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# News from Top/QCD

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# Program

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## Top/~~QCD~~ Session

- C. Schwinn: Top coupling to Higgs and gauge bosons: 6 and 8 fermion final states → top couplings in the continuum
- S. Boogert:  $t\bar{t}$  threshold simulation update → top couplings at the threshold



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- M. Schumacher: Top Yukawa coupling from LC & LHC → synergy of LHC & ILC



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- M. Schumacher: Top Yukawa coupling from LC & LHC → synergy of LHC & ILC
- A. Signer: Effective theory for unstable particles → new conceptual and theoretical developments
- M. Slusarczyk: Two-loop QCD corrections to  $\Gamma_t$



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- A. Signer: Effective theory for unstable particles → new conceptual and theoretical developments
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## Other Sessions

- T. Gehrmann:  $e^+e^- \rightarrow 3$  jets at NNLO → Loopverein
- I. Melo: Signatures of EWSB in  $e^+e^- \rightarrow t\bar{t}\nu\bar{\nu}$  → EW & Altern. Theo.
- M. Spira: SUSY QCD corrections to  $e^+e^- \rightarrow t\bar{t}h$  → Loopverein
- M. Krämer: NLO Parton Showers → Loopverein



# Top Yukawa Coupling

## Linear Collider

threshold:  $\sigma(e^+e^- \rightarrow t\bar{t})$  at  $\sqrt{s} \approx 350$  GeV

$$\rightarrow V(r) = -\frac{C_F\alpha_s}{r} - \frac{g_{tth}^2}{r} e^{-m_h r}$$

$\mathcal{O}(5 - 10\%)$  correction

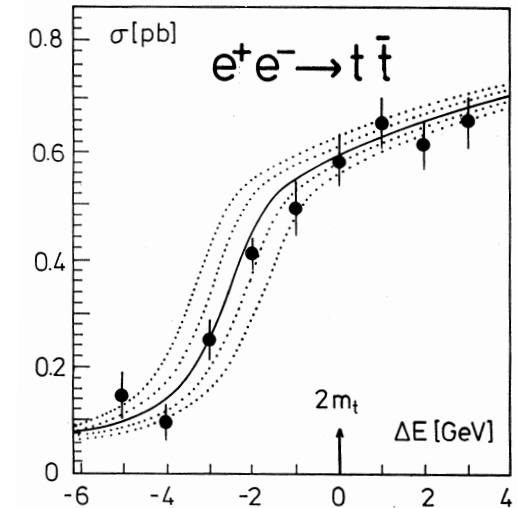
$$\rightarrow \delta g_{tth}/g_{tth} = 20 - 50\%$$

$$\delta M_{1S} \leq 50 \text{ MeV}, \delta\Gamma_t \sim 30 \text{ MeV}, \delta\alpha_s \sim 0.001$$

$$(\mathcal{L} = 300 \text{ fb}^{-1}, m_h \lesssim 120 \text{ GeV})$$

(assumed perfectly known Lumi spectrum)

- perfect knowledge of luminosity spectrum assumed
- only for light Higgs
- depends on knowledge other parameters, QCD theory
- 1st phase



Martinez, Miquel



# Top Yukawa Coupling

## Linear Collider

threshold:  $\sigma(e^+e^- \rightarrow t\bar{t})$  at  $\sqrt{s} \approx 350$  GeV  $\rightarrow$  difficult, 1st phase

continuum:  $\sigma(e^+e^- \rightarrow t\bar{t}h) \sim g_{tth}^2$

$\text{Br}(h \rightarrow W^+W^-)$   
 $\text{Br}(h \rightarrow b\bar{b})$       precision: 2 – 5% ( $e^+e^- \rightarrow Zh$ )

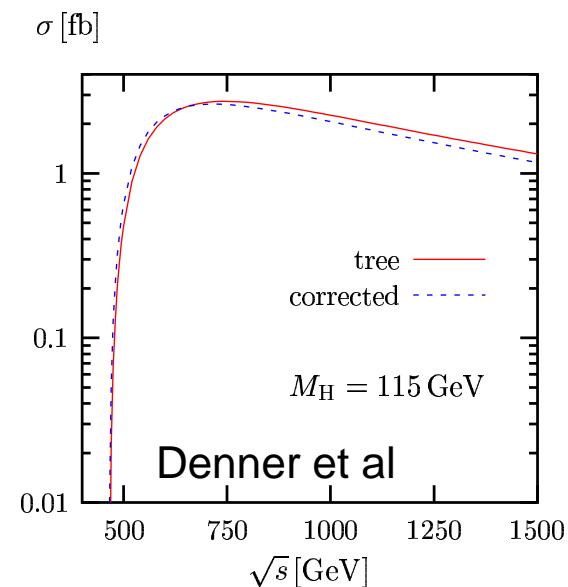
$\rightarrow \delta g_{tth}/g_{tth} = 5 - 6\%$  ( $m_h = 120$  GeV)

$\delta g_{tth}/g_{tth} = 10\%$  ( $m_h = 190$  GeV)

( $\sqrt{s} = 800$  GeV ,  $\mathcal{L} = 1000$  fb $^{-1}$ )

- $\sqrt{s} > 500$  GeV crucially needed
- 2nd phase

Gay, Besson, Winter



# Top Yukawa Coupling

## Linear Collider

threshold:  $\sigma(e^+e^- \rightarrow t\bar{t})$  at  $\sqrt{s} \approx 350$  GeV

→ difficult, 1st phase

continuum:  $\sigma(e^+e^- \rightarrow t\bar{t}h) \sim g_{t\bar{t}h}^2$

→ 2nd phase

LHC  $gg \rightarrow t\bar{t}h$ ,  $h \rightarrow W^+W^-$   
 $h \rightarrow b\bar{b}$

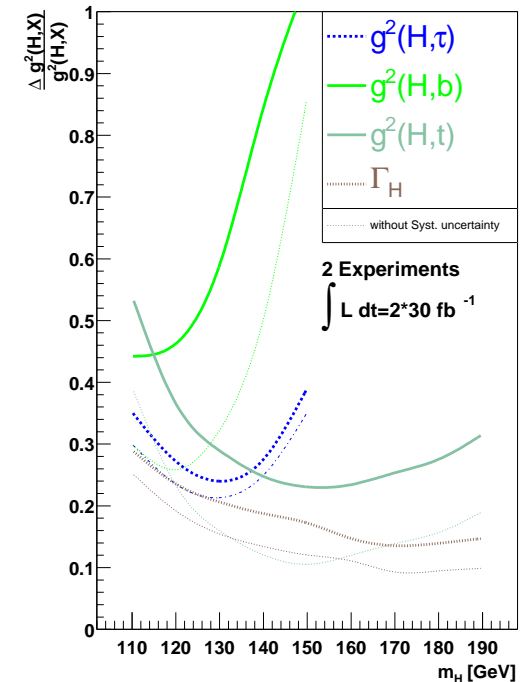
(many analyses)

- no absolute measurement of  $\sigma_{\text{tot}}$  or  $\Gamma(h \rightarrow XX)$   
 $\rightarrow g_{t\bar{t}h}^2 \times Br$

- recent analysis:  $g_{hW} = g_{hW}^{\text{SM}} \pm 2.5\%$   
 $g_{hZ} = g_{hZ}^{\text{SM}} \pm 2.5\%$   
 SM particle content

Dührssen et al.

$\rightarrow \delta g_{t\bar{t}h} / g_{t\bar{t}h} \sim 12 - 25\%$





# Top Yukawa Coupling

## LHC & Linear Collider

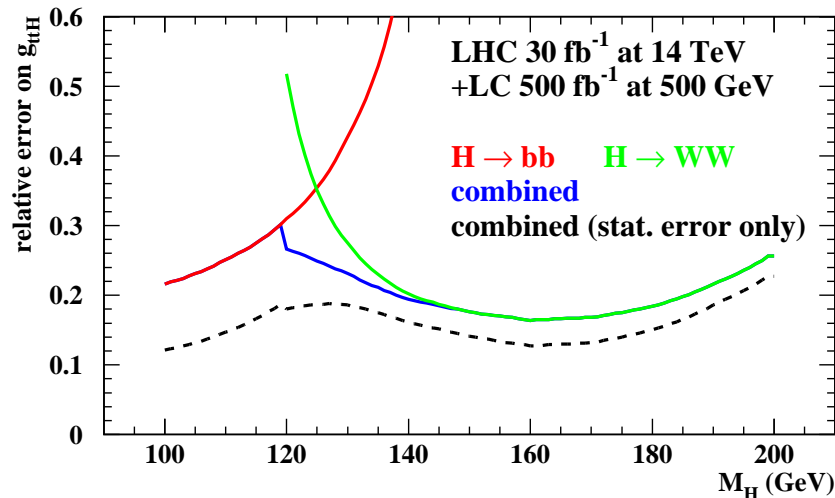
Schuhmacher, Desch

- LC, 1st phase:  $\Gamma(h \rightarrow b\bar{b})$ ,  $\Gamma(h \rightarrow W^+W^-)$   
from  $e^+e^- \rightarrow Zh$   
use  $Z \rightarrow l^+l^-$  recoil mass spectrum

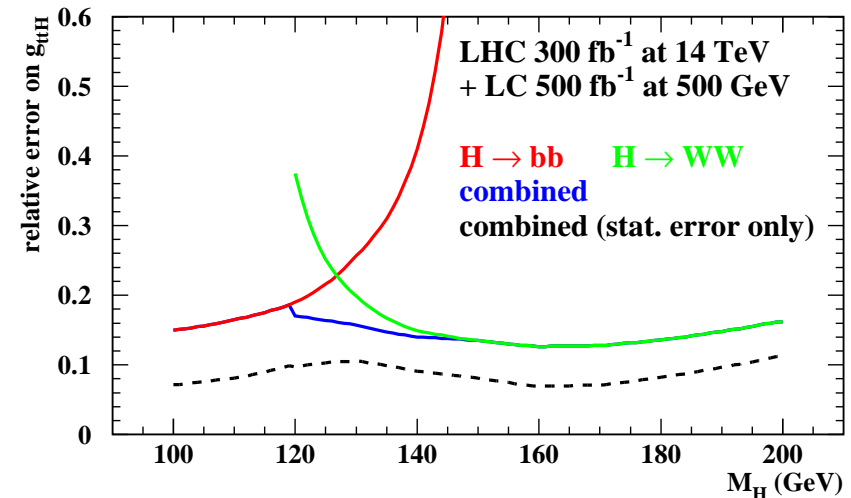
↓  
Input

- LHC:  $gg \rightarrow tth$

⇒ 1st phase measurement



$$\delta g_{tth}/g_{tth} = 16 - 27\%$$



$$\delta g_{tth}/g_{tth} = 13 - 17\%$$

(incl. systematic errors)

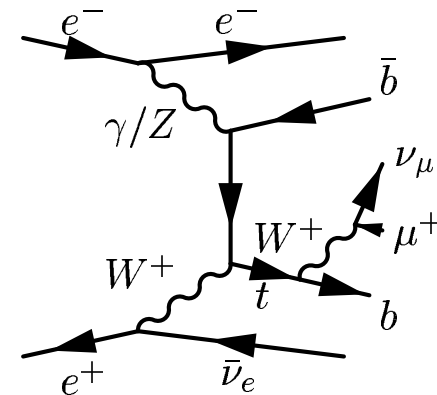


# 6 and 8 Fermion Final States

→  $\Gamma_t = 1.4 \text{ GeV}$ : study of fermionic final states in top production

Schwinn

- O'Mega & WHIZARD updates
- single top production:  $e^+e^- \rightarrow e\bar{\nu}_e t\bar{b}$  →  $|V_{tb}|$ 
  - signal & background diagrams & cuts
  - inconsistencies selecting only top diagrams
  - gauge invariance for small electron scattering angle
  - background  $\sim 5\%$  effect after cuts
  - dependence on prescription for finite top lifetime



$\sigma(e^+e^- \rightarrow b\bar{b}e^-\bar{\nu}_e\mu^+\nu_\mu)(fb)$  with  $\theta(e^-) > 0.01^\circ$

$\sqrt{s}$	Fixed Width	Complex Mass	Fudge Factor	Step Width
500	5.91 (1)	5.92 (2)	5.83 (1)	9.3 (1.9)
800	3.541 (8)	3.549 (8)	3.528 (8)	4.5 (3)
2000	3.62 (2)	3.64 (1)	3.62 (2)	98.0 (4)

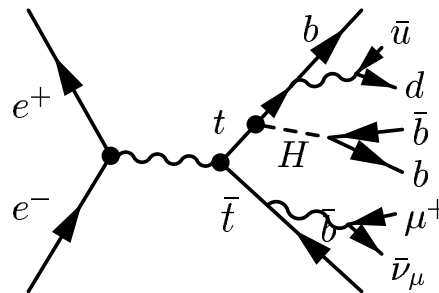


# 6 and 8 Fermion Final States

→  $\Gamma_t = 1.4 \text{ GeV}$ : study of fermionic final states in top production

Schwinn

- $e^+e^- \rightarrow t\bar{t}h \rightarrow g_{tth}^2$ 
  - 6-fermion final state  $b\bar{b}b\bar{b}W^+W^-$ :  $\sim 3\%$
  - 8-fermion final state  $< 3\%$  (first studies)



→ plans: anomalous couplings  
QCD effects  
polarizations



# Unstable Particles

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- processes with (near) on-shell massive & unstable particles
    - resonances (Z-pole,  $n$ -fermion final states)
    - non-relativistic systems ( $t\bar{t}$  threshold,  $W^+W^-$ )
    - finite-T QCD
  - issues: factorizable vs. non-factorizable, on-shell vs. off-shell, gauge invariance, double counting, scheme-dependence, etc.
  - traditional approaches:
    - pole scheme
    - complex mass scheme
    - fermion loop scheme, . . .
- guiding principles:
- gauge invariance
  - validity for all energies

Fadin, Khoze; Denner et al., . . .  
Stuart; Aepli et al; . . .  
Beenakker et al

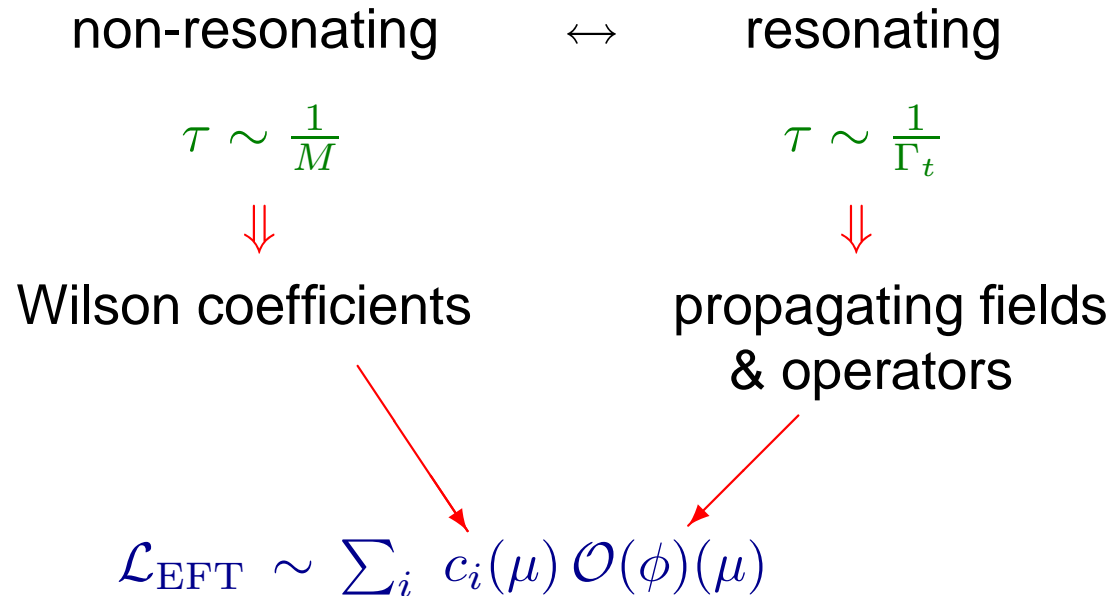


# Unstable Particles

## Alternative Approach: Effective Field Theory

Signer

- separation of effects at different length scales



# Unstable Particles

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## Alternative Approach: Effective Field Theory

- separation of effects at different length scales
- power counting in terms of  $\delta = \frac{\Gamma_t}{M} \sim \alpha$ 
  - unique  $\delta$ -scaling for field, operators & loops
  - double counting avoided



# Unstable Particles

## Alternative Approach: Effective Field Theory

- separation of effects at different length scales
- power counting in terms of  $\delta = \frac{\Gamma_t}{M} \sim \alpha$ 
  - unique  $\delta$ -scaling for field, operators & loops
  - double counting avoided
- gauge invariance “automatic” (on-shell matching, operators)
- exact form of EFT depends on system
- no description off resonance (breakdown of  $\delta$ -expansion)
- gimmicks:
  - general (Feynman) rules to any order
  - factorization scheme & UV-divergences
    - ↔ renormalization, anomalous dimensions
    - ↔ summation of  $\ln(\Gamma/M)$  to all orders
- toy model Signer, Beneke, Chapovsky, Zanderighi  
“real” application in progress . . . no free lunch!



# The Top Decay Width

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- **SM:**  $\text{Br}(t \rightarrow bW) \approx 100\%$  & rare decays
- MSSM:**  $\text{Br}(t \rightarrow bH^+) \approx \text{several}\%$  ( $1 \ll \tan\beta < 100$ )
- $\text{Br}(t \rightarrow \tilde{t}\tilde{\chi}) \lesssim 10\%$





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- **Corrections to  $\Gamma(t \rightarrow bW)$**

$\mathcal{O}(\alpha_s):$   $= -8.4\%$

Jezbek, Kühn

$\mathcal{O}(\alpha, \text{ew}):$   $\simeq -2\%$

Denner, Sack

$\mathcal{O}(\alpha_s^2):$   $\longrightarrow$  required for  $t\bar{t}$  threshold at NNLL

$\longrightarrow$  **BLM:**  $\mathcal{O}(\alpha_s^2\beta_0)$

Voloshin, Smith

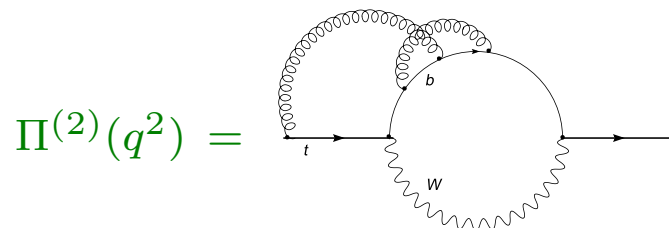
$\longrightarrow M_W = 0, m_b = 0$

Czarnecki, Melnikov

$\longrightarrow M_W \neq 0, m_b = 0$

**Pade approximation**

Chetyrkin et al.



$\longrightarrow$  expansion for  $\frac{q^2}{m_t^2} \ll 1, \frac{M_W^2}{q^2} \ll 1$

use  $q^2 = m_t^2, M_W^2 = 0$

impose analytic properties, cuts



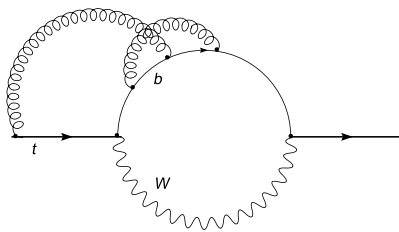
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- $\mathcal{O}(\alpha_s^2)$  corrections to  $\Gamma(t \rightarrow bW)$   $M_W \neq 0, m_b = 0$

Analytic computation

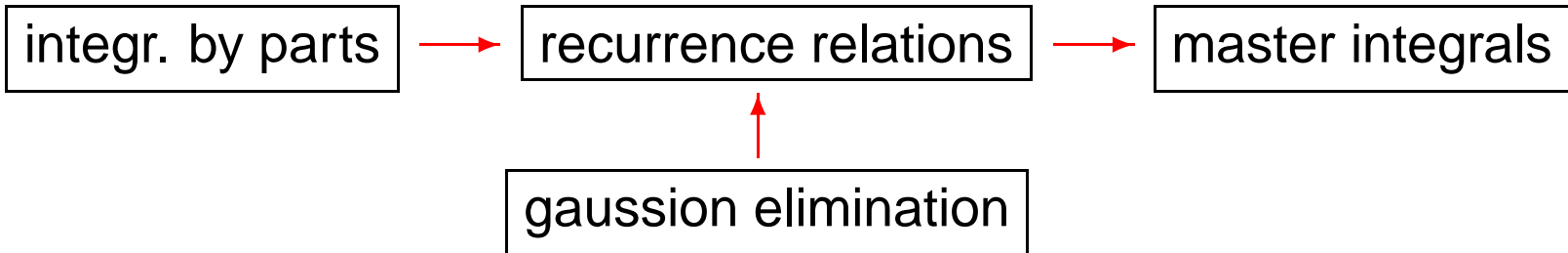
Slusarczyk, Czarnecki

$\Pi^{(2)}(m_t^2) =$  

→ start with  $M_W = 0$  ( $\frac{M_W^2}{m_t^2} = 0.213$ )

asymptotic expansion in  $\frac{M_W^2}{m_t^2}$

use optical theorem



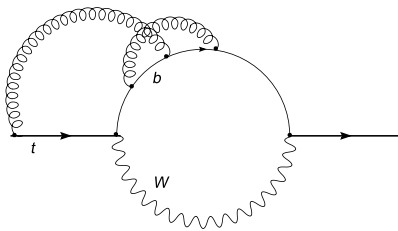
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asymptotic expansion in  $\frac{M_W^2}{m_t^2}$

use optical theorem

→ expansion up to  $(\frac{M_W^2}{m_t^2})^5$

$$\rightarrow \Gamma(t \rightarrow bW) = \Gamma_0 \left[ 1 + \frac{\alpha_s}{\pi} X_1 + \left( \frac{\alpha_s}{\pi} \right)^2 15.5(1) \right]$$

↓  
-2.15%

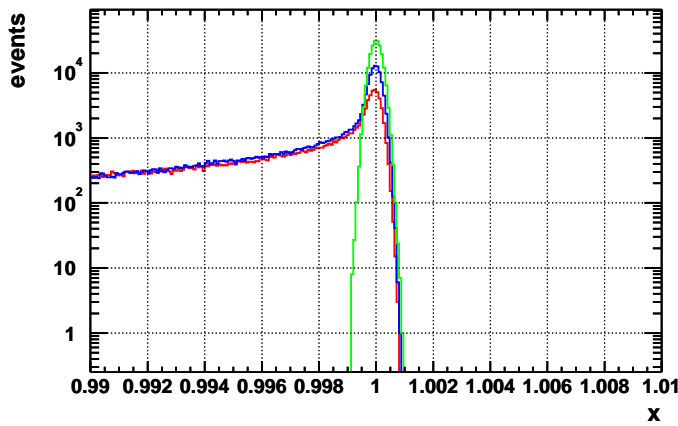
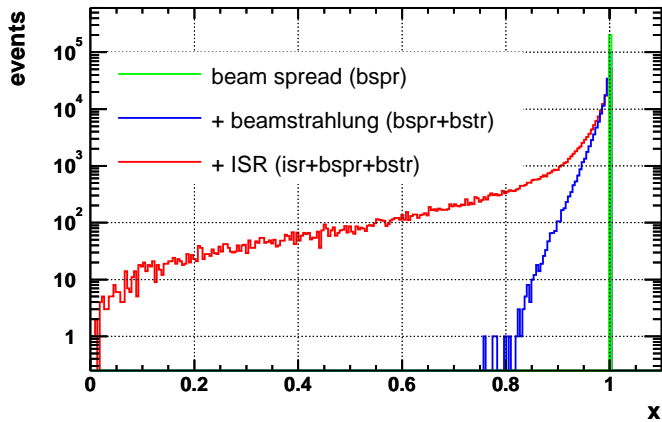


# Top-Antitop Threshold

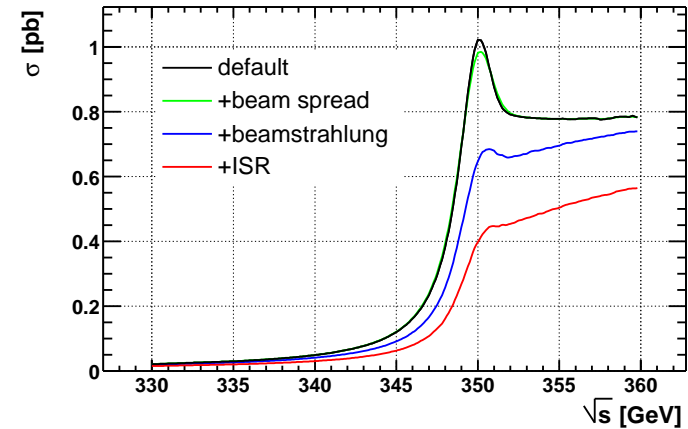
$\sigma(e^+e^- \rightarrow t\bar{t})$  at  $\sqrt{s} \approx 350$  GeV  $\Rightarrow m_t, \alpha_s, \Gamma_t, (g_{tth})$

Influence of Luminosity spectrum

Boogert



$$\sigma(s) = \int_0^1 dx L(x) \sigma^0(x^2 s)$$



# Top-Antitop Threshold

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$$\sigma(e^+e^- \rightarrow t\bar{t}) \text{ at } \sqrt{s} \approx 350 \text{ GeV} \quad \Rightarrow m_t, \alpha_s, \Gamma_t, (g_{tth})$$

## Influence of Luminosity spectrum

Boogert

- previous WS's:
- measurement of  $L(x)$  (excl. beam energy spread)
    - Bhabba acollinearity
    - accelerator & beam simulations
  - TOPPIK interpolation

- this WS:
- beam energy spread included (cold & warm designs)
  - $L(x)$  parametrized ( $\sigma, a_0, a_2, a_3$ )



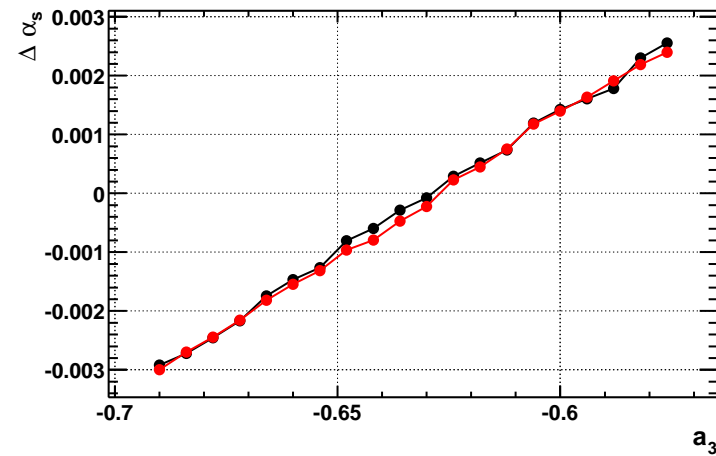
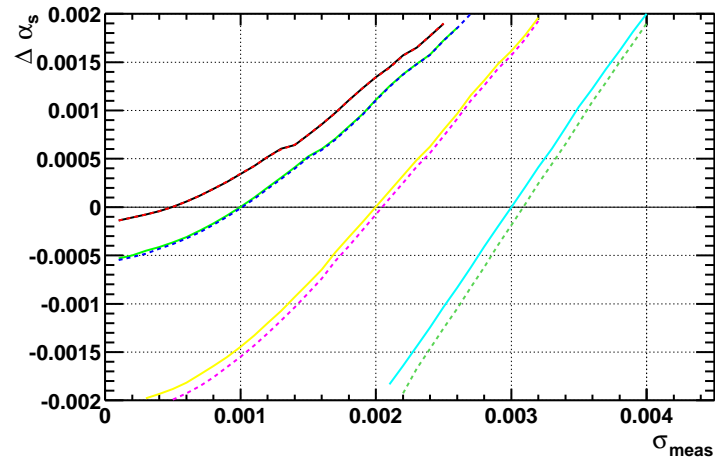
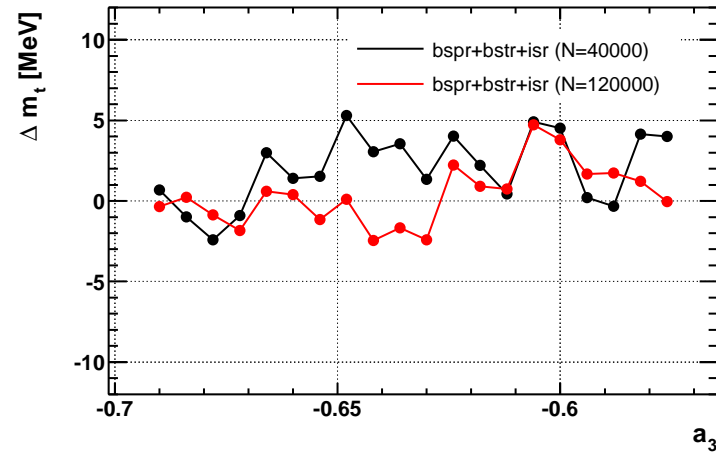
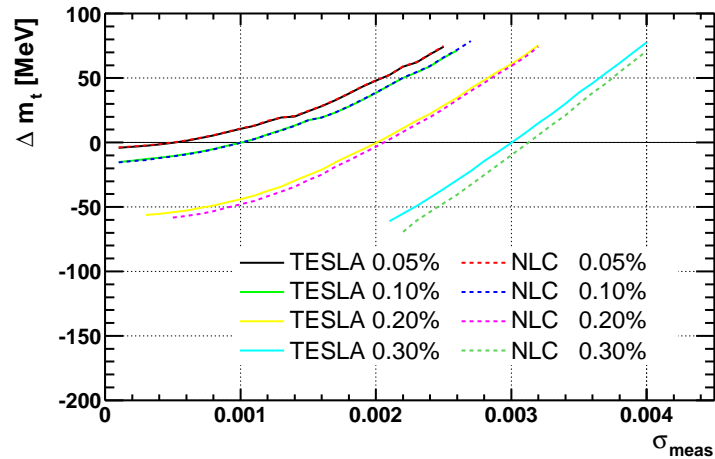
# Top-Antitop Threshold

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Influence of Luminosity spectrum

Boogert



# Top-Antitop Threshold

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$$\sigma(e^+e^- \rightarrow t\bar{t}) \text{ at } \sqrt{s} \approx 350 \text{ GeV} \quad \Rightarrow m_t, \alpha_s, \Gamma_t, (g_{tth})$$

Influence of Luminosity spectrum

Boogert

$$\begin{aligned} \rightarrow \Delta m_t &\approx -50 \text{ MeV} && \text{(Paris numbers)} \\ \Delta \alpha_s &\approx -0.0017 \text{ MeV} \\ \Delta \Gamma_t &\approx -13 \text{ MeV} \end{aligned}$$

... things to think of:

- optimized scan strategy
- top event generator
  - $A_{FB}$ , distributions, cuts
  - electroweak corrections  $\leftrightarrow$  unstable particles
- other thresholds



# Final Words

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- Plenty of problems to work on in SM top precision physics !  
NO Free Lunches !  
Kein Freibier !

