

Higer Orders in Parton Showers

Frank Krauss

Institute for Particle Physics Phenomenology
Durham University

Heavy Flavour Production at the LHC (IPPP 2017)



Reminder: How parton showers work

- parton showers are approximations, based on
 - leading colour, leading logarithmic accuracy, spin-average
- parametric accuracy by comparing Sudakov form factors:

$$\Delta = \exp \left\{ - \int \frac{dk_{\perp}^2}{k_{\perp}^2} \left[A \log \frac{k_{\perp}^2}{Q^2} + B \right] \right\},$$

where A and B can be expanded in $\alpha_S(k_{\perp}^2)$

- Q_T resummation includes $A_{1,2,3}$ and $B_{1,2}$
(transverse momentum of Higgs boson etc.)
- showers usually include terms $A_{1,2}$ and B_1
 A = cusp terms (“soft emissions”), $B \sim$ anomalous dimensions γ

Matching at NLO and NNLO

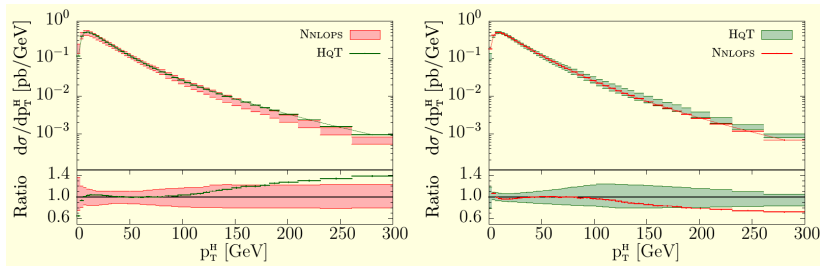
- avoid double-counting of emissions
- two schemes at NLO: MC@NLO and POWHEG
 - mismatches of K factors in transition to hard jet region
 - MC@NLO: \rightarrow visible structures, especially in $gg \rightarrow H$
 - POWHEG: \rightarrow high tails, cured by h dampening factor
 - well-established and well-known methods

(no need to discuss them any further)

- two schemes at NNLO: MINLO & UN²LOPS (singlets S only)
 - different basic ideas
 - MINLO: $S + j$ at NLO with $p_T^{(S)} \rightarrow 0$ and capture divergences by reweighting internal line with analytic Sudakov, NNLO accuracy ensured by reweighting with full NNLO calculation for S production
 - UN²LOPS identifies and subtracts and adds parton shower terms at FO from $S + j$ contributions, maintaining unitarity
 - available for two simple processes only: DY and $gg \rightarrow H$

NNLOs for H production: MINLO

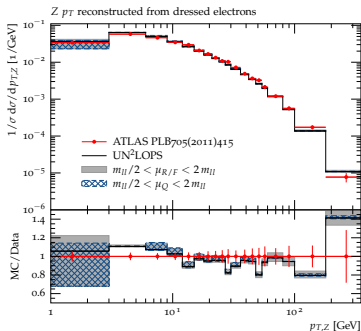
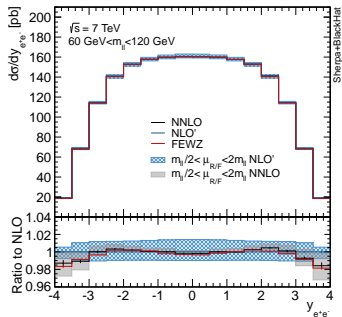
K. Hamilton, P. Nason, E. Re & G. Zanderighi, JHEP 1310



- also available for $Z/W/VH$ production

NNLOs for Z production: UN²LOs

S. Hoche, Y. Li, & S. Prestel, Phys.Rev.D90 & D91



- also available for H production

A new shower implementation in DIRE

(S.Höche & S.Prestel, Eur.Phys.J. C75 (2015) 461)

- evolution and splitting parameter ($((ij) + k \rightarrow i + j + k)$):

$$\kappa_{j,ik}^2 = \frac{4(p_i p_j)(p_j p_k)}{Q^4} \quad \text{and} \quad z_j = \frac{2(p_j p_k)}{Q^2}.$$

- splitting functions including IR regularisation

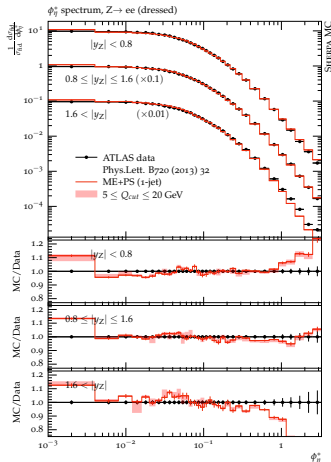
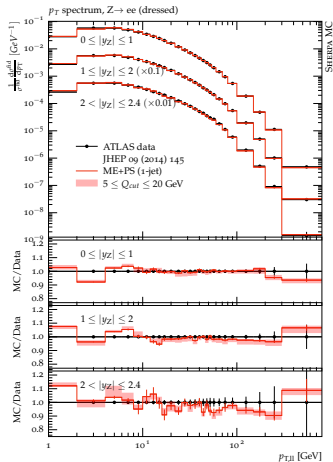
(a la Curci, Furmanski & Petronzio, Nucl.Phys. B175 (1980) 27-92)

$$\begin{aligned} P_{qq}^{(0)}(z, \kappa^2) &= 2C_F \left[\frac{1-z}{(1-z)^2 + \kappa^2} - \frac{1+z}{2} \right], \\ P_{qg}^{(0)}(z, \kappa^2) &= 2C_F \left[\frac{z}{z^2 + \kappa^2} - \frac{2-z}{2} \right], \\ P_{gg}^{s(0)}(z, \kappa^2) &= 2C_A \left[\frac{1-z}{(1-z)^2 + \kappa^2} - 1 + \frac{z(1-z)}{2} \right], \\ P_{gq}^{(0)}(z, \kappa^2) &= T_R \left[z^2 + (1-z)^2 \right] \end{aligned}$$

- renormalisation/factorisation scale given by $\mu = \kappa^2 Q^2$
- combine gluon splitting from two splitting functions with different spectators $k \rightarrow$ accounts for different colour flows

LO results for Drell-Yan

(example of accuracy in description of standard precision observable)



Including NLO splitting kernels

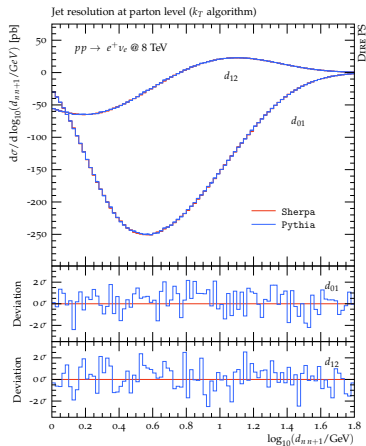
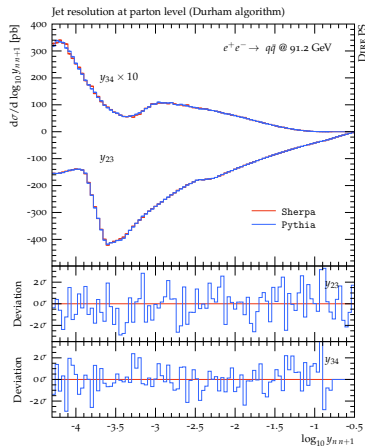
(Hoeche, FK & Prestel, 1705.00982, and Hoeche & Prestel, 1705.00742)

- expand splitting kernels as

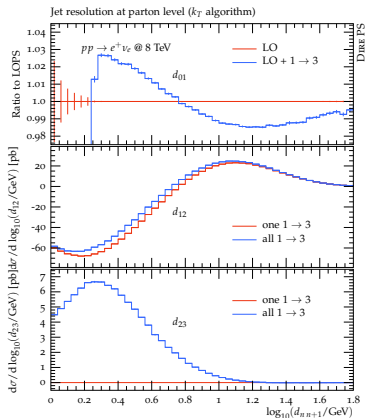
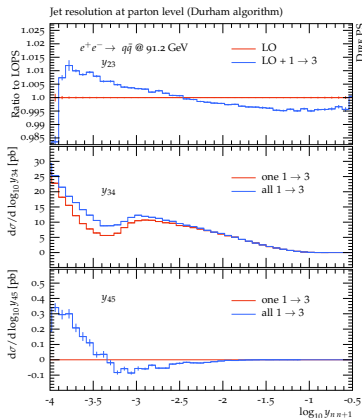
$$P(z, \kappa^2) = P^{(0)}(z, \kappa^2) + \frac{\alpha_S}{2\pi} P^{(1)}(z, \kappa^2)$$

- aim: reproduce DGLAP evolution at NLO
include all NLO splitting kernels
- three categories of terms in $P^{(1)}$:
 - cusp (universal soft-enhanced correction) (already included in original showers)
 - corrections to $1 \rightarrow 2$
 - new flavour structures (e.g. $q \rightarrow q'$), identified as $1 \rightarrow 3$
- new paradigm: **two independent implementations**

Validation of $1 \rightarrow 3$ splittings

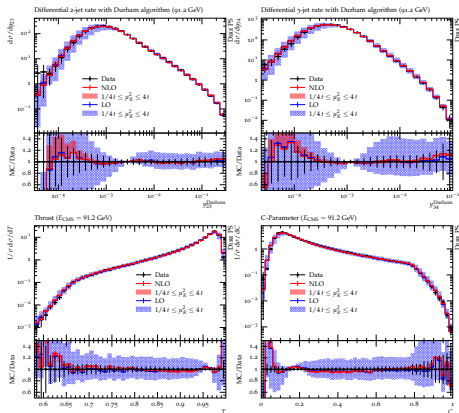


Impact of $1 \rightarrow 3$ splittings



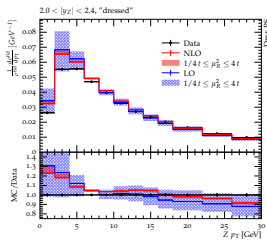
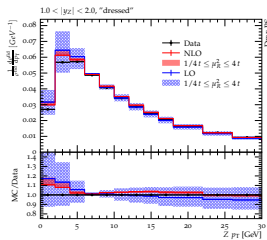
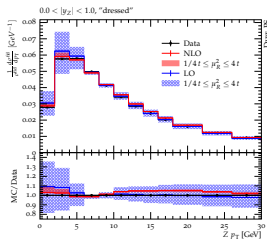
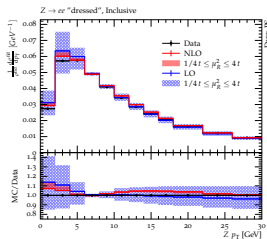
Physical results: $e^-e^+ \rightarrow \text{hadrons}$

(Hoeche, FK & Prestel, 1705.00982)

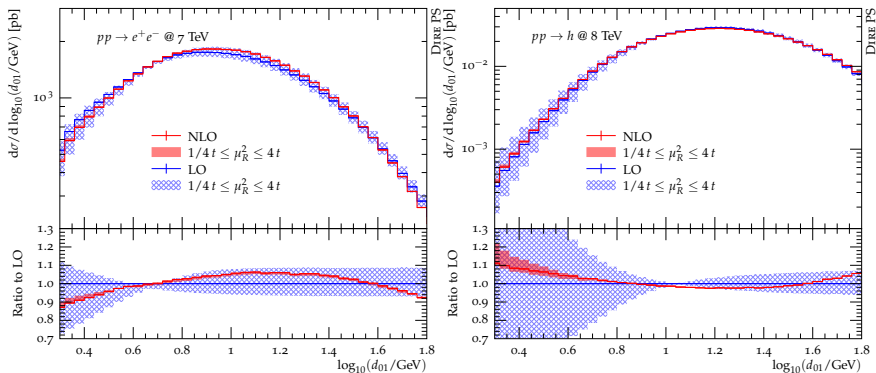


Physical results: DY at LHC

(untuned showers vs. 7 TeV ATLAS data)



Physical results: differential jet rates at LHC



Summary

- implemented NLO DGLAP kernels into two independent showers
will allow cross checks/validation of NP effects
- cross-validated implementations PYTHIA \longleftrightarrow SHERPA
- matching to NNLO/multijet merging at NLO ongoing work
- extension to include loop-corrections to 1 to 2 straightforward
will allow to use triple-collinear splitting functions throughout
- future plans: soft-gluon emissions and non-trivial colour correlations



LIMITATIONS

UNTIL YOU SPREAD YOUR WINGS,
YOU'LL HAVE NO IDEA HOW FAR YOU CAN WALK.