# High pT Jets and PDFs (NLOGRID)

Integration grids for quick NLO QCD crosssection calculations

Dan Clements, Claire Gwenlan, Craig Buttar, G.Salam Tancredi Carli, Amanda Cooper-Sarkar, Mark Sutton,

(With the help of Z. Nagy)

Dan Clements - ATLAS UK SM meeting (Sep 2006)

# **Motivation**

- 1. NLO Monte-Carlo QCD calculations are necessary to provide accurate predictions for experimental cross-section measurements.
- 2. NLO Monte-Carlo calculations however can require long CPU times to achieve sufficient accuracy (typically of order days/weeks).
- 3. If the PDF is changed the cross-section must be recalculated.

This makes it difficult to use data from hadron-colliders to constrain PDFs using iterative techniques.



Want a method to separate PDFs from the QCD cross-section calculation.....

Dan Clements – ATLAS UK SM meeting (Sep 2006)

#### **Scattering Processes At A Hadron-Collider**



•The PDFs can be separated from the cross-section by using an integration grid.

•The first step to doing this is to represent the PDF by a set of discrete values on a grid...

Dan Clements – ATLAS UK SM meeting (Sep 2006)

#### **Representing a PDF on a grid**

•Consider a proton PDF:  $q(x,Q^2)$ , where 'x' is the parton momentum fraction and 'Q<sup>2</sup>' is the factorisation scale.

•Instead of defining a grid in x and Q<sup>2</sup> perform a co-ordindate transform:

$$y(x) = \ln \frac{1}{x}$$
  $\tau(Q^2) = \ln \ln \frac{Q^2}{\Lambda^2}$   $\Lambda \approx \Lambda_{QCD}$ 

•The PDF then becomes:

$$q(x,Q^2) = \sum_{i=0}^{n} \sum_{j=0}^{n'} q_{k+i,l+j} I_i^n(y(x)) I_j^{n'}(\tau(Q^2))$$
(1)

Where the I are interpolation functions of order n and n'.

#### **Representing a PDF on a grid**



Dan Clements – ATLAS UK SM meeting (Sep 2006)

#### **LO Monte-Carlo Cross-Sections (DIS)**

•Consider a Monte-Carlo generator producing N events where each event 'm' has  $x=x_m Q^2=Q_m^2$  and a weight  $w_m$ .

•The cross-section is given by:

$$W = \sum_{m=1}^{N} \left( \frac{\alpha_s(Q_m^2)}{2\pi} \right)^2 w_m \cdot q(x_m, Q_m^2)$$

•But if we believe our interpolation formula we can replace  $q(x_m, Q_m^2)$  in the above by (1).

•This is good as the interpolation relies only on the discrete PDF grid points. So we can introduce a weight-grid and for each event update a portion of the grid.....

#### **LO Monte-Carlo Cross-Sections (DIS)**

•Define a weight-grid in x and Q<sup>2</sup> similar to the PDF grid and for each event update a portion:

$$W_{k+i,l+j} \to W_{k+i,l+j} + w_m \cdot I_i^n(y(x_m))I_j^{n'}(\tau(Q_m^2))$$

n.b. have pushed the PDF interpolation onto the MC weights

•Can now find the result W for an arbitrary PDF after the Monte-Carlo calculation:



# **LO Monte-Carlo Cross-Sections (DIS)**

What's actually going on:



Monte Carlo weight is split up into several weights on the grid according to the PDF interpolation formula.

The split weight is multiplied by the corresponding value on the PDF grid after Monte-Carlo production.

Dan Clements – ATLAS UK SM meeting (Sep 2006)

# **Moving to NLO Hadron-Hadron Collisions**

•For NLO Hadron-Hadron collisions things are a little more complicated:

- 1. Need to consider two incoming hadrons, hence 2 PDFs and the combinations of partons possible: e.g quark-antiquark, gluon-quark etc, etc, (n.b. use 7 generalised PDF combinations).
- 2. Need to have grids for both LO and NLO contributions.

•Now the grid generated cross-section looks like.....

$$W = \sum_{p} \sum_{l=0}^{6} \sum_{i_{y1}}^{N_{y1}} \sum_{i_{y2}}^{N_{y2}} \sum_{i_{\tau}}^{N_{\tau}} W_{i_{y1},i_{y2},i_{\tau}}^{(p)(l)} \cdot \alpha_{s}^{p} \left(Q_{i_{\tau}}^{2}\right) \cdot F^{(l)}\left(x_{i_{y1}}, x_{i_{y2}}, Q_{i_{\tau}}^{2}\right)$$
  

$$\bigcap_{Order} \int_{3D \text{ grids}} \int_{3D \text{ grids}} Generalised PDF combinations}$$



Step 2: Multiply grid by PDFs to generate Cross-Section



# **Implementing Grids....**

•The grid implementation used was developed by Carli, Salam, Siegert and is described in (hep-ph/0510324).

•A set of grids is required for calculation of the jet cross-section in a given observable (e.g in pT) of the cross-section.

| Need grids for each order: | 2 |
|----------------------------|---|
| For each subprocess:       | 7 |

Total No. grid per observable: 14

•Each grid is split up into 10 bins in  $x_1, x_2, Q^2$  giving 1000 points.

•Typical file size of grid is 0.1Mb per cross-section and observable bin.

•Code is in C++ and makes use of ROOT libraries, although PDF analyses can be easily carried out in FORTRAN if desired.

•The grid software currently uses the NLOJET++ generator (Z.Nagy)

Dan Clements - ATLAS UK SM meeting (Sep 2006)

# **A Few More Tricks...**

•An initial trial run is carried out to optimise the boundaries in x and  $Q^2$  of the grid (for an observable).

•The co-ordinate transform is designed to reflect the kinematics of the process concerned (i.e. LHC, more bins at low x, high Q<sup>2</sup>) but this can leave the very high x-region under represented.

1. Implement a variable grid spacing:

$$y = \ln\frac{1}{x} + a(1-x)$$

Recall standard co-ordinate transform y=ln(1/x),  $\tau=lnln(Q^2/\Lambda)$ 

2. Employ PDF reweighting to flatten the PDFs in x and hence improve interpolation accuracy.

$$q(x,Q^2) \rightarrow f(x)q(x,Q^2)$$

#### How good are the grids?

•Compared the inclusive jet cross-section at ATLAS as generated using grids and standard NLO calculation (reference) agreement is better than 0.2%



13

Dan Clements - ATLAS UK SM meeting (Sep 2006)

# **Changing the Renormalisation/Factorisation Scales**

•The renormalisation and factorisation scales can be changed after grid production (hep-ph/0510324).

•One grid can be used to generate cross-sections at arbitrary scales.....

•Shown below is the inclusive jet cross-section at ATLAS for 3 scale choices:



Dan Clements – ATLAS UK SM meeting (Sep 2006)

# **PDF Fitting Using Pseudodata**

•Grids were generated for the inclusive jet cross-section at ATLAS in the pseudorapidity ranges  $0 < \eta < 1$ ,  $1 < \eta < 2$ , and  $2 < \eta < 3$  up to pT=3TeV (NLOJET).

•In addition pseudodata for the same process was generated using JETRAD [4].

•The pseudo-data was then used in a global fit to assess the impact of ATLAS data on constraining PDFs and will include TEVATRON data in the future:



# **Effect Of Increased Statistics on PDF Fits**

#### Increase 10×statistics



•Increasing the statistics from 1fb<sup>-1</sup> to 10fb<sup>-1</sup> has little effect on constraining the PDFs at ATLAS.



•Decreasing the uncorrelated systematic errors (on the ATLAS experiment) creates a significant improvement in constraining the PDFS.

# **BootStrap Method To Determine JES Error**

•Standard jet calibration schemes link the hadronic energy scale to the better known EM scale through channels such as Z+jet,  $\gamma$ +jet.

•The cross-sections for these processes decrease with pT, and they become ineffective for determining the JES above pT~500GeV.

#### **Bootstrap Method**

•Use QCD multijet events to bring the calibration at low pT up the pT scale:

Well known low pT jets are used to calibrate high pT jets by demanding a pT balance in the transverse plane.



•Have to be careful not to introduce a selection bias due to resolution fluctutations.

Very Preliminary! – ATLFAST and PYTHIA results.....

•Plotted the means of the distribution pT(jet) - pT(jet balanced) in bins of  $\eta$  and jet pT. In spite of selecting a jet at random there appears to be a bias of ~1% in the balancing procedure....under investigation.....



Dan Clements – ATLAS UK SM meeting (Sep 2006)

# <u>Summary</u>

•Integration grids using high order interpolation methods can be used to recreate NLO cross-sections to accuracies of better than 0.02%.

•Preliminary results using pseudodata indicate that ATLAS jet data can be useful in constraining the gluon PDF.

•Error on gluon PDF that can be extracted from the jet cross-section is dominated by systematics (particularly JES), the statistical error being negligible even for 1fb<sup>-1</sup>

# **Ongoing Developments With Grids And Analysis**

•Documentation being prepared for grid software and LCG interface.

•Software freely available from the authors.

•We are willing to provide grids and provide help to interface to existing Fit-package (CTEQ, MRS etc.)

•Bootstrap method of JES determination under investigation