QCD Effects in B Physics Patricia Ball

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(a) test SM picture of flavour violation: the unitarity triangle

Unitarity of CKM matrix:

$$\sum V_{dj}V_{jb}^*=0$$



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Basic problem: flavour physics masked by strong interactions

How to control QCD effects?

- disentangle physics governed by different mass scales (SM: $m_W, m_t \gg m_b \gg \Lambda_{\rm QCD}$)
- Fermi's 4-fermion theory $(1/m_W)$, heavy quark effective theory $(1/m_b)$, soft-collinear effective theory $(1/\sqrt{m_b}, 1/m_b)$

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- nonperturbative methods (for all the dirty rest)
 - Iattice, QCD sum rules...

A simple 3 step procedure...

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Step 1: obtain effective Lagrangian at scale $\sim m_W$ by integrating out effects from heavy particles: W, t and any BSM particles:



SM diagrams \rightarrow short-distance coefficient $C(m_W) \times$ effective operator



Step 2: include radiative corrections:

and resum large logs in $\alpha_s \ln(m_W/m_b)$:

$$\mathcal{L}_{\text{eff}} = \frac{G_F}{\sqrt{2}} \sum_i \frac{C_i(\mu)O_i(\mu)}{\sum_i} \left\{ 1 + \mathcal{O}\left(\frac{m_b^2}{m_W^2}\right) \right\}$$

- C_i : Wilson-coefficients, containing short-distance effects
- O_i : dim-6 operators, e.g. $(\bar{d}u)_{V-A}(\bar{c}b)_{V-A}$, describing long-distance effects
- \mathcal{L}_{eff} for nonleptonic decays known to NNLO
- \mathcal{L}_{eff} for radiative decays almost known to NNLO
- BSM effects in some scenarios known to NLO, e.g. MSSM with Minimal Flavour Violation (Degrassi/Gambino/Slavich 06)

(Gorbahn/Haisch 04)

(Misiak et al. 06)

Step 3: take hadronic matrix elements

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- full calculation on the lattice or from QCD sum rules
 - form factors, i.e. matrix elements $\langle F|O_i|B\rangle$

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 - total width of inclusive decays and moments of $b \rightarrow ce\nu$ transitions
- expansion in $1/m_b$ and factorisation in terms of nonlocal (light-cone) matrix elements
 - inclusive $b \rightarrow \text{light}$ transitions with experimental cuts
 - exclusive (in particular nonleptonic and radiative) decays, e.g. $B \to \pi \pi, B \to K^* \gamma$

Let's focus on a few examples...

B_s Mixing & New Physics

Ball/Fleischer, hep-ph/0604249

Phenomenology of *B* Mixing

- $\bar{B}^0 = (b\bar{q})$ and $B^0 = (q\bar{b})$ (q = d, s) with definite flavour content, but not mass eigenstates \rightsquigarrow Mixing!
- mixing induces mass and width mixing matrices M_{ab} , Γ_{ab}
- observables: ΔM , $\Delta \Gamma$, mixing-induced CP asymmetries $A_{\rm CP}(B_d \to J/\psi K_S)$, $A_{\rm CP}(B_s \to J/\psi \phi)$, semileptonic CP asymmetry $A_{\rm SL}^q$
- ΔM_d well known, ΔM_s first measured in 2006 (CDF)
- $\arg M_{12}^d = 2\beta$ (in the SM); $\arg M_{12}^s \approx 0$ (in the SM): no direct measurement yet, wait for LHC(b)
- M_{12} loop induced, sensitive to new physics

Any hint of new physics yet?

ΔM_q in the SM



$$= \frac{G_{\rm F}^2 M_W^2}{12\pi^2} M_{B_q} \hat{\eta}^B \hat{B}_{B_q} f_{B_q}^2 (V_{tq}^* V_{tb})^2 S_0(x_t)$$

• $S_0(x_t = m_t^2/M_W^2) = 2.35 \pm 0.06$: Inami-Lim function

• $\hat{\eta}^B = 0.552$: NLO QCD correction (Buras/Jamin/Weiss '90)

• $\hat{B}_{B_q} f_{B_q}^2 \propto \langle B_q^0 | (\bar{q}b)_{V-A} (\bar{q}b)_{V-A} | \bar{B}_q^0 \rangle$: hadronic matrix element, from lattice

• $V_{tq}^*V_{tb}$: from tree-level processes

Generic Parametrisation of New Physics

 $\Delta M_s = 2 |M_{12}^s|$ with

•
$$M_{12}^s = M_{12}^{s, \text{SM}} (1 + \kappa_s e^{i\sigma_s})$$

• $\kappa_s > 0$: NP amplitude • σ_s : new CP-violating phase Lines of $\rho_s = \text{const.}$:



Deviation from SM measured by

$$\rho_s \equiv \left| \frac{\Delta M_s}{\Delta M_s^{\rm SM}} \right| = (1 + 2\kappa_s \cos \sigma_s + \kappa_s^2)^{1/2}$$

Q: What is the SM prediction of ΔM_s ?

Predictions of $\Delta M_s^{ m SM}$

Need hadronic matrix elements from lattice.

Two unquenched calculations available:

- JLQCD: $N_f = 2$ Wilson fermions
- HPQCD: $N_f = 2 + 1$ staggered light + NRQCD heavy fermions



Predictions of $\Delta M_s^{ m SM}$

$$\begin{split} \Delta M_s^{\rm SM} \big|_{\rm JLQCD} &= (16.1 \pm 2.8) \, {\rm ps}^{-1} \\ \rho_s \big|_{\rm JLQCD} &= 1.08^{+0.03}_{-0.01} (\exp) \pm 0.19 ({\rm th}) \\ \Delta M_s^{\rm SM} \big|_{\rm HPQCD} &= (21.2 \pm 3.2) \, {\rm ps}^{-1} \\ \rho_s \big|_{\rm HPQCD} &= 0.82^{+0.02}_{-0.01} (\exp) \pm 0.12 ({\rm th}) \quad 1.5\sigma! \end{split}$$



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Conclusion from this exercise:

 $\Delta M_s^{\rm SM}$ is actually not very well known!

For better constraints, need mixing phase $\phi_s = \arg M_{12}^s!$

Constraints from ϕ_q

 $\rho_q = \text{const.:}$



$$\phi_q = \arg M_{12}^q = \phi_q^{\mathrm{SM}} + \phi_q^{\mathrm{NP}}$$
 with $\phi_s^{\mathrm{SM}} = -2\lambda^2 R_b \sin \gamma \approx -2^\circ$

Status of ϕ_s

• brand-new constraints from $A_{\rm SL}^s$ and $\Delta \Gamma_s$: (Lenz/Nierste, hep-ph/0612167)

 $\sin \phi_s = -0.77 \pm 0.04 (\text{th}) \pm 0.34 (\text{exp})$ (SM: ≈ -0.06)

result heavily theory dependent!

• for more precise results, have to wait for $A_{\rm CP}(B_s \rightarrow J/\psi \phi)$ at LHC



$|V_{td}/V_{ts}|$ & UT angle γ from $B ightarrow (ho, K^*) \gamma$

Ball/Jones/Zwicky, hep-ph/0612081

Radiative Penguins





 $B
ightarrow (
ho, \omega) \gamma \quad \longleftrightarrow \quad b
ightarrow d\gamma$

• QCD factorisation:

$$\begin{aligned} A(B \to V\gamma) &= \sum_{i=1}^{8} \sum_{U=u,c} \lambda_{U} C_{i} \langle V\gamma | Q_{i}^{U} | B \rangle \\ \langle V\gamma | Q_{i}^{U} | B \rangle &= \left[T_{1}^{B \to V}(0) T_{i}^{I} + \int_{0}^{1} d\xi \, du \, T_{i}^{II}(\xi, u) \, \phi_{B}(\xi) \, \phi_{2;V}^{\perp}(u) \right] \cdot e \end{aligned}$$

- λ_U : CKM factors
- $C_i, T_i^{I,II}$: perturbative QCD quantities
- $T_1, \phi_B, \phi_{2;V}^{\perp}$: non-perturbative QCD quantities

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• QCD factorisation formula valid to leading order in $1/m_b$, only some corrections in $1/m_b$ can be treated in QCDF

QCD factorisation:

$$\begin{split} A(B \to V\gamma) &= \sum_{i=1}^{8} \sum_{U=u,c} \lambda_U C_i \langle V\gamma | Q_i^U | B \rangle \\ \langle V\gamma | Q_i^U | B \rangle &= \left[T_1^{B \to V}(0) T_i^I + \int_0^1 d\xi \, du \, T_i^{II}(\xi, u) \, \phi_B(\xi) \, \phi_{2;V}^\perp(u) \right] \cdot e \\ T_i^I &= \underbrace{I_i^{O \circ O}}_{I_i^O \circ O} \underbrace{I_i^O \circ O}_{I_i^O \circ O} \underbrace{I_i$$

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Contributions at $O(1/m_b)$:





- weak annihilation
- can be treated in QCDF
- relevant for $\mathcal{B}(B \to \rho \gamma)$ and isospin asymmetries
- long-distance photon emission, beyond QCDF, relevant for $\mathcal{B}(B^{\pm} \rightarrow \rho^{\pm}\gamma)$



- soft gluon emission
- beyond QCDF, new method developed by Ball/Jones/Zwicky 06
- relevant for $\mathcal{B}(B \to V\gamma)$ and time-dependent CP asymmetry

Form Factors

state-of-the-art results from QCD sum rules on the light-cone: (Ball/Zwicky 04)

$$T_1^{\rho}(0)$$
 $T_1^{\omega}(0)$ $T_1^{K^*}(0)$ 0.27 ± 0.04 0.25 ± 0.04 0.31 ± 0.04

better accuracy for ratios:

$$\boldsymbol{\xi_{\rho}} \equiv \frac{T_1^{K^*}}{T_1^{\rho}} = 1.17 \pm 0.09 \qquad \boldsymbol{\xi_{\omega}} \equiv \frac{T_1^{K^*}}{T_1^{\omega}} = 1.30 \pm 0.10$$

strategy for predicting branching ratios:

$$\overline{\mathcal{B}}(B \to V\gamma)\big|_{\mathrm{th}} = \left[\frac{\overline{\mathcal{B}}(B \to V\gamma)}{\overline{\mathcal{B}}(B \to K^*\gamma)}\right]_{\mathrm{th}, \xi_V} \overline{\mathcal{B}}(B \to K^*\gamma)\big|_{\mathrm{exp}}$$

Theory Predictions for $B ightarrow (ho, \omega) \gamma$



 $\left|V_{td}/V_{ts}
ight|$

$$\frac{\overline{\mathcal{B}}(B \to (\rho, \omega)\gamma)}{\overline{\mathcal{B}}(B \to K^*\gamma)} \equiv R_{\rho/\omega} = \left|\frac{V_{td}}{V_{ts}}\right|^2 \left(\frac{1 - m_{\rho}^2/m_B^2}{1 - m_{K^*}^2/m_B^2}\right)^3 \frac{1}{\xi_{\rho}^2} \left[1 + \Delta R\right]$$

BaBar 06: $R_{\rho/\omega} = 0.030 \pm 0.006$, Belle 05: 0.032 ± 0.008

Ball/Zwicky 06: $\xi_{\rho} = 1.17 \pm 0.09$

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 ΔR depends on $|V_{td}/V_{ts}|$ itself!

- p.21

ΔR

Solution: use truly independent set of CKM parameters:



Results

From 2006 BaBar data:

$$\left|\frac{V_{td}}{V_{ts}}\right| = 0.199^{+0.022}_{-0.025}(\exp) \pm 0.014(\text{th}) \longleftrightarrow \gamma = (61.0^{+13.5}_{-16.0}(\exp)^{+8.9}_{-9.3}(\text{th}))^{\circ}$$

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Results from other methods:

• from *B* mixing: $\Delta M_s / \Delta M_d$:

$$\left|\frac{V_{td}}{V_{ts}}\right| = 0.206^{+0.0081}_{-0.0060}(\text{th}) \pm 0.0007(\text{syst})$$

• depends on lattice input: $f_{B_s} \sqrt{B_{B_s}} / f_{B_d} \sqrt{B_{B_d}} = 1.21^{+0.047}_{-0.035}$ (Okamoto, Lattice 2005)

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Results from other methods:

theory independent: Dalitz plot analysis of CP asymmetry in $B^- \rightarrow D^0 K^-$ with $(D^0, \overline{D}{}^0) \rightarrow K_S \pi^+ \pi^-$: BaBar : $\gamma = (92 \pm 41 \pm 11 \pm 12)^{\circ}$, Belle: $\gamma = (53^{+15}_{-18} \pm 3 \pm 9)^{\circ}$ • SU(3) fits $(B \to \pi \pi \text{ and } B \to \pi K)$: $\gamma = (70.0^{+3.8}_{-4.3})^{\circ}$ (Fleischer 06) • QCD factorisation in $B \to PV$: $\gamma = (62 \pm 8)^{\circ}$ (Beneke/Neubert 03) • SCET in $B \to \pi \pi$: $\gamma = (73.9^{+7.4}_{-10.7})^{\circ}$ (Stewart 06)

Time-dependent CP Asymmetry in $B \to K^* \gamma$

Ball/Zwicky, hep-ph/0609037

 $A_{
m CP}(B
ightarrow K^* \gamma)$

- $b \rightarrow s \gamma$ is actually either
 - $b_R \rightarrow s_L \gamma_L$ (with helicity factor m_b) or
 - $b_L \rightarrow s_R \gamma_R$ (with helicity factor m_s)
- γ dominantly left-polarised, γ_R suppressed by m_s/m_b
- entails a small time-dependent CP asymmetry (interference of γ_L/γ_R amplitudes):

$$A_{\rm CP} = \frac{\Gamma(\bar{B}^0(t) \to \bar{K}^{*0}\gamma) - \Gamma(B^0(t) \to K^{*0}\gamma)}{\Gamma(\bar{B}^0(t) \to \bar{K}^{*0}\gamma) + \Gamma(B^0(t) \to K^{*0}\gamma)}$$
$$\approx -2\frac{m_s}{m_b}\sin(2\beta)\sin(\Delta M_d t) \approx -3\%$$

null-test of the SM!

(Gershon/Soni 06)

 helicity suppression removed by new physics if splin flip can occur on internal line (e.g. in left-right symmetric models)

$$A_{
m CP}(B
ightarrow K^* \gamma)$$

- helicity suppression removed by new physics if splin flip can occur on internal line (e.g. in left-right symmetric models)
- caveat emptor! No helicity suppression in 3-parton process $b \rightarrow s\gamma g$:



- all contributions $b \to s \gamma_R g \sim O(1/m_b)$
- dominant contribution from charm loop (with large Wilson coefficient ~ 1)
- contributes to $B \to K^* \gamma$ if B or K^* in 3-particle quark-antiquark-gluon state
- previous estimate: c loop increases $|A_{CP}|$ to 10% with large uncertainties, up from 3% (Grinstein/Pirjol 05)

Can one do better?



- calculate effective operator for soft-gluon emission in $1/m_c$ expansion
- calculate matrix element from QCD sum rules on the light-cone
- contribution $A_{\rm CP}^{\rm c\ loop} = +(0.5 \pm 1)\%$

• all together:
$$A_{\rm CP}(B \to K^* \gamma) = -(2.2 \pm 1.5^{+1}_{-0})\%$$

- experimental result: $-(28 \pm 26)\%$
- $B \to K^* \gamma$ difficult for LHC; $B_s \to \phi \gamma$ better suited;

SM prediction of CP asymmetry: $A_{\rm CP}(B_s \rightarrow \phi \gamma) = (0.1 \pm 0.1)\%$

• any measured CP violation larger than a few percent unambiguous signal for new physics with non-standard weak couplings (not V - A)!

Summary

Summary

- in order to fully explore (both old and new) flavour physics in B decays, need to understand strong interaction physics
- QCD enters at all scales (m_W , m_b , $\sqrt{m_b\Lambda_{\rm QCD}}$, $\Lambda_{\rm QCD}$)
- the perturbative treatment of QCD effects is organised in terms of short-distance coefficients in effective field theories and scattering amplitudes in factorisation formulas; they are well under control
- nonperturbative QCD effects are organised in terms of matrix elements of effective local or nonlocal (light-cone) operators and are under good to reasonable control
- determination of CKM matrix elements fine except for possible tension between $|V_{ub}|$ from UTangles and inclusive $b \rightarrow ue\nu$ (2.5 σ)
- for new physics searches, identify observables sensitive to new physics which are zero or near zero in the SM: null tests of the SM
 - Example: time-dependent CP asymmetry in $B \to K^* \gamma$

Happy Penguins...



Happy Penguins...

Who would have thought it would be a Little Higgs?



