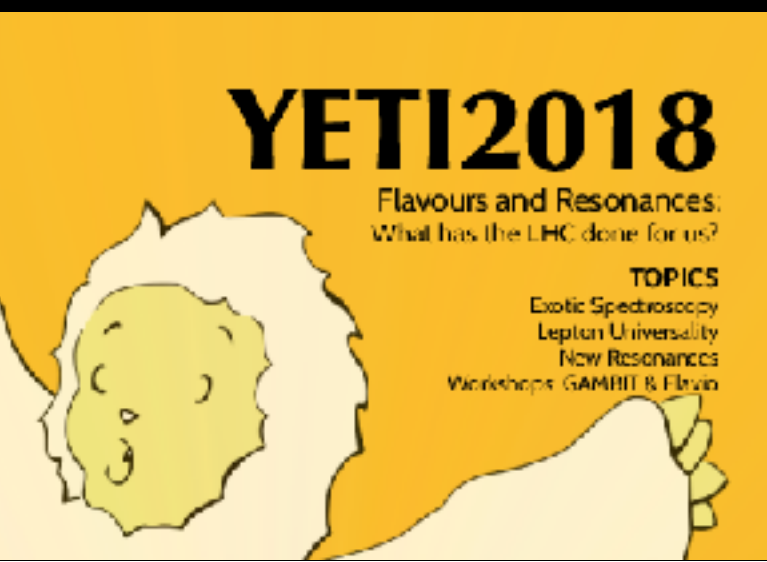
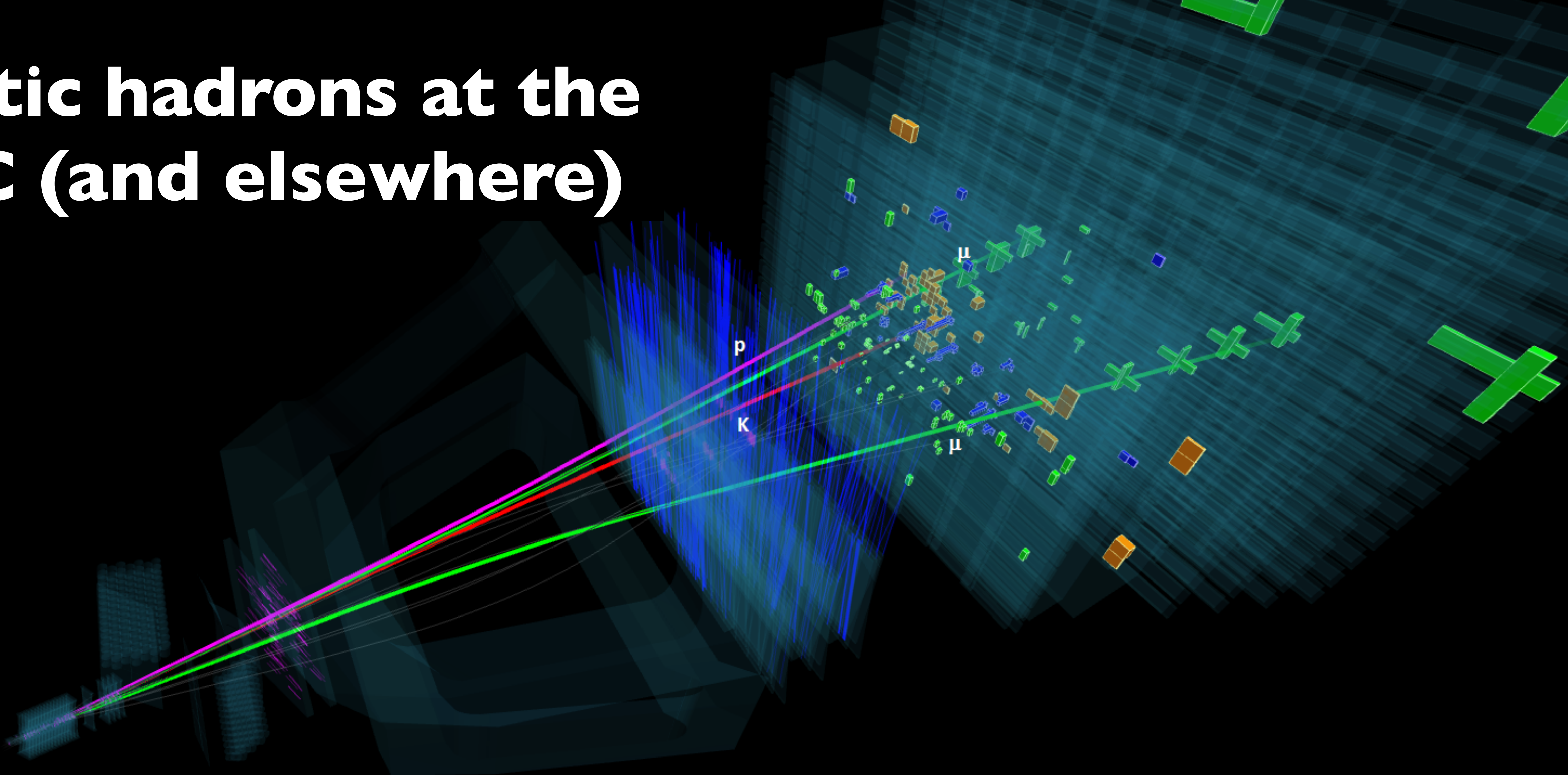


Exotic hadrons at the LHC (and elsewhere)



 [@GreigCowan](https://twitter.com/GreigCowan) (Edinburgh)
YETI 2018
IPPP Durham



Science & Technology
Facilities Council

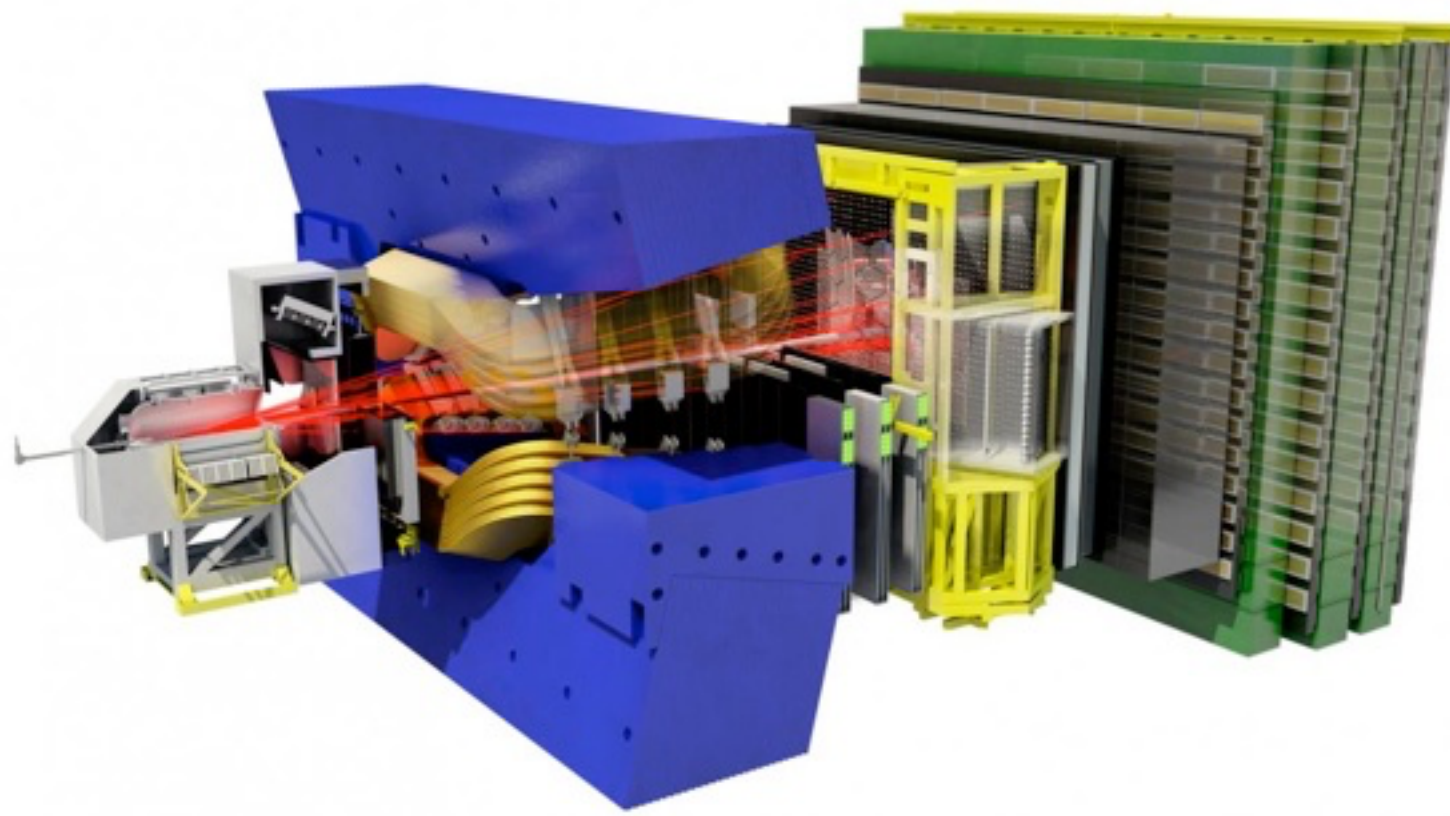
Rough outline

See lecture from A.Alves for details on many experimental analysis methods

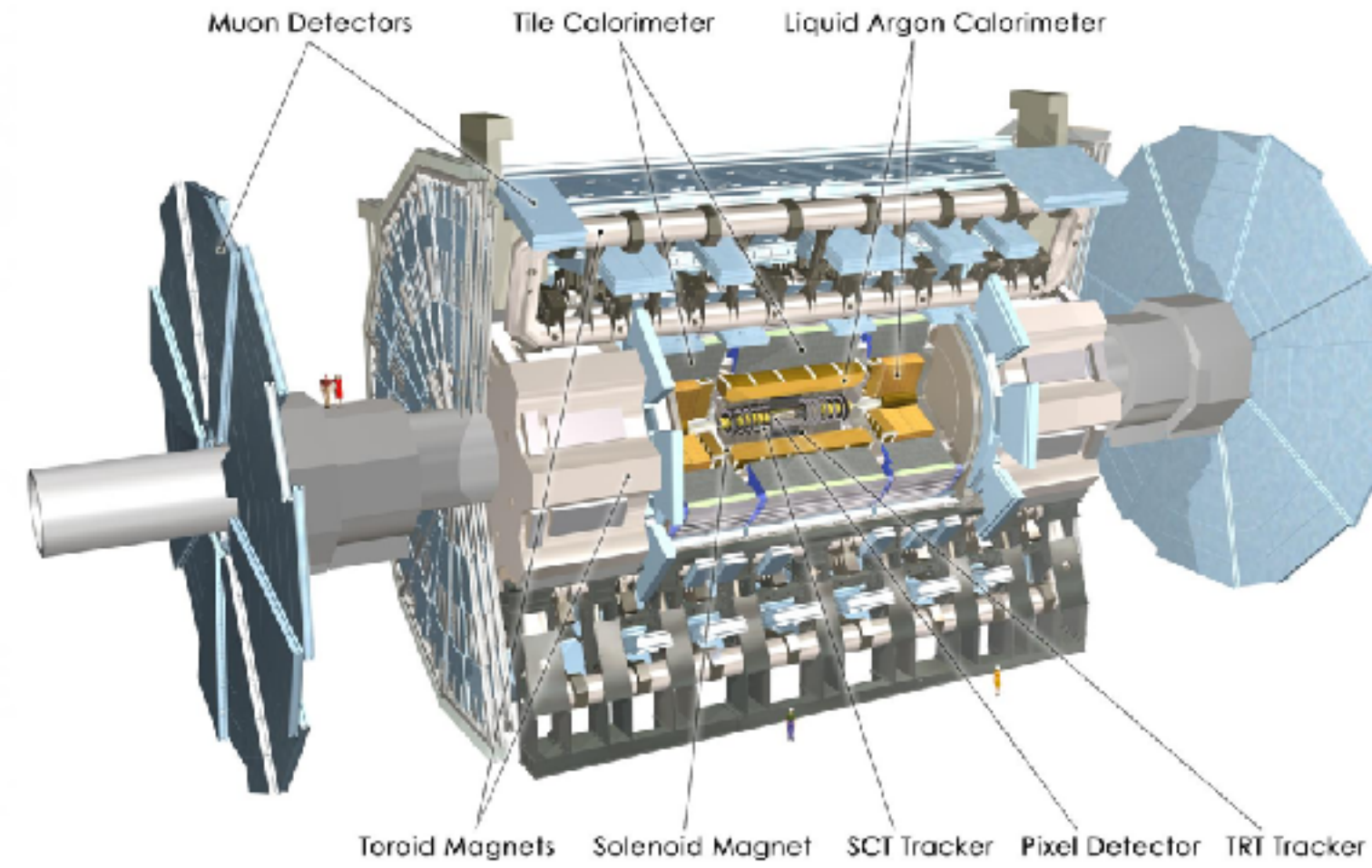
1. Experimental facilities
2. The quark model → new results about “conventional” baryons
3. The charmonium system as a portal to exotic hadrons
 - a. Tetraquarks
 - b. Pentaquarks

Experimental facilities

LHCb

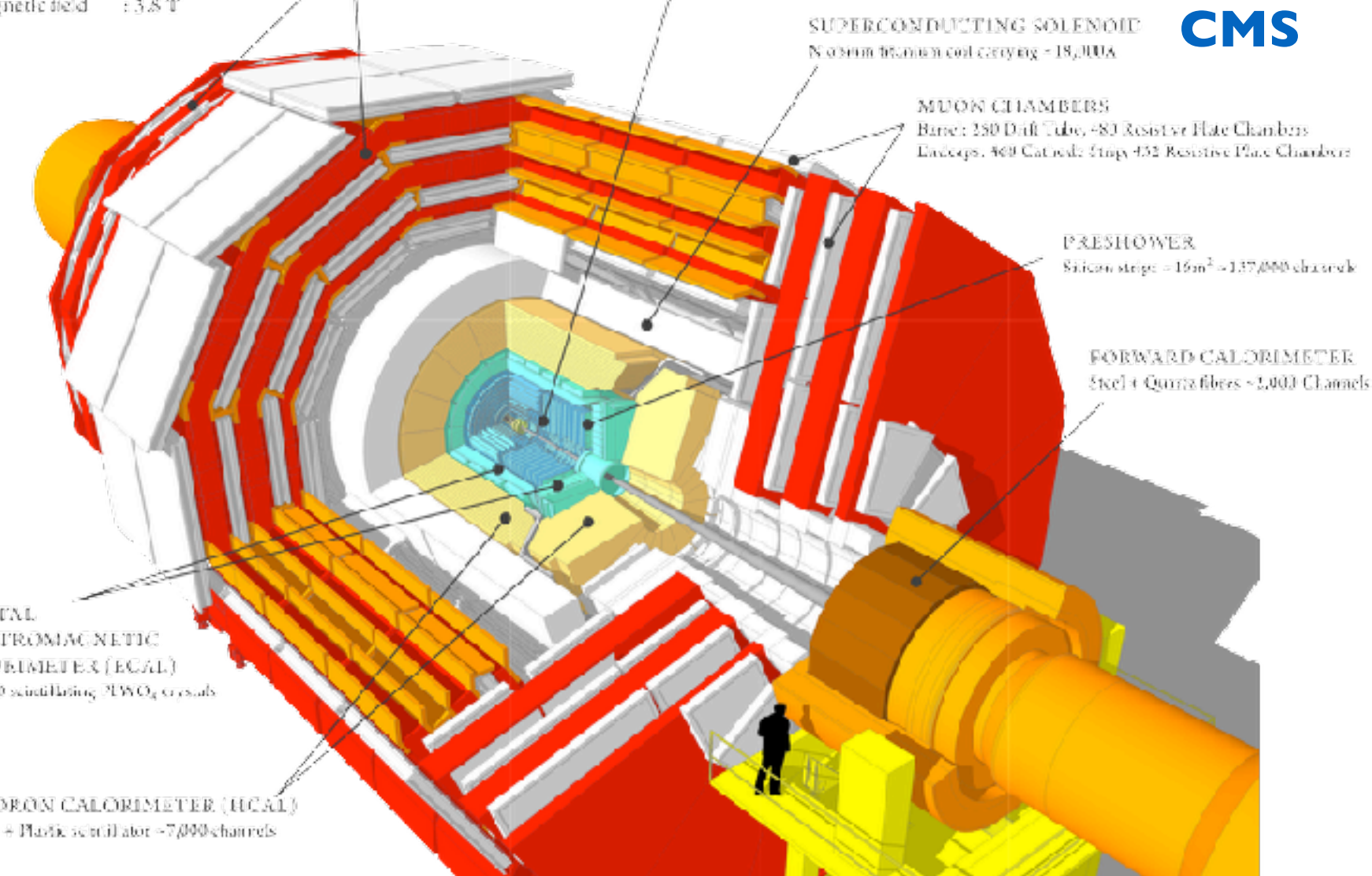


ATLAS



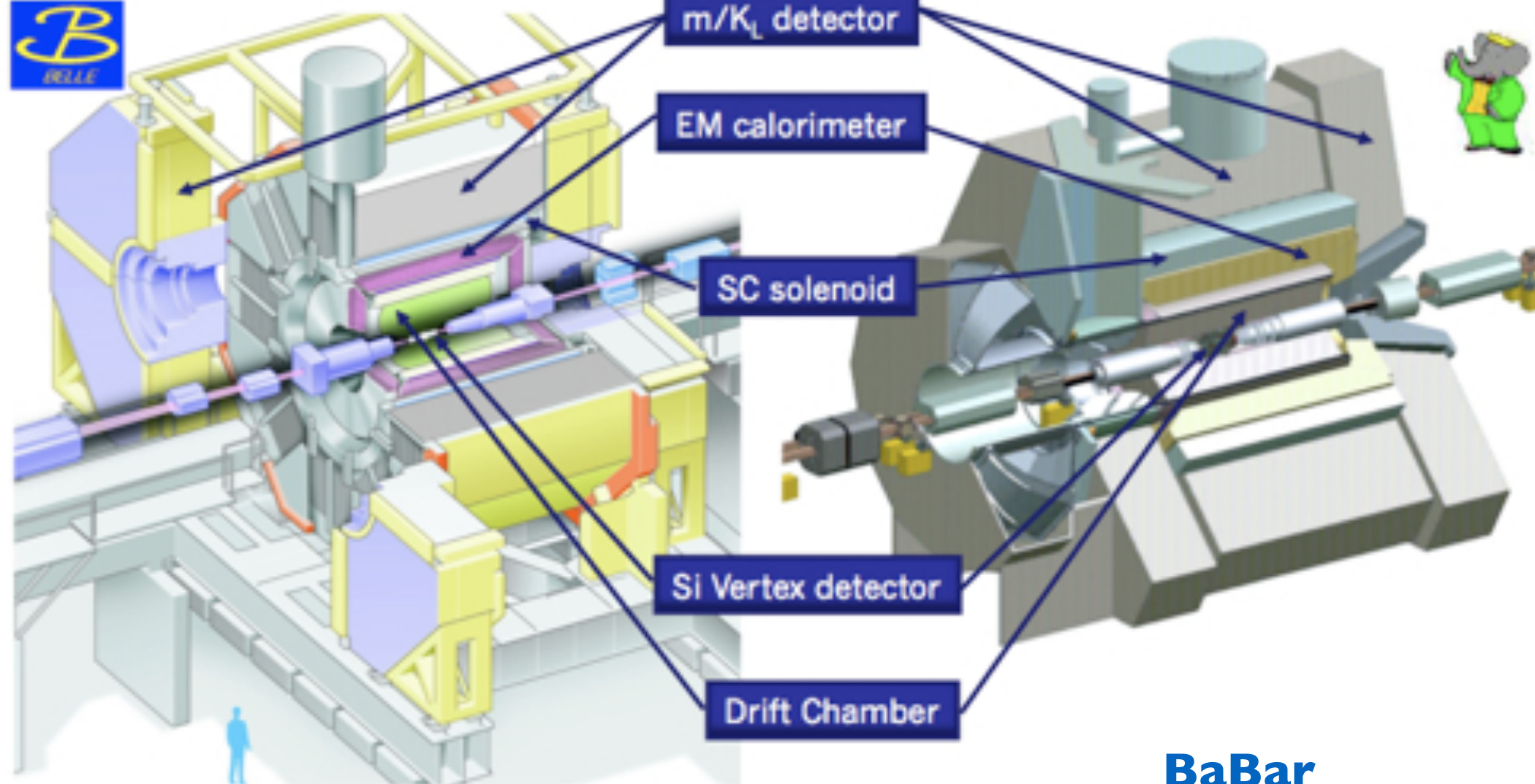
CMS DETECTOR

Total weight : 14,000 tonnes
 Overall diameter : 15.0 m
 Overall length : 28.7 m
 magnetic field : 3.8 T



CMS

Belle



BaBar

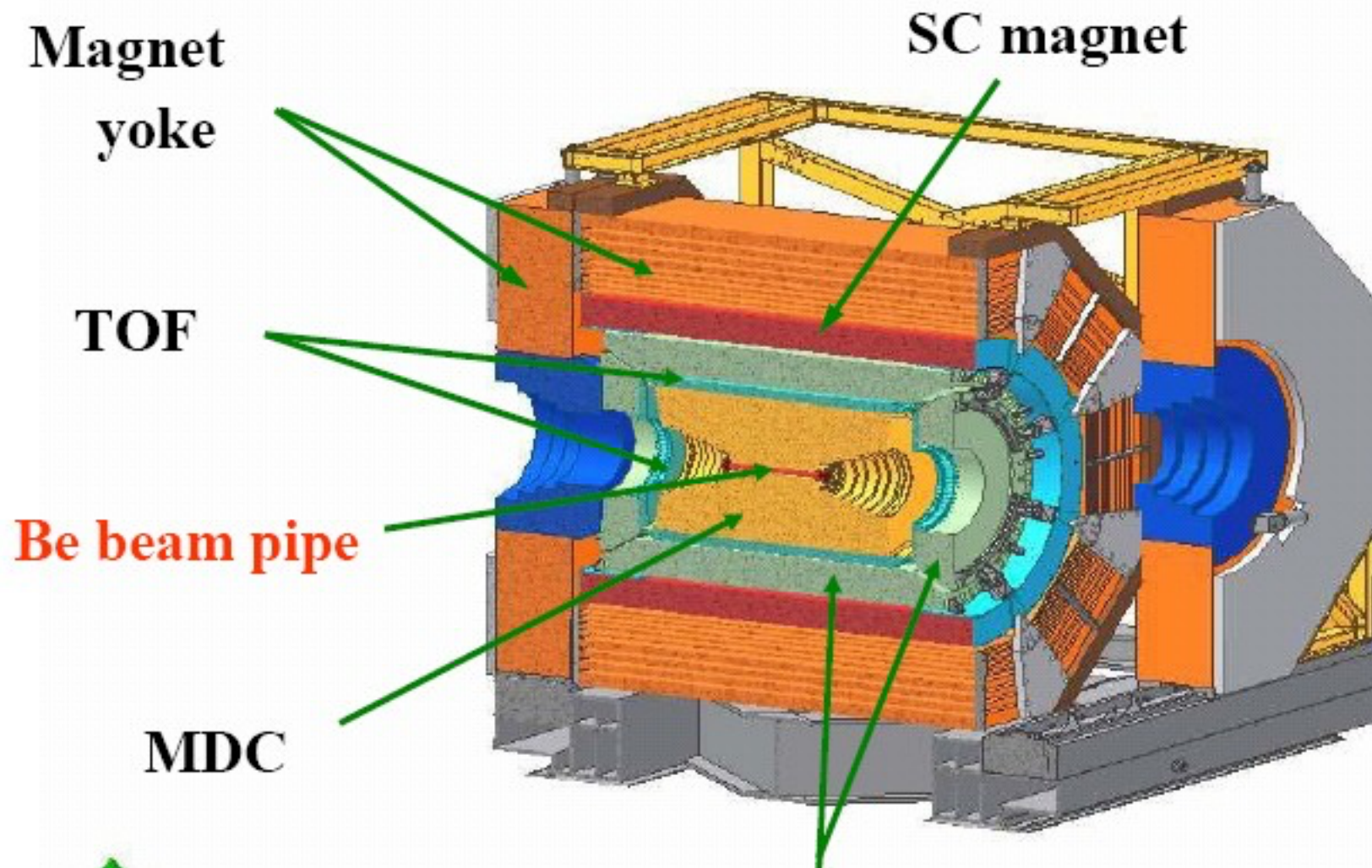
Magnet yoke

TOF

Be beam pipe

MDC

SC magnet



CsI calorimeter

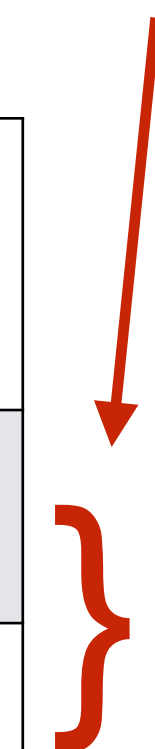
BES-III

+ **CDF, D0 @ Tevatron**
 + **CLEO**

Experimental facilities

B-factories

Experiments	Laboratory	Collider	Production environment	Approximate operational period
Belle/Belle-II	KEK, Japan	KEKB	$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$	1999-2010 (2018-2025)
BaBar	SLAC, USA	PEP-II	$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$	1999-2008
CDF/D0	Fermilab, USA	Tevatron	$p\bar{p} \rightarrow b\bar{b}X$ (2 TeV)	1987-2011
BES-III	IHEP, China	BEPC	$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$	2008-present
CLEO	Cornell, USA	CESR	$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$	~2000
ATLAS/CMS/LHCb	CERN, Switzerland	LHC	$pp \rightarrow b\bar{b}X$ (7-13 TeV)	2011-present



+ **COMPASS (CERN)** and **CLAS/GlueX (Jefferson Lab)** fixed target experiments

The birth of the quark model

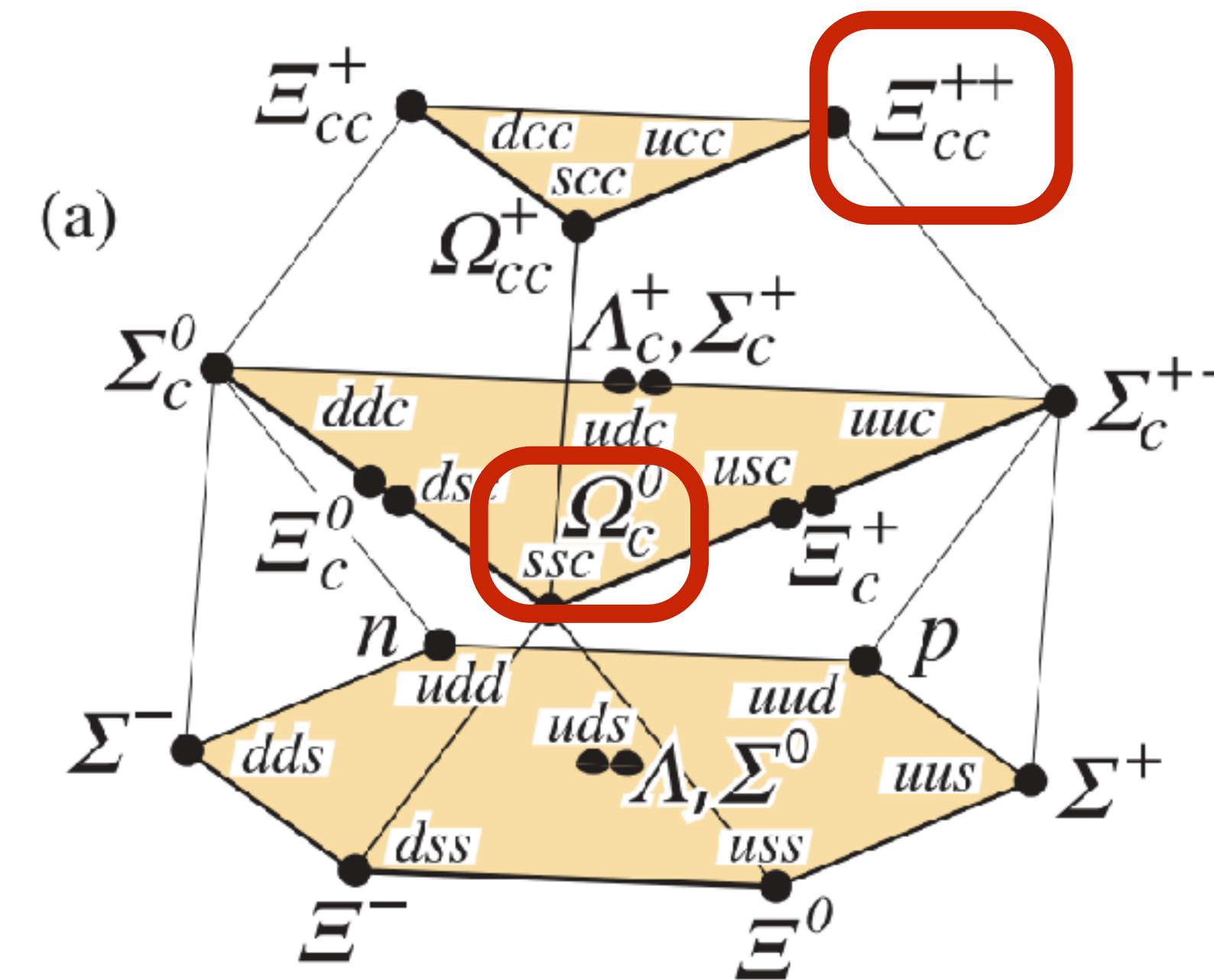
Volume 8, number 3 PHYSICS LETTERS 1 February 1964

A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN
California Institute of Technology, Pasadena, California

Received 4 January 1964

We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" q and the members of the anti-triplet as anti-quarks \bar{q} . Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. It is assuming that the lowest



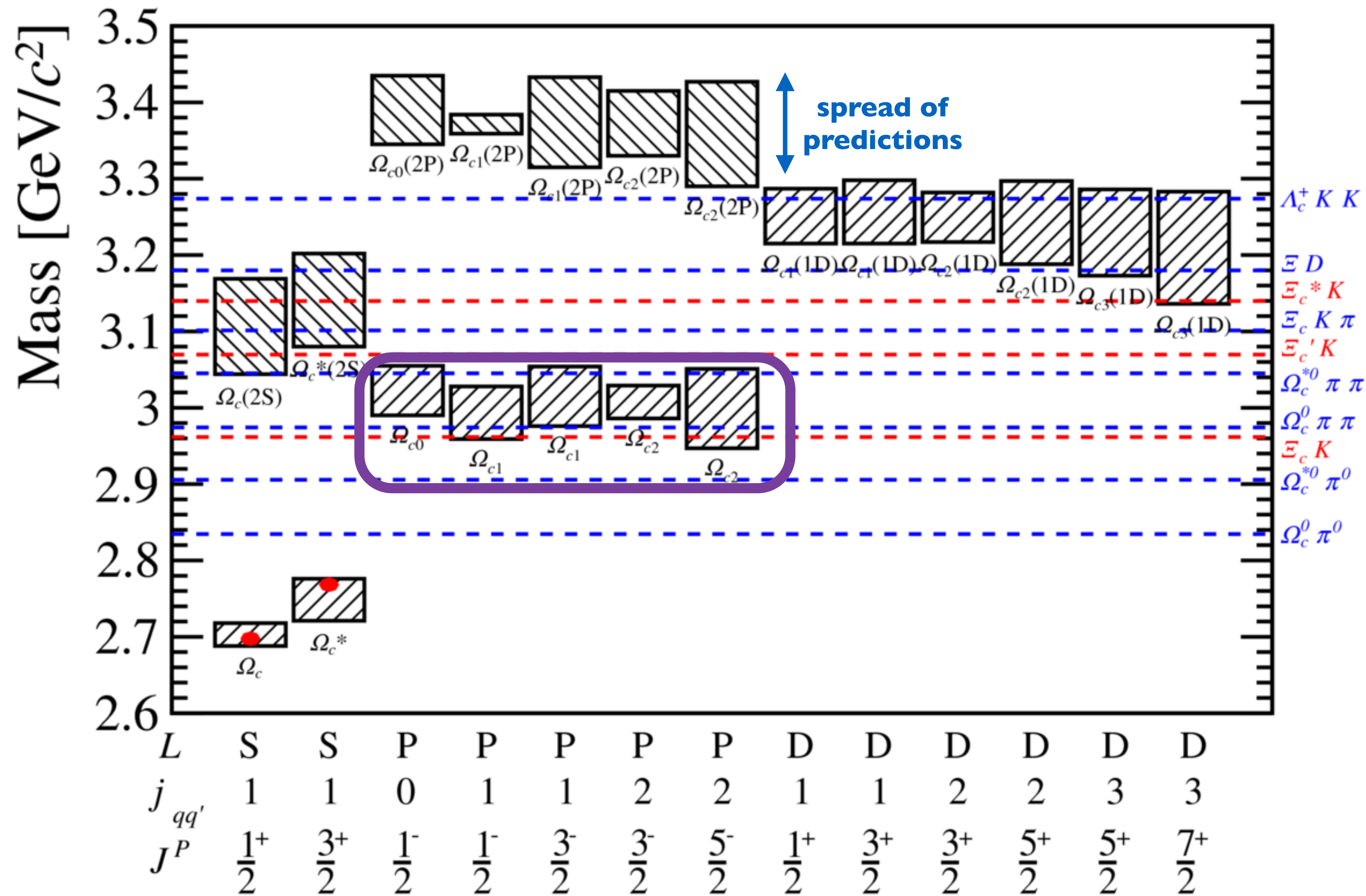
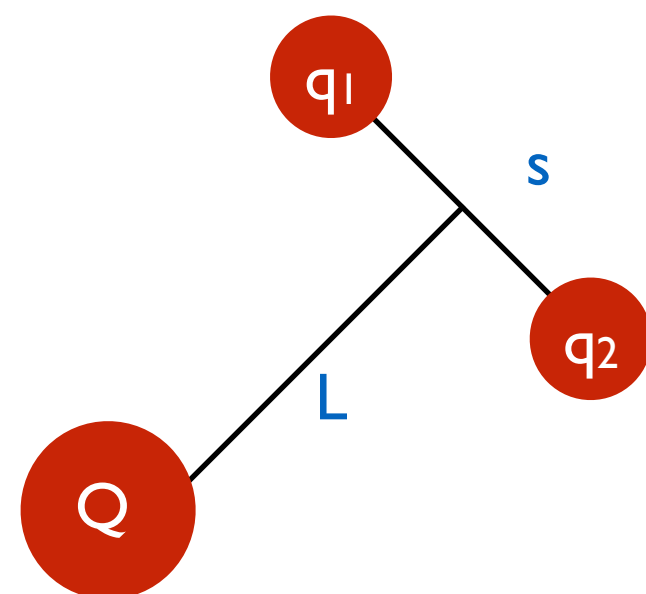
Quarks as the building blocks of mesons and baryons was first proposed in 1964 by Gell-Mann and Zweig

Strange-charm baryons

The **CSS** system can be used to test HQET and Lattice, as many states expected

Static heavy quark (Q) + light **ss** diquark

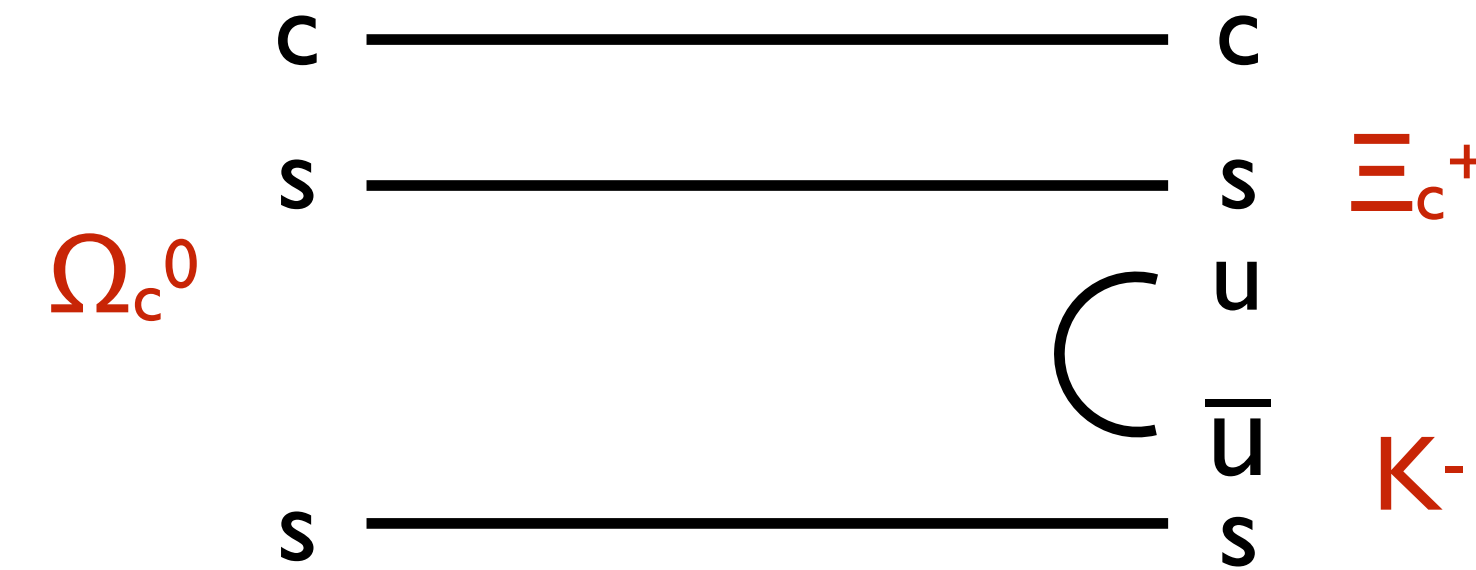
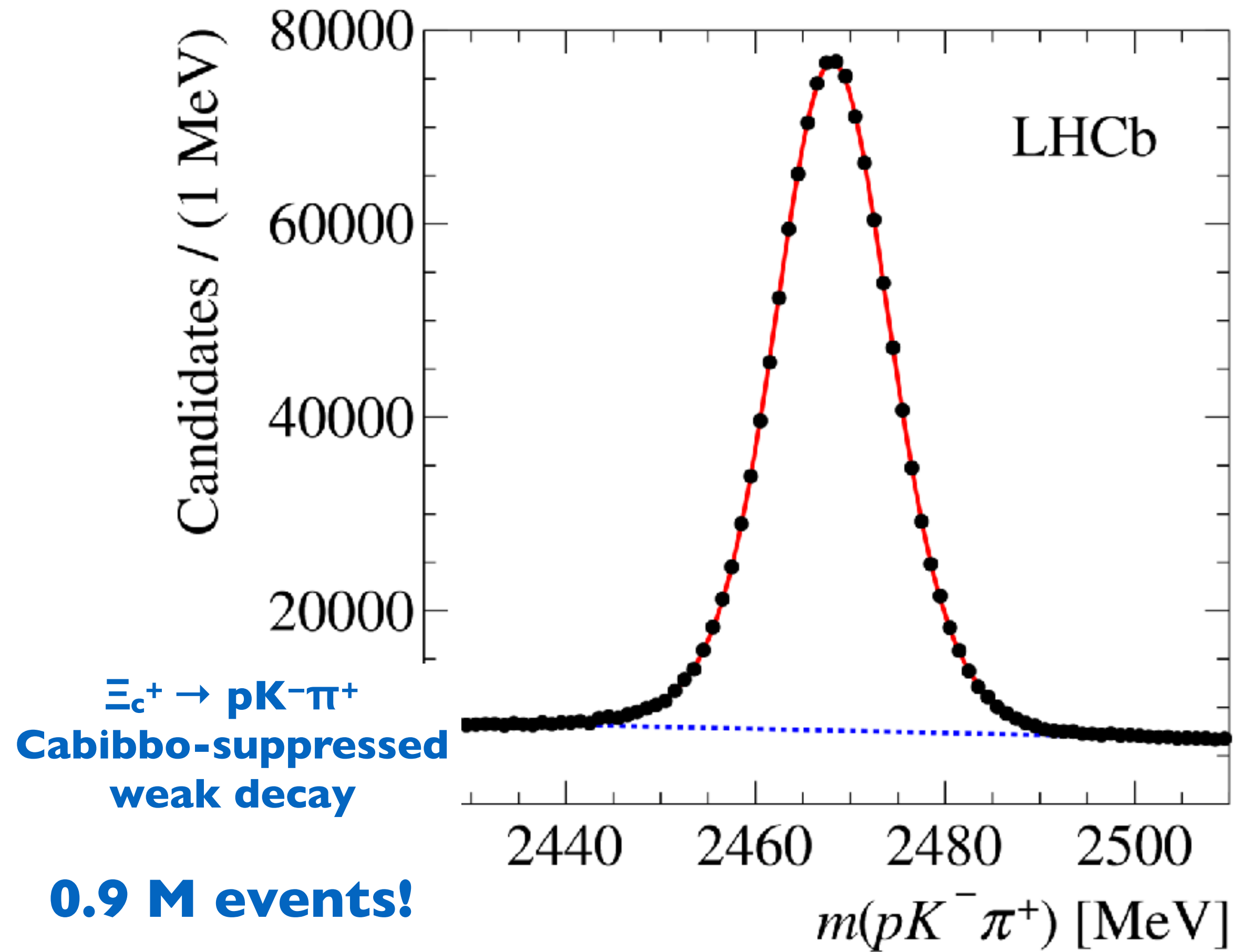
5 P-wave states predicted (*)



(*) 7 if you include possible excitations between the quarks in the diquark

Strange-charm baryons

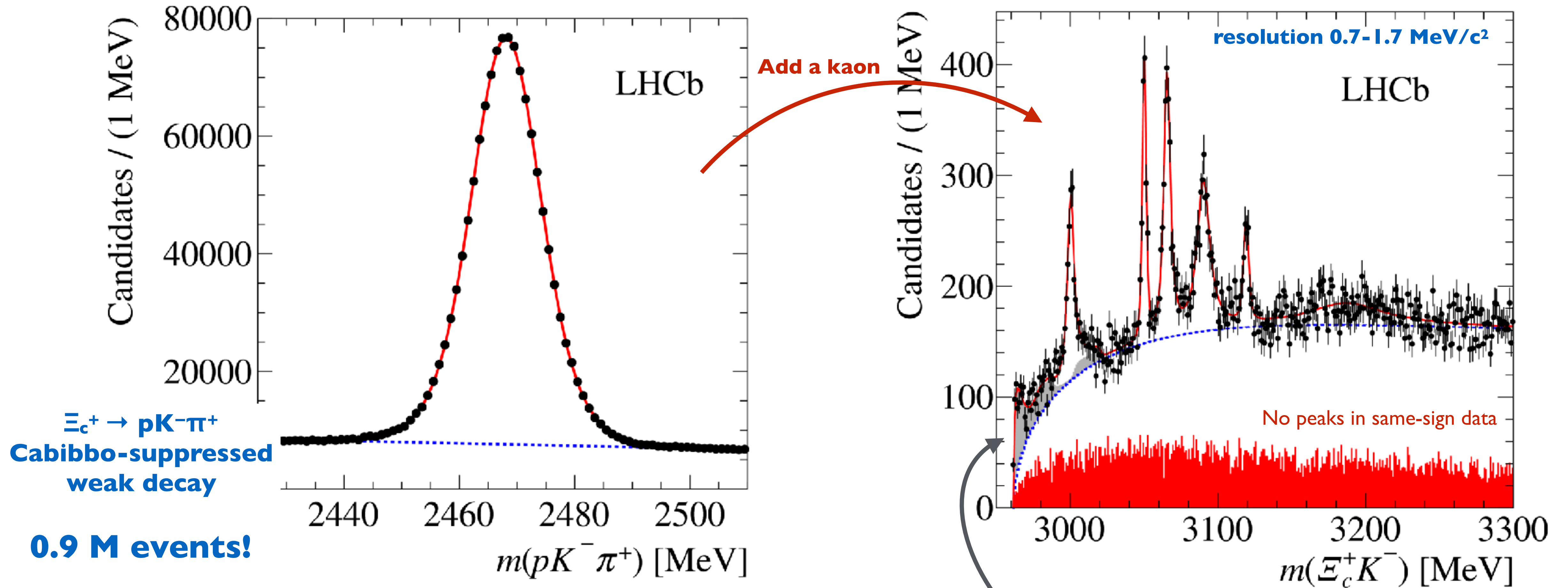
[PRL 118 (2017) 182001]



Ξ_c^+ detached from, but pointing back to, the primary pp vertex
LHCb-RICH system to identify particle type of daughter tracks

Strange-charm baryons

[PRL 118 (2017) 182001]

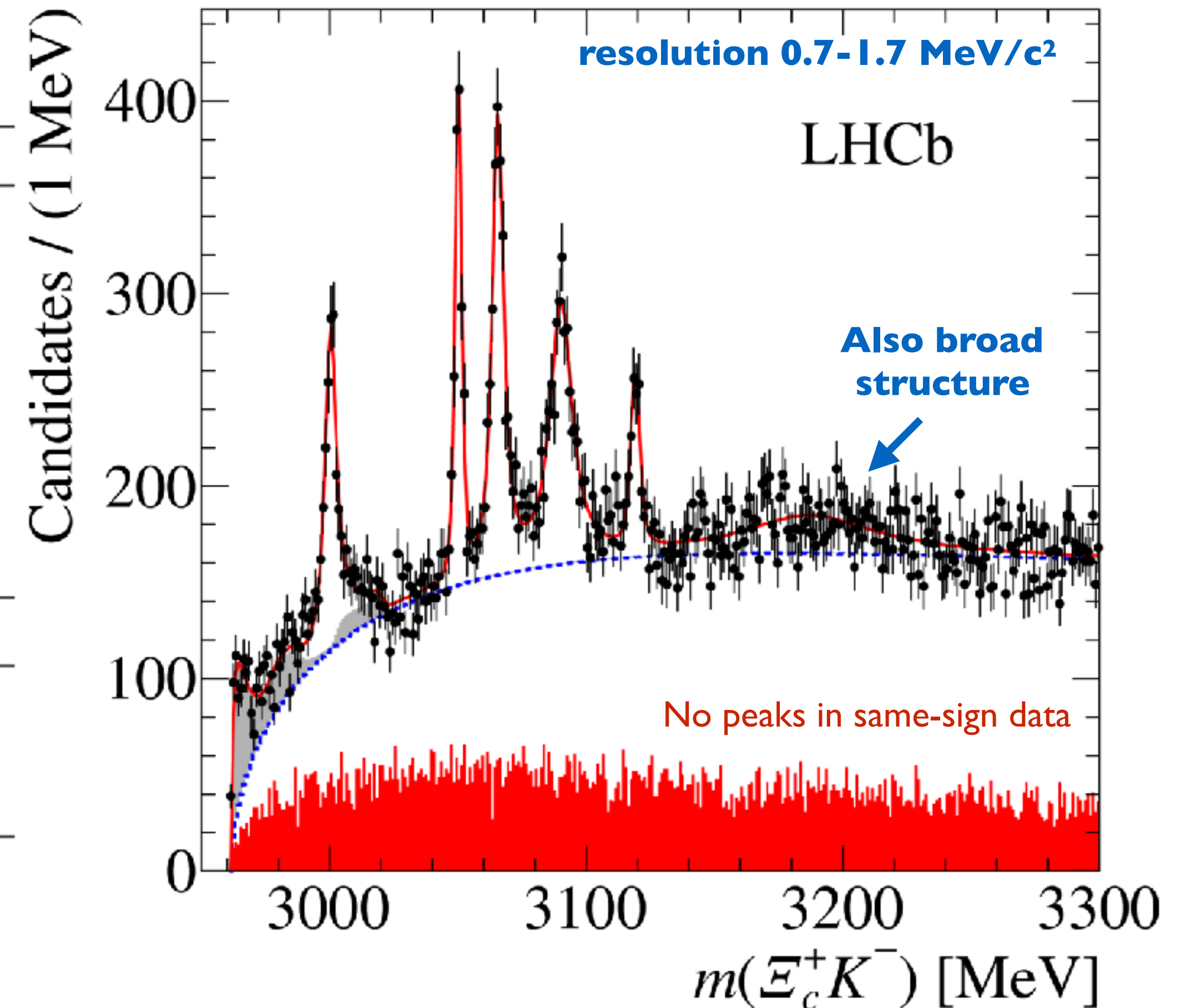


Ξ_c^+ detached from, but pointing back to, the primary pp vertex
LHCb-RICH system to identify particle type of daughter tracks

Strange-charm baryons

[PRL 118 (2017) 182001]

Resonance	Mass (MeV)	Γ (MeV)	Yield	N_σ
$\Omega_c(3000)^0$	$3000.4 \pm 0.2 \pm 0.1^{+0.3}_{-0.5}$	$4.5 \pm 0.6 \pm 0.3$	$1300 \pm 100 \pm 80$	20.4
$\Omega_c(3050)^0$	$3050.2 \pm 0.1 \pm 0.1^{+0.3}_{-0.5}$	$0.8 \pm 0.2 \pm 0.1$	$970 \pm 60 \pm 20$	20.4
		$< 1.2 \text{ MeV, 95\% CL}$	Very narrow!	
$\Omega_c(3066)^0$	$3065.6 \pm 0.1 \pm 0.3^{+0.3}_{-0.5}$	$3.5 \pm 0.4 \pm 0.2$	$1740 \pm 100 \pm 50$	23.9
$\Omega_c(3090)^0$	$3090.2 \pm 0.3 \pm 0.5^{+0.3}_{-0.5}$	$8.7 \pm 1.0 \pm 0.8$	$2000 \pm 140 \pm 130$	21.1
$\Omega_c(3119)^0$	$3119.1 \pm 0.3 \pm 0.9^{+0.3}_{-0.5}$	$1.1 \pm 0.8 \pm 0.4$	$480 \pm 70 \pm 30$	10.4
		$< 2.6 \text{ MeV, 95\% CL}$	Very narrow!	
$\Omega_c(3188)^0$	$3188 \pm 5 \pm 13$	$60 \pm 15 \pm 11$	$1670 \pm 450 \pm 360$	
$\Omega_c(3066)_{fd}^0$			$700 \pm 40 \pm 140$	
$\Omega_c(3090)_{fd}^0$			$220 \pm 60 \pm 90$	
$\Omega_c(3119)_{fd}^0$			$190 \pm 70 \pm 20$	



What are the quantum numbers? Use $\Omega_b^- \rightarrow (\Xi_c^+ K^-) \pi^-$

Why are they so narrow?

Are the narrowest states pentaquark candidates ($cs\bar{s}u\bar{u}$)?

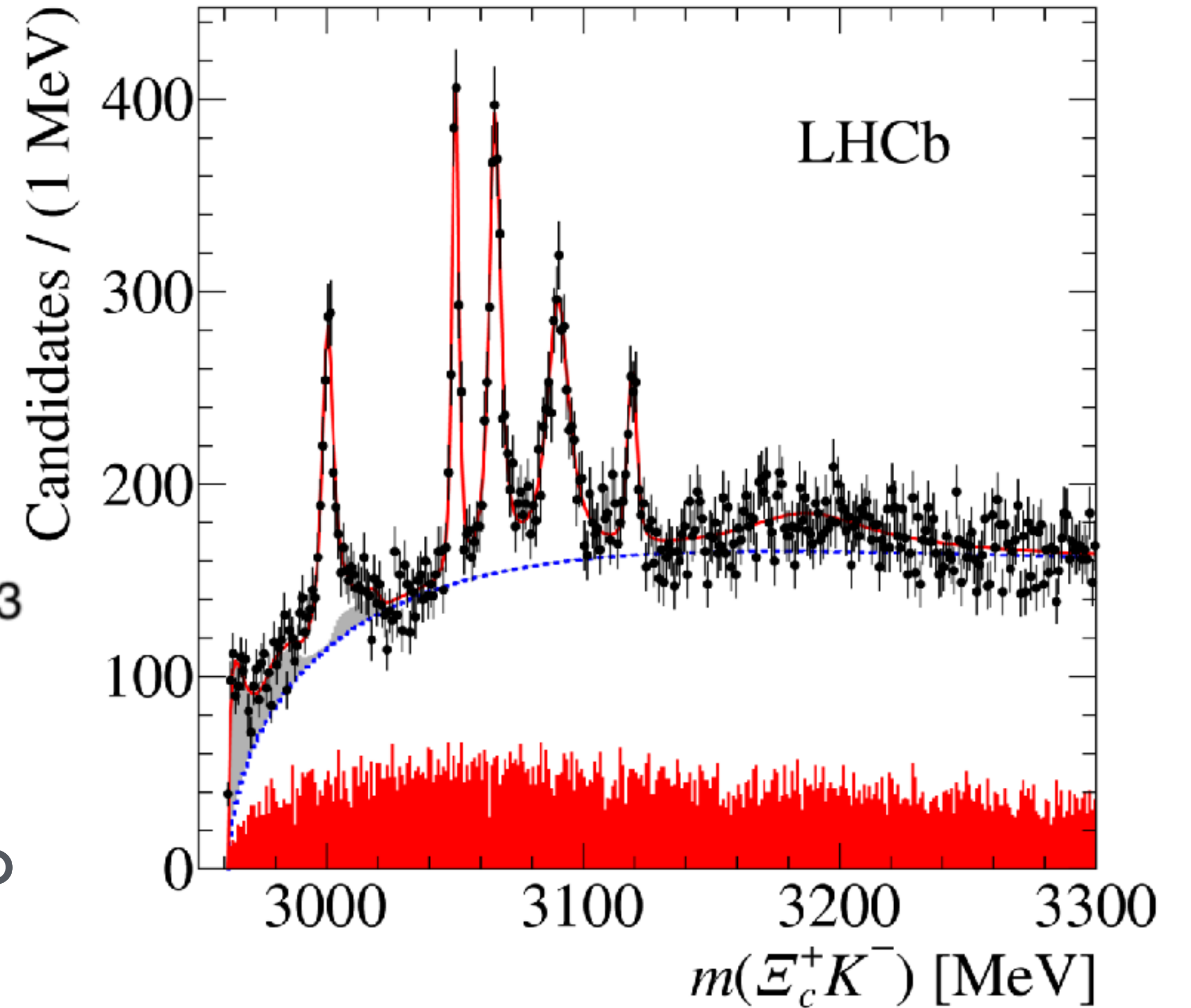
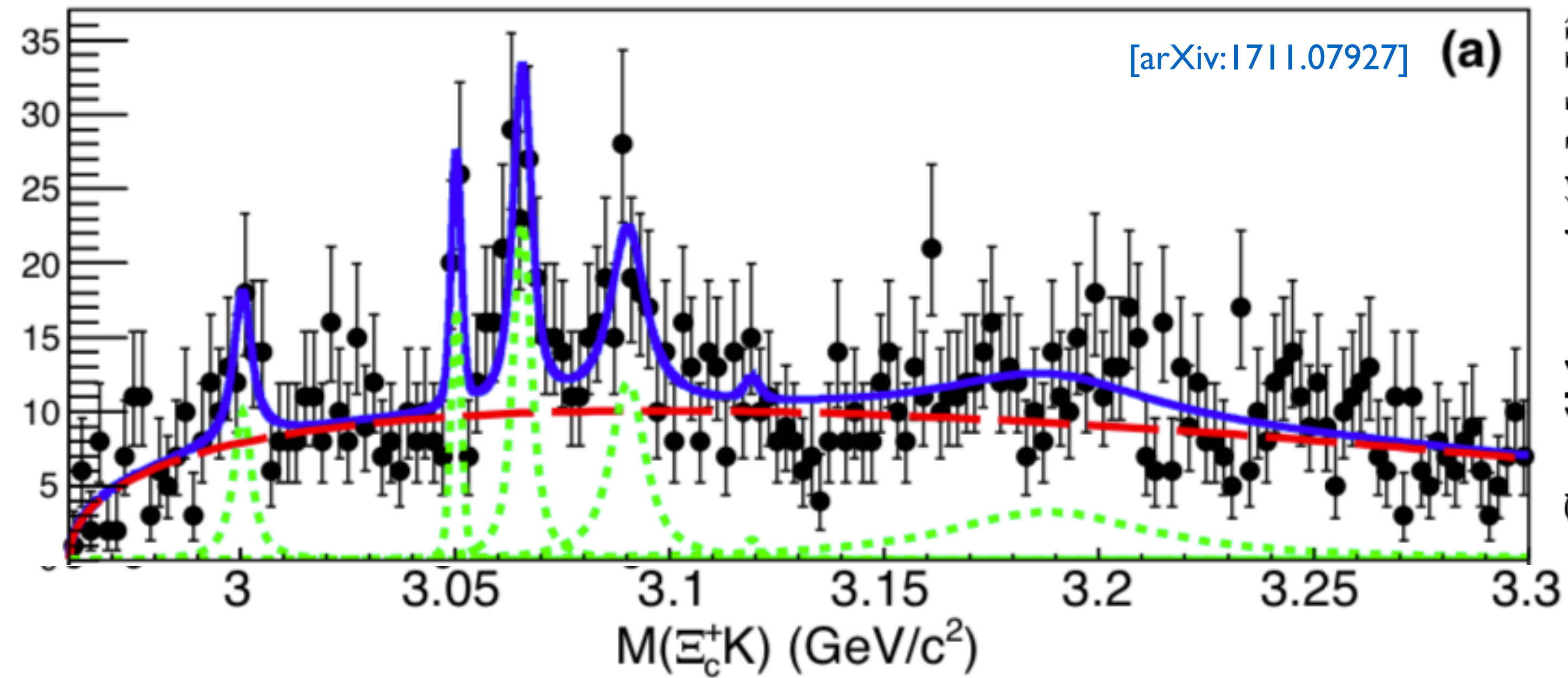
Which are orbital ($L=1$) or radial ($\Omega_c(2S)$) excitations?

Do they have isospin partners?

[Karliner, Rosner, PRD 95 (2017) 114012]

[Kim et al., PRD 96 (2017) 014009]

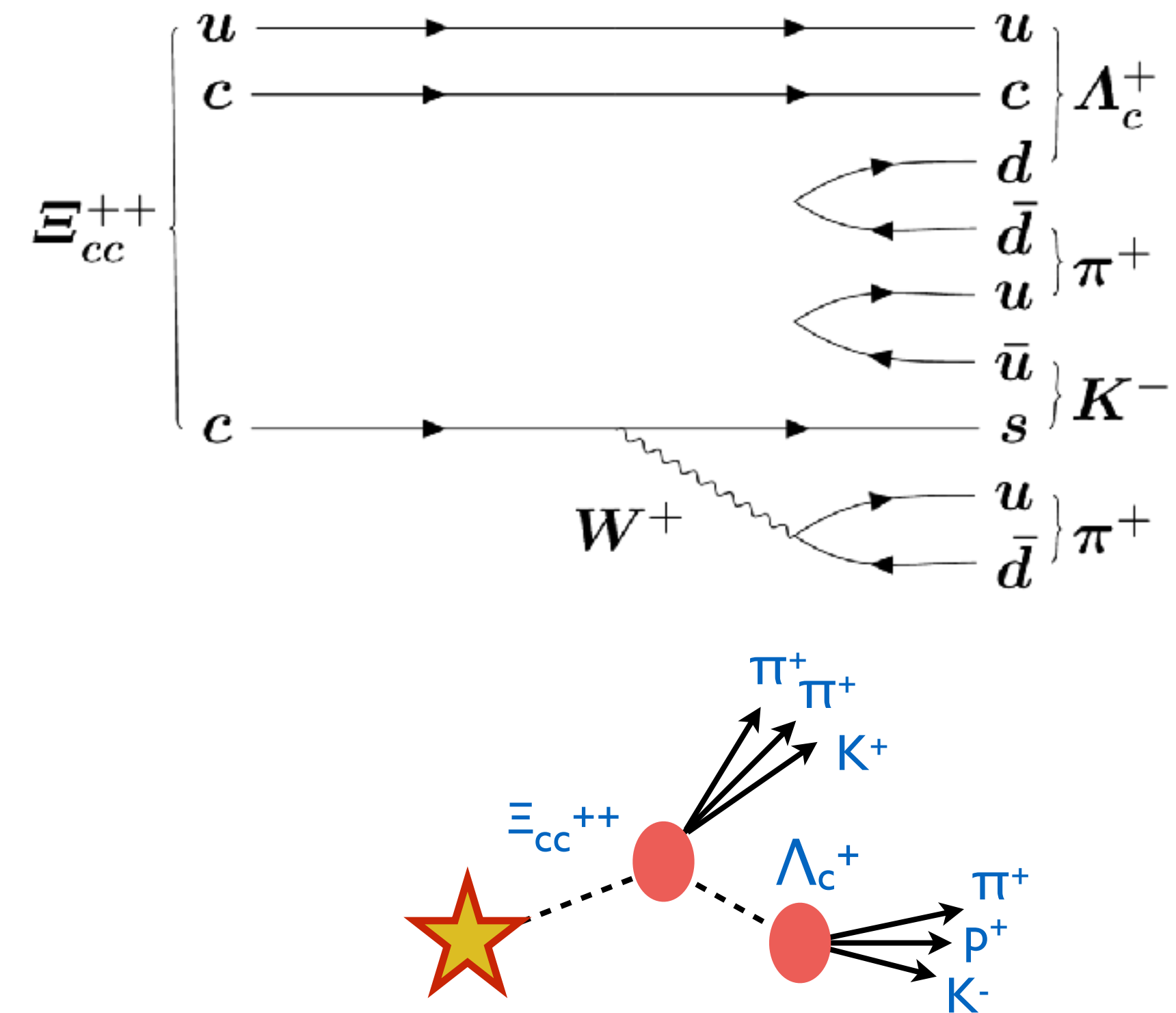
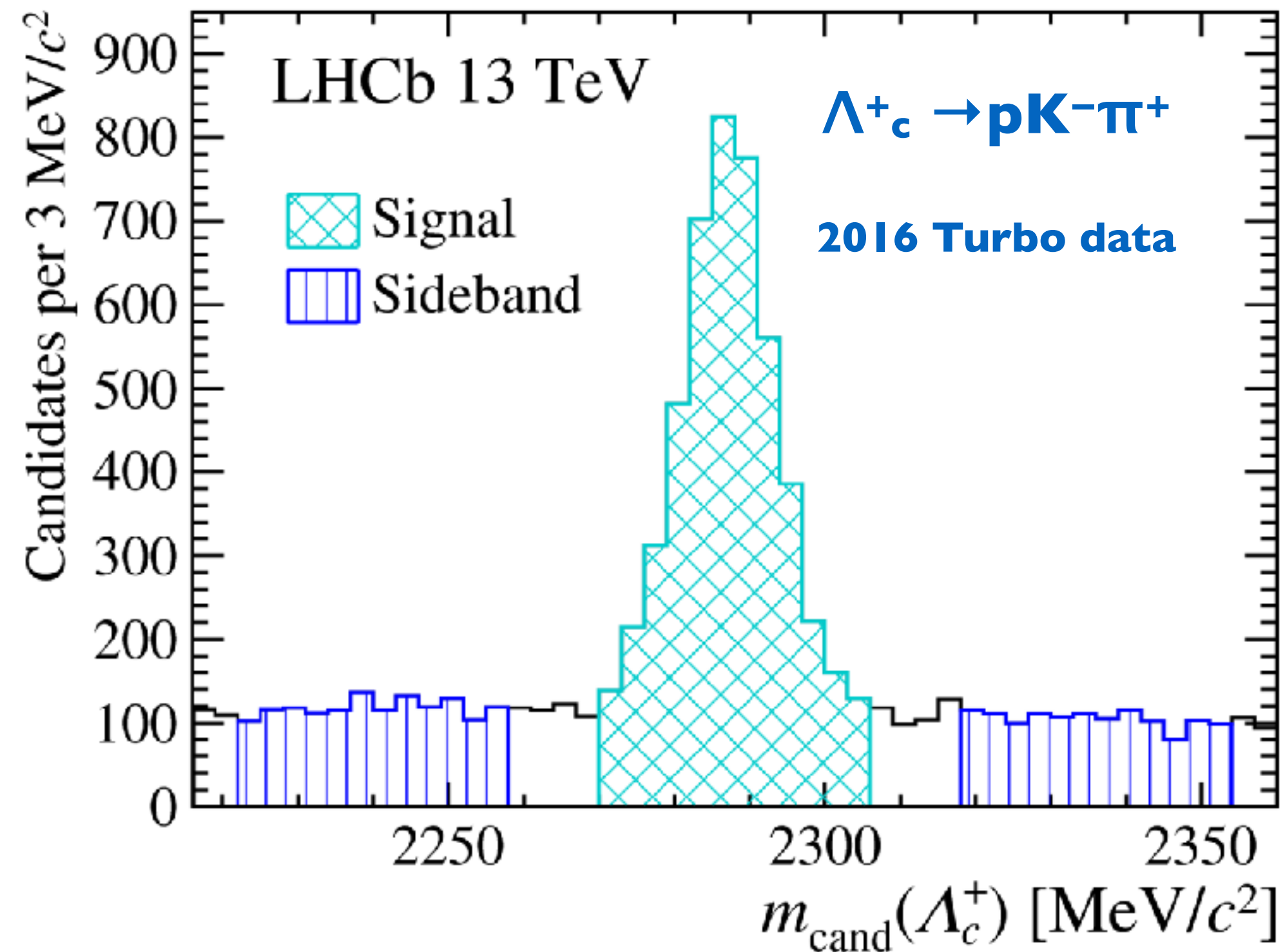
Confirmation by Belle



Higher state appears to be suppressed relative to LHCb data. May indicate that it is a pentaquark state that had suppressed production in e^+e^- collisions at Belle.

Doubly-charmed baryon

[PRL 119 (2017) 112001]



Novel online data processing → Turbo!

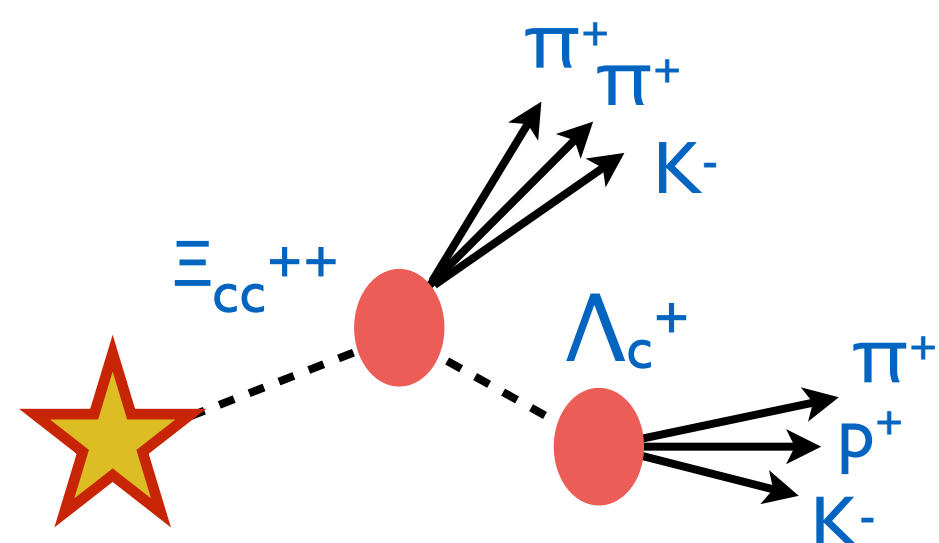
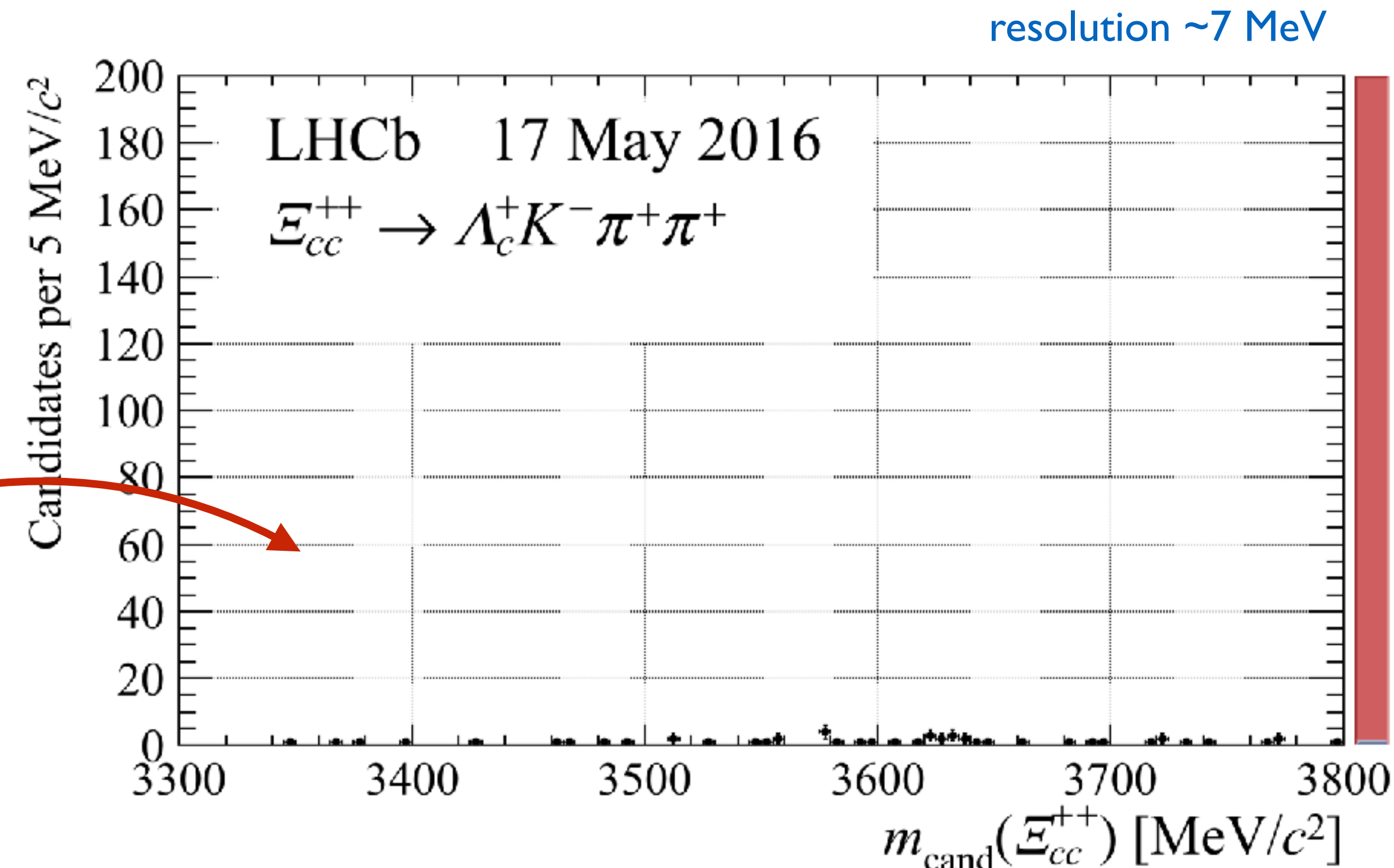
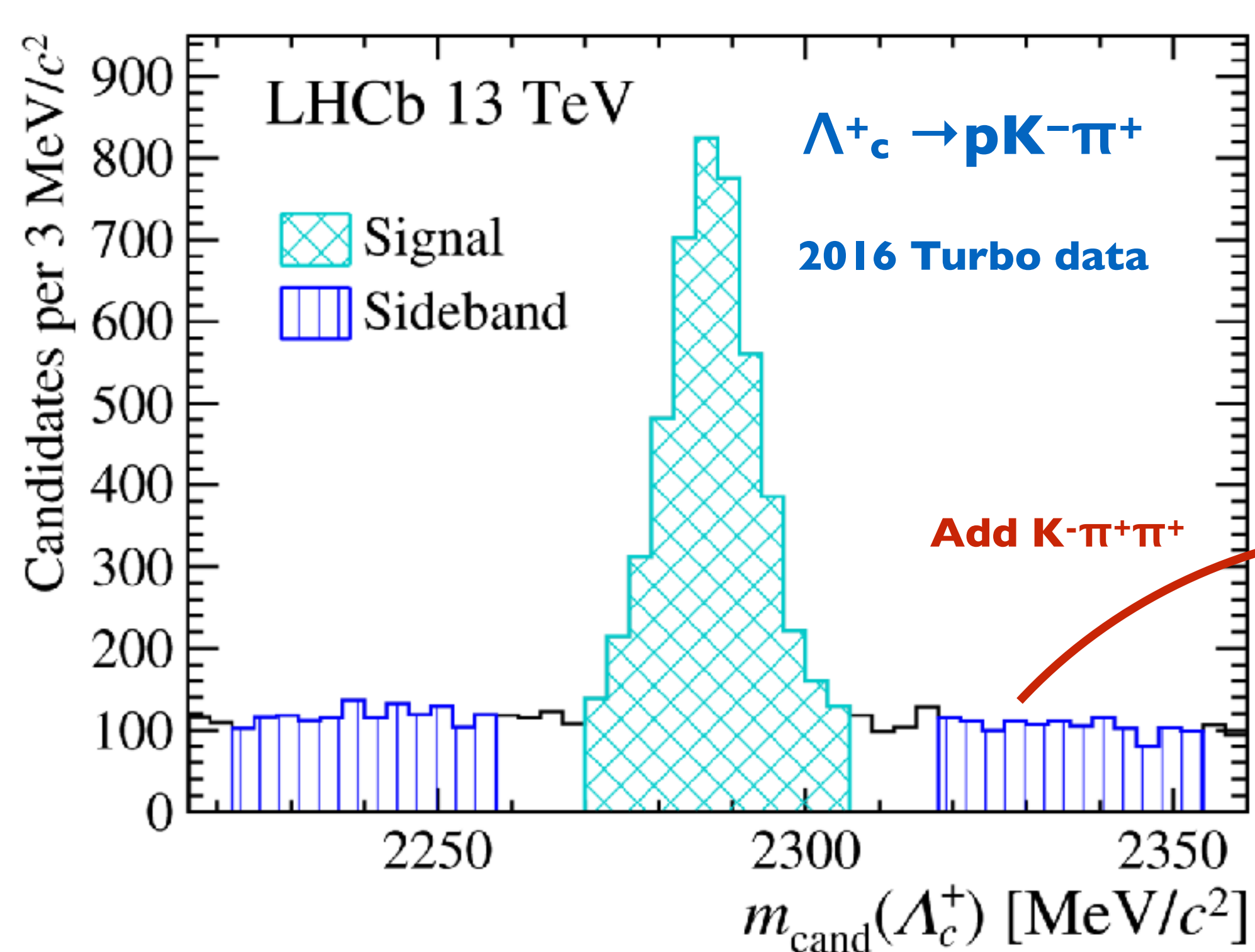
Full event reconstruction used in trigger (exploiting real-time alignment capabilities of LHCb in Run 2)

Write out events in ready-to-analyse format ⇒ no need for additional offline processing.

Only save part of the event that is needed → less disk space, crucial for states with large production cross-sections

Doubly-charmed baryon

[PRL 119 (2017) 112001]



> 12 σ significant signal observed consistent with a **weakly** decaying state

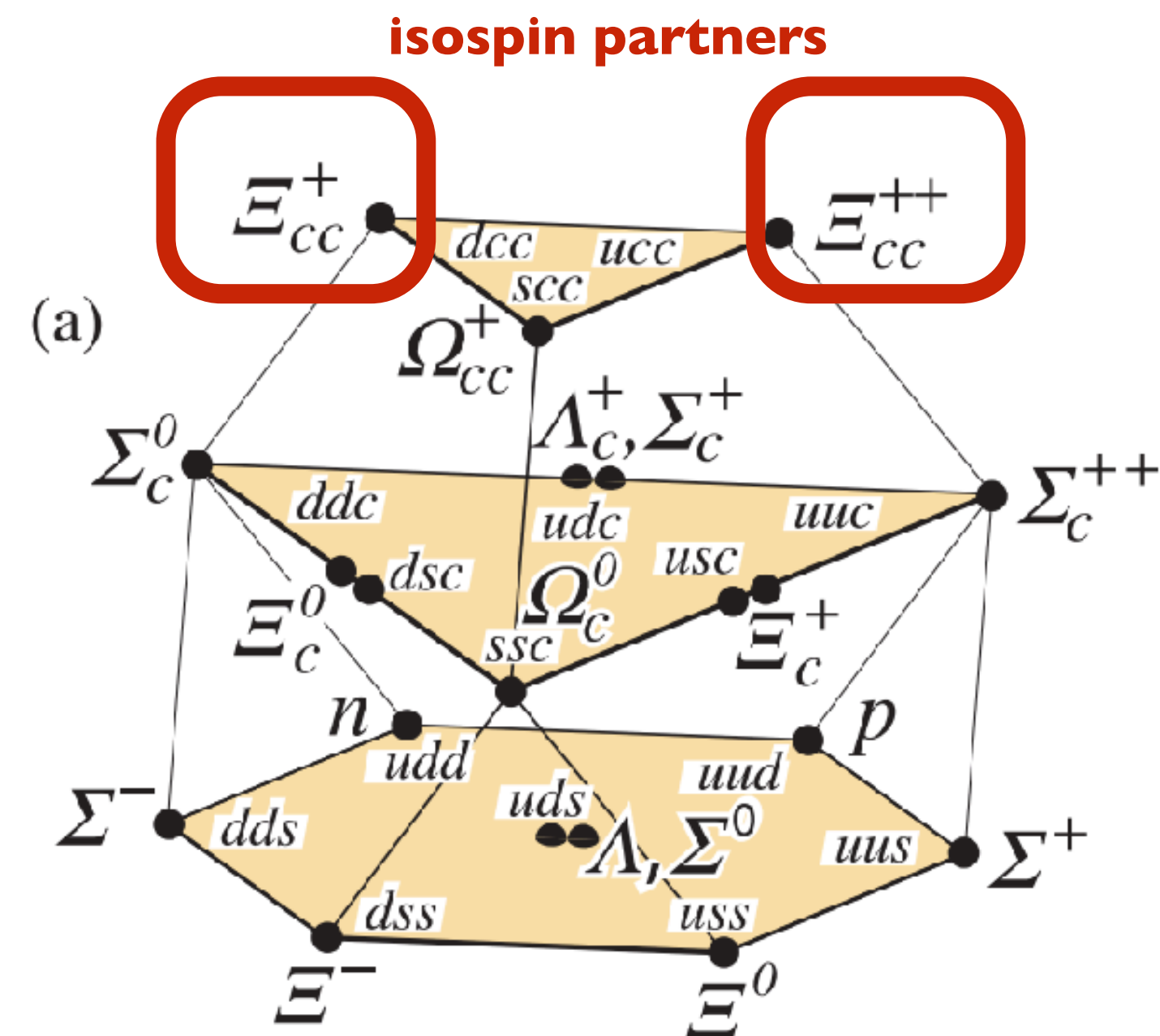
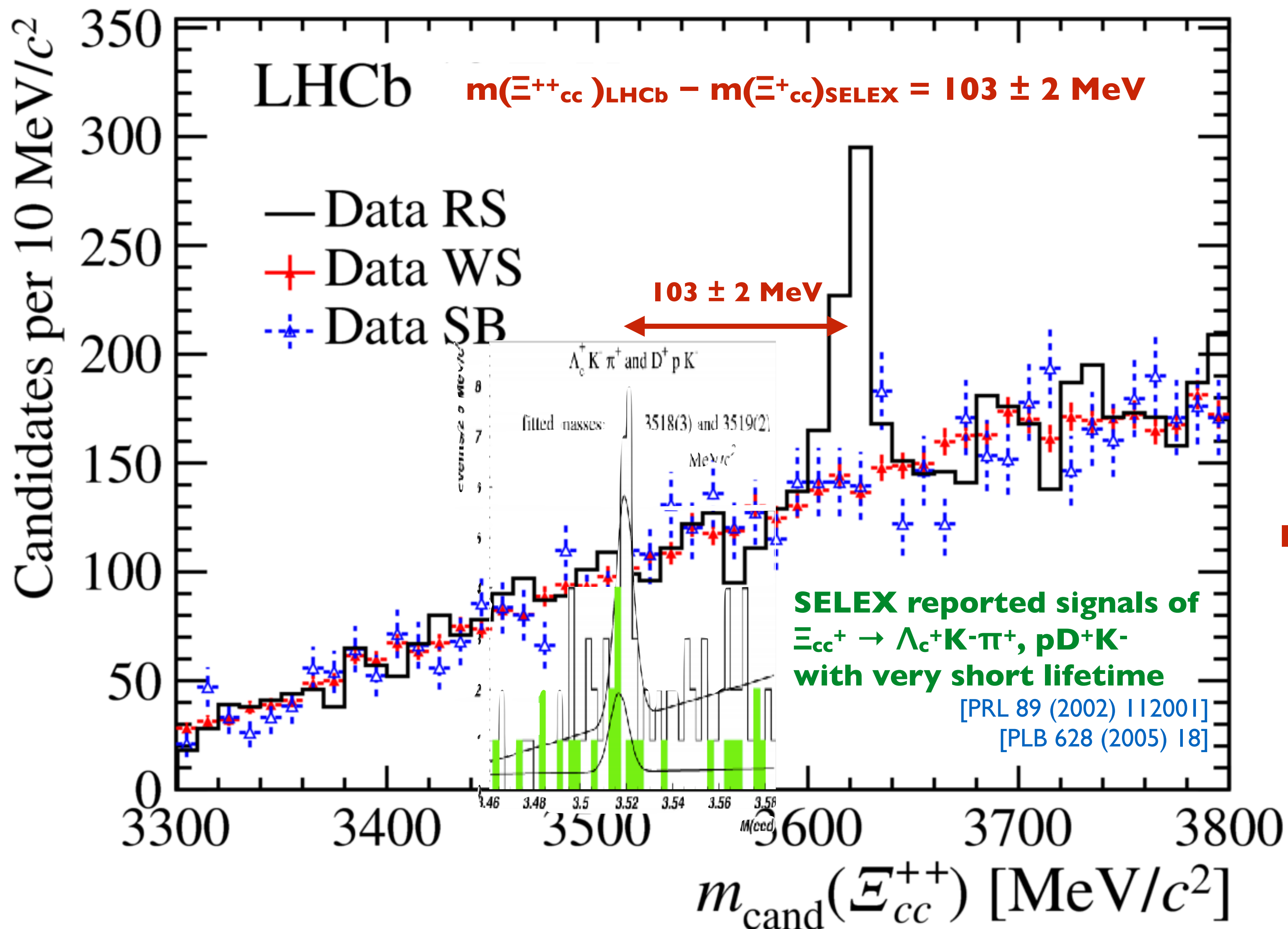
$$m(\Xi_{cc}^{++}) = 3621.40 \pm 0.72 \text{ (stat)} \pm 0.27 \text{ (syst)} \pm 0.14 \text{ } (\Lambda_c^+) \text{ MeV}$$

consistent with many theory predictions
 e.g. Lattice [Alexandrou PRD 96 (2017) 034511]

[link](#)

Comparison with SELEX

[PRL 119 (2017) 112001]



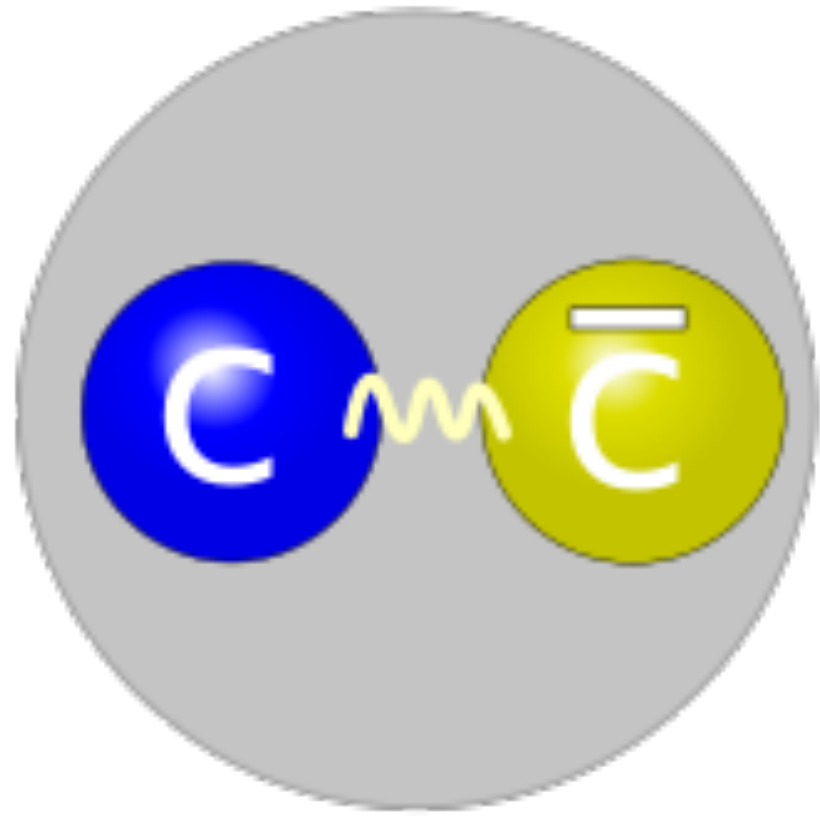
Inconsistent with being isospin partners

[Brodsky et al., PLB 698 (2011) 251]

[Karliner, Rosner, PRD 96 (2017) 033004]

Next steps: measure lifetime, new decay modes and search for other **double-heavies** Ξ_{cc}^{+} , Ω_{cc}^{+} , Ξ_{bc} , Ω_{bb} and Ξ_{bb}

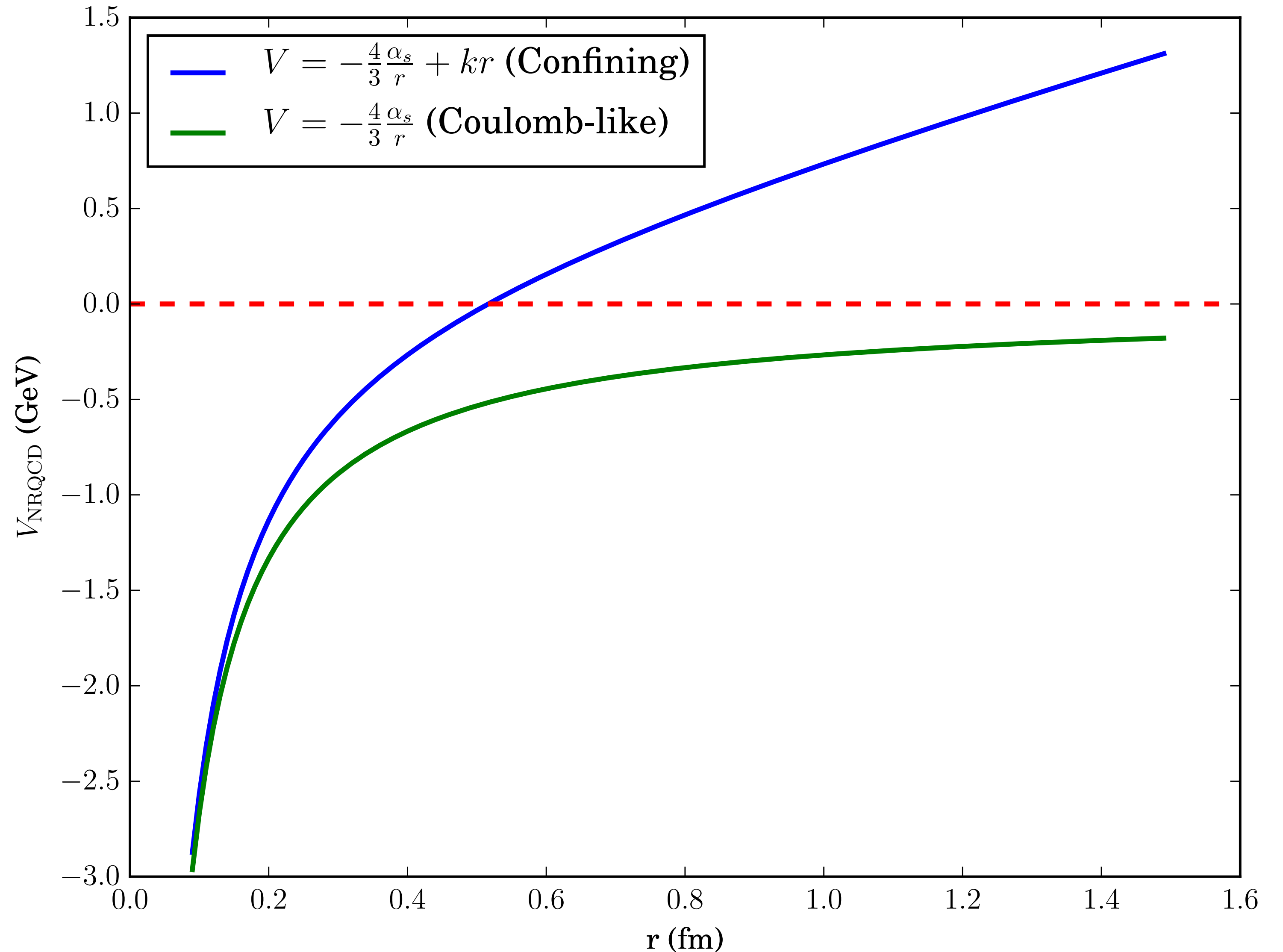
Quarkonium



$m(\text{bottom}) \sim 5000 \text{ MeV}$
 $m(\text{charm}) \sim 1500 \text{ MeV}$
 $\Lambda_{\text{QCD}} \sim 100 \text{ MeV}$
 $\alpha_s \sim 0.3$

Velocities of heavy-quarks are low
so can use V_{NRQCD} to predict
spectrum of $c\bar{c}$ and $b\bar{b}$ states

gluon self-interaction gives linear (confining) term at large distances

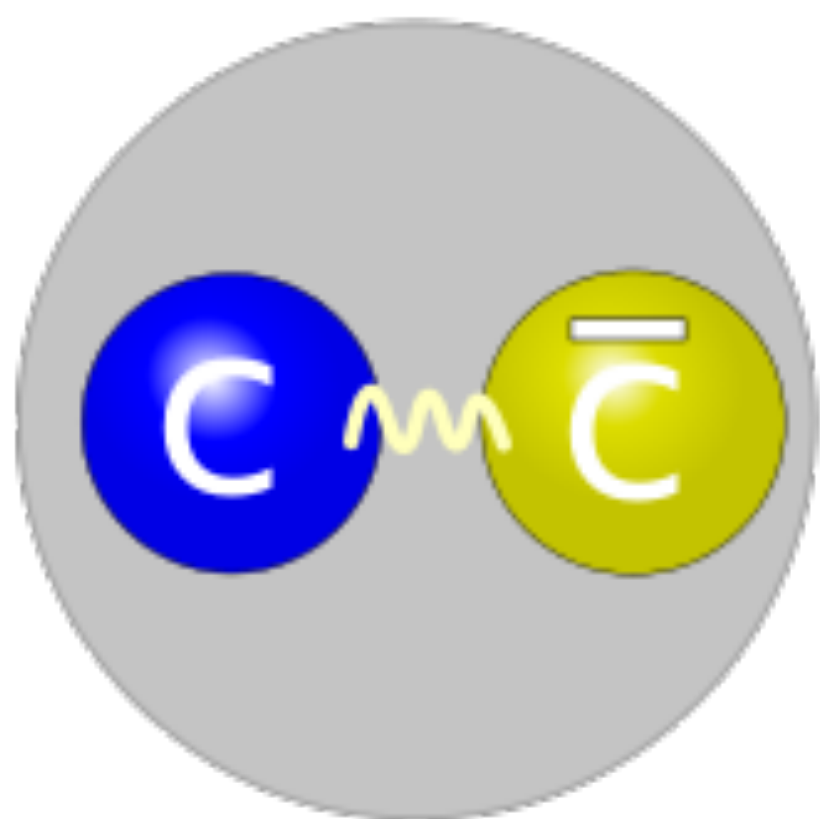


Potential model:

[Radford and Repko, PRD 75 (2007) 074031]

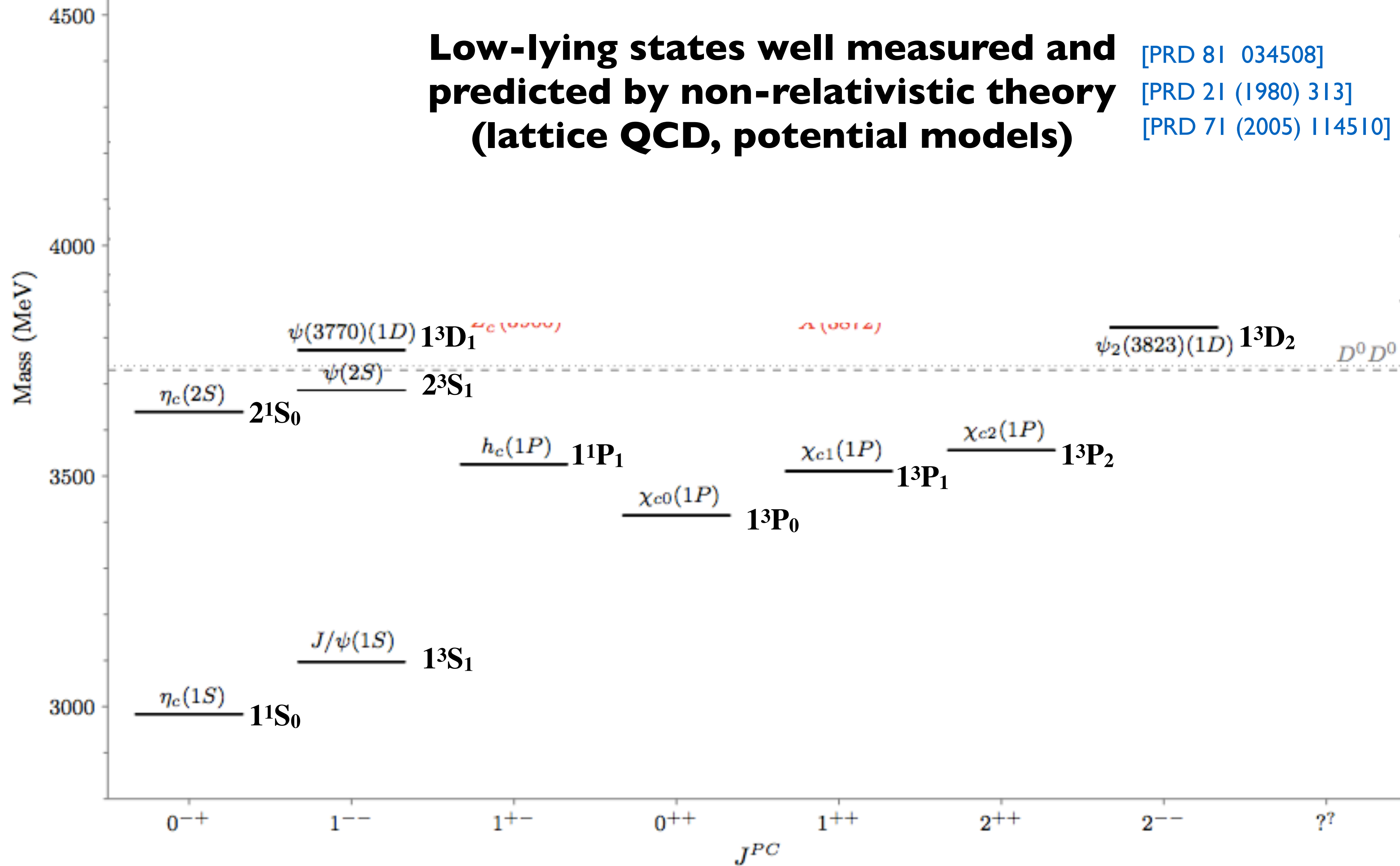
Charmonium

[Lebed et al, arXiv:1610.04528]



Low-lying states well measured and predicted by non-relativistic theory (lattice QCD, potential models)

[PRD 81 034508]
 [PRD 21 (1980) 313]
 [PRD 71 (2005) 114510]



Classify using J^{PC}

$$J = L \oplus S$$

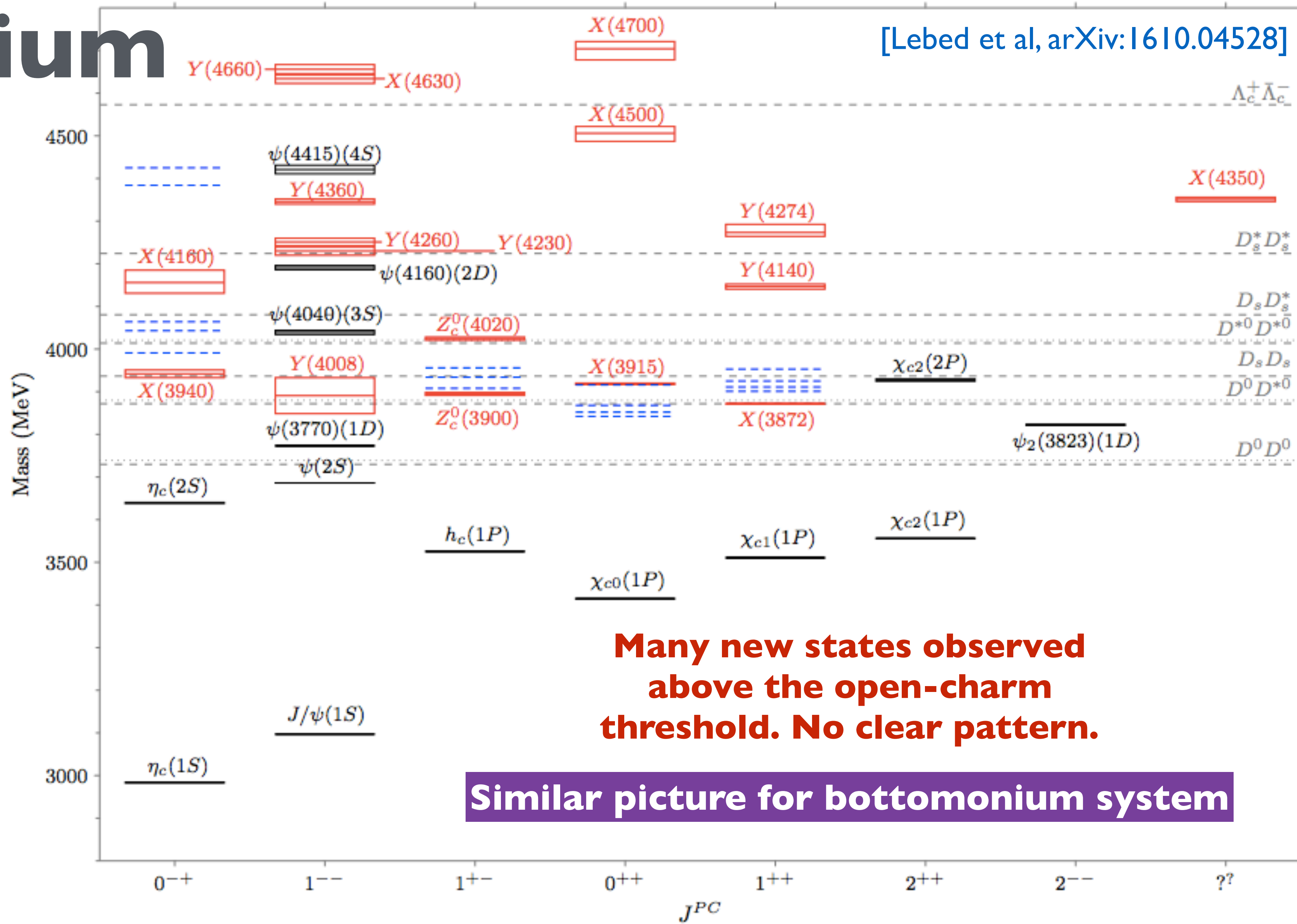
$$P = (-1)^{L+1}$$

$$C = (-1)^{L+S}$$

$$n^{2S+1}L_J$$

Charmonium

[Lebed et al, arXiv:1610.04528]



Classify using J^{PC}

$$J = L \oplus S$$

$$P = (-1)^{L+1}$$

$$C = (-1)^{L+S}$$

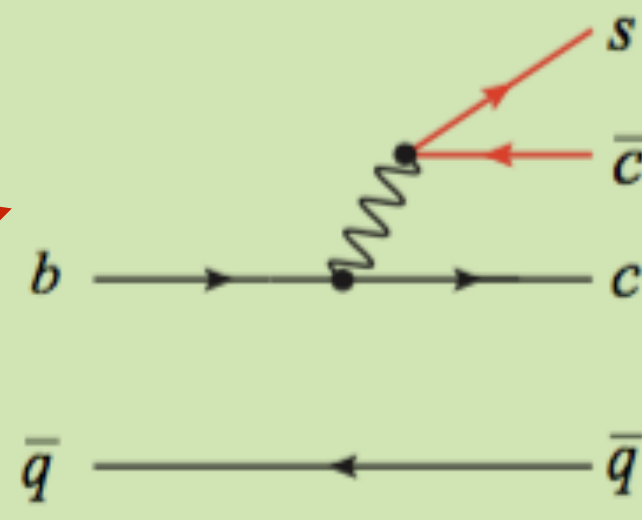
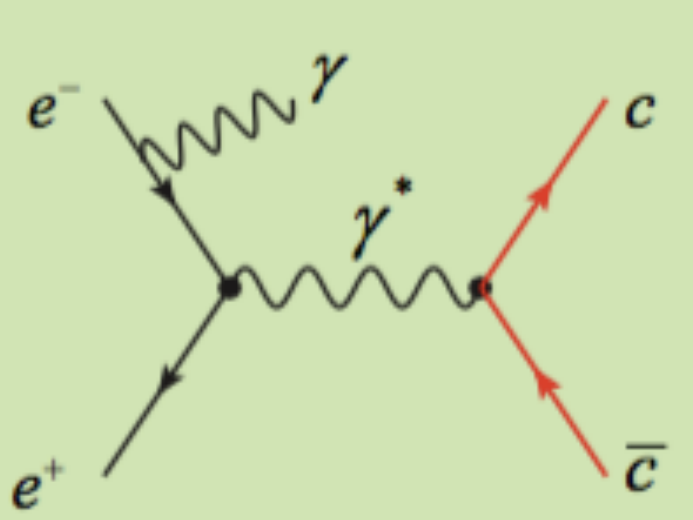
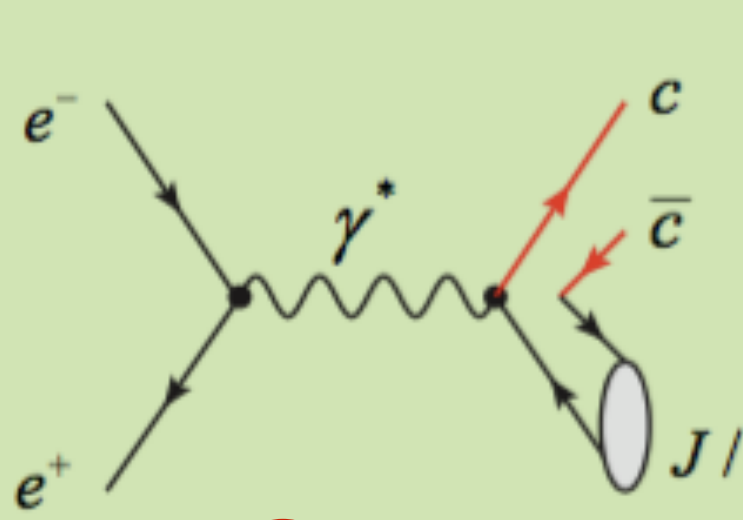
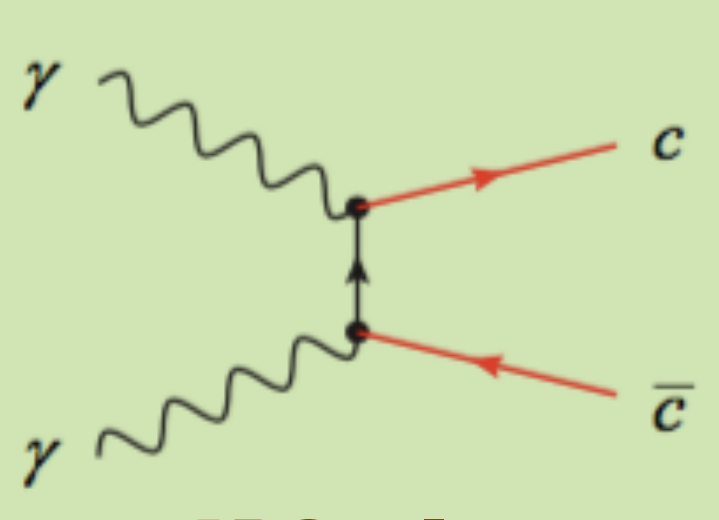
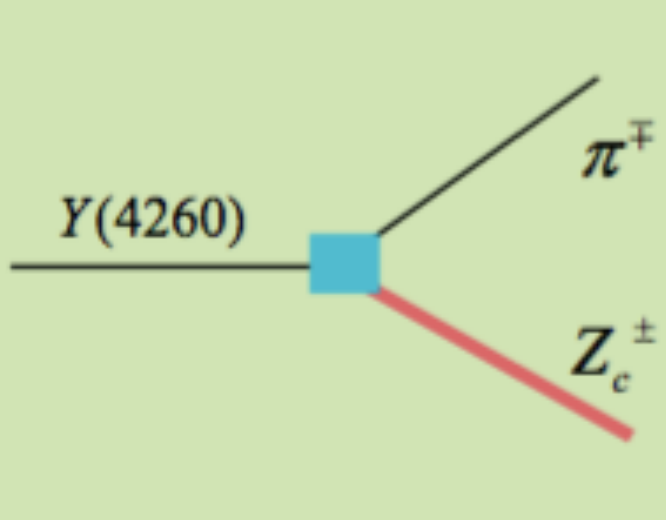
$$n^{2S+1}L_J$$

Many new states observed above the open-charm threshold. No clear pattern.

Similar picture for bottomonium system

Production mechanisms

Relevant for LHC

b hadrons	Initial state radiation	double charmonium	$\gamma\gamma$ collisions ($e^+e^- \rightarrow e^+e^-X$)	ISR $\rightarrow Y(4260)$
		 <p>C=+</p>	 <p>JPC = 1--</p>	
<p>X(3872)</p> <p>Y(3940)</p> <p>Z⁺(4430)</p> <p>Z⁺(4051)</p> <p>Z⁺(4248)</p> <p>Y(4140)</p> <p>Y(4274)</p> <p>Z_c⁺(4200)</p> <p>Z⁺(4240)</p> <p>X(3823)</p>	<p>Y(4260)</p> <p>Y(4008)</p> <p>Y(4360)</p> <p>Y(4630)</p> <p>Y(4660)</p> <p>$1^3D_2 c\bar{c}$</p>	<p>X(3940)</p> <p>X(4160)</p> <p>Recent review articles - [Olsen et al, arXiv:1708.04012] [Ali et al, arXiv:1706.00610] [Guo et al, arXiv:1705.00141] [Esposito et al, arXiv:1611.07920] [Lebed et al, arXiv:1610.04528] [Chen et al, arXiv:1601.02092]</p>	<p>X(3915)</p> <p>X(4350)</p> <p>Z(3930)</p>	<p>Z_c(3900)</p> <p>Z_c(4025)</p> <p>Z_c(4020)</p> <p>Z_c(3885)</p>
<p>P_c(4380)</p> <p>P_c(4450)</p>	<p>X(3872) also observed in prompt $pp, p\bar{p}$ collisions and ISR</p>			

See backup

(Exotic) Hadron physics at LHCb

nPVs ~ 2

nTracks ~ 200

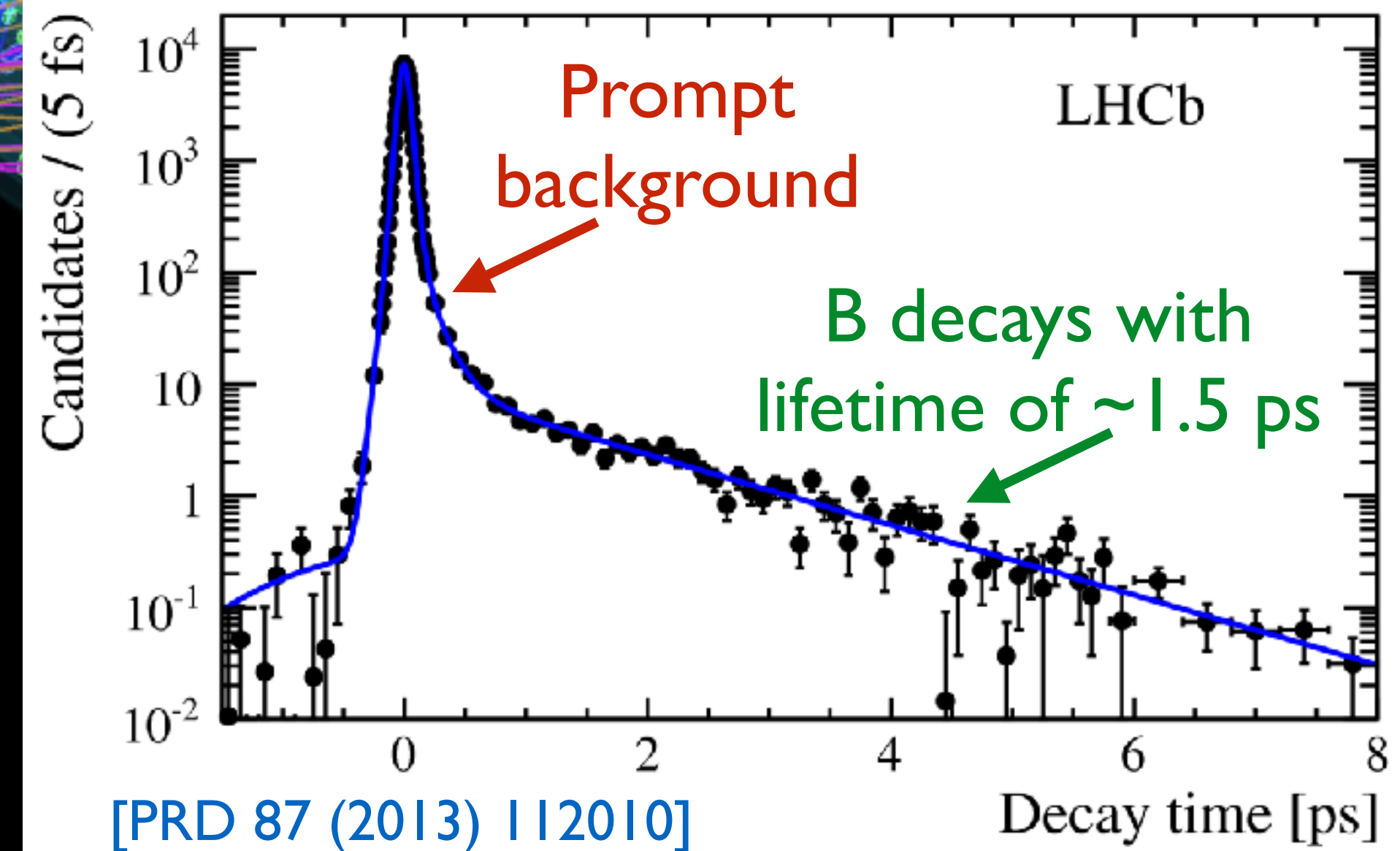
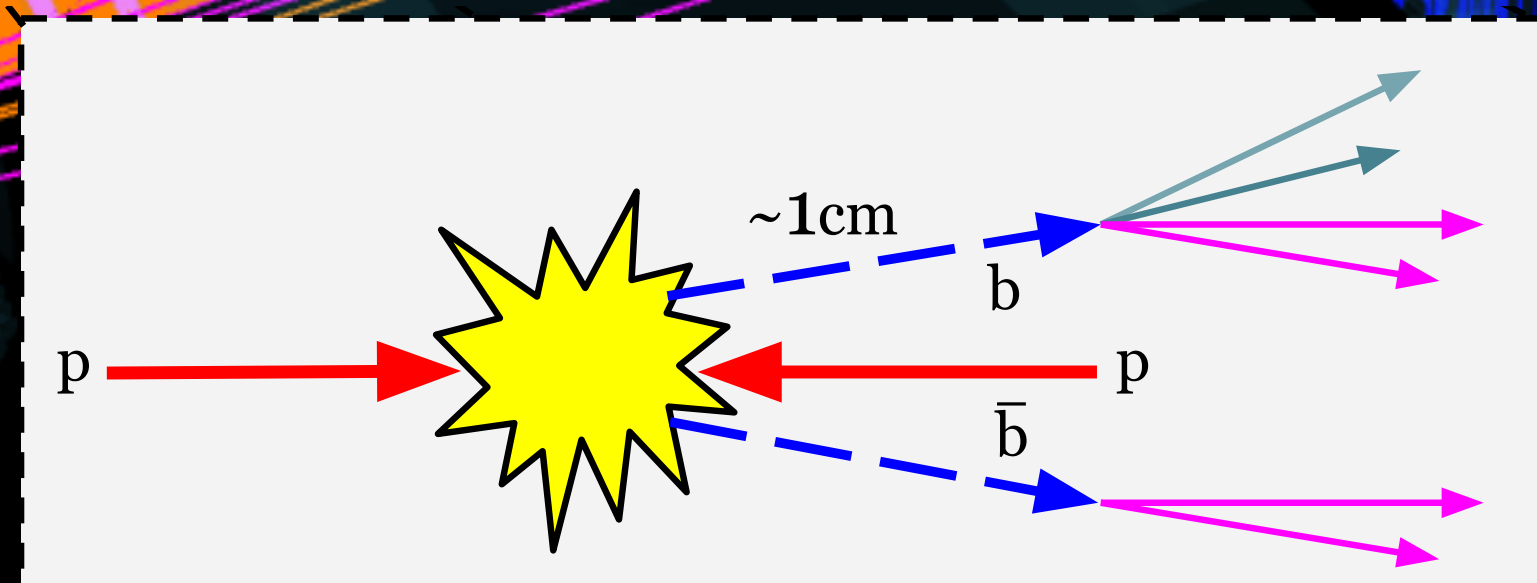
pT(B) ~ 5 GeV

pT(daughter) ~ 1 GeV

$\sigma_{bb}(7 \text{ TeV}) = 72.0 \pm 0.3 \pm 6.8 \mu\text{b}$

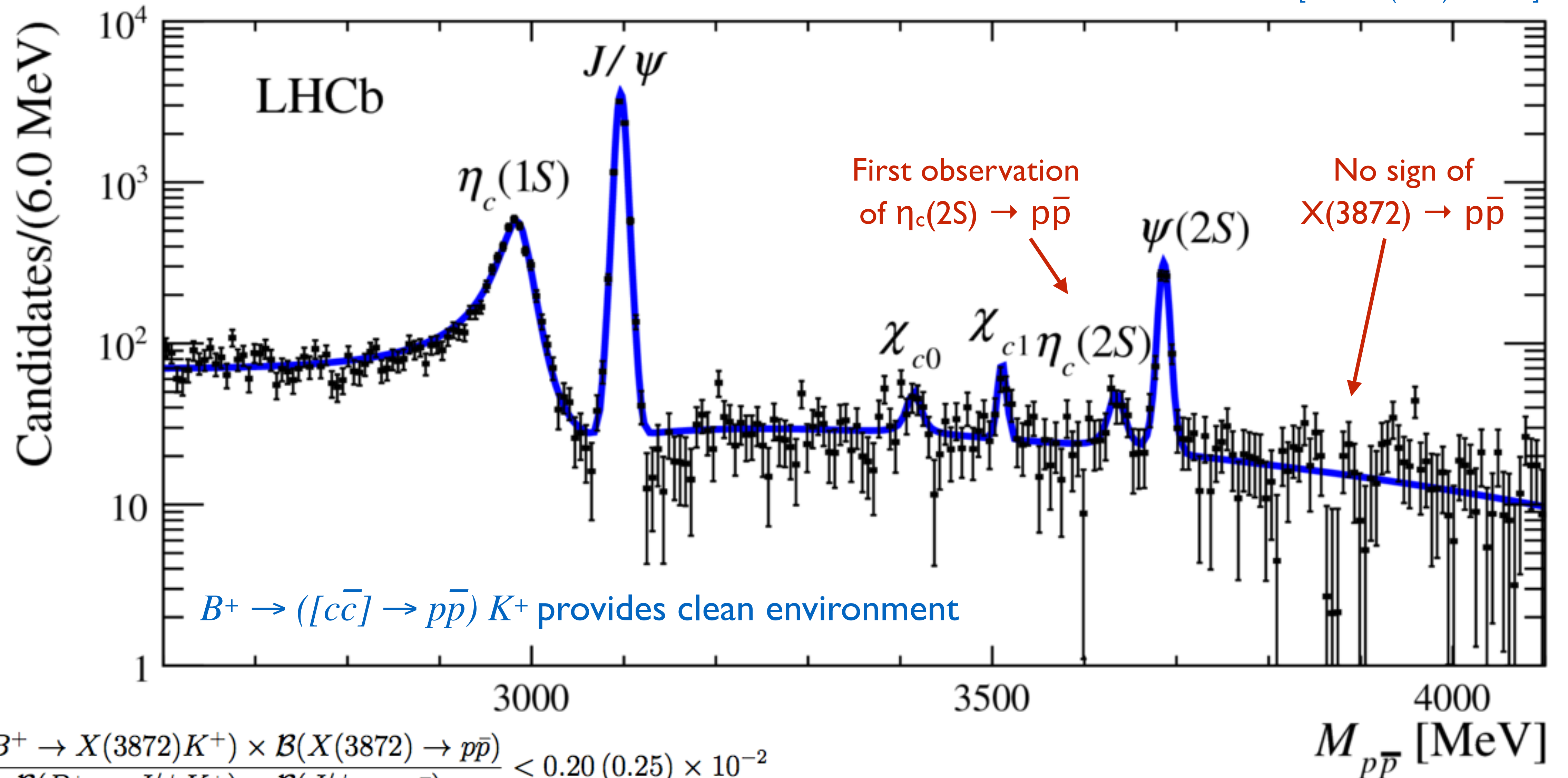
$\sigma_{bb}(13 \text{ TeV}) = 154.3 \pm 1.5 \pm 14.3 \mu\text{b}$

[PRL 118 (2017) 052002]



Charmonium production in b-hadron decays

[PLB 769 (2016) 305-313]



$$\frac{\mathcal{B}(B^+ \rightarrow X(3872)K^+) \times \mathcal{B}(X(3872) \rightarrow p\bar{p})}{\mathcal{B}(B^+ \rightarrow J/\psi K^+) \times \mathcal{B}(J/\psi \rightarrow p\bar{p})} < 0.20 \text{ (0.25)} \times 10^{-2}$$

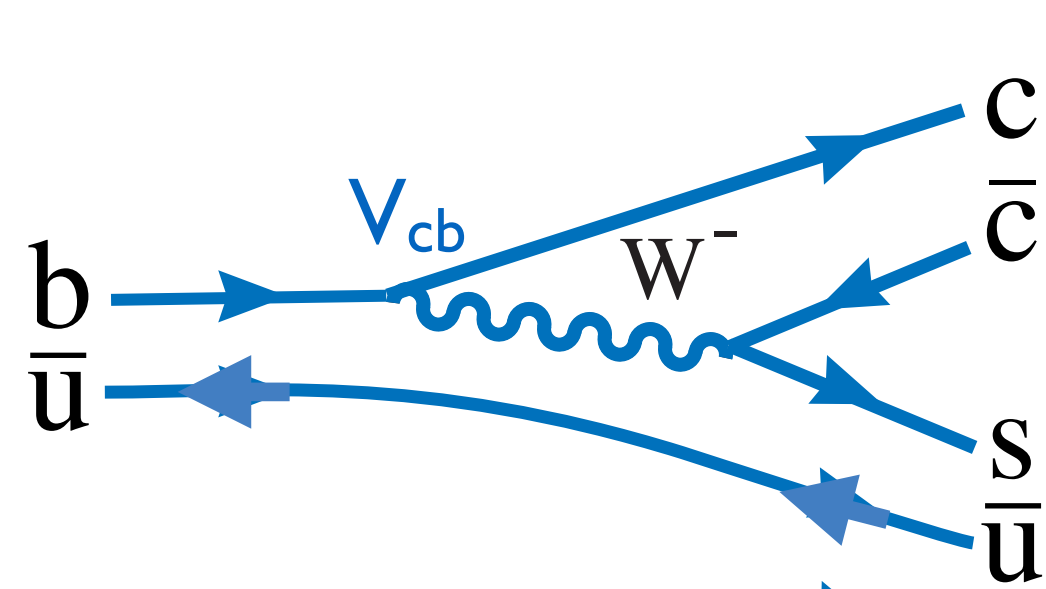
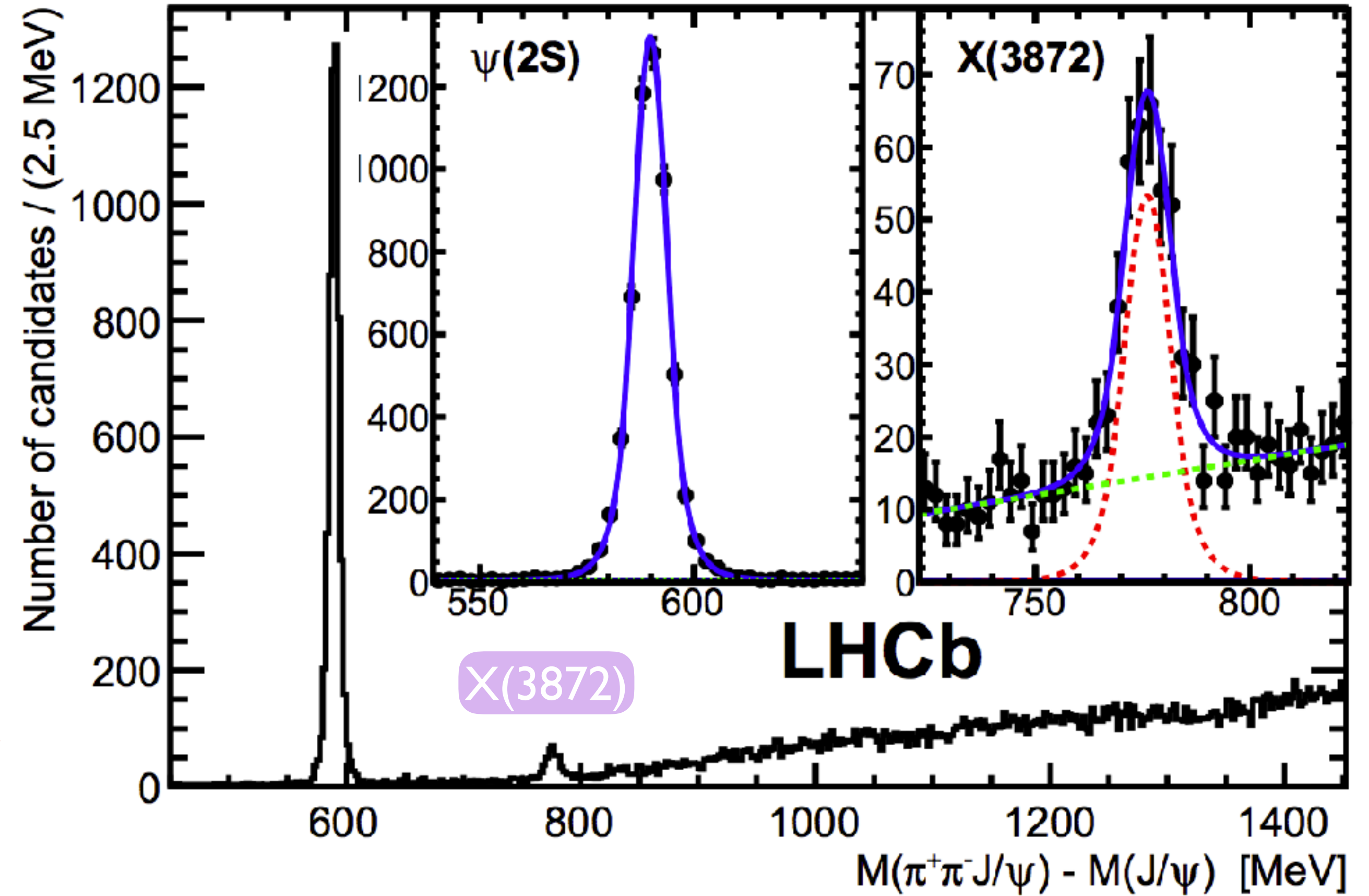
Exotic charmonium production

[PRL 110 (2013) 222001]

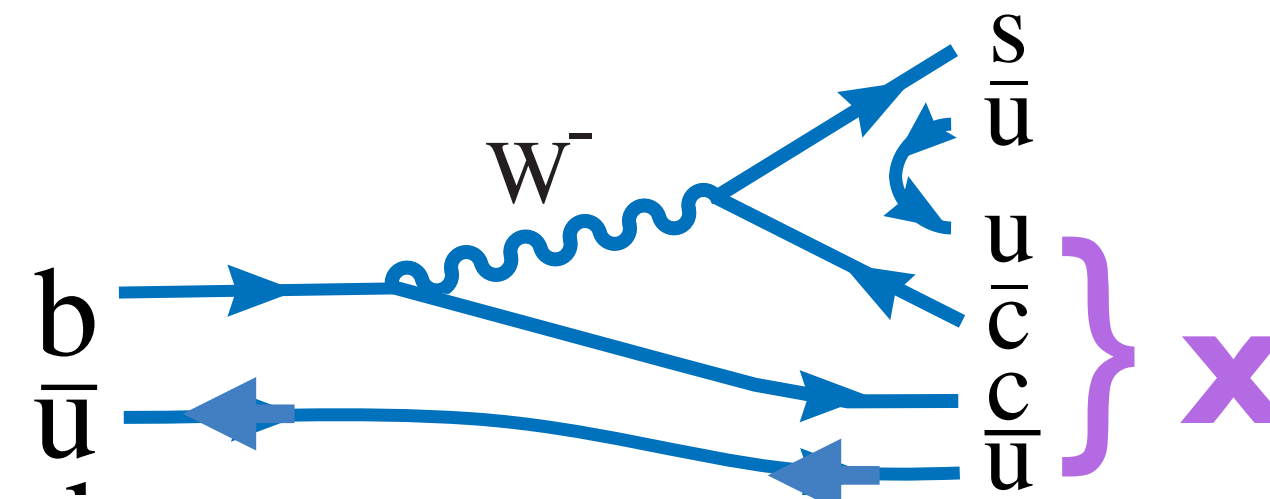
Charmonium in the final state is experimentally useful for triggering, particularly using muon/electron decay modes of J/ψ or $\psi(2S)$

Both decay chains lead to the same particles in the final state

Mass fit is sufficient to identify exotic if state isolated and narrow, otherwise need **Dalitz or amplitude analysis**



$$B^+ \rightarrow \psi(2S)K^+, \psi(2S) \rightarrow J/\psi\pi^+\pi^-$$



$$B^+ \rightarrow X(3872)K^+, X(3872) \rightarrow J/\psi\pi^+\pi^-$$

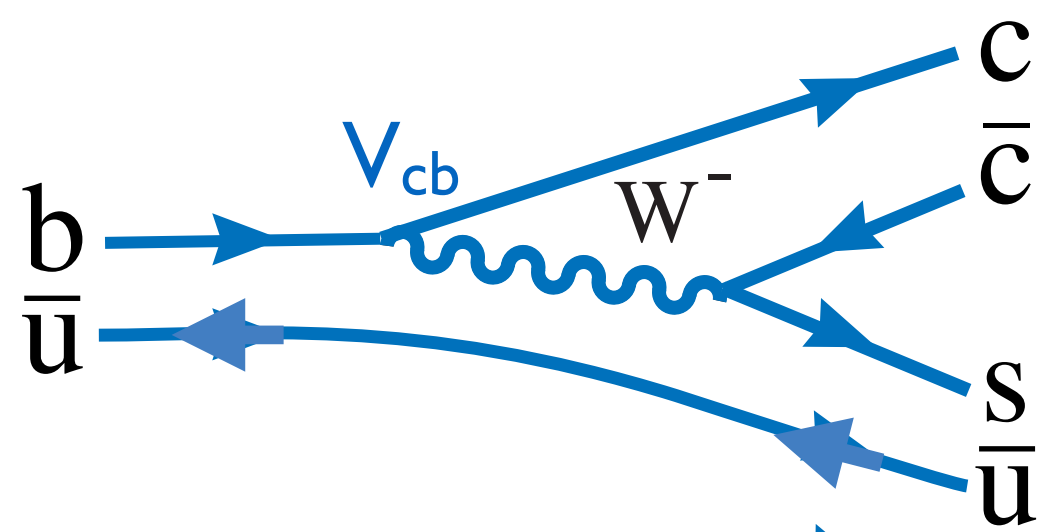
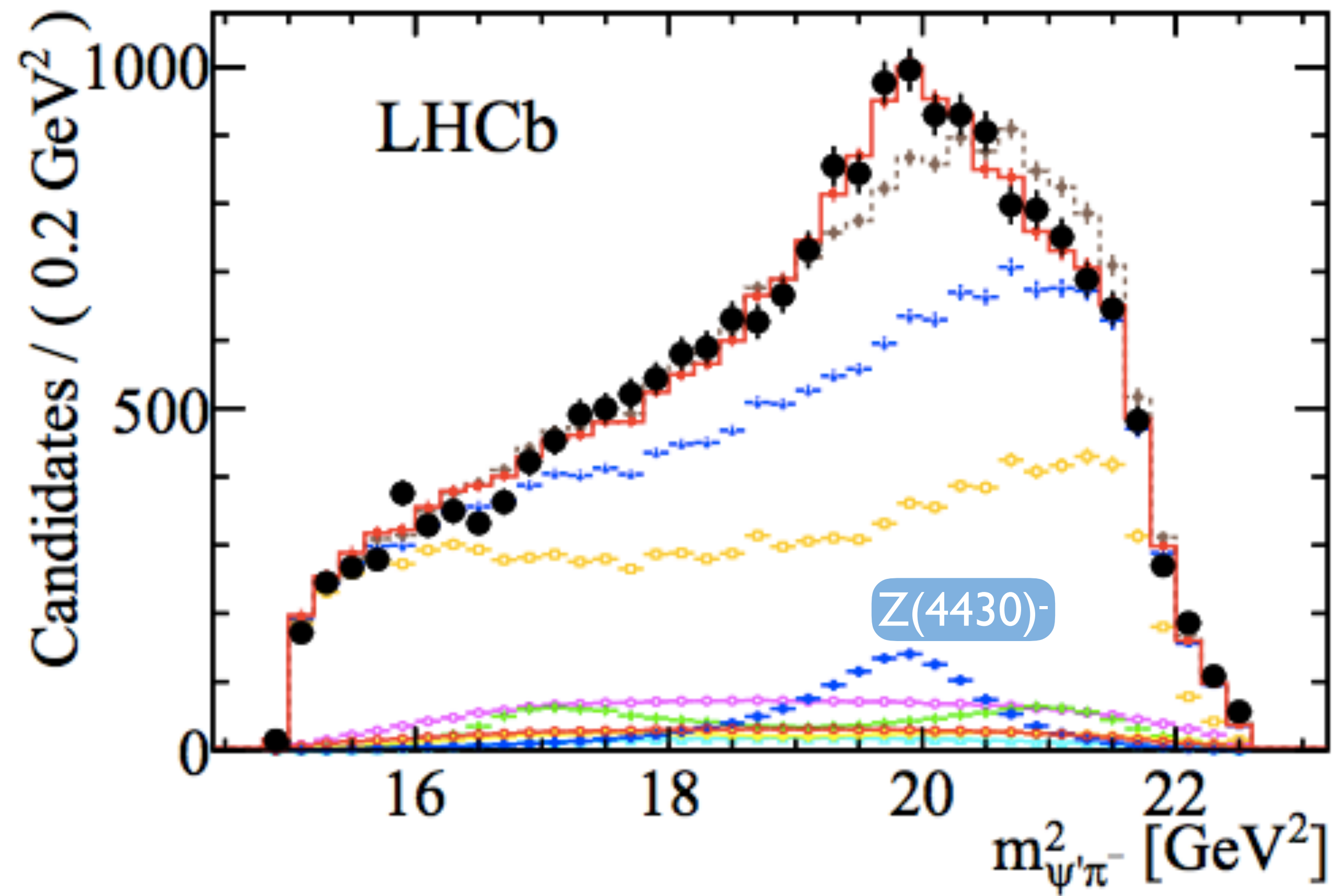
Exotic charmonium production

[PRL 112 (2014) 222002]

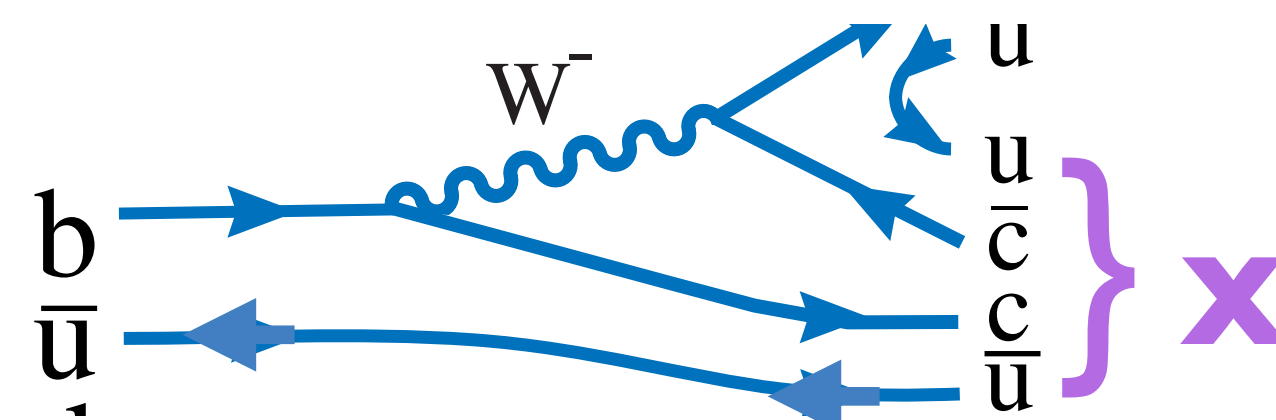
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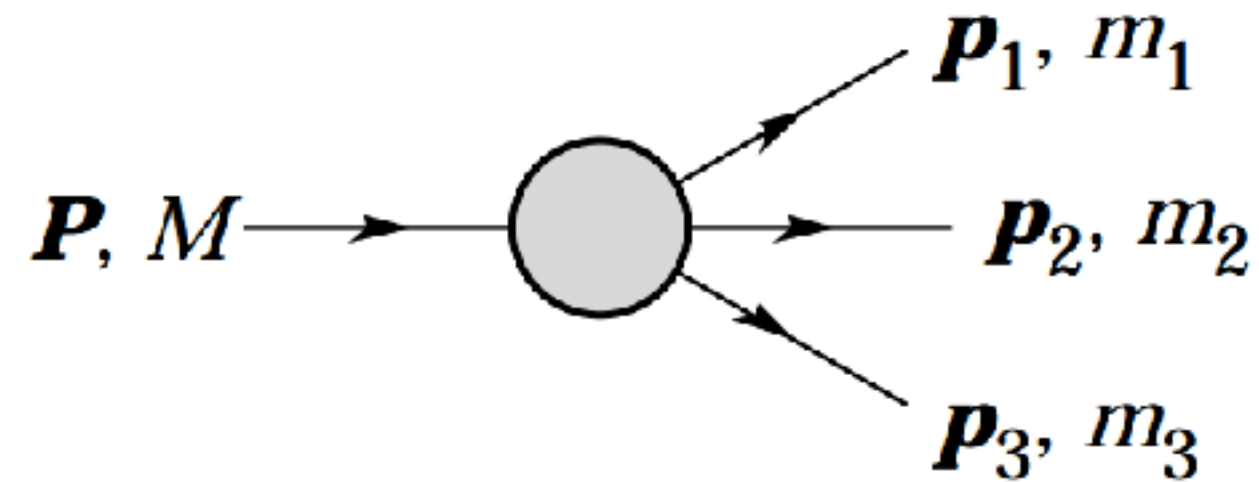
$$B^+ \rightarrow \psi(2S)K^+, \psi(2S) \rightarrow J/\psi\pi^+\pi^-$$



$$B^+ \rightarrow X(3872)K^+, X(3872) \rightarrow J/\psi\pi^+\pi^-$$

Reminder about Dalitz plots

scalar \rightarrow 3 scalars



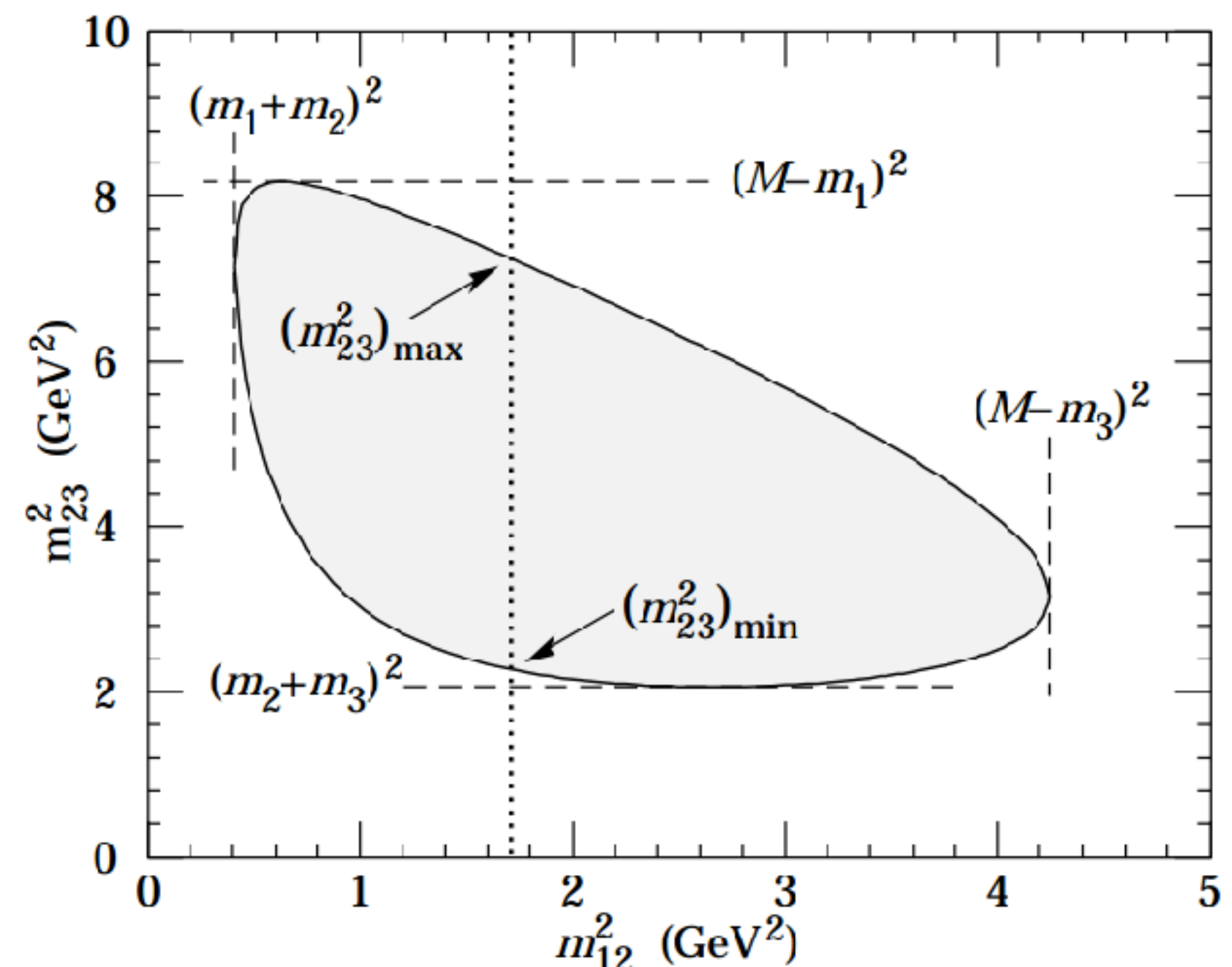
$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{32M^3} |\overline{\mathcal{M}}|^2 dm_{12}^2 dm_{23}^2$$

Configuration of parent particle decay depends on angular momentum of decay products

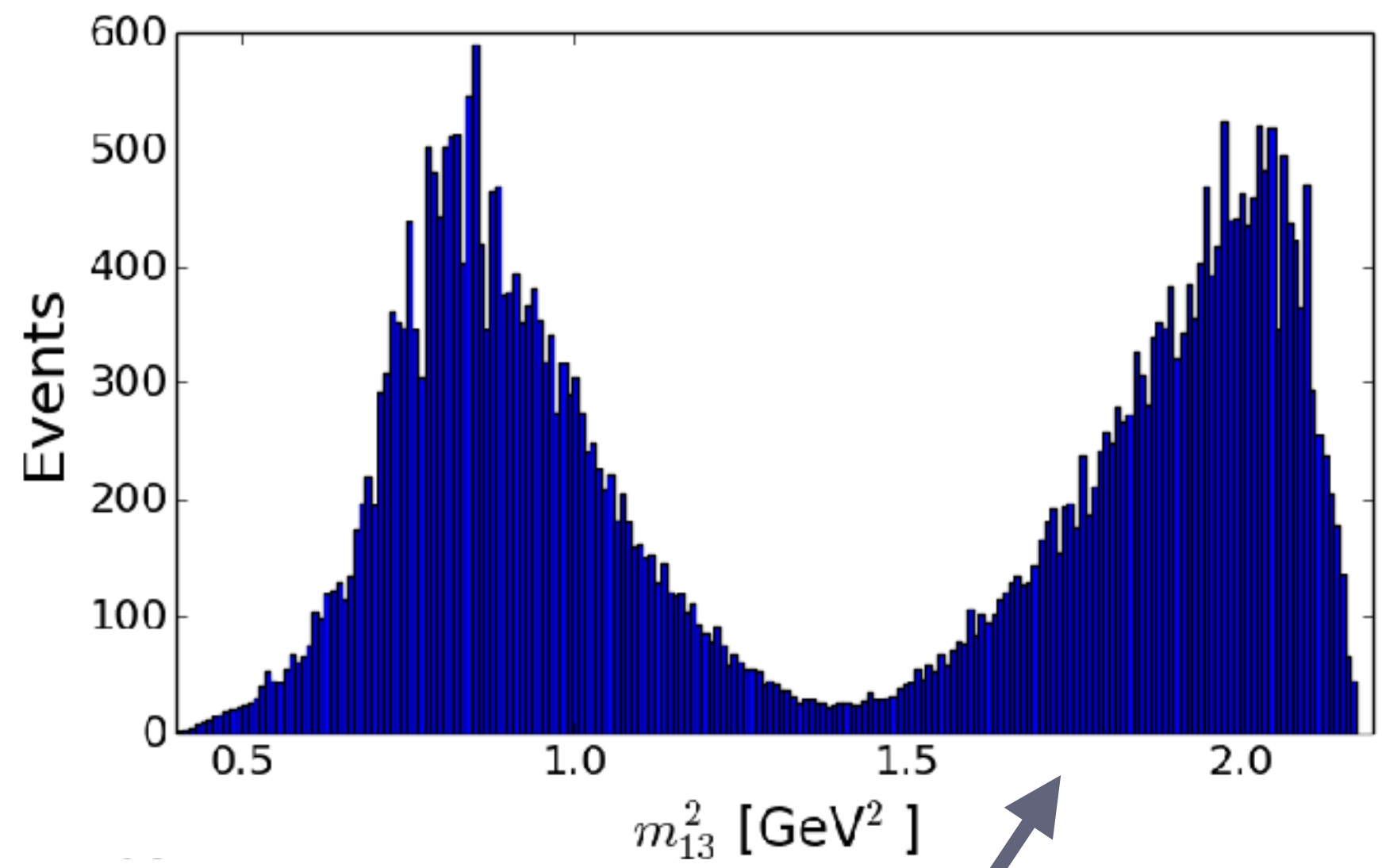
All dynamical information contained in $|\overline{\mathcal{M}}|^2$

Density plot of m_{12}^2 vs. m_{23}^2 to infer information on $|\overline{\mathcal{M}}|^2$

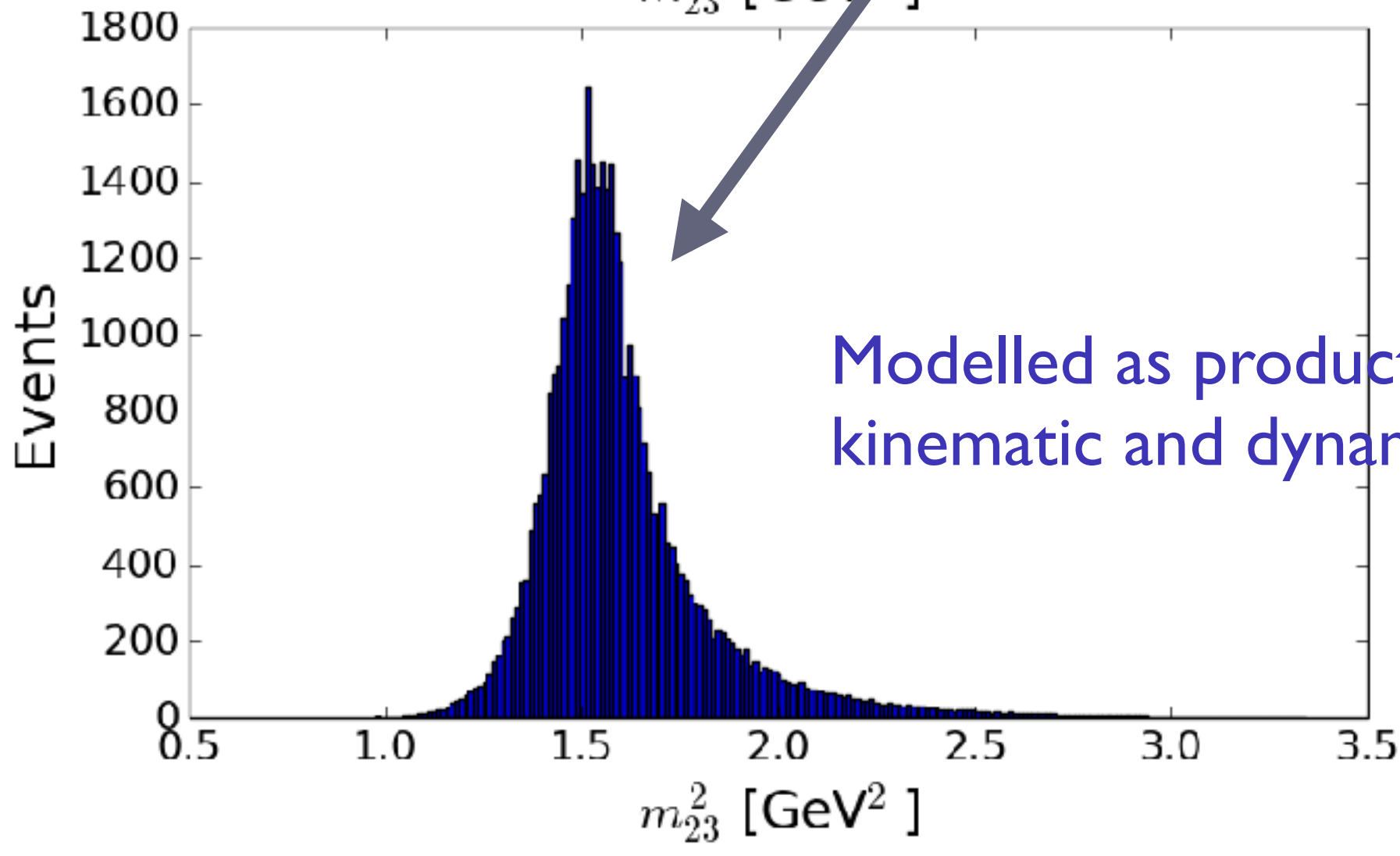
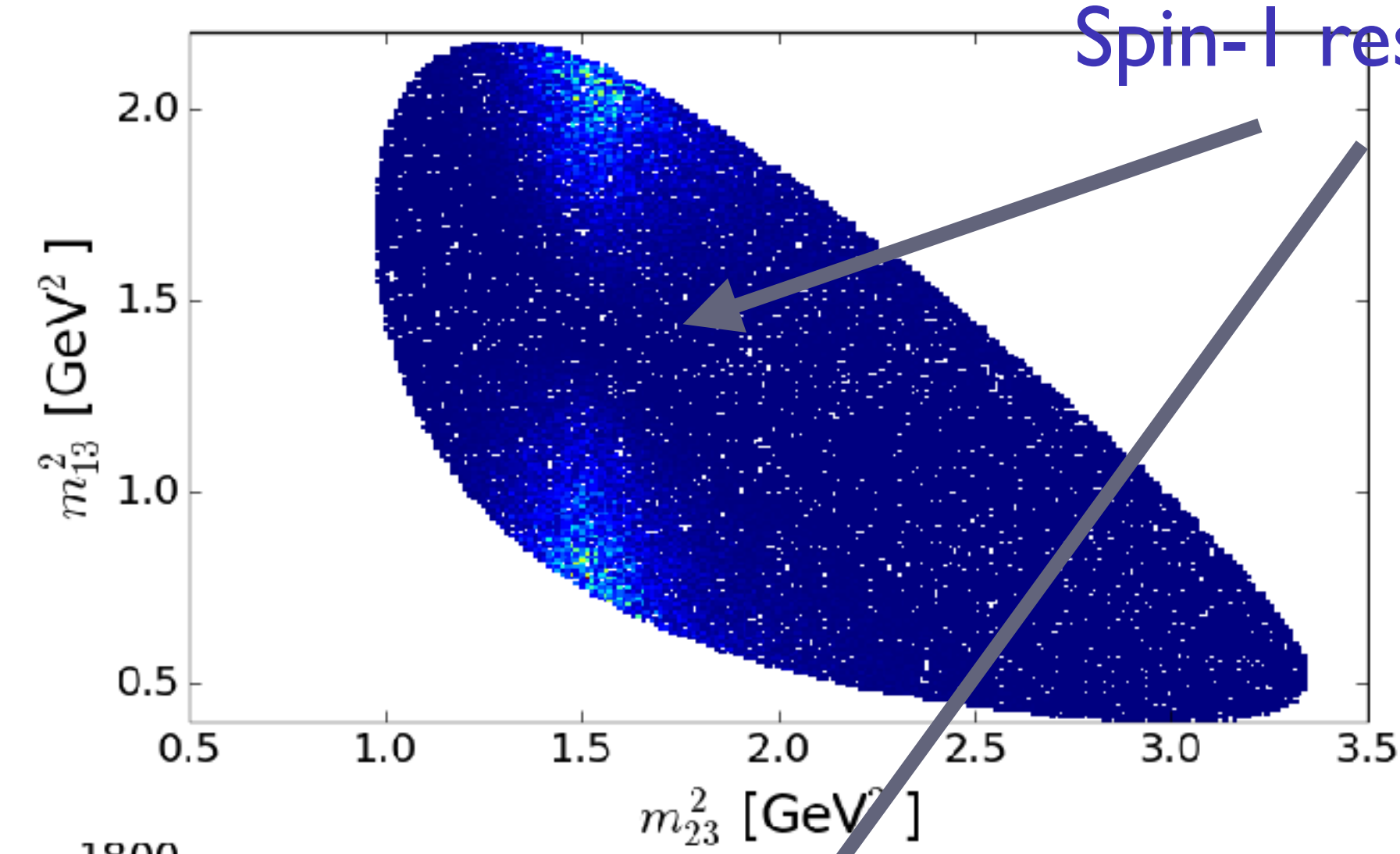
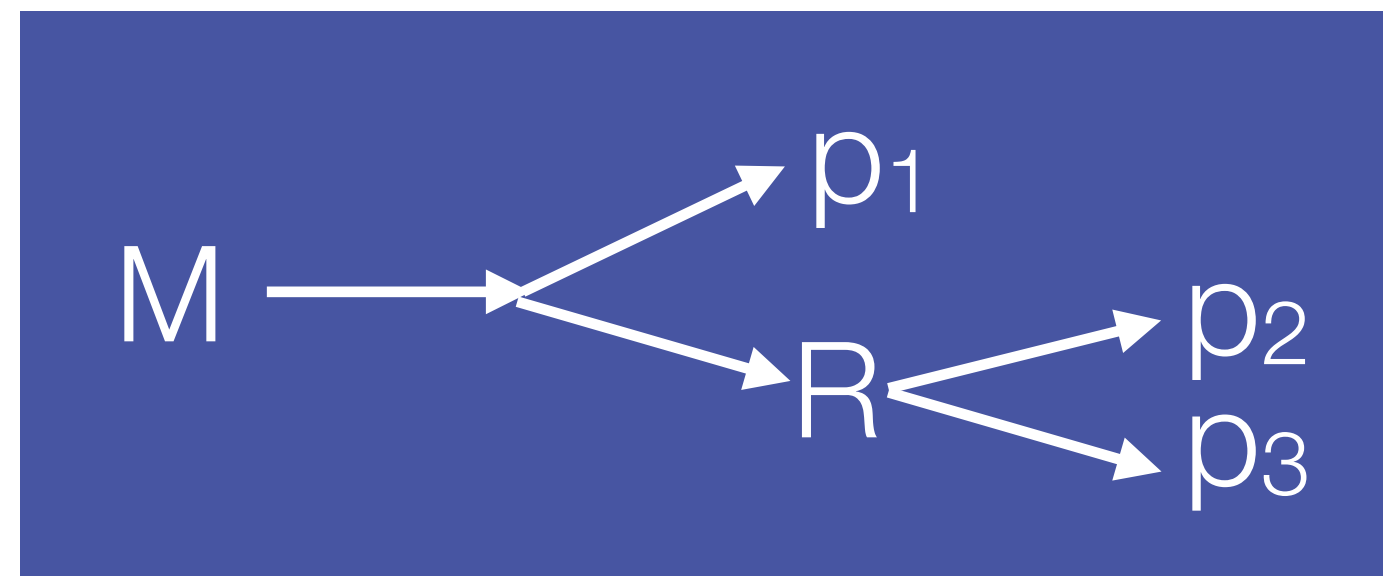
Constraints	Degrees of freedom
3 four-vectors	+12
All decay in same plane ($p_{i,z} = 0$)	-3
$E_i^2 = m_i^2 + p_i^2$	-3
Energy + momentum conservation	-3
Rotate system in plane	-1
Total	+2



Reminder about Dalitz plots



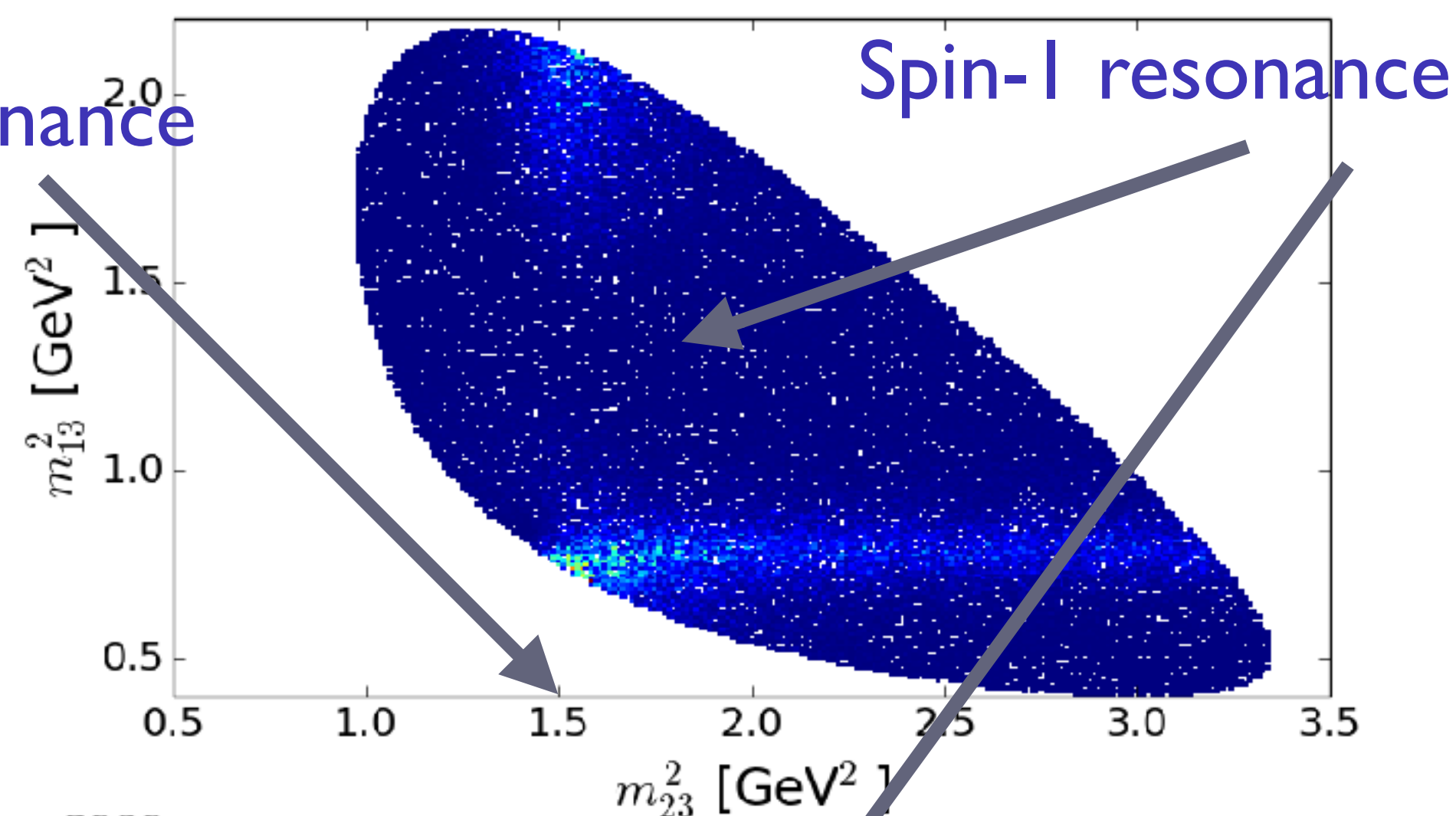
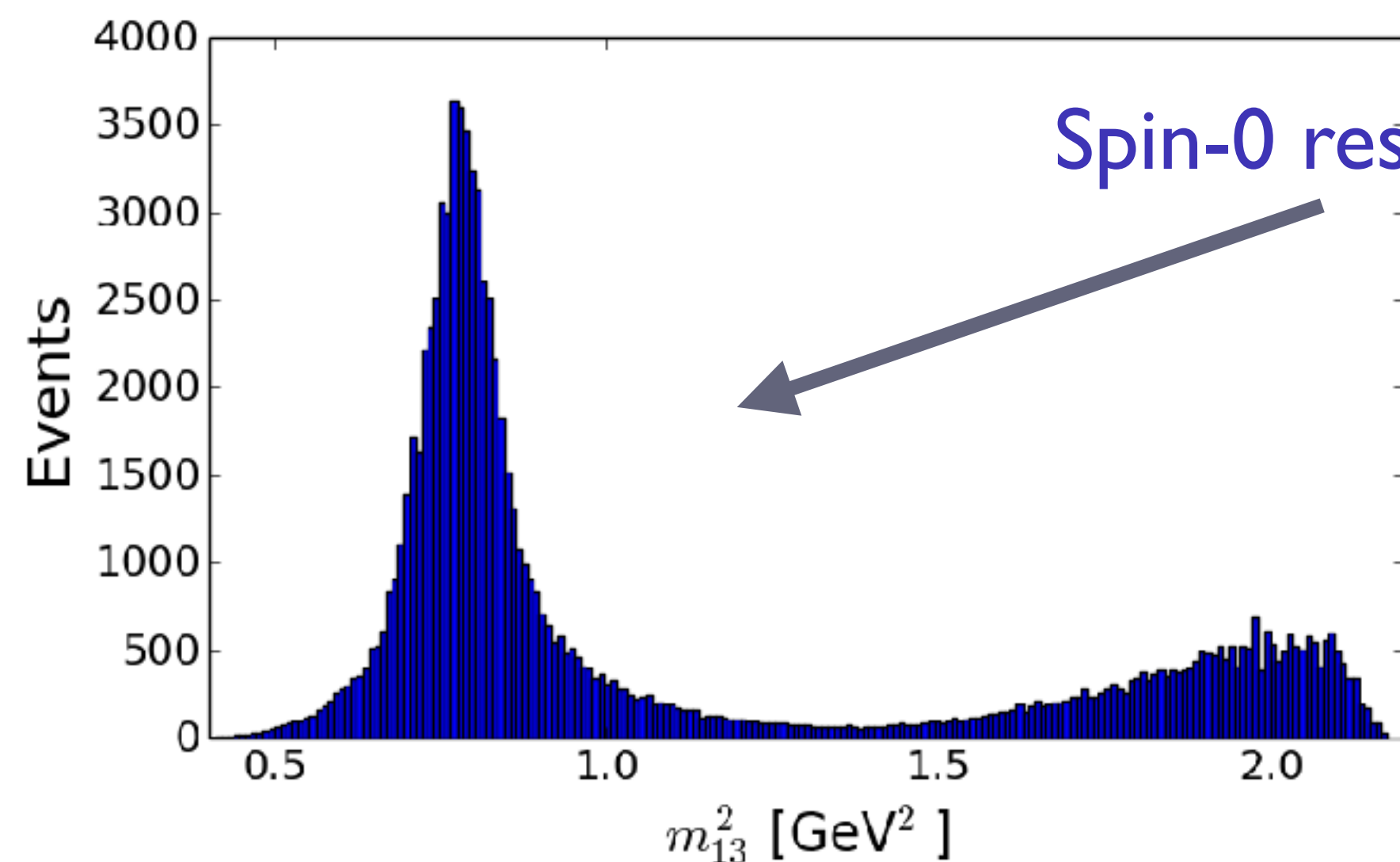
Peaks in distribution do not correspond to a real resonance - just a shadow/reflection



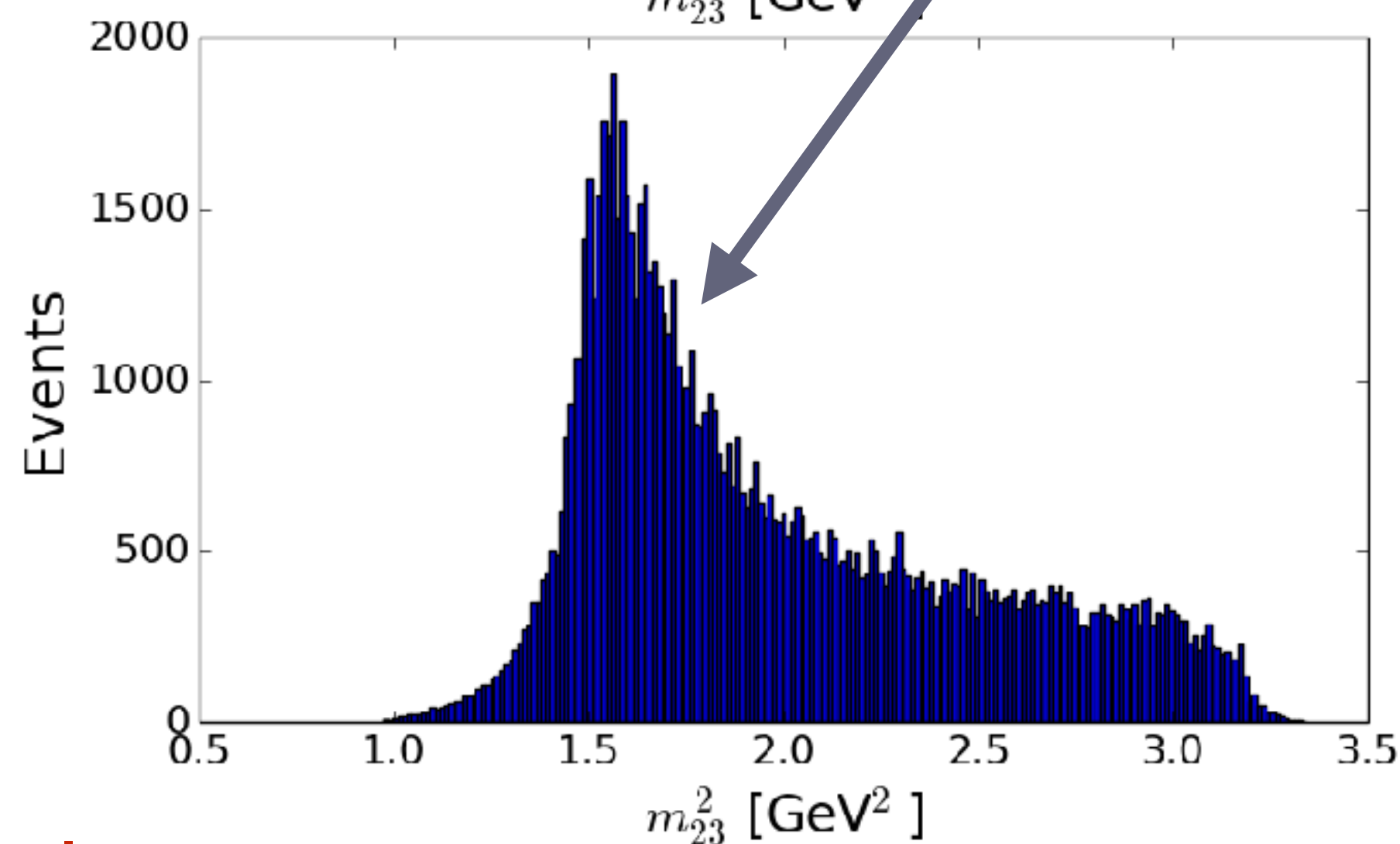
Modelled as product of Breit-Wigner, kinematic and dynamic factors

$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{32M^3} |\overline{\mathcal{M}}|^2 dm_{12}^2 dm_{23}^2$$

Reminder about Dalitz plots



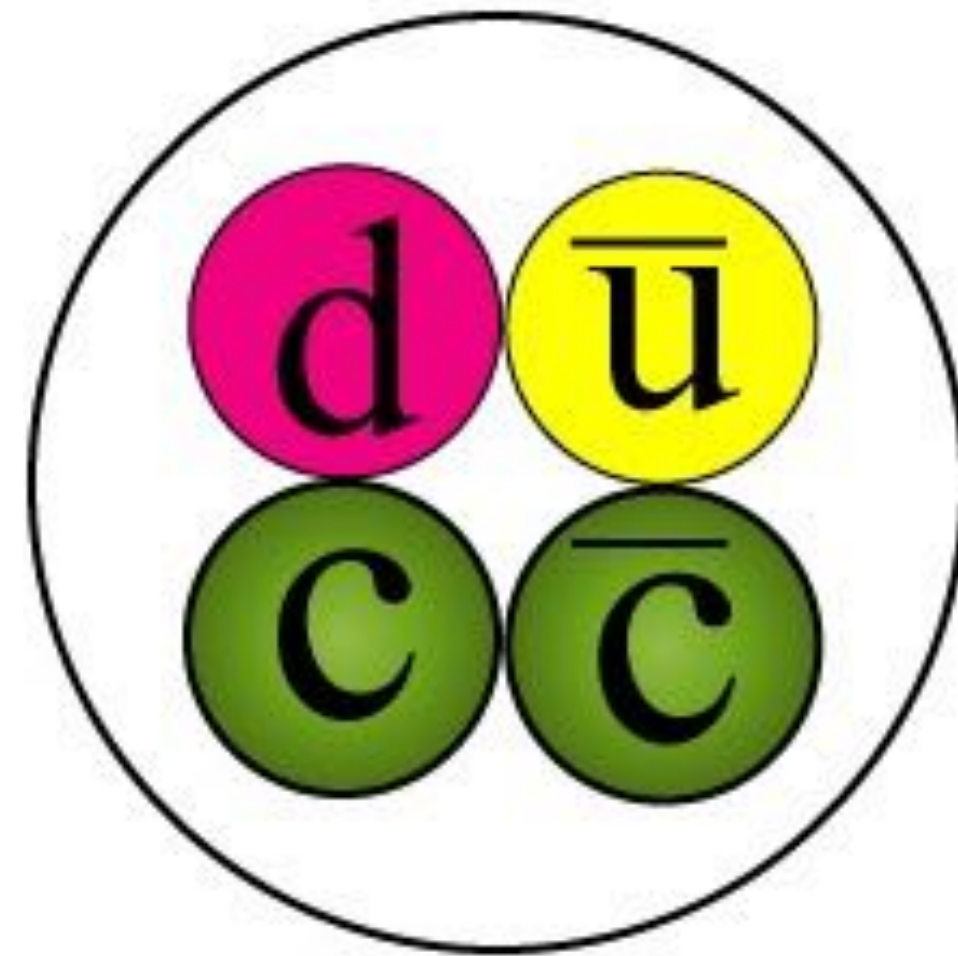
Use an **amplitude model** to disentangle interfering resonances and determine their properties



For decays involving fermions and/or vector particles then need to extend to more than 2 dimensions

$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{32M^3} |\overline{\mathcal{M}}|^2 dm_{12}^2 dm_{23}^2$$

Exotic mesons

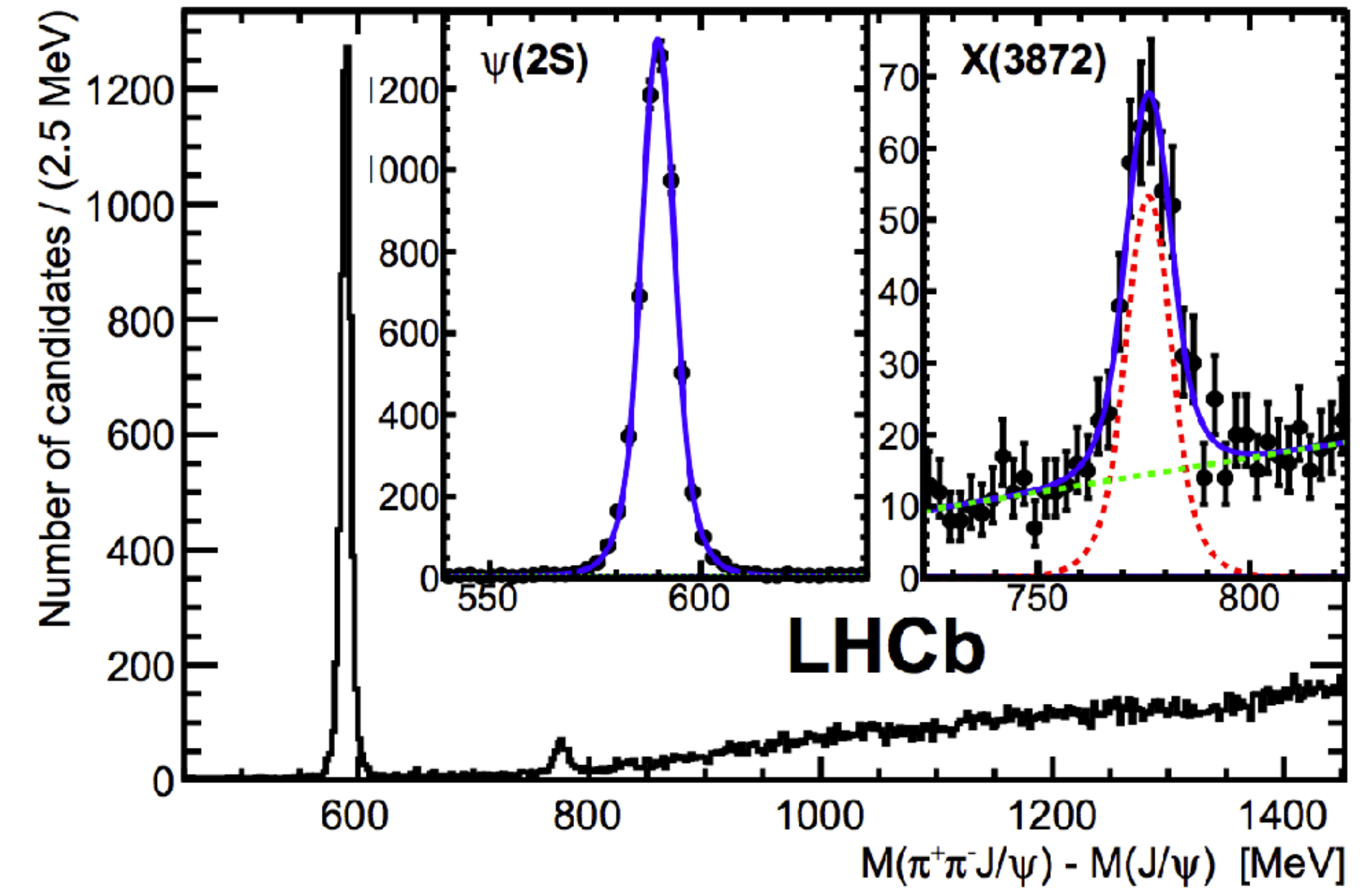


The X(3872) revolution

[PRL 110 (2013) 222001]

Observation in 2003 by Belle has led to a revolution in exotic hadron spectroscopy [PRL 91 (2003) 262001 with >1100 citations!]

Many phenomenological models: $[c\bar{u}][\bar{c}u]$ tetraquark, $D^0\bar{D}^{*0} = (c\bar{u})(\bar{c}u)$ molecule, $c\bar{c}g$ hybrid, hadrocharmonium...



Observation

Note

Most studied state, but many open questions

$$\Gamma_{X(3872)} < 1.2 \text{ MeV}/c^2$$

$$M_{X(3872)} = 3871.69 \pm 0.17 \text{ MeV}/c^2$$

$$M_{D^0} + M_{D^{*0}} = 3871.81 \pm 0.09 \text{ MeV}/c^2$$

[PDG]

$B \rightarrow KX(3872)$	$\left\{ \begin{array}{l} \rightarrow J/\psi\rho^0, J/\psi\pi^+\pi^- \\ \rightarrow J/\psi\omega(\rightarrow \pi^+\pi^-\pi^0) \\ \rightarrow D^0\bar{D}^{*0}, D^0\bar{D}^0\pi^0 \\ \rightarrow \gamma J/\psi, \gamma\psi(3686) \end{array} \right.$	Belle [63], BaBar [84]
		Belle [75], BaBar [90]
		Belle [76], BaBar [87]
		Belle [75], BaBar [86]
$p\bar{p} \rightarrow \dots + X(3872)(\rightarrow J/\psi\pi^+\pi^-)$		CDF [67], D0 [68]
$pp \rightarrow \dots + X(3872)$	$\left\{ \begin{array}{l} \rightarrow J/\psi\pi^+\pi^- \\ \rightarrow \gamma J/\psi, \gamma\psi(3686) \end{array} \right.$	LHCb [91], CMS [73]
		LHCb [92]
$e^+e^- [\rightarrow Y(4260)] \rightarrow \gamma X(3872)(\rightarrow J/\psi\pi^+\pi^-)$		BESIII [93]

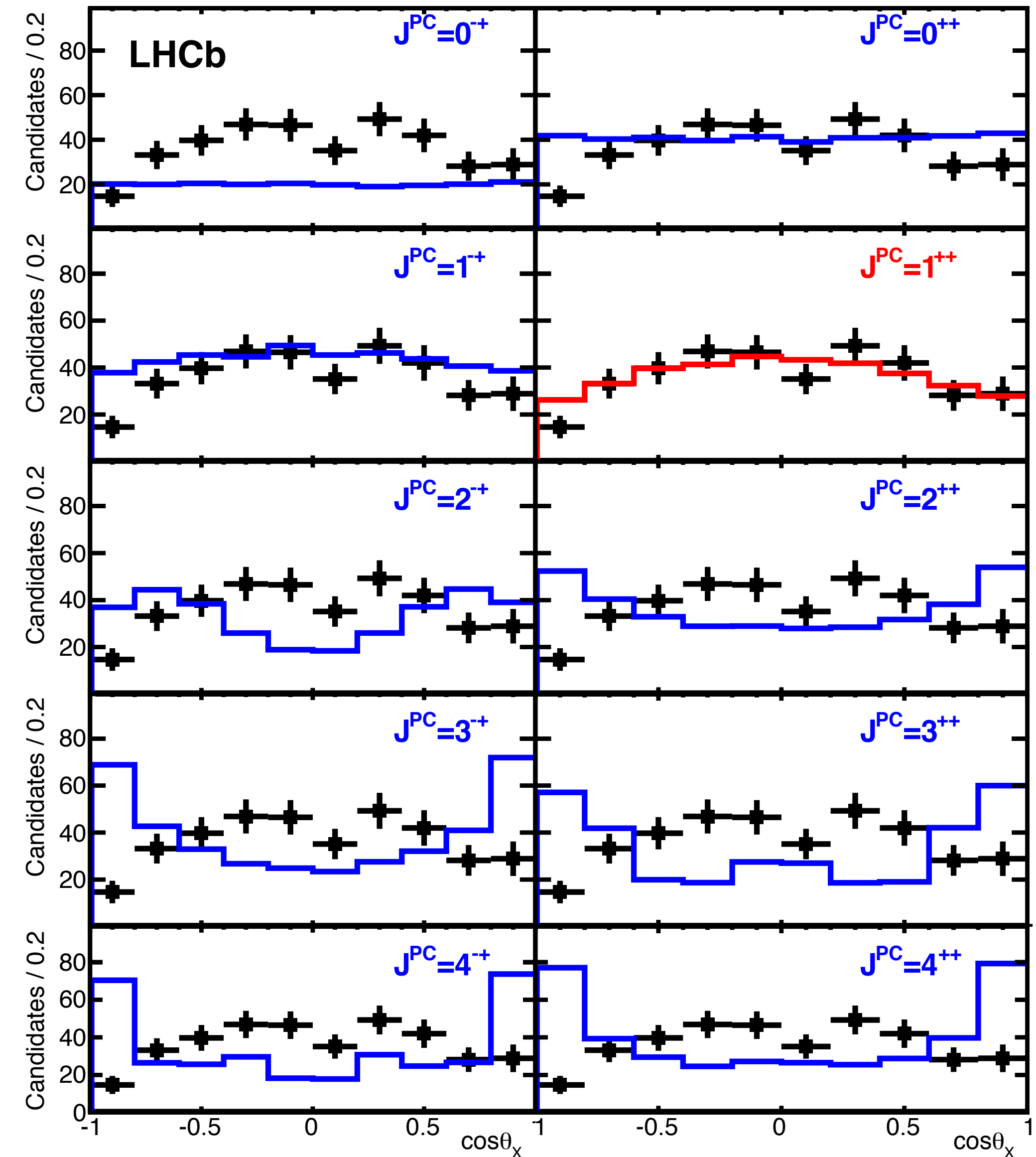
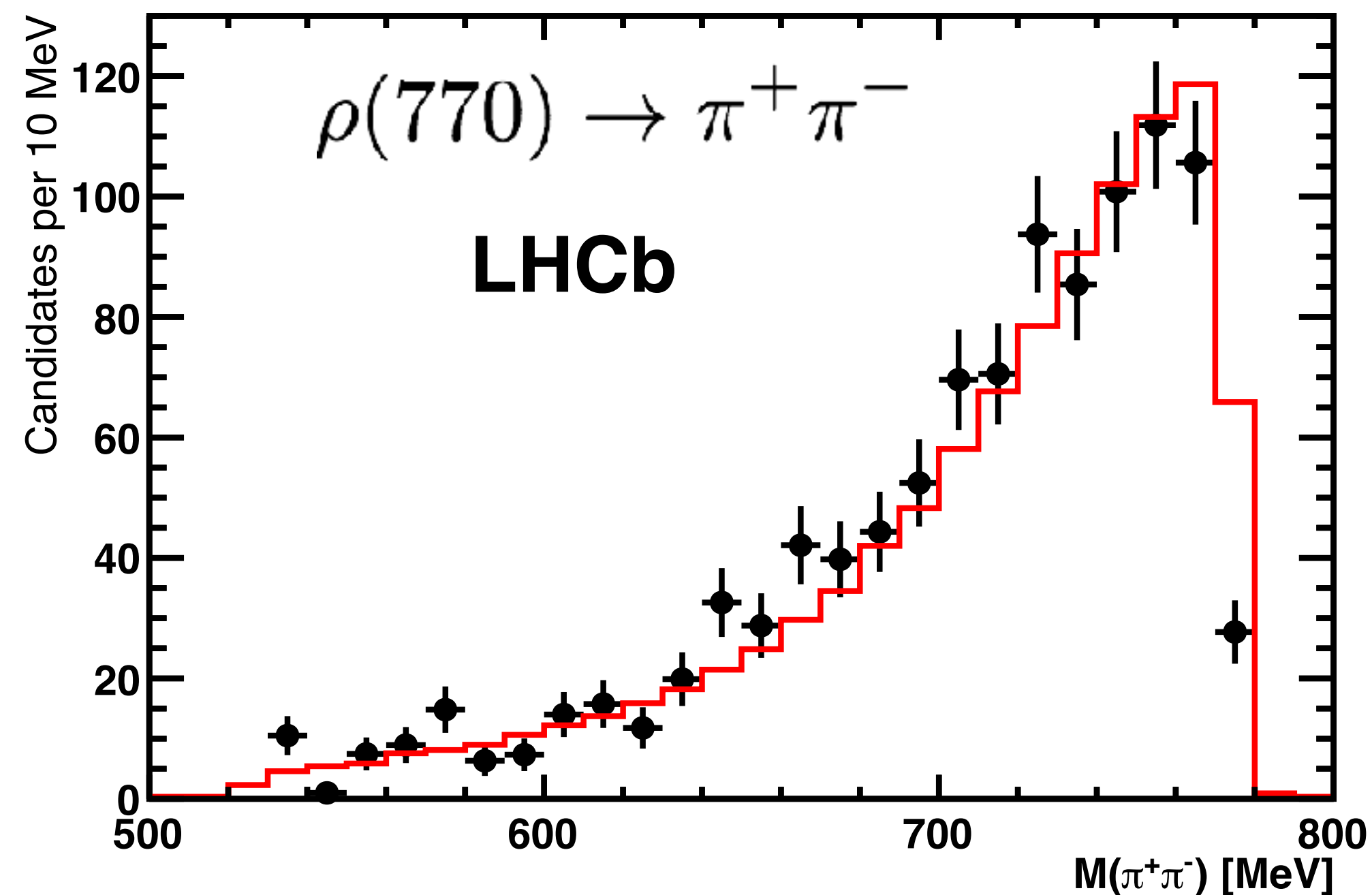
X(3872) quantum numbers

[PRD 92 (2015) 011102]

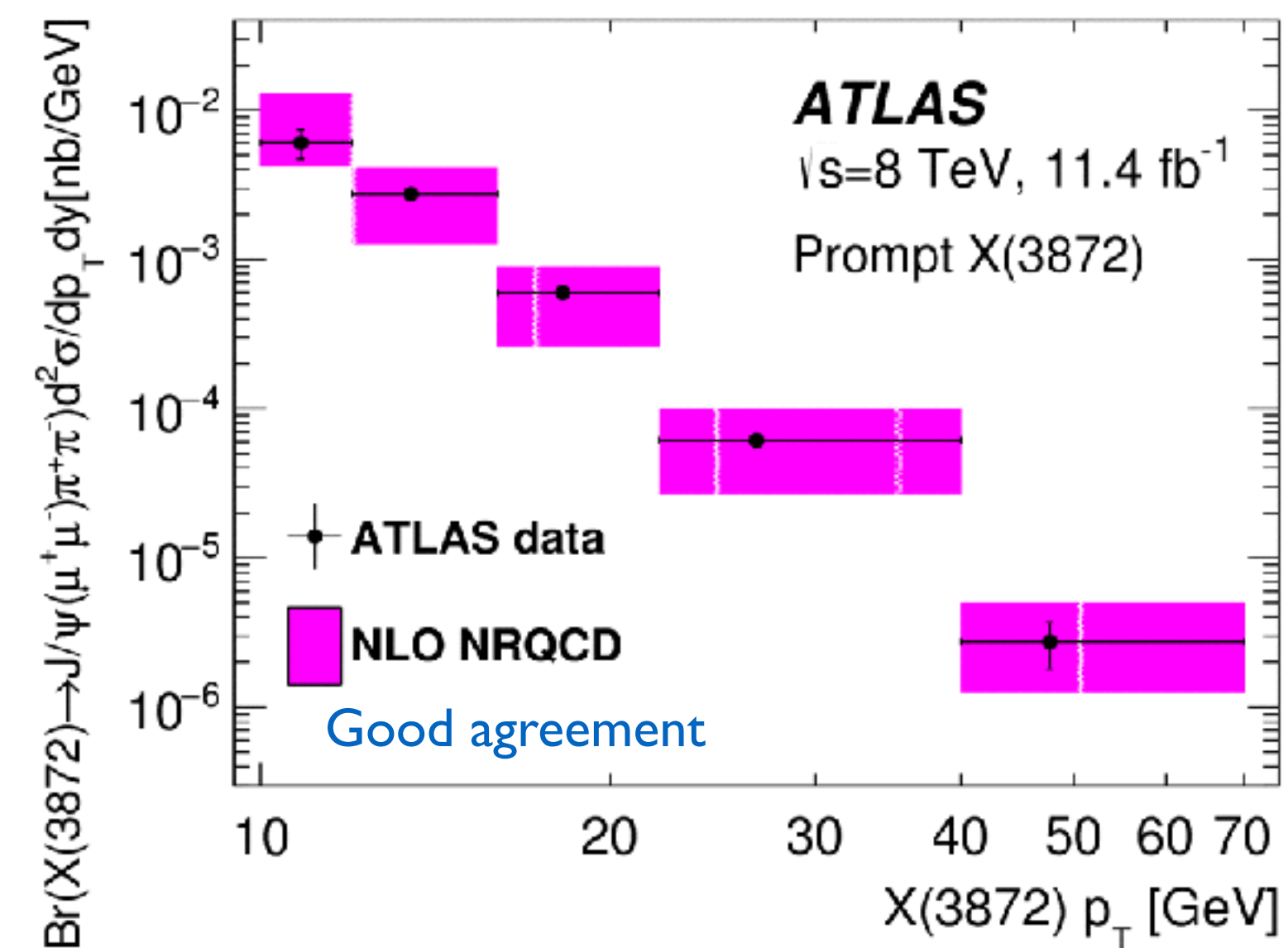
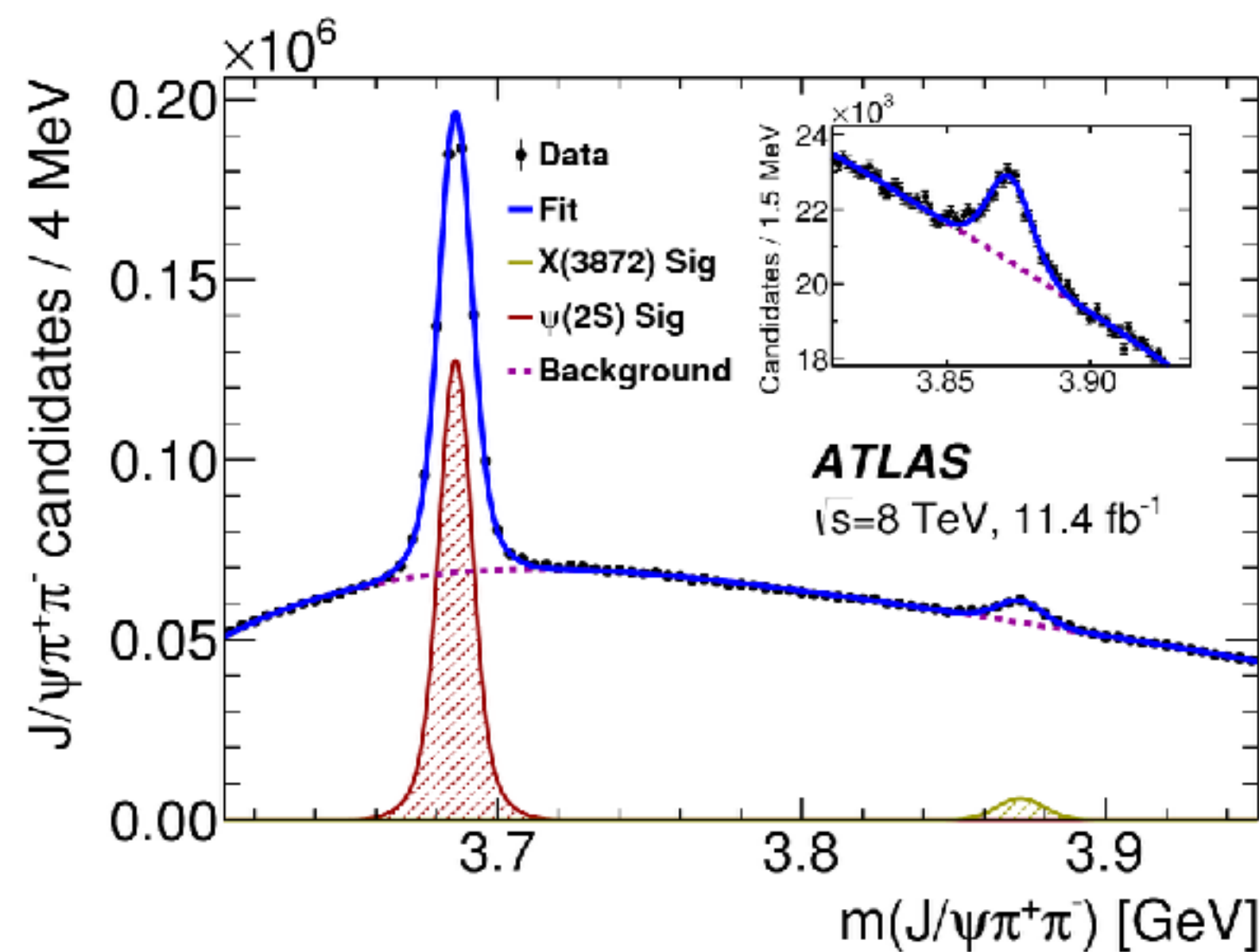
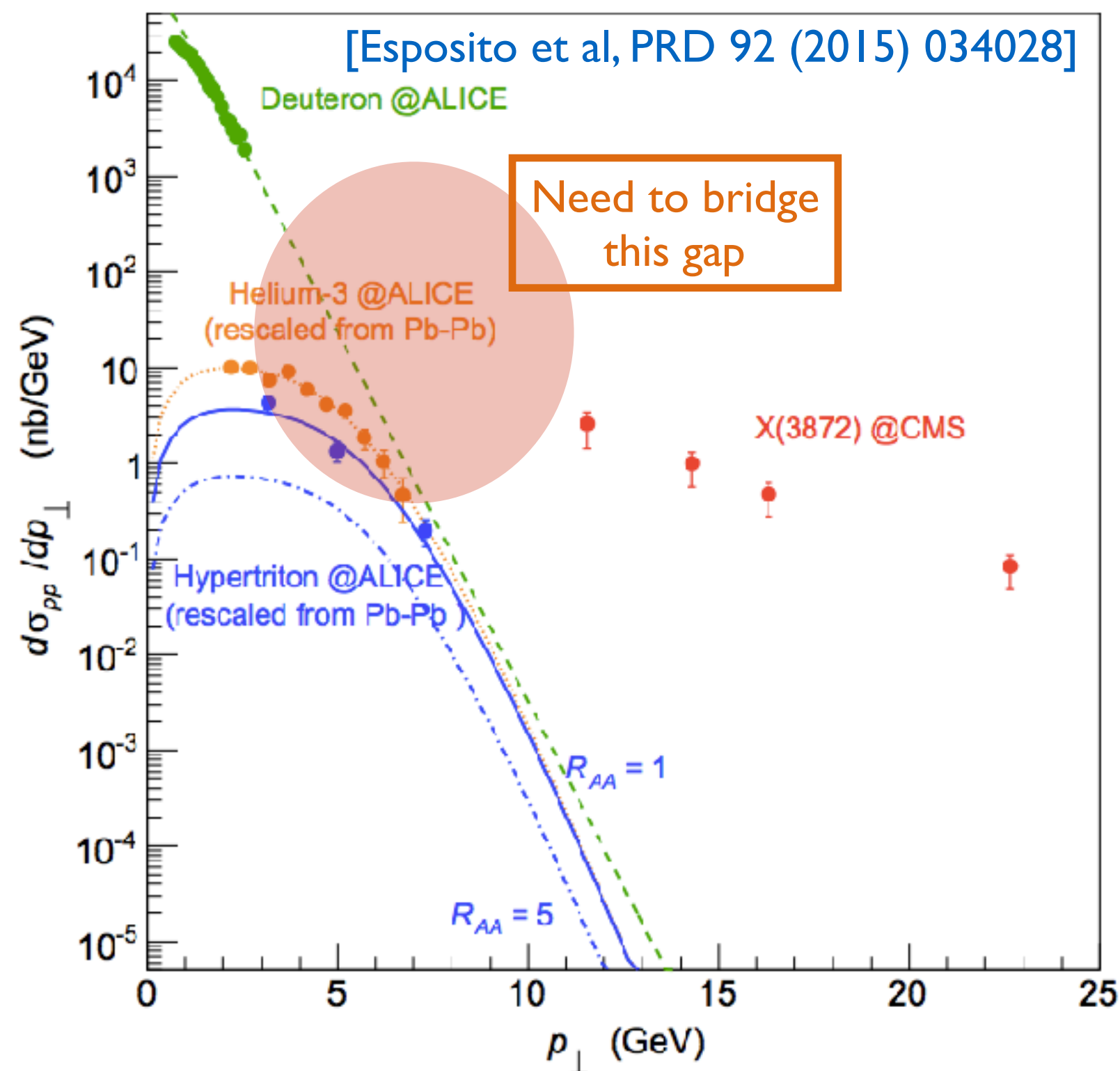
$J^{PC} = 1^{++}$ confirmed!

D-wave $< 4\%$ @ 95% CL (i.e., negligible)

$\rho(770)$ dominates \rightarrow decay violates isospin so unlikely to be conventional $c\bar{c}$



X(3872) production



X(3872) seen in pp and $p\bar{p}$ collisions.

[D0, PRL 103 (2009) 152001] [ATLAS, JHEP 01 (2017) 117] [LHCb, JHEP 04 (2013) 154]
[CDF, PRL 103 (2009) 152001] [CMS, JHEP 04 (2013) 154]

Compare cross-section with that of known molecules to understand X(3872) nature.

NLO NRQCD considers X(3872) to be a mixture of $\chi_{c1}(2P)$ and a $D^0\bar{D}^{*0}$ molecular state, with the production dominated by the $\chi_{c1}(2P)$ part

[Artoisenet and Braaten, PRD 81 (2010) 114018]

Supported by BR of
X(3872) → [c \bar{c}] γ decays
[NPB 886 (2014) 665]

$Z(4430)^-$ charged charmonium exotic

[Belle, PRL 100 (2008) 142001] 1D fit to $m(\psi'\pi^-)$

[BaBar, PRD 79 (2009) 112001] Not observed but does not contradict Belle!

[Belle, PRD 80 (2009) 031104] 2D amplitude fit to $m(\psi'\pi^-)$ vs $m(K^+\pi^-)$

[Belle, PRD 88 (2013) 074026] 4D amplitude fit

6.5σ

6.4σ

6.4σ

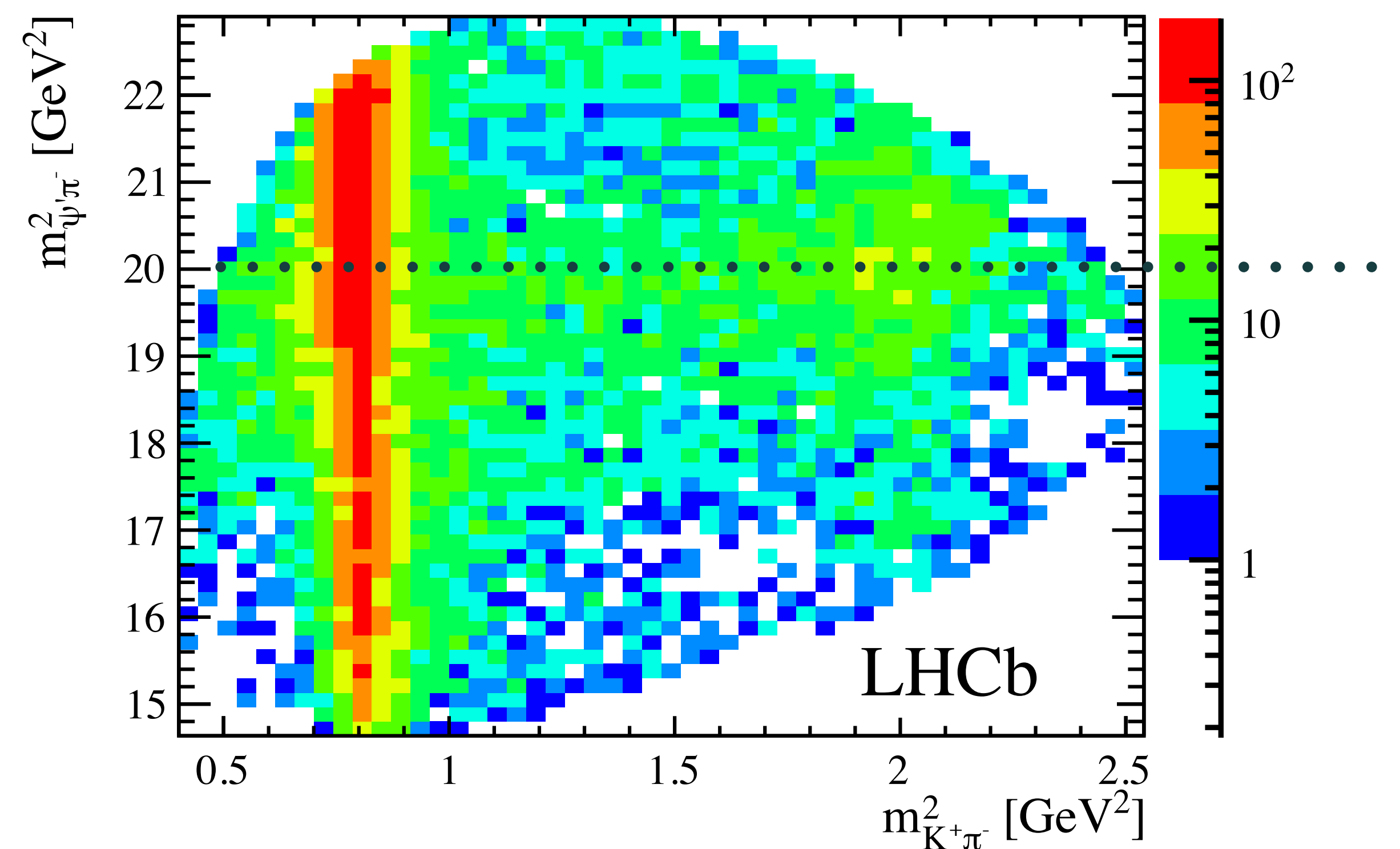
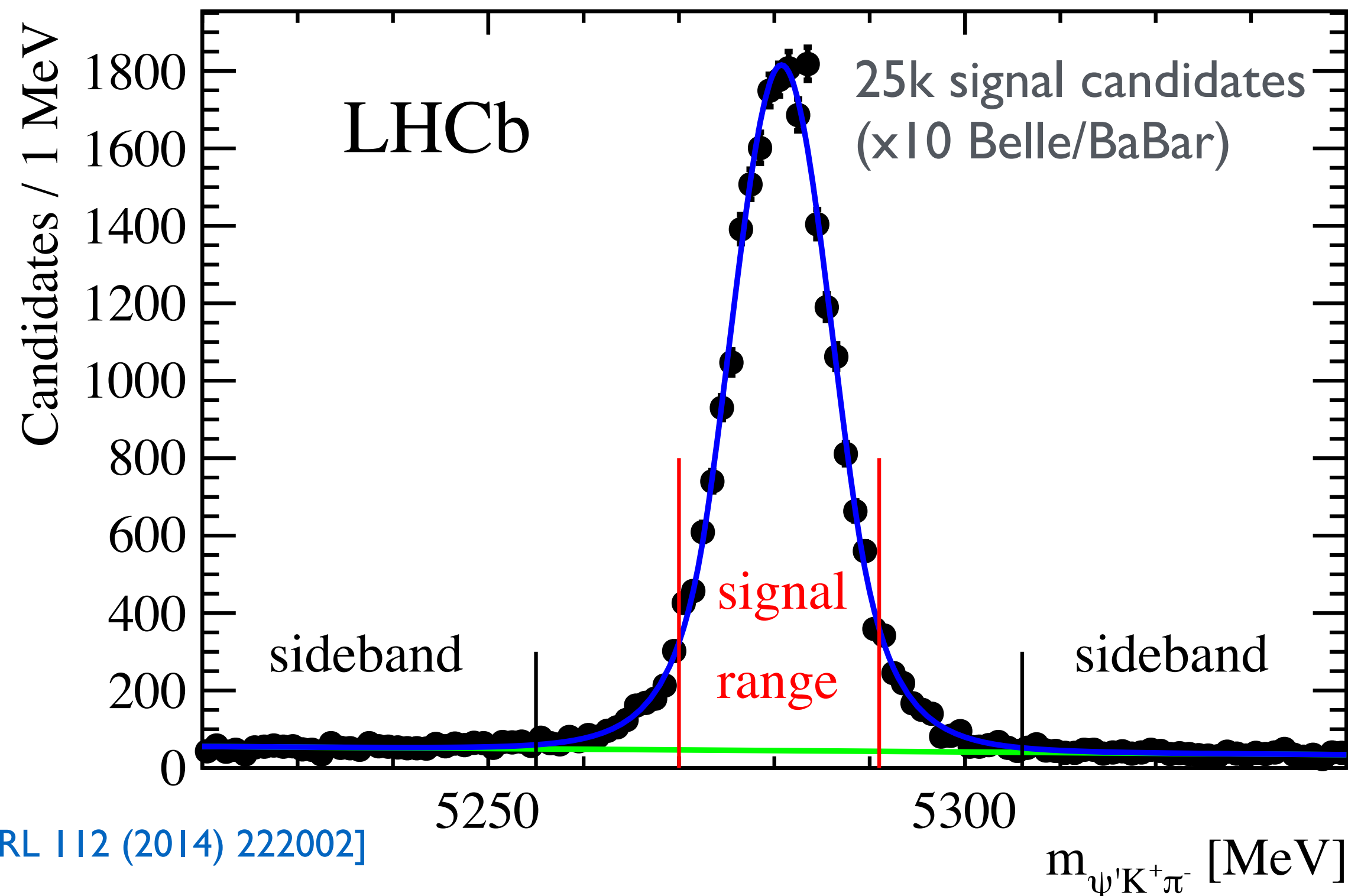


$$B^0 \rightarrow \psi(2S)K^+\pi^-, \psi(2S) \rightarrow \mu^+\mu^-$$

- dimuon in final state \rightarrow highly efficient for triggering

$$B^0 \rightarrow Z(4430)^-K^+, Z(4430)^- \rightarrow \psi(2S)\pi^-$$

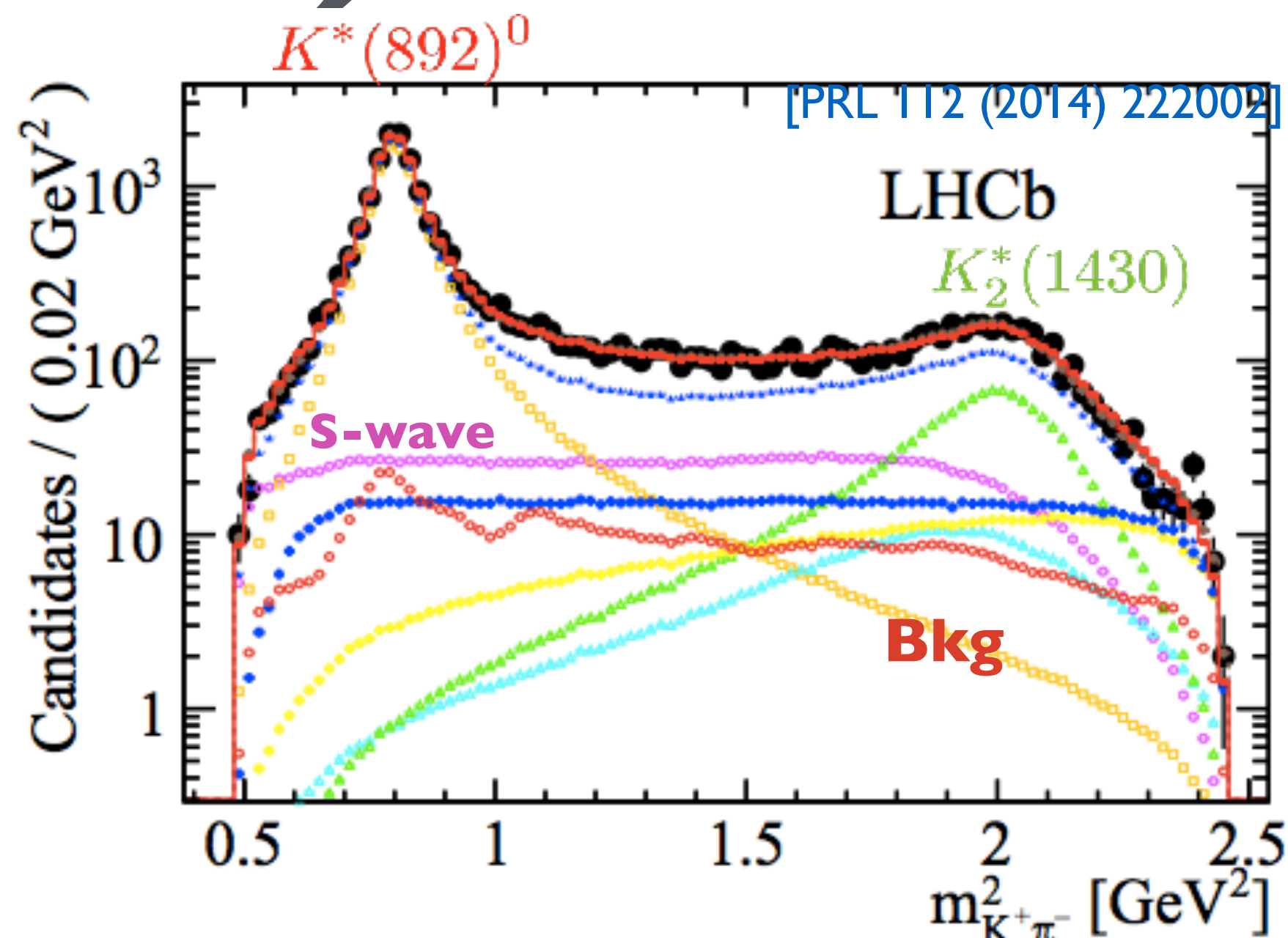
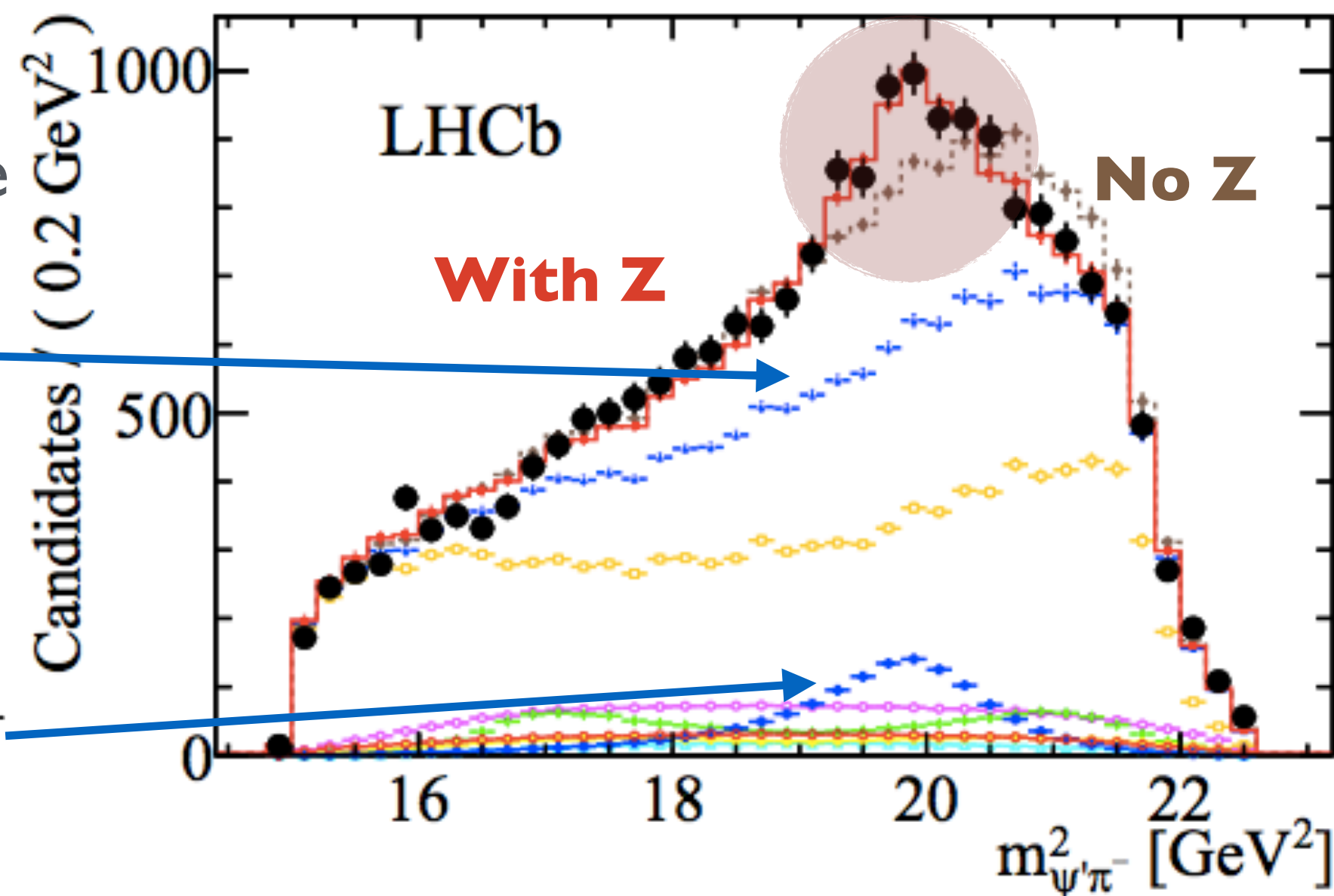
Only 2 of the 4 dimensions...



Confirmation of the $Z(4430)^-$

Everything except the $Z^- \Rightarrow$ large interference between Z^- and $K^+\pi^-$ sector

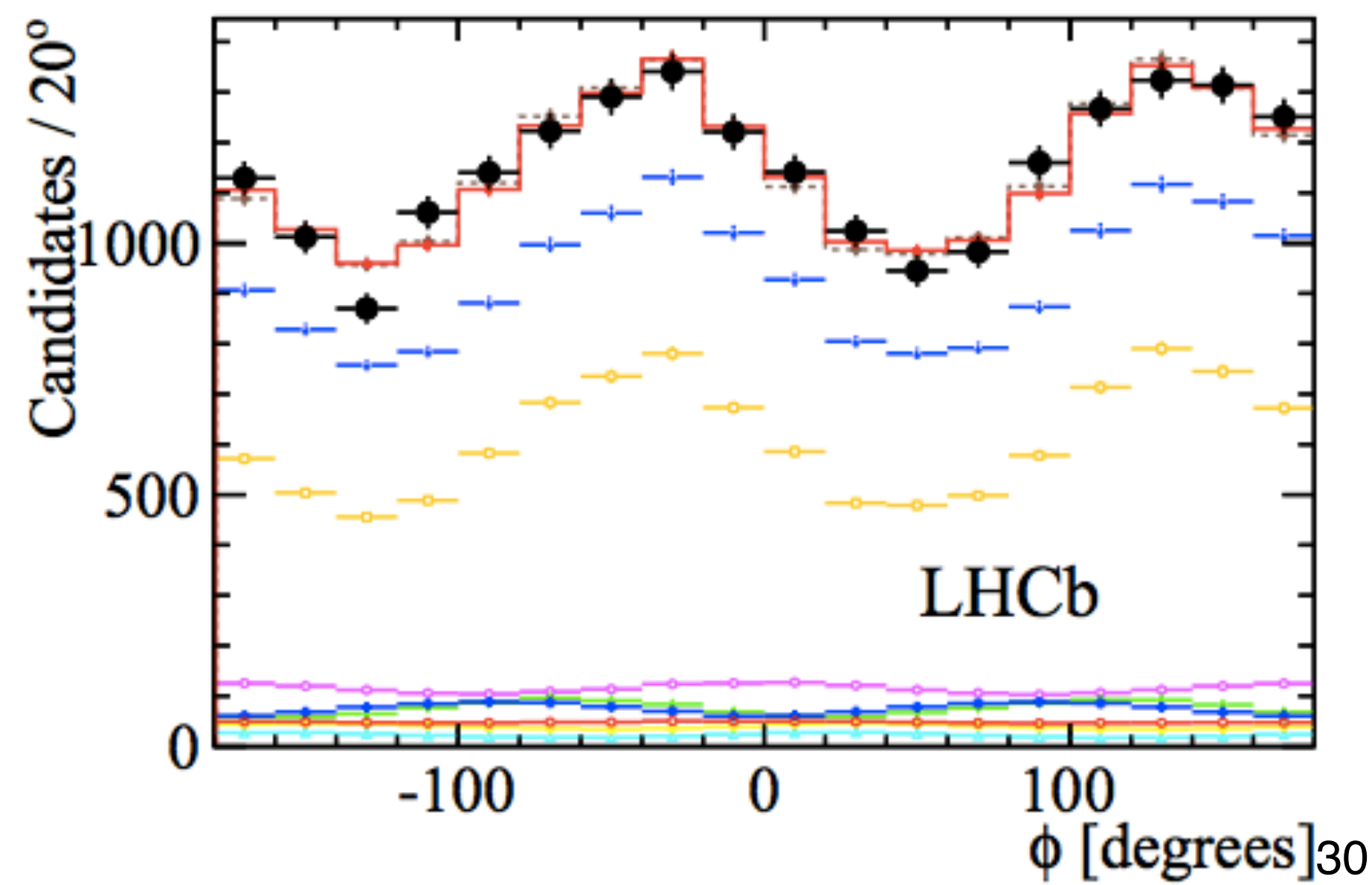
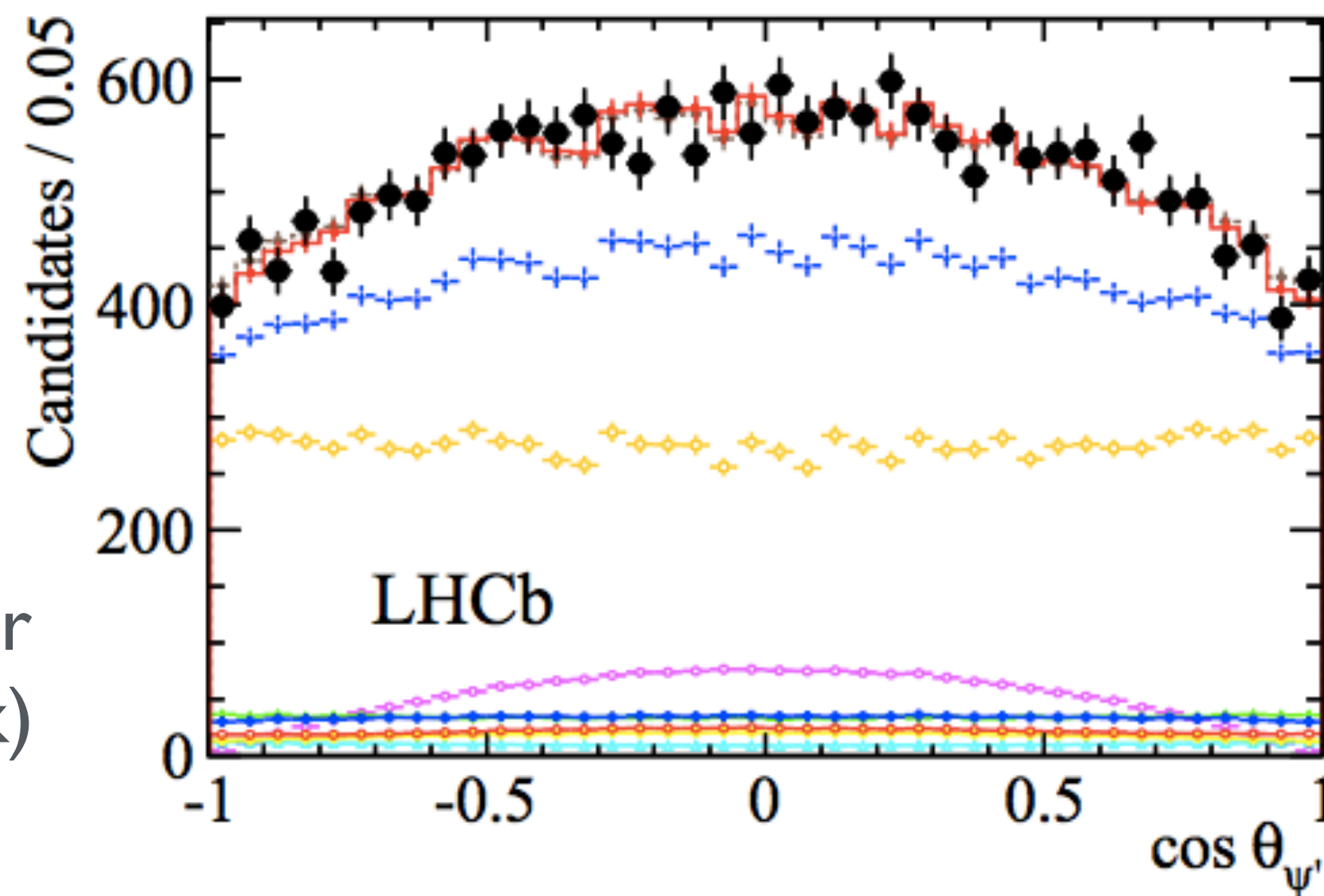
Z^- component
 $J^P = 1^+$



4D amplitude analysis used to measure Z^- parameters (BW mass and width) and J^P

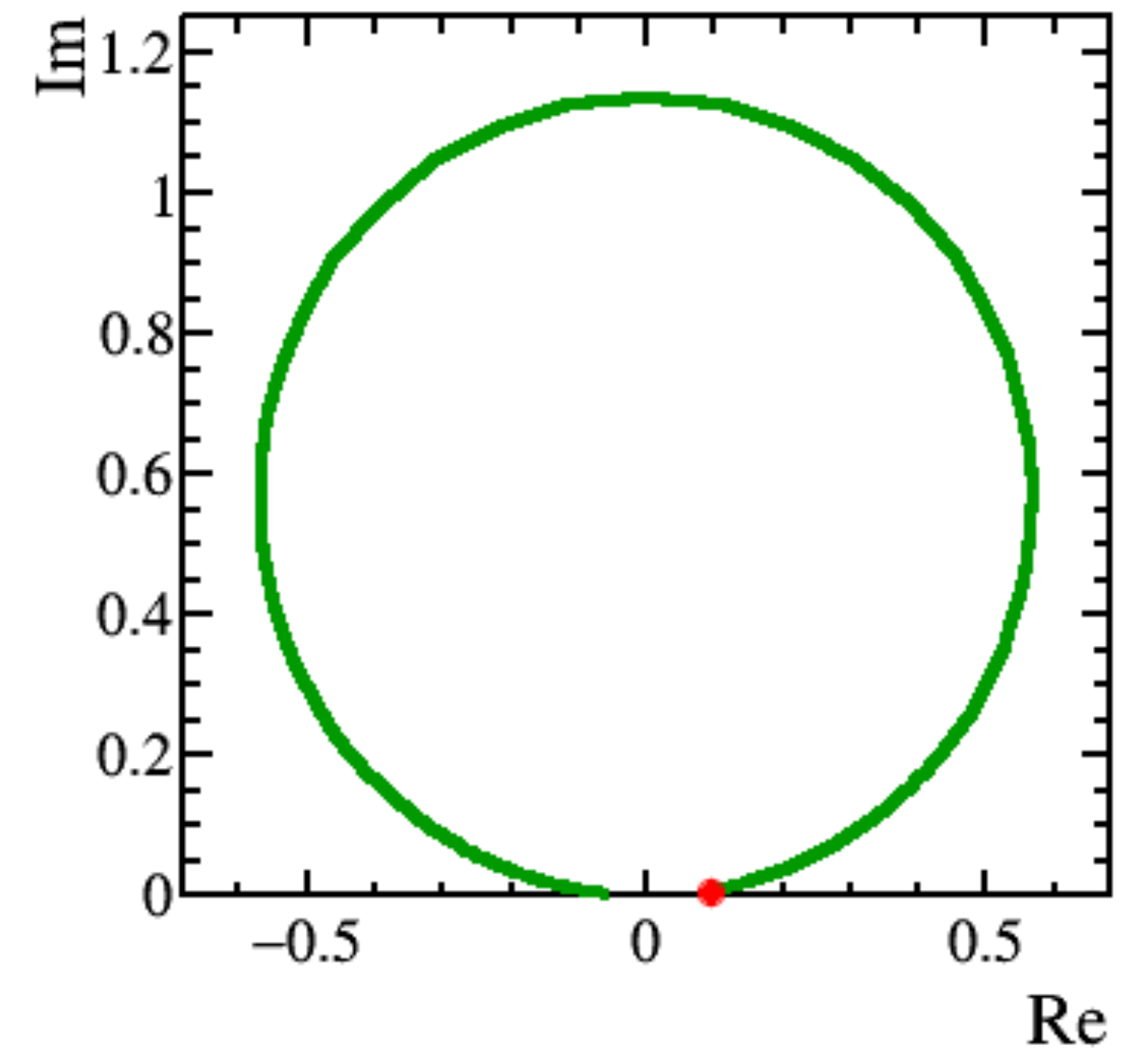
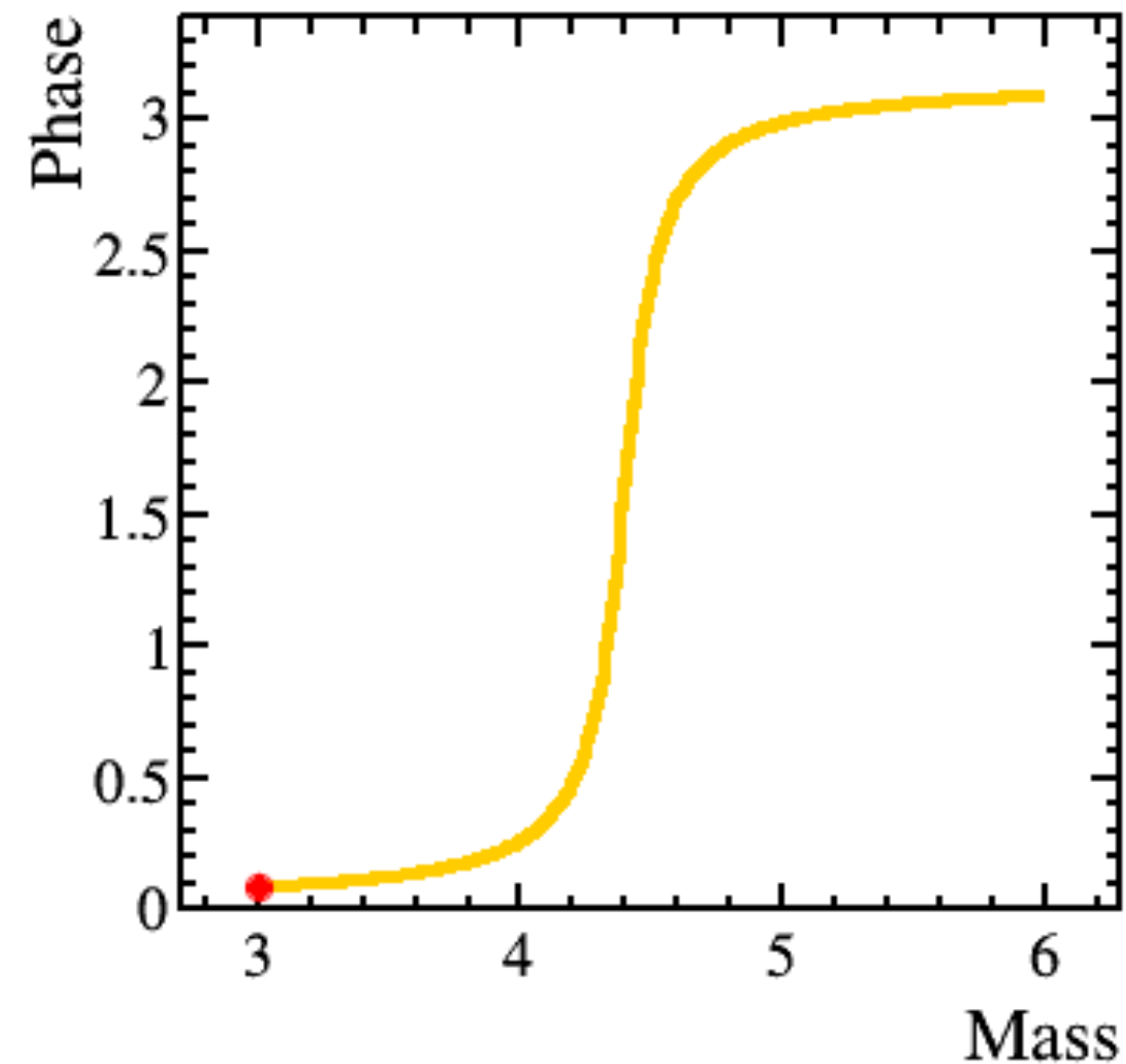
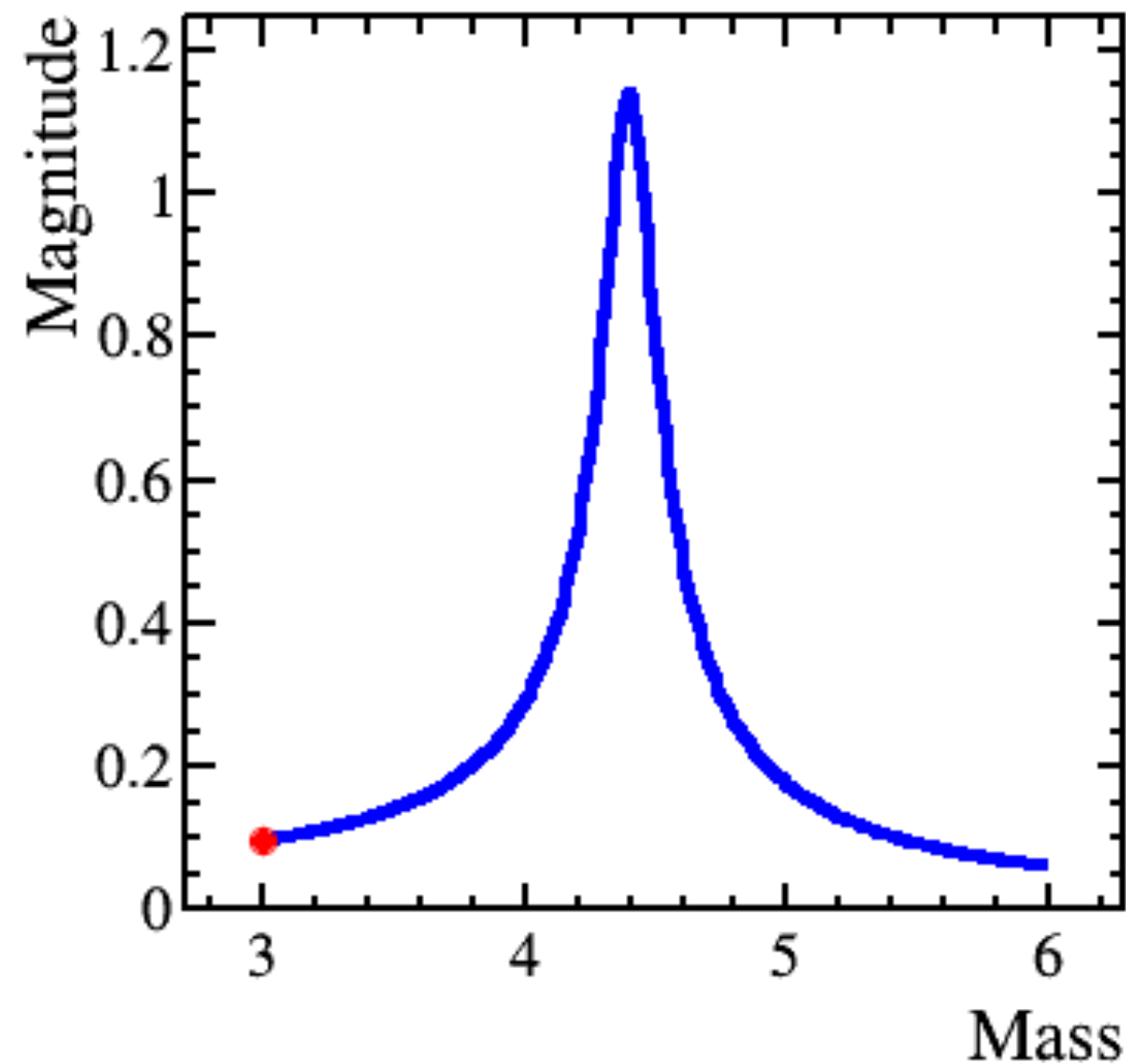
Study angular moments in model-independent way (similar to what is done for pentaquark)

[PRD 92 (2015) 112009]



Resonant behaviour

Observe rapid change of phase near maximum of magnitude \Rightarrow **resonance!**



$$BW(m|m_0, \Gamma_0) = \frac{1}{m_0^2 - m^2 - im_0\Gamma(m)}$$

**Breit-Wigner resonance
parameterisation**

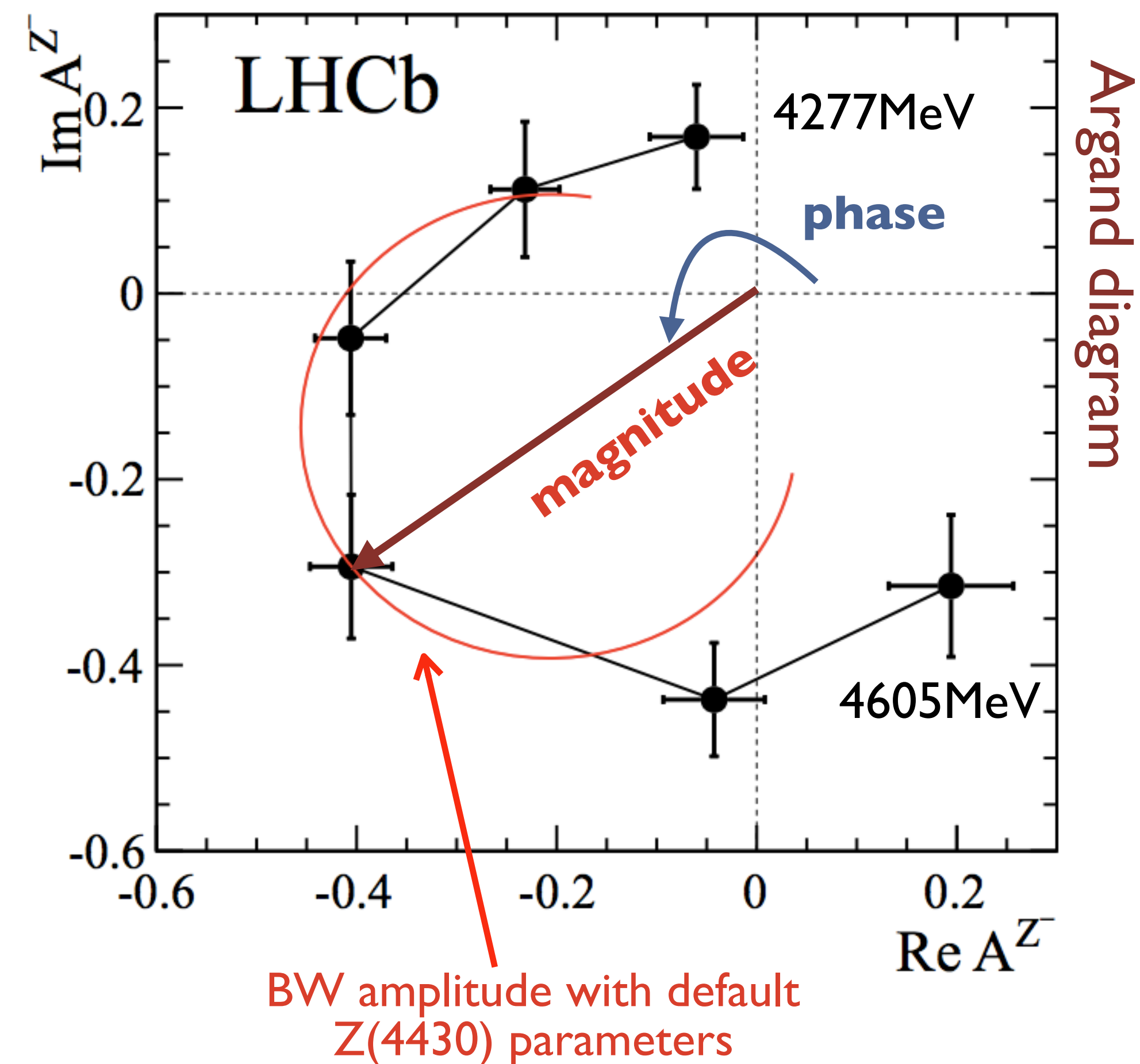
$$\Gamma(m) = \Gamma_0 \left(\frac{q}{q_0} \right)^{2L_{K^*}+1} \frac{m_0}{m} B'_{L_{K^*}}(q, q_0, d)^2$$

Argand diagram

[link](#)

Resonant behaviour

	LHCb	Belle
$M(Z)$ [MeV]	$4475 \pm 7^{+15}_{-25}$	$4485 \pm 22^{+28}_{-11}$
$\Gamma(Z)$ [MeV]	$172 \pm 13^{+37}_{-34}$	200^{+41+26}_{-46-35}
f_Z [%]	$5.9 \pm 0.9^{+1.5}_{-3.3}$	$10.3^{+3.0+4.3}_{-3.5-2.3}$
f_Z^I [%]	$16.7 \pm 1.6^{+2.6}_{-5.2}$	–
significance	$> 13.9\sigma$	$> 5.2\sigma$
J^P	1^+	1^+



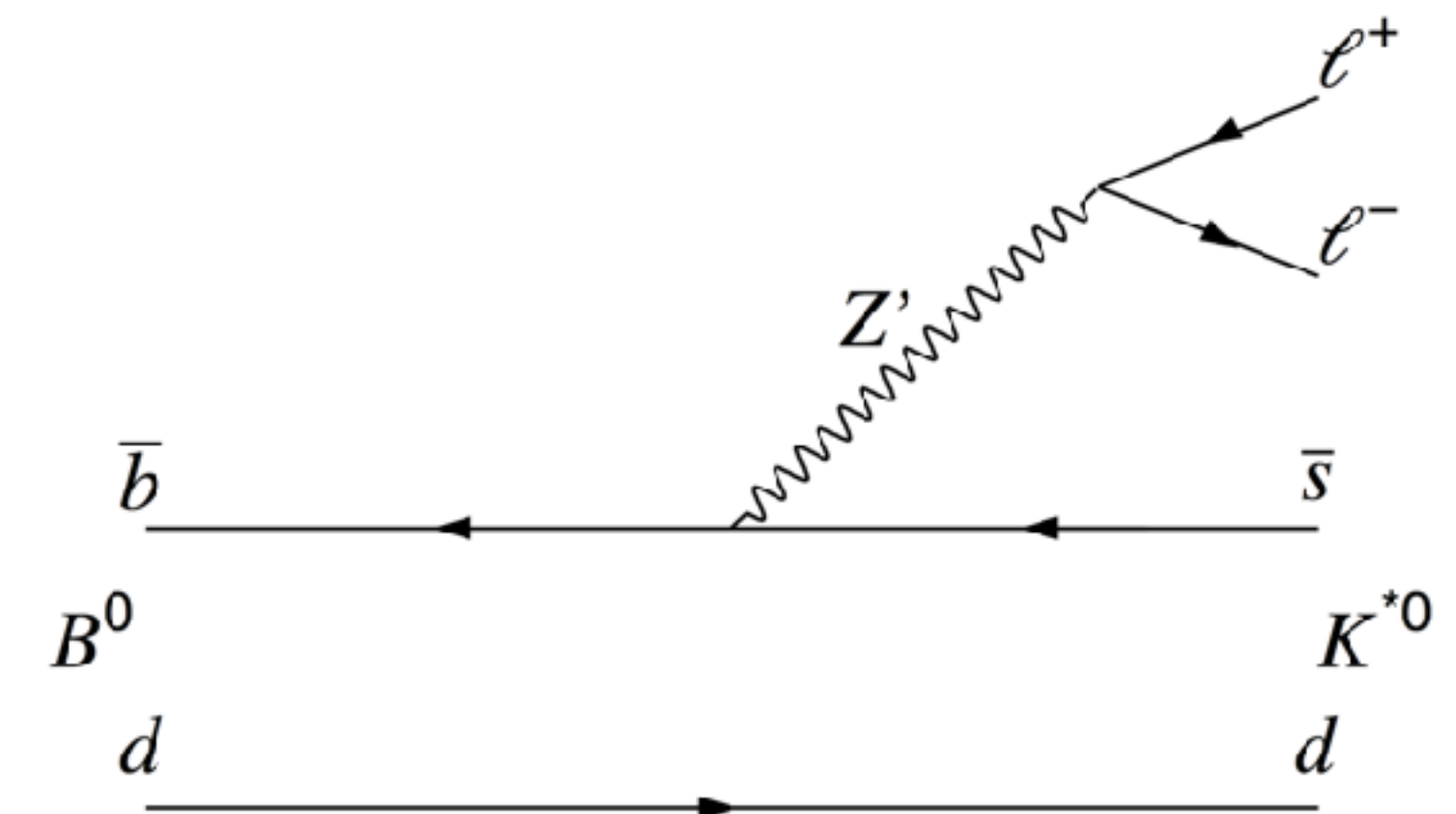
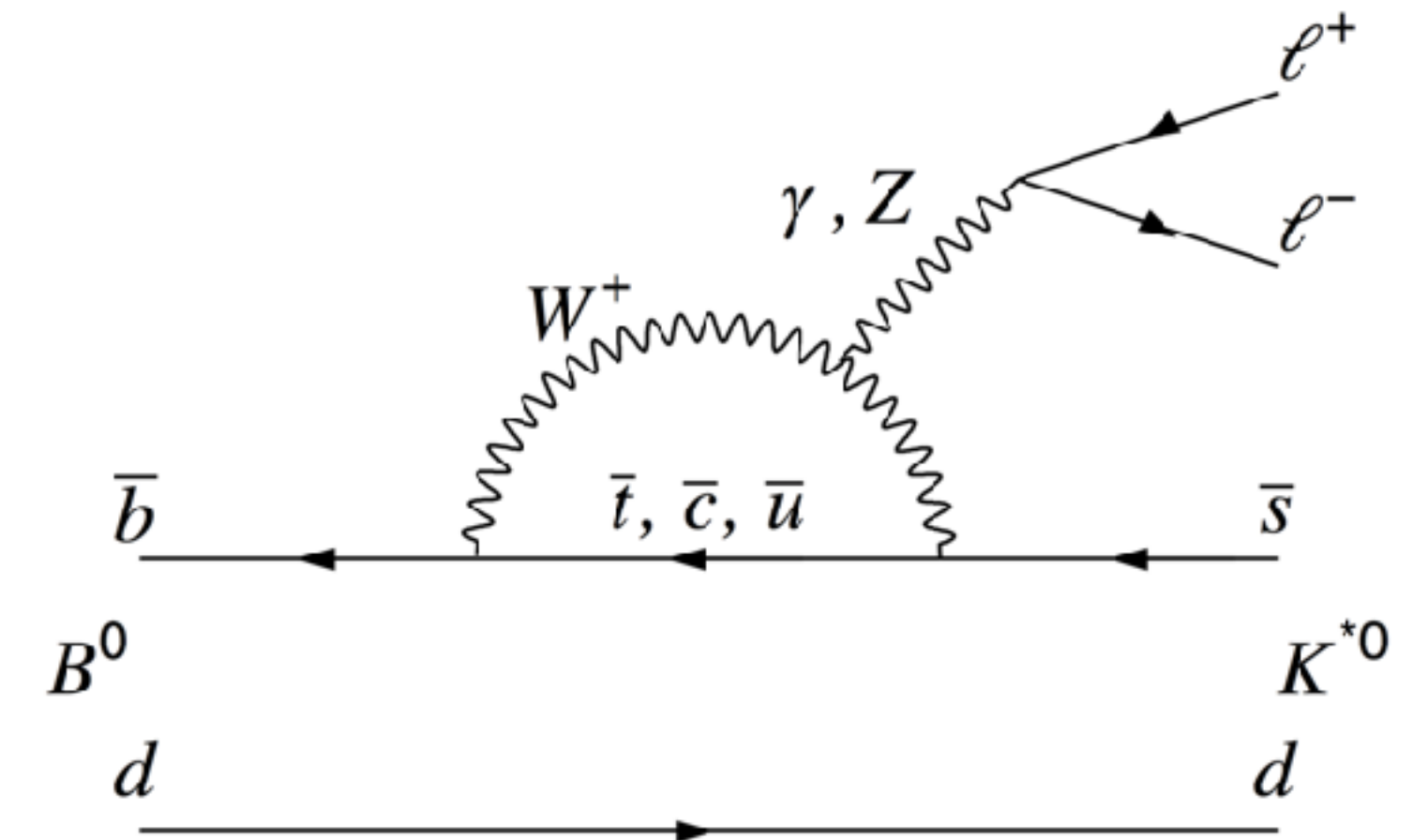
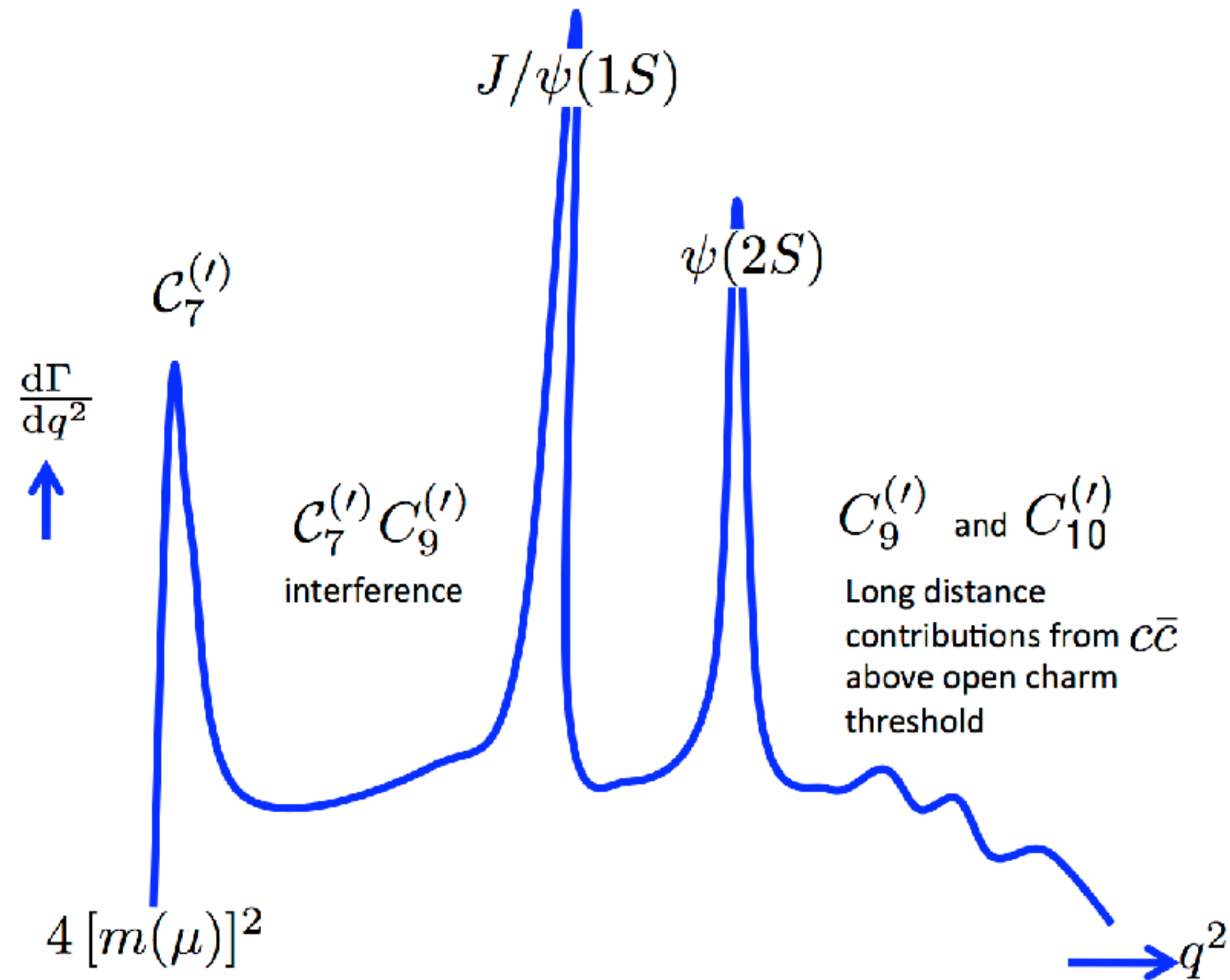
Excellent agreement between LHCb and Belle.

Belle evidence for $Z(4430)^\pm \rightarrow J/\psi\pi^\pm$ and observation of a new resonant state $Z(4200)^\pm \rightarrow J/\psi\pi^\pm$ [PRD 90 (2014) 112009]

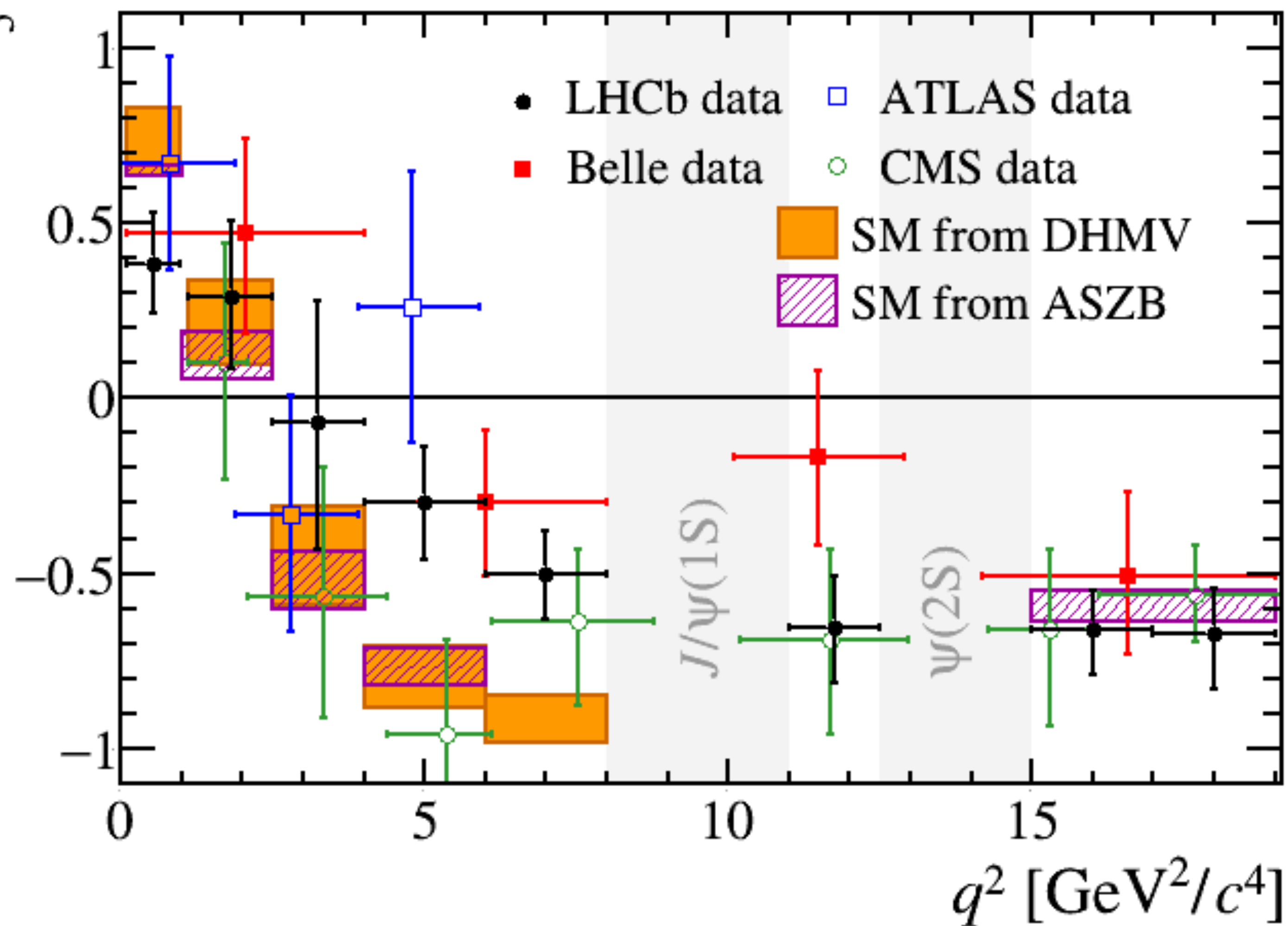
$$\frac{\mathcal{B}(Z(4430)^+ \rightarrow \psi(2S)\pi^+)}{\mathcal{B}(Z(4430)^+ \rightarrow J/\psi\pi^+)} \approx 10$$

Link to new physics searches with $B \rightarrow K^* \mu^+ \mu^-$

$$H_{eff} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i \left[\underbrace{C_i(\mu) O_i(\mu)}_{\text{left-handed part}} + \underbrace{C'_i(\mu) O'_i(\mu)}_{\text{right-handed part}} \right]$$



Link to new physics searches with $B \rightarrow K^* \mu^+ \mu^-$



Theory uncertainty from hadronic contributions in the $c\bar{c}$ regions

Theoretical attempts to cross the charmonium region use inputs from $B \rightarrow K^*(\rightarrow K\pi)\psi$ decays, but currently ignore exotic $\psi\pi$ resonance contributions

[Bobeth et al., arXiv:1707.07305]

[Blake et al., arXiv:1709.03921]

This will be important to control in the future!

$X(4140) \rightarrow J/\psi\phi$: some history

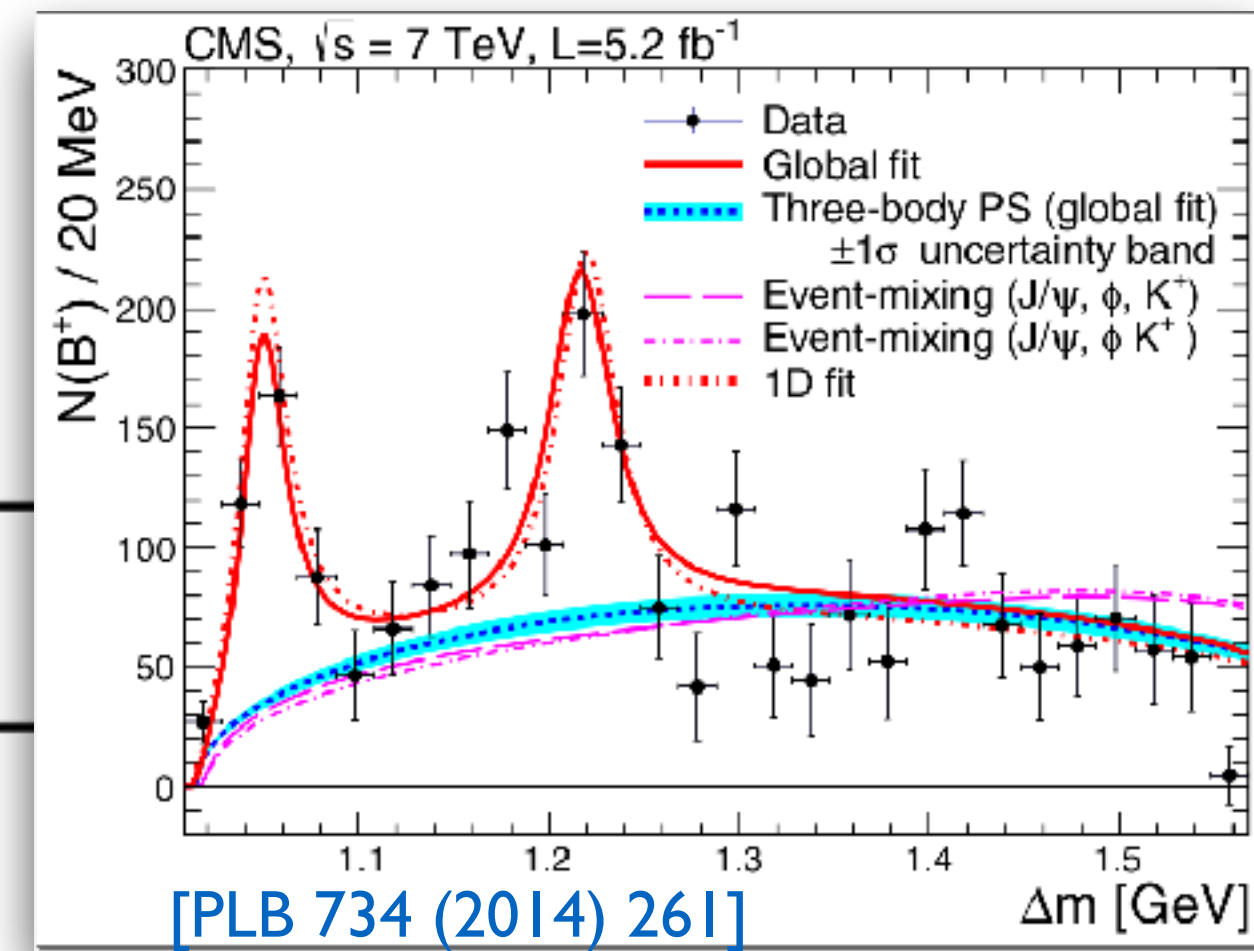
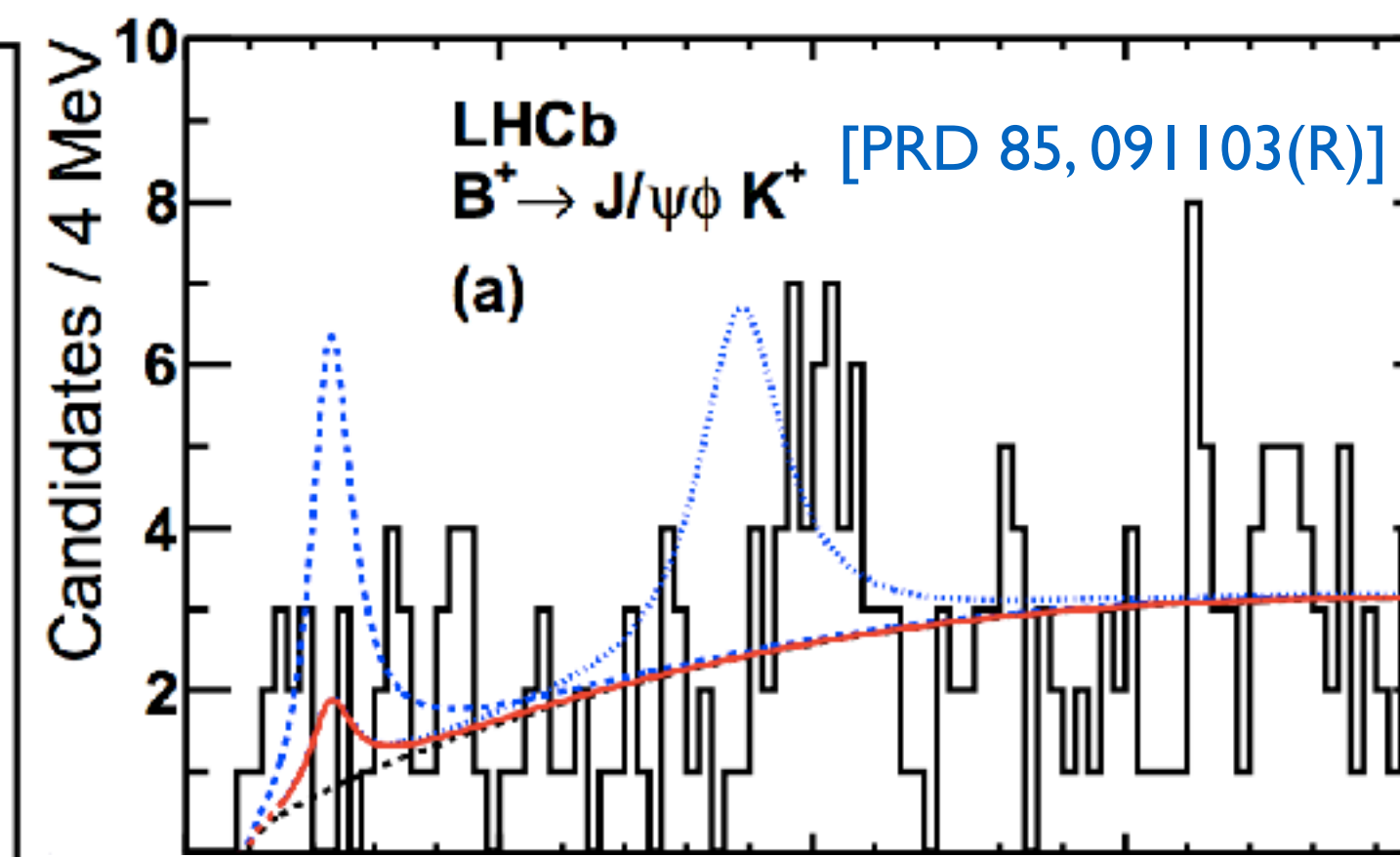
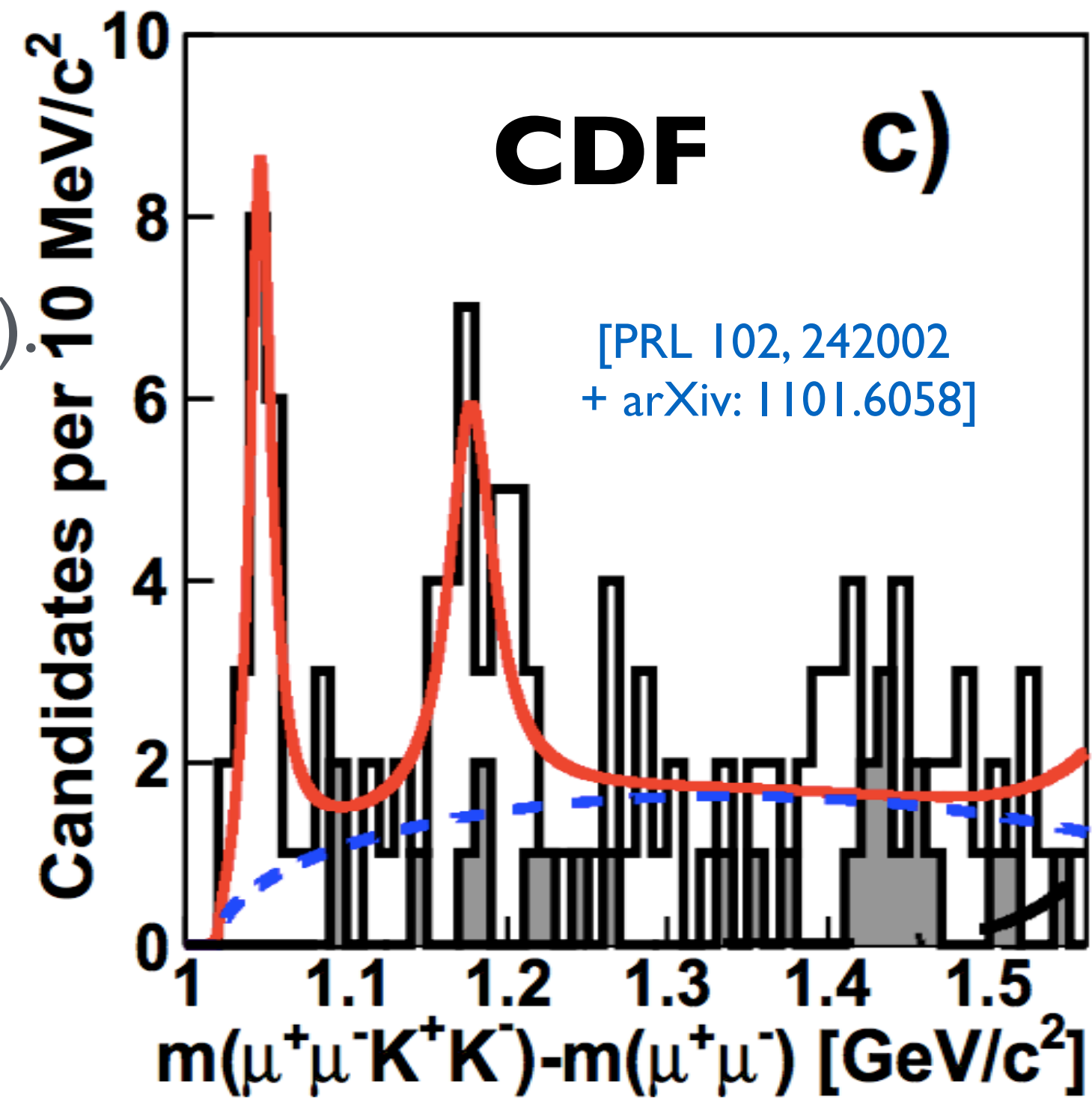
Seen by CDF, D0 and CMS

Not seen by LHCb, BaBar, BES-III, Belle ($\gamma\gamma$ fusion).

Well above open-charm threshold but has **narrow width** \rightarrow not conventional $c\bar{c}$.

Also second state at higher mass...

Full amplitude analysis of decay is essential!



Experiment	Y(4140)	Y(4274)
CDF [69]	$M = 4143.0 \pm 2.9 \pm 1.2, \Gamma = 11.7^{+8.3}_{-5.0} \pm 3.7$	—
CDF [100]	$M = 4143.4^{+2.9}_{-3.0} \pm 0.6, \Gamma = 15.3^{+10.4}_{-6.1} \pm 2.5$	$M = 4274.4^{+8.4}_{-6.7} \pm 1.9, \Gamma = 32.3^{+21.9}_{-15.3} \pm 7.6$
DØ [102]	$M = 4159.0 \pm 4.3 \pm 6.6, \Gamma = 19.9 \pm 12.6^{+1.0}_{-8.0}$	—
CMS [74]	$M = 4148.0 \pm 2.4 \pm 6.3, \Gamma = 28^{+15}_{-11} \pm 19$	$M = 4313.8 \pm 5.3 \pm 7.3, \Gamma = 38^{+30}_{-15} \pm 16$

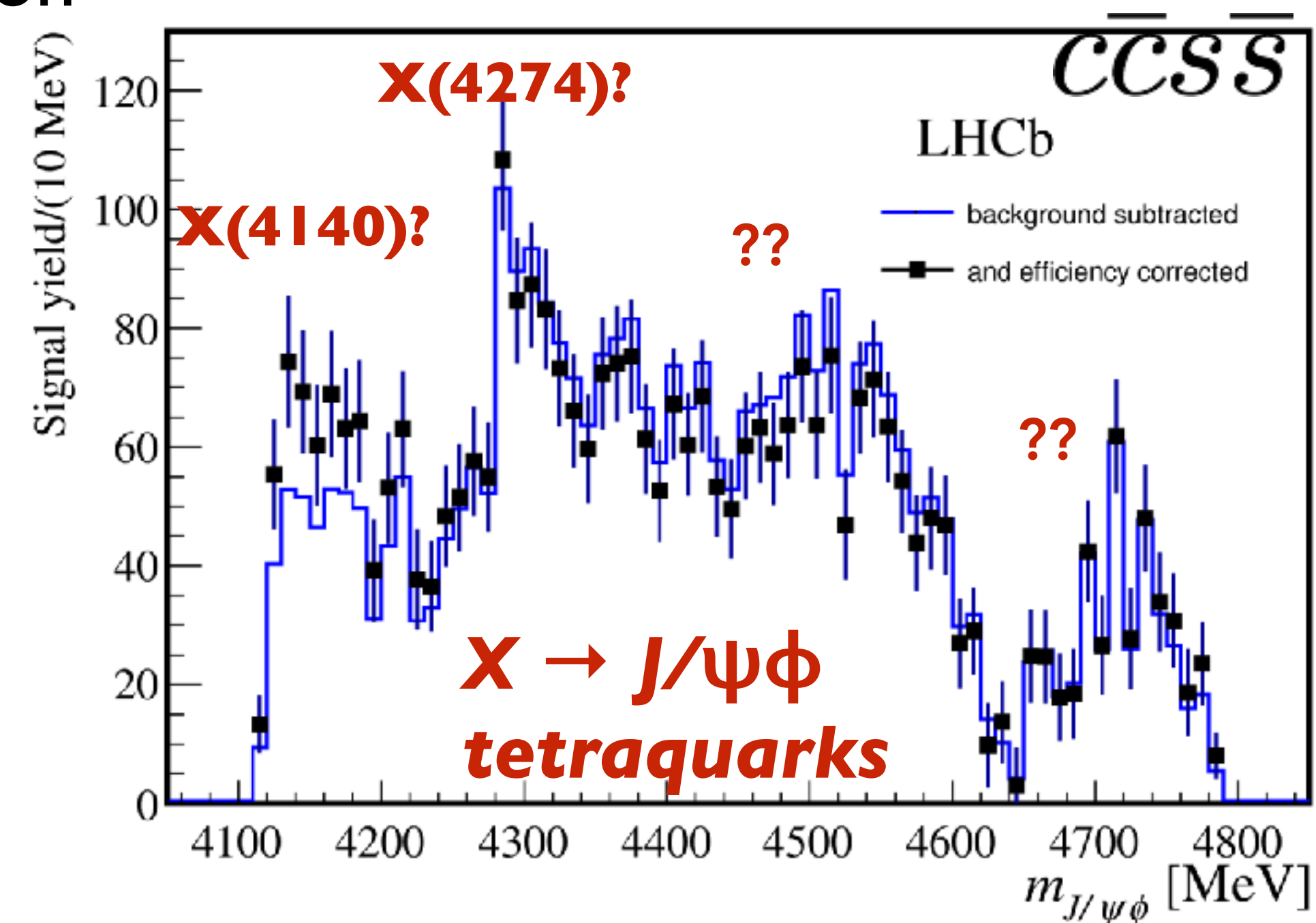
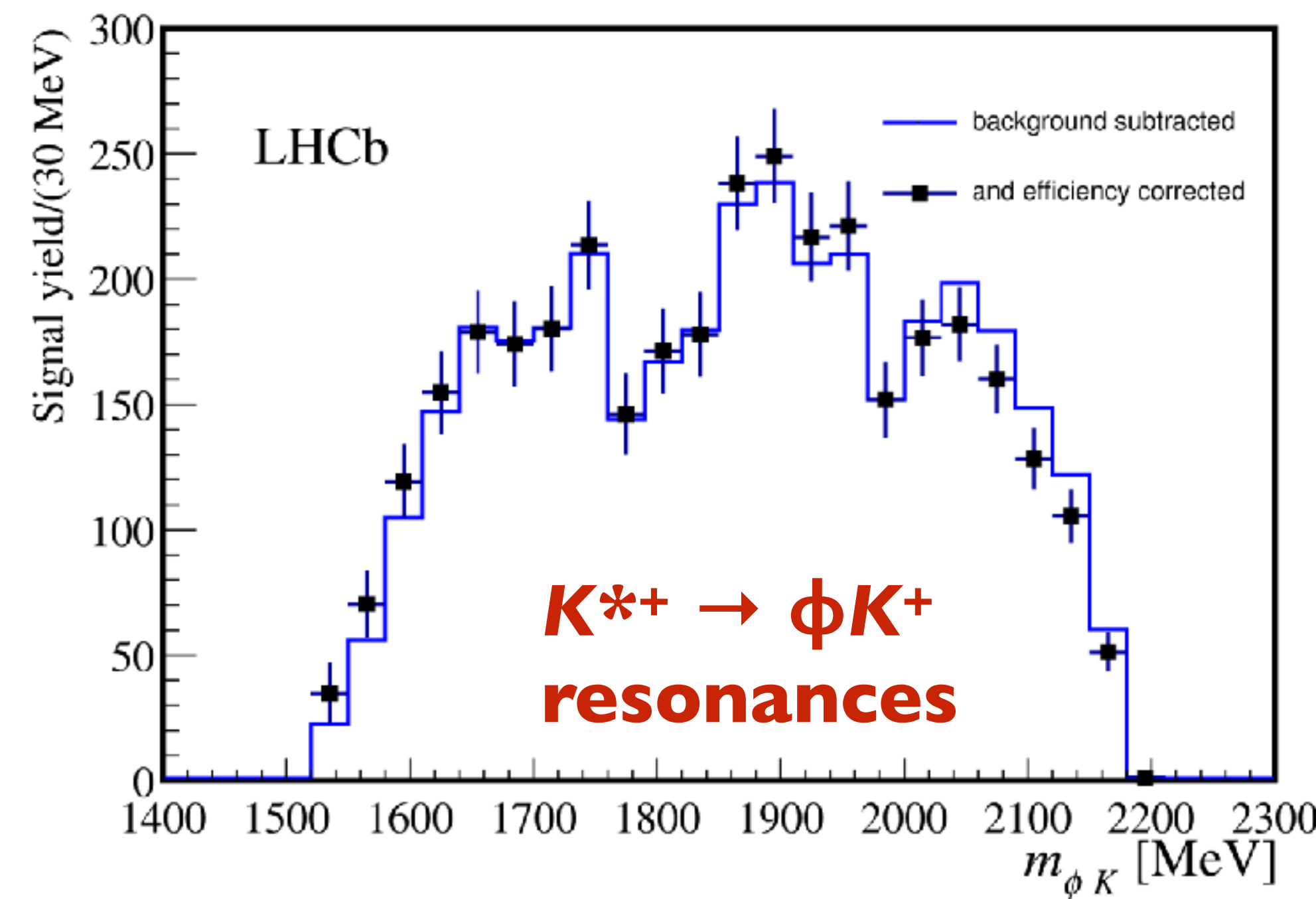
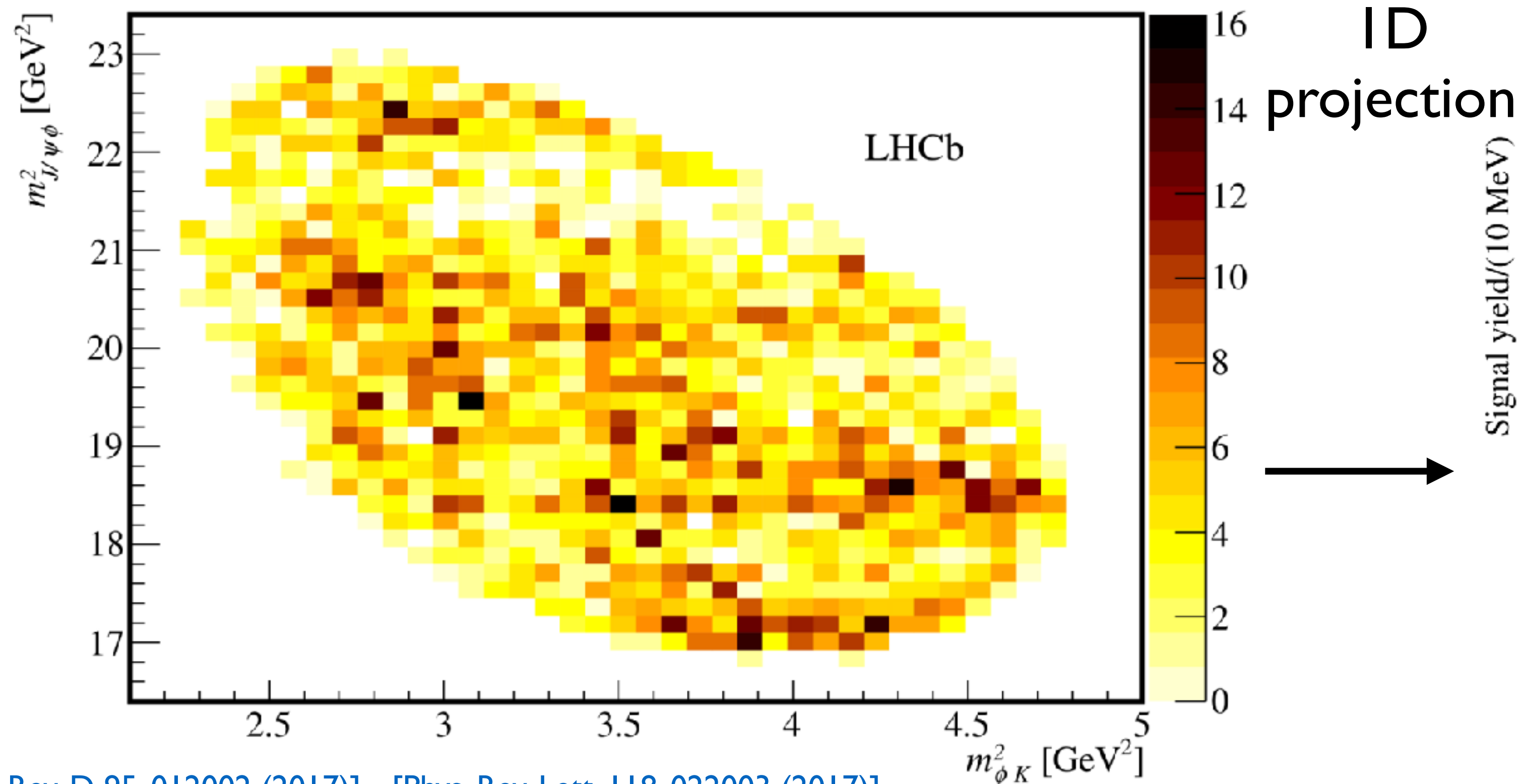
[D0 PRD 89, 012004]
 [Belle PRL 104, 112004]
 [BES-III PRD 91 (2015) 032002]

$B^+ \rightarrow J/\psi \phi K^+$ data sample

Are reflections from K^* system causing structure in $J/\psi \phi$?

Not sufficient to just fit ID mass distributions with ad-hoc assumptions about K^* contributions

K^{*+} resonances expected to be broad (scattering expts)



$B^+ \rightarrow J/\psi \phi K^+$ data sample

Are reflections from K^* system causing structure in $J/\psi \phi$?

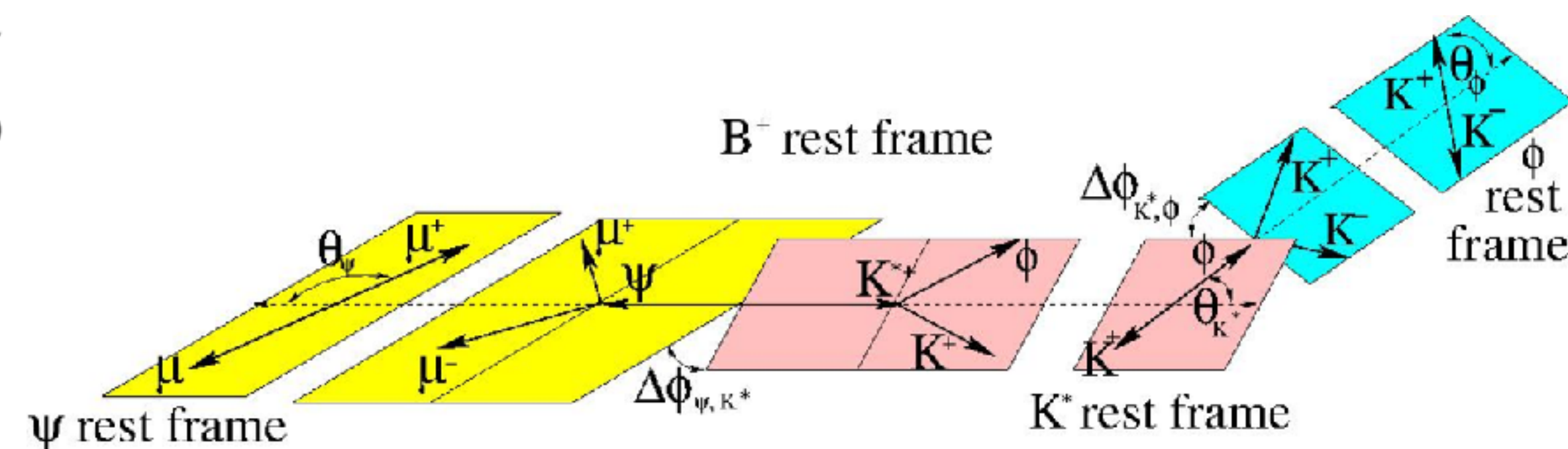
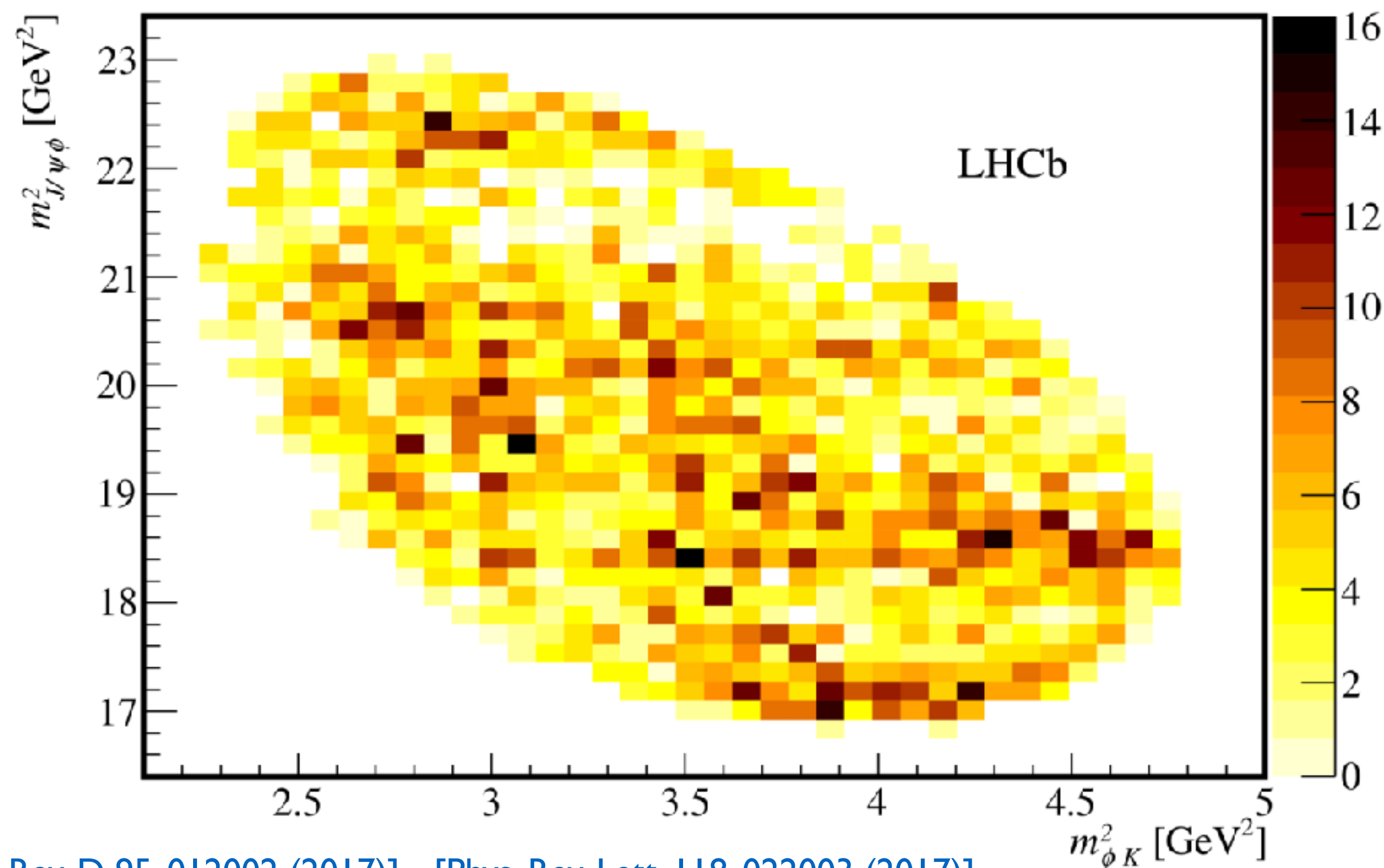
Not sufficient to just fit 1D mass distributions with ad-hoc assumptions about K^* contributions

K^{*+} resonances expected to be broad (scattering expts)

6D amplitude analysis to understand structure in final state

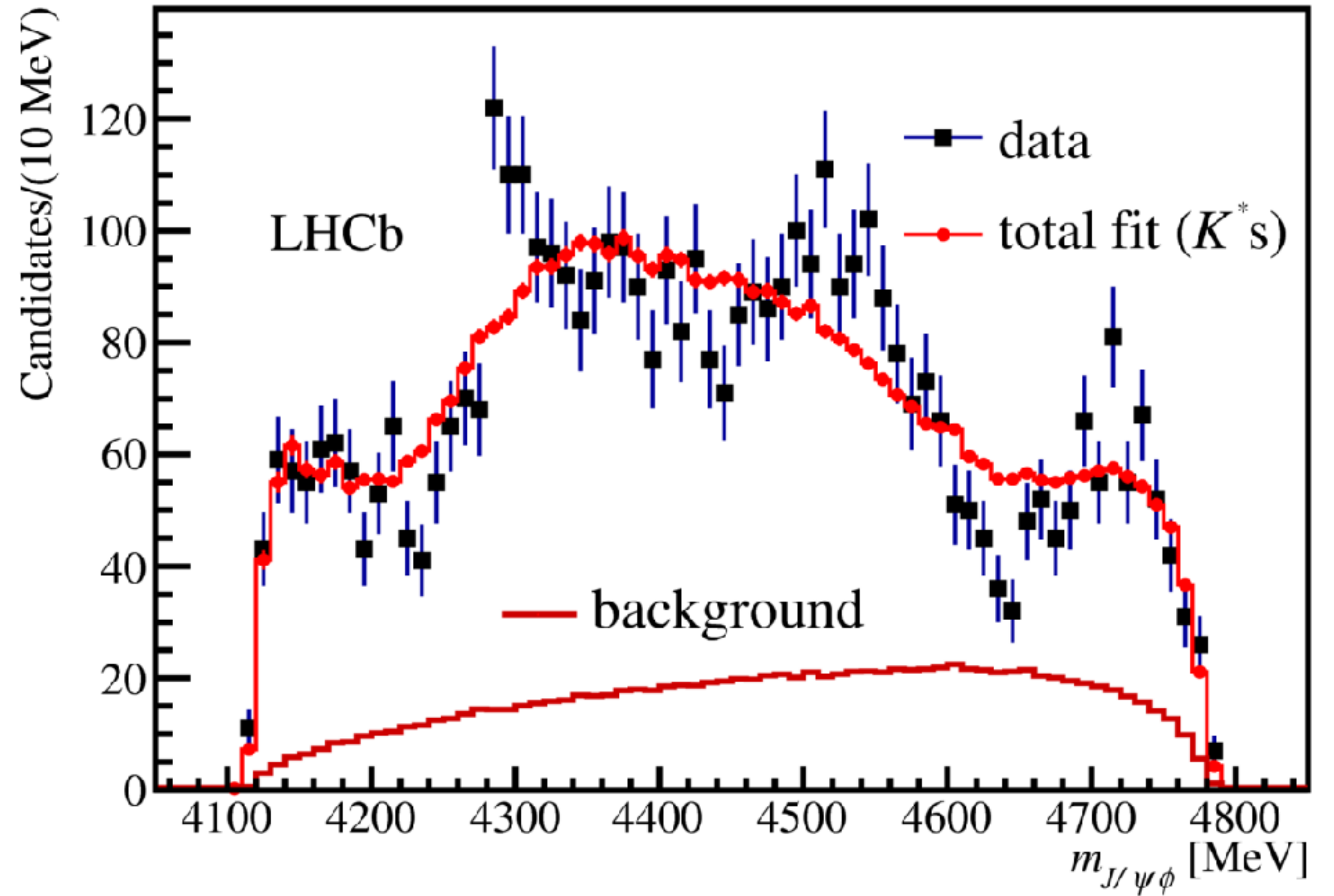
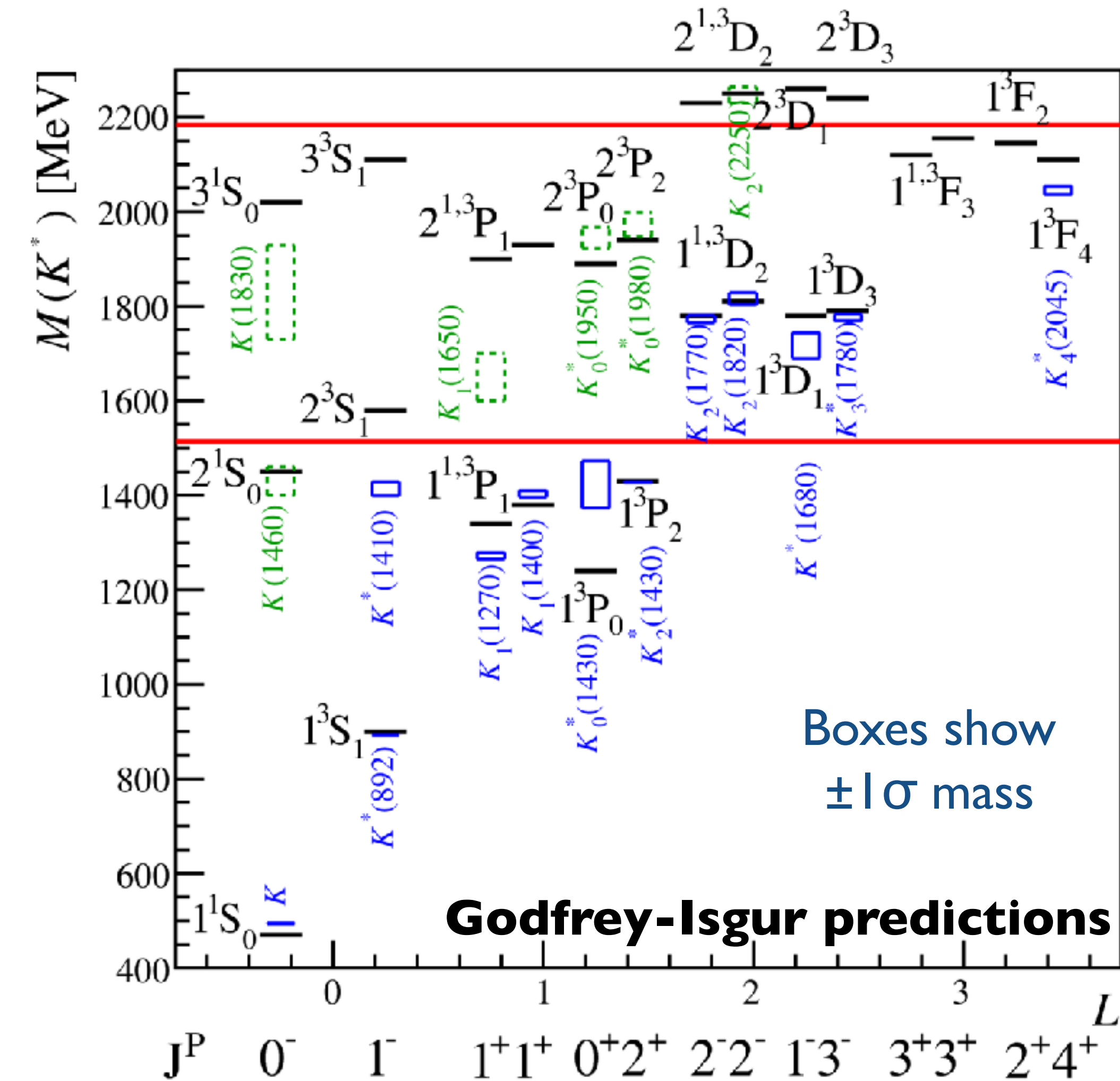
Three interfering decay chains:

1. $B^+ \rightarrow K^{*+} J/\psi, K^{*+} \rightarrow \phi K^+$
2. $B^+ \rightarrow X K^+, X \rightarrow J/\psi \phi$
3. $B^+ \rightarrow Z^+ \phi, Z^+ \rightarrow J/\psi K^+$



$$\Omega \equiv (\theta_{K^*}, \theta_\psi, \Delta\phi_{\psi, K^*}, \theta_\phi, \Delta\phi_{K^*, \phi})$$

Which K^* resonances to include?

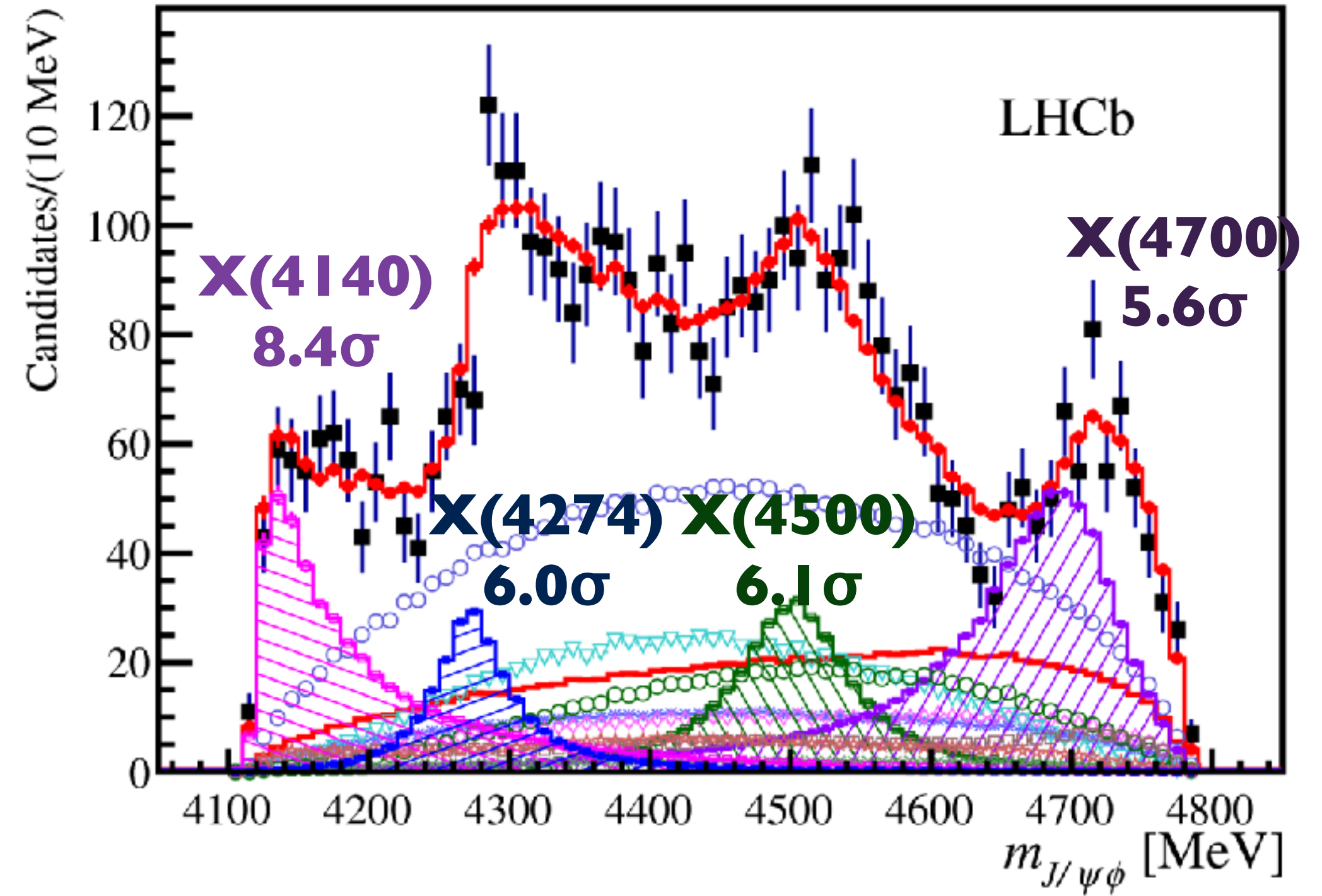
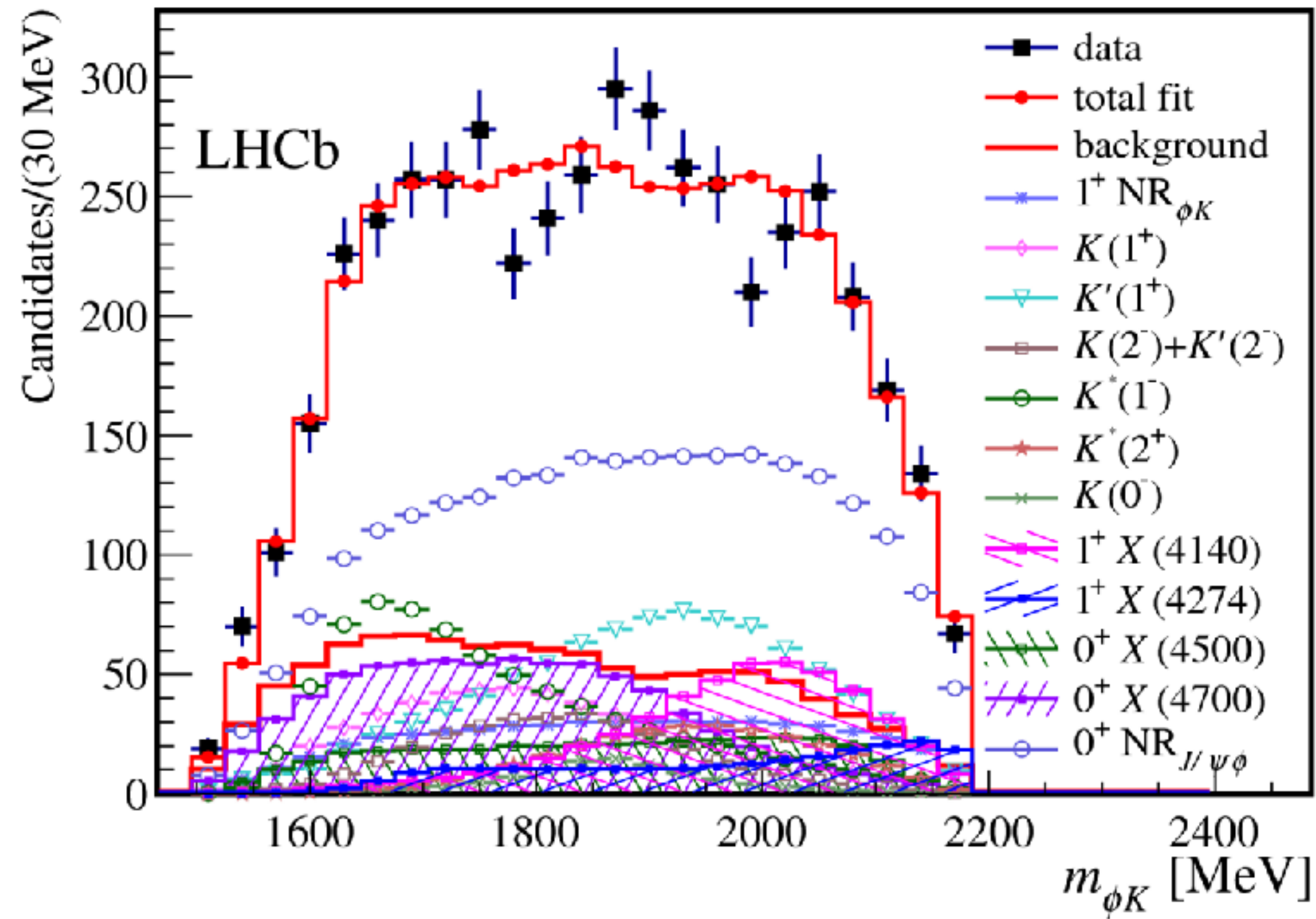


Experimental measurements of **well-established** and **unconfirmed** K^* resonances

Higher spin states expected to be suppressed in B decays due to orbital angular momentum required to produce them

104 free parameters in fit
 p-value H_0 (only K^* resonances) $< 10^{-4}$

Fit results including $X \rightarrow J/\psi\phi$ states



7 K^* states, 4 exotic X states and NR $J/\psi\phi$ and ϕK^* components.

Inclusion of exotic Z states does not improve fit.

Contri- bution	sign. or Ref.	Fit results		
		M_0 [MeV]	Γ_0 [MeV]	FF %
All $X(1^+)$				16 ± 3 $^{+6}_{-2}$
$X(4140)$	8.4σ	4146.5 ± 4.5 $^{+4.6}_{-2.8}$	83 ± 21 $^{+21}_{-14}$	13 ± 3.2 $^{+4.8}_{-2.0}$
ave.	Table 1	4143.4 ± 1.9	15.7 ± 6.3	
$X(4274)$	6.0σ	4273.3 ± 8.3 $^{+17.2}_{-3.6}$	56 ± 11 $^{+8}_{-11}$	7.1 ± 2.5 $^{+3.5}_{-2.4}$
CDF	[28]	4274.4 $^{+8.4}_{-6.7} \pm 1.9$	32 $^{+22}_{-15} \pm 8$	
CMS	[25]	$4313.8 \pm 5.3 \pm 7.3$	38 $^{+30}_{-15} \pm 16$	
All $X(0^+)$				$28 \pm 5 \pm 7$
NR $_{J/\psi\phi}$	6.4σ			46 ± 11 $^{+11}_{-21}$
$X(4500)$	6.1σ	4506 ± 11 $^{+12}_{-15}$	92 ± 21 $^{+21}_{-20}$	6.6 ± 2.4 $^{+3.5}_{-2.3}$
$X(4700)$	5.6σ	4704 ± 10 $^{+14}_{-24}$	120 ± 31 $^{+42}_{-33}$	12 ± 5 $^{+9}_{-5}$

98 free parameters in fit
p-value = 22%

**first
observation**

The $X(5568)^\pm \rightarrow B_s \pi^\pm$?

$\sim 5\sigma$ claim for exotic state

Large B_s production fraction: $\rho_X = (8.6 \pm 1.9 \pm 1.4)\%$

Not due to reflections from kaons/pions

$$M = 5567.8 \pm 2.9_{-1.9}^{+0.9} \text{MeV}/c^2$$

$$\Gamma = 21.9 \pm 6.4_{-2.5}^{+5.0} \text{MeV}/c^2$$

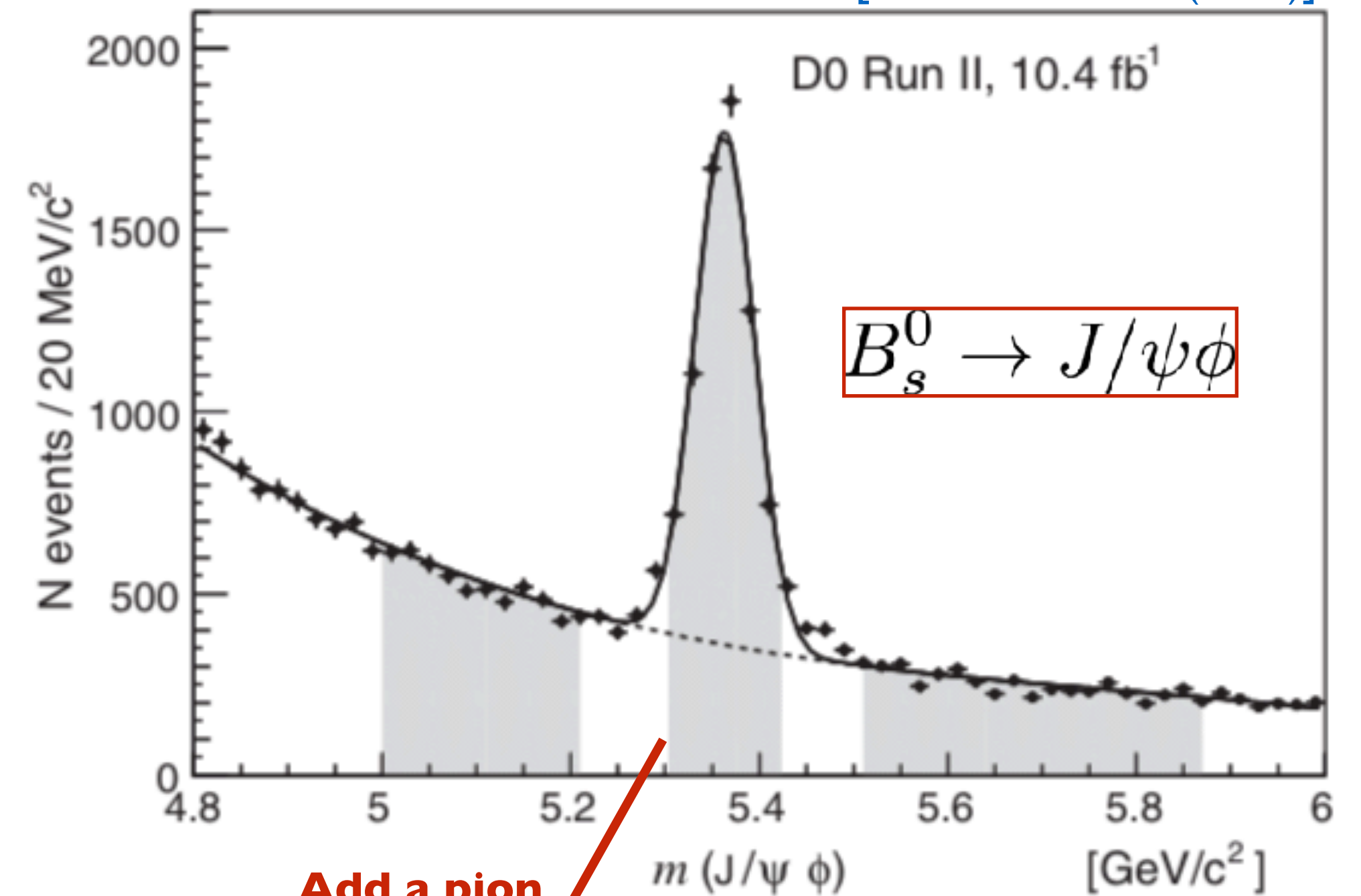
Possible $bsud$ tetraquark/molecule but difficult to explain when considering QCD chiral symmetry, heavy quark symmetry and threshold effects.

[Burns, Swanson, arXiv:1603.04366]

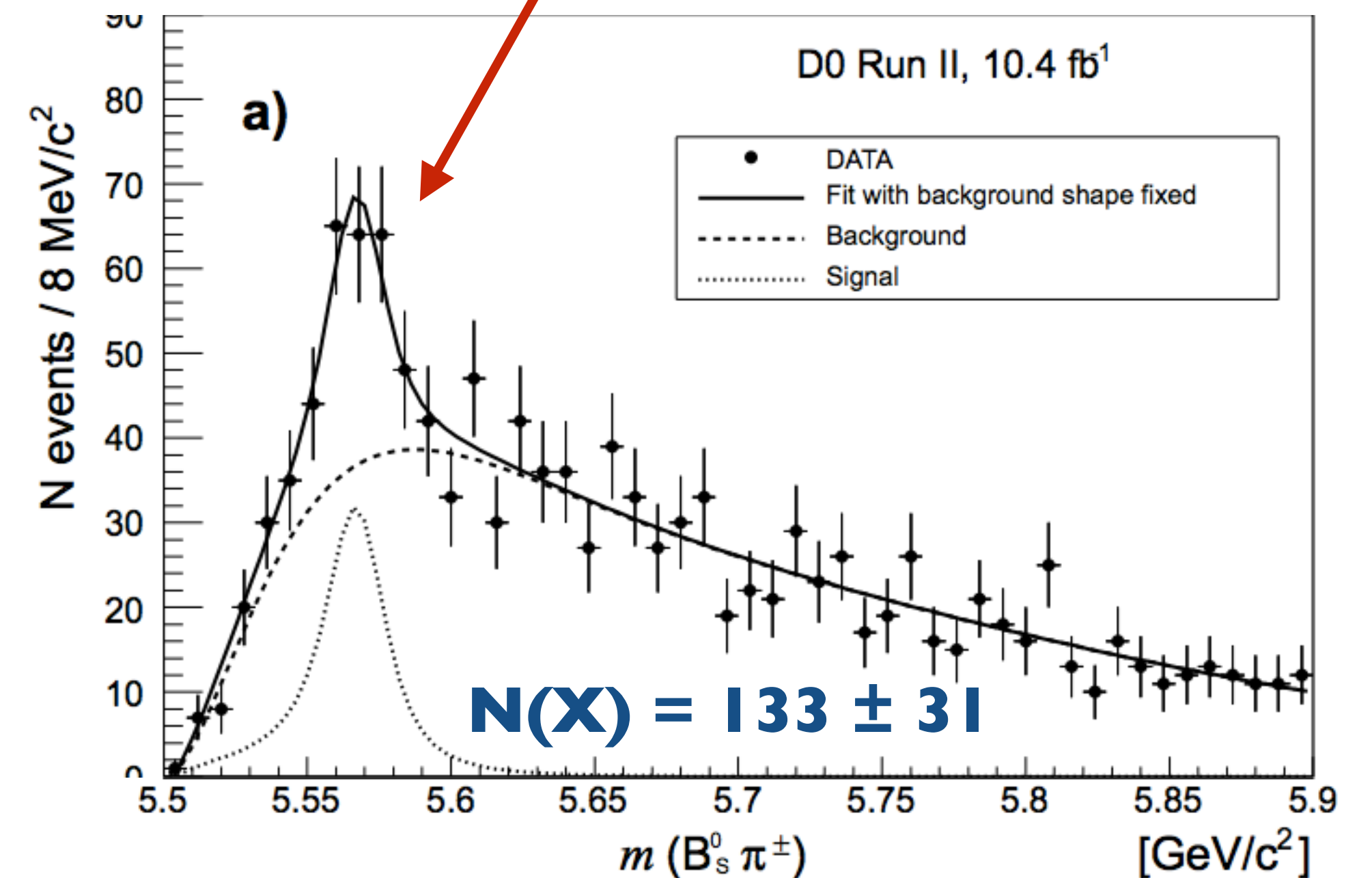
[Guo et al, arXiv:1603.06316]

[Liu, Li, arXiv:1603.04366]

No sign on the lattice [Lang et al., PRD 94 074509 (2016)]



Add a pion



LHC searches for $X(5568)^\pm$

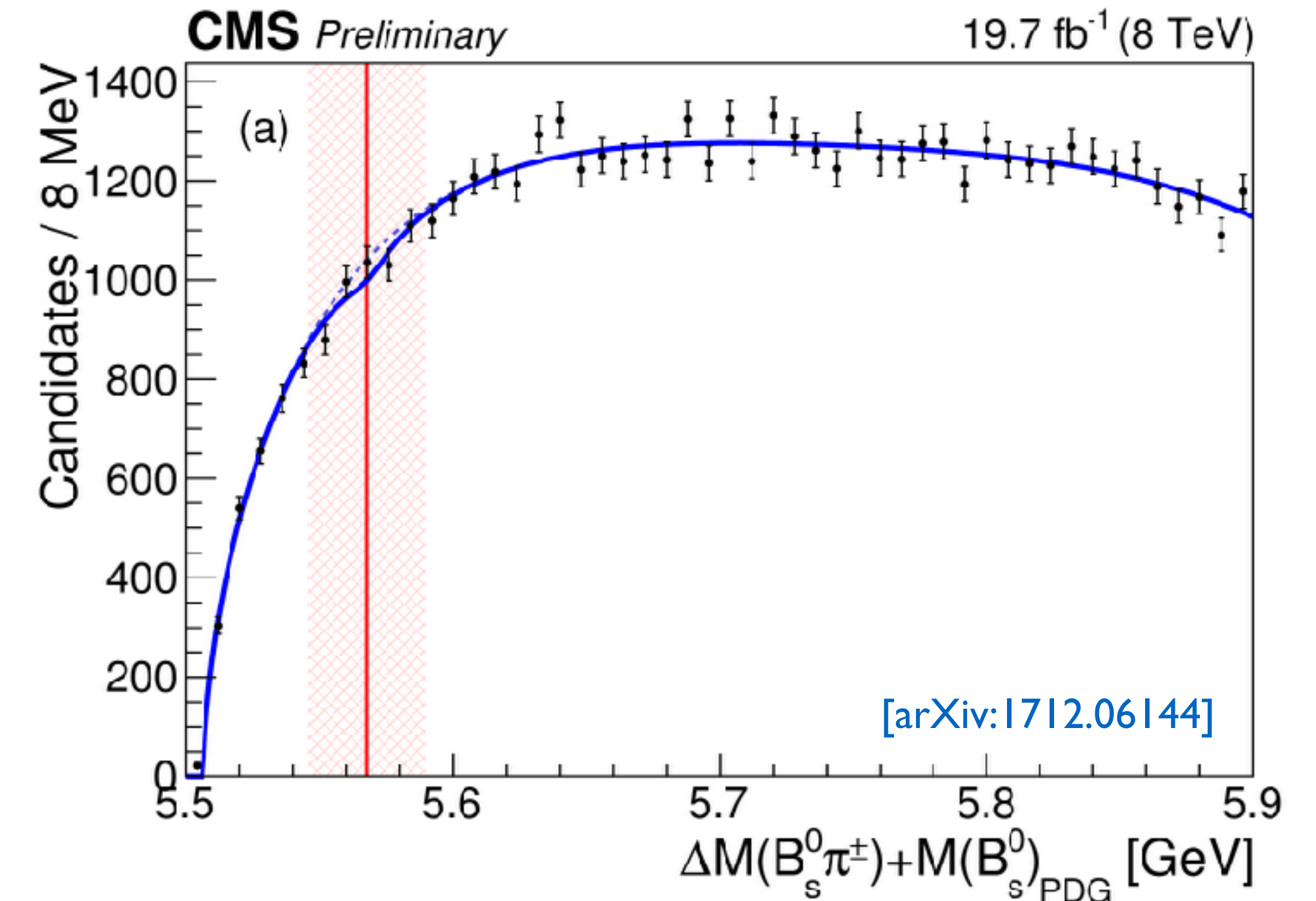
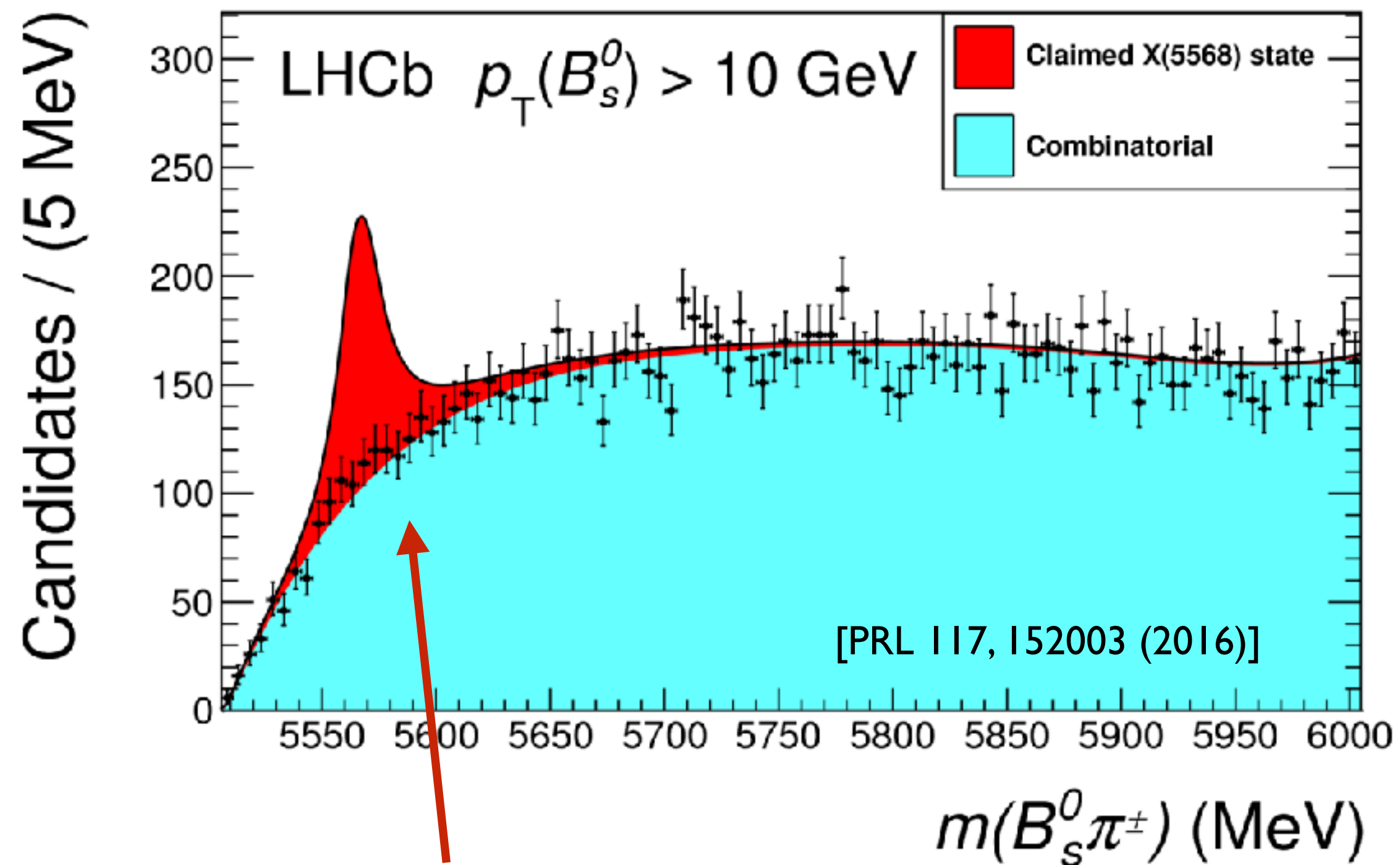
LHCb use $>100k$ B_s mesons and combine with π^\pm .
 Sample 20x larger than D0 and much less background.

B_s and π^\pm required to come from same PV.

Fit signal using S-wave Breit-Wigner with mass and width of claimed D0 signal.

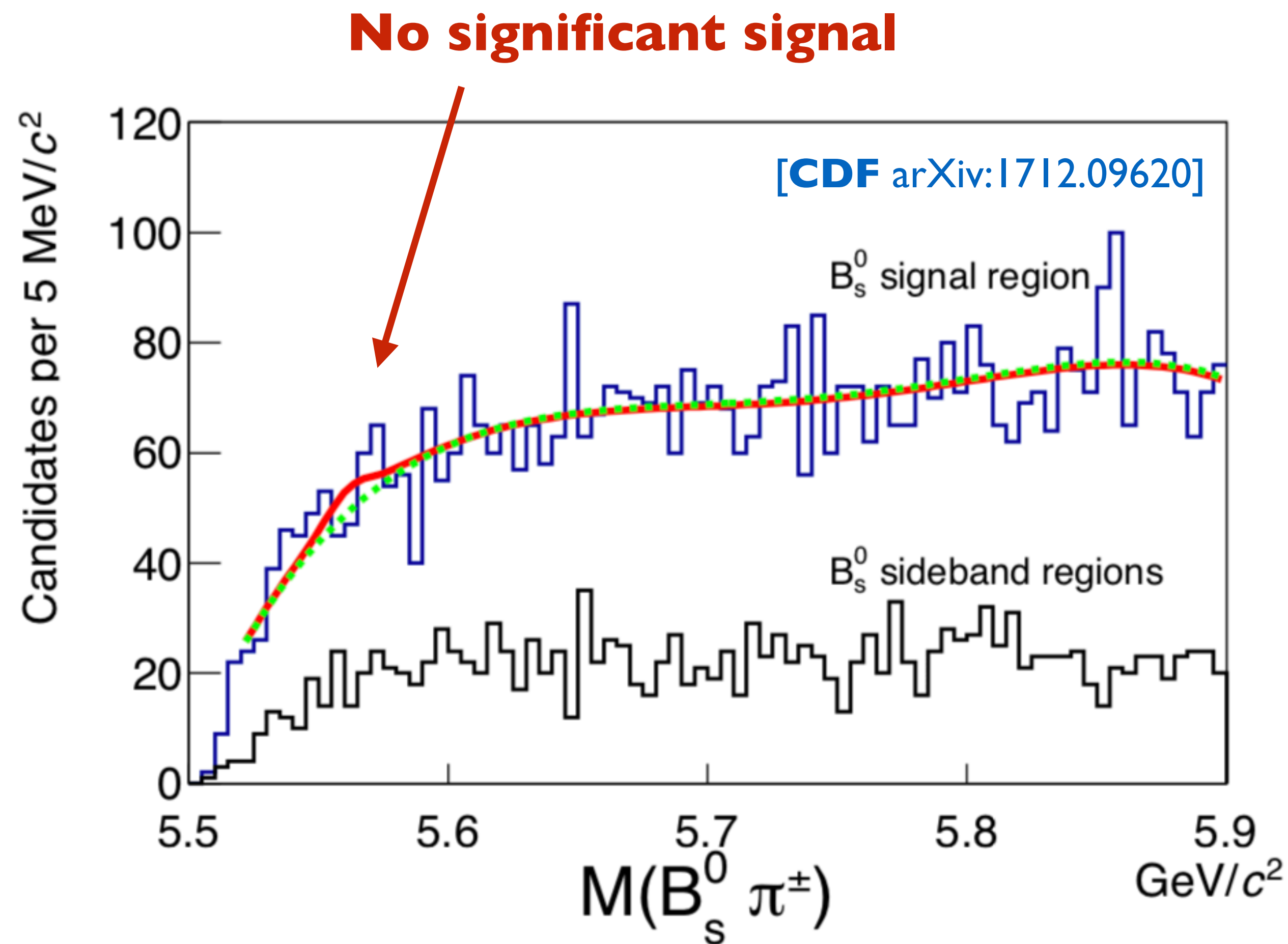
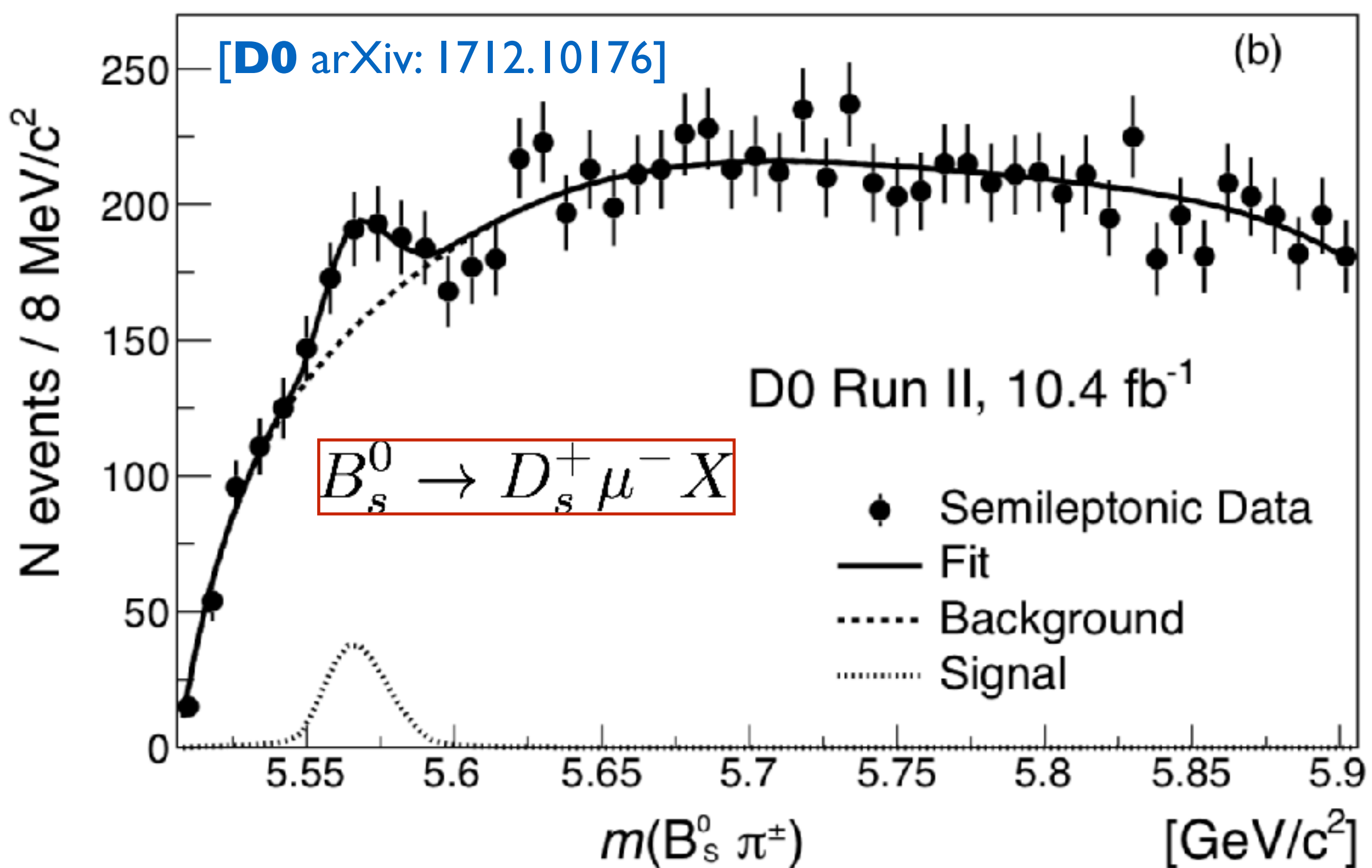
$$\rho_X^{\text{LHCb}}(B_s^0 p_T > 5 \text{ GeV}/c) < 0.009 (0.010) @ 90 (95) \% \text{ CL}$$

$$\rho_X^{\text{LHCb}}(B_s^0 p_T > 10 \text{ GeV}/c) < 0.016 (0.018) @ 90 (95) \% \text{ CL}$$



How signal would look according to D0 result

Hot off the press!

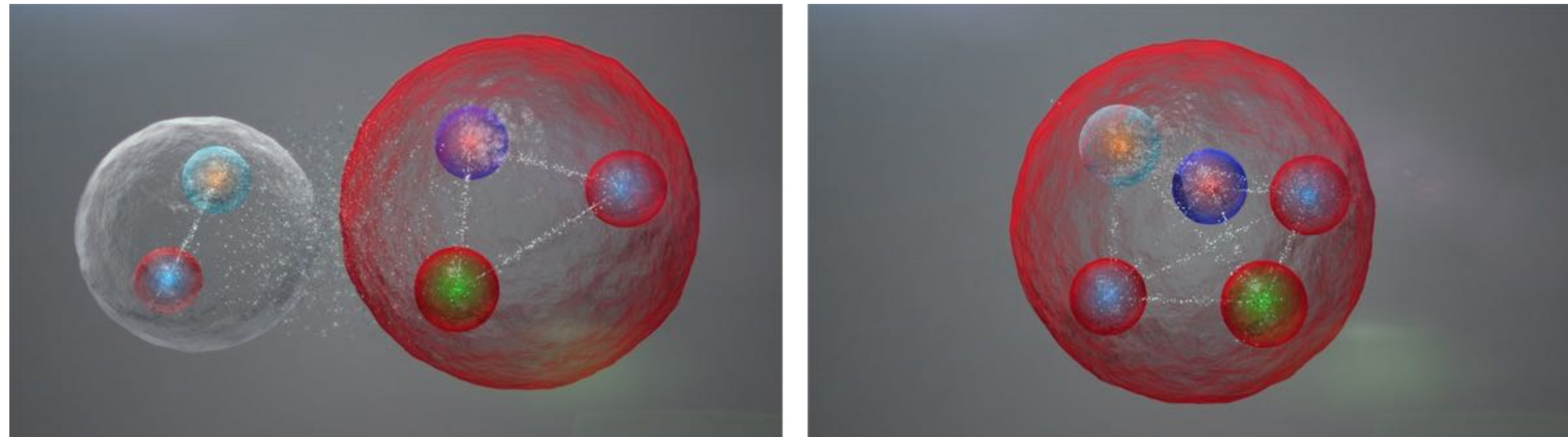


Over Christmas D0 published result showing the X(5568) signal using a different B_s decay mode while CDF show data consistent with background only.

Could D0 “signal” be due to some underestimated background? → **more work needed**

CDF result removes possibility that X(5568) is predominately produced at in $p\bar{p}$ collisions.

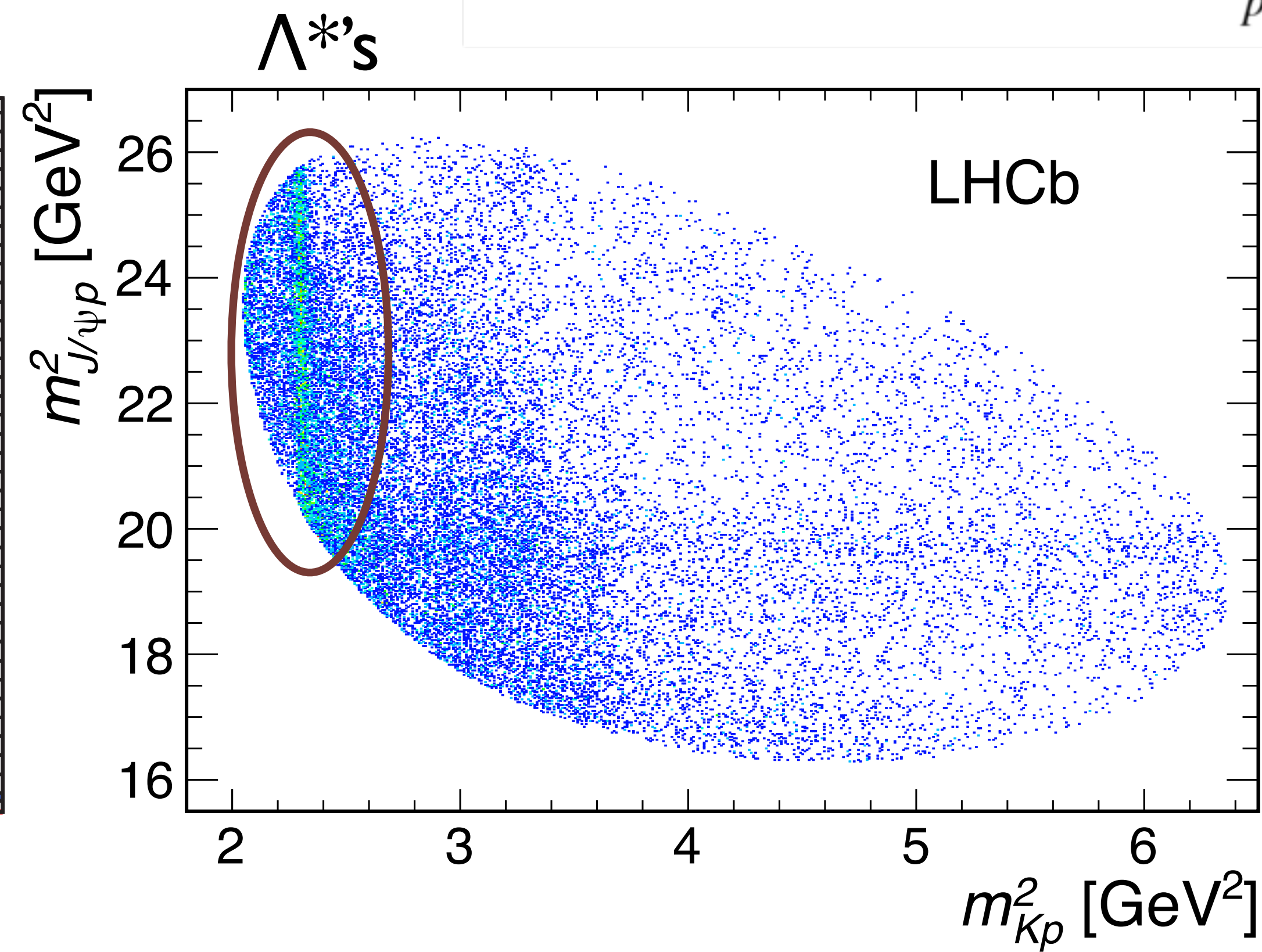
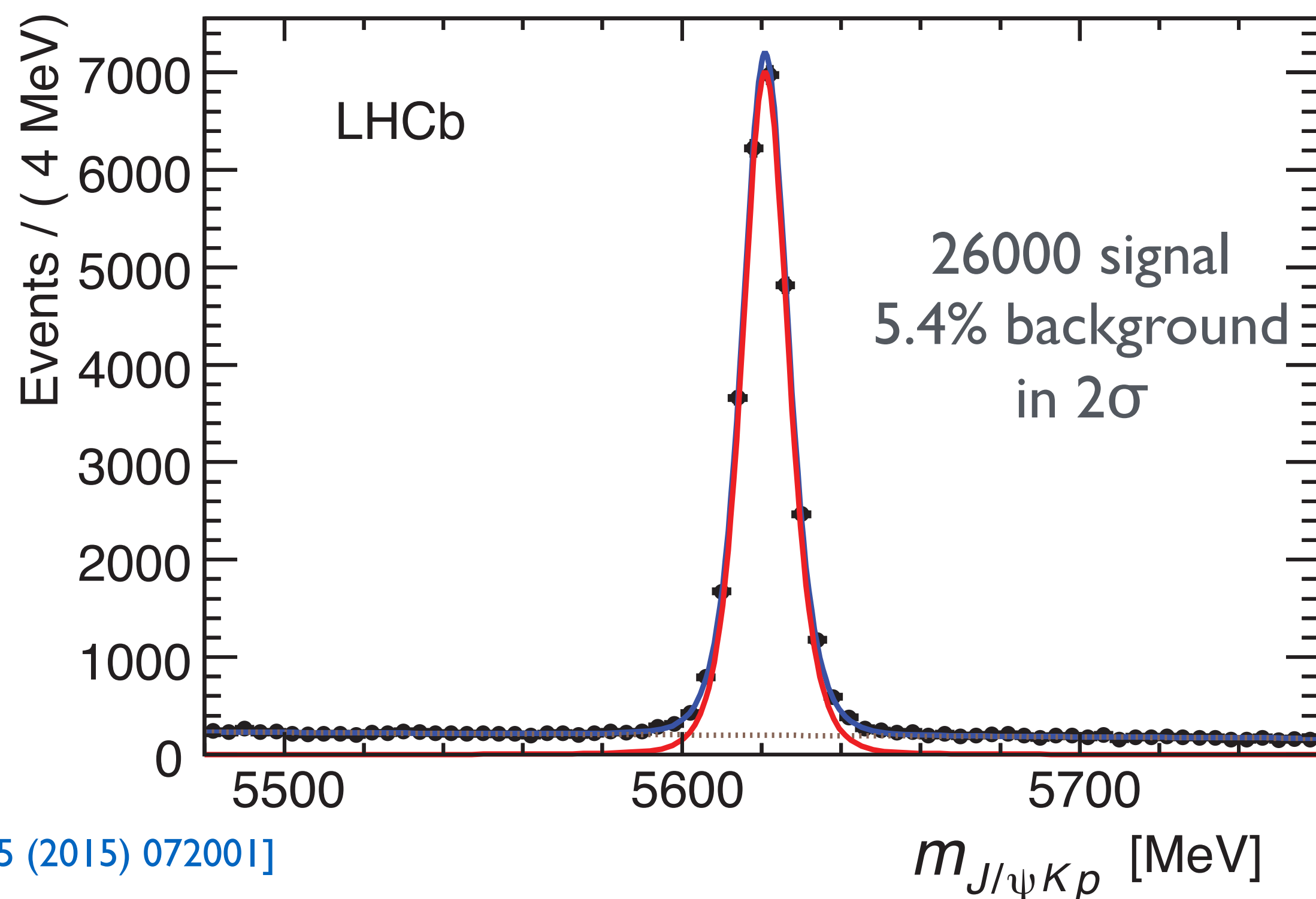
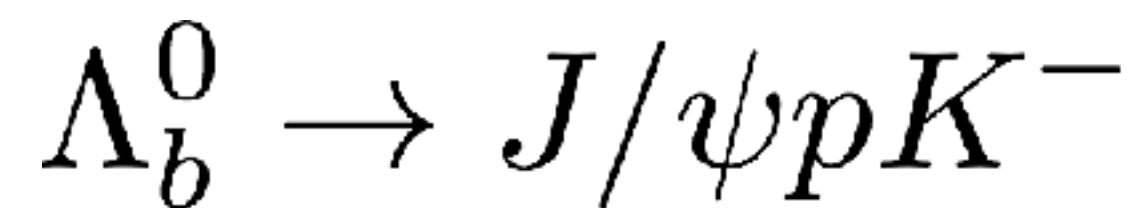
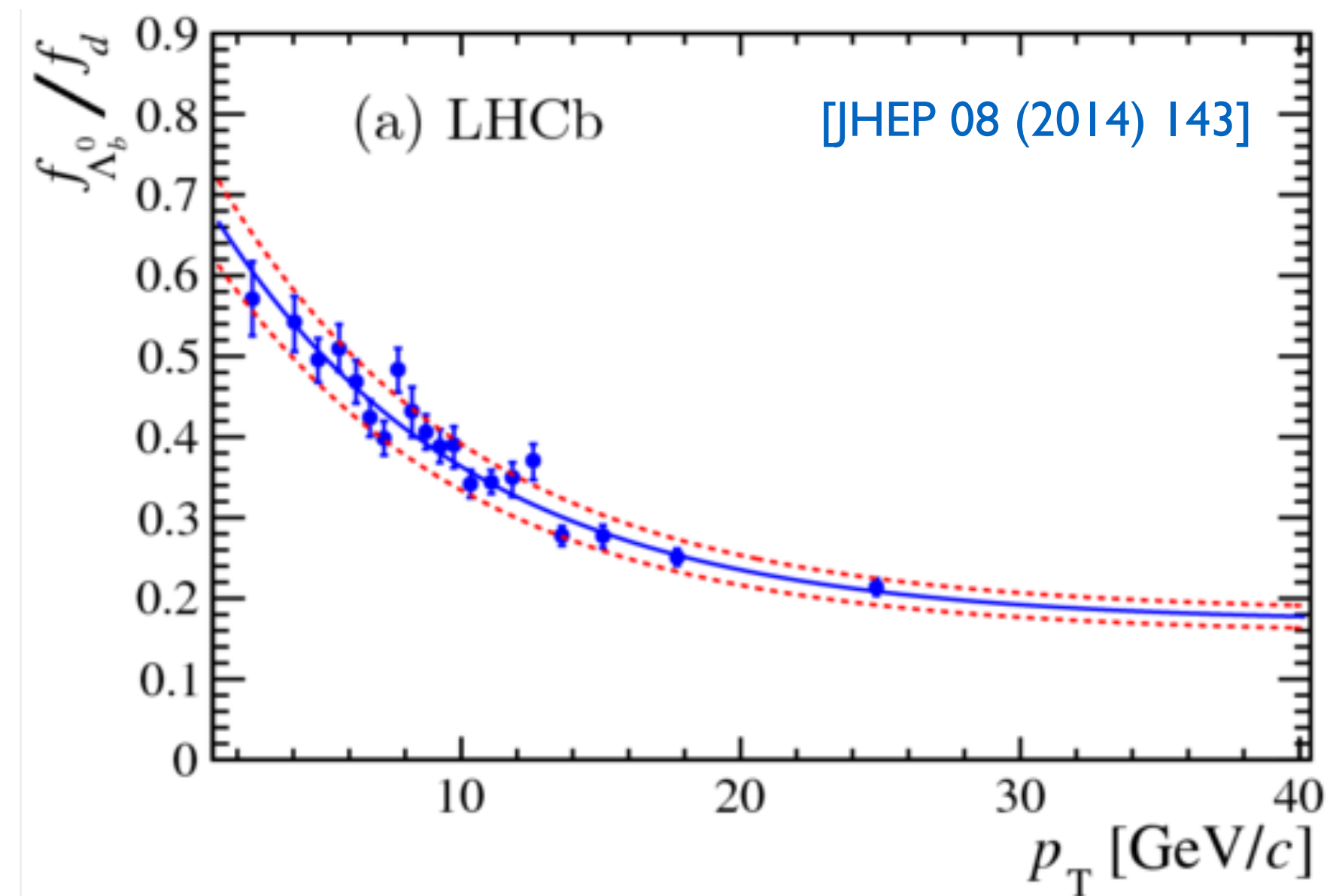
Exotic baryons



Pentaquark observation

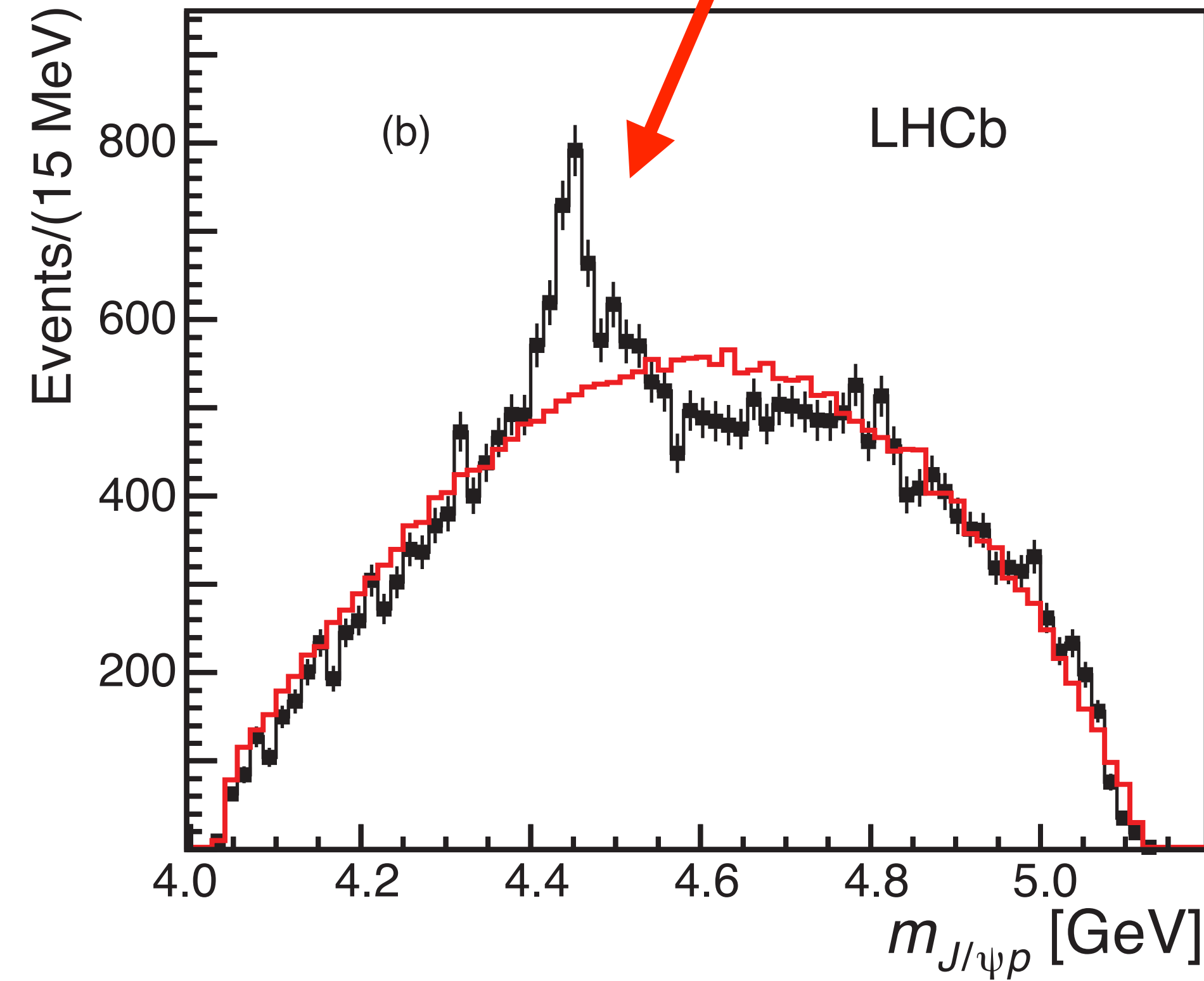
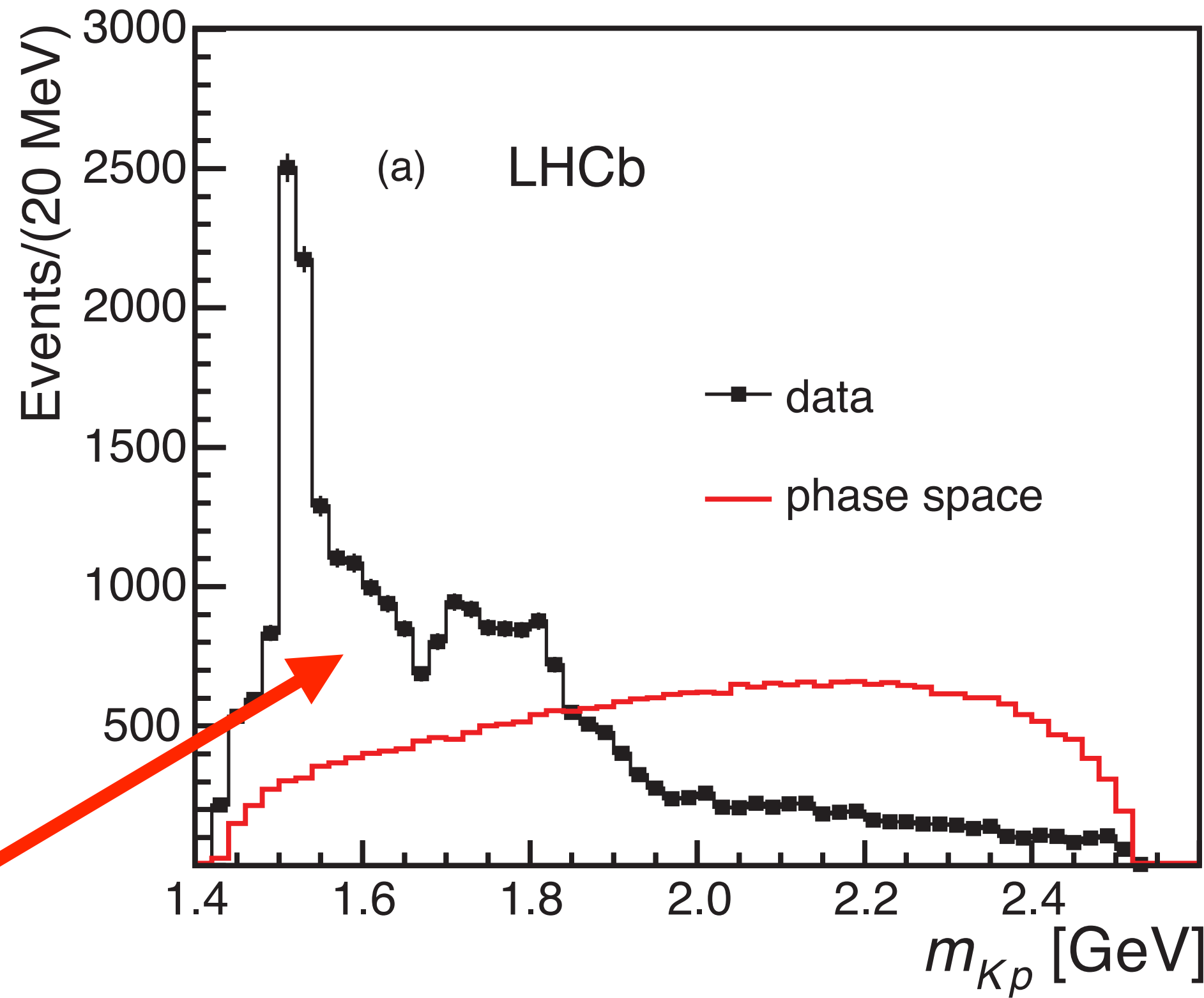
Large production of b-baryons at LHC.

Many more Λ_b in LHCb than central detectors.



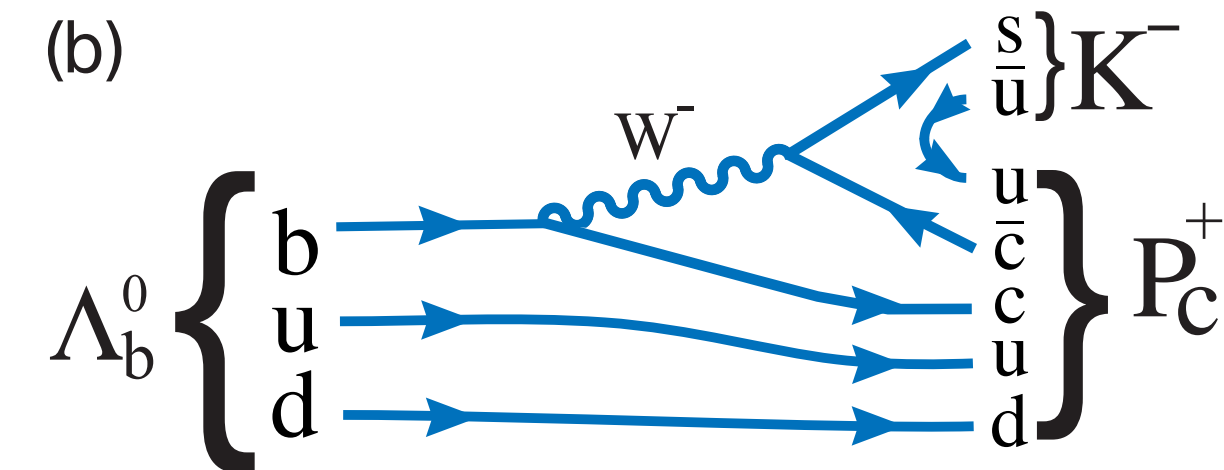
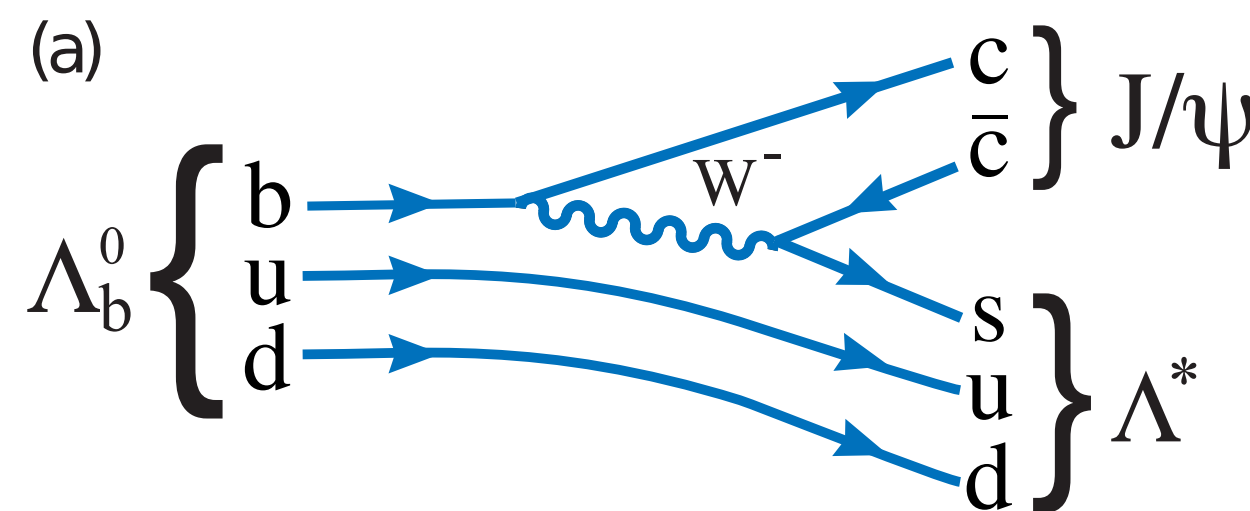
Pentaquark observation

State	J^P	M_0 (MeV)	Γ_0 (MeV)
$\Lambda(1405)$	$1/2^-$	$1405.1^{+1.3}_{-1.0}$	50.5 ± 2.0
$\Lambda(1520)$	$3/2^-$	1519.5 ± 1.0	15.6 ± 1.0
$\Lambda(1600)$	$1/2^+$	1600	150
$\Lambda(1670)$	$1/2^-$	1670	35
$\Lambda(1690)$	$3/2^-$	1690	60
$\Lambda(1800)$	$1/2^-$	1800	300
$\Lambda(1810)$	$1/2^+$	1810	150
$\Lambda(1820)$	$5/2^+$	1820	80
$\Lambda(1830)$	$5/2^-$	1830	95
$\Lambda(1890)$	$3/2^+$	1890	100
$\Lambda(2100)$	$7/2^-$	2100	200
$\Lambda(2110)$	$5/2^+$	2110	200
$\Lambda(2350)$	$9/2^+$	2350	150
$\Lambda(2585)$?	≈ 2585	200

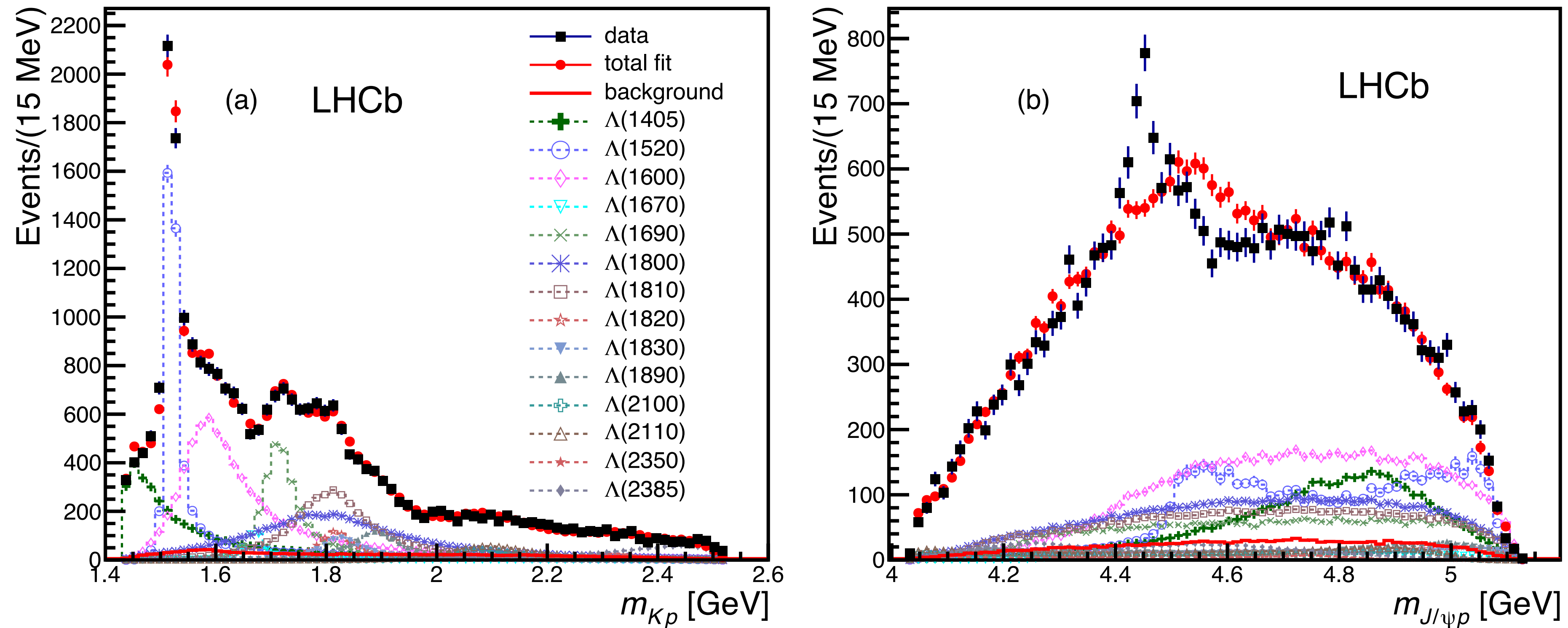


Can this be caused by reflections in $m(Kp)$, background or detector efficiency?

Interfering $\Lambda^* \rightarrow pK$ resonances



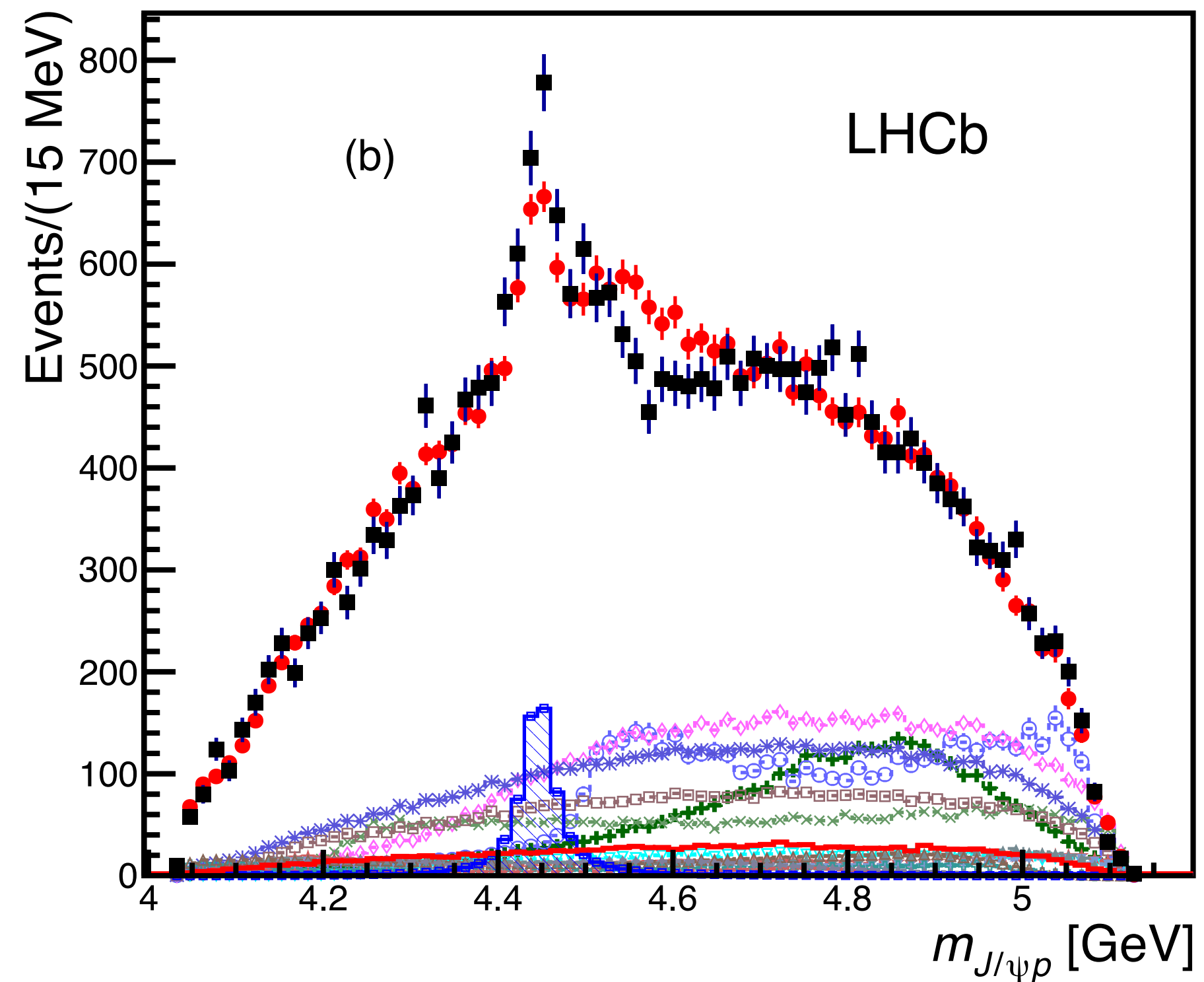
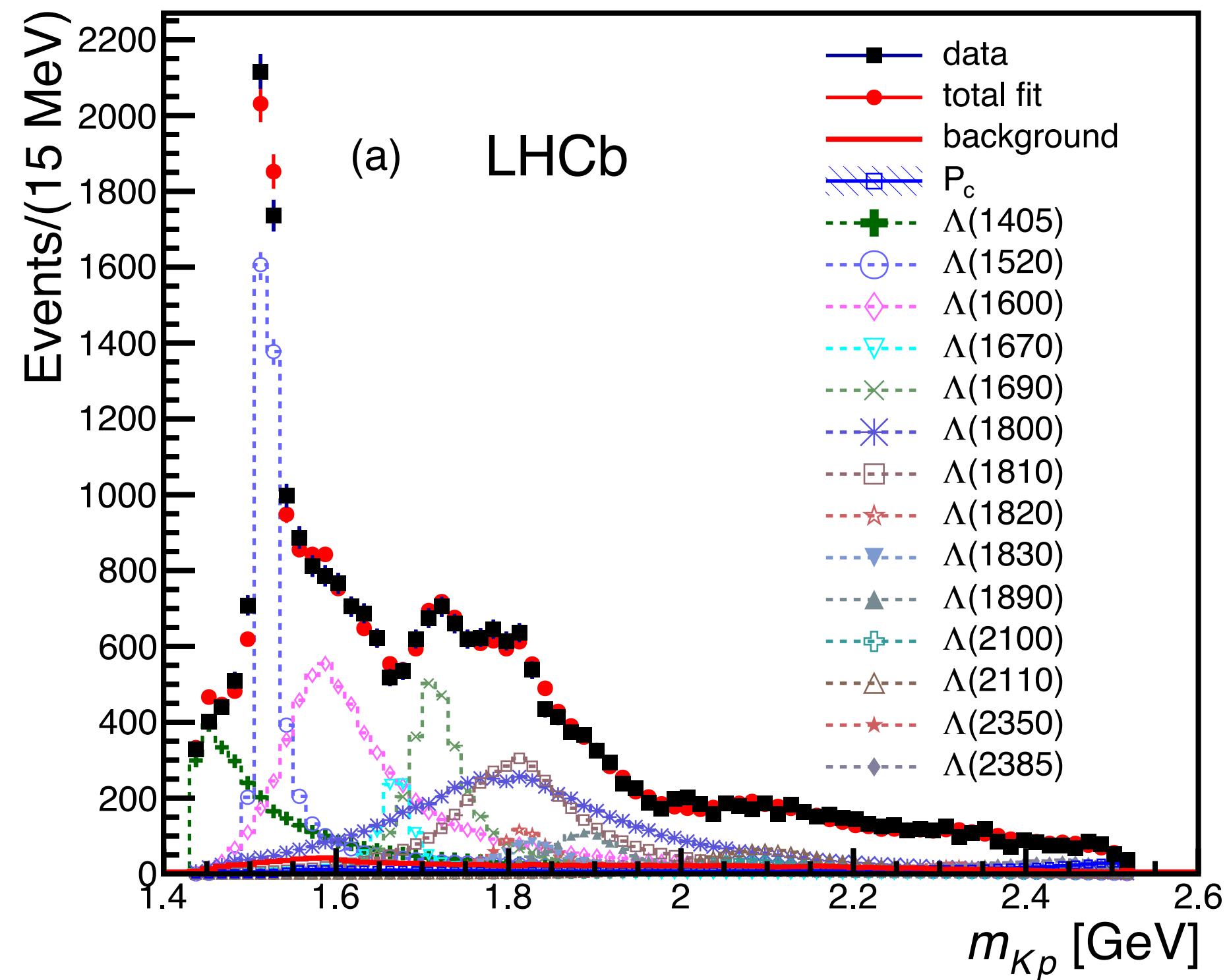
Results without P_c states



Using full set of Λ^* 's the $m(Kp)$ distribution looks good but not $m(J/\psi p)$.

Addition of non-resonant, extra Λ^* 's, all Σ^* (isospin violating process) does not help.

Extended model with one P_c

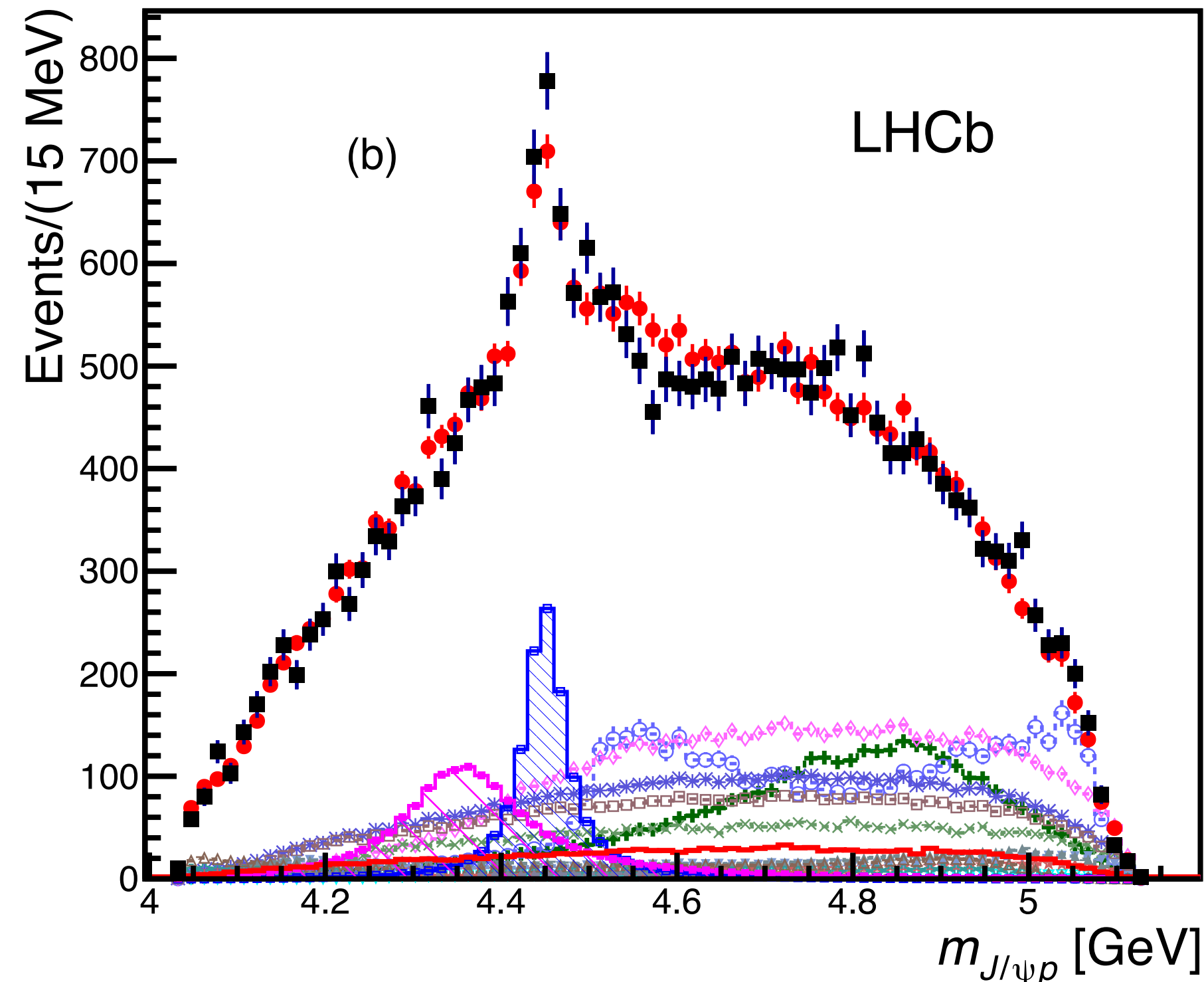
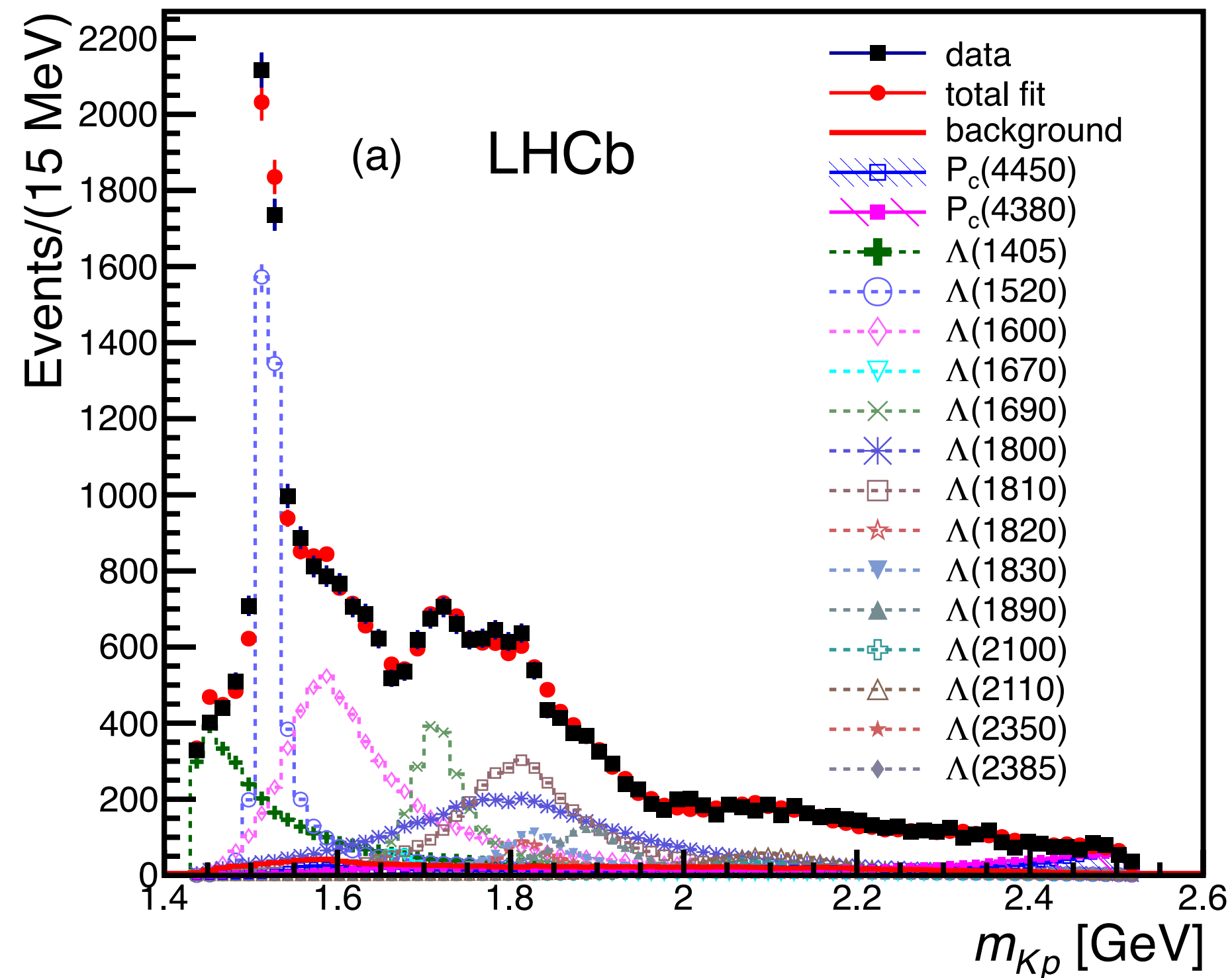


Try all Λ^* 's with J^P up to $7/2^\pm$

Best fit with a $J^P = 5/2^\pm$ pentaquark gives improvement, but $m(J/\psi p)$ still not good

$$\sqrt{\Delta 2\mathcal{L}} = 14.7\sigma$$

Reduced model with two P_c 's



$uudc\bar{c}$

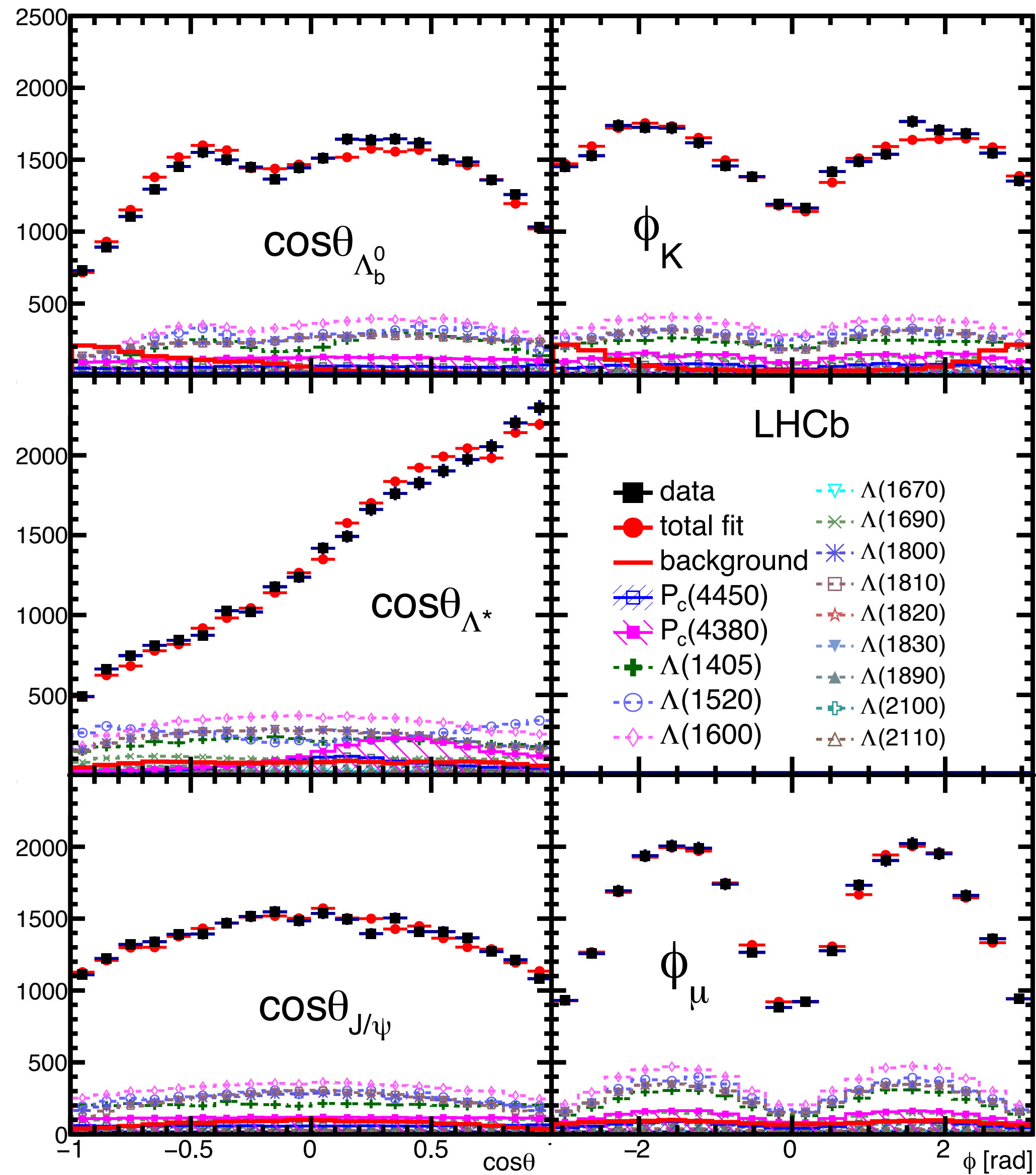
$J^P = (3/2^+, 5/2^-)$ and $(5/2^+, 3/2^-)$ also give good fits:
need more data.

No improvement with addition of other resonances
 Significance evaluated using toy simulation
 Need opposite parity to explain the data

	$P_c(4380)^+$	$P_c(4450)^+$
J^P	$\frac{3}{2}^-$	$\frac{5}{2}^+$
Mass [MeV/ c^2]	$4380 \pm 8 \pm 29$	$4449.8 \pm 1.7 \pm 2.5$
Width [MeV/ c^2]	$205 \pm 18 \pm 86$	$39 \pm 5 \pm 19$
Fit fraction [%]	$8.4 \pm 0.7 \pm 4.2$	$4.1 \pm 0.5 \pm 1.1$
Significance	9σ	12σ

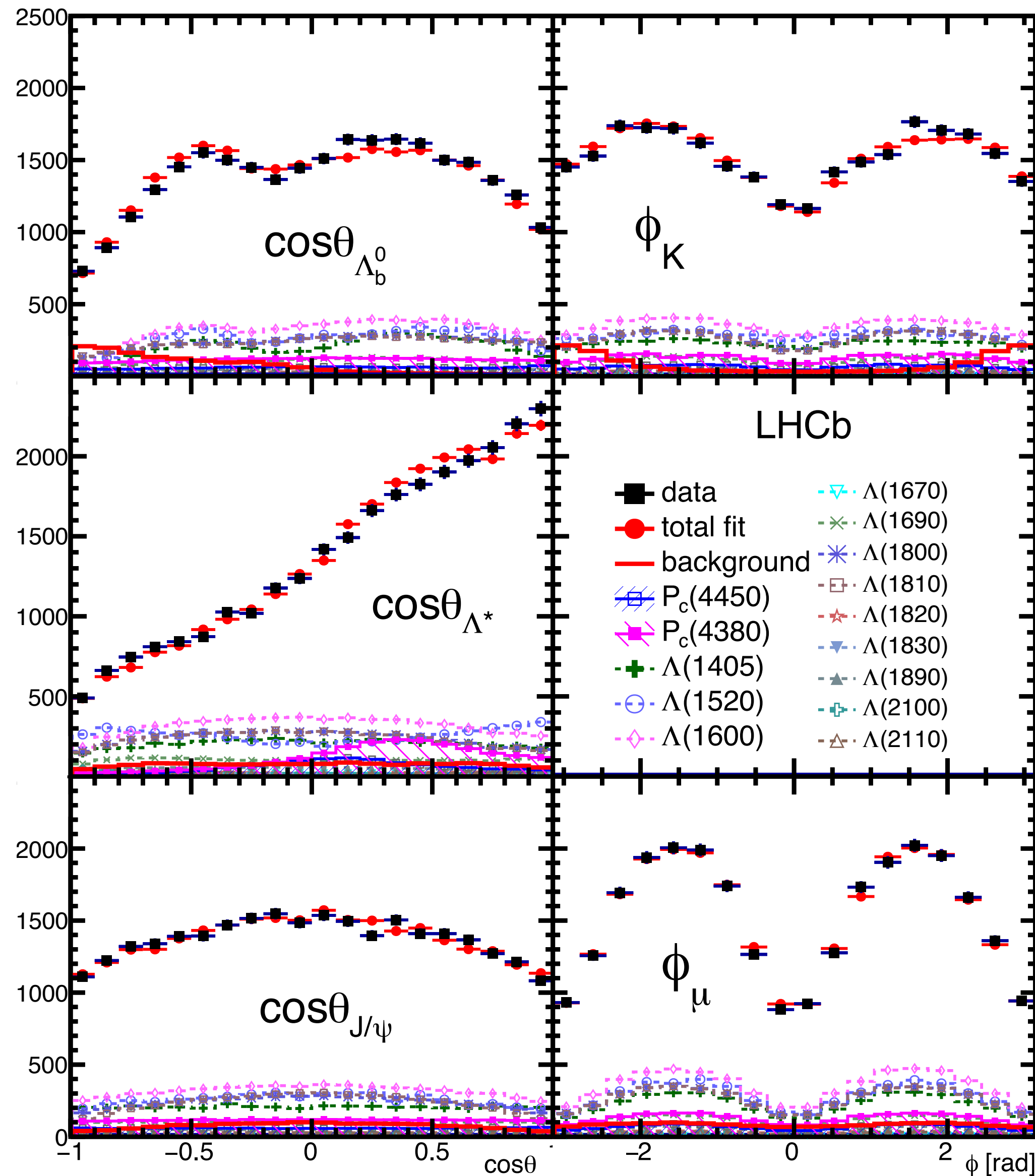
Angular distributions

Good fit to the angular observables

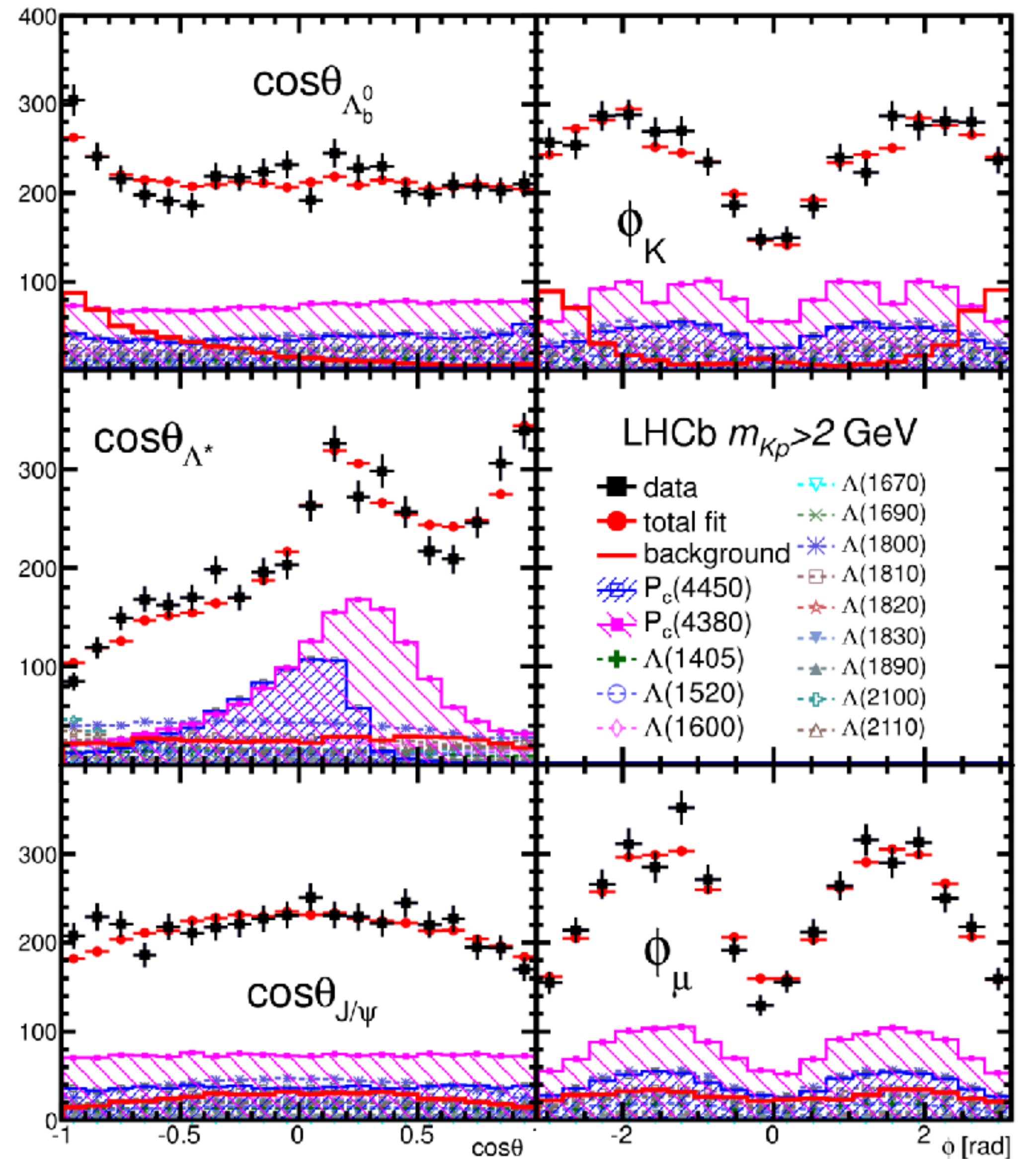


Angular distributions

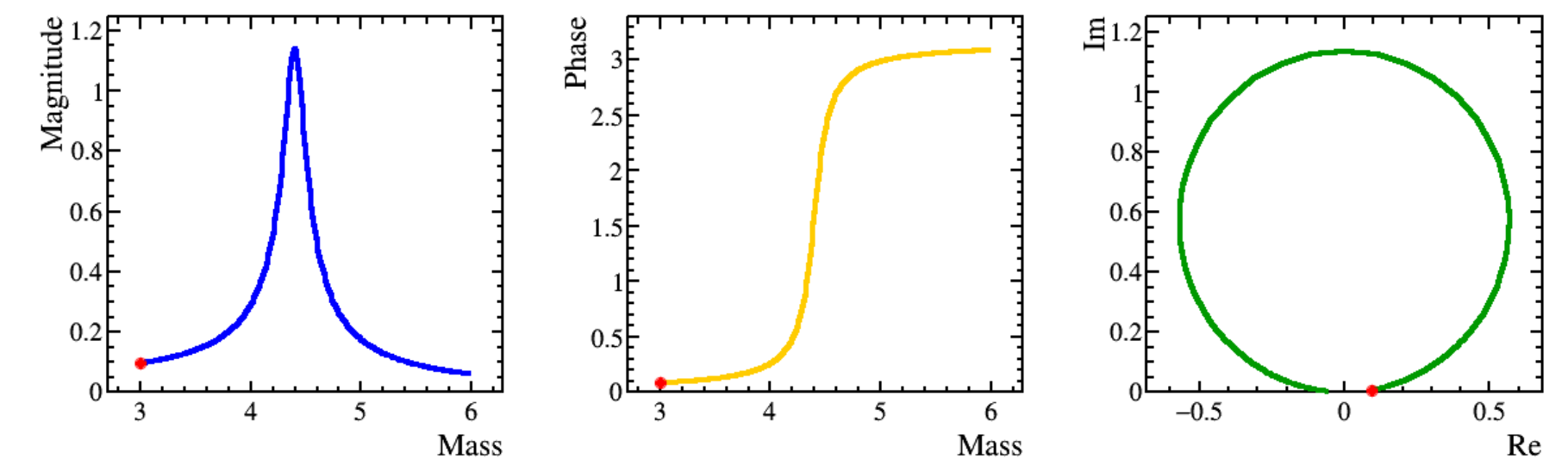
Good fit to the angular observables



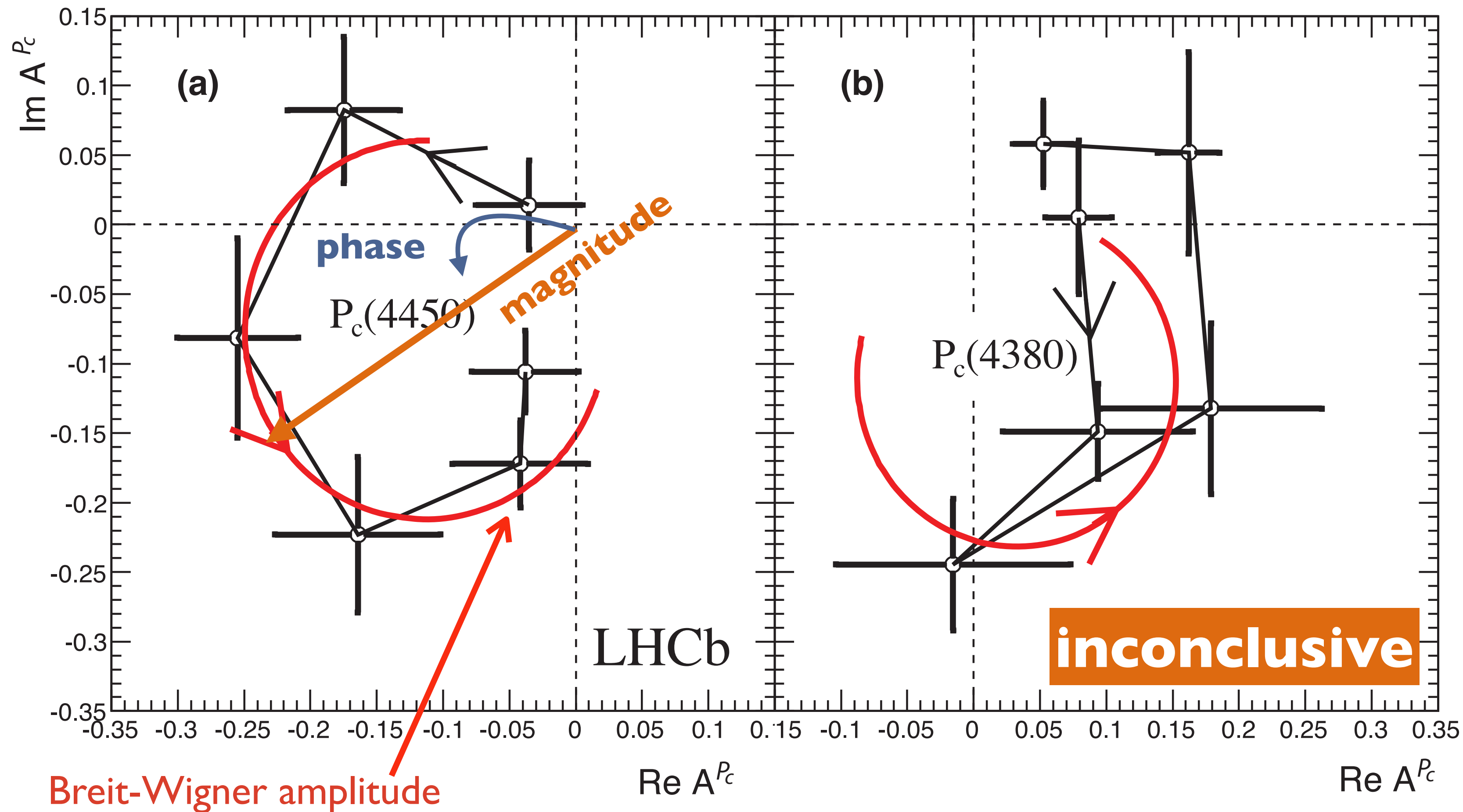
High $m(Kp)$ region > 2 GeV



Resonant behaviour



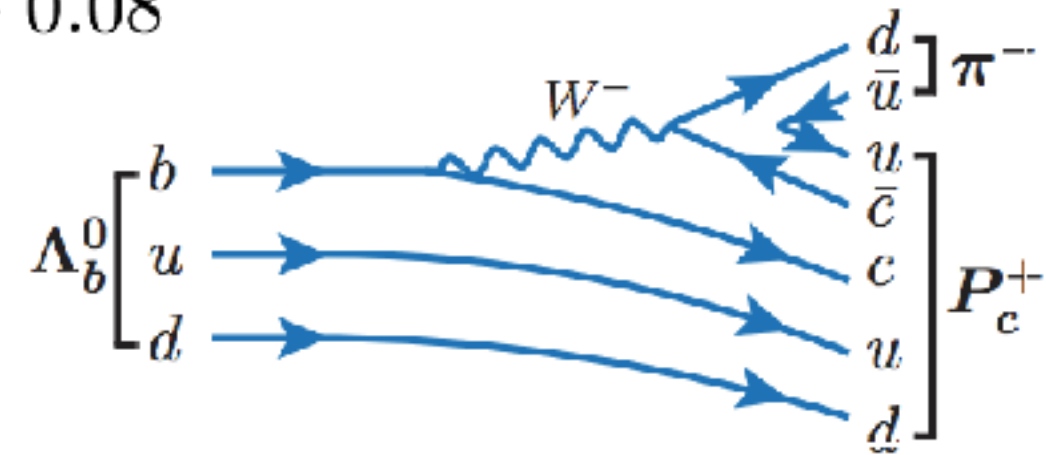
Observe rapid change of phase near maximum of magnitude \Rightarrow **resonance!**



$\Lambda_b \rightarrow J/\psi p \pi^-$ pentaquark search

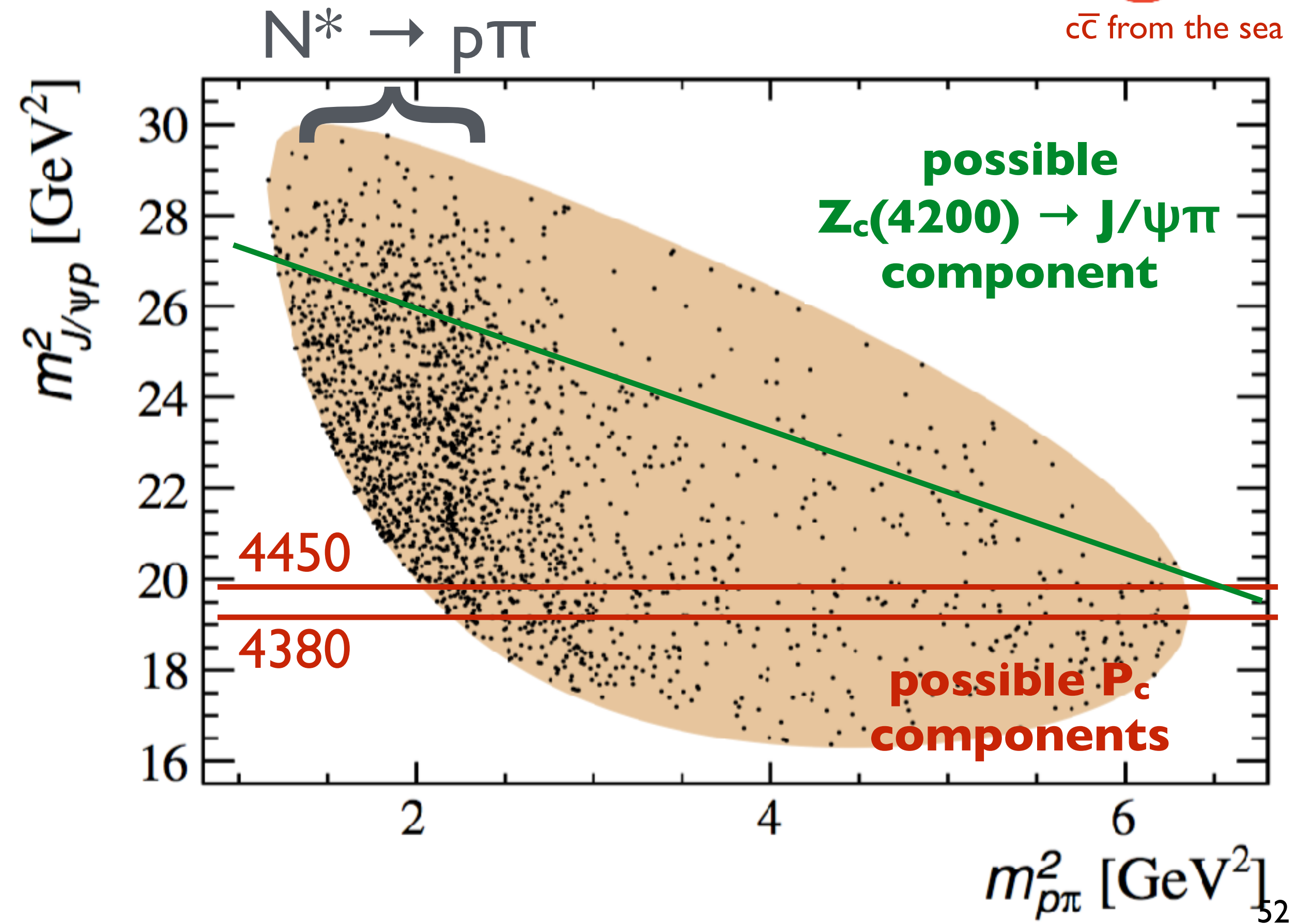
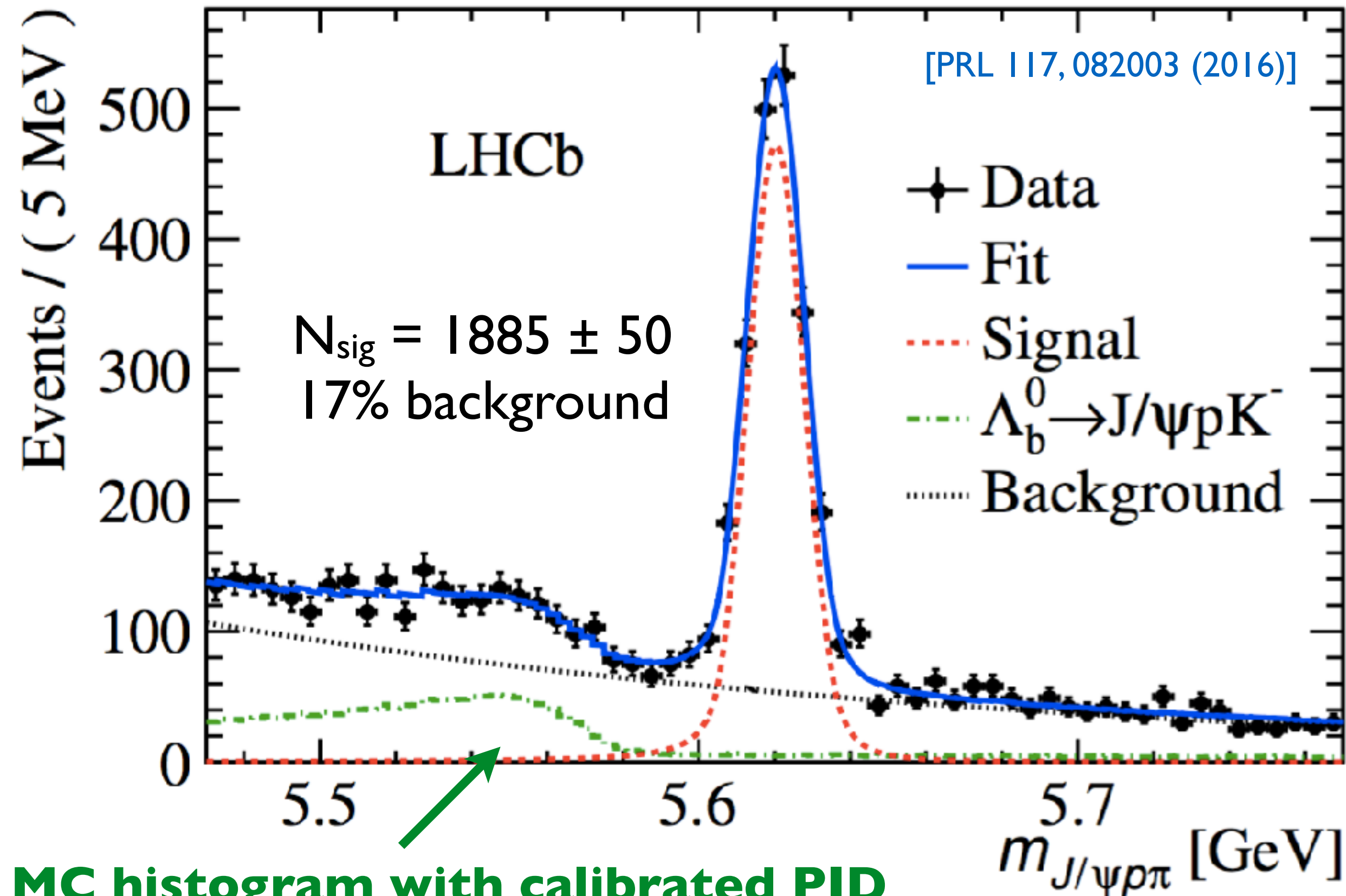
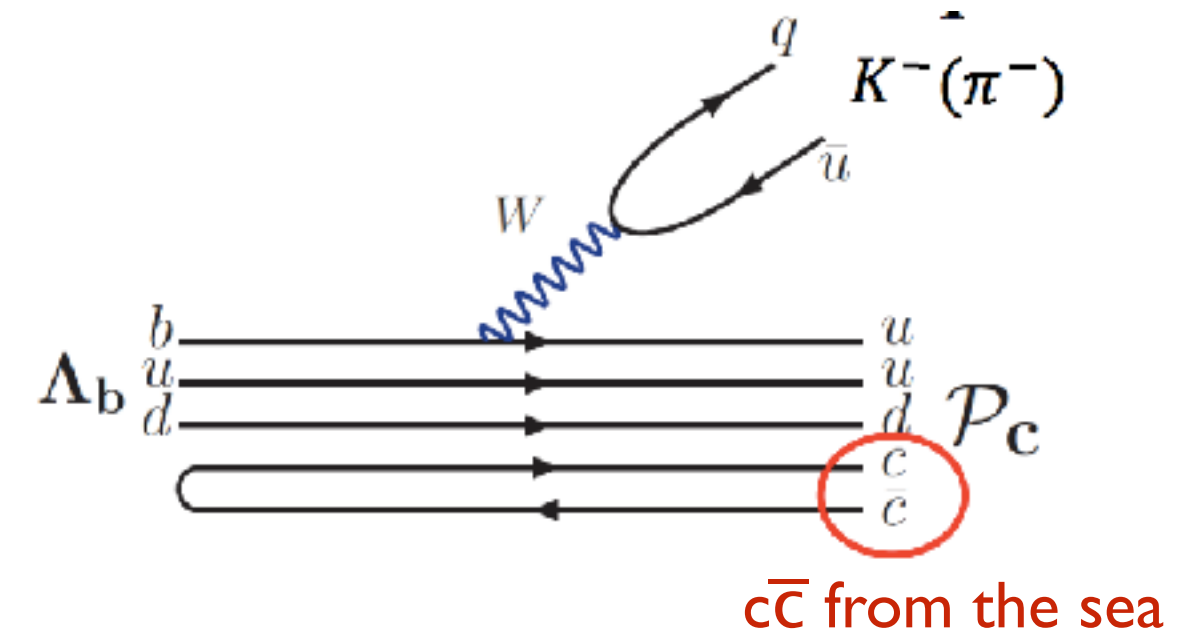
$$R_{\pi^-/K^-} \equiv \frac{\mathcal{B}(\Lambda_b^0 \rightarrow \pi^- P_c^+)}{\mathcal{B}(\Lambda_b^0 \rightarrow K^- P_c^+)} \approx 0.07 - 0.08$$

[Cheng et al. PRD 92, 096009 (2015)]



$$R_{\pi^-/K^-} = 0.58 \pm 0.05$$

[Hsiao, Phys. Lett. B 751, 572 (2015)]



$\Lambda_b \rightarrow J/\psi p \pi^-$ pentaquark search

[PRL 117, 082003 (2016)]

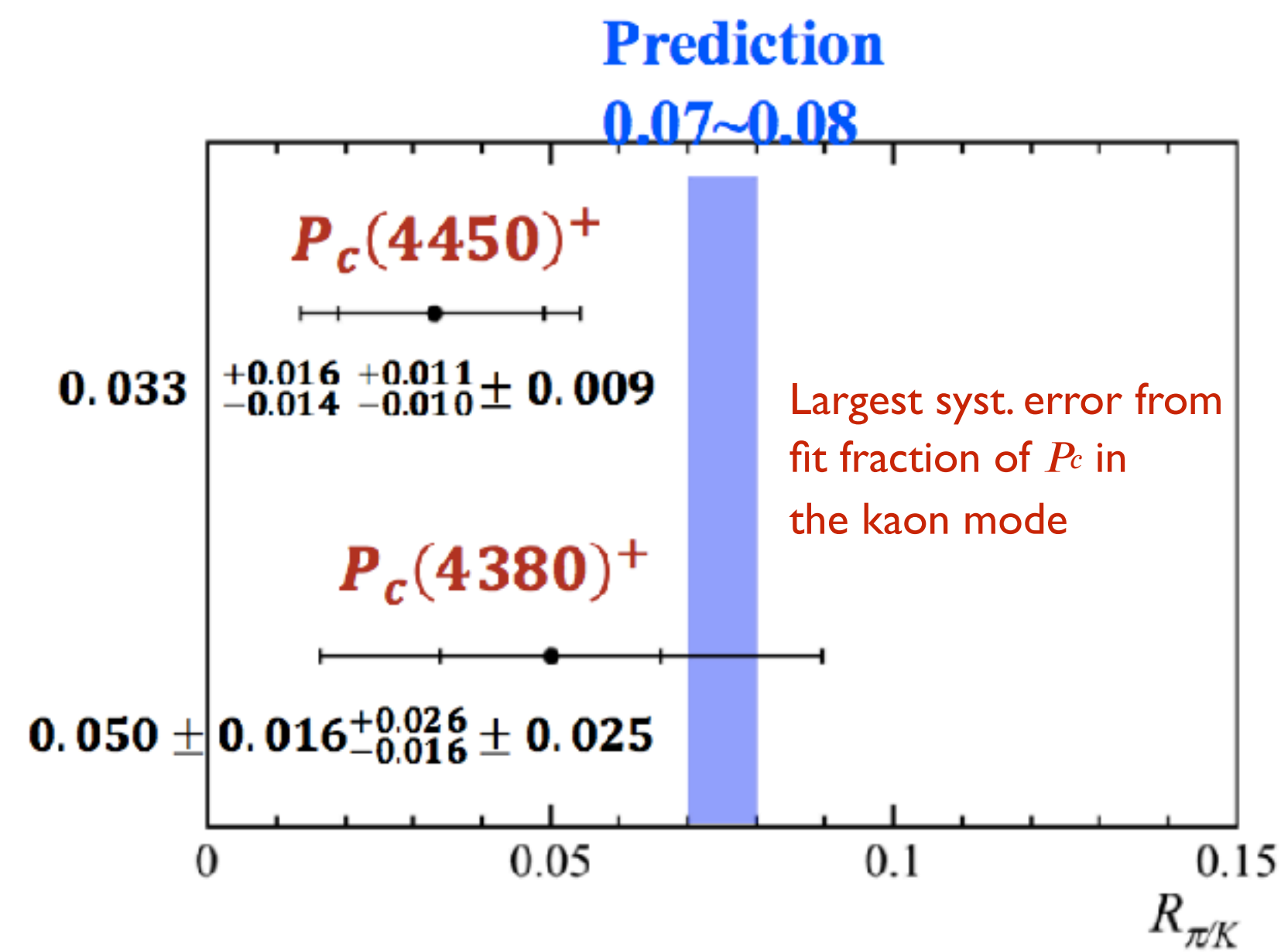
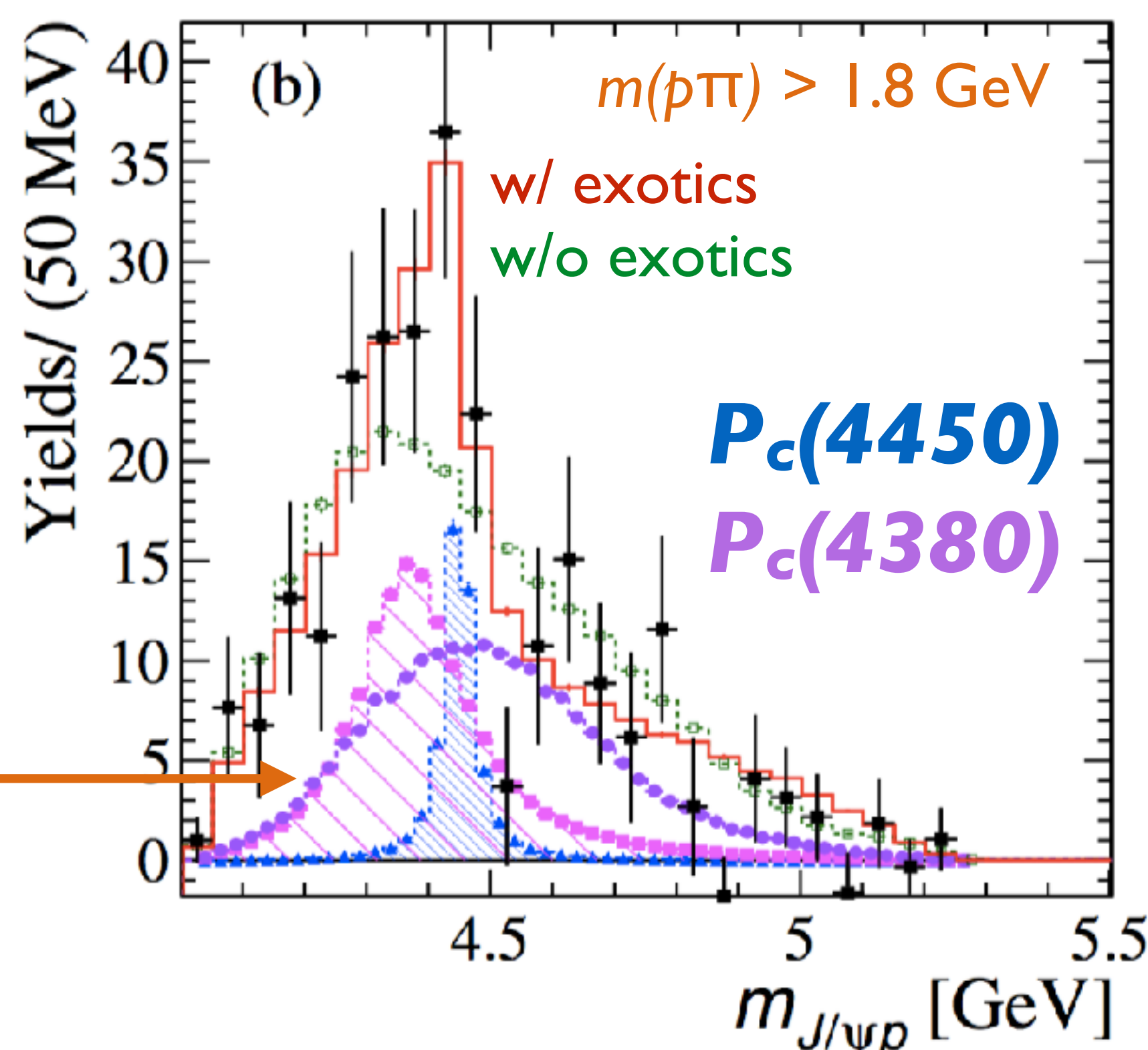
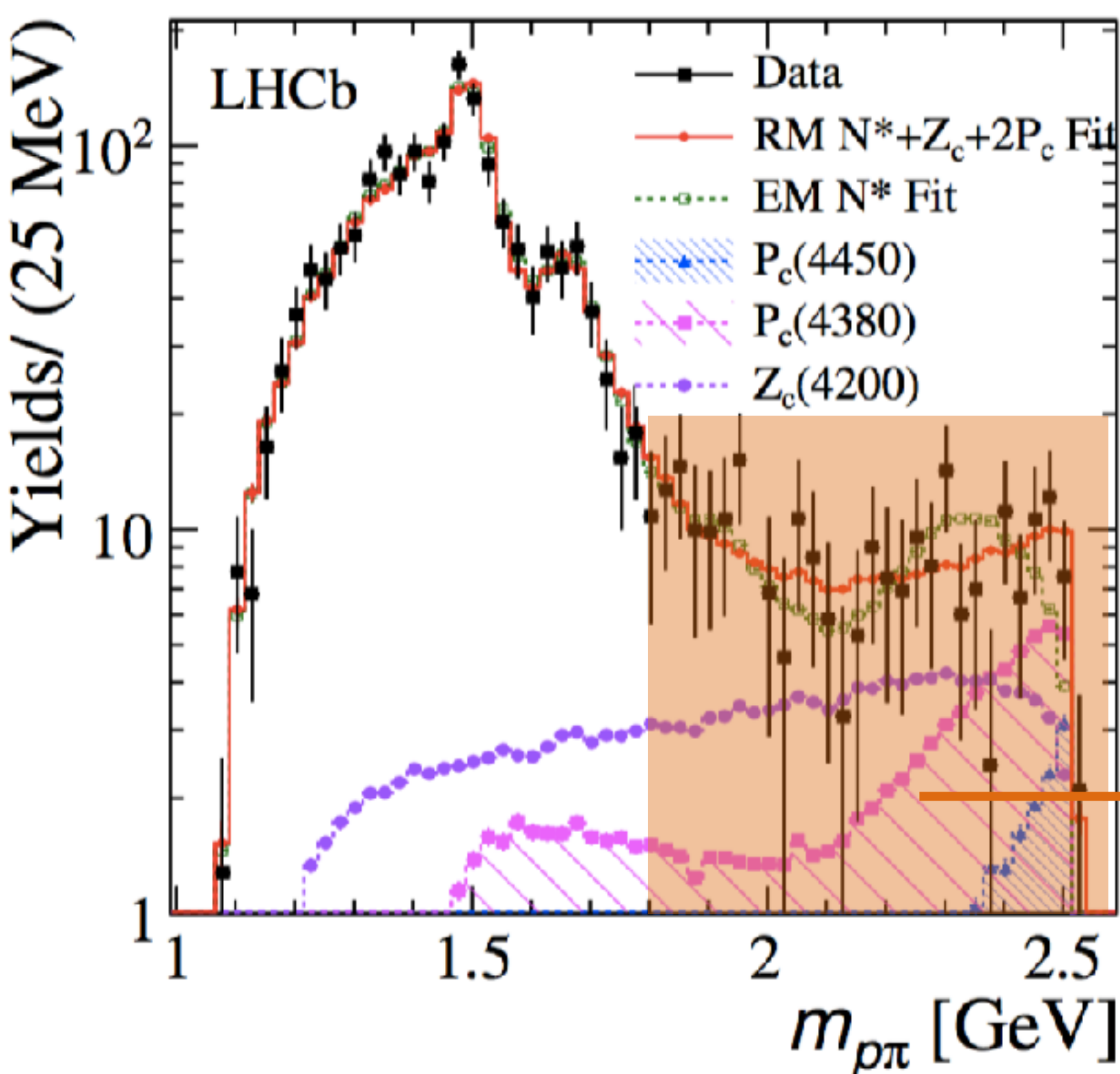
N*-only model not a good fit

Good fit using 15 N* components + exotic components

3.1 σ for (2 P_c + Z_c) or 3.3 σ for 2 P_c states

Main systematics from fixed P_c/Z_c mass/width parameters, N* model and P_c spin

States	Fit fraction (%)
$P_c(4380)^+$	$5.1 \pm 1.5^{+2.1}_{-1.6}$
$P_c(4450)^+$	$1.6^{+0.8+0.6}_{-0.6-0.5}$
$Z_c(4200)^-$	$7.7 \pm 2.8^{+3.4}_{-4.0}$

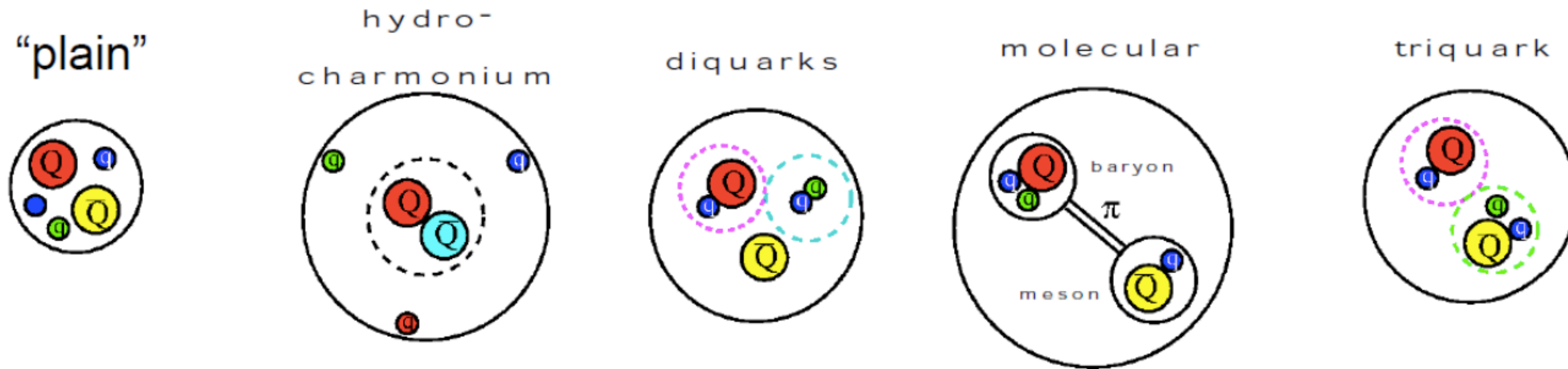


rules out
[Hsiao, Phys. Lett. B 751, 572 (2015)]

Phenomenological models

[Maiani et al arXiv:1507.04980]
[Lebed arXiv:1507.05867]
[Zhu arXiv:1510.08693]
[Roca et al, PRD 92 (2015) 094003]
.....

Many phenomenological models on the market, e.g., $D^*\Sigma_c - D^*\Sigma_c^*$ molecular state, tightly bound di-quarks, hadro-charmonium?



None of them can explain all observed exotic states, so may need several models to describe everything we see.

The di-quark model

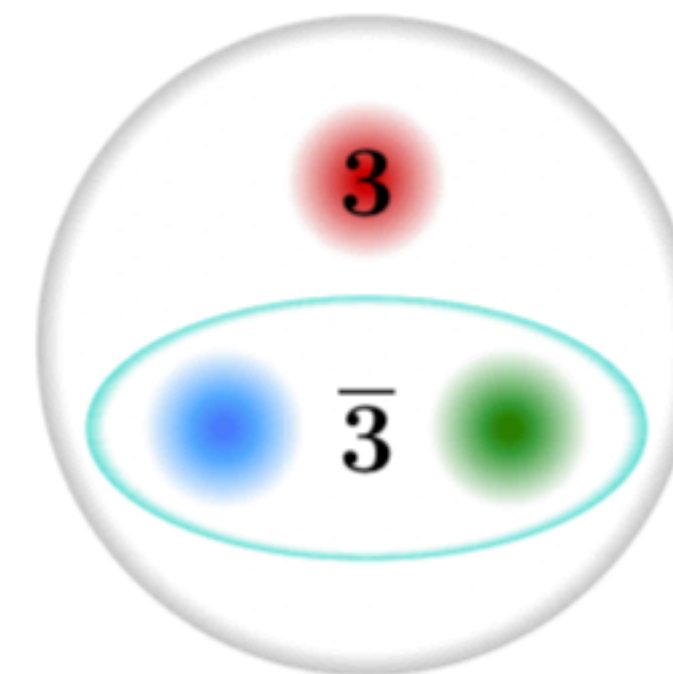
Can build colour-neutral objects from coloured constituents

Meson



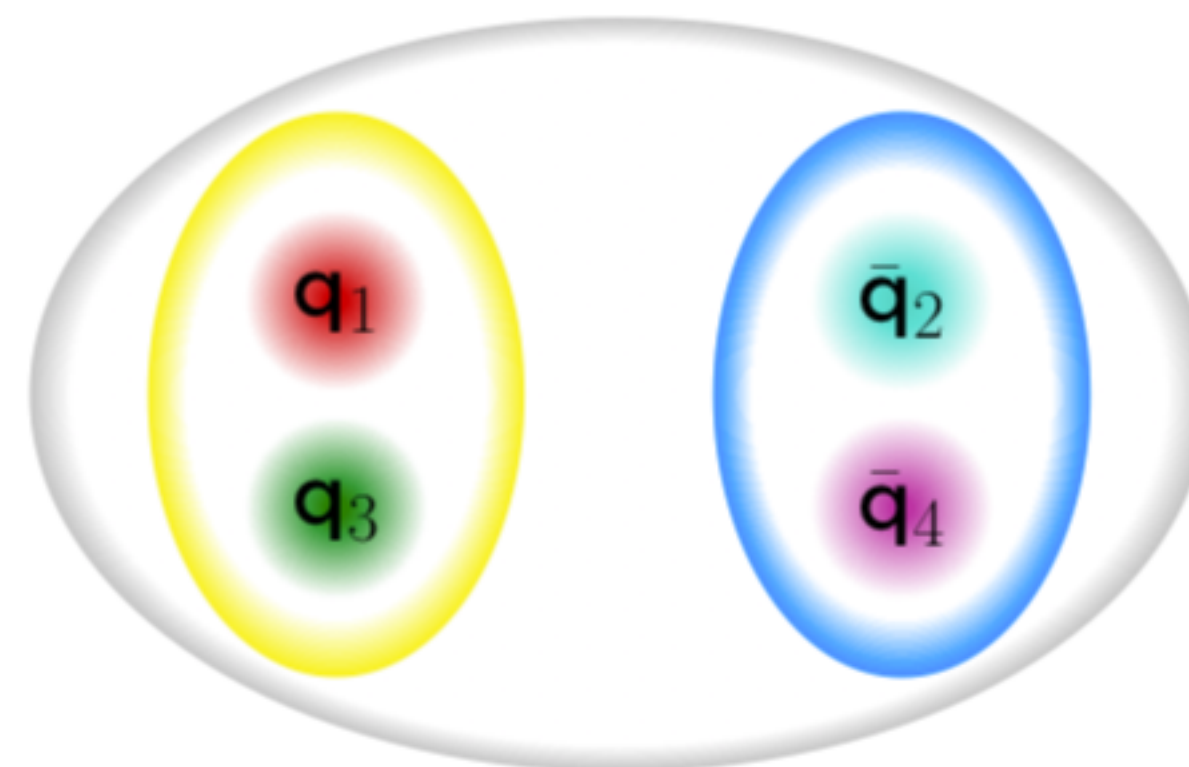
Mesons are bound through attractive $3\bar{3}$ colour coupling

Baryon



$3 \otimes 3 \rightarrow \bar{3}$, allowing for qq diquark to bind with the other quark to make the baryon

Tetraquark



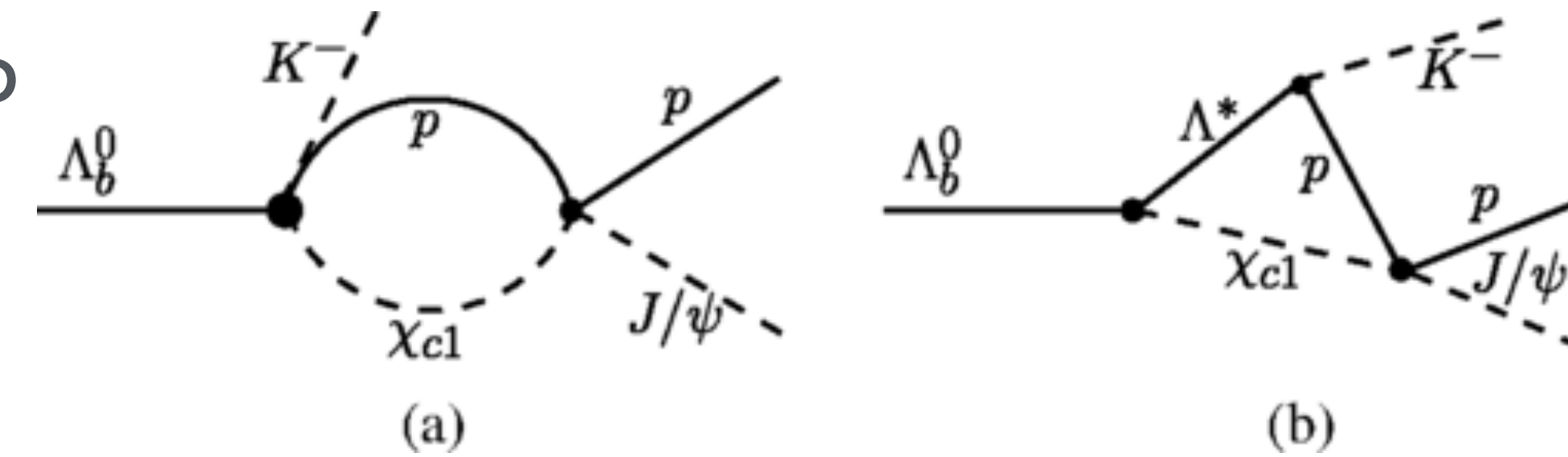
Bind two diquarks together

Could rescattering explain exotics?

$P_c(4450)$ has mass at threshold of χ_{c1p} so could be due to $J/\psi p$
→ χ_{c1p} kinematic rescattering

Reproduces $P_c(4450)$ phase motion but what about $P_c(4380)$?

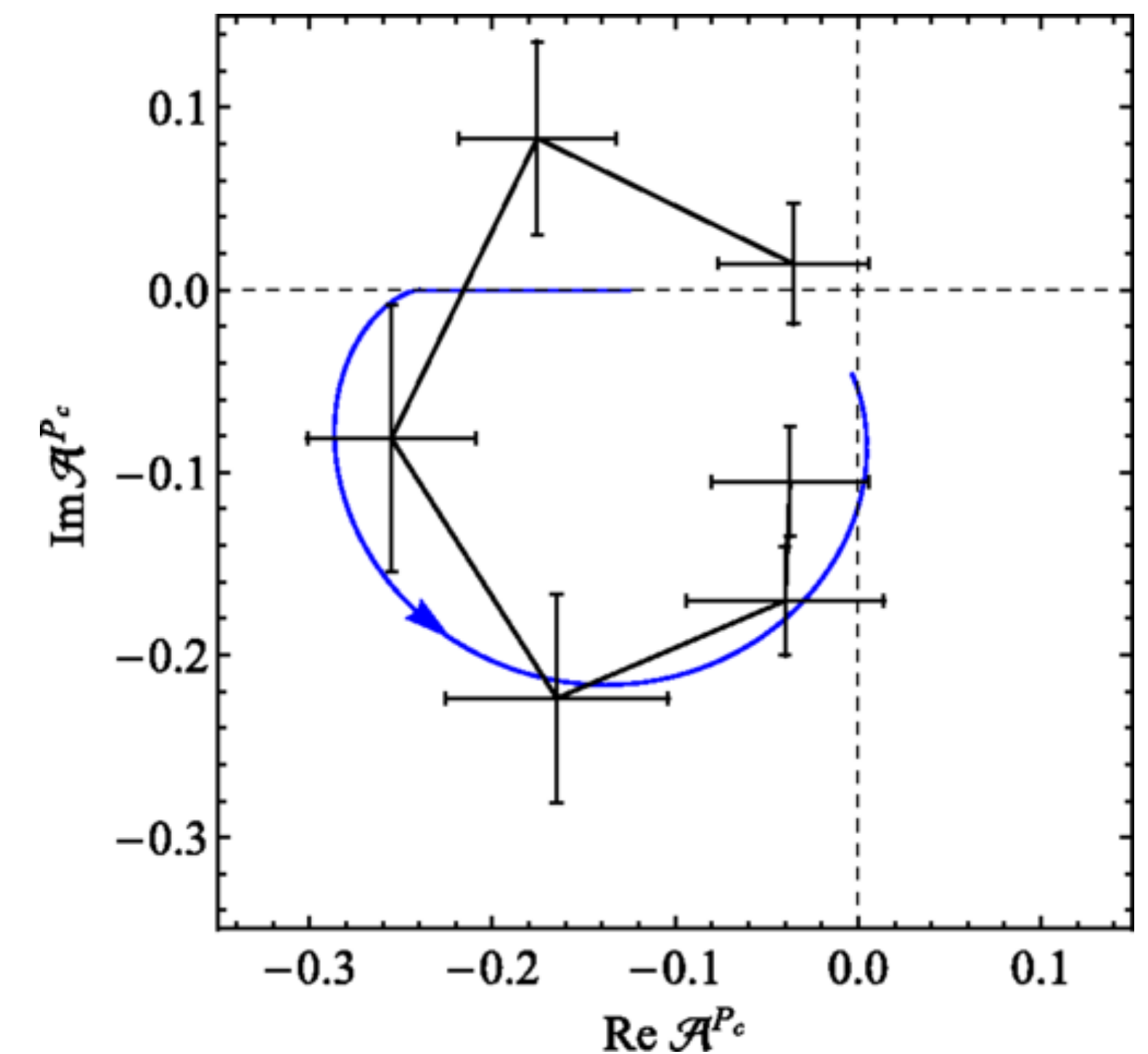
Rescattering would not explain narrow enhancement above
 χ_{c1p} threshold.



[Guo et al., PRD 91 (2015) 051504]

[Guo et al, PRD 92 (2015) 071502(R)]

[Bayer et al., PRD 94 (2016) 074039]

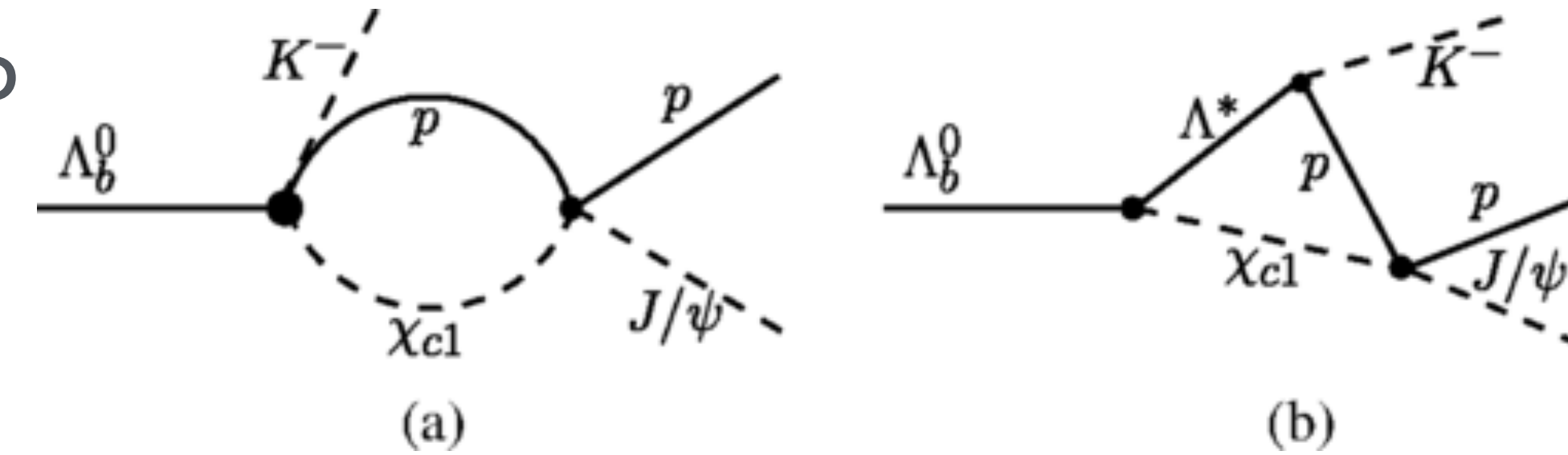


Could rescattering explain exotics?

$P_c(4450)$ has mass at threshold of $\chi_{c1}p$ so could be due to $J/\psi p \rightarrow \chi_{c1}p$ kinematic rescattering

Reproduces $P_c(4450)$ phase motion but what about $P_c(4380)$?

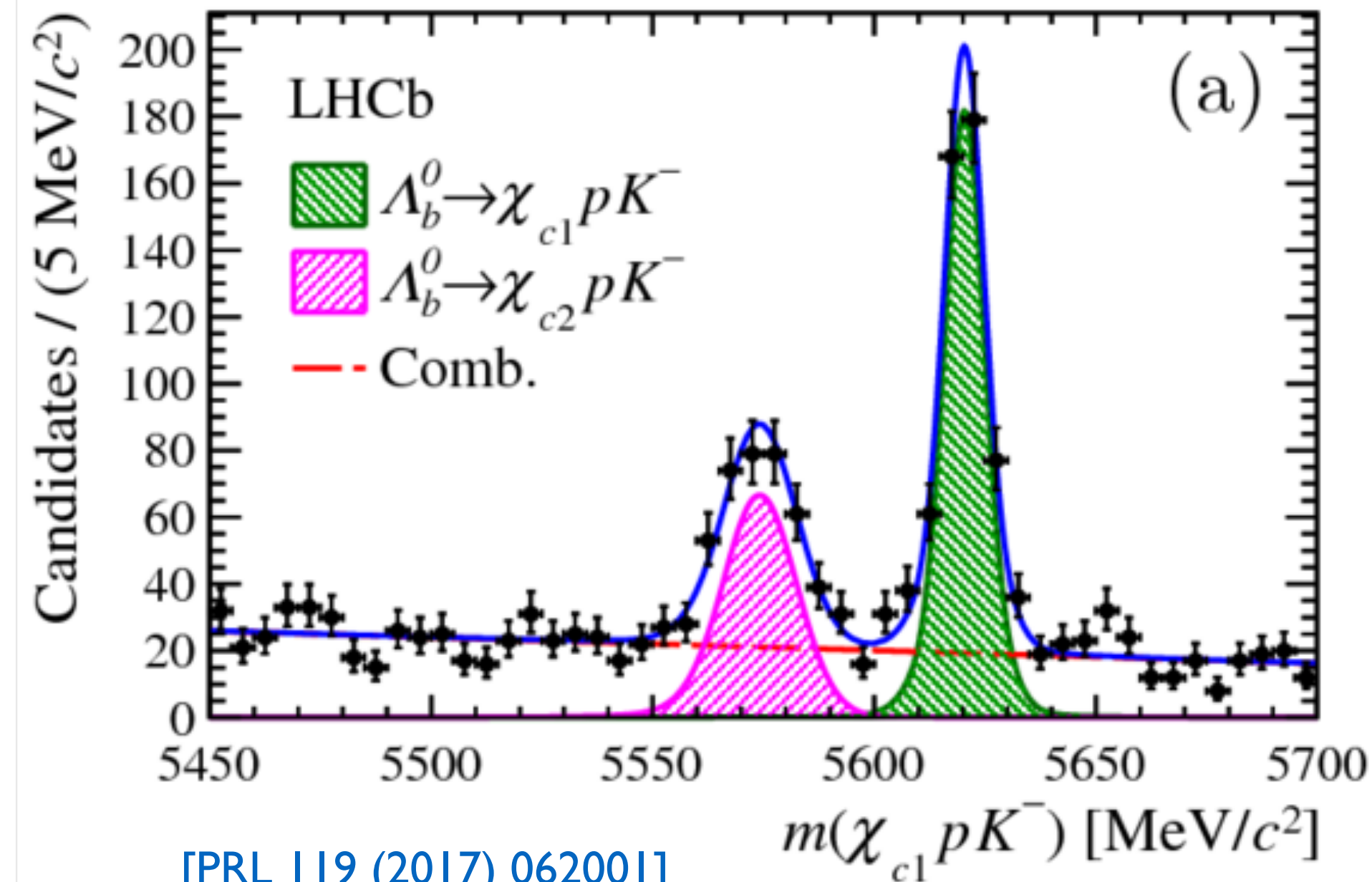
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[Guo et al., PRD 91 (2015) 051504]

[Guo et al, PRD 92 (2015) 071502(R)]

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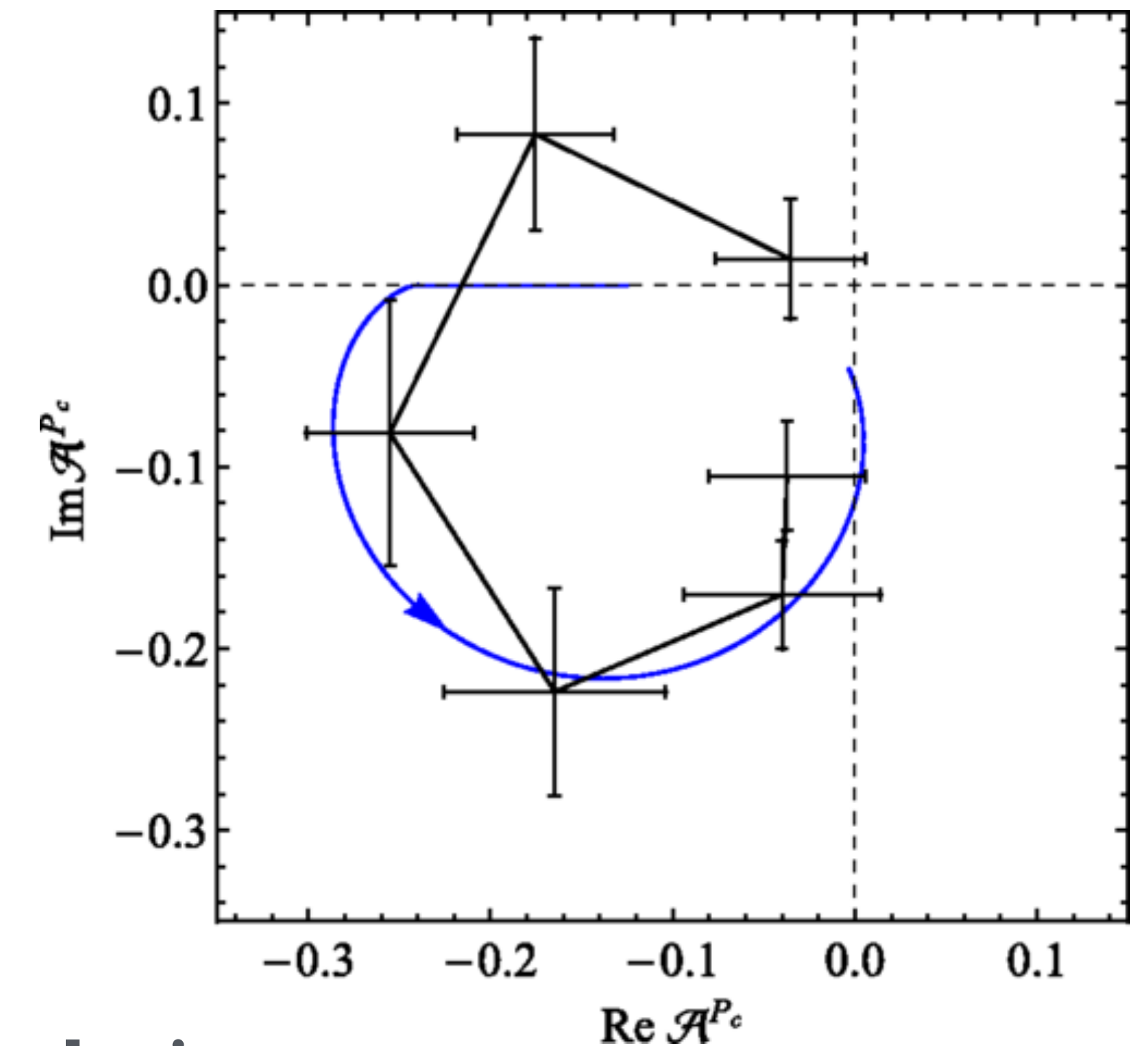


[PRL 119 (2017) 062001]

$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow \chi_{c1} p K^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi p K^-)} = 0.242 \pm 0.014 \pm 0.013 \pm 0.009$$

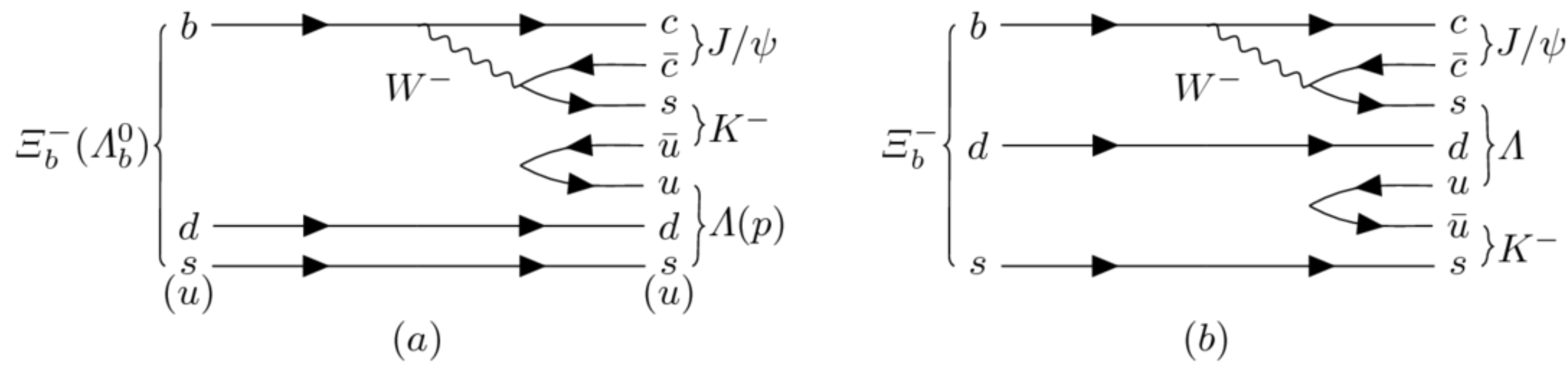
$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow \chi_{c2} p K^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi p K^-)} = 0.248 \pm 0.020 \pm 0.014 \pm 0.009$$

\uparrow $\mathcal{B}(\chi_{c1})$
 \downarrow



Next step: amplitude analysis

Observation of the $\Xi_b^- \rightarrow J/\psi \Lambda K^-$ decay



Strange pentaquark ($udsc\bar{c}$) predicted

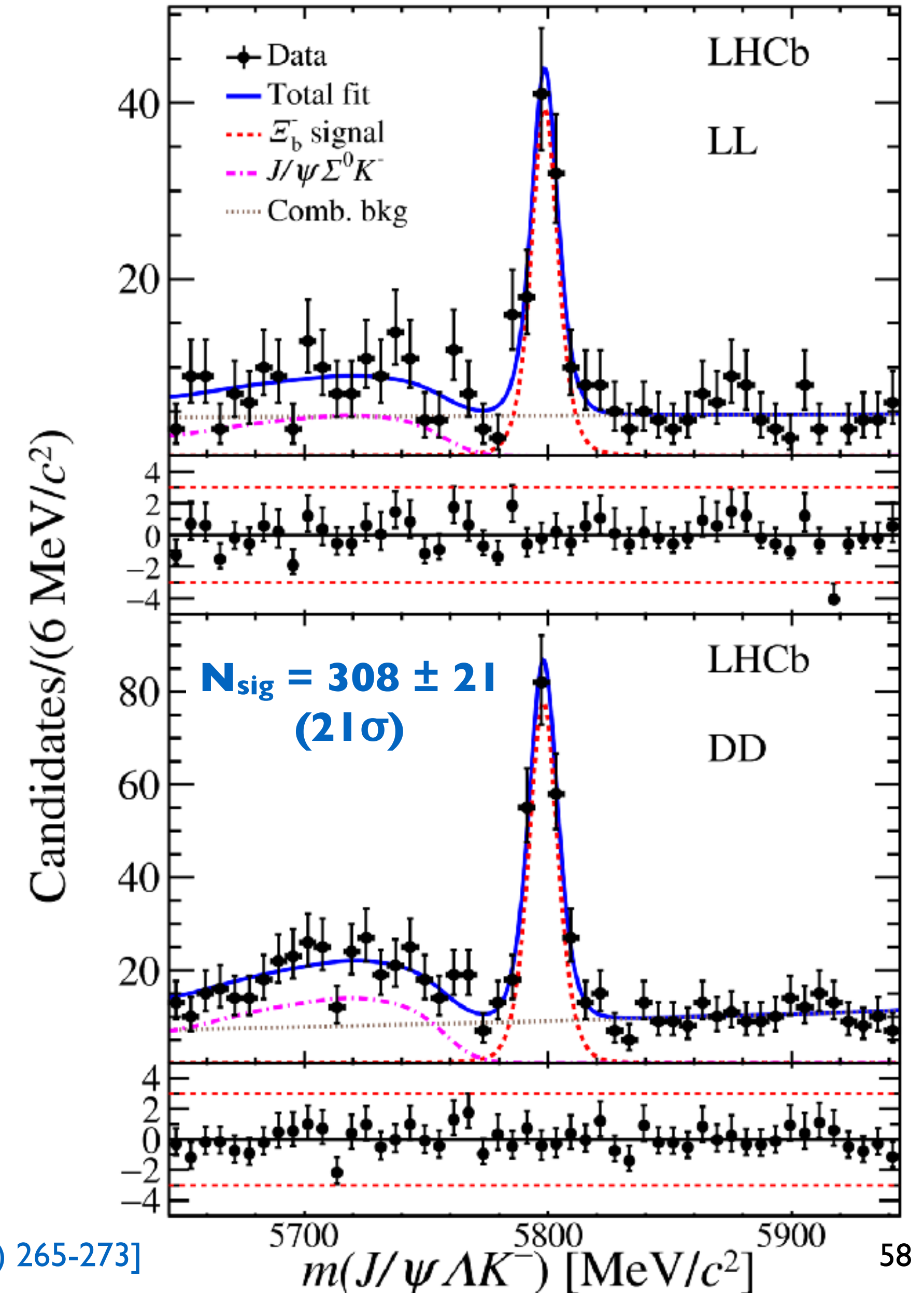
[PRL 105, 232001 (2010)]

Can be searched for in the Ξ_b^- decay

[PRC 93, 065203 (2016)]

Expect ~ 1500 signal events after 2018

→ amplitude analysis



[Phys. Lett. B 772 (2017) 265-273]

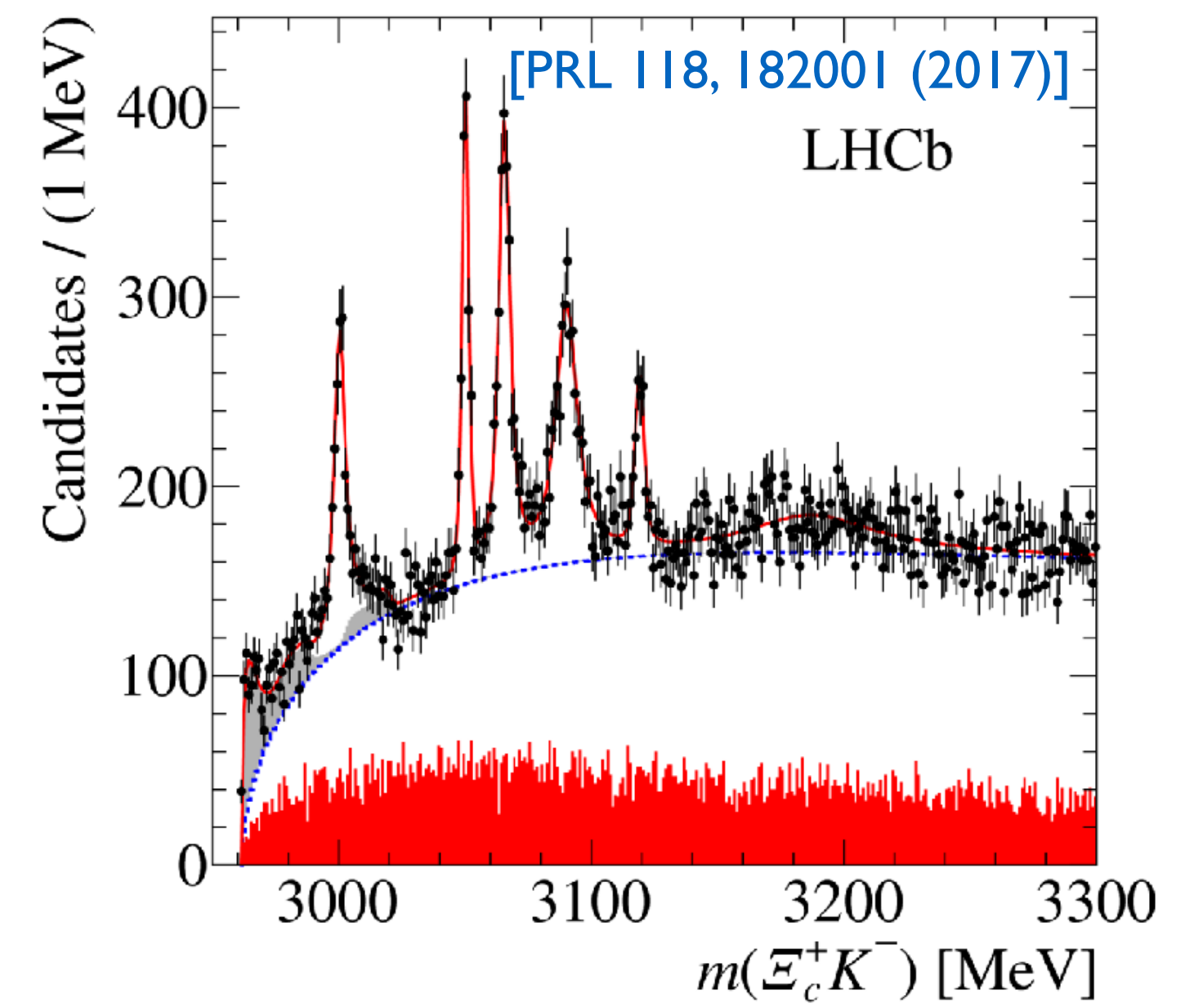
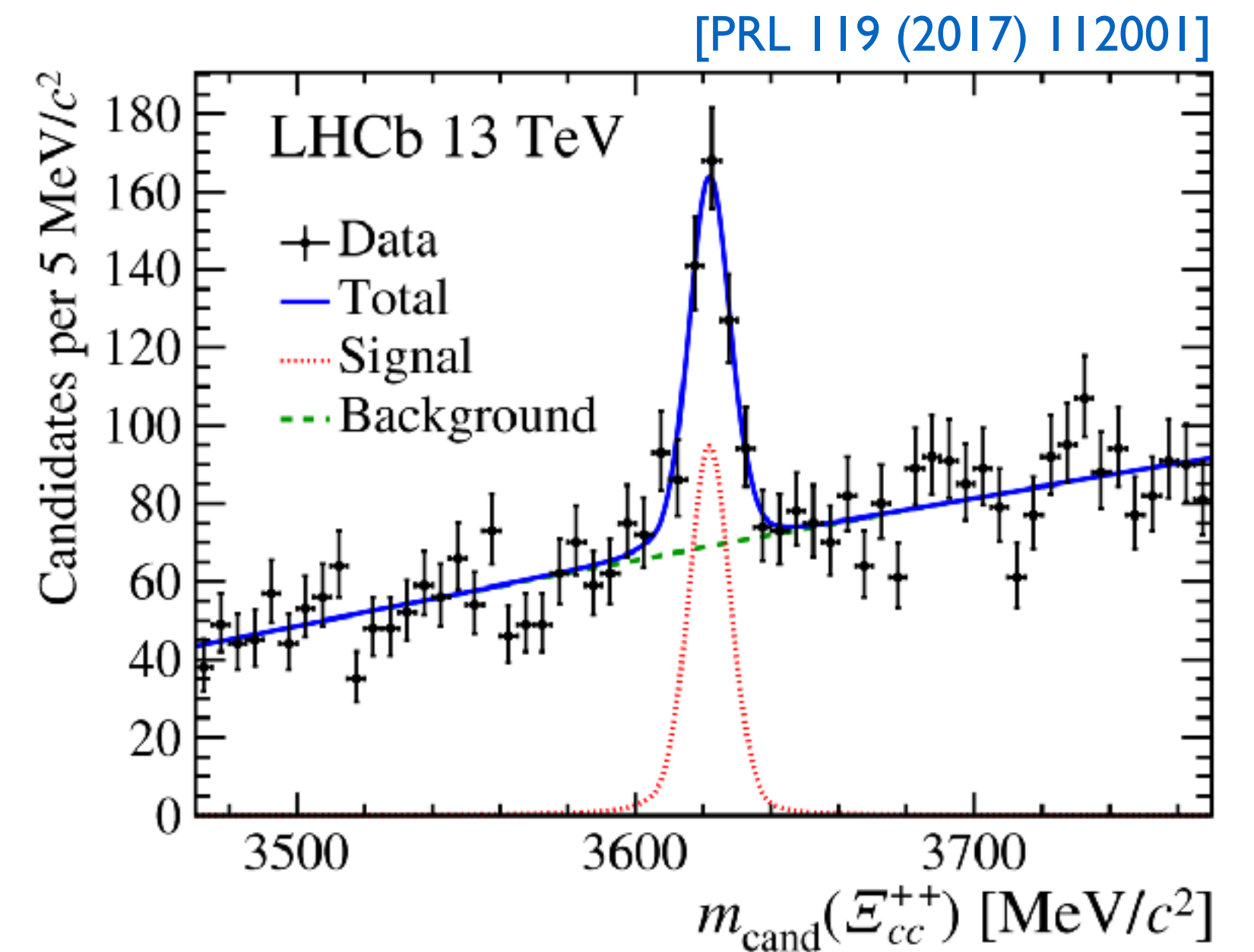
Connections with “conventional” spectroscopy

Discovery of Ω_c^{**} and Ξ_{cc}^{++} have spurred theoretical investigations, motivated by the calibration of the binding energy of their constituent **diquarks**.

Calibrating diquark model parameters from Ω_c^{**} , treating them as [ss]c diquark-quark objects. Can then use this to make predictions about the Y states. [\[Ali et al., arXiv:1708.04650\]](#)

Not only are some of the Ω_c^{**} states now thought of as potential pentaquarks, but theorists are using these as a basis to propose other candidates. [\[Mehen arXiv:1708.05020\]](#) [\[Karliner and Rosner arXiv:1707.07666\]](#)

e.g., doubly-bottom tetraquark (~ 10.4 GeV) that is stable to EM/strong interactions, potentially narrow, with very interesting decay modes (B, D, double-J/ ψ ...)



Future experimental programme

I. Observe states in different **production** mechanisms

e.g. Photo-production $\gamma p \rightarrow J/\psi p$ experiment has been approved at JLab

[Meziani et al., arXiv:1609.00676]

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2. Observe states in different **decay** modes

Search for $c\bar{c}$, open-charm and charm-less modes using all flavours of b-hadron

Transitions between exotic states (e.g., $Y(4260) \rightarrow X(3872)\gamma$)

Publish **non-observations!**

$$\Lambda_b^0 \rightarrow \Sigma_c^+ D^-$$
$$\Lambda_b^0 \rightarrow \Lambda_c^+ \bar{D}^{*0}$$

If exotic states are molecules then their open-charm decays may be dominant

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3. Look for **isospin** (ccudd), **strangeness** (ccuds), **bottom** (bbuud) partners

[PRL 105, 232001 (2010)]

$$\Lambda_b^0 \rightarrow P_{cs}^0 \phi \rightarrow J/\psi \Lambda \phi$$

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4. Measure **branching ratios**

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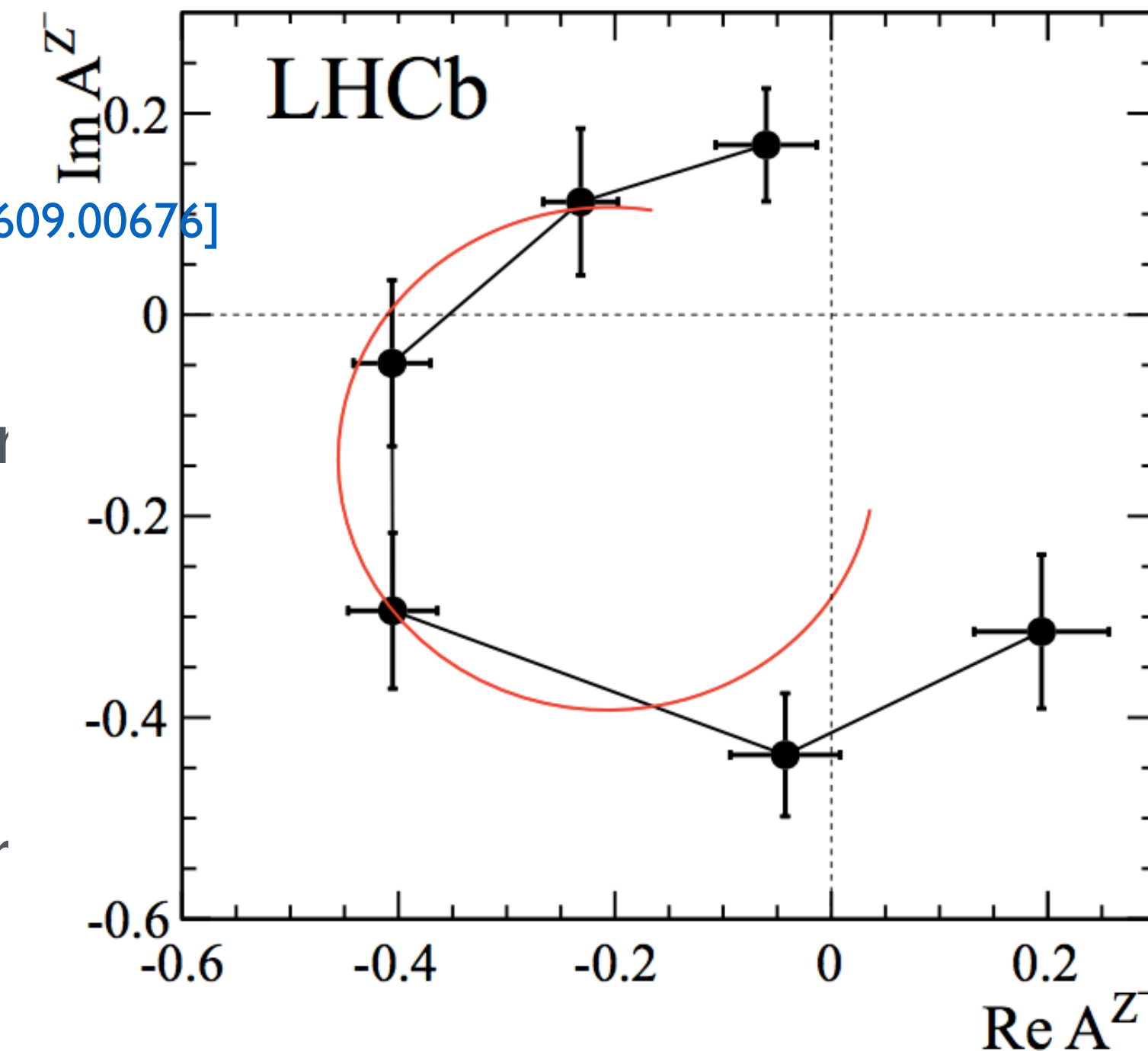
[PRL 105, 232001 (2010)]

4. Measure **branching ratios**

5. Measure angular distributions and **quantum numbers**

Amplitude (partial wave) analyses are crucial, as are accounting for threshold effects

Publish experimental efficiencies to allow others to better use results



LHC, Belle-II, BES-III, COMPASS, JLab and PANDA all have role to play!

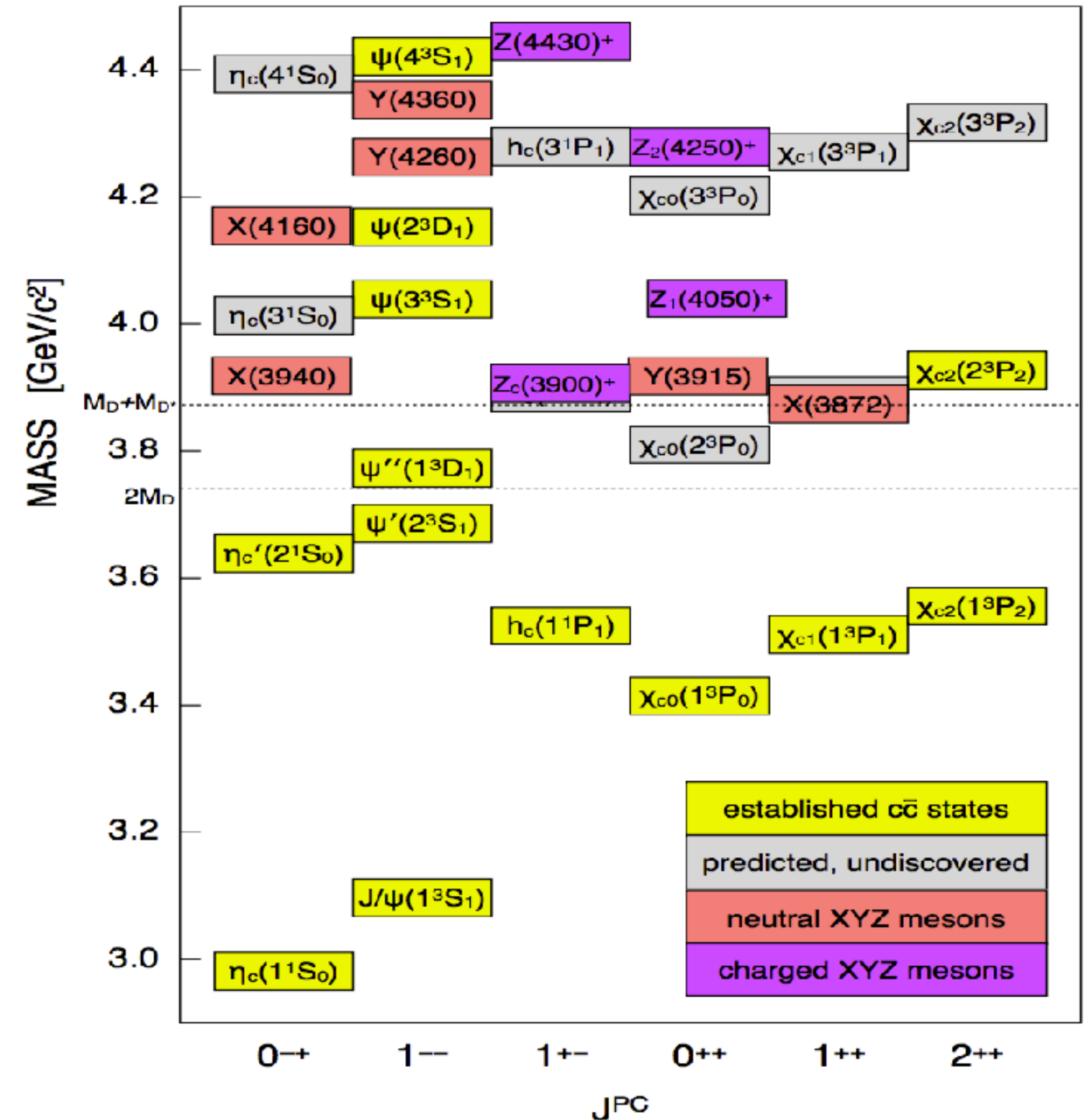
Summary

Revolution in heavy-quark spectroscopy since 2003 discovery of X(3872).

~30 XYZ and P_c states observed using different production and decay mechanisms.

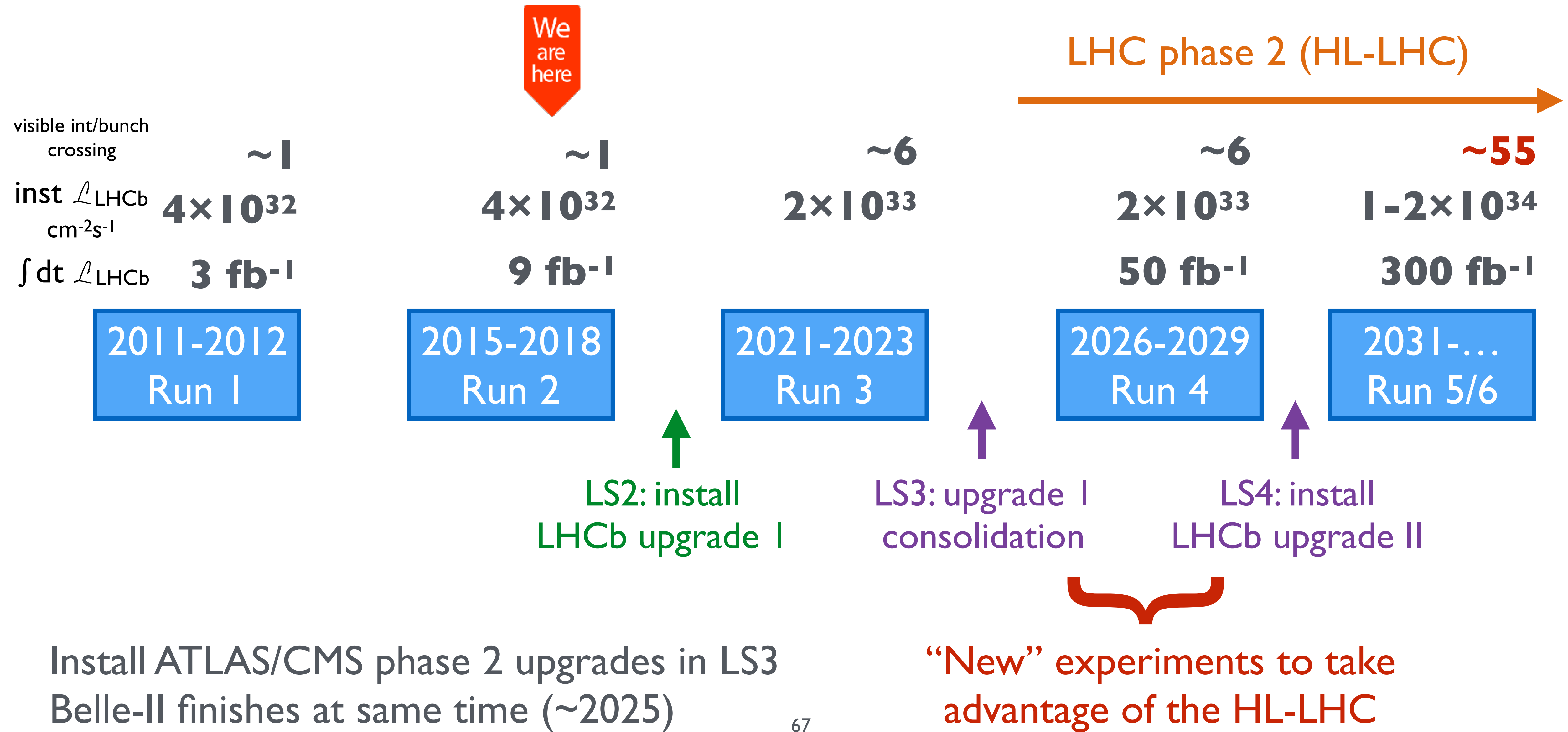
Exotic states provide ideal foundation to deepen understanding of non-perturbative QCD dynamics.

Crucial to confirm observations where possible and use state-of-the-art amplitude analyses and collaboration with theorists to understand observed states.



Backup

The next ~20 years...

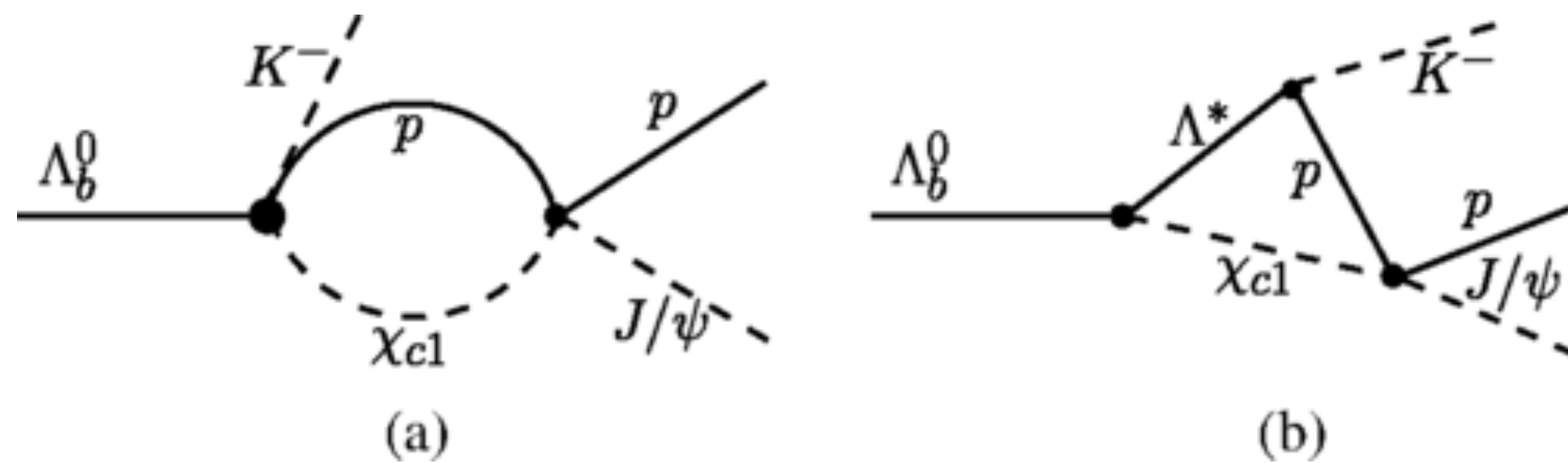


What is a resonance?

Formally, taken as meaning a pole in the S-matrix (scattering matrix) of a particular process.

They are dynamical (and non-perturbative) in nature: the interactions between quarks/gluons (or among hadrons) give the poles in the scattering amplitude.

S-matrix can also have “kinematic” singularities, such as at two-body thresholds or the triangle singularity (originating from three on-shell particles)



Important to be able to distinguish the dynamical and kinematics singularities

[Guo, arXiv:1712.10126]

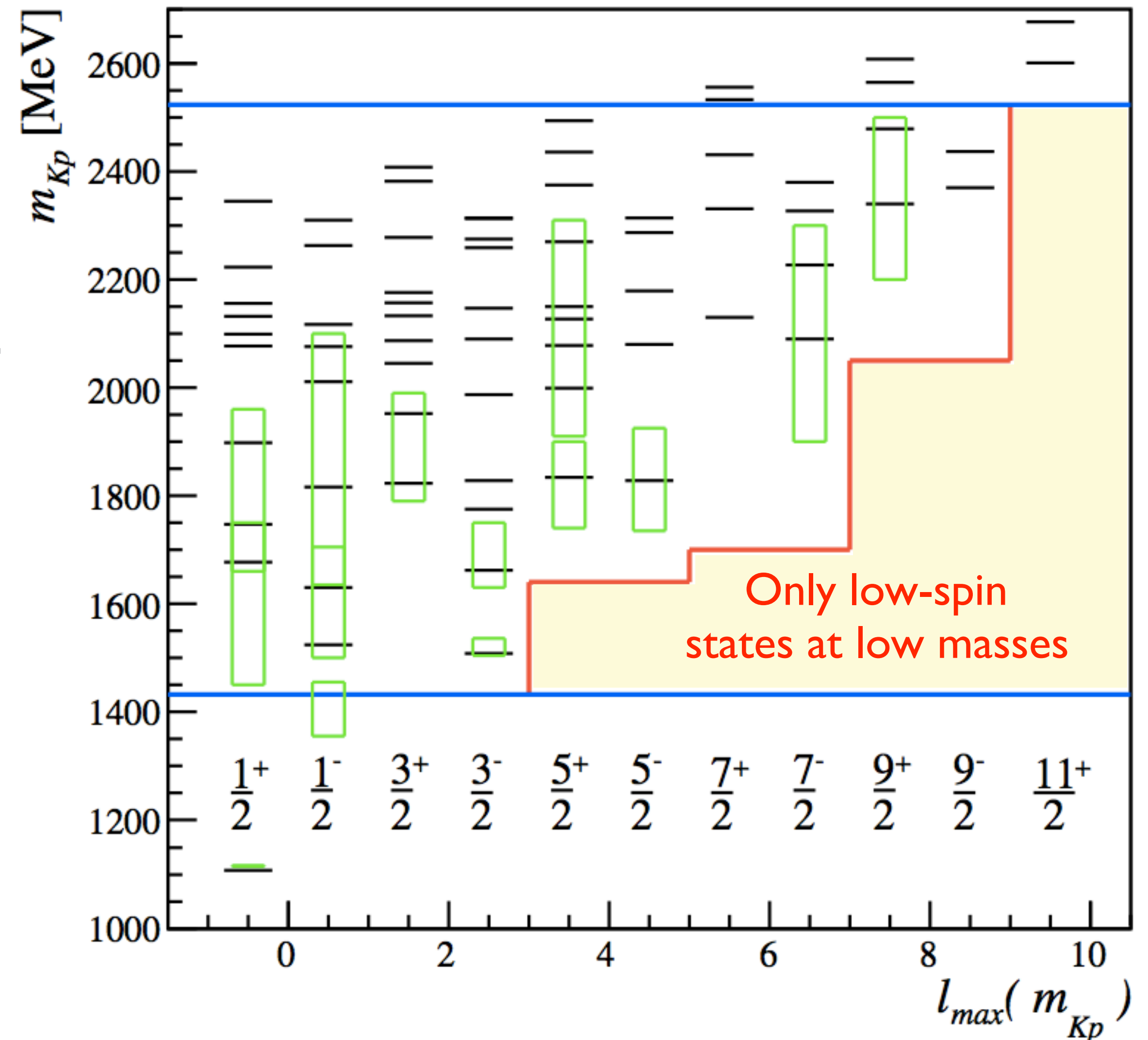
Pentaquark model-independent

Λ^* spectrum is largest systematic uncertainty in observation of P_c states.

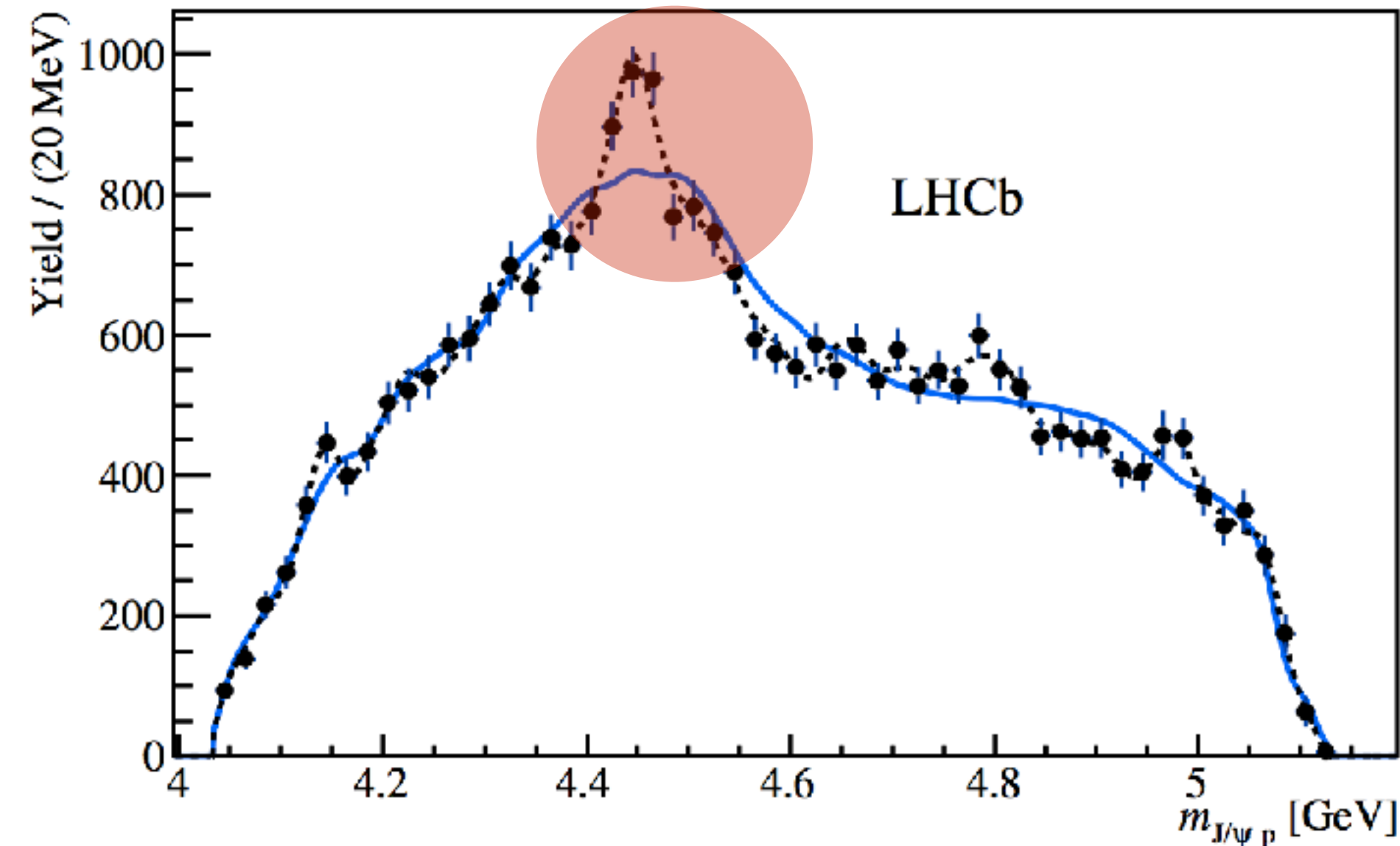
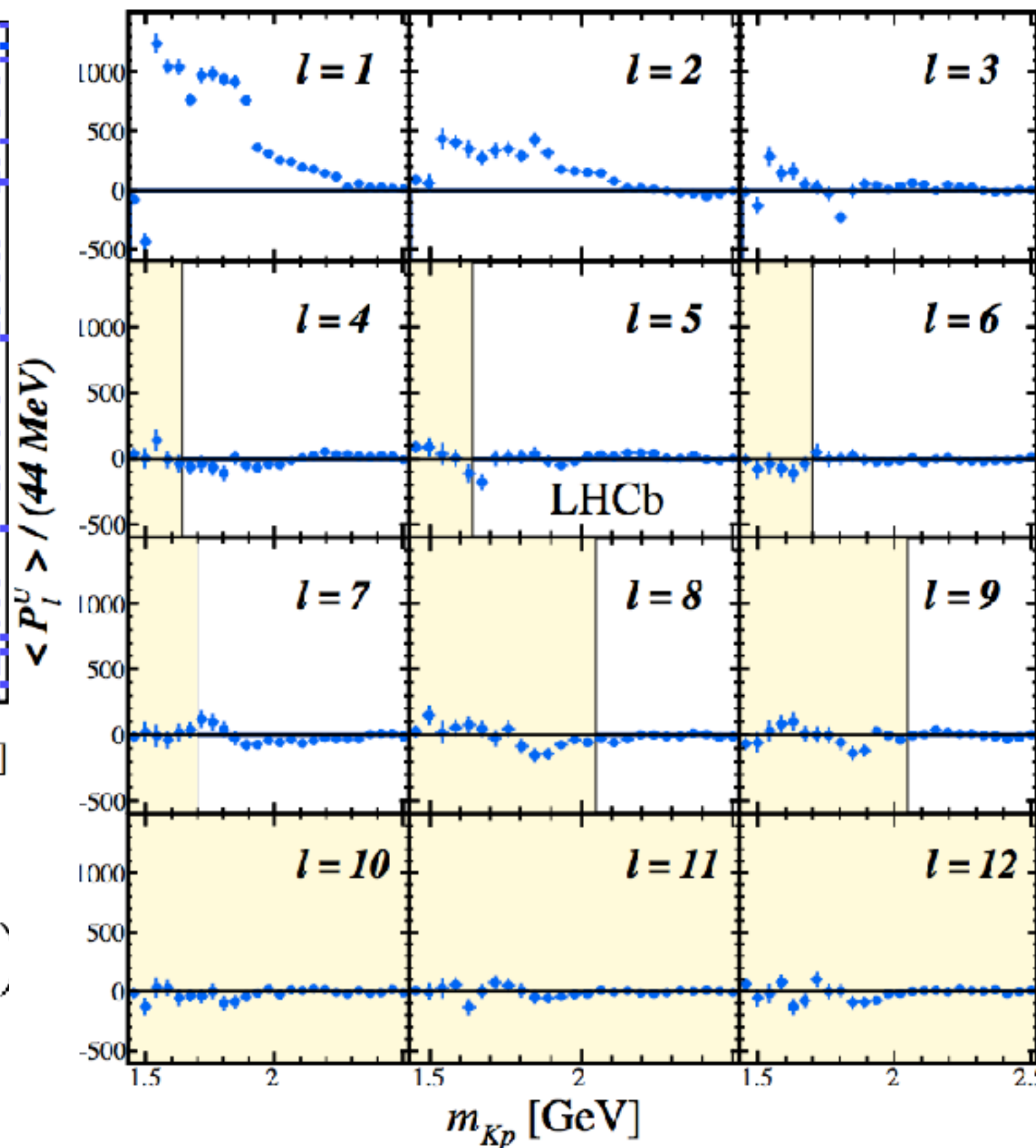
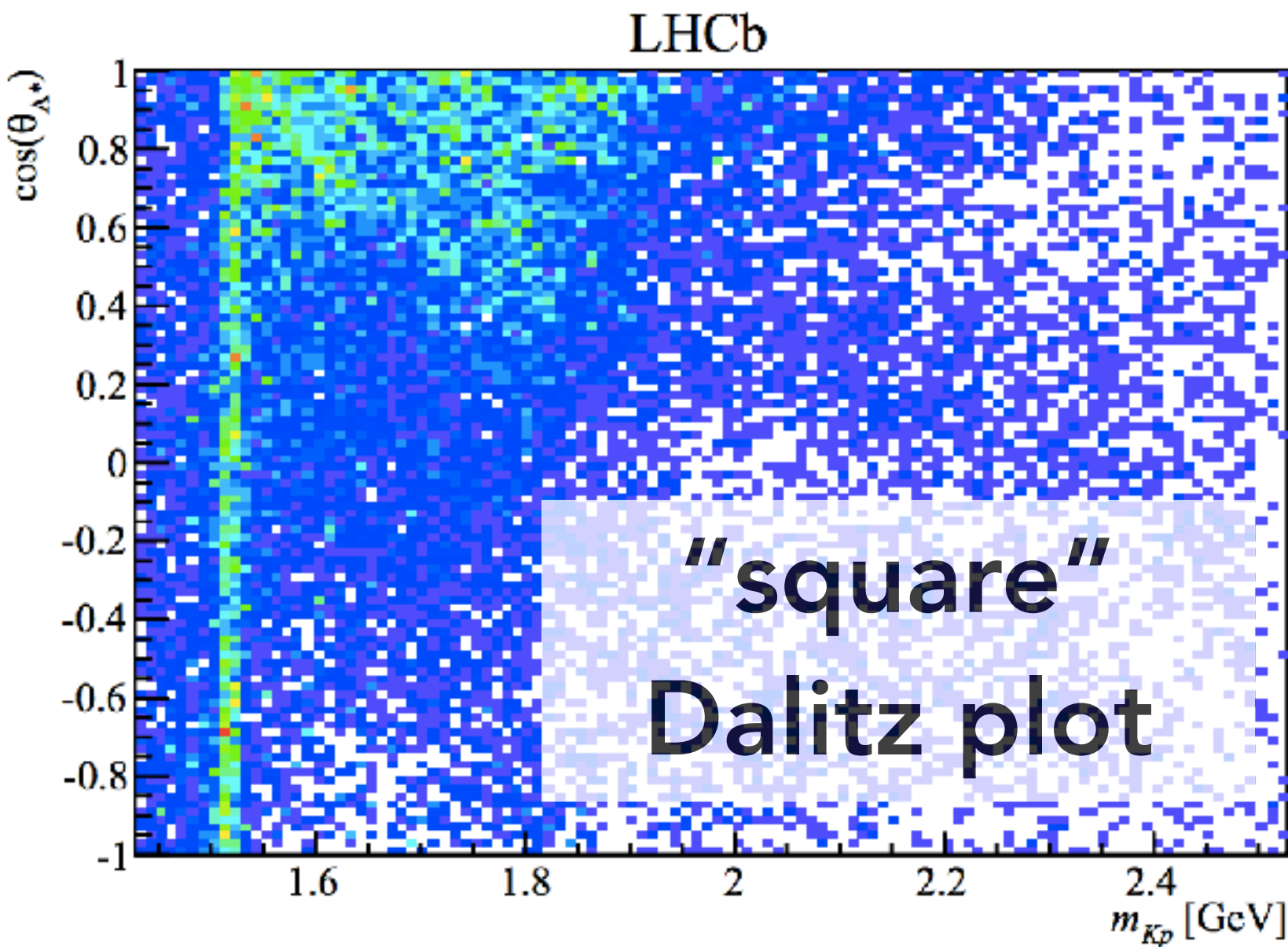
Model-independent approach: do not assume anything about Λ^* , Σ^* or NR composition, spin, masses, widths or mass-shape.

Only restrict the maximal spin of allowed Λ^* components at given $m(Kp)$.

Theory predictions for Λ^*
Well established Λ^* states



Pentaquark model-independent [PRL 117 (2016) 082002]



$$\frac{dN}{d \cos \theta_{\Lambda^*}} = \sum_{l=0}^{l_{\max}} \langle P_l^U \rangle P_l(\cos \theta_{\Lambda^*})$$

$$\langle P_l^U \rangle^k = \sum_{i=1}^{n_{\text{cand}}^k} (w_i / \epsilon_i) P_l(\cos \theta_{\Lambda^*}^i)$$

Maximal rank of the Legendre polynomial l_{\max} cannot be higher than $2J_{\max}$, where J_{\max} is twice the highest (Kp) spin which is present in the data at a given $m(Kp)$ value

filter out maximum spin for each $m(Kp)$

Null hypothesis (Λ^* only) rejected at 9σ

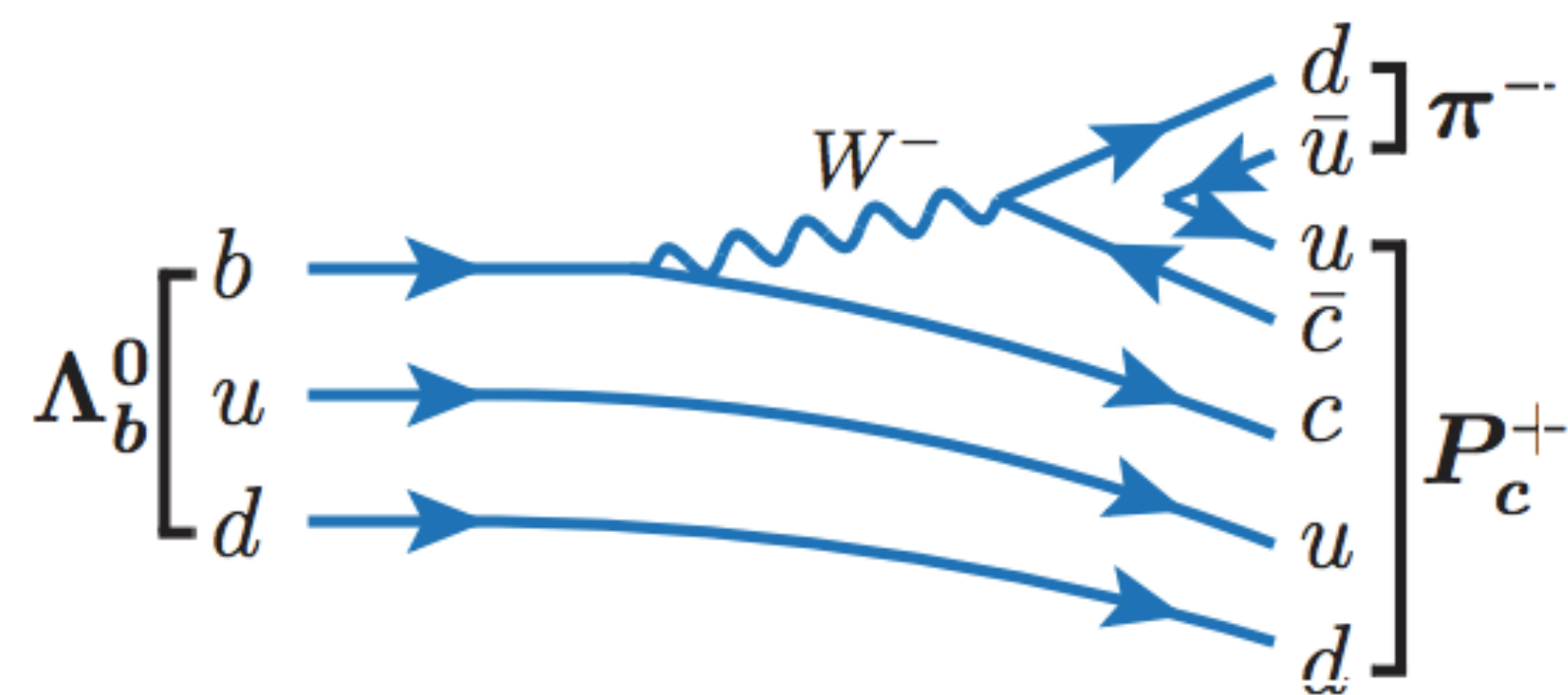
Working with JPAC to use better models of Λ^* resonances in future amplitude fits

Evidence for exotics in $\Lambda_b \rightarrow J/\psi p \pi^-$

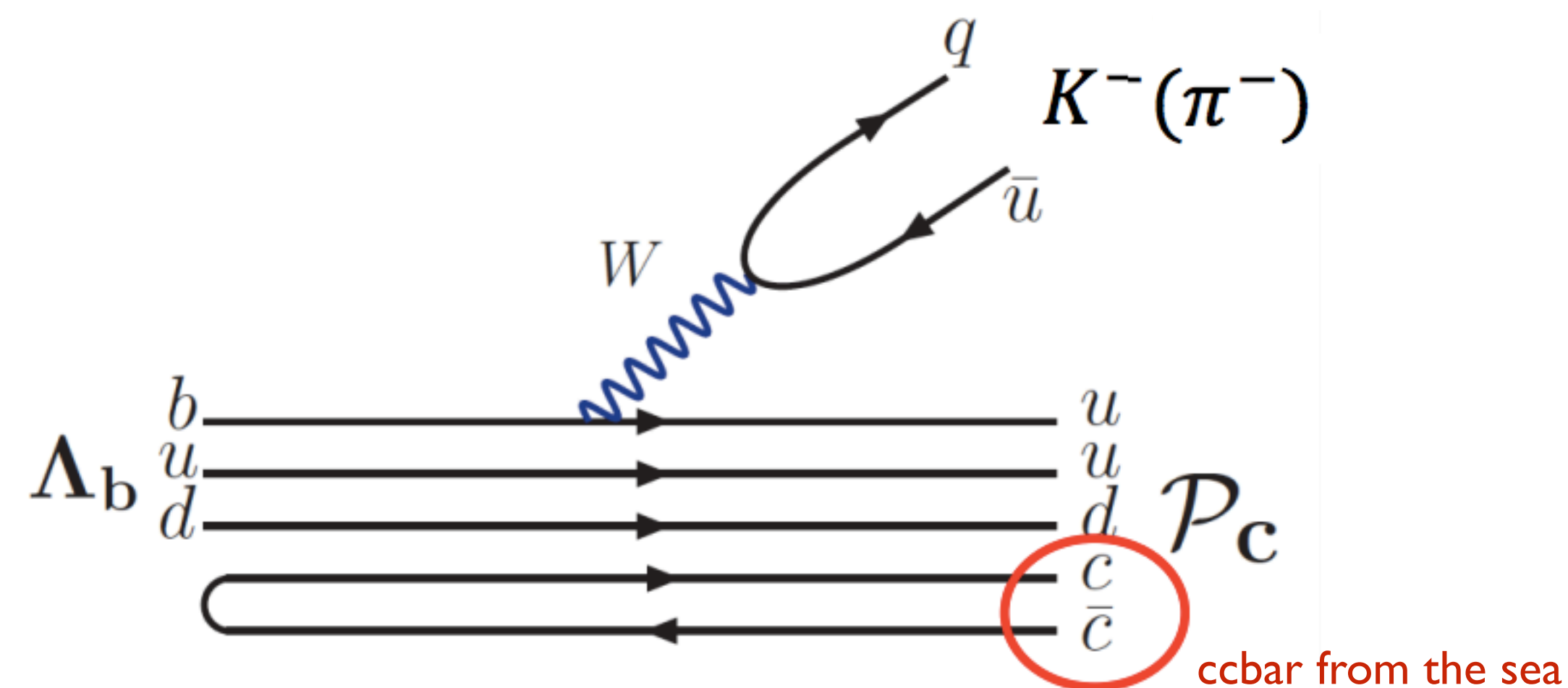
$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi p \pi^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi p K^-)} = 0.0824 \pm 0.0025 \text{ (stat)} \pm 0.0042 \text{ (syst)} \quad [\text{LHCb JHEP 1407, 103 (2014)}]$$

Observations of the P_c^+ states in another decay could imply they are genuine exotic baryonic states, other than kinematical effects, e.g. so-called triangle singularity. [arXiv:1512.01959]

$$R_{\pi^-/K^-} \equiv \frac{\mathcal{B}(\Lambda_b^0 \rightarrow \pi^- P_c^+)}{\mathcal{B}(\Lambda_b^0 \rightarrow K^- P_c^+)} \approx 0.07 - 0.08$$

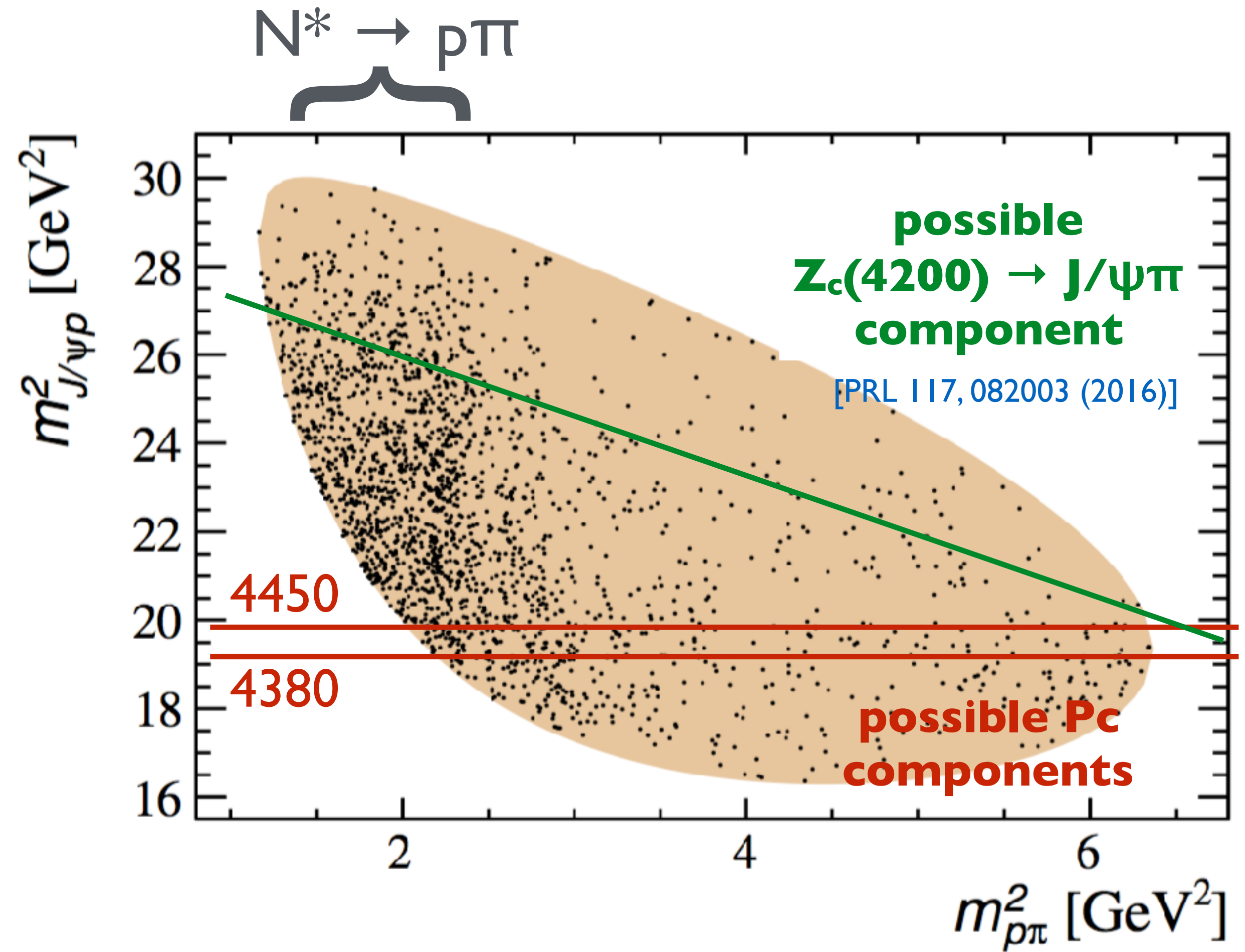
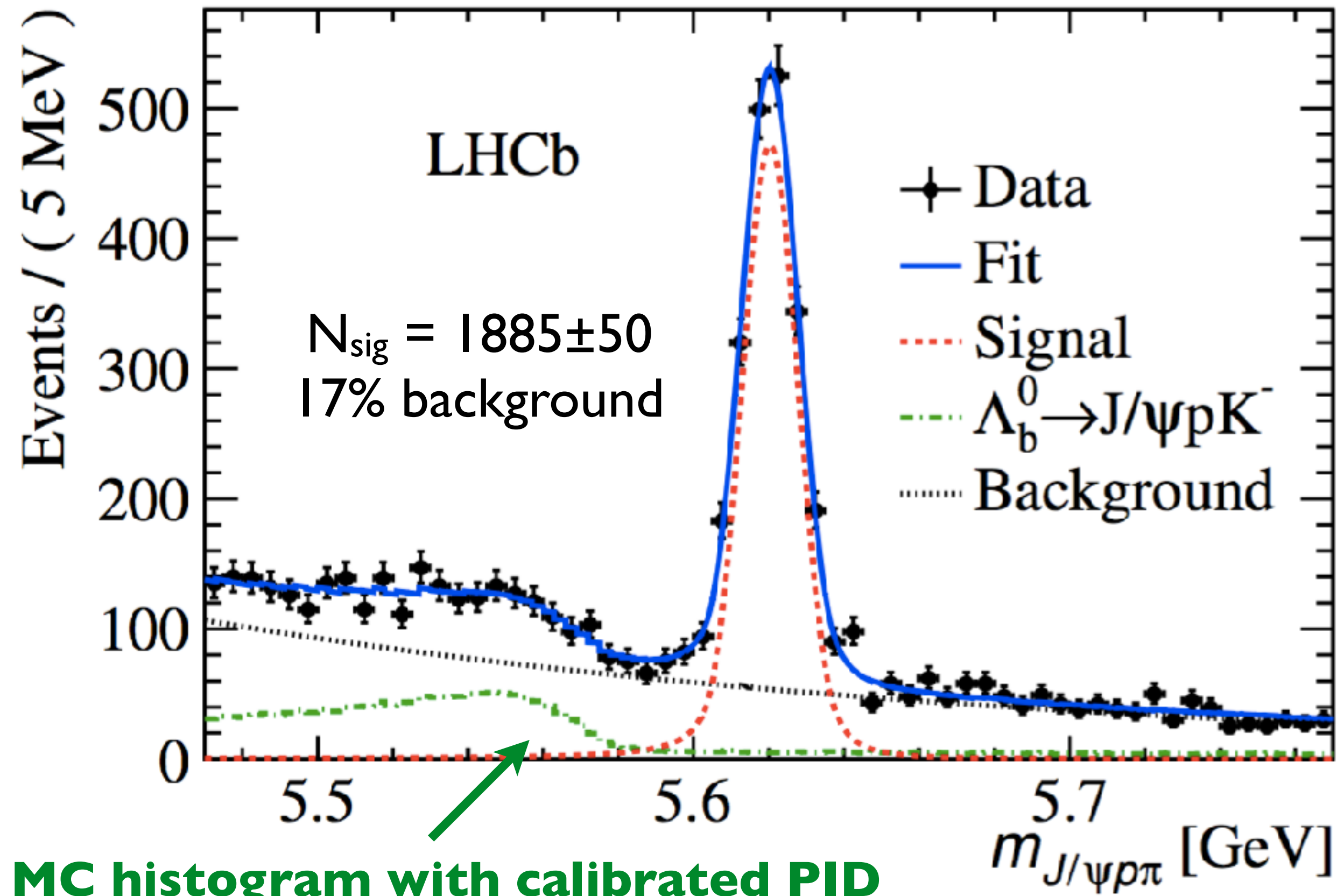


$$R_{\pi^-/K^-} = 0.58 \pm 0.05$$



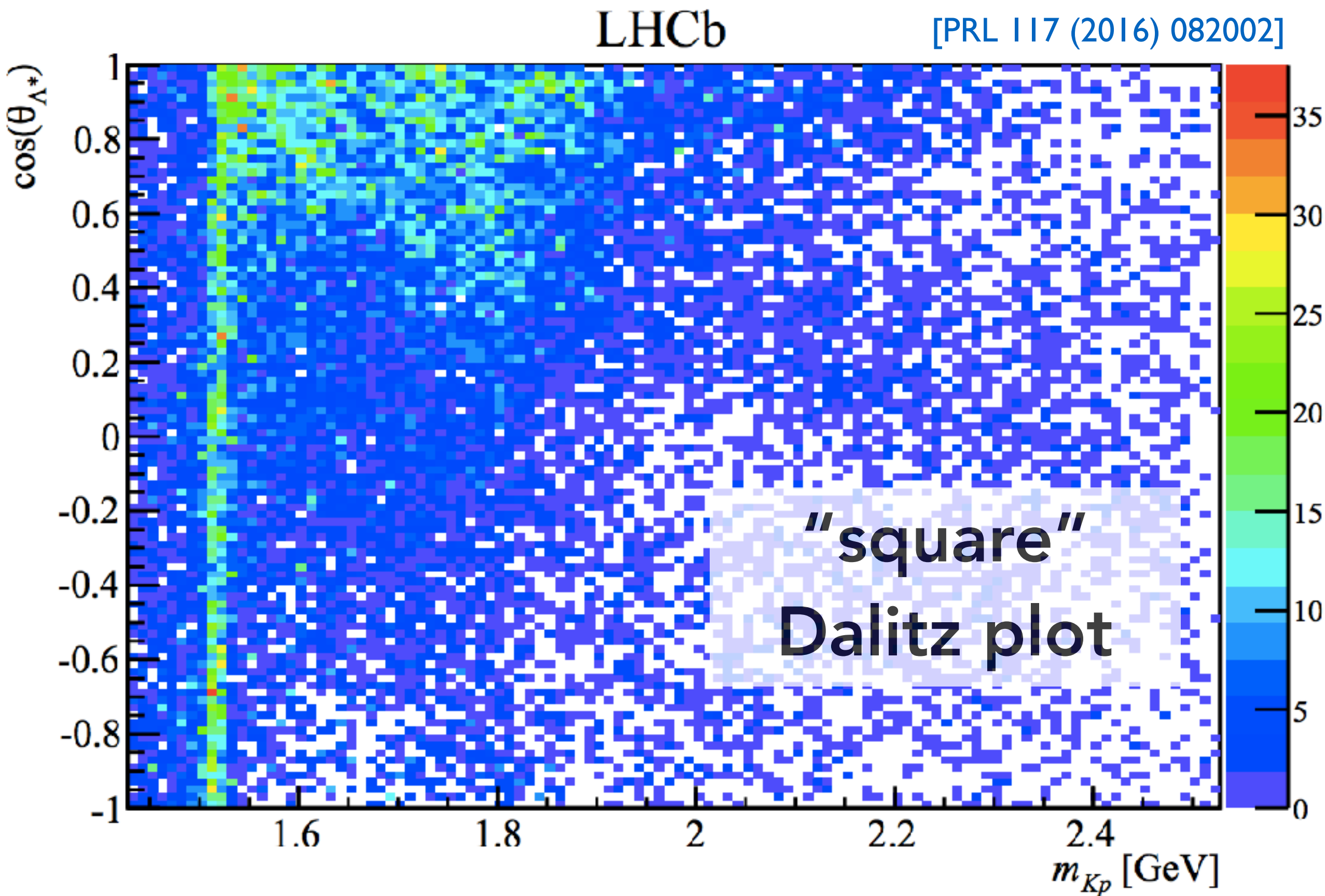
$\Lambda_b \rightarrow J/\psi p \pi^-$ pentaquark search

[PRL 117, 082003 (2016)]



No prominent pentaquark-like peaks

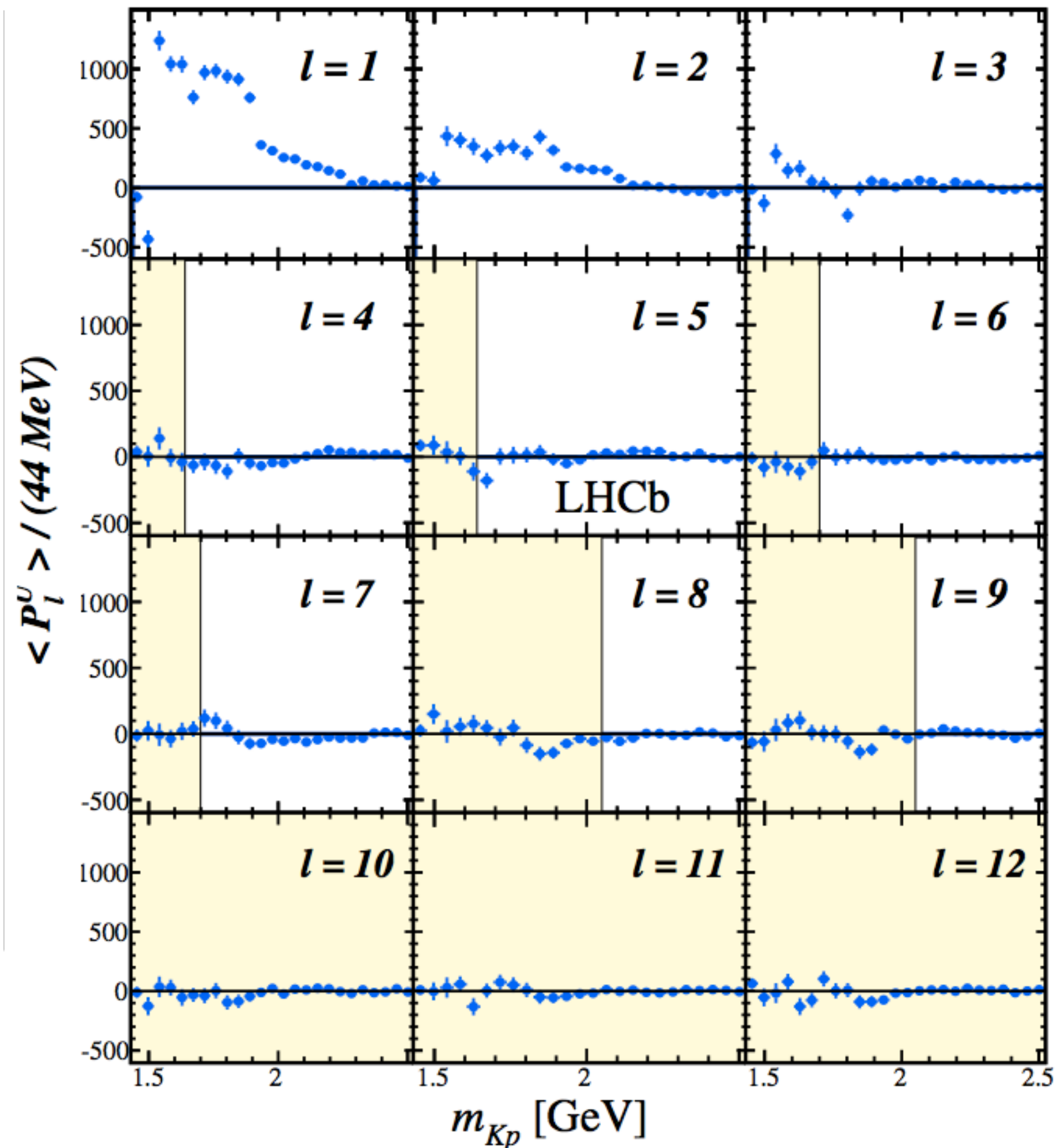
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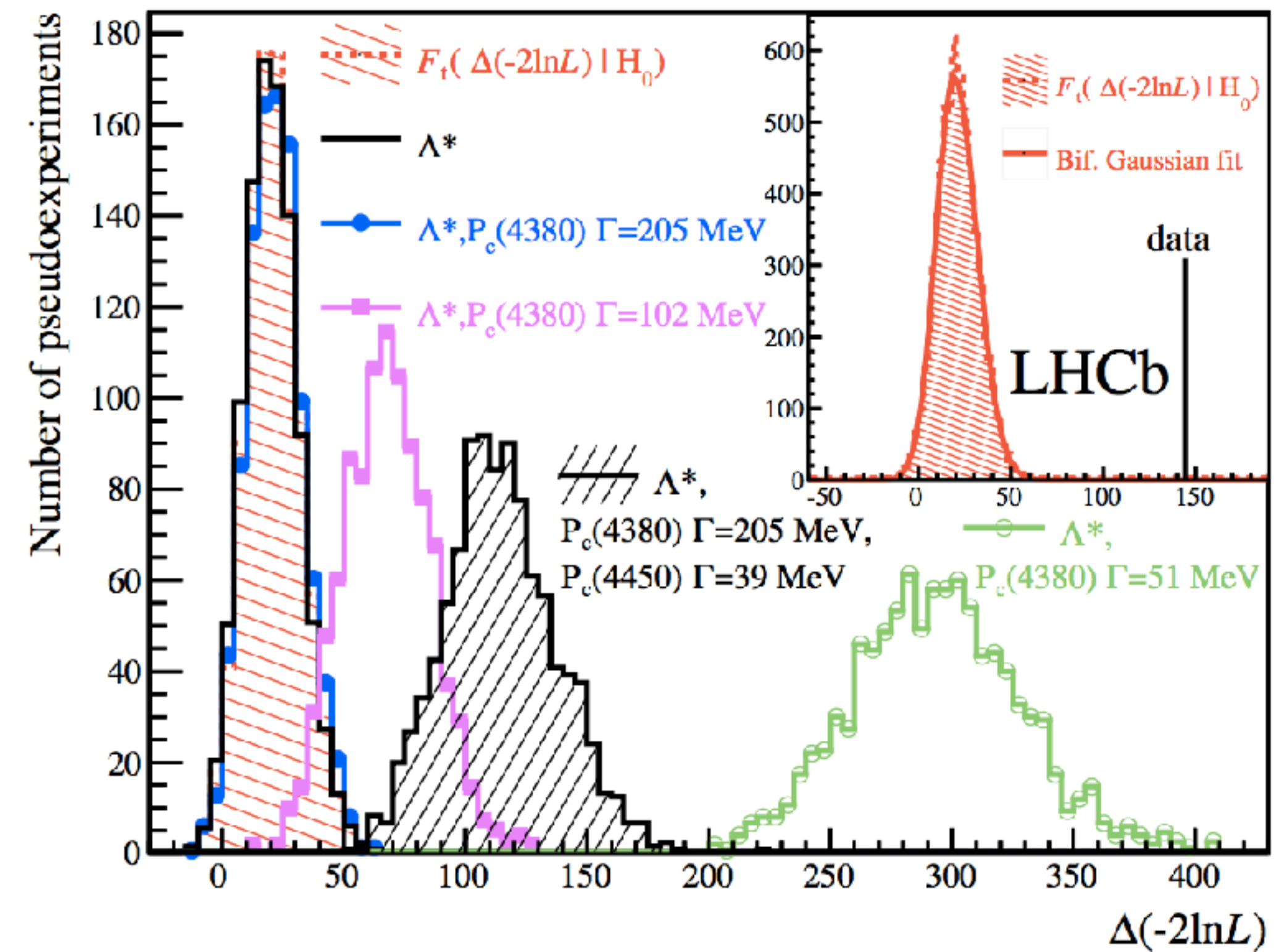
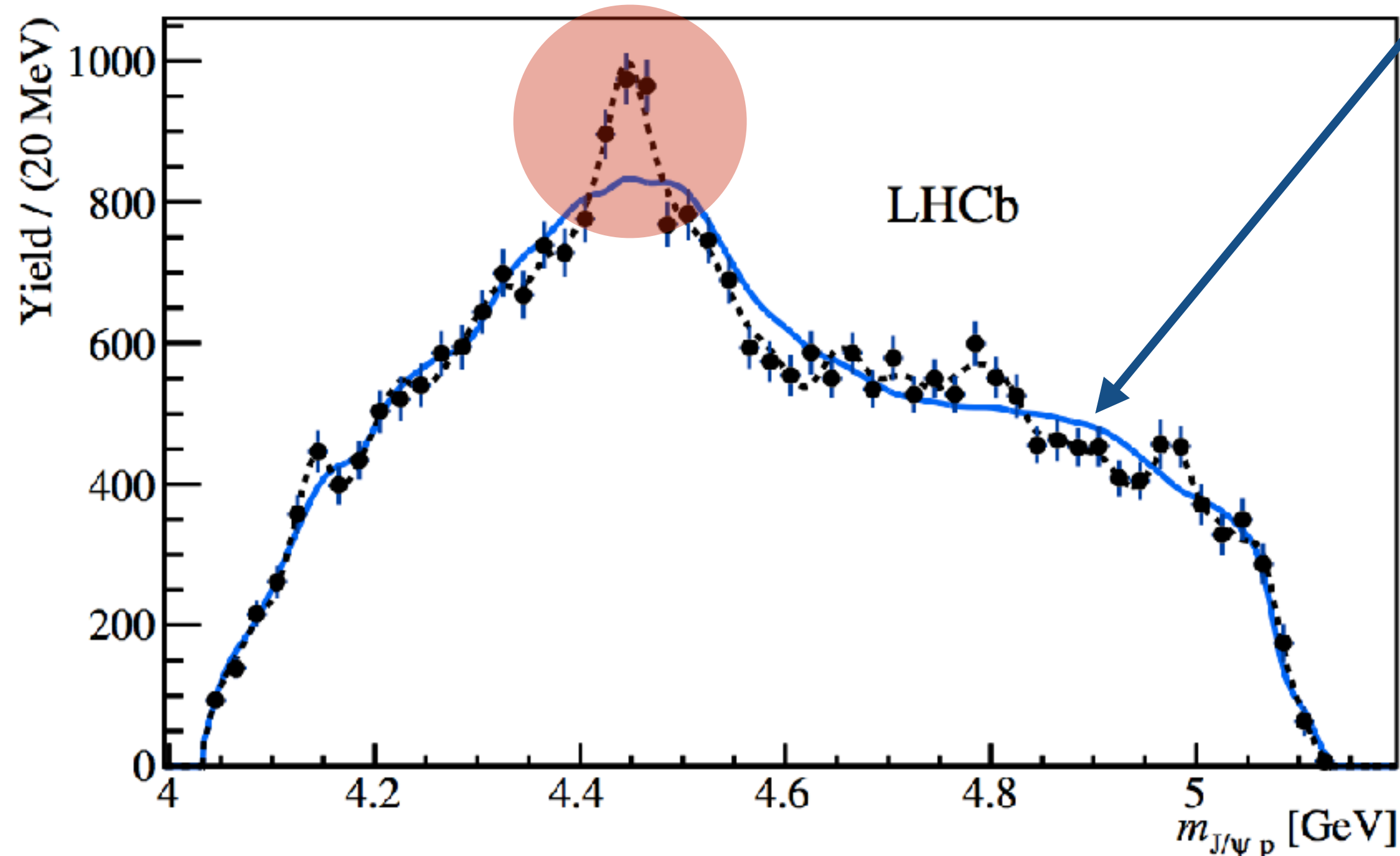
Simulate phase-space decays of $\Lambda_b^0 \rightarrow J/\psi p K^-$

[PRL 117 (2016) 082002]

Weight according to $m(Kp)$ and the moments (with l_{max} -filter applied)

Look at reflections of the pK system into the $J/\psi p$ system \rightarrow **pK reflections cannot explain narrow structure!**

Use likelihood ratio to test various hypotheses - **Null hypothesis (Λ^* only)** rejected at **9σ**



For the future: $B_s^0 \rightarrow J/\psi \phi \phi$

Possible threshold effects in $B_s^0 \rightarrow J/\psi \phi \phi$ and other modes [\[Swanson PRD 91 \(2015\) 034009\]](#)

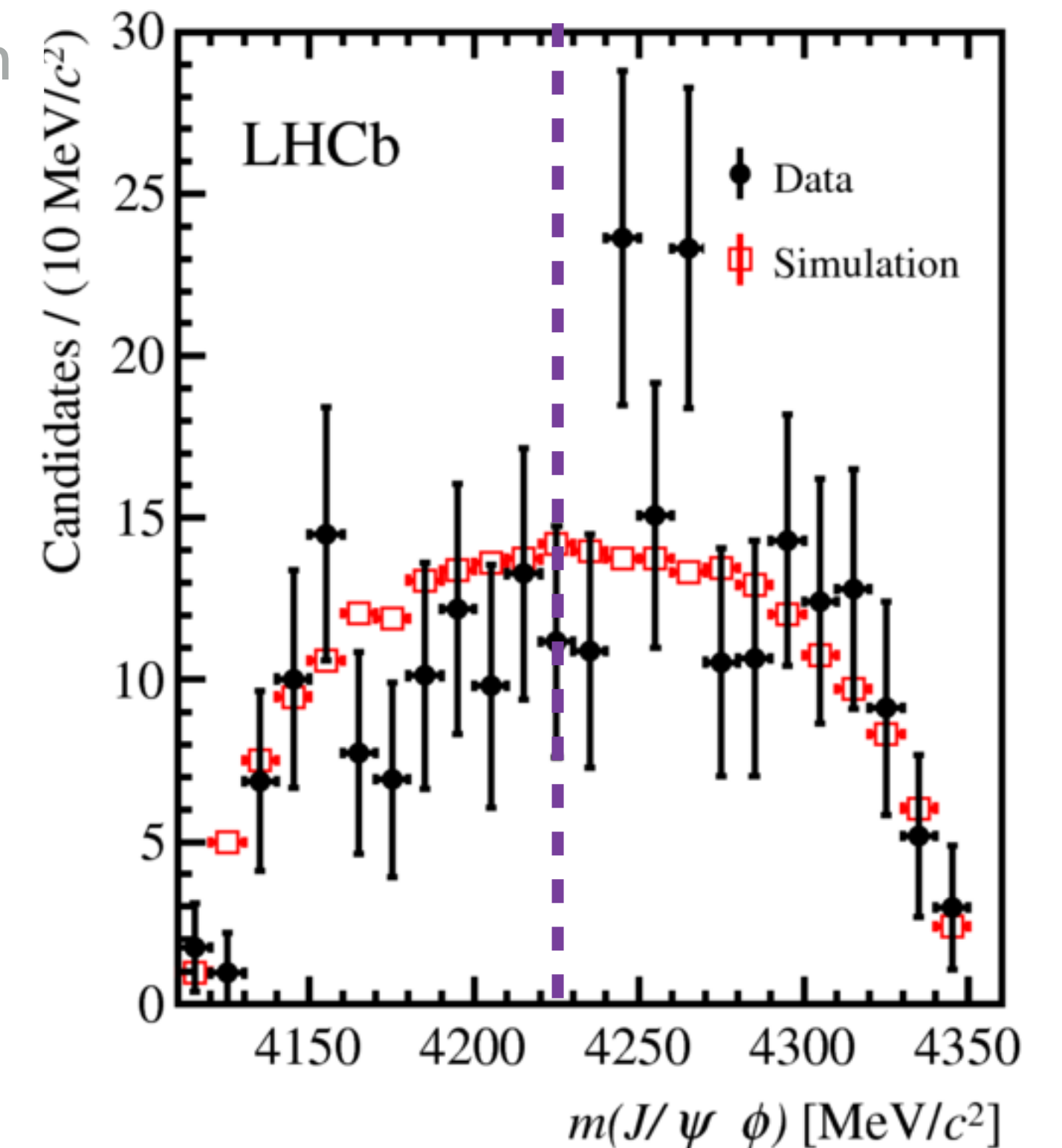
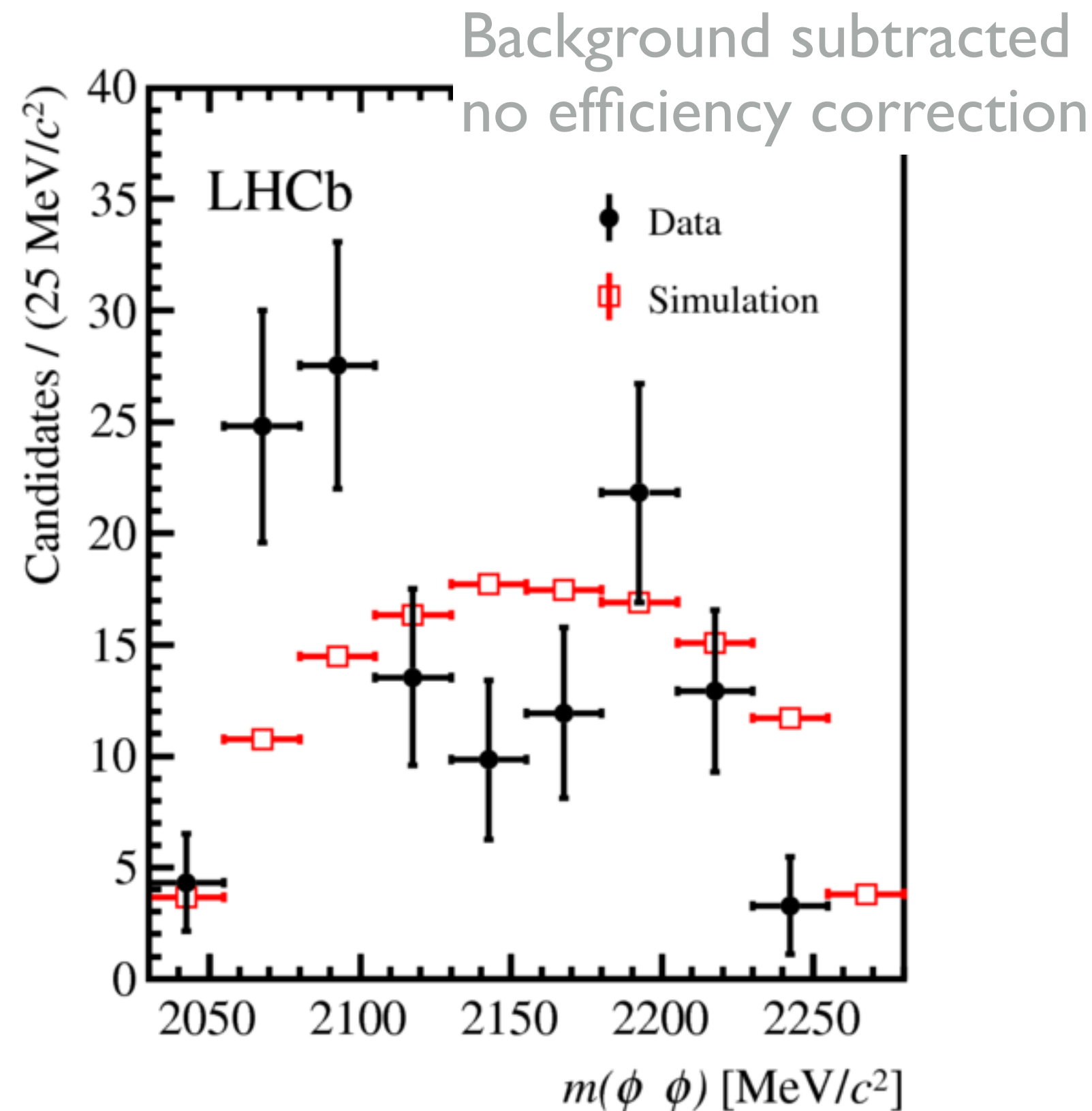
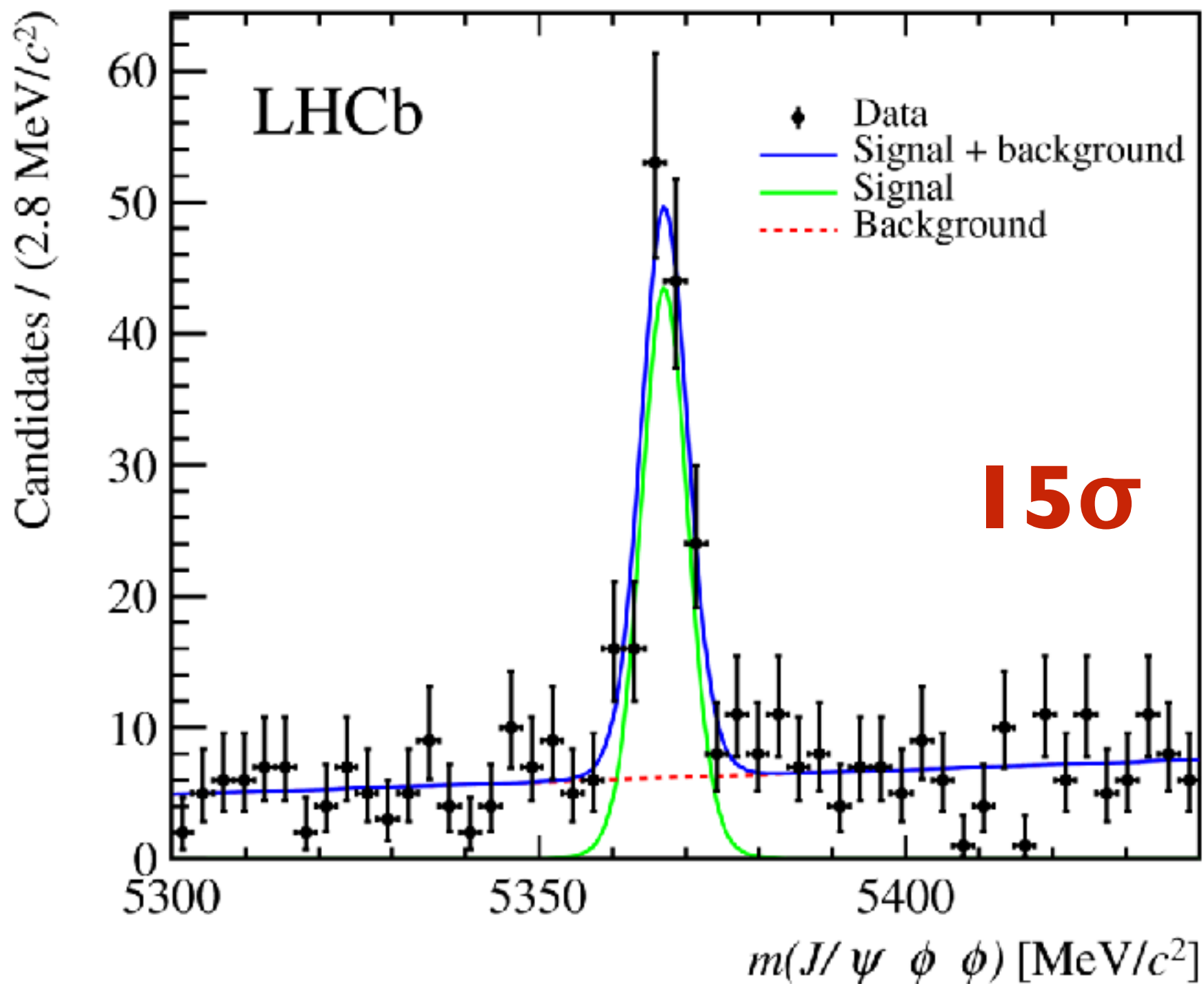
Simplified phase-space simulation inadequate to describe structure

Looking forward to more data in Run-2 of LHCb

Contamination from non-res decays

$$\frac{B(B_s^0 \rightarrow J/\psi \phi \phi)}{B(B_s^0 \rightarrow J/\psi \phi)} = 0.0115 \pm 0.0012^{+0.0005}_{-0.0009}$$

$D_s^* D_s^*$



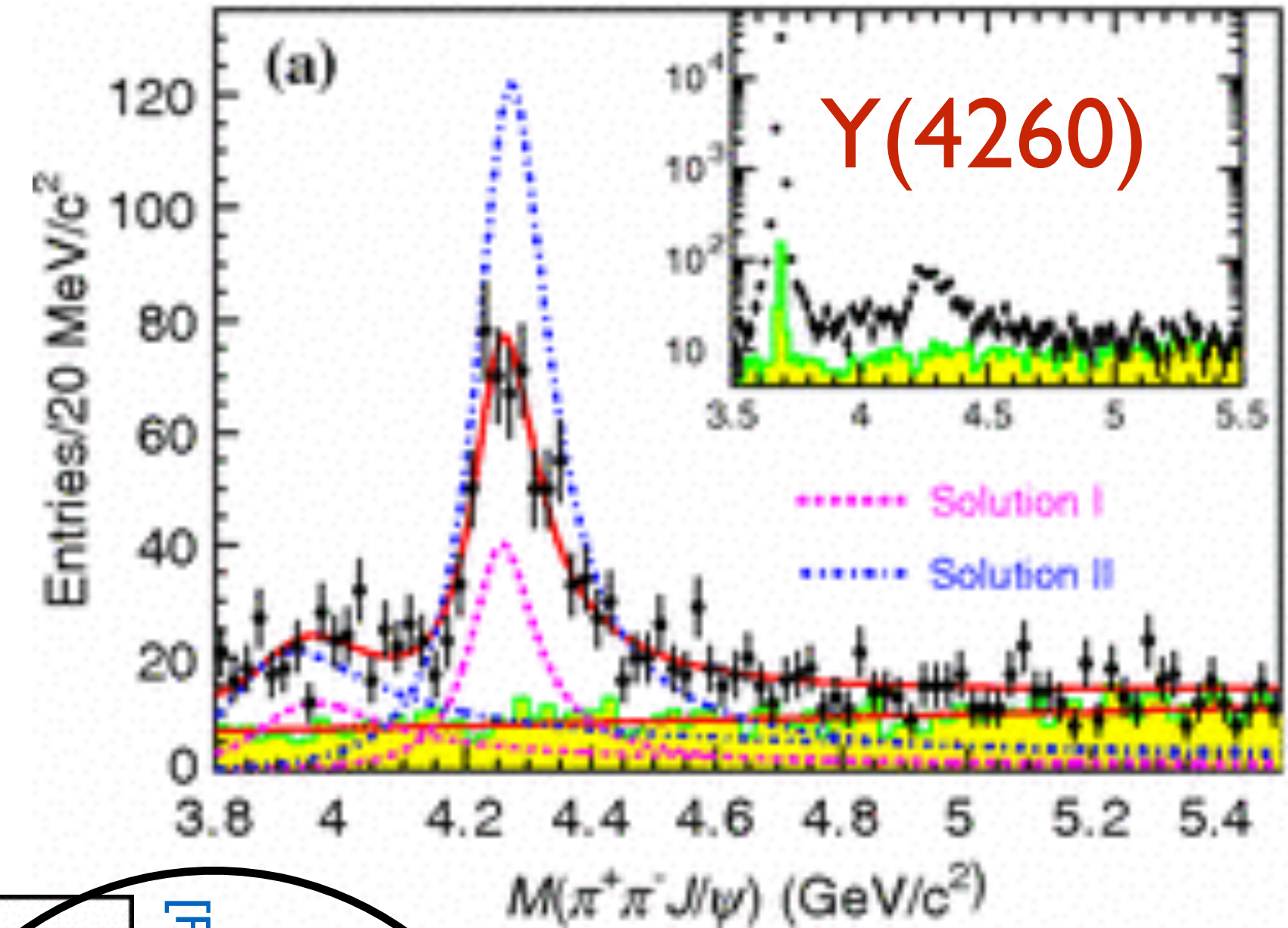
$Z_c(3900)^\pm$ in $e^+e^- \rightarrow Y(4260) \rightarrow \pi^+\pi^-J/\psi$

Observation of another possible **exotic charged state**.

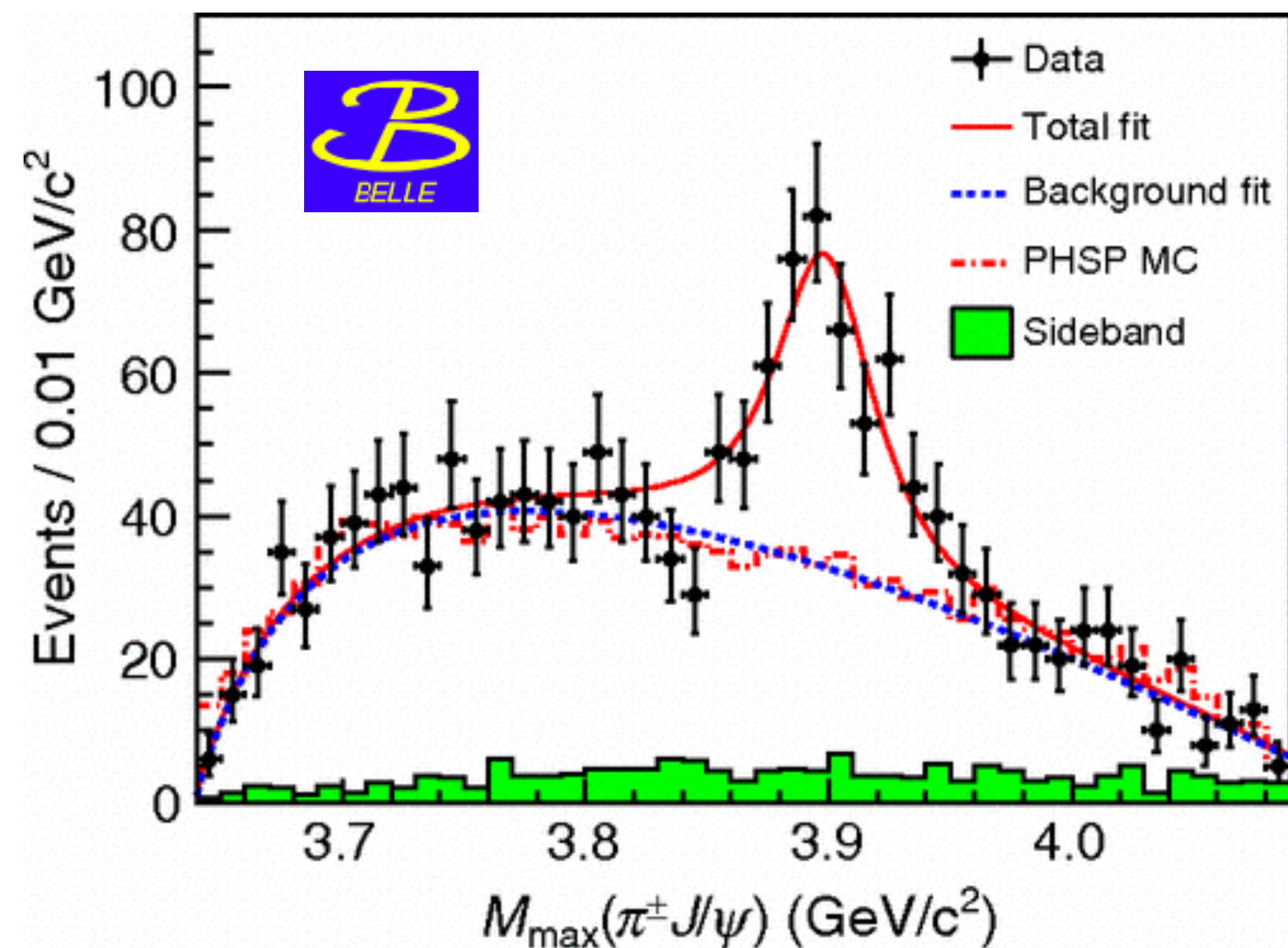
Is $Z(4430)^\pm$ a radial excitation of $Z_c(3900)^\pm$? [Maiani et al, NJP 10 (2008) 073004]
[Wang, arXiv:1405.3581]
[Agaev et al, arXiv:1706.01216]

CLEO-c and BES-III have evidence/observation for neutral member of **isospin triplet** decaying to π^0J/ψ . [PLB 727 (2013) 366] [PRL 115 (2015) 112003]

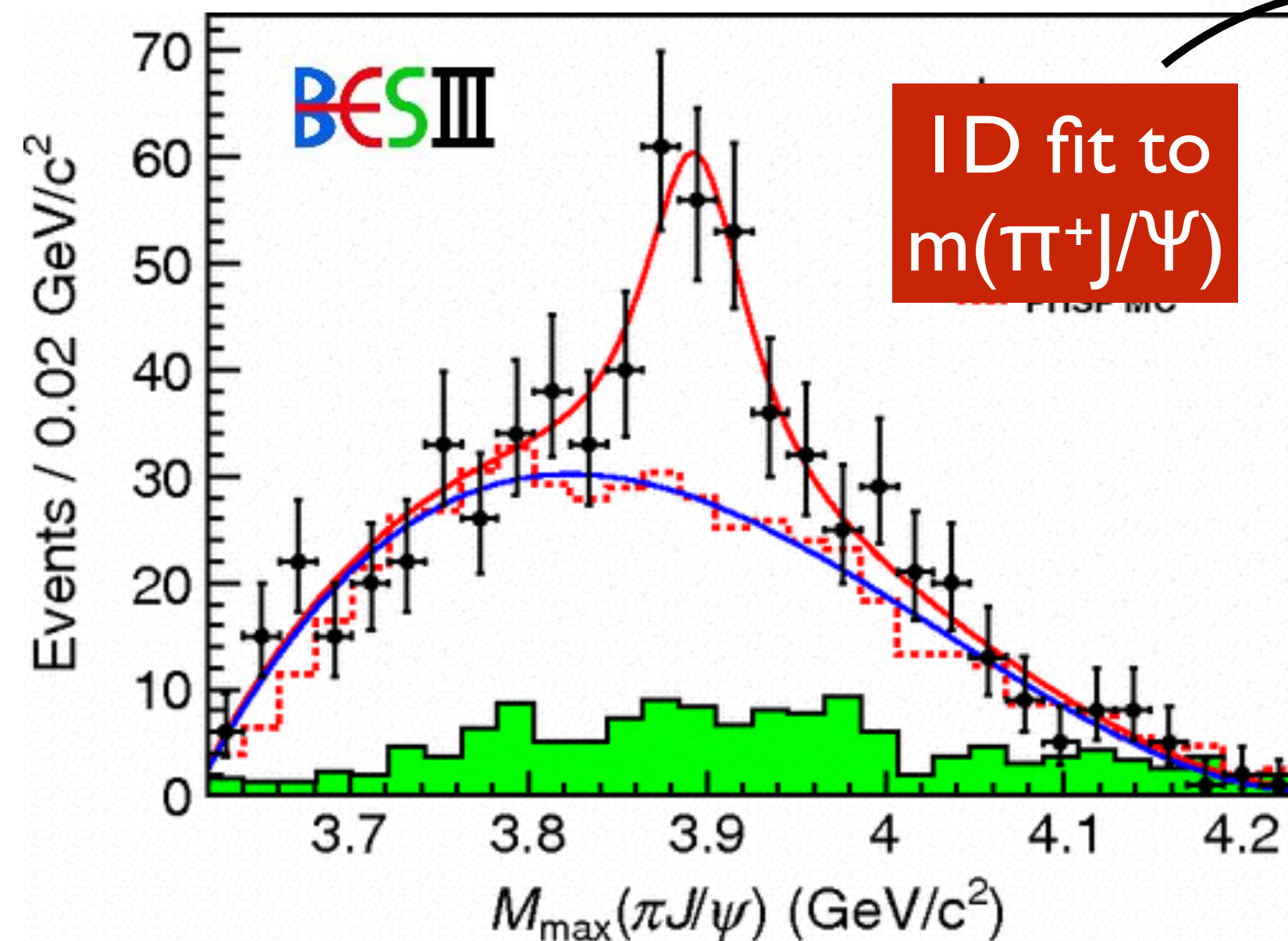
Also appears in $D^\pm D^*$ decay mode ($Z_c(3885)^\pm$)



[PRL 110 (2013) 252002]



[PRL 110 (2013) 252001]



[PRL 110 (2013) 252002]

Brand-new amplitude analysis
[PRL 119, 072001 (2017)]

$$M = (3894.5 \pm 6.6 \pm 4.5) \text{ MeV}/c^2$$

$$\Gamma = (63 \pm 24 \pm 26) \text{ MeV}$$

Understanding the $Z_c(3900)^\pm$

Some lattice QCD calculations do not support existence of $Z_c(3900)^\pm$

[Prelovsek et al PRD 91 (2015) 014504]

No sign of $Z_c(3900)^\pm \rightarrow J/\psi \pi^\pm$ in B decays or photo-production ($\gamma p \rightarrow J/\psi \pi^\pm n$) [COMPASS, PLB 742, 330 (2015)]

Indicates that $Z_c(3900)^\pm$ (and $Z_c(4020)^\pm$) may not be dynamical in nature but some kinematic effect (e.g., threshold cusp)?

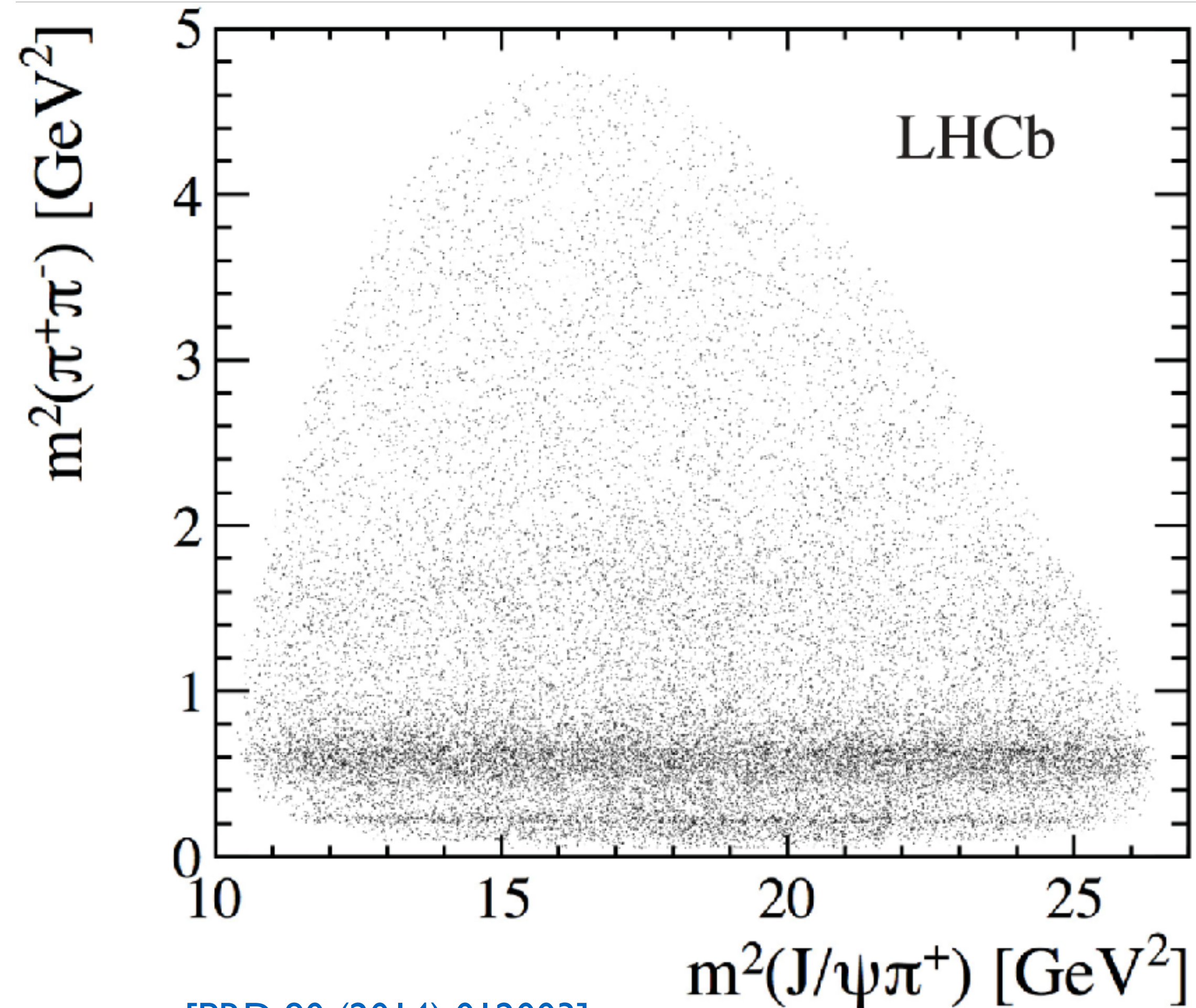
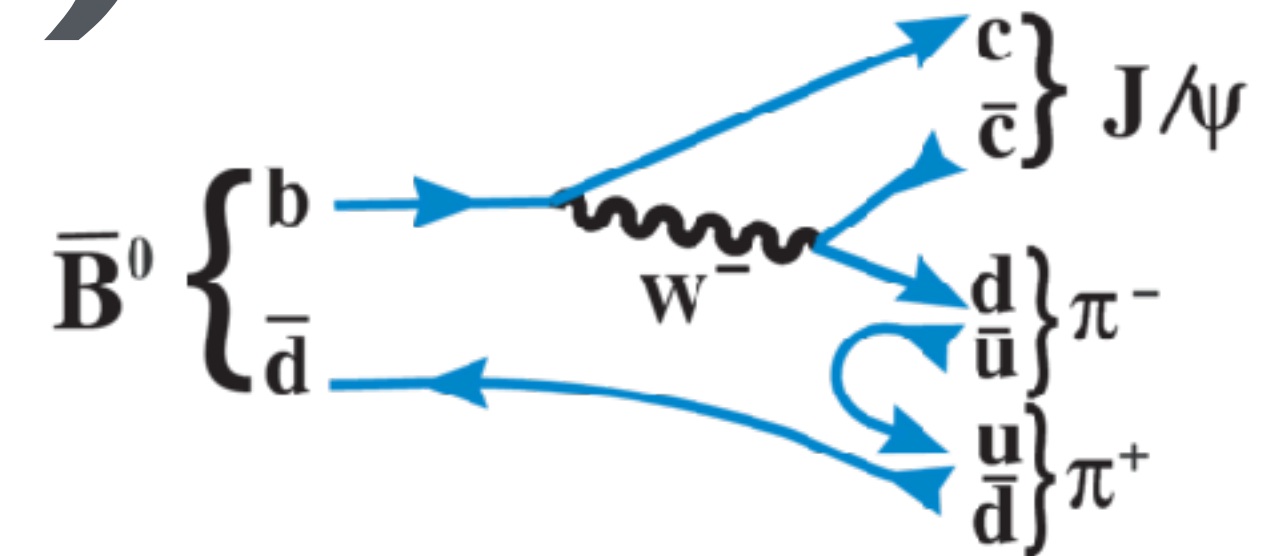
[Swanson PRD 91 (2015) 034009]

[Ikeda et al arXiv:1602.03465]

[Szczepaniak PLB 747 (2015) 410]

Or maybe not?

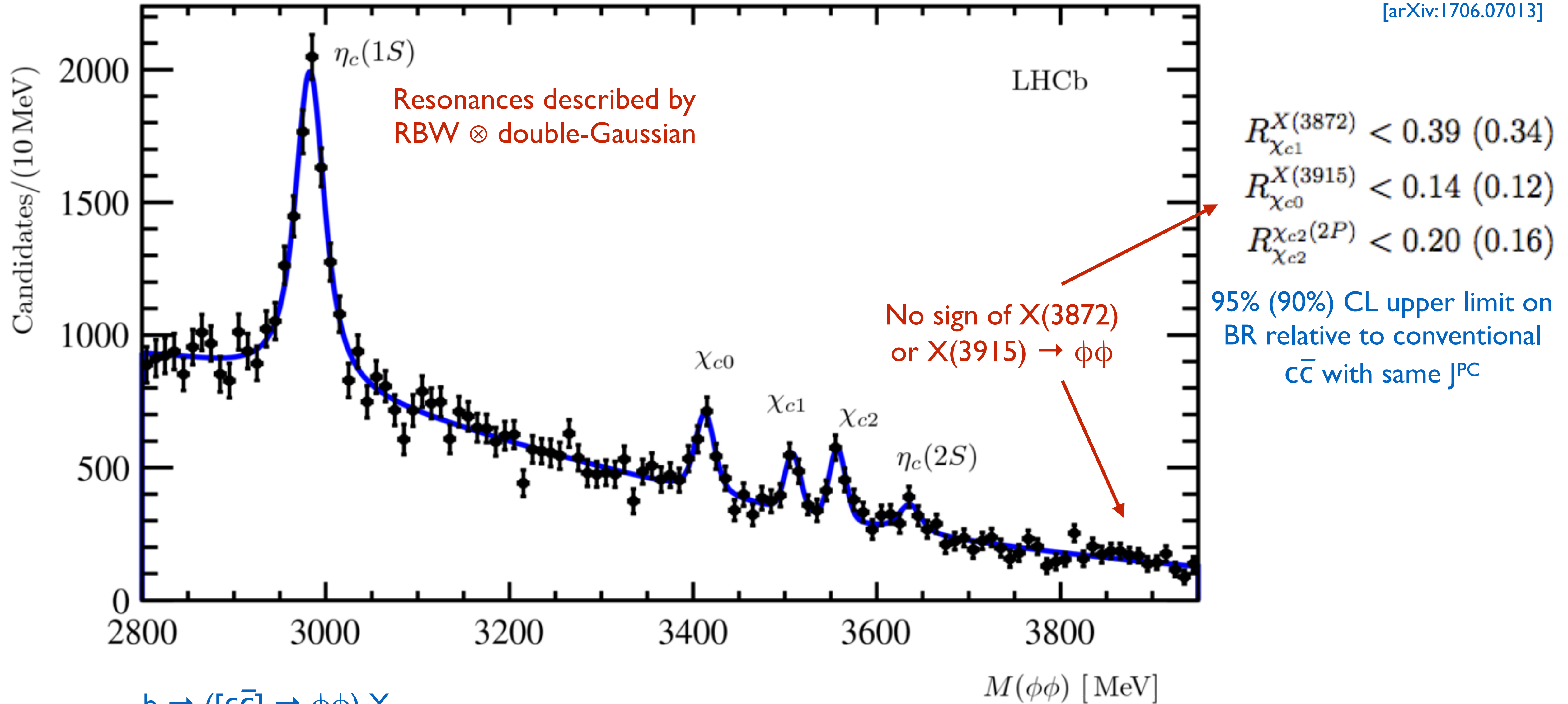
[Cleven et al arXiv:1510.00854]



[PRD 90 (2014) 012003]

Charmonium production in b-hadron decays

[arXiv:1706.07013]



$b \rightarrow ([c\bar{c}] \rightarrow \phi\phi) X$
 by requiring separation between primary and secondary vertices

Future X(3872) measurements

Charged partners of X(3872) predicted by some tetraquark models [Maiani et al]

Partners not observed in B decays and limits below what would be expected for isospin conservation \rightarrow X(3872) is iso-singlet?

Alternatively, the partners may be **broad** due to presence of thresholds, so may have evaded detection \rightarrow **amplitude analysis**

Make more precise width and mass measurement

[Belle PRD 84 (2011) 052004]
[BaBar PRD 71 (2005) 031501]

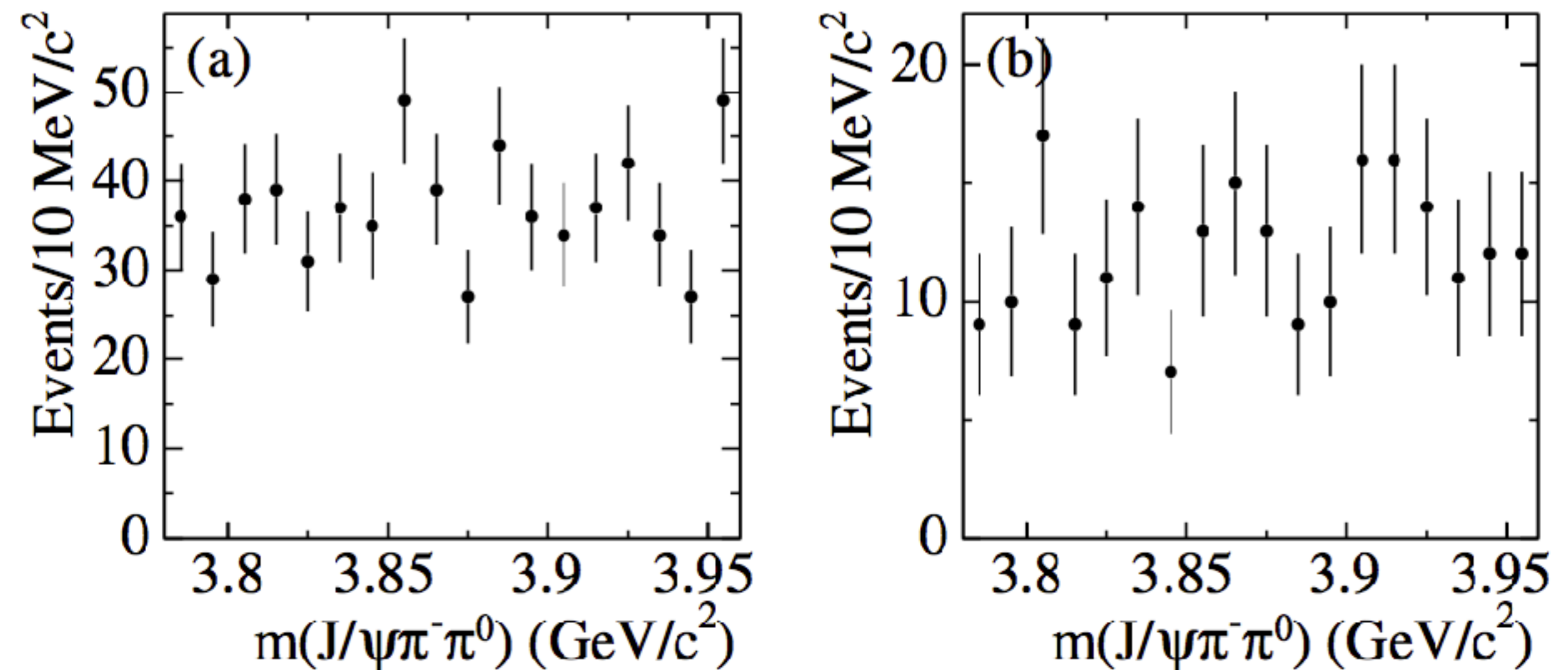


FIG. 3. The $J/\psi\pi^-\pi^0$ invariant mass in $10 \text{ MeV}/c^2$ bins for (a) $B^0 \rightarrow J/\psi\pi^-\pi^0 K^+$ and (b) for $B^- \rightarrow J/\psi\pi^-\pi^0 K_S^0$. No indication for the decay $X^- \rightarrow J/\psi\pi^-\pi^0$ can be found.

$$\mathcal{B}(\bar{B}^0 \rightarrow K^- X^+) \times \mathcal{B}(X^+ \rightarrow \rho^+ J/\psi) < 4.2 \times 10^{-6},$$

$$\mathcal{B}(B^+ \rightarrow K^0 X^+) \times \mathcal{B}(X^+ \rightarrow \rho^+ J/\psi) < 6.1 \times 10^{-6},$$

Z(4430) interpretations

Result confirms existence of the Z(4430), measures $J^P = 1^+$ and, for the first time, demonstrates **resonant behaviour**.

Mass close to DD^* thresholds - perhaps this is the organising principle of these exotic states?

Large width - unlikely to be molecule?

$P=+$ rules out interpretation in terms of $\bar{D}^*(2010)D^*(2420)$ molecule or threshold effect (cusp).

[Rosner, PRD 76 (2007) 114002] [Bugg, J. Phys. G35 (2008) 075005]

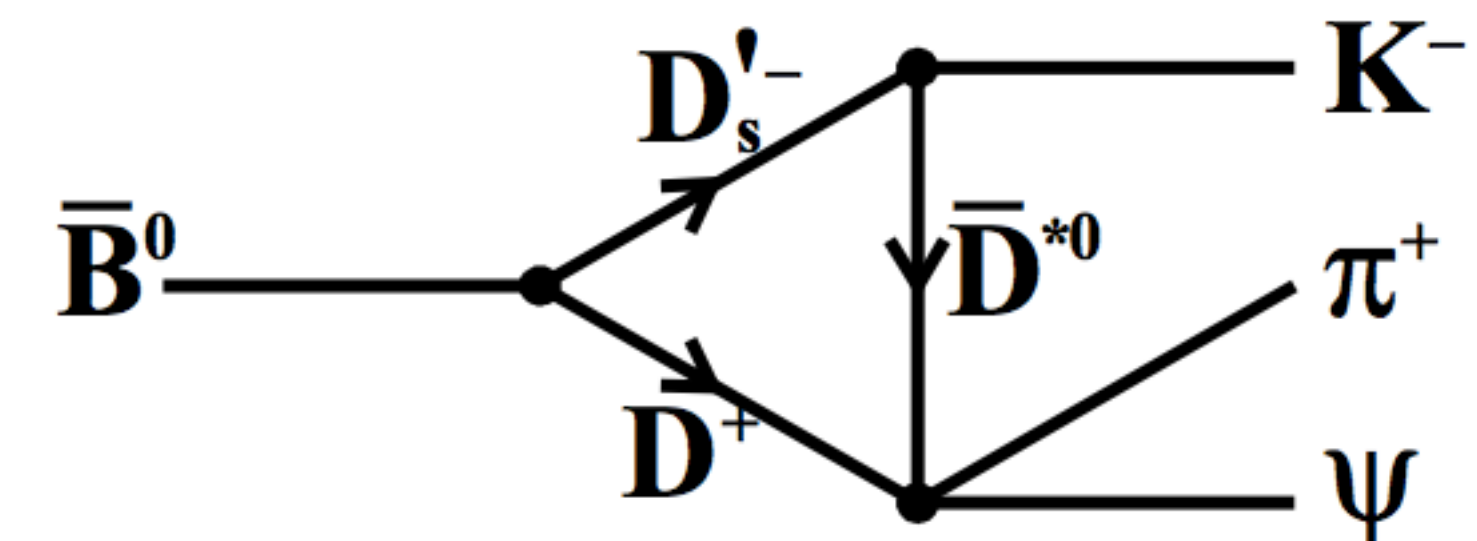
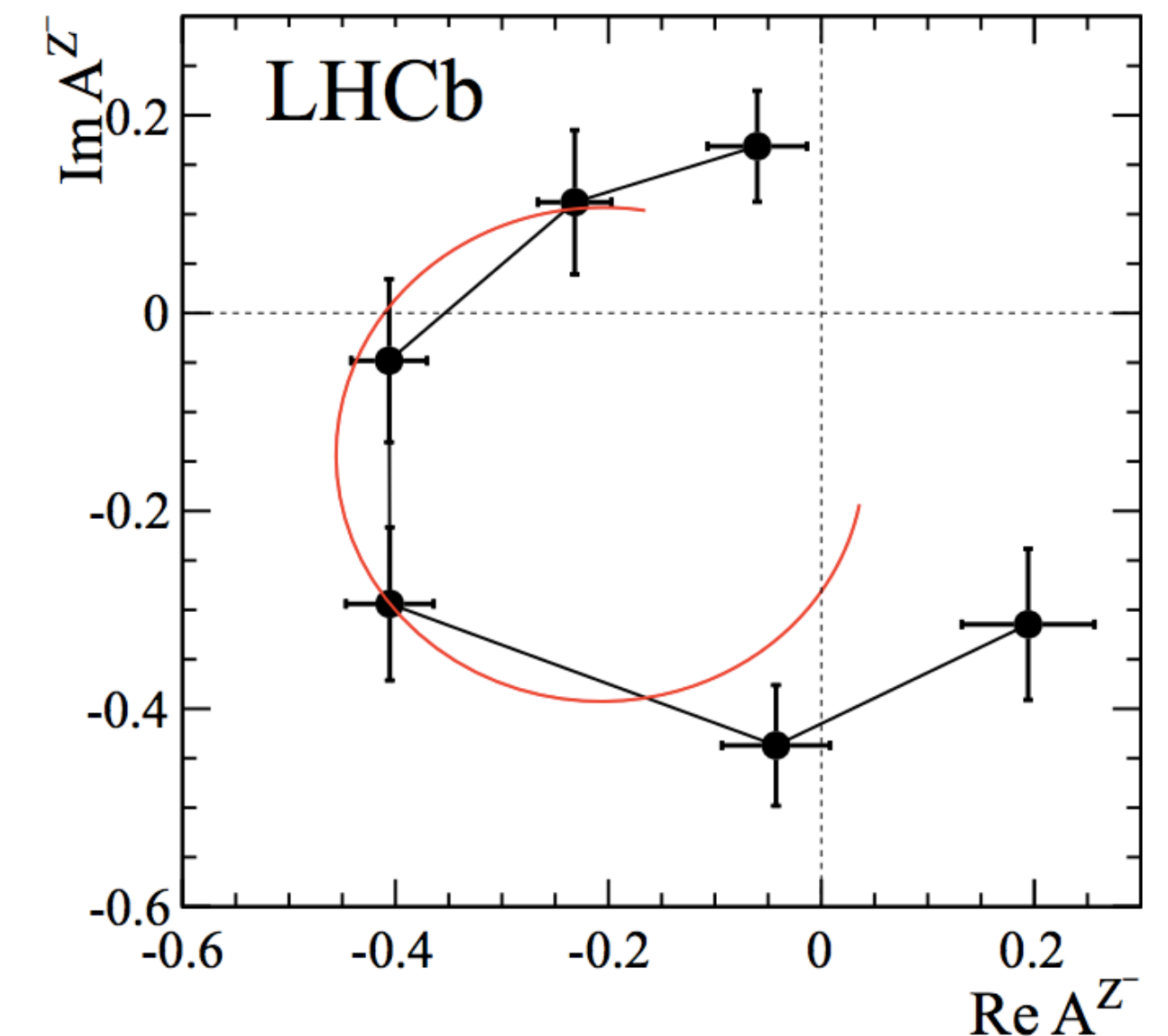
Rescattering effect proposed, but phase motion in wrong direction?

[Pakhov, Ugllov PLB748 (2015) 183]

Diquark-antidiquark bound state is an explanation. [Maiani et al, PRD 89 114010]

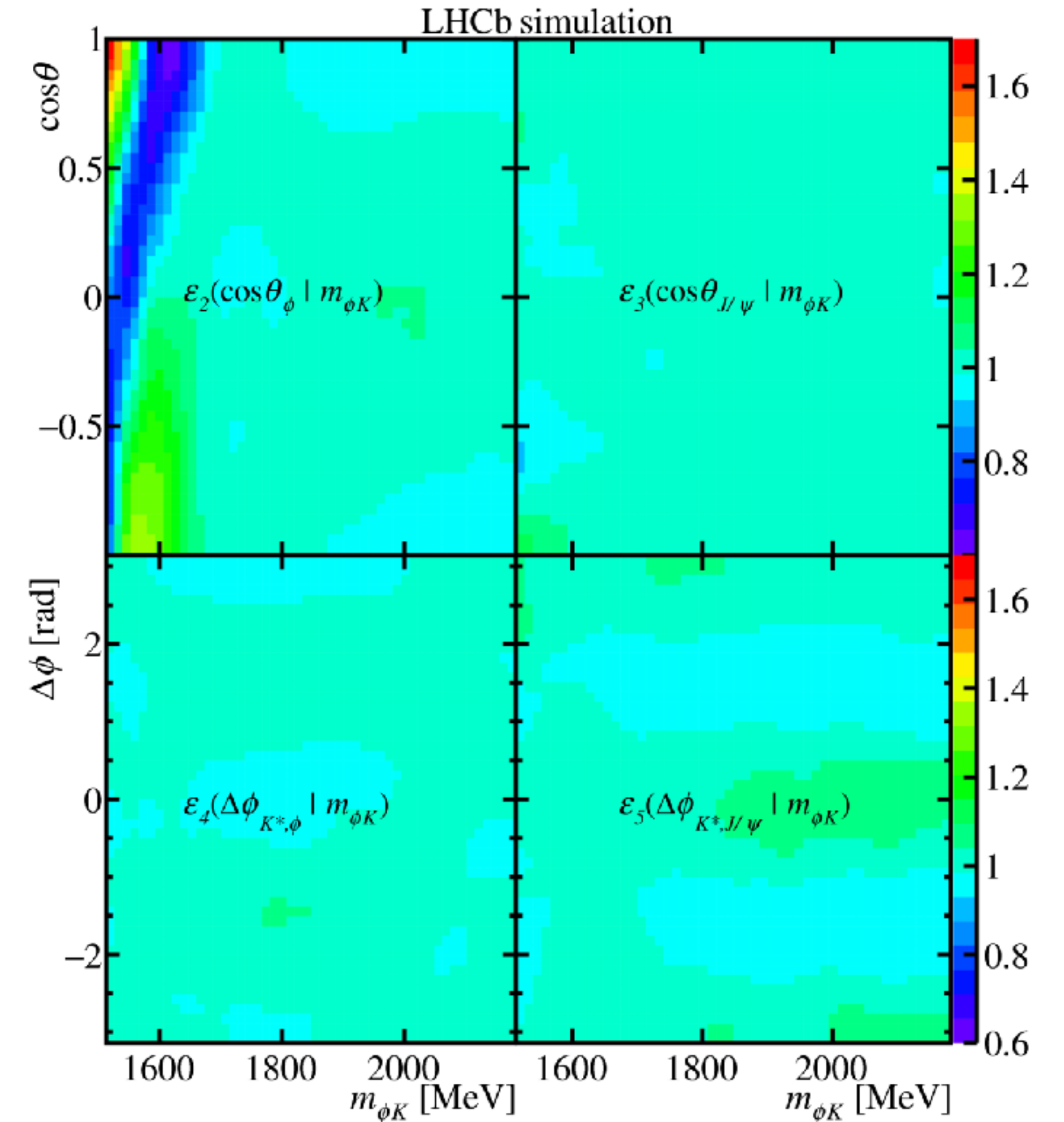
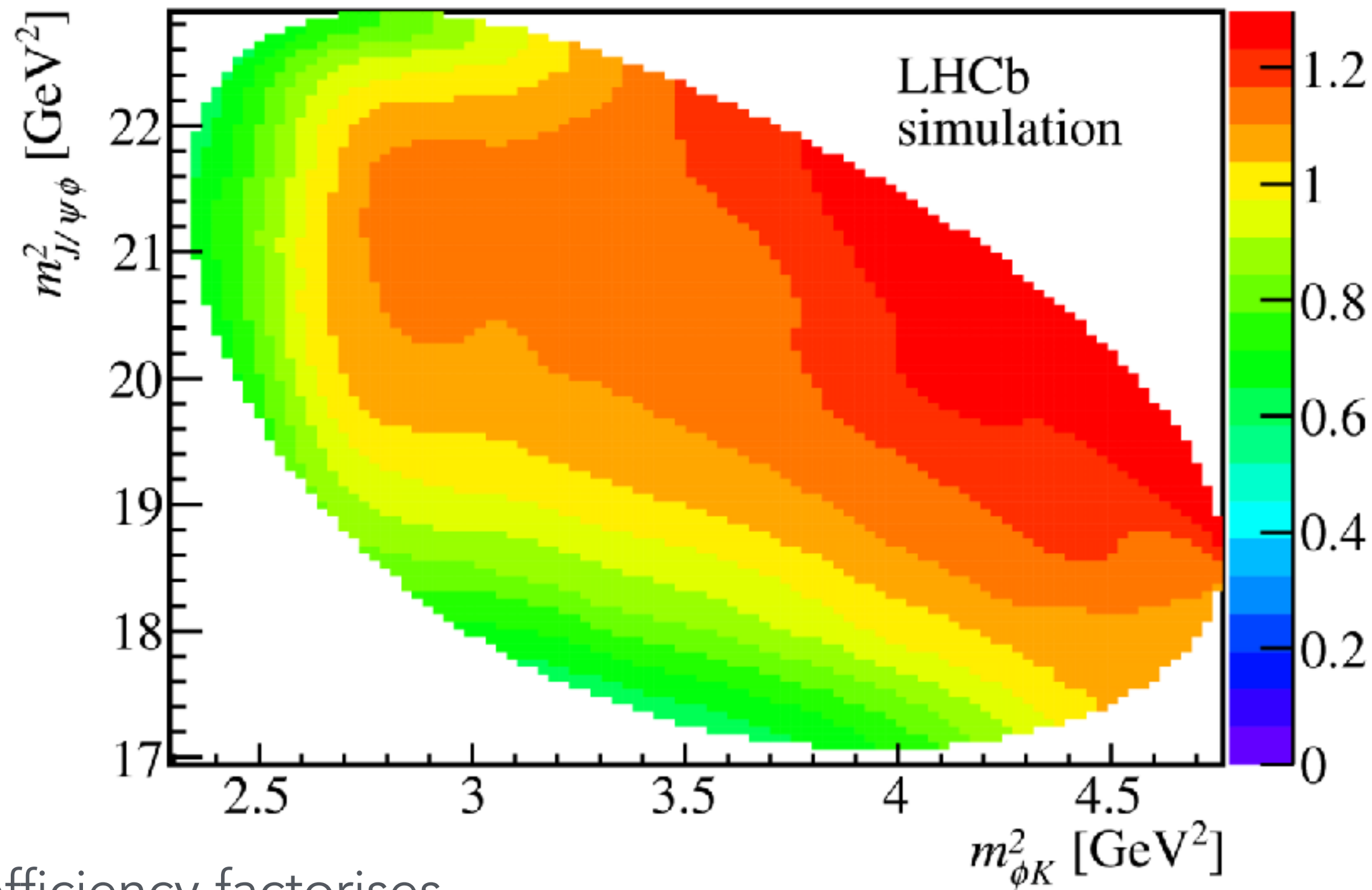
Potential neutral **isospin partner?**

$Z(4430)^0$ in $B^+ \rightarrow \psi(2S)\pi^0 K^+$



Efficiency

$$\epsilon(m_{\phi K}, \Omega) = \epsilon_1(m_{\phi K}, \cos \theta_{K^*}) \cdot \epsilon_2(\cos \theta_{\phi} | m_{\phi K}) \cdot \epsilon_3(\cos \theta_{J/\psi} | m_{\phi K}) \cdot \epsilon_4(\Delta \phi_{K^*, \phi} | m_{\phi K}) \cdot \epsilon_5(\Delta \phi_{K^*, J/\psi} | m_{\phi K})$$



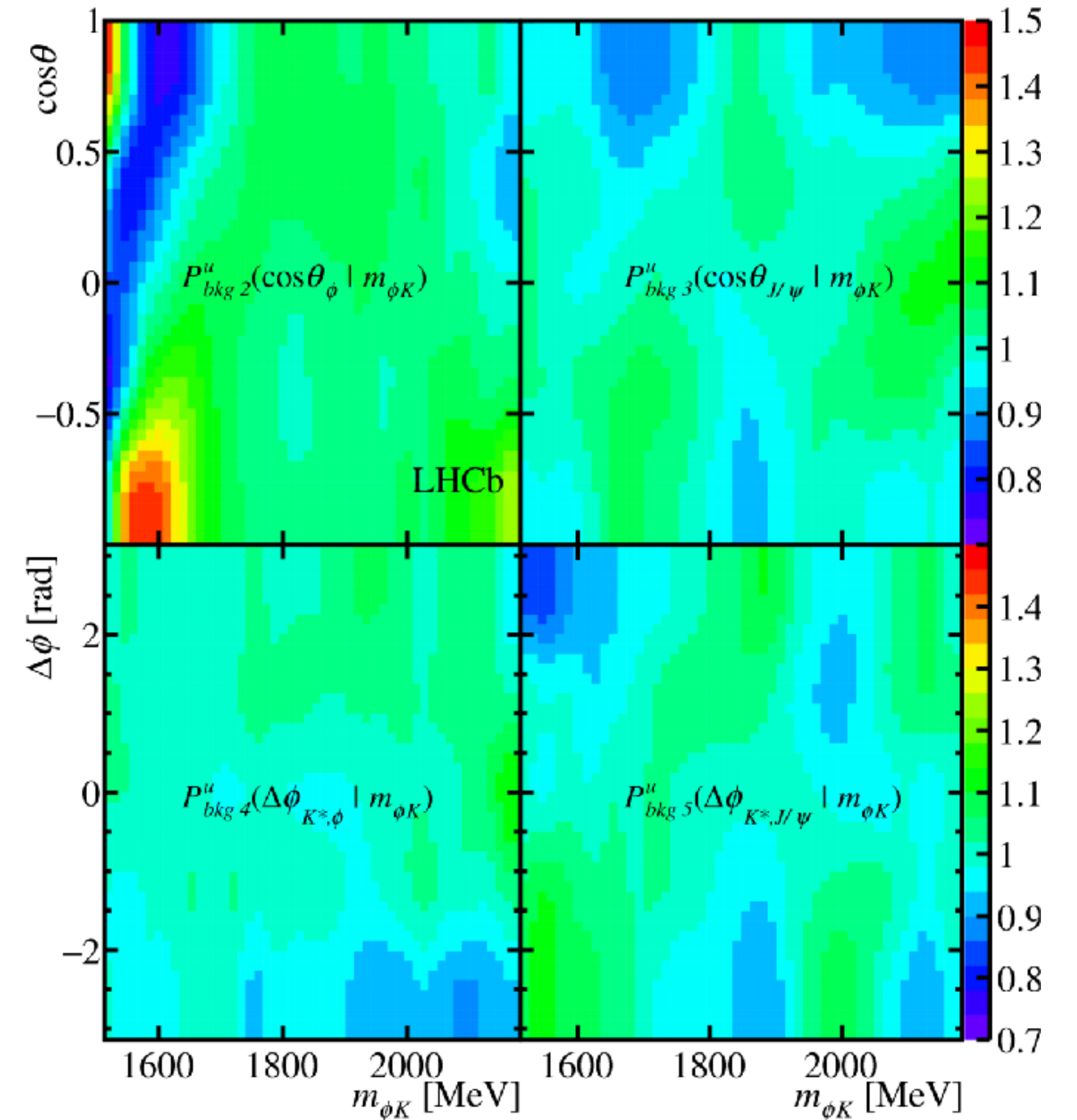
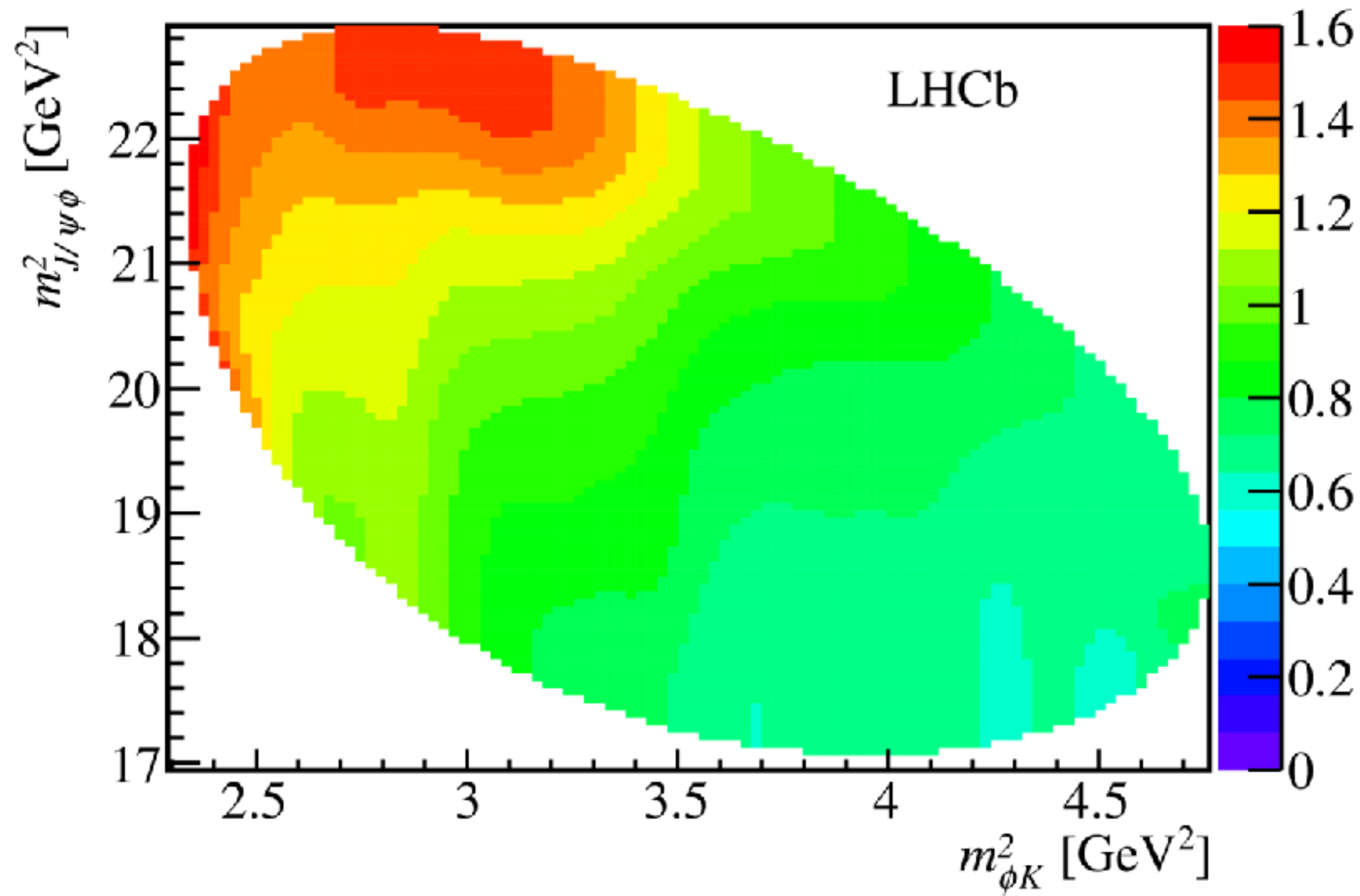
Assume efficiency factorises.

Fully simulated signal decay used to get parameterisation (bi-cubic interpolation between bin centres).

Simulation is weighted to match $p(K)$, $pT(B)$ and nTracks distributions in data Band in ϵ_2 from veto on double $\varphi \rightarrow K+K^-$.

Background

$$\frac{\mathcal{P}_{\text{bkg}}^u(m_{\phi K}, \Omega)}{\Phi(m_{\phi K})} = P_{\text{bkg}1}(m_{\phi K}, \cos \theta_{K^*}) \cdot P_{\text{bkg}2}(\cos \theta_{\phi} | m_{\phi K}) \cdot P_{\text{bkg}3}(\cos \theta_{J/\psi} | m_{\phi K}) \cdot P_{\text{bkg}4}(\Delta \phi_{K^*, \phi} | m_{\phi K}) \cdot P_{\text{bkg}5}(\Delta \phi_{K^*, J/\psi} | m_{\phi K}).$$



Same factorisation method as for efficiency.
Use sidebands of the B mass to get distribution.

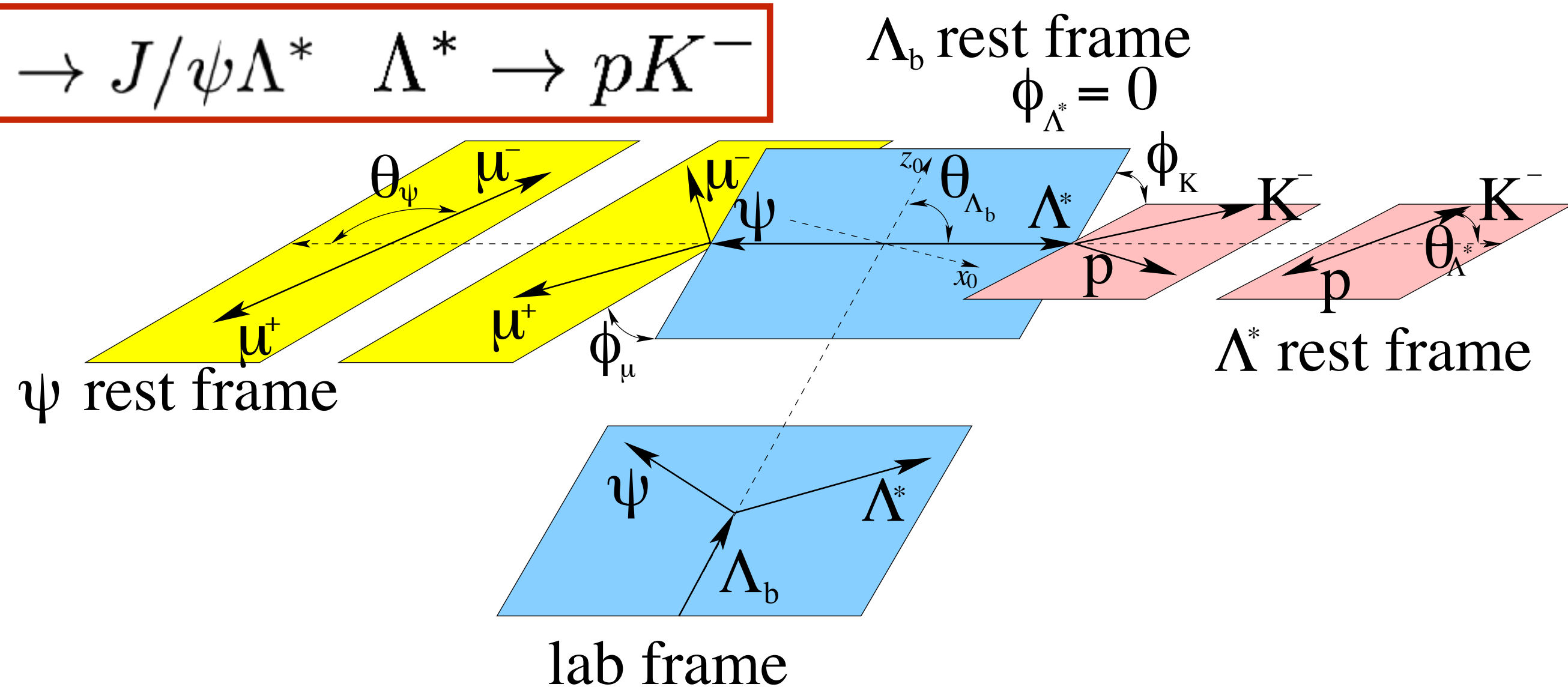
Amplitude model

Two interfering channels.

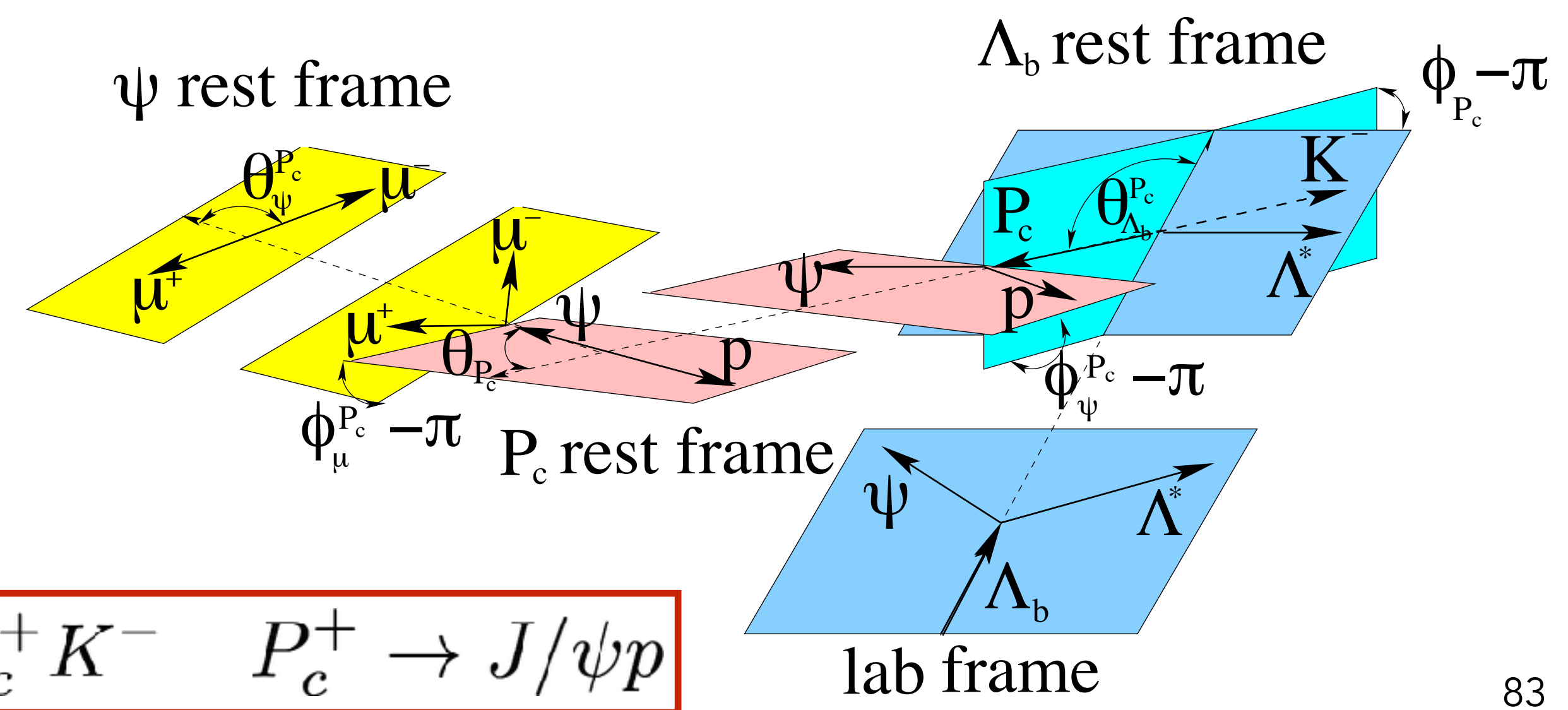
Use 5 angles and $m(Kp)$ as fit observables.

Resonance mass-shapes: Breit-Wigner or Flatté.

$$\Lambda_b^0 \rightarrow J/\psi \Lambda^* \quad \Lambda^* \rightarrow p K^-$$



State	J^P	M_0 (MeV)	Γ_0 (MeV)
$\Lambda(1405)$	$1/2^-$	$1405.1^{+1.3}_{-1.0}$	50.5 ± 2.0
$\Lambda(1520)$	$3/2^-$	1519.5 ± 1.0	15.6 ± 1.0
$\Lambda(1600)$	$1/2^+$	1600	150
$\Lambda(1670)$	$1/2^-$	1670	35
$\Lambda(1690)$	$3/2^-$	1690	60
$\Lambda(1800)$	$1/2^-$	1800	300
$\Lambda(1810)$	$1/2^+$	1810	150
$\Lambda(1820)$	$5/2^+$	1820	80
$\Lambda(1830)$	$5/2^-$	1830	95
$\Lambda(1890)$	$3/2^+$	1890	100
$\Lambda(2100)$	$7/2^-$	2100	200
$\Lambda(2110)$	$5/2^+$	2110	200
$\Lambda(2350)$	$9/2^+$	2350	150
$\Lambda(2585)$?	≈ 2585	200



$$\Lambda_b^0 \rightarrow P_c^+ K^- \quad P_c^+ \rightarrow J/\psi p$$

$Z_c(3900)^\pm$ amplitude analysis

Original ID fits from BES
3899.0 \pm 3.6 \pm 4.9 MeV
46 \pm 10 \pm 20 MeV

From Belle

$$M = (3894.5 \pm 6.6 \pm 4.5) \text{ MeV}/c^2$$

$$\Gamma = (63 \pm 24 \pm 26) \text{ MeV}/c^2$$

I^+ state preferred. [PRL 119, 072001 (2017)]

Large systematic from knowledge about σ and $f_0(980)$ and $f_0(1370)$ lineshapes

$$M_{\text{pole}} = (3881.2 \pm 4.2 \text{ stat} \pm 52.7 \text{ syst}) \text{ MeV}/c^2, \Gamma_{\text{pole}} = (51.8 \pm 4.6 \text{ stat} \pm 36.0 \text{ syst}) \text{ MeV}$$

$$M_{\text{pole}} = (3883.9 \pm 1.5 \text{ stat} \pm 4.2 \text{ syst}) \text{ MeV}/c^2, \Gamma_{\text{pole}} = (24.8 \pm 3.3 \text{ stat} \pm 11.0 \text{ syst}) \text{ MeV}$$

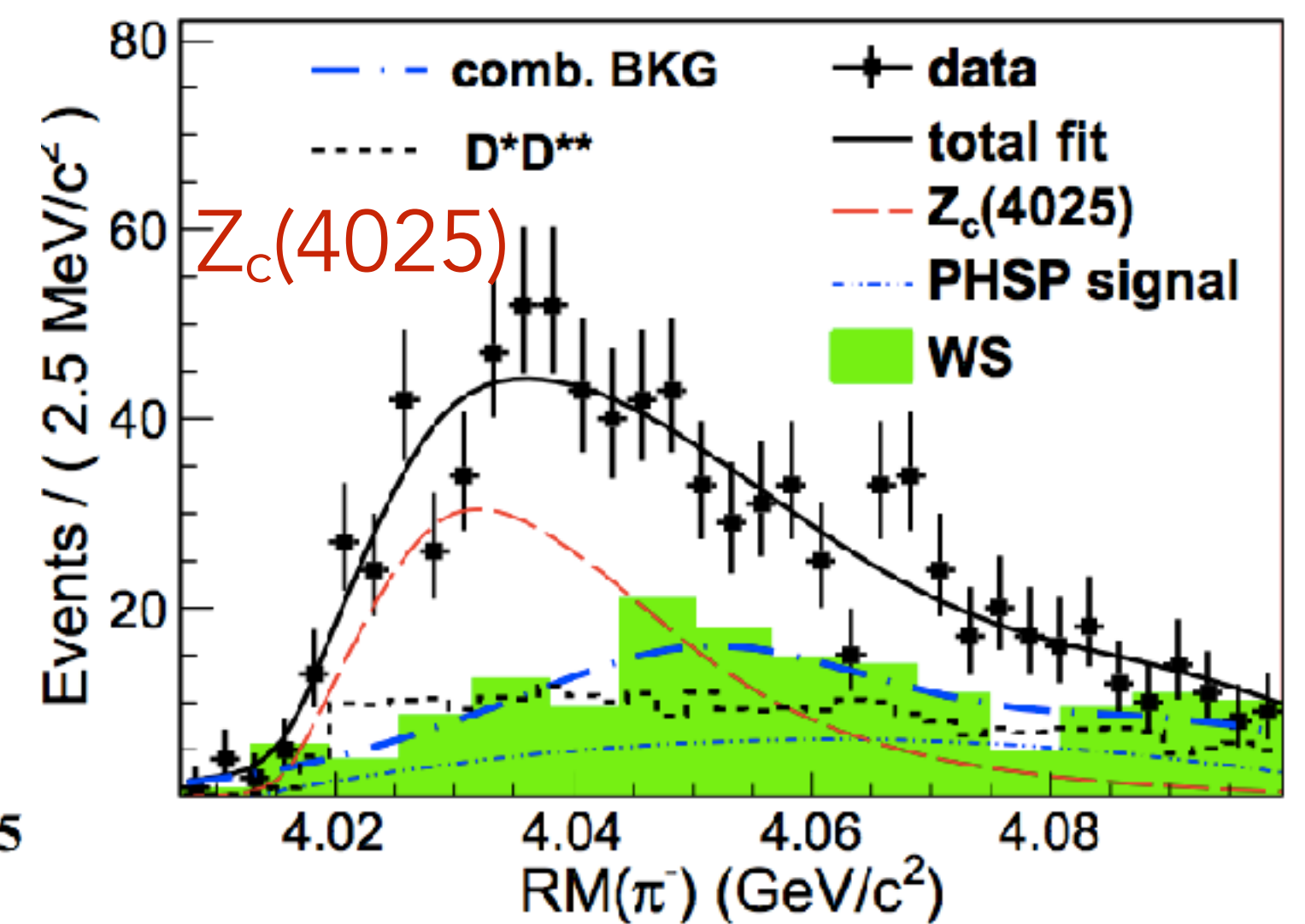
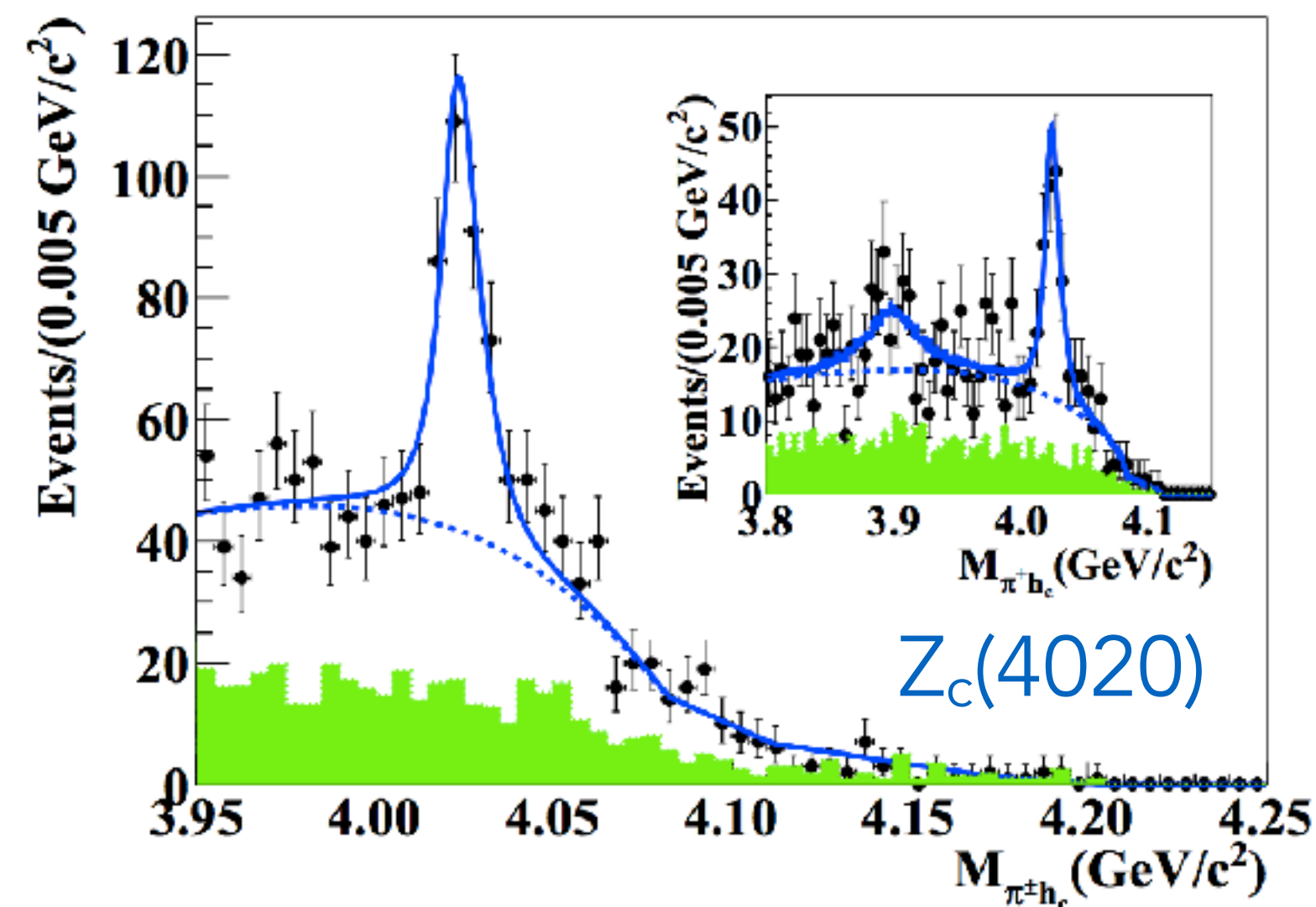
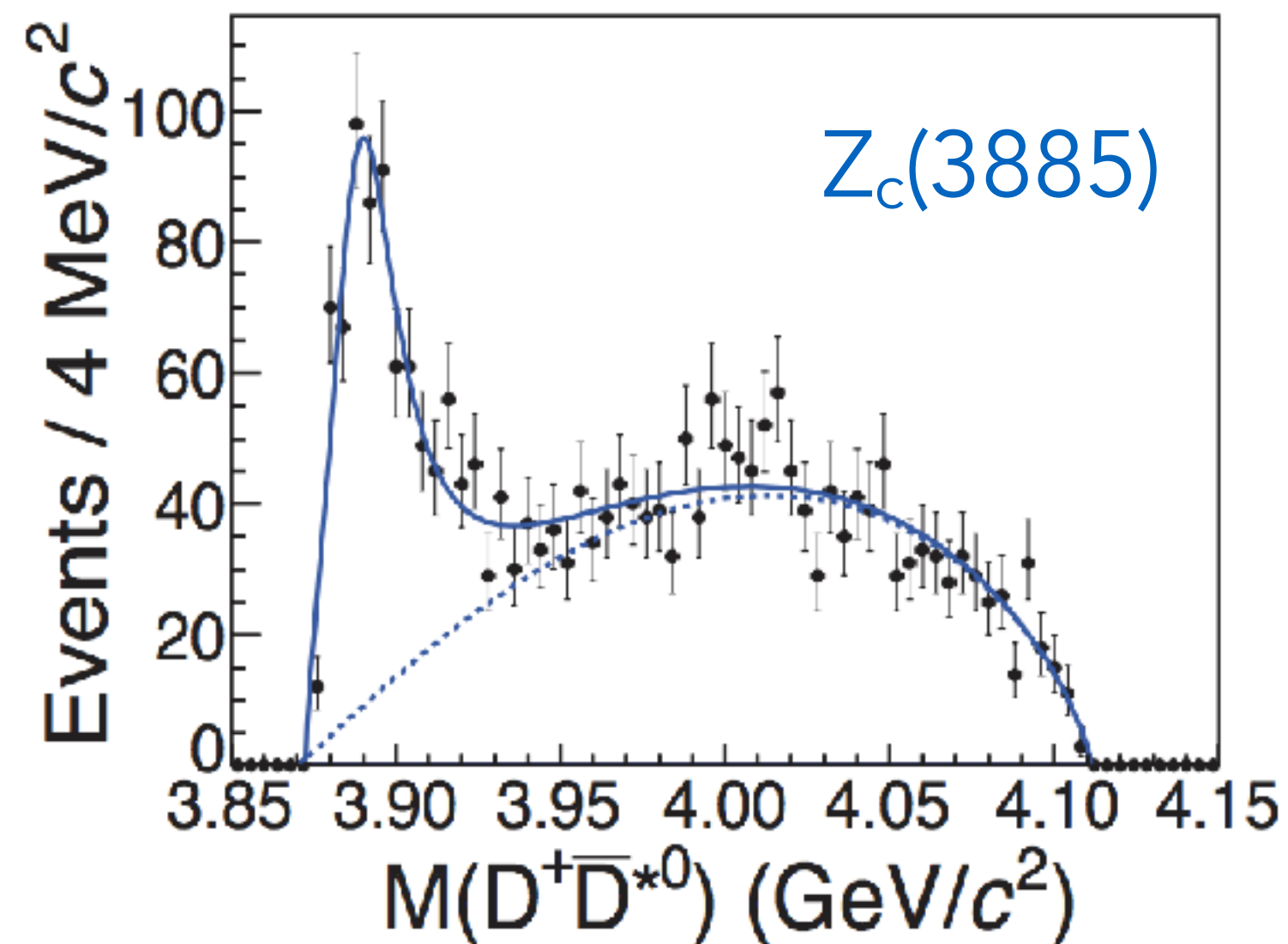
Does D^*-D^0 analysis use full amplitude fit?

Other exotic states

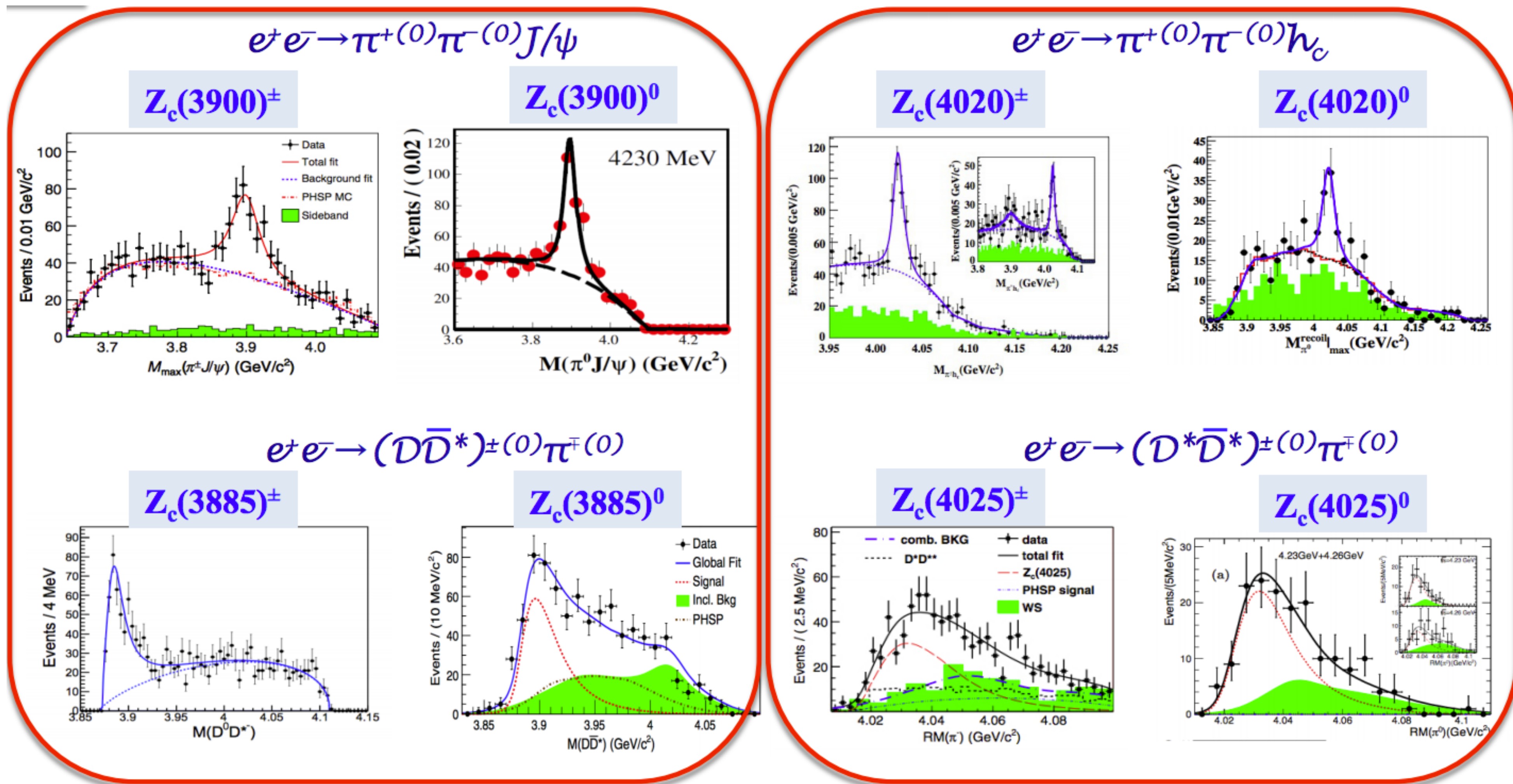
$Z_c(3900)^+$ seen in $J/\psi\pi^+$. Also have $Z_c(3885)^+$ in $(D\bar{D}^*)^+$, showing a dramatic near threshold peak. These could be the same state. Need partial wave analysis of $J/\psi\pi\pi$ final state to determine this.

$Z_c(4020)^+$ seen in $h_c(1P)\pi^+$ by BESIII. Very narrow width. This could be charm-sector equivalent of $Z_b(10650)^+$. Isospin triplet?

$Z_c(4025)^+$ seen recently by BESIII just above $(D^*\bar{D}^*)^+$ threshold. $m(D^*\bar{D}^*)$ distribution not described by phase space. This could be same state as $Z_c(4020)^+$.



Exotic Z_c states from BES-III

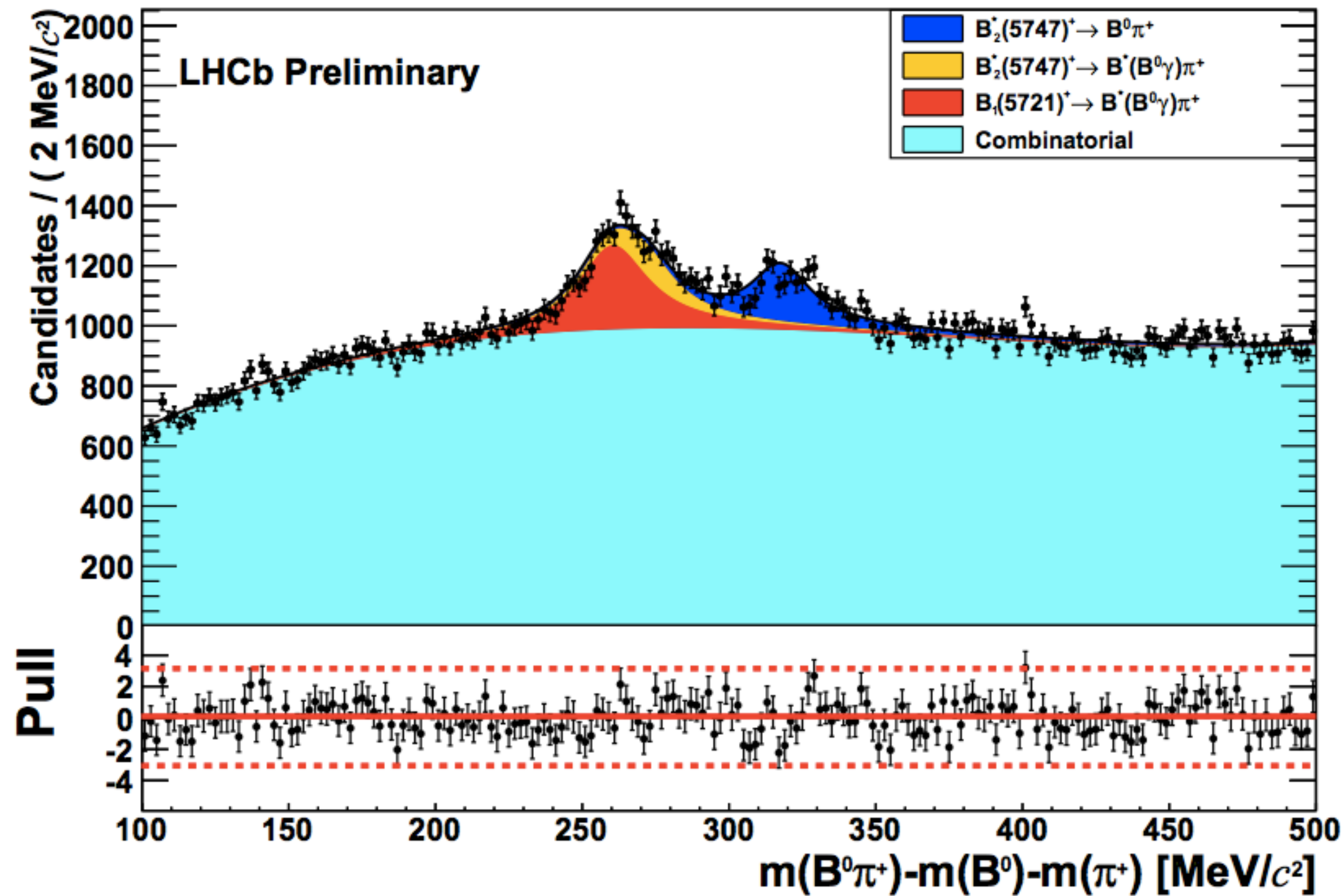


- Nature of these states? Isospin triplets?
- Different decay channels of the same states observed?
- Other decay modes?

<http://moriond.in2p3.fr/QCD/2016/WednesdayAfternoon/Garzia.pdf>

LHCb limits on the X(5568)

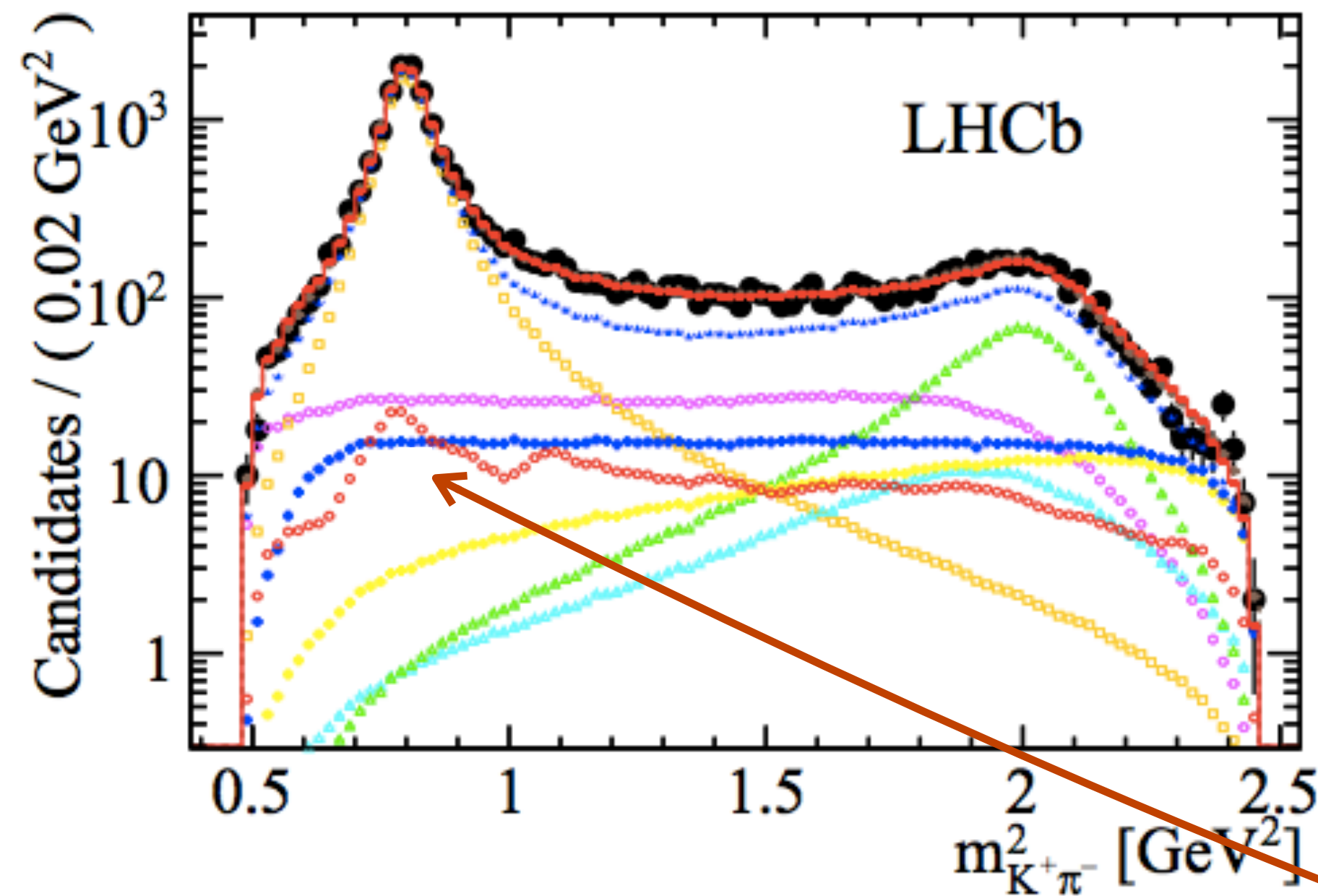
[LHCb-CONF-2016-004]



Well known excited B states found using same analysis techniques

Which resonances should we add?

[From PDG]



Resonance	J^P	Likely $n^{2S+1}L_J$	Mass (MeV)	Width (MeV)	$\mathcal{B}(K^{*0} \rightarrow K^+ \pi^-)$
$K_0^*(800)^0$ (κ)	0^+	—	682 ± 29	547 ± 24	$\sim 100\%$
$K^*(892)^0$	1^-	1^3S_1	895.94 ± 0.26	48.7 ± 0.7	$\sim 100\%$
$K_0^*(1430)^0$	0^+	1^3P_0	1425 ± 50	270 ± 80	$(93 \pm 10)\%$
$K_1^*(1410)^0$	1^-	2^3S_1	1414 ± 15	232 ± 21	$(6.6 \pm 1.3)\%$
$K_2^*(1430)^0$	2^+	1^3P_2	1432.4 ± 1.3	109 ± 5	$(49.9 \pm 1.2)\%$
$B^0 \rightarrow \psi(2S)K^+ \pi^-$ phase space limit			1593		
$K_1^*(1680)^0$	1^-	1^3D_1	1717 ± 27	322 ± 110	$(38.7 \pm 2.5)\%$
$K_3^*(1780)^0$	3^-	1^3D_3	1776 ± 7	159 ± 21	$(18.8 \pm 1.0)\%$
$K_0^*(1950)^0$	0^+	2^3P_0	1945 ± 22	201 ± 78	$(52 \pm 14)\%$
$K_4^*(2045)^0$	4^+	1^3F_4	2045 ± 9	198 ± 30	$(9.9 \pm 1.2)\%$
$B^0 \rightarrow J/\psi K^+ \pi^-$ phase space limit			2183		
$K_5^*(2380)^0$	5^-	1^3G_5	2382 ± 9	178 ± 32	$(6.1 \pm 1.2)\%$

Background from sidebands of B mass

$K^+ \pi^-$ spectrum contains many overlapping resonances.

Each resonance has a complex amplitude for **each** helicity component.

Measure all amplitudes relative to $K^*(892)$ helicity-0 component.

Default result includes all resonances up to $K_1^*(1680)$ ($J \leq 2$).

Main **systematic uncertainty** comes from varying model to include higher $K^+ \pi^-$ spin-states ($J = 3, 4, 5$).

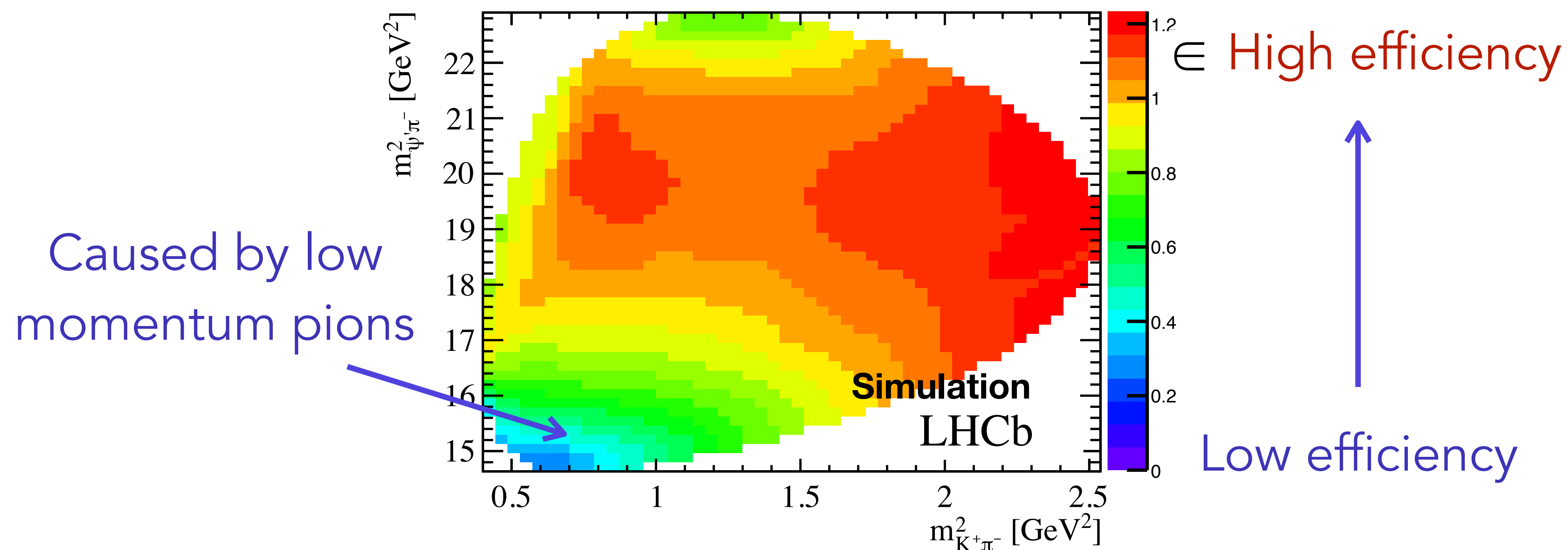
Reconstruction and selection efficiency

LHCb < 100% efficient at reconstructing the decay particles in 4D space.

Extract efficiency model from events simulated uniformly in phase space and passed through detector reconstruction.

Also, remove events (~12%) near edge of kinematic boundary since efficiency not well modelled there.

2D representation...



Fitting the model to the data

$$-\ln L(\vec{\omega}) = - \sum_i^{N_{\text{data}}} \ln P_{\text{tot}}^u(\vec{v}_i | \vec{\omega}) = - \sum_i^{N_{\text{data}}} \ln (|\mathcal{M}(\vec{v}_i | \vec{\omega})|^2 \epsilon(\vec{v}_i) / I(\vec{\omega}))$$

PDF Observables (mass, angles) Parameters Efficiency drops out

Likelihood fit to measure **~50** free parameters: amplitudes, phases, resonance mass/widths.

$$I(\vec{\omega}) = \sum_i^{N_{\text{MC}}} |\mathcal{M}(\vec{v}_i | \vec{\omega})|^2$$

- In any amplitude fit, difficulty comes from **integrating** the matrix element.
- Solution: sum over fully simulated, reconstructed phase space MC.
 - This automatically **includes the efficiency** in the normalisation.
 - Alternative approach explicitly parameterises the 4D efficiency.

Try different models for $K^+\pi^-$ and $Z(4430)$, compare values of L.

$Z(4430)^\pm$ parameters from amplitude fit

	LHCb	Belle
$M(Z)$ [MeV]	$4475 \pm 7^{+15}_{-25}$	$4485 \pm 22^{+28}_{-11}$
$\Gamma(Z)$ [MeV]	$172 \pm 13^{+37}_{-34}$	200^{+41+26}_{-46-35}
f_Z [%]	$5.9 \pm 0.9^{+1.5}_{-3.3}$	$10.3^{+3.0+4.3}_{-3.5-2.3}$
f_Z^I [%] <small>(with interference)</small>	$16.7 \pm 1.6^{+2.6}_{-5.2}$	–
significance	$> 13.9\sigma$	$> 5.2\sigma$
J^P	1^+	1^+
	New (large) systematic included	

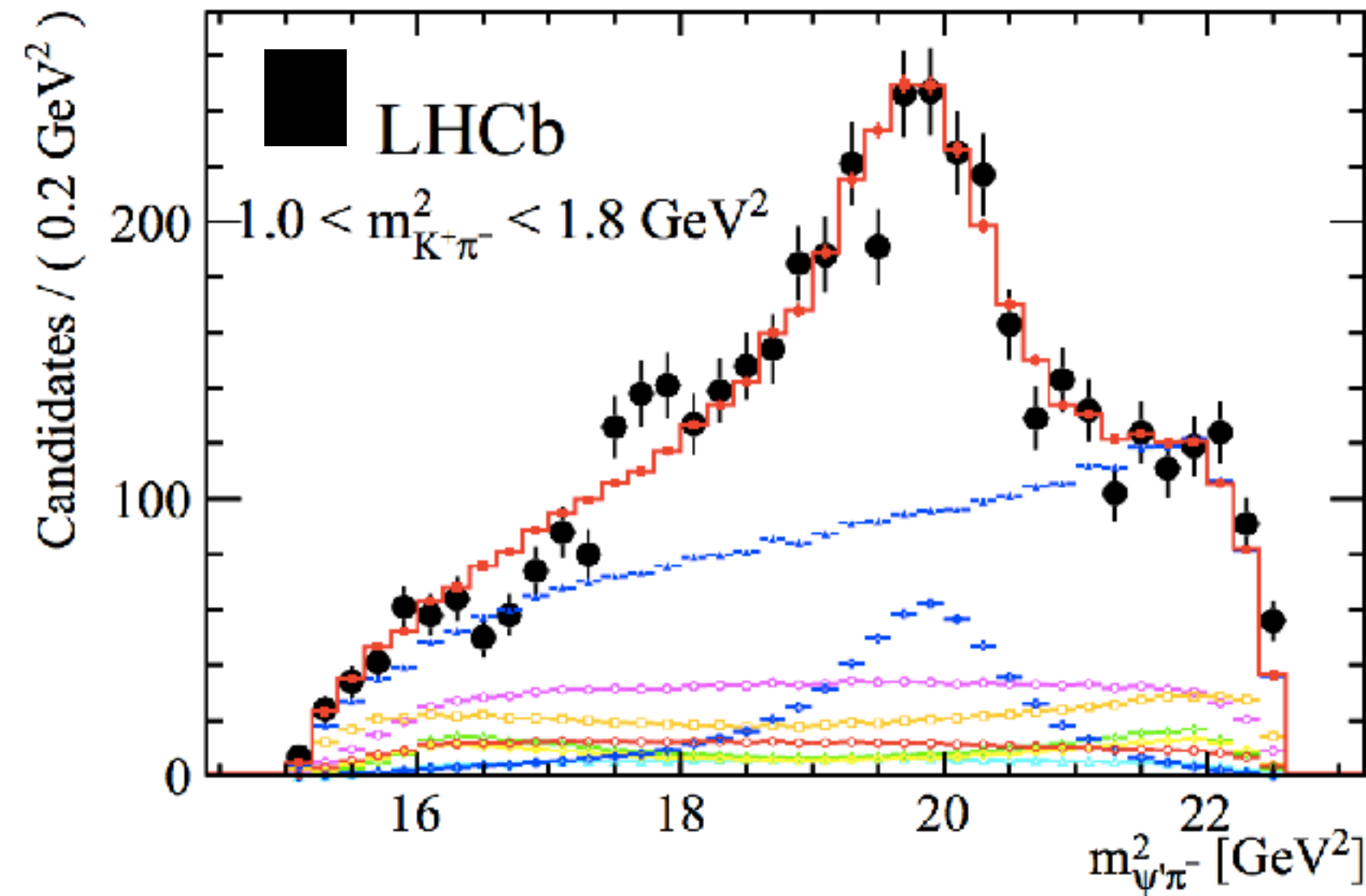
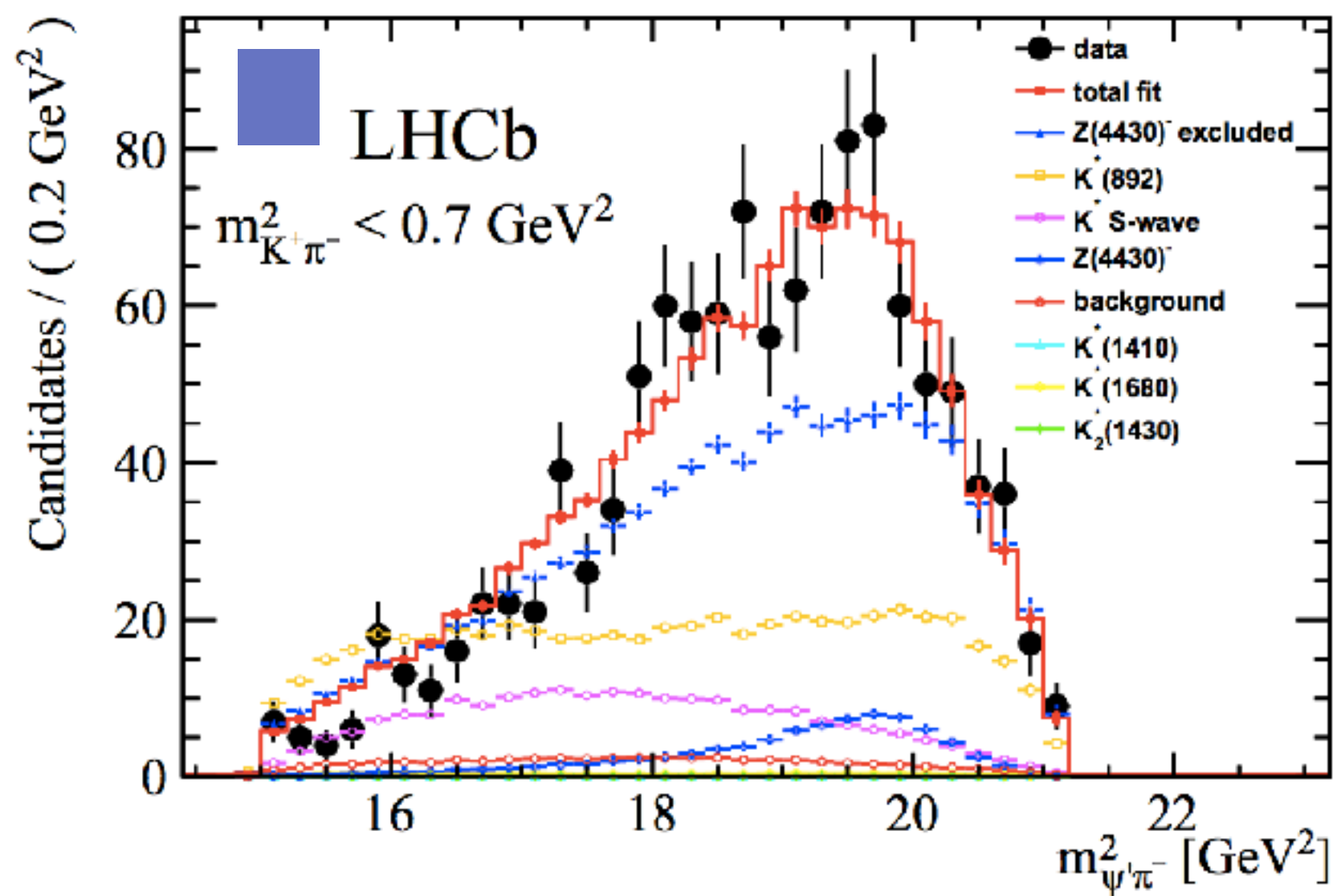
Amplitude fractions [%]

Contribution	LHCb	Belle
S -wave total	10.8 ± 1.3	
NR	0.3 ± 0.8	
$K_0^*(800)$	3.2 ± 2.2	5.8 ± 2.1
$K_0^*(1430)$	3.6 ± 1.1	1.1 ± 1.4
$K^*(892)$	59.1 ± 0.9	63.8 ± 2.6
$K_2^*(1430)$	7.0 ± 0.4	4.5 ± 1.0
$K_1^*(1410)$	1.7 ± 0.8	4.3 ± 2.3
$K_1^*(1680)$	4.0 ± 1.5	4.4 ± 1.9
$Z(4430)^-$	5.9 ± 0.9	$10.3^{+3.0}_{-3.5}$

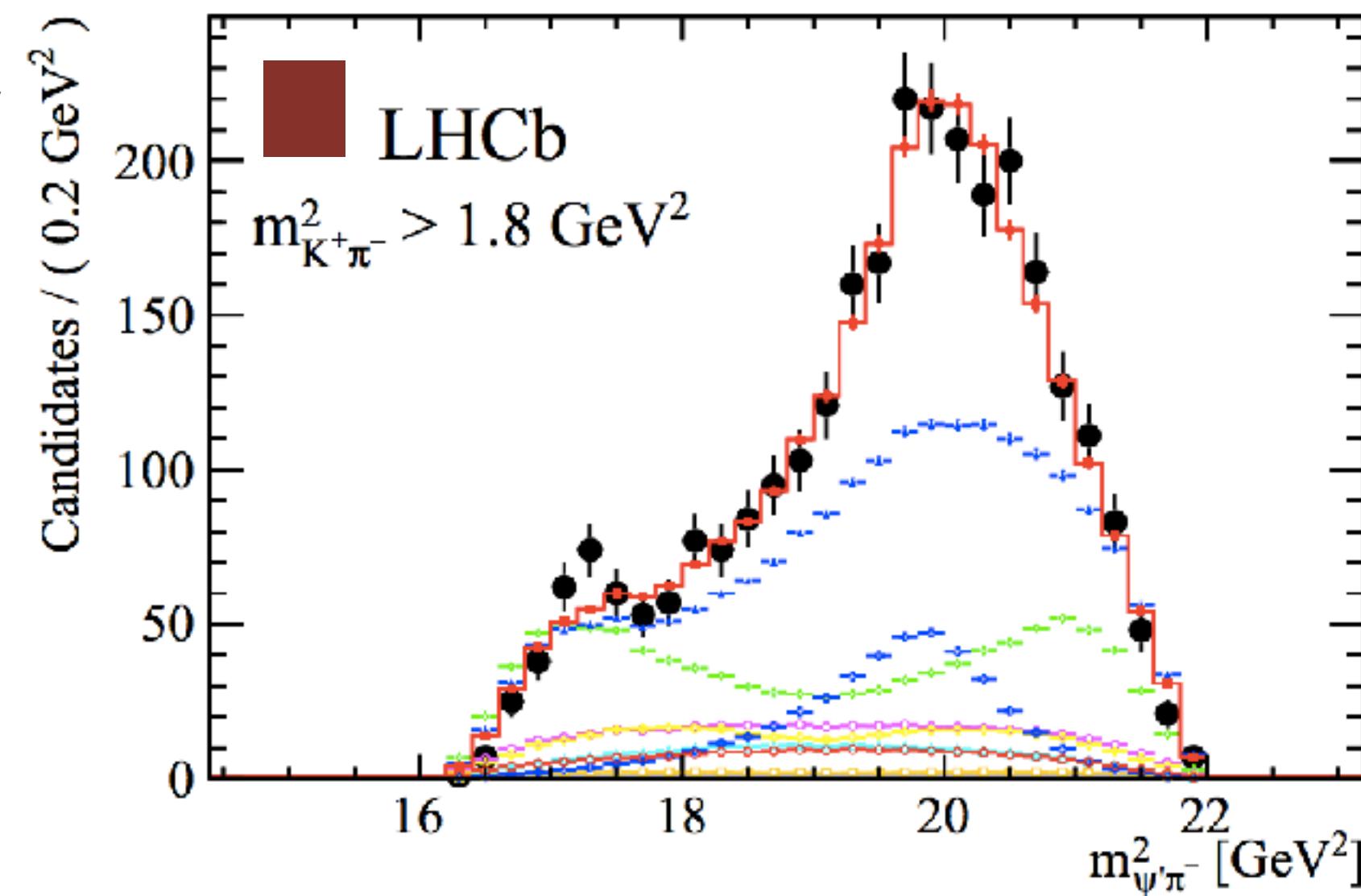
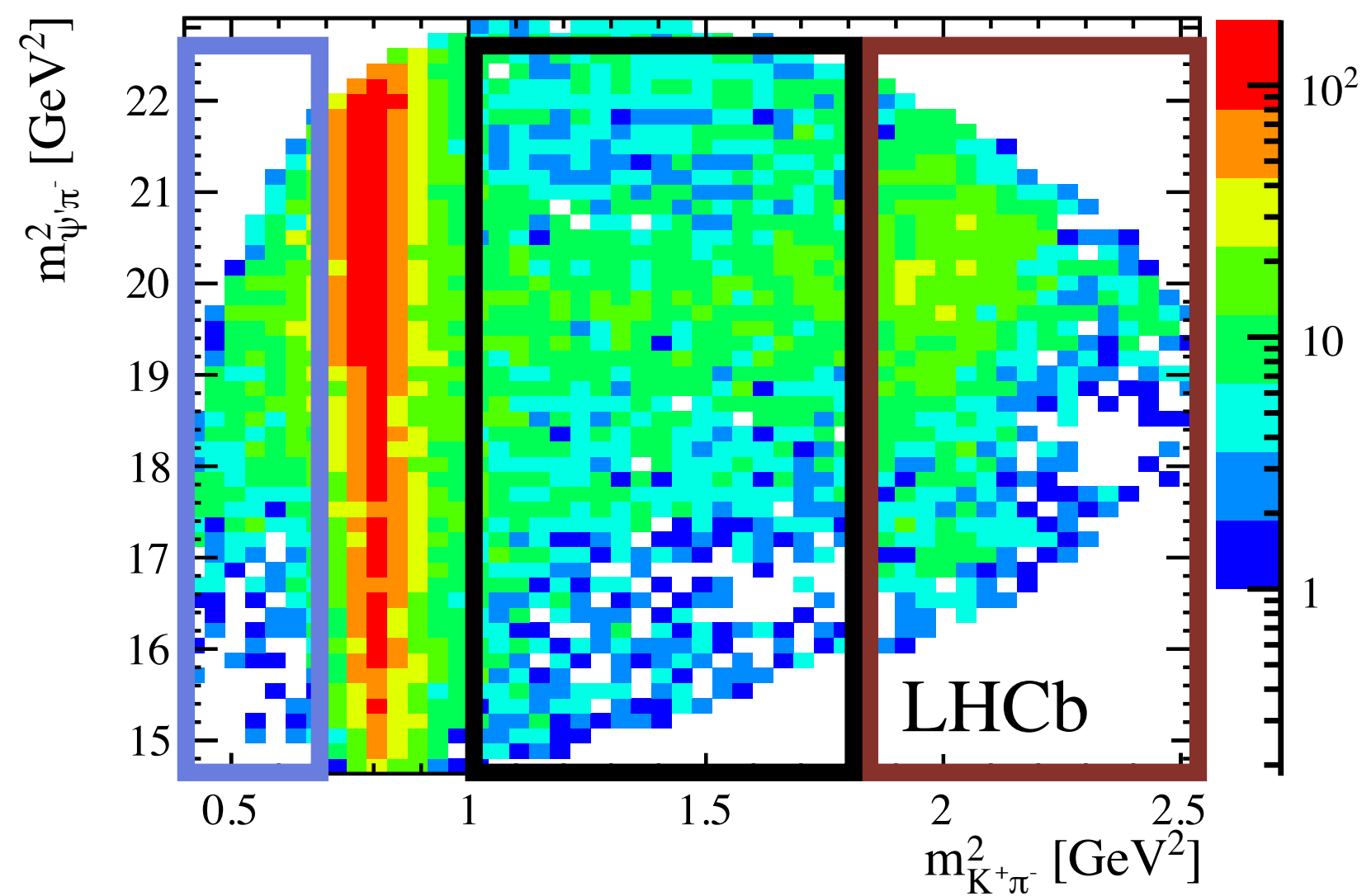
- Excellent agreement between LHCb and Belle.
- Large width - unlikely to be molecule?

$$f_i = \frac{\int |A_i(m_{K\pi}, \Omega)|^2 dm_{K\pi} d\Omega}{\int |\sum_k A_k(m_{K\pi}, \Omega)|^2 dm_{K\pi} d\Omega}$$

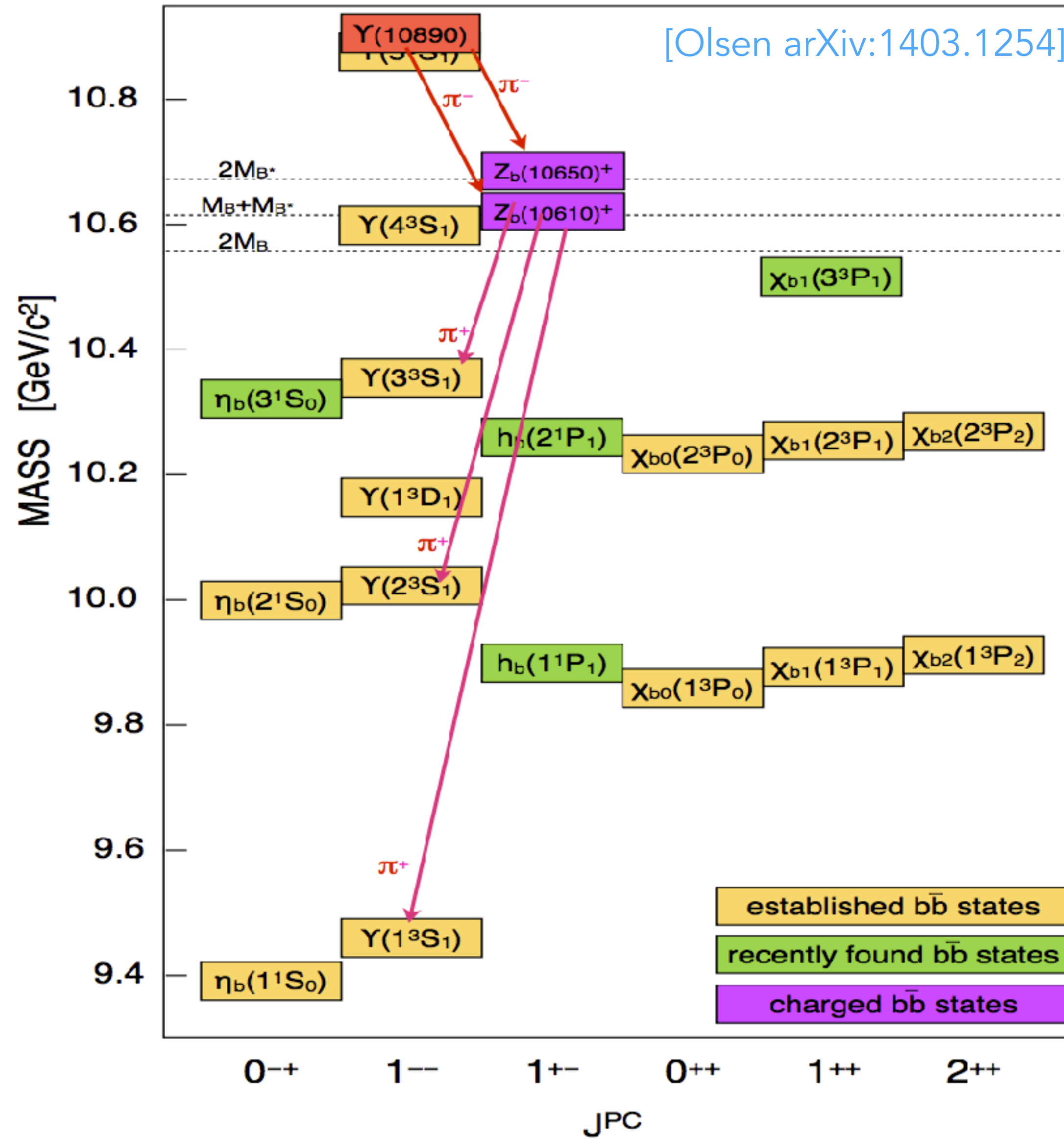
Fit projections in slices of $m(K^+\pi^-)$



[PRL 112 (2014) 222002]



Bottomonium spectrum



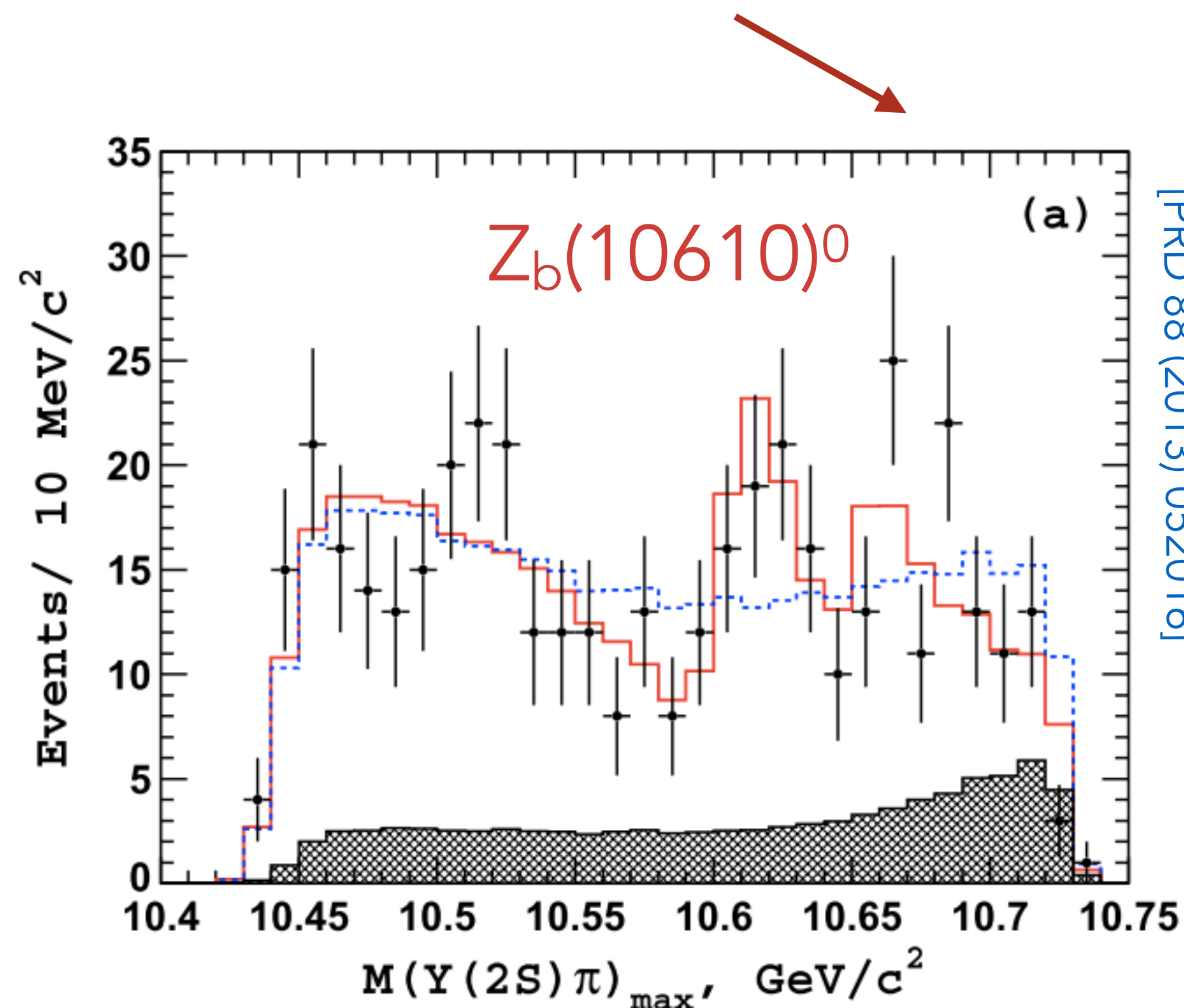
Bottomonium-like states

Belle has evidence for $Z_b(10610)^+$ and $Z_b(10650)^+$ resonances when looking at $\pi^+\pi^-\Upsilon(nS)$ and $\pi^+\pi^-h_b(mP)$.

[arXiv:1403.0992v1]

$I^G(J^P) = I^+(I^+)$, Virtual $B\bar{B}^*$ and $B^*\bar{B}^*$ S-wave molecule-like states?

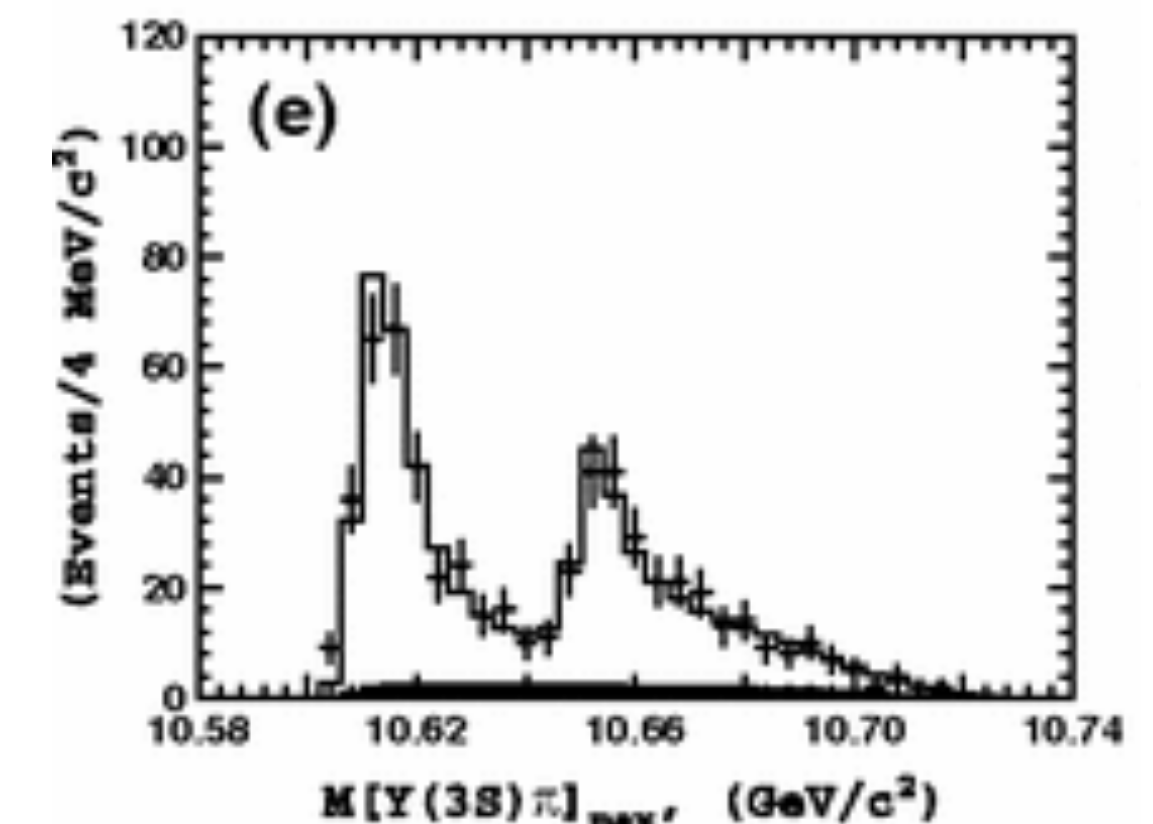
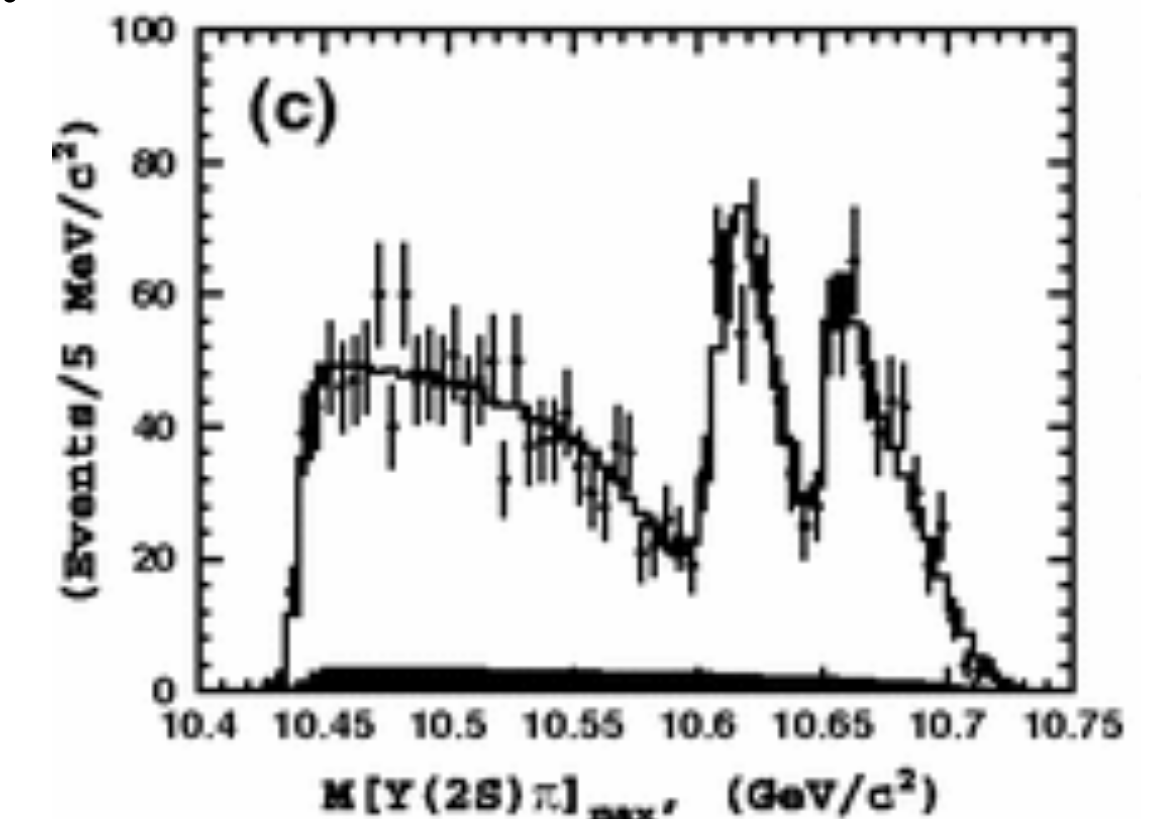
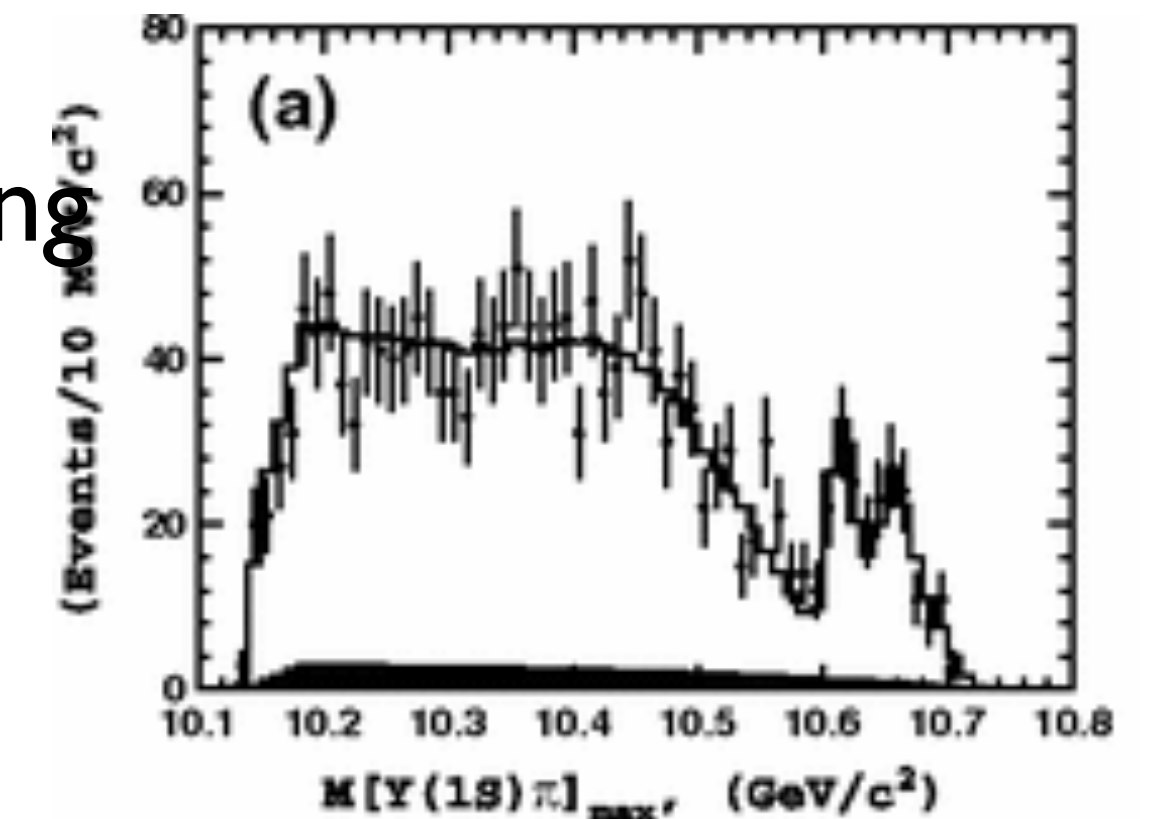
Also first evidence for neutral isospin partners in $\pi^0\pi^0\Upsilon(2S)$ amplitude fit.



[PRD 88 (2013) 052016]

Projections of Dalitz plots

Use Breit-Wigner (without energy dependent width) to model resonances



[PRL 108 (2012) 122001]