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# Status on the disformally coupled galileon from cosmological data and GW170817

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September 4, 2018

IRN Terascale 2018 - IPPP Durham





#### I. Presentation of the galileon model

#### II. Methodology and datasets

III. Results





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#### II. Methodology and datasets

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- Simple principles for a successful extension of General Relativity :
  - Additional scalar field :  $\pi$
  - Galilean symmetry in Minkowskii space-time :

$$\pi \to \pi + c + b_\mu x^\mu$$

- $2^{nd}$  order e.o.m in  $\pi$  derivatives : avoid Ostrogradski ghosts
- Direct couplings to matter : conformal and/or disformal



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Disfavoured by Neveu et al. 2016



#### Most general action :

$$\mathcal{S}[\phi, g, \pi] = \mathcal{S}_{SM}[\phi, g] + \int d^4x \sqrt{-g} \left[ \frac{M_P^2}{2} R - \frac{1}{2} \sum_{i=1}^5 \frac{c_i}{M^{3(i-2)}} \mathcal{L}_i - \frac{M_P}{M^3} c_G G^{\mu\nu} \pi_{;\mu} \pi_{;\nu} \right]$$

$$\mathcal{L}_{1} = \pi$$
  

$$\mathcal{L}_{2} = \pi_{;\mu}\pi^{;\mu} \equiv X$$
  

$$\mathcal{L}_{3} = X \Box \pi$$
  

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 Non-linear lagrangians necessary to screen the galileon at small scales (Vainshtein effect)





#### I. Presentation of the galileon model

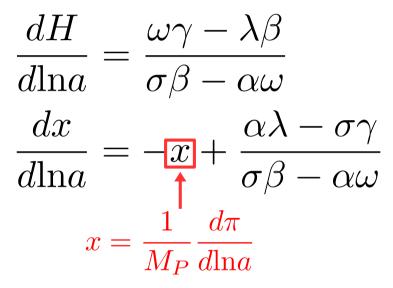
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#### **III.Results**



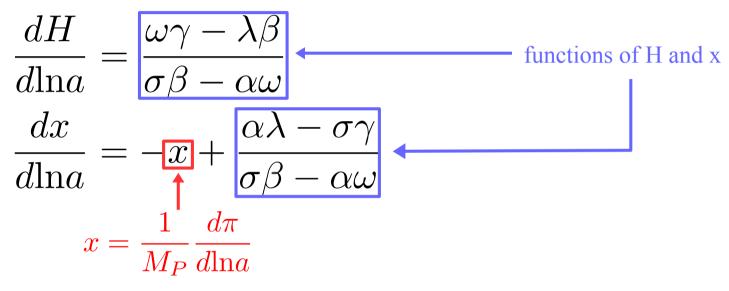
$$\frac{dH}{d\ln a} = \frac{\omega\gamma - \lambda\beta}{\sigma\beta - \alpha\omega}$$
$$\frac{dx}{d\ln a} = -x + \frac{\alpha\lambda - \sigma\gamma}{\sigma\beta - \alpha\omega}$$





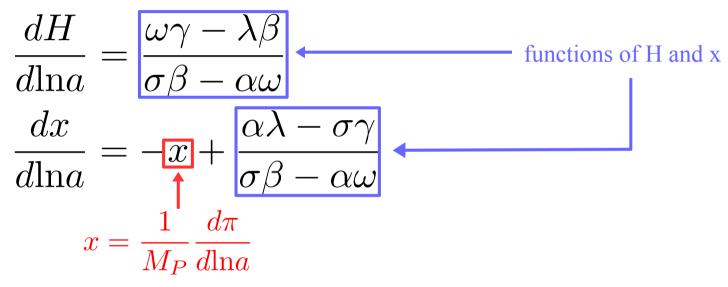








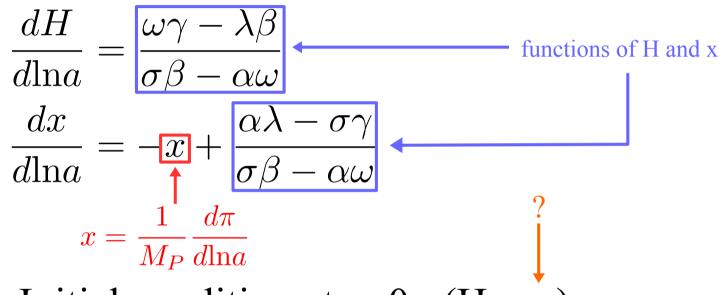




> Initial condition at z=0: (H<sub>0</sub>, x<sub>0</sub>)



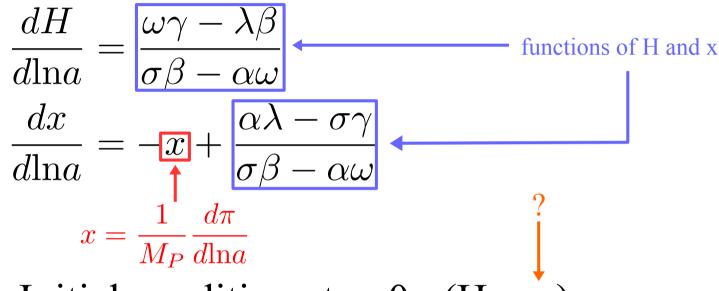




> Initial condition at  $z=0: (H_0, x_0)$ 





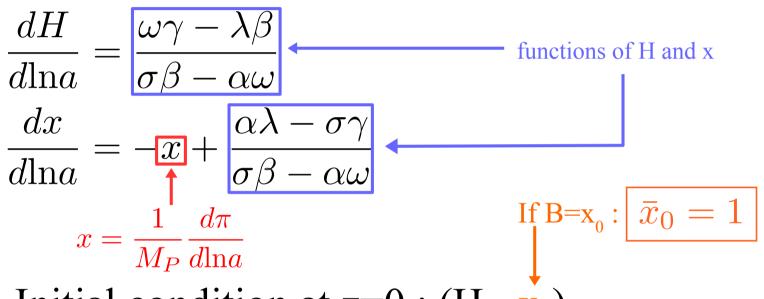


- > Initial condition at  $z=0:(H_0, x_0)$
- Scaling invariance :

$$\begin{array}{rccc} c_i & \to & \bar{c}_i \equiv c_i B^i, & i = 2, ..., 5 \\ c_G & \to & \bar{c}_G \equiv c_G B^2 \\ x & \to & \bar{x} \equiv x/B \end{array}$$







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  - Full galileon :  $\{\overline{c}_2, \overline{c}_3, \overline{c}_4, \overline{c}_5, \overline{c}_G, \overline{x}_0\}$



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Fixed by re-scaling

Fixed by flatness condition at z=0 :  $\Omega_{\pi}^{0} = 1 - \Omega_{m}^{0} - \Omega_{r}^{0}$ 



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Free parameters Fixed by flatness condition at z=0 :  $\Omega_{\pi}^{0} = 1 - \Omega_{m}^{0} - \Omega_{r}^{0}$ 





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  - Cubic galileon :  $\{\overline{c_2}, \overline{c_3}, \overline{c_4}, \overline{c_5}, \overline{c_G}, \overline{x_0}\}$

Fixed by flatness condition

Set to 0



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  - attractor solutions
  - additional relation on the  $\bar{c}_i$  parameters
  - analytic solutions for the background evolution



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- Galileon predictions obtained using our own modified version of Boltzmann code CAMB



- MCMC exploration of the parameter space against cosmological observations
  - $\rightarrow$  Our own modified version of CosmoMC
  - $\rightarrow$  Reject sets of parameters that fail stability conditions
  - CMB : Planck 2015 TTTEEE+lowP+lensing
  - BAO : 6dF, MGS, BOSS DR12
  - SN Ia : JLA sample



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→ base parameters { $\Omega_b h^2$ ,  $\Omega_c h^2$ ,  $100\theta_{MC}$ ,  $\tau$ ,  $A_s$ ,  $n_s$ }



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- A posteriori comparison to GW speed constraint from GW170817



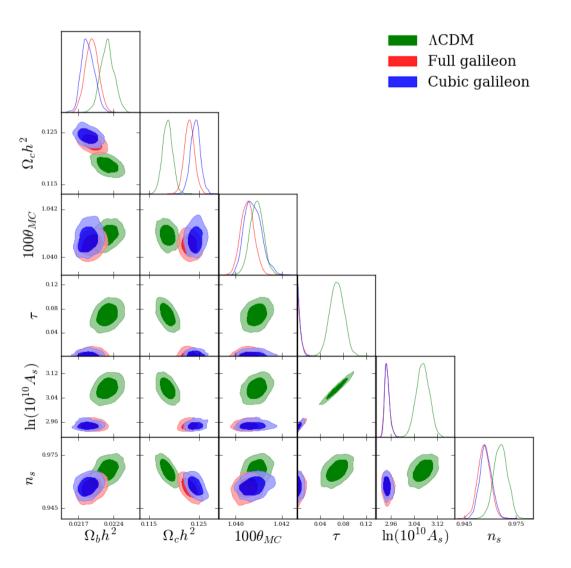


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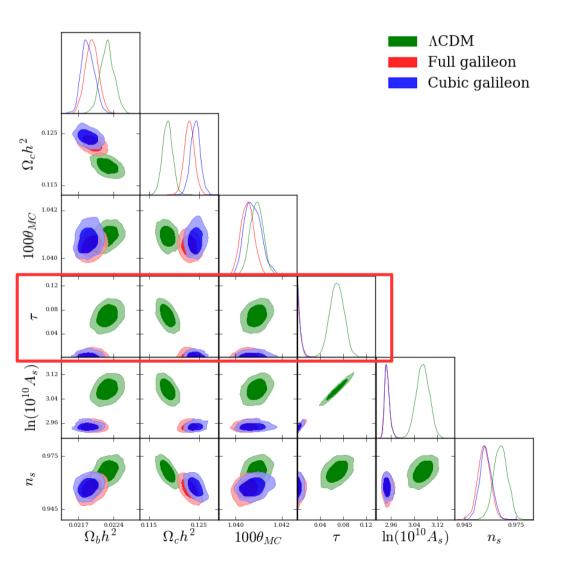
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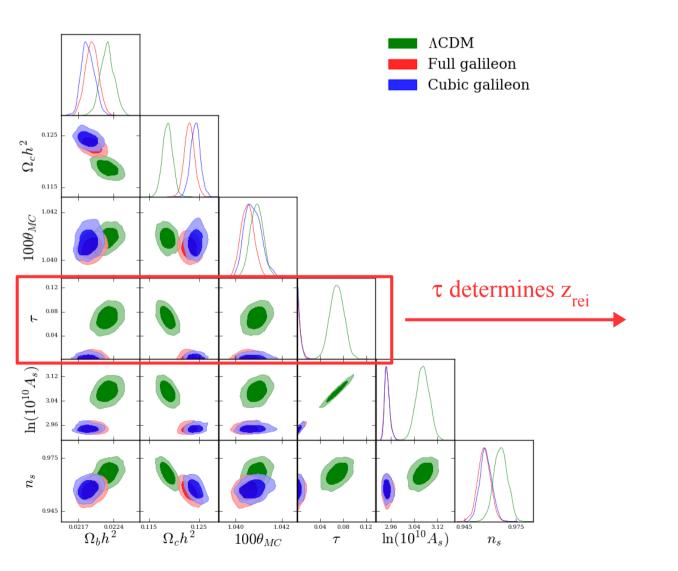




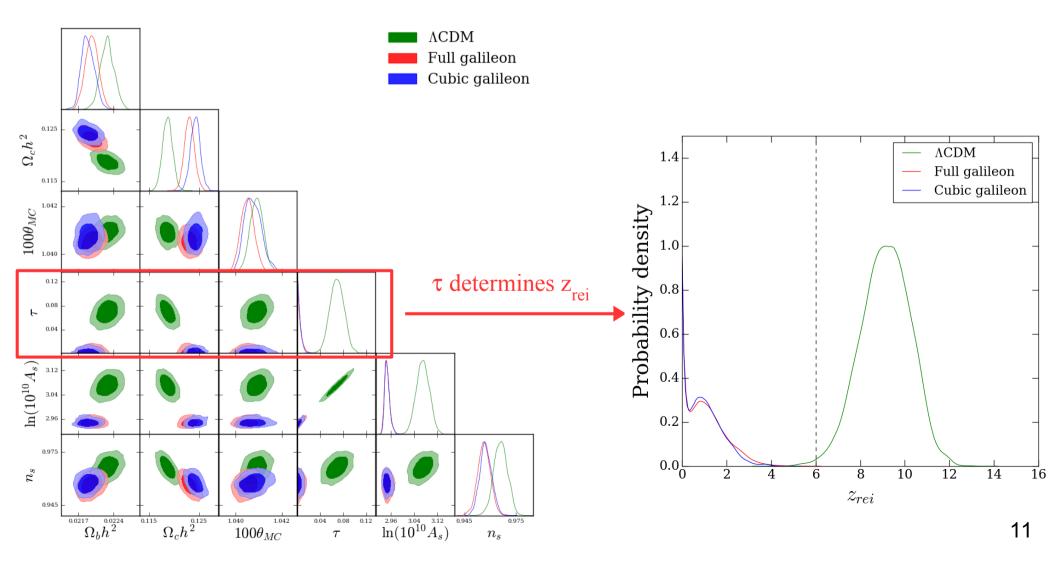














		$\chi^2(\text{CMB})$	$\chi^2(BAO)$	$\chi^2(\text{JLA})$
Λ	CDM	12946	5.6	706.7
Full	galileon	12966	30.4	723.3
Cubic	galileon	12993	29.9	723.6

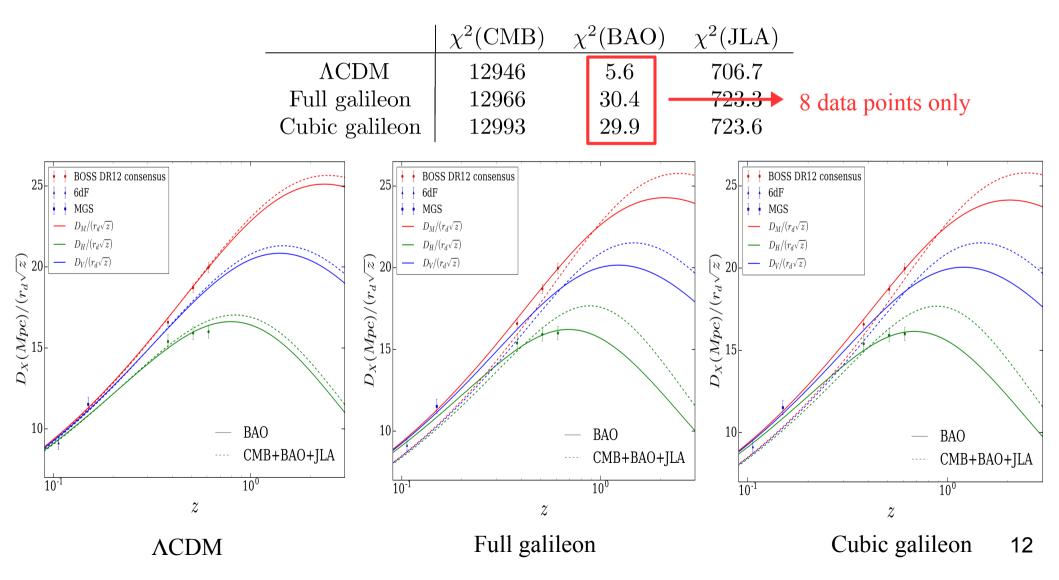


Fit to combined cosmological data (CMB+BAO+JLA) :

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ΛCDM	12946	5.6	706.7	
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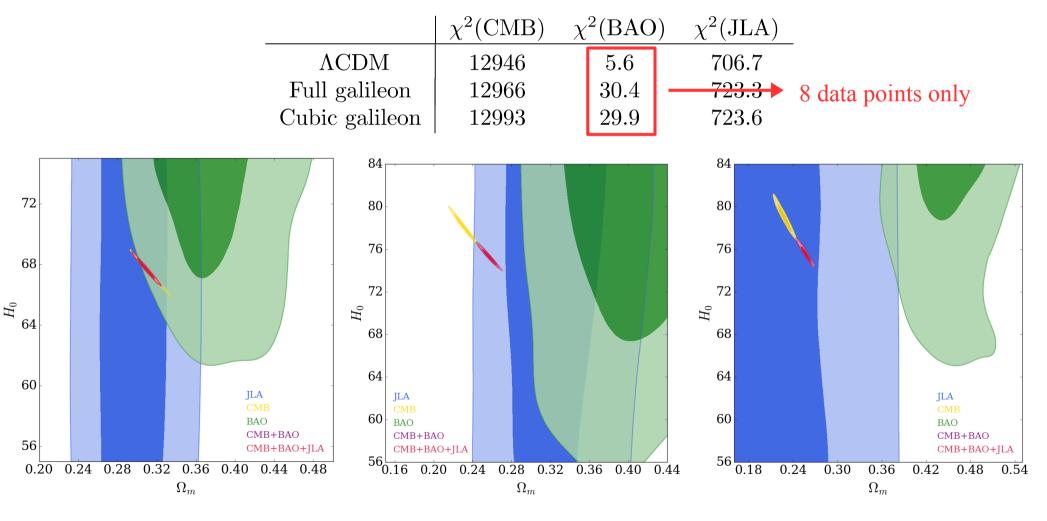


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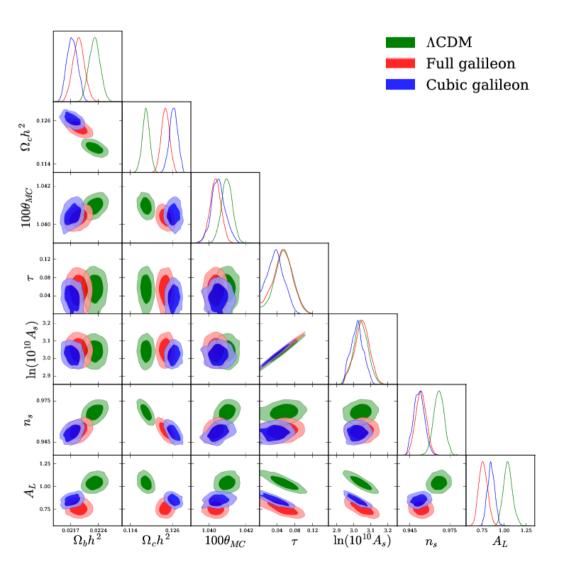


ΛCDM

Full galileon

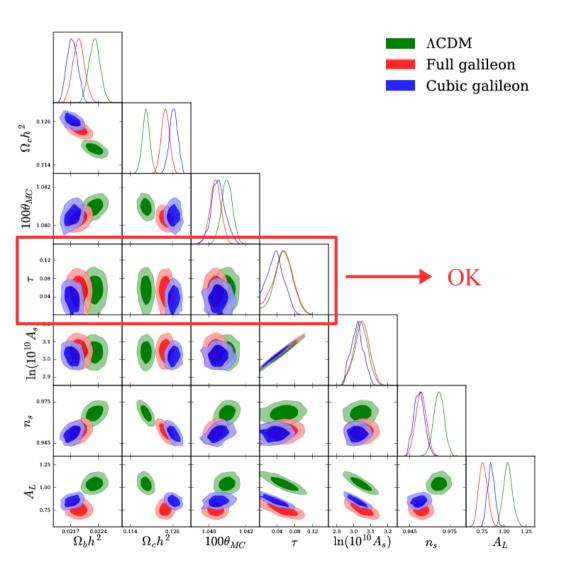


> Model extended to the parameter  $A_L$ :



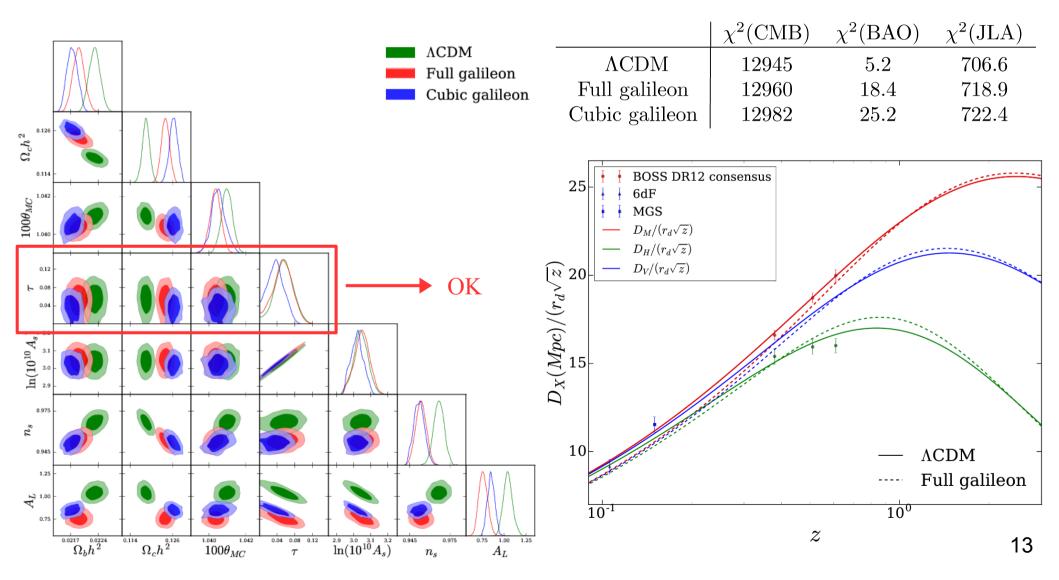


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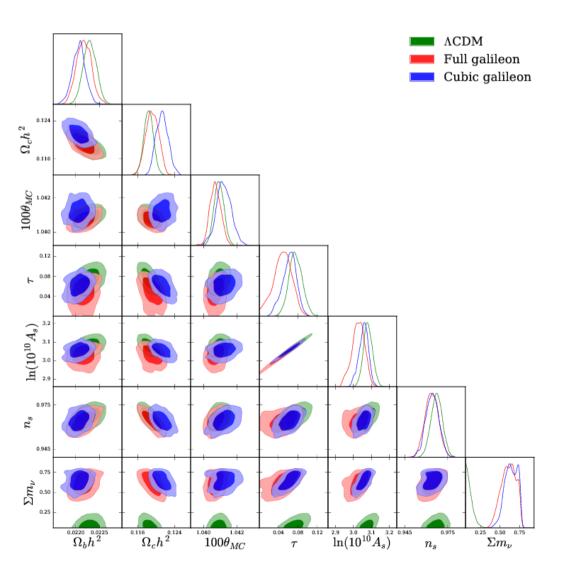


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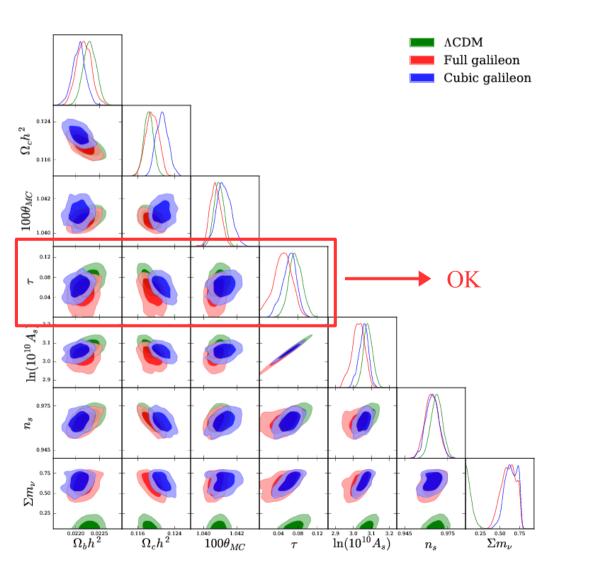


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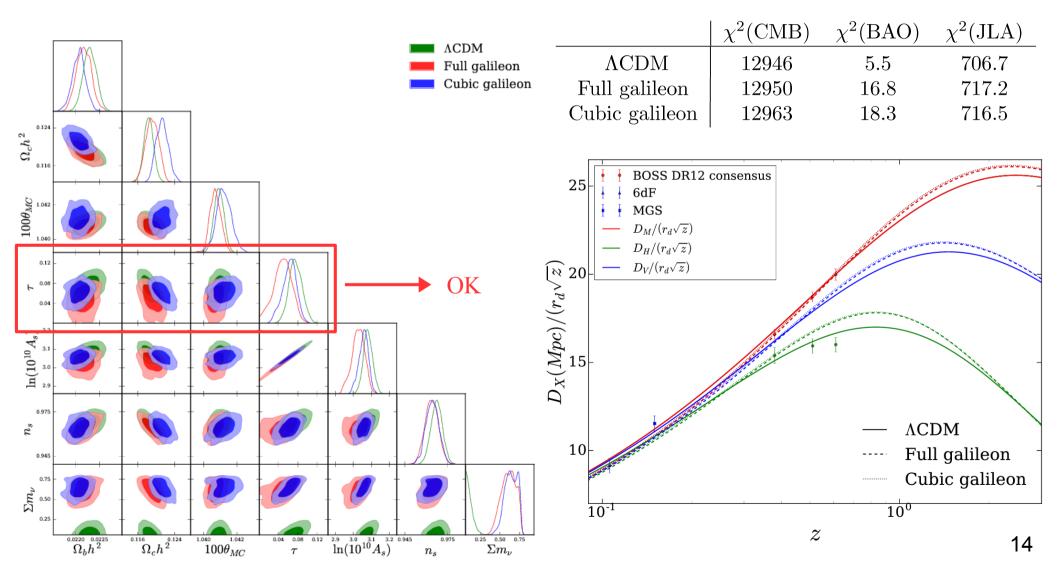


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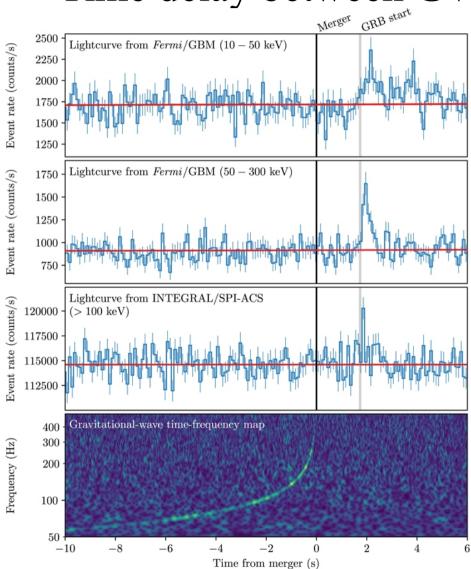


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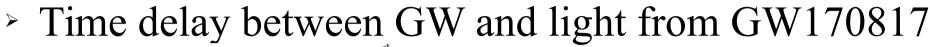


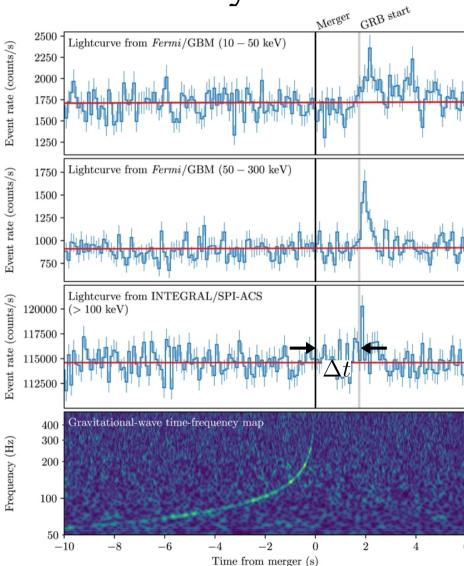
### > Time delay between GW and light from GW170817



arXiv:1710.05834



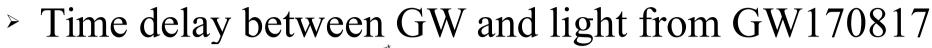


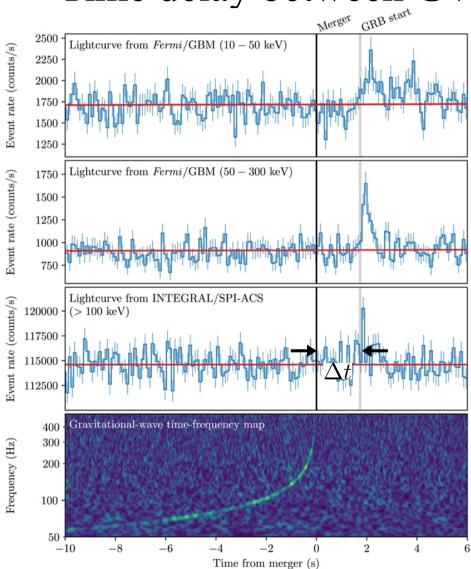


arXiv:1710.05834

 $\Delta t = \int_{a_c}^{1} \frac{da}{aH} \left( 1 - \frac{c}{c_g(a)} \right) + \delta t$  $= 1.74 \pm 0.05 s$ 

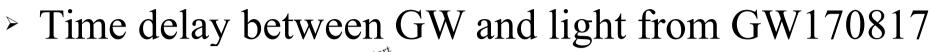


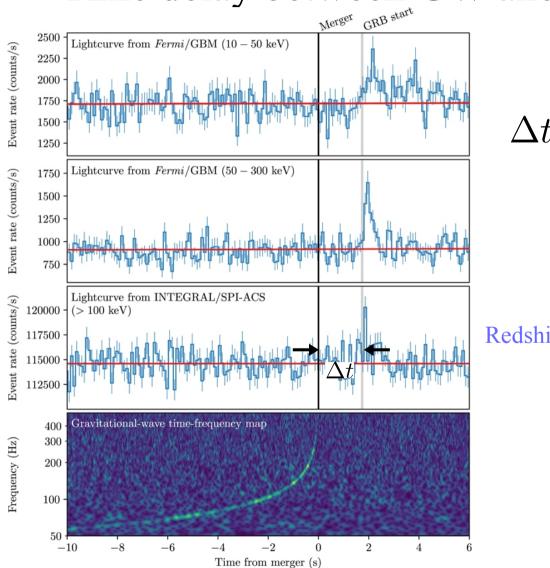




$$\Delta t = \int_{a_e}^{1} \frac{da}{aH} \left( 1 - \frac{c}{c_g(a)} \right) + \delta t$$
  
= 1.74 ± 0.05s   
Speed of GW



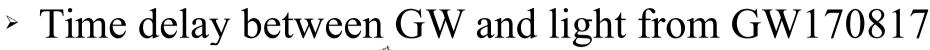


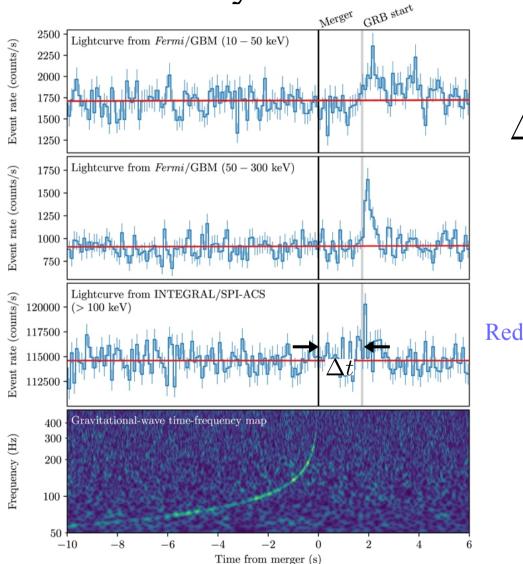


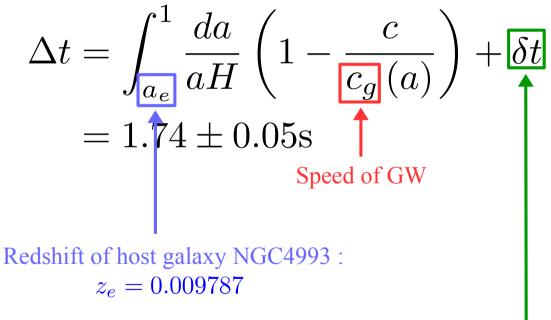
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Speed of GW

 $z_e = 0.009787$ 





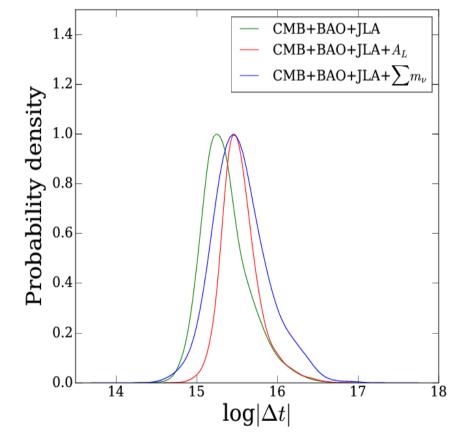




Time delay between GW emission and light emission. Conservative assumption (arXiv:1710.05834) :  $\delta t \in [-1000s, 100s]$ 



▹ Modification of GW speed only due to  $c_4$ ,  $c_5$  and  $c_G$ ⇒ affects only the full galileon model



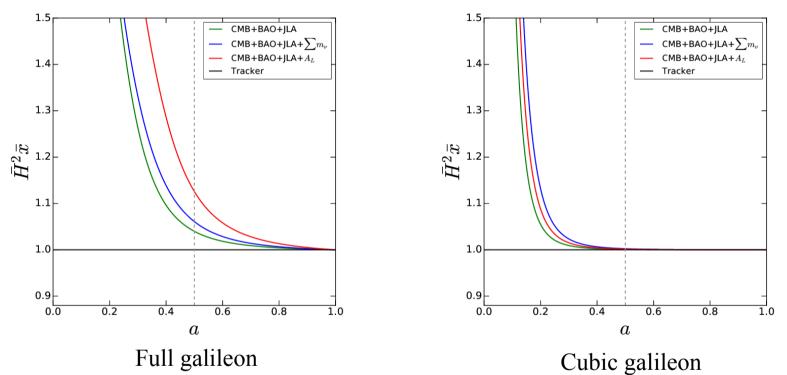
>  $\Delta t > 10^{14}$  sec ~ a few million years



- Study of a theoretically well motivated extension of General Relativity
- Base galileon models in strong tension with BAO data and reionization constraints
- > Extended models with  $A_L$  and  $\Sigma m_v$  better, but still in tension with BAO
- > GW170817 excludes completely the full galileon model
- First full galileon parameter space exploration after Planck



Was the full exploration useful ?



- Best fits of extended full galileon models converge towards tracker later than the beginning of DE dominated era
  - $\Rightarrow$  risk of missing interesting scenarios if restraining to tracker



### Thank you !



 $\tilde{g}_{\mu\nu} = A(\pi, X) g_{\mu\nu} + B(\pi, X) \nabla_{\mu} \pi \nabla_{\nu} \pi$ 

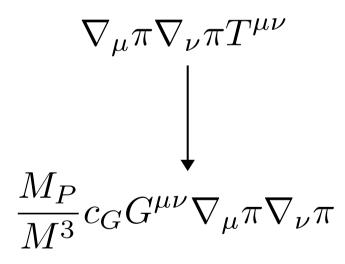
Conformal transformation

$$\pi T^{\mu}_{\mu}$$

$$\downarrow$$

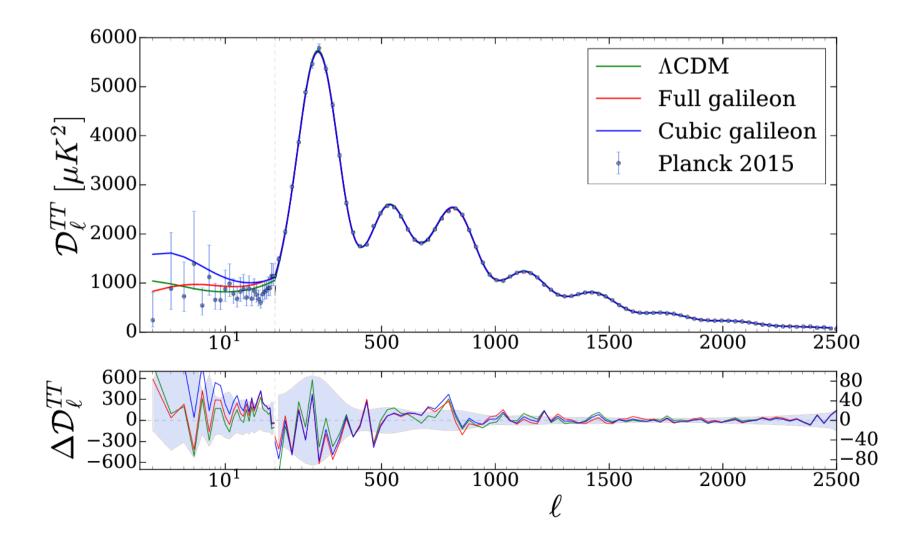
$$M_P c_0 \pi R$$

Disformal transformation



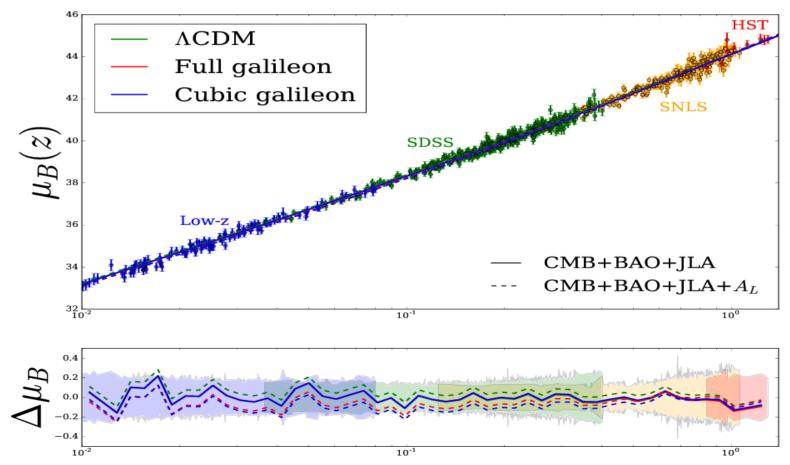


### > TT powerspectrum with $A_L$



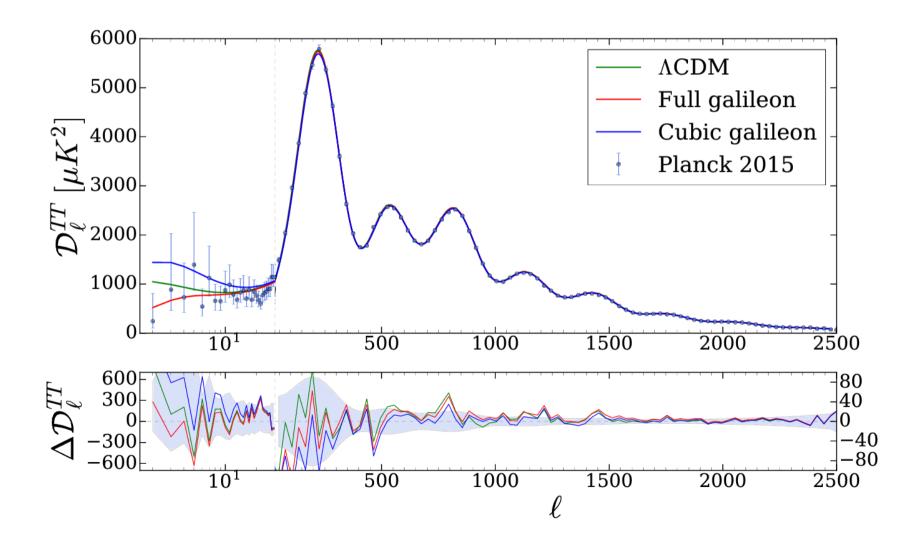


> SN hubble diagram with  $A_L$ 





### > TT powerspectrum with $\Sigma m_v$





> SN hubble diagram with  $\Sigma m_{\nu}$ 

