
T-odd Asymmetries in Chargino and Neutralino Production and Decay

Stefan Hesselbach

Institut für Theoretische Physik der Universität Wien

A. Bartl, H. Fraas, K. Hohenwarter-Sodek, G. Moortgat-Pick

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Outline

- Introduction
 - MSSM with complex parameters
 - complex parameters in chargino and neutralino sectors
- Aim: deriving the phases and analysing the CP structure of the theory
- T-odd asymmetries in chargino and neutralino sectors
 - full spin correlations between production and decay
 - triple products and T-odd asymmetries
 - for three-body and two-body decays
- Conclusions and outlook

- General MSSM:
 - Complex parameters in Higgs potential and soft SUSY breaking terms
- Physical phases of the parameters
 - μ : Higgs-higgsino mass parameter
 - M_1 : U(1) gaugino mass parameter
 - $m_{\tilde{g}}$: gluino mass
 - A_f : trilinear couplings of sfermions
- Introduction of CP violation
 - may help to explain baryon asymmetry of universe
 - constraints from electric dipole moments (EDMs) of e, n, Hg, Tl

[Ibrahim, Nath, '99; Barger, Falk, Han, Jiang, Li, Plehn, '01; Abel, Khalil, Lebedev, '01]

● **Chargino** mass matrix:
$$X = \begin{pmatrix} M_2 & \sqrt{2} m_W s_\beta \\ \sqrt{2} m_W c_\beta & \mu \end{pmatrix}$$

● **Neutralino** mass matrix:

$$Y = \begin{pmatrix} M_1 & 0 & -m_Z s_W c_\beta & m_Z s_W s_\beta \\ 0 & M_2 & m_Z c_W c_\beta & -m_Z c_W s_\beta \\ -m_Z s_W c_\beta & m_Z c_W c_\beta & 0 & -\mu \\ m_Z c_W c_\beta & -m_Z c_W s_\beta & -\mu & 0 \end{pmatrix}$$

$$s_\beta \equiv \sin \beta, c_\beta \equiv \cos \beta$$

μ : Higgs-higgsino mass parameter $\rightarrow |\mu|, \varphi_\mu$

M_1 : U(1) gaugino mass parameter $\rightarrow |M_1|, \varphi_{M_1}$

M_2 : SU(2) gaugino mass parameter

$\tan \beta = \frac{v_2}{v_1}$: ratio of Higgs vevs

T-odd asymmetries in $\tilde{\chi}^{\pm}, \tilde{\chi}^0$ sectors

Chargino/neutralino production with subsequent three-body decays

$$e^+e^- \longrightarrow \tilde{\chi}_i + \tilde{\chi}_j \longrightarrow \tilde{\chi}_i + \tilde{\chi}_1^0 f \bar{f}^{(')}$$

- **full spin correlation** between production and decay

[Moortgat-Pick, Fraas, '97; Moortgat-Pick, Fraas, Bartl, Majerotto, '98, '99; Choi, Song, Song, '99]

- amplitude squared $|T|^2 = PD + \Sigma_P^a \Sigma_D^a$

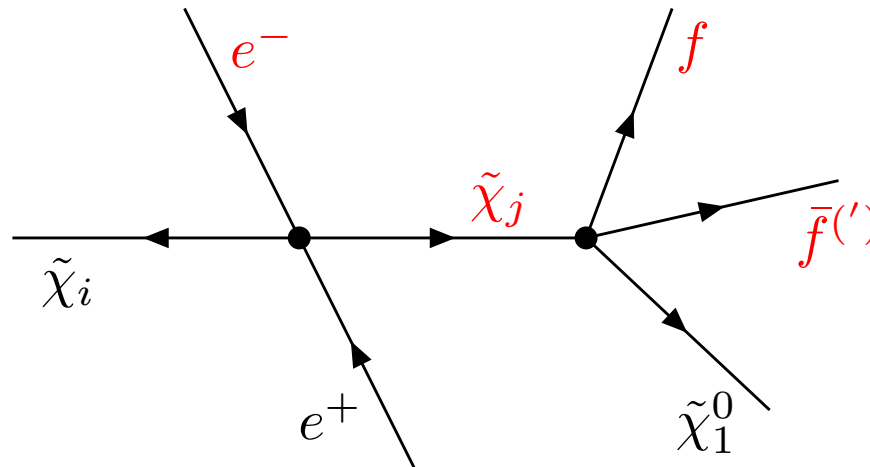
- in Σ_P^a and Σ_D^a : products like $i\epsilon_{\mu\nu\rho\sigma} p_i^\mu p_j^\nu p_k^\rho p_l^\sigma$

⇒ with **complex couplings**: real contributions to observables

⇒ CP violation at tree level

T-odd asymmetries in $\tilde{\chi}^{\pm}, \tilde{\chi}^0$ sectors

Triple products: $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_f \times \vec{p}_{\bar{f}'})$ or $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\tilde{\chi}_j} \times \vec{p}_f)$



→ T-odd asymmetry:

$$A_T = \frac{\sigma(\mathcal{T} > 0) - \sigma(\mathcal{T} < 0)}{\sigma(\mathcal{T} > 0) + \sigma(\mathcal{T} < 0)} = \frac{\int \text{sign}(\mathcal{T}) |\mathcal{T}|^2 d\text{Lips}}{\int |\mathcal{T}|^2 d\text{Lips}}$$

→ CP-odd, if final state interactions and finite-widths effects can be neglected

T-odd asymmetry in $\tilde{\chi}^0$ sector

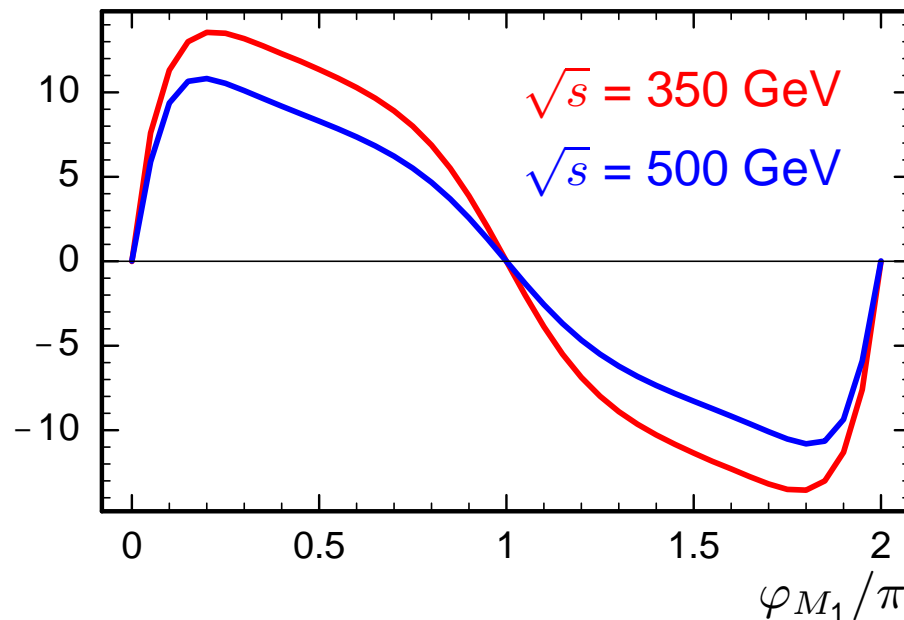
Asymmetry A_T for $e^+e^- \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_1^0 \ell^+ \ell^-$, $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\ell^+} \times \vec{p}_{\ell^-})$
 [Bartl, Fraas, SH, Hohenwarter-Sodek, Moortgat-Pick, hep-ph/0406190]

● $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$ for

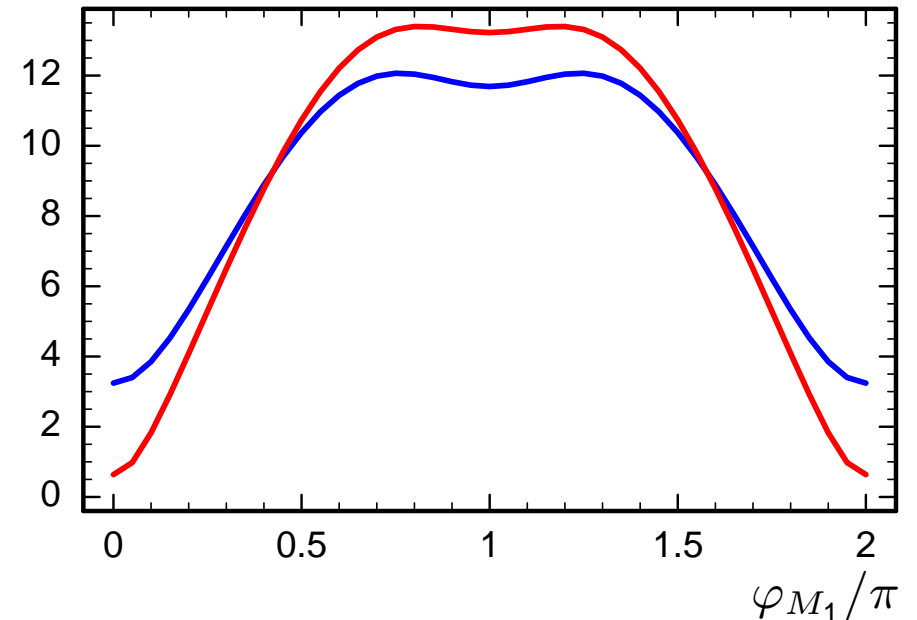
$\tan \beta = 10$, $M_2 = 300$ GeV, $|M_1| = 150$ GeV, $|\mu| = 200$ GeV, $\varphi_\mu = 0$

$m_{\tilde{e}_L} = 267.6$ GeV, $m_{\tilde{e}_R} = 224.4$ GeV, $P_{e^-} = -0.8$, $P_{e^+} = +0.6$

A_T in %

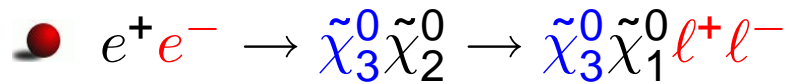


$\sigma(e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0) \cdot BR(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \ell^+ \ell^-) / \text{fb}$



→ A_T larger closer to threshold (spin correlations)

T-odd asymmetry in $\tilde{\chi}^0$ sector



Contours of A_T [in %] for

$$\tan\beta = 10, |M_1| = M_2 \frac{5}{3} \tan^2\theta_W,$$

$$m_{\tilde{e}_L} = 267.6 \text{ GeV}, m_{\tilde{e}_R} = 224.4 \text{ GeV}$$

$$\sqrt{s} = 500 \text{ GeV}, P_{e^-} = -0.8, P_{e^+} = +0.6$$

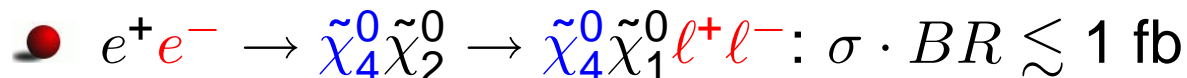
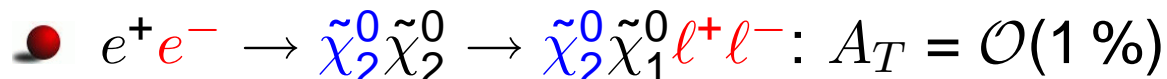
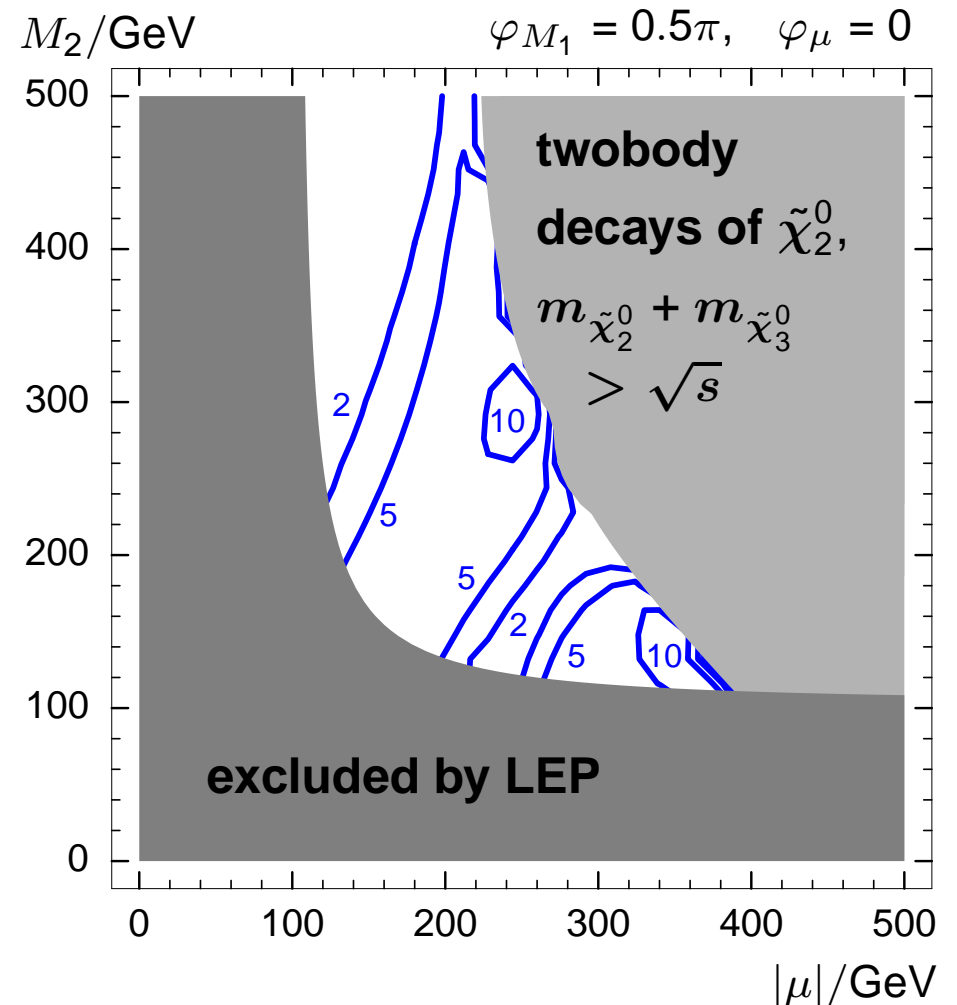
Dark shaded area:

$$m_{\tilde{\chi}_1^\pm} < 103 \text{ GeV}$$

Light shaded area:

$$m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0} > m_Z, m_{\tilde{\chi}_2^0} > m_{\tilde{e}_R} \text{ or}$$

$$m_{\tilde{\chi}_2^0} + m_{\tilde{\chi}_3^0} > \sqrt{s}$$



T-odd asymmetry in $\tilde{\chi}^\pm$ sector

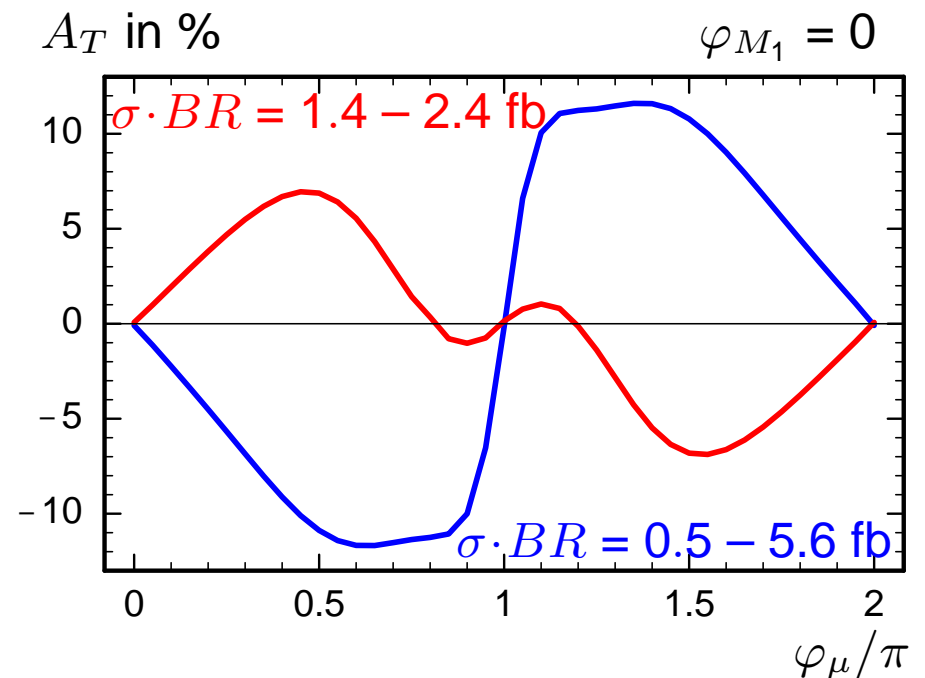
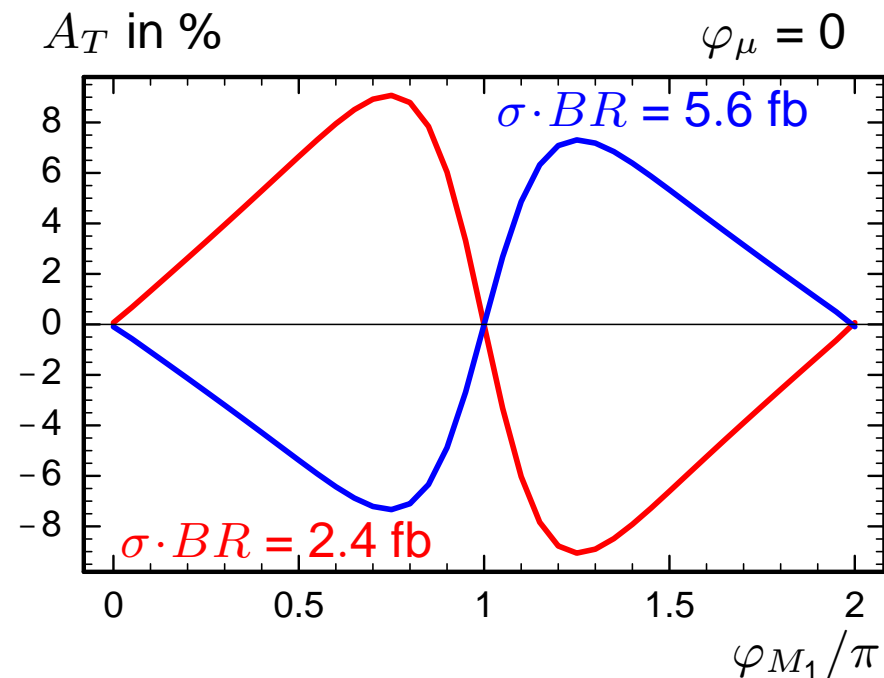
Asymmetry A_T for $e^+e^- \rightarrow \tilde{\chi}_j^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_j^- \tilde{\chi}_1^0 c\bar{s}$, $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\bar{s}} \times \vec{p}_c)$

→ tagging of c jet important

● $e^+e^- \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^0 c\bar{s}$ for

$\tan\beta = 5$, $M_2 = 150$ GeV, $|M_1| = M_2 5/3 \tan^2\theta_W$, $|\mu| = 320$ GeV, $m_{\tilde{\nu}} = 250$ GeV,

$m_{\tilde{u}_L} = 500$ GeV, $\sqrt{s} = 500$ GeV, $P_{e^-} = -0.8$, $P_{e^+} = +0.6$, $P_{e^-} = +0.8$, $P_{e^+} = -0.6$



T-odd asymmetry in $\tilde{\chi}^\pm$ sector

- Contours of A_T [in %] for $e^+e^- \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^0 c\bar{s}$

$$\tan \beta = 5, |M_1| = M_2 \frac{5}{3} \tan^2 \theta_W,$$

$$m_{\tilde{\nu}} = 250 \text{ GeV}, m_{\tilde{u}_L} = 500 \text{ GeV}$$

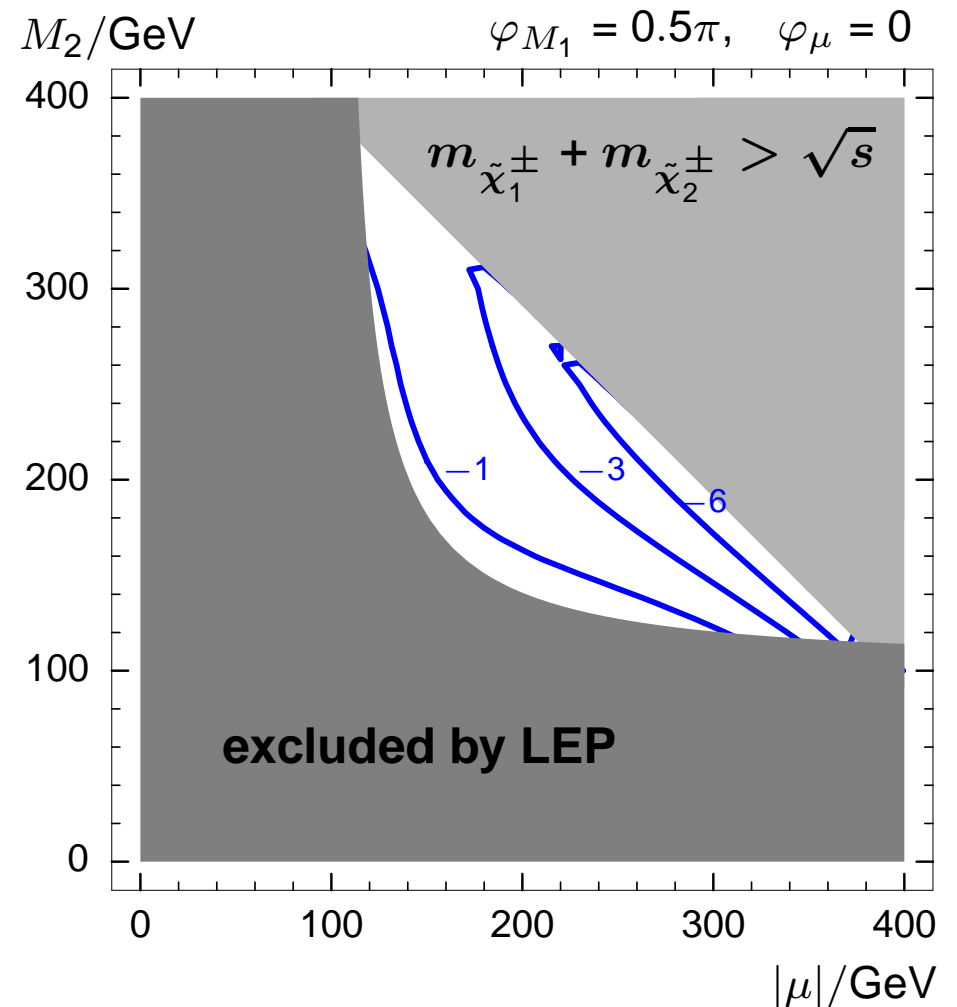
$$\sqrt{s} = 500 \text{ GeV}, P_{e^-} = -0.8, P_{e^+} = +0.6$$

Dark shaded area:

$$m_{\tilde{\chi}_1^\pm} < 103 \text{ GeV}$$

Light shaded area:

$$m_{\tilde{\chi}_1^\pm} + m_{\tilde{\chi}_2^\pm} > \sqrt{s}$$



T-odd asymmetry in $\tilde{\chi}^\pm$ sector

- Contours of A_T [in %] for $e^+e^- \rightarrow \tilde{\chi}_1^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^- \tilde{\chi}_1^0 c\bar{s}$

$$\tan \beta = 5, |M_1| = M_2 \frac{5}{3} \tan^2 \theta_W,$$

$$m_{\tilde{\nu}} = 250 \text{ GeV}, m_{\tilde{u}_L} = 500 \text{ GeV}$$

$$\sqrt{s} = 500 \text{ GeV}, P_{e^-} = -0.8, P_{e^+} = +0.6$$

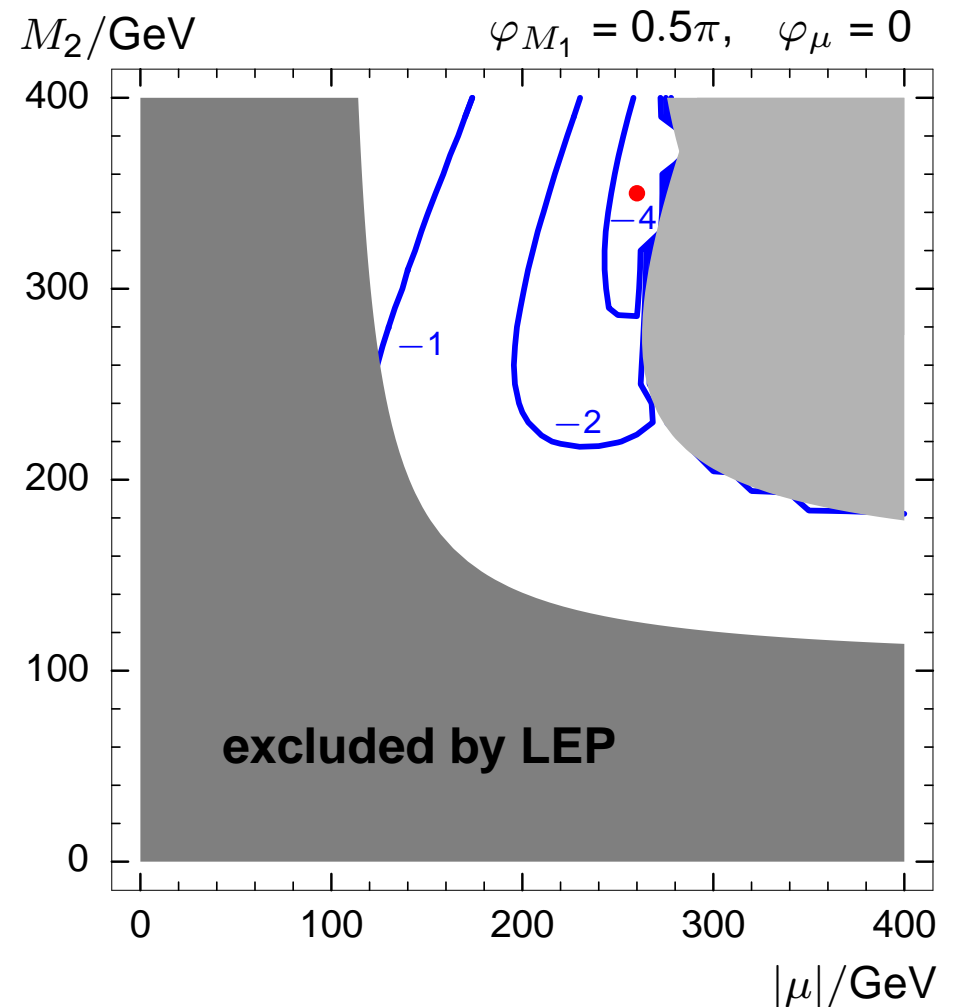
Dark shaded area:

$$m_{\tilde{\chi}_1^\pm} < 103 \text{ GeV}$$

Light shaded area:

$$2m_{\tilde{\chi}_1^\pm} > \sqrt{s} \text{ or}$$

$$m_{\tilde{\chi}_1^\pm} > m_W + m_{\tilde{\chi}_1^0}$$



$$|\mu| = 260 \text{ GeV}, M_2 = 350 \text{ GeV}: \sigma(e^+e^- \rightarrow \tilde{\chi}_1^- \tilde{\chi}_1^+) \cdot BR(\tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^0 c\bar{s}) = 117 \text{ fb}$$

T-odd asymmetry in $\tilde{\chi}^\pm$ sector

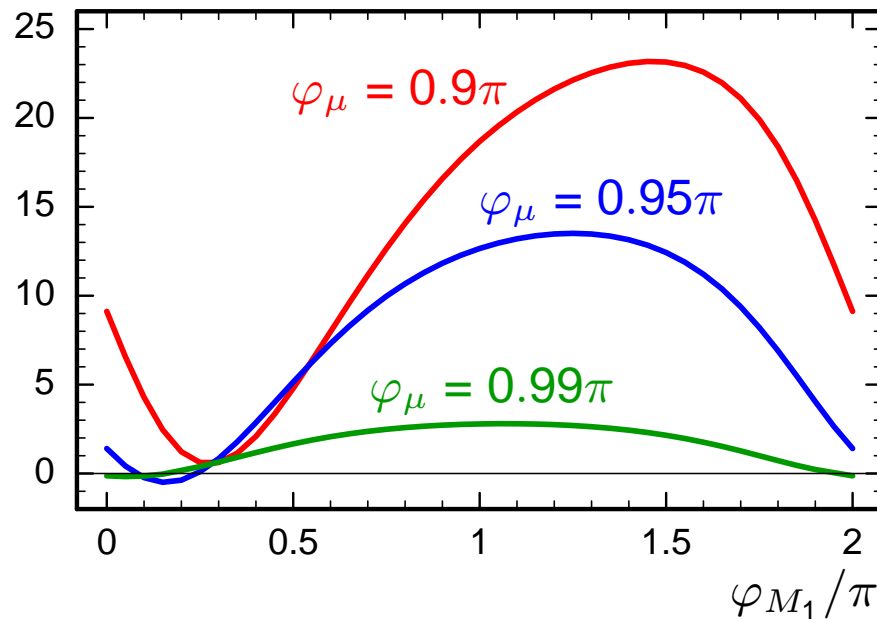
Asymmetry A_T for $e^+e^- \rightarrow \tilde{\chi}_j^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_j^- \tilde{\chi}_1^0 \ell^+ \nu$, $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\tilde{\chi}_1^+} \times \vec{p}_{\ell^+})$

→ reconstruction of $\vec{p}_{\tilde{\chi}_1^+}$ with information from $\tilde{\chi}_j^-$ decay

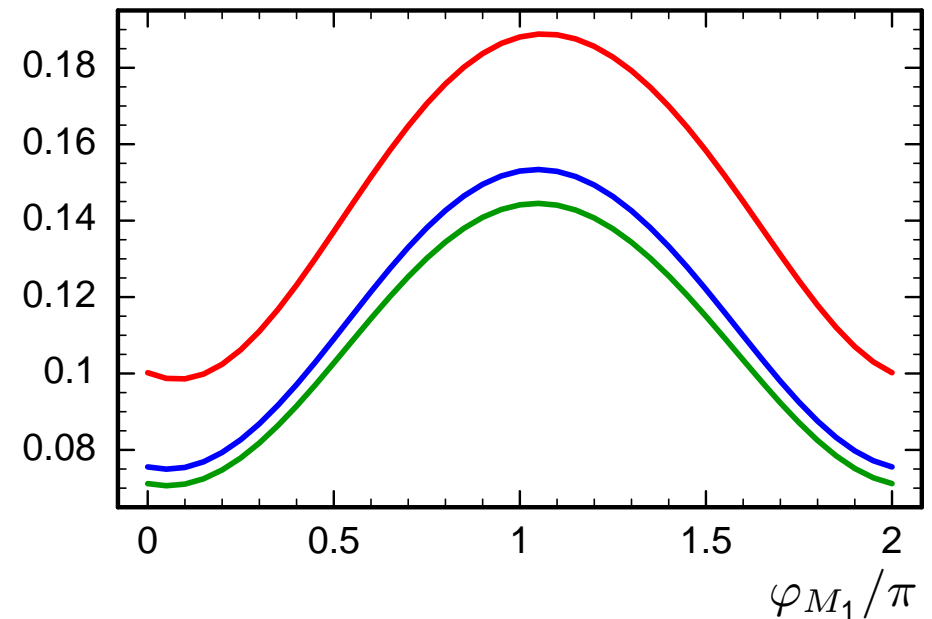
● $e^+e^- \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^0 \ell^+ \nu$ for

$\tan \beta = 5$, $M_2 = 120$ GeV, $|M_1| = M_2 5/3 \tan^2 \theta_W$, $|\mu| = 320$ GeV, $m_{\tilde{\nu}} = 250$ GeV,
 $m_{\tilde{u}_L} = 500$ GeV, $\sqrt{s} = 500$ GeV, $P_{e^-} = -0.8$, $P_{e^+} = +0.6$

A_T in %



$\sigma(e^+e^- \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^+) \cdot BR(\tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^0 \ell^+ \nu)/\text{fb}$



T-odd asymmetry in $\tilde{\chi}^\pm$ sector

- Contours of A_T [in %] for $e^+e^- \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^0 \ell^+ \nu$

$$\tan \beta = 5, |M_1| = M_2 \frac{5}{3} \tan^2 \theta_W,$$

$$m_{\tilde{\nu}} = 250 \text{ GeV}, m_{\tilde{u}_L} = 500 \text{ GeV}$$

$$\sqrt{s} = 500 \text{ GeV}, P_{e^-} = -0.8, P_{e^+} = +0.6$$

Dark shaded area:

$$m_{\tilde{\chi}_1^\pm} < 103 \text{ GeV}$$

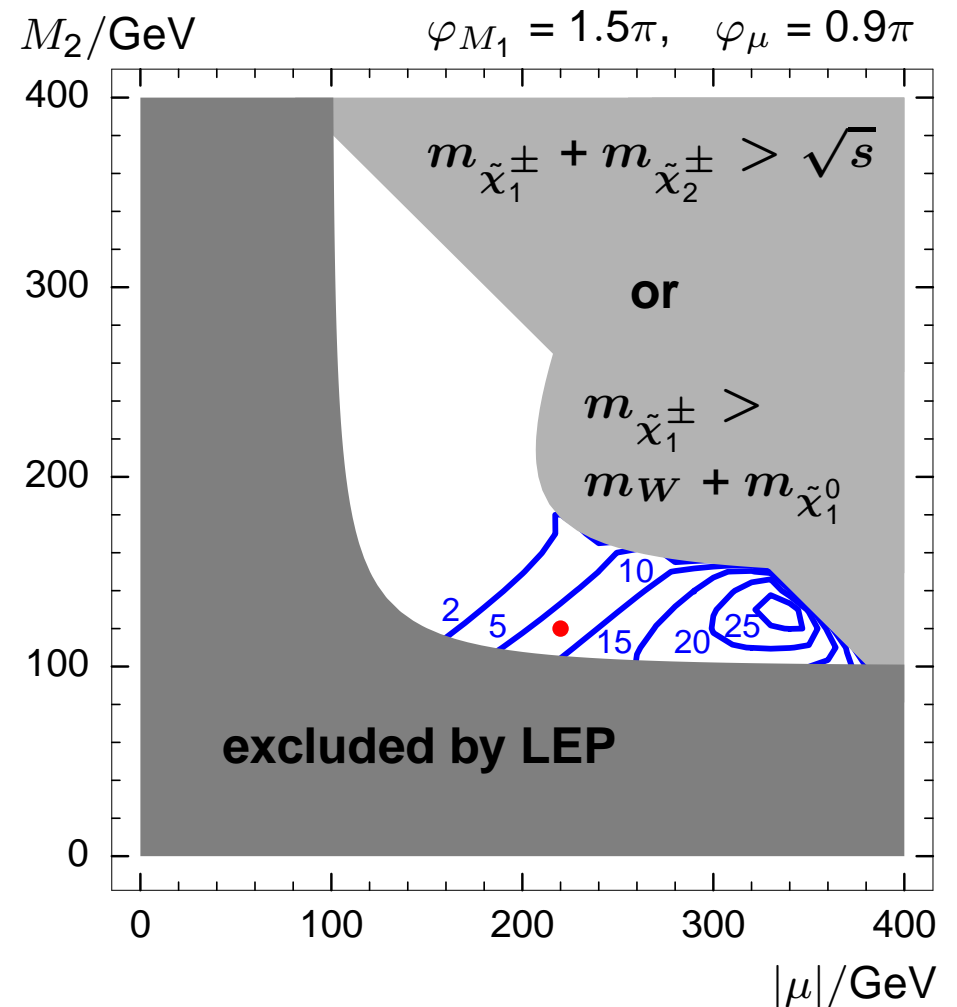
Light shaded area:

$$m_{\tilde{\chi}_1^\pm} + m_{\tilde{\chi}_2^\pm} > \sqrt{s} \text{ or}$$

$$m_{\tilde{\chi}_1^\pm} > m_W + m_{\tilde{\chi}_1^0}$$

$$|\mu| = 220 \text{ GeV}, M_2 = 120 \text{ GeV}:$$

$$\sigma \cdot BR = 2.0 \text{ fb}$$



- $e^+e^- \rightarrow \tilde{\chi}_1^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^- \tilde{\chi}_1^0 \ell^+ \nu: A_T = \mathcal{O}(1\%)$

T-odd asymmetries for two-body decays

Chargino/neutralino production with subsequent two-body decays

- Leptonic decays:

$$e^+e^- \rightarrow \tilde{\chi}_1^0 + \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 + \tilde{\ell}\ell_1, \quad \tilde{\ell} \rightarrow \tilde{\chi}_1^0\ell_2 \quad (\ell = e, \mu, \tau)$$

[Bartl, Fraas, Kittel, Majerotto, hep-ph/0308141, hep-ph/0308143]

[Bartl, Fraas, Kernreiter, Kittel, W. Majerotto, hep-ph/0310011]

$$e^+e^- \rightarrow \tilde{\chi}_i^- + \tilde{\chi}_j^+ \rightarrow \tilde{\chi}_i^- + \tilde{\nu}\ell^+ \quad [\text{Bartl, Fraas, Kittel, Majerotto, hep-ph/0406309}]$$

- Decays into Z and W :

$$e^+e^- \rightarrow \tilde{\chi}_i^0 + \tilde{\chi}_j^0 \rightarrow \tilde{\chi}_i^0 + \tilde{\chi}_n^0 Z, \quad Z \rightarrow \ell\bar{\ell}, q\bar{q}$$

[Bartl, Fraas, Kittel, Majerotto, hep-ph/0402016]

$$e^+e^- \rightarrow \tilde{\chi}_i^- + \tilde{\chi}_j^+ \rightarrow \tilde{\chi}_i^- + \tilde{\chi}_n^0 W^+, \quad W^+ \rightarrow c\bar{s}$$

[Bartl, Fraas, Kernreiter, Kittel, Majerotto, '04]

- CP asymmetries using tau polarisation for $\ell = \tau$

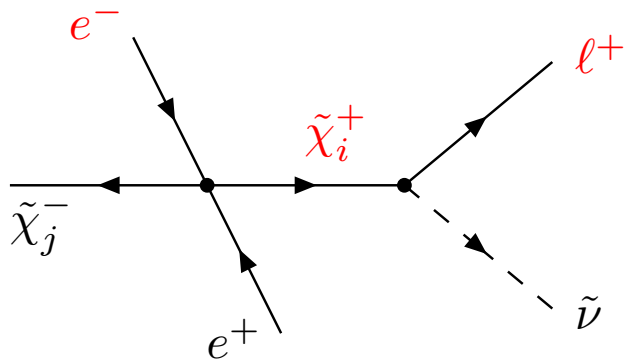
[Bartl, Kernreiter, Kittel, hep-ph/0309340; Choi, Drees, Gaissmaier, Song, hep-ph/0310284]

T-odd asymmetry for $\tilde{\chi}^\pm$ two-body decays

Asymmetry A_T for two-body decay of charginos into sneutrino

[Bartl, Fraas, Kittel, Majerotto, hep-ph/0406309]

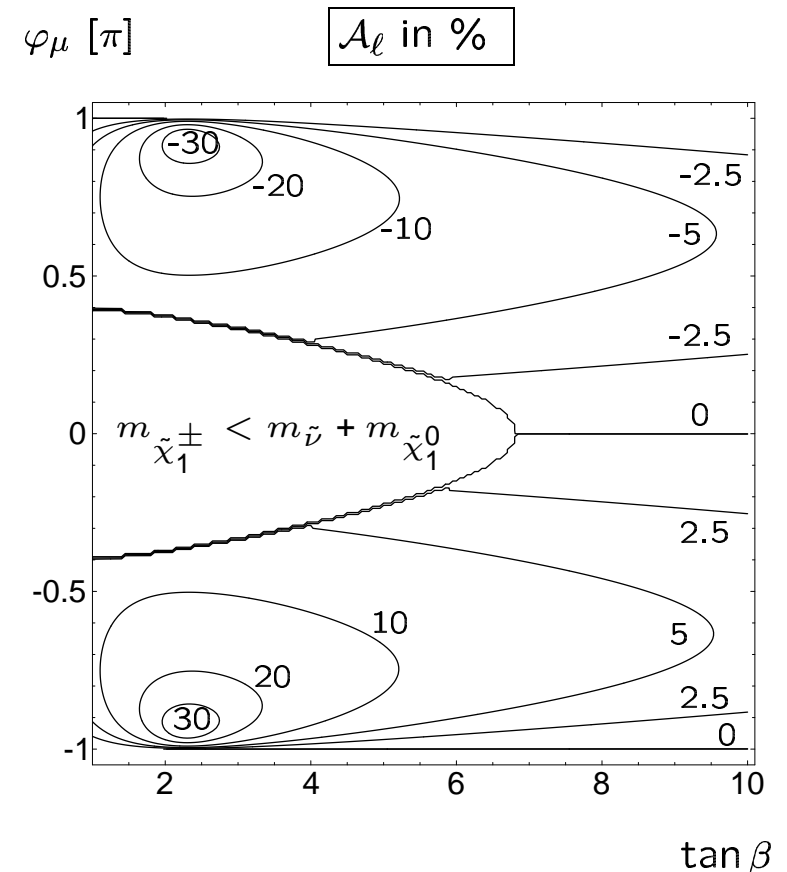
$$e^+ e^- \rightarrow \tilde{\chi}_2^- + \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_2^- + \tilde{\nu} \ell^+, \quad \mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\tilde{\chi}_1^+} \times \vec{p}_{\ell^+})$$



in scenario: $M_2 = 200$ GeV, $|\mu| = 400$ GeV, $m_{\tilde{\nu}} = 185$ GeV

$\sqrt{s} = 800$ GeV, $P_{e^-} = -0.8$, $P_{e^+} = 0.6$

$\sigma \cdot BR = 2 \text{ fb} - 20 \text{ fb}$

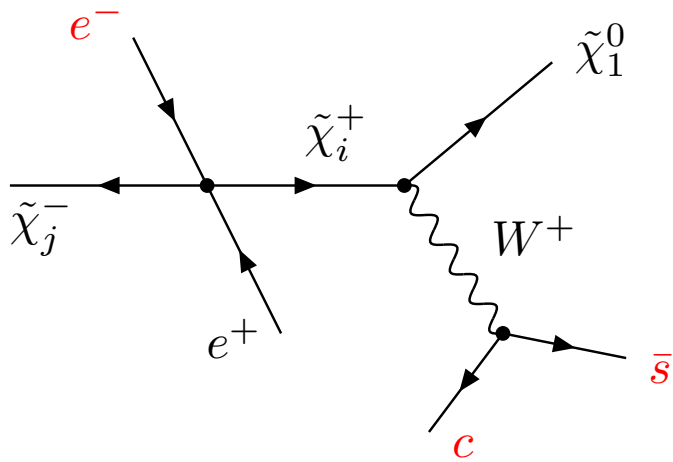


T-odd asymmetry for $\tilde{\chi}^\pm$ two-body decays

Asymmetry A_T for two-body decay of charginos into W

[Bartl, Fraas, Kernreiter, Kittel, Majerotto, '04]

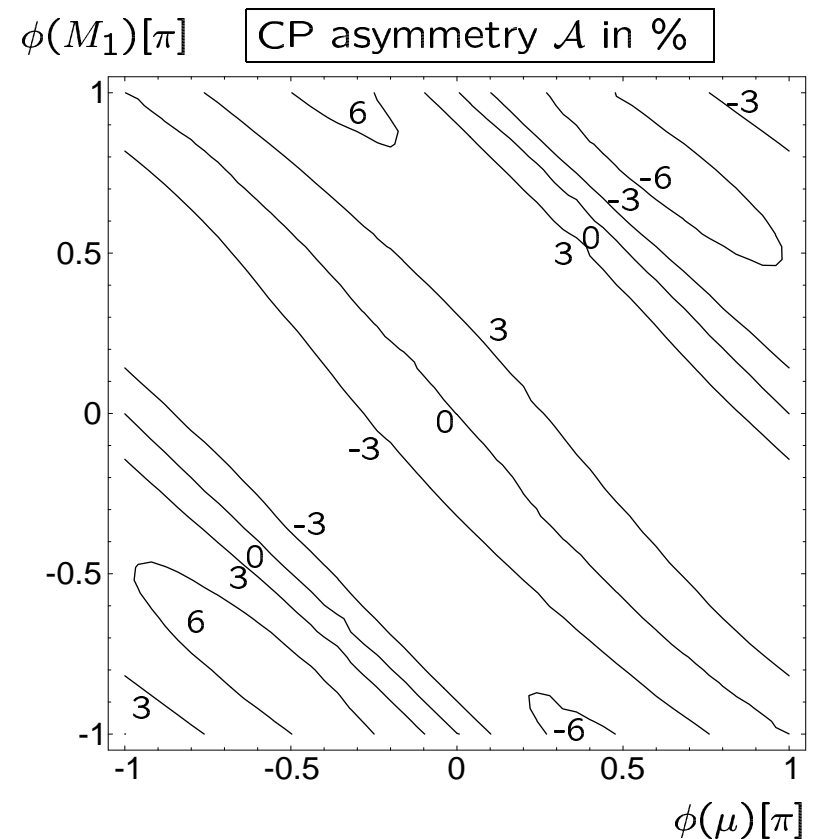
$$e^+e^- \rightarrow \tilde{\chi}_1^- + \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^- + \tilde{\chi}_1^0 W^+, \quad W^+ \rightarrow c\bar{s}, \quad \mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_c \times \vec{p}_{\bar{s}})$$



in scenario: $|M_1| = 200$ GeV, $M_2 = 400$ GeV, $|\mu| = 350$ GeV
 $m_0 = 300$ GeV, $\tan\beta = 10$

$\sqrt{s} = 800$ GeV, $P_{e^-} = -0.8$, $P_{e^+} = 0.6$

$\sigma \cdot BR = 66$ fb – 74 fb



Conclusions and outlook

- Aim: revealing the CP structure of the underlying model
- T-odd asymmetries in chargino and neutralino sectors
 - based on **triple product correlations**
 - **full spin correlations** between production and decay necessary
 - for three-body and two-body decays
- Asymmetries of $\mathcal{O}(30\%)$ ($\tilde{\chi}^{\pm}$) and $\mathcal{O}(10\%)$ ($\tilde{\chi}^0$) possible
 - ⇒ important tool for → search for CP violation in SUSY
 - determination of SUSY phases
- Monte Carlo study in neutralino sector → next talk
[Aguilar-Saavedra, hep-ph/0404104]
- Outlook: incorporation in strategies for parameter determination