

# Determination of the basic Higgs-boson couplings from combined analysis of $WW/ZZ$ decays at LHC, LC and Photon Collider

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NŻK

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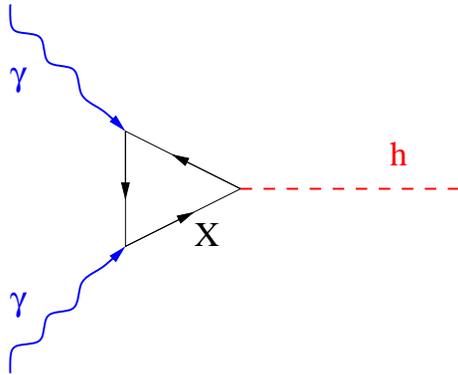
## Outline:

- Introduction: Higgs boson production and decays to  $WW$  and  $ZZ$  at PC  
JHEP 0211 (2002) 034 [[hep-ph/0207294](#)]
- CP conserving 2HDM(II)
  - ⇒ Photon Collider results
  - ⇒ comparison with LHC and LC
- 2HDM(II) with CP violation
  - ⇒ Combined analysis: LHC, LC & PC

# Introduction

## Higgs boson production at the Photon Collider

Cross section proportional to the **two-photon width**



$$\Gamma(h \rightarrow \gamma\gamma) = \frac{G_F \alpha^2 M_h^3}{128 \sqrt{2} \pi^3} \cdot |\mathcal{A}|^2$$

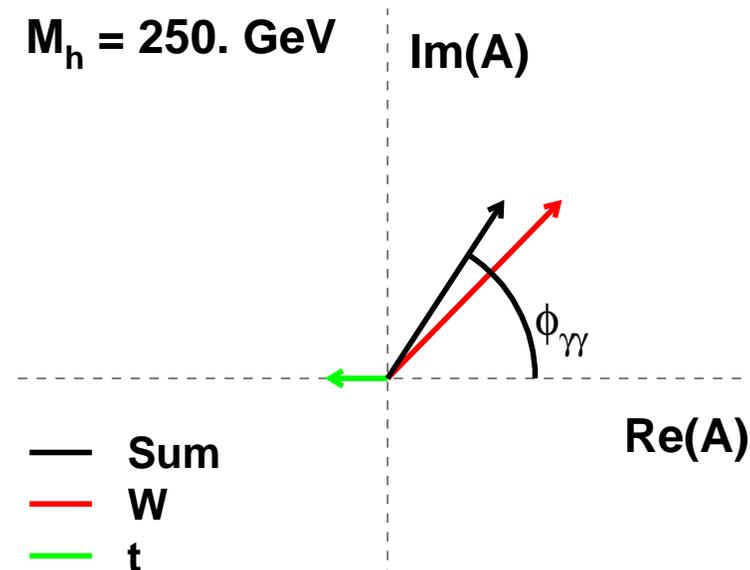
two-photon amplitude:

$$\mathcal{A} = A_W(M_W) + \sum_f N_c Q_f^2 A_f(M_f) + \dots$$

$$\mathcal{A} = |\mathcal{A}| e^{i \phi_{\gamma\gamma}}$$

In SM, dominant contributions to  $\mathcal{A}$  from  $W^\pm$  and top loops

$M_h = 250. \text{ GeV}$



Different phases of  $W^\pm$  and top contributions

$\Rightarrow$  both  $\Gamma_{\gamma\gamma}$  and  $\phi_{\gamma\gamma}$  depend on Higgs couplings!

# Introduction

## Simulation

$\gamma\gamma$  spectra from **CompAZ** [hep-ex/0207021](#)

$\gamma\gamma \rightarrow W^+W^-, ZZ$  events  
generated with PYTHIA 6.152

events reweighted to take into account:

- beam polarization
- Higgs production and interference

detector simulation with SIMDET v. 3.01

total  $\gamma\gamma$  luminosity:  $600 - 1000 \text{ fb}^{-1}$

High  $W_{\gamma\gamma}$  peak:  $75 - 115 \text{ fb}^{-1}$

for  $\sqrt{s_{ee}} = 305 - 500 \text{ GeV}$

## Parametrization

“Measured” invariant mass distribution  
for selected  $W^+W^-$  and  $ZZ$  events  
described by convolution of:

- analytical luminosity Spectra **CompAZ**
- cross section formula  
for signal + background + **interf.**
- invariant mass resolution  
parametrized as a function of  $W_{\gamma\gamma}$

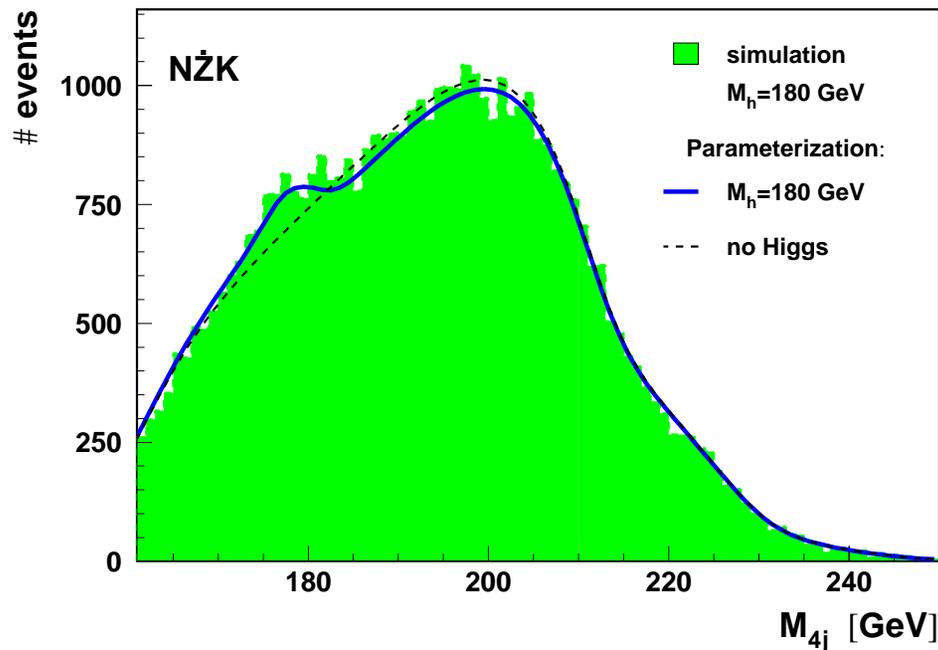
$\Rightarrow$  mass spectra can be calculated for any  
 $\sqrt{s_{ee}}$  and  $M_h$  without time-consuming MC  
simulation

$\Rightarrow$  can be used for fast simulation and fitting

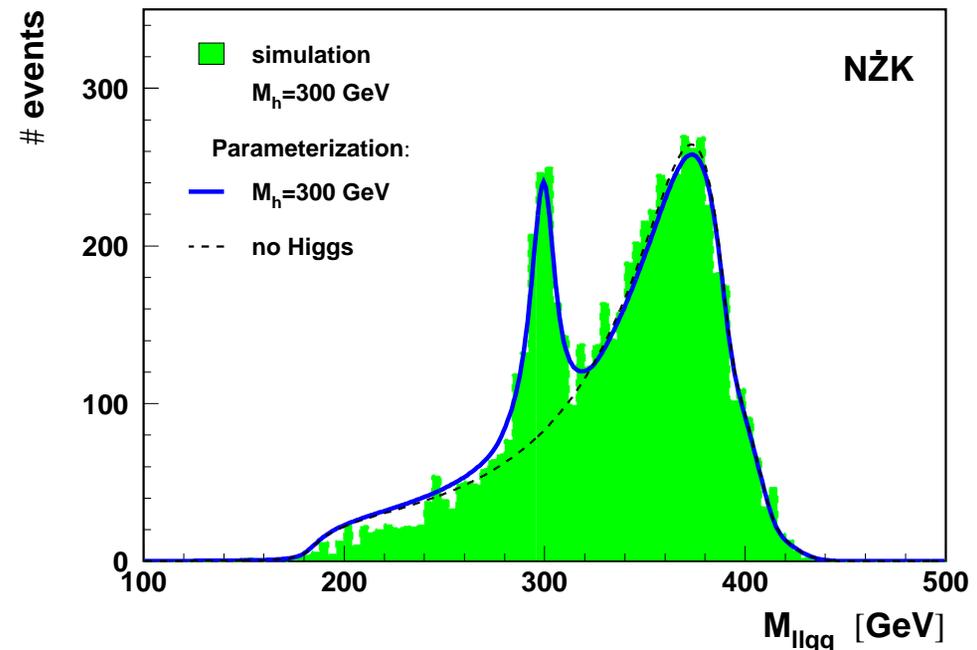
# Introduction

From the **simultaneous fit** to the observed  $W^+W^-$  and  $ZZ$  mass spectra both the two-photon width  $\Gamma_{\gamma\gamma}$  and phase  $\phi_{\gamma\gamma}$  can be determined

$W^+W^-$



$ZZ$



For SM:  $\Gamma_{\gamma\gamma}$  with precision  $\sim 4 - 9\%$ ,  $\phi_{\gamma\gamma}$  with precision  $40 - 120$  mrad (stat.+sys.)

JHEP 0211 (2002) 034 [hep-ph/0207294] (stat. uncertainties only)

ECFA/DESY workshop, Praha 2002 (stat. and sys. uncertainties)

# CP conserving 2HDM (II)

## Higgs boson couplings

Scalar Higgs bosons  $h$  and  $H$

with basic couplings (relative to SM):

$$\chi_x = g_{\mathcal{H}xx} / g_{\mathcal{H}xx}^{SM} \quad \mathcal{H} = h, H, A$$

	$h$	$H$	$A$
$\chi_u$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$-i \gamma_5 \frac{1}{\tan \beta}$
$\chi_d$	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$-i \gamma_5 \tan \beta$
$\chi_V$	$\sin(\beta - \alpha)$	$\cos(\beta - \alpha)$	0

For charged Higgs boson couplings (loop contribution to  $\Gamma_{\gamma\gamma}$ ) we set

$$M_{H^\pm} = 800 \text{ GeV} \quad \mu = 0$$

Higgs couplings are related by “patter relation”

$$(\chi_V - \chi_d)(\chi_u - \chi_V) + \chi_V^2 = 1$$

I. F. Ginzburg, M. Krawczyk and P. Osland,  
hep-ph/0101331

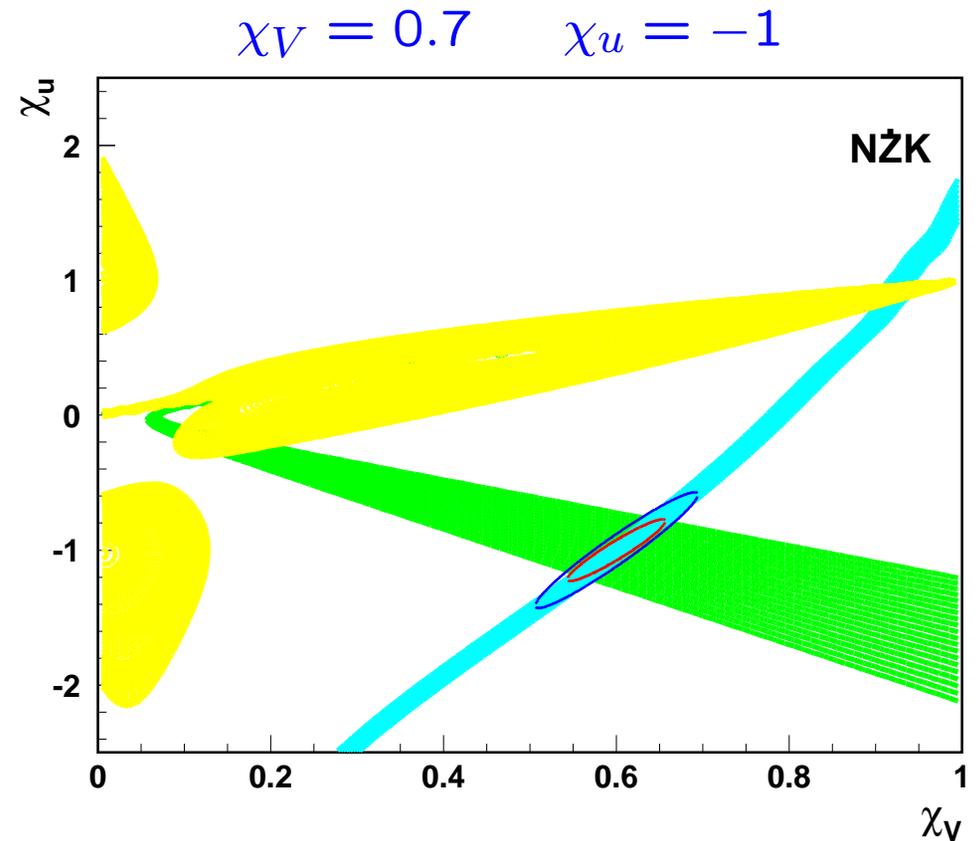
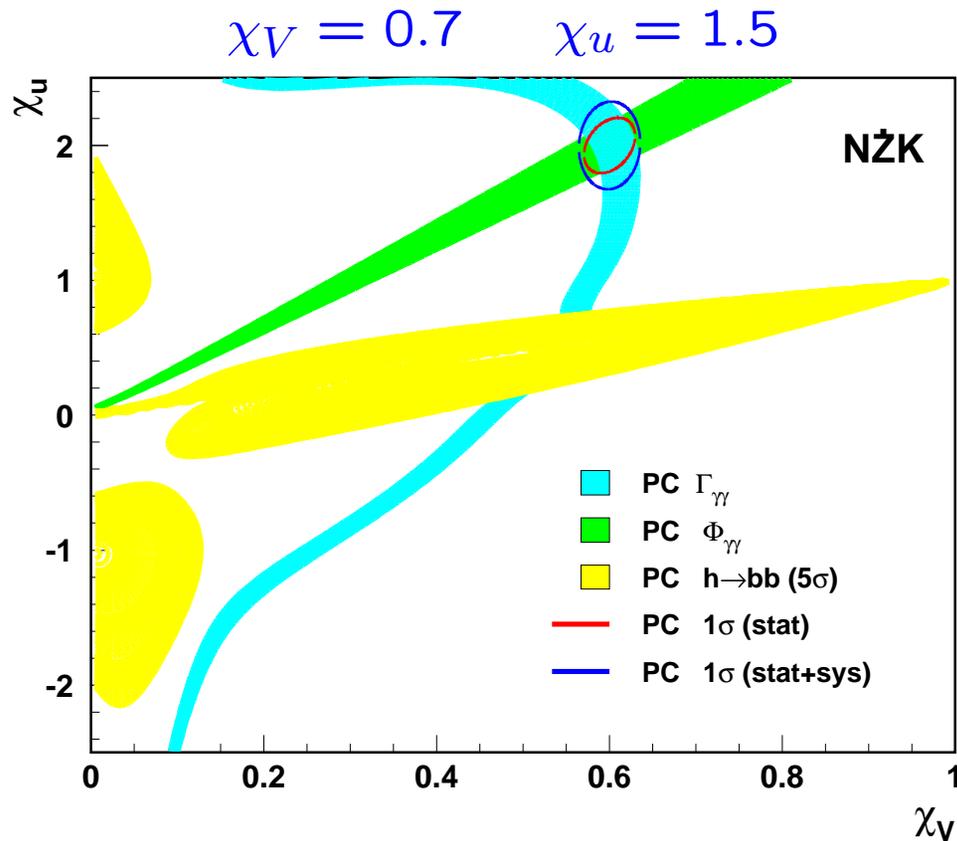
Instead of angles  $\alpha$  and  $\beta$  use couplings  $\chi_V$  and  $\chi_u$  to parametrize cross sections

$$0 \leq \chi_V \leq 1$$

If we neglect  $H$  decays to  $h$  and  $A$  (small) cross sections and BRs calculated for  $H$  are also valid for  $h$

# Photon Collider

Combined fit to  $W^+W^-$  and  $ZZ$  invariant mass distributions  $\Rightarrow \Gamma_{\gamma\gamma}$  and  $\phi_{\gamma\gamma}$   
 $\Rightarrow$  couplings to both vector bosons ( $\chi_V$ ) and up fermions ( $\chi_u$ ) can be determined  
 $1\sigma$  contours for 1 year of PC running,  $M_H = 250$  GeV



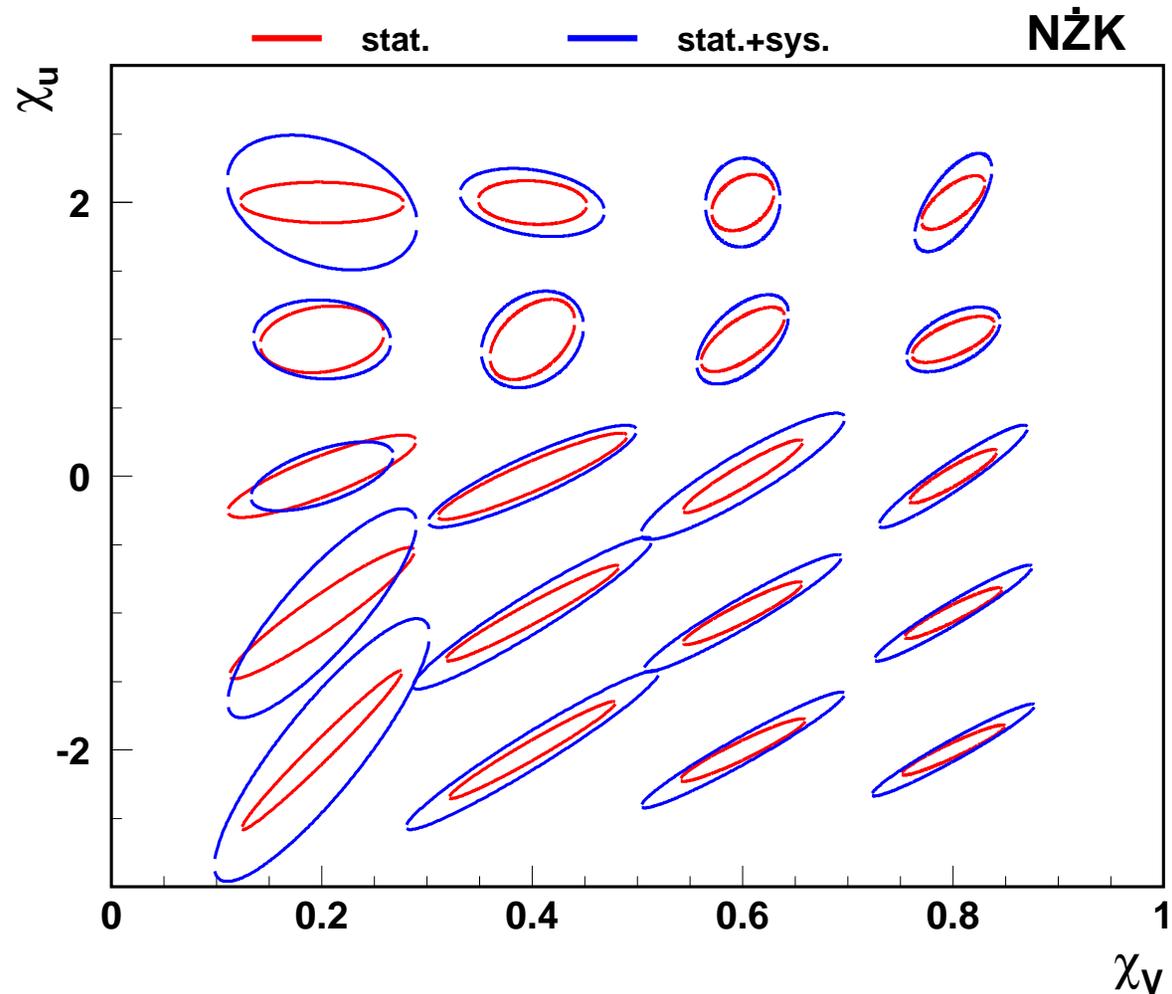
Systematic uncertainties affect mainly  $\phi_{\gamma\gamma}$  measurement !

# Photon Collider

Comparison of **statistical** and **total (stat+sys)** error estimates, for  $M_H = 250$  GeV

$H$  couplings to vector bosons ( $\chi_V$ ) and up fermions ( $\chi_u$ ) from combined fit to  $W^+W^-$  and  $ZZ$  invariant mass distributions

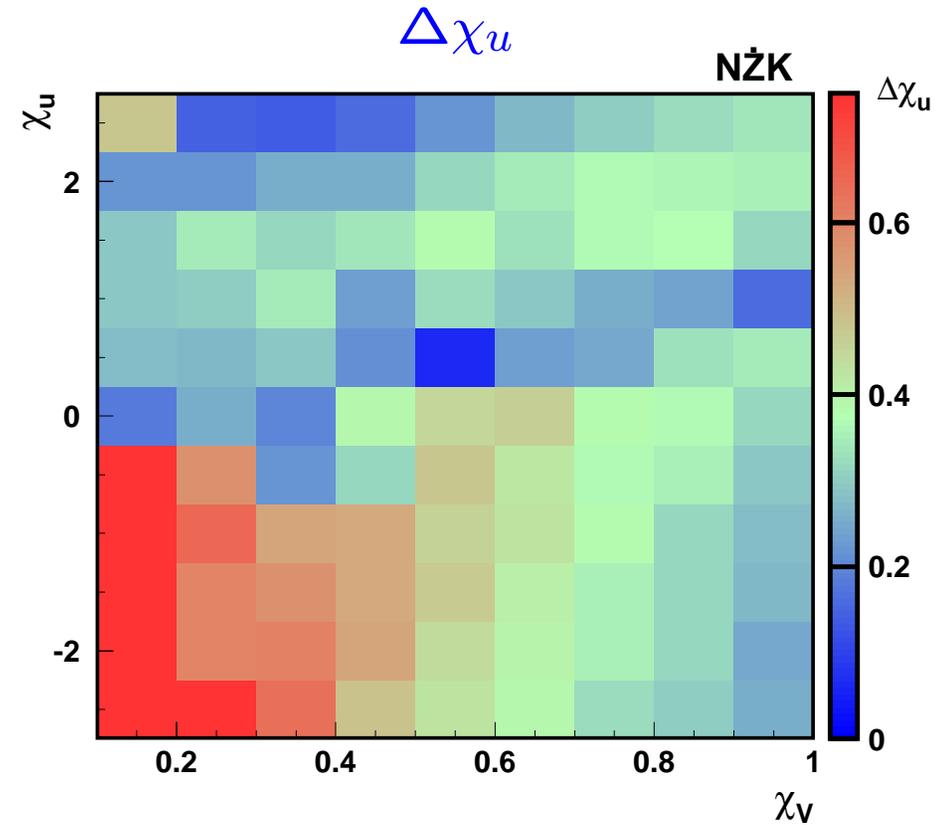
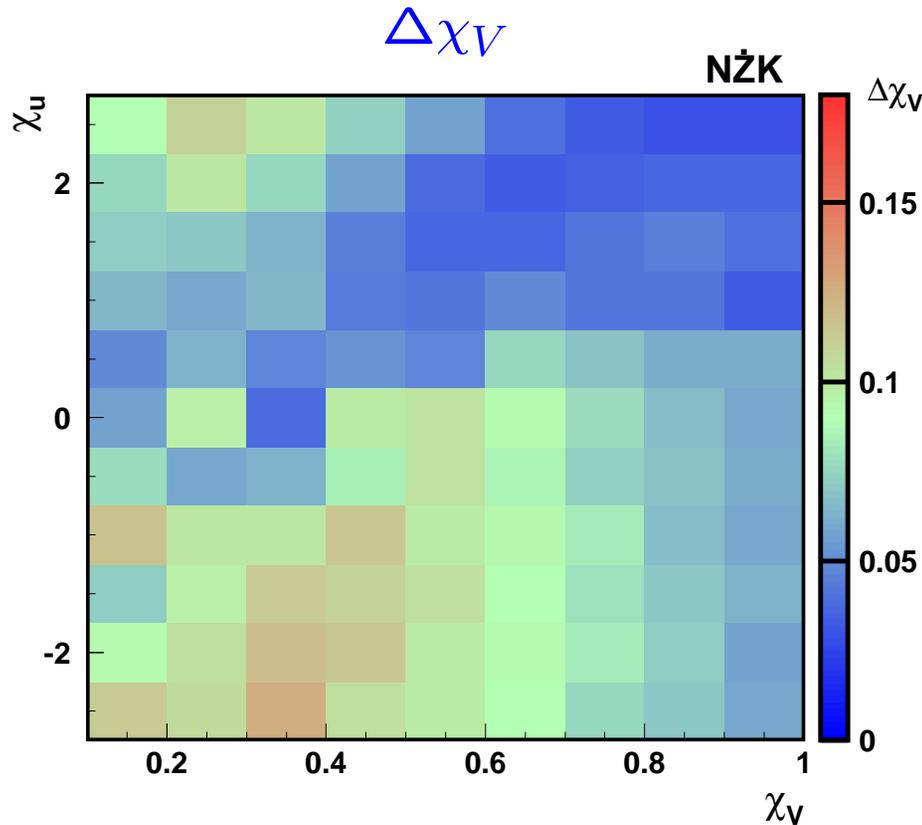
$1\sigma$  contours for 1 year of PC



# Photon Collider

## Coupling uncertainties

Estimated total errors on Higgs boson couplings for  $M_H=250$  GeV (1 year of PC running)



For a wide range of couplings  $\Delta\chi_V \leq 0.1$   $\Delta\chi_u \leq 0.4$

For  $M_H = 200 \rightarrow 300$  GeV:  $\langle \Delta\chi_V \rangle = 0.082 \rightarrow 0.090$   $\langle \Delta\chi_u \rangle = 0.49 \rightarrow 0.36$

# LHC

In the considered mass range Higgs production at LHC is dominated by the **gluon fusion** process (top loop)

$$\sigma(gg \rightarrow h) \sim \chi_u^2$$

**WW fusion** process ( $\sim 15\%$ )

$$\sigma(qq \rightarrow qqh) \sim \chi_V^2$$

Measurement of

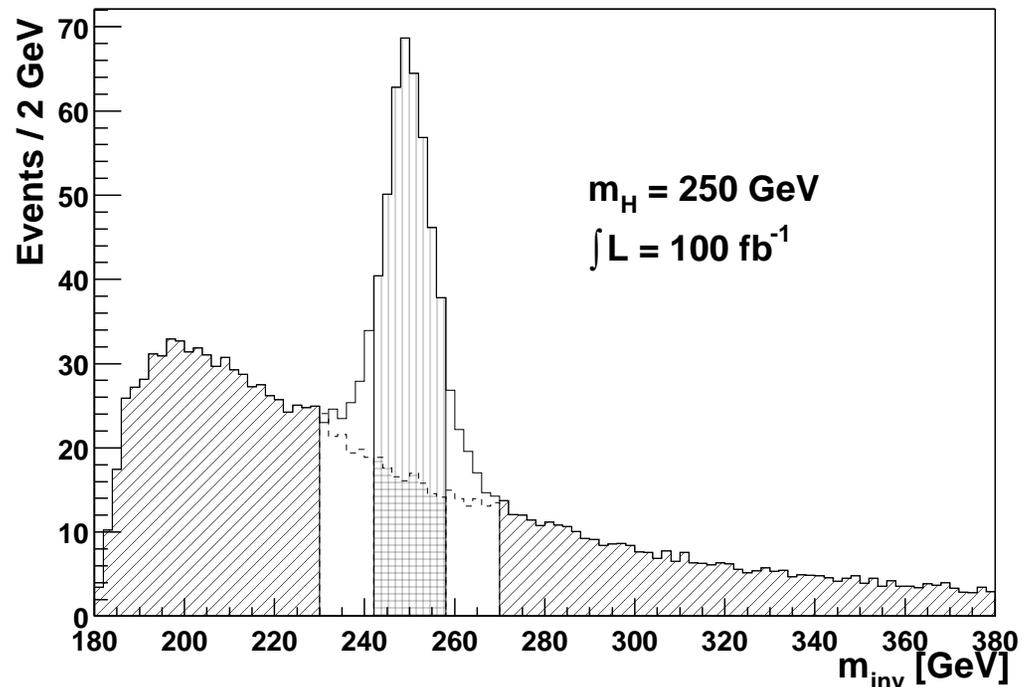
$$\sigma(pp \rightarrow hX) \cdot BR(h \rightarrow ZZ \rightarrow 4l)$$

is possible with precision  $\sim 15\%$

We use results of

**C.P.Buszello, I.Fleck, P.Marquard, J.J. van der Bij,**  
**Eur. Phys. J. C32 (2004) 209**    **hep-ph/0212396**

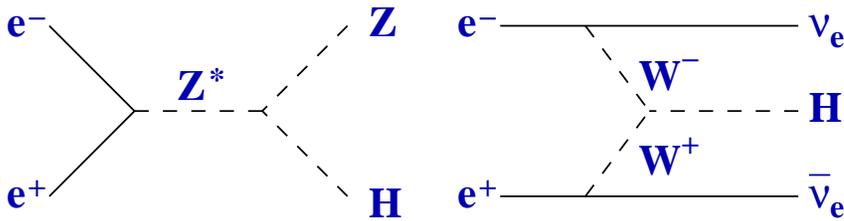
4 Lepton Invariant Mass Distribution



This will constrain mainly the  $|\chi_u|$  value, provided  $\chi_V$  is not too small.

# LC

At LC, two processes contribute to the Higgs boson production



We thank Niels Meyer for providing us the data  
 N.Meyer, Eur. Phys. J. C35 (2004) 171

hep-ph/0308142

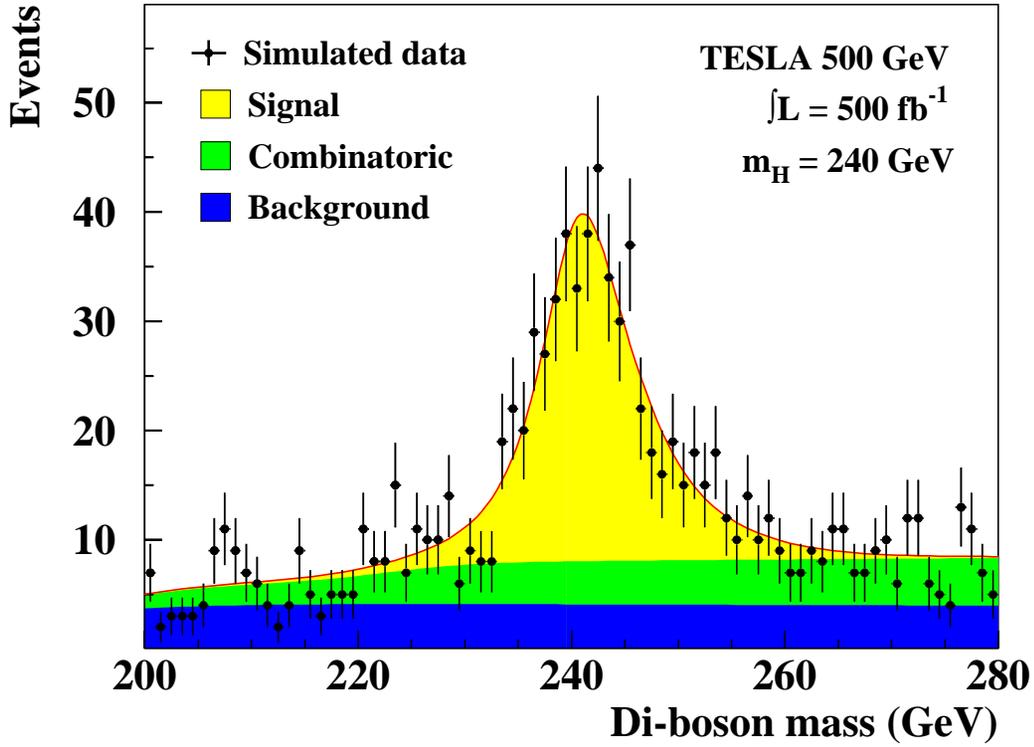
Cross section is sensitive only to  $\chi_V$

Measurement of

$$\sigma(e^+e^- \rightarrow hX) \cdot BR(h \rightarrow WW/ZZ)$$

is possible with precision  $\sim 4 - 7\%$

This will constrain the  $\chi_V$  value

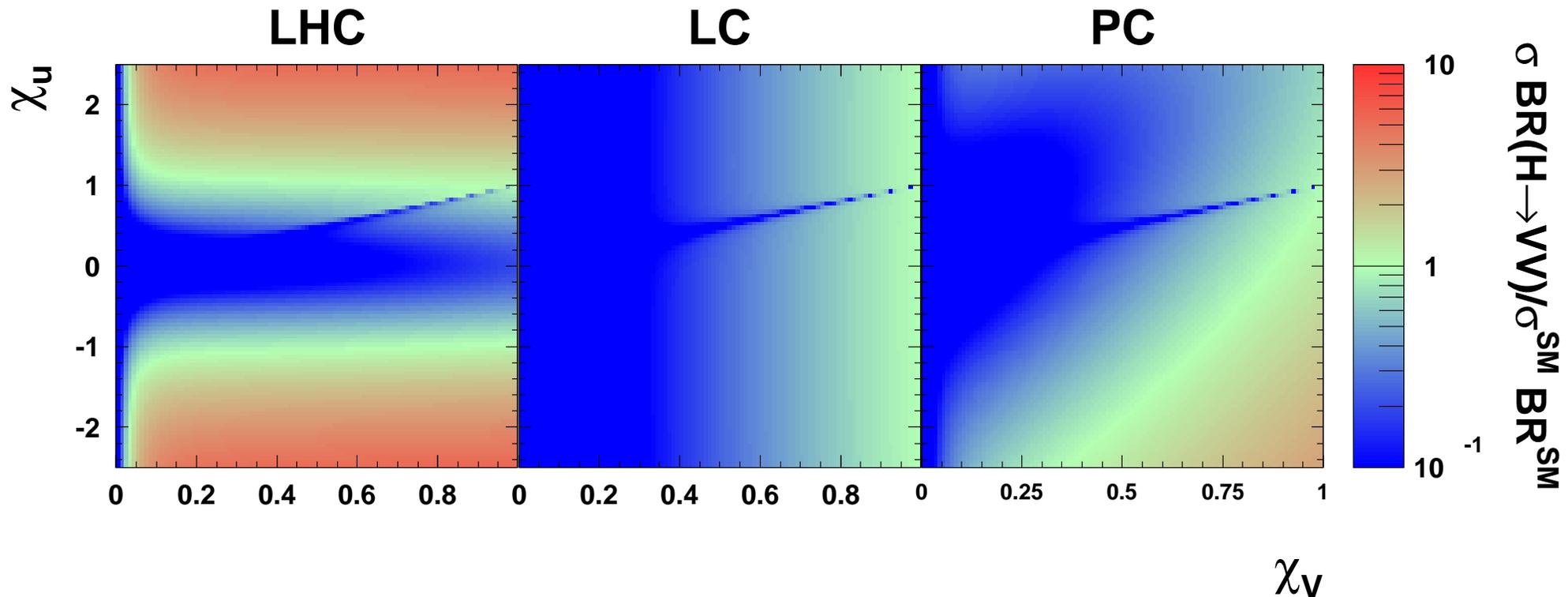


# LHC ⊕ LC ⊕ PC

Measurements at LHC, LC and Photon Collider are complementary, being sensitive to different combinations of Higgs-boson couplings

Cross sections × BR relative to SM

$M_H = 250 GeV$



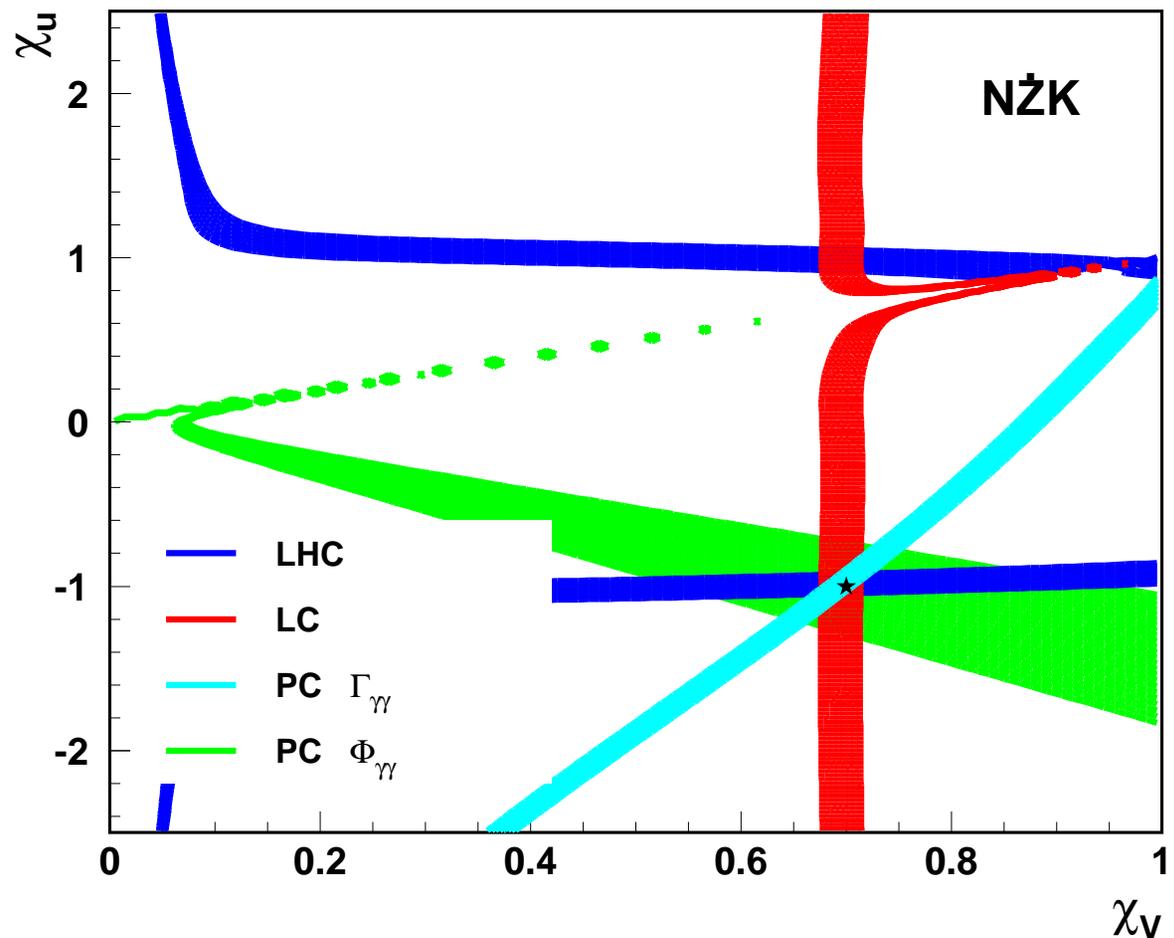
# LHC ⊕ LC ⊕ PC

Allowed coupling values ( $1\sigma$ ) from cross section measurements at LHC, LC and PC, and the phase measurement at PC.

Consistency of all these measurements verifies the coupling structure of the model

statistical errors only

$$\chi_V = 0.7 \quad \chi_u = -1 \quad M_H = 250 \text{ GeV}$$



## 2HDM (II) with CP violation

### $H - A$ mixing

Mass eigenstates of the neutral Higgs-bosons  $h_1$ ,  $h_2$  and  $h_3$  do not need to match CP eigenstates  $h$ ,  $H$  and  $A$ .

We consider weak CP violation through a small mixing between  $H$  and  $A$  states:

$$\begin{aligned}\chi_X^{h_1} &\approx \chi_X^h \\ \chi_X^{h_2} &\approx \chi_X^H \cdot \cos \Phi_{HA} + \chi_X^A \cdot \sin \Phi_{HA} \\ \chi_X^{h_3} &\approx \chi_X^A \cdot \cos \Phi_{HA} - \chi_X^H \cdot \sin \Phi_{HA}\end{aligned}$$

⇒ additional model parameter: CP-violating mixing phase  $\Phi_{HA}$

⇒ see our paper hep-ph/0403138

In general case

combined analysis of LHC, Linear Collider and Photon Collider data is needed

Results for  $h_2$  production and decays...

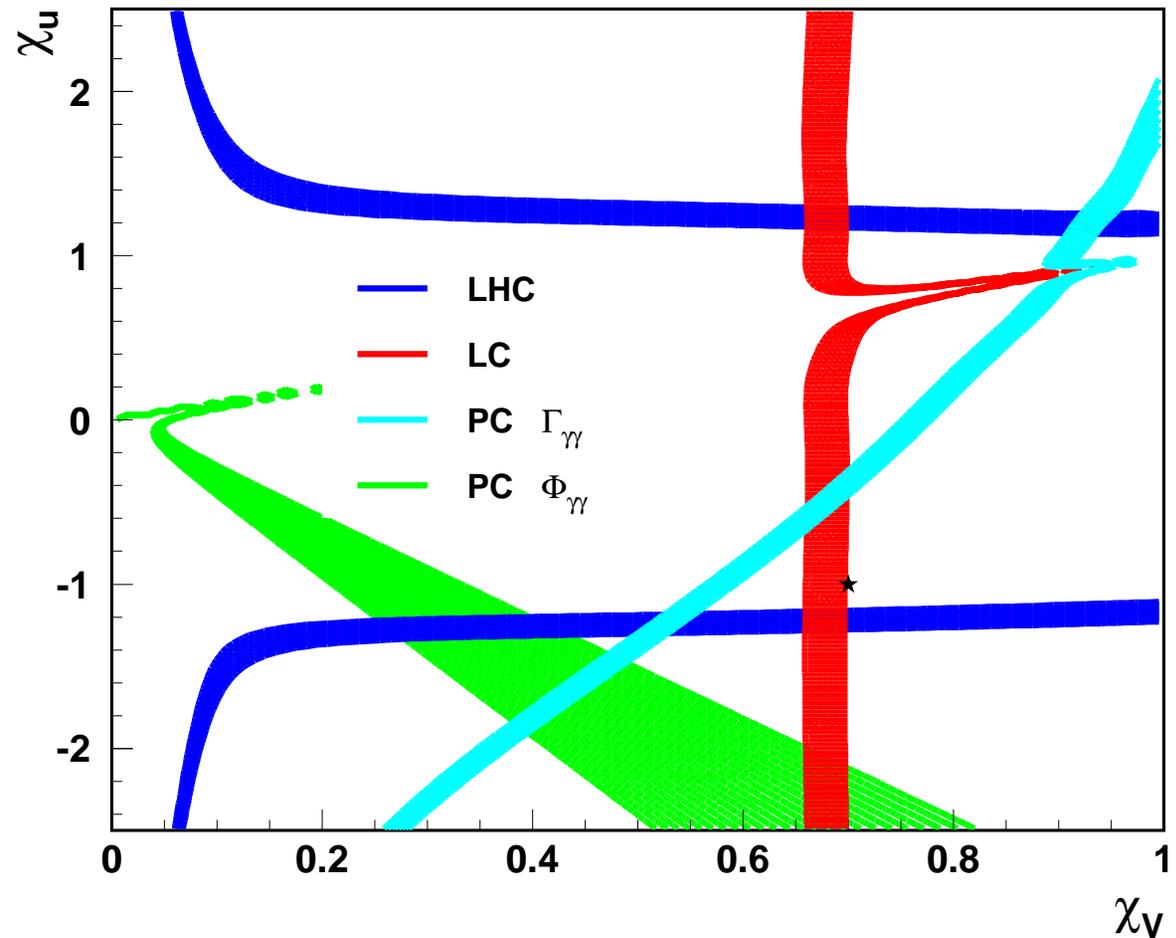
# LHC ⊕ LC ⊕ PC

Allowed coupling values from **cross section** measurements at **LHC**, **LC** and **PC**, and the phase measurement at **PC**.

Inconsistency would indicate “**new physics**”:

- different **coupling structure** or
- existence of **new heavy particles** contributing to  $\Gamma_{gg}$  and  $\Gamma_{\gamma\gamma}$

Results for 2HDM (II) with **weak CP violation**:  
NŻK



# LHC ⊕ LC ⊕ PC

Combined fit to the expected invariant mass distributions:

LHC

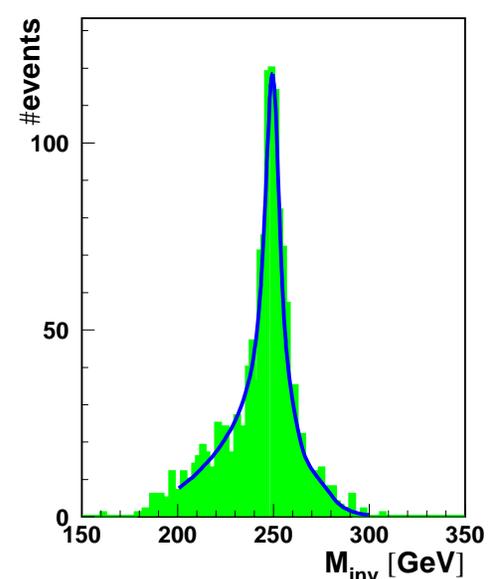
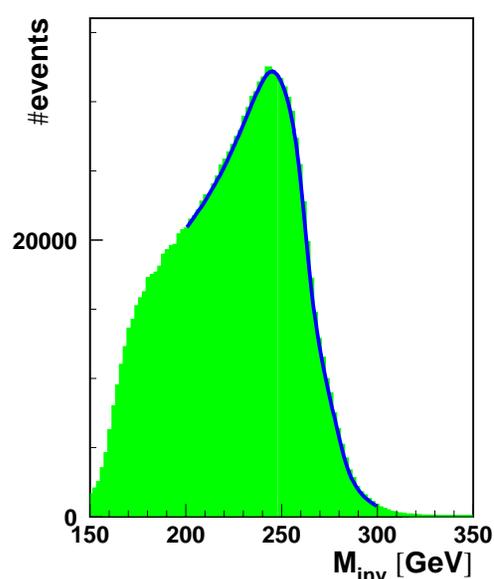
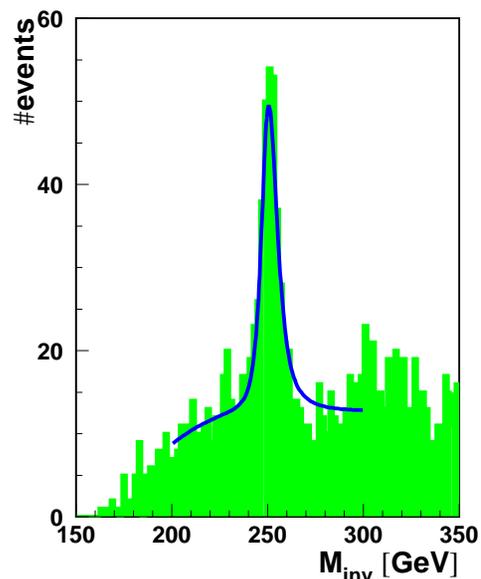
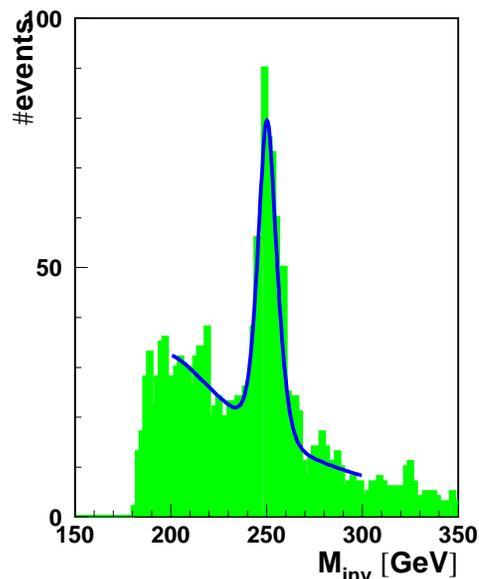
LC

PC

$H \rightarrow WW$

PC

$H \rightarrow ZZ$



9 or 10 parameter fit: ●  $\chi_V$  ●  $\chi_u$  ●  $M_H$  ●  $\Phi_{HA}$  (for model with CP violation)  
 + 6 normalization and  $\gamma\gamma$ -spectra shape parameters (systematic uncertainties)

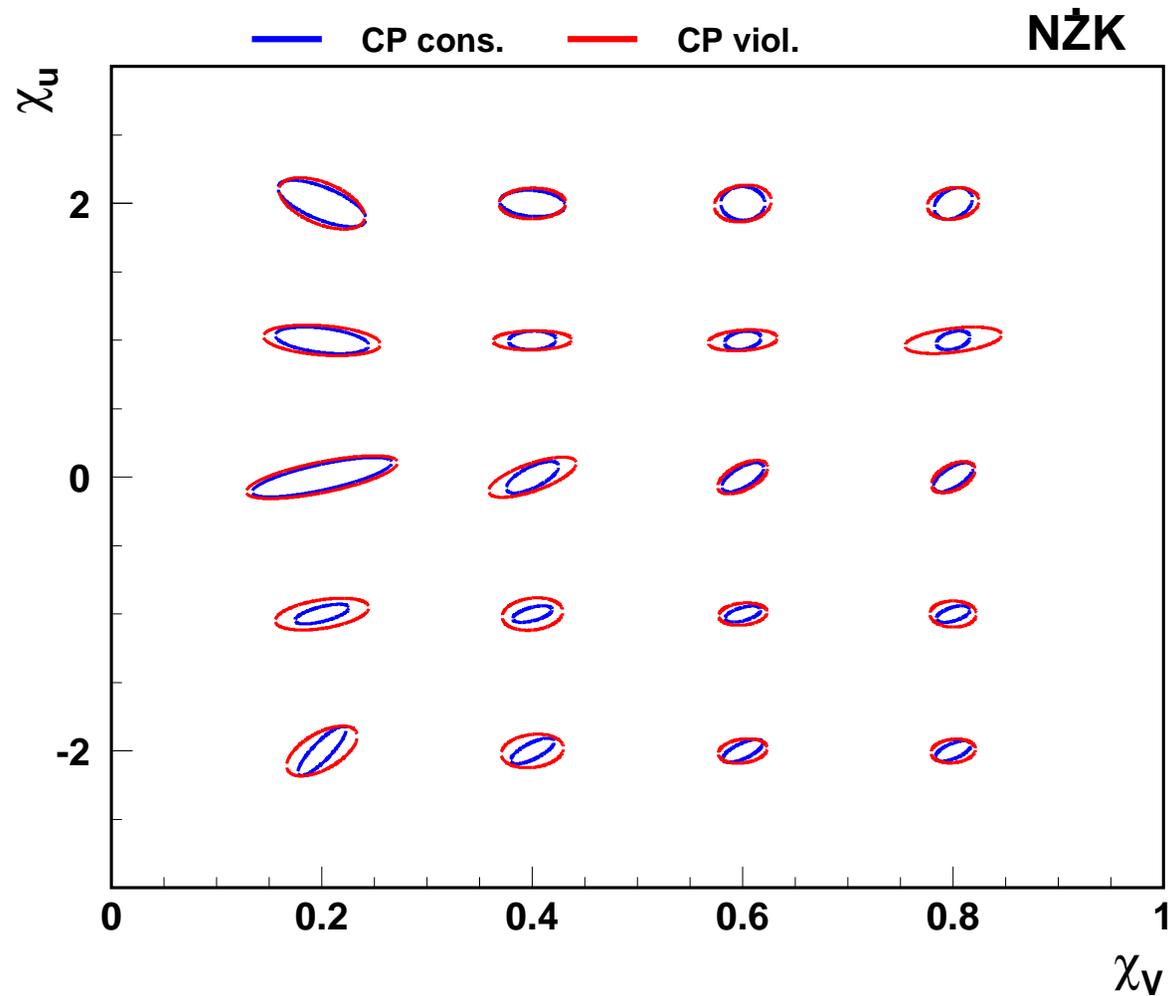
# LHC ⊕ LC ⊕ PC

Simultaneous fit to **LHC**, **LC** and **PC** ( $W^+W^-$  and  $ZZ$ ) invariant mass distributions

$1\sigma$  (stat.+sys.) contours

Comparison of **error contours** for model **without** and **with** weak **CP violation**

$H$  couplings to vector bosons ( $\chi_V$ ) and up fermions ( $\chi_u$ ) for  $M_H = 250$  GeV

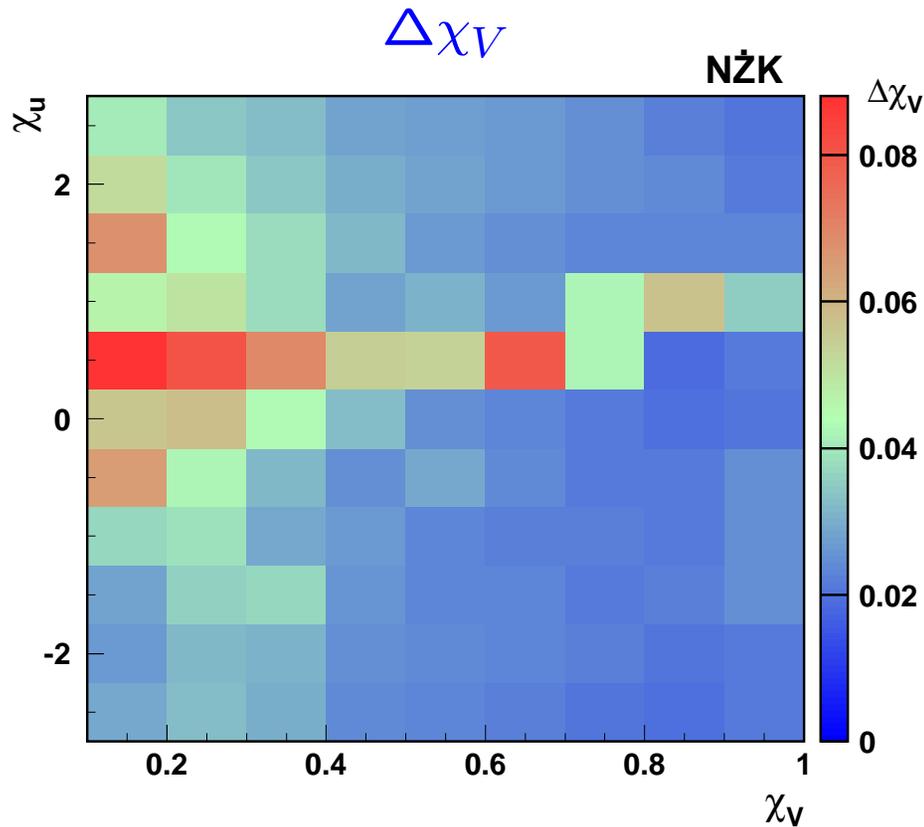


coupling errors  $\Rightarrow$  next slide

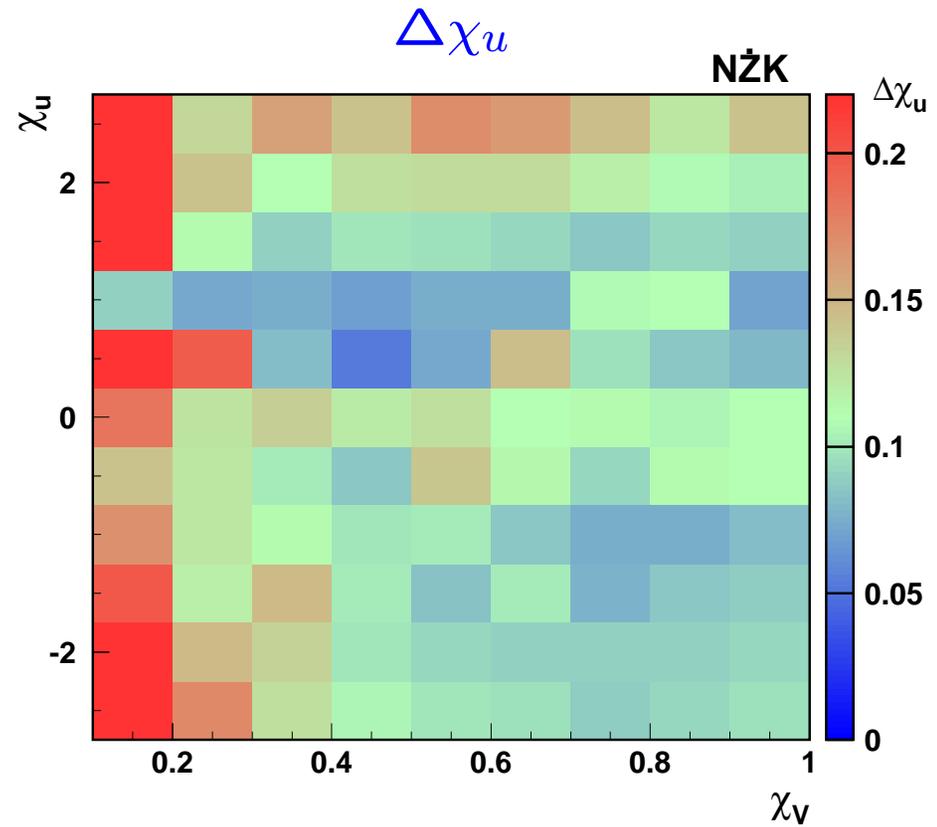
LHC ⊕ LC ⊕ PC

## Coupling errors

Estimated total errors on Higgs boson **couplings** for  $M_H=250$  GeV



$$\langle \Delta\chi_V \rangle = 0.033$$

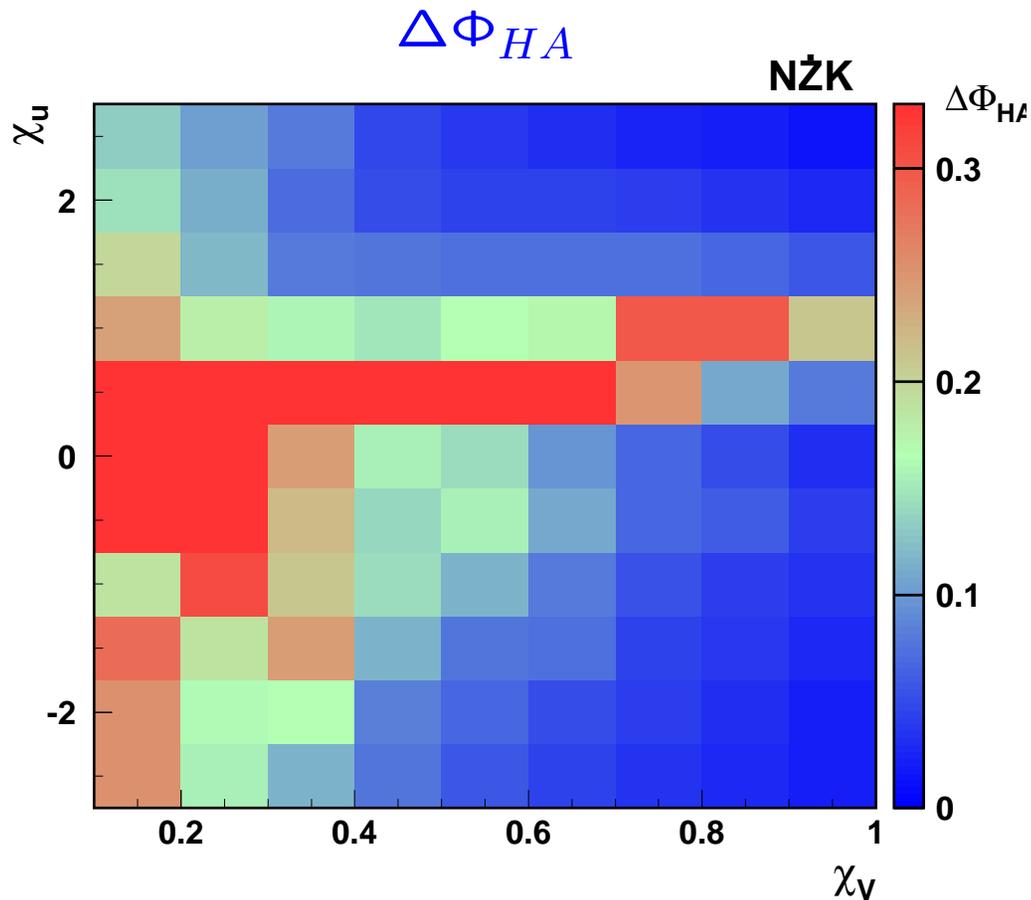


$$\langle \Delta\chi_u \rangle = 0.12$$

LHC ⊕ LC ⊕ PC

$\Phi_{HA}$  error

Estimated total errors on  $H - A$  mixing angle, for  $M_H=250$  GeV



For a wide range of couplings

$$\Delta\Phi_{HA} \leq 100 \text{ mrad}$$

$$\langle \Delta\Phi_{HA} \rangle = 150 \text{ mrad}$$

# Summary

## CP-conserving 2HDM(II)

Higgs-boson couplings to vector bosons,  $\chi_V$ , and to up-type fermions,  $\chi_u$ , can be determined at the Photon Collider with  $\Delta\chi_V \sim 0.1$  and  $\Delta\chi_u \sim 0.4$

Measurements at Photon Collider complementary to those at LHC and LC, being sensitive to different combinations of Higgs-boson couplings.

## 2HDM (II) with CP violation

Only the combined analysis of LHC, LC and PC measurements allows for the determination of the CP-violating  $H - A$  mixing angle  $\Phi_{HA}$ .

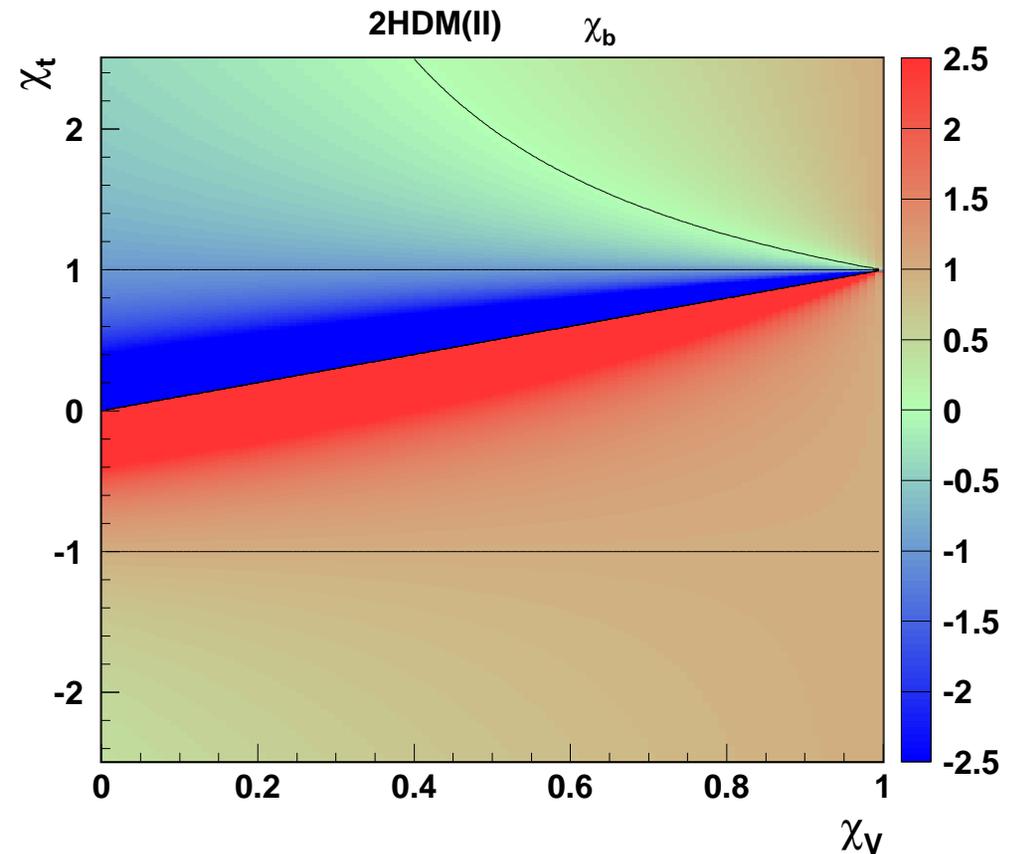
In most of the considered parameter space  $\Phi_{HA}$  measured to better than 100 mrad.

Results submitted to ICHEP'04 (abstract 12-0740) and as an LC-Note

## 2HDM (II)

Basic relative coupling to **down-type** fermions as a function of **vector boson** and **top** (up-type fermions) couplings:

$$\chi_d = \chi_V + \frac{1 - \chi_V^2}{\chi_V - \chi_u}$$



# Systematic uncertainties

## PC analysis

Influence of **systematic uncertainties** on the  $\tan \beta$  determination is estimated by adding additional **free parameters** to the fit:

### Uncertainties:

### Parameters:

- luminosity  $\Rightarrow$  overall normalization
- energy scale  $\Rightarrow$  relative normalization of  $WW$  and  $ZZ$  samples fixed
- Higgs boson mass }  $\Rightarrow$  Higgs boson mass
- mass resolution }  $\Rightarrow$  Higgs boson width
- Higgs boson width
- luminosity spectra  $\Rightarrow$  spectra shape variations:

$$\frac{dL}{dW_{\gamma\gamma}} = \frac{dL^{CompAZ}}{dW_{\gamma\gamma}} (1 + A \cdot \sin \pi x + B \cdot \sin 2\pi x) \quad x = \frac{W_{\gamma\gamma} - W_{min}}{W_{max} - W_{min}}$$

# Systematic uncertainties

## LHC ⊕ LC ⊕ PC analysis

### Parameter:

- Higgs boson mass
- $\gamma\gamma$  luminosity
- $\gamma\gamma$  spectra shape parameters
- background normalization for  $e^+e^-$
- signal normalization for  $pp$
- background normalization for  $pp$

### Assumed uncertainty:

- ⇒ unconstrained
- ⇒ unconstrained
- ⇒ 5% uncertainty
- ⇒ 5% uncertainty
- ⇒ 10% uncertainty
- ⇒ 10% uncertainty