Opening unexplored frontiers for new physics at the LHC

Young Theorists Forum @ Durham 10 Jan 2018

Jesse Liu University of Oxford



Where is the new physics hiding?

What opportunities remain under the search lamppost?

Case study: hunting Higgsinos Why are MSSM compressed scenarios so challenging?

Surpassing two-decade old LEP limits

How do we detect Higgsino dark matter at hadron colliders?

Allowed massless particles by consistency between* RELATIVITY + QUANTUM



Higgs et al.MatterYang-Mills[Unseen]Gravity

Highly constrained theory space

for what structure of (sub-Planckian) fundamental physics can look like

Very difficult for new physics to evade principles

underpinning Standard Model & General Relativity

*No-go theorems by Weinberg (1968), Grisaru & Pendleton (1977). NB 'continuous-spin particles' allowed Schuster & Toro [arXiv:1302.1198]

$$S_{\rm SM} \sim \int \sqrt{-g} \, \mathrm{d}^4 x \Big[-\frac{1}{4} F^2 + \theta F * F + \mathrm{i} \bar{\psi} \gamma \cdot D \psi + |DH|^2 + \mu^2 H^2 + \lambda H^4 - y H \bar{\psi} \psi \Big]$$

Spin 0, $\frac{1}{2}$, 1, 2 states encoded in field representations of Poincaré group

(Spin 2 only dynamical with extra non-renormalisable Einstein–Hilbert kinematic term $\mathscr{L}_{EH} = M_{Pl}^2 R/2$, then SM couples to sub-Planckian gravity at leading order via $\sim h_{\mu\nu} \tau_{SM}^{\mu\nu}/M_{Pl}^2$)

(1) Fundamental hierachies & UV sensitivity $\mu^2 \ll M_{Pl}$ (i.e. 'The hierarchiy problem') a) Why is weak scale $\sim \mu \ll$ Planck scale M_{Pl} ?

b) IR physics should not be severely sensitive to UV dynamics but $\delta\mu^2 \propto M_{
m UV}^2$

(2) Parametric hierachies in Yukawa sector yH (e.g. YETI 2018)

EW symmetry breaking: $y_f H \sim m_f \cdot \text{vev}$: Why is $m_{\text{top quark}}/m_{\text{electron}} \sim 10^6$?

$$S_{\text{SM+GR}} \sim \int \sqrt{-g} \, \mathrm{d}^4 x \left[\frac{M_{\text{Pl}}^2 R}{2} - \frac{1}{4} F^2 + \theta F * F + \mathrm{i} \bar{\psi} \gamma \cdot D \psi + |DH|^2 + \mu^2 H^2 + \lambda H^4 - y H \bar{\psi} \psi \right]$$

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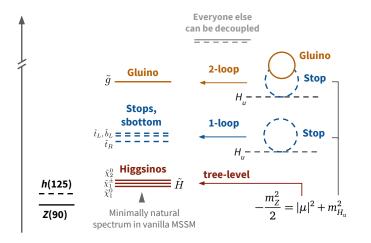
$$S_{\rm SM+GR} \sim \int \sqrt{-g} \, \mathrm{d}^4 x \left[\frac{M_{\rm Pl}^2 R}{2} - \frac{1}{4} F^2 + \theta F * F + \mathrm{i} \bar{\psi} \gamma \cdot D \psi + |DH|^2 + \mu^2 H^2 + \lambda H^4 - y H \bar{\psi} \psi \right]$$

SM fermion masses are technically natural (e.g. 't Hooft 1979) Light mass protected by chiral symmetry – scalars lack such custodial symmetry

Supersymmetry makes mystery (1b) technically natural Tie Higgs h to Higgsino \tilde{H} fermionic partner with SUSY to keep scalar mass light

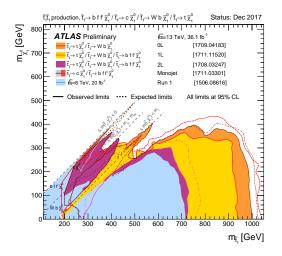


Further elevate naturalness into a guide for SUSY mass scale



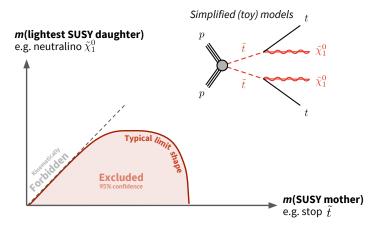
Adapted from Papucci et al [arXiv:1110.6926] **Naturalness desires low fine-tuning** between $m_Z^2 \text{ vs } |\mu|^2 + m_{H_U}^2$ **Light gluino & stops** keep $m_{H_U}^2$ near weak-scale Higgsino μ parameter **probes MSSM naturalness condition at tree-level**

Stop sensitivity approaching 1 TeV

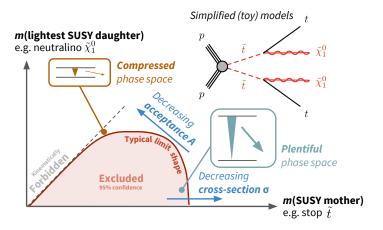


2015–17: formidable efforts to probe **'diagonal regions': objects typically soft** From ATLAS SUSY summary plots

How to read typical SUSY simplified model exclusion plots



How to read typical SUSY simplified model exclusion plots



THE SEARCHLIGHT IS SHIFTING from spectacular to subtle discoveries



Opportunities & challenges for **soft, rare, quirky signals**

Soft stuff Particle identification Trigaer thresholds

Rare SUSY

Colourless sparticles Dark sector

Quirky creatures

Displaced difficulties Long-lived exotica

> Case study *Higgsino*

HUNTING HIGGSINOS

A benchmark for probing the soft, rare & long-lived frontiers

Mass splitting governed by electroweak mixing [e.g. arXiv:1704.01577]

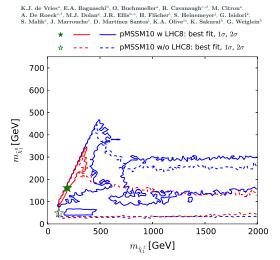
$$\Delta m(\tilde{\chi}_{2}^{0}, \tilde{\chi}_{1}^{0}) \simeq \frac{m_{W}^{2}}{g_{2}^{2}} \left(\frac{g_{1}^{2}}{M_{1}} + \frac{g_{2}^{2}}{M_{2}} \right)$$

Like W^{\pm} and Z boson masses ~ 10% apart due to EW mixing

 $g_1: U(1)_Y$ coupling, M_1 : mass of **bino** \widetilde{B} (fermionic partner of $U(1)_Y$ boson) $g_2: SU(2)_L$ coupling, M_2 : mass of **winos** \widetilde{W} (fermionic partners of $SU(2)_L$ bosons)

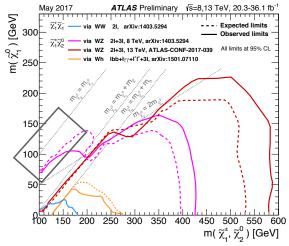
Data-driven motivations: compressed chargino-neutralinos favoured by global fits

The pMSSM10 after LHC Run 1



Green star is best fit to collider & non-collider data in 10-dim parameter space [1504.03260]

Striking gaps in ATLAS sensitivity



 $pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^{\pm}$ (wino) $\rightarrow W^{(*)} Z^{(*)} \tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow \text{leptons} + E_T^{\text{miss}}$

'Smoking-gun' lamppost of high p_T objects is focus of first LHC searches. Confront the **soft lepton frontier** to open sensitivity to diagonal.

Theorists very active in this area recently

Nearly Degenerate Gauginos and Dark Matter at the LHC

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b Department of Physics, University of Wisconsin, Madison, WI 53706, USA

- ^e Institute for the Physics and Mathematics of the Universe,
 - University of Tokyo, Kashiwa, Chiba 277-8568, Japan

^d Department of Physics, Princeton University, Princeton, NJ 08540, USA

1004.4902

Cornering electroweakinos at the LHC

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^aEnrico Fermi Institute and Department of Physics, University of Chicago, Chicago, IL, 60637

^bHEP Division, Argonne National Laboratory, 9700 Cass Ave., Argonne, IL 60439 ^cSchool of Physics, Korea Institute for Advanced Study, Seoul 130-722, Korea ^dKavli Institute for Cosmological Physics, University of Chicago, Chicago, IL, 60637

1307.5952

Monojet plus soft dilepton signal from light higgsino pair production at LHC14

Hunting Quasi-Degenerate Higgsinos

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1401.1235

Howard Baer^{1,2*}, Azar Mustafayev^{3†} and Xerxes Tata^{3§}

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1409.7058

A boost for the EW SUSY hunt: monojet-like search for compressed sleptons at LHC14 with $100~{\rm fb}^{-1}$

M_{T2} to the Rescue – Searching for Sleptons in Compressed Spectra at the LHC

Zhenyu Han Institute for Theoretical Science, University of Oregon, Eugene, OR 97403, USA

Yandong Liu Department of Physics and State Key Laboratory of Nuclear Physics and Technology. Peking University. Beijing 100871, China

1412.0618

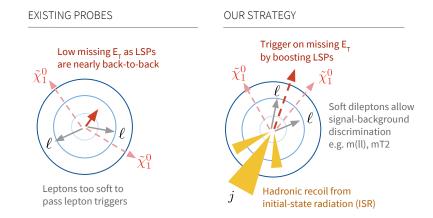
Alan Barr,^a James Scoville^{a,b}

^aDepartment of Physics, Denys Wilkinson Building, Keble Road, Oxford OX1 3RH, UK
^bUnited States Air Force Institute of Technology, Wright-Patterson Air Force Base, OH 45433, USA

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1501.02511

ATLAS & CMS Collaborations listened & looked



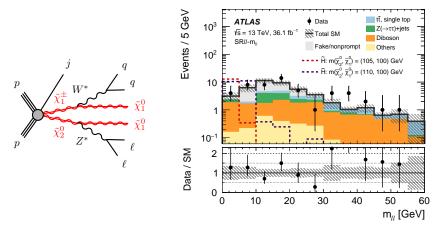
ATLAS 1712.08119 [ATLAS-SUSY-2016-25]

Trigger on E_T^{miss} , offline $E_T^{\text{miss}} > 200$ GeV, perform compressed sleptons search too

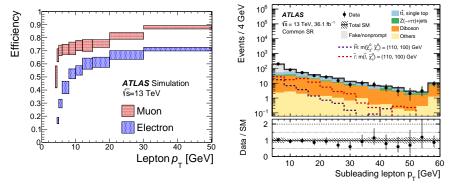
CMS 1801.01846 [CMS-SUS-16-048]

Also $2\mu + E_T^{\text{miss}}$ triggers, offline $E_T^{\text{miss}} > 125$ GeV, perform compressed stop search too

Signals localised at low $m_{\ell\ell}$: bump-hunt SUSY style!



Sensitivity driven by $\tilde{\chi}_2^0 \rightarrow \ell^+ \ell^- \tilde{\chi}_1^0$ (same-flavour opposite-sign) Signal kinematic endpoint: $m_{\ell\ell} < \Delta M(\tilde{\chi}_2^0, \tilde{\chi}_1^0)$ gives dramatic background discrimination



How well we reconstruct leptons from signals

Lepton with lower transverse momentum

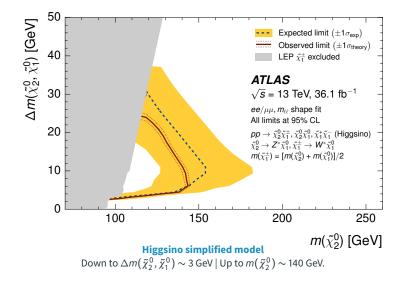
Confronting experimental limitations of soft lepton reconstruction crucial for sensitivity

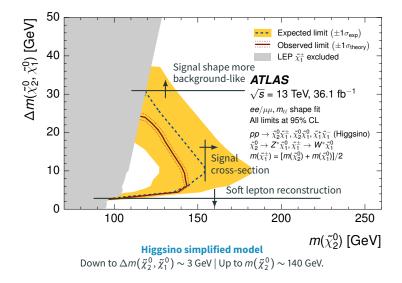
Fun fact: a muon loses 3 GeV of energy before reaching the ATLAS muon spectrometer Soft lepton regime dominated by challenging fake/nonprompt lepton* backgrounds

*These include misidentified jets, photon conversions, semi-leptonic decays of B-hadrons, pileup

LHC HIGGSINO SENSITIVITY

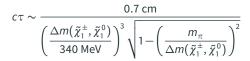
A hadron collider extends nearly 20 year old LEP limits





Recall particle lifetime inversely related to phase space.

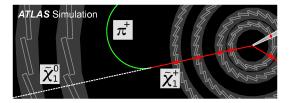
Pure Higgsino (ultra-compressed) limit, chargino becomes long-lived



From Fukuda, Nagata, Otono, Shirai [arXiv:1703.09675], ATL-PHYS-PUB-2017-019

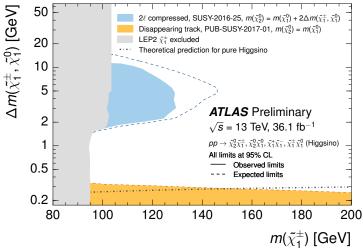
Signature: partial 'disappearing' track

(Trigger on E^{miss} from ISR)



How do we close the Higgsino prompt-long-lived gap?

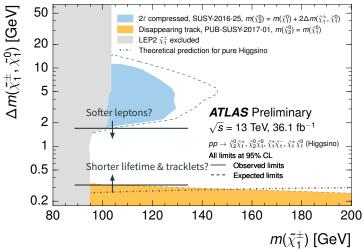
December 2017



Sub-100 GeV Higgsinos in 0.3 $\lesssim \Delta m(\tilde{\chi}_1^{\pm}, \tilde{\chi}_1^0) \lesssim$ 2 GeV regime remain viable!

How do we close the Higgsino prompt-long-lived gap?

December 2017



Need new techniques to overcome limiting factors in sensitivity

REFLECTIVE EPILOGUE

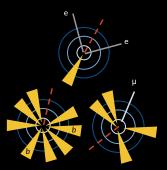
Being PhD students amidst confusion in fundamental physics

Expectation: a new golden age of striking discoveries + robust measurement

Signature storm

 \rightarrow particle zoo -

underlying theory





 $\mathcal{L}(old) + \mathcal{L}(new)$

Supersymmetry? Dark matter? Extra dimensions? Hidden gauge sectors? Exciting exotica?

What is the structure of new physics data?

Use simplified models to organise kinematics & structures in data as **detector-independent signatures**.

E.g. Alwall, Schuster, Toro [arXiv:0810.3921]

How do we measure mass, spin, coupling?

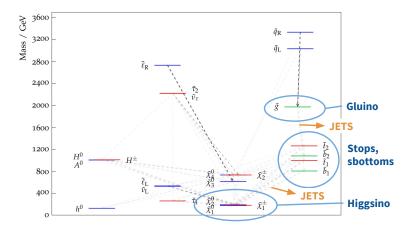
Timing, tracking, flavour, angles, endpoints, proxies like mT, mT2 to perform spectroscopy.

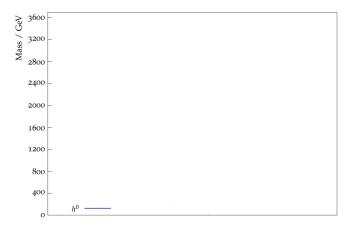
E.g. Barr, Gripaios, Lester [arXiv:0711.4008]

Which underlying theory is it?

Two distinct theories can give the same signature: study how to lift signature degeneracies.

E.g. Arkani-Hamed, Kane, Thaler, Wang [hep-ph/0512190]





A GOLDEN AGE FOR NEW IDEAS

Actually, striking opportunities for critical reflection & fruitful innovation

How can experimentalists open uncharted sensitivity?

Use detector beyond original design goals e.g. soft lepton frontier, new triggers Explore exotic signatures at lifetime frontier [LLP workshops]

What is the nature of dark matter?

Dark sector potentially rich & vast beyond vanilla WIMP paradigm Sub-GeV thermal relics? Sub-MeV ultra-light particles? Table-top frontier? [e.g. 1707.04591]

Why is naturalness not a robust guide for new physics?

Critically re-examine long-standing theoretical assumptions E.g. Cosmological relaxation? [1504.07551] Nnaturalness? [1607.06821]

Gratitude



Bucharest

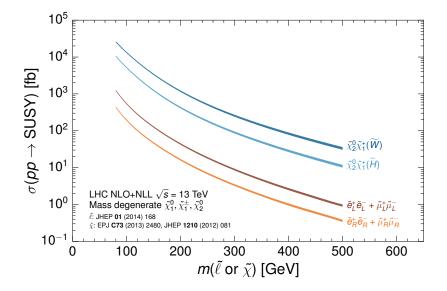


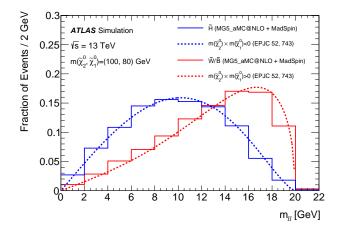
Geneva

Thanks to excellent leadership and collaboration of international analysis team from British Columbia, Cambridge, Harvard, Milano, Oklahoma, Santa Cruz, UPenn, Urbana–Champaign, Valencia, Würzburg et al across 9 time zones

Thanks to CERN, ATLAS Experiment, STFC, Oxford for support & hospitality

EXTRAS





LHC can probe composition of electroweakinos i.e. underlying SUSY parameters $m_{\ell\ell}$ shape differs for Higgsino \tilde{H} vs wino-bino \tilde{W}/\tilde{B} scenarios. Using MadSpin to model $\tilde{\chi}_2^0 \rightarrow \ell^+ \ell^- \tilde{\chi}_1^0$ decays to match predicted shape.

Background estimation strategy: schematic overview

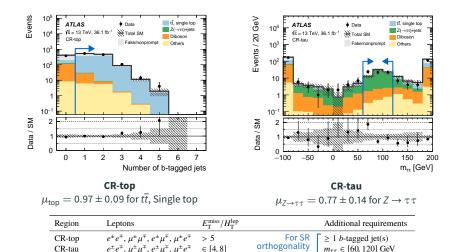
Prediction Mix of data & MC methods	Signal region Same flavour leptons	Validation Check background modelling	
Fake Factor Data-driven method	≥ 1 lepton fake/non-prompt > 50% at low lepton pT	VR-SS MET/HT(lep) > 5.	VR-DF
CR-top N(b-jets) ≥ 1 ttbar, tW MC normalisation	E.g. W+jets Top quark 2L ttbar & tW missed b-jet Z $\rightarrow \tau\tau$ 2L decays Diboson WW 2L WZ missed 3rd lepton Others E.g. $Z \rightarrow ee/\mu\mu$, Higgs	Same sign leptons. Fakes purity > 90%.	Different flavour leptons. Exactly the same kinematic regimes as SRs. Global check of background modelling.
CR-tau 60 < m(ττ) < 120 GeV MC normalisation		VR-VV MET/HT(lep) < 3. Diboson purity ~40%.	
Monte Carlo only Monte Carlo only			

Irreducible: 2 real & prompt leptons and MET from neutrinos

Reducible: ≥ 1 or more fake/non-prompt lepton(s), instrumental MET (negligible)

List of MC samples in backup p??, more details of strategy in backup p??.

Control regions for irreducible backgrounds



Background-only fit to CR-top & CR-tau (each single-bins).

This derives normalisation factors μ_{top} , $\mu_{Z \rightarrow \tau \tau}$ respectively.

Highlight ATLAS $2\ell + E_T^{miss}$ + ISR search

	Variable	Common requirement
	Number of leptons	= 2
Select 2 soft SFOS leptons	Lepton charge and flavour	e^+e^- or $\mu^+\mu^-$
Select 2 solt SPOS leptons	Leading lepton $p_{\rm T}^{\ell_1}$ Subleading lepton $p_{\rm T}^{\ell_2}$	> 5 (5) GeV for electron (muon)
	Subleading lepton $p_{\rm T}^{\ell_2}$	> 4.5 (4) GeV for electron (muon)
Conversions/fake muons	$\Delta R_{\ell\ell}$	> 0.05
Drell-Yan resonances	$m_{\ell\ell}$	∈ [1, 60] GeV excluding [3.0, 3.2] GeV
	$E_{\mathrm{T}}^{\mathrm{miss}}$	> 200 GeV
Select ISR topology	Leading jet $p_{\rm T}^{j_1}$	> 100 GeV
	Leading jet $p_{\rm T}^{j_1}$ $\Delta \phi(j_1, \mathbf{p}_{\rm T}^{\rm miss})$	> 2.0
Mis-measured jets	$\min(\Delta \phi(\text{any jet}, \mathbf{p}_{T}^{\text{miss}}))$	> 0.4
Top quarks	Number of <i>b</i> -jets	= 0
$Z \rightarrow \tau \tau$	$m_{\tau\tau}$	< 0 or > 160 GeV

Same-flavour opposite sign (SFOS) signature

Higgsino sensitivity dominated by $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0(Z^* \rightarrow \ell^+ \ell^-)$.

Select ISR topology

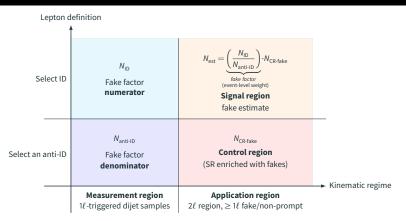
 $E_{\rm T}^{\rm miss} > 200 \,{\rm GeV}, p_{\rm T}^{j_1} > 100 \,{\rm GeV}, \Delta \phi(j_1, {\bf p}_{\rm T}^{\rm miss}) > 2.0.$

Suppress backgrounds

Other common requirements reduce various backgrounds labelled above.

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Schematic of data-driven Fake Factor method



Numerator (denominator) intuition: given fake leptons, fraction that pass (fail) signal requirements.

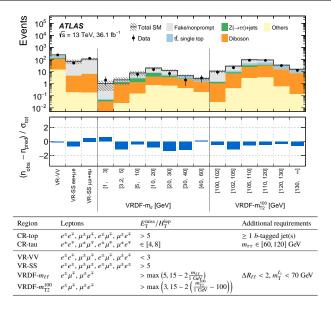
ID Electrons: Tight identification, GradientLoose isolation. ID Muons: Medium identification, FixedCutTightTrackOnly isolation.

ID leptons: same as signal leptons | Anti-ID leptons: invert \geq 1 ID requirements.

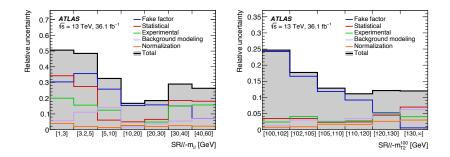
Bin in p_T for $e \& \mu$, bin in N_{b-iet} only for μ fake factors.

Fake Factor developed in H to WW analysis. Studied fake composition in MC (mostly heavy flavour), optimised object definitions. Opening unexplored frontiers for new physics at the LHC | Jesse Liu | 10 Jan 2018

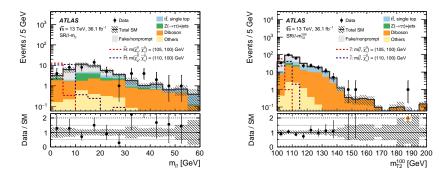
Summary of background estimation validation



Breakdown of systematics in SRs



Electroweakino and slepton SRs

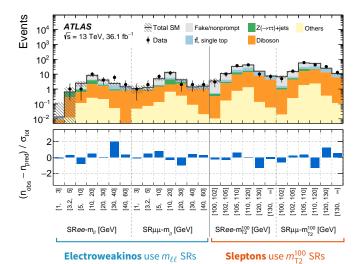


Variable	Common requirement			
Number of leptons	= 2			
Lepton charge and flavour	e^+e^- or $\mu^+\mu^-$			
Leading lepton $p_T^{\ell_1}$	> 5 (5) GeV for electron (muon)			
Subleading lepton $p_T^{\ell_2}$	> 4.5 (4) GeV for electron (muon)			
$\Delta R_{\ell\ell}$	> 0.05			
$m_{\ell\ell}$	∈ [1,60] GeV excluding [3.0, 3.2] GeV			
E_{T}^{miss}	> 200 GeV			
Leading jet $p_T^{j_1}$	> 100 GeV			
$\Delta \phi(j_1, \mathbf{p}_T^{\text{miss}})$	> 2.0			
$min(\Delta \phi(any jet, \mathbf{p}_T^{miss}))$	> 0.4			
Number of b-jets	= 0			
m _{TT}	< 0 or > 160 GeV			
	Electroweakino SRs	Slepton SRs		
$\Delta R_{\ell\ell}$	< 2	-		
$m_T^{\ell_1}$	< 70 GeV	_		
physics at the LHC \ddagger Jesse Eiu $2 \frac{\pi}{100}$ Jan 201 $\left\{3, 15 - 2\left(\frac{m_{100}^{100}}{1 \text{ GeV}} - 100\right)\right\}$				
Binned in	$m_{\ell\ell}$	m ¹⁰⁰ _{T2}		

Opening unexplored frontiers for

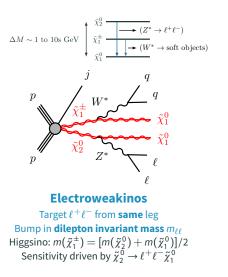
41

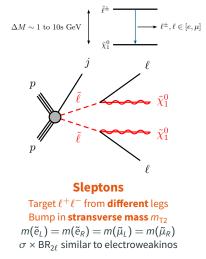
Electroweakino SRs								
Exclusive Inclusive	$SRee-m_{\ell\ell}, SR\mu\mu-m_{\ell\ell}$ $SR\ell\ell-m_{\ell\ell}$	[1, 3] [1, 3]	[3.2, 5] [1, 5]	[5, 10] [1, 10]	[10, 20] [1, 20]	[20, 30] [1, 30]	[30, 40] [1, 40]	[40, 60] [1, 60]
Slepton SRs								
Exclusive Inclusive	$\frac{\text{SR}ee\text{-}m_{\text{T2}}^{100},\text{SR}\mu\mu\text{-}m_{\text{T2}}^{100}}{\text{SR}\ell\ell\text{-}m_{\text{T2}}^{100}}$		[100, 102] [100, 102]	[102, 105] [100, 105]	[105, 110] [100, 110]	[110, 120] [100, 120]	[120, 130] [100, 130]	[130, ∞] [100, ∞]



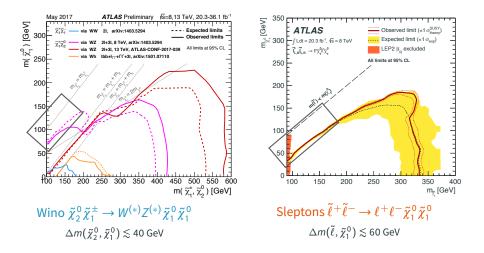
Make bins orthogonal, split by $ee/\mu\mu$ to statistically combine, improving exclusion.

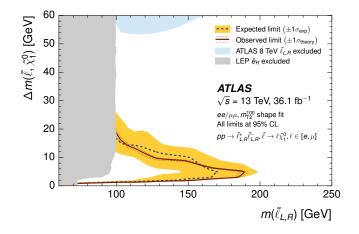
Showing fit with $\mu_{signal} = 0$.





Striking gaps in ATLAS sensitivity



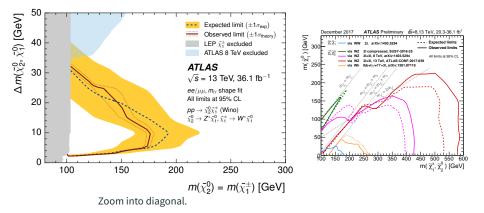


Slepton simplified model

Down to $\Delta M \sim 1 \text{ GeV} \mid \text{Up to } m(\tilde{\ell}) \sim 180 \text{ GeV}.$

2 years after being asked, realised Barr–Scoville [1501.02511] strategy using data! :) Moderately compressed gap $20 \lesssim m(\tilde{\ell}) - m(\tilde{\chi}_1^0) \lesssim 60$ GeV challenging due to e.g. WW. Opening unexplored frontiers for new physics at the LHC | Jesse Liu | 10 Jan 2018

Closing the ATLAS wino-bino gap

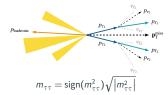


Wino-bino simplified model

Down to $\Delta M \sim 2.5 \text{ GeV} \mid \text{Up to } m(\tilde{\chi}_2^0) \sim 170 \text{ GeV}.$ Priority in 2018: close gap at $m(\tilde{\chi}_2^0) - m(\tilde{\chi}_1^0) \approx 30 \text{ GeV}.$

Simplified models considered		Slepton	Wino	
	Higgsino LSP	Bino LSP	Bino LSP	
Use in this analysis	Optimisation &	Interpretation		
Compression	Radiative/mixing	Accidental		
SM splitting analogy	W/Z bosons ~10% apart	Charm quark & tau lepton mass ~30% apart		
Desirable feature	Weak scale naturalness§	Resolve $(g-2)_{\mu}$ tension [%]	Favoured by global fits	
LSP as dark matter	'Well-tempered' mixing [£] Bino saturates relic density via coannihilati			
E.g. cross-sections [#]	$\begin{array}{l} m(\tilde{\chi}_{2^{\circ}}^{0},\tilde{\chi}_{1}^{\pm})=(110,105)\;GeV\\ \sigma(pp\to\tilde{\chi}_{2}^{0}\tilde{\chi}_{1}^{\pm})=4.3\;pb \end{array}$		$ \begin{array}{l} m(\tilde{\chi}_2^0 = \tilde{\chi}_1^{\pm}) = 110 \; GeV \\ \sigma(pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^{\pm}) = 16 \; pb \end{array} $	

E.g. arXiv: ⁵1110.6926, [%]1505.05896, **1504.0326, [£]hep-ph/0601041 [^]1508.06608, [#]Resummino NLO+NLL 1304.0790



The construction assumes the τ leptons decay products are nearly collinear.

 $p_{\tau_i} = p_{\ell_i} + p_{\nu_i}$. Then the τ momentum is a rescaling of the observable lepton momenta p_{ℓ_i}

$$p_{\tau_i} = (1 + \xi_i)p_{\ell_i} \equiv f_i p_{\ell_i}$$
, (7)

where $f_i \equiv 1 + \xi_i$. To solve for the two unknown scalars ξ_i , one constrains the neutrino momenta using the missing transverse momentum ¹ as Ref. [46] prescribes

$$\mathbf{p}_{T}^{miss} = \xi_{1} \mathbf{p}_{T}^{\ell_{1}} + \xi_{2} \mathbf{p}_{T}^{\ell_{2}}.$$
 (8)

Equation (8) assumes the lepton-invisible colinearity limit $p_{r_i} \simeq \xi_i p_{\ell_i}$ and comprises two independent constraints in the transverse plane for the two unknown scalars ξ_i . This is solved by performing 2 × 2 matrix inversion in for example the x-y transverse plane

$$\begin{pmatrix} \xi_1 \\ \xi_2 \end{pmatrix} = \frac{1}{p_x^{\ell_1} p_y^{\ell_2} - p_x^{\ell_2} p_y^{\ell_1}} \begin{pmatrix} p_x^{miss} p_y^{\ell_2} - p_x^{\ell_2} p_y^{miss} \\ p_y^{miss} p_x^{\ell_1} - p_x^{miss} p_y^{\ell_1} \end{pmatrix}.$$
(9)

Assuming highly boosted taus such that $m_{T_{\ell}}^2 \simeq 0$, the di-tau invariant mass squared is then given by

$$m_{\tau\tau}^2 = (p_{\tau_1} + p_{\tau_2})^2 \simeq 2p_{\ell_1} \cdot p_{\ell_2}(1 + \xi_1)(1 + \xi_2).$$
 (10)

 $m_{\tau\tau}^2$ can go negative when $f_i \equiv 1 + \xi_i < 0$. This happens when one of the leptons is anti-aligned with $\mathbf{p}_T^{\text{miss}}$ and $E_T^{\text{miss}} > |\mathbf{p}_T^\ell|$, such that the rescaling has to invert the direction to approximate the tau-momentum.

In slepton-pair production (Figure 1(b)), the event topology can be used to infer the slepton mass given the LSP mass. The stransverse mass [37, 38] is defined by

$$m_{\text{T2}}^{m_{\chi}}\left(\mathbf{p}_{\text{T}}^{\ell_{1}}, \mathbf{p}_{\text{T}}^{\ell_{2}}, \mathbf{p}_{\text{T}}^{\text{miss}}\right) = \min_{\mathbf{q}_{\text{T}}}\left(\max\left[m_{\text{T}}\left(\mathbf{p}_{\text{T}}^{\ell_{1}}, \mathbf{q}_{\text{T}}, m_{\chi}\right), m_{\text{T}}\left(\mathbf{p}_{\text{T}}^{\ell_{2}}, \mathbf{p}_{\text{T}}^{\text{miss}} - \mathbf{q}_{\text{T}}, m_{\chi}\right)\right]\right)$$

where the transverse vector \mathbf{q}_{T} is chosen to minimize the larger of the two transverse masses, defined by

$$m_{\mathrm{T}}\left(\mathbf{p}_{\mathrm{T}},\mathbf{q}_{\mathrm{T}},m_{\chi}\right) = \sqrt{m_{\ell}^{2} + m_{\chi}^{2} + 2\left(\sqrt{p_{\mathrm{T}}^{2} + m_{\ell}^{2}}\sqrt{q_{\mathrm{T}}^{2} + m_{\chi}^{2}} - \mathbf{p}_{\mathrm{T}}\cdot\mathbf{q}_{\mathrm{T}}\right)}.$$

The values of $m_{T2}^{m_{\chi}}$ are bounded by the slepton mass from above when the hypothesis invisible mass m_{χ} is set to the LSP mass. The stransverse mass m_{T2}^{100} with $m_{\chi} = 100$ GeV is used to define the binning of the slepton SRs as further described below. The value of 100 GeV is chosen based on the expected LSP masses of the slepton signals targeted by this analysis.