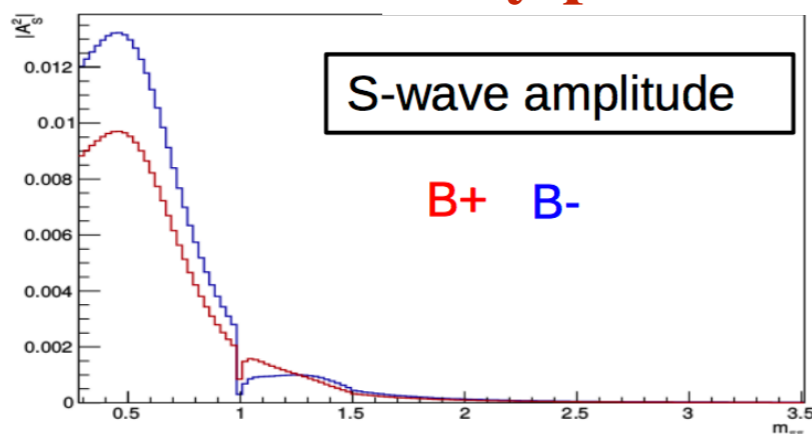
EPJA 16 (2003) 229

- Model independent approach (QMI): $\pi\pi$ S-wave binned into 13 bins; amplitudes in each bin obtained from fit to data (26 free parameters)

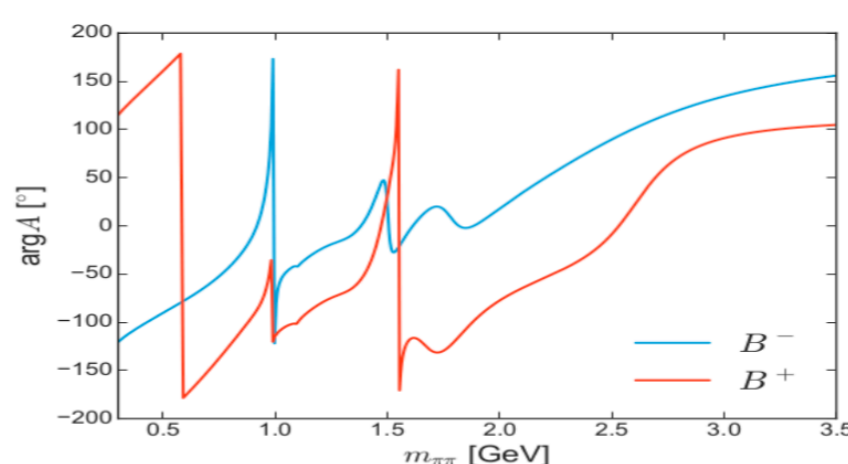
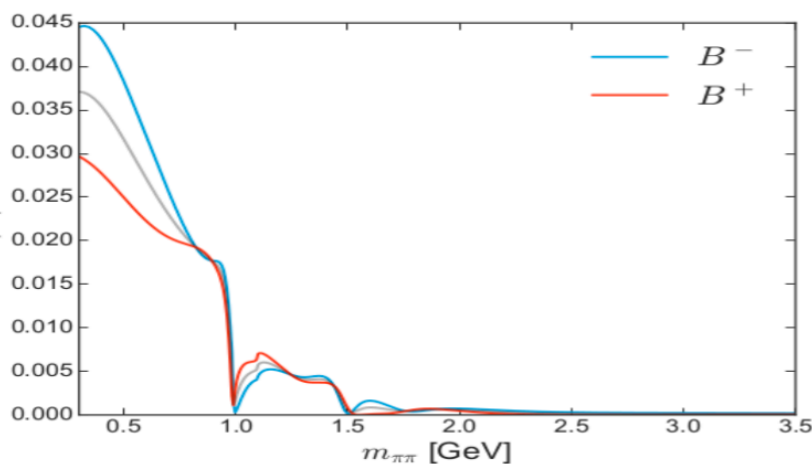
$\pi\pi$ S-wave from data

Very preliminary, un-official results

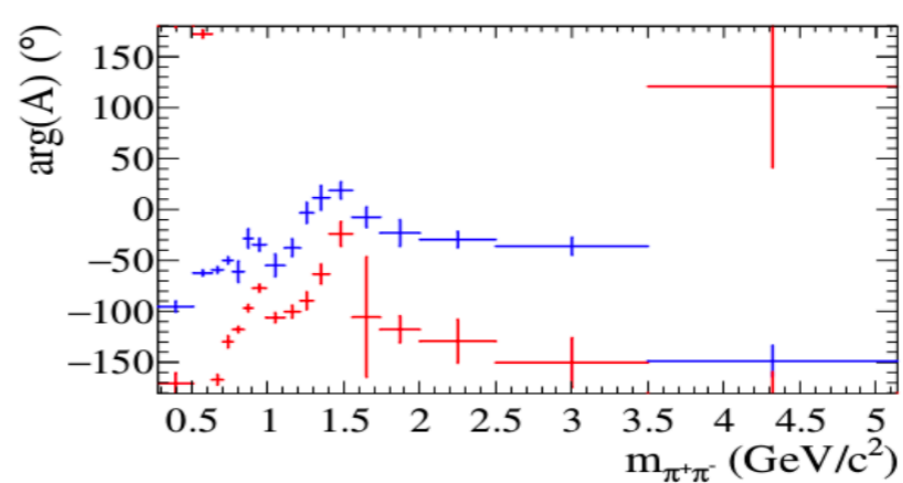
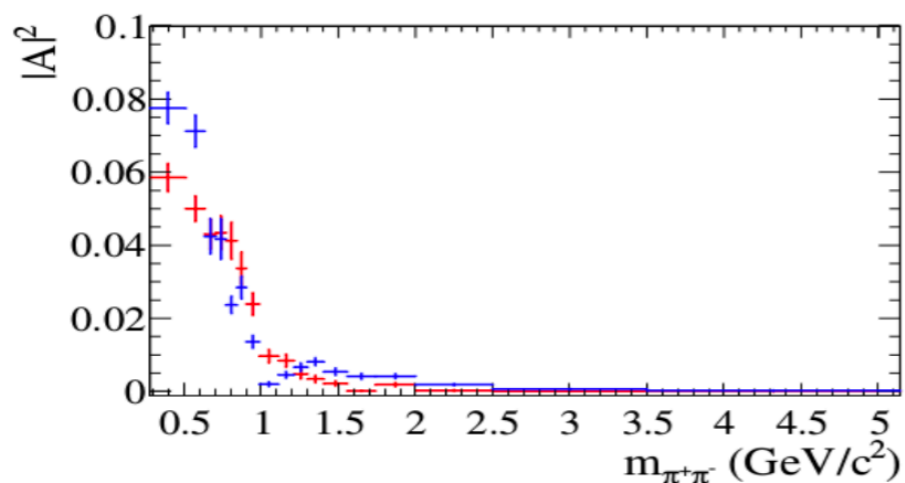
Isobar



K-Matrix



QMI



Similar pictures between different models over broad range

CPV modeling and results

- Amplitude over Dalitz plot will be expressed as: c_i w.r.t. $\rho(770)$

$$A \equiv A(m_{\max}^2, m_{\min}^2) = \sum_j c_j F_j(m_{\max}^2, m_{\min}^2),$$

$$\bar{A} \equiv \bar{A}(m_{\max}^2, m_{\min}^2) = \sum_j \bar{c}_j \bar{F}_j(m_{\max}^2, m_{\min}^2).$$

With

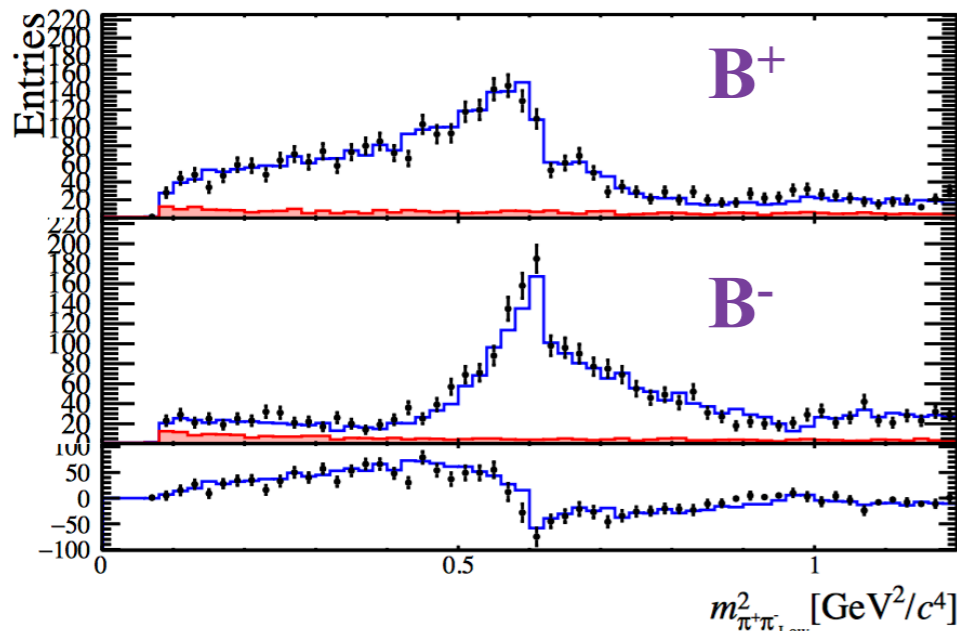
$$c_i = (x_i + \Delta x_i) + i(y_i + \Delta y_i)$$

$$\bar{c}_i = (x_i - \Delta x_i) + i(y_i - \Delta y_i)$$

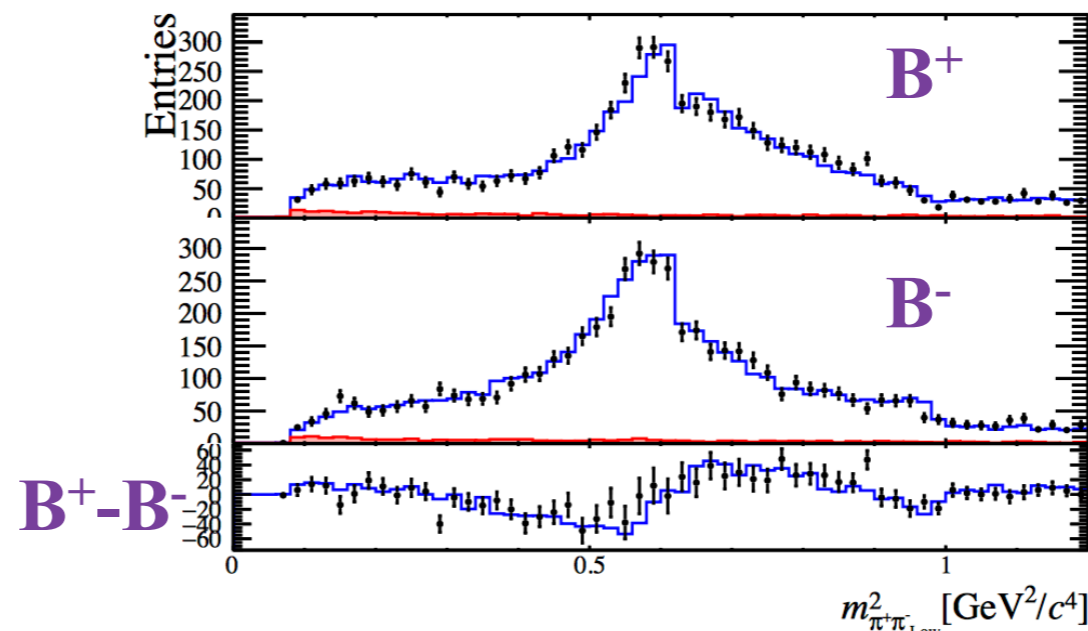
- Results on c_i , A_{CP} and fit fractions will be given

$$A_{CP} = -2 \left[\frac{x \delta_x + y \delta_y}{x^2 + \delta_x^2 + y^2 + \delta_y^2} \right],$$

- A fit example of ρ - ω region



$\text{Cos}\theta < 0$



$\text{Cos}\theta > 0$

Very preliminary,
un-official results

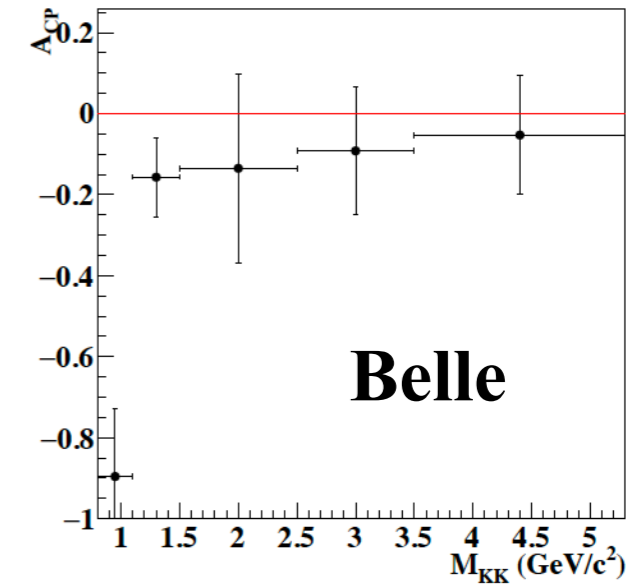
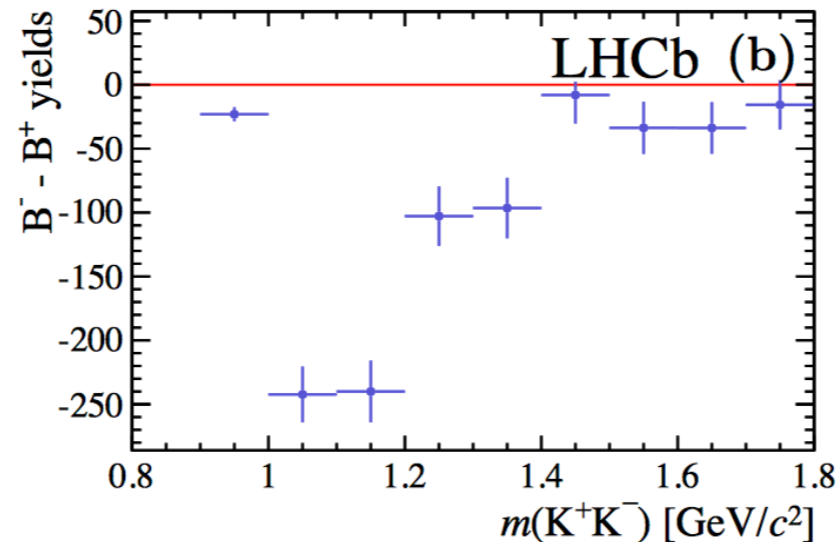
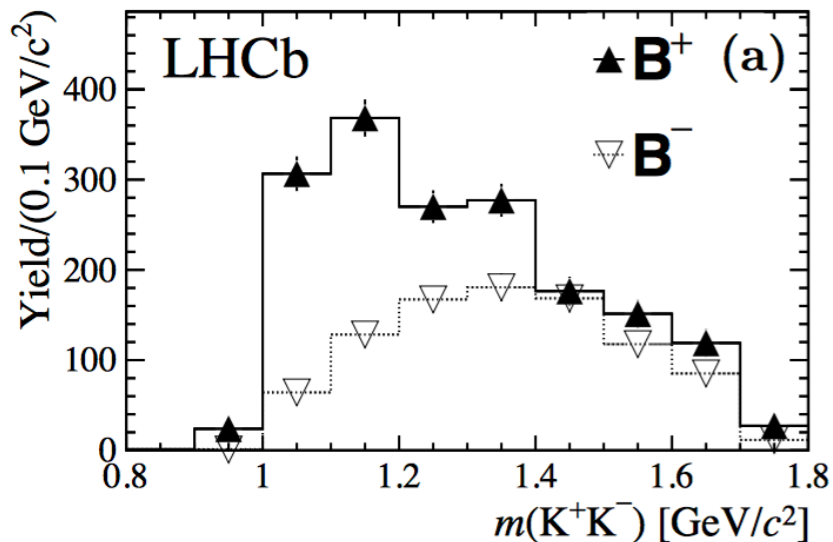
θ : helicity angle

Measurements with $B \rightarrow KK\pi$

➤ Previous LHCb A_{CP} measurement with 6k signals:

PRD 90, 112004 (2014)

arXiv:1705.02640



➤ Belle join the game recently with around 660 signal events: results consistent with LHCb

arXiv:1705.02640

➤ LHCb is also working on amplitude analysis; reasonable fit has already achieved

$K\pi$ resonances: $K^*(800)$, $K^*(892)$, $K_0^*(1430)$

KK resonances: $f_0(980)$, $f_0(1370)$, $f_2(1270)$, $\rho^0(1450)$, possible P-wave contribution

Alternative models also tried: like rescattering model for KK S-wave

PRD 92 (2015) 054010, PRD 71 (2005) 074016

Branching fraction updates for $B_{d(s)} \rightarrow K_s h h^{(\prime)}$

JHEP 10 (2013) 143

➤ Previous LHCb measurements with 1 fb^{-1} data observes $B_s \rightarrow K_s K \pi$, $K_s \pi \pi$ and confirms $B^0 \rightarrow K_s K \pi$

arXiv:1707.01665

➤ Updates performed with full Run 1 data, aiming at finding $B_s \rightarrow K_s K K$; though a bit unlucky, only 2.5σ significance

➤ Measurements normalized to $B^0 \rightarrow K_s \pi \pi$ channel

	stat.	sys.	normalization
$\mathcal{B}(B^0 \rightarrow \bar{K}^0 K^\pm \pi^\mp)$	6.1 ± 0.5	± 0.7	± 0.3
$\mathcal{B}(B^0 \rightarrow K^0 K^+ K^-)$	27.2 ± 0.9	± 1.6	± 1.1
$\mathcal{B}(B_s^0 \rightarrow K^0 \pi^+ \pi^-)$	9.5 ± 1.3	± 1.5	± 0.4
$\mathcal{B}(B_s^0 \rightarrow \bar{K}^0 K^\pm \pi^\mp)$	84.3 ± 3.5	± 7.4	± 3.4
$\mathcal{B}(B_s^0 \rightarrow K^0 K^+ K^-)$	$\in [0.4 - 2.5] \times 10^{-6}$ at 90% C.L.,		

Decay outside/inside VELO

2766±66 1411±45

261±24 160±17

1133±39 685±29

146±19 74±11

1100±41 568±28

12±6 7±4

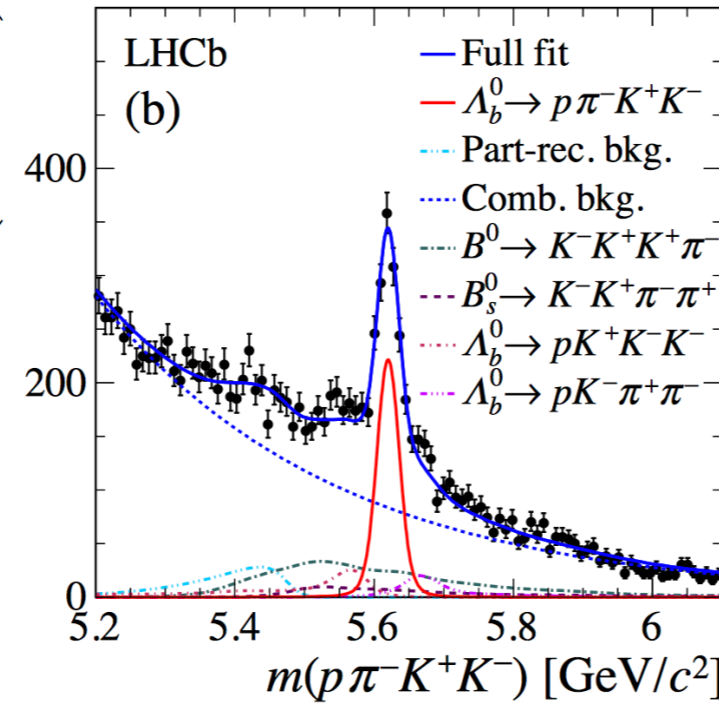
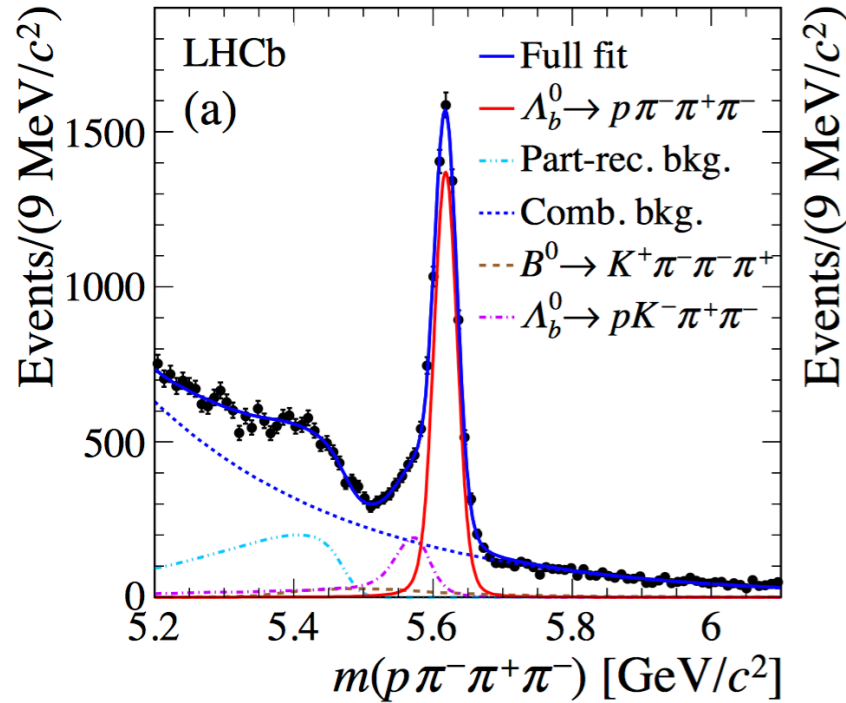
➤ Dalitz-plot analyses of $B^0 \rightarrow K_s \pi \pi$, $K_s K K$ and $B_s \rightarrow K_s K \pi$ underway

CPV in charmless baryon decays

- **Similar as B^+ mode, only direct CPV in baryon sector expected**
- **Two body charmless baryon decays have small Br; only one CPV measurement from CDF where no clear CPV found; Potential large CPV expected in $b \rightarrow su\bar{u}$ and $b \rightarrow du\bar{u}$**
[PRL113 \(2014\) 242001, PRD 91 \(2015\) 116007](#)
- **Several CPV measurements have been performed on three body charmless baryon decays by LHCb and no clear CPV found**
[JHEP 04 \(2014\) 087, JHEP 05 \(2016\) 08, PLB 759 \(2016\) 282](#)
- **CPV measurements in baryon sectors limited by statistics; Unlike meson decays, baryon decays tend to have larger Br for final states with more tracks (4 body > 3 body > 2 body); rich resonant interference and strong phase variation over phase space offer larger chance to have large CPV and interesting CPV pattern**
- **CPV measurement in four body baryon decays can be performed either similarly as those for $B \rightarrow hhh$ (ongoing) or using technics like triple product; ultimate procedure is full amplitude analysis**

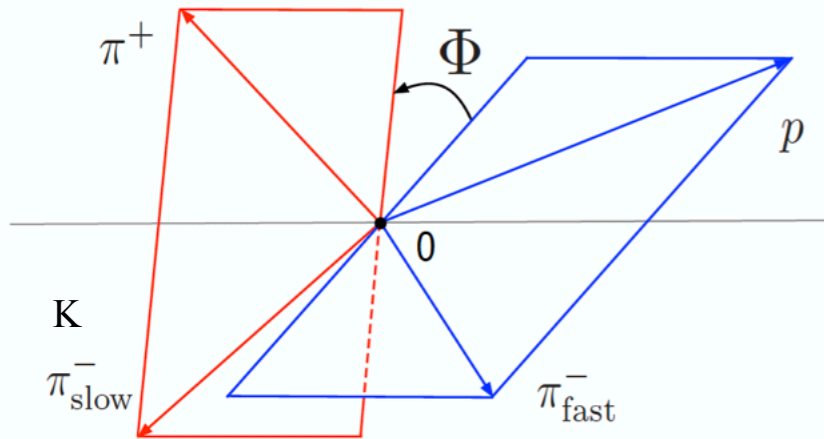
CPV in $\Lambda_b \rightarrow p\pi h h$ decays from LHCb

Nature Physics 13 (2017) 391



$p\pi\pi\pi$: 6.6k signals
 $pK\pi\pi$: 1k signals
vs
three body decays: less than 1k signals

➤ Phase space integrated CPV:



CP violation observable

$$a_{CP}^{\hat{T}\text{-odd}} = \frac{1}{2} (A_{\hat{T}} - \bar{A}_{\hat{T}})$$

P-violating observable

$$a_P^{\hat{T}\text{-odd}} = \frac{1}{2} (A_{\hat{T}} + \bar{A}_{\hat{T}})$$

$$A_{\hat{T}}(C_{\hat{T}}) = \frac{N(C_{\hat{T}} > 0) - N(C_{\hat{T}} < 0)}{N(C_{\hat{T}} > 0) + N(C_{\hat{T}} < 0)}, \text{ for } \Lambda_b^0$$

$$\bar{A}_{\hat{T}}(\bar{C}_{\hat{T}}) = \frac{\bar{N}(-\bar{C}_{\hat{T}} > 0) - \bar{N}(-\bar{C}_{\hat{T}} < 0)}{\bar{N}(-\bar{C}_{\hat{T}} > 0) + \bar{N}(-\bar{C}_{\hat{T}} < 0)}, \text{ for } \bar{\Lambda}_b^0$$

$$C_{\hat{T}} = \vec{p}_p \cdot (\vec{p}_{h_1^-} \times \vec{p}_{h_2^+}) \propto \sin \Phi, \text{ for } \Lambda_b^0$$

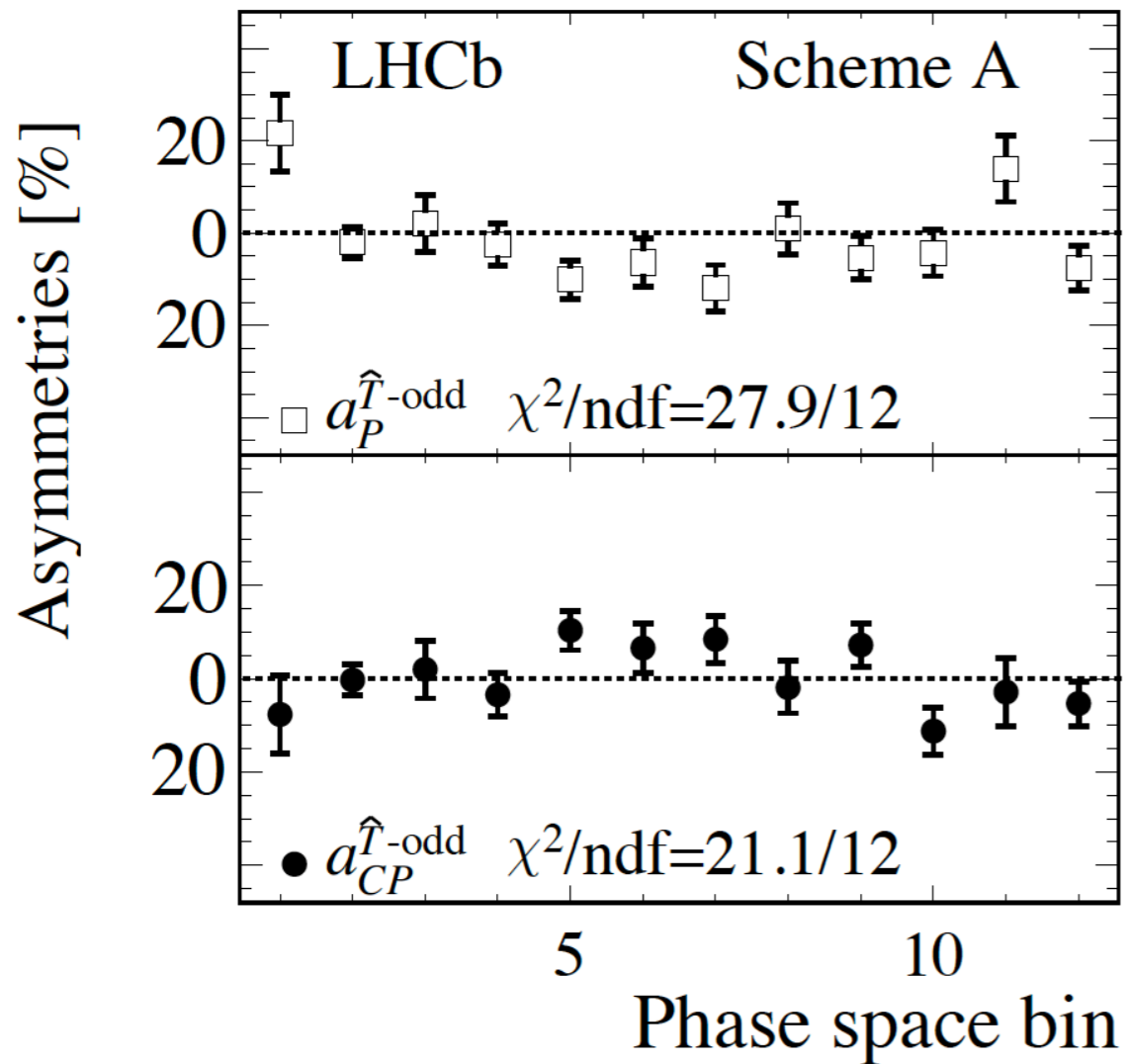
$$\bar{C}_{\hat{T}} = \vec{p}_{\bar{p}} \cdot (\vec{p}_{h_1^+} \times \vec{p}_{h_2^-}) \propto \sin \bar{\Phi}, \text{ for } \bar{\Lambda}_b^0$$

$$a_P^{\hat{T}\text{-odd}} = (-3.71 \pm 1.45 \pm 0.32)\%$$

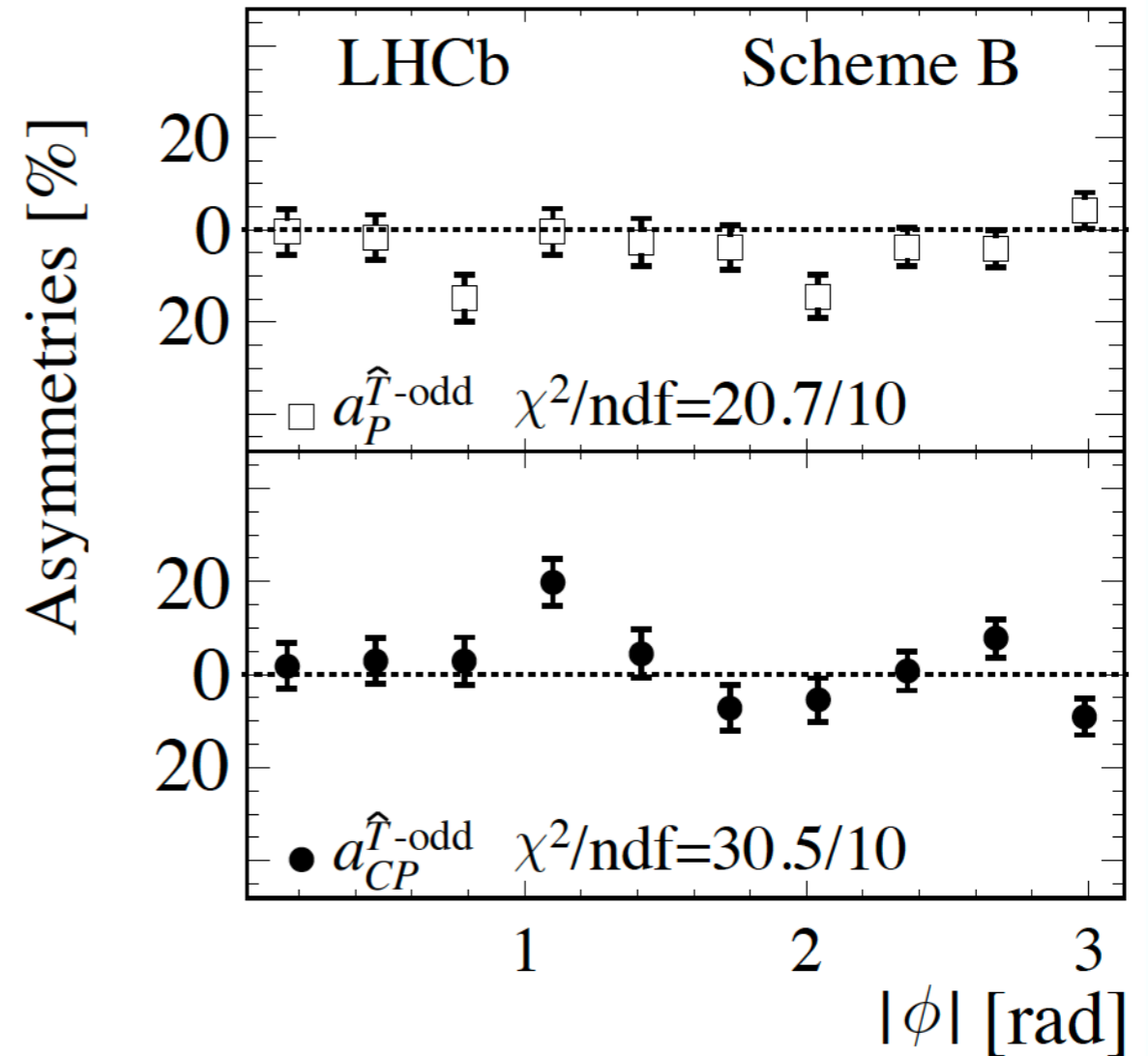
$$a_{CP}^{\hat{T}\text{-odd}} = (1.15 \pm 1.45 \pm 0.32)\%$$

CPV in different regions

Nature Physics 13 (2017) 391



Binning based on resonant structures, e.g. $\rho(770)$, N^* , Δ^{++}



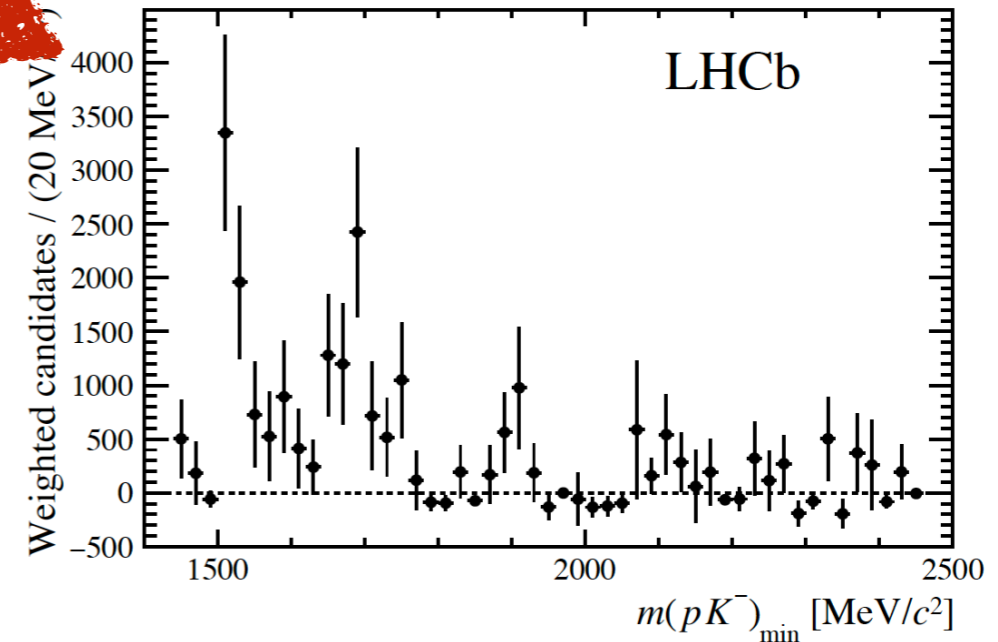
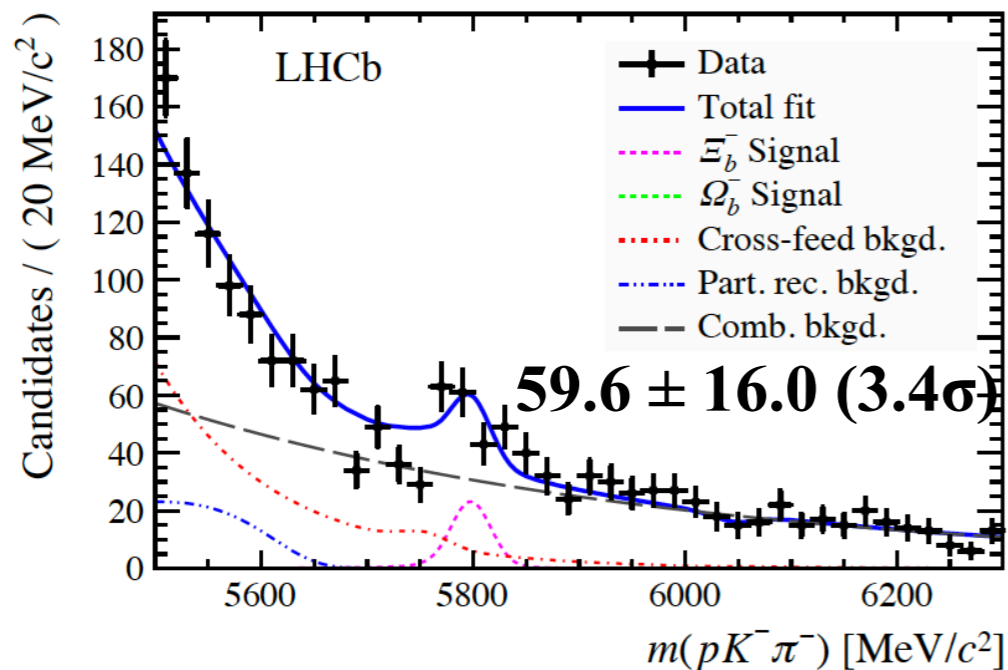
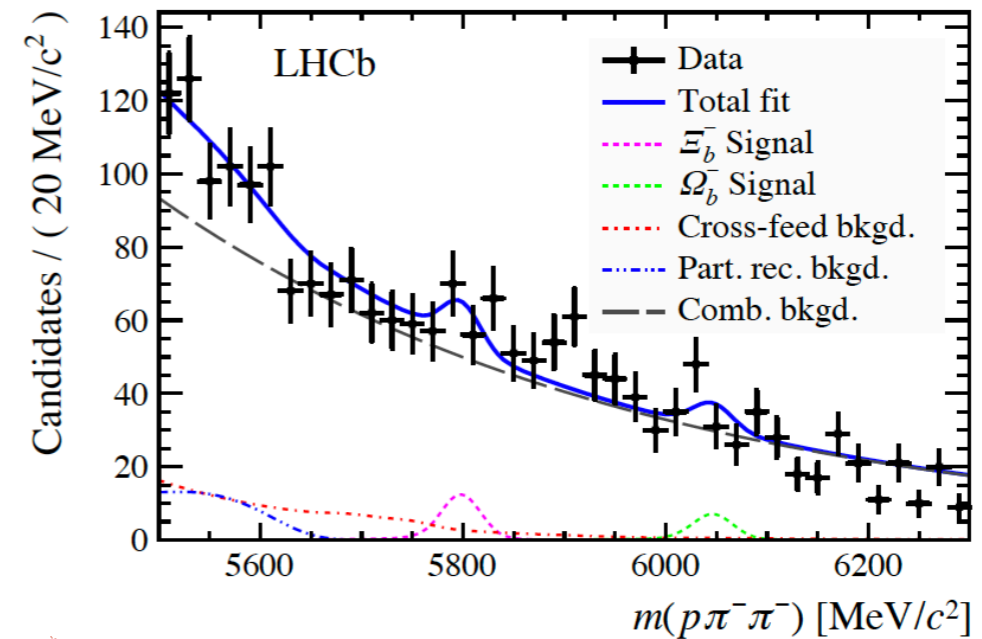
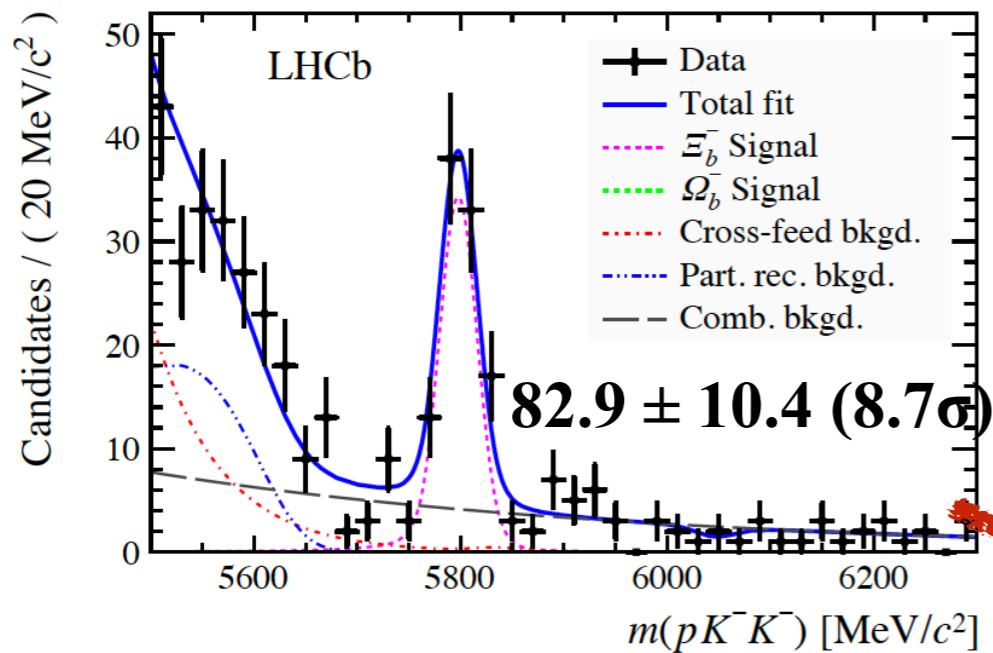
Binning based on ϕ angle

First evidence for CPV with 3.3σ

Search for $\Xi_b, \Omega_b \rightarrow phh^{(c)}$

➤ Decays interesting CPV measurement from P and T interference

PRL 118 (2017) 071801

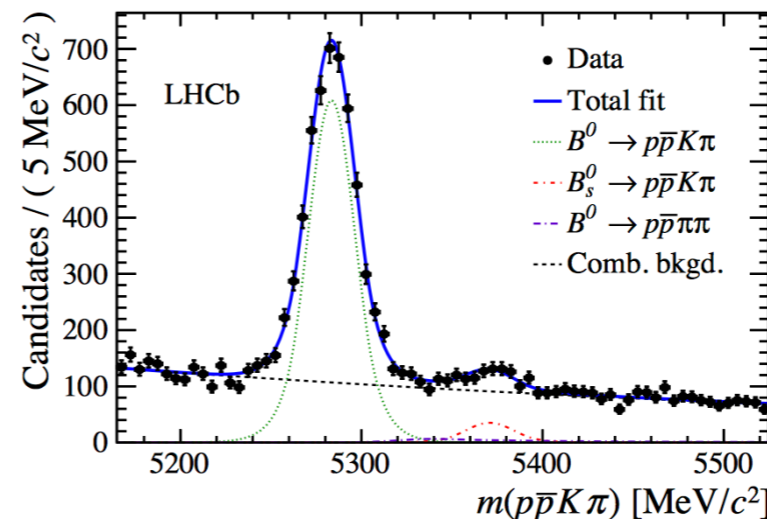
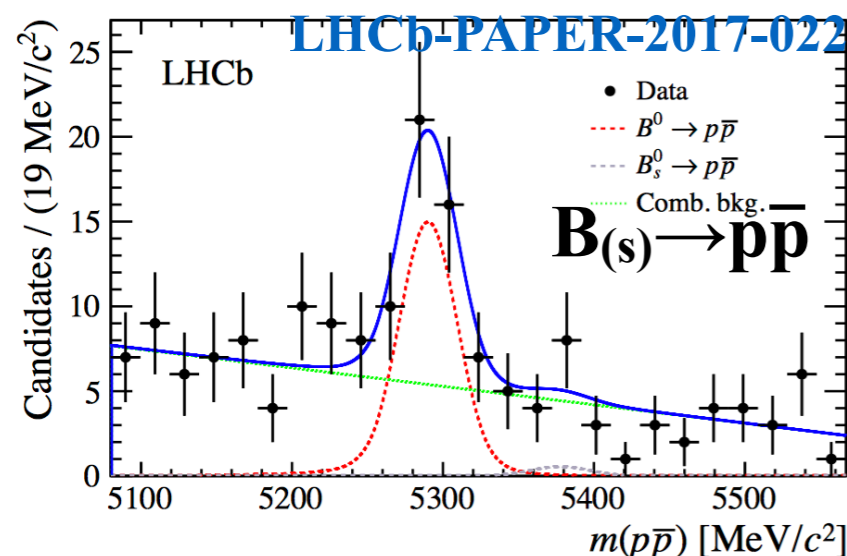
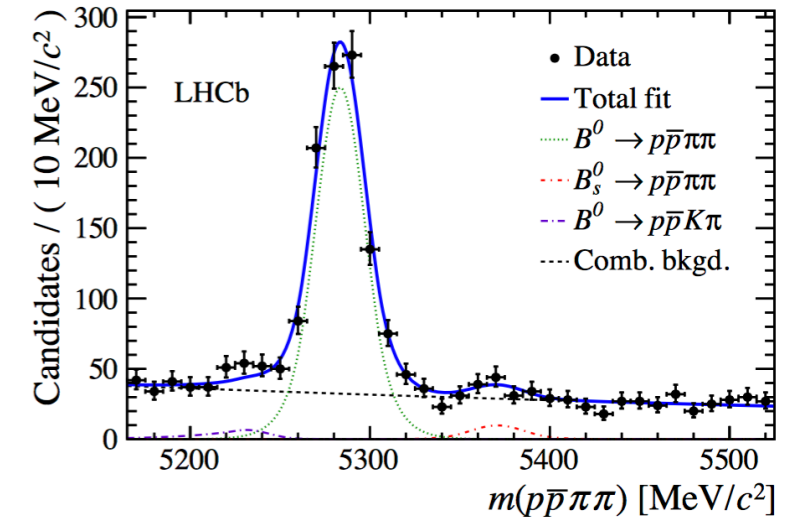
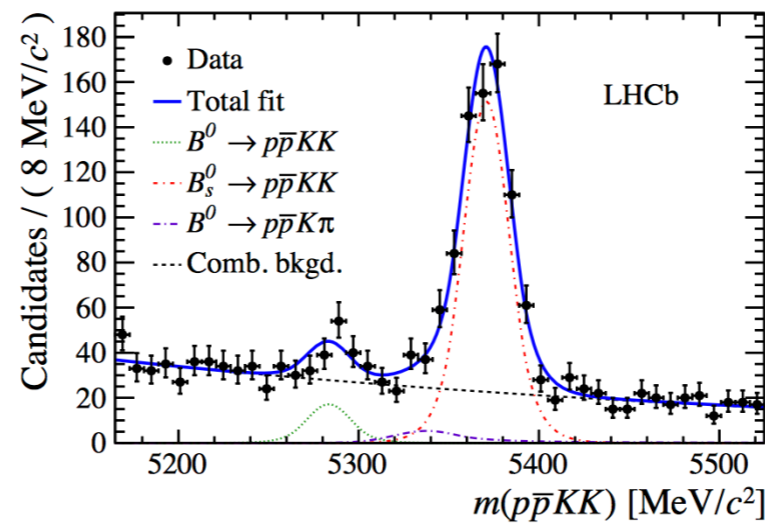
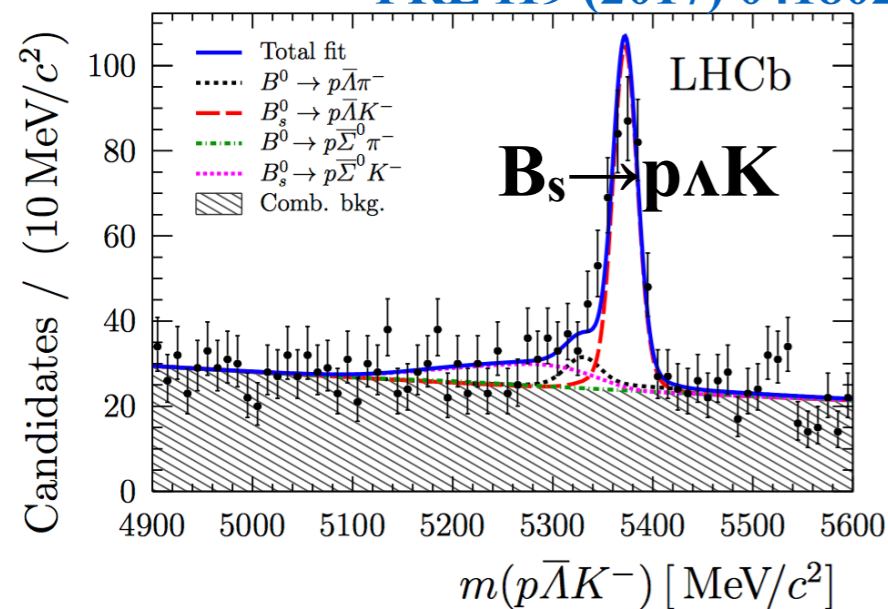


➤ Interesting resonant structures over $m(pK)$ and amplitude analysis with Run 2 data is planned

Baryonic B decays

PRL 88 (2002) 181803

- First baryonic B decay ($p\bar{p}K$) has been observed in 2002 by B factories
- First CPV evidence seen in 2013 by LHCb also in $p\bar{p}K$ decay [PRL 113 \(2014\) 141801](#)
- More interesting baryonic B decays found recently, potential place for CPV studies [PRL 119 \(2017\) 041802](#)



$B_{(s)} \rightarrow p\bar{p}hh^{(\prime)}$

[arXiv:1704.08497](#)

Conclusion

- **Many interesting CPV measurements/searches have been performed by LHCb (Run 1 data) and B factories**
- **Already put useful information in determining CKM angle precisely and in constraining new physics**
- **More new/interesting results are in the pipeline from LHCb (including Run 2 data) and from Belle (Belle II soon)**
- **Stay tuned!!!**

Many Thanks

Measurement on $B_s \rightarrow \phi\phi$

PRD 90 (2014) 052011

➤ $B_s \rightarrow \phi\phi$ decay dominated by $b \rightarrow s\bar{s}\bar{s}$ penguin contribution: no large direct CPV expected; weak phase from mixing and decay cancels → excellent place for new physics search

➤ Time dependent amplitude analysis performed with 3 fb⁻¹ LHCb data

➤ Using 4000 signal events, the CPV phase is measured to be

$$\phi_s = -0.17 \pm 0.15 \text{ (stat)} \pm 0.03 \text{ (syst) rad.}$$

➤ Triple-product asymmetries offered complementary information; the measurement is consistent with CP conservation

$$A_U \equiv \frac{\Gamma(U > 0) - \Gamma(U < 0)}{\Gamma(U > 0) + \Gamma(U < 0)} \quad U = \sin \phi \cos \phi \quad \sin \Phi = (\hat{n}_{V_1} \times \hat{n}_{V_2}) \cdot \hat{p}_{V_1}$$
$$A_V \equiv \frac{\Gamma(V > 0) - \Gamma(V < 0)}{\Gamma(V > 0) + \Gamma(V < 0)} \quad V = \sin(\pm\phi) \quad \begin{array}{l} + \text{ for } \cos \theta_1 \cos \theta_2 \geq 0 \\ - \text{ for } \cos \theta_1 \cos \theta_2 \leq 0 \end{array}$$

$$A_V = -0.017 \pm 0.017 \text{ (stat)} \pm 0.006 \text{ (syst)} \quad A_U = -0.003 \pm 0.017 \text{ (stat)} \pm 0.006 \text{ (syst)}$$

➤ Updates with RUN1 + 2015 + 2016 data ongoing and at least twice signal expected

Other recent studies in $B_s \rightarrow \phi X$ sector by LHCb

➤ Search on $B_s \rightarrow \phi \eta' (\pi\pi\gamma)$ performed with full Run 1 data:

JHEP 05 (2017) 158

$$\mathcal{B}(B_s^0 \rightarrow \eta' \phi) < 0.82 (1.01) \times 10^{-6} \quad \text{at } 90\% (95\%) \text{ CL}$$

➤ Observation of $B_s \rightarrow \phi \pi\pi$ and evidence for $B^0 \rightarrow \phi \pi\pi$ with Run 1 data

Time-independent amplitude analysis performed and resonance structures like $\rho(770)$, $f_0(980)$, $f_2(1270)$ and $f_0(1500)$ identified

➤ Studies also expands to higher KK mass and a time-independent amplitude analysis ongoing with Run 1 3 fb^{-1} data in LHCb

➤ New quasi-two body decays observed in higher mass region could be interesting for future CPV measurements

