

# Composite Higgs Models

or: Collider probes of Composite Dark Matter

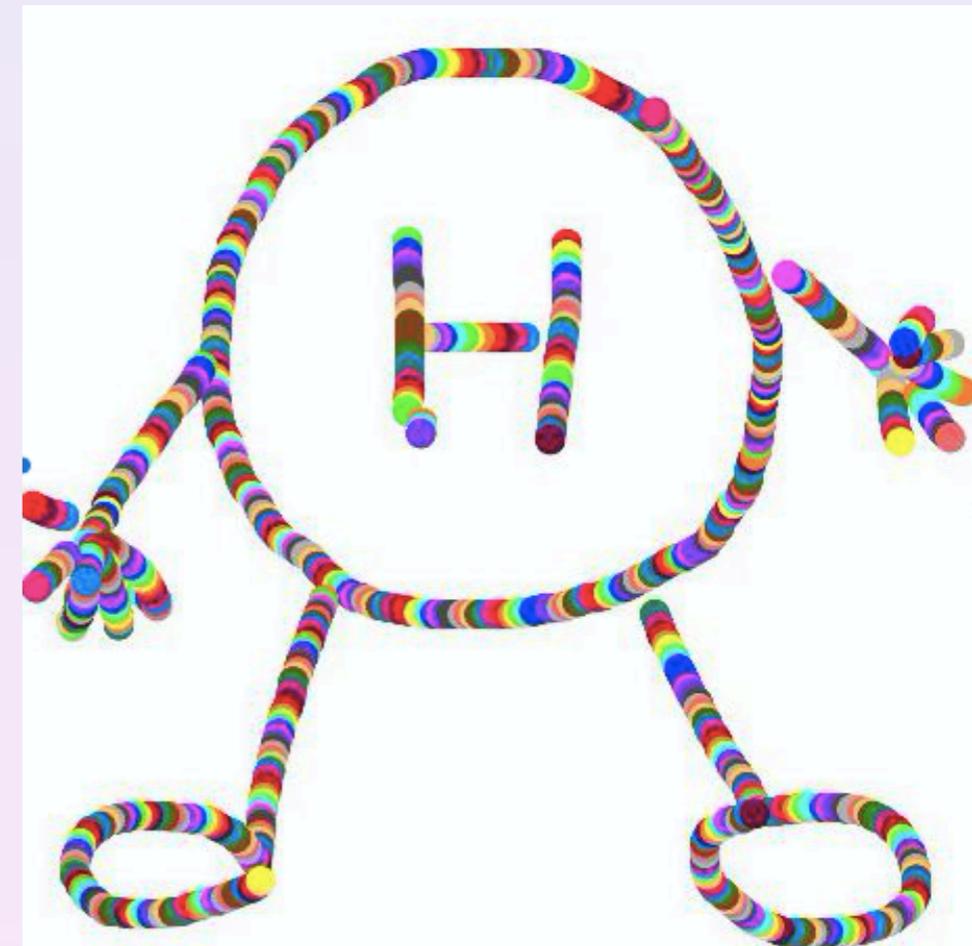
Ramona Gröber

based on work in collaboration with  
M. Chala and M. Spannowsky,  
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IPPP,  
Durham University

MC4BSM 2018

21/04/2018



# The Higgs boson discovery...



With the Higgs boson the last missing ingredient of the Standard Model is found ...

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With the Higgs boson the last missing ingredient of the Standard Model is found ...

...but is it the only Higgs boson? Is it elementary or composite?  
Is the Higgs sector really as predicted by the SM?

# Open problems of the Standard Model

- Hierarchy the electroweak scale?  
Why is  $m_H \ll \Lambda_{\text{Planck}}$ ?



connected to Higgs sector

- Dark matter



could there be a connection  
to the Higgs sector?

- ....

# Open problems of the Standard Model

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Why is  $m_H \ll \Lambda_{\text{Planck}}$ ?



connected to Higgs sector

Explain both within the  
same framework?

- Dark matter



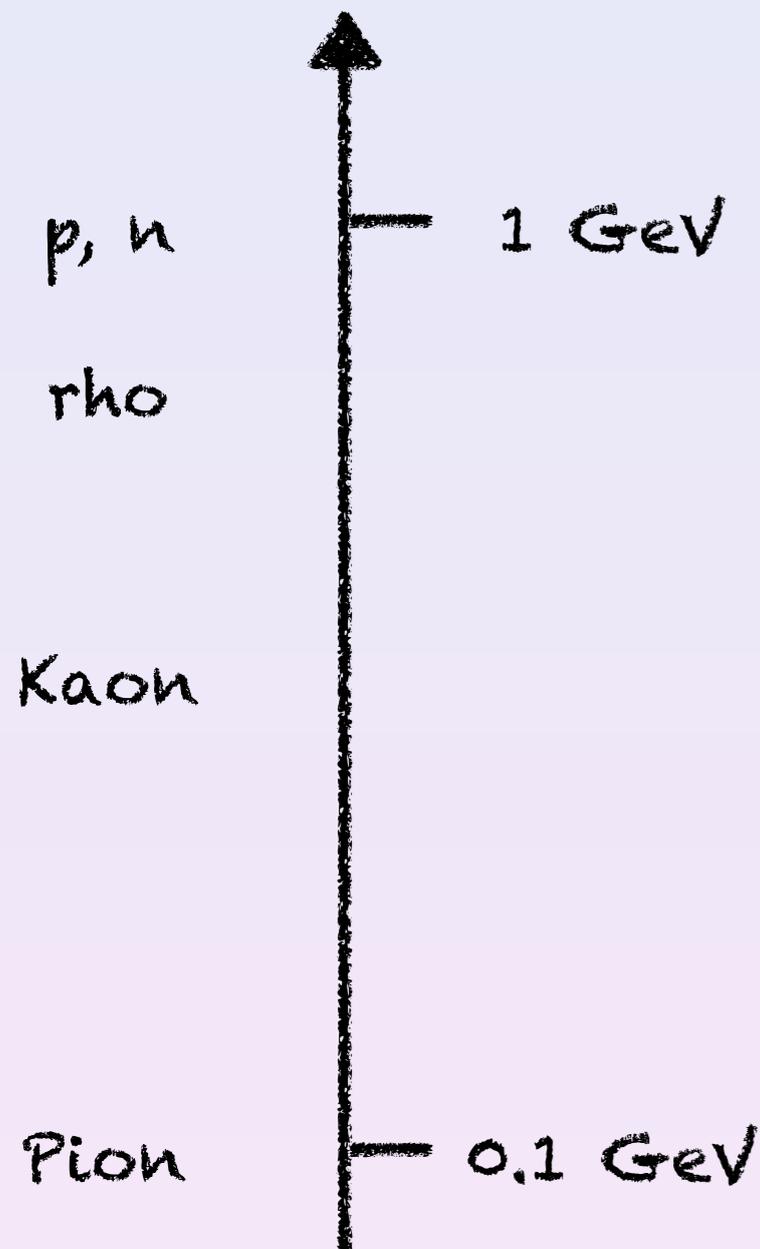
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- ....

# Outline

- Introduction to Composite Higgs Models
- Parameterisation of Dark Matter in Composite Higgs Models
- Collider probes of Dark Matter in Composite Higgs Models

# Composite Scalars in QCD



Spectrum of QCD:

Scalars without hierarchy problem

The QCD scale cuts their quantum corrections naturally off

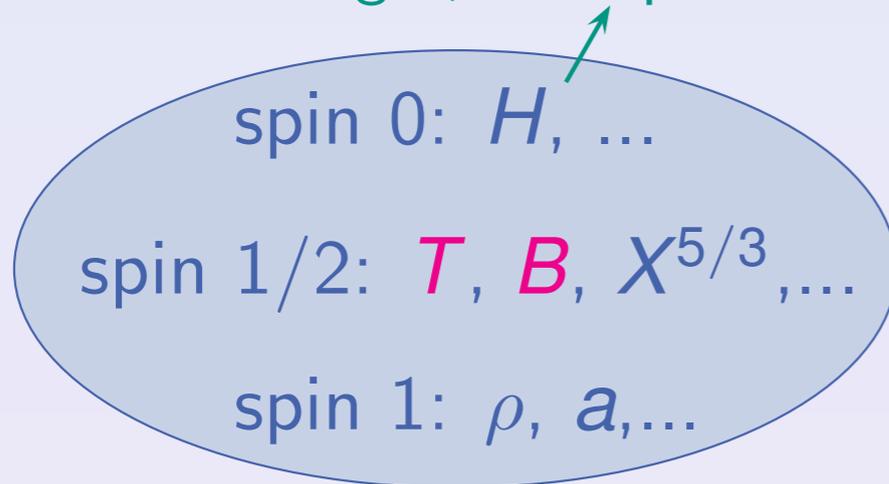
Pions as pseudo-Nambu Goldstone bosons, naturally much lighter than QCD scale

QCD scale is natural, can be largely separated from any high scale due to logarithmical running

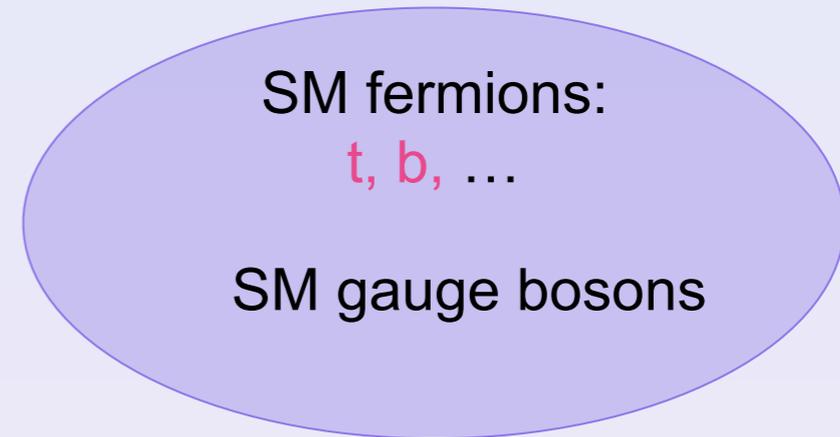
# Composite Higgs Models

[Georgi, Kaplan '84]

light, since pseudo-Goldstone boson



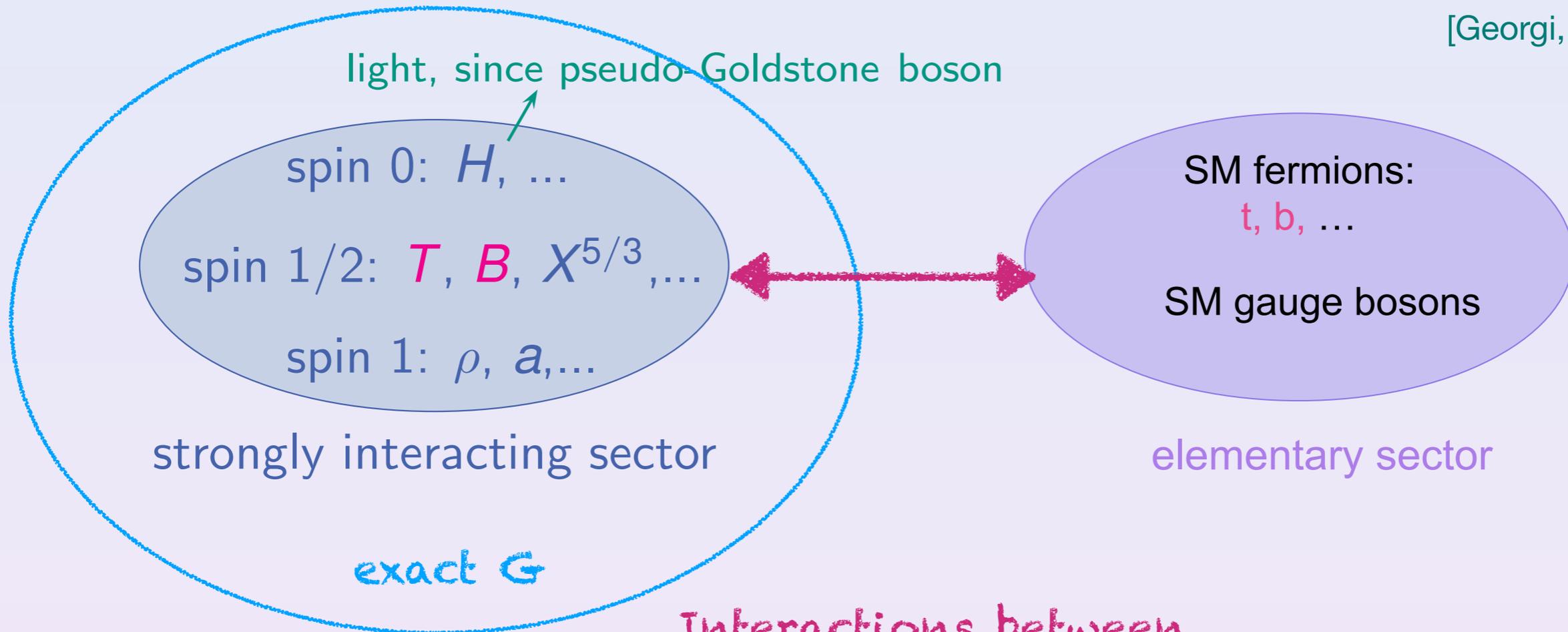
strongly interacting sector



elementary sector

# Composite Higgs Models

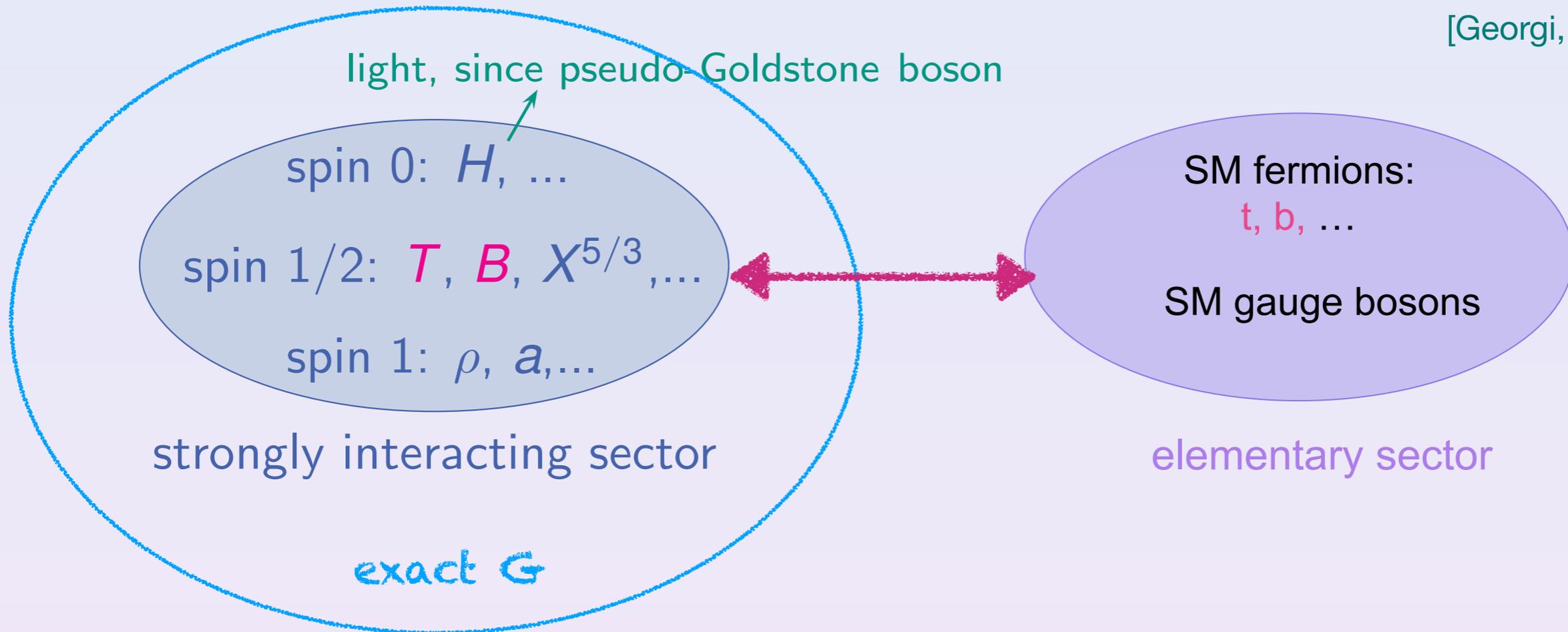
[Georgi, Kaplan '84]



Interactions between elementary and strongly interacting sector break  $G$  at scale  $f$ ; coset  $G/H$  should contain the SM gauge group

# Composite Higgs Models

[Georgi, Kaplan '84]



Higgs mass generated by quantum corrections

**Partial compositeness:** top quark mass generated by linear interactions with strongly interacting sector

**Minimal Model:**  $SO(5)/SO(4)$  [Agashe, Contino, Pomarol '04]

4 Goldstone bosons  
(1 Higgs + 3 usual would-be GBs)

# Lagrangian for a Composite Higgs

Lagrangian from CCWZ construction: [Callan, Coleman, Wess, Zumino '69]

Goldstone matrix ( $X$  denote the broken generators)

$$U = e^{-i\frac{\sqrt{2}}{f}\pi^{\hat{a}}X^a}$$

Defining

$$iU^{-1}\partial_{\mu}U = d_{\mu,a}X^a + e_{\mu,a}T^a$$

the Lagrangian is

$$\mathcal{L} = \frac{f^2}{4}\text{Tr}(d_{\mu}d^{\mu})$$

Minimal model: [Agashe, Contino, Pomarol '04]

more details in [Panico, Wulzer '15]

We take a  $\Sigma_0 = (0, 0, 0, 0, 1)^T$  to project on coset space.

Then

$$\mathcal{L} = \frac{f^2}{2}(D_{\mu}\Sigma)^{\dagger}D^{\mu}\Sigma, \quad \text{with } \Sigma = U\Sigma_0,$$

$$\mathcal{L} = \frac{1}{2}\partial_{\mu}h\partial^{\mu}h + \frac{g^2}{4}f^2\sin^2\left(\frac{h}{f}\right)W_{\mu}^{+}W^{\mu-} + \frac{g^2}{8c_W^2}f^2\sin^2\left(\frac{h}{f}\right)Z_{\mu}Z^{\mu}.$$

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Leads to non-linearities

$$\xi = \frac{v^2}{f^2} = \sin^2\frac{\langle h \rangle}{f}$$

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$$\frac{g_{hVV}}{g_{hVV}^{SM}} = \sqrt{1 - \xi}$$

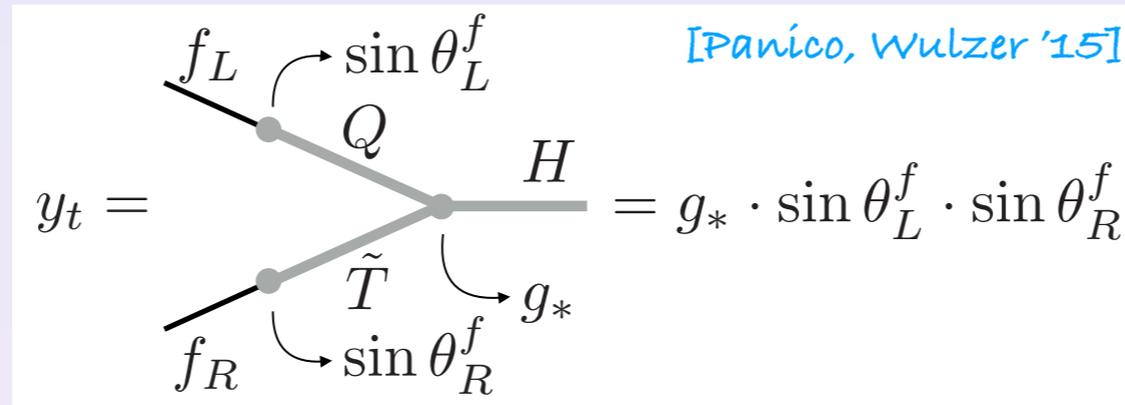
# Partial compositeness

[Kaplan '91]

Elementary fermions mix with strong-interacting sector by linear couplings

$$\mathcal{L} = \lambda_L \bar{q}_L \mathcal{O}_R + \lambda_R \bar{t}_R \mathcal{O}_L$$

Mixing with top partners generate the top Yukawas



If we are only interested in the non-linearities:

Example: fermions transforming in the fundamental of  $SO(5)$

$$Q_L^{2/3} = \frac{1}{\sqrt{2}} \left( d_L, -id_L, u_L, iu_L, 0 \right)^T, \quad U_R = \frac{1}{\sqrt{2}} \left( 0, 0, 0, 0, \sqrt{2}u_R \right)^T$$

$$\mathcal{L}_Y = f \left[ -y_u (\bar{U}_R \Sigma) (\Sigma^T Q_L^{2/3}) - y_d (\bar{D}_R \Sigma) (\Sigma^T Q_L^{-1/3}) \right] + \text{h.c.}$$

$$\longrightarrow \text{MCHM5: } \frac{g_{h\bar{f}f}}{g_{h\bar{f}f}^{SM}} = \frac{1-2\xi}{\sqrt{1-\xi}} \quad \text{MCHM10: } \frac{g_{h\bar{f}f}}{g_{h\bar{f}f}^{SM}} = \frac{1-2\xi}{\sqrt{1-\xi}} \quad \text{MCHM4: } \frac{g_{h\bar{f}f}}{g_{h\bar{f}f}^{SM}} = \sqrt{1-\xi}$$

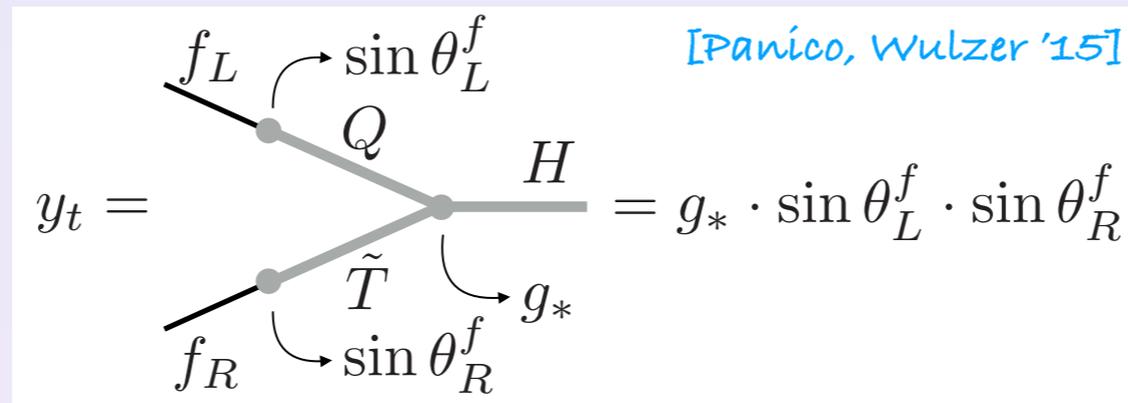
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The couplings break the global symmetry explicitly

→ Connection between top partner masses and Higgs mass

$$\frac{m_h^2}{m_t^2} \simeq \frac{N_c}{\pi^2} \frac{m_\psi^2}{f^2}$$

Low tuning = light top partner masses

[Matsedonskyi, Panico, Wulzer '12,  
Marzocca, Serone, Shu '12, Pomarol, Riva '12,  
Panico, Redi, Tesi, Wulzer '12,  
Pappadopulo, Thamm, Torre '13]

# Dark Matter in Composite Higgs Models

# Non-minimal Composite Higgs Models

[Mrazek et al '11]

$G$	$H$	$N_G$	NGBs rep. $[H] = \text{rep.}[SU(2) \times SU(2)]$
SO(5)	SO(4)	4	$4 = (\mathbf{2}, \mathbf{2})$
SO(6)	SO(5)	5	$5 = (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$ [Gripaios et al '09; Frigerio et al '12; Marzocca, Urbano '14]
SO(6)	SO(4) $\times$ SO(2)	8	$4_{+2} + \bar{4}_{-2} = 2 \times (\mathbf{2}, \mathbf{2})$ [Mrazek et al '11, De Curtis et al '16]
SO(7)	SO(6)	6	$6 = 2 \times (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$ [Balkin et al '17]
SO(7)	$G_2$	7	$7 = (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$ [Chala '12; Ballesteros et al '16]
SO(7)	SO(5) $\times$ SO(2)	10	$10_0 = (\mathbf{3}, \mathbf{1}) + (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$
SO(7)	$[SO(3)]^3$	12	$(\mathbf{2}, \mathbf{2}, \mathbf{3}) = 3 \times (\mathbf{2}, \mathbf{2})$
Sp(6)	Sp(4) $\times$ SU(2)	8	$(\mathbf{4}, \mathbf{2}) = 2 \times (\mathbf{2}, \mathbf{2}), (\mathbf{2}, \mathbf{2}) + 2 \times (\mathbf{2}, \mathbf{1})$
SU(5)	SU(4) $\times$ U(1)	8	$4_{-5} + \bar{4}_{+5} = 2 \times (\mathbf{2}, \mathbf{2})$
SU(5)	SO(5)	14	$14 = (\mathbf{3}, \mathbf{3}) + (\mathbf{2}, \mathbf{2}) + (\mathbf{1}, \mathbf{1})$

Larger coset space



extended Higgs sector

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Larger coset space



extended Higgs sector

If new scalar stable

i.e. if there is a  $Z_2$  or  $U(1)$  symmetry



possible dark matter candidate

explanation why

WIMP mass scale  $\approx$  electroweak scale

# Composite Higgs Dark Matter

General parameterisation: [Chala, RG, Spannowsky '18]

$$L = |D_\mu H|^2 \left[ 1 - a_1 \frac{S^2}{f^2} \right] + \frac{a_2}{f^2} \partial_\mu |H|^2 (S \partial_\mu S) + \frac{1}{2} (\partial_\mu S)^2 \left[ 1 - 2a_3 \frac{|H|^2}{f^2} \right] \\ - m_\rho^2 f^2 \frac{N_c y_t^2}{(4\pi)^2} \left[ -\alpha \frac{|H|^2}{f^2} + \beta \frac{|H|^4}{f^4} + \gamma \frac{S^2}{f^2} + \delta \frac{S^2 |H|^2}{f^4} \right] + \left[ i\epsilon \frac{y_t}{f^2} S^2 \bar{q}_L H t_R + \text{h.c.} \right] + \dots$$

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Annihilation  
cross section  
dominated by  
 $H^2 S^2$  interactions

Relic density

$$\Omega h^2 \sim m_S^2 / V^2 \sim f^2 / g_\rho^2$$

using MicrOmegas

$$a = a_1 = a_3 = a_3$$

$$V \sim \frac{2iN_c m_\rho^2}{(4\pi)^2 f^2} [2(2a_1 + 2a_2 + a_3)\gamma - \delta]$$

Main difference to non-composite case: derivative interactions

# Matching to concrete models

[Chala, RG, Spannowsky '18]

$\mathcal{G}/\mathcal{H}$	$q_L + t_R$	$a_1$	$a_2$	$a_3$	$\gamma$	$\delta$
$SO(6)/SO(5)$	<b>6 + 1</b>				–	–
	<b>6 + 15</b>	1/3	1/3	1/3	$\ll 1$	$\ll 1$
	<b>15 + 15</b>				$\ll 1$	$\ll 1$
	<b>20 + 1</b>				1/4	1/5
$SO(7)/SO(6)$	<b>7 + 1</b>				–	–
	<b>7 + 7</b>	1/3	1/3	1/3	–	–
	<b>27 + 1</b>				$\leq 1/4$	$\leq 1/5$
$SO(7)/G_2$	<b>8 + 8</b>	1/3	1/3	1/3	–	–
	<b>35 + 1</b>				1/4	1/5
$SO(6)/SO(4)$	<b>6 + 6</b>	0	1/6	1/3	–	–
$SO(5) \times U(1)/SO(4)$	<b>5 + 5</b>	0	0	0	$\ll 1$	$\ll 1$
$SO(7)/SO(5)$	<b>7 + 7</b>	$< 1/3$	$< 1/3$	1/3	–	–
$SO(7)/SO(6)$ [complex case]	<b>27 + 1</b>	$\sim 0.3$	$\sim 0.3$	$\sim 0.3$	$\sim 1/4$	$\sim \sqrt{2}/5$

# Collider searches: vector-like quarks

Bi-doublet under  $SU(2)_L \times SU(2)_R$

$$\text{BR}(T, X_{2/3} \rightarrow ht) \sim \text{BR}(T, X_{2/3} \rightarrow Zt) \sim 0.5$$

$$\text{BR}(B \rightarrow W^- t) \sim \text{BR}(X_{5/3} \rightarrow W^+ t) \sim 1$$

Singlet

$$\text{BR}(T' \rightarrow St) \sim 1$$

Current limits with VLQ limits [\[Chala '17\]](#)

$$m_\rho = g_\rho f < 1.2 \text{ TeV}$$

High luminosity LHC

$$m_\rho = g_\rho f < 1.7 \text{ TeV}$$

# vector-like quarks @ 100 TeV

3-lepton final state

lepton cuts

$$|\eta_\ell| < 2.5$$

$$p_{T,\ell_1} > 250 \text{ GeV}$$

$$p_{T,\ell_2} > 100 \text{ GeV}$$

$$p_{T,\ell_3} > 20 \text{ GeV}$$

at least 4 jets with

$$p_{T,j} > 40 \text{ GeV}$$

$$|\eta_j| < 5$$

$$p_{T,j_1} > 70 \text{ GeV}$$

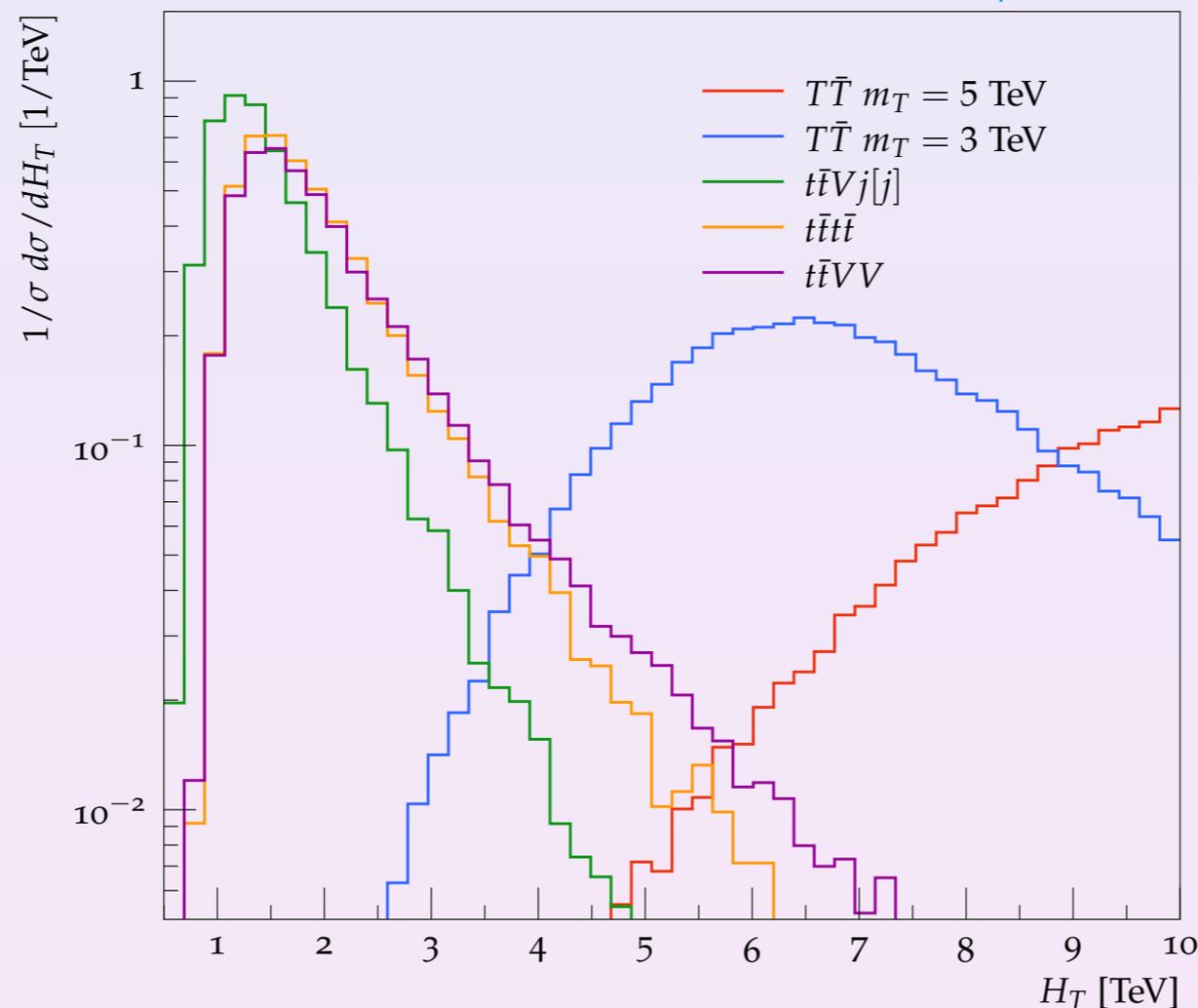
angular separation

$$\Delta R(j, \ell) = \sqrt{\Delta\phi_{j\ell}^2 + \Delta\eta_{j\ell}^2} > 0.3$$

exactly two b-jets

$$\Delta R(j, b) > 0.3.$$

[Chala, RG, Spannowsky '18]



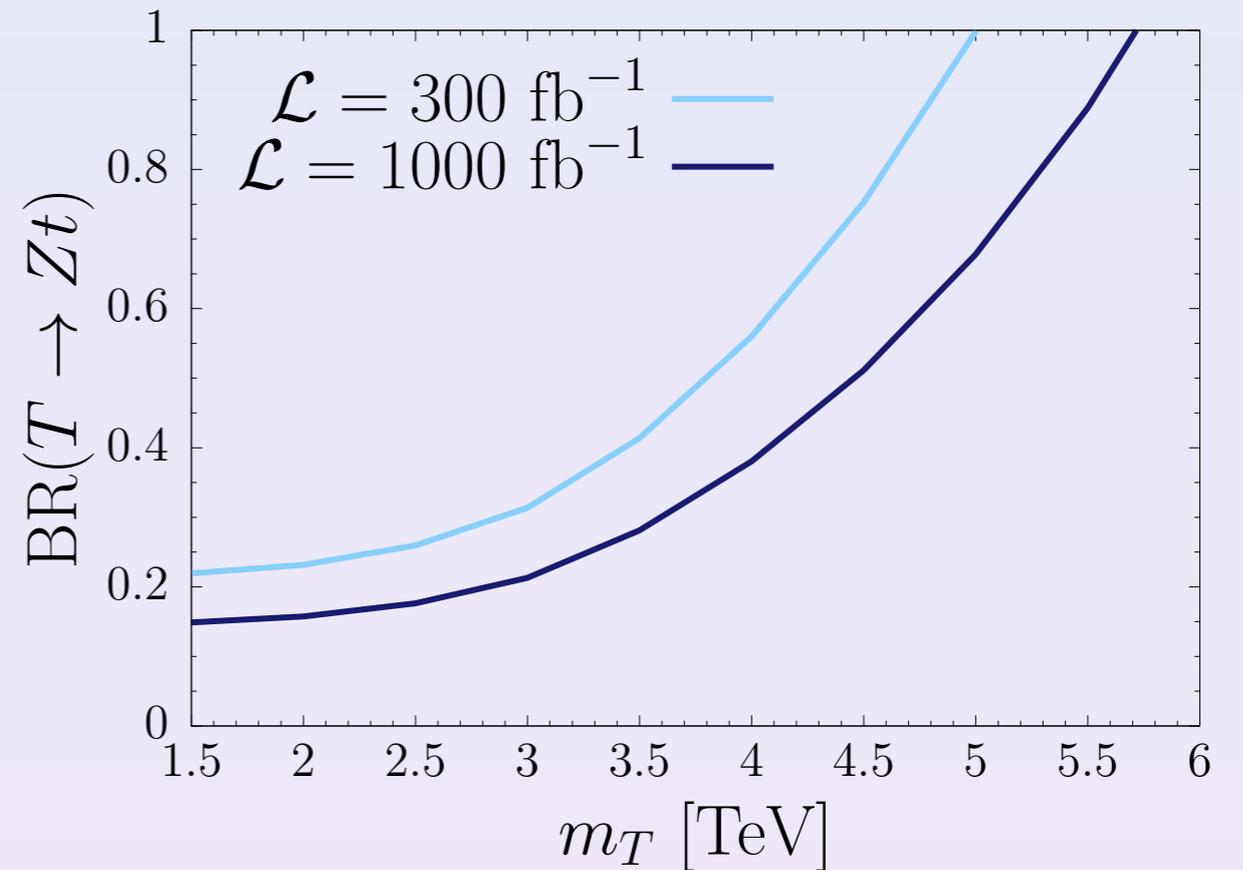
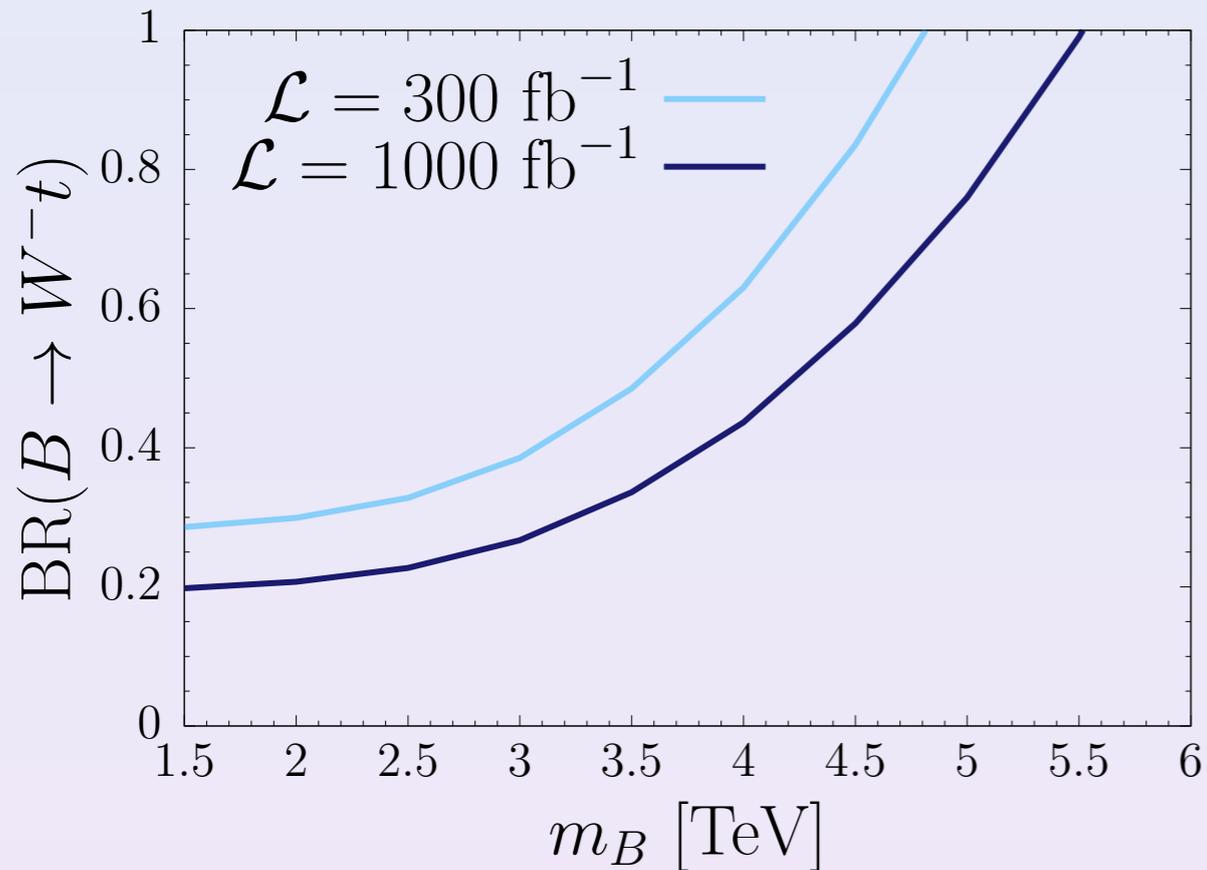
cut on  $H_T > 6 \text{ TeV}$

for top-partner also  
one reconstructed  
Z boson

$$71 \text{ GeV} < M_{\ell^+\ell^-} < 111 \text{ GeV}$$

using  
MG5\_AMC@NLO,  
Herwig, Sherpa,  
Rivet

# vector-like quarks @ 100 TeV



VLQs can be excluded up to at  $\mathcal{L} = 1000 \text{ fb}^{-1}$

bottom-partner/(5/3)-charged  $m_{X_{5/3}} = 5.5 \text{ TeV}$

top-partner  $m_T = 5.7 \text{ TeV}$

4-plet  $m_\rho = 6.4 \text{ TeV}$

# vector-like quarks @ 100 TeV

singlet VLQ can decay with  $BR \approx 1$  to  $S t$

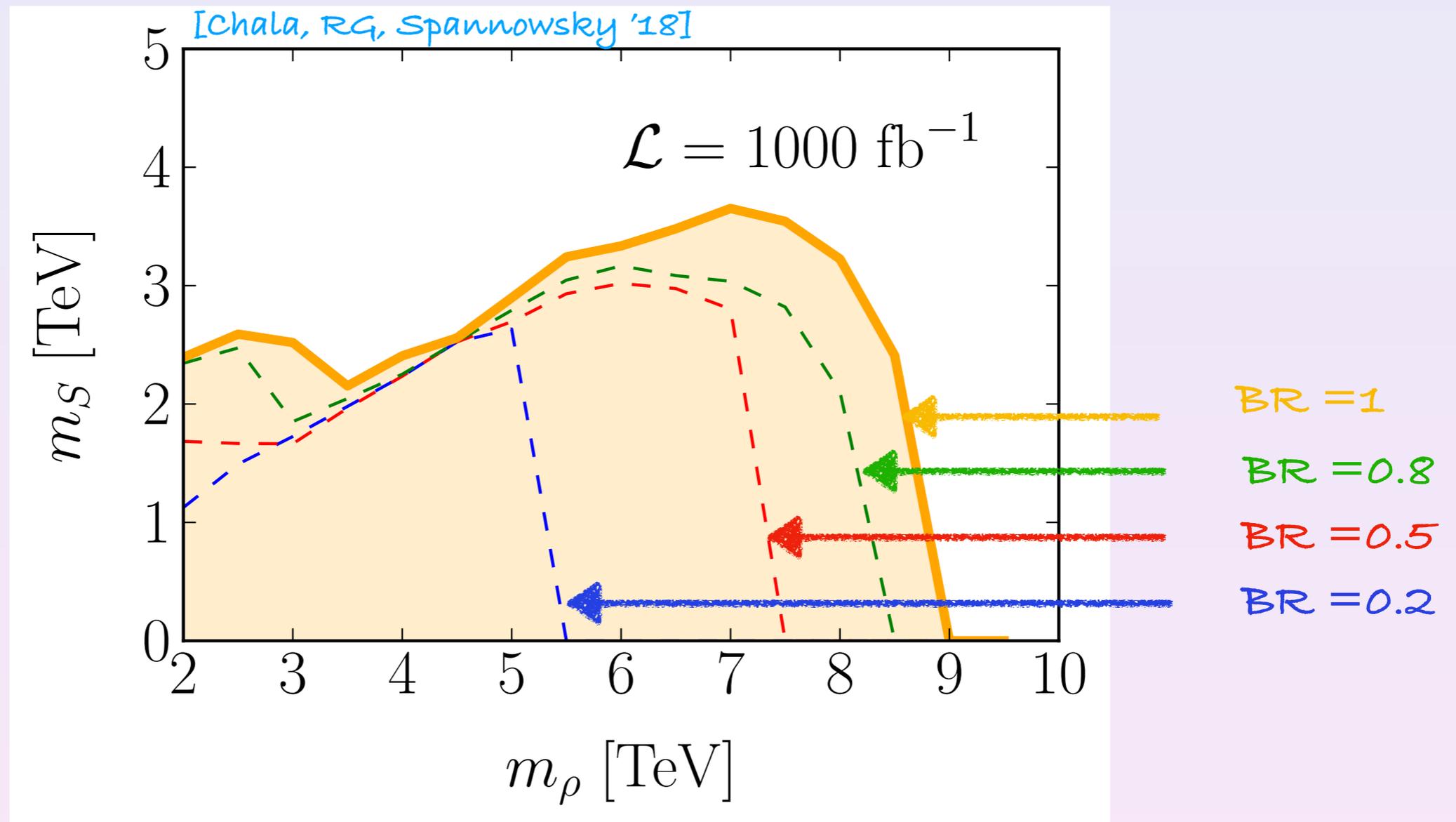
missing  $E_T$  and top quarks



SUSY searches for stops

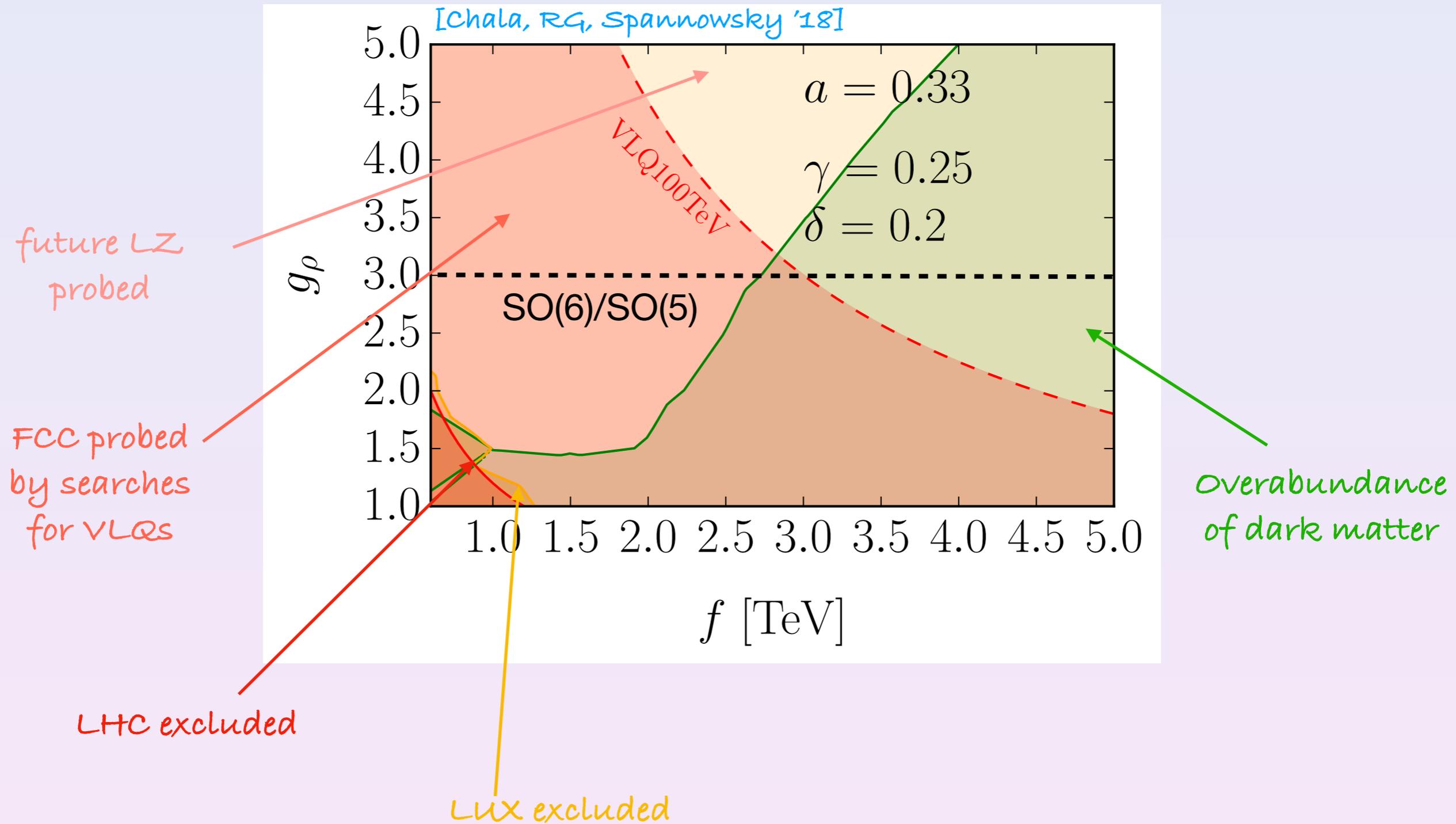
recast sensitivity study of

[Cohen, D'Angelo, Hance, Lou, Wacker '14]



# Results

more results in appendix



# Summary Composite Higgs Models

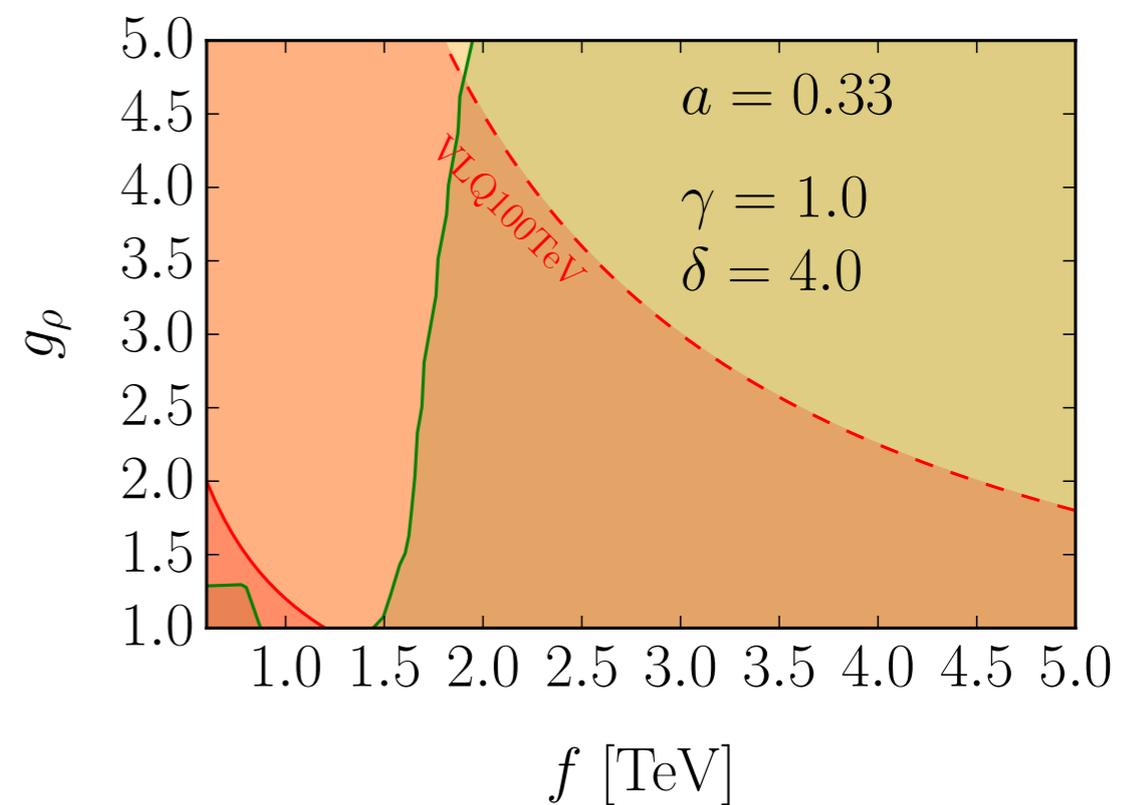
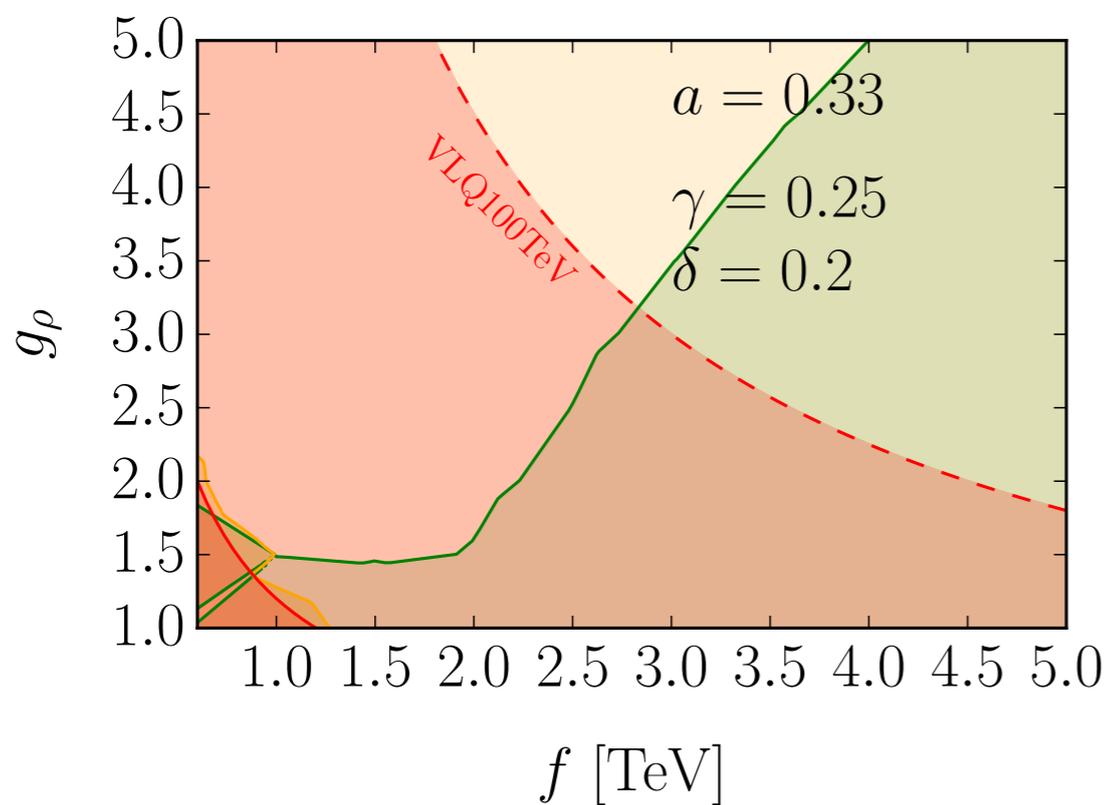
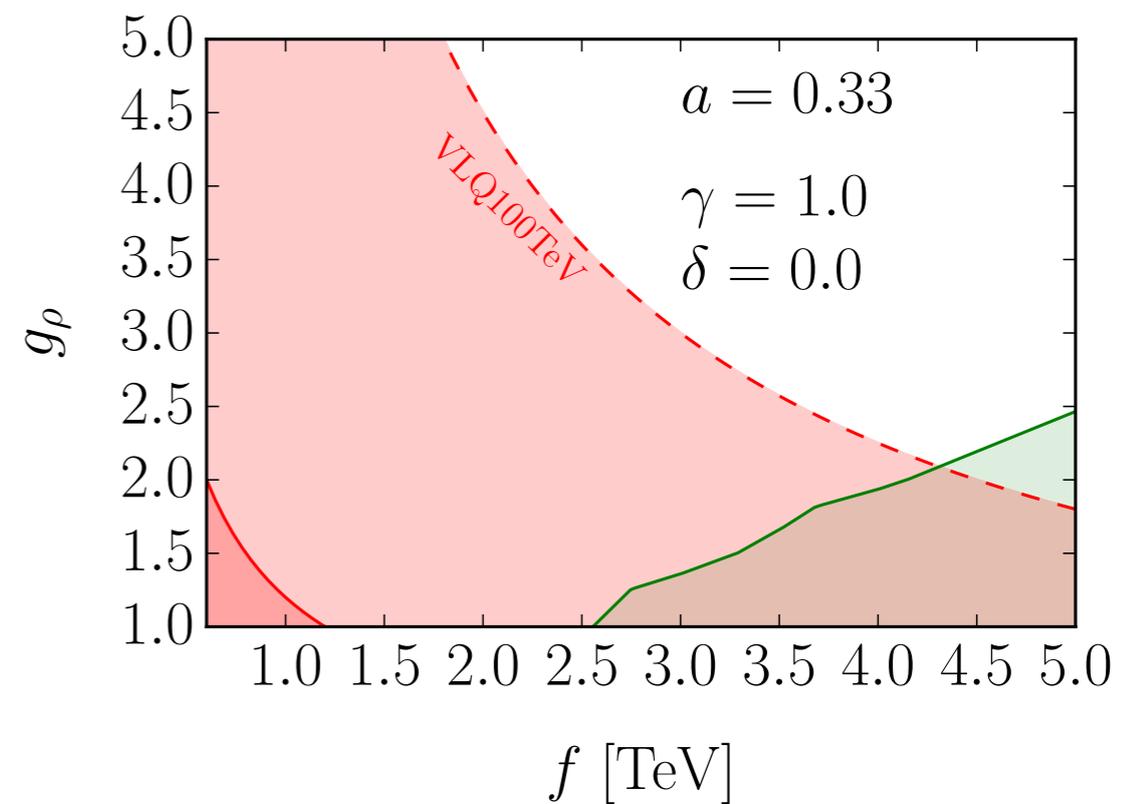
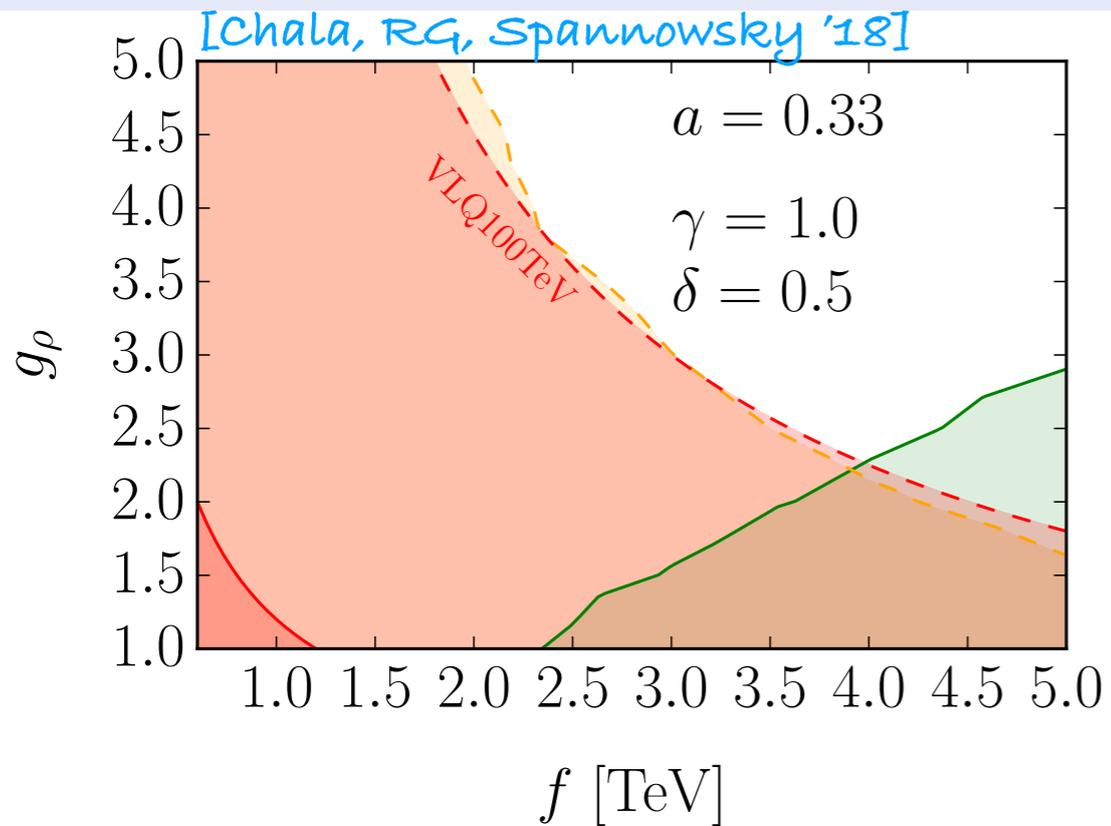
- Non-minimal Composite Higgs Models can provide a framework addressing both the Hierarchy problem and Dark matter
- Explanation for similarity of WIMP scale and electroweak scale
- We proposed a model-independent framework to parameterise Composite Higgs Models with Dark Matter
- Dark Matter scenarios in Composite Higgs Models can be probed at future experiments
  - Collider experiments : searches for VLQs
    - $m_\rho = 6.4 \text{ TeV}$  for VLQ decays to SM particles @ 100 TeV collider
    - $m_\rho = 9 \text{ TeV}$  for VLQ decays to dark matter @ 100 TeV collider
  - dark matter direct detection

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Thanks for your attention!

# More results



# Effect fermion couplings

effect sizeable if there is a cancellation in the computation of the relic density

$$L = |D_\mu H|^2 \left[ 1 - a_1 \frac{S^2}{f^2} \right] + \frac{a_2}{f^2} \partial_\mu |H|^2 (S \partial_\mu S) + \frac{1}{2} (\partial_\mu S)^2 \left[ 1 - 2a_3 \frac{|H|^2}{f^2} \right] \\ - m_\rho^2 f^2 \frac{N_c y_t^2}{(4\pi)^2} \left[ -\alpha \frac{|H|^2}{f^2} + \beta \frac{|H|^4}{f^4} + \gamma \frac{S^2}{f^2} + \delta \frac{S^2 |H|^2}{f^4} \right] + \left[ i\epsilon \frac{y_t}{f^2} S^2 \bar{q}_L H t_R + \text{h.c.} \right] + \dots$$

taking  $\epsilon$  into account

$\epsilon = 0$

