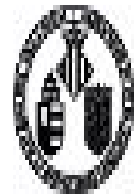


Electro- and neutrino- nucleus interactions at intermediate energies

J. Nieves

IFIC (CSIC & UV)



VNIVERSITAT
ID VALÈNCIA



Outline

1. Motivation: Neutrino oscillations, neutrino detectors, nuclear cross sections
2. Intermediate energies: QE and $\Delta(1232)$ peaks and the dip region
3. Many body approach
4. Neutrino-nucleus inclusive QE scattering: Multinucleon mechanisms, RPA correlations and MiniBooNE M_A puzzle
5. Neutrino energy reconstruction
6. Conclusions

Further details:

Reviews

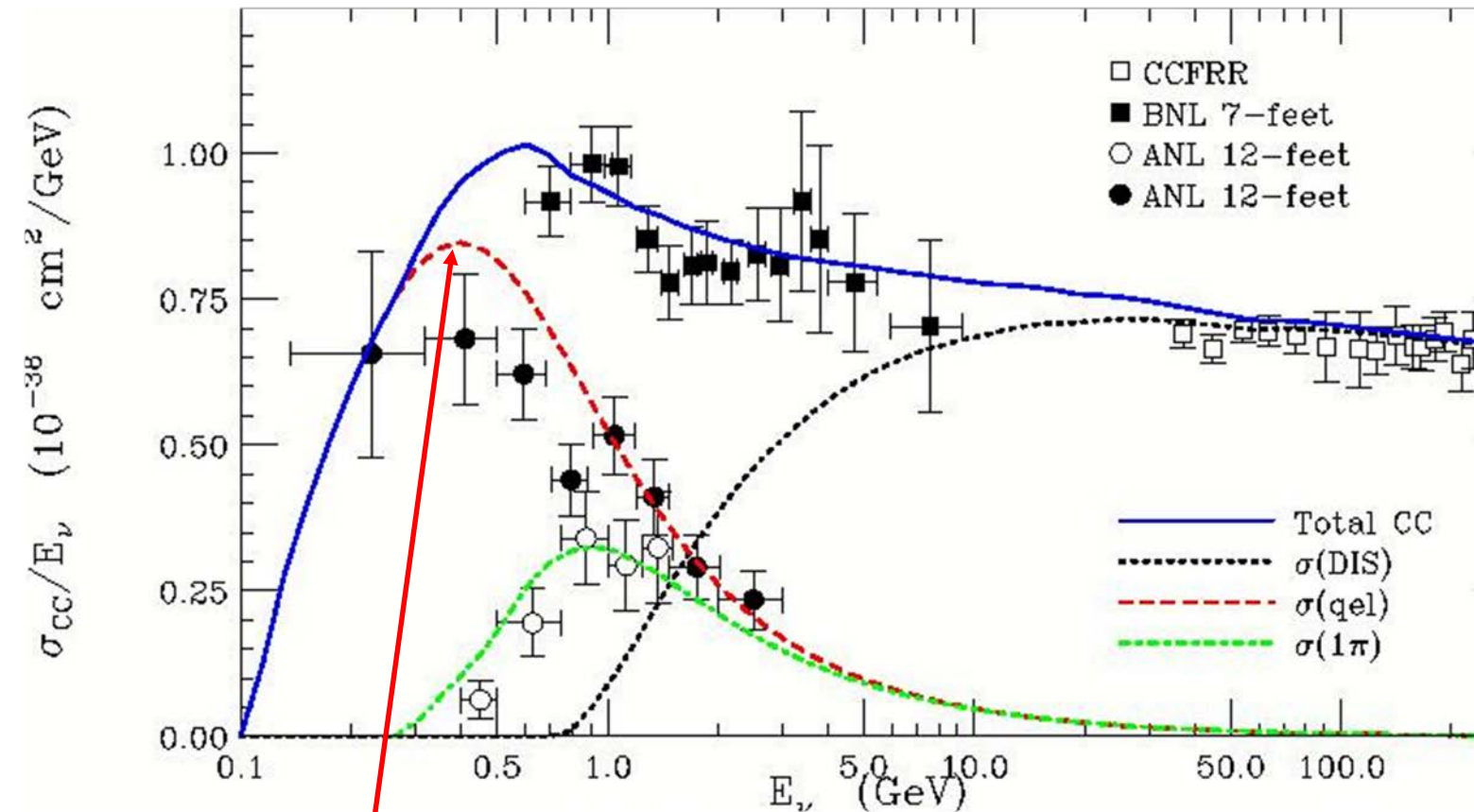
CCQE: latest work

- Alvarez-Ruso L., Hayato Y. and Nieves J., New J.Phys. 16 (2014) 075015
- Morfin J. G., Nieves J. and Sobczyk J.T., Adv.High Energy Phys. 2012 (2012) 934597
- Nieves J., Sobczyk J.E.: *In medium dispersion relation effects in nuclear inclusive reactions at intermediate and low energies.: arXiv: 1701.03628*
- arXiv:1307.8105: PRD 88 (2013) 113007 ($\nu, \bar{\nu}$ CCQE-like up to 10 GeV)
- arXiv:1106.5374: PLB 707 (2012) 72 (ν CCQE-like) & arXiv:1302.0703: PLB 721 (2013) 90 ($\bar{\nu}$ CCQE-like)
- arXiv:1204.5404: PRD 85 (2012) 113008 (E_ν reconstruct.) CCQE & NCQE
- arXiv:1102.2777: PRC 83 (2011) 045501 (CCQE, 2p2h, ...)
- nucl-th/0408005: PRC 70 (2004) 055503 (CCQE) & hep-ph/0604042: PLB 638 (2006) 325 (Errors in CCQE) & hep-ph/0511204 : PRC 73 (2006) 025504 (NCQE & MC)
- arXiv:1612.02343: PRD 95 (2017) 053007 & arXiv: 1510.06266: PRD 93 (2016) 014016 & arXiv: 1001.4416: PRD 81 (2016) 085046 & hep-ph/0701149: PRD 76 (2007) 033005 ($\nu_l N \rightarrow l N' \pi$)
- arXiv: 1304.1320: PRD 87 (2013) 113009 ($\nu_l A \rightarrow l \pi X$) π production
- arXiv: 1007.3685: PRD 82 (2010) 077303 & arXiv: 0903.5285: PRD 80 (2009) 013003 & arXiv: 0811.1421: PRD 79 (2009) 013002 (coherent π production in nuclei)
- nucl-th/9711009 : NPA 627 (1997) 543 (inclusive (e, e')) electron-nucleus
- nucl-th/9710070 : NPA 627 (1997) 599 (inclusive $(e, e'N), (e, e'NN), (e, e', \pi)....$

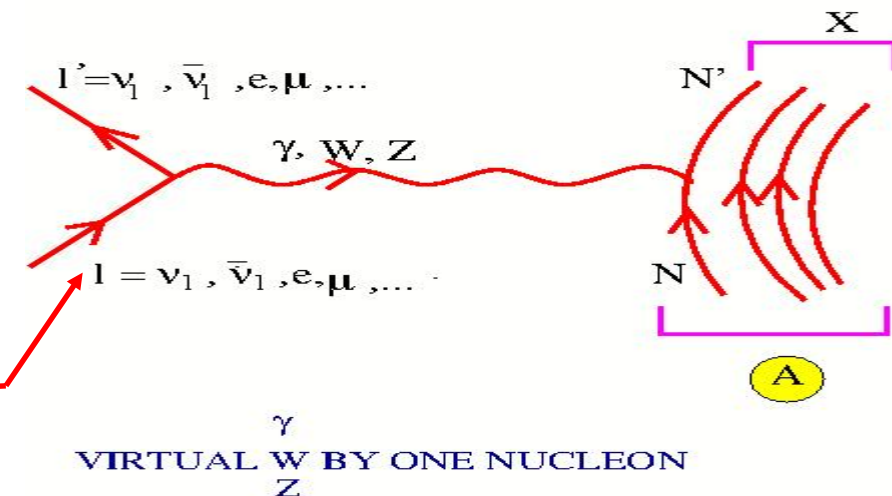
Motivation: Details on the axial structure of hadrons in the free space and inside of nuclei, and

Theoretical knowledge of QE and 1π cross sections is important to carry out a precise neutrino oscillation data analysis...

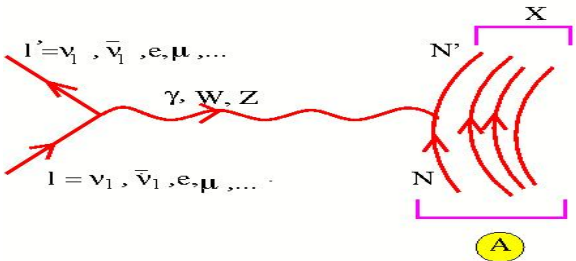
$^{12}\text{C} \rightarrow$ Liquid scintillators
 $^{16}\text{O} \rightarrow$ Cerenkov detectors
 $^{40}\text{Ar} \rightarrow$ TPC's (time projection chambers)



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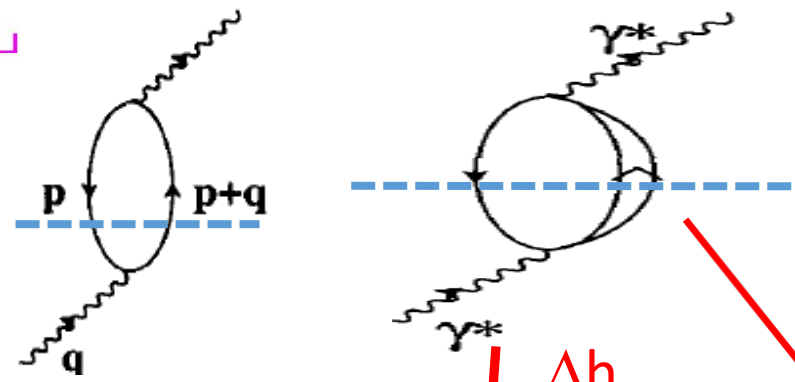


QUASIELASTIC PEAK



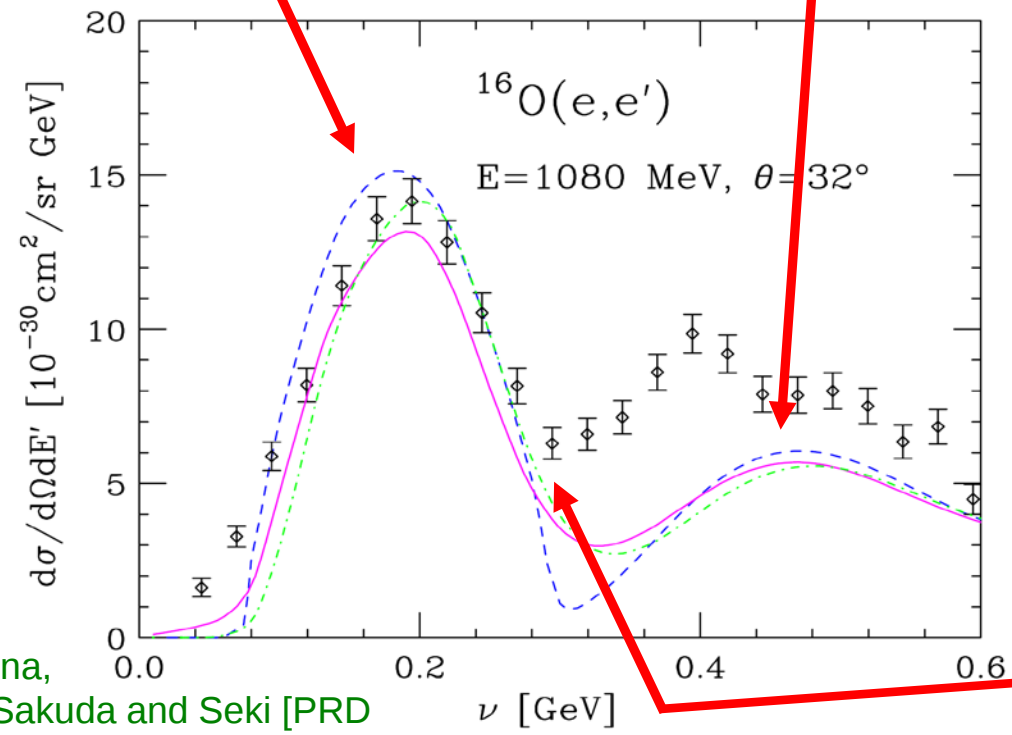
VIRTUAL γ BY ONE NUCLEON
Z

Intermediate energies: QE and $\Delta(1232)$ peaks and the dip region

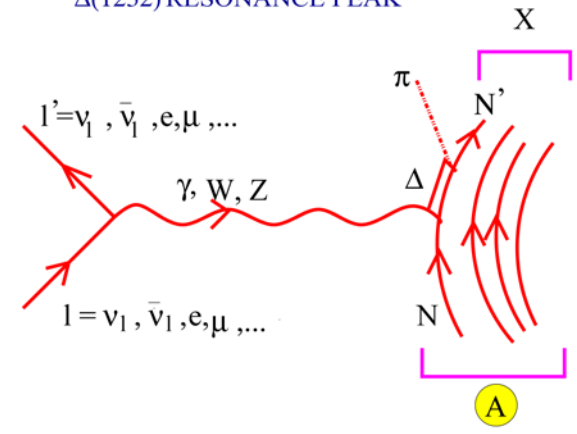


1p1h

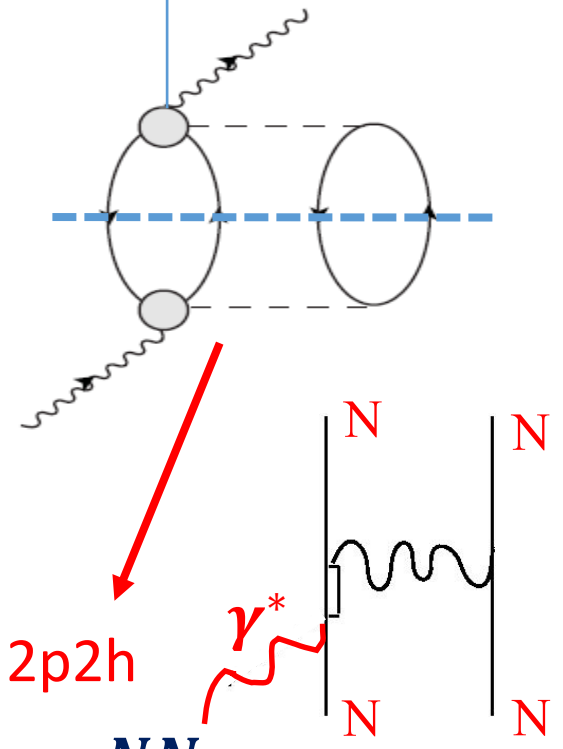
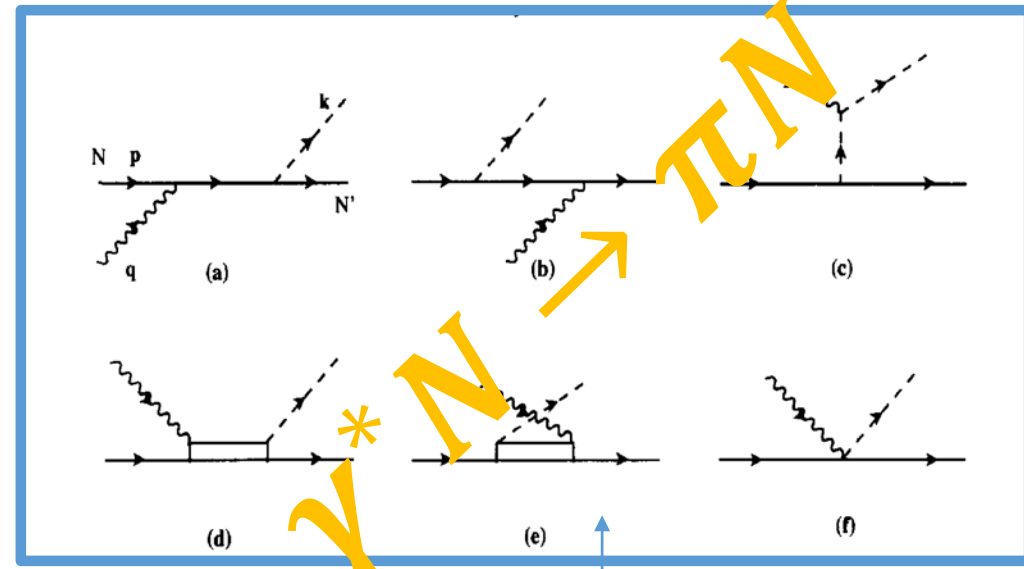
Δh



$\Delta(1232)$ RESONANCE PEAK



EXCITATION OF $\Delta(1232)$ DEGREES OF FREEDOM



Dip region 2p2h

$\gamma^* NN \rightarrow NN$

Benhar, Farina,
Nakamura, Sakuda and Seki [PRD
72 (2005) 053005]

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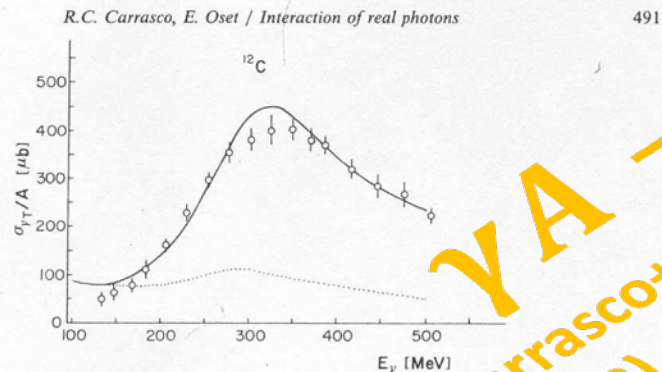


Fig. 45. Results for σ_A/A as a function of the photon energy for ^{12}C . Experiment from ref. ⁶⁾. The lower curve is the result for direct photon absorption.

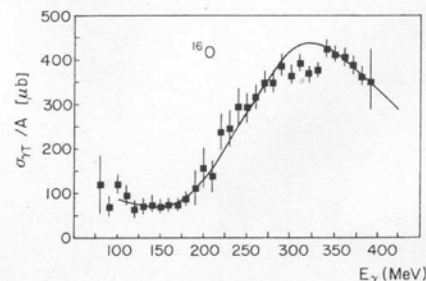


Fig. 46. Results for σ_A/A as a function of the photon energy for ^{16}O . Experiment from ref. ⁵⁾.

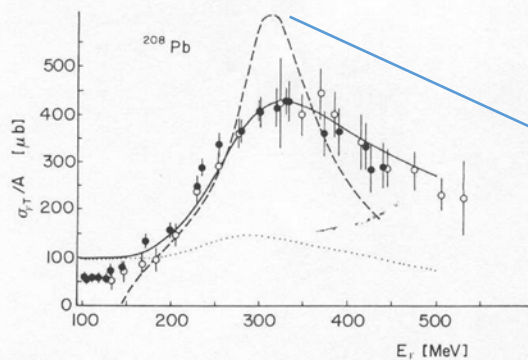
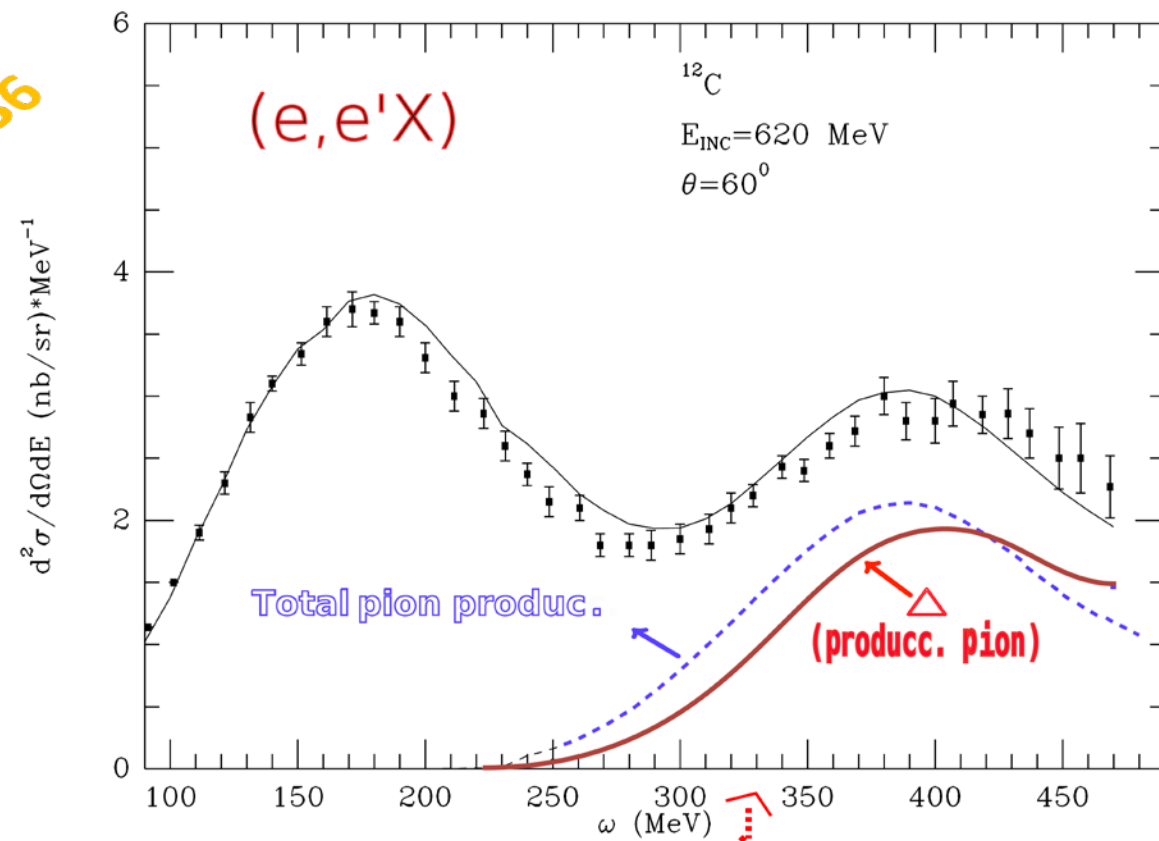


Fig. 47. Continuous line: results for σ_A/A as a function of the photon energy for ^{208}Pb . The dashed line shows the impulse approximation result $(Z\sigma_{\gamma p} + N\sigma_{\gamma n})/A$ for comparison. The dotted line is the result for direct photon absorption. Experimental data: dark dots from ref. ³⁾, while dots from ref. ⁶⁾.



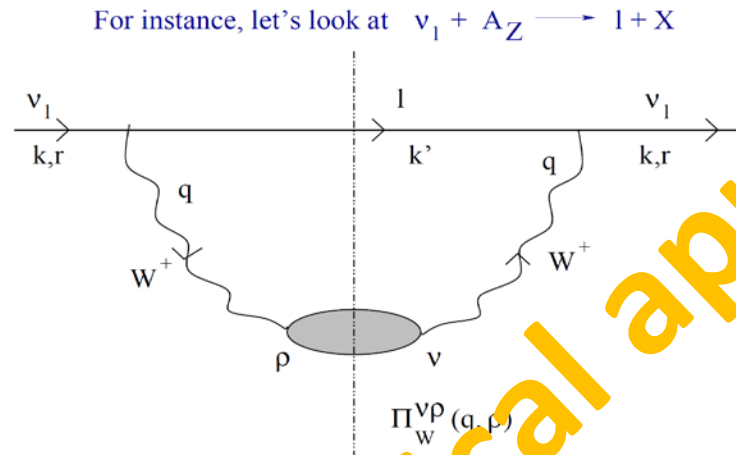
$$eA \rightarrow e'X$$

Gil+Nieves+Oset NPA 627 (1997) 543

Impulse approximation

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Many body approach



$$\frac{d^2\sigma}{d\Omega(k')dE'} = \frac{|\vec{k}'|}{|\vec{k}|} \frac{G^2}{4\pi^2} L_{\mu\sigma} W^{\mu\sigma}$$

$$L_{\mu\sigma} = k'_\mu k_\sigma + k'_\sigma k_\mu - g_{\mu\sigma} k \cdot k' + i\epsilon_{\mu\sigma\alpha\beta} k'^\alpha k^\beta$$

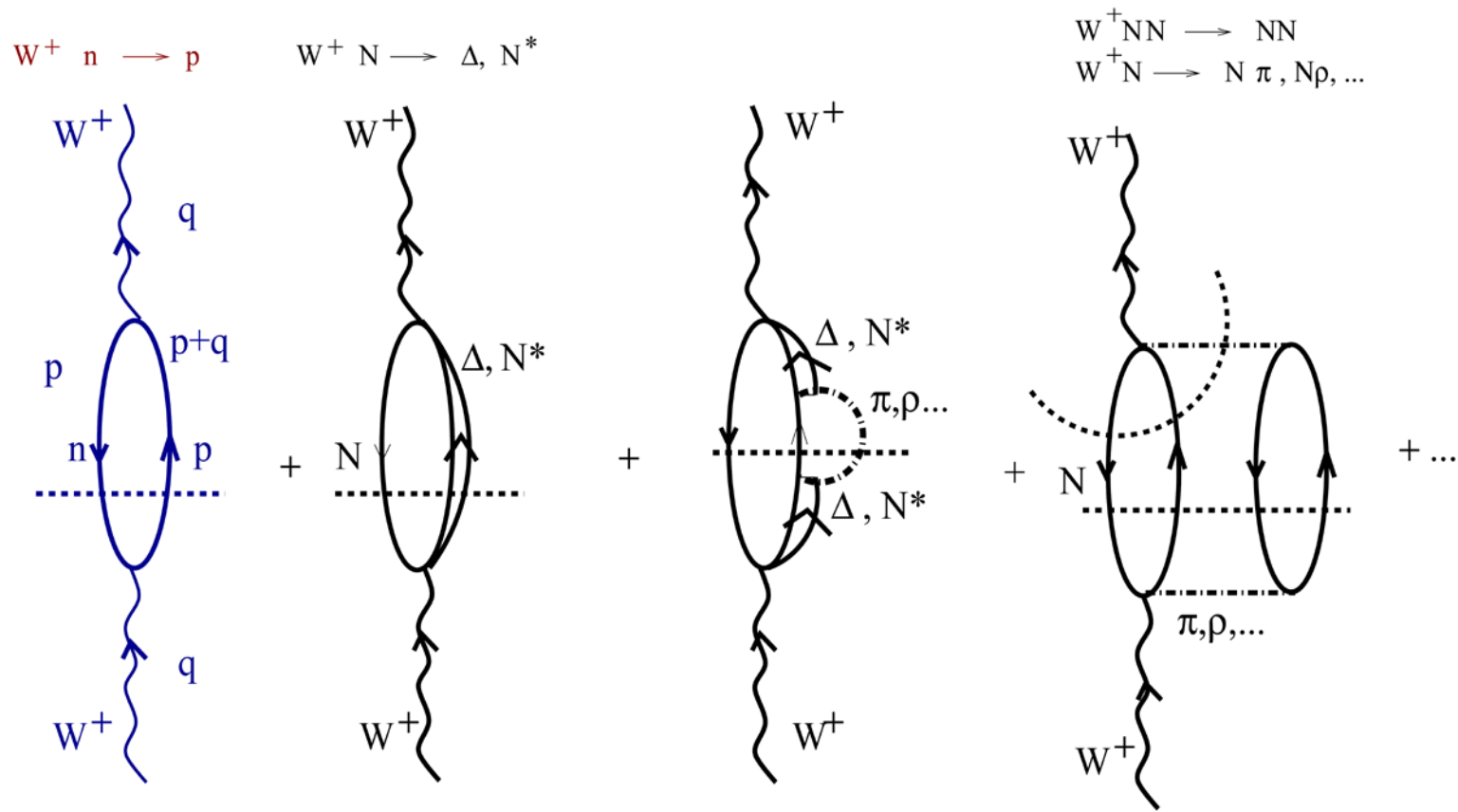
$$W^{\mu\sigma} = W_s^{\mu\sigma} + iW_a^{\mu\sigma}$$

$$W_s^{\mu\sigma} \propto \int \frac{d^3r}{2\pi} \text{Im} \left\{ \Pi_W^{\mu\sigma}(q, \rho) + \Pi_W^{\sigma\mu}(q, \rho) \right\} \Theta(q^0)$$

$$W_a^{\mu\sigma} \propto \int \frac{d^3r}{2\pi} \text{Re} \left\{ \Pi_W^{\mu\sigma}(q, \rho) - \Pi_W^{\sigma\mu}(q, \rho) \right\} \Theta(q^0)$$

Basic object $\Pi_{W,Z^0,\gamma}^{\nu\rho}(q, \rho) \equiv$ Selfenergy of the Gauge Boson ($W^\pm, Z^0, \gamma$)

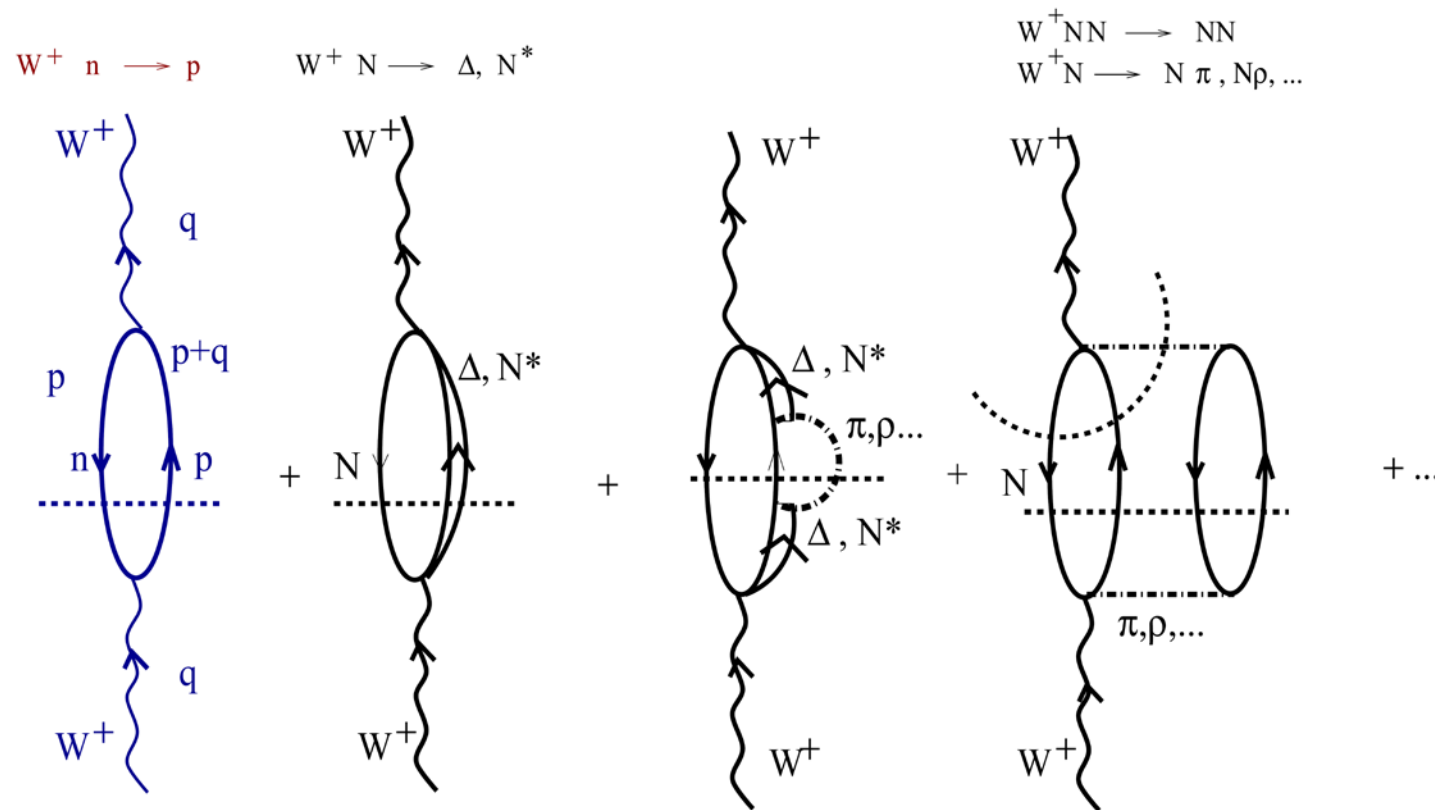
inside of the nuclear medium. Perform a Many Body expansion, where the relevant gauge boson absorption modes should be systematically incorporated: absorption by one N, or NN or even 3N, real and virtual (MEC) meson ($\pi, \rho, \dots$) production, Δ excitation, etc...



$\sum_{n < F} \left| \left[\text{Diagram} \right] \right|^2$

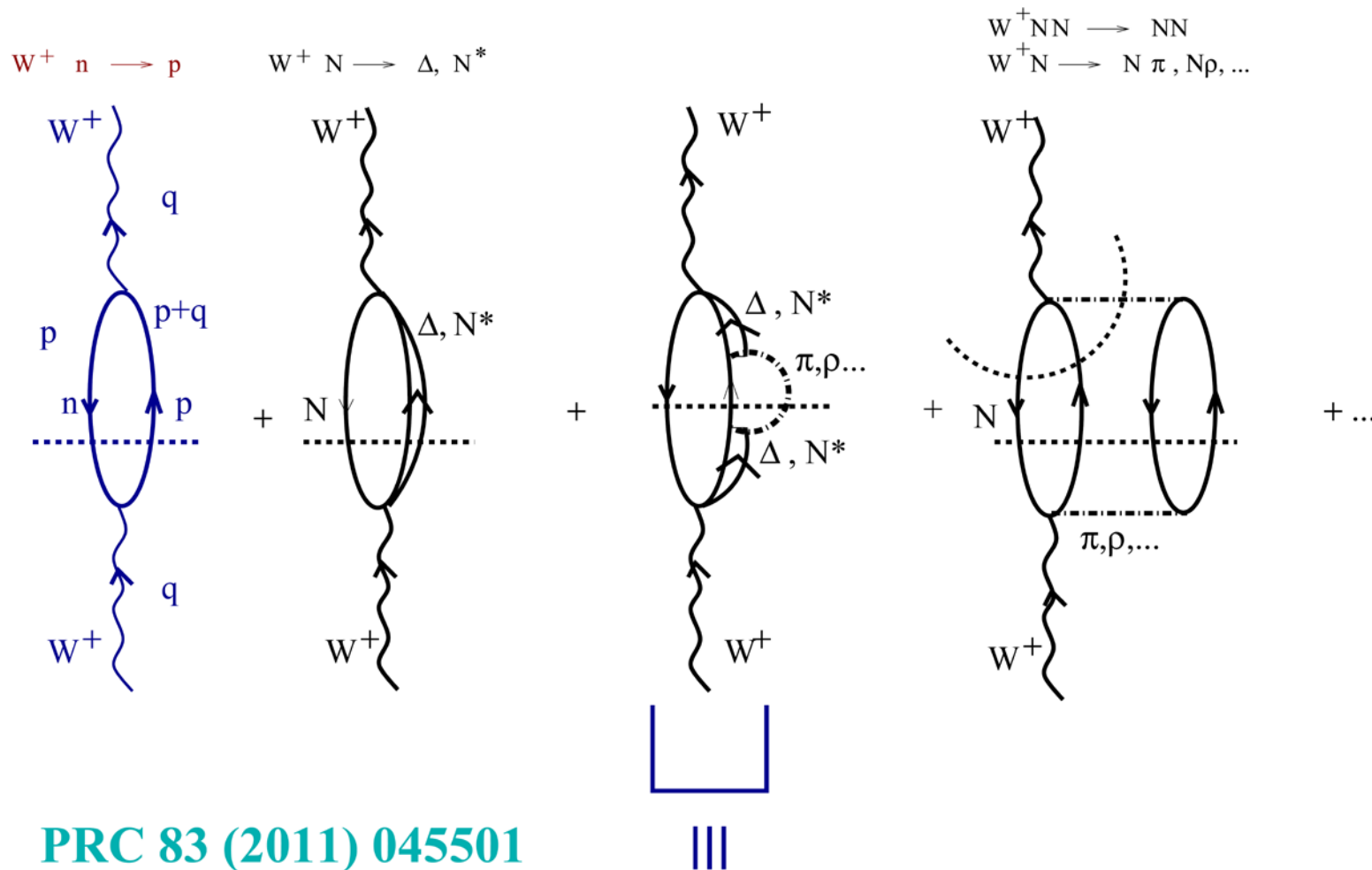
QE

PRC 70 (2004) 055503 (CC)
 PRC 73 (2006) 025504 (NC)

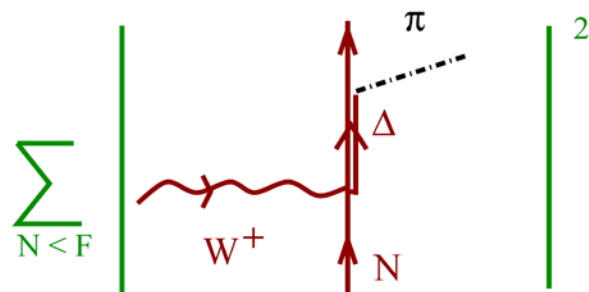


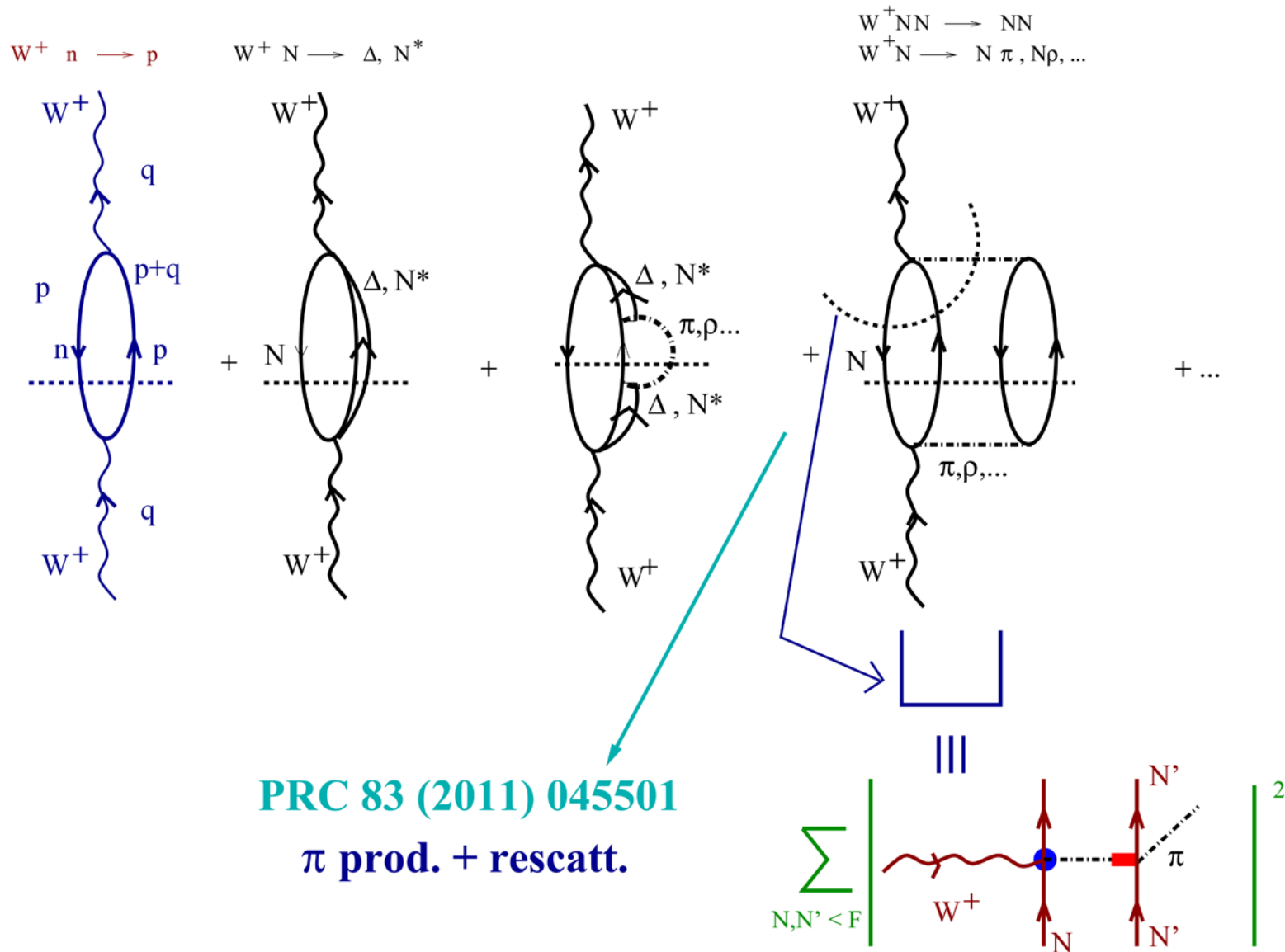
$$\sum_{N < F} \left| \text{Diagram} \right|^2$$

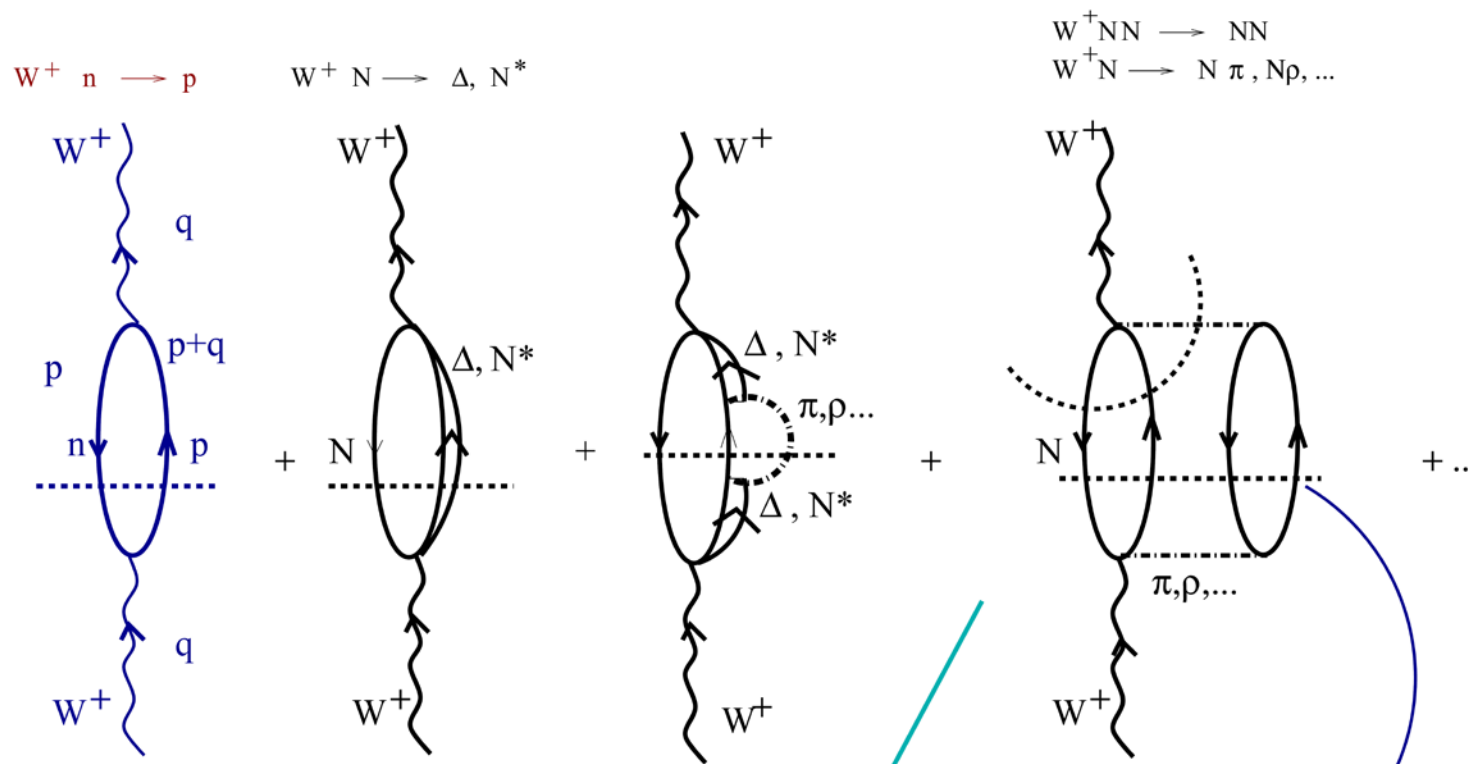
Δh prod.
 PRC 83 (2011) 045501



π prod.







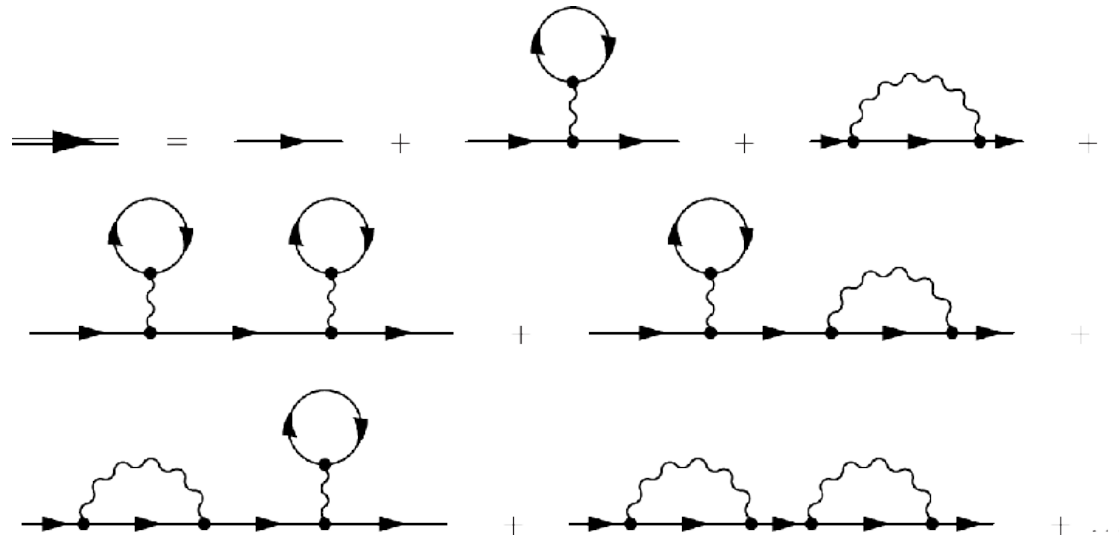
QE-like !

PRC 83 (2011) 045501
 2N absorption (MEC)

$$\sum_{N, N' < F} \left| \begin{array}{c} \text{Diagram showing } W^+ \text{ absorption by a nucleon pair } (N, N') \text{ to produce } \pi, \rho, \dots \end{array} \right|^2$$

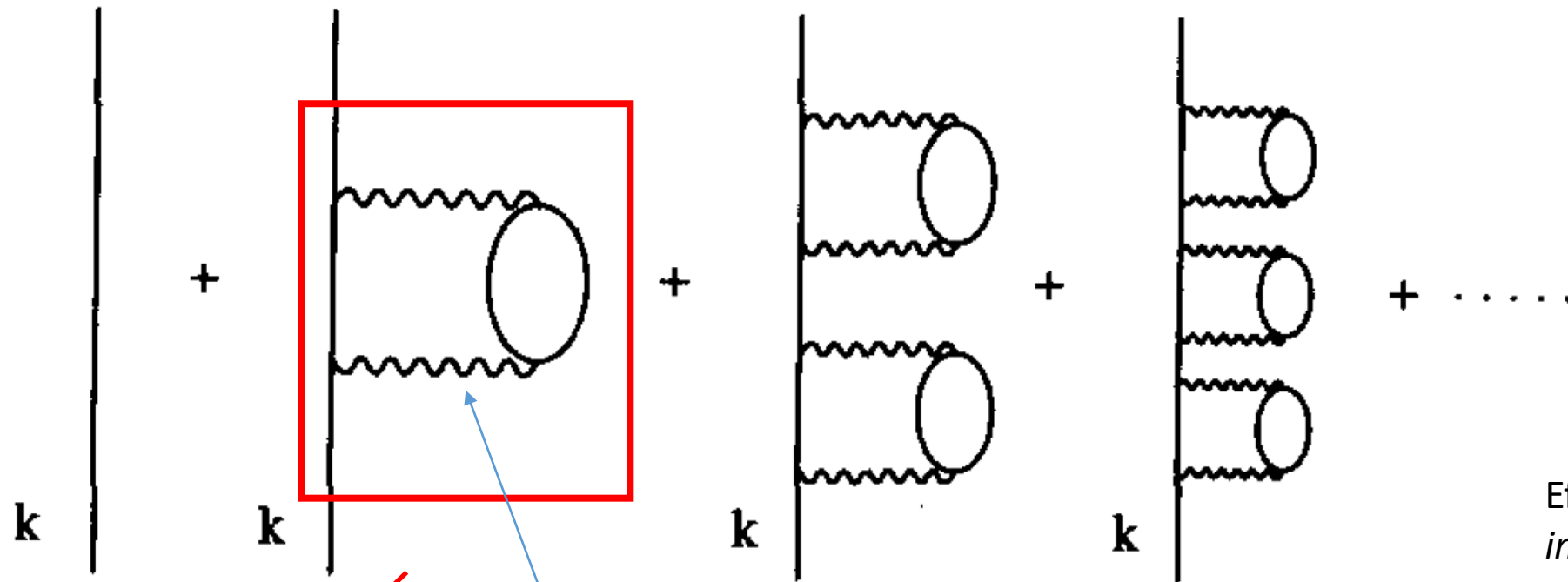
QE nuclear corrections

- Spectral Functions: dressing the nucleon lines in the medium

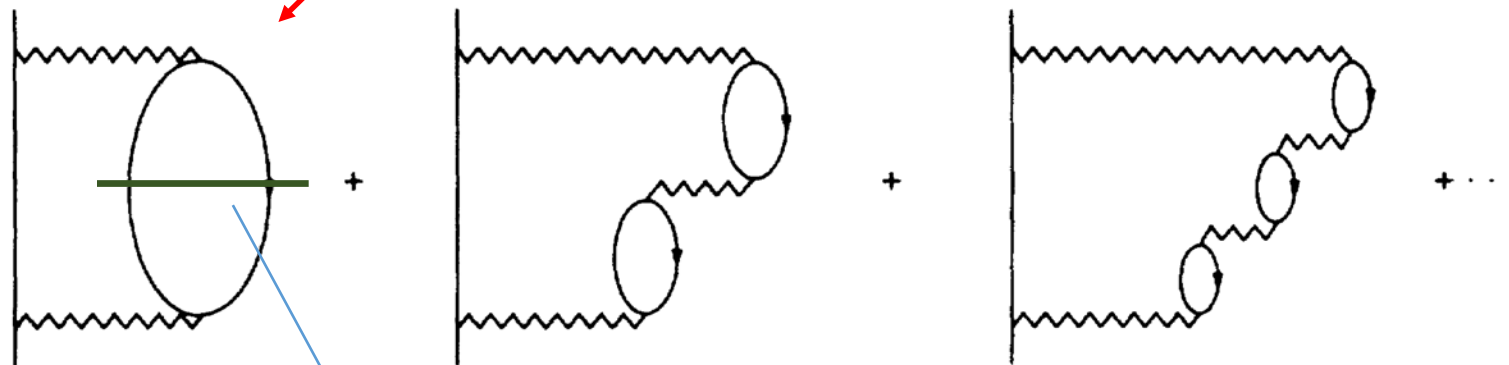


Beyond the Hartree-Fock
approximation





Effective NN interaction in the medium. **It is not just a pion and should account for short-range-correlations and RPA corrections**



Imaginary part

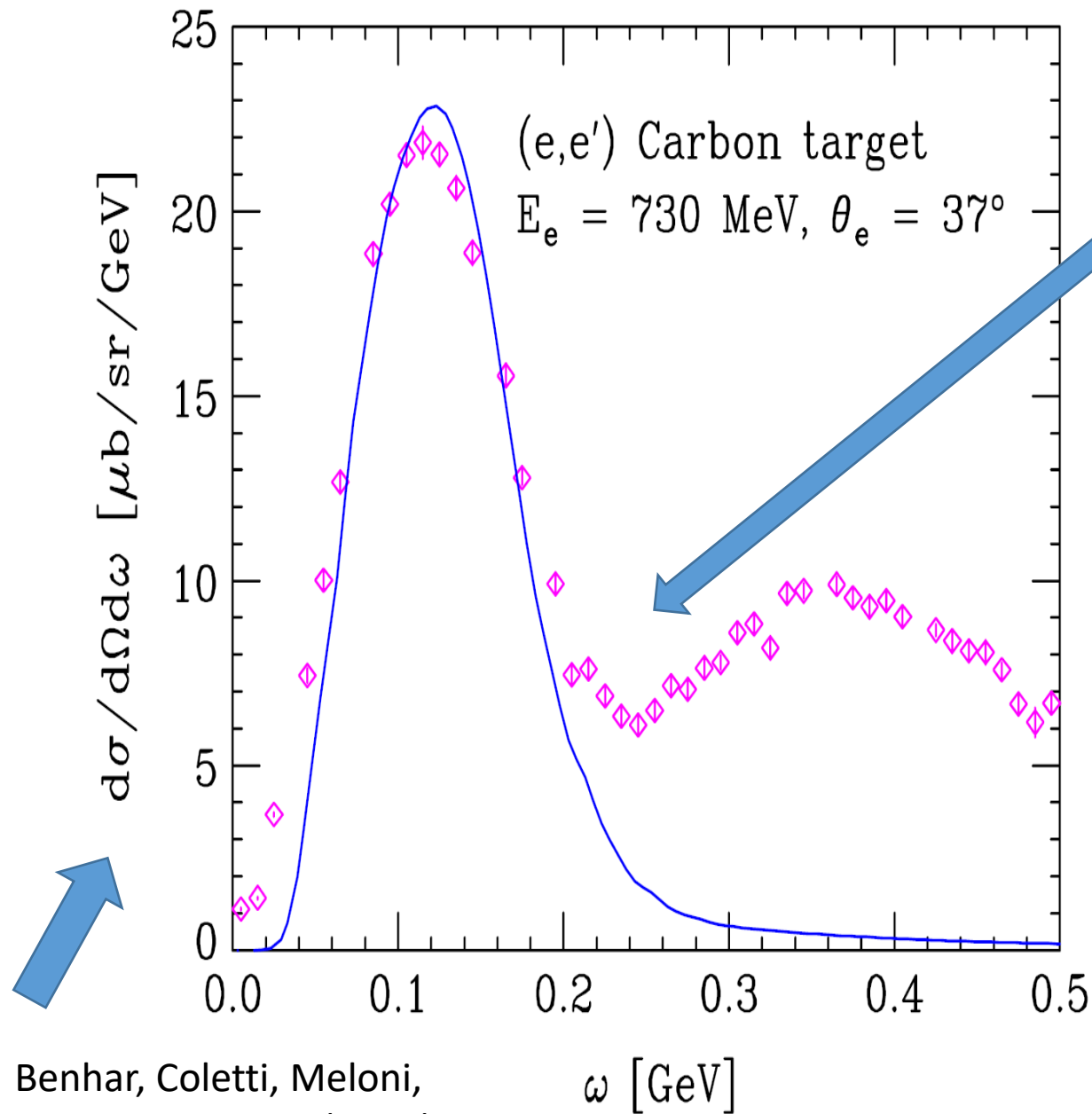
$$S_{p,h}(\omega, \vec{p}) = \mp \frac{1}{\pi} \frac{\text{Im}\Sigma(\omega, \vec{p})}{[\omega^2 - \vec{p}^2 - M^2 - \text{Re}\Sigma(\omega, \vec{p})]^2 + [\text{Im}\Sigma(\omega, \vec{p})]^2}$$

with $\omega \geq \mu$ or $\omega \leq \mu$ for S_p and S_h , respectively
(μ is the chemical potential).

Basic object: nucleon selfenergy in the medium: Σ (from realistic NN interactions in the medium).

This nuclear effect is additional to those due to RPA (long range) correlations !!

***Nuclear medium
dispersion relation effects:
Spectral Functions***

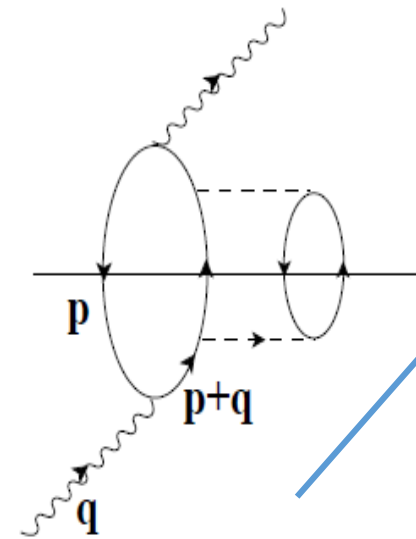


Benhar, Coletti, Meloni,
 PRL 105, 132301 (2010)

Spectral Function (SRC) do not populate the dip region

- **Spectral Function (SF) + Final State Interaction (FSI):**
 dressing up the nucleon propagator of the hole (SF) and particle (FSI) states in the ph excitation

- Change of nucleon dispersion relation:
 - * hole $\Rightarrow$ Interacting Fermi sea (SF)
 - * particle $\Rightarrow$ Interaction of the ejected nucleon with the final nuclear state (FSI)



$$G(p) \rightarrow \int_{-\infty}^{\mu} d\omega \frac{S_h(\omega, \vec{p})}{p^0 - \omega - i\epsilon} + \int_{\mu}^{+\infty} d\omega \frac{S_p(\omega, \vec{p})}{p^0 - \omega + i\epsilon}$$

The hole and particle spectral functions are related to nucleon self-energy Σ in the medium,

$$G(p) = \frac{n(\vec{p})}{p^0 - \varepsilon(\vec{p}) - i\epsilon} + \frac{1 - n(\vec{p})}{p^0 - \varepsilon(\vec{p}) + i\epsilon}$$

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The simplest description $\Rightarrow$ relativistic Fermi Gas with
 non interacting fermions $\boxed{\Sigma = 0}$,

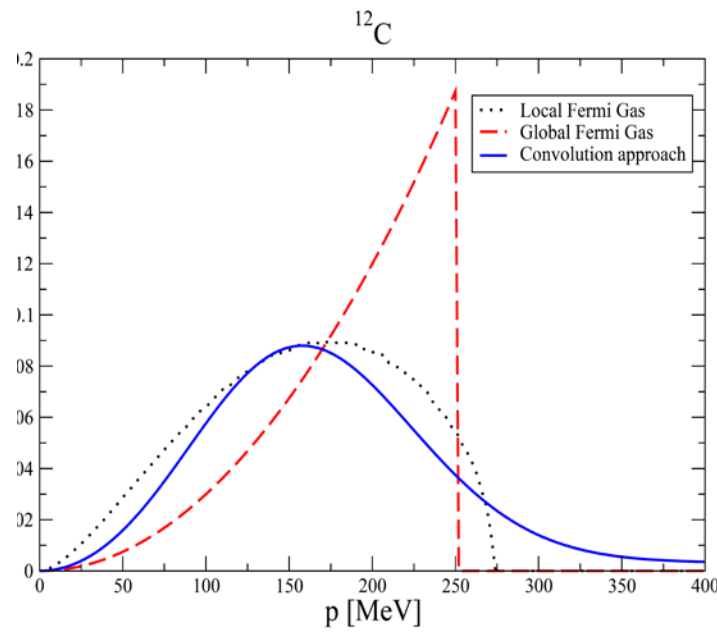
$$S_p(\omega, \vec{p}) = \frac{\theta(|\vec{p}| - k_F)}{2E(\vec{p})} \delta(\omega - E(\vec{p}))$$

$$S_h(\omega, \vec{p}) = \frac{\theta(k_F - |\vec{p}|)}{2E(\vec{p})} \delta(\omega - E(\vec{p}))$$

and only Pauli blocking is incorporated!!

Local vs Global Fermi Gas ?

$$k_F^{p,n}(r) = [3\pi^2 \rho^{p,n}(r)]^{1/3} \text{ vs } k_F^{p,n} = \text{cte} ?$$



Local vs Global Fermi Gas ?

$$k_F(r) = [3\pi^2 \rho(r)/2]^{1/3} \text{ vs } k_F = \text{cte} ?$$

$$S_h(\omega, \vec{p}) = \delta(\omega - E(\vec{p})) \theta(k_F - |\vec{p}|) / 2\omega$$

$$n^{\text{RgFG}}(|\vec{p}|) = \frac{4V}{(2\pi)^3} \int d\omega 2\omega S_h(\omega, \vec{p})$$

$$= \frac{3A}{4\pi k_F^3} \theta(k_F - |\vec{p}|)$$

$$n^{\text{LDA}}(|\vec{p}|) = 4 \int \frac{d^3r}{(2\pi)^3} \int d\omega 2\omega S_h(\omega, \vec{p})$$

$$= 4 \int \frac{d^3r}{(2\pi)^3} \theta(\mathbf{k_F}(\mathbf{r}) - |\vec{p}|)$$

$$(\int d^3p n(|\vec{p}|) = A)$$

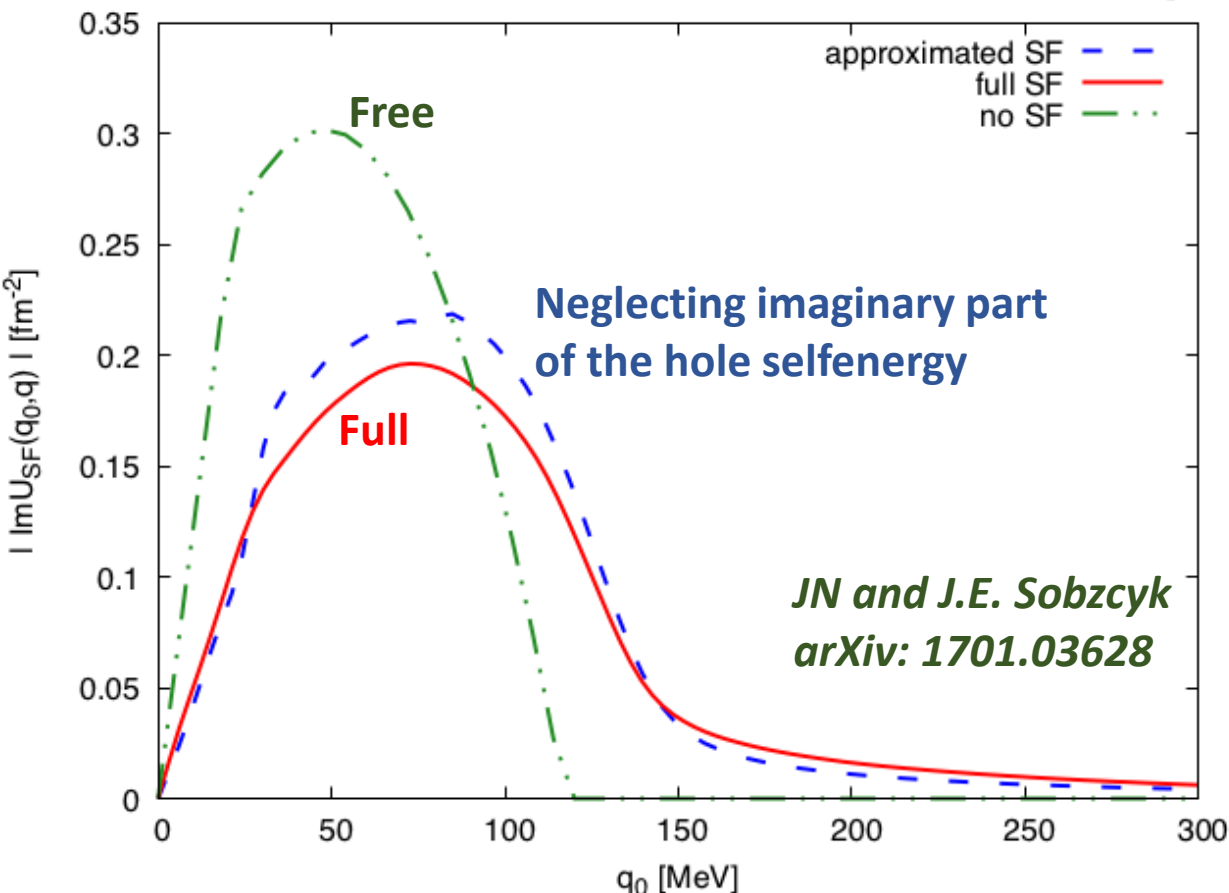
Convolution approach: C. Ciofi degli Atti, S. Liuti, and S. Simula, PRC 53, 1689 (1996), provide realistic distribution due to short-range correlations !

Semiphenomenological approach to nucleon properties in nuclear matter

P. Fernández de Córdoba and E. Oset

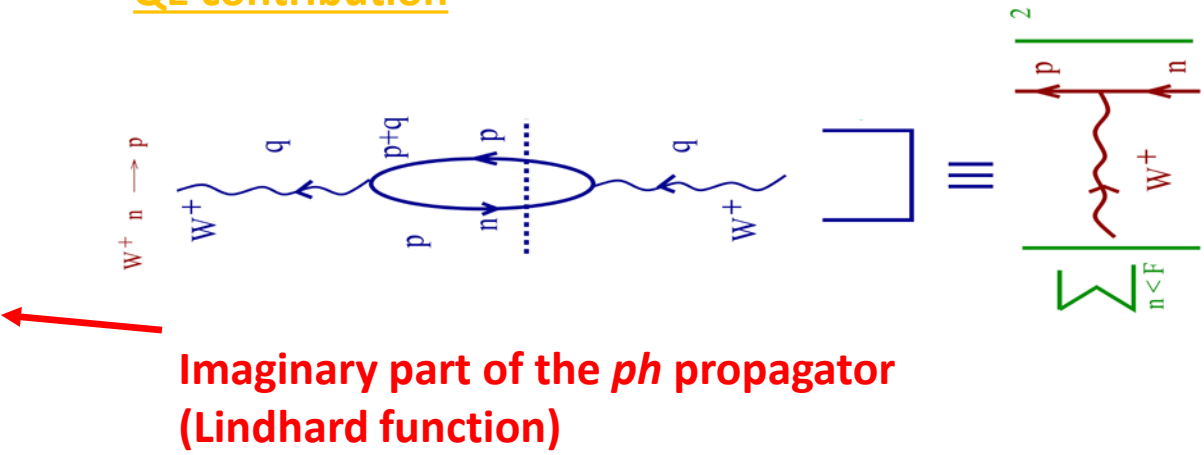
Departamento de Física Teórica and Instituto de Física Corpuscular,
Centro Mixto Universidad de Valencia Consejo Superior de Investigaciones Científicas, 46100 Burjassot (Valencia), Spain

(Received 20 April 1992)

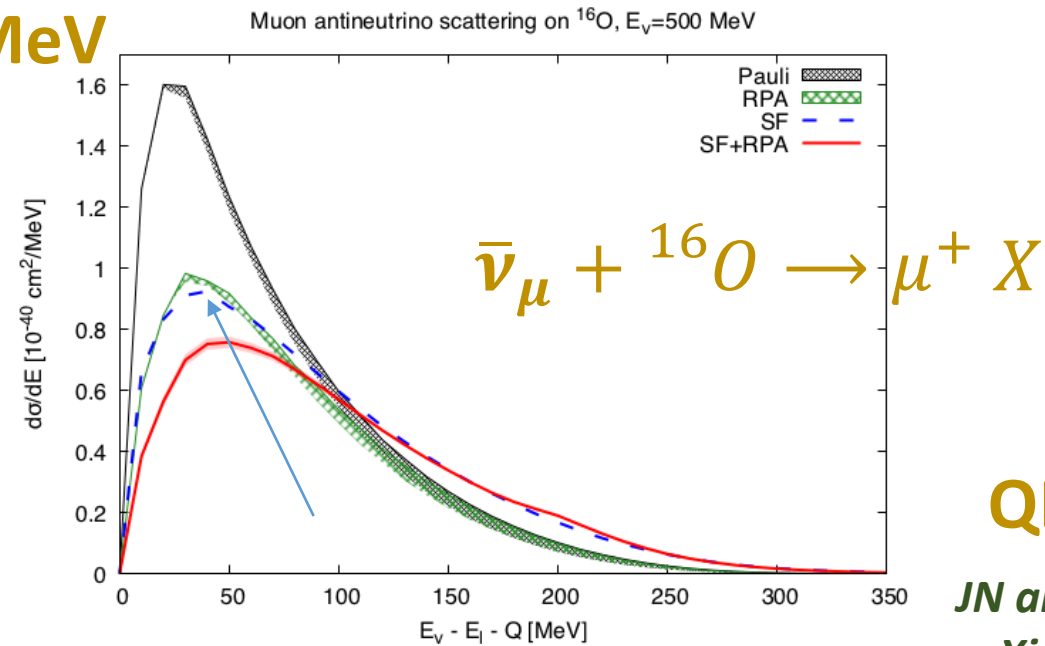
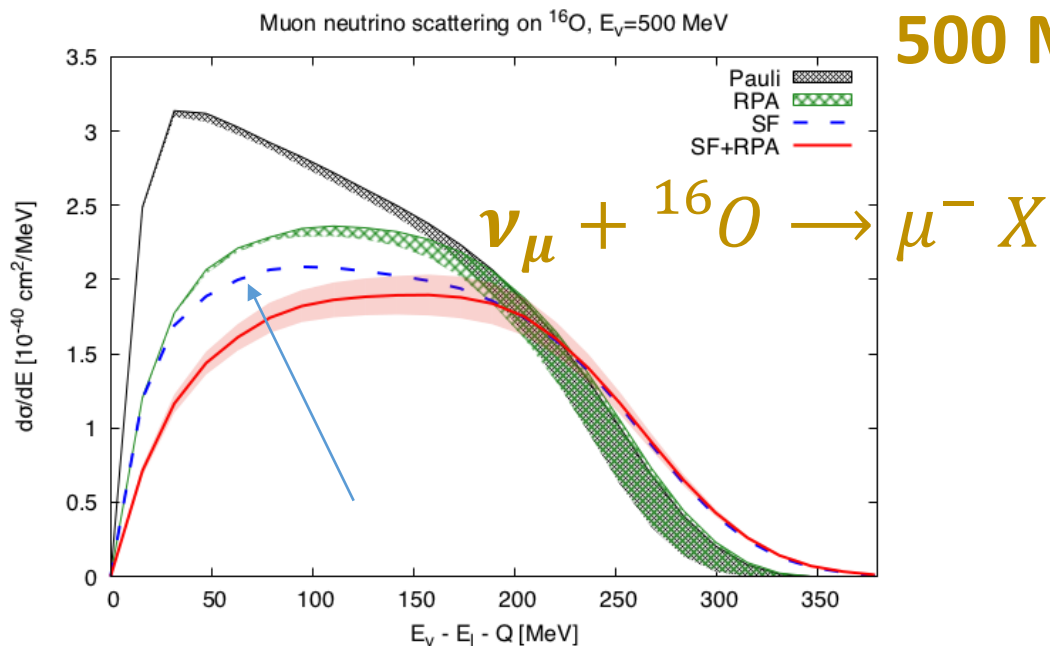


Effective NN interaction in the medium constructed from the experimental NN cross section + some medium corrections

QE contribution

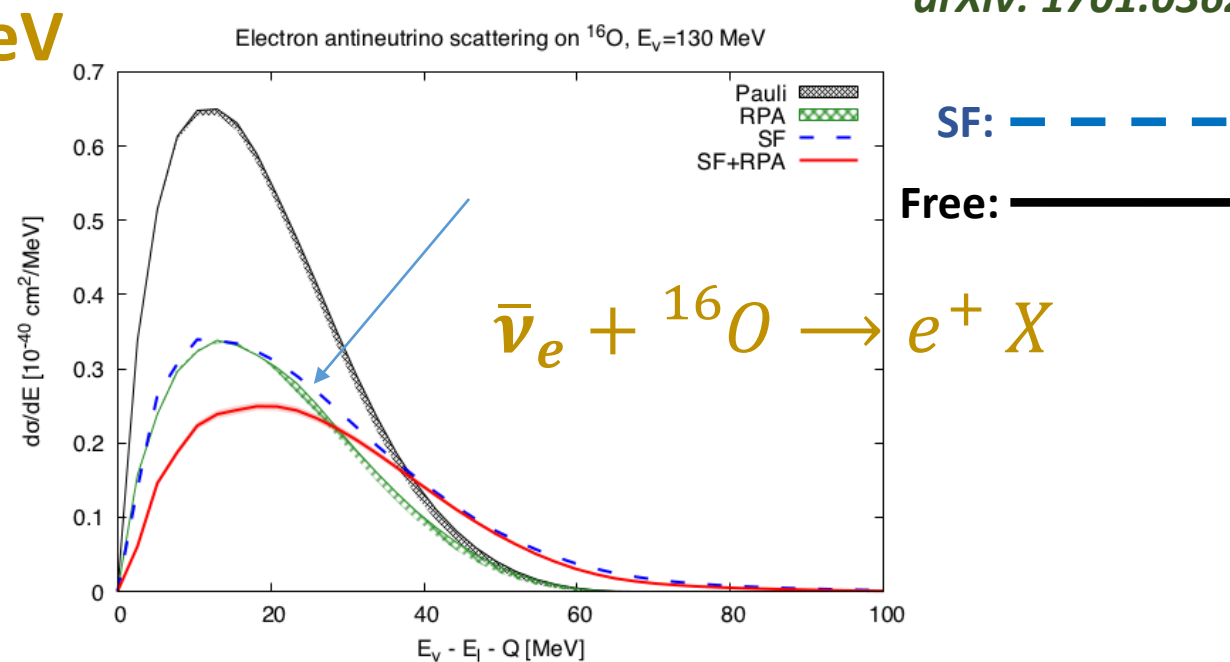
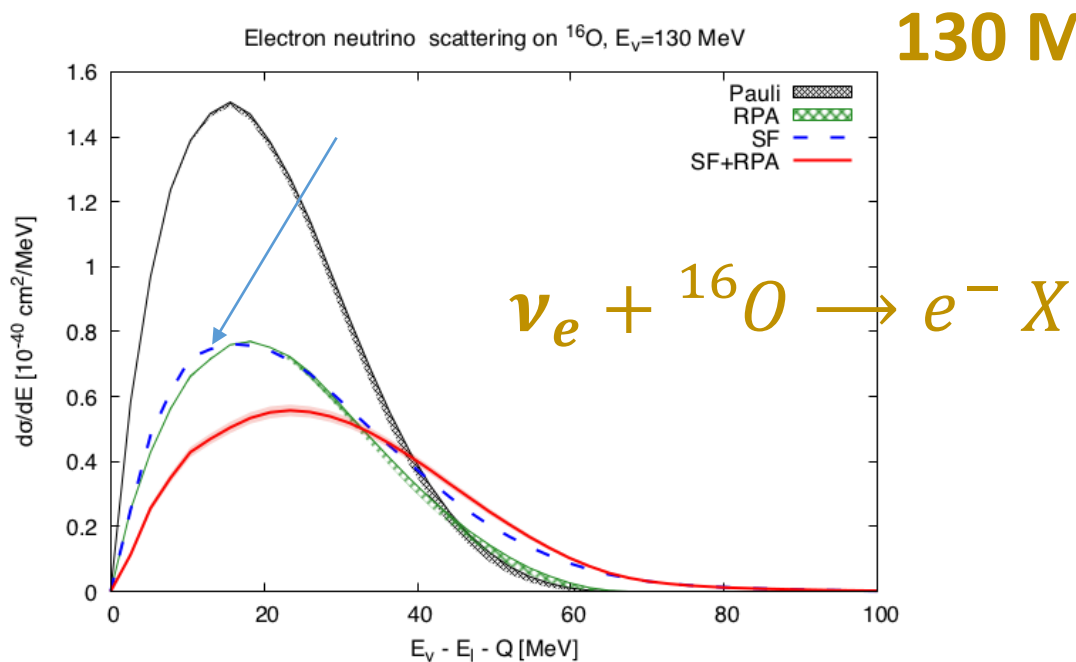


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QE: 1p1h

JN and J.E. Sobczyk
arXiv: 1701.03628



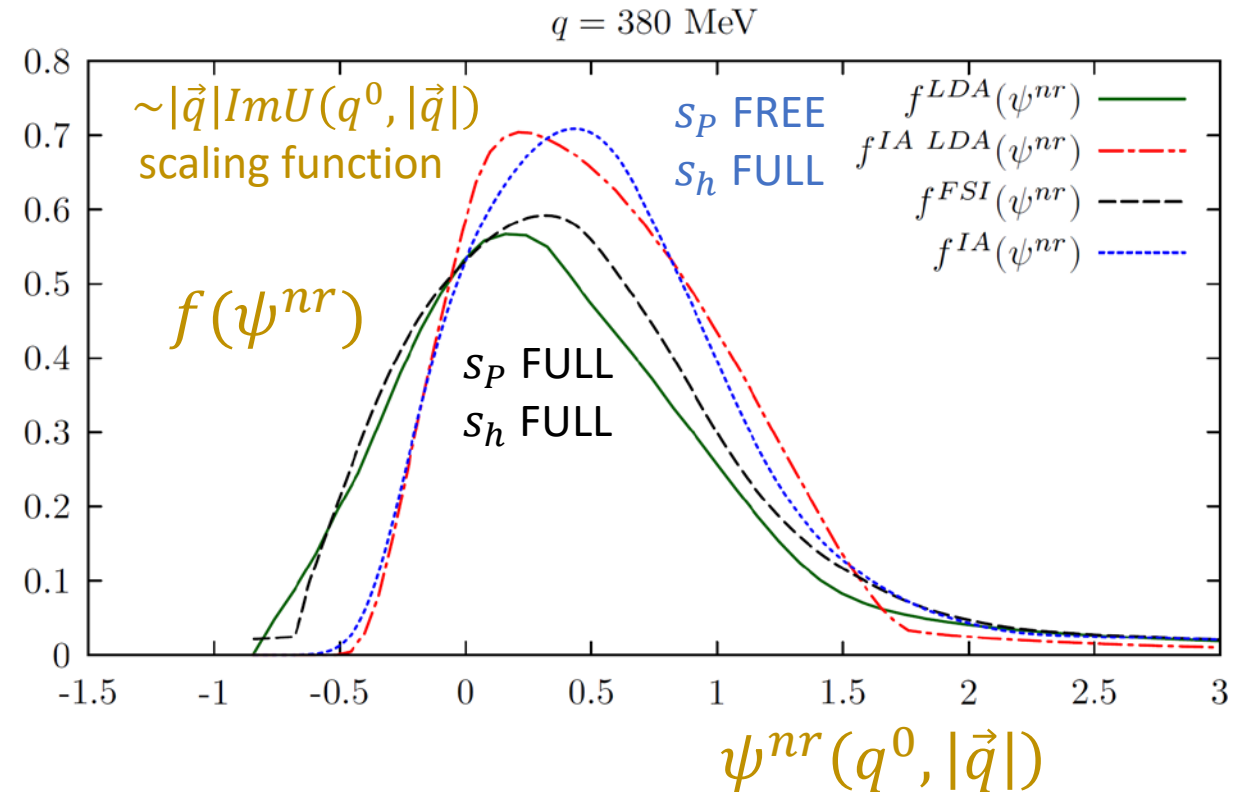
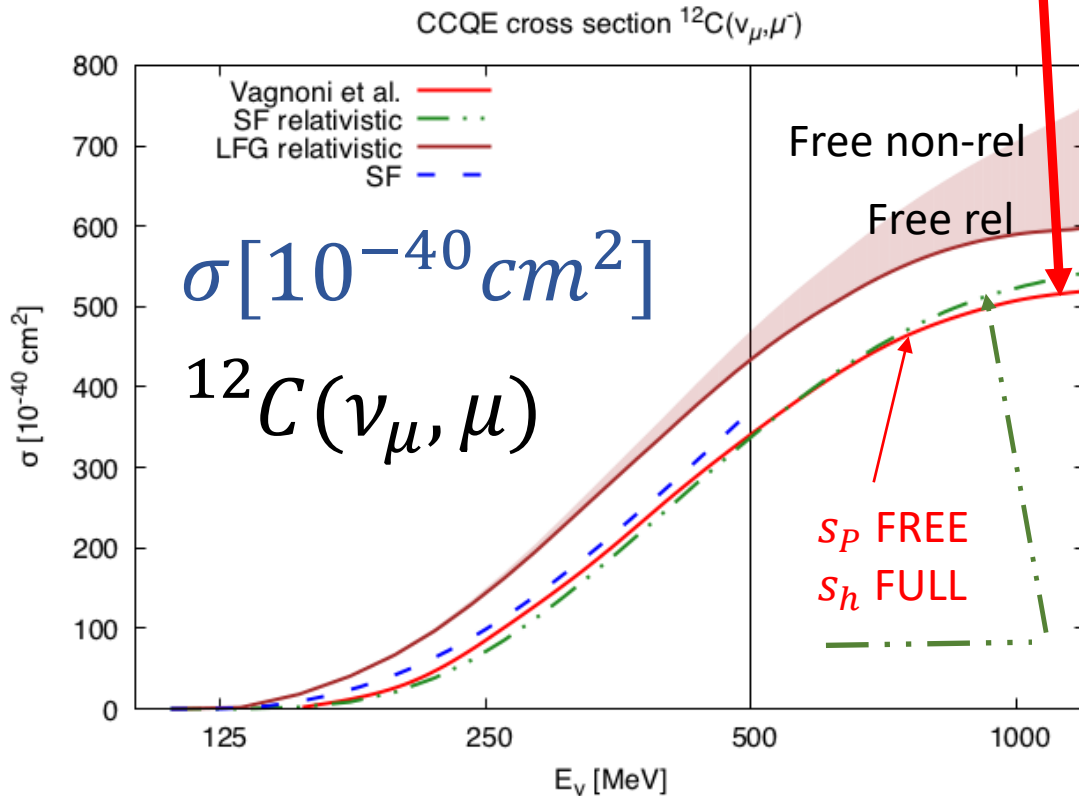
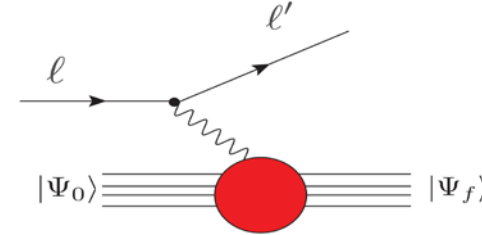
reasonable agreement !

Inelastic Neutrino-Nucleus Interactions within the Spectral Function Formalism

Erica Vagnoni,^{1,*} Omar Benhar,^{2,3,†} and Davide Meloni^{1,‡}

Noemi Rocco

“FermiLab Theory Seminar” March 2nd 2017

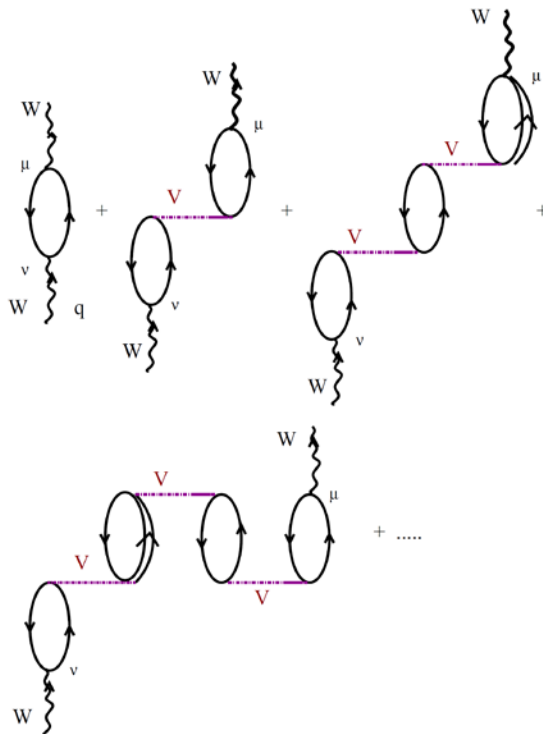


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QE nuclear corrections

- **RPA: long range correlations**

- Polarization (RPA) effects. Substitute the ph excitation by an RPA response: series of ph and Δh excitations.



1. Effective Landau-Migdal interaction

$$V(\vec{r}_1, \vec{r}_2) = c_0 \delta(\vec{r}_1 - \vec{r}_2) \left\{ \boxed{f_0(\rho)} + f'_0(\rho) \vec{\tau}_1 \vec{\tau}_2 + \boxed{g_0(\rho) \vec{\sigma}_1 \vec{\sigma}_2} + g'_0(\rho) \vec{\sigma}_1 \vec{\sigma}_2 \vec{\tau}_1 \vec{\tau}_2 \right\}$$

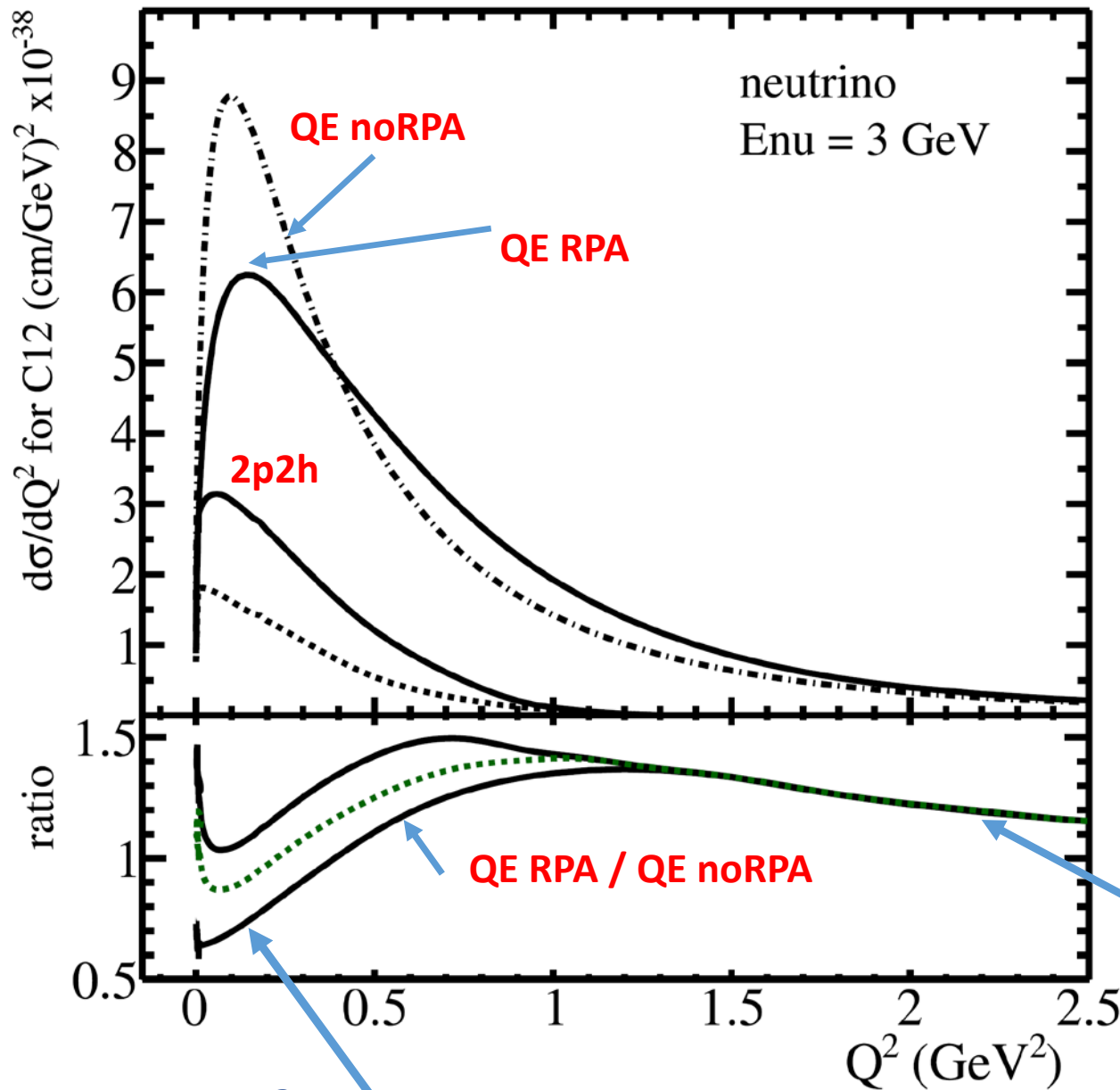
Isoscalar terms $\boxed{}$ do not contribute to CC

2. $S = T = 1$ channel of the $ph-ph$ interaction $\rightarrow$ s longitudinal (π) and transverse (ρ) + SRC

$$g'_0 \vec{\sigma}_1 \vec{\sigma}_2 \vec{\tau}_1 \vec{\tau}_2 \rightarrow [V_l(q) \hat{q}_i \hat{q}_j + V_t(q) (\delta_{ij} - \hat{q}_i \hat{q}_j)] \sigma_1^i \sigma_2^j \vec{\tau}_1 \vec{\tau}_2$$

$$V_{l,t}(q) = \frac{f_{\pi NN, \rho NN}}{m_{\pi, \rho}^2} \left(F_{\pi, \rho}(q^2) \frac{\vec{q}^2}{q^2 - m_{\pi, \rho}^2} + g'_{l,t}(q) \right)$$

3. Contribution of Δh excitations important

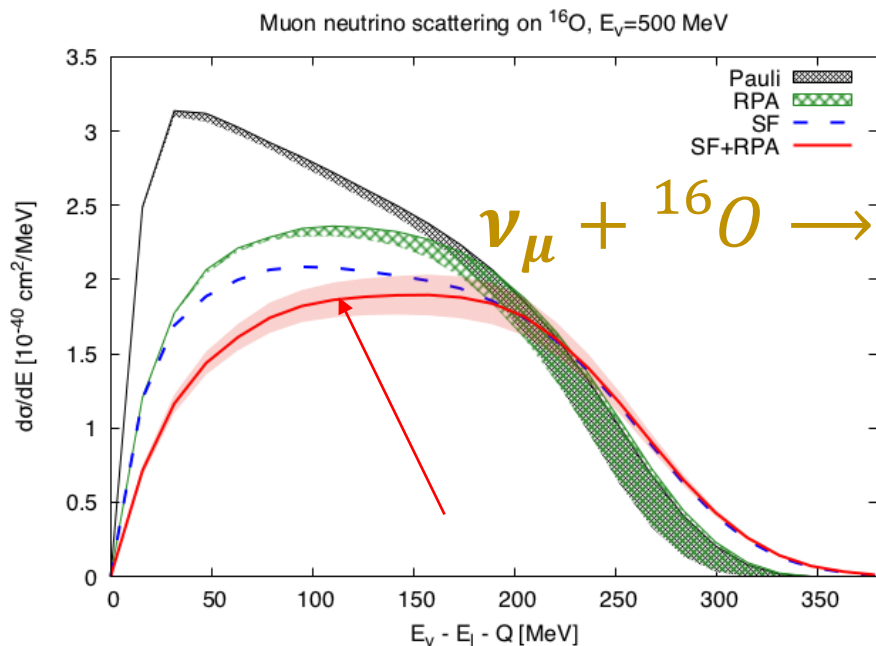


RPA (long range correlations) the weak probe interacts with the nucleus as a whole,

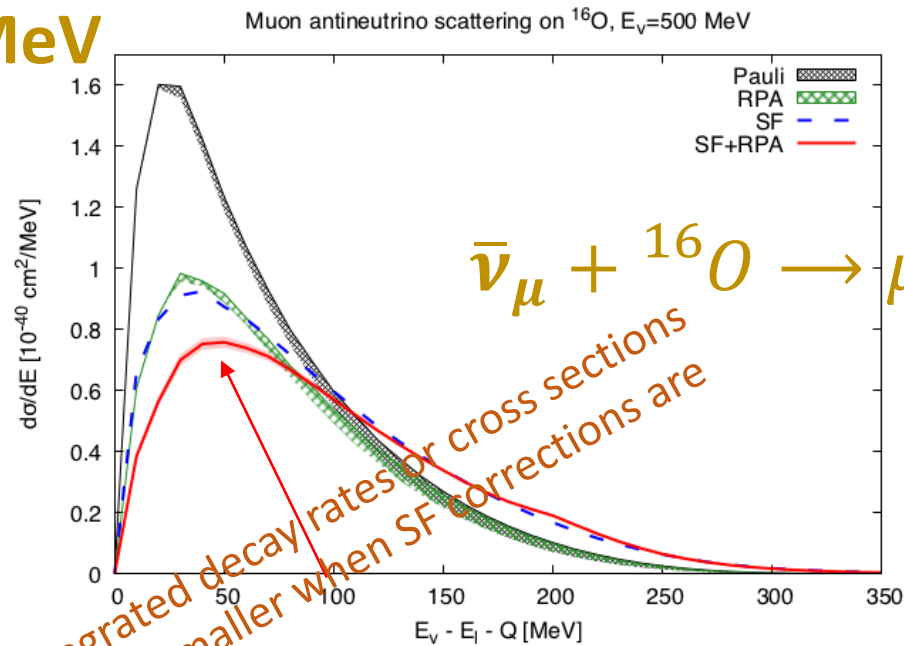


RPA effects $\rightarrow 0$, when $1/\sqrt{Q^2} \ll \text{nuclear radius}$, since then the probe would see the individual nucleons or even the partons

Depletion at low Q^2 values

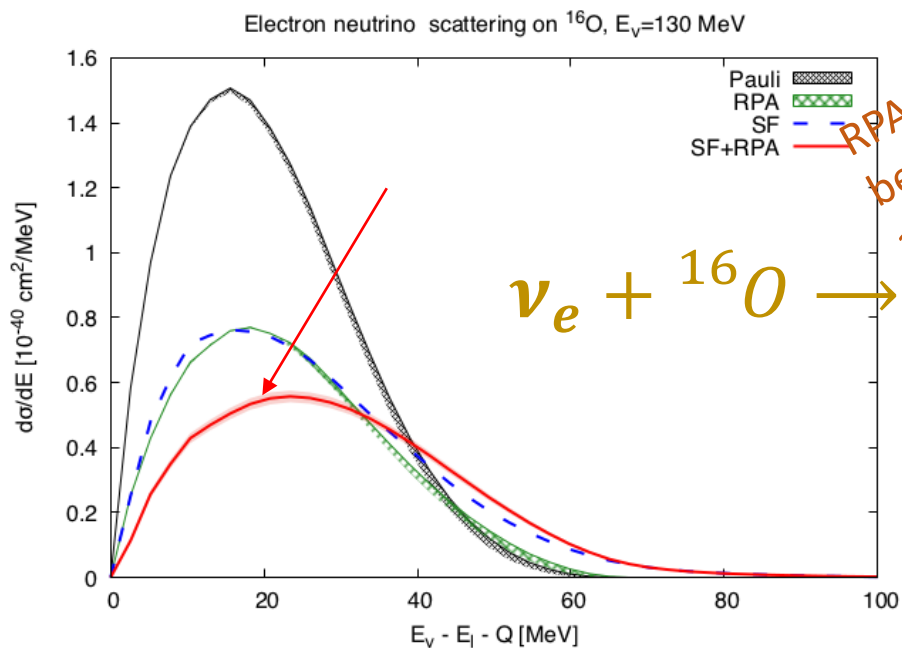


500 MeV

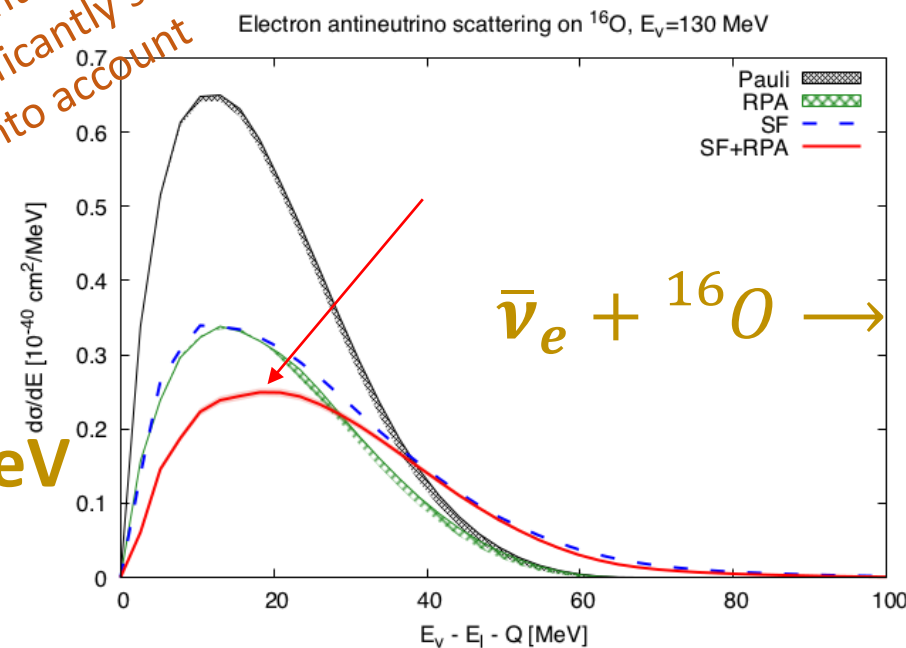


QE: 1p1h

JN and J.E. Sobczyk
arXiv: 1701.03628



130 MeV

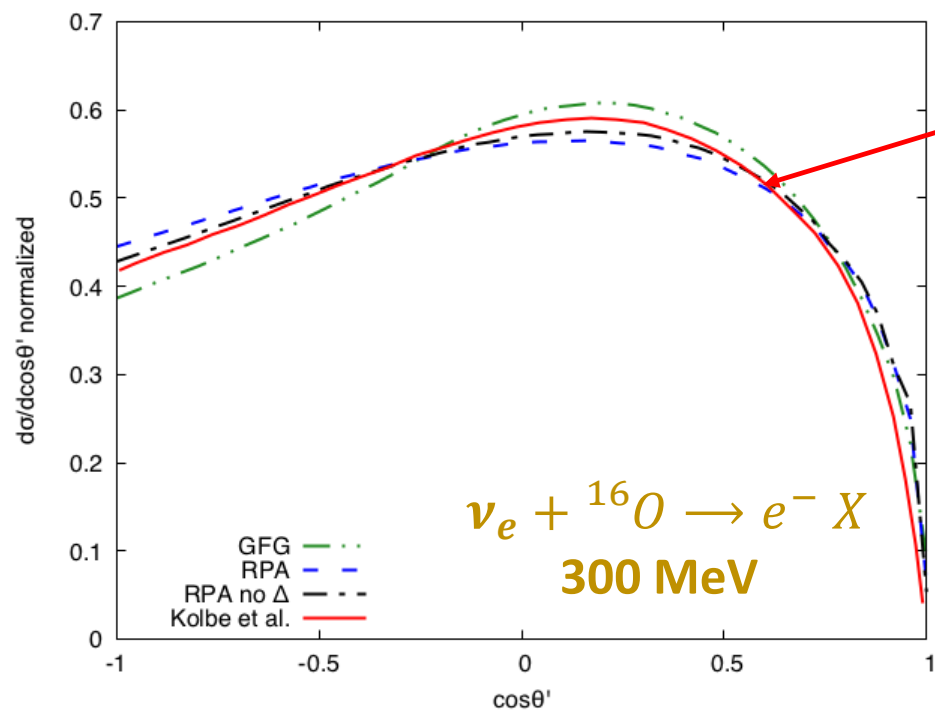


RPA effects in integrated decay rates or cross sections become significantly smaller when SF corrections are also taken into account

SF+RPA

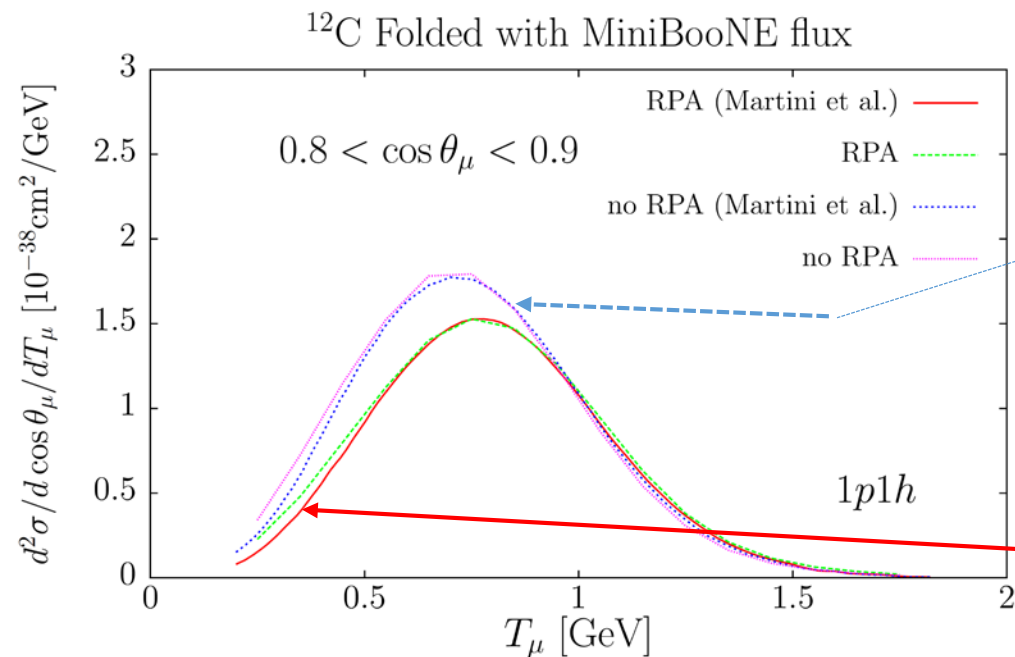
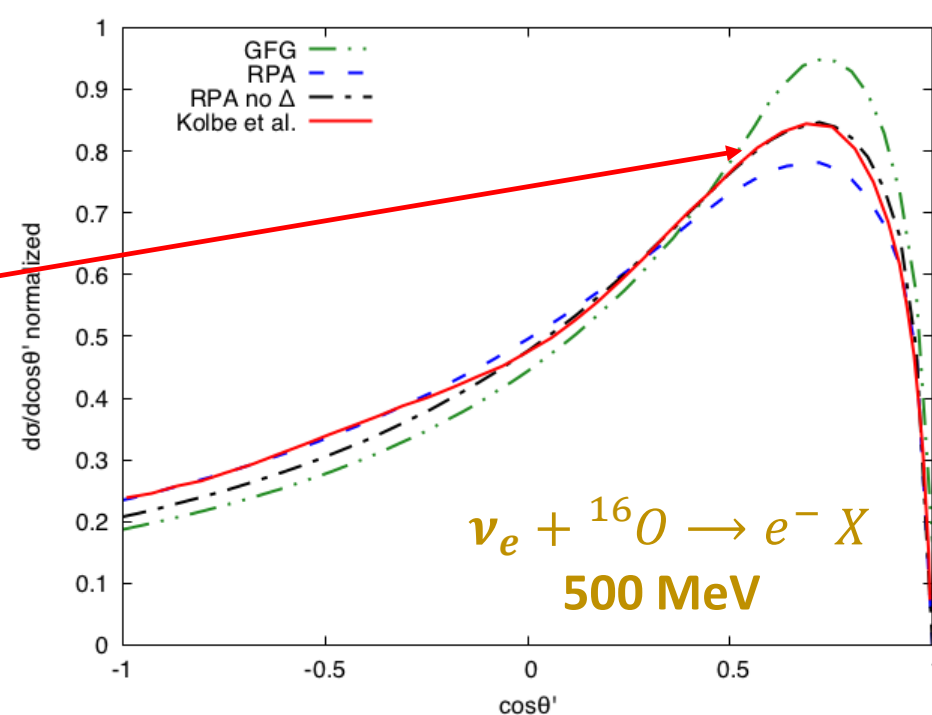
Free

Free+RPA



Kolbe, Langanke,
Martinez-Pinedo,
Vogel, J. Phys.
G29, 2569 (2003)

$d\sigma/d\cos(\theta')$

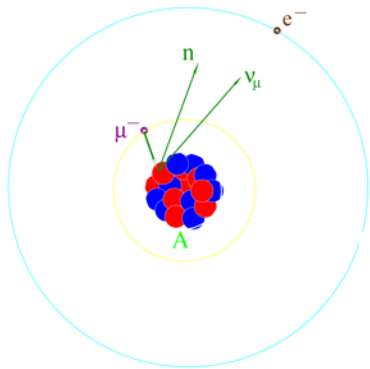


M. Martini, M. Ericson, and G. Chanfray, Phys.Rev. C84,
055502 (2011)

reasonable agreement !

JN and J.E. Sobczyk
arXiv: 1701.03628

Juan Nieves, IFIC (CSIC & UV)



JN and J.E. Sobczyk
arXiv: 1701.03628

Inclusive Muon Capture: $\Gamma \left[(A_Z - \mu^-)^{1s}_{\text{bound}} \right]$

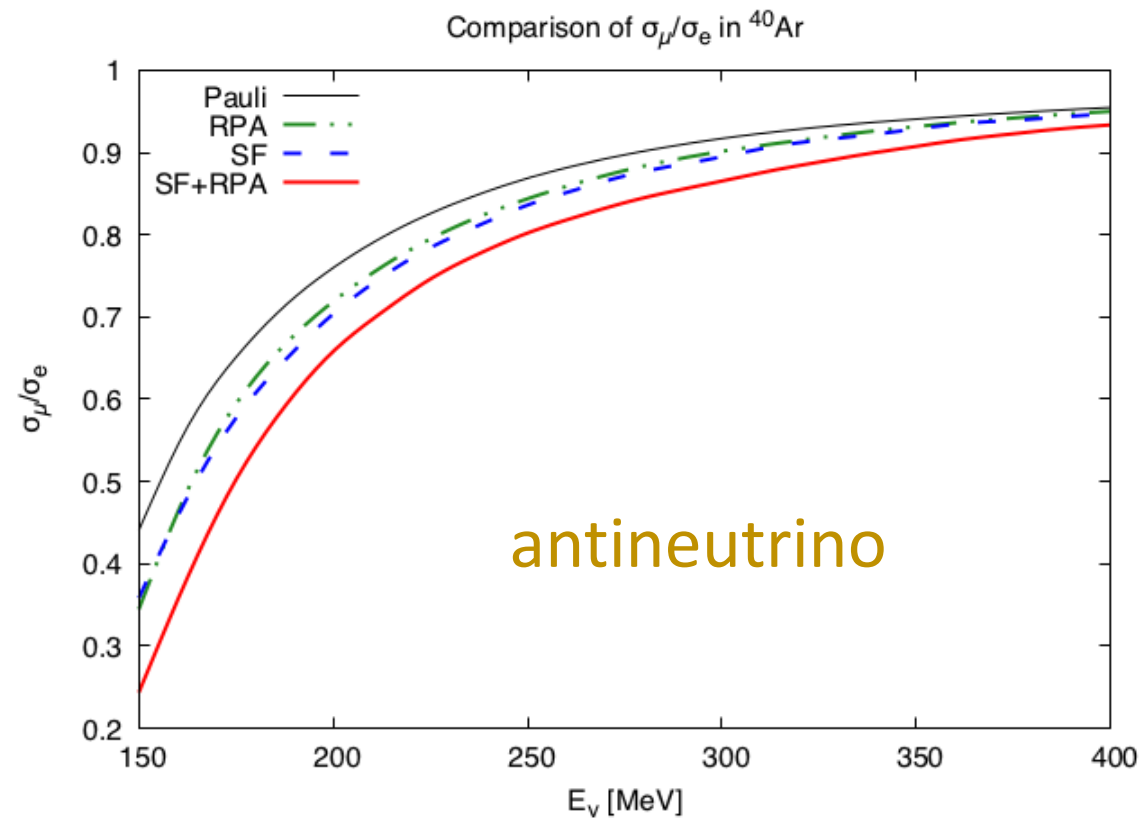
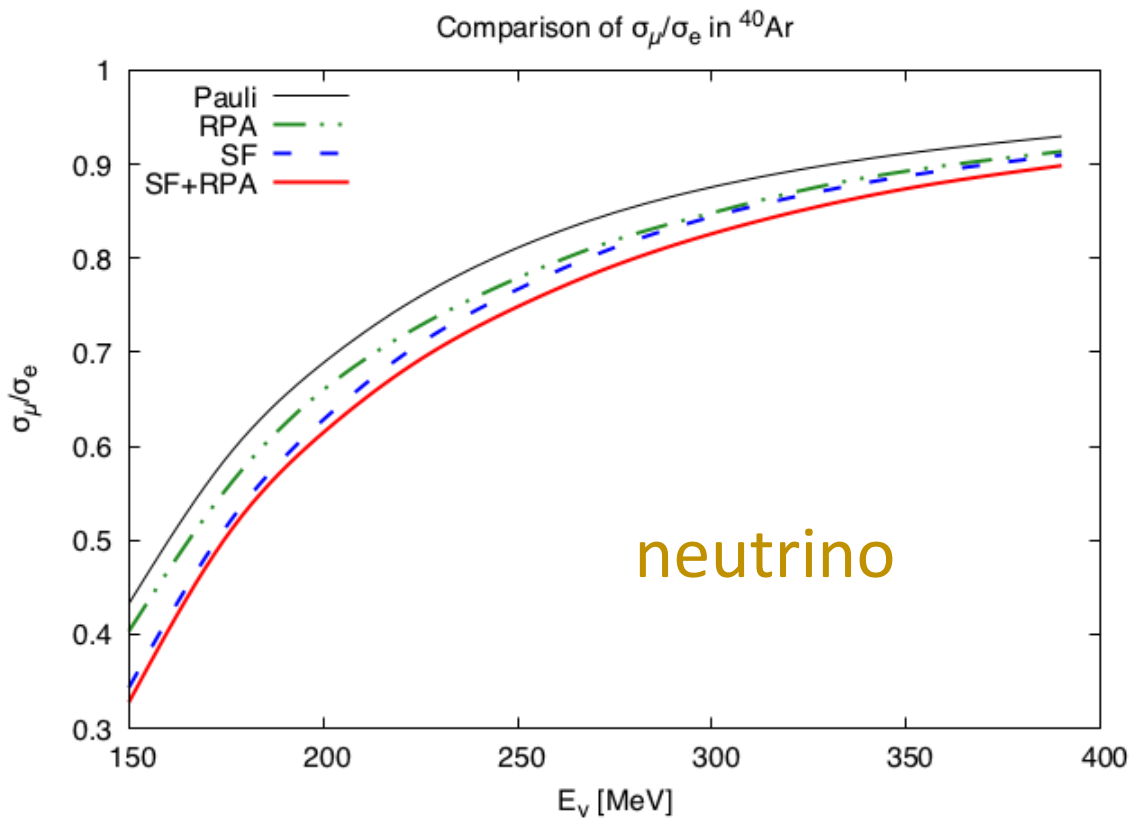
Nucleus	Pauli (10^4 s^{-1})	RPA (10^4 s^{-1})	SF (10^4 s^{-1})	SF+RPA (10^4 s^{-1})	Exp. (10^4 s^{-1})
^{12}C	5.76	3.37 ± 0.16	3.22	3.19 ± 0.06	3.79 ± 0.03
^{16}O	18.7	10.9 ± 0.4	10.6	10.3 ± 0.2	10.24 ± 0.06
^{18}O	13.8	8.2 ± 0.4	7.0	8.7 ± 0.1	8.80 ± 0.15
^{23}Na	64.5	37.0 ± 1.5	30.9	34.3 ± 0.4	37.73 ± 0.14
^{40}Ca	498	272 ± 11	242	242 ± 6	252.5 ± 0.6

The inclusive $^{12}\text{C}(\nu_\mu, \mu^-)X$ and $^{12}\text{C}(\nu_e, e^-)X$ reactions near threshold

10^{-40} cm^2
Flux-
averaged
cross
sections

	Pauli	RPA	SF	SF+RPA	SM	SM	CRPA	Experiment		
					[125]	[44]	[45]	LSND [115]	LSND [116]	LSND [117]
$\bar{\sigma}(\nu_\mu, \mu^-)$	23.1	13.2 ± 0.7	12.2	9.7 ± 0.3	13.2	15.2	19.2	$8.3 \pm 0.7 \pm 1.6$	$11.2 \pm 0.3 \pm 1.8$	$10.6 \pm 0.3 \pm 1.8$
$\bar{\sigma}(\nu_e, e^-)$	0.200	0.143 ± 0.006	0.086	0.138 ± 0.004	0.12	0.16	0.15	KARMEN [120]	LSND [118]	LAMPF [119]
								$0.15 \pm 0.01 \pm 0.01$	0.15 ± 0.01	0.141 ± 0.023

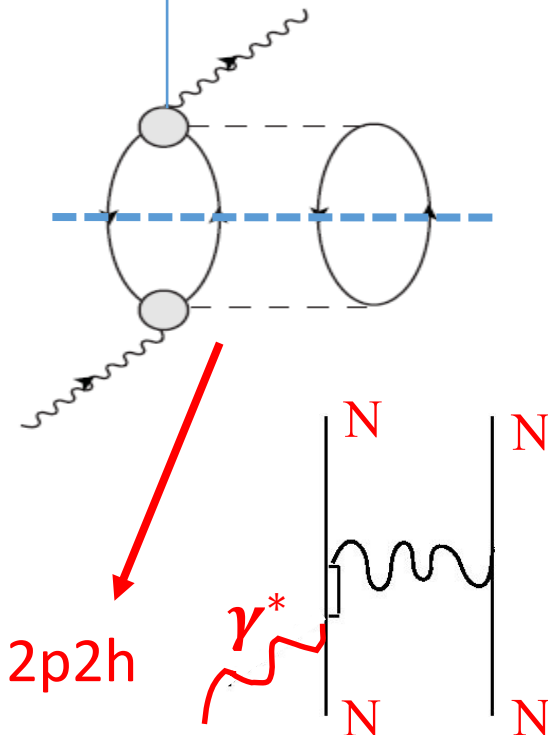
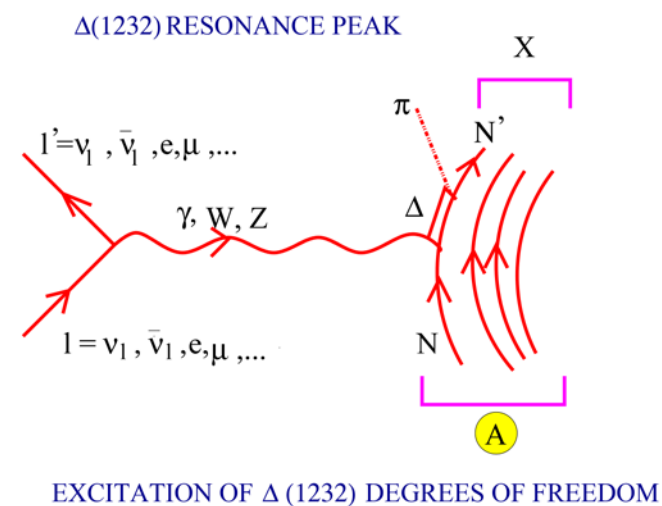
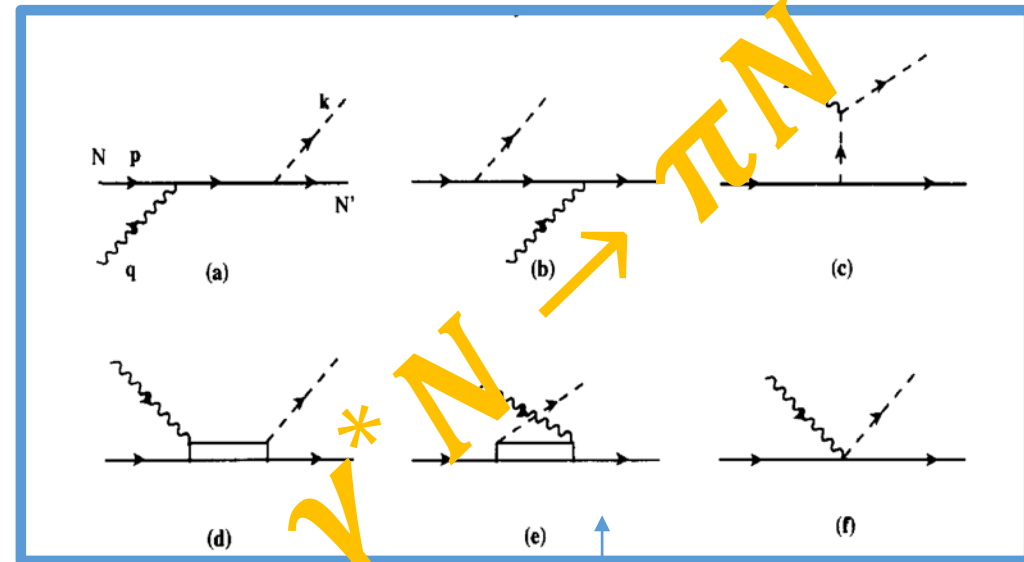
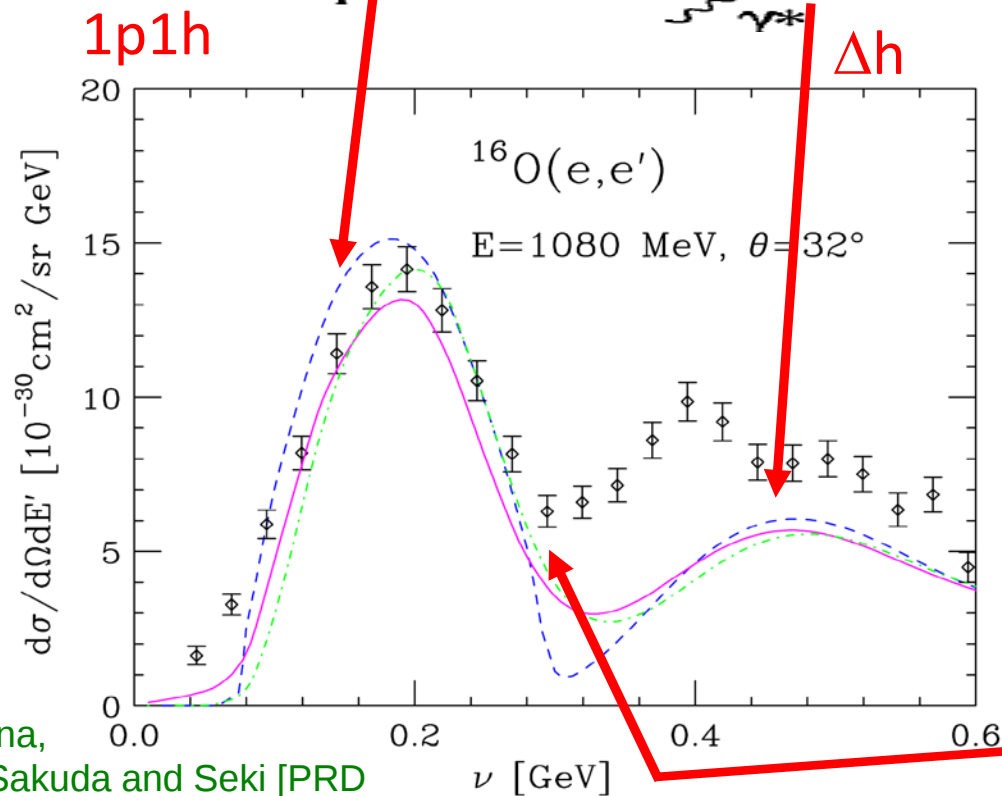
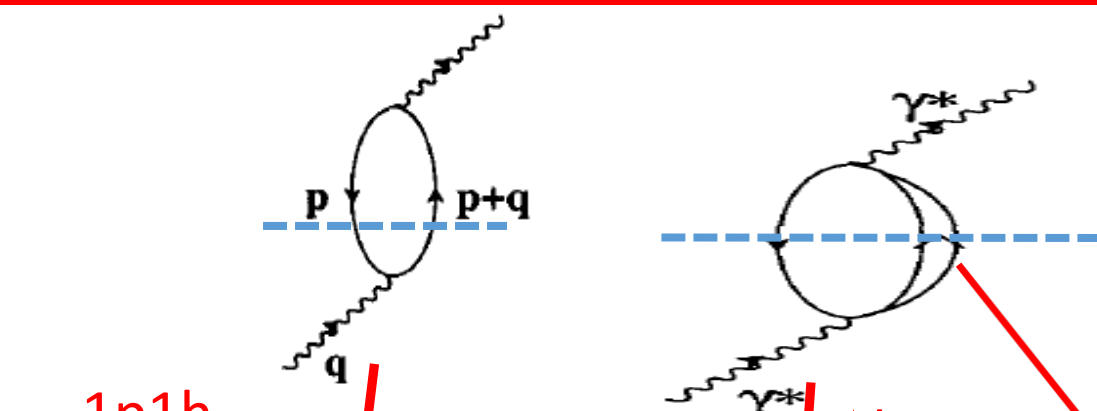
[125]: Hayes & Towner, PRC61, 044603;
[44]: Volpe et al., PRC62, 015501; [45]: Kolbe et al., J. Phys. G29, 2569



$$^{40}\text{Ar} \quad \sigma_\mu/\sigma_e$$

- Important deviations from 1 ($150 \text{ MeV} < E_\nu < 400 \text{ MeV}$)
- SFs & RPA effects strongly affect the ratio and become essential to perform a correct analysis of appearance neutrino oscillation events in LBE.

2p2h: Inclusive electron-nucleus scattering

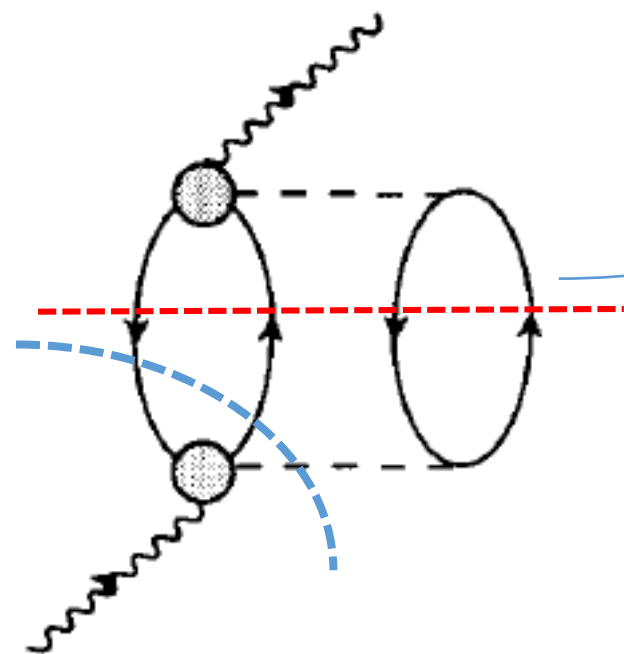


Benhar, Farina,
Nakamura, Sakuda and Seki [PRD
72 (2005) 053005]

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Dip region 2p2h
 $\gamma^* NN \rightarrow NN$

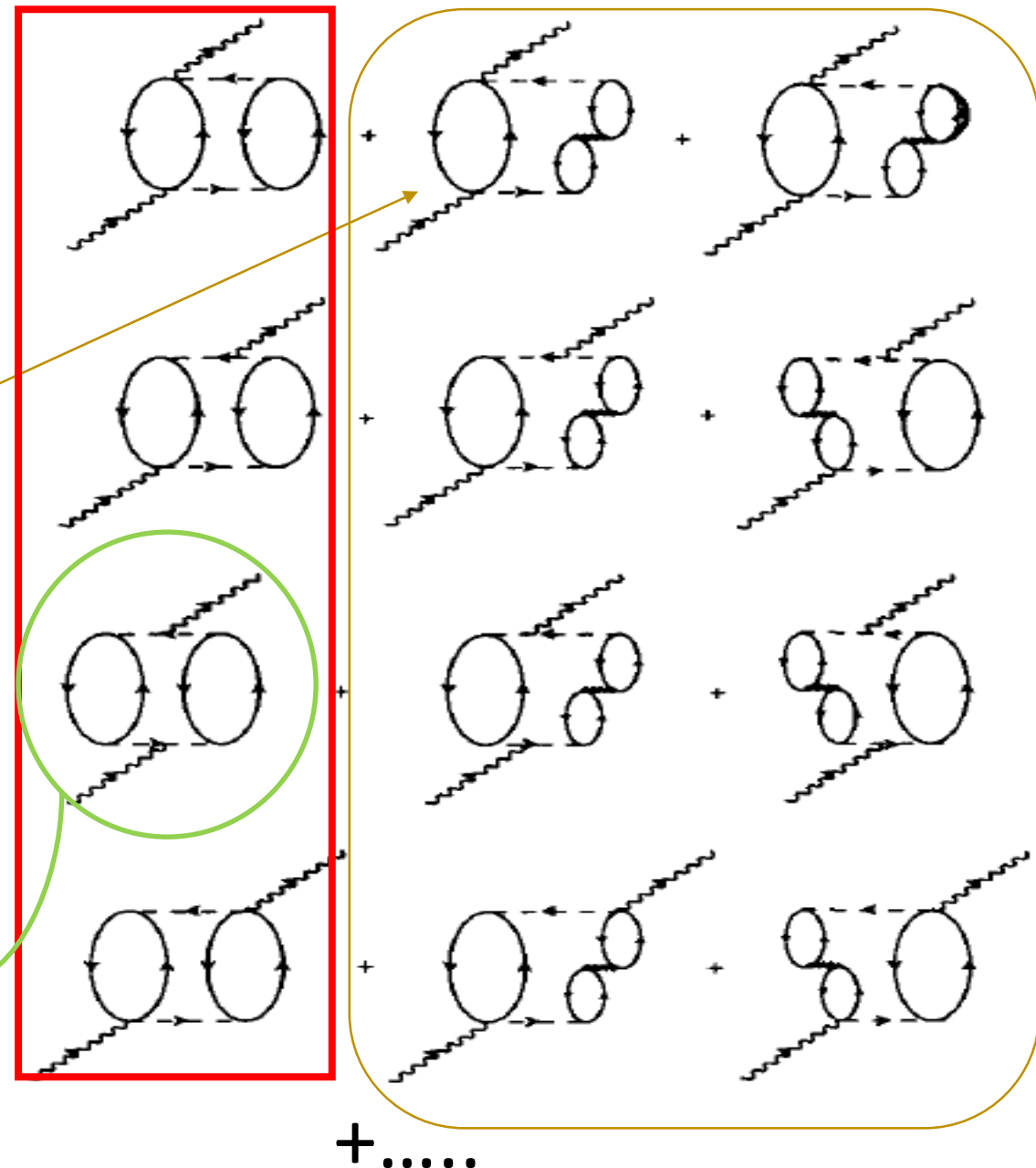
2p2h (two body absorption) contributions

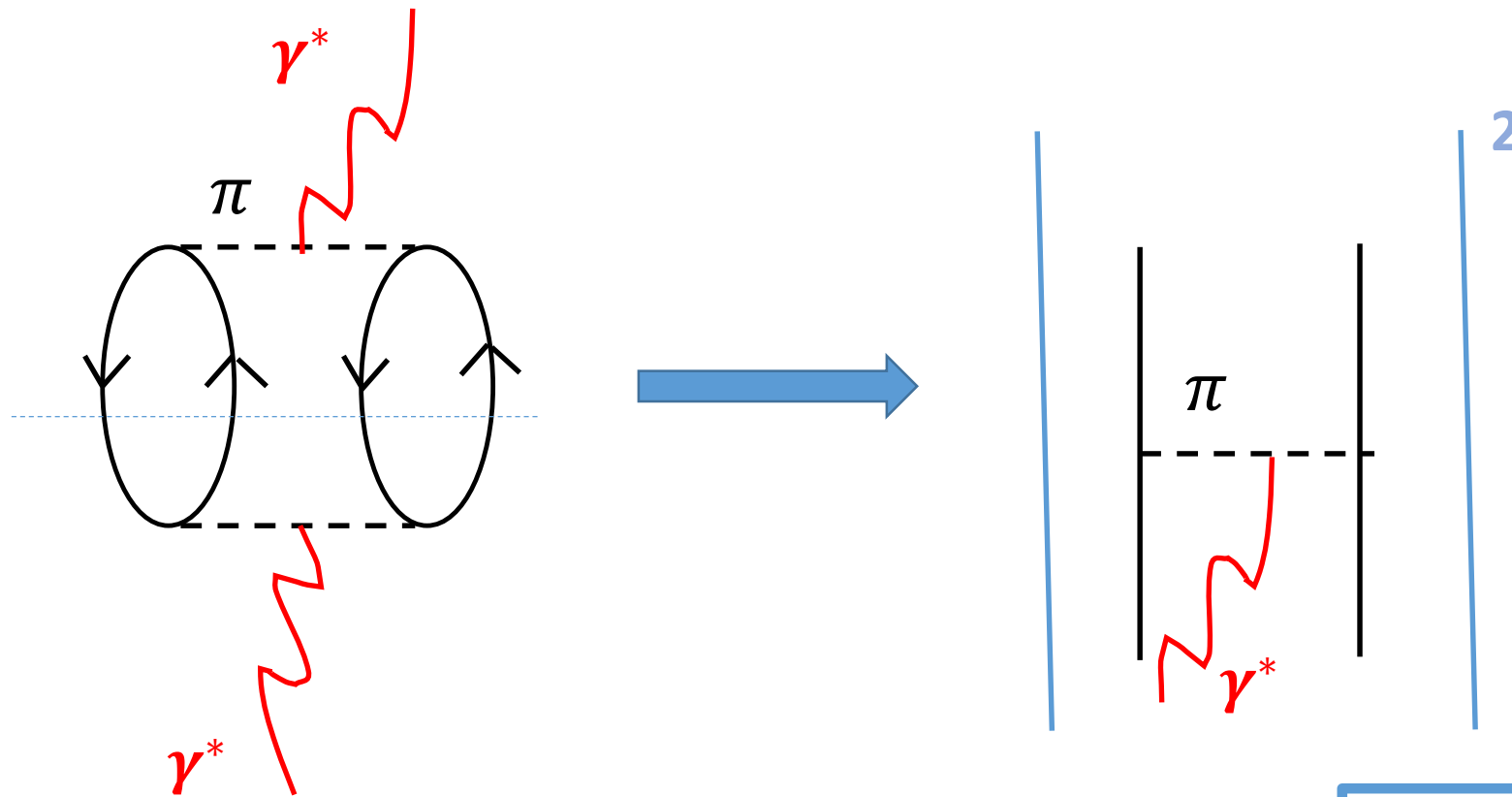


RPA corrections to 2p2h contributions

$$\text{Im } U_N \rightarrow a \frac{\text{Im } U_N}{|1 - U_\lambda(q) V_l|^2} + b \frac{\text{Im } U_N}{|1 - U_\lambda V_l|^2}$$

Two cuts: $\gamma^* NN \rightarrow NN$
 $\gamma^* N \rightarrow N\pi$ (*dressed*)

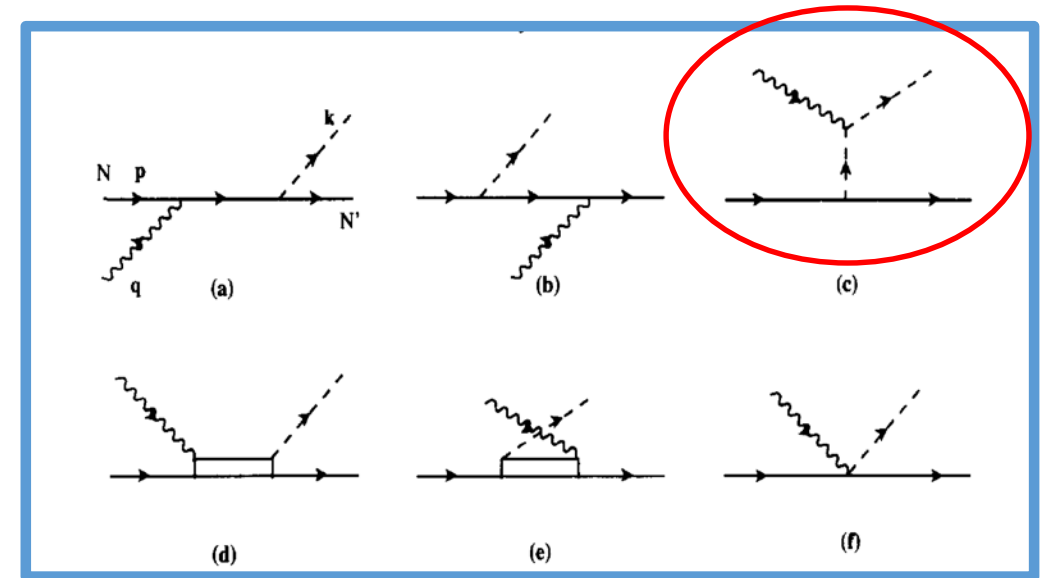


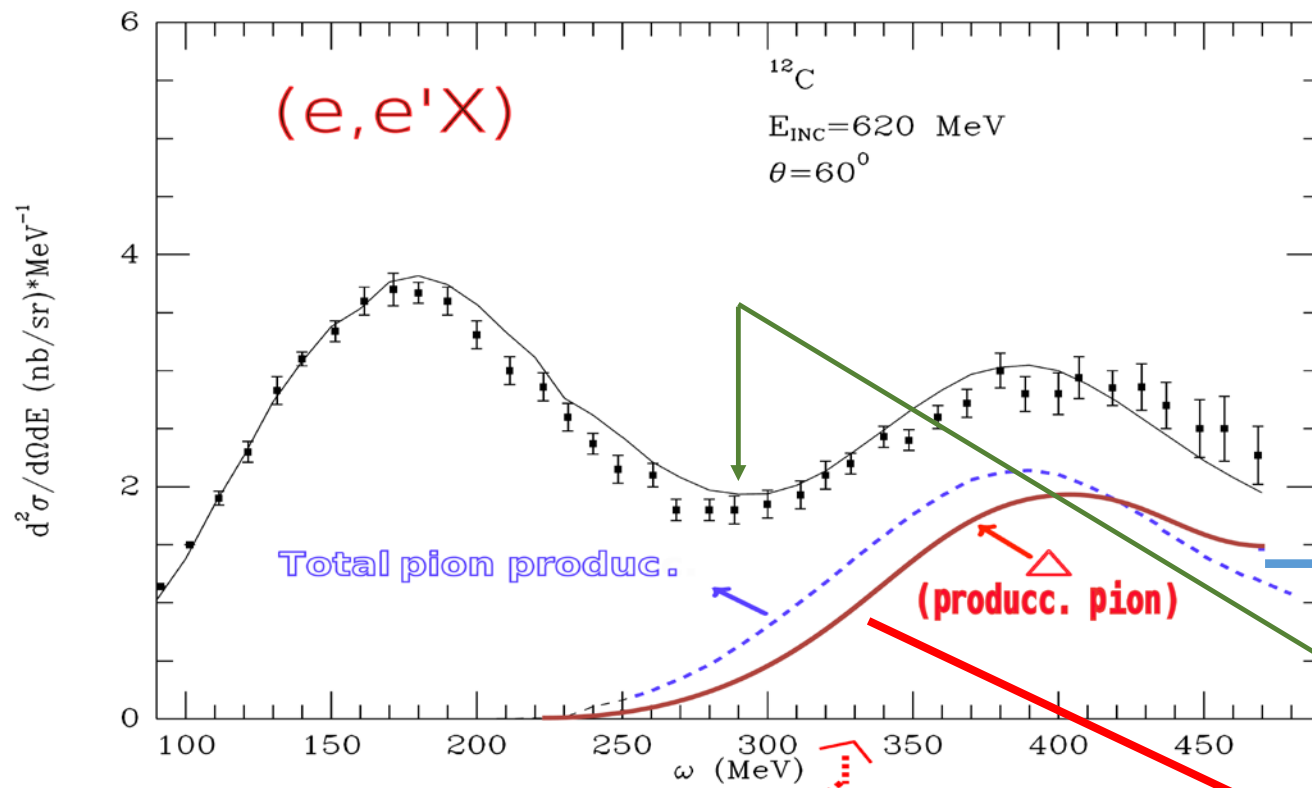


$$\gamma^* N \rightarrow \pi N$$

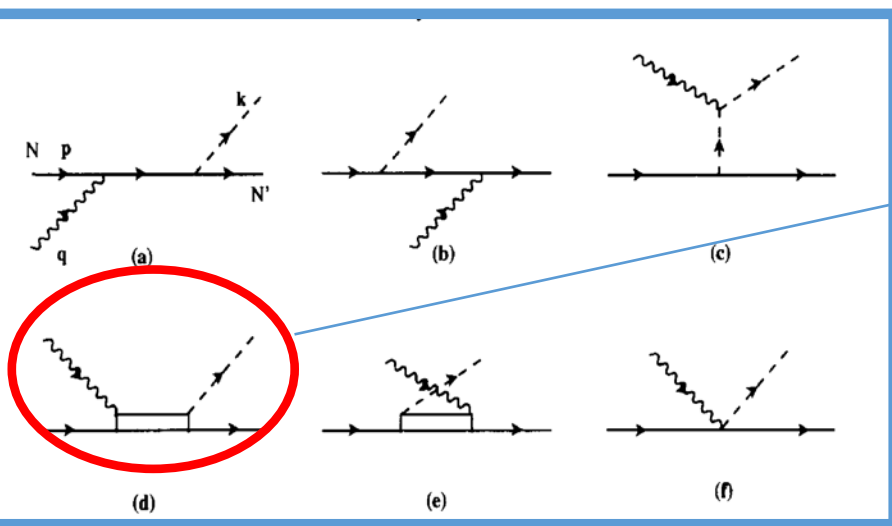
Meson Exchange Contribution

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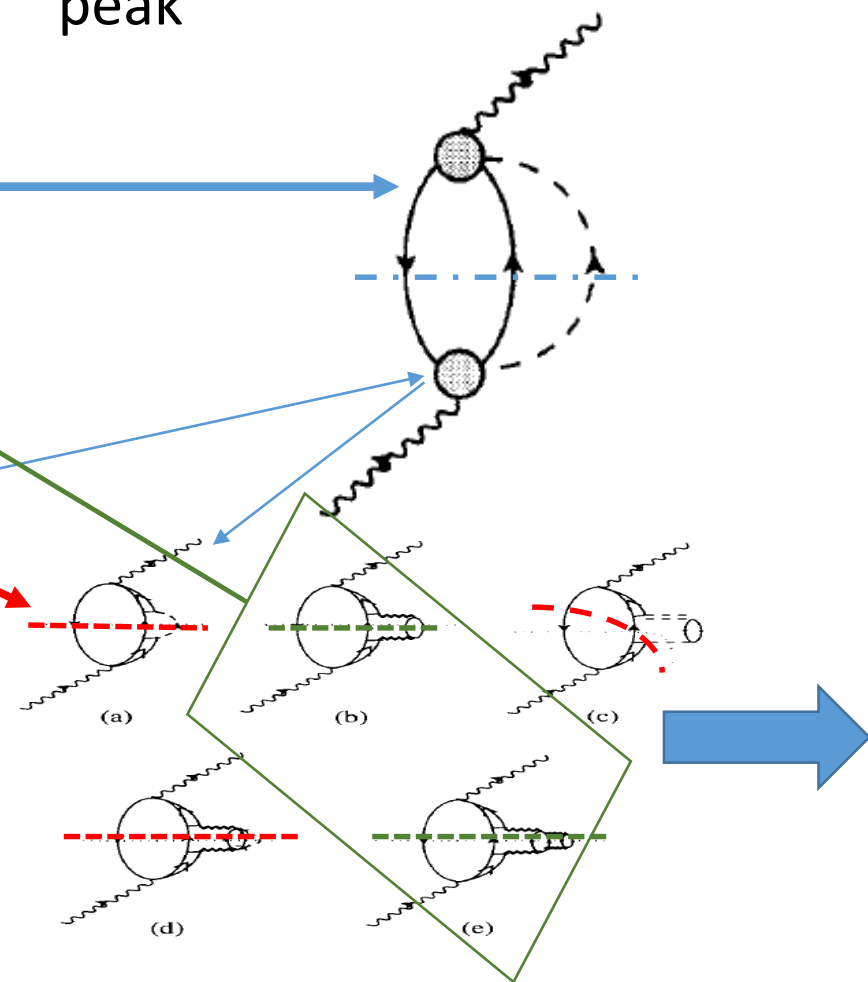


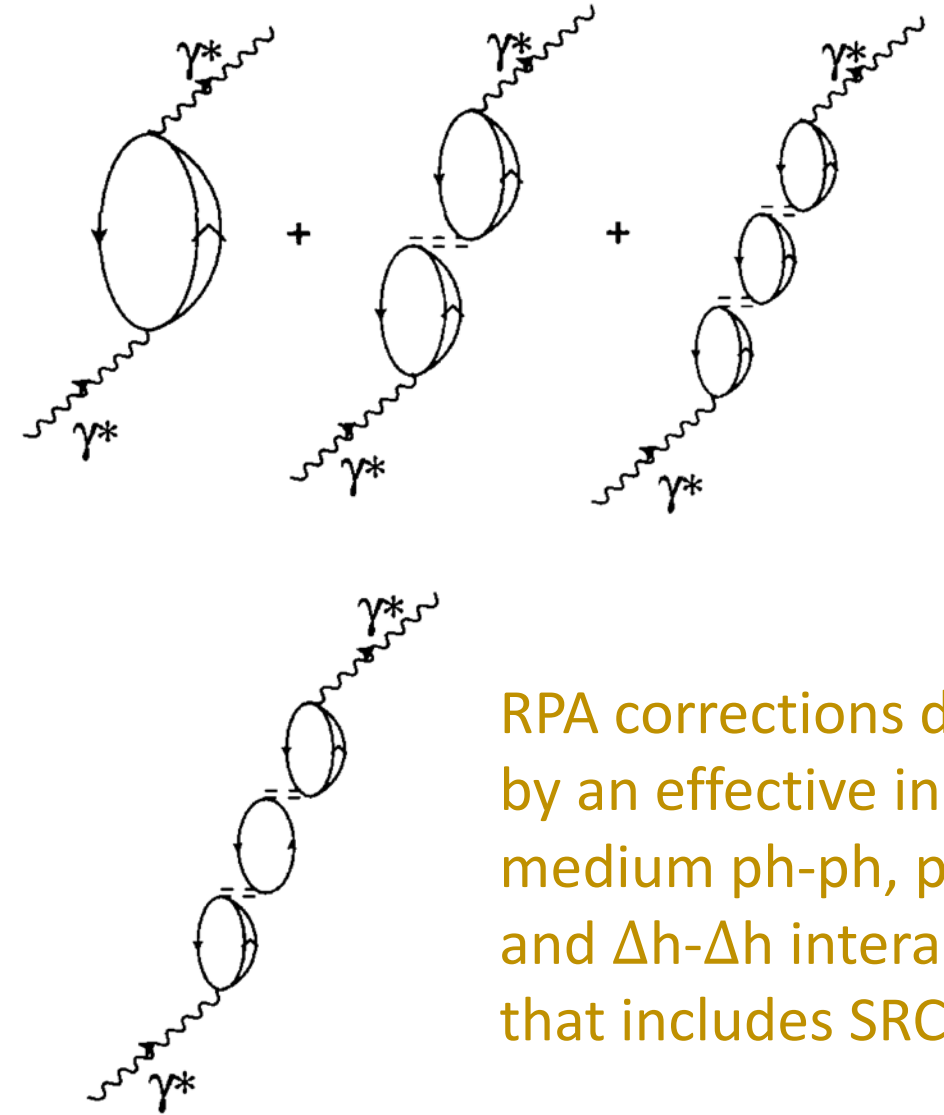
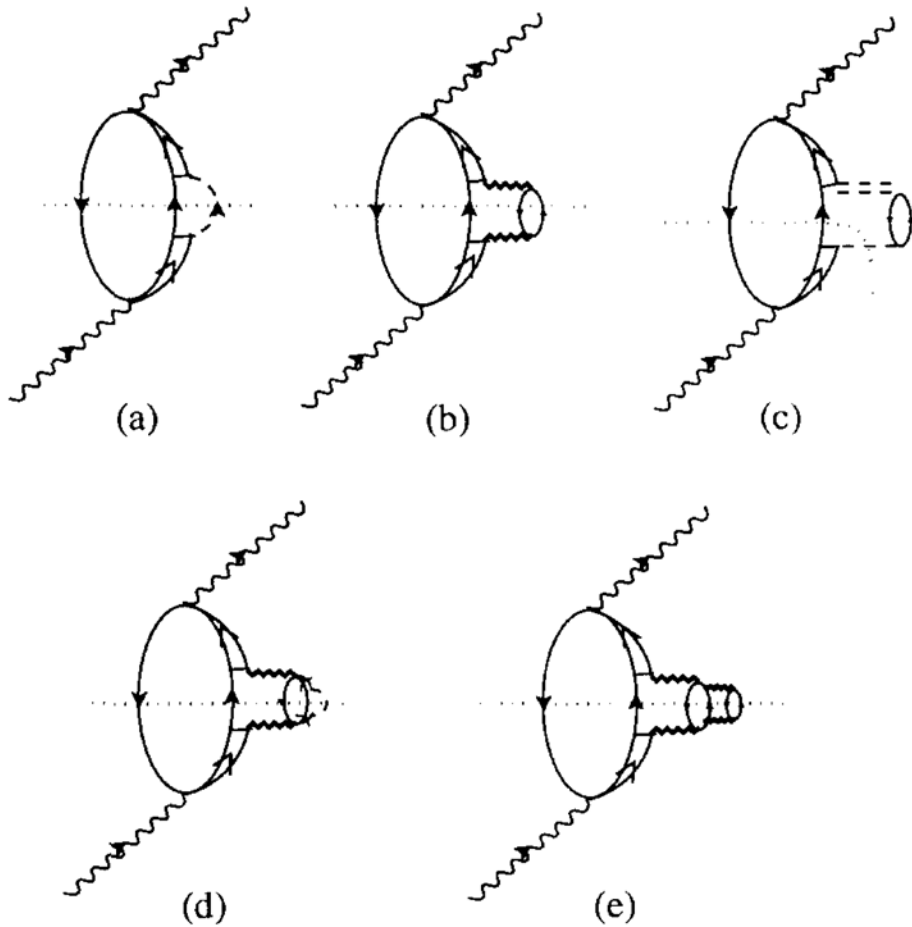
- Δ dominant component of the pion production contribution
- Missing strength both at the dip region and the Δ peak



one of the terms generates the Δ contribution

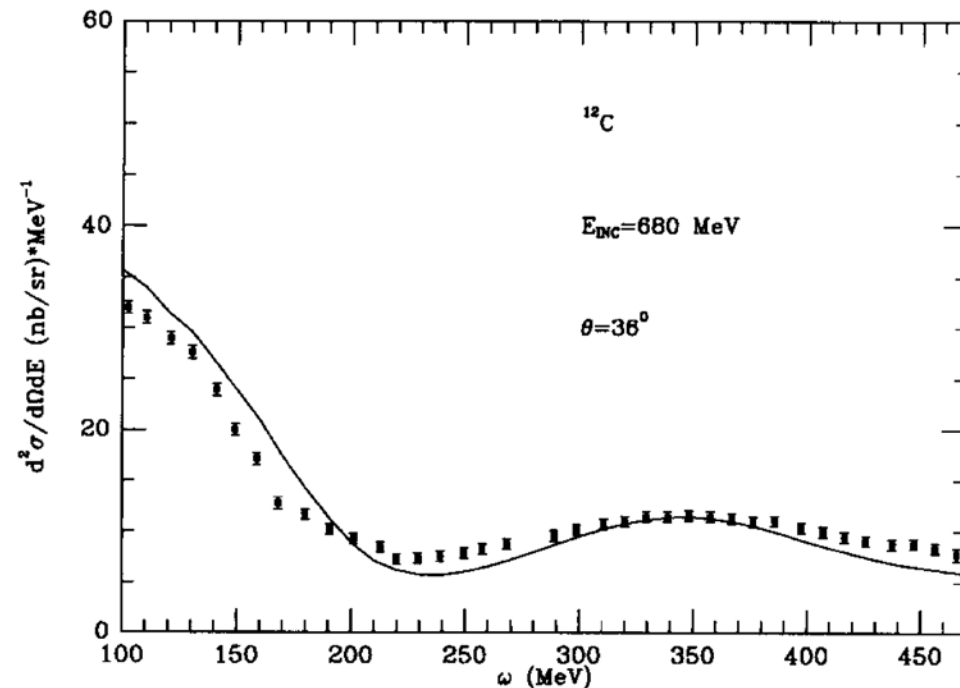
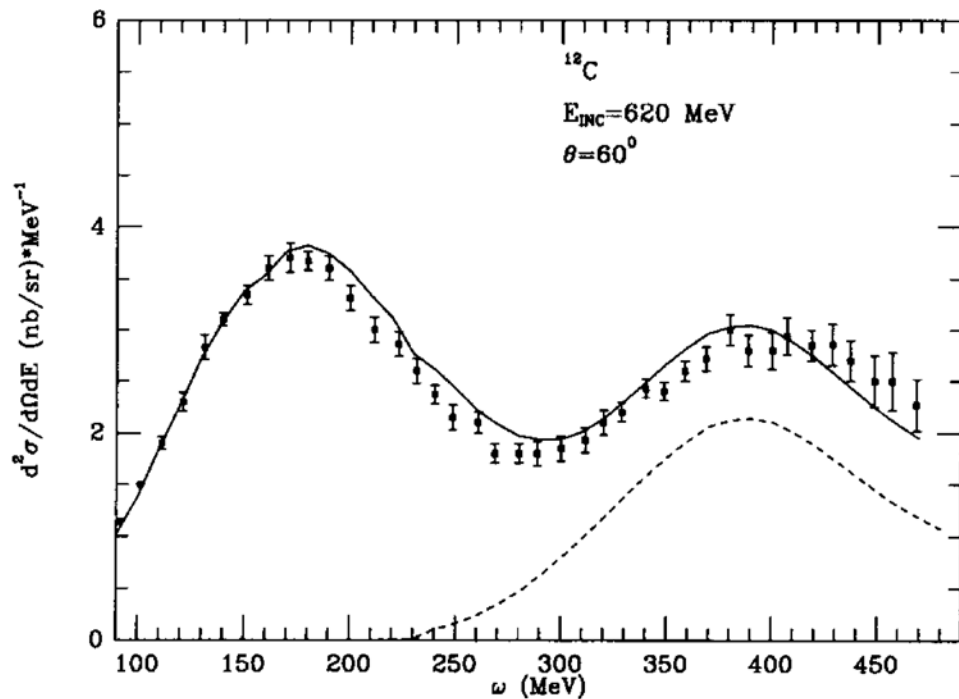
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RPA corrections driven
by an effective in
medium ph - ph , ph - Δh
and Δh - Δh interaction
that includes SRC

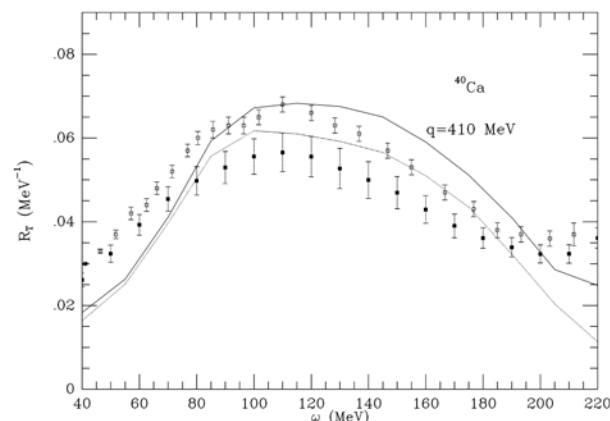
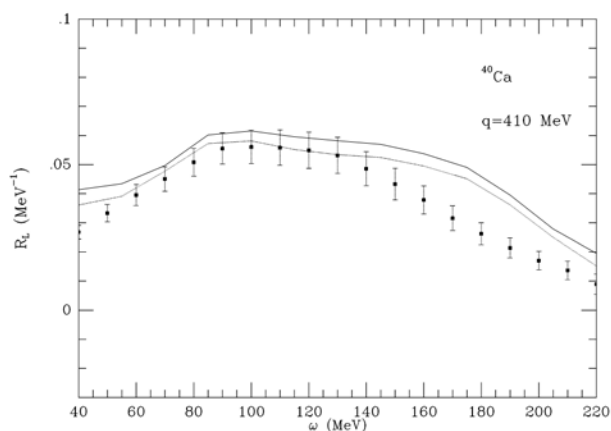
pionless Δ decay modes:
Oset+Salcedo, NPA 468 (1987) 631



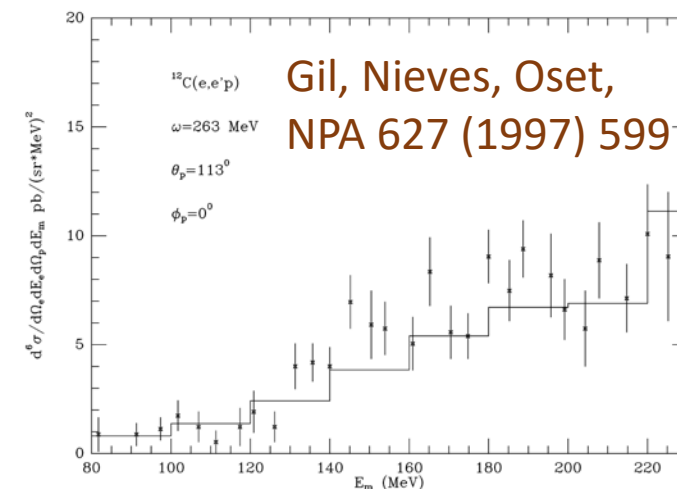
$^{12}\text{C} (e, e' X)$

Gil, Nieves, Oset,
 NPA 627 (1997) 543

and by means of a **Monte Carlo simulation** we obtain cross sections for the processes $(e, e'N)$, $(e, e'NN)$, $(e, e'\pi)$, ...



R_L and R_T QE response functions for $e + ^{40}\text{Ca} \rightarrow e' + X$



Gil, Nieves, Oset,
 NPA 627 (1997) 599

$^{12}\text{C} (e, e'p)$

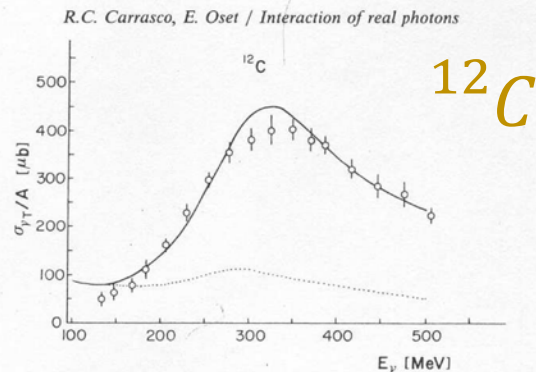


Fig. 45. Results for σ_A/A as a function of the photon energy for ^{12}C . Experiment from ref. ⁶⁾. The lower curve is the result for direct photon absorption.

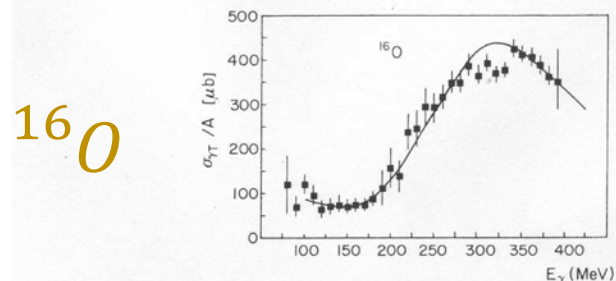


Fig. 46. Results for σ_A/A as a function of the photon energy for ^{16}O . Experiment from ref. ⁵⁾.

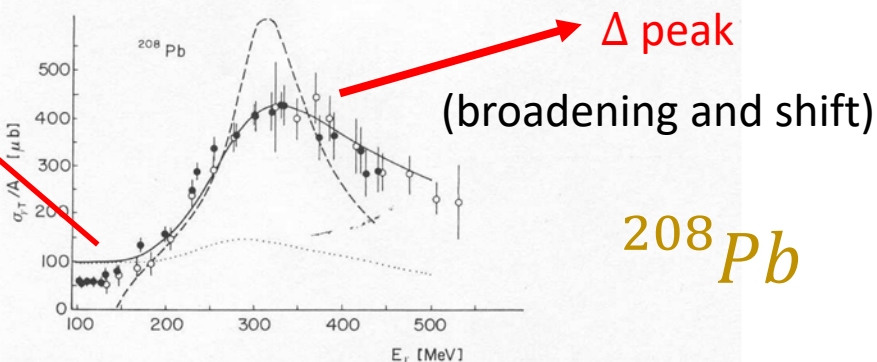


Fig. 47. Continuous line: results for σ_A/A as a function of the photon energy for ^{208}Pb . The dashed line shows the impulse approximation result $(Z\sigma_{\gamma p} + N\sigma_{\gamma n})/A$ for comparison. The dotted line is the result for direct photon absorption. Experimental data: dark dots from ref. ³⁾, while dots from ref. ⁶⁾.

$$\frac{d^2\sigma}{d\Omega dp}$$

Carrasco+Oset+Salcedo, NPA 541
(1992) 583

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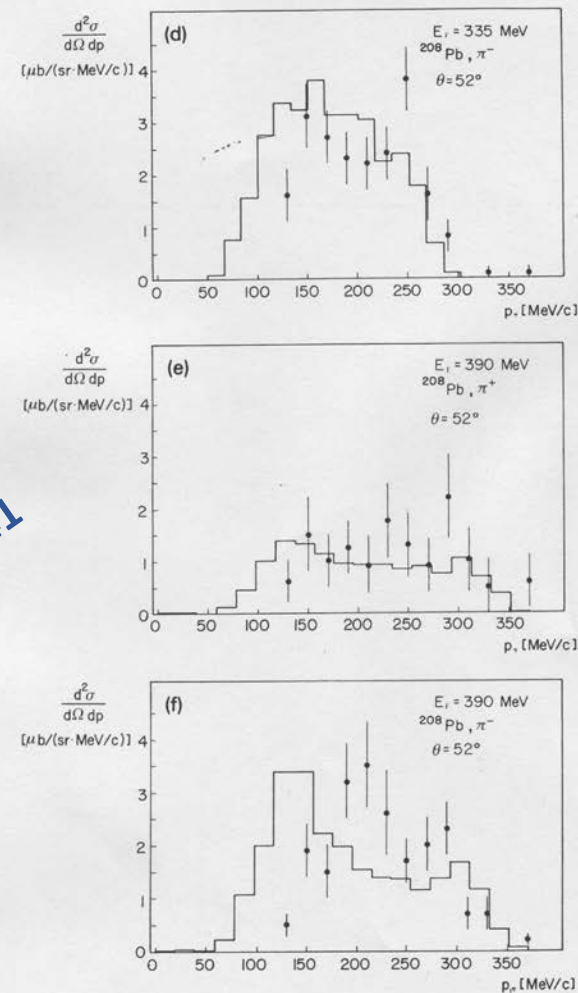
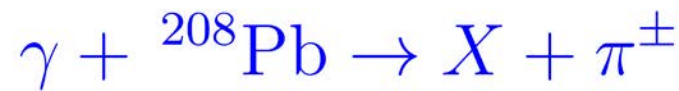
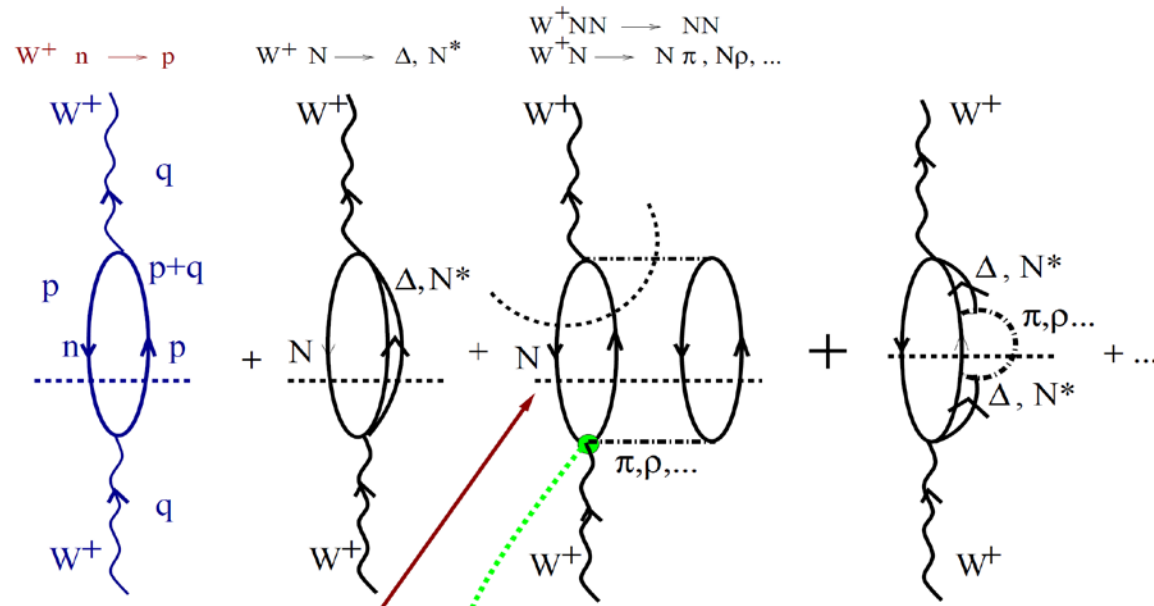


Fig. 17—continued.



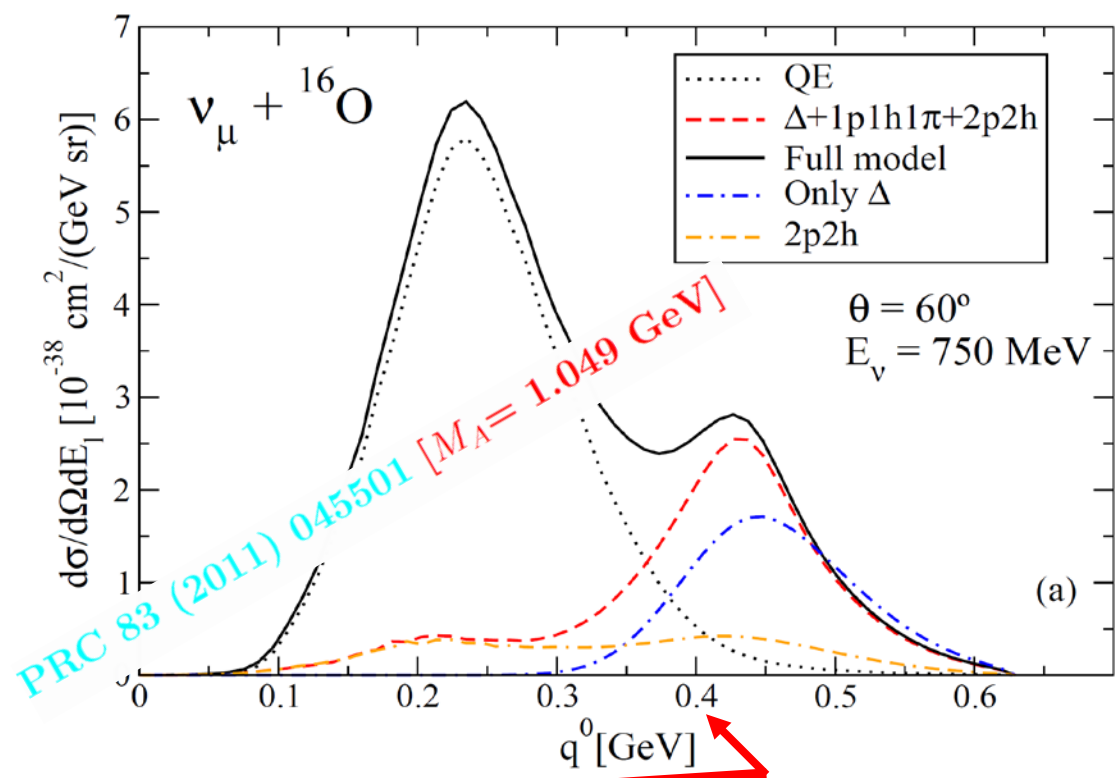
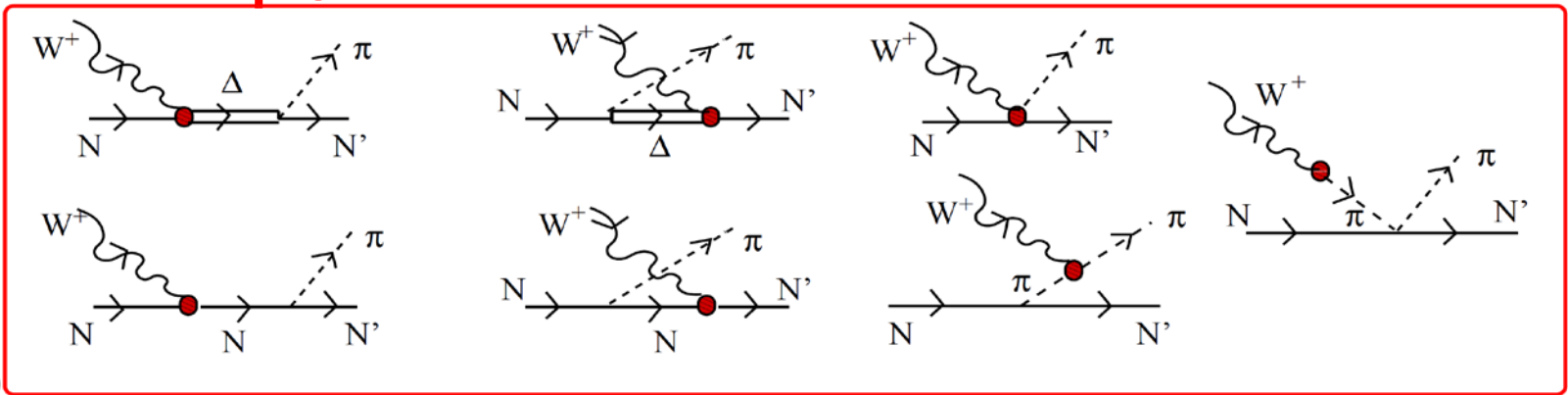
$\nu + A \rightarrow l + X$



MEC $\rightarrow$ QE like !

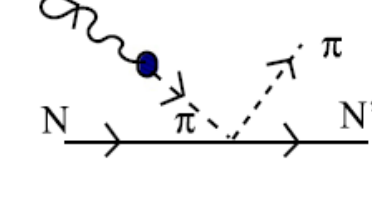
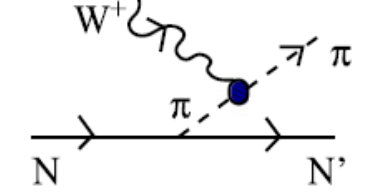
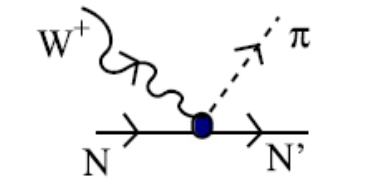
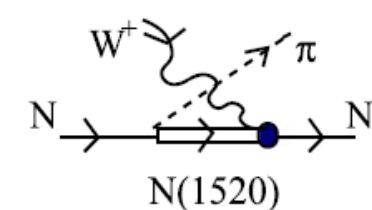
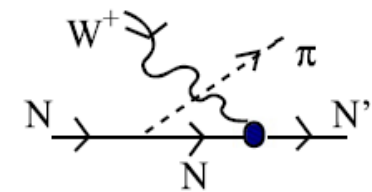
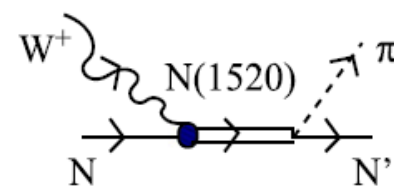
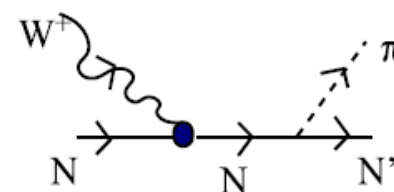
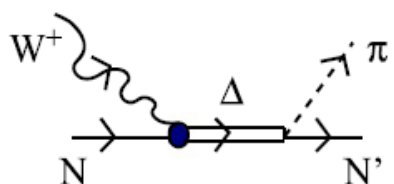
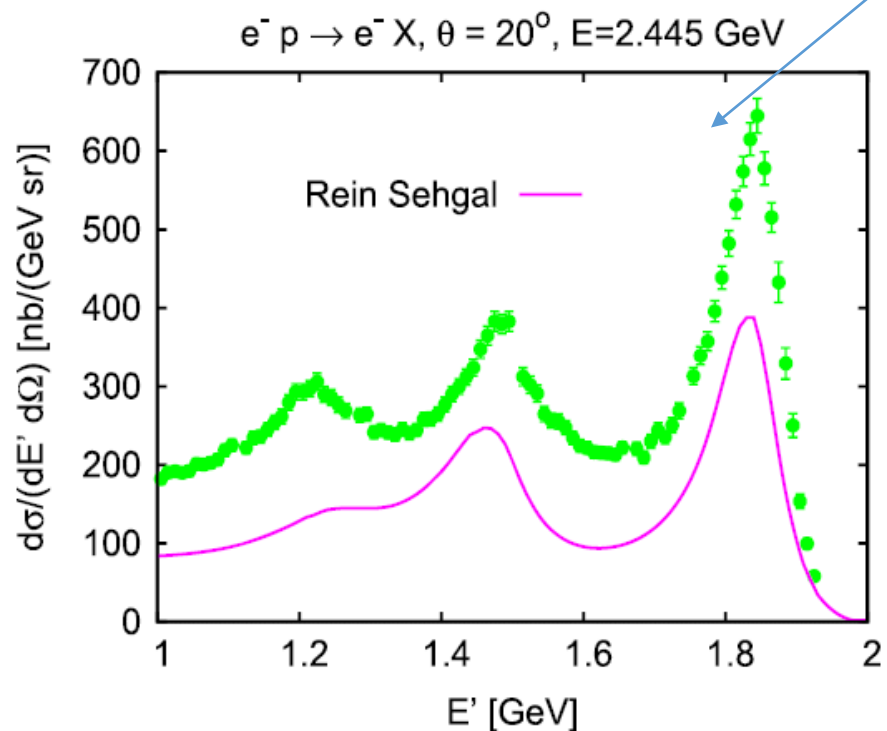
PRD D76 (2007) 033005
 PRD D81 (2010) 085046

+ PRD 93 (2016) 014016 (Watson's theorem)
 + PRD 95 (2017) 053007 (local terms in Δ propagator)



Neutrino Resonance Production

Deficiencies of the Rein Sehgal model ! $\Rightarrow$ Improved models



Electron data $\Rightarrow$ Resonance vector form factors !

PCAC $\Rightarrow$ Resonance axial form factors !

Background: chiral symmetry (when possible !)

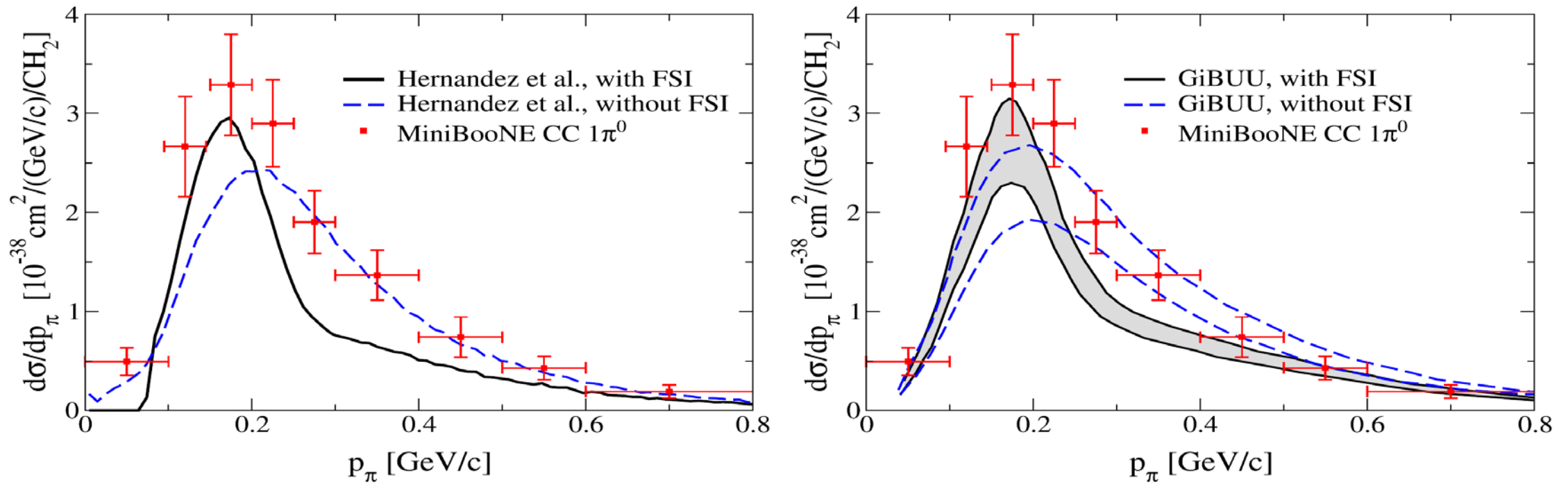
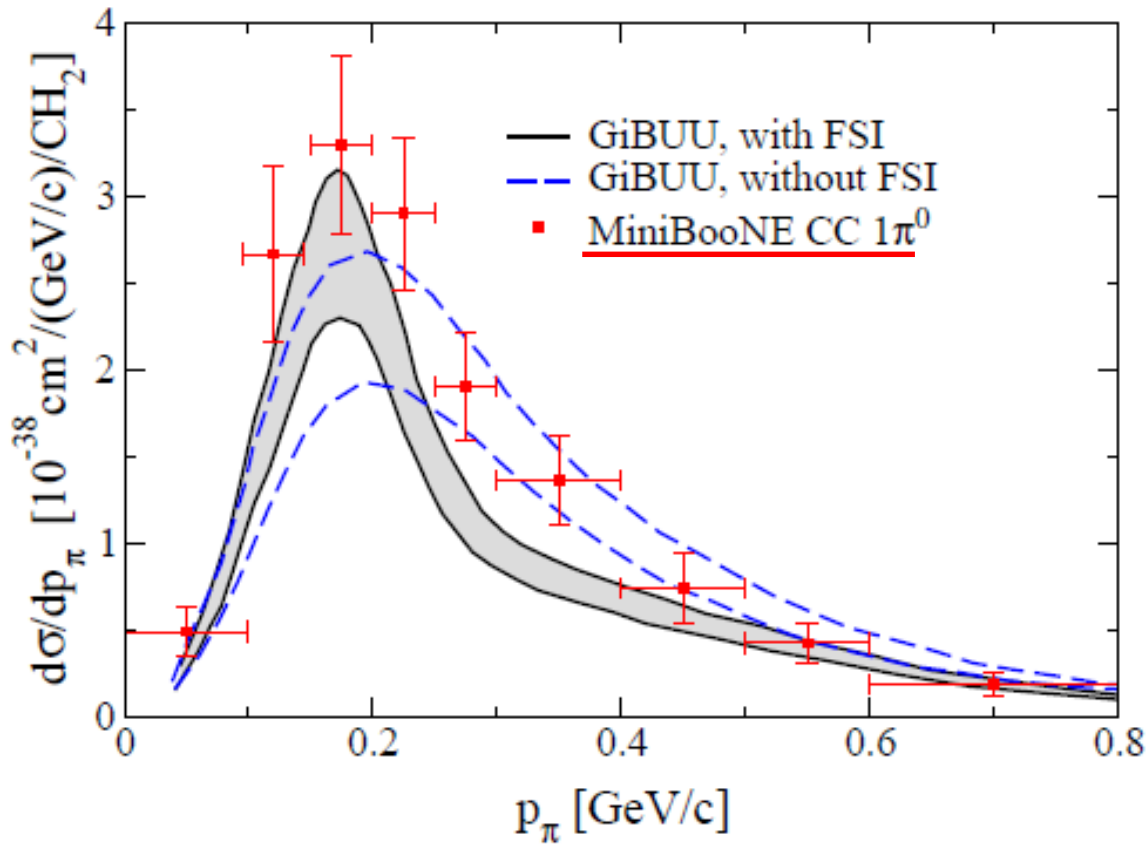


Figure 15. MiniBooNE flux-folded differential $d\sigma/dp_\pi$ cross section for $CC1\pi^0$ production by ν_μ in mineral oil. Data are from [27]. Left: predictions from the cascade approach of [184]. The solid curve corresponds to the full model and the dashed one stands for the results obtained neglecting FSI effects. Right: predictions from the GiBUU transport model of [207]. The dashed curves give the results before FSI, the solid curves those with all FSI effects included. Two different form factors $C_5^A(q^2)$, tuned to the ANL and BNL data-sets have been employed and give rise to the systematic uncertainty bands displayed in the figure.

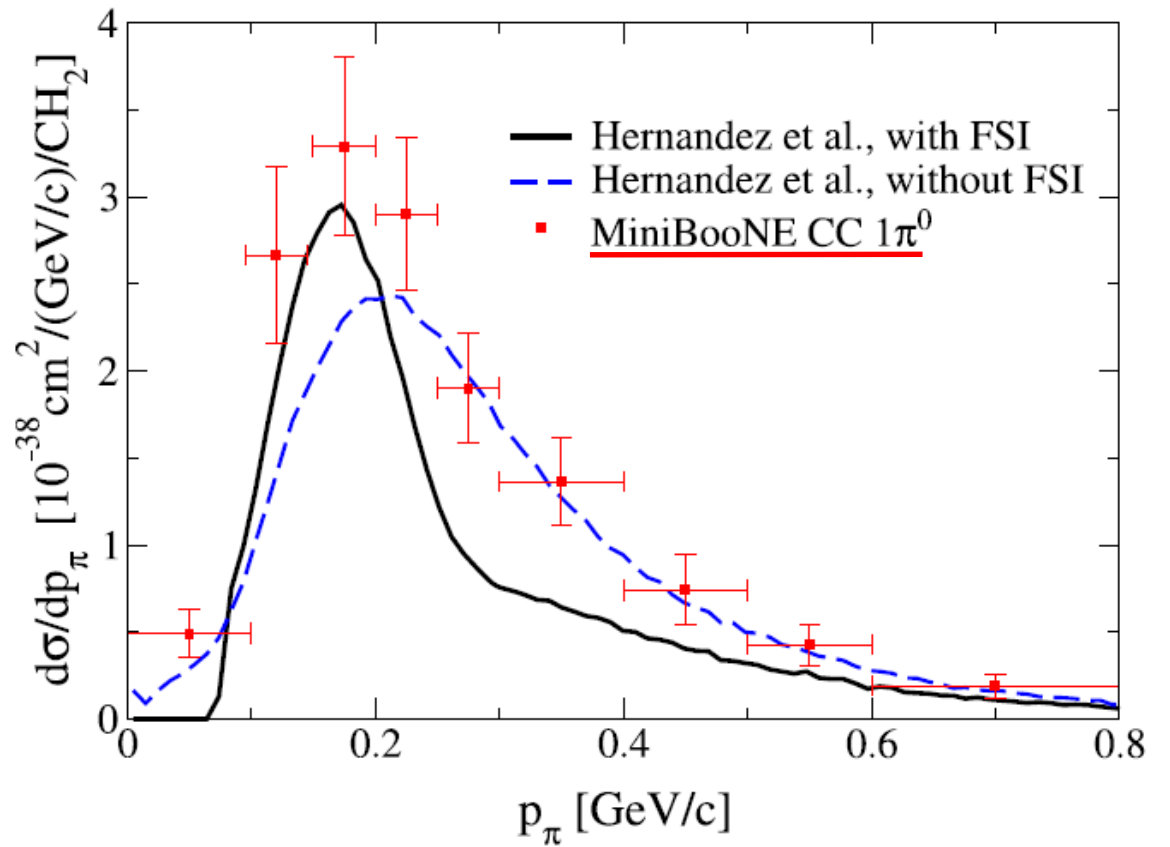
New J.Phys. 16 (2014) 075015

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There exist
some
discrepancies
between
theoretical
predictions
and data!



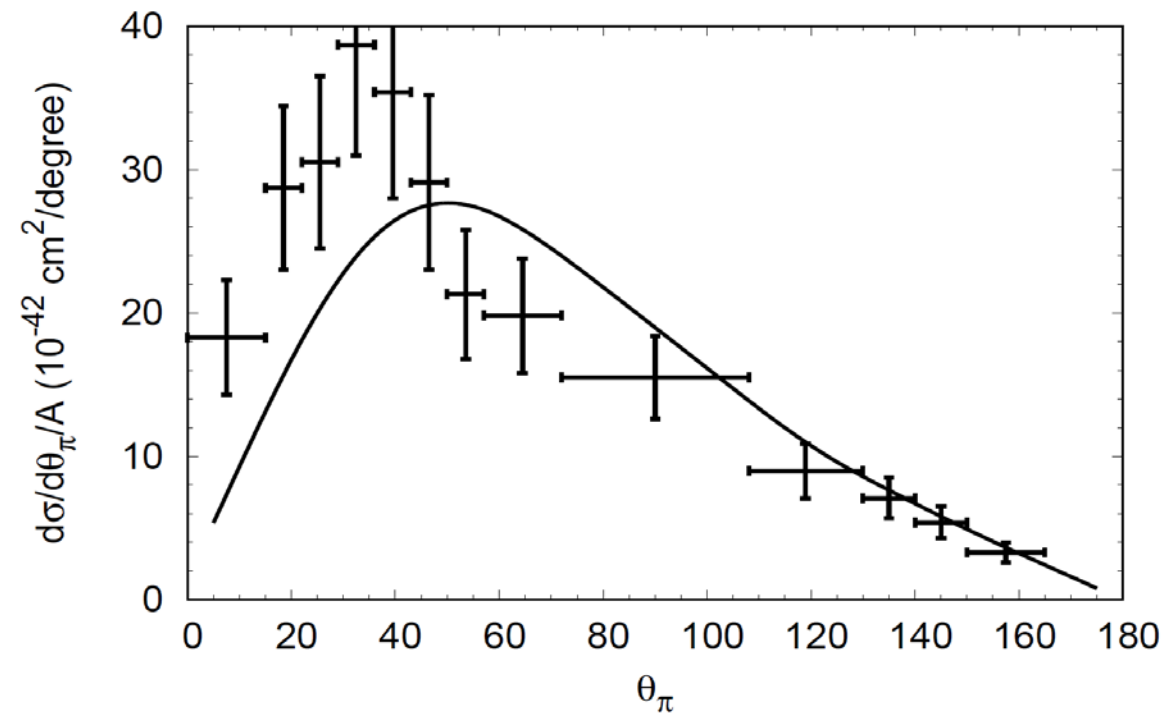
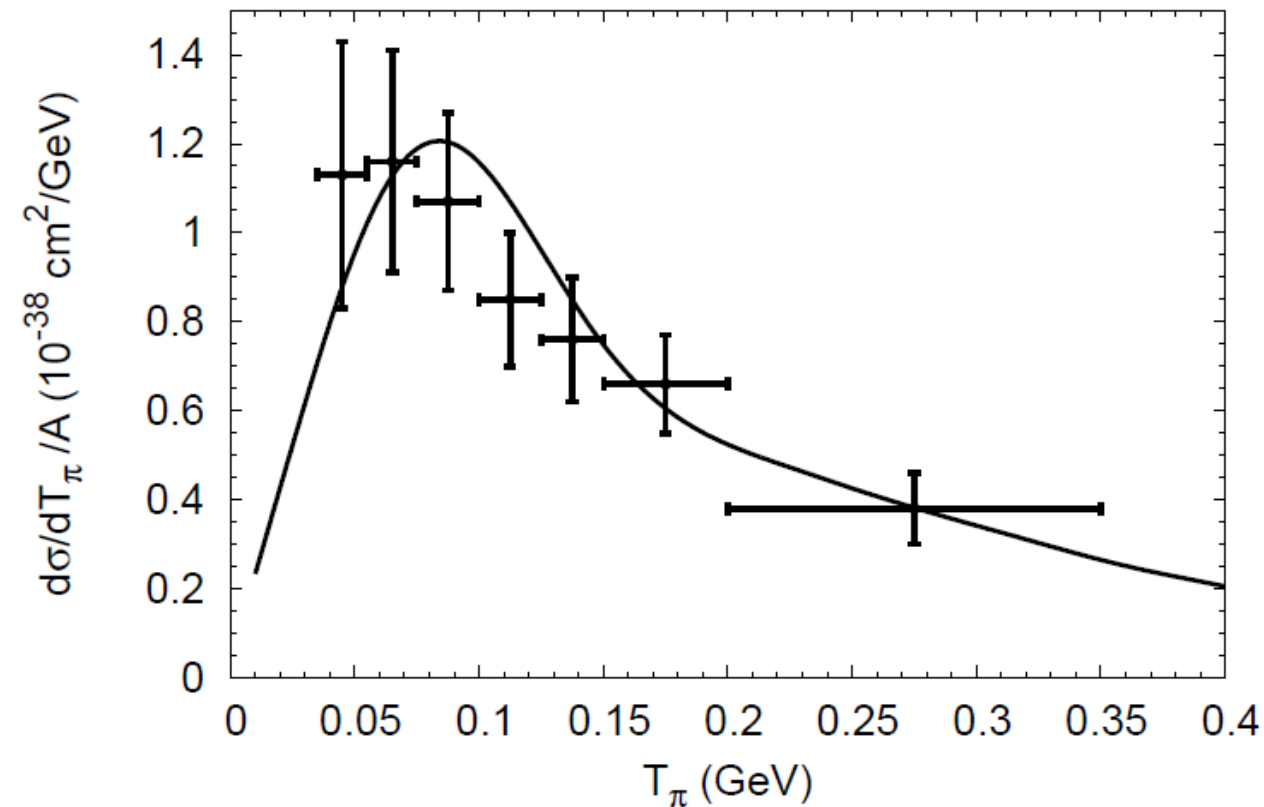
O. Lalakulich, U. Mosel, PRC 87 (2013)



E. Hernandez, J. Nieves M.J. Vicente-Vacas, PRD 87 (2013)

Problems to describe pion production in nuclei (FSI, coherent production ...)  **MINERvA and T2K will shed light**

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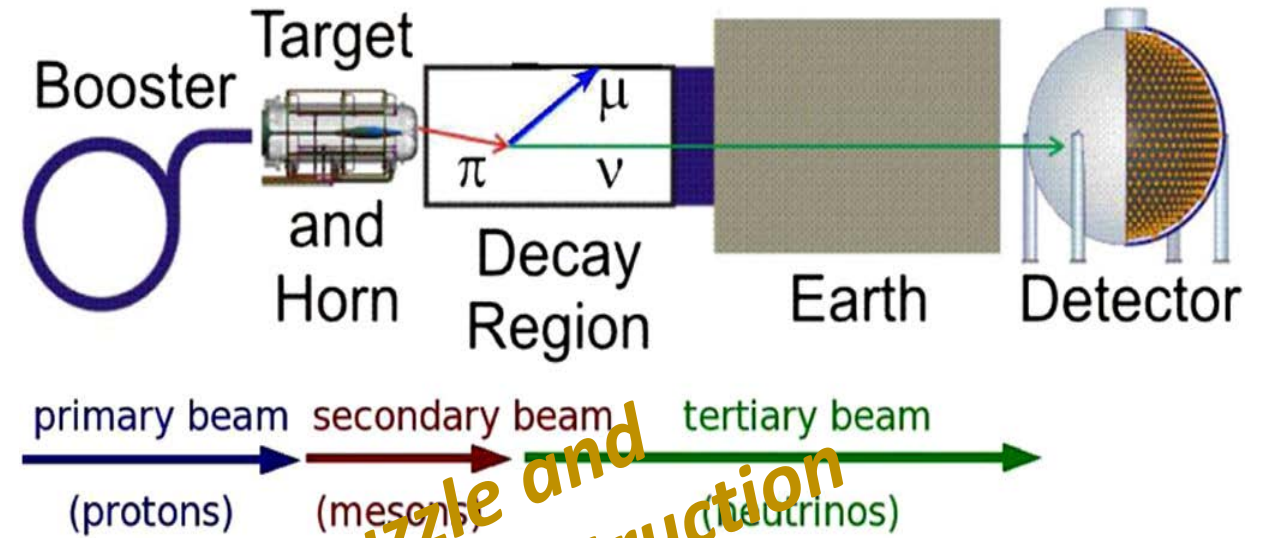
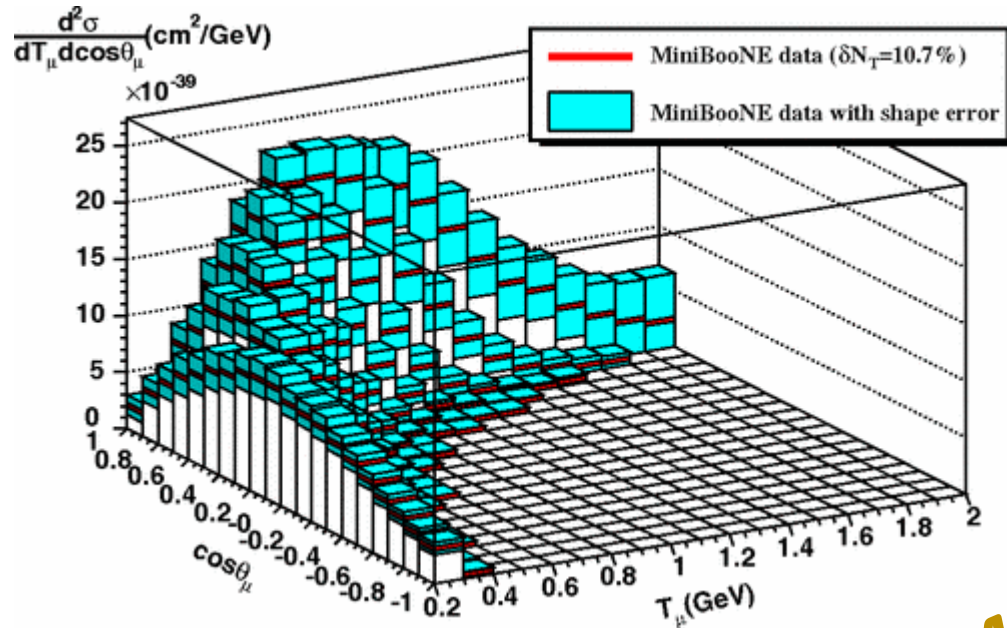
U. Mosel and K. Gallmeister (GiBUU), 1702.04932: Comparison to MINERvA data with $W_{\pi N} < 1.4$ GeV



MINERvA and MiniBooNE data compatible?

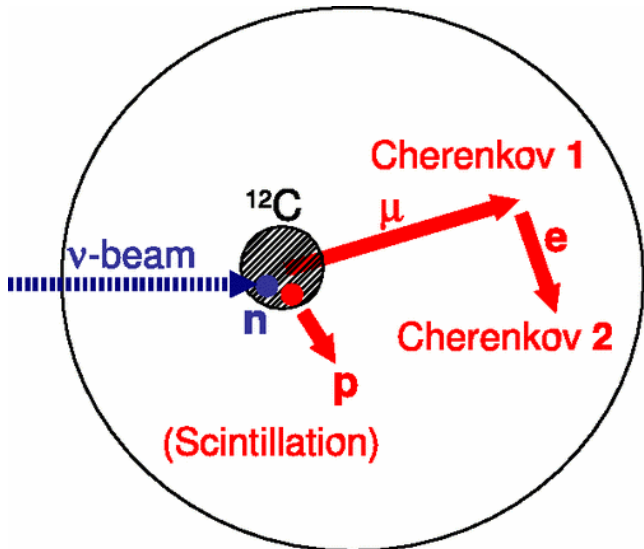
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MiniBooNE CCQE (PRD 81, 092005)



MiniBooNE M A puzzle and Neutrino energy reconstruction

The largest background is from CC single pion production: $\text{CC}1\pi^+$



$$1: \nu_\mu + n \rightarrow \mu^- + p$$

$$2: \hookrightarrow e^- + \bar{\nu}_e + \nu_\mu$$

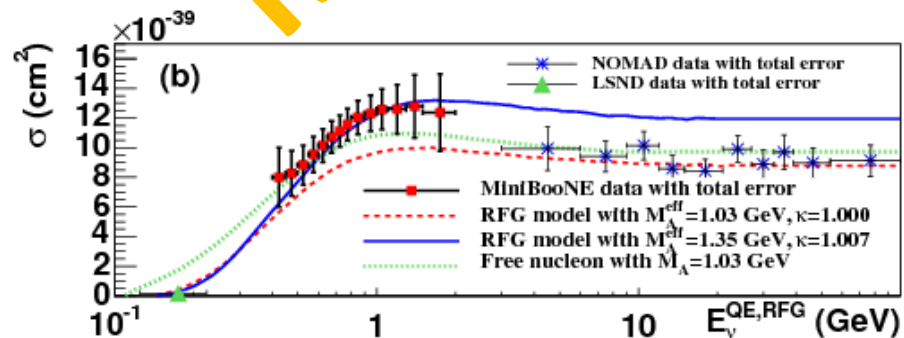
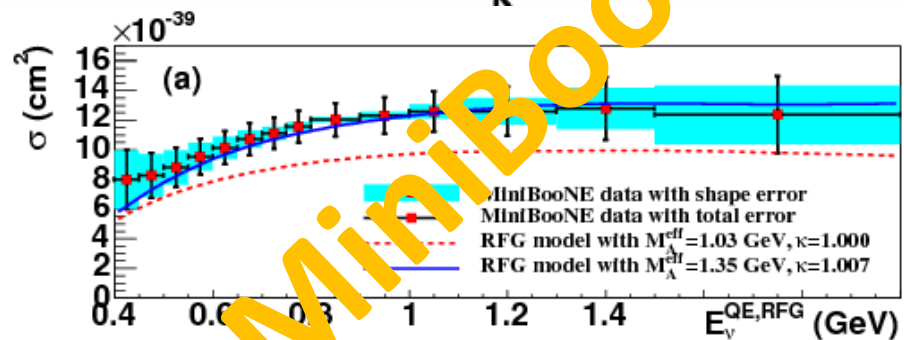
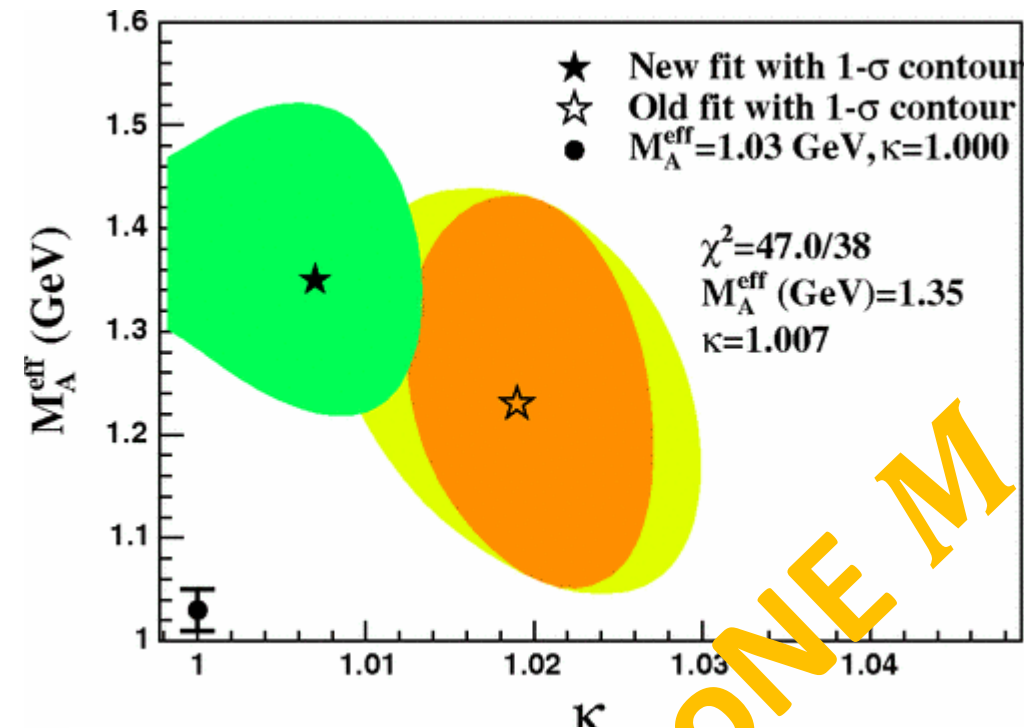
1 muon events !

$$1: \nu_\mu + p(n) \rightarrow \mu^- + p(n) + \pi^+ \hookrightarrow \mu^+ + \nu_\mu$$

$$2: \hookrightarrow e^- + \bar{\nu}_e + \nu_\mu$$

$$3: \hookrightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

2 muon events

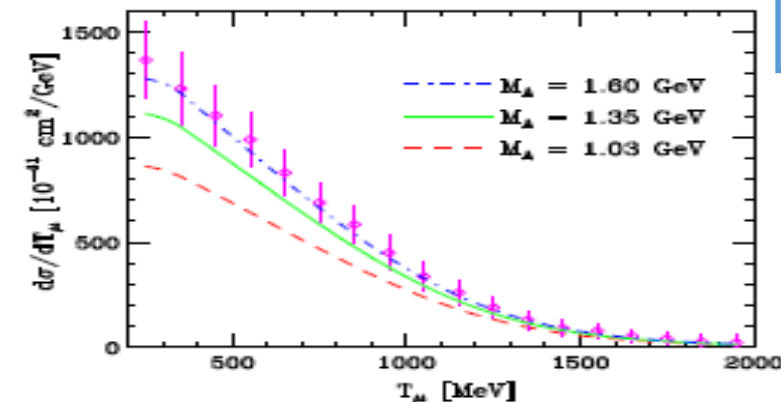


$$M_A^{\text{eff}} = 1.35 \text{ GeV}$$

vs

1.03 GeV (world avg)

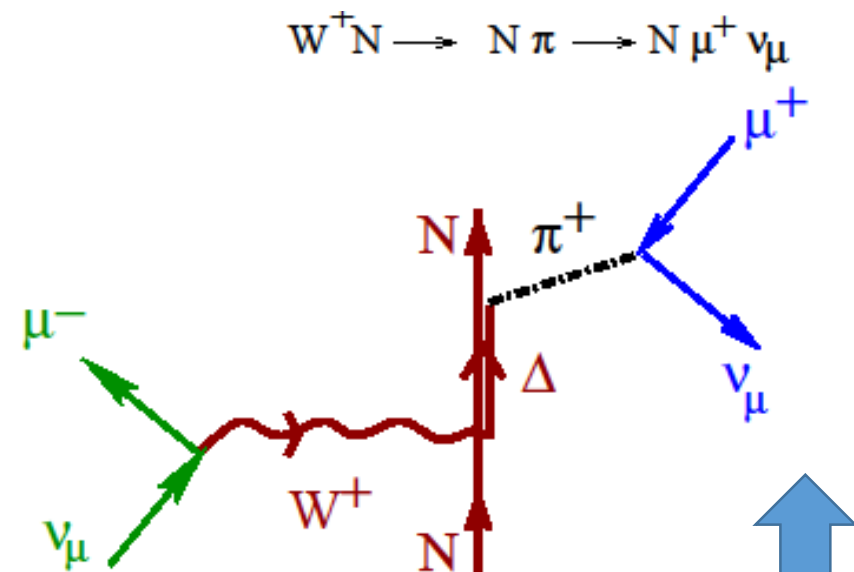
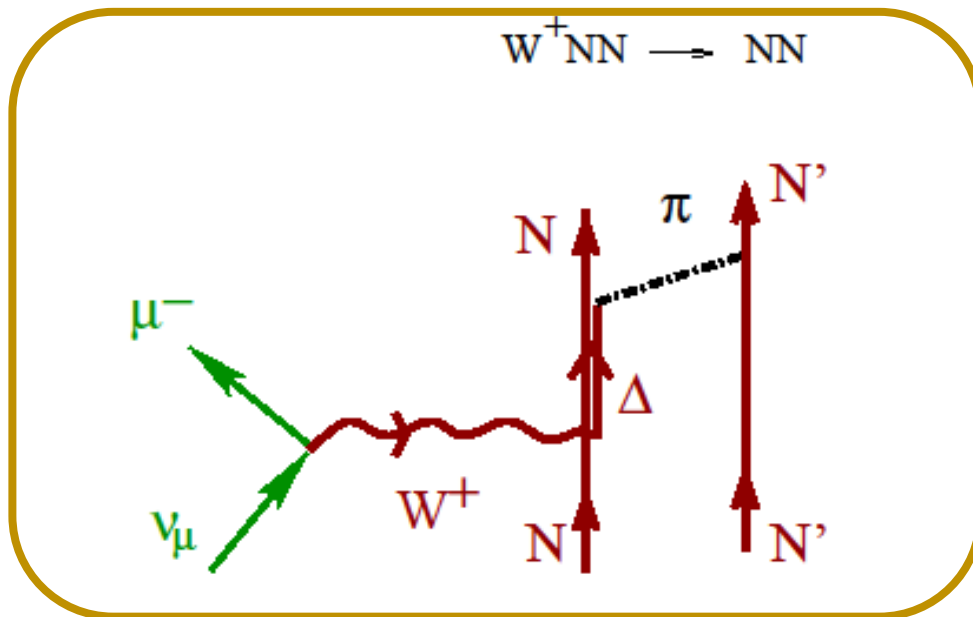
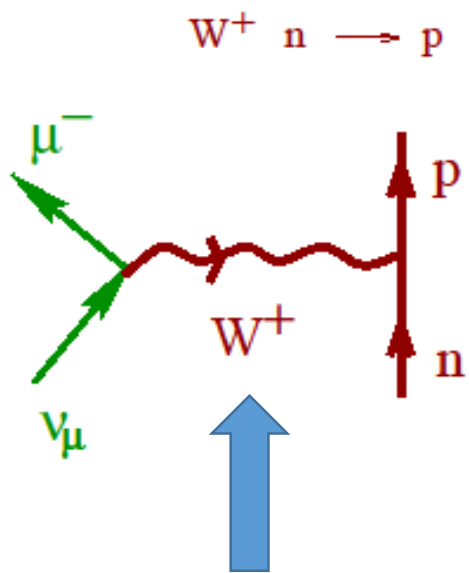
confirmed by many other groups,
for instance by Benhar et al. (PRL
105, 132301)



ChPT $O(p^3)$ + single pion electroproduction data: $M_A = 1.014 \pm 0.016$ GeV (V. Bernard, N. Kaiser, and U. G. Meissner, PRL 69, 1877 (1992))

- CCQE measurements on deuterium and, to lesser extent, hydrogen targets is $M_A = 1.016 \pm 0.026$ GeV (A. Bodek, S. Avvakumov, R. Bradford, and H. S. Budd, EPJC 53, 349 (2008))

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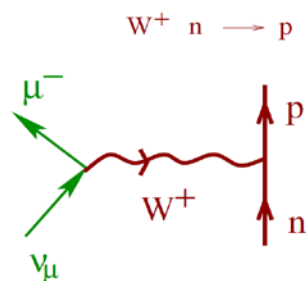
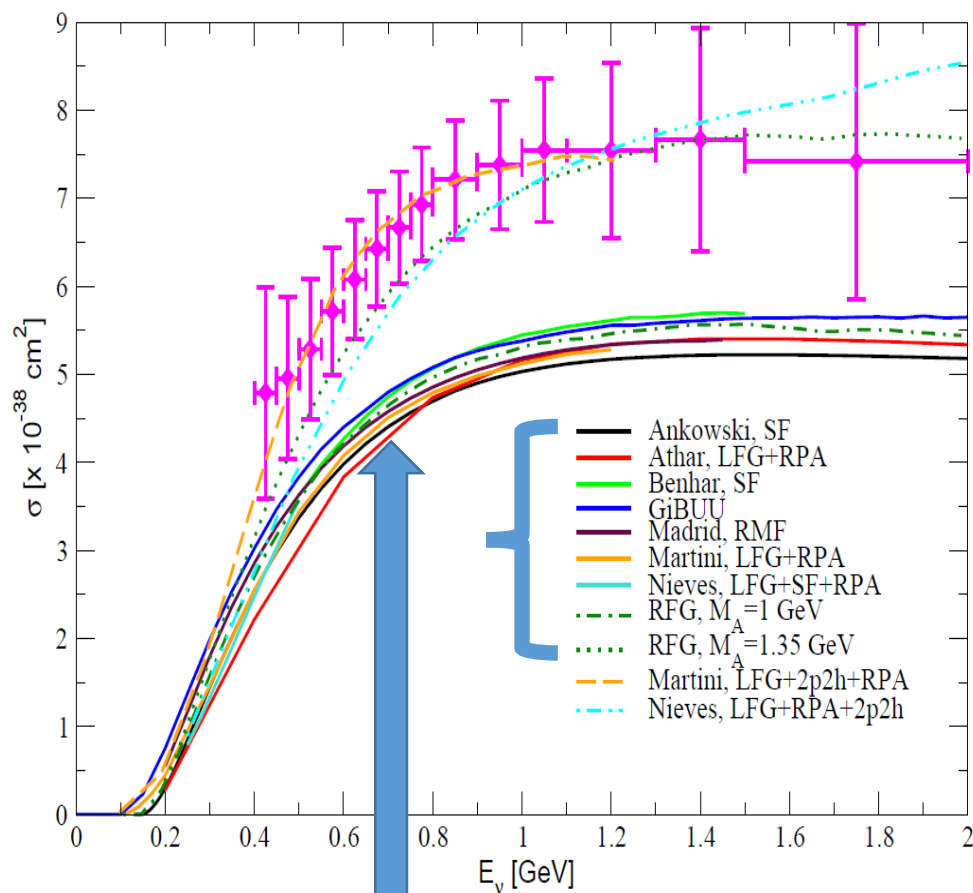


...but key observation (Martini et al., PRC 81, 045502): in most **theoretical** works QE is used for processes where the gauge boson $W^\pm$ or Z^0 is absorbed by just one nucleon, which together with a lepton is emitted.

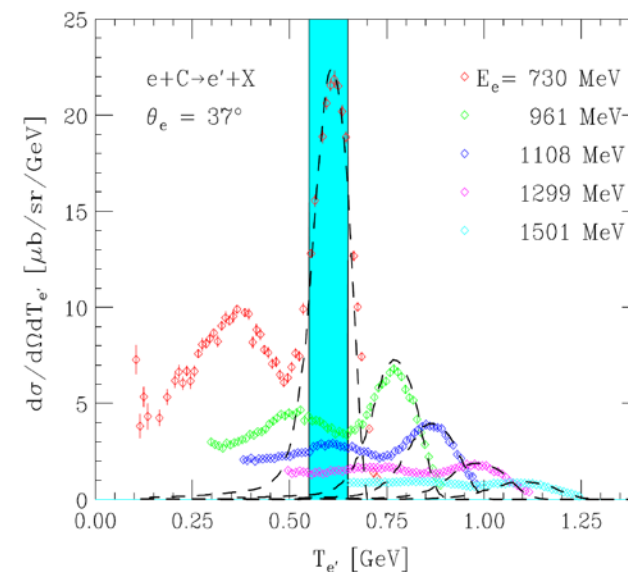
However in the recent MiniBooNE measurements, QE is related to processes in which only a muon is **detected** (ejected nucleons are not detected !) $\equiv$ **CCQE-like**
It discards pions coming off the nucleus, since they will give rise to additional leptons after their decay.

It includes multinucleon processes and others like π production followed by **absorption** (MBooNE analysis Monte Carlo corrects for these latter events).

CCQE on ^{12}C

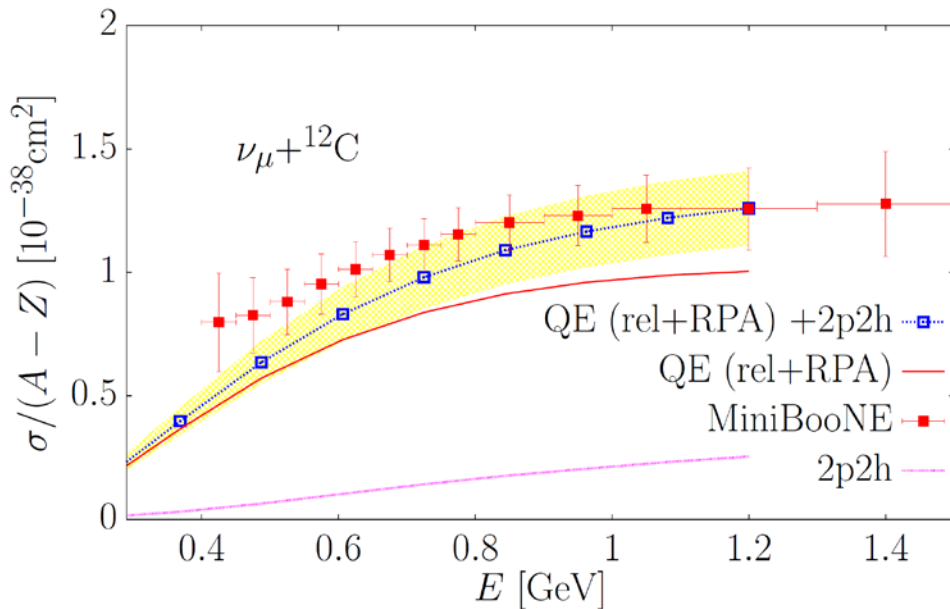
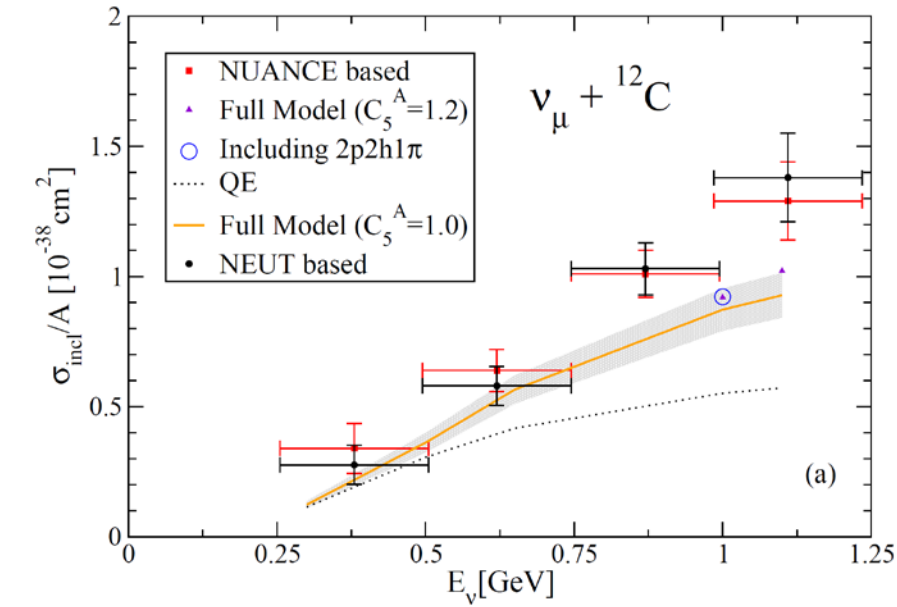


O. Benhar@NuFacT11: [arXiv : 1110.1835] measured electron-carbon scattering cross sections for a fixed outgoing electron angle $\theta = 37^\circ$ and different beam energies $\in [730, 1501]$ GeV, plotted as a function of E_e ,



The energy bin corresponding to **the top of the QE peak at $E_e = 730$ MeV** receives **significant contributions from** cross sections corresponding to different beam energies and **different mechanisms!**

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MiniBooNE CCQE-like double differential cross section $\frac{d^2\sigma}{dT_\mu d\cos\theta_\mu}$

We define a **merit function** and consider our **QE+2p2h** results

$$\chi^2 = \sum_{i=1}^{137} \left[\frac{\lambda \left(\frac{d^2\sigma^{exp}}{dT_\mu d\cos\theta} \right)_i - \left(\frac{d^2\sigma^{th}}{dT_\mu d\cos\theta} \right)_i}{\lambda \Delta \left(\frac{d^2\sigma}{dT_\mu d\cos\theta} \right)_i} \right]^2 + \left(\frac{\lambda - 1}{\Delta\lambda} \right)^2,$$

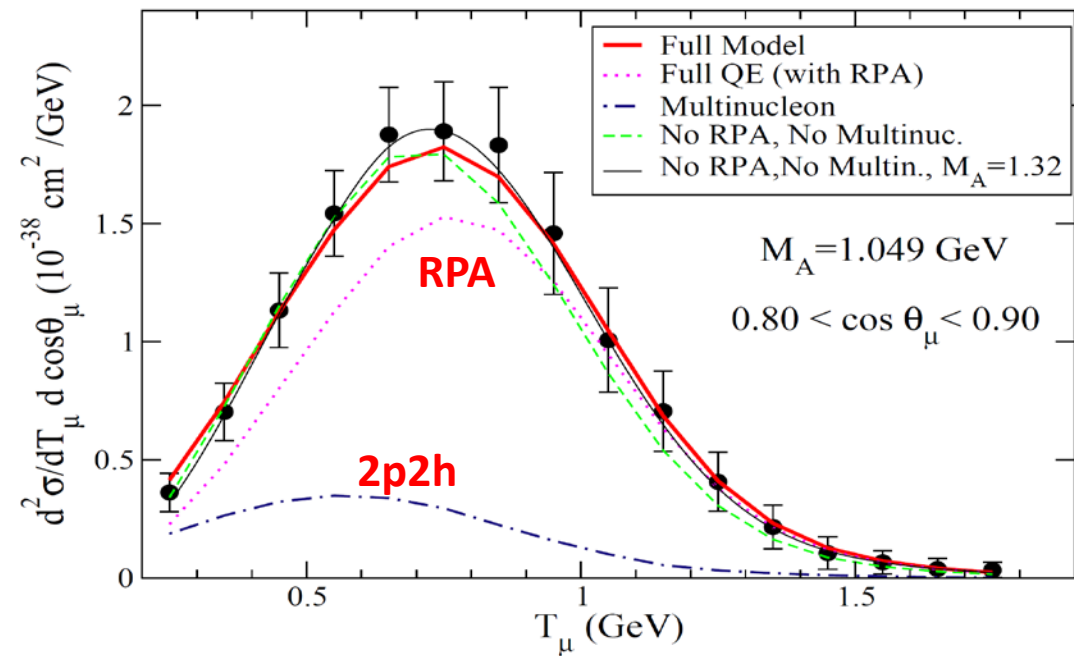
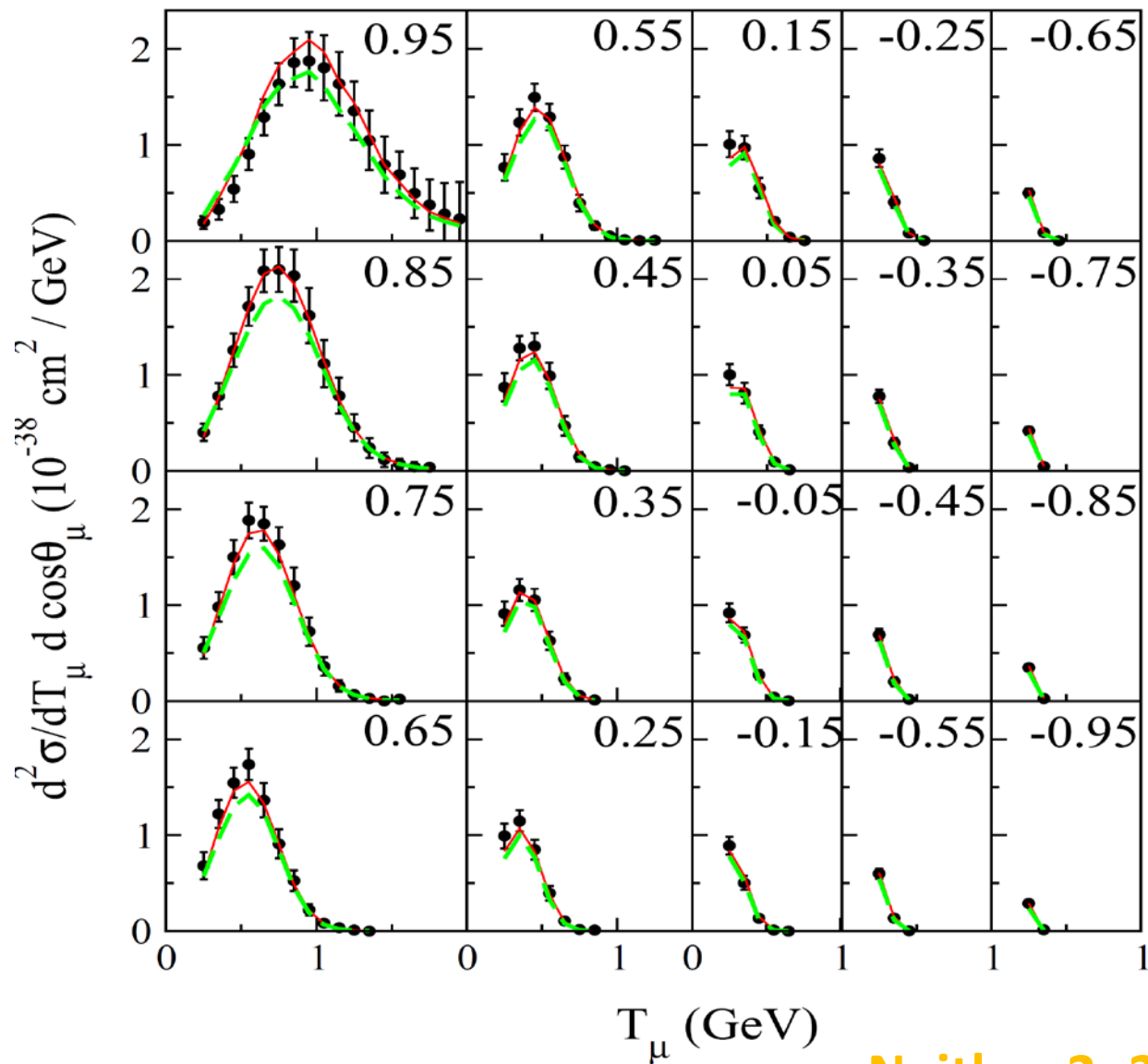
that takes into account the **global normalization uncertainty** ($\Delta\lambda = 0.107$) claimed by the MiniBooNE collaboration.

We fit λ to data with a fixed value of M_A ($=1.049$ GeV).

We obtain $\chi^2/\# \text{ bins} = 52/137$ with $\lambda = 0.89 \pm 0.01$.

The microscopical model, with no free parameters, agrees remarkably well with data! The shape is very good and χ^2 strongly depends on λ , which is strongly correlated with M_A .





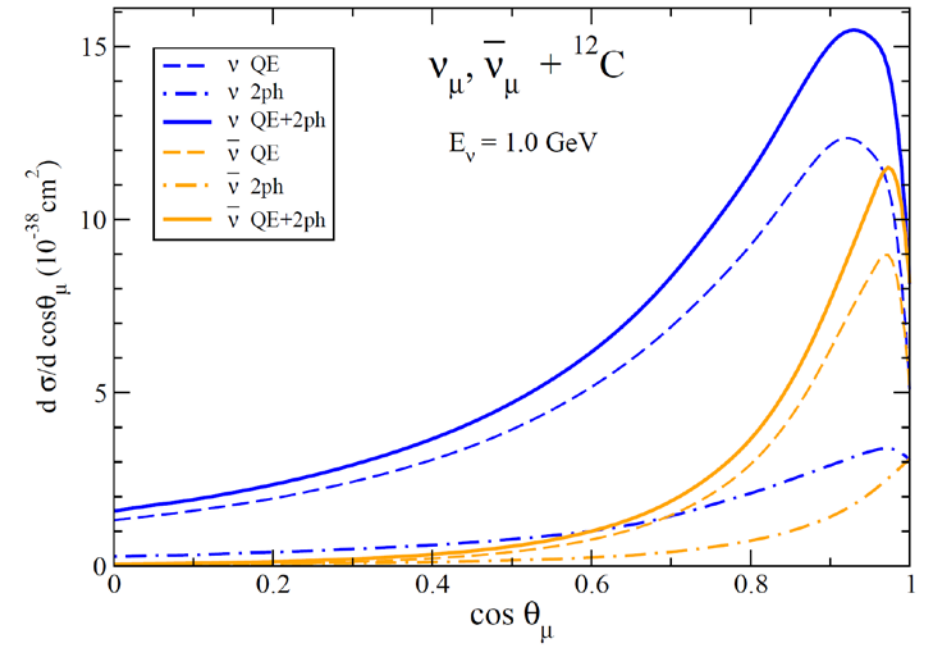
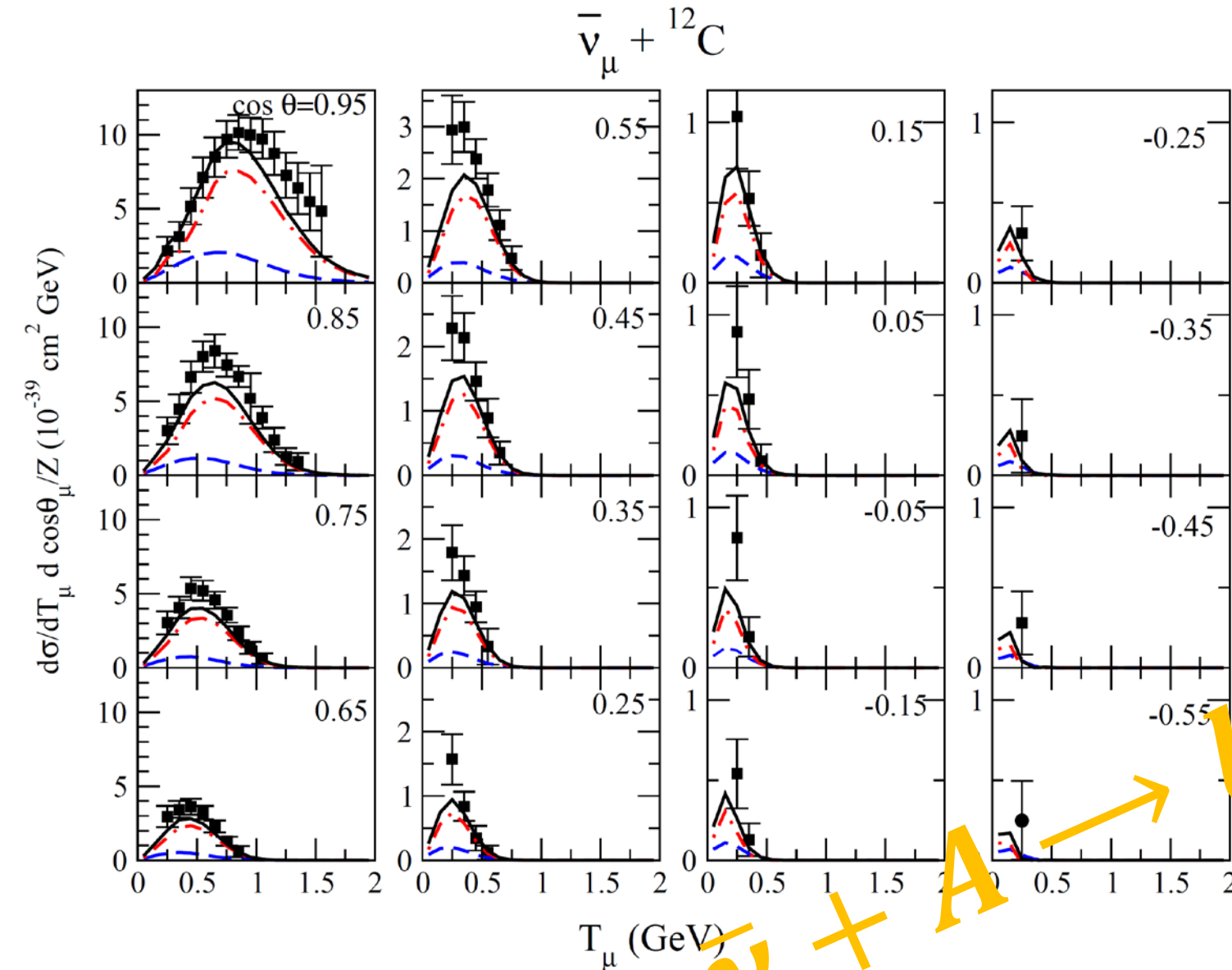
Model	Scale	M_A (GeV)	$\frac{\chi^2}{\text{\#bins}}$
LFG	0.96 ± 0.03	1.32 ± 0.03	35/137
Full	0.92 ± 0.03	1.08 ± 0.03	50/137
Full $ q > 0.4^\dagger$ GeV	0.83 ± 0.04	1.01 ± 0.03	30/123

† : As suggested by Sobczyk et al. PRC 82, 045502

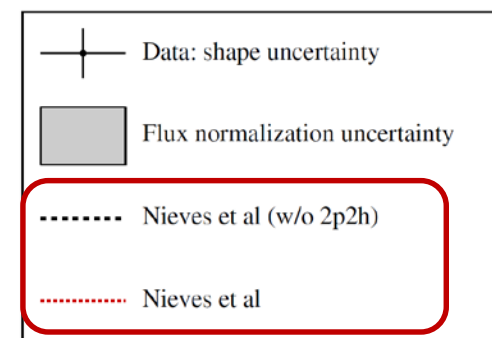
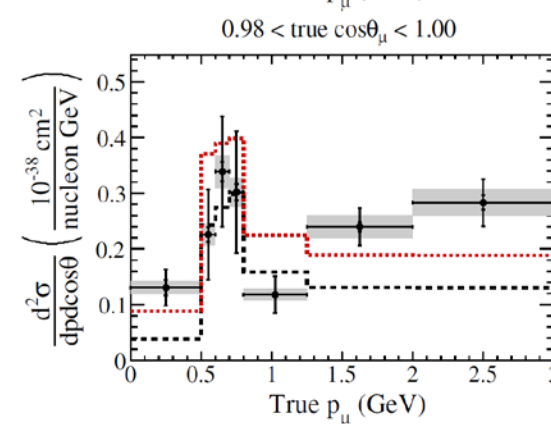
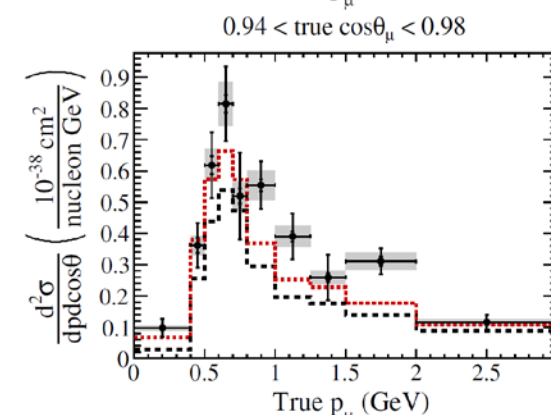
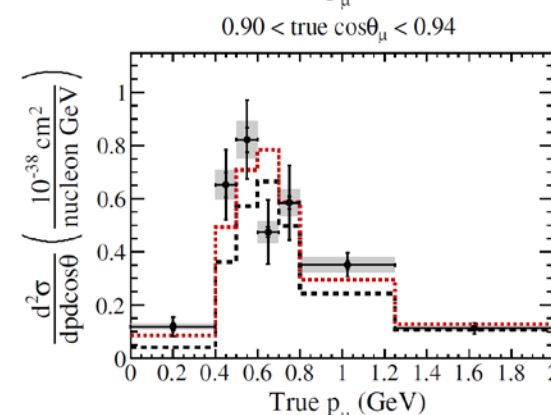
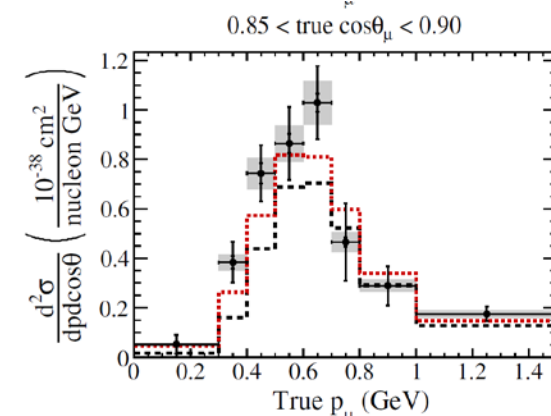
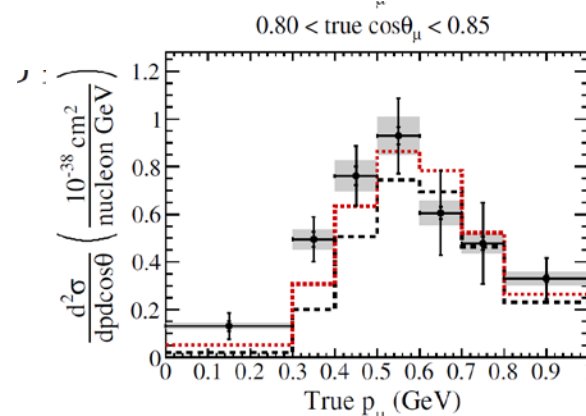
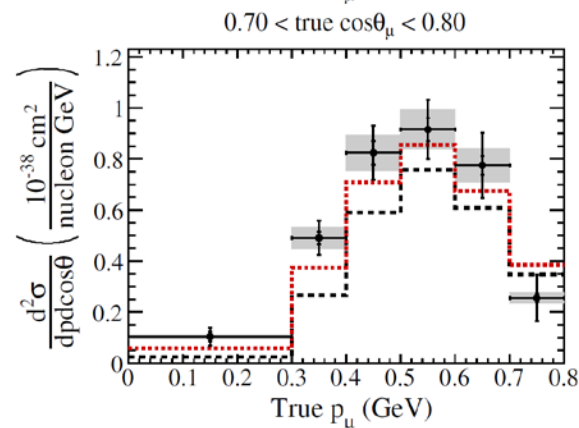
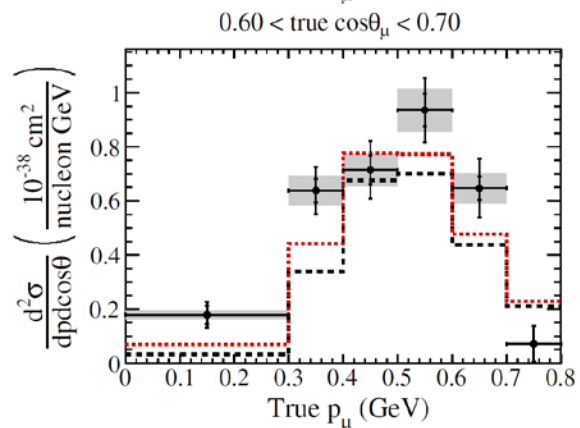
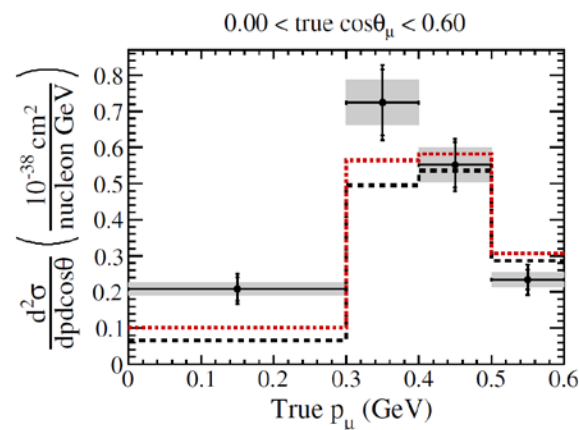
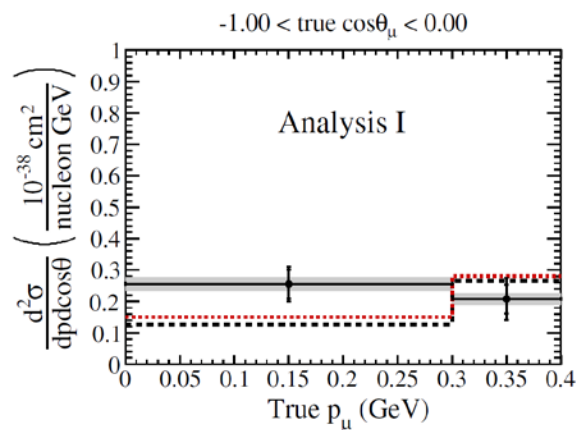
Juan Nieves, IFIC (CSIC & UV)

Neither 2p2h contributions nor RPA effects alone describe the MB 2D dataset, which is however described by the combination of both nuclear mechanisms!

$$M_A \sim 1.03 \text{ GeV}$$



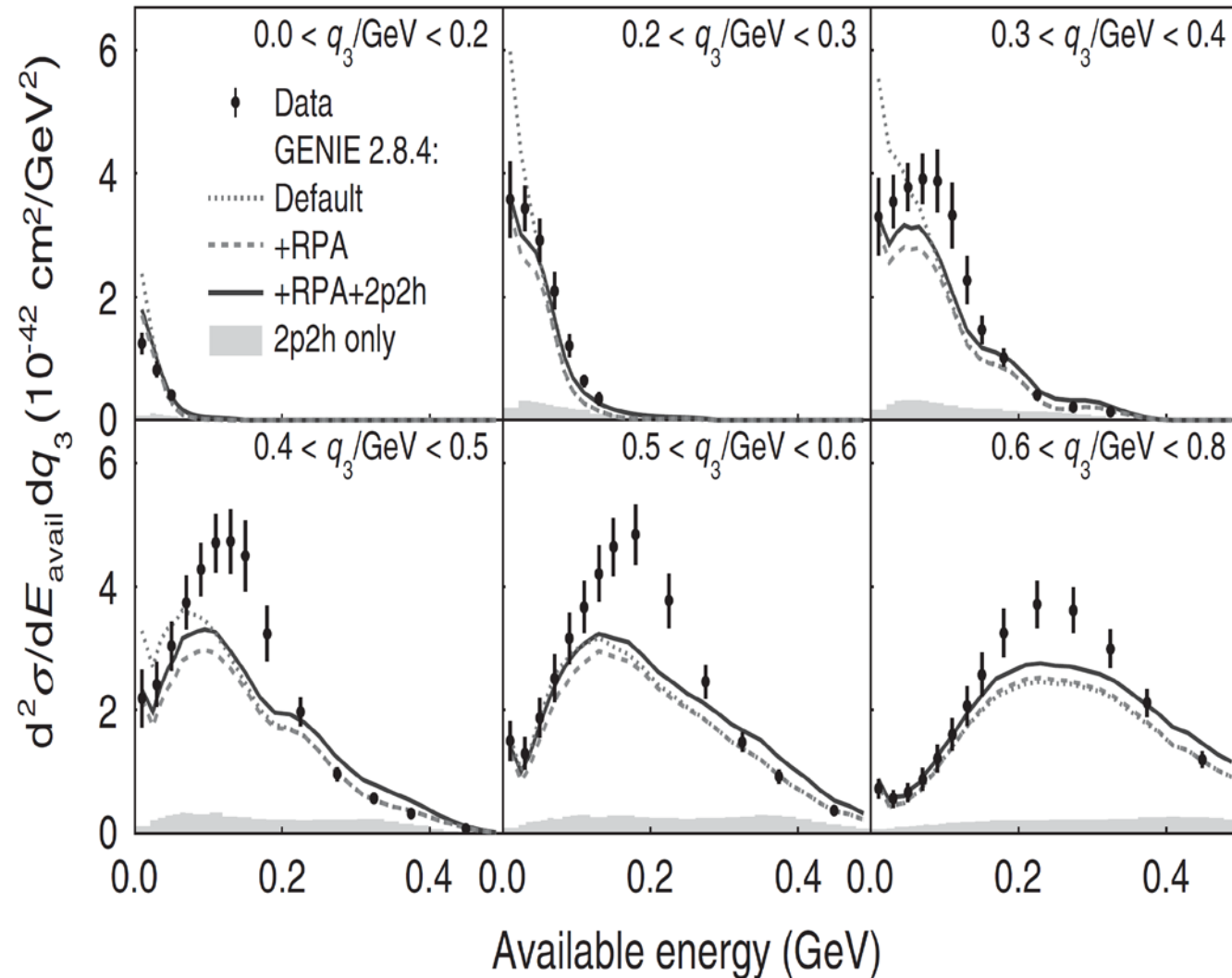
- Antineutrino distributions are more forward peaked
- Relative importance of 2p2h contributions in ν and $\bar{\nu}$ are similar



T2K [PRD 93 112012 (2016)]: Results show sizable nuclear effects for all muon kinematics. Models including 2p2h+RPA contributions agree well with the data

Juan Nieves, IFIC (CSIC & UV)

T2K: CCQE-like



The data make clear two distinct multinucleon effects that are essential for complete modeling of neutrino interactions at low momentum transfer. The $2p2h$ model tested in this analysis improves the description of the event rate in the region between QE and Δ peaks, and the rate for multiproton events, but does not go far enough to fully describe the data. Oscillation experiments sensitive to energy reconstruction effects from these events must account for this event rate. The cross section presented here will lead to models with significantly improved accuracy.

MINERvA:
CCQE-like

PRL 116, 071802 (2016)

Juan Nieves, IFIC (CSIC & UV)

3. Neutrino energy reconstruction

Neutrino beams **ARE NOT monochromatic**. For QE-like events, only the charged lepton is observed and the only measurable quantities are then its direction (scattering angle θ_μ with respect to the neutrino beam direction) and its energy E_μ . **The energy of the neutrino that has originated the event is unknown.** Assuming QE dynamics is defined a “reconstructed” energy

$$E_{\text{rec}} = \frac{ME_\mu - m_\mu^2/2}{M - E_\mu + |\vec{p}_\mu| \cos \theta_\mu}$$

(genuine quasielastic event on a nucleon at rest, ie. E_{rec} is determined by the QE-peak condition $q^0 = -q^2/2M$). Note that **each event contributing to the flux averaged double differential cross section $d\sigma/dE_\mu d\cos\theta_\mu$ defines unambiguously a value of E_{rec} .** The actual (“true”) energy, E , of the neutrino that has produced the event will not be exactly E_{rec} .

Flux-folded $d\sigma/dT_\mu d\cos\theta_\mu$ $\overset{?}{\rightarrow}$ CCQE-like unfolded $\sigma(E)$

Unfolding procedure needs theoretical input!

$$P_{\text{true}}(E) = \int dE_{\text{rec}} \underbrace{P_{\text{rec}}(E_{\text{rec}})}_{\text{EXP}} \underbrace{P(E|E_{\text{rec}})}_{\text{theory!}}$$

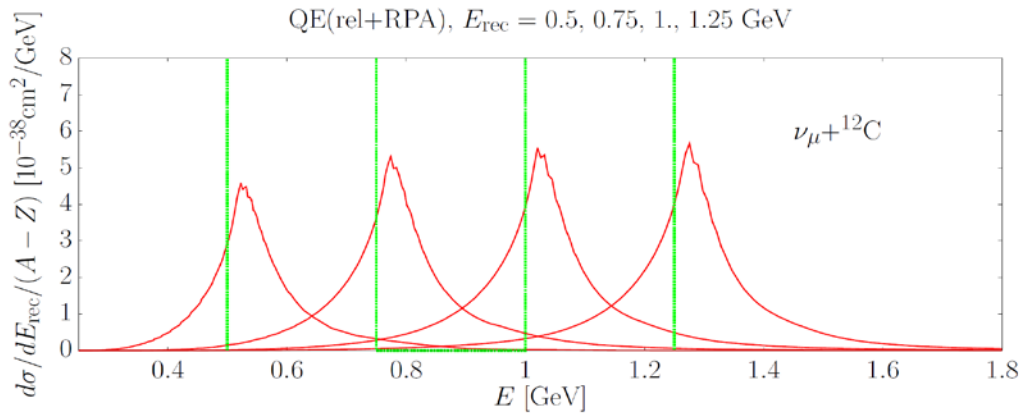
$P_{\text{rec}}(E_{\text{rec}})$ is the *pd* of measuring an event with reconstructed energy E_{rec} . $P(E|E_{\text{rec}})$ is, given an event of reconstructed energy E_{rec} , the conditional *pd* of being produced by a neutrino of energy E .

...using Bayes’s theorem $P(E|E_{\text{rec}})$ could be related to

$P(E_{\text{rec}}|E)$ is determined by $\frac{d\sigma}{dE_{\text{rec}}}(E; E_{\text{rec}})$

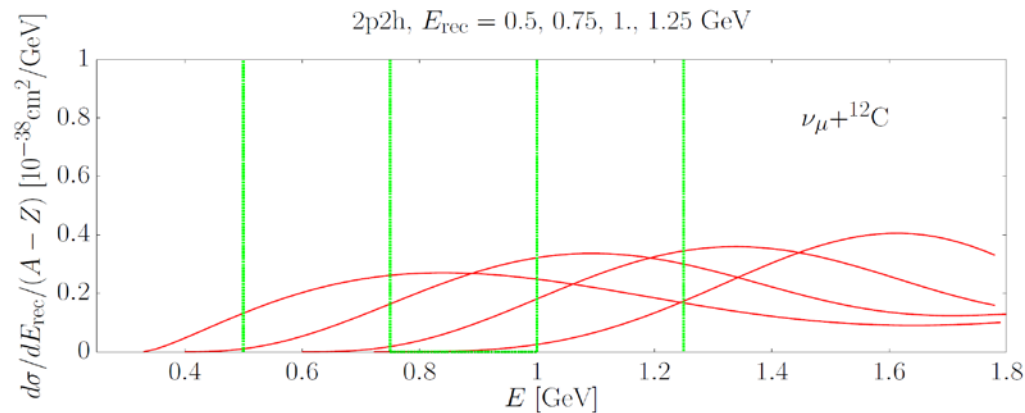
Neutrino Energy Reconstruction and the Shape of the CCQE-like Total Cross Section

(qualitatively in agreement with Martini et al., PRD85 093012)

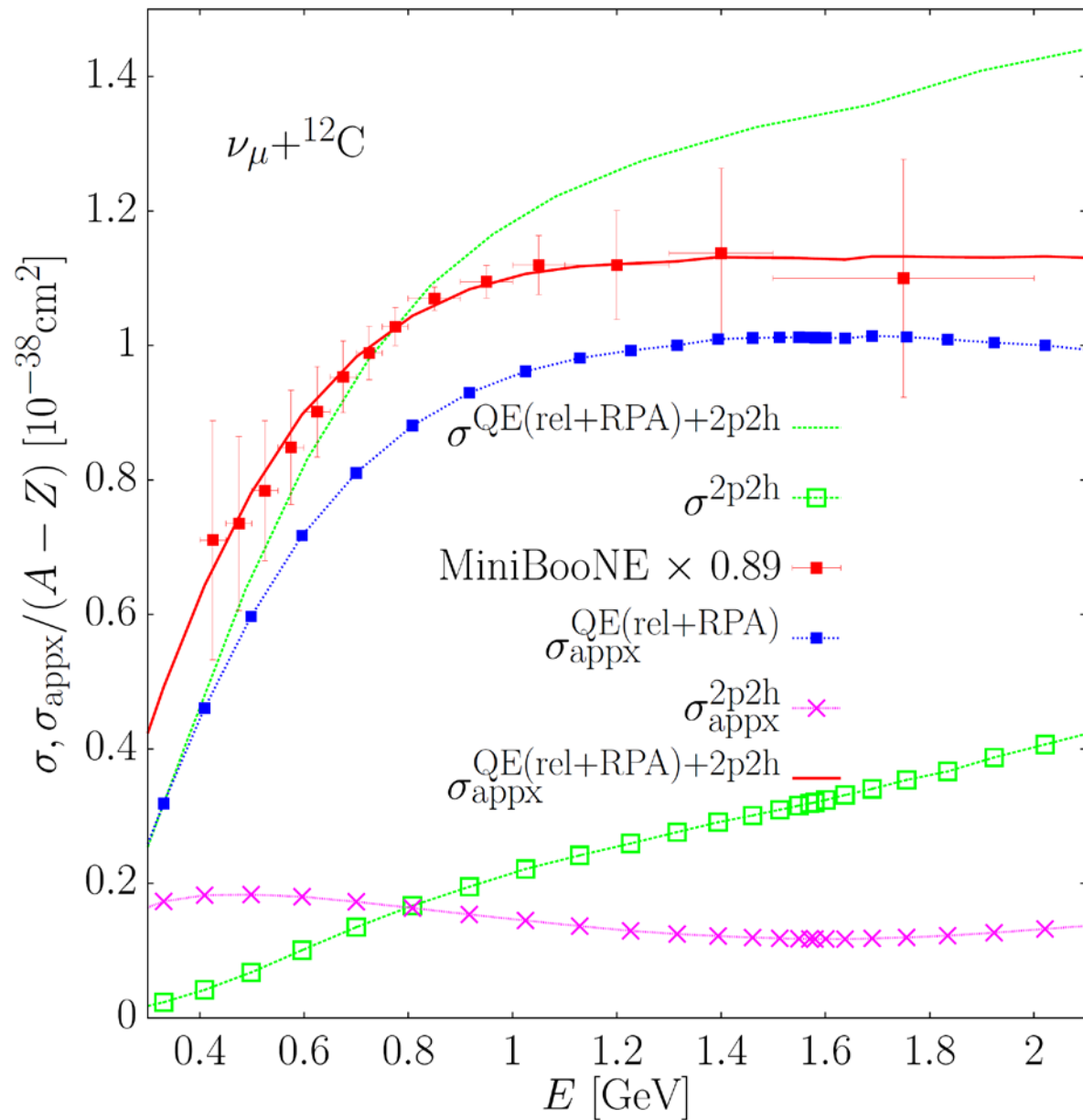


$$\frac{d\sigma}{dE_{\text{rec}}}(E; E_{\text{rec}}^0) = \int_{m_\mu}^E dE_\mu \frac{d^2\sigma}{dE_{\text{rec}} dE_\mu}(E; E_{\text{rec}}^0) = \int_{m_\mu}^E dE_\mu \left| \frac{\partial(\cos \theta_\mu)}{\partial E_{\text{rec}}} \right| \frac{d^2\sigma}{d(\cos \theta_\mu) dE_\mu}(E; E_{\text{rec}}^0)$$

theory !



For each E_{rec} , there exists a distribution of true neutrino energies that could give rise to events whose muon kinematics would lead to the given value of E_{rec} .

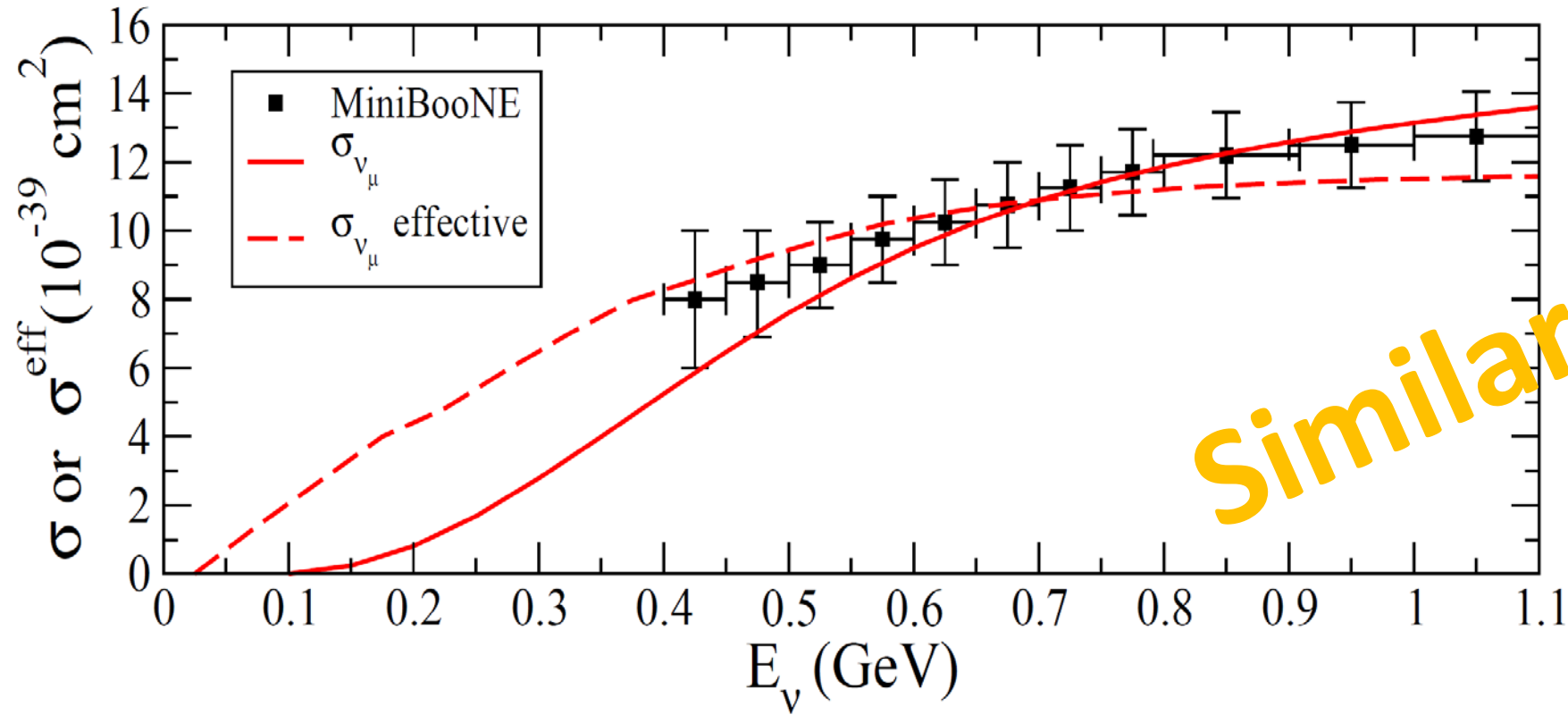


$$\left[\langle \sigma \rangle P_{\text{rec}}(E_{\text{rec}}) \right]_{\text{Exp}} \sim \int \left(\left. \frac{d\sigma}{dE_{\text{rec}}}(E'; E_{\text{rec}}) \right|_{\text{QE}+\text{RPA}, M_A=1.049 \text{ GeV}} + \frac{d\sigma^{2\text{p2h}}}{dE_{\text{rec}}}(E'; E_{\text{rec}}) \right) \Phi(E') dE'$$

... and

$$\left[\frac{d\sigma/dE_{\text{rec}}(E; E_{\text{rec}})}{\int dE'' \Phi(E'') d\sigma/dE_{\text{rec}}(E''; E_{\text{rec}})} \right]$$

ONLY QE, $M_A=1.32 \text{ GeV}$ and noRPA



Similar results

Martini, Ericson, Chanfray [Phys.Rev. D87 (2013), 013009]

Conclusions

- We have presented a theoretical description of effects produced by the inclusion of SFs, which account for the change of the dispersion relations of the interacting nucleons embedded in a nuclear medium.
- SFs are responsible for the quenching of the QE peak, produce a spreading of the strength of the response functions to higher energy transfers and shift the peak position in the same direction. The overall result is a decrease of the integrated cross sections and a considerable change of the differential shapes.
- RPA effects in integrated decay rates or cross sections become significantly smaller when SF corrections are also taken into account, in sharp contrast to the case of a free LFG where they lead to large reductions, even of around 40%.
- We have analyzed the MiniBooNE CCQE 2D cross section data using a theoretical model that has proved to be quite successful in the analysis of nuclear reactions with electron, photon and pion probes and contains no additional free parameters.

- RPA and multinucleon knockout have been found to be essential for the description of the data.
- MiniBooNE ν and $\bar{\nu}$ CCQE-like data are fully compatible with former determinations of M_A in contrast with several previous analyses. We find, $M_A = 1.08 \pm 0.03$ GeV.
- The MiniBooNE ν_μ flux could have been underestimated ($\sim 10\%$).
- Because of the multinucleon mechanism effects, the algorithm used to reconstruct the neutrino energy is not adequate when dealing with QE-like events.
- The inclusion of nucleon-nucleon correlation effects in the RPA series yields a much larger shape distortion toward relatively more high- q^2 interactions, with the 2p2h component filling in the suppression at very low q^2 .

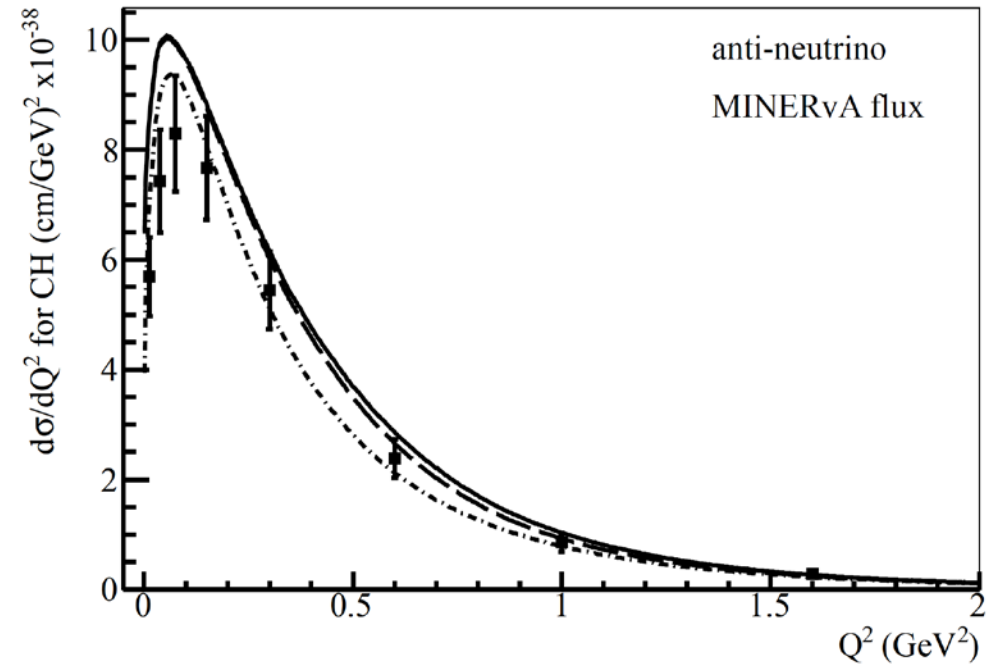
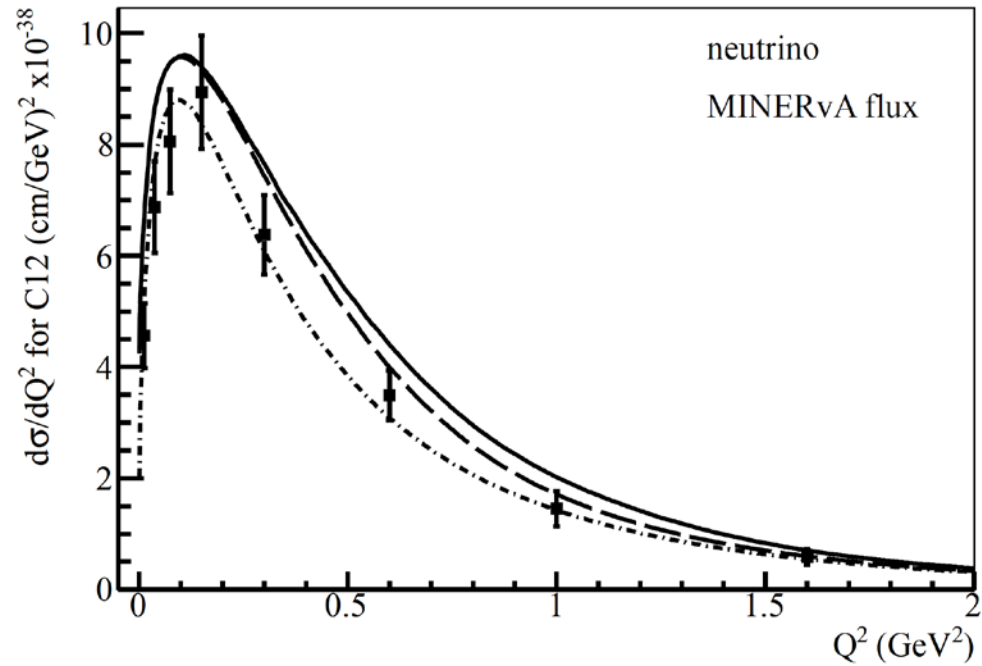
Final remark:

Nuclear effects lead to sizable uncertainties on the neutrino nucleus cross sections at low $-q^2 = Q^2 < 1 \text{ GeV}^2$

It is important to incorporate these effects in event generators (GENIE, etc..)

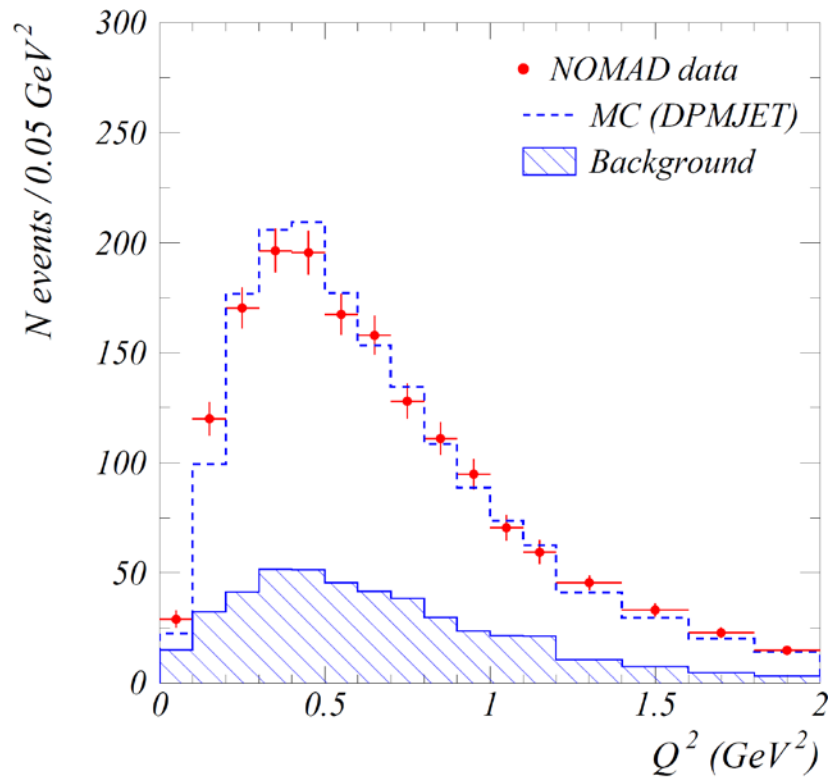
Back up Slides

MINER ν A



PHYSICAL REVIEW D 88, 113007 (2013)

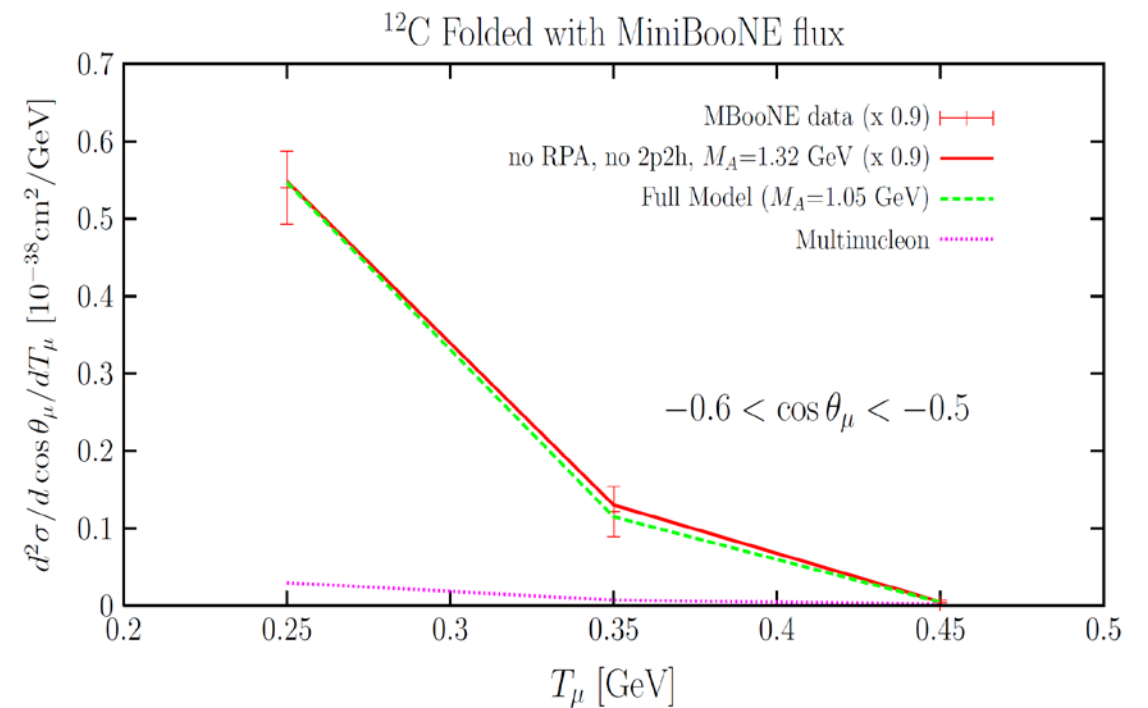
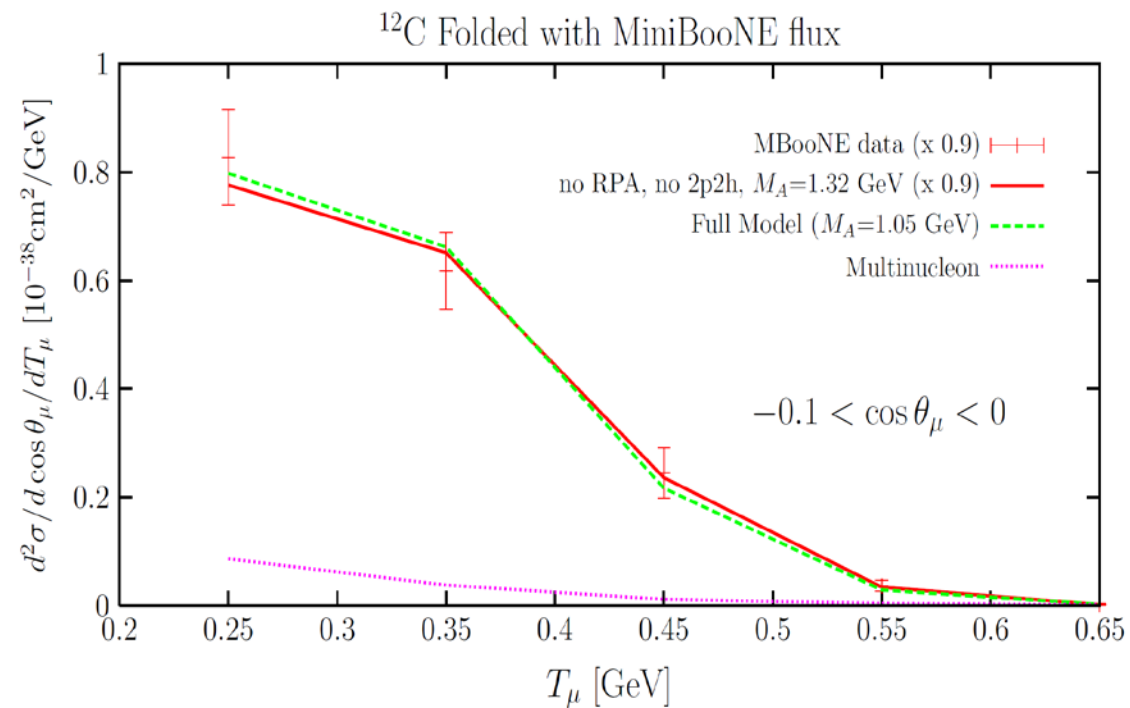
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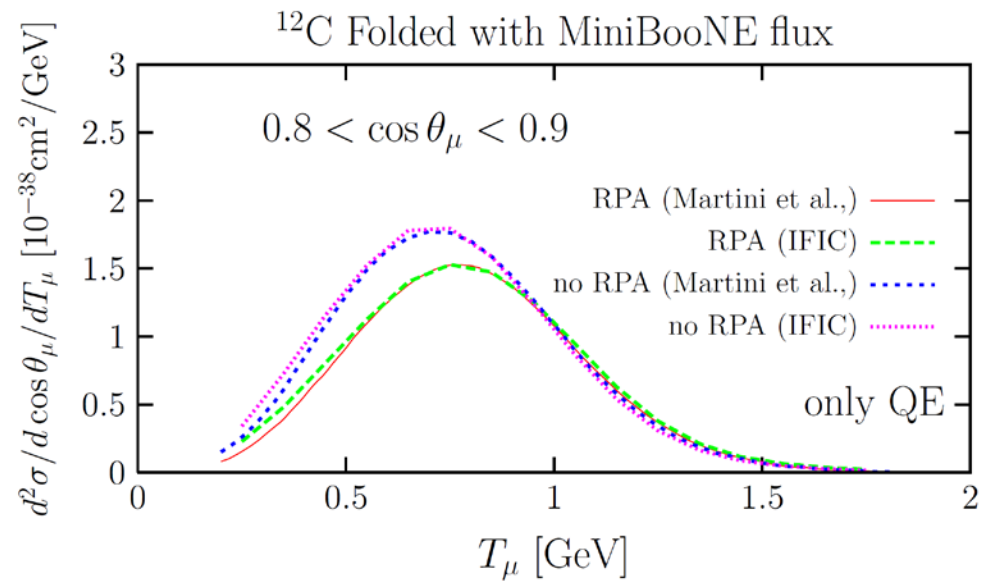


V. Lyubushkin et al. (**NOMAD Collaboration**), Eur. Phys. J. C 63, 355 (2009). In the **two-track sample**, which is primarily Q^2 above 0.3 GeV^2 , a **large fraction of the 2p2h component**, as well as QE and pion production where the hadrons rescattered as they exited the nucleus, are **rejected**.

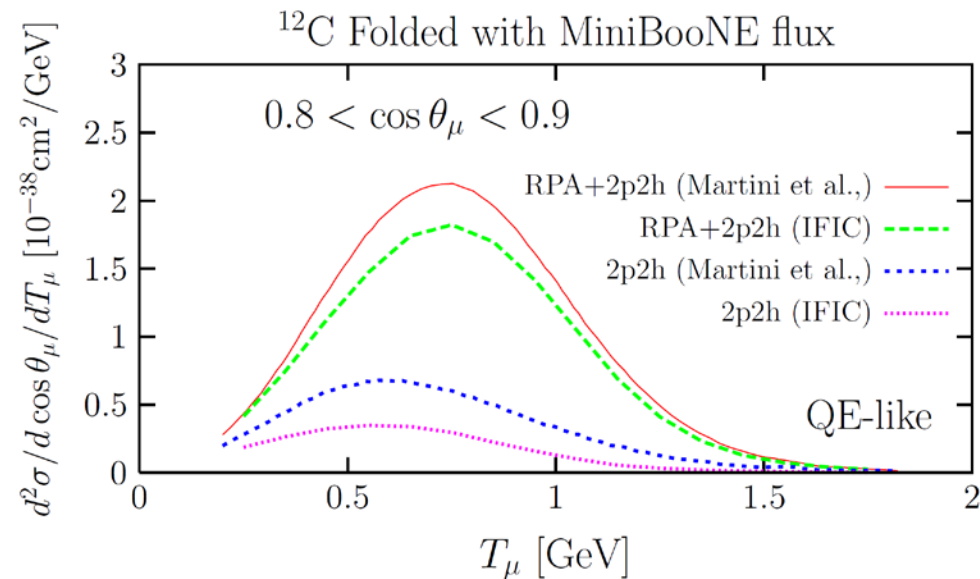
It is observed a relative **deficit at $Q^2 = 0.3$ and excess at 1.5 GeV^2 compared to QE without RPA**. If the first two or three points are eliminated, the distribution will be consistent with $M_A \sim 1.2 \text{ GeV}$.

Dependence of the 2p2h contribution on $\cos \theta_\mu$





We compare rather well with Martini et al., PRC 84, 055502 for bare QE and QE+RPA



...however our 2p2h contribution is about a factor of 2 smaller!



Differences with the work of Martini et al. (PRC80,065501)

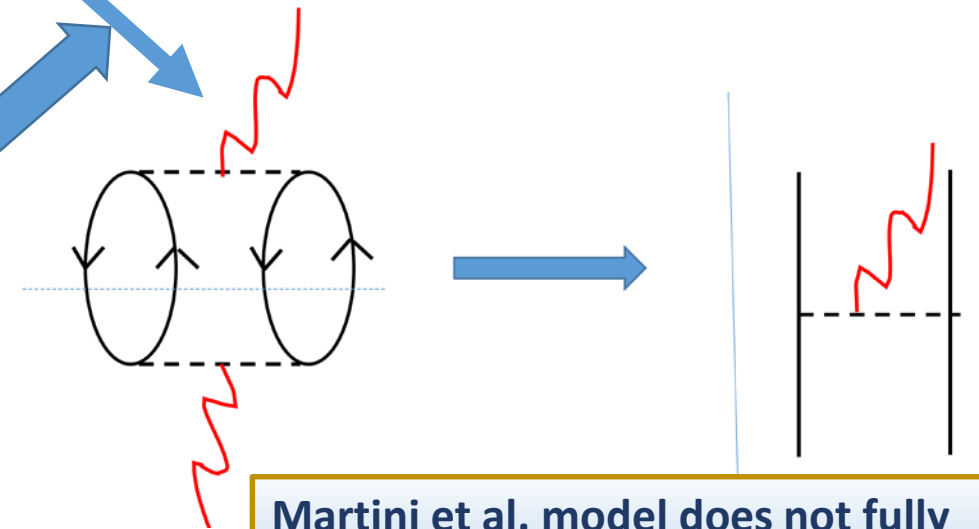
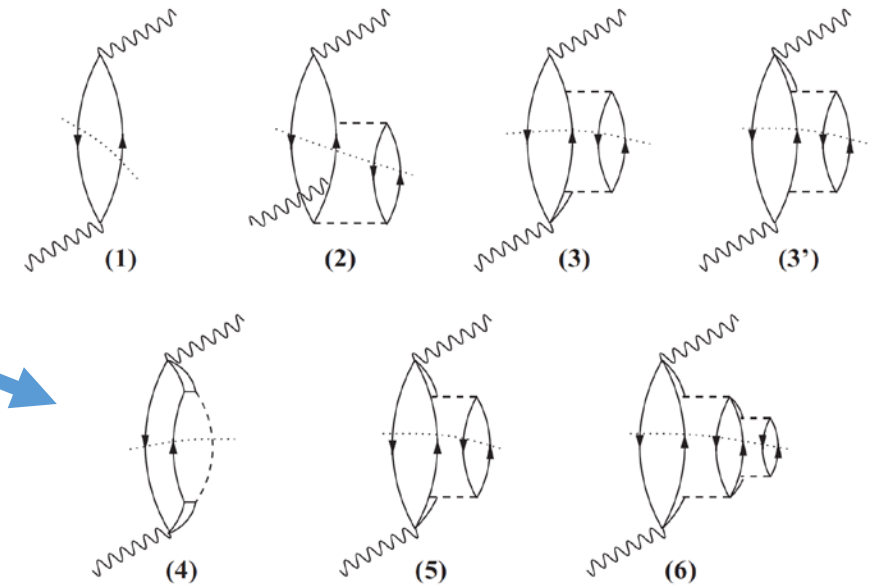
1. Similar for the 2p2h contributions driven by Δh excitation (both groups use the same model for the Δ -selfenergy in the medium).

2. Martini et al. do not consider 2p2h contributions driven by contact, pion pole and pion in flight terms.

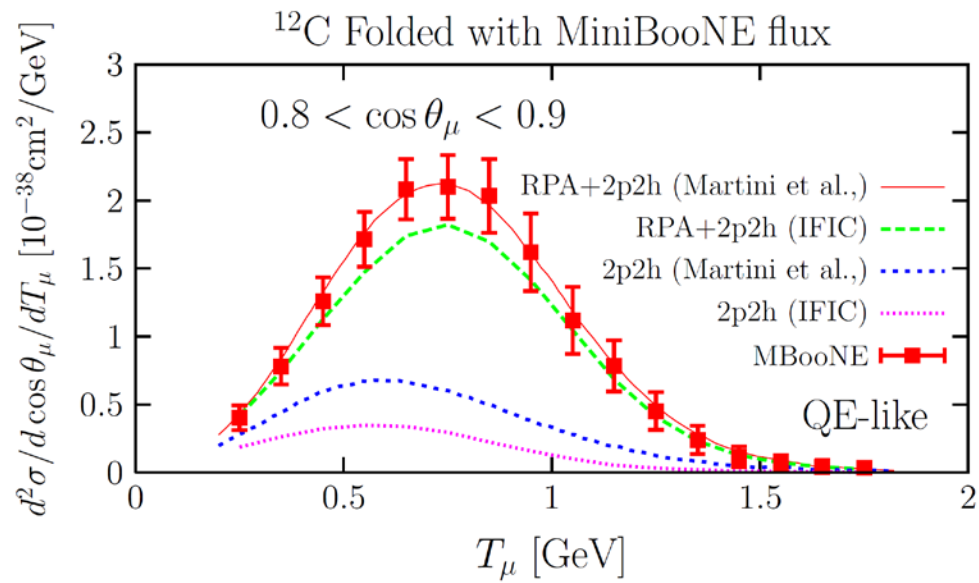
3. Martini et al. give approximate estimates (no microscopical calculation) for the rest of 2p2h contributions [relate them to the absorptive part of the p -wave pion-nucleus optical potential at threshold or to a microscopic calculation by Alberico et al. (Annals Phys. 154, 356) specifically aimed at the evaluation of the 2p-2h contribution to the isospin spin-transverse response, measured in inclusive (e, e') scattering].

This 2p2h parametrization includes MEC effects driven by the vector current !

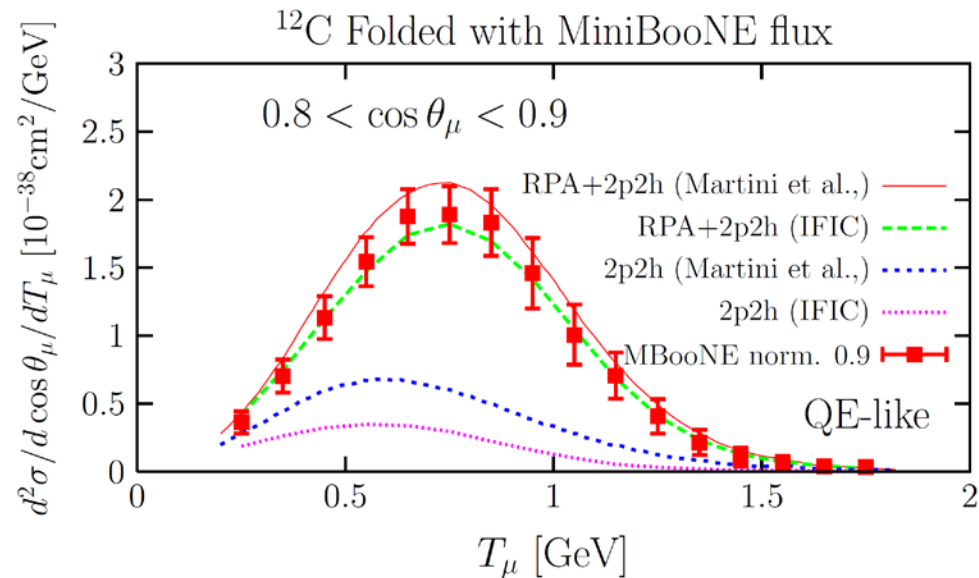
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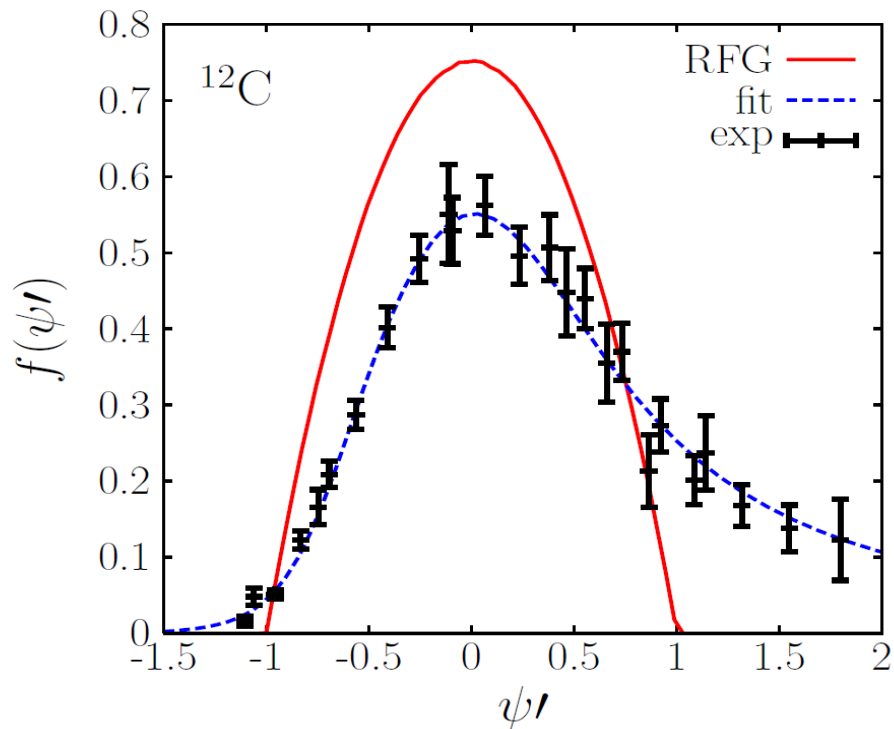
Martini et al. model does not fully account for the axial and axial-vector interference contributions !



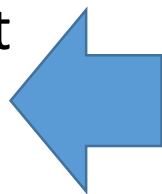
Martini et al., predictions look consistent with MiniBooNE data ..., **but their estimate rely on some computation of the 2p2h mechanisms for (e, e') (Alberico et al.) $\Rightarrow$ no info on axial part of the interaction!**



...however our predictions for the 2p2h contribution would favor a global normalization scale of about 0.9. This would be consistent with the MiniBooNE estimate of a total normalization error of 10.7%.



Superscaling function does not take into account dip region events



Superscaling approach: Inclusive electron scattering data exhibit interesting systematics that can be used to predict (anti)neutrino-nucleus cross sections (T. Donnelly and I. Sick, PRL 82, 3212 (1999)),

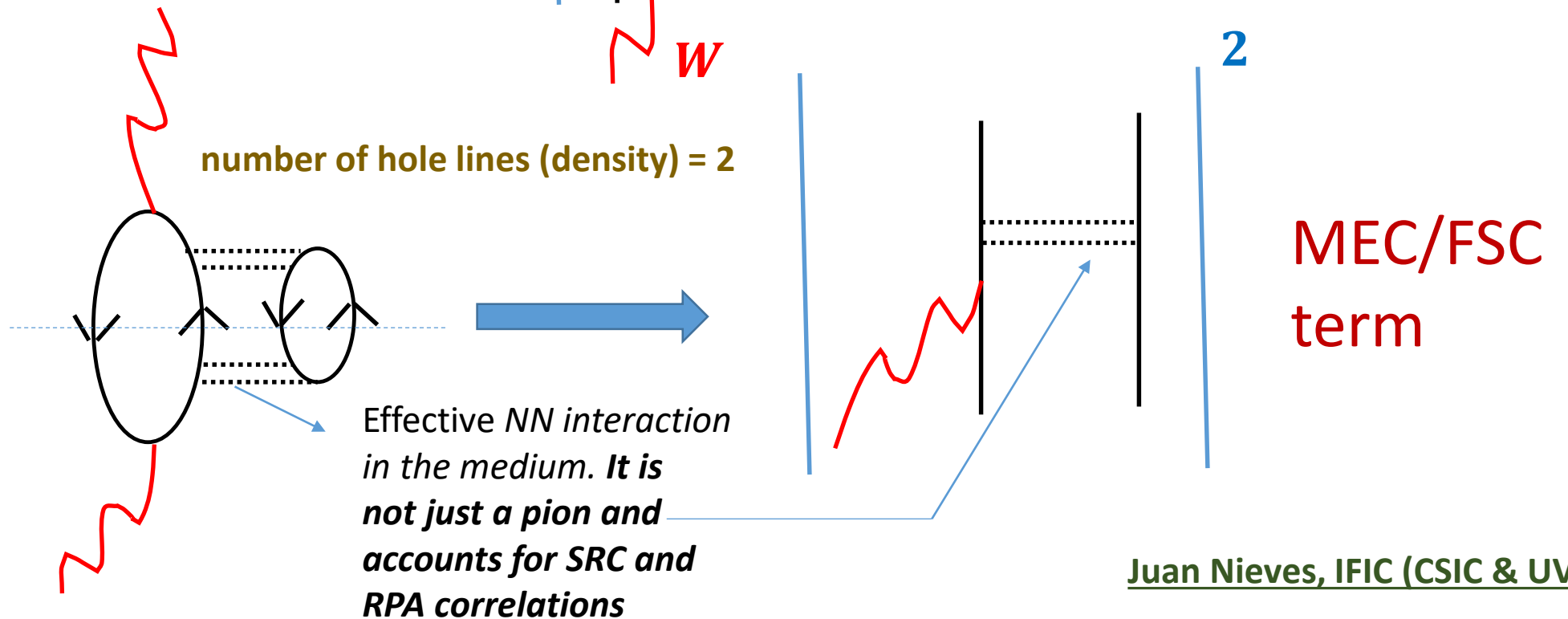
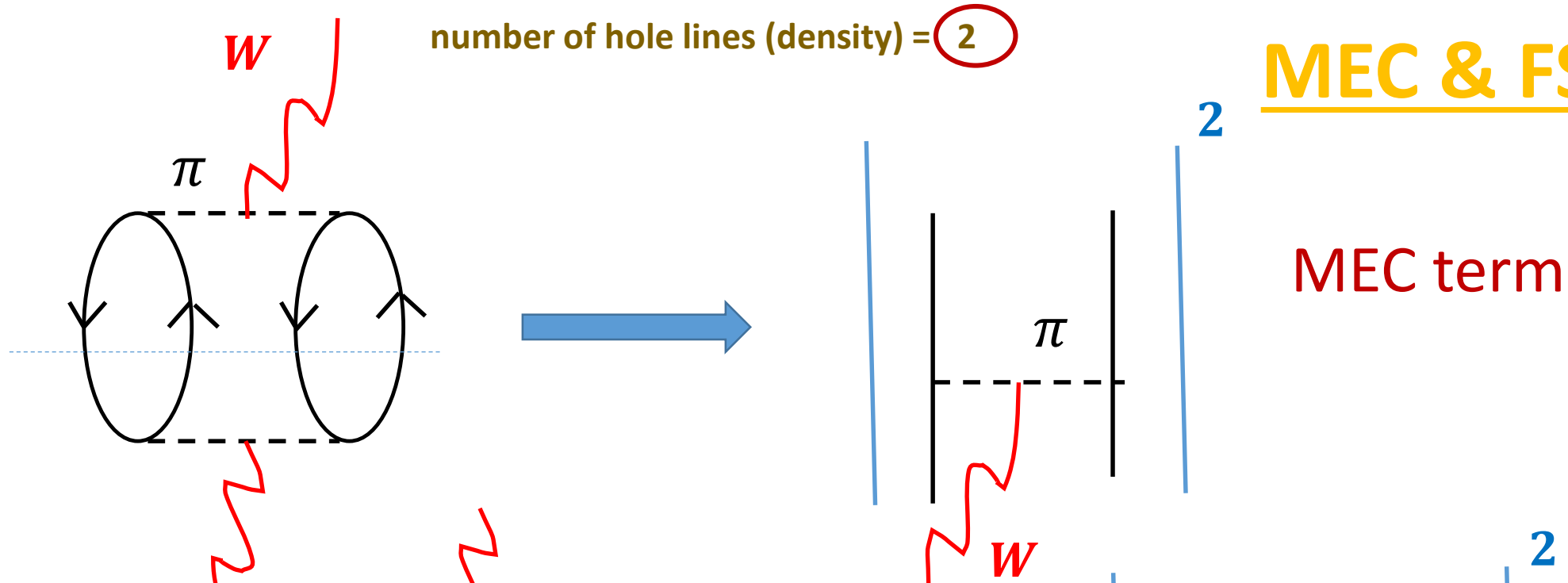
$$f = k_F \frac{\frac{d\sigma}{d\Omega' dE'}}{Z\sigma_{ep} + N\sigma_{en}}$$

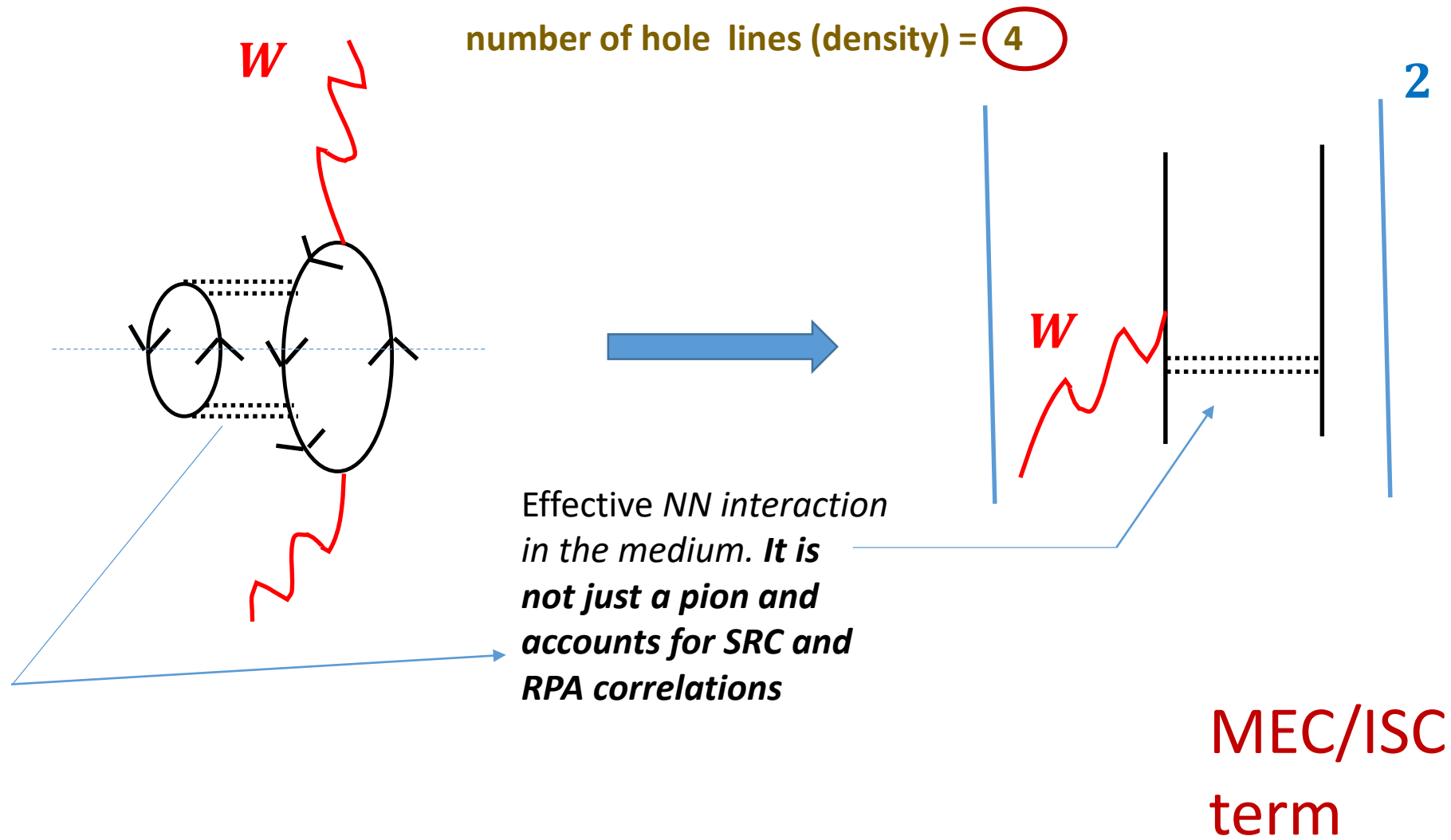
- $f = f(\psi')$, with $\psi' = \psi'(q^0, |\vec{q}|)$
- f is largely independent of the specific nucleus

Scaling violations reside mainly in R_T : excitation of resonances, meson production, 2p2h mechanisms and even the tail of DIS. An experimental scaling function $f(\psi')$ could be reliably extracted by fitting the data for R_L .

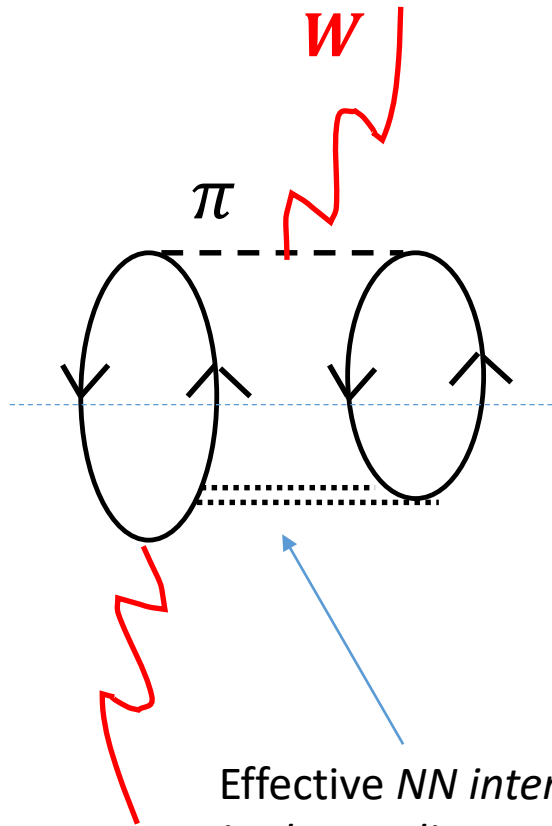
ν QE cross sections can be calculated with the simple RgFG model followed by the replacement $f_{RgFG} \rightarrow f_{exp}$.

MEC & FSC & ISC

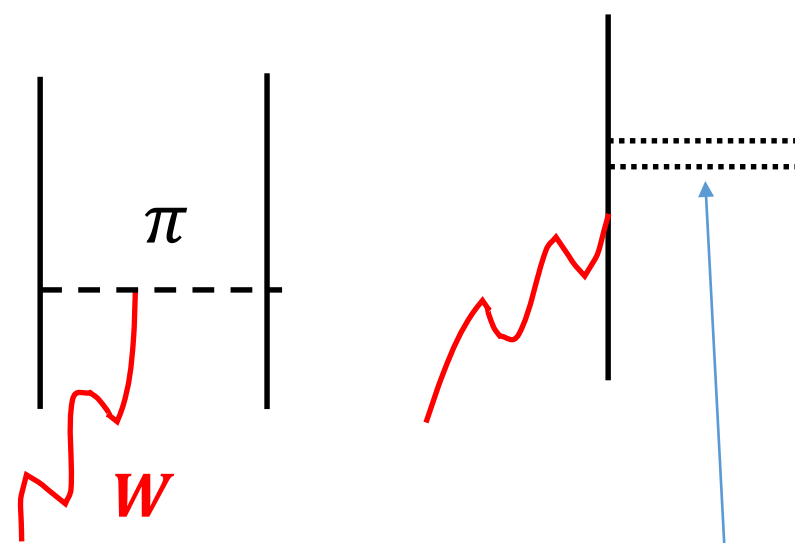




number of hole lines (density) = 2



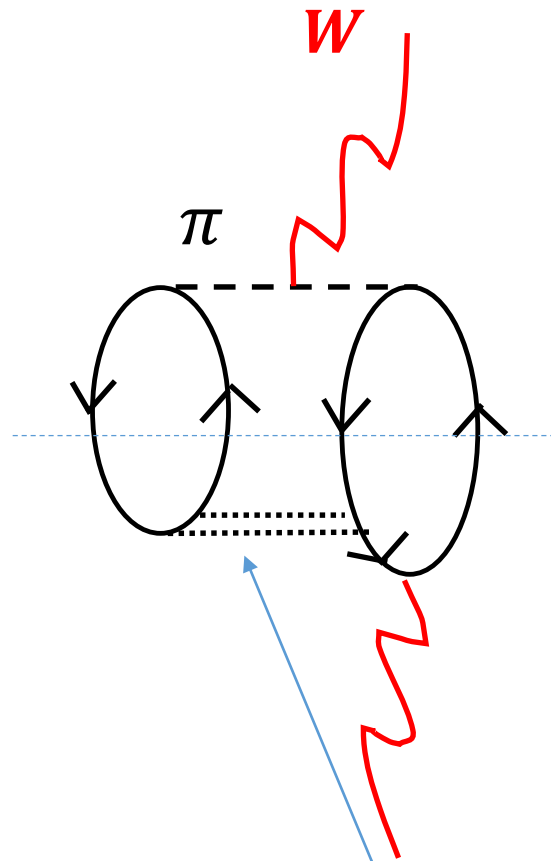
Effective NN interaction
in the medium. It is
not just a pion and
**accounts for SRC and
RPA correlations**



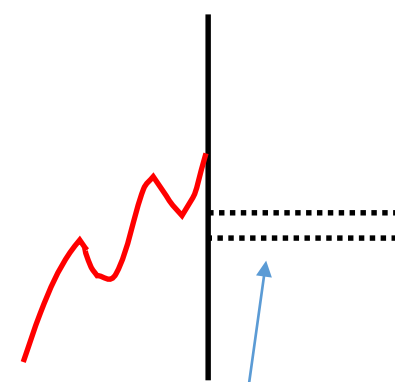
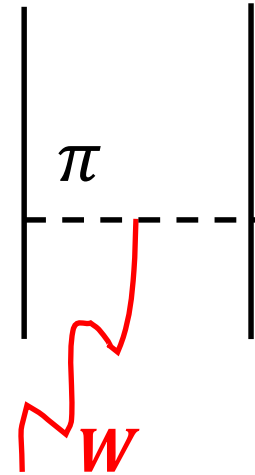
FSC-MEC interference term

number of hole lines (density) = 3

MEC-ISC interference term

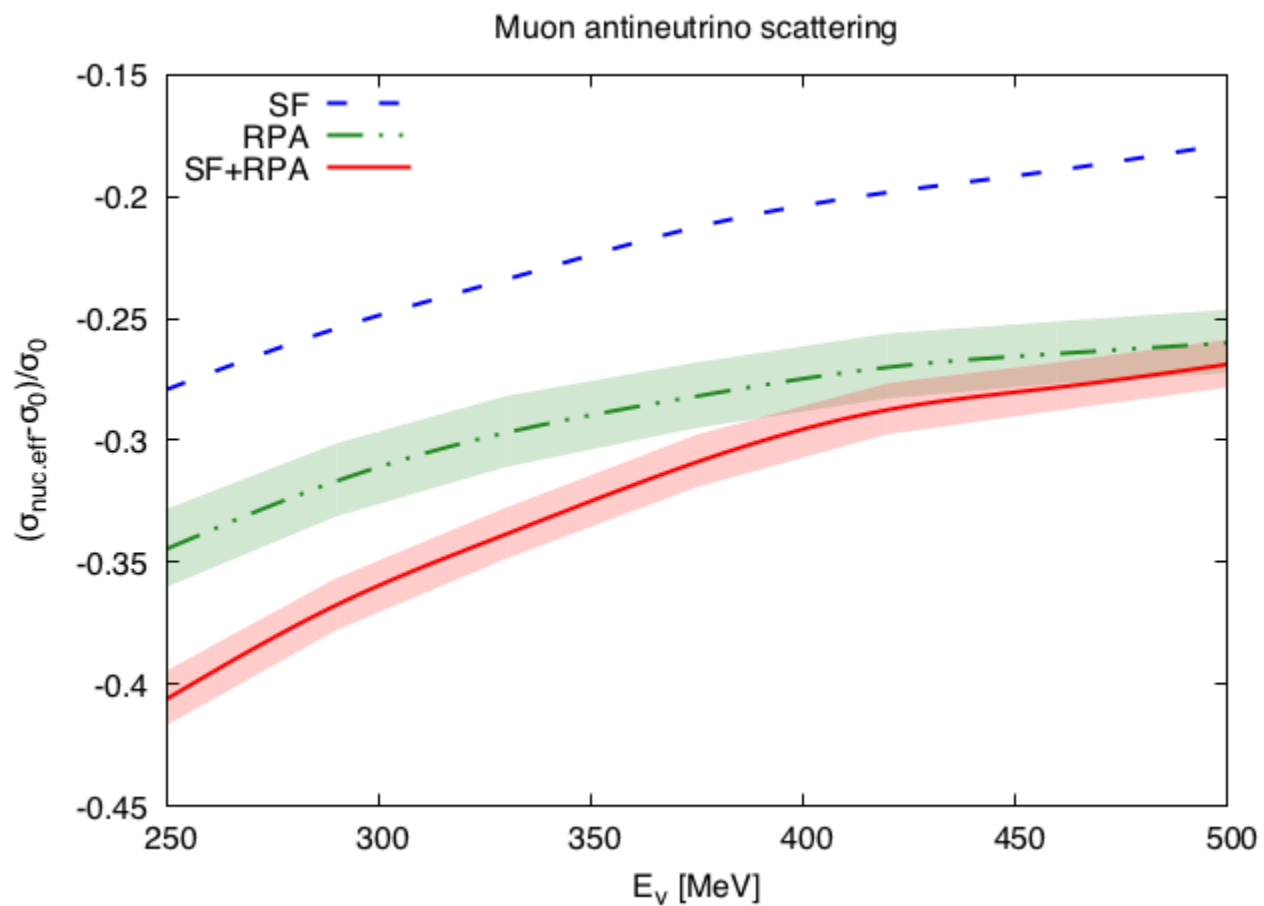
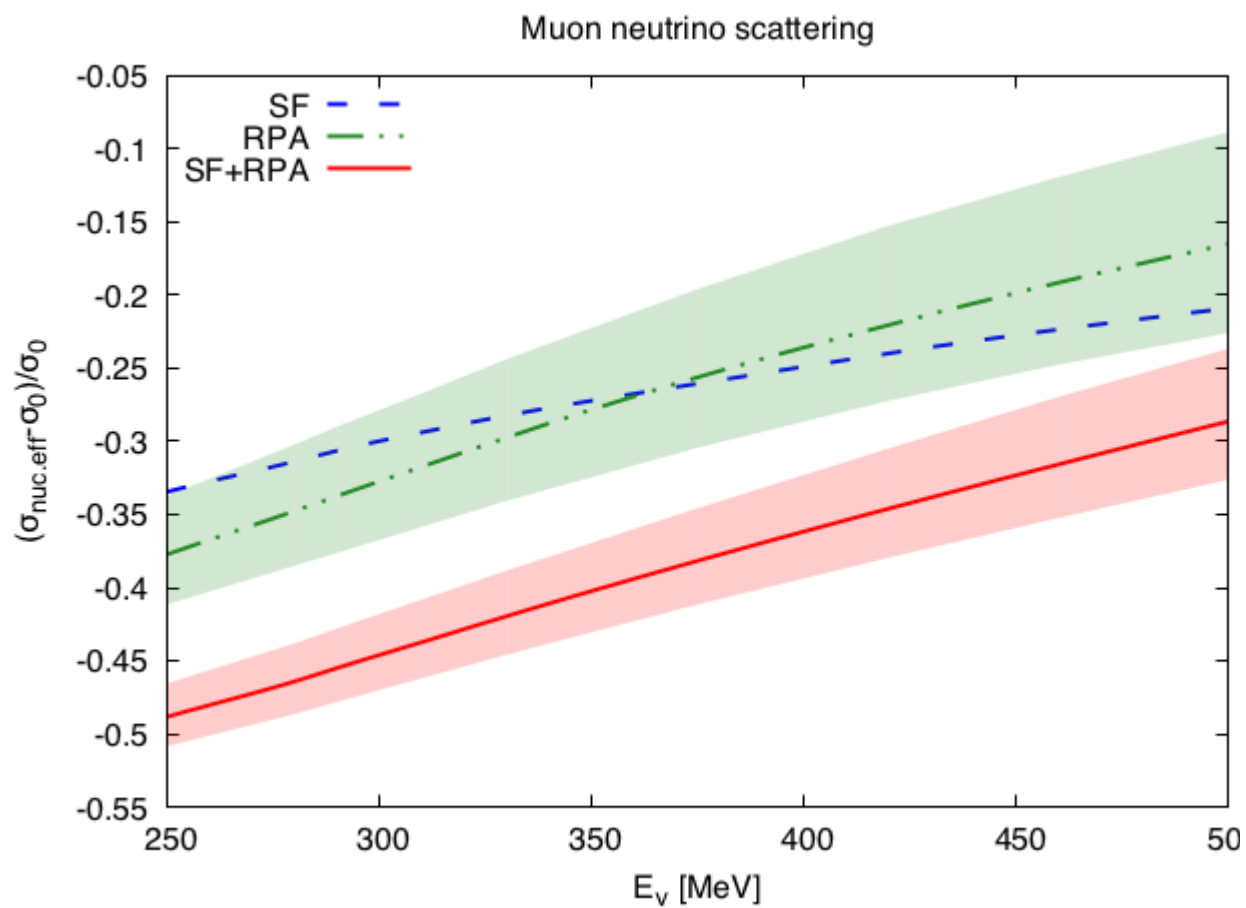


Effective NN interaction in the medium. **It is not just a pion and accounts for SRC and RPA correlations**

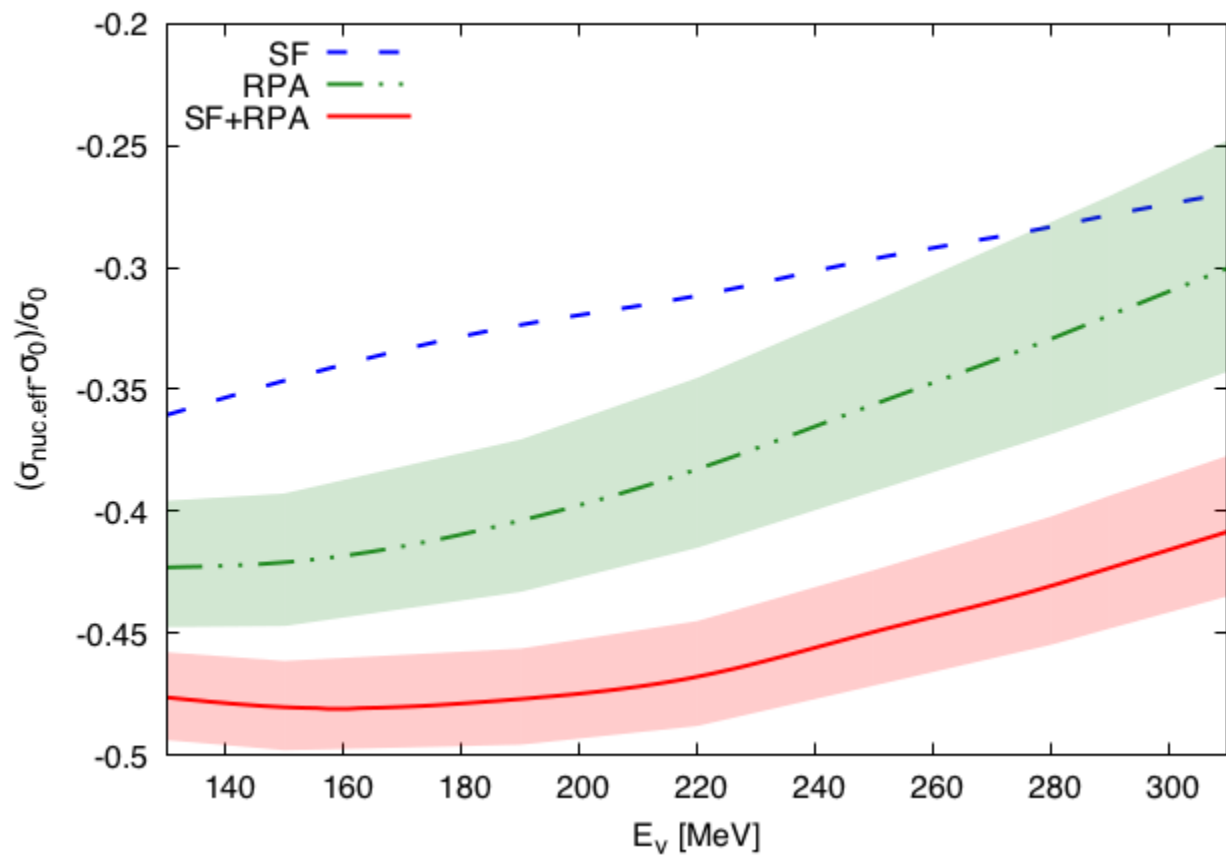


Important?
Benhar, Lovato,
Rocco [PRC 92
(2015) 024602]

- IFIC 2p2h calculation does not incorporate these terms.
- Martini et al. predictions are based on a 2p2h calculation for $(e, e'X)$ [Alberico et al.,] that accounts for such contributions (only vector current)



Electron neutrino scattering



Electron antineutrino scattering

