### FeynRules

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- FeynRules in a nutshell
- New in FeynRules :
  - NLO
  - AllYourBases (Liam Moore)
- Final remarks



### FeynRules



### FeynRules outputs



FeynRules outputs can be used directly by event generators

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UFO : output with the full information used by several generators



### FeynRules outputs



FeynRules outputs can be used directly by event generators

UFO : output with the full information used by several generators



### UFO

- Generator independent output with full model information
- Contains the list of particles, parameters, vertices, decays (Ito 2), coupling orders
- vertices are split into Lorentz structures, colours and couplings and all are included in the model!

$$-ig_s T^a_{ij} \gamma_{\mu}$$

• Used in MG5, Herwig, Gosam, Sherpa, ...





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### Madgraph5\_aMC@NLO

# Automated NLO computation MG5 Computation of the born MadFKS (IR)

- Computation of the real
   Computation of the loop
   MadLoop
  - Computation of the loop
- Matching with parton shower 'à la' MC@NLO



### MadLoop

$$\mathcal{A}^{1-loop} = \sum_{i} \frac{d_{i}}{d_{i}} \operatorname{Box}_{i} + \sum_{i} \frac{c_{i}}{r_{i}} \operatorname{Triangle}_{i} + \sum_{i} \frac{b_{i}}{b_{i}} \operatorname{Bubble}_{i} + \sum_{i} \frac{a_{i}}{r_{i}} \operatorname{Tadpole}_{i} + \frac{R}{r_{i}}$$

- Box, Triangle, Bubble and Tadpole are known scalar integrals
- Loop computation = find the coefficients
  - Tensor reduction (OPP)
- R : rational terms should be partially provided
- UV counterterm vertices have to be provided

### To be provided : R<sub>2</sub>

$$ar{A}(ar{q}) = rac{1}{\left(2\pi
ight)^4} \int d^d ar{q} rac{ar{N}(ar{q})}{ar{D}_0 ar{D}_1 \dots ar{D}_{m-1}}, \qquad ar{D}_i = (ar{q} + p_i)^2 - m_i^2$$



$$R_{2} \equiv \lim_{\epsilon \to 0} \frac{1}{\left(2\pi\right)^{4}} \int d^{d}\overline{q} \frac{\tilde{N}\left(\tilde{q}, q, \epsilon\right)}{\overline{D}_{0}\overline{D}_{1}\dots\overline{D}_{m-1}}$$

# Finite set of vertices that can be computed once for all

# Computed in MadLoop :R

Due to the  $\mathcal{E}$  dimensional parts of the denominators

Like for the 4 dimensional part but with a different set of integrals  $2^{-2}$  integrals

$$\int d^n \bar{q} \frac{\tilde{q}^2}{\bar{D}_i \bar{D}_j} = -\frac{i\pi^2}{2} \left[ m_i^2 + m_j^2 - \frac{(p_i - p_j)^2}{3} \right] + \mathcal{O}(\epsilon) ,$$

$$\int d^n \bar{q} \frac{\tilde{q}^2}{\bar{D}_i \bar{D}_j \bar{D}_k} = -\frac{i\pi^2}{2} + \mathcal{O}(\epsilon) ,$$

$$\int d^n \bar{q} \frac{\tilde{q}^4}{\bar{D}_i \bar{D}_j \bar{D}_k \bar{D}_l} = -\frac{i\pi^2}{6} + \mathcal{O}(\epsilon) .$$

Only  $R = R_1 + R_2$  is gauge invariant Check

### UV

 $\bar{A}(\bar{q}) = \frac{1}{(2\pi)^4} \int d^d \bar{q} \frac{N(\bar{q})}{\bar{D}_0 \bar{D}_1 \dots \bar{D}_{m-1}} = K \frac{1}{\epsilon} + \mathcal{O}\left(\epsilon^0\right)$ 



# Finite set of vertices that can be computed once for all

### Renormalization



Internal parameters are renormalised by replacing the external parameters in their expressions



### Renormalization conditions

On-shell scheme (or complex mass scheme):

Renormalized mass = Physical mass

Two-point function vanishes on-shell (No external bubbles)



$$i\delta_{ij} (\not p - m_i) + i \left[ f_{ij}^L (p^2) \not p \gamma_- + f_{ij}^R (p^2) \not p \gamma_+ + f_{ij}^{SL} (p^2) \gamma_- + f_{ij}^{SR} (p^2) \gamma_+ \right]$$

$$\begin{split} \tilde{\Re} \left[ f_{ij}^{L} \left( p^{2} \right) m_{i} + f_{ij}^{SR} \left( p^{2} \right) \right] \Big|_{p^{2} = m_{i}^{2}} &= 0 \\ \tilde{\Re} \left[ f_{ij}^{R} \left( p^{2} \right) m_{i} + f_{ij}^{SL} \left( p^{2} \right) \right] \Big|_{p^{2} = m_{i}^{2}} &= 0 \\ \tilde{\Re} \left[ 2m_{i} \frac{\partial}{\partial p^{2}} \left[ \left( f_{ii}^{L} \left( p^{2} \right) + f_{ii}^{R} \left( p^{2} \right) \right) m_{i} + f_{ii}^{SL} \left( p^{2} \right) + f_{ii}^{SR} \left( p^{2} \right) \right] + f_{ii}^{L} \left( p^{2} \right) + f_{ii}^{R} \left( p^{2} \right) \right] \Big|_{p^{2} = m_{i}^{2}} &= 0 \\ \\ \mathbf{Similar for the vectors and scalars} \end{split}$$

### Renormalization conditions

On-shell scheme (or complex mass scheme):

Renormalized mass = Physical mass

Two-point function vanishes on-shell (No external bubbles)



$$i\delta_{ij} (\not p - m_i) + i \left[ f_{ij}^L (p^2) \not p \gamma_- + f_{ij}^R (p^2) \not p \gamma_+ + f_{ij}^{SL} (p^2) \gamma_- + f_{ij}^{SR} (p^2) \gamma_+ \right]$$

$$\tilde{\kappa} \left[ f_{ij}^L \left( p^2 \right) m_i + f_{ij}^{SR} \left( p^2 \right) \right] \Big|_{p^2 = m_i^2} = 0$$
  
$$\tilde{\kappa} \left[ f_{ij}^R \left( p^2 \right) m_i + f_{ij}^{SL} \left( p^2 \right) \right] \Big|_{p^2 = m_i^2} = 0$$

 $\tilde{\mathscr{X}}\left[2m_{i}\frac{\partial}{\partial p^{2}}\left[\left(f_{ii}^{L}\left(p^{2}\right)+f_{ii}^{R}\left(p^{2}\right)\right)m_{i}+f_{ii}^{SL}\left(p^{2}\right)+f_{ii}^{SR}\left(p^{2}\right)\right]+f_{ii}^{L}\left(p^{2}\right)+f_{ii}^{R}\left(p^{2}\right)\right]\right|_{p^{2}=m_{i}^{2}}=0$ 

Similar for the vectors and scalars

### H<sup>+</sup> production : m<sub>H</sub>~m<sub>t</sub>





- Goal : Automate the one-loop computation for BSM models
- Required ingredients :
  - Tree-level vertices
     R2 vertices (OPP)
     Missing

- UV counterterm vertices
- Solution : UFO at NLO



### R2:Validation

- tested\* on the SM (QCD:P. Draggiotis et al. +QED:M.V. Garzelli et al)
- tested\* on MSSM (QCD:H.-S. Shao,Y.-J. Zhang) : test the Majorana

\*Analytic comparison of the expressions

### **UV Validation**

- SM QCD : tested\* (W. Beenakker, S. Dittmaier, M. Kramer, B. Plumper)
- SM EW : tested\* (expressions given by H.-S. Shao from A. Denner)

\*Analytic comparison of the expressions

### Tests in event generators

- aMC@NLO
- The SM QCD has been tested by V. Hirschi (Comparison with the built-in version)
- SM EW (MZ scheme): comparison to published results for ME by H.-S. Shao and V. Hirschi
- Various BSM
  - gauge invariance
  - pole cancelation



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#### Massive and massless b

== a a > t t~ ['QED'] == == a a > t t~ a ['QED'] == == a a > w+ w- ['QED'] == == a b > t w- ['QED'] ==  $== d \sim d > w + w - ['QCD'] ==$  $== d \sim d > w + w - ['QED'] ==$  $== d \sim d > z z ['QCD'] ==$  $== d \sim d > z z ['QED'] ==$ == e+ e- > t t~ a ['QED'] == == e+ e- > t t~ q ['QED'] == == g b > t w- ['QED'] == == g g > h h ['QCD'] == == g g > t t~ ['QED'] == == g g > t t~ g ['QED'] == == g g > t t~ h ['QCD'] == == g g > t t~ h ['QED'] == == h h > h h ['QED'] == == h h > h h h ['QED'] == $== t t \sim > w + w - ['QED'] ==$ 

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### Test EW

# **Restrictions/Assumptions**

- Renormalizable Lagrangian, maximum dimension of the operators is 4
- Feynman Gauge
- $\bullet \quad \{\gamma_{\mu}, \gamma_5\} = 0$
- 't Hooft-Veltman scheme
- On-shell scheme for the masses and wave functions
- MS by default for everything else (zero-momentum possible for fermion gauge boson interaction)

### EFT at NLO



In the loop: same as SM



 $f^{ABC}G^{A\nu}_{\mu}G^{B\rho}_{\nu}G^{C\mu}_{\rho}$  $\varphi^{\dagger}\varphi G^{A}_{\mu\nu}G^{A\mu\nu}$ 

More momenta: higher rank of the integral numerator

Additional gamma algebra  $(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \widetilde{\varphi} G^A_{\mu\nu}$ 





Evanescent operators:

 $O_{ut}^{(8)} = \left(\bar{u}\gamma^{\mu}T^{A}u\right)\left(\bar{t}\gamma_{\mu}T^{A}t\right)$ 



 $\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}P_{R}\otimes\gamma_{\mu}\gamma_{\nu}\gamma_{\rho}P_{R} = E + (16 - 4a\varepsilon)\gamma^{\mu}P_{R}\otimes\gamma_{\mu}P_{R}$  $\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}P_{R}\otimes\gamma_{\rho}\gamma_{\nu}\gamma_{\mu}P_{R} = -E + [4 - (12 - 4a)\varepsilon]\gamma^{\mu}P_{R}\otimes\gamma_{\mu}P_{R}$ 

Extra R2 (gauge invariant) Change the UV matching

### EFT at NLO

- UV counterterms :
  - Basis reduction needed for the anomalous matrix (By Liam Moore)
    - Check (R.Alonso, E. E. Jenkins, A.V. Manohar, M.Trott, JHEP 1404 (2014) 159)
  - MSbar :  $I/\varepsilon$  from the amplitudes not from the renomalization

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• Running (UFO 2.0)

### Top FCNC CD, F. Maltoni, J. Wang, C. Zhang, PRD91 (2015) 034024

	LO		NLO	
Coefficient	$\sigma$ [fb]	Scale uncertainty	$\sigma$ [fb]	Scale uncertainty
$C_{u\varphi}^{(13)} = 3.5$	2603	+13.0% -11.0%	3858	+7.4% -6.7%
$C_{uG}^{(13)} = 0.04$	40.1	+16.5% $-13.2%$	50.7	+4.0% $-5.2%$
$C_{u\varphi}^{(23)} = 3.5$	171	+9.7% $-8.7%$	310	+7.3% -6.3%
$C_{uG}^{(23)} = 0.09$	9.53	+11.0% $-9.7%$	16.6	+5.5% $-5.1%$



$$\mathcal{L}_{\rm EFT} = \mathcal{L}_{\rm SM} + \sum_{i} \frac{C_i}{\Lambda^2} O_i + H.c.$$

#### Small when constraints from $10^2$ $ug \rightarrow t$ are taken into account

$$\begin{aligned} O_{\varphi q}^{(3,i+3)} &= i \left( \varphi^{\dagger} \overleftrightarrow{D}_{\mu}^{I} \varphi \right) \left( \bar{q}_{i} \gamma^{\mu} \tau^{I} Q \right) \\ O_{\varphi q}^{(1,i+3)} &= i \left( \varphi^{\dagger} \overleftrightarrow{D}_{\mu} \varphi \right) \left( \bar{q}_{i} \gamma^{\mu} Q \right) \\ O_{\varphi u}^{(i+3)} &= i \left( \varphi^{\dagger} \overleftrightarrow{D}_{\mu} \varphi \right) \left( \bar{u}_{i} \gamma^{\mu} t \right) \\ O_{uB}^{(i3)} &= g_{Y} (\bar{q}_{i} \sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu}, \\ O_{uG}^{(i3)} &= g_{s} (\bar{q}_{i} \sigma^{\mu\nu} T^{A} t) \tilde{\varphi} G_{\mu\nu}^{A}, \\ O_{uW}^{(i3)} &= g_{W} (\bar{q}_{i} \sigma^{\mu\nu} \tau^{I} t) \tilde{\varphi} W_{\mu\nu}^{I} \\ O_{uW}^{(i3)} &= (\varphi^{\dagger} \varphi) (\bar{q}_{i} t) \tilde{\varphi} \end{aligned}$$





# **Restrictions/Assumptions**

- Renormalizable Lagrangian, maximum dimension of the operators is 4 <u>FFT with max 4F (Evanescent op.)</u>
- Feynman Gauge any gauge (any rank for EFT)
- $\bullet \quad \{\gamma_{\mu}, \gamma_5\} = 0$
- 't Hooft-Veltman scheme
- On-shell scheme for the masses and wave functions
- MS by default for everything else (zero-momentum possible for fermion gauge boson interaction)
   MZ scheme for EW coupling<sub>C. Degrande</sub>



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### Operators bases in the SMEFT

 $\mathcal{L}_{\mathsf{BSM}}(\{\Phi_{\mathsf{SM}}\}, \{\mathcal{X}_{\mathsf{NP}}\}) \to \mathcal{L}_{\mathsf{SM}}(\{\Phi_{\mathsf{SM}}\}) + \frac{C_i}{\Lambda^2} \mathcal{O}_i(\{\Phi_{\mathsf{SM}}\}) + \dots$ 

- Below heavy thresholds, UV states decouple  $\leftrightarrow$  local operators  $\mathcal{O}_i$
- BSM model determines pattern of effective couplings  $\frac{C_i}{\Lambda^2} = \frac{f(g_{\chi})}{m_{\pi^2}^2}$

 $D \geq 6$  operators exhibit nontrivial relationships -  $\mathcal{O}_i^{(6)} = k_{ij} \mathcal{O}_j^{(6)}$ :

e.g.: 
$$(\bar{u}\gamma^{\mu}T^{A}u)(\bar{t}\gamma_{\mu}T^{A}t) = \frac{1}{2}(\bar{u}\gamma^{\mu}t)(\bar{t}\gamma_{\mu}u) - \frac{1}{6}(\bar{u}\gamma^{\mu}u)(\bar{t}\gamma_{\mu}t)$$

Redundancies eliminated by fixing an operator basis. Several options:

- Model-independent choice e.g. Warsaw (Grzadkowski++ 1008.4884)
- Choose for UV interpretation e.g. SILH (Giudice++ 0703164)
- Simplicity of relationship to observables e.g. Mass (Gupta++ 1405.0181)

### The Warsaw procedure

Warsaw - tackle problem systematically at D = 6. In a nutshell:

- Divide operators into classifications according to generic building blocks:  $\{X, \psi, \varphi, D\}$ , e.g.  $(\varphi^{\dagger}\varphi)G^{A}_{\mu\nu}G^{A\mu\nu} \in X^{2}\varphi^{2}$
- Impose a hierarchy: fewer  $D_{\mu} \implies$  `lower' classification
- For each classification with  $n_D \ge 1$ , use identities (e.g. IBP) to express operators as  $\mathcal{O}^{(6)}(\{\varphi\}) \propto \frac{\delta S_0}{\delta \varphi_i}$ , the classical EoM
- Use EoM as far as possible, e.g.  $i D\!\!\!/ u o \Gamma_{\!\!u}^\dagger \widetilde{arphi}^\dagger q$  to eliminate  $D_{\!\mu}$

**Result**: proof all operators expressible as a linear combination of 59, spread over 12 classifications.

But - when decomposition of redundant operators is necessary (e.g. in matching, NLO calculations) it must be done by hand.

#### AllYourBases-Automatic basis reduction in FeynRules

ALLYOURBASES - get FEYNRULES to derive explicit decomposition of any operator onto the Warsaw basis automatically:

$$\mathcal{L}_{ ext{eff}} \supset C_j \mathcal{O}_j^{(6)}, \quad \mathcal{O}_j^{(6)} = \sum_{i=1}^{59} k_{ij} \mathcal{O}_i^{ ext{Warsaw}}$$

... by directed application of necessary identities at Lagrangian level:

- EoMs:  $(D^{\rho}G_{\rho\mu})^A \rightarrow g_s \sum (\bar{q}\gamma_{\mu}T^Aq) , \dots$
- Fierz identities:  $M_{ij}^I M_{kj}^I \to \sum c_J M_{il}^J M_{kj}^J$ ,  $M^J \in \{\Gamma^A, T, \tau, \delta \dots\}$
- Integration-by-Parts:  $\mathcal{A}^{\mu}(D_{\mu}\mathcal{B}) \rightarrow -(D_{\mu}\mathcal{A})\mathcal{B}^{\mu} + T$
- Gamma matrix algebra:  $\eta_{\mu\nu}\gamma_{\rho} \rightarrow \gamma_{\nu}\eta_{\mu\rho} + i\gamma_{\mu}\sigma_{\nu\rho} + i\epsilon^{\sigma}_{\nu\rho\mu}\gamma_{\sigma}\gamma_{5}$
- Bianchi identities:  $(D_{\mu}X_{\nu\rho})^{A} + (D_{\rho}X_{\mu\nu})^{A} + (D_{\nu}X_{\rho\mu})^{A} = 0 \dots$

# A simple example

 $\mathcal{O} = (\varphi^{\dagger}\varphi)(D_{\mu}\varphi^{\dagger}D^{\mu}\varphi) \text{ can be integrated-by-parts to use EoM}(\varphi):$  $(D^{\mu}D_{\mu}\varphi)^{j} = \mu^{2}\varphi^{j} - \lambda (\varphi^{\dagger}\varphi) \varphi^{j} - \bar{e} \Gamma_{e}^{\dagger} l^{j} + \varepsilon_{jk} \bar{q}^{k} \Gamma_{u} u - \bar{d} \Gamma_{d}^{\dagger} q^{j}$ 

... and the coefficients in the EoM become those of the decomposition of this operator onto the Warsaw basis classifications, represented as:

$$\left[\varphi^4 D^2\right] \rightarrow \left[\varphi^4 D^2\right] + \left[\varphi^3 \psi^2\right] + \left[\varphi^6\right] + \mu^2 \left[\varphi^4\right] + \left[T\right] + \left[E\right]$$

- ALLYOURBASES identifies and applies the necessary algebraic steps (in this case, just integration-by-parts) recursively.
- Returns a FeynRules expression for the operator's decomposition

In FeynRules syntax:

O = (Phibar[i]Phi[i]) (DC[Phibar[j],mu] DC[Phi[j],mu])

. . . returns:

### Returns:



### AYB-in short

ALLYOURBASES automates laborious procedure prevalent in EFT calculations.

- Explicit operator relationships in  $\mathcal{L}^{(6)}_{\text{SMEFT}}$  are derived by a symbolic implementation of the Warsaw procedure in FeynRules
- Applications in aiding calculations involving redundant operators,
   e.g. matching calculations, renormalization, translating limits. . .
- Algorithm only partially tied to D = 6 SM, very feasible to generalise to D > 6, non-SM theories in future. . .
- Currently in testing and validation. . .



### Summary

BSM in HE tools made easy in FeynRules

- Automatic BSM@NLO
  - Renormalizable (Public)
  - For EFT (Private)
- Automatic basis reduction for EFT (under validation) C. Degrande