#### Markov Chain Monte Carlo Oscillation Fits (with an emphasis on systematics)

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## Outline

- Basics of T2K and MCMC
- Lessons learned from fits
- The importance of fake data fits
- Near-term future work







#### Long Baseline Neutrino Oscillation





#### T2K Off-Axis Far Detector



#### Primary Interaction Material: Oxygen







$$\begin{split} & \mathsf{P}(\vec{z}|\text{data}) \propto \mathcal{P}(\text{data}|\vec{z}) \mathcal{P}(\vec{z}) \\ & -\ln(P) = c \\ & + \sum_{i}^{ND280bins} N_{i}^{p}(\vec{b},\vec{x},\vec{d}) - N_{i}^{d}\ln N_{i}^{p}(\vec{b},\vec{x},\vec{d}) \\ & + \sum_{i}^{N_{\mu}} N_{\mu,i}^{p}(\vec{\theta},\vec{b},\vec{x},\vec{s}) - N_{\mu,i}^{d}\ln N_{\mu,i}^{p}(\vec{\theta},\vec{b},\vec{x},\vec{s}) \\ & + \sum_{i}^{N_{e}} N_{\mu,i}^{p}(\vec{\theta},\vec{b},\vec{x},\vec{s}) - N_{\mu,i}^{d}\ln N_{\mu,i}^{p}(\vec{\theta},\vec{b},\vec{x},\vec{s}) \\ & + \sum_{i}^{N_{e}} N_{e,i}^{p}(\vec{\theta},\vec{b},\vec{x},\vec{s}) - N_{e,i}^{d}\ln N_{e,i}^{p}(\vec{\theta},\vec{b},\vec{x},\vec{s}) \\ & + \frac{1}{2}\Delta\vec{b}^{T}V_{b}^{-1}\Delta\vec{b} + \frac{1}{2}\Delta\vec{x}^{T}V_{x}^{-1}\Delta\vec{x} + \frac{1}{2}\Delta\vec{d}^{T}V_{d}^{-1}\Delta\vec{d} \\ & + \frac{1}{2}\Delta\vec{s}^{T}V_{s}^{-1}\Delta\vec{s} + \frac{1}{2}\Delta\vec{\theta}_{sr}^{T}V_{osr}^{-1}\Delta\vec{\theta}_{sr} \end{split}$$

What prior understanding did we put into our prediction? 8





#### Markov Chain Monte Carlo and GPUs

Don't step here-

A Markov Chain maps out the probability density of a likelihood function, P



Propose another point Calculate P<sub>proposed</sub>; if better, step to that point if not, step with probability P<sub>proposed</sub>/P<sub>current</sub>

 High dimensionality problem: 750 parameters

 Use Metropolis-Hastings algorithm with MCMC; doesn't require calculating likelihood derivatives



#### Estimating Parameters and Uncertainties



### Current Cross Section Model

- Try to use fundamental parameters of the models
- Simulation is NEUT (numbers)
- Twenty-six parameters
  - Five for 1p1h
  - Three for 2p2h
  - Three for  $1\pi$  (CC and NC)
  - Six FSI
  - Nine for CC Coherent, CC DIS, NC



# Focus on 1p1h

- $M_A^{QE}$  is the only nucleon level parameter
- Assume a RFG nuclear model
  - Separate pF and Eb parameters for carbon and oxygen
- Apply fixed RPA correction
- Binned  $p_{\mu}$ -cos $\theta_{\mu}$  '1p1h' uncertainty coming from different models
- For 2017: include uncertainties for RPA



# Focus on 2p2h

- Use 'Nieves' 2p2h model
- Normalization parameter for carbon and oxygen separately
- $\odot$  Relative uncertainty for  $\overline{\nu}$  vs  $\nu$
- For 2017:
  - Add 'shape' parameter to allow slosh between π-less-Δ-like and non-π-less-Δ-like







- Three samples allow sensitivity to different beam energies and cross section interaction modes
- High statistics in neutrino mode provide strong constraints
- CC0π and CC Other samples are underestimated by model; CC1π<sup>+</sup> is overestimated





#### Beam





#### v<sub>µ</sub> CC-NTrack (wrong sign)



### ND280 V-mode Samples

#### Stacked histograms are MC before data fit



 Samples are still statistically small compared to vmode



#### Near Detector Results 2016

- Flux parameters are generally increased
- Some cross section parameters—especially the carbon multinucleon parameter—are changed significantly from prior values





- Clear that data is in better agreement after the analysis
- Multinucleon component of distribution is noticeably increased





 CC Res 1π component is reduced in both absolute and relative terms as part of the CC1π sample



#### Near Detector Results







# Two Models?

- Big question: why not include alternate nuclear models?
- We tried this,
  several analyses
  ago!
- Gave up on this because what does
   0.25 spectral functions mean?





# Marginalization

- There are (at least) two ways to eliminate systematic parameters from your analysis: marginalization and profiling
- On T2K, we have found that cross section parameters, because they can be significantly non-gaussian, are a notable source of difference between the methods







# Fake Data Sets

- Take set of model changes
- Make fake data without statistical error for both ND and SK
- Fit with the 'default' model
- Adjust model, if necessary



# Model Choices



# Figure of Merit

Bias 
$$1 = \frac{fit_{\text{Fake data}} - fit_{\text{Asimov}}}{\sigma_{\text{Asimov 1}}}$$
With current  
T2K statisticsBias  $2 = \frac{fit_{\text{Fake data}} - fit_{\text{Asimov}}}{\sigma_{\text{Asimov 2}}}$ With full T2K  
statistics

Choose several sets of oscillation parameters, including non-maximal  $\theta_{23}$  and  $\delta_{CP} = 0, -\pi/2$ 



## Differences in 1p1h model





## Flux generally pushed down; no large changes in cross section parameters





### Differences in 1p1h model



# Martini 2p2h





# Something wacky happens to flux; no huge changes in cross section parameters





## Martini 2p2h

 $\Delta\,\chi^2$ 





## Spectral Function





(d)  $sin^2(\theta_{23})$ 





(c)  $\delta_{cp}$ 



## A Note on NOvA





## **Conclusions and Pleas**

- Current data statistics seem to indicate that we can hide behind statistical errors for model differences at the moment, but that day ends soon!
- Fake data sets, though an imperfect tool, are extremely important for testing how sensitive oscillation analyses are to cross section models
- Plea: if you release a model, make sure it has the hadronic side!
- Plea: Models that come with reasonable sets of uncertainties are more likely to be used!
- Plea: Help us check our generators!

