

Standard Model theory (EW & top)

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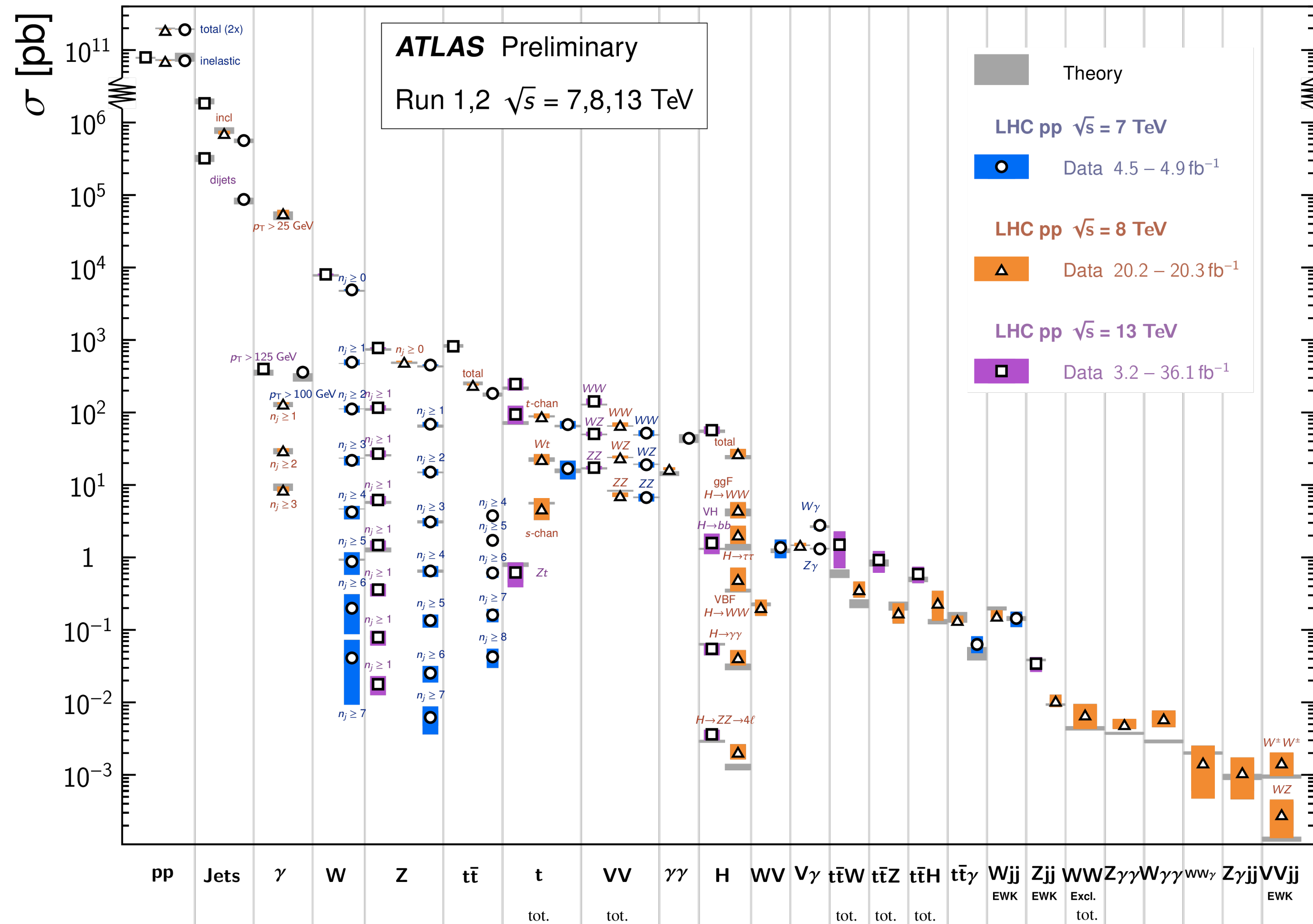


Pushing the Boundaries of the Energy and Intensity Frontiers
-- the HL-LHC and Beyond
IPPP, 4.7.18

The success of the SM

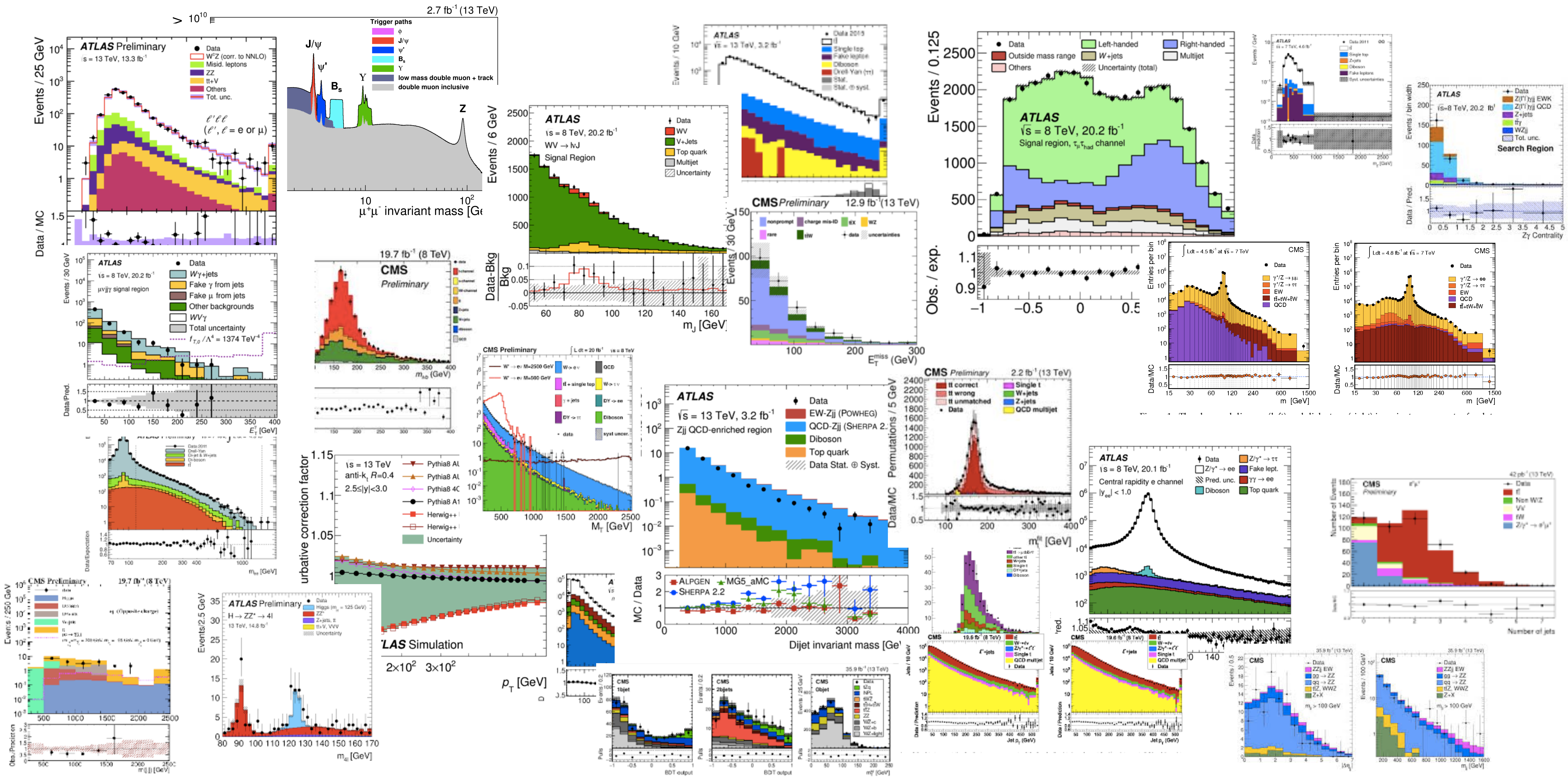
Standard Model Production Cross Section Measurements

Status: March 2018



Overall extremely good
experiment-theory agreement

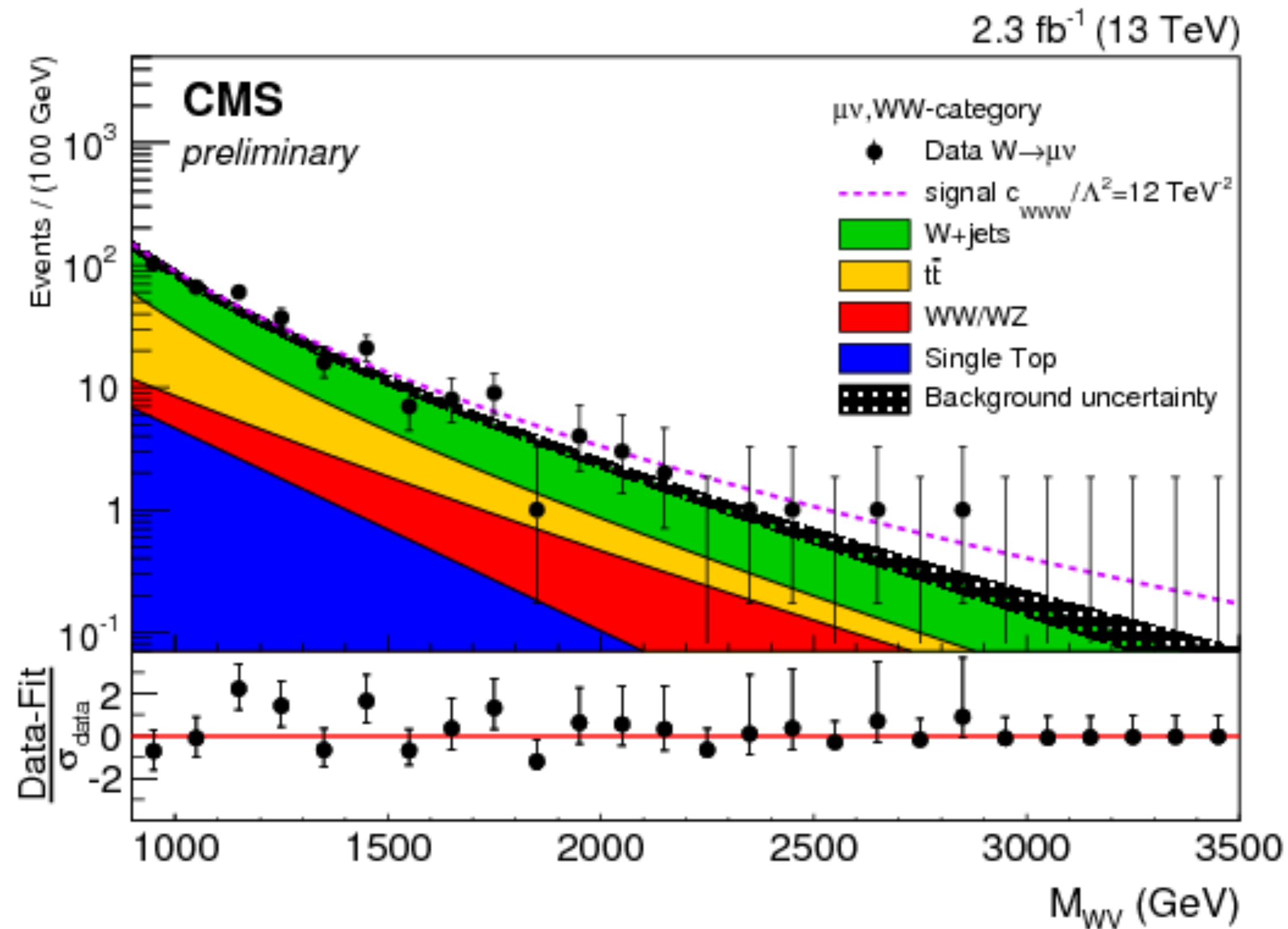
Differential SM measurements



The need for precision in tails

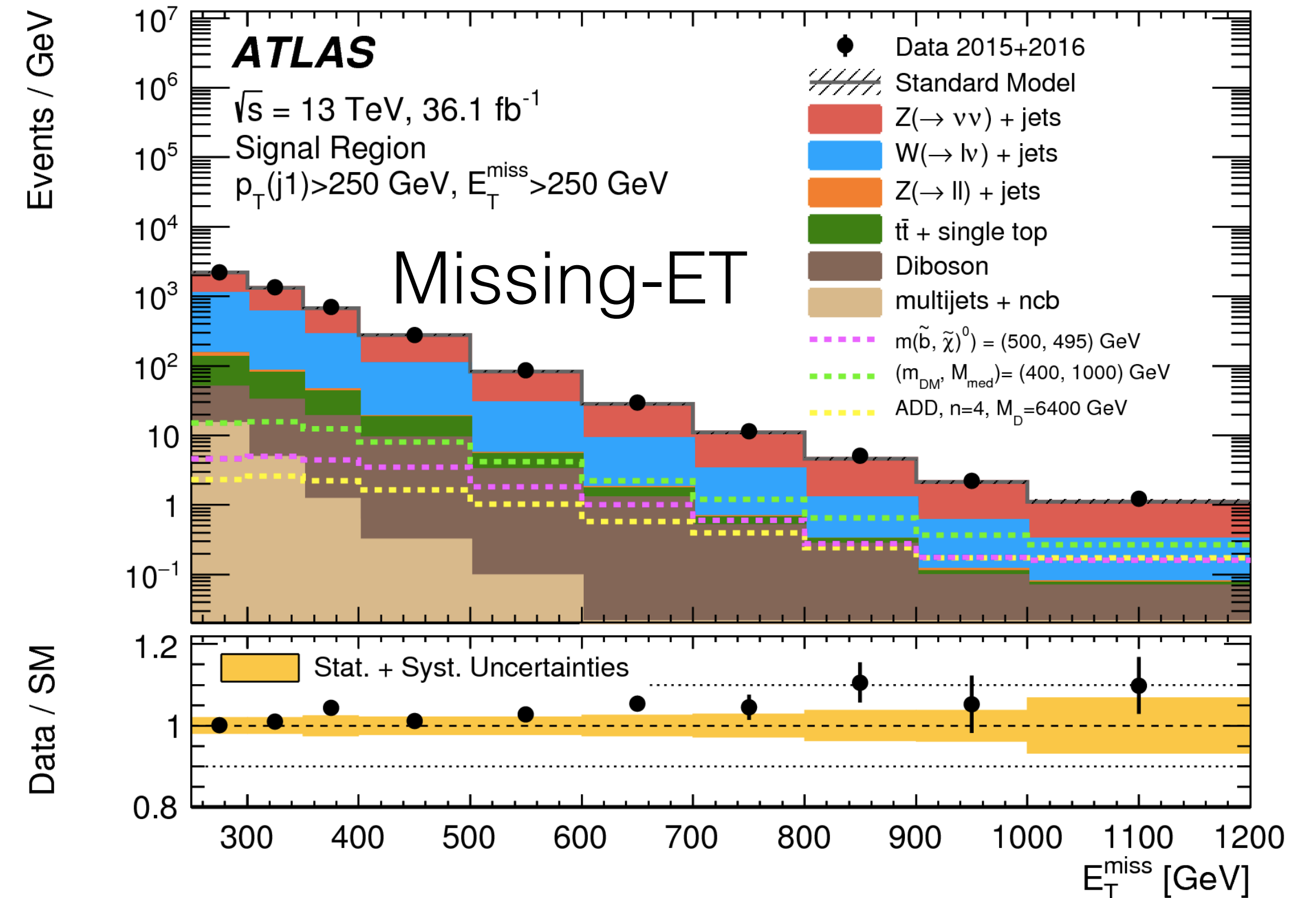
Diboson

Dark Matter



- In case new physics is heavy: expect small deviations in tails of distributions

→ good control on theory necessary!

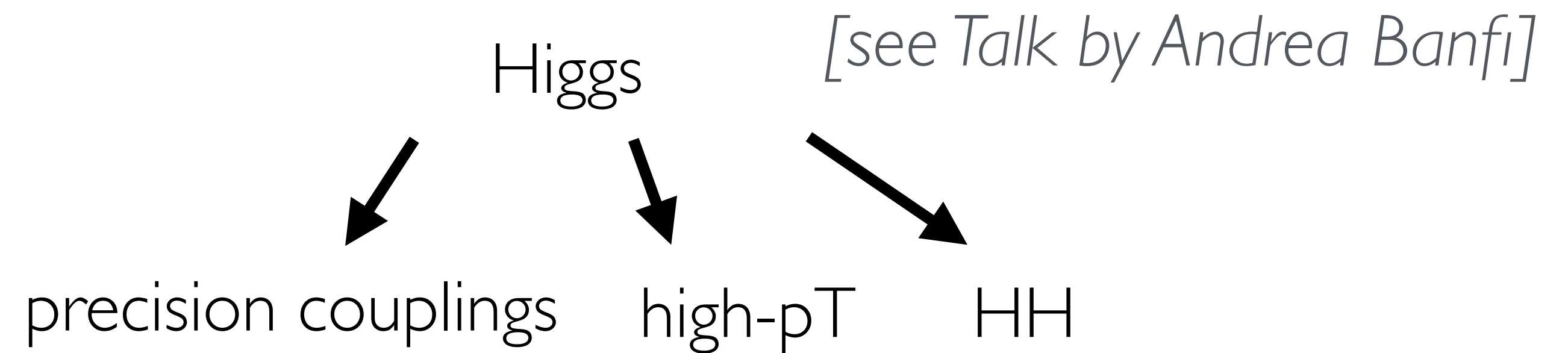
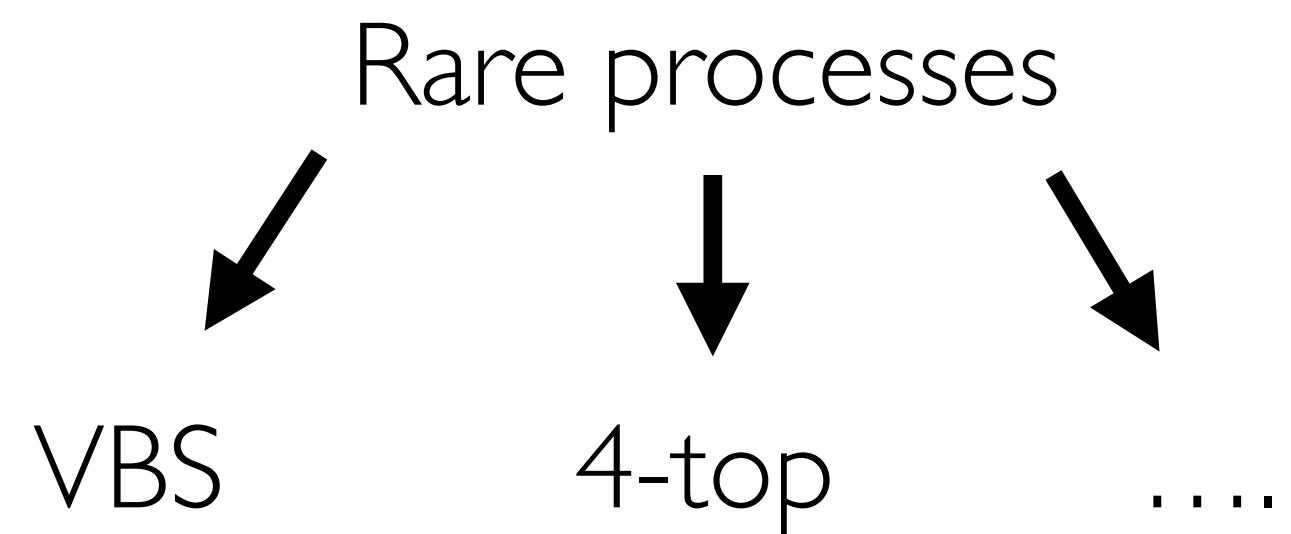
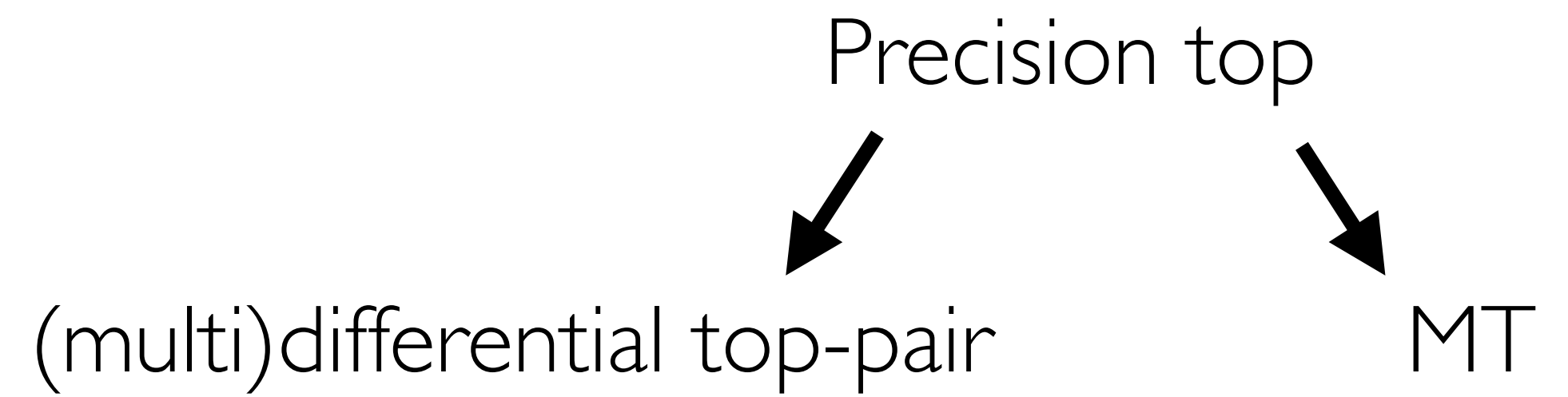
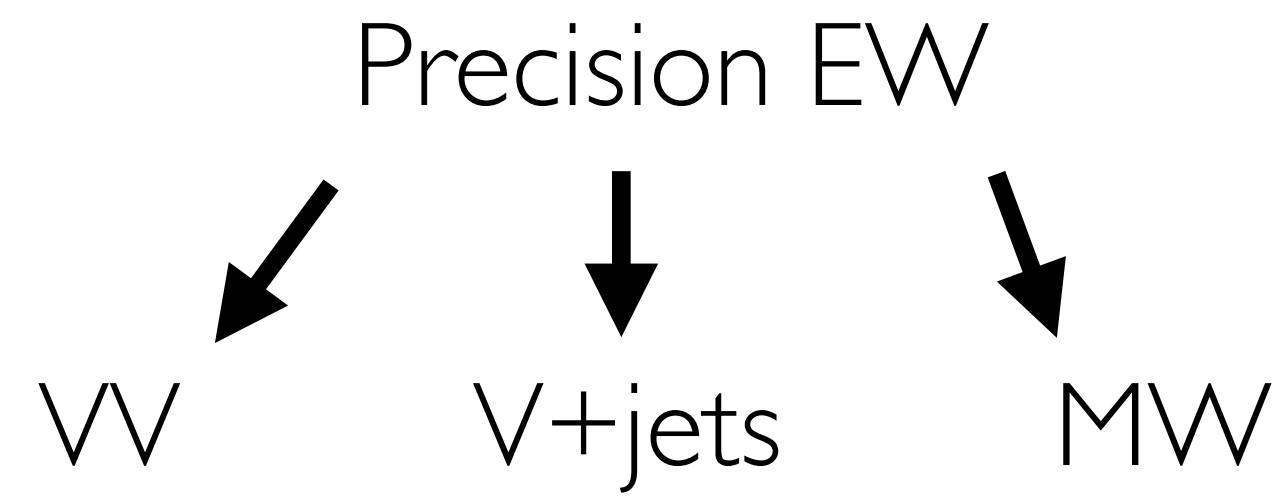


- Dark Matter particles produced at the LHC
leave the detectors unobserved:
signature missing transverse energy

- large irreducible SM backgrounds

→ good control on theory necessary!

SM physics at Run-III/HL/HE-LHC



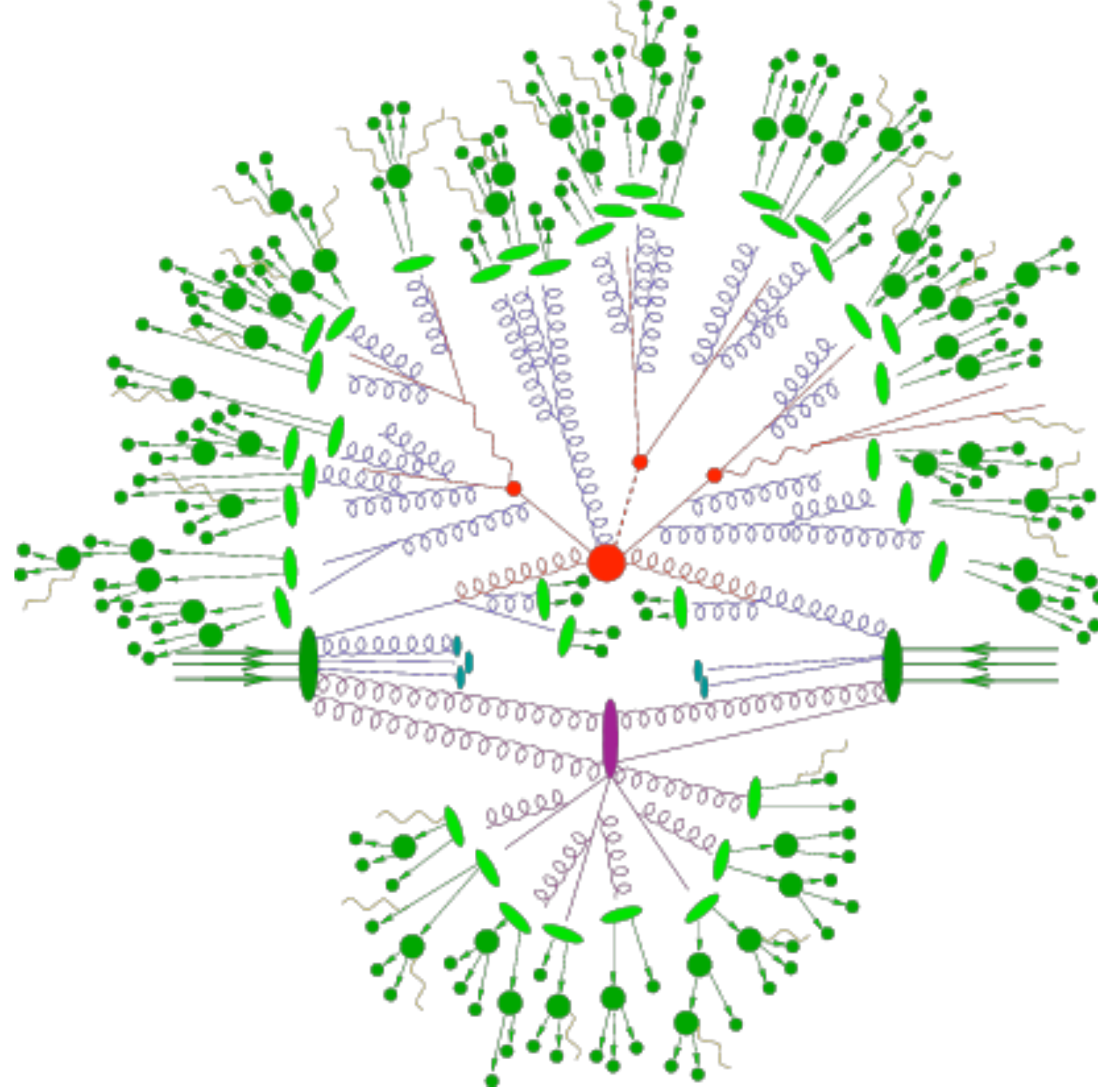
Precision at the LHC

$$\begin{aligned}
\mathcal{L}_{SM} = & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
& M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - igc_w (\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
& W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)) - \\
& ig s_w (\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - \\
& W_\nu^- \partial_\nu W_\mu^+)) - \frac{1}{2}g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - \\
& Z_\mu^0 Z_\mu^0 W_\nu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w (A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\
& W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-) - \frac{1}{2}\partial_\mu H \partial_\mu H - 2M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \\
& \beta_h \left(\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right) + \frac{2M^4}{g^4} \alpha_h - \\
& g\alpha_h M (H^3 + H\phi^0 \phi^0 + 2H\phi^+ \phi^-) - \\
& \frac{1}{8}g^2 \alpha_h (H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2) - \\
& gM W_\mu^+ W_\mu^- H - \frac{1}{2}g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \\
& \frac{1}{2}ig (W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)) + \\
& \frac{1}{2}g (W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) + W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)) + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) + \\
& M (\frac{1}{c_w} Z_\mu^0 \partial_\mu \phi^0 + W_\mu^+ \partial_\mu \phi^- + W_\mu^- \partial_\mu \phi^+) - ig \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + ig s_w M A_\mu (W_\mu^+ \phi^- - \\
& W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \\
& \frac{1}{4}g^2 W_\mu^+ W_\mu^- (H^2 + (\phi^0)^2 + 2\phi^+ \phi^-) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 (H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-) - \\
& \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
& W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
& g^2 s_w^2 A_\mu A_\mu \phi^+ \phi^- + \frac{1}{2}ig_s \lambda_{ij}^a (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda (\gamma \partial + m_\nu^\lambda) \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + \\
& m_u^\lambda) u_j^\lambda - \bar{d}_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + ig s_w A_\mu (-\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda) + \\
& \frac{ig}{4c_w} Z_\mu^0 \{(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - 1 - \gamma^5) d_j^\lambda) + \\
& (\bar{u}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 + \gamma^5) u_j^\lambda)\} + \frac{ig}{2\sqrt{2}} W_\mu^+ ((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}_{\lambda\kappa} e^\kappa) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)) + \\
& \frac{ig}{2\sqrt{2}} W_\mu^- ((\bar{e}^\kappa U^{lep\dagger}_{\kappa\lambda} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\kappa\lambda}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)) + \\
& \frac{ig}{2M\sqrt{2}} \phi^+ (-m_e^\kappa (\bar{\nu}^\lambda U^{lep}_{\lambda\kappa} (1 - \gamma^5) e^\kappa) + m_\nu^\lambda (\bar{\nu}^\lambda U^{lep}_{\lambda\kappa} (1 + \gamma^5) e^\kappa) + \\
& \frac{ig}{2M\sqrt{2}} \phi^- (m_e^\lambda (\bar{e}^\lambda U^{lep\dagger}_{\lambda\kappa} (1 + \gamma^5) \nu^\kappa) - m_\nu^\kappa (\bar{e}^\lambda U^{lep\dagger}_{\lambda\kappa} (1 - \gamma^5) \nu^\kappa) - \frac{g}{2} \frac{m_\nu^\lambda}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\
& \frac{g}{2} \frac{m_\kappa^\lambda}{M} H (\bar{e}^\lambda e^\lambda) + \frac{ig}{2} \frac{m_\kappa^\lambda}{M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{ig}{2} \frac{m_\kappa^\lambda}{M} \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \bar{\nu}_\kappa - \\
& \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \bar{\nu}_\kappa + \frac{ig}{2M\sqrt{2}} \phi^+ (-m_d^\kappa (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa) + \\
& \frac{ig}{2M\sqrt{2}} \phi^- (m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) - \frac{g}{2} \frac{m_\lambda^\lambda}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \\
& \frac{g}{2} \frac{m_\lambda^\lambda}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_\lambda^\lambda}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig}{2} \frac{m_\lambda^\lambda}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c + \\
& \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + igc_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \\
& \partial_\mu \bar{X}^+ X^0) + ig s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ \bar{Y}) + igc_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \\
& \partial_\mu \bar{X}^0 X^+) + ig s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + igc_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \\
& \partial_\mu \bar{X}^- X^+) + ig s_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \\
& \partial_\mu \bar{X}^- X^-) - \frac{1}{2}gM (\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w^2} \bar{X}^0 X^0 H) + \frac{1-2c_w^2}{2c_w} igM (\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-) + \\
& \frac{1}{2c_w} igM (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + igM s_w (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + \\
& \frac{1}{2}igM (\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0) .
\end{aligned}$$

$$\hookrightarrow |\mathcal{M}|^2 \hookrightarrow \sigma$$

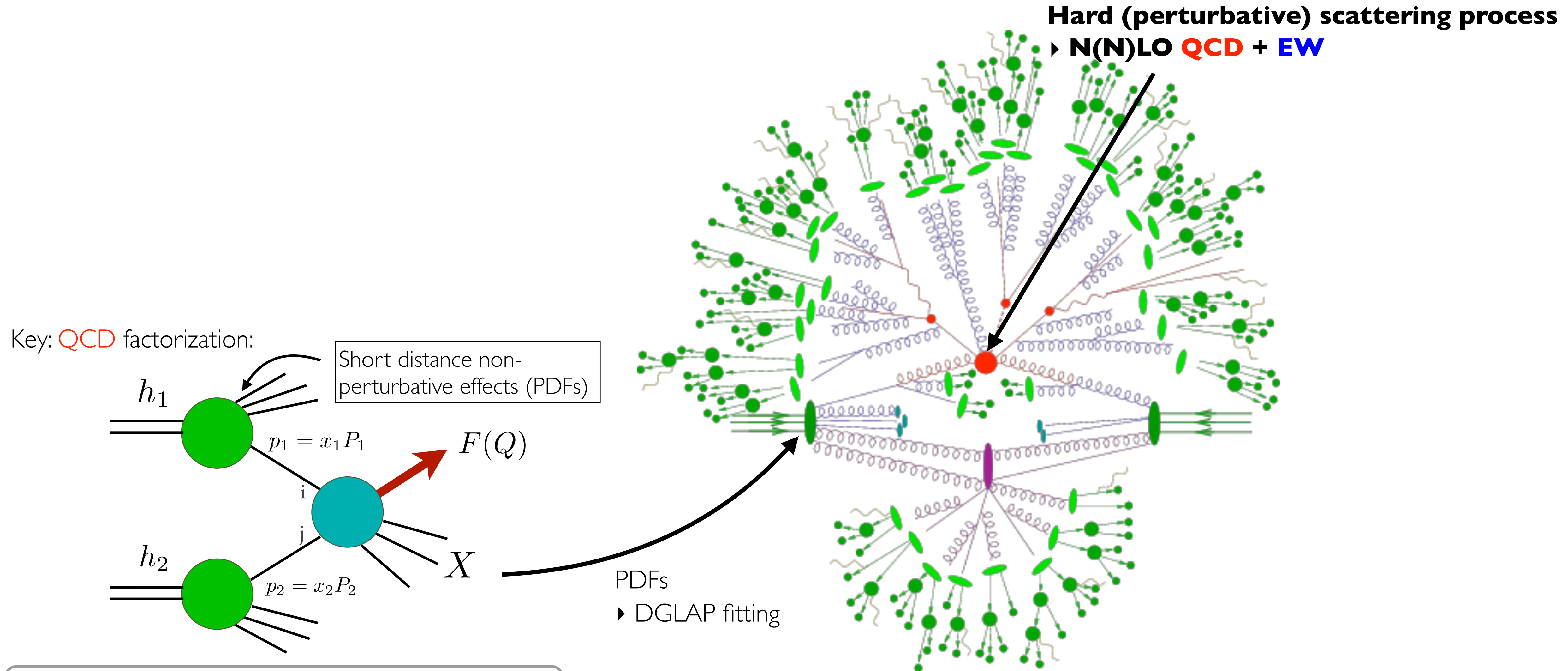
Precision at the LHC

$$\begin{aligned}
 \mathcal{L}_{SM} = & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - igc_w (\partial_\nu Z_\mu^0 (W_\mu^+ W_\mu^- - \\
 & W_\mu^+ W_\mu^-) - Z_\mu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+)) - \\
 & ig s_w (\partial_\nu A_\mu (W_\mu^+ W_\mu^- - W_\mu^- W_\mu^+) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\mu^+ \partial_\nu W_\mu^- - \\
 & W_\mu^- \partial_\nu W_\mu^+)) - \frac{1}{2}g^2 W_\mu^+ W_\mu^- W_\mu^+ W_\mu^- + \frac{1}{2}g^2 W_\mu^+ W_\mu^- W_\mu^+ W_\mu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\mu^0 W_\mu^- - \\
 & Z_\mu^0 Z_\mu^0 W_\mu^+ W_\mu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\mu W_\mu^- - A_\mu A_\mu W_\mu^+ W_\mu^-) + g^2 s_w c_w (A_\mu Z_\mu^0 (W_\mu^+ W_\mu^- - \\
 & W_\mu^- W_\mu^+) - 2A_\mu Z_\mu^0 W_\mu^+ W_\mu^-) - \frac{1}{2}\partial_\mu H \partial_\mu H - 2M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \\
 & \beta_h \left(\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right) + \frac{2M^4}{g^4} \alpha_h - \\
 & \frac{g\alpha_h M}{\frac{1}{8}g^2 \alpha_h} (H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2) - \\
 & g M W_\mu^+ W_\mu^- H - \frac{1}{2}g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \\
 & \frac{1}{2}ig (W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)) + \\
 & \frac{1}{2}g (W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) + W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)) + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) + \\
 & M (\frac{1}{c_w} Z_\mu^0 \partial_\mu \phi^0 + W_\mu^+ \partial_\mu \phi^- + W_\mu^- \partial_\mu \phi^+) - ig \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + ig s_w M A_\mu (W_\mu^+ \phi^- - \\
 & W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \\
 & \frac{1}{4}g^2 W_\mu^+ W_\mu^- (H^2 + (\phi^0)^2 + 2\phi^+ \phi^-) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 (H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-) - \\
 & \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & g^2 s_w^2 A_\mu A_\mu \phi^+ \phi^- + \frac{1}{2}ig_s \lambda_{ij}^a (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda (\gamma \partial + m_\nu^\lambda) \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + \\
 & m_u^\lambda) u_j^\lambda - \bar{d}_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + ig s_w A_\mu (-\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda) + \\
 & \frac{ig}{4c_w} Z_\mu^0 \{ (\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - 1 - \gamma^5) d_j^\lambda) + \\
 & (\bar{u}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 + \gamma^5) u_j^\lambda) \} + \frac{ig}{2\sqrt{2}} W_\mu^+ ((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}_{\lambda\kappa} e^\kappa) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)) + \\
 & \frac{ig}{2\sqrt{2}} W_\mu^- ((\bar{e}^\kappa U^{lep\dagger}_{\kappa\lambda} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\kappa\lambda}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)) + \\
 & \frac{ig}{2M\sqrt{2}} \phi^+ (-m_e^\kappa (\bar{\nu}^\lambda U^{lep}_{\lambda\kappa} (1 - \gamma^5) e^\kappa) + m_\nu^\lambda (\bar{\nu}^\lambda U^{lep}_{\lambda\kappa} (1 + \gamma^5) e^\kappa) + \\
 & \frac{ig}{2M\sqrt{2}} \phi^- (m_e^\lambda (\bar{e}^\lambda U^{lep\dagger}_{\lambda\kappa} (1 + \gamma^5) \nu^\kappa) - m_\nu^\kappa (\bar{e}^\lambda U^{lep\dagger}_{\lambda\kappa} (1 - \gamma^5) \nu^\kappa) - \frac{g}{2} \frac{m_\lambda^\lambda}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\
 & \frac{g}{2} \frac{m_\lambda^\lambda}{M} H (\bar{e}^\lambda e^\lambda) + \frac{ig}{2} \frac{m_\lambda^\lambda}{M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{ig}{2} \frac{m_\lambda^\lambda}{M} \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \bar{\nu}_\kappa - \\
 & \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \bar{\nu}_\kappa + \frac{ig}{2M\sqrt{2}} \phi^+ (-m_d^\kappa (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa) + \\
 & \frac{ig}{2M\sqrt{2}} \phi^- (m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) - \frac{g}{2} \frac{m_\lambda^\lambda}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \\
 & \frac{g}{2} \frac{m_\lambda^\lambda}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_\lambda^\lambda}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig}{2} \frac{m_\lambda^\lambda}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c + \\
 & \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + igc_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \\
 & \partial_\mu \bar{X}^+ X^0) + ig s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ \bar{Y}) + igc_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \\
 & \partial_\mu \bar{X}^0 X^+) + ig s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + igc_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \\
 & \partial_\mu \bar{X}^- X^+) + ig s_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \\
 & \partial_\mu \bar{X}^- X^-) - \frac{1}{2}gM (\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w^2} \bar{X}^0 X^0 H) + \frac{1-2c_w^2}{2c_w} igM (\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-) + \\
 & \frac{1}{2c_w} igM (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + igM s_w (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + \\
 & \frac{1}{2}igM (\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0) .
 \end{aligned}$$



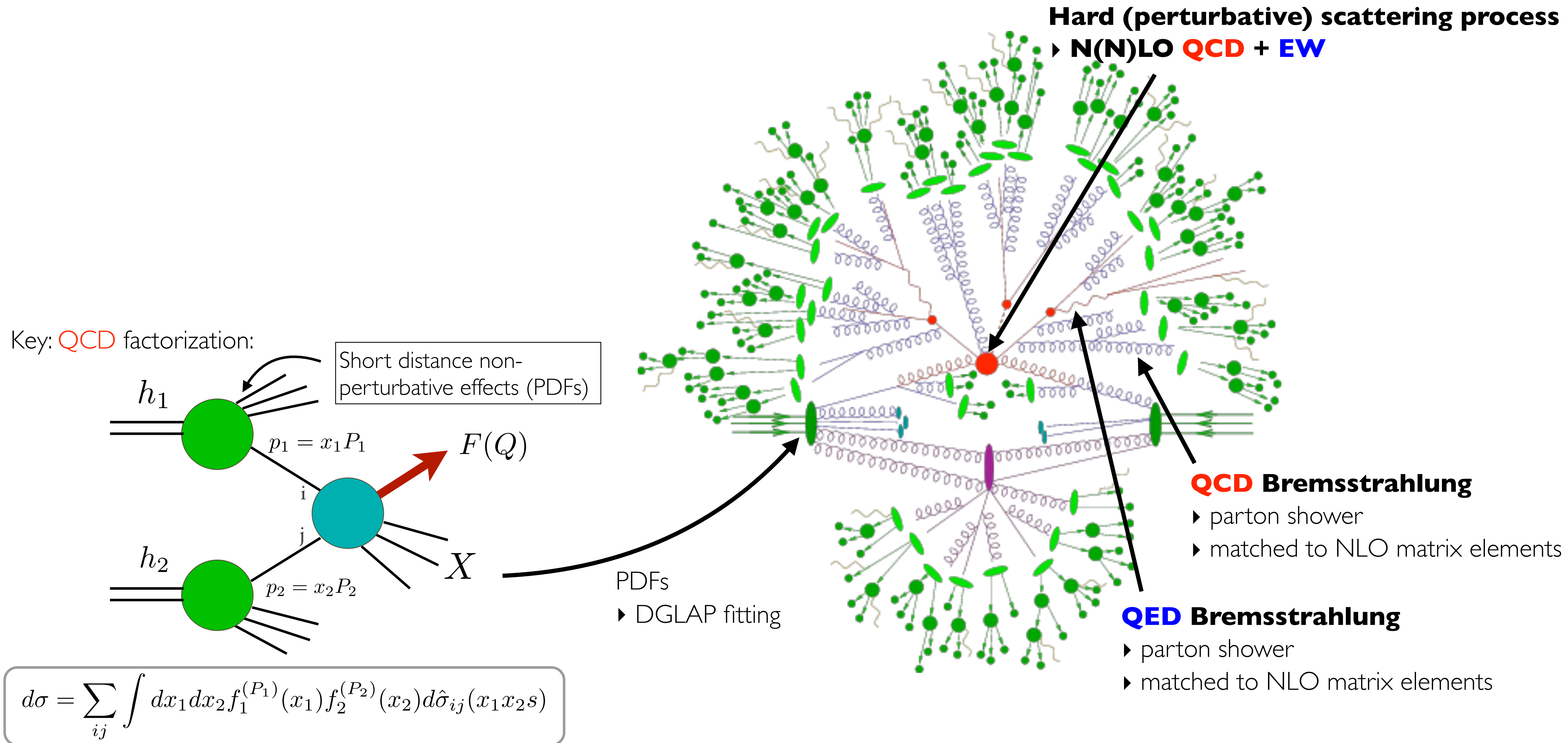
$$\hookrightarrow |\mathcal{M}|^2 \hookrightarrow \sigma$$

Precision at the LHC

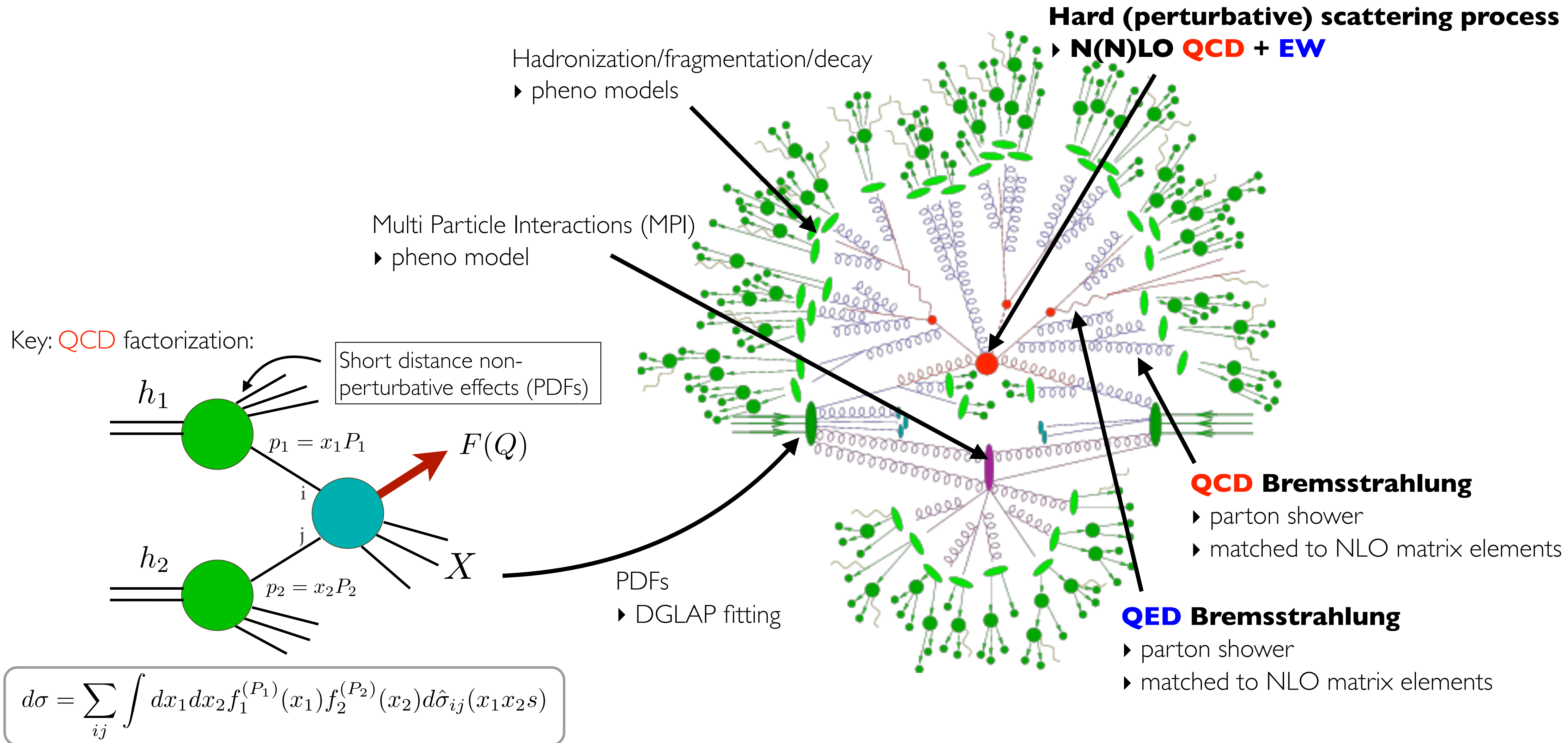


$$d\sigma = \sum_{ij} \int dx_1 dx_2 f_1^{(P_1)}(x_1) f_2^{(P_2)}(x_2) d\hat{\sigma}_{ij}(x_1 x_2 s)$$

Precision at the LHC



Precision at the LHC



Theoretical Predictions for the LHC

Hard (perturbative) scattering process:

$$d\sigma = d\sigma_{\text{LO}} + \alpha_S d\sigma_{\text{NLO}} + \alpha_{\text{EW}} d\sigma_{\text{NLO EW}}$$

$$+ \alpha_S^2 d\sigma_{\text{NNLO}} + \alpha_{\text{EW}}^2 d\sigma_{\text{NNLO EW}} + \alpha_S \alpha_{\text{EW}} d\sigma_{\text{NNLO QCDxEW}}$$

$$\begin{aligned} \mathcal{L}_{SM} = & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4} g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\ & M^2 W_\mu^+ W_\mu^- - \frac{1}{2} \partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2\alpha^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2} \partial_\mu A_\nu \partial_\mu A_\nu - i g c_w (\partial_\nu W_\mu^+ (W_\mu^- W_\nu^- - \\ & W_\nu^+ W_\mu^-) - Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\nu^- \partial_\mu W_\mu^+) + Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\nu^- \partial_\mu W_\mu^+)) - \\ & i g s_w (\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\mu W_\mu^+) + A_\nu (W_\mu^+ \partial_\nu W_\mu^- - \\ & W_\nu^- \partial_\mu W_\mu^+)) - \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\nu^+ W_\mu^- + \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - \\ & Z_\mu^0 Z_\nu^0 W_\mu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 s_w c_w (A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\ & W_\nu^+ W_\mu^-) - 2 A_\mu Z_\mu^0 W_\nu^+ W_\nu^-) - \frac{1}{2} \partial_\mu H \partial_\mu H - 2 M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2} \partial_\mu \phi^0 \partial_\mu \phi^0 - \\ & \beta_h \left(\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2} (H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right) + \frac{2M^4}{g^2} \alpha_h - \\ & \frac{g \alpha_h M}{\frac{1}{8} g^2 \alpha_h (H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2) -} \\ & g M W_\mu^+ W_\mu^- H - \frac{1}{2} g \frac{M}{c_w} Z_\mu^0 Z_\mu^0 H - \\ & \frac{1}{2} i g (W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)) + \\ & \frac{1}{2} g (W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) + W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)) + \frac{1}{2} g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) + \\ & M (\frac{1}{c_w} Z_\mu^0 \partial_\mu \phi^0 + W_\mu^+ \partial_\mu \phi^- + W_\mu^- \partial_\mu \phi^+) - i g \frac{2M}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + i g s_w M A_\mu (W_\mu^+ \phi^- - \\ & W_\mu^- \phi^+) - i g \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + i g s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \\ & \frac{1}{4} g^2 W_\mu^+ W_\mu^- (H^2 + (\phi^0)^2 + 2\phi^+ \phi^-) - \frac{1}{2} g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 (H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-) - \\ & \frac{1}{2} g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2} i g^2 \frac{s_w^2}{c_w} H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2} g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\ & W_\mu^- \phi^+) + \frac{1}{2} i g^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 2c_w^2 (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\ & g^2 s_w^2 A_\mu A_\mu \phi^+ \phi^- + \frac{1}{2} i g_s \lambda_{ij}^a (\bar{q}_i^c \gamma^\mu q_j^c) g_\mu^a - e^\lambda (\gamma \partial + m_\lambda^2) e^\lambda - \bar{\nu}^\lambda (\gamma \partial + m_\nu^2) \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + \\ & m_u^2) u_j^\lambda - \bar{d}_j^\lambda (\gamma \partial + m_d^2) d_j^\lambda + i g s_w A_\mu (- (e^\lambda \gamma^\mu e^\lambda) + \frac{2}{3} (\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3} (\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)) + \\ & \frac{i g}{4 c_w} Z_\mu^0 ((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (e^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (\frac{2}{3} s_w^2 - 1 - \gamma^5) d_j^\lambda) + \\ & (\bar{u}_j^\lambda \gamma^\mu (1 - \frac{2}{3} s_w^2 + \gamma^5) u_j^\lambda)) + \frac{i g}{2 \sqrt{2}} W_\mu^+ ((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}{}_{\lambda e} e^\kappa) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda e} d_j^\kappa)) + \\ & \frac{i g}{2 \sqrt{2}} W_\mu^- ((e^\kappa U^{lep}{}_{\kappa \lambda} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\kappa \lambda}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)) + \\ & \frac{i g}{2 M \sqrt{2}} \phi^+ (-m_\nu^2 (\bar{\nu}^\lambda U^{lep}{}_{\lambda e} (1 - \gamma^5) e^\kappa) + m_\nu^2 (\bar{\nu}^\lambda U^{lep}{}_{\lambda e} (1 - \gamma^5) \nu^\kappa) - \frac{g}{2} \frac{m_\nu^2}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\ & \frac{i g}{2 M \sqrt{2}} \phi^- (m_\nu^2 (e^\lambda U^{lep}{}_{\lambda e}^\dagger (1 + \gamma^5) \nu^\kappa) - m_\nu^2 (e^\lambda U^{lep}{}_{\lambda e}^\dagger (1 - \gamma^5) \nu^\kappa) - \frac{g}{2} \frac{m_\nu^2}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\ & \frac{g}{2} \frac{m_\nu^2}{M} H (e^\lambda e^\lambda) + \frac{i g}{2} \frac{m_\nu^2}{M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{i g}{2} \frac{m_\nu^2}{M} \phi^0 (e^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda e}^R (1 - \gamma_5) \hat{\nu}_\kappa - \\ & \frac{1}{4} \bar{\nu}_\lambda M_{\lambda e}^L (1 - \gamma_5) \hat{\nu}_\kappa + \frac{i g}{2 M \sqrt{2}} \phi^+ (-m_\nu^2 (\bar{u}_j^\lambda C_{\lambda e} (1 - \gamma^5) d_j^\kappa) + m_\nu^2 (\bar{u}_j^\lambda C_{\lambda e} (1 + \gamma^5) d_j^\kappa) + \\ & \frac{i g}{2 M \sqrt{2}} \phi^- (m_\nu^2 (\bar{d}_j^\lambda C_{\lambda e}^\dagger (1 + \gamma^5) u_j^\kappa) - m_\nu^2 (\bar{d}_j^\lambda C_{\lambda e}^\dagger (1 - \gamma^5) u_j^\kappa) - \frac{g}{2} \frac{m_\nu^2}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \\ & \frac{g}{2} \frac{m_\nu^2}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{i g}{2} \frac{m_\nu^2}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{i g}{2} \frac{m_\nu^2}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c + \\ & \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + i g c_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \\ & \partial_\mu \bar{X}^+ X^0) + i g s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ Y) + i g c_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \\ & \partial_\mu \bar{X}^0 X^+) + i g s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + i g c_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \\ & \partial_\mu \bar{X}^- X^+) + i g s_w A_\mu (\partial_\mu \bar{X}^+ X^- - \\ & \partial_\mu \bar{X}^- X^+) - \frac{1}{2} g M (\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w} \bar{X}^0 X^0 H) + \frac{1-2c_w^2}{c_w} i g M (\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-) + \\ & \frac{1}{2 c_w} i g M (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + i g M s_w (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + \\ & \frac{1}{2} i g M (\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0) . \end{aligned}$$

$$\hookrightarrow |\mathcal{M}|^2 \hookrightarrow \sigma$$

Theoretical Predictions for the LHC

Hard (perturbative) scattering process:

$$d\sigma = d\sigma_{\text{LO}} + \alpha_S d\sigma_{\text{NLO}} + \alpha_{\text{EW}} d\sigma_{\text{NLO EW}}$$

$$+ \alpha_S^2 d\sigma_{\text{NNLO}} + \alpha_{\text{EW}}^2 d\sigma_{\text{NNLO EW}} + \alpha_S \alpha_{\text{EW}} d\sigma_{\text{NNLO QCDxEW}}$$

$$\begin{aligned} \mathcal{L}_{SM} = & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- \\ & - M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2\alpha^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - ig c_w (\partial_\nu W_\mu^+ (W_\mu^- W_\nu^- \\ & - W_\nu^+ W_\mu^-) - Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\nu^- \partial_\mu W_\mu^+) + Z_\mu^0 (W_\mu^- \partial_\nu W_\nu^+ - W_\nu^+ \partial_\mu W_\mu^-)) \\ & - ig s_w (\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\mu W_\mu^+) + A_\nu (W_\mu^- \partial_\nu W_\mu^+ \\ & - W_\nu^+ \partial_\mu W_\mu^-)) - \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\nu^+ W_\mu^- + \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- \\ & - Z_\nu^0 Z_\mu^0 W_\mu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\nu A_\mu W_\mu^+ W_\nu^-) + g^2 s_w c_w (A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- \\ & - W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-) - \frac{1}{2}\partial_\mu H \partial_\mu H - 2M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \\ & \beta_h \left(\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right) + \frac{2M^4}{g^2} \alpha_h - \\ & \frac{1}{8}g^2 \alpha_h (H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2) - \\ & g M W_\mu^+ W_\mu^- H - \frac{1}{2}g \frac{M}{c_w} Z_\mu^0 Z_\mu^0 H - \\ & \frac{1}{2}ig (W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)) + \\ & \frac{1}{2}g (W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) + W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)) + \frac{1}{2}g \frac{M}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) + \\ & M (\frac{1}{c_w} Z_\mu^0 \partial_\mu \phi^0 + W_\mu^+ \partial_\mu \phi^- + W_\mu^- \partial_\mu \phi^+) - ig \frac{2M}{c_w} Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + ig s_w M A_\mu (W_\mu^+ \phi^- - \\ & W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \\ & \frac{1}{4}g^2 W_\mu^+ W_\mu^- (H^2 + (\phi^0)^2 + 2\phi^+ \phi^-) - \frac{1}{2}g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 (H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-) - \\ & \frac{1}{2}g^2 \frac{2s_w^2}{c_w^2} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{2s_w^2}{c_w^2} H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\ & W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{2M}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\ & g^2 s_w^2 A_\mu A_\mu \phi^+ \phi^- + \frac{1}{2}ig_s \lambda_{ij}^a (\bar{q}_i^c \gamma^\mu q_j^c) g_\mu^a - e^\lambda (\gamma^\partial + m_\lambda^2) e^\lambda - \bar{\nu}^\lambda (\gamma^\partial + m_\lambda^2) \nu^\lambda - \bar{u}_j^\lambda (\gamma^\partial + \\ & m_u^2) u_j^\lambda - \bar{d}_j^\lambda (\gamma^\partial + m_d^2) d_j^\lambda + ig s_w A_\mu (-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)) + \\ & \frac{ig}{4c_w} Z_\mu^0 \bar{l} (\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (\frac{2}{3}s_w^2 - 1 - \gamma^5) d_j^\lambda) + \\ & (\bar{u}_j^\lambda \gamma^\mu (1 - \frac{2}{3}s_w^2 + \gamma^5) u_j^\lambda)) + \frac{ig}{2\sqrt{2}} W_\mu^+ ((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}_{\lambda e} e^\mu) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda e} d_j^\mu)) + \\ & \frac{ig}{2\sqrt{2}} W_\mu^- ((\bar{e}^\mu U^{lep}_{\kappa \lambda} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\mu C_{\kappa \lambda}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\mu)) + \\ & \frac{ig}{2M\sqrt{2}} \phi^+ (-m_\kappa^2 (\bar{\nu}^\lambda U^{lep}_{\lambda \kappa} (1 - \gamma^5) e^\kappa) + m_\lambda^2 (\bar{\nu}^\lambda U^{lep}_{\lambda \kappa} (1 + \gamma^5) e^\kappa) + \\ & \frac{ig}{2M\sqrt{2}} \phi^- (m_\lambda^2 (\bar{e}^\lambda U^{lep}_{\lambda \kappa} (1 + \gamma^5) \nu^\kappa) - m_\kappa^2 (\bar{e}^\lambda U^{lep}_{\lambda \kappa} (1 - \gamma^5) \nu^\kappa) - \frac{g}{2} \frac{m_\lambda}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\ & \frac{g}{2} \frac{m_\lambda}{M} H (\bar{e}^\lambda e^\lambda) + \frac{ig}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{ig}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda \kappa}^R (1 - \gamma_5) \bar{\nu}_\kappa - \\ & \frac{1}{4} \bar{\nu}_\lambda M_{\lambda \kappa}^R (1 - \gamma_5) \bar{\nu}_\kappa + \frac{ig}{2M\sqrt{2}} \phi^+ (-m_\lambda^2 (\bar{u}_j^\lambda C_{\lambda \kappa} (1 - \gamma^5) d_j^\kappa) + m_\kappa^2 (\bar{u}_j^\lambda C_{\lambda \kappa} (1 + \gamma^5) d_j^\kappa) + \\ & \frac{ig}{2M\sqrt{2}} \phi^- (m_\lambda^2 (\bar{d}_j^\lambda C_{\lambda \kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_\kappa^2 (\bar{d}_j^\lambda C_{\lambda \kappa}^\dagger (1 - \gamma^5) u_j^\kappa) - \frac{g}{2} \frac{m_\lambda}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \\ & \frac{g}{2} \frac{m_\lambda}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c + \\ & \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \frac{M^2}{\alpha^2}) X^0 + \bar{Y} \partial^2 Y + ig c_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \\ & \partial_\mu \bar{X}^+ X^0) + ig s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ Y) + ig c_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \\ & \partial_\mu \bar{X}^0 X^+) + ig s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + ig c_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \\ & \partial_\mu \bar{X}^- X^+) + ig s_w A_\mu (\partial_\mu \bar{X}^+ X^- - \\ & \partial_\mu \bar{X}^- X^+) - \frac{1}{2}ig M (\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{\alpha^2} \bar{X}^0 X^0 H) + \frac{1-2c_w^2}{2c_w} ig M (\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-) + \\ & \frac{1}{2c_w} ig M (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + ig M s_w (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + \\ & \frac{1}{2}ig M (\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0) . \end{aligned}$$

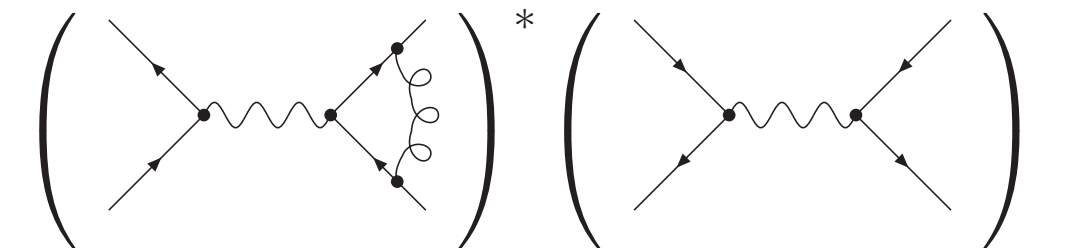
$$d\sigma_{\text{NLO}} = \frac{1}{2s} \int d\Phi_n [|\mathcal{M}_{\text{LO}}|^2 + 2\text{Re}\{\mathcal{M}_{\text{LO}} \mathcal{M}_{\text{NLO,V}}^*\}] + \frac{1}{2s} \int d\Phi_{n+1} |\mathcal{M}_{\text{NLO,R}}|^2$$

$$\text{NLO} = \text{B} + \text{V} + \text{R}$$

$\mathcal{M}_{\text{NLO,V}}$

virtual one-loop matrix element

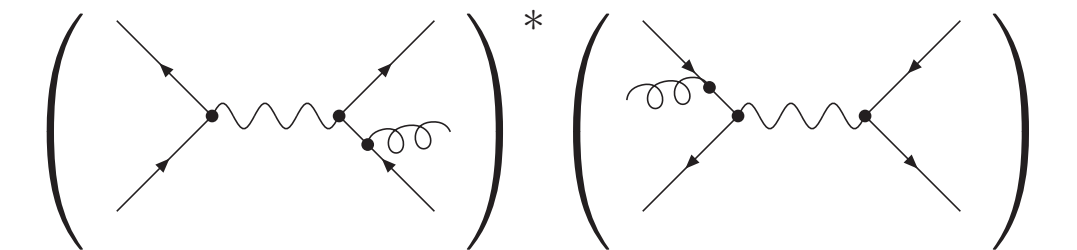
$$\text{Re}\{\mathcal{M}_{\text{LO}} \mathcal{M}_{\text{NLO,V}}^*\}$$



$\mathcal{M}_{\text{NLO,R}}$

real tree-level matrix element

$$|\mathcal{M}_{\text{NLO,R}}|^2$$



•UV renormalisation \Rightarrow reduction of μ_R dependence

•soft/collinear cancellations+PDF renormalisation \Rightarrow reduction of μ_F dependence

$$\hookrightarrow |\mathcal{M}|^2 \hookrightarrow \sigma$$

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$$d\sigma = d\sigma_{\text{LO}} + \alpha_S d\sigma_{\text{NLO}} + \alpha_{\text{EW}} d\sigma_{\text{NLO EW}}$$

$$+ \alpha_S^2 d\sigma_{\text{NNLO}} + \alpha_{\text{EW}}^2 d\sigma_{\text{NNLO EW}} + \alpha_S \alpha_{\text{EW}} d\sigma_{\text{NNLO QCDxEW}}$$

$$\begin{aligned} \mathcal{L}_{SM} = & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- \\ & - M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2\alpha^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - ig c_w (\partial_\nu W_\mu^+ (W_\mu^- W_\nu^- \\ & - W_\nu^+ W_\mu^-) - Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\nu^- \partial_\mu W_\mu^+) + Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\nu^- \partial_\mu W_\mu^+)) \\ & - ig s_w (\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\mu W_\mu^+) + A_\nu (W_\mu^+ \partial_\nu W_\mu^- \\ & - W_\nu^- \partial_\mu W_\mu^+)) - \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\nu^+ W_\mu^- + \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- \\ & - Z_\nu^0 Z_\mu^0 W_\mu^+ W_\nu^-) + g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 s_w c_w (A_\mu Z_\mu^0 (W_\mu^+ W_\nu^- \\ & - W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-) - \frac{1}{2}\partial_\mu H \partial_\mu H - 2M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \\ & \beta_h \left(\frac{2M^2}{g^2} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right) + \frac{2M^4}{g^2} \alpha_h - \\ & \frac{1}{8}g^2 \alpha_h (H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2) - \\ & g M W_\mu^+ W_\mu^- H - \frac{1}{2}g \frac{M}{c_w} Z_\mu^0 Z_\mu^0 H - \\ & \frac{1}{2}ig (W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)) + \\ & \frac{1}{2}g (W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) + W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)) + \frac{1}{2}g \frac{M}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) + \\ & M (\frac{1}{c_w} Z_\mu^0 \partial_\mu \phi^0 + W_\mu^+ \partial_\mu \phi^- + W_\mu^- \partial_\mu \phi^+) - ig \frac{2M}{c_w} Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + ig s_w M A_\mu (W_\mu^+ \phi^- \\ & - W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \\ & \frac{1}{4}g^2 W_\mu^+ W_\nu^- (H^2 + (\phi^0)^2 + 2\phi^+ \phi^-) - \frac{1}{2}g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\nu^0 (H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-) - \\ & \frac{1}{2}g^2 \frac{2s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{2s_w^2}{c_w} H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\ & W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{2s_w^2}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\ & g^2 s_w^2 A_\mu A_\nu \phi^+ \phi^- + \frac{1}{2}ig_s \lambda_{ij}^a (\bar{q}_i^c \gamma^\mu q_j^a) g_\mu^a - e^2 (\gamma^\mu + m_\nu^2) e^\lambda - \bar{\nu}^\lambda (\gamma^\mu + m_\nu^2) \nu^\lambda - \bar{u}_j^\lambda (\gamma^\mu + \\ & m_u^2) u_j^\lambda - \bar{d}_j^\lambda (\gamma^\mu + m_d^2) d_j^\lambda + ig s_w A_\mu (-e^2 \gamma^\mu e^\lambda + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)) + \\ & \frac{ig}{4c_w} Z_\mu^0 \bar{l} (\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (e^2 \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (\frac{2}{3}s_w^2 - 1 - \gamma^5) d_j^\lambda) + \\ & (\bar{u}_j^\lambda \gamma^\mu (1 - \frac{2}{3}s_w^2 + \gamma^5) u_j^\lambda)) + \frac{ig}{2\sqrt{2}} W_\mu^+ ((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}_{\lambda e} e^\mu) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda e} d_j^\mu)) + \\ & \frac{ig}{2\sqrt{2}} W_\mu^- ((e^c U^{lep}_{\lambda e} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\lambda C_{\lambda e}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda)) + \\ & \frac{ig}{2M\sqrt{2}} \phi^+ (-m_\nu^2 (\bar{\nu}^\lambda U^{lep}_{\lambda e} (1 - \gamma^5) e^\mu) + m_\nu^2 (\bar{\nu}^\lambda U^{lep}_{\lambda e} (1 + \gamma^5) e^\mu) - \frac{g}{2} \frac{m_\nu^2}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\ & \frac{ig}{2M\sqrt{2}} \phi^- (m_\nu^2 (e^\lambda U^{lep}_{\lambda e} (1 + \gamma^5) \nu^\mu) - m_\nu^2 (e^\lambda U^{lep}_{\lambda e} (1 - \gamma^5) \nu^\mu) - \frac{g}{2} \frac{m_\nu^2}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\ & \frac{g}{2} \frac{m_\nu^2}{M} H (e^\lambda e^\lambda) + \frac{ig}{2} \frac{m_\nu^2}{M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{ig}{2} \frac{m_\nu^2}{M} \phi^0 (e^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda e}^R (1 - \gamma_5) \bar{\nu}_\kappa - \\ & \frac{1}{4} \bar{\nu}_\lambda M_{\lambda e}^R (1 - \gamma_5) \bar{\nu}_\kappa + \frac{ig}{2M\sqrt{2}} \phi^+ (-m_\nu^2 (\bar{u}_j^\lambda C_{\lambda e} (1 - \gamma^5) d_j^\mu) + m_\nu^2 (\bar{u}_j^\lambda C_{\lambda e} (1 + \gamma^5) d_j^\mu) + \\ & \frac{ig}{2M\sqrt{2}} \phi^- (m_\nu^2 (\bar{d}_j^\lambda C_{\lambda e}^\dagger (1 + \gamma^5) u_j^\mu) - m_\nu^2 (\bar{d}_j^\lambda C_{\lambda e}^\dagger (1 - \gamma^5) u_j^\mu) - \frac{g}{2} \frac{m_\nu^2}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \\ & \frac{g}{2} \frac{m_\nu^2}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_\nu^2}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig}{2} \frac{m_\nu^2}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c + \\ & \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + ig c_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \\ & \partial_\mu \bar{X}^+ X^0) + ig s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ Y) + ig c_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \\ & \partial_\mu \bar{X}^0 X^+) + ig s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + ig c_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \\ & \partial_\mu \bar{X}^- X^+) + ig s_w A_\mu (\partial_\mu \bar{X}^+ X^- - \\ & \partial_\mu \bar{X}^- X^+) - \frac{1}{2}gM (\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w} \bar{X}^0 X^0 H) + \frac{1-2c_w^2}{c_w} igM (\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-) + \\ & \frac{1}{2c_w} igM (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + igM s_w (\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-) + \\ & \frac{1}{2}igM (\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0) . \end{aligned}$$

$$\begin{aligned} d\hat{\sigma}_{\text{NNLO}} = & \frac{1}{2s} \int d\Phi_n [|\mathcal{M}_{\text{LO}}|^2 + 2\text{Re}\{\mathcal{M}_{\text{LO}}\mathcal{M}_{\text{NLO},\text{V}}^*\} + 2\text{Re}\{\mathcal{M}_{\text{LO}}\mathcal{M}_{\text{NNLO},\text{V}}^*\}] \\ & + \frac{1}{2s} \int d\Phi_{n+1} [|\mathcal{M}_{\text{NLO},\text{R}}|^2 + 2\text{Re}\{\mathcal{M}_{\text{NLO},\text{R}}\mathcal{M}_{\text{NNLO},\text{RV}}^*\}] + \frac{1}{2s} \int d\Phi_{n+2} |\mathcal{M}_{\text{NNLO},\text{RR}}|^2 \end{aligned}$$

$\text{NNLO} = \text{B} + \text{V} + \text{V2} + \dots$

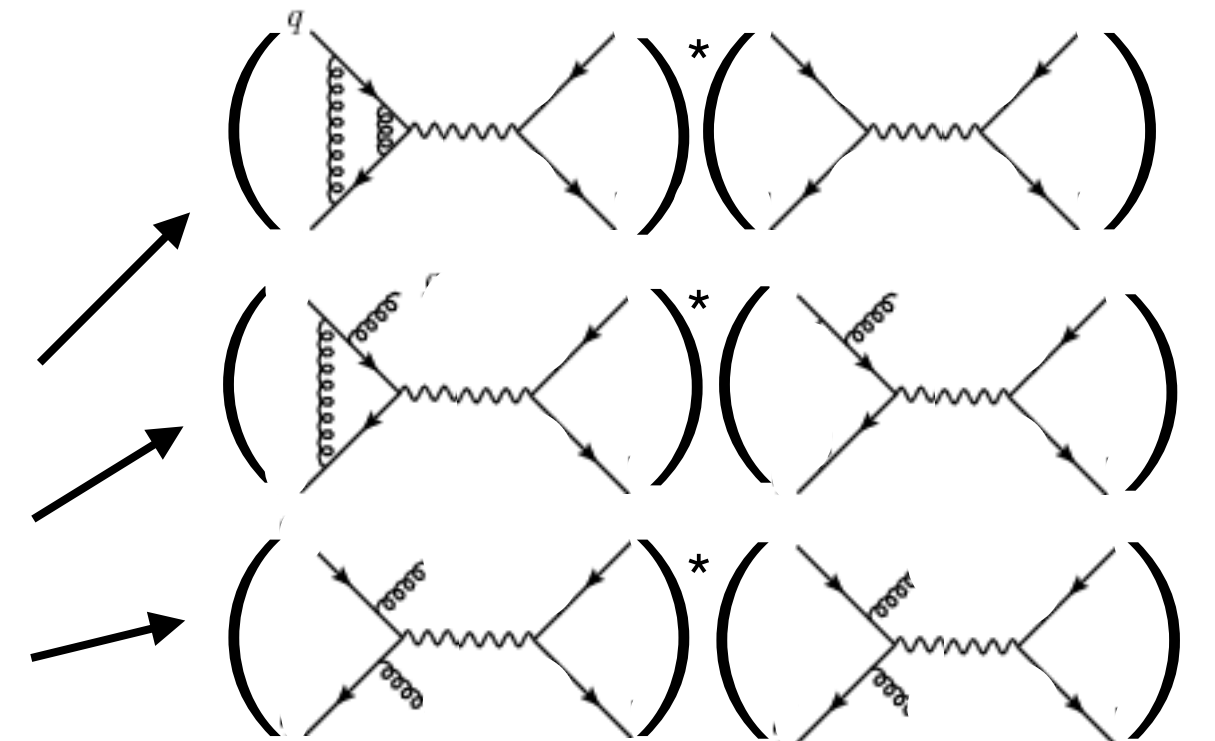
$+ \text{R} + \text{RV} + \text{RR}$

$$\hookrightarrow |\mathcal{M}|^2 \hookrightarrow \sigma$$

$$\int d\Phi_{n(+1)} \quad n, n+1, n+2 \text{ particle phase space}$$

$$\Delta_{\text{NLO}} \propto \alpha \begin{cases} \mathcal{M}_{\text{NLO},\text{V}} & \text{virtual one-loop matrix element} \\ \mathcal{M}_{\text{NLO},\text{R}} & \text{real tree-level matrix element} \end{cases}$$

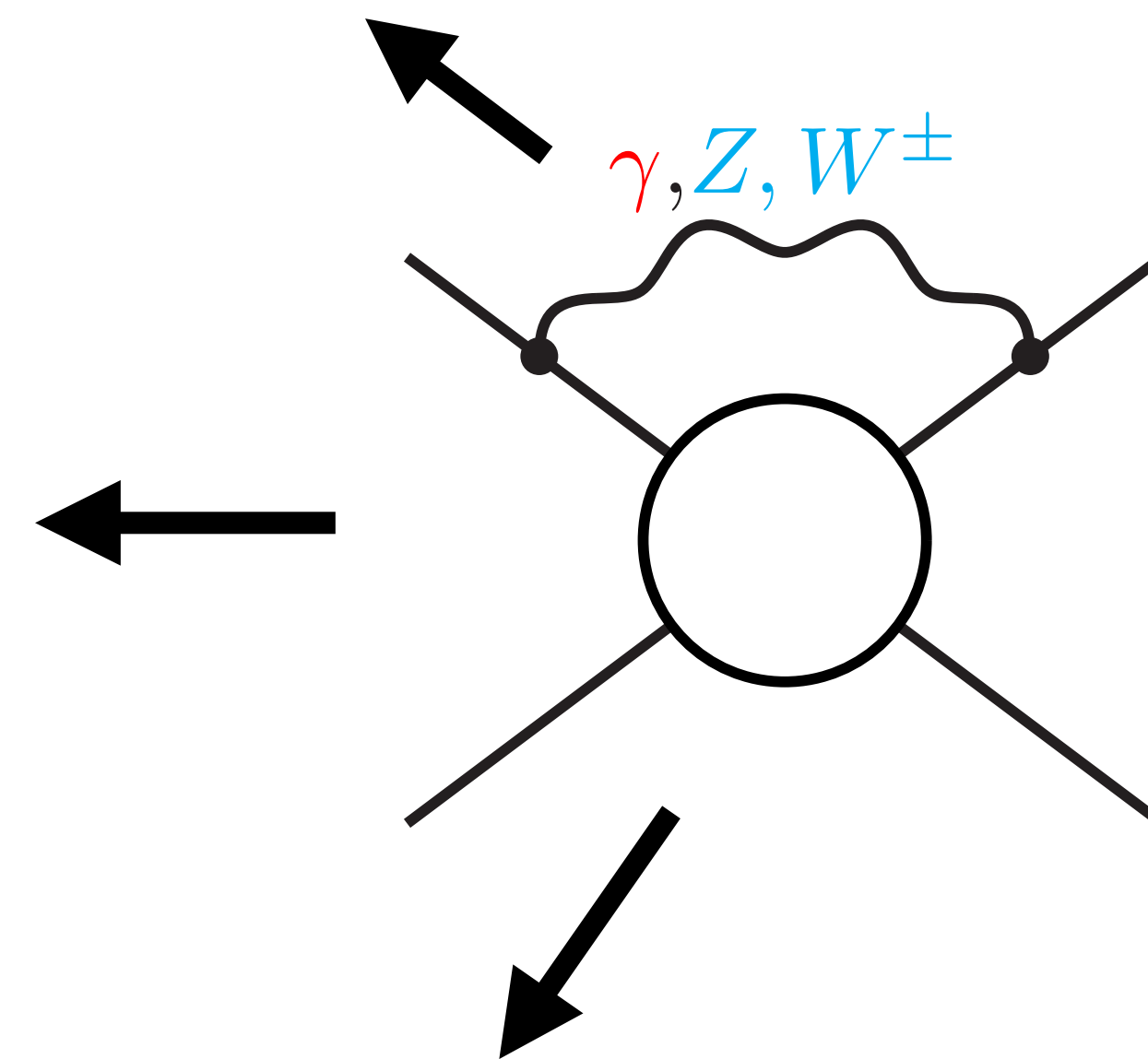
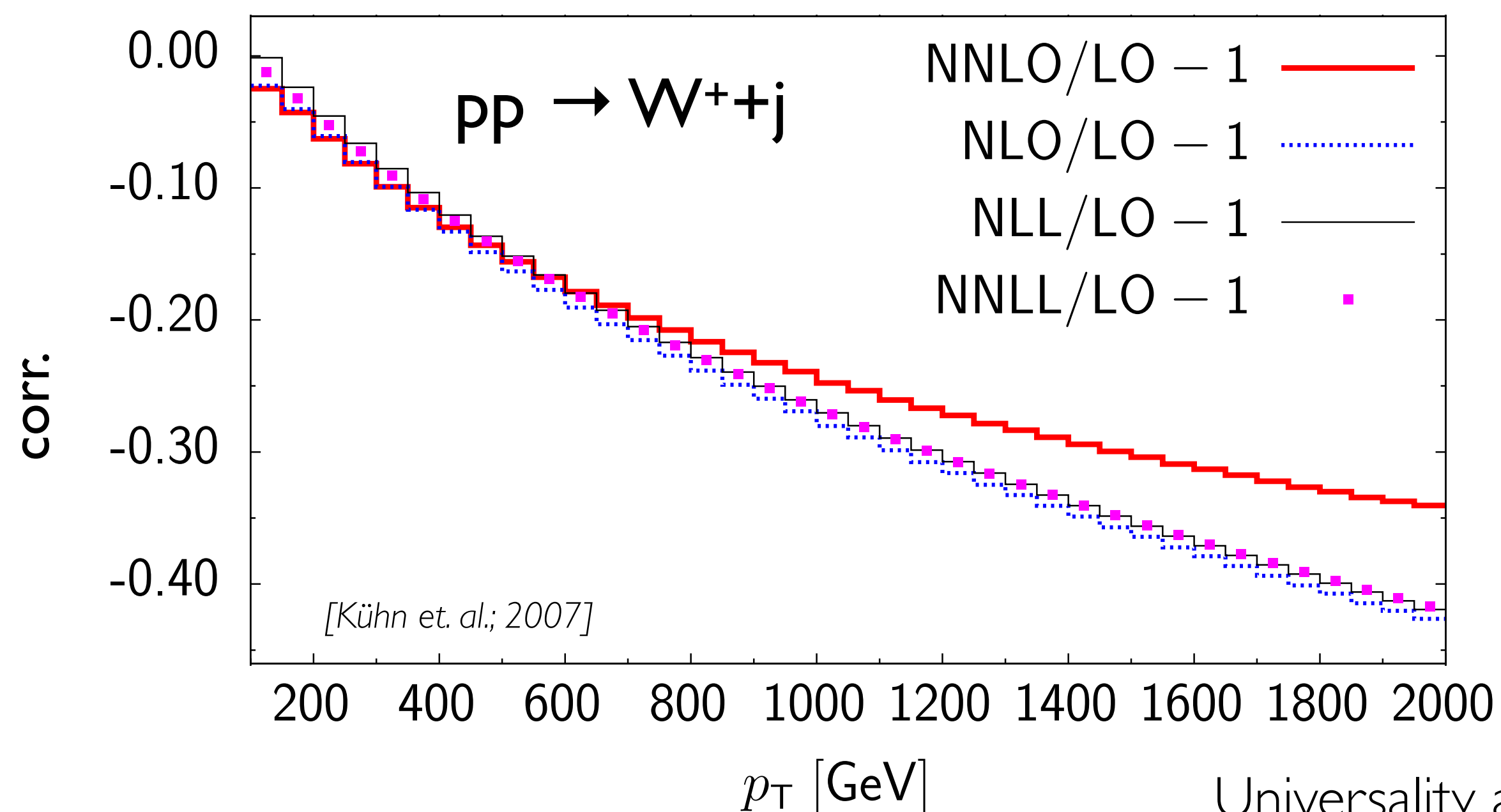
$$\Delta_{\text{NNLO}} \propto \alpha^2 \begin{cases} \mathcal{M}_{\text{NNLO},\text{V}} & \text{double-virtual two-loop matrix element} \\ \mathcal{M}_{\text{NNLO},\text{RV}} & \text{real-virtual one-loop matrix element} \\ \mathcal{M}_{\text{NNLO},\text{RR}} & \text{double-real tree-level matrix element} \end{cases}$$



Relevance of EW higher-order corrections I

Numerically $\mathcal{O}(\alpha) \sim \mathcal{O}(\alpha_s^2) \Rightarrow$ **NLO EW \sim NNLO QCD**

I. Possible large (negative) enhancement due to soft/collinear **logs** from virtual EW gauge bosons:



[Ciafaloni, Comelli, '98;
Lipatov, Fadin, Martin, Melles, '99;
Kuehen, Penin, Smirnov, '99;
Denner, Pozzorini, '00]

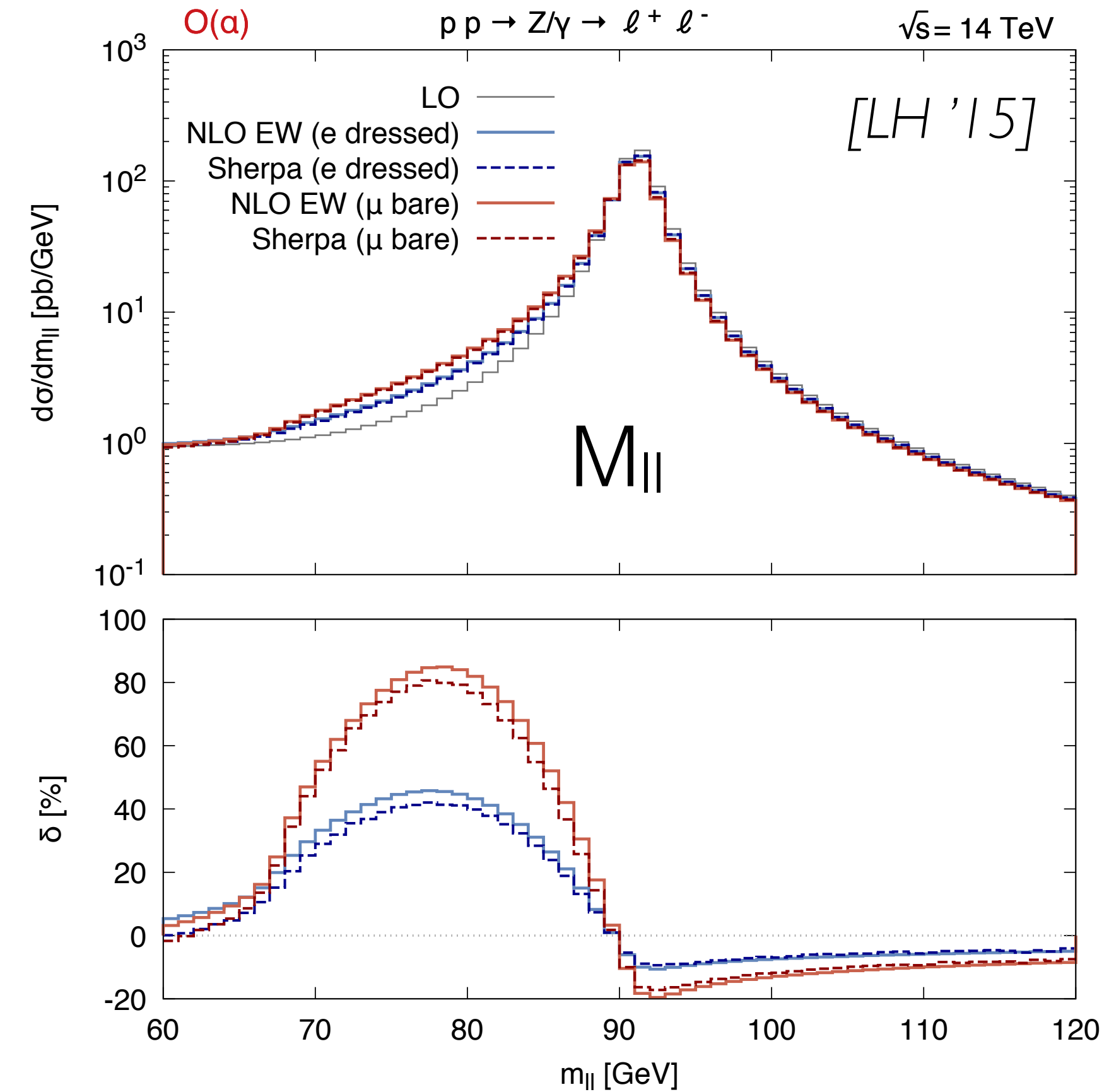
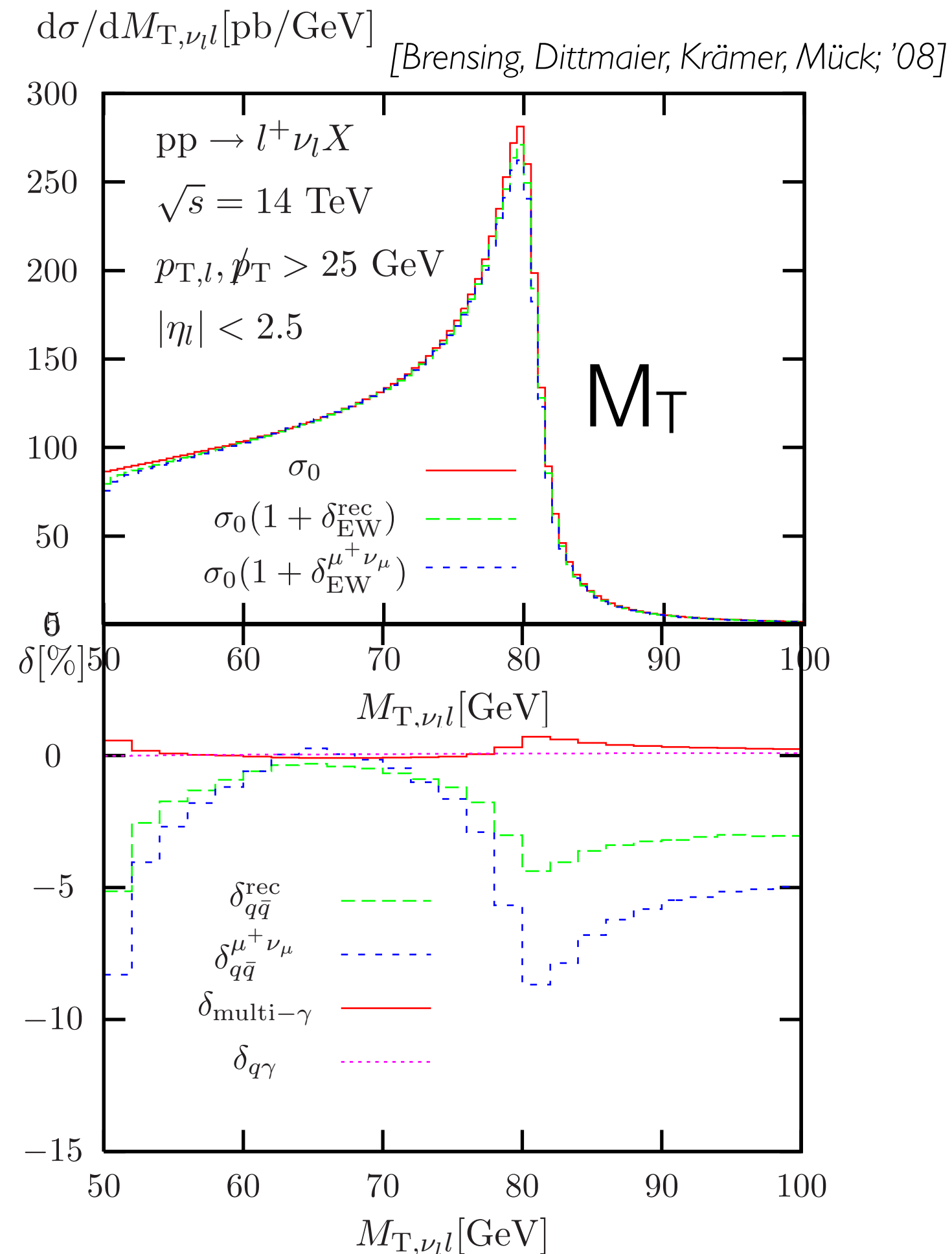
Universality and factorisation: [Denner, Pozzorini; '01]

$$\delta \mathcal{M}_{\text{LL+NLL}}^{1\text{-loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^n \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^\pm} I^a(k) I^{\bar{a}}(l) \ln^2 \frac{\hat{s}_{kl}}{M^2} + \gamma^{\text{ew}}(k) \ln \frac{\hat{s}}{M^2} \right\} \mathcal{M}_0$$

→ overall large effect in the tails of distributions: $p_T, m_{\text{inv}}, H_T, \dots$ (relevant for BSM searches!)

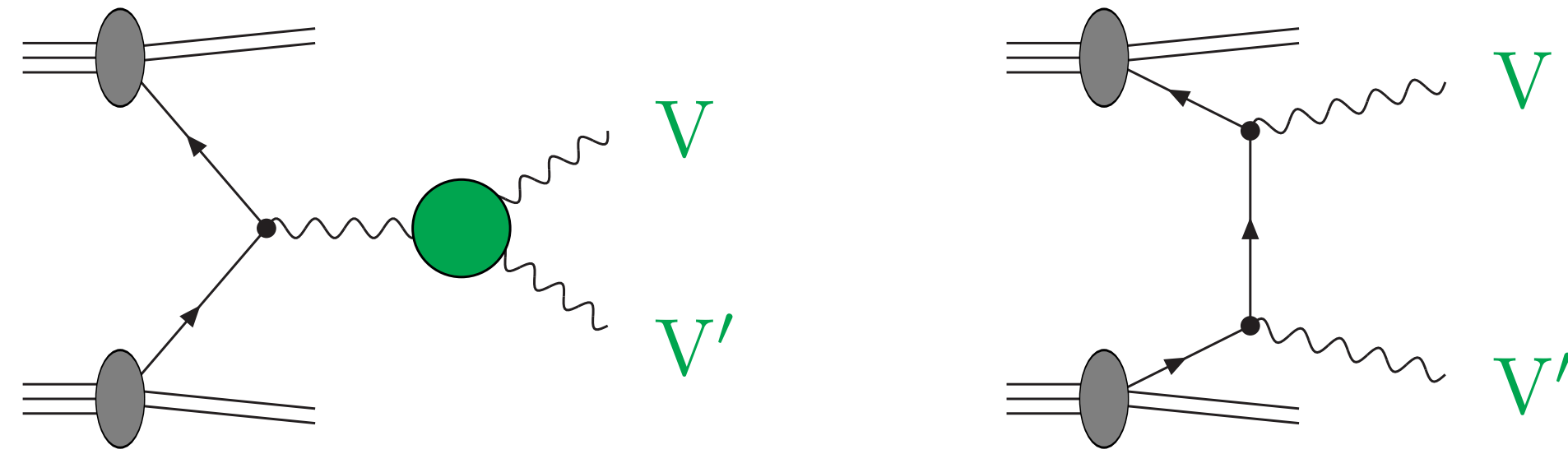
Relevance of EW higher-order corrections II

- Possible large enhancement due to soft/collinear **logs** from photon radiation $\sim \alpha \log \left(\frac{m_f^2}{Q^2} \right)$ in sufficiently exclusive observables.

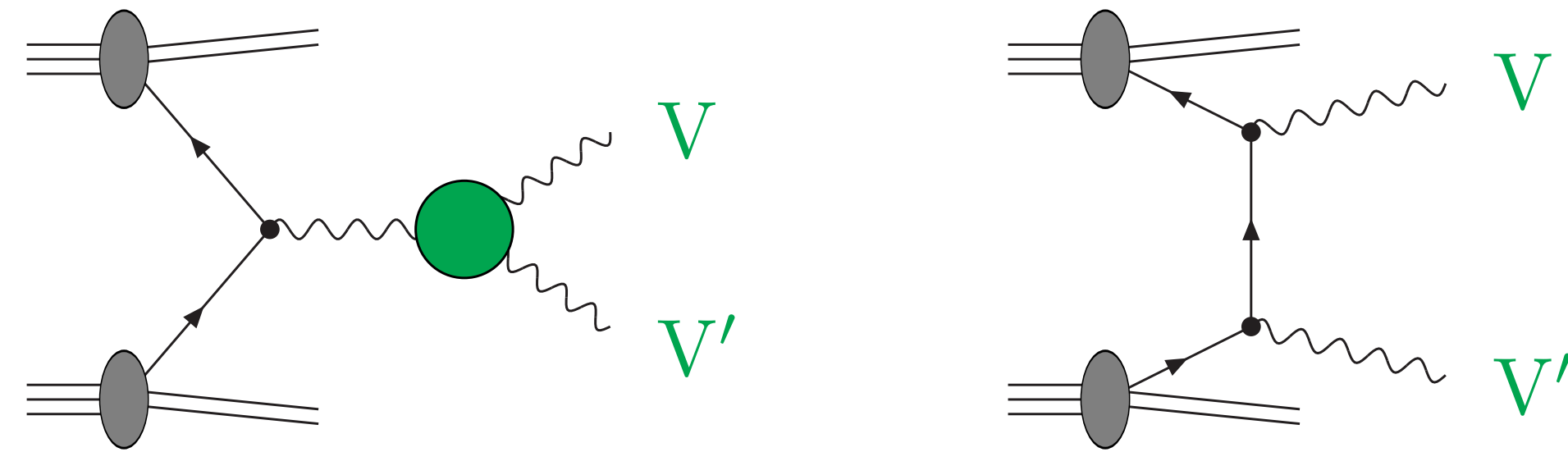


→ important for various precision observables, e.g. for determination of M_W in DY

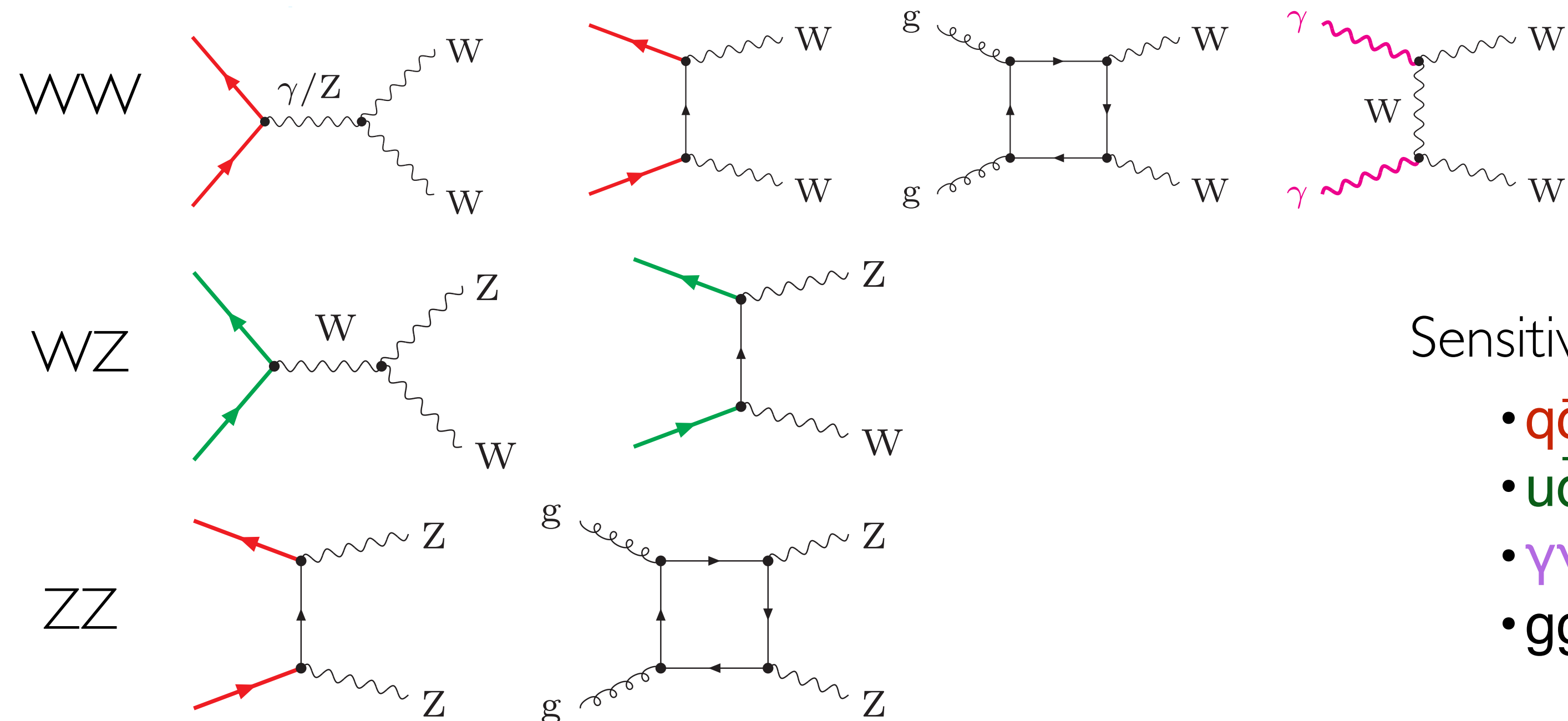
Diboson production



Diboson production



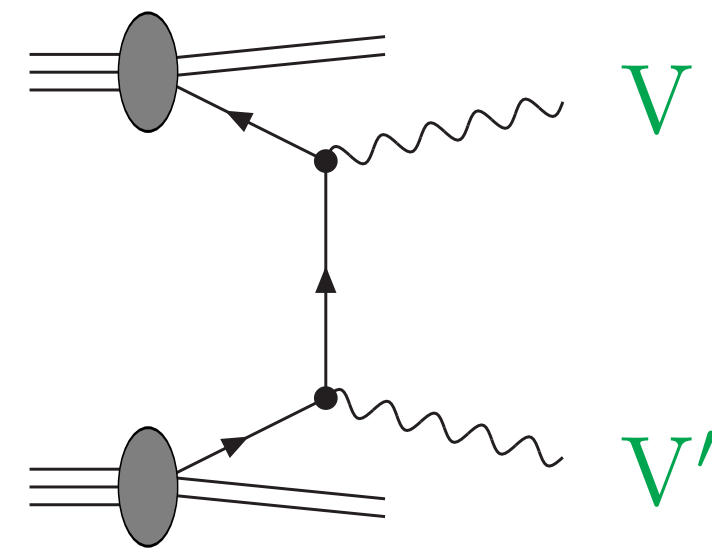
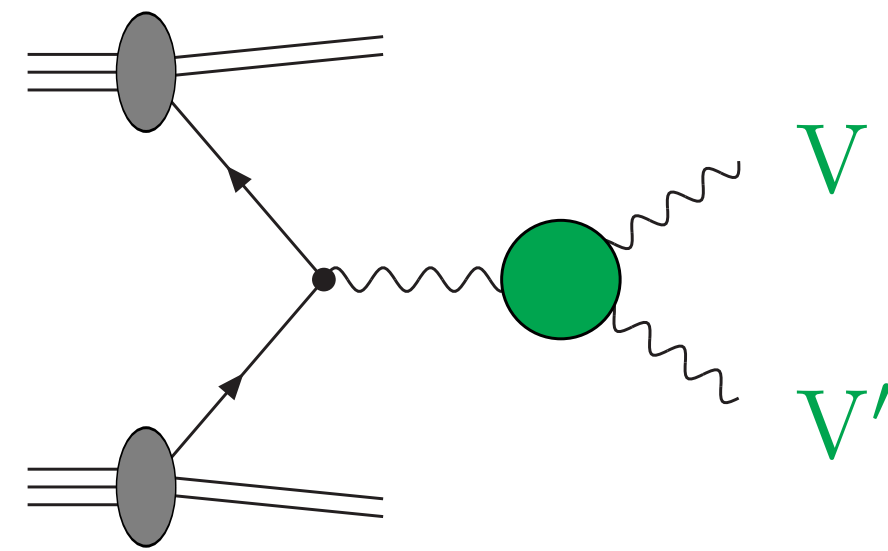
Complementarity in WW / WZ / ZZ production



Sensitivity to different PDF combinations:

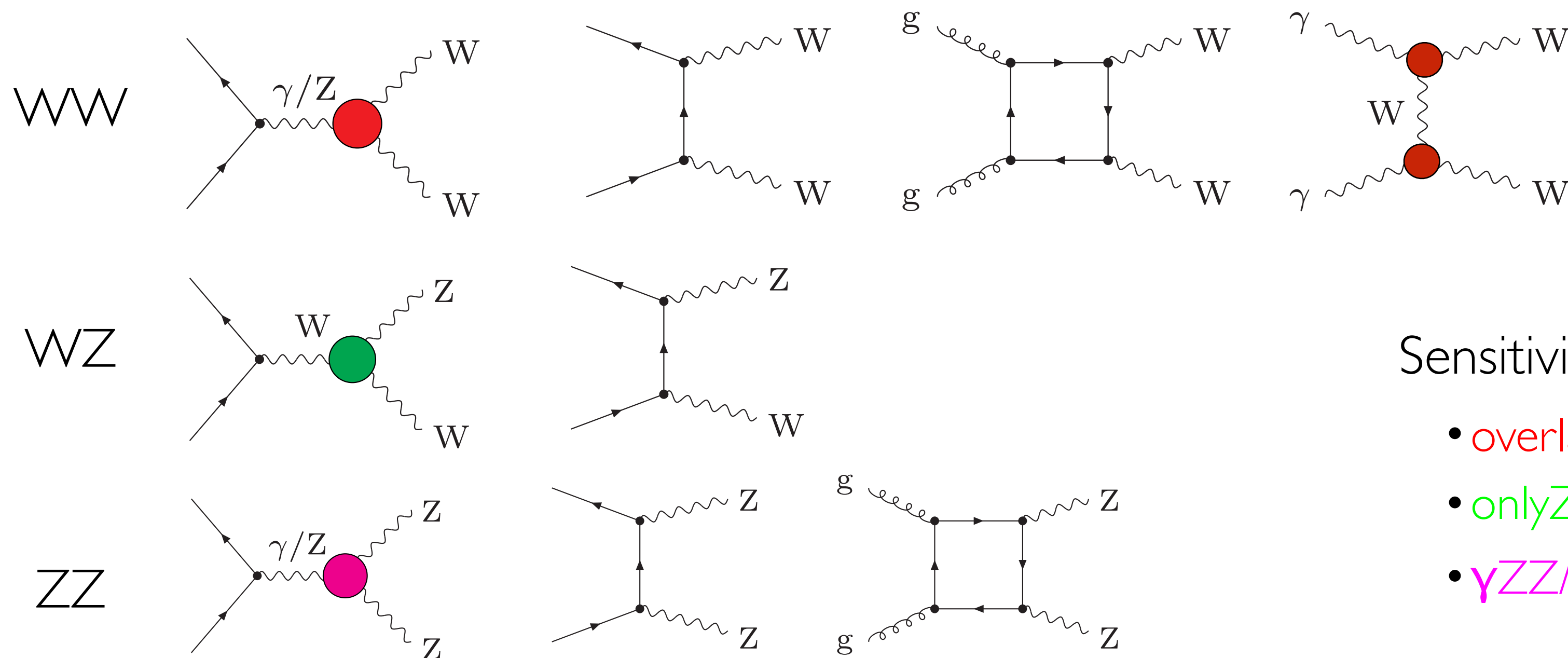
- $q\bar{q}$ in WW/ZZ
- $u\bar{d}/d\bar{u}$ in WZ
- $\gamma\gamma$ in WW
- gg in WW/ZZ

Diboson production



Complementarity in WW / WZ / ZZ production

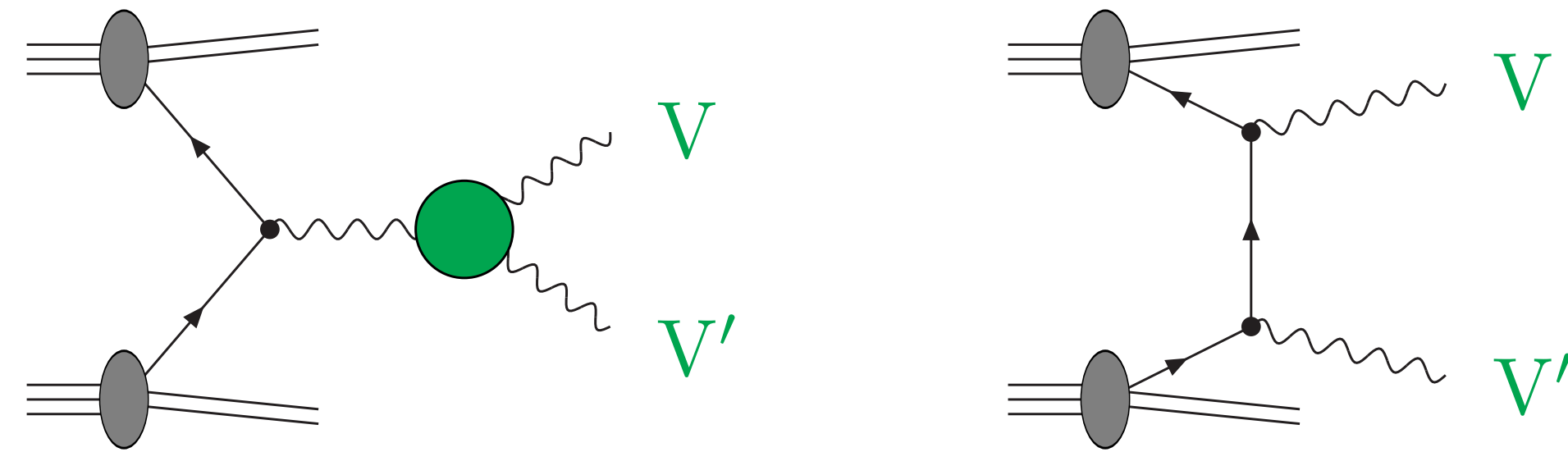
[see Talk by Francesco Riva]



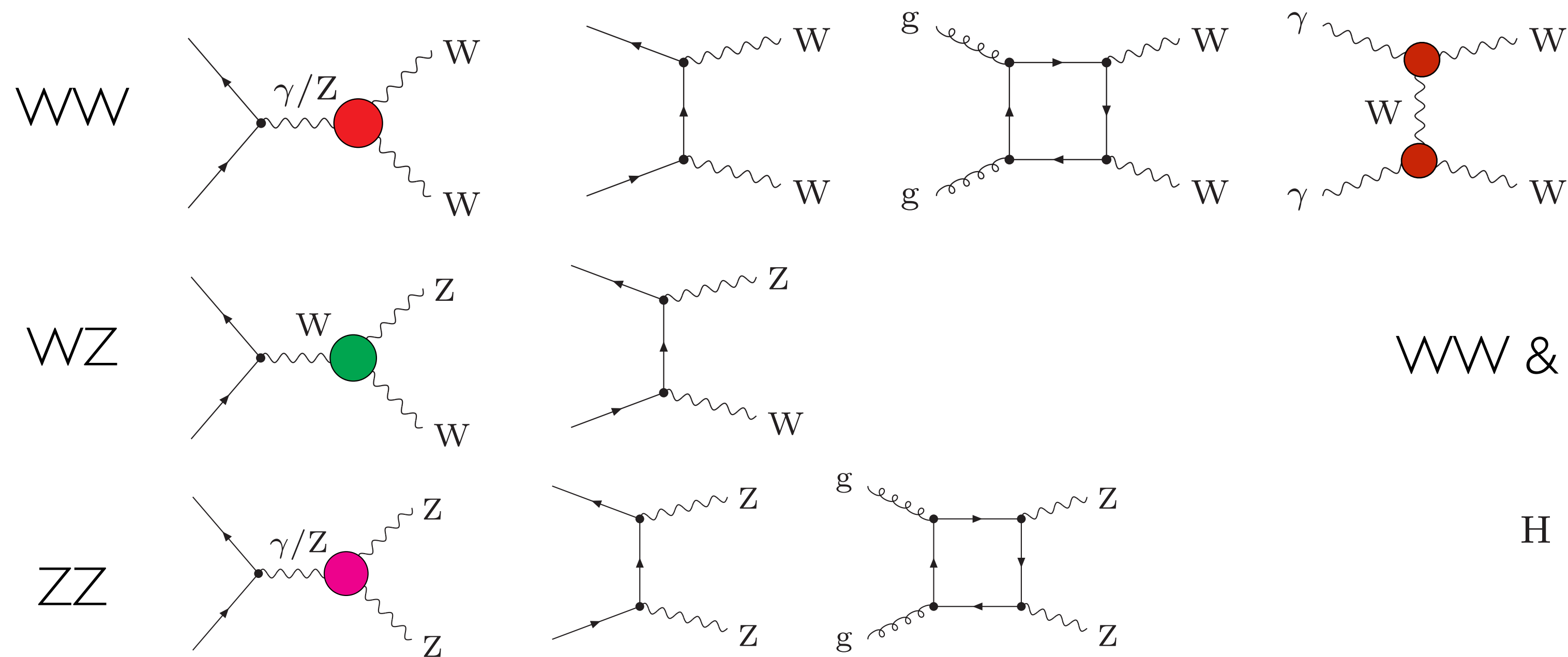
Sensitivity to different aTGCs:

- overlay of $\gamma WW/Z WW$ in WW
- only $Z WW$ in WZ
- $\gamma ZZ/Z ZZ$ in ZZ

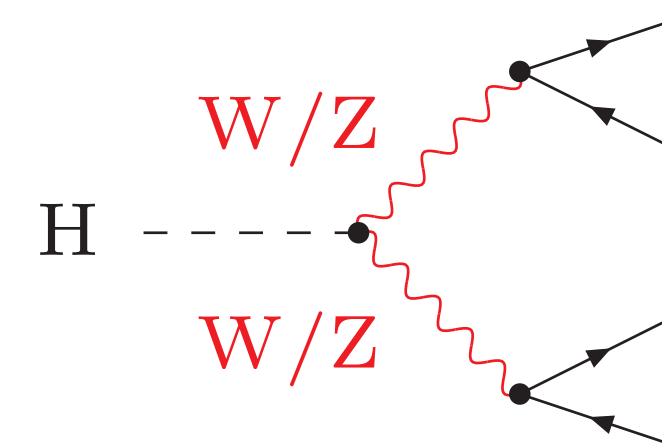
Diboson production



Complementarity in WW / WZ / ZZ production

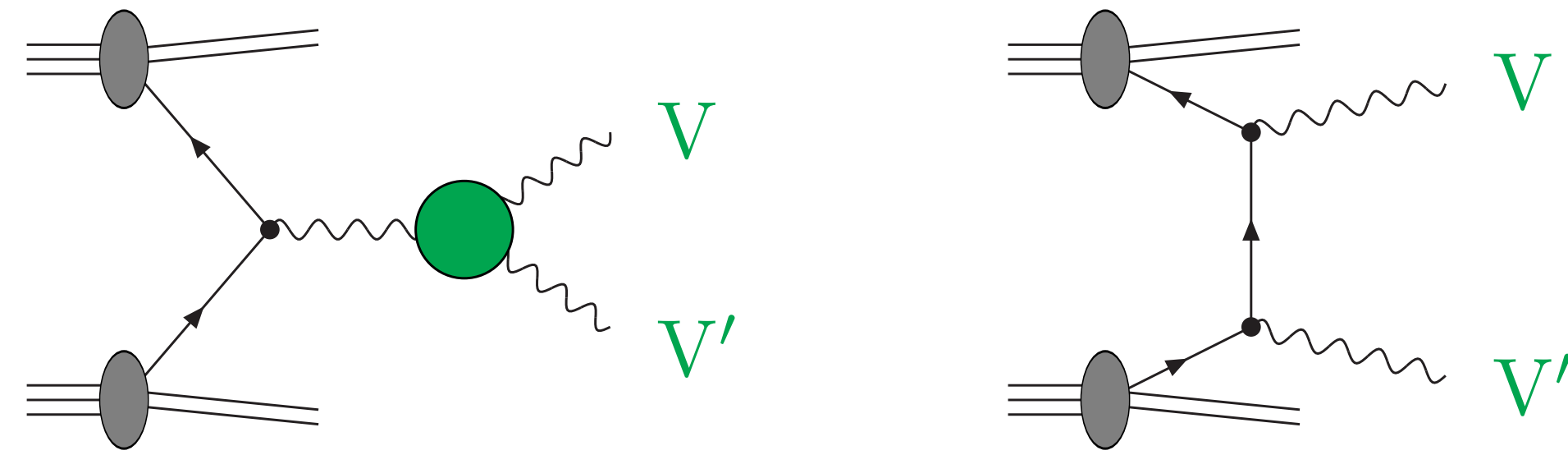


WW & ZZ are background in $H \rightarrow VV$:



(off-shell calculations mandatory)

Diboson production



Theoretical status: NNLO **QCD** + NLO **EW**

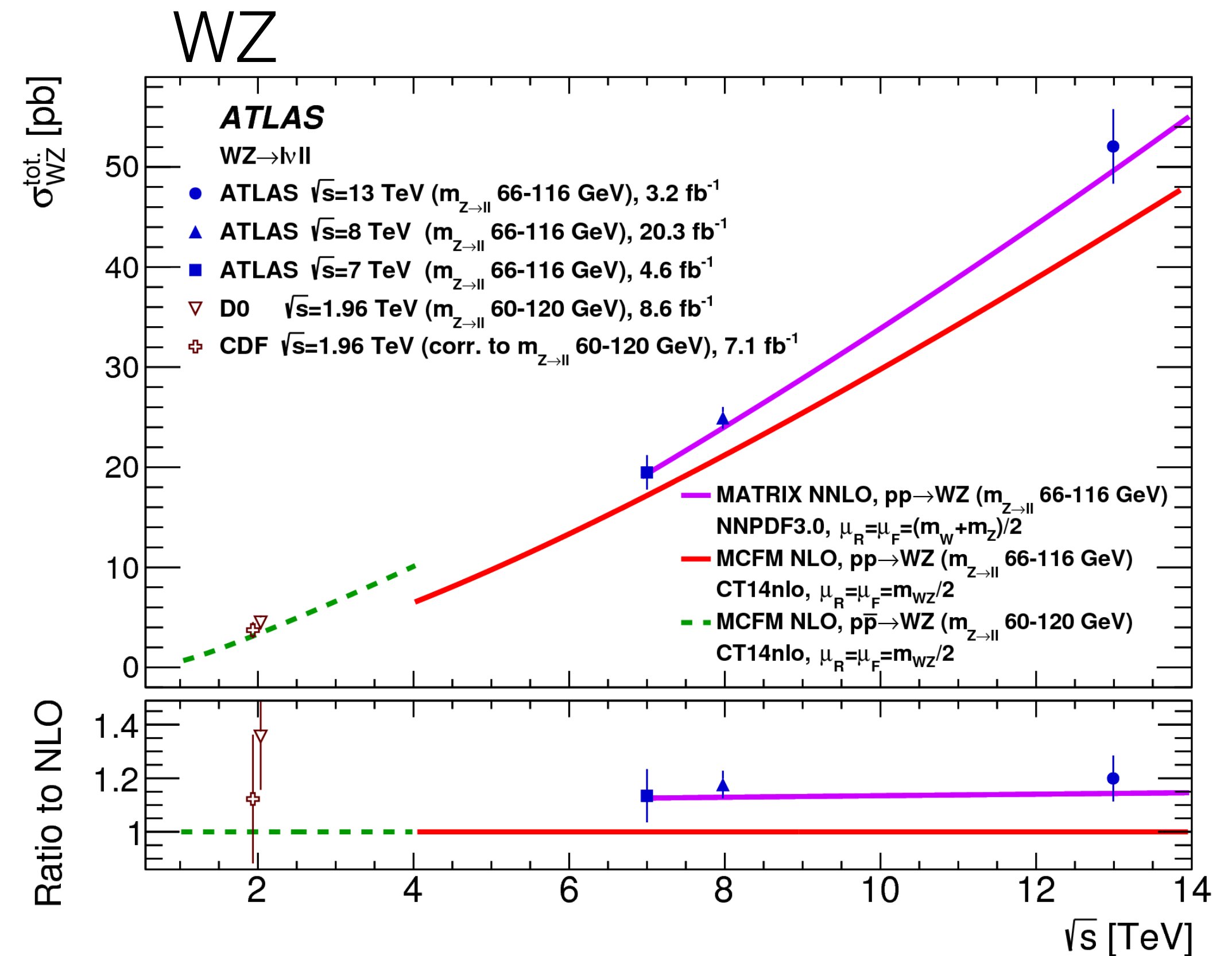
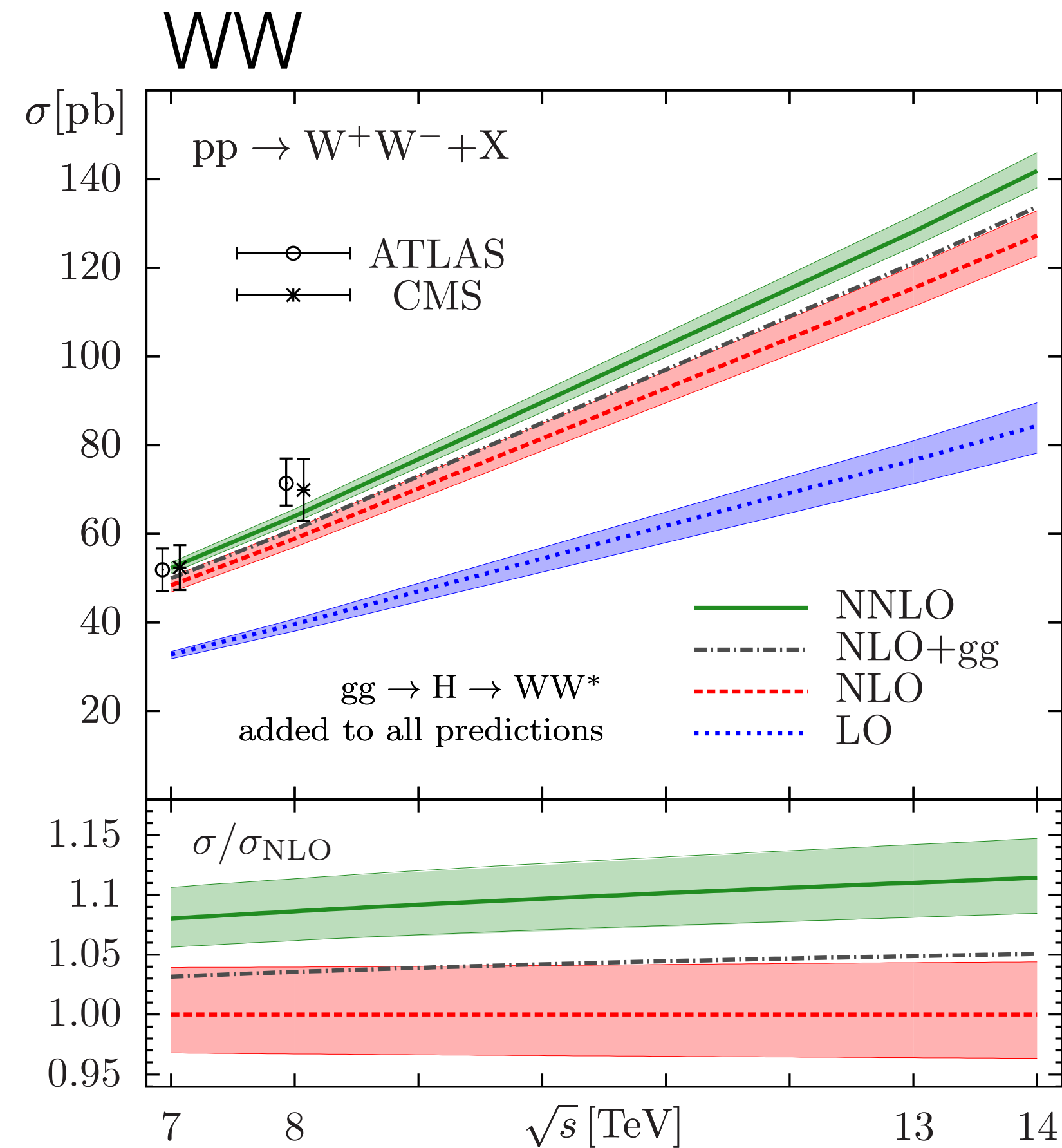
- WW [Gehrmann et. al. '14, Grazzini et. al. '16]
- WZ [Grazzini et. al. '16+'17]
- ZZ [Cascioli et.al. '14, Grazzini et. al. '15, Kallweit '18]
- $Z\gamma/W\gamma$ [Grazzini et. al. '15]
- $gg \rightarrow WW/ZZ$ [Caola et. al. '15+'16]
- NNLO+PS for WW [Re et. al. '18]

Tool: MATRIX [Grazzini et. al '17]

- stable VV [Bierweiler, Kasprzik, Kühn '13, Baglio, Ninh, Weber '13]
- DPA [Biloni et. al. '13]
- off-shell ZZ (4l) [Biedermann et. al. '16]
- off-shell WW (2l2v) [Biedermann et. al. '16, Kallweit et.al '17]
- off-shell WZ (3lv) [Biedermann et. al. '17]
- off-shell $Z\gamma/W\gamma$ [Denner et. al. '14+'15]

Tools: - Sherpa+OpenLoops/Recola/GoSam
- MadGraph_aMC@NLO

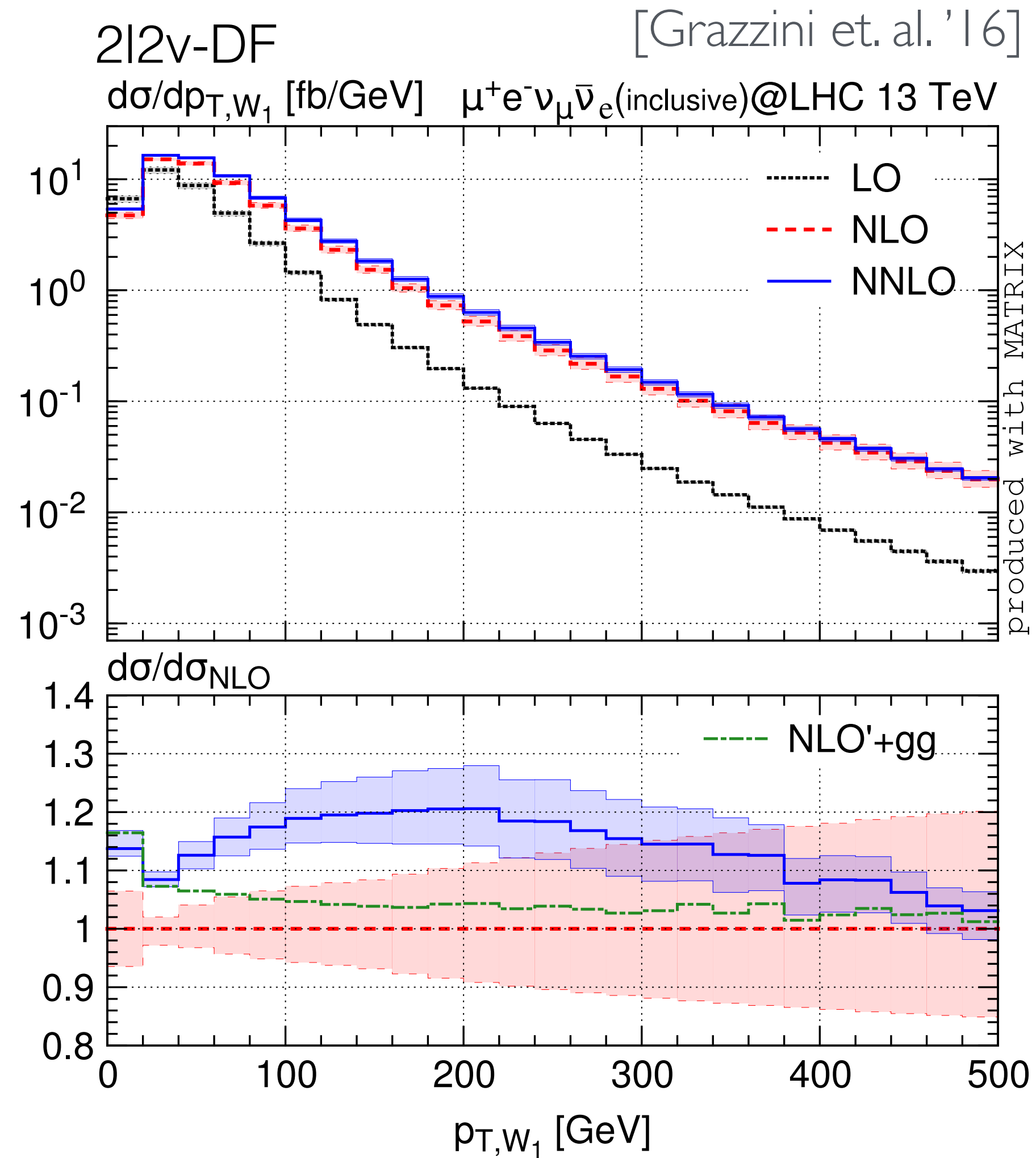
Diboson production at NNLO QCD



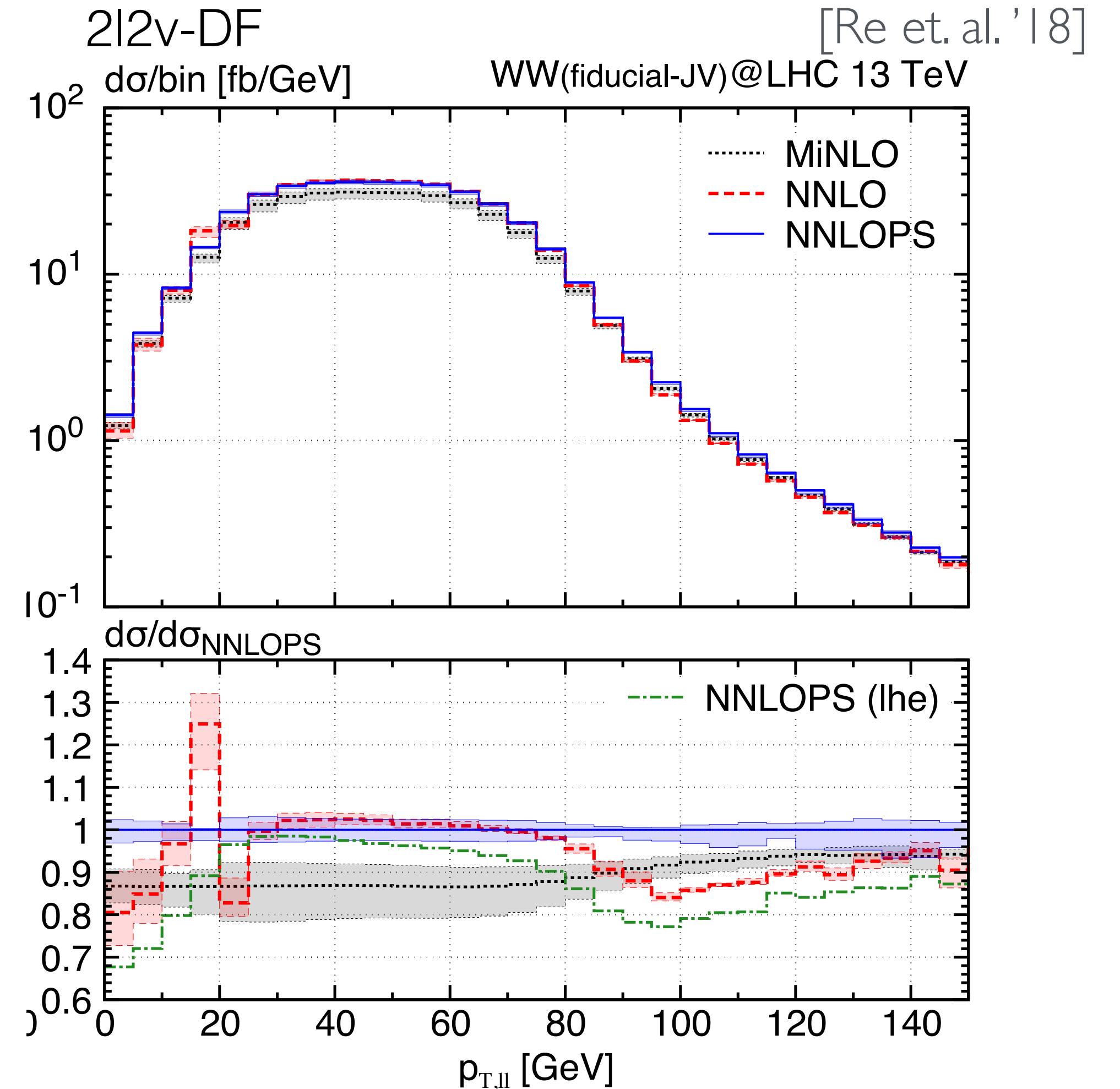
- Quite large QCD corrections well beyond expected size from scale uncertainties and $gg \rightarrow W^+W^-$ (+4%): +58% NLO & +12% NNLO at 14 TeV
- Residual scale uncertainty: 3% at NNLO

➡ NNLO mandatory to describe the data!

Diboson production at NNLO QCD (+ PS)



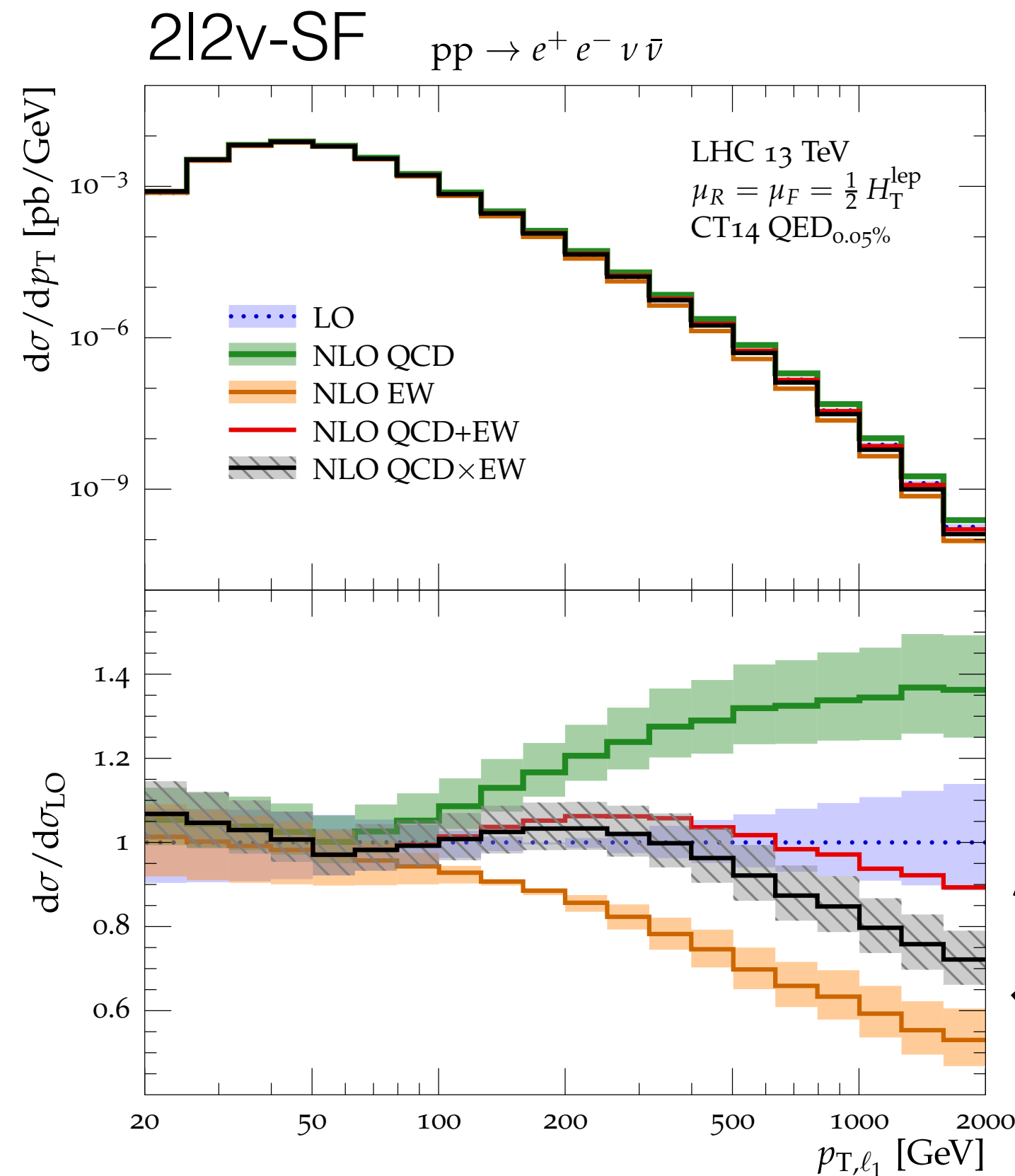
- NNLO corrections quite strongly observable dependent
- scale uncertainties reduced to few percent level



- NNLO+PS via reweighting of WW+1jet @ NLO-MiNLO
- NNLO+PS cures perturbative instabilities at phase-space boundaries

(off-shell) Diboson production at NLO QCD+EW

[Kallweit, JML, Pozzorini, Schönherr; '17]



p_T of hardest lepton

► +40 % QCD corrections in the tail (Note: slight jet veto applied)

► LARGE negative EW corrections due to **Sudakov behaviour**: -40% @ 1 TeV

► Combination of QCD and EW corrections:

→ Additive combination

$$\sigma_{\text{QCD+EW}}^{\text{NLO}} = \sigma^{\text{LO}} + \delta\sigma_{\text{QCD}}^{\text{NLO}} + \delta\sigma_{\text{EW}}^{\text{NLO}} \quad (\text{no } \mathcal{O}(\alpha\alpha_s) \text{ contributions})$$

→ Multiplicative combination

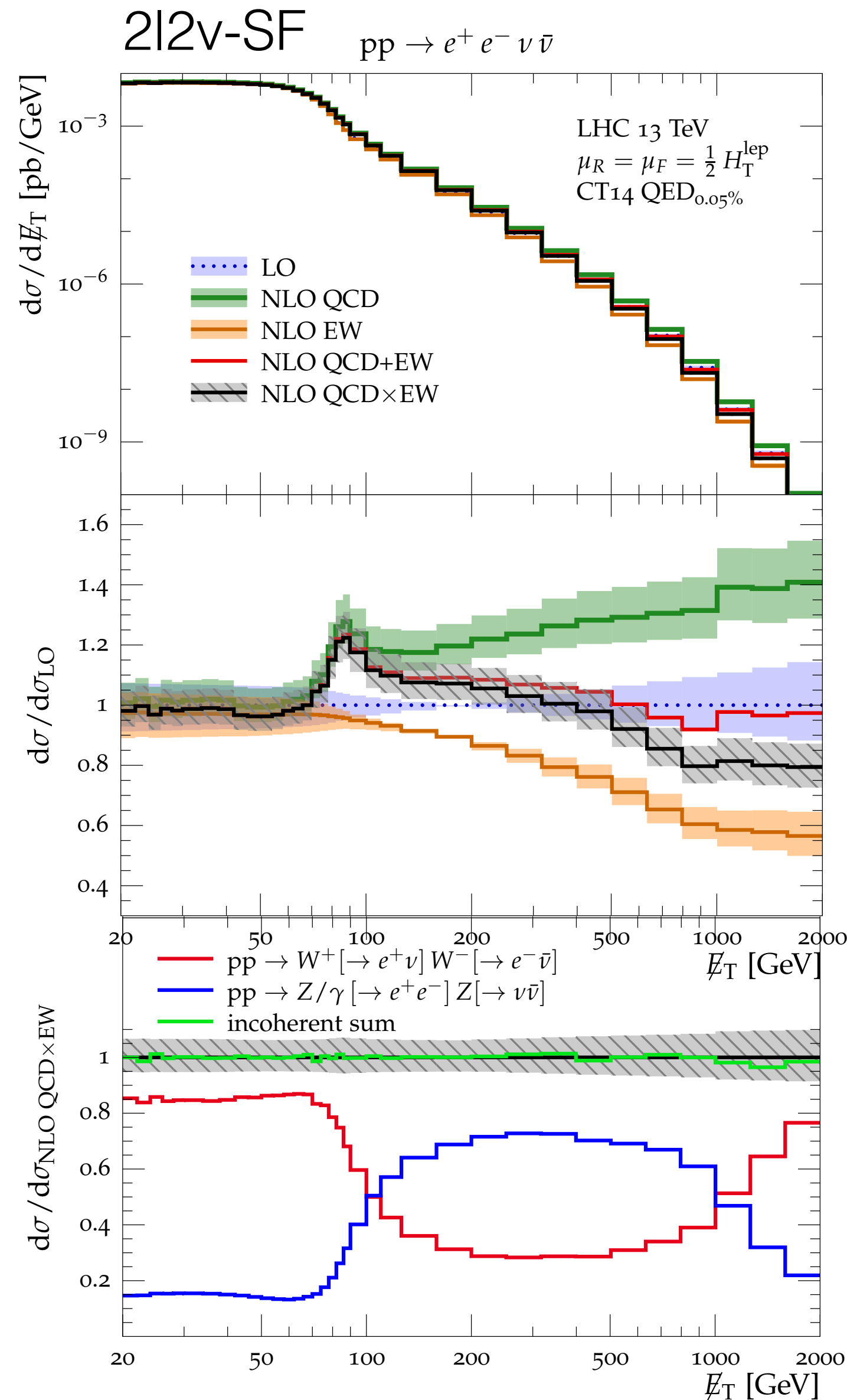
$$\sigma_{\text{QCD}\times\text{EW}}^{\text{NLO}} = \sigma_{\text{QCD}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right)$$

$|\text{QCD+EW} - \text{QCD}\times\text{EW}| \sim \delta_{\text{QCD}}\times\delta_{\text{EW}} \sim \text{NNLO QCD}\times\text{EW}$
 $\sim 10\text{-}20\%$ in the tail!

Note: exact NNLO QCD×EW extremely hard!

(off-shell) Diboson production at NLO QCD+EW

[Kallweit, JML, Pozzorini, Schönherr; '17]

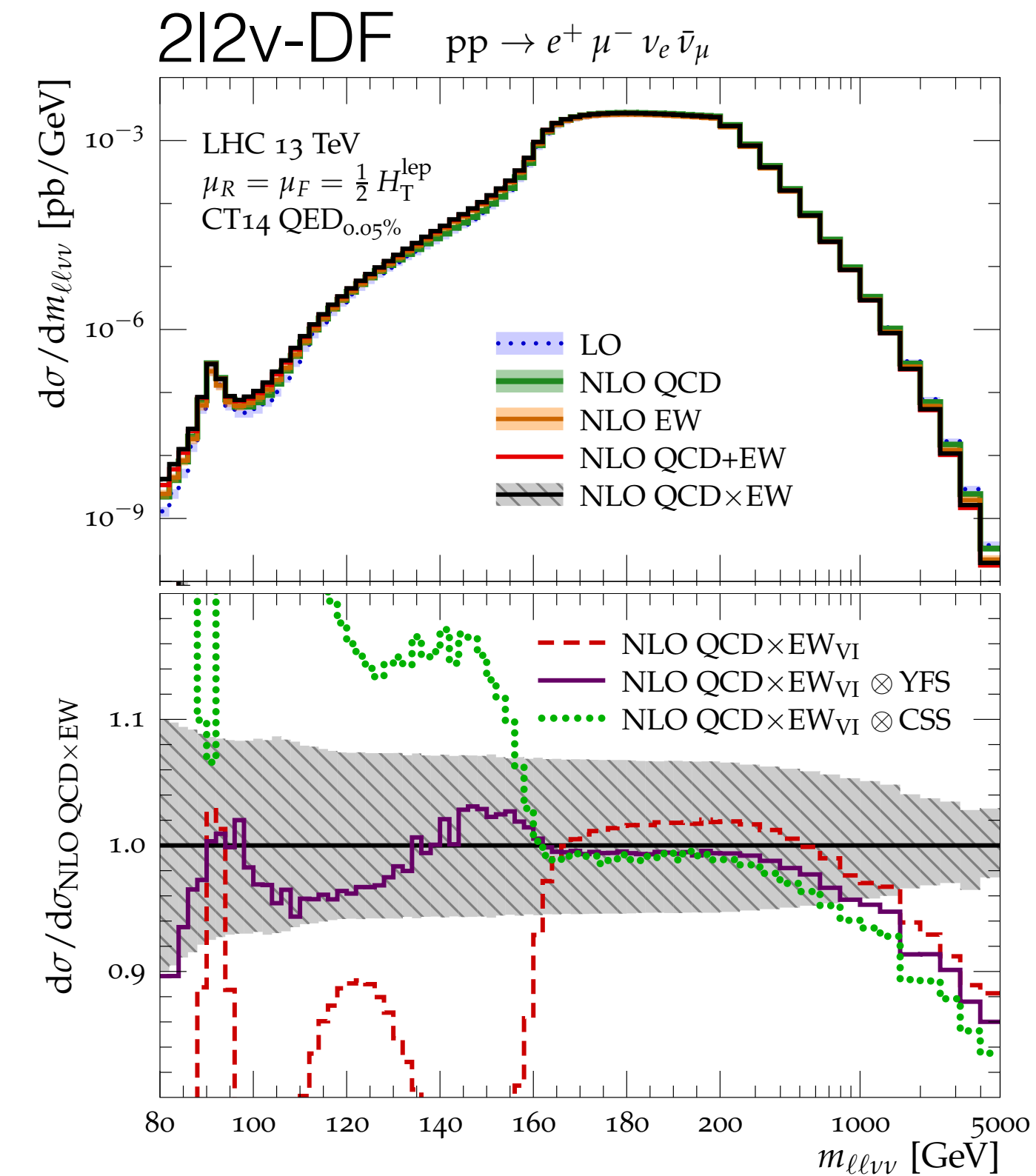
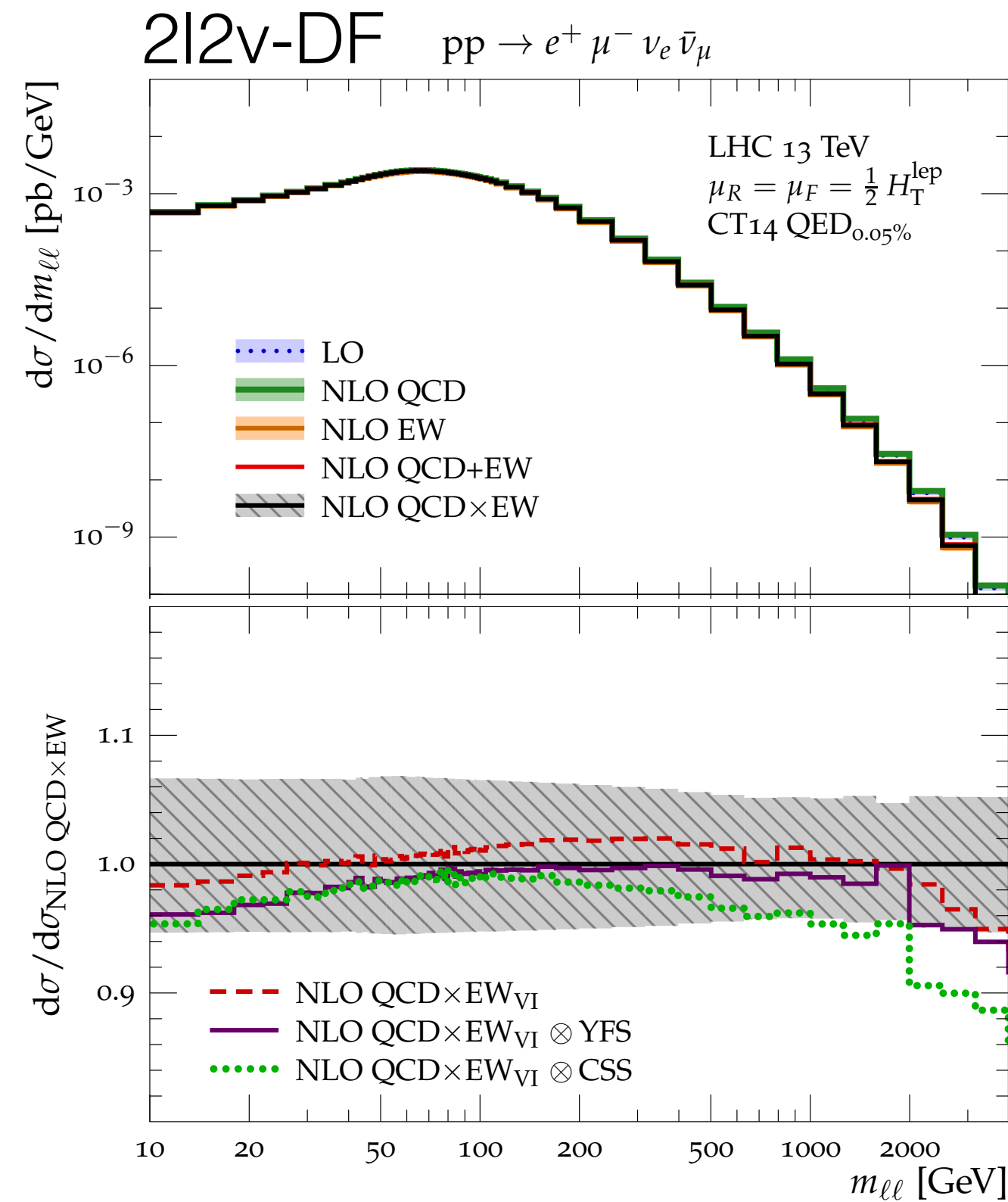


MET

- ▶ at large MET $> M_W$:
 W's are forced off-shell
- ▶ jump in QCD corrections
 (extra jet unlocks back-to-back configuration)
- ▶ very large EW corrections: up to 50% (WW/ZZ dependent!)
- ▶ WW-ZZ interference very suppressed (as expected from LO)
- ▶ Combination of QCD and EW corrections:
 $|QCD+EW - QCD \times EW| \sim \delta_{QCD} \times \delta_{EW} \sim \text{NNLO } QCD \times EW$
 $\sim 10\text{-}20\%$ in the ETmiss tail

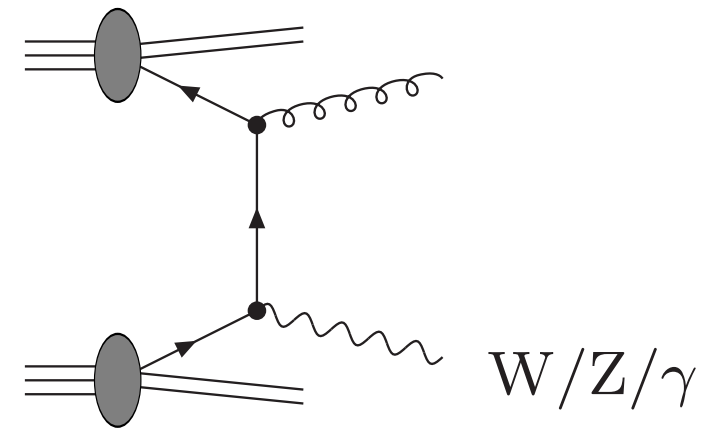
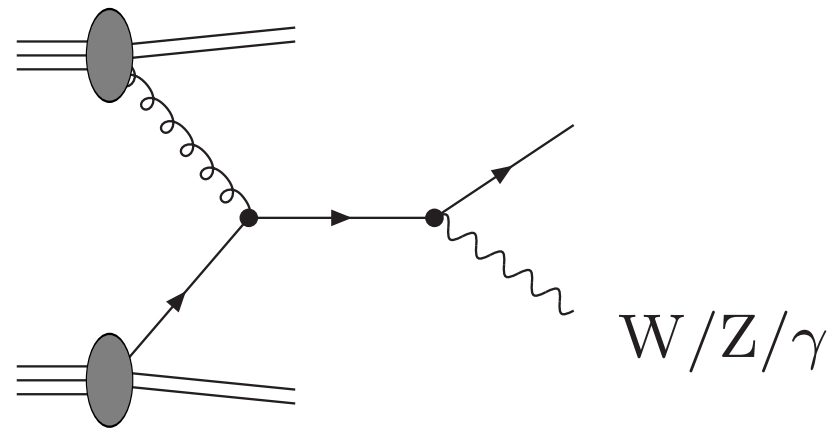
(off-shell) Diboson production at NLO QCD+EW

[Kallweit, JML, Pozzorini, Schönherr; '17]

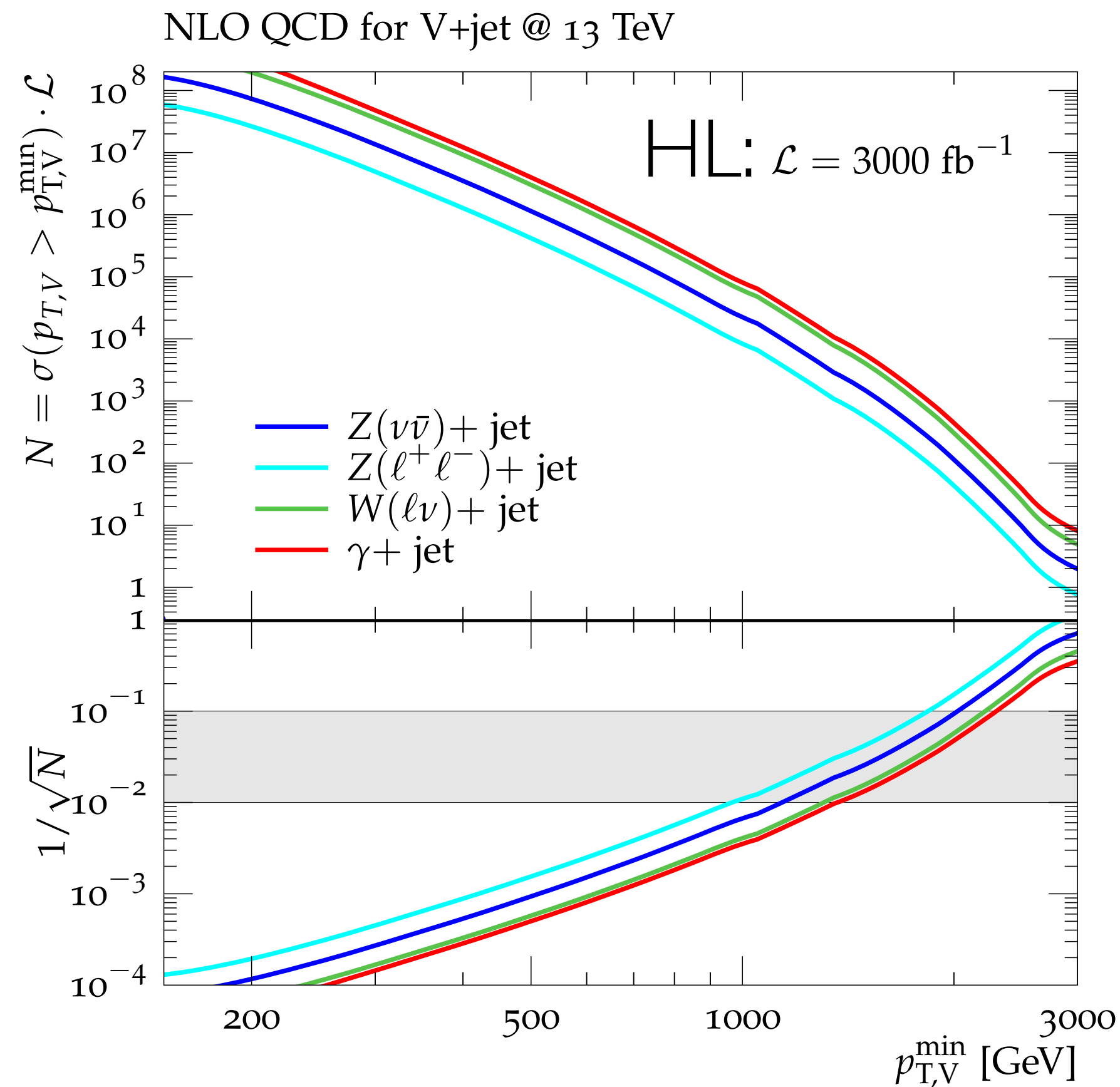
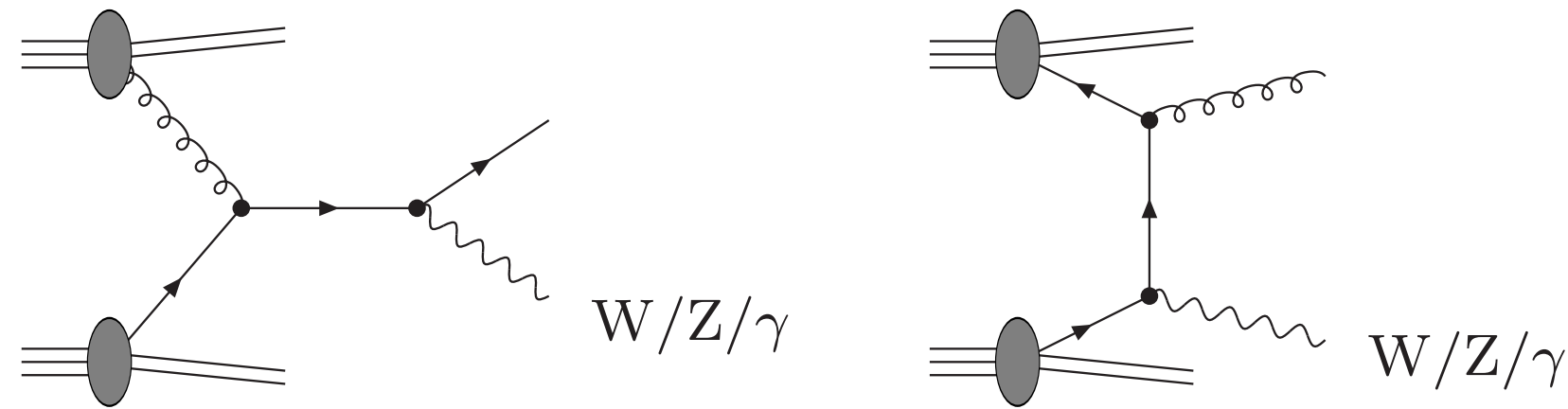


- Fully consistent PS matching at NLO EW under development
- Naive NLO EW+PS matching available in Sherpa+OpenLoops (applicable at particle level)
 - ➔ CSS dipole shower (not resonance aware) \Rightarrow significant mismodelling
 - ➔ YFS resummation (**resonance aware**) \Rightarrow valid approximation

V+jets



V+jets



V+jets is crucial background

- Important/dominant background for various BSM searches (lepton(s) + jets + missing E_T)
- Dominant background in many DM searches: MET+X
- Dominant background for top physics (W+jets)
- Important background for Higgs physics, e.g. VH

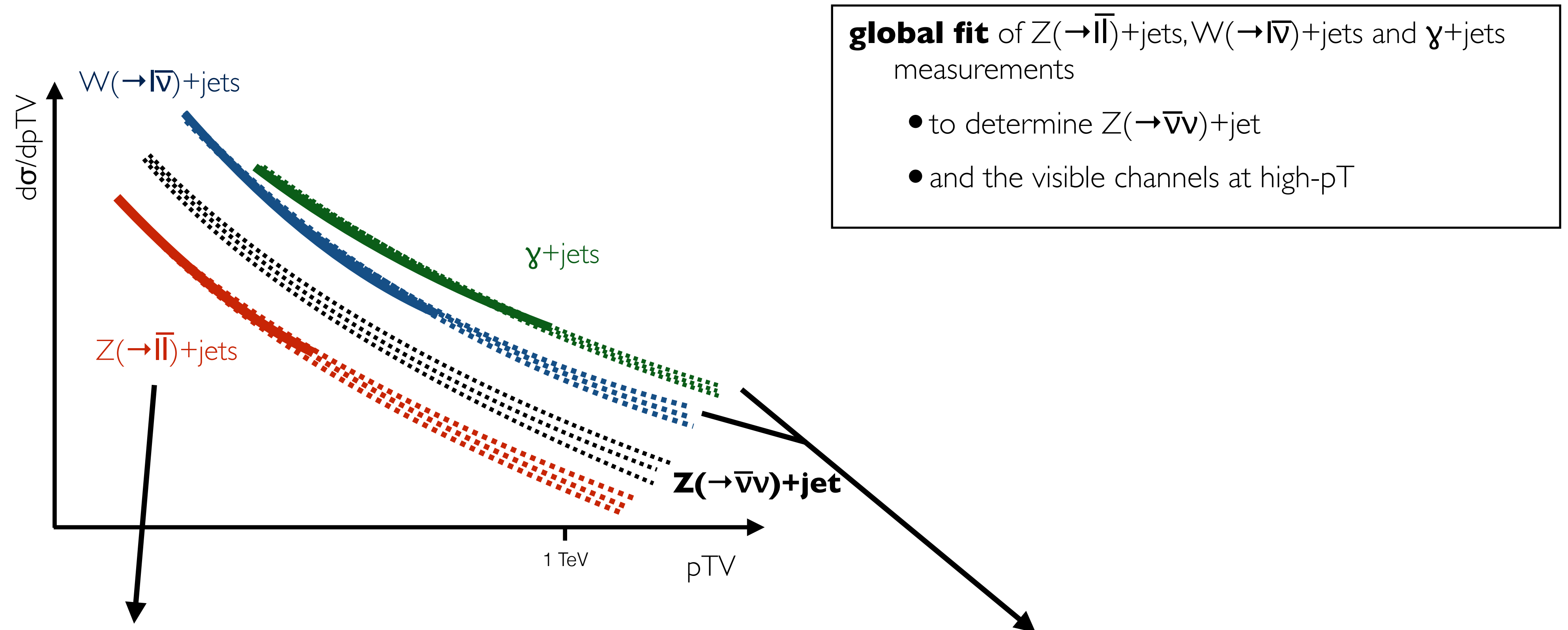
► statistical uncertainty at the **1% level** for $p_{T,V} \gtrsim 1\text{-}1.5 \text{ TeV}$

► statistical uncertainty at the **10% level** for $p_{T,V} \gtrsim 2 \text{ TeV}$

➡ need to consider state of the art higher-order corrections:

NNLO QCD + NNLO EW

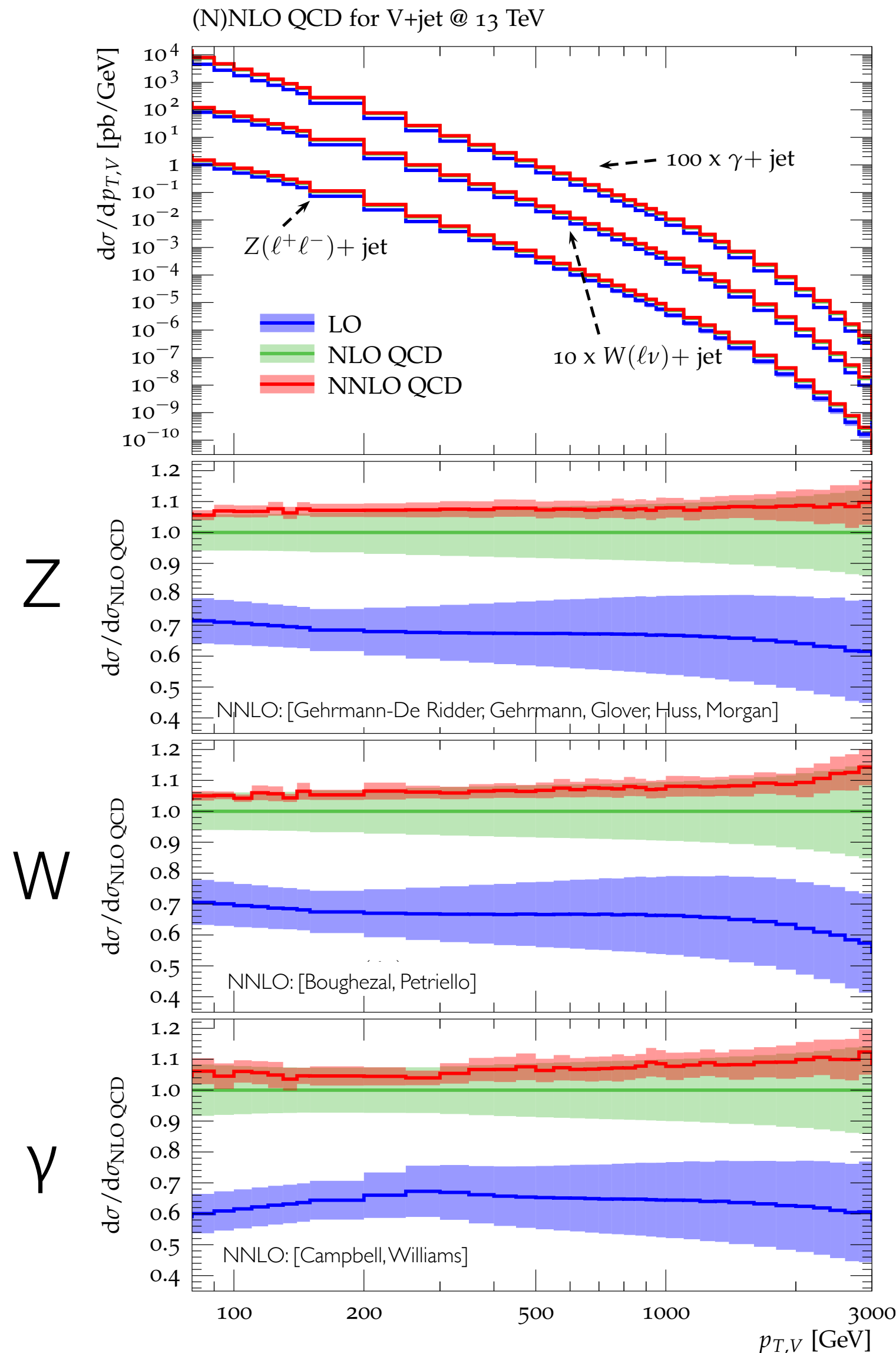
Determine V+jets backgrounds: the DM case



- hardly any systematics (just QED dressing)
- very precise at low p_T
- but: limited statistics at large p_T
- fairly large data samples at large p_T
- systematics from transfer factors: ratios of V+jets processes

Pure QCD uncertainties

[JML et. al.: 1705.04664]



$$\frac{d}{dx}\sigma_{\text{QCD}}^{(V)} = \frac{d}{dx}\sigma_{\text{LO QCD}}^{(V)} + \frac{d}{dx}\sigma_{\text{NLO QCD}}^{(V)} + \frac{d}{dx}\sigma_{\text{NNLO QCD}}^{(V)}$$

$$\mu_0 = \frac{1}{2} \left(\sqrt{p_{T,\ell+\ell-}^2 + m_{\ell+\ell-}^2} + \sum_{i \in \{q,g,\gamma\}} |p_{T,i}| \right)$$

this is a 'good' scale for V+jets

- at large p_{TV} : $HT'/2 \approx p_{TV}$
- modest higher-order corrections
- sufficient convergence

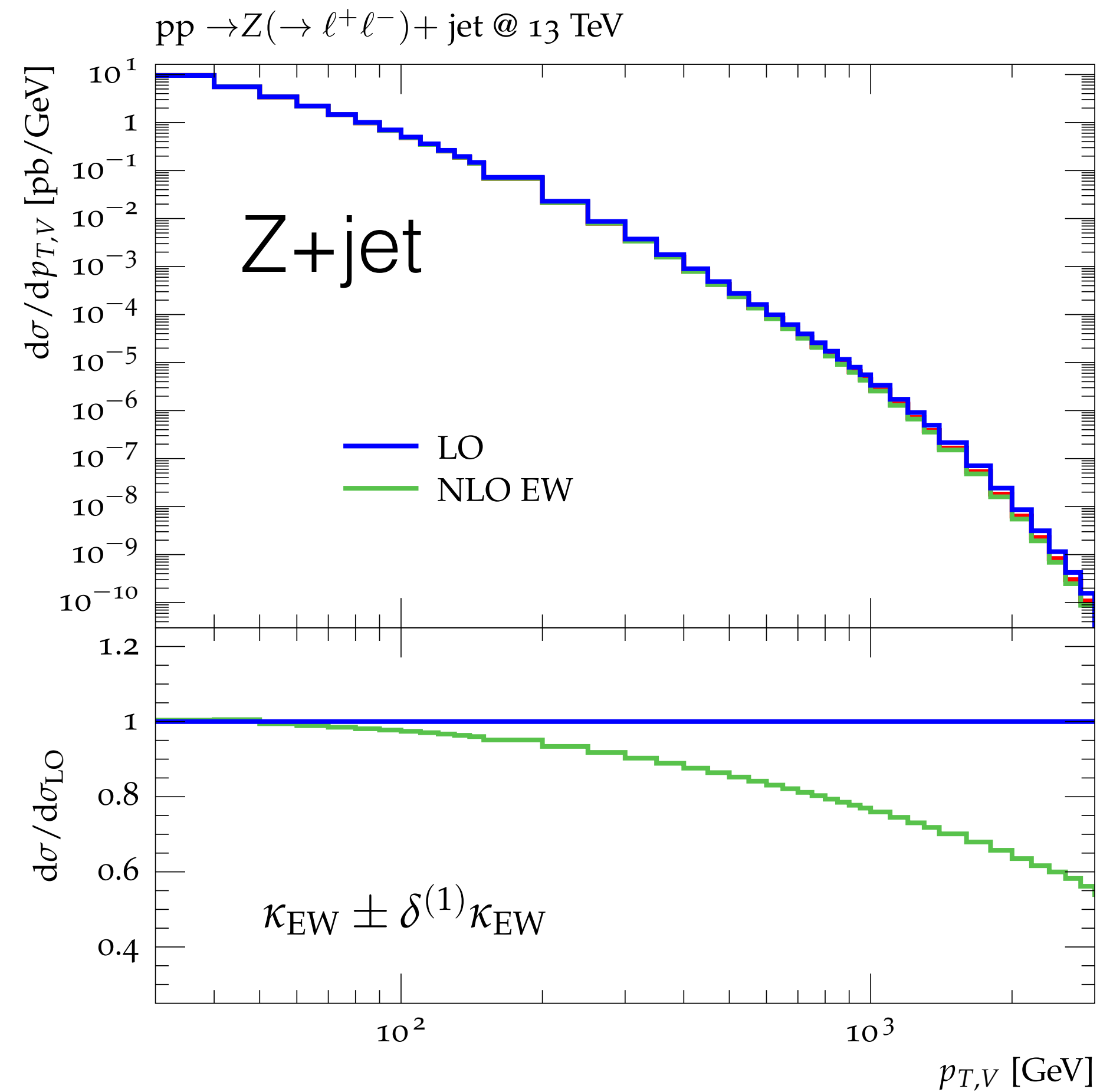
scale uncertainties due to 7-pt variations:

O(20%) uncertainties at LO
O(10%) uncertainties at NLO
O(5%) uncertainties at NNLO

with minor shape variations

How to correlate these uncertainties across processes?

Pure EW uncertainties



EW corrections become sizeable
at large $p_{T,V}$: -30% @ 1 TeV

Origin: virtual EW Sudakov logarithms

How to estimate corresponding pure EW uncertainties
of relative $\mathcal{O}(\alpha^2)$?

Precise predictions for V+jet DM backgrounds

[1705.04664]

work in collaboration with:

R. Boughezal, J.M. Campell, A. Denner, S. Dittmaier, A. Huss, A. Gehrmann-De Ridder, T. Gehrmann, N. Glover, S. Kallweit, M. L. Mangano, P. Maierhöfer, T.A. Morgan, A. Mück, M. Schönherr, F. Petriello, S. Pozzorini, G. P. Salam, C. Williams

- Combination of state-of-the-art predictions: (N)NLO **QCD** + (N)NLO **EW** in order to match (future) experimental sensitivities (1-10% accuracy in the few hundred GeV-TeV range)

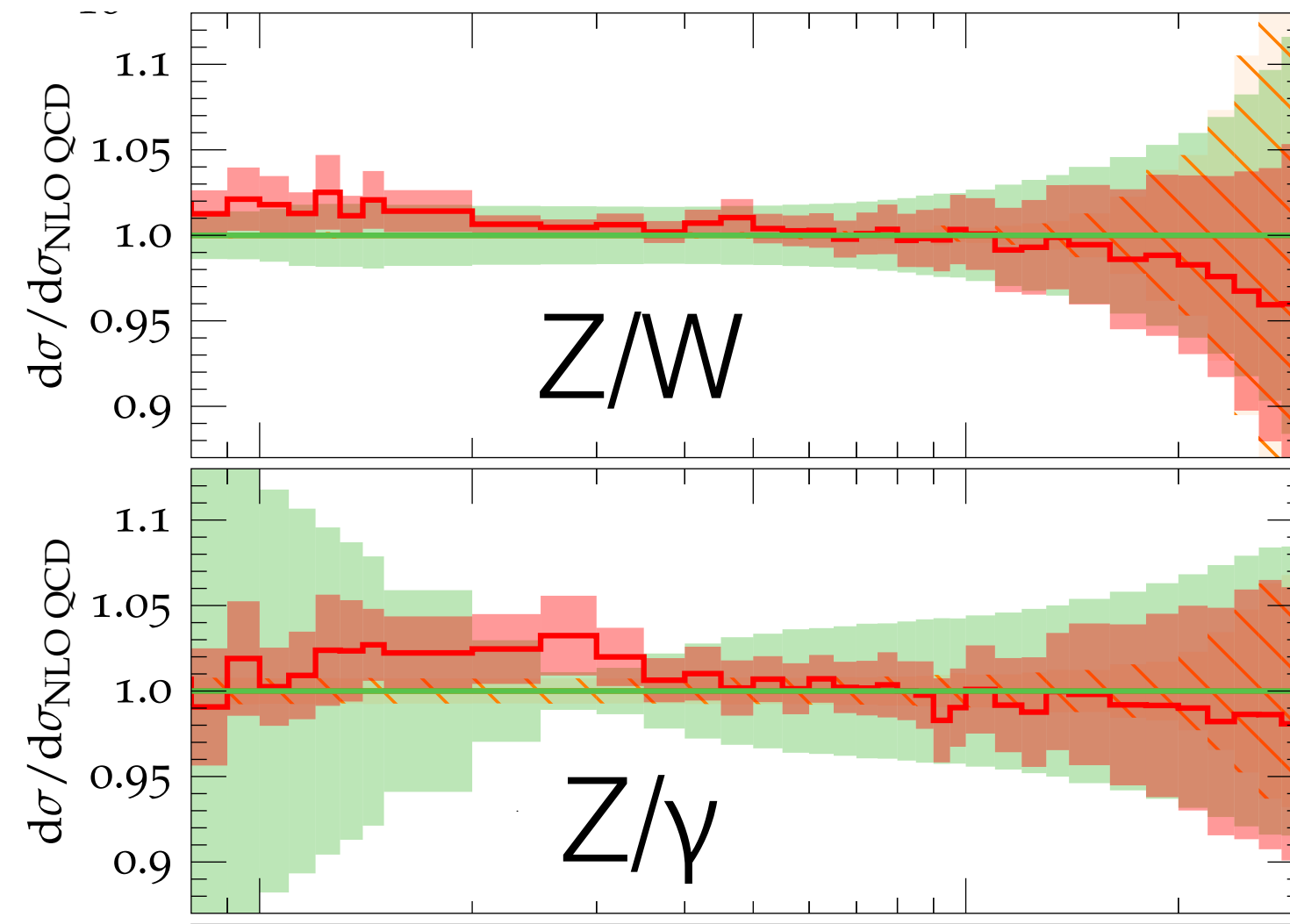
$$\frac{d}{dx} \frac{d}{dy} \sigma^{(V)}(\vec{\epsilon}_{\text{MC}}, \vec{\epsilon}_{\text{TH}}) := \frac{d}{dx} \frac{d}{dy} \sigma_{\text{MC}}^{(V)}(\vec{\epsilon}_{\text{MC}}) \left[\frac{\frac{d}{dx} \sigma_{\text{TH}}^{(V)}(\vec{\epsilon}_{\text{TH}})}{\frac{d}{dx} \sigma_{\text{MC}}^{(V)}(\vec{\epsilon}_{\text{MC}})} \right]$$

one-dimensional reweighting of MC samples in $x = p_{\text{T}}^{(V)}$

with
$$\frac{d}{dx} \sigma_{\text{TH}}^{(V)} = \frac{d}{dx} \sigma_{\text{QCD}}^{(V)} + \frac{d}{dx} \sigma_{\text{mix}}^{(V)} + \frac{d}{dx} \Delta \sigma_{\text{EW}}^{(V)} + \frac{d}{dx} \sigma_{\gamma\text{-ind.}}^{(V)}$$

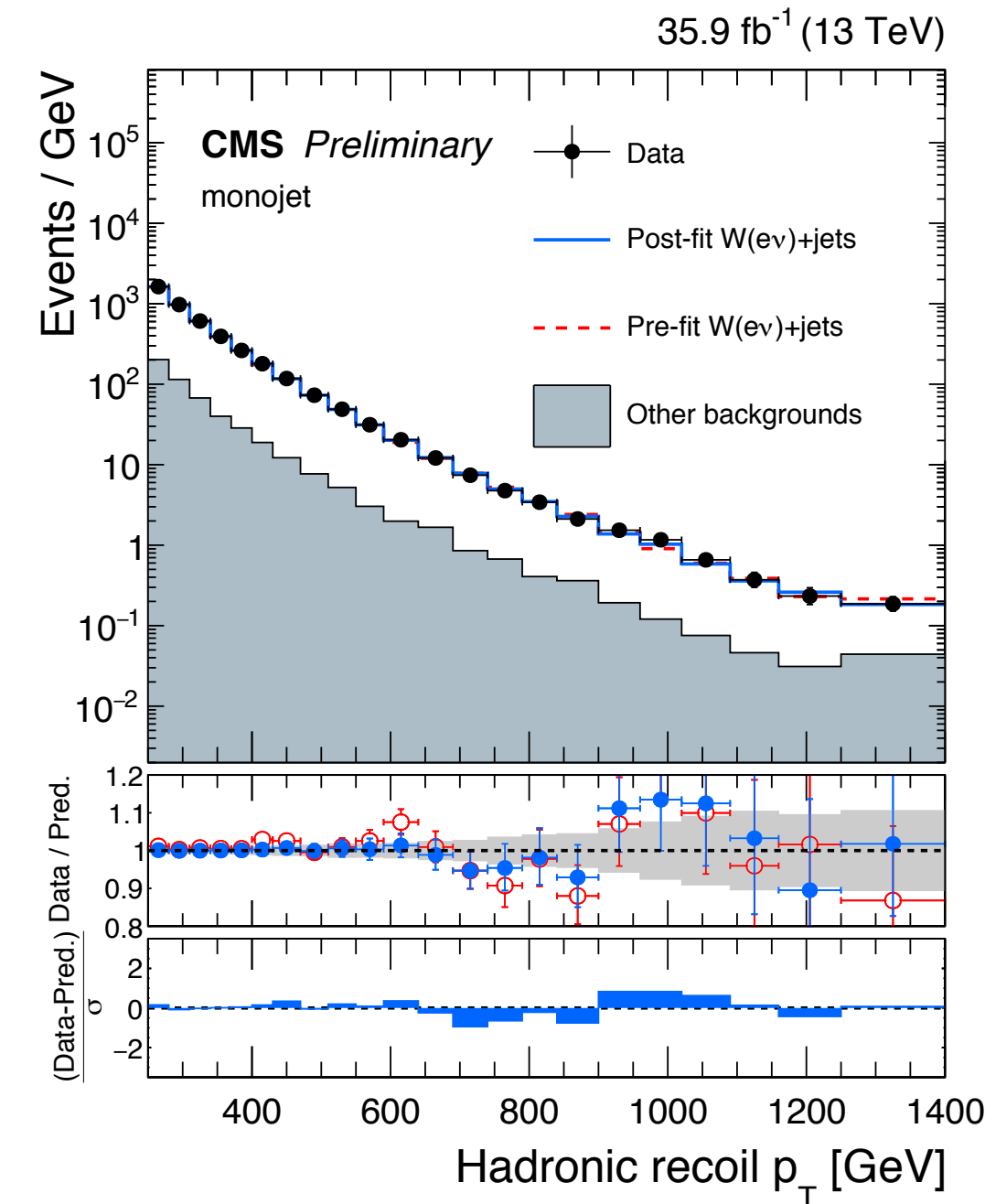
- Robust uncertainty estimates including
 1. Pure **QCD** uncertainties
 2. Pure **EW** uncertainties
 3. Mixed **QCD-EW** uncertainties
 4. PDF, γ -induced uncertainties
- Prescription for **correlation** of these uncertainties
 - ▶ within a process (between low-pT and high-pT)
 - ▶ across processes

Combined uncertainties on V+jets ratios



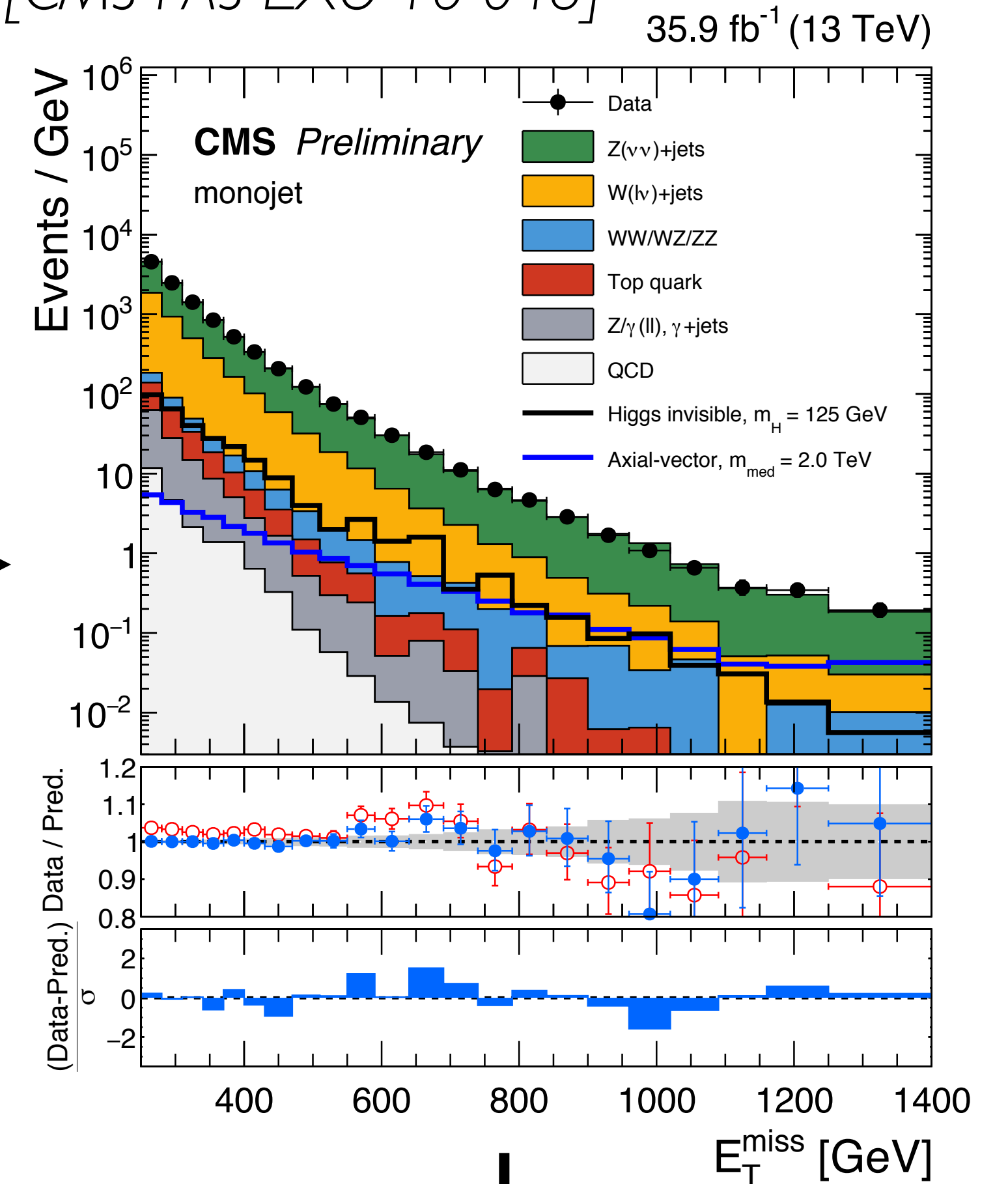
- $\delta_{Z/W} = 1-3\%$ for $p_T < 1$ TeV
- $\delta_{Z/\gamma} = 3-5\%$ for $p_T < 1$ TeV

CR

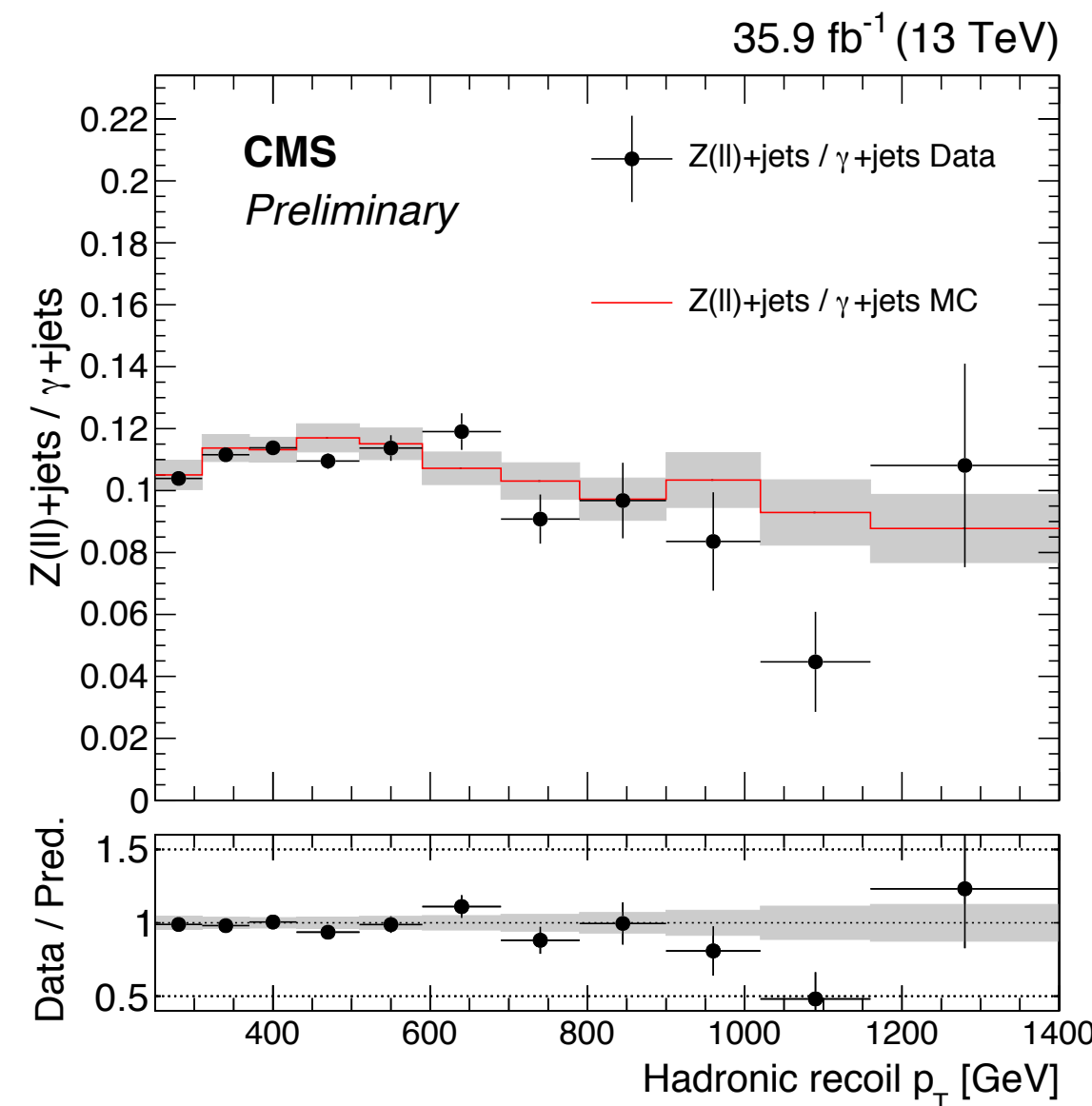


SR

[CMS PAS EXO-16-048]

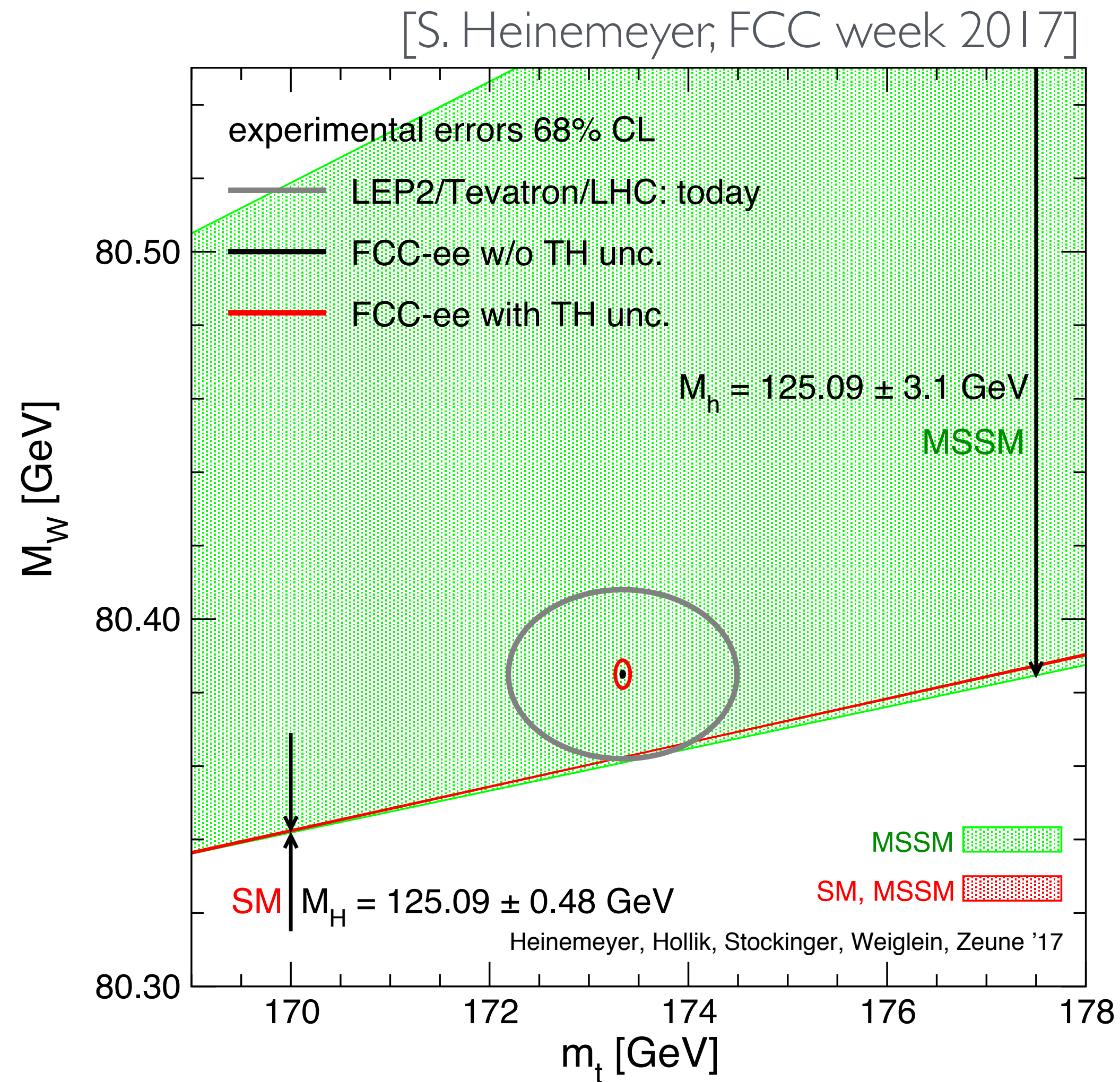


Unprecedented limits on monojet DM production!



M_W measurements (precision DY)

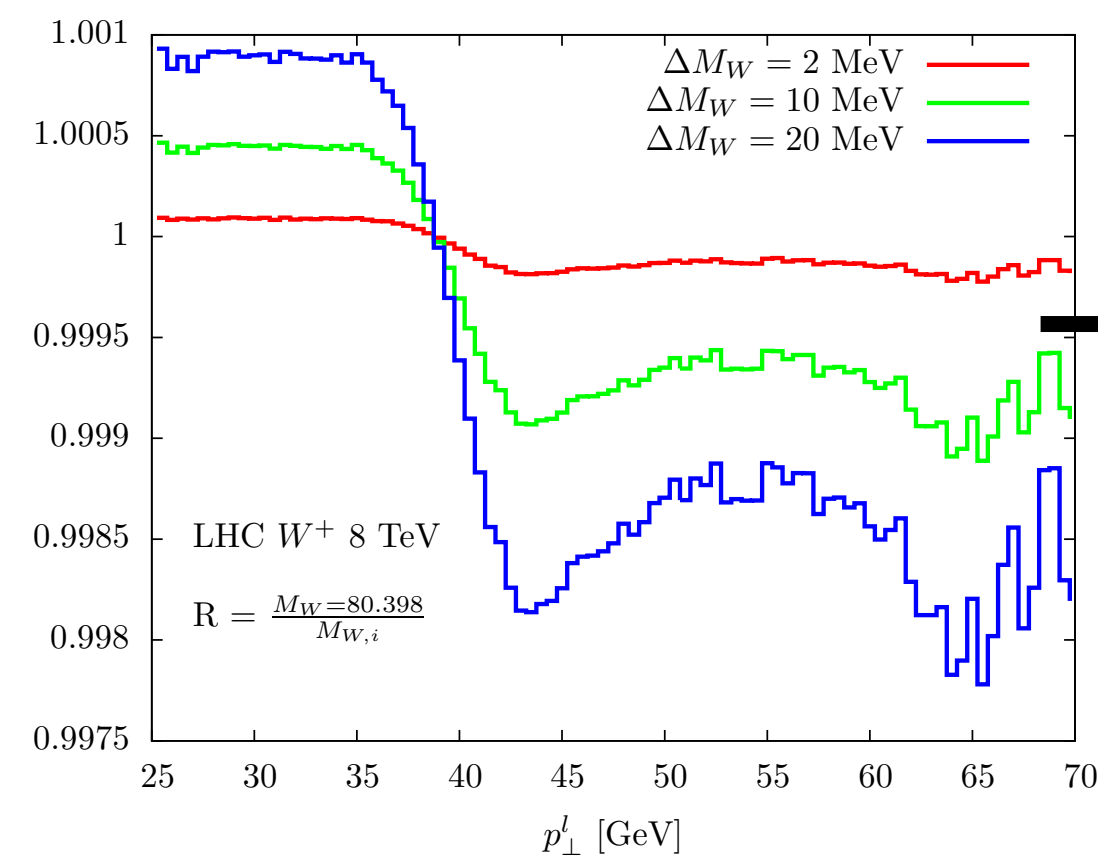
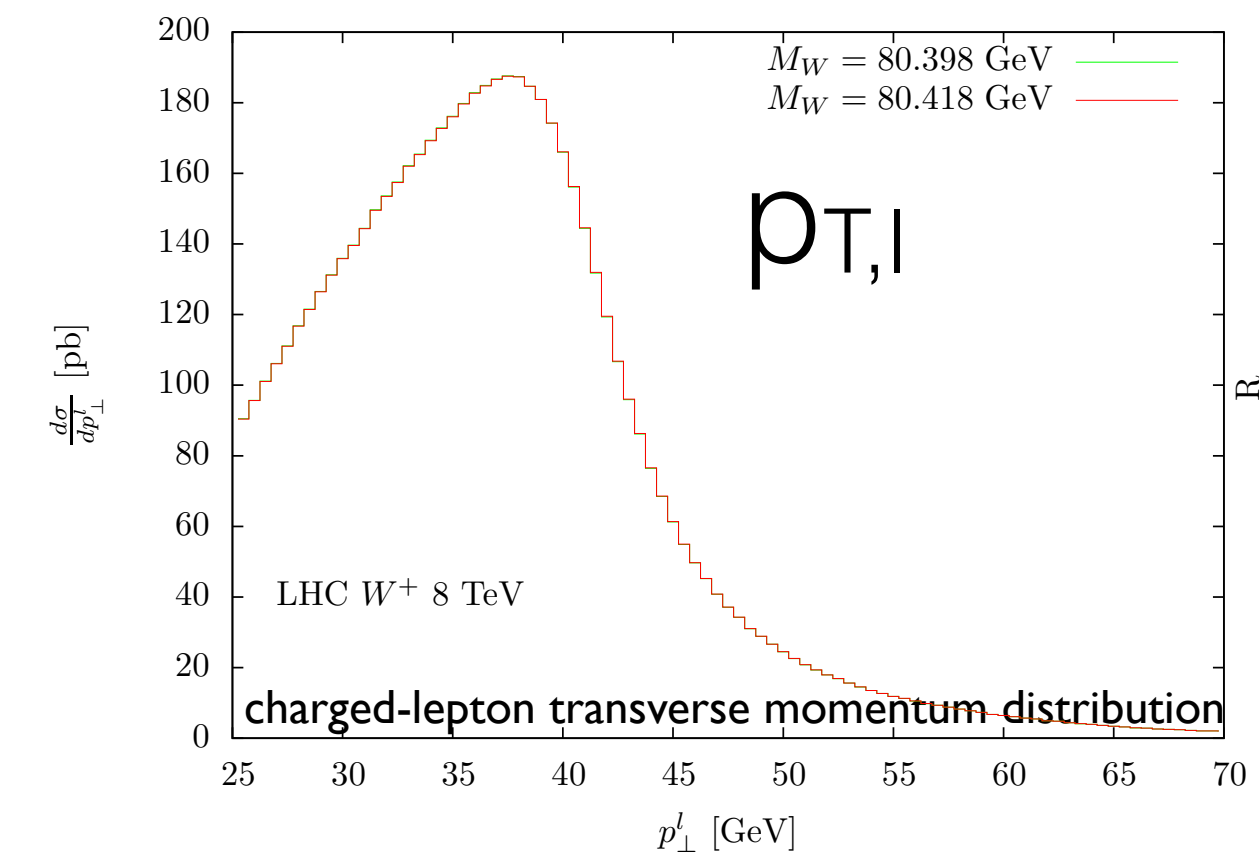
- Motivation: precise measurement of $M_W \rightarrow$ stringent test of SM!



M_W measurements (precision DY)

- Motivation: precise measurement of $M_W \rightarrow$ stringent test of SM!
- Method: **template fits** of sensitive CC DY distributions ($p_{T,l}$, M_T , E_{miss})

$$M_W = 80.385 \pm 0.015 \text{ GeV}$$

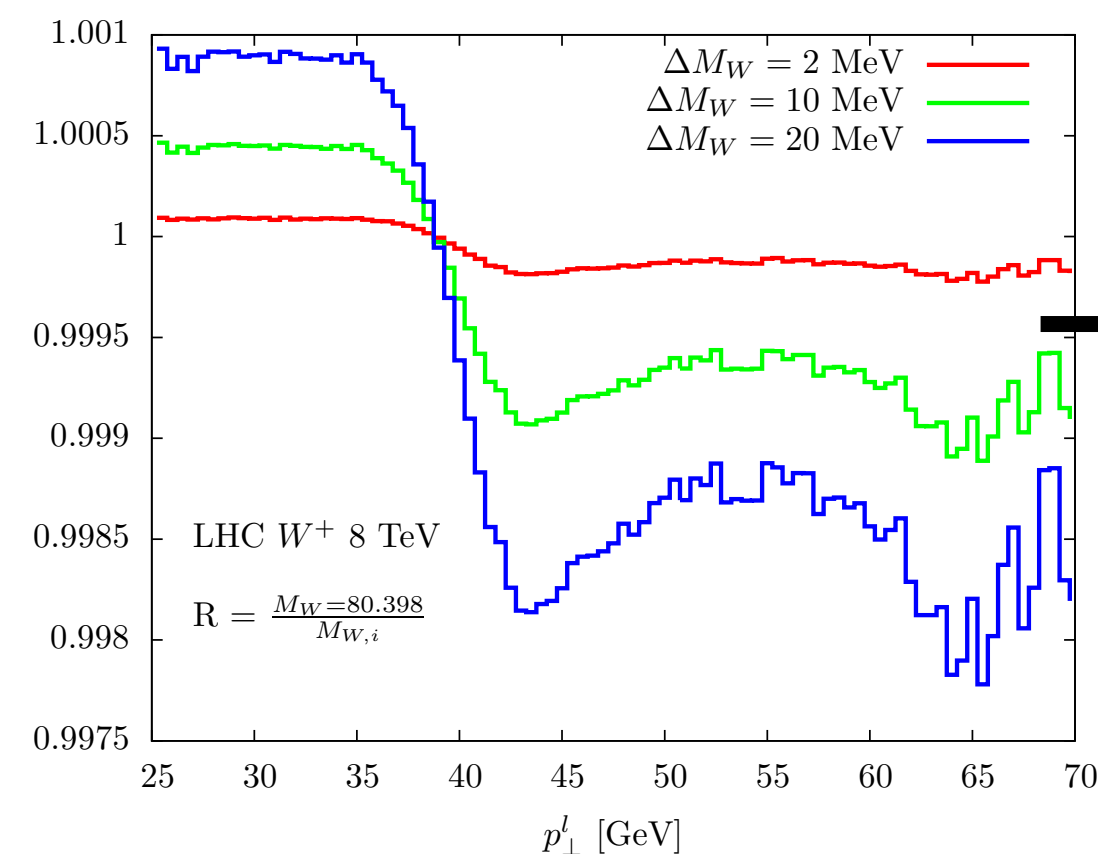
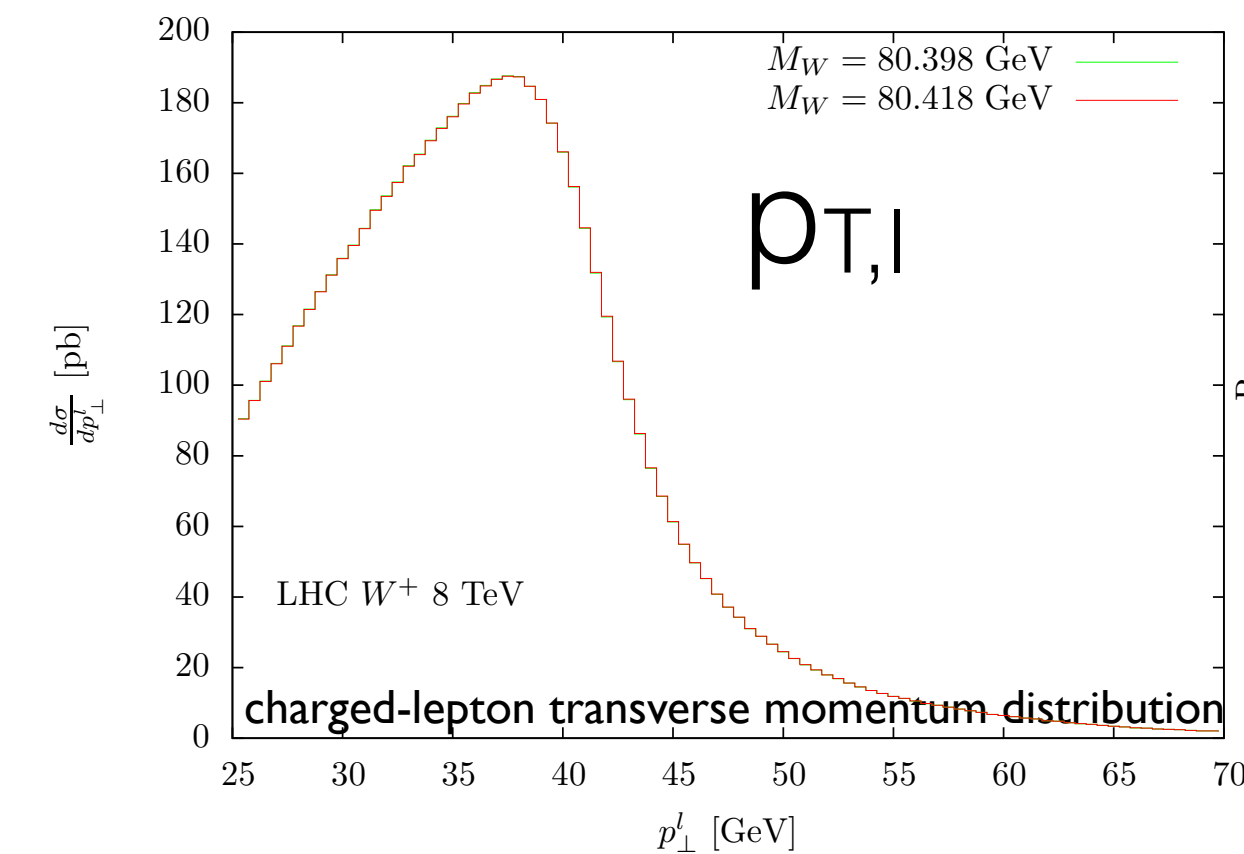


- Need to control shape effects at the sub-1% level!
- Normalization not relevant
- Dominant effects: **QCD** ISR and **QED** FSR

M_W measurements (precision DY)

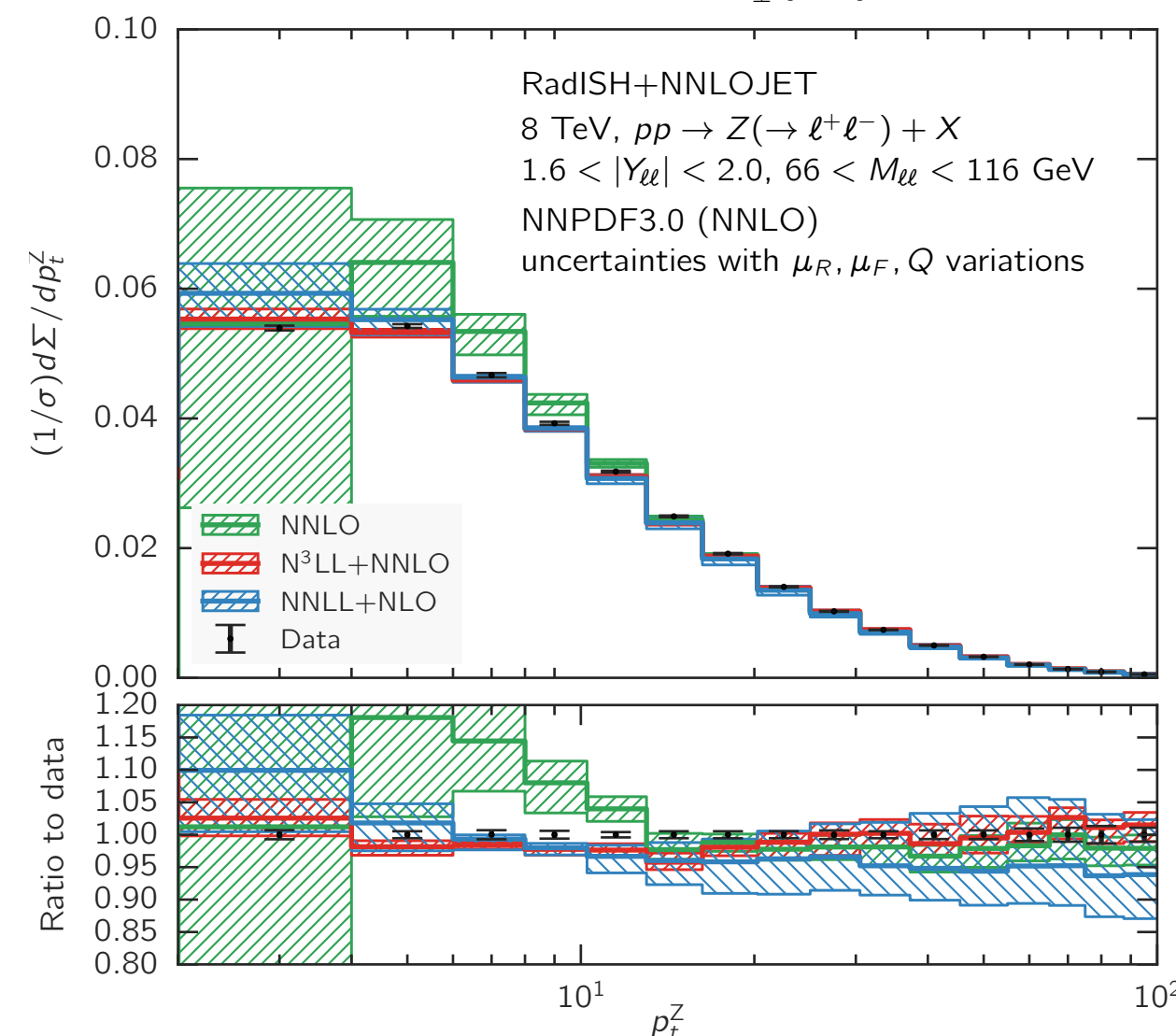
- Motivation: precise measurement of $M_W \rightarrow$ stringent test of SM!
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$$M_W = 80.385 \pm 0.015 \text{ GeV}$$



- Need to control shape effects at the sub-1% level!
- Normalization not relevant
- Dominant effects: **QCD** ISR and **QED** FSR

DY@NNLO+N3LL
[Bizon et. al. '18]

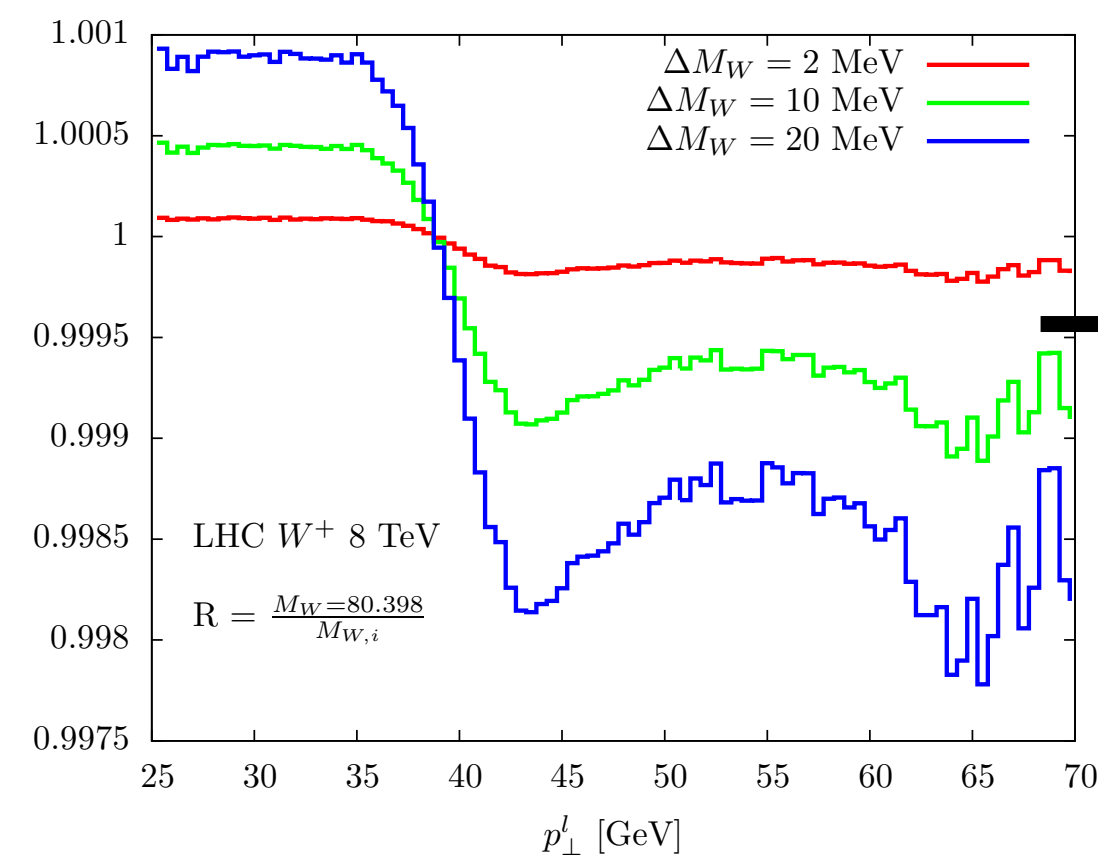
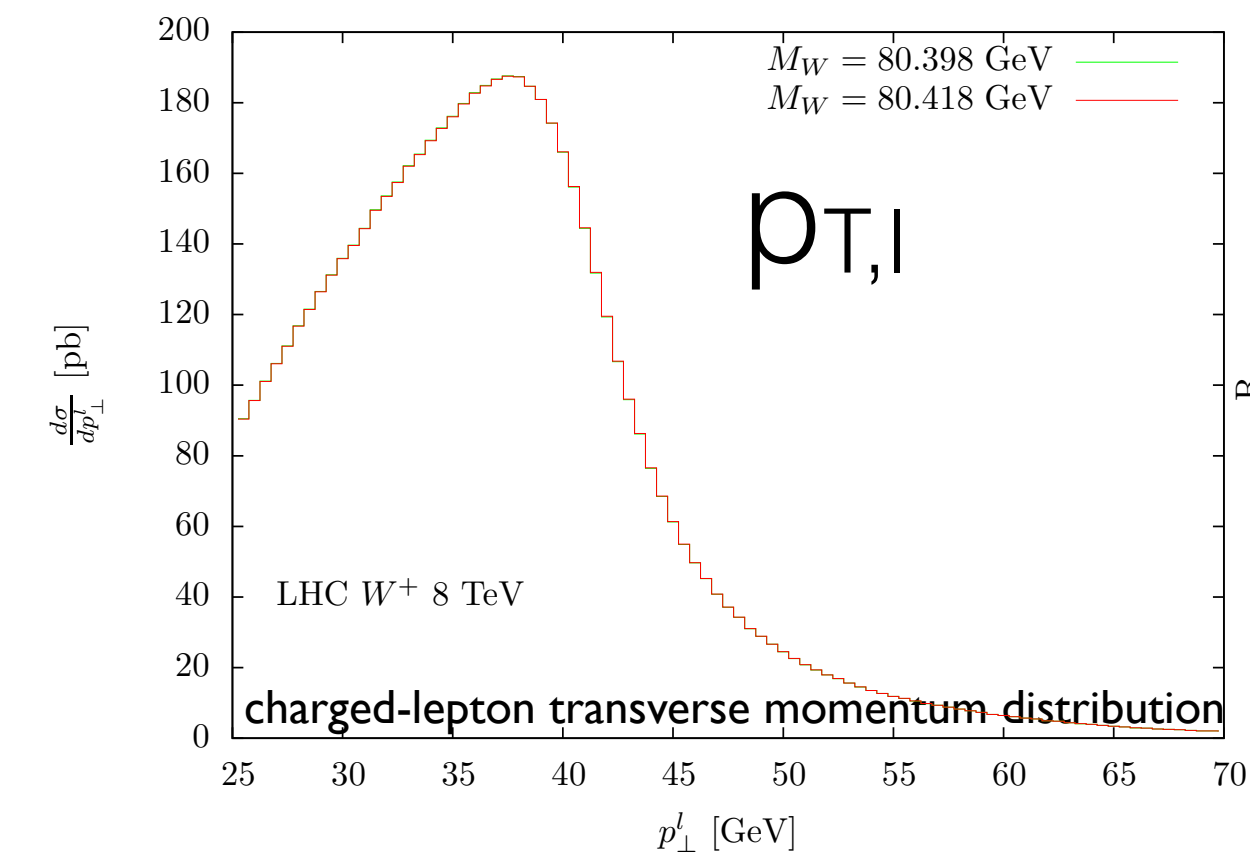


- Need to control W-pT spectrum at the sub-% level!
- Idea: use measurement of Z-pT to control W-pT
- Problem: precision in transfer-factor has to match experimental precision

M_W measurements (precision DY)

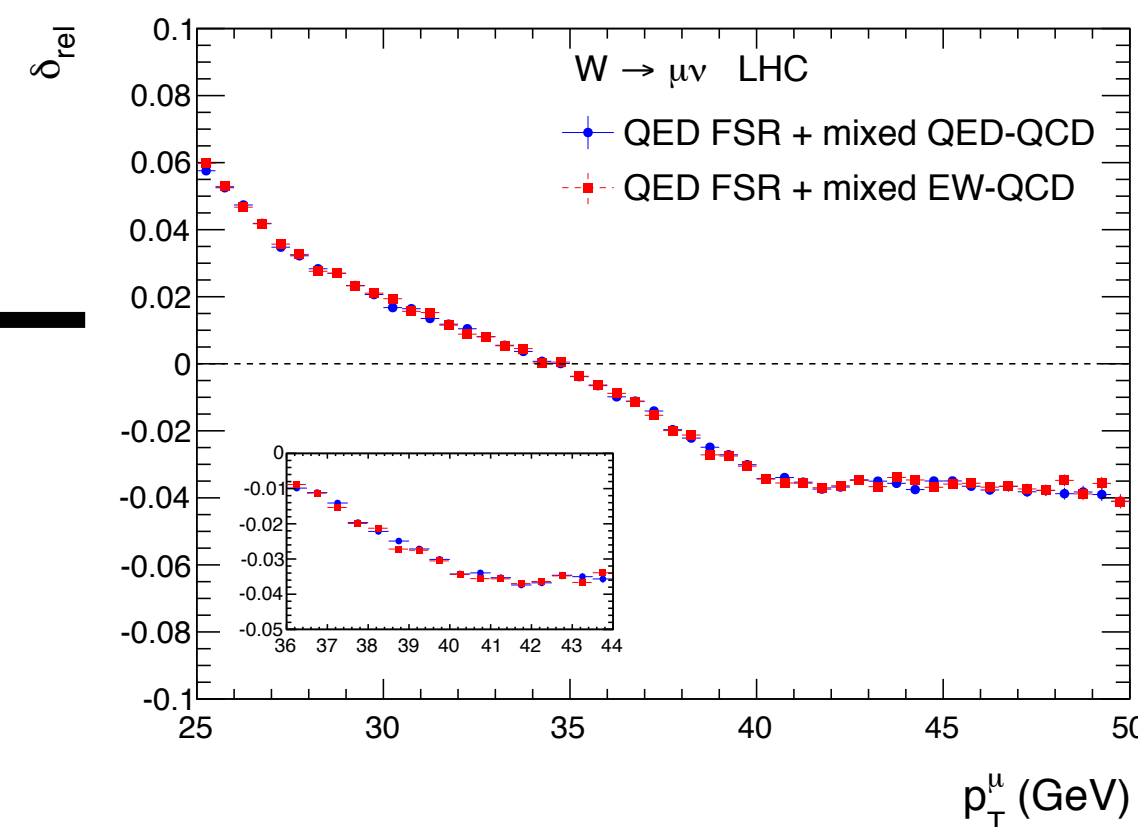
- Motivation: precise measurement of $M_W \rightarrow$ stringent test of SM!
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- Need to control shape effects at the sub-1% level!
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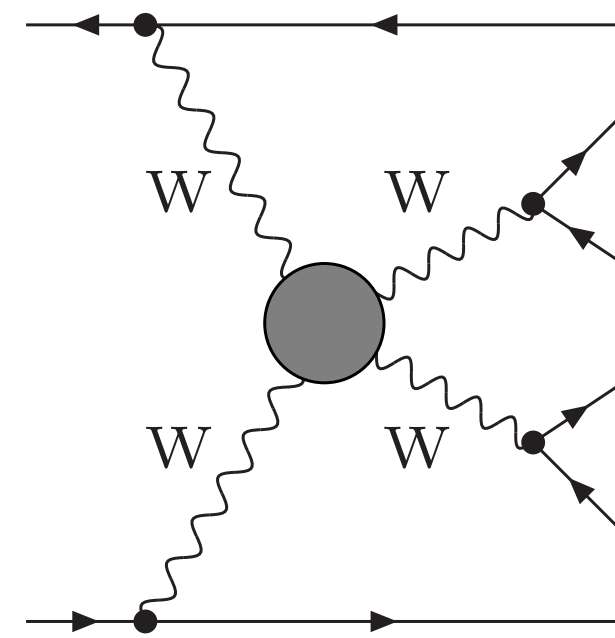
mixed **QCD**x**EW**
seems to be under
good control!



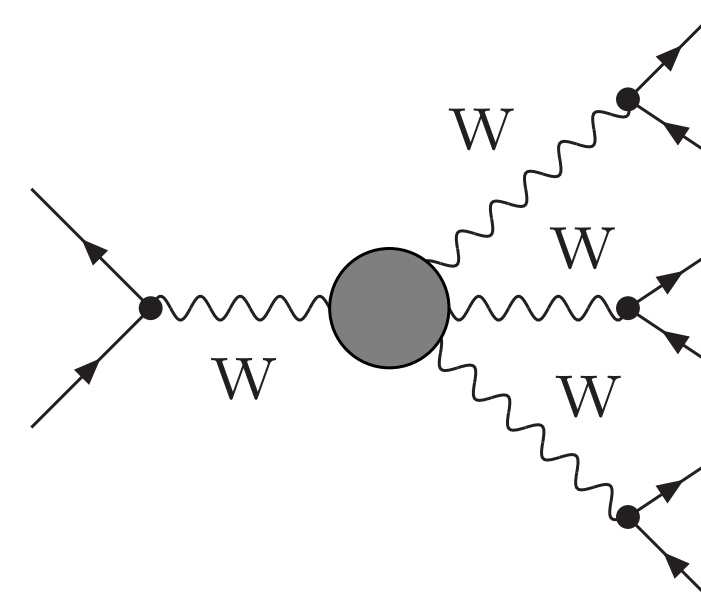
- new (resonance aware) POWHEG generators:
NLO+PS QCDxEW for CC/NC DY
- simultaneously **QED** and **QCD** radiation thanks
to multiplicative matching in POWHEG

[Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, Vicini; '16]

Rare EW processes

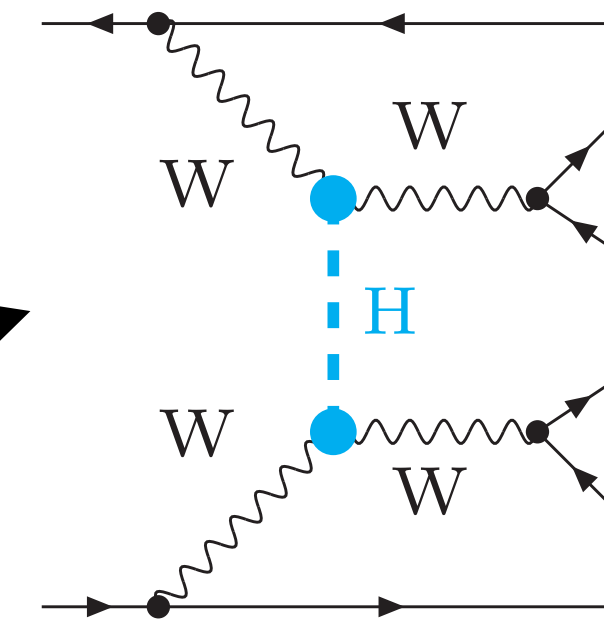


VBS



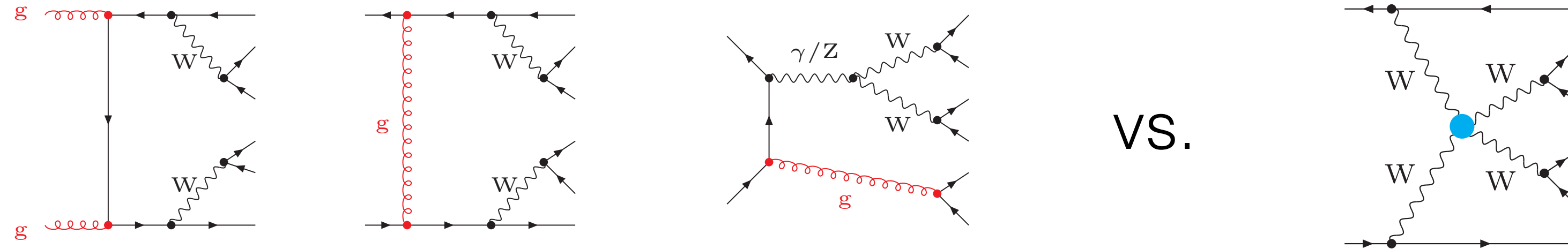
Triboson

- direct access to quartic EW gauge couplings
- VBS: longitudinal gauge bosons at high energies
- window to electroweak symmetry breaking via off-shell Higgs exchange



VBS

Note: severe QCD background to VBS signatures + interference:



$$d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots$$

LO

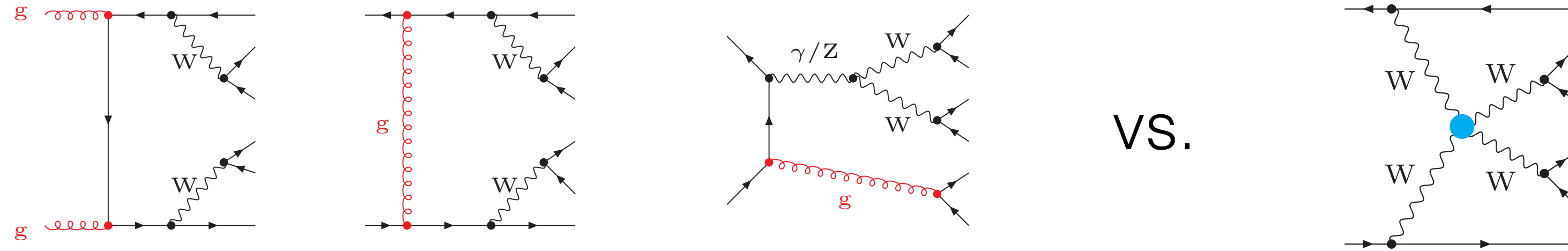
QCD-background

interference

VBS-signal

VBS

Note: severe QCD background to VBS signatures + interference:



VS.

$$d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots$$

LO

QCD-background

interference

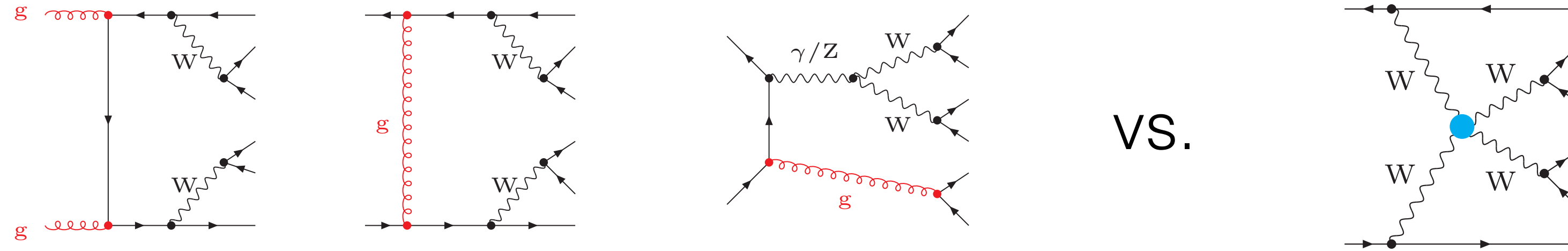
VBS-signal

$$\dots + d\sigma(\alpha_S^3 \alpha^4) + d\sigma(\alpha_S^2 \alpha^5) + d\sigma(\alpha_S \alpha^6) + \sigma(\alpha^7)$$

NLO

VBS

Note: severe QCD background to VBS signatures + interference:



$$d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots \quad \text{LO}$$

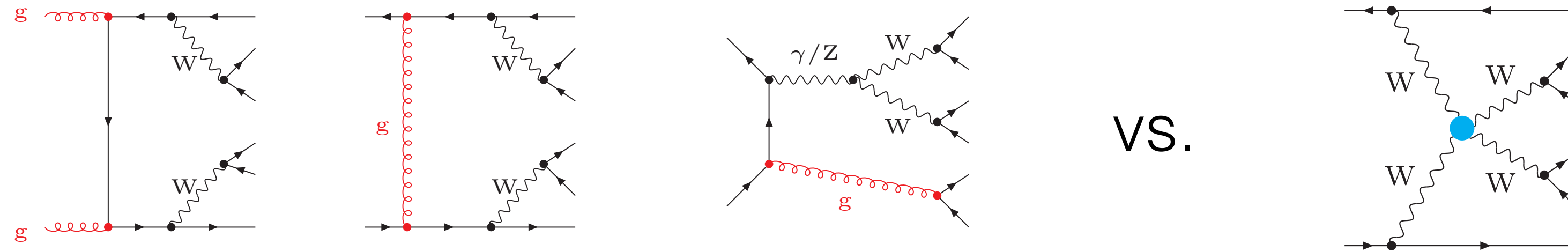
The diagram illustrates the expansion of a cross-section to NLO order. It shows the following terms and their associated orders:

- $\cdots + d\sigma(\alpha_S^3 \alpha^4)$: Labeled "NLO QCD" (red text). An arrow from "QCD-background" points to this term, with $\mathcal{O}(\alpha_s)$ written next to the arrow.
- $+ d\sigma(\alpha_S^2 \alpha^5)$: Labeled "NLO EW" (blue text). An arrow from "interference" points to this term, with $\mathcal{O}(\alpha)$ written next to the arrow.
- $+ d\sigma(\alpha_S \alpha^6)$: Labeled "NLO QCD" (red text). An arrow from "VBS-signal" points to this term, with $\mathcal{O}(\alpha_s)$ written next to the arrow.
- $+ \sigma(\alpha^7)$: Labeled "NLO EW" (blue text). An arrow from "VBS-signal" points to this term, with $\mathcal{O}(\alpha)$ written next to the arrow.

The overall result is labeled "NLO" on the right.

VBS

Note: severe QCD background to VBS signatures + interference:



VS.

$$d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots$$

LO

QCD-background

interference

VBS-signal

$\mathcal{O}(\alpha_S)$

$\mathcal{O}(\alpha)$

$$\dots + d\sigma(\alpha_S^3 \alpha^4) + d\sigma(\alpha_S^2 \alpha^5) + d\sigma(\alpha_S \alpha^6) + \sigma(\alpha^7)$$

NLO

“NLO QCD”

“NLO EW”

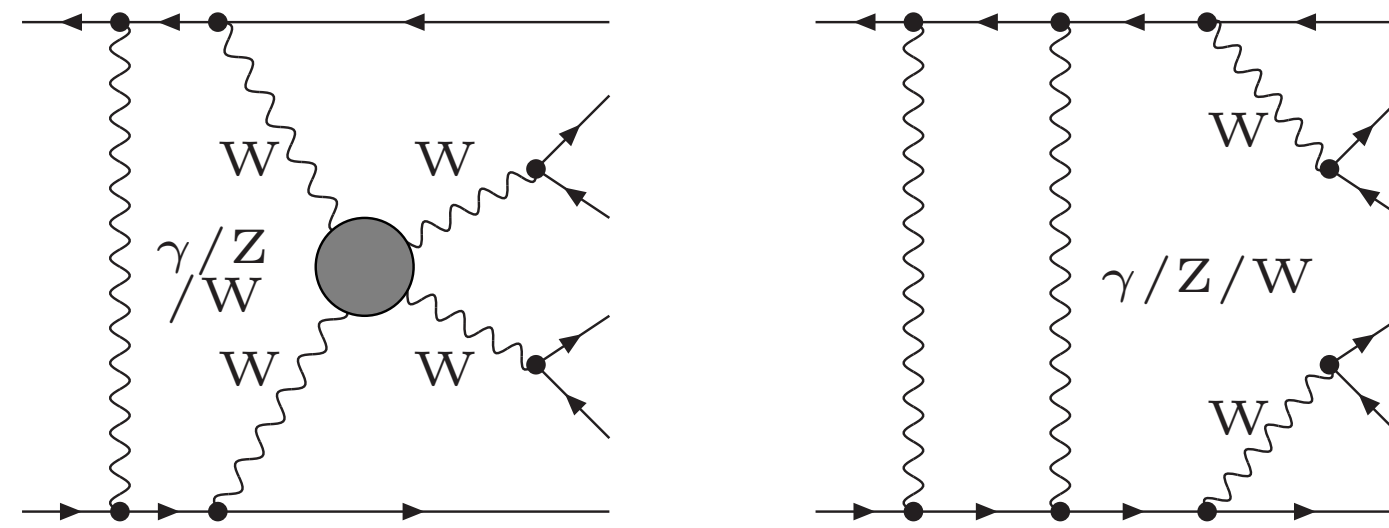
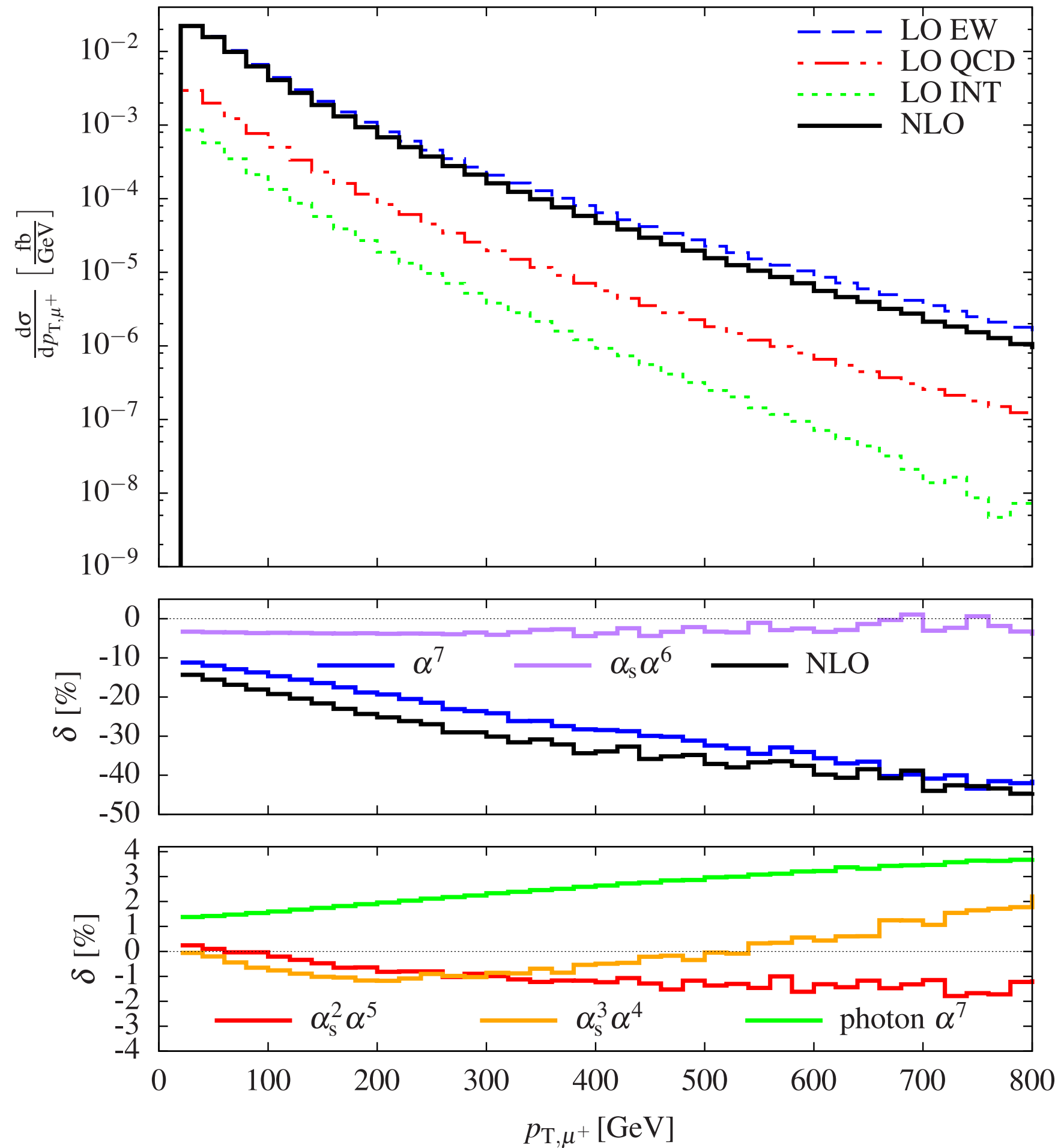
“NLO QCD”

“NLO EW”

➡ separation meaningless at NLO

VBS: $W^+W^++2\text{jets}$ @ full NLO

[Biedermann, Denner, Pellen '16+'17]



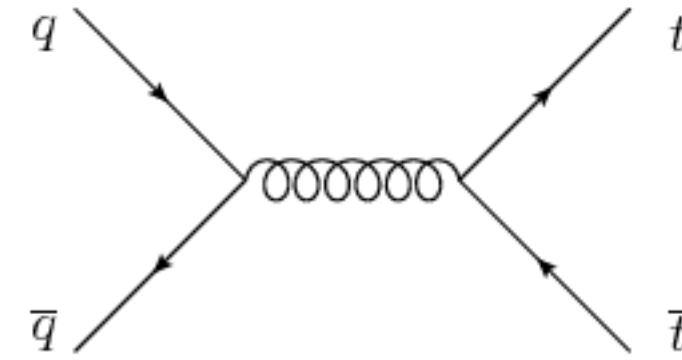
$2 \rightarrow 6$ particles at NLO EW !

- NLO corrections dominated by α^7 :

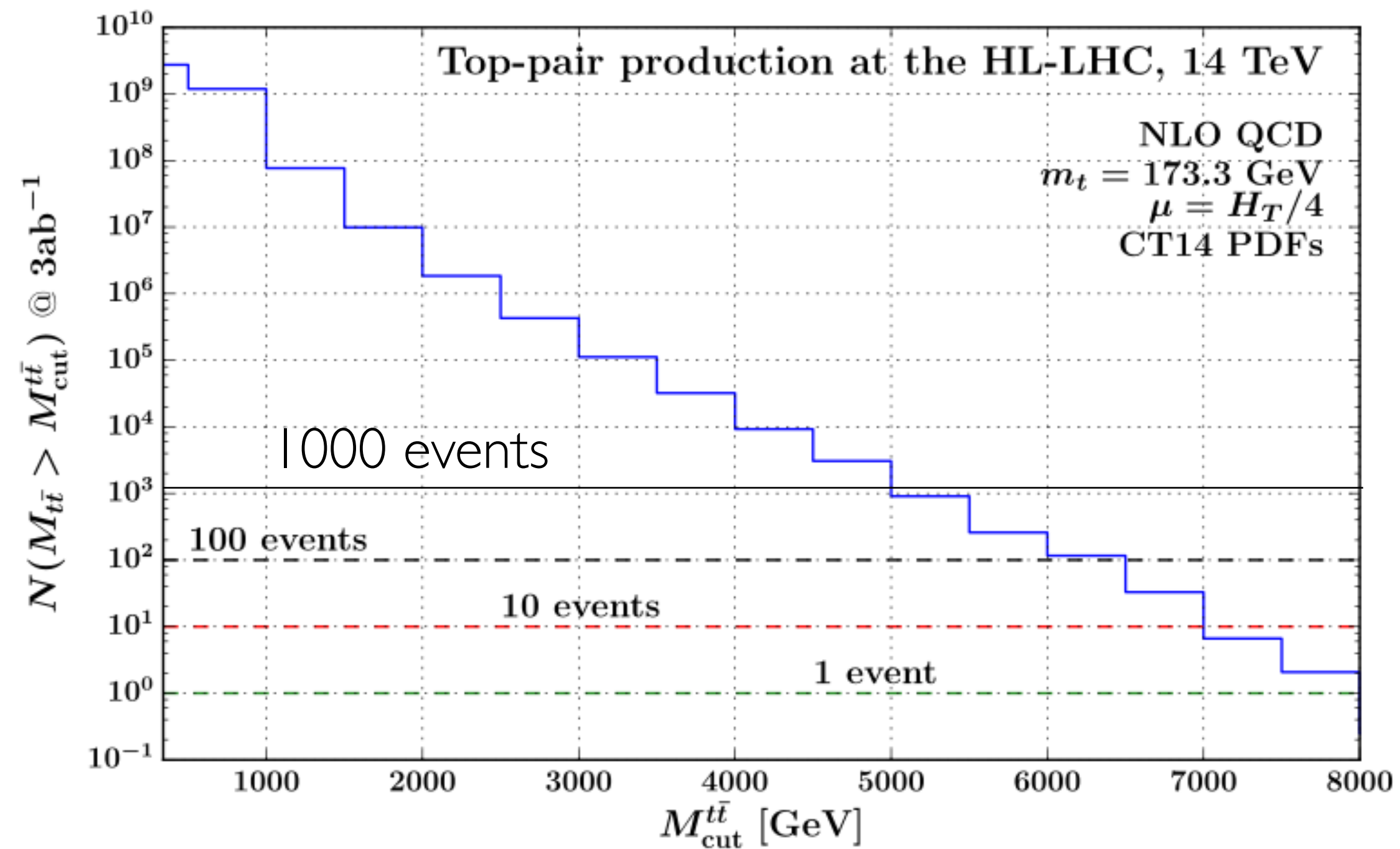
| Order | $\mathcal{O}(\alpha^7)$ | $\mathcal{O}(\alpha_s \alpha^6)$ | $\mathcal{O}(\alpha_s^2 \alpha^5)$ | $\mathcal{O}(\alpha_s^3 \alpha^4)$ | Sum |
|--|-------------------------|----------------------------------|------------------------------------|------------------------------------|------------|
| $\delta\sigma_{\text{NLO}}$ [fb] | -0.2169(3) | -0.0568(5) | -0.00032(13) | -0.0063(4) | -0.2804(7) |
| $\delta\sigma_{\text{NLO}}/\sigma_{\text{LO}}$ [%] | -13.2 | -3.5 | 0.0 | -0.4 | -17.1 |

with $M_{jj} > 500 \text{ GeV}$, $p_{T,j} > 30 \text{ GeV}$, $p_{T,\ell} > 20 \text{ GeV}$,

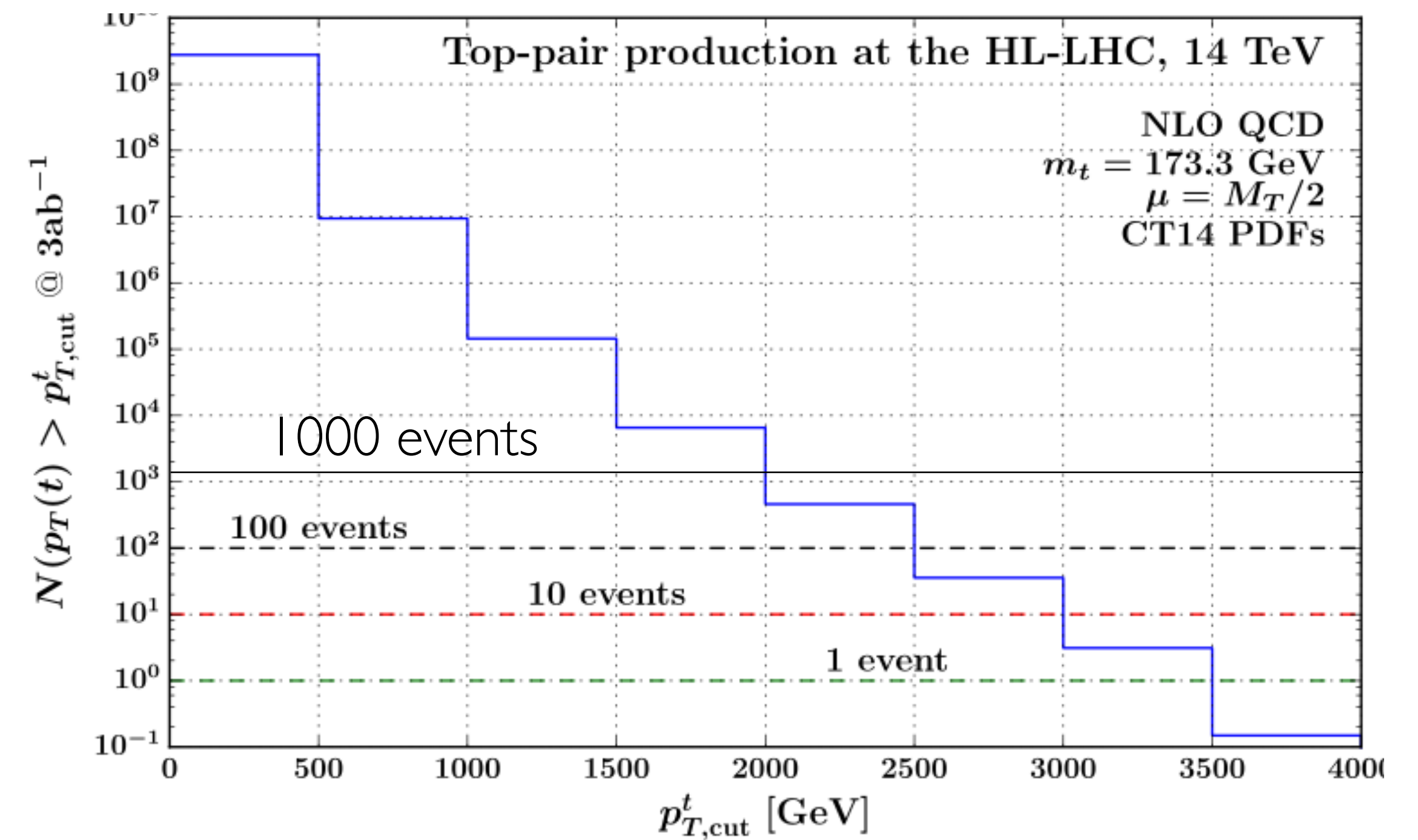
Precision Top physics



[M. Zaro, HL/HE LHC workshop, June 2018]



- 1-10% precision for $M_{t\bar{t}}=5000\text{-}6000 \text{ GeV}$



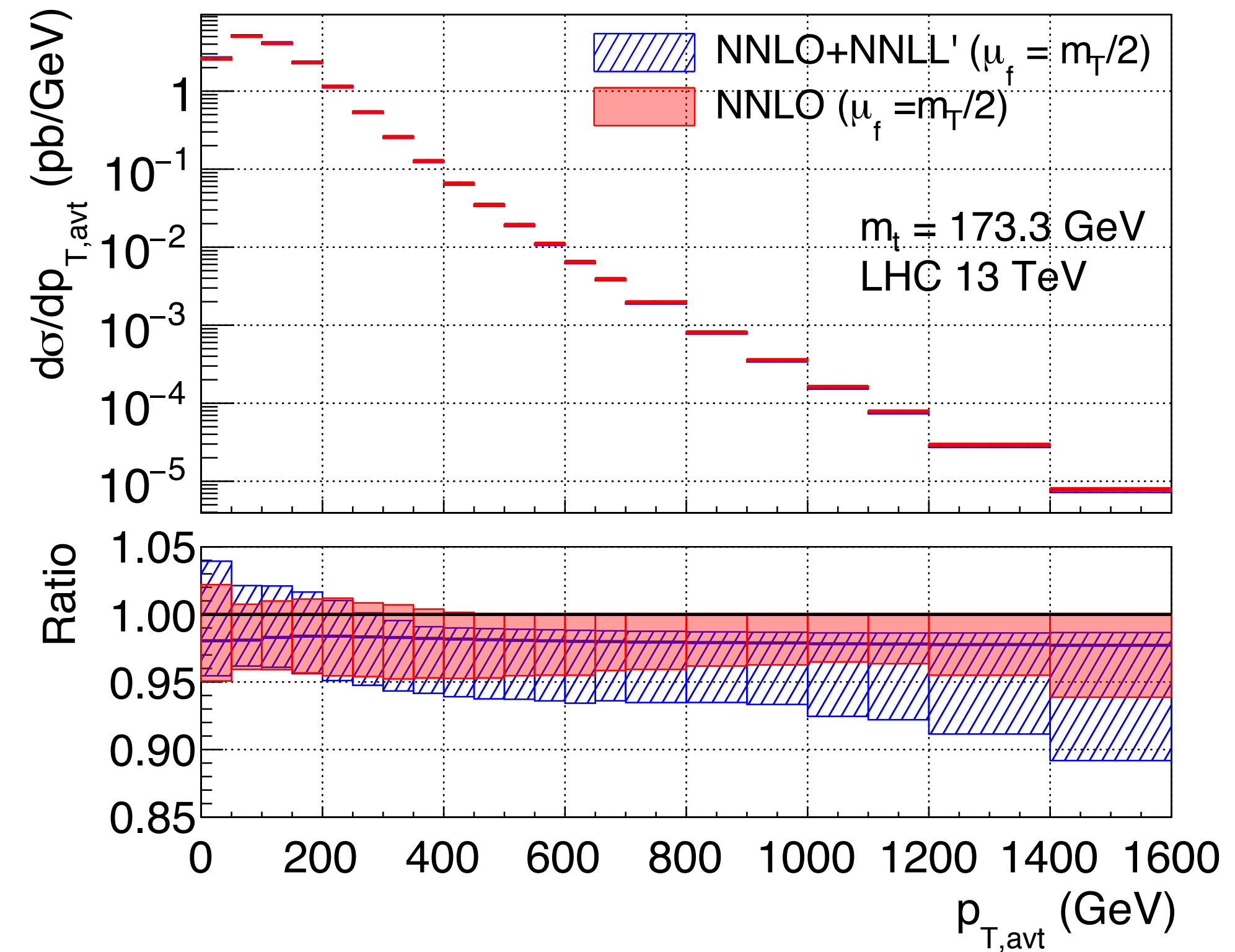
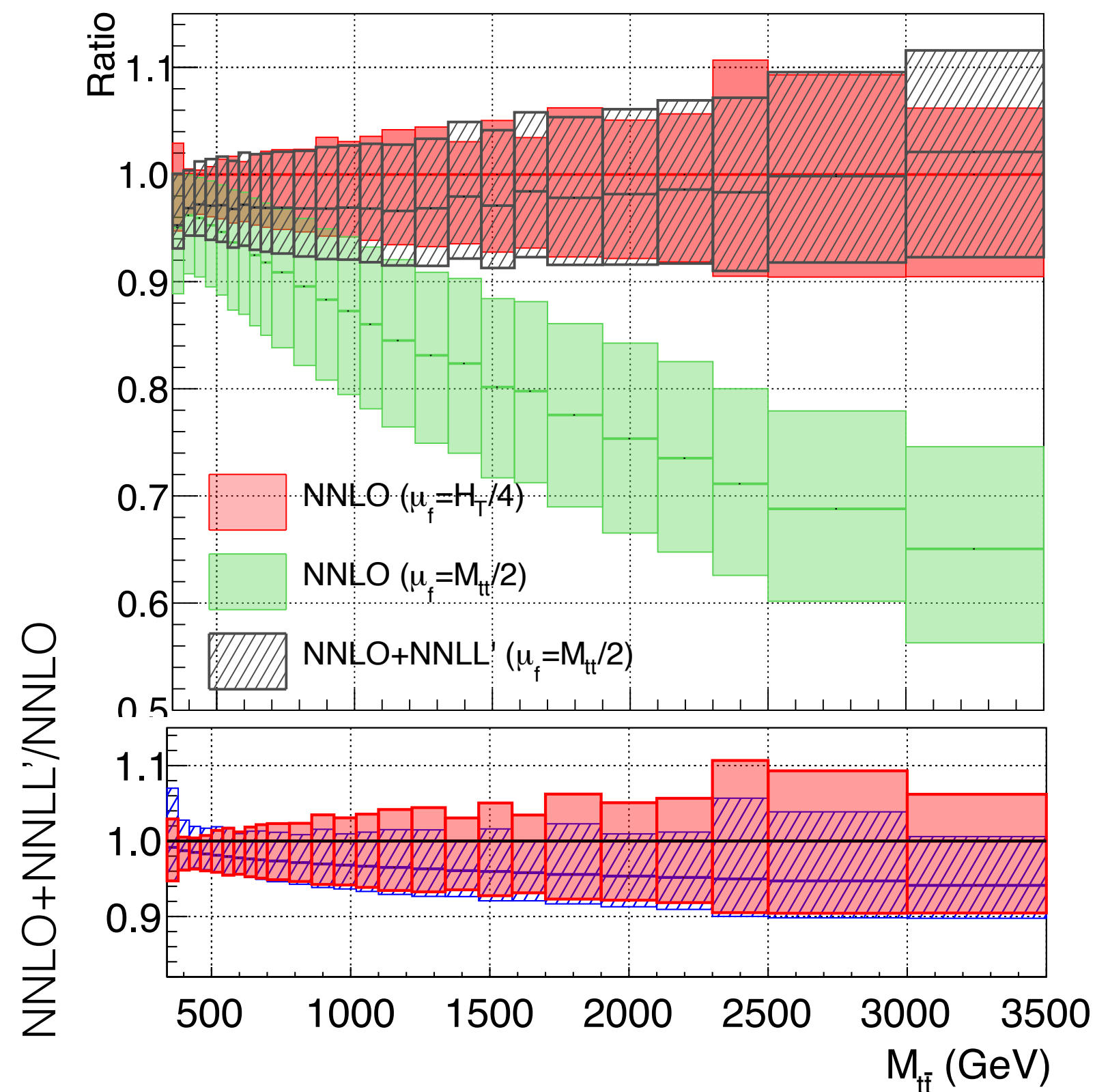
- 1-10% precision for $p_{T_{\text{top}}}=2000\text{-}2500 \text{ GeV}$

Precision Top physics

- 1-10% precision for $M_{t\bar{t}}=5000-6000$ GeV

- 1-10% precision for $pT_{top}=2000-2500$ GeV

NNLO+NNLL' for top-pair production [Czakon et. al., '18]



- most relevant hard scale is not $M_{t\bar{t}}$ itself but rather H_T
- remaining scale uncertainties at the level of 5%

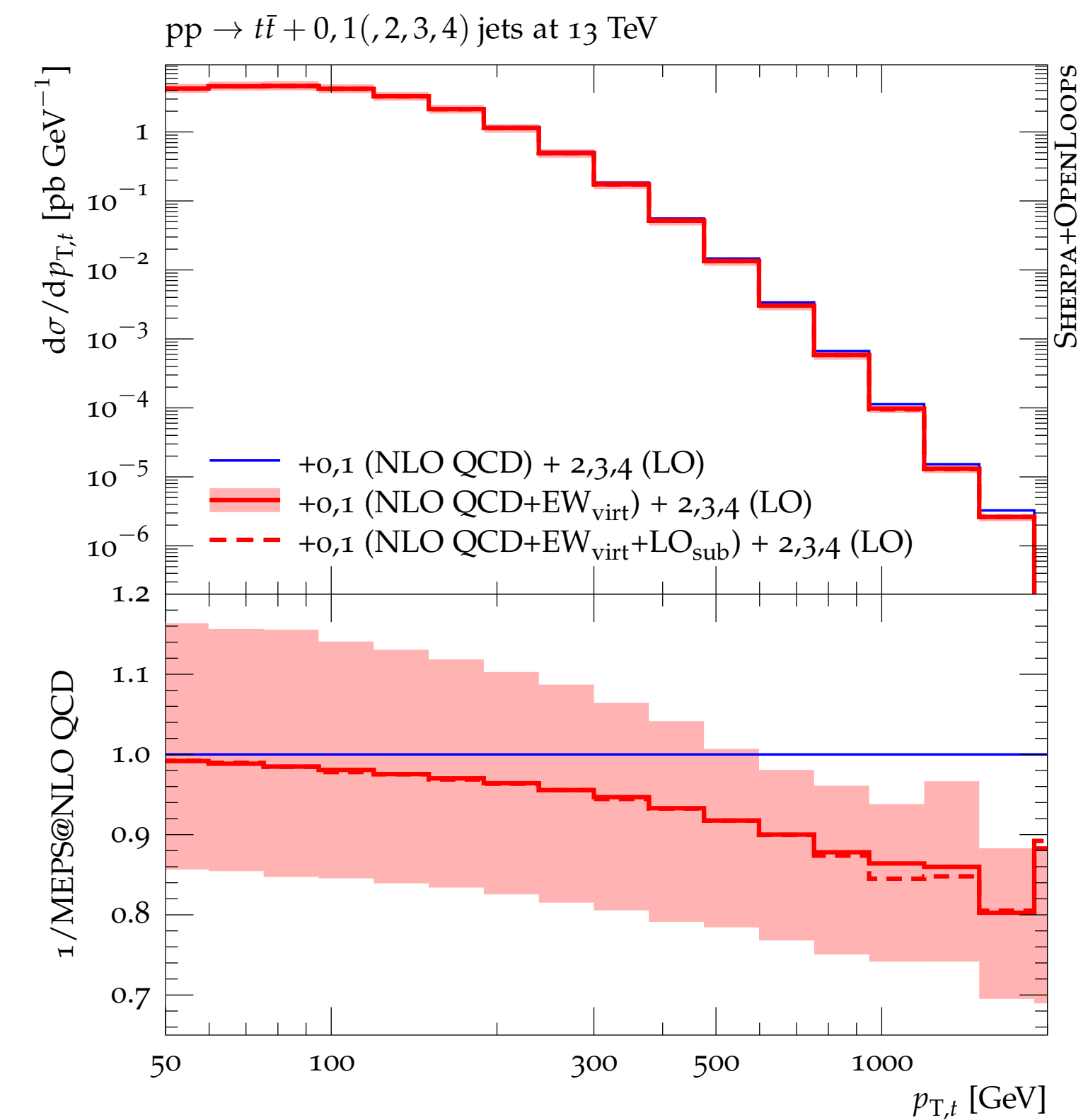
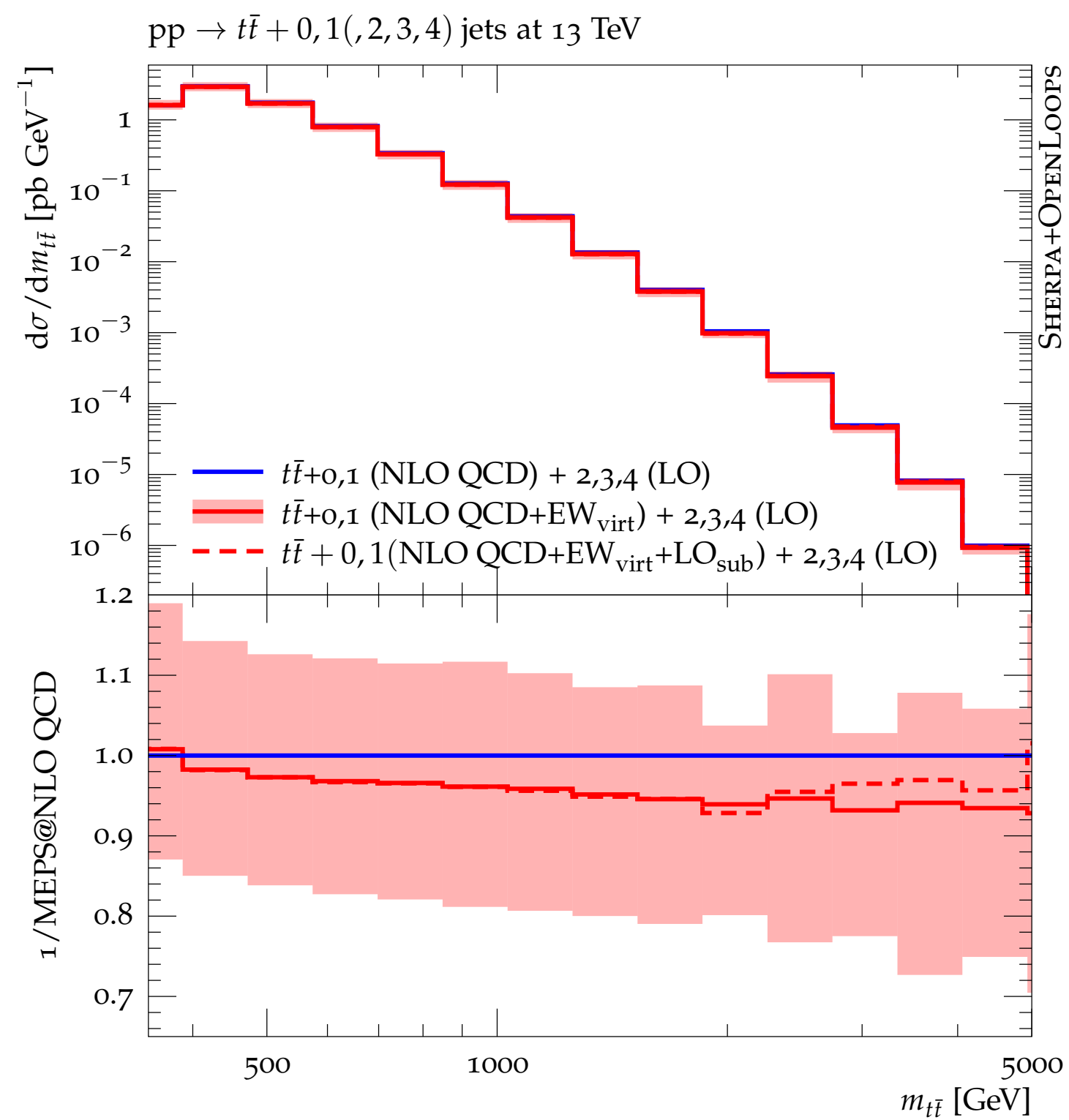
- remaining scale uncertainties in the tail at the level of 5-10%

Precision Top physics

- 1-10% precision for $M_{t\bar{t}}=5000-6000$ GeV

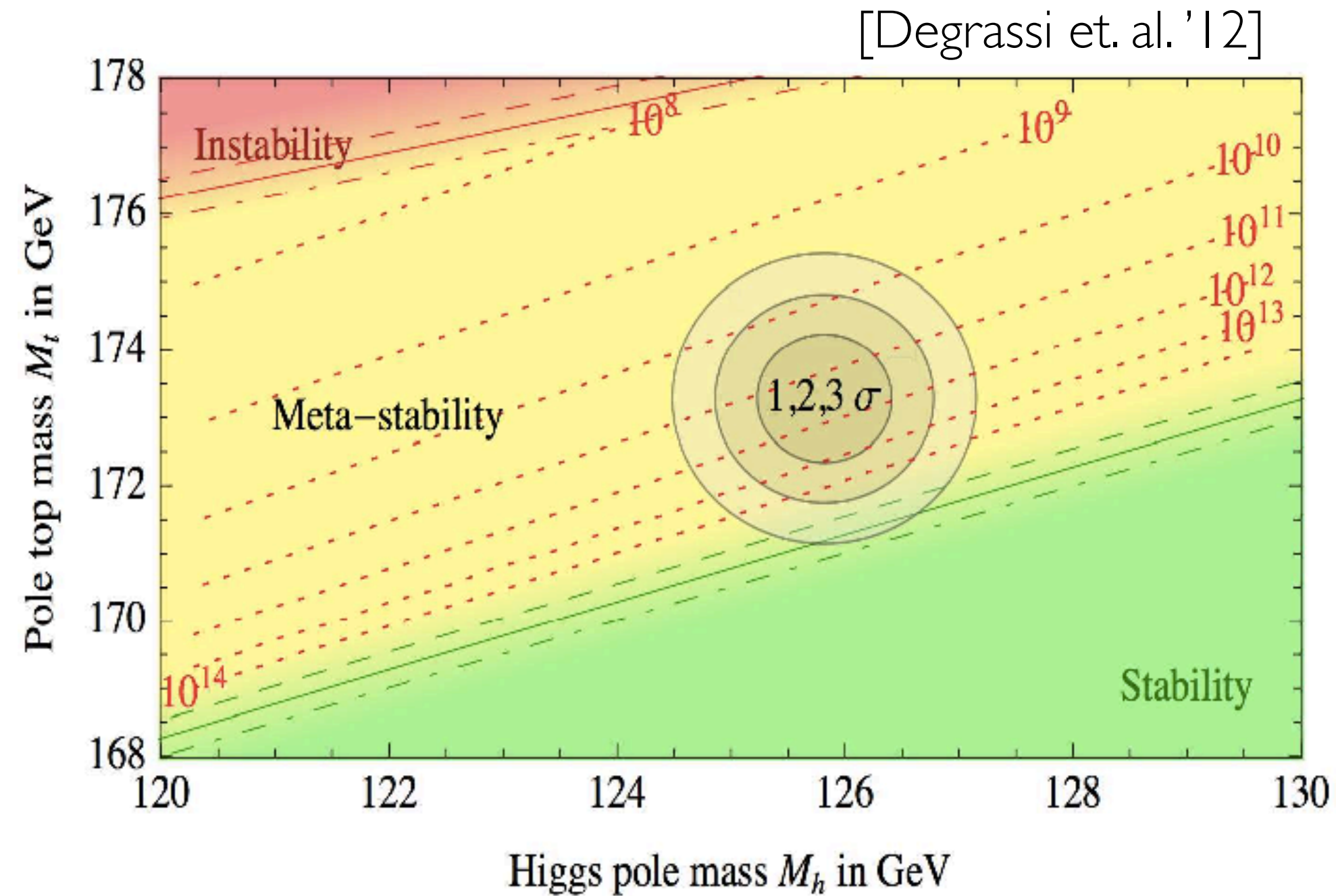
- 1-10% precision for $p_{T,\text{top}}=2000-2500$ GeV

MEPS@NLO QCD+EW_{virt} 0,1 jets merged [Gütschow, JML, Schönherr, '18]

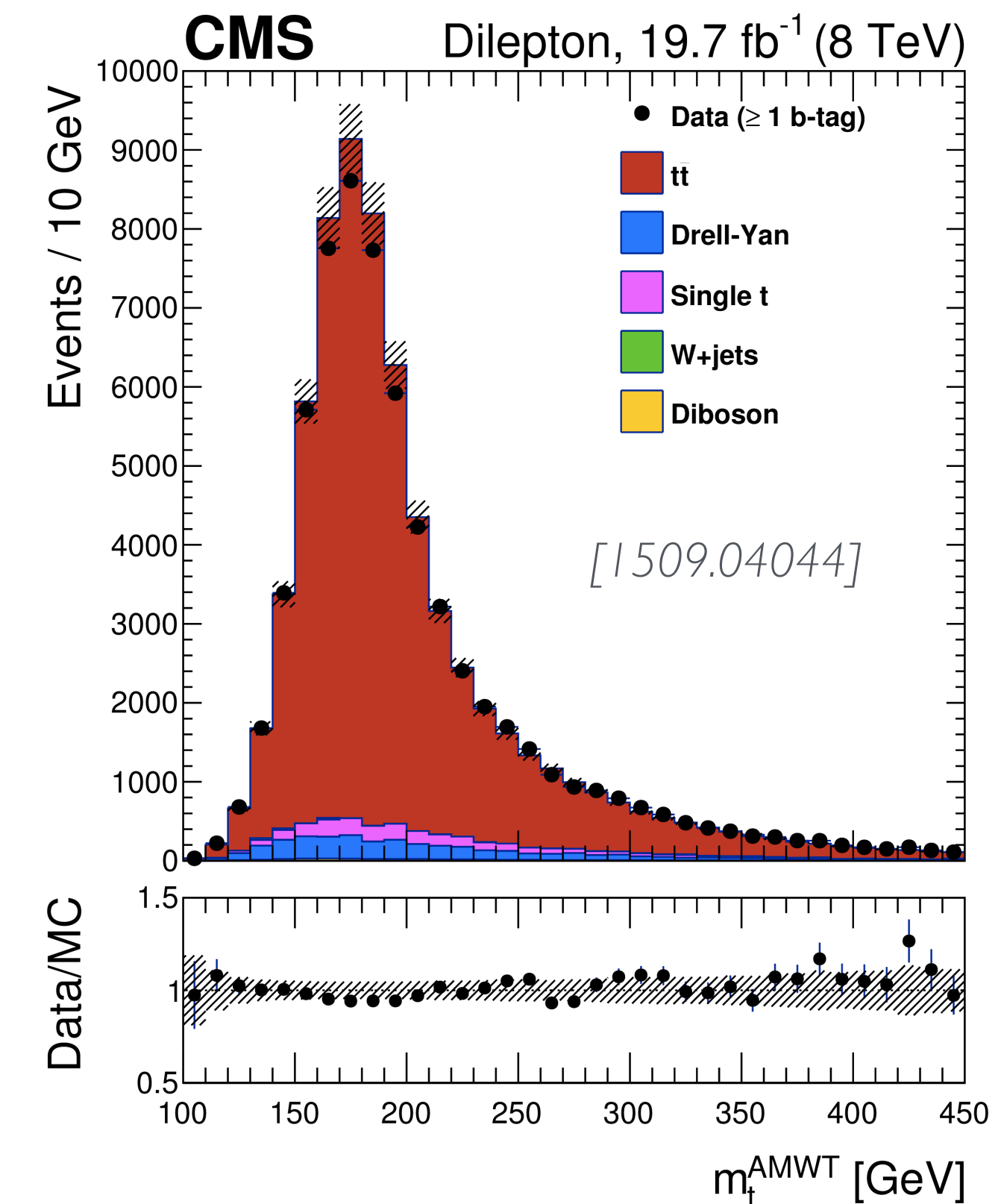


Top-mass

reconstruction using analytical distributions
derived from simulated samples



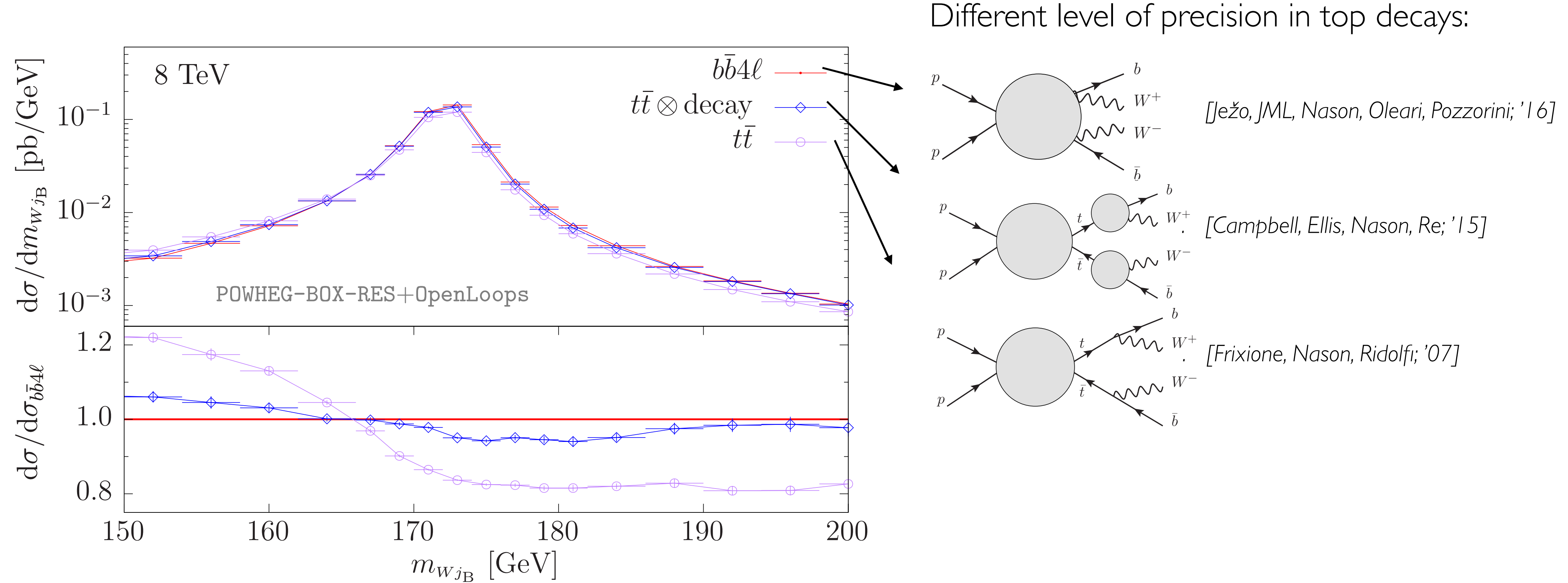
- precise value of top mass crucial for stability of EW vacuum



$$m_{\text{top}} = 172.82 \pm 0.19 \text{ (stat)} \pm 1.22 \text{ (syst)} \text{ GeV}$$

- kinematic measurements strongly rely on MC modelling!
- these are based on on-shell $t\bar{t}$ production @ NLO + LO decays
- what about **NLO in decay and off-shell effects**?

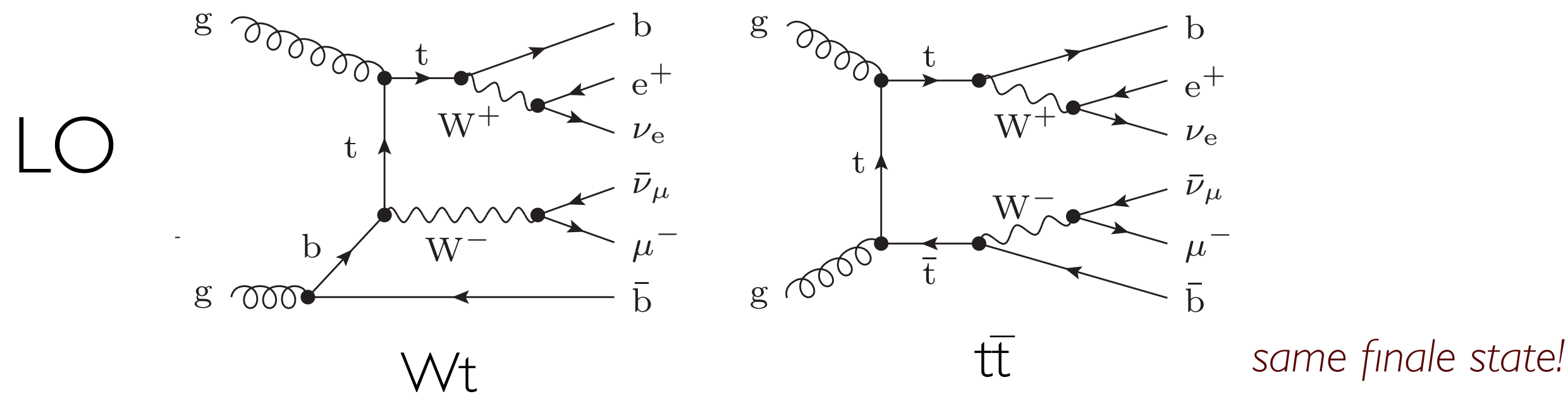
Reconstructed top-quark mass at NLO+PS



- significant shape distortions around resonance with respect to on-shell $t\bar{t}$ calculation
- very relevant for top mass determination
 - ★ average m_{Wj_B} roughly 500 MeV smaller in on-shell $t\bar{t}$ (in ± 30 GeV around m_{top})
- very good agreement (mostly $< 5\%$) level between $b\bar{b}4\ell$ and $t\bar{t} \otimes \text{decay}$
 - ◆ average m_{Wj_B} roughly 100 MeV smaller in $t\bar{t} \otimes \text{decay}$ (in ± 30 GeV around m_{top})

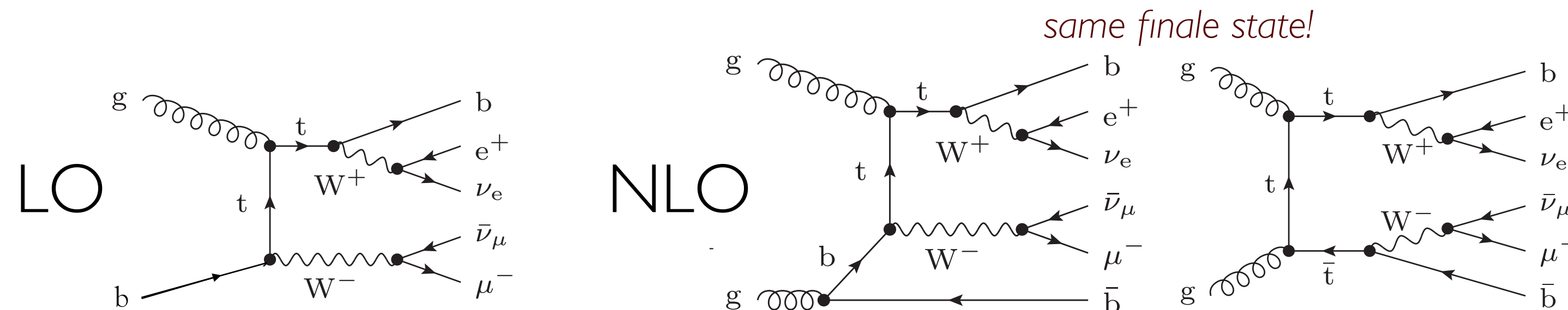
Interplay between top-pair and Wt single-top production

4FS

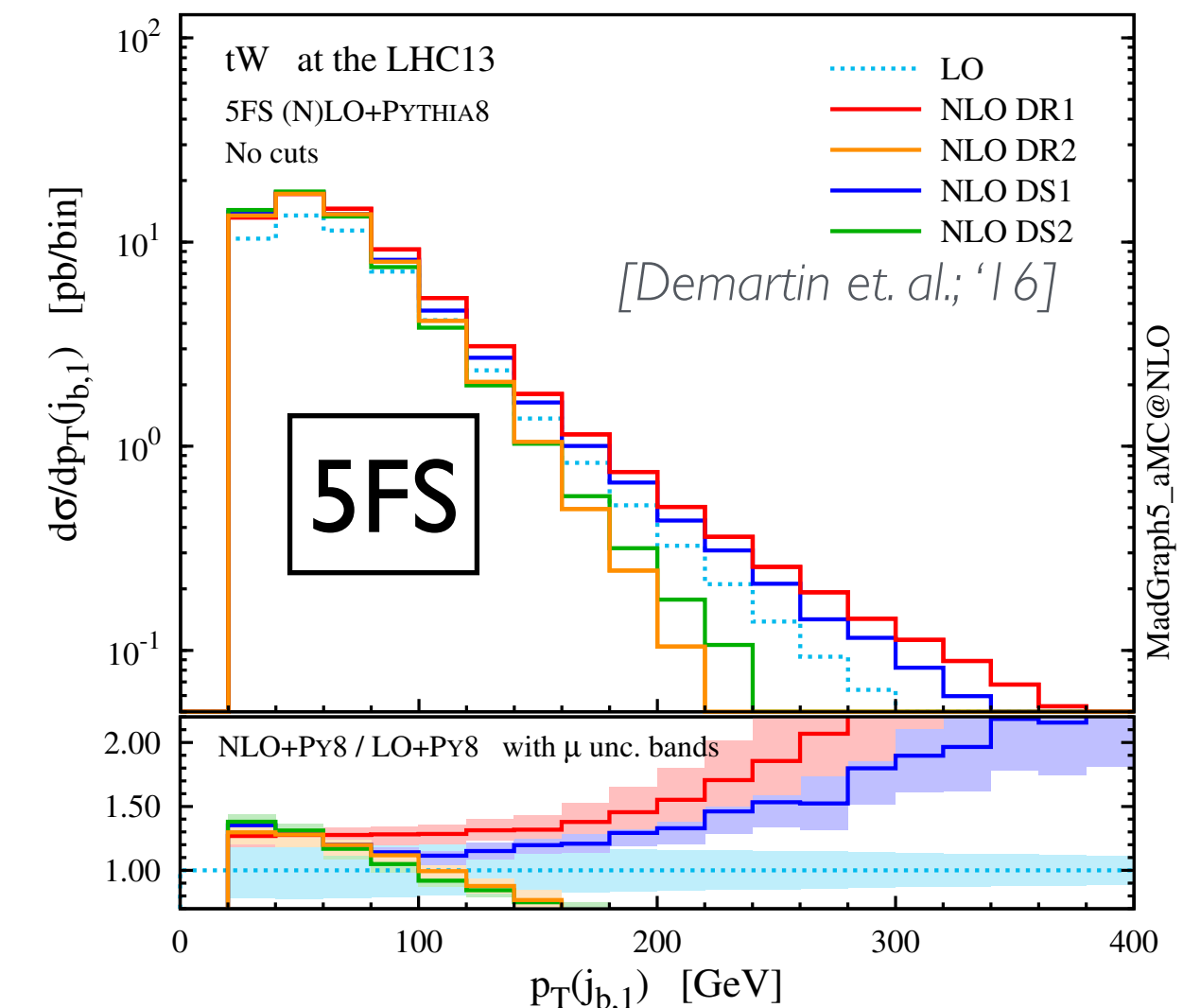


- unified treatment of top-pair and Wt including **interference**
- Wt enhanced in phase-space regions where one b becomes unresolved/vetoed
- requires off-shell WWbb calculation (with massive b's)

5FS

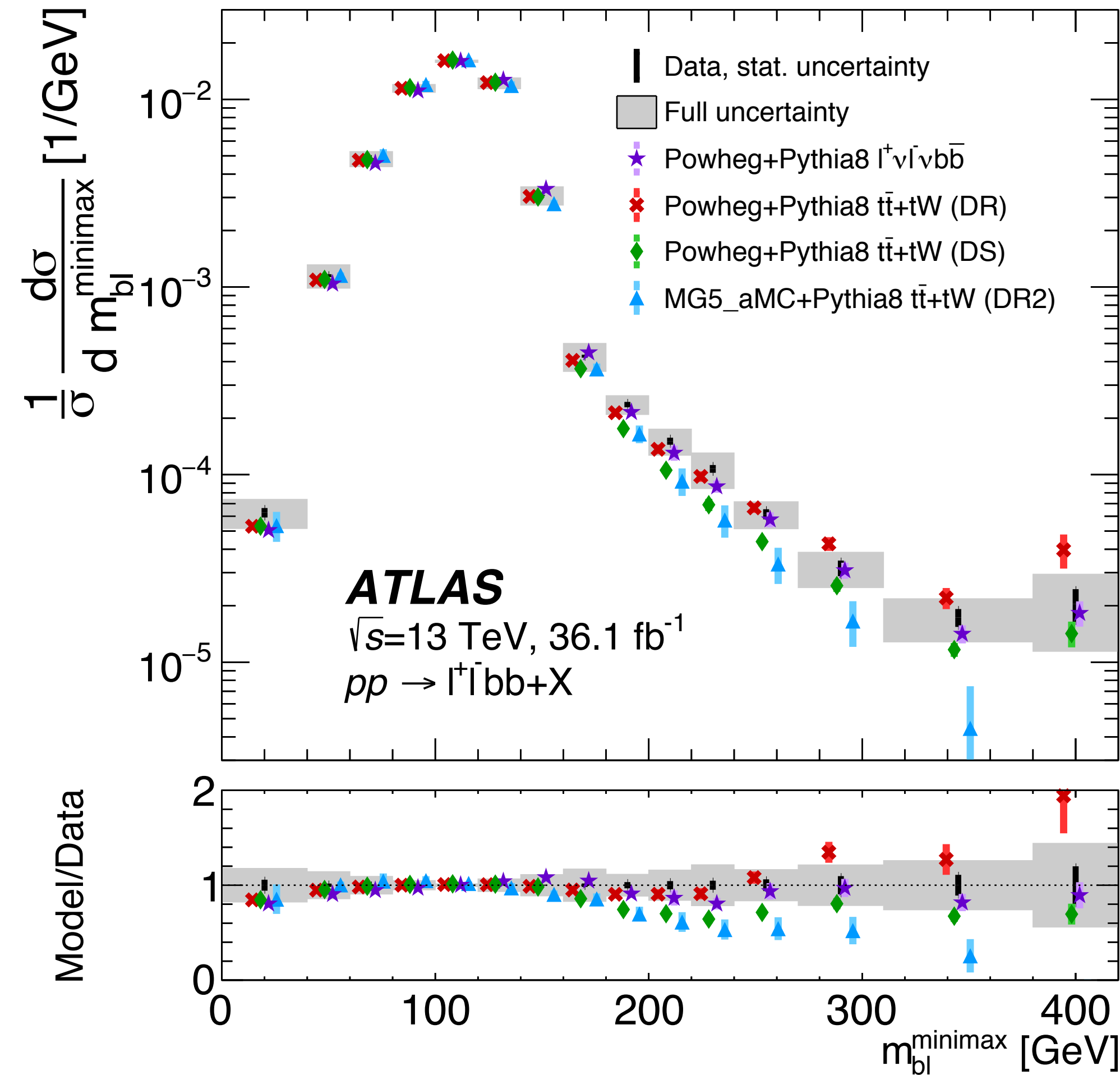


- NLO corrections to Wt swamped by LO $t\bar{t}$ decay
- requires ad-hoc subtraction prescription: DRI, DRII, DSI, DSII
- NLO+PS for Wt available in MC@NLO [Frixione, et. al.; '08], POWHEG [Re; '11] and Madgraph_aMC@NLO [Demartin et. al.; '16]



Interplay between top-pair and Wt single-top production

[CERN-EP-2018-087]



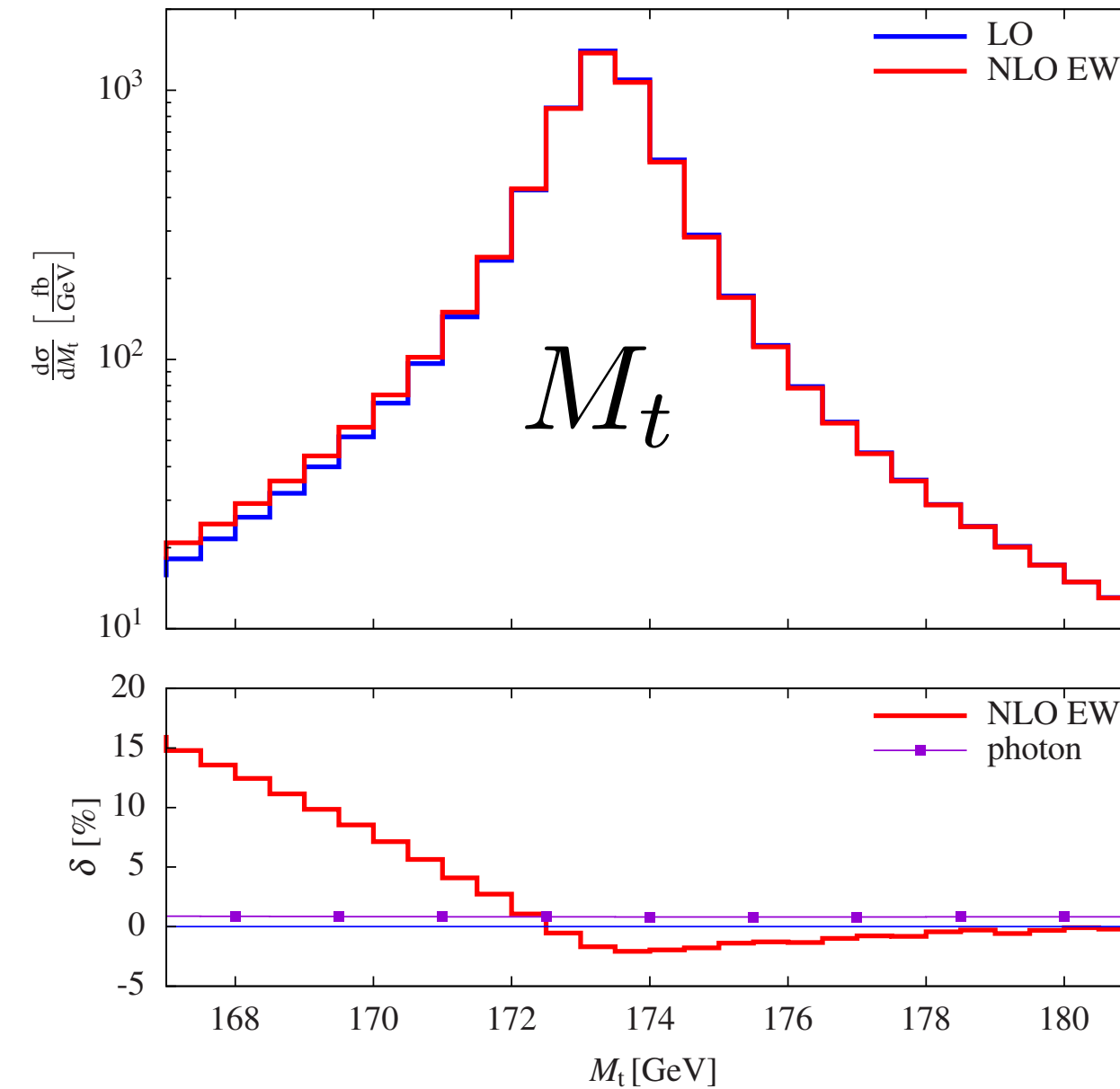
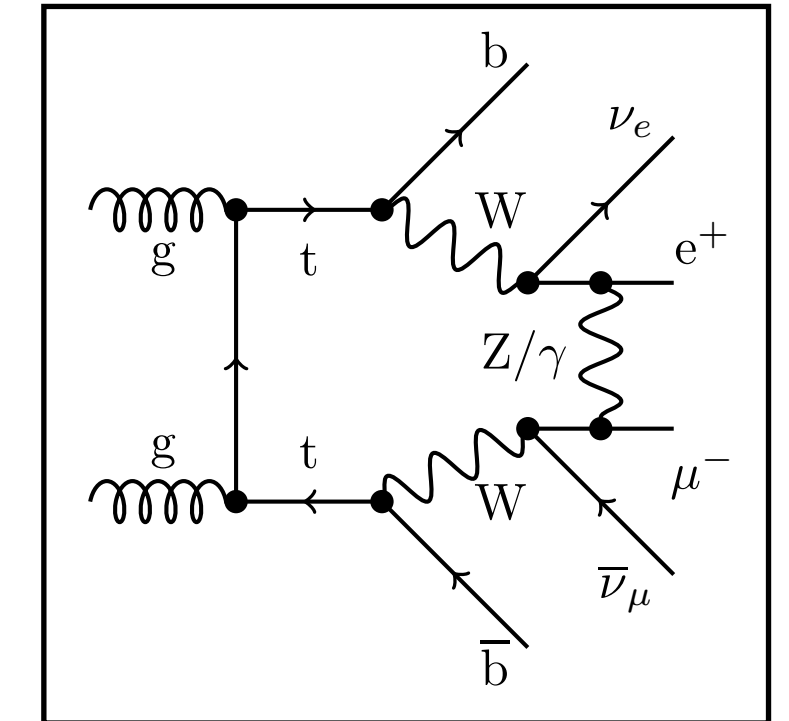
$$m_{b\ell}^{minimax} \equiv \min\{\max(m_{b_1\ell_1}, m_{b_2\ell_2}), \max(m_{b_1\ell_2}, m_{b_2\ell_1})\}$$

- sizeable $t\bar{t}$ -Wt interference expected for large $m_{bl}^{minimax}$
- very good data vs. off-shell 4FS agreement
- DR vs. DS yields conservative uncertainty estimate

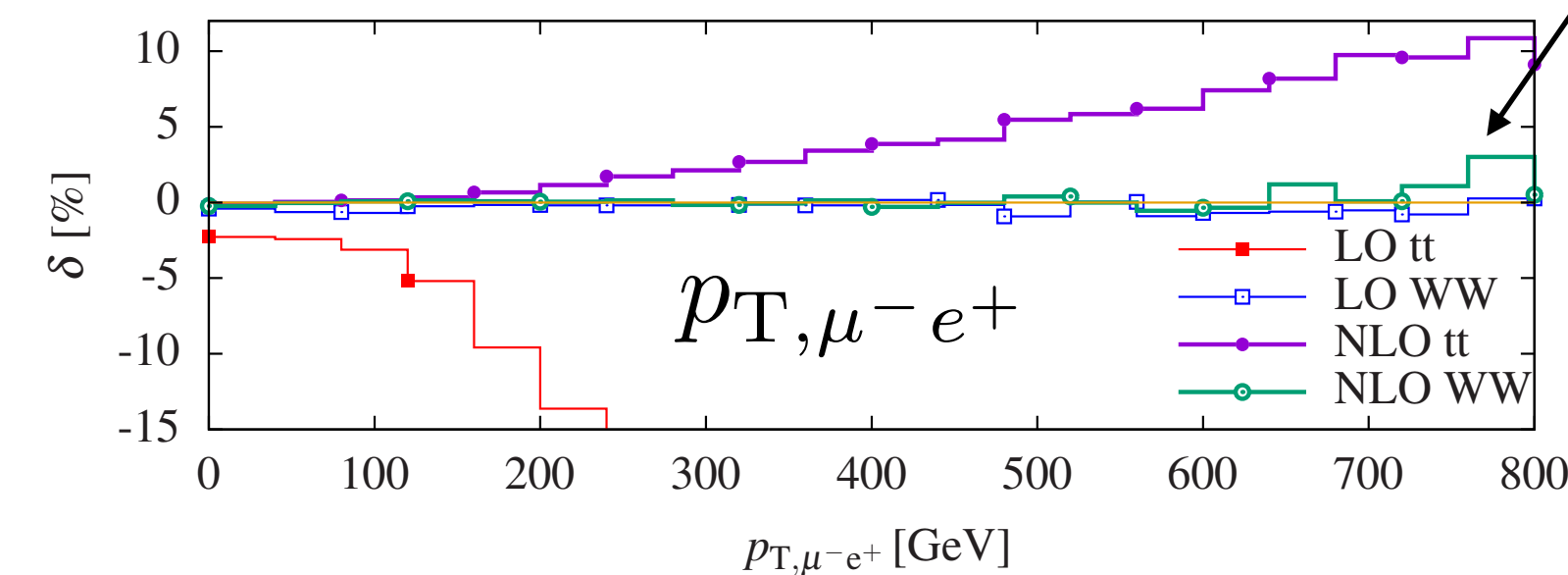
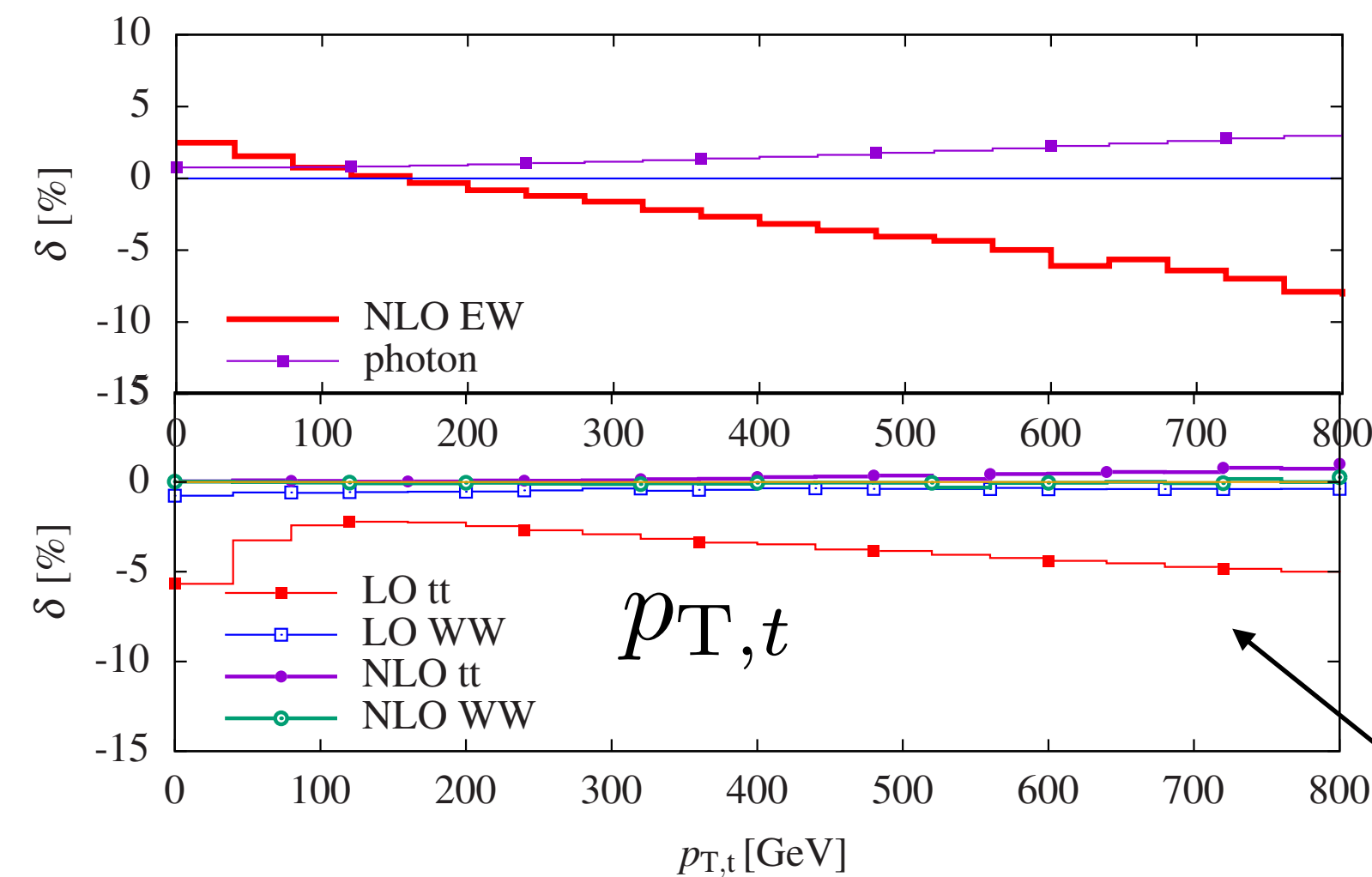
Top-pair: off-shell NLO EW

[Denner, Pellen; '16]

Technical challenge: full $2 \rightarrow 6$ process, i.e. $pp \rightarrow \bar{b}b e^+ \nu_e \mu^- \bar{\nu}_\mu$ @ NLO EW (*)



- O(2-5%) around top resonance
- possible relevance for top mass measurements



- typical Sudakov behaviour O(10%) for $p_{T,t} = 800$ GeV

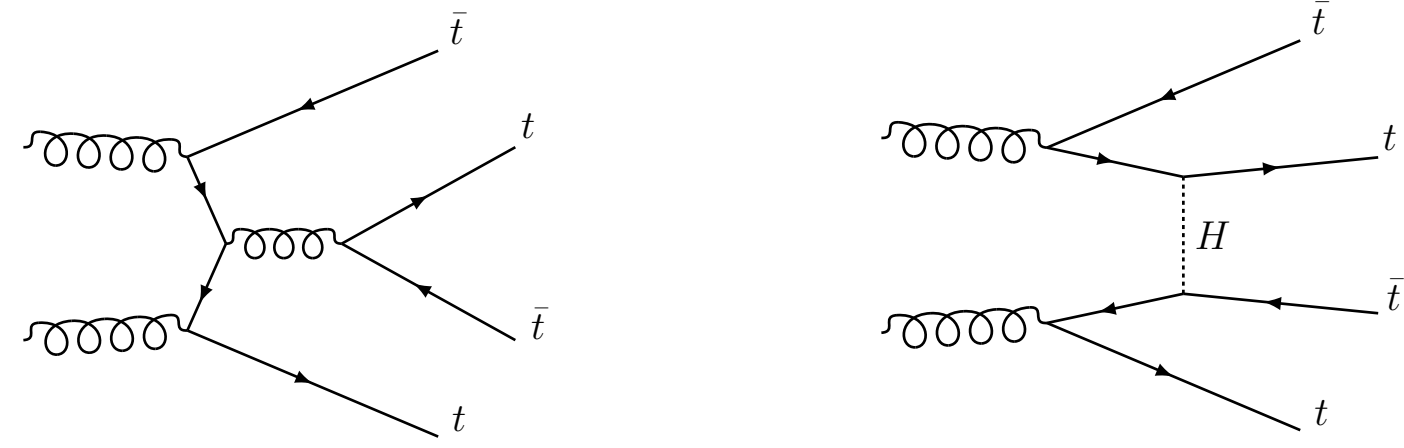
- LO non-resonant: 5% for $p_{T,t} = 800$ GeV

pole approximations/full

- non-resonant configurations important in various observables!
- well described by WWbb approximation

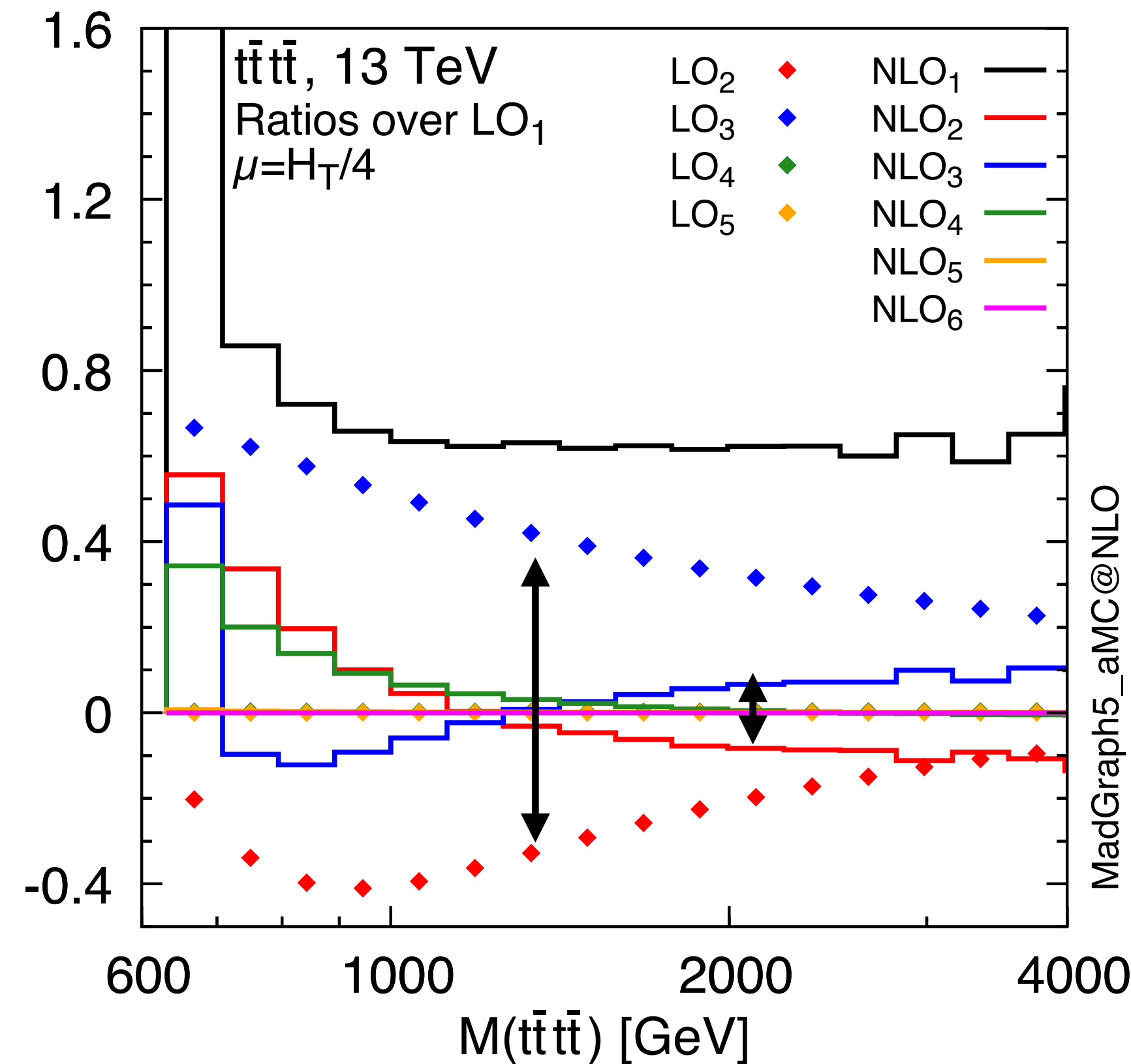
(*) also: $pp \rightarrow \bar{b}b e^+ \nu_e \mu^- \bar{\nu}_\mu H$ [Denner, Lang, Pellen, Uccirati; '16]

Rare top processes



Motivation:

- Constraining top-quark flavour violation [1804.05598]
- Constraining qqtt operators [1708.05928]
- Higgs width and top quark Yukawa coupling [1602.01934]



[Frederix, Pagani, Zaro; '17]

$$\begin{aligned}\Sigma_{\text{LO}}^{t\bar{t}t\bar{t}}(\alpha_s, \alpha) &= \alpha_s^4 \Sigma_{4,0}^{t\bar{t}t\bar{t}} + \alpha_s^3 \alpha \Sigma_{4,1}^{t\bar{t}t\bar{t}} + \alpha_s^2 \alpha^2 \Sigma_{4,2}^{t\bar{t}t\bar{t}} + \alpha_s \alpha^3 \Sigma_{4,3}^{t\bar{t}t\bar{t}} + \alpha^4 \Sigma_{4,4}^{t\bar{t}t\bar{t}} \\ &\equiv \Sigma_{\text{LO}_1} + \Sigma_{\text{LO}_2} + \Sigma_{\text{LO}_3} + \Sigma_{\text{LO}_4} + \Sigma_{\text{LO}_5} .\end{aligned}$$

$$\begin{aligned}\Sigma_{\text{NLO}}^{t\bar{t}t\bar{t}}(\alpha_s, \alpha) &= \alpha_s^5 \Sigma_{5,0}^{t\bar{t}t\bar{t}} + \alpha_s^4 \alpha \Sigma_{5,1}^{t\bar{t}t\bar{t}} + \alpha_s^3 \alpha^2 \Sigma_{5,2}^{t\bar{t}t\bar{t}} + \alpha_s^2 \alpha^3 \Sigma_{5,3}^{t\bar{t}t\bar{t}} + \alpha_s \alpha^4 \Sigma_{5,4}^{t\bar{t}t\bar{t}} + \alpha^5 \Sigma_{5,5}^{t\bar{t}t\bar{t}} \\ &\equiv \Sigma_{\text{NLO}_1} + \Sigma_{\text{NLO}_2} + \Sigma_{\text{NLO}_3} + \Sigma_{\text{NLO}_4} + \Sigma_{\text{NLO}_5} + \Sigma_{\text{NLO}_6} .\end{aligned}$$

- Sizeable (accidental) cancellation between different LO and NLO orders
- calculation of only part of the complete-NLO results would be misleading
- cancellation could be spiked by BSM effects

Conclusions

- SM is in excellent shape
- High-precision (Theo + Exp) allows to push limits to unprecedented levels (LHC completes LEP)
- NNLO **QCD** + NLO **EW** is the new standard: VV, V+jets, dijets, tt, HV, VBF
- Explore the unknown: **tail, tails, tails!!**

New theoretical, mathematical, and computational concepts

?



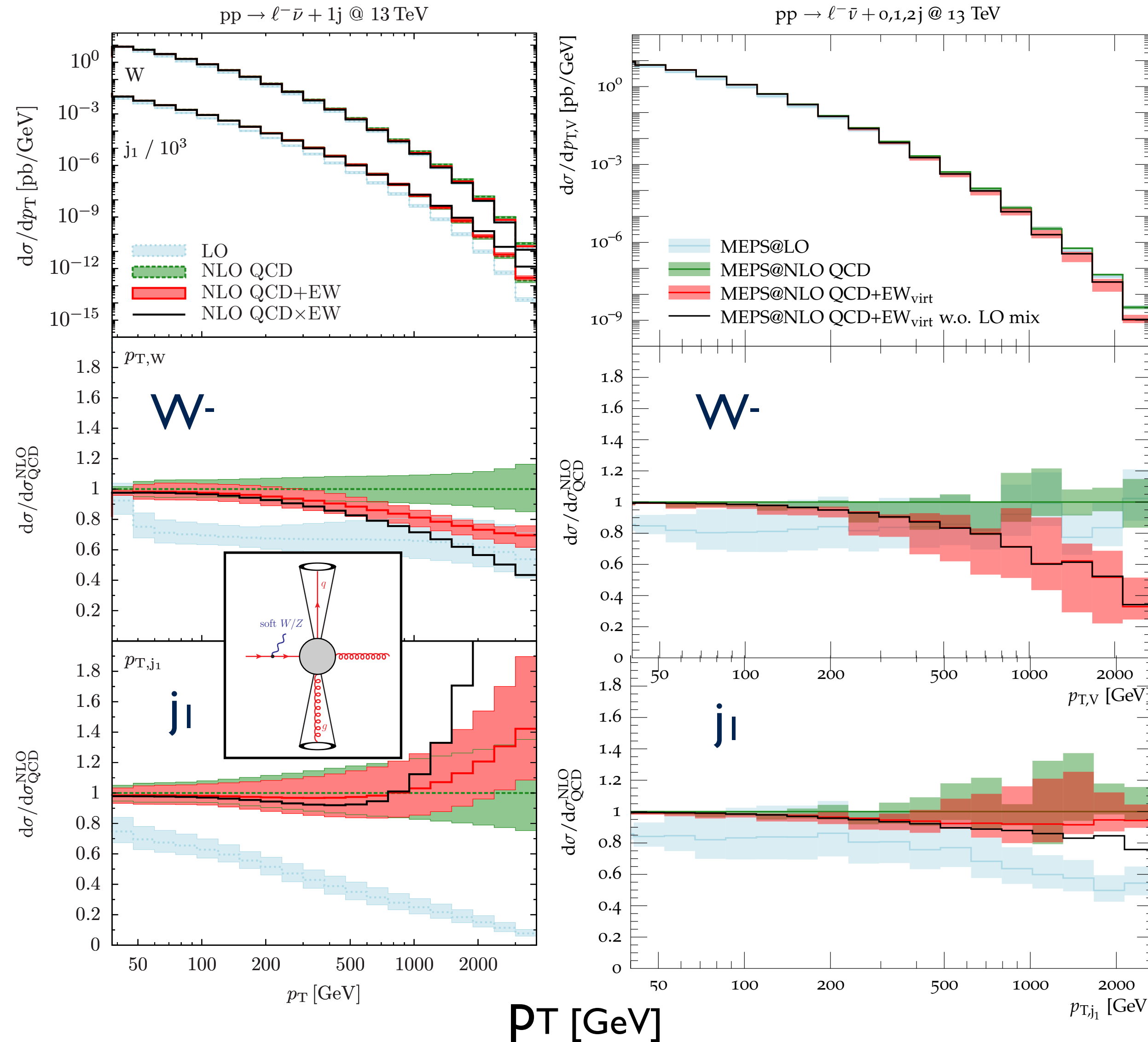
Possible technical developments towards HL/HE-LHC

- NNLO **QCD** + PS
- PS matching and multi-jet merging @ NLO **QCD**+**EW**
- NNLO **QCD** for $2 \rightarrow 3(4)$
- NNLO **QCD**x**EW** & NNLO **EW**
- N3LO **QCD** for $2 \rightarrow 2$

precision for HL/HE-LHC

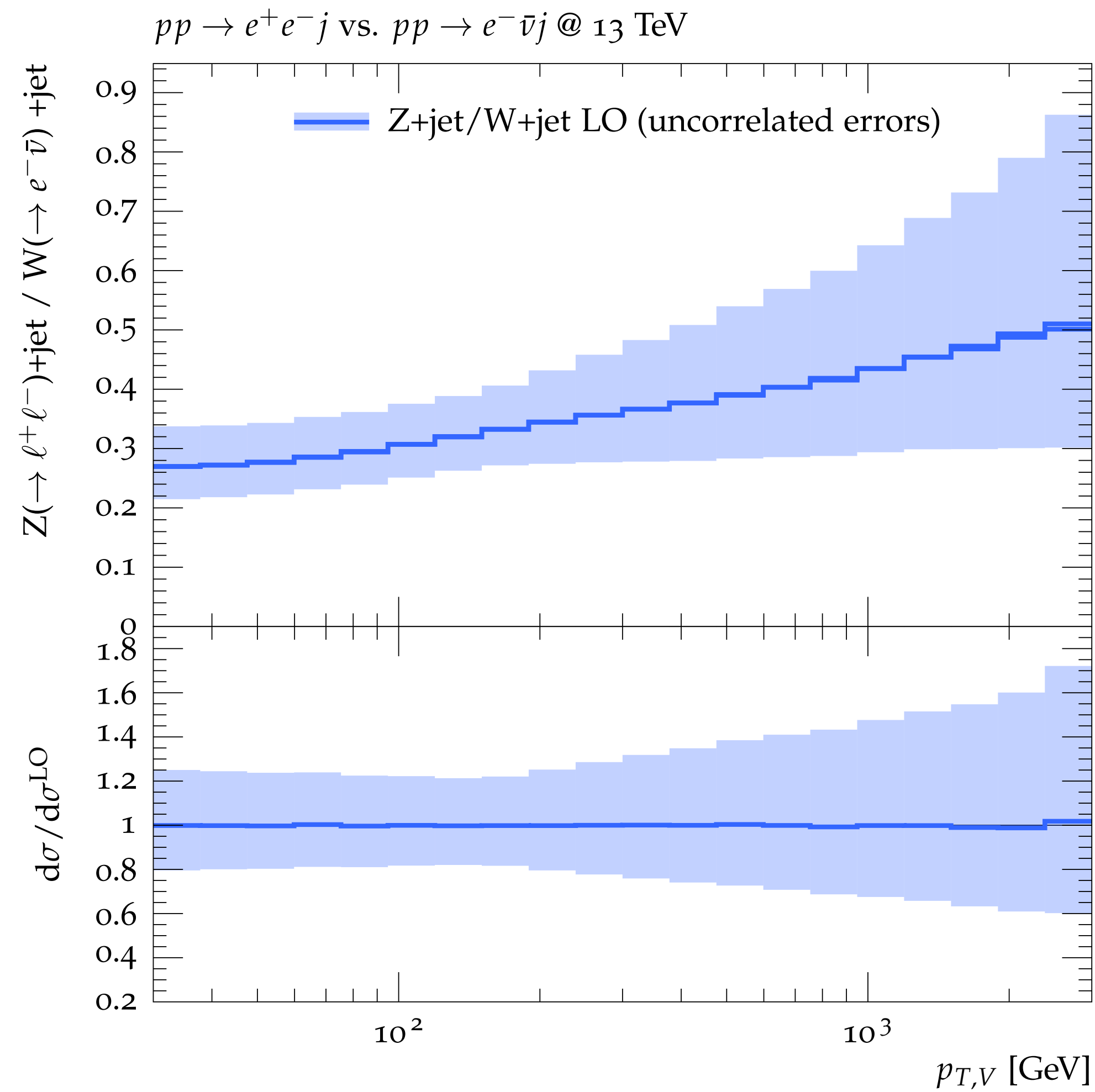
Backup

inclusive V: MEPS@NLO $\text{QCD} + \text{EW}_{\text{virt}}$



- Bases on Sherpa's standard MEPS@NLO
- Stable NLO $\text{QCD} + \text{EW}$ predictions in all of the phase-space...
- ...including Parton-Shower effects.
- Can directly be used by the experimental collaborations
- $p_{T,V}$: MEPS@NLO $\text{QCD} + \text{EW}$ in agreement with $\text{QCD} \times \text{EW}$ (fixed-order)
- $p_{T,j1}$:
 - merging ensures stable results (dijet topology at LO)
 - compensation between negative Sudakov and LO mix

How to correlate QCD uncertainties across processes?



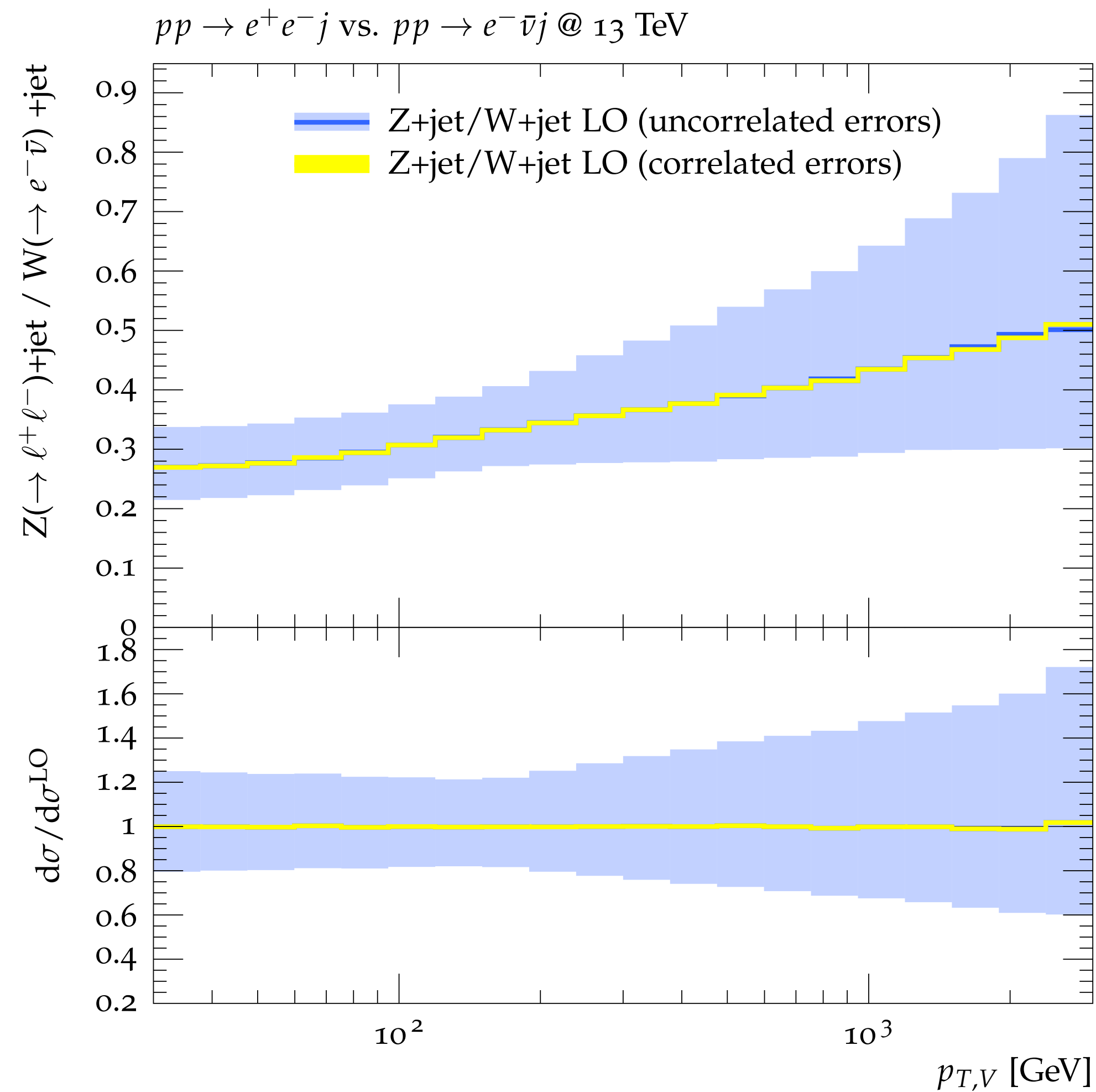
consider Z+jet / W+jet $p_{T,V}$ -ratio @ LO

uncorrelated treatment yields

O(40%) uncertainties

How to correlate QCD uncertainties across processes?

[1705.04664]



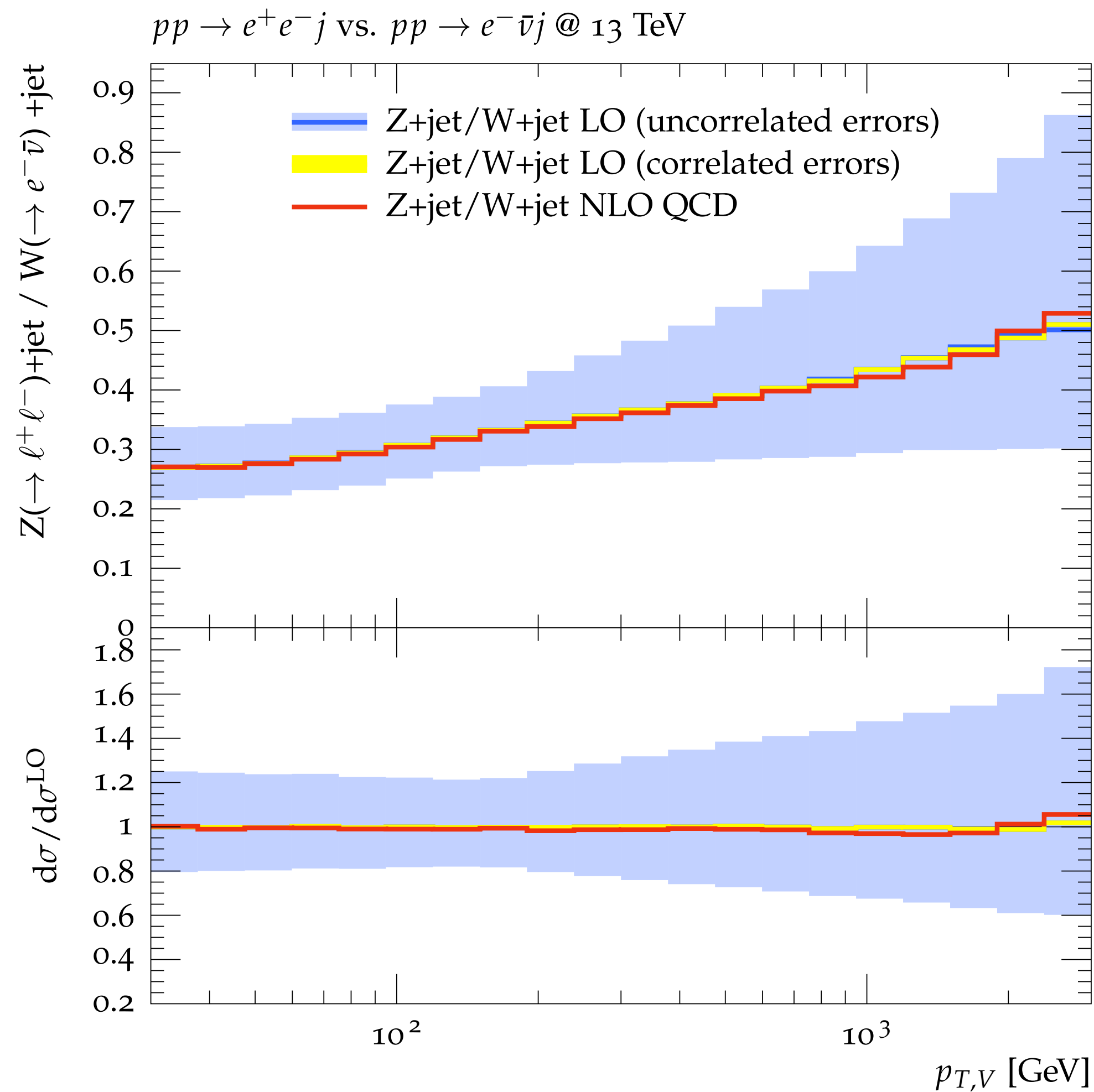
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uncorrelated treatment yields
 $\mathcal{O}(40\%)$ uncertainties

correlated treatment yields tiny
 $\mathcal{O}(<\sim 1\%)$ uncertainties

How to correlate QCD uncertainties across processes?

[1705.04664]



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 $O(<\sim 1\%)$ uncertainties

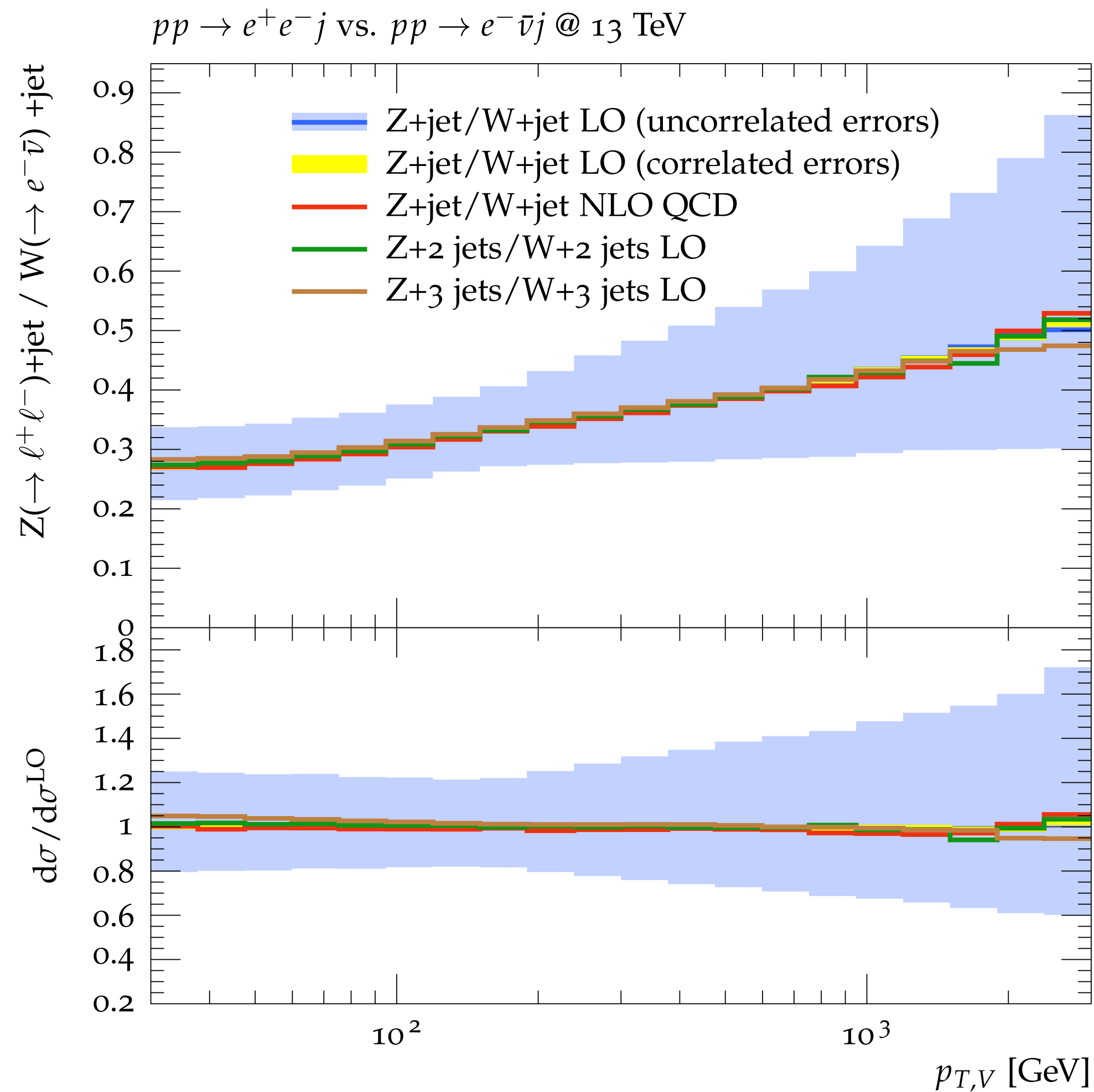
check against NLO QCD!

NLO QCD corrections remarkably flat
in Z+jet / W+jet ratio!

→ supports correlated treatment of
uncertainties!

How to correlate QCD uncertainties across processes?

[1705.04664]



consider Z+jet / W+jet $p_{T,V}$ -ratio @ LO

uncorrelated treatment yields
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O(<~ 1%) uncertainties

check against NLO QCD!

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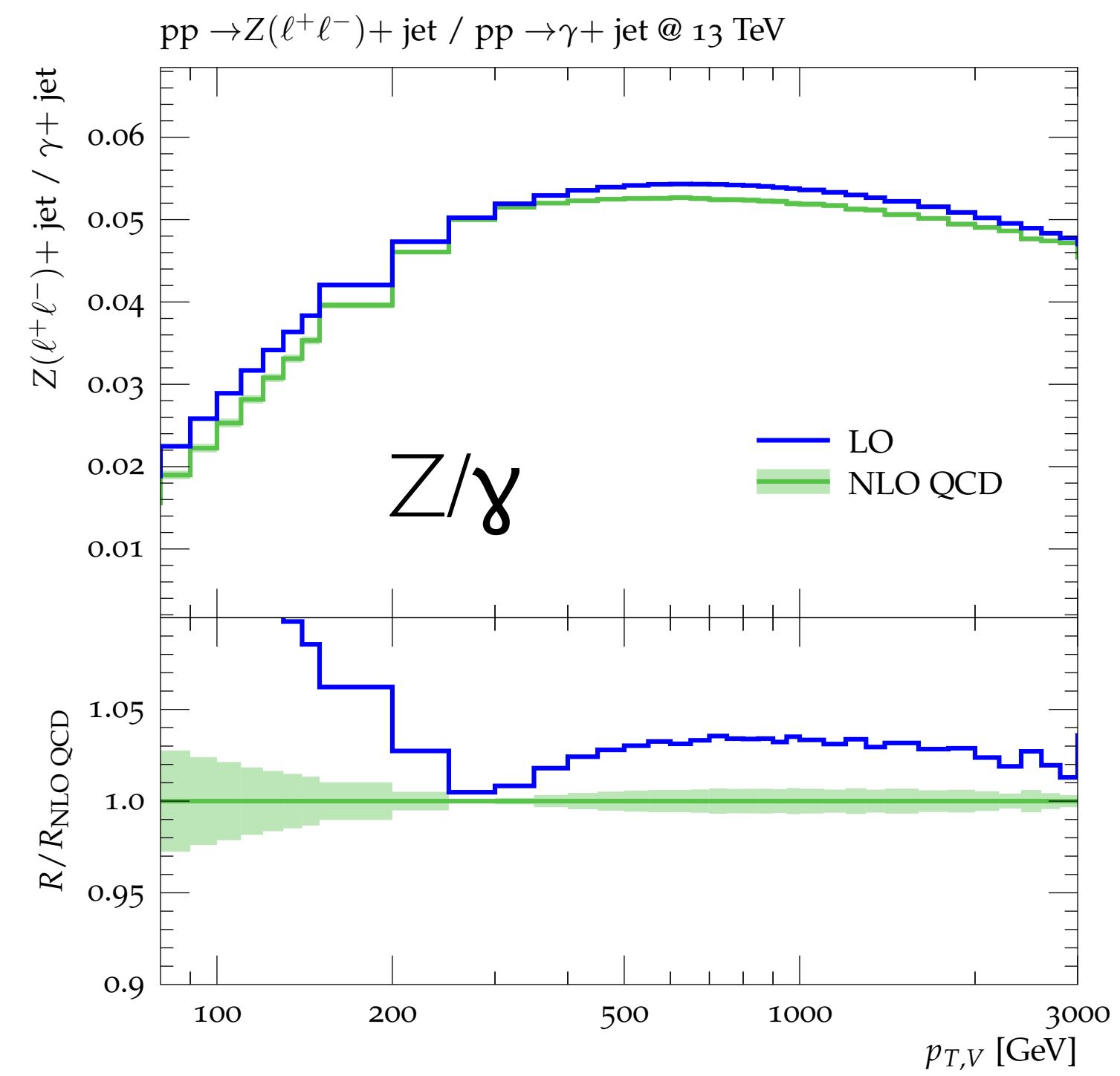
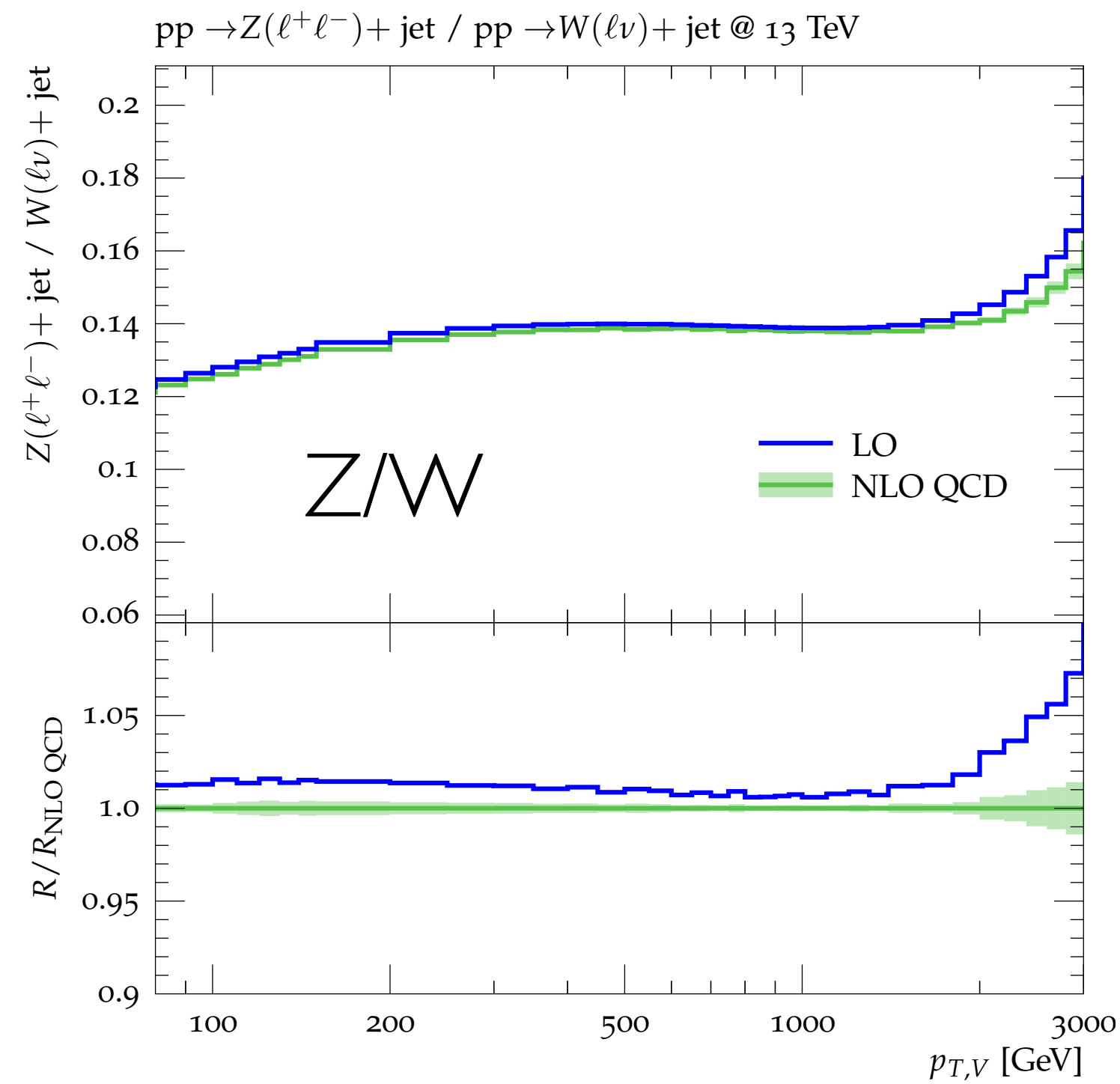
Also holds for higher jet-multiplicities

→ indication of correlation also in
higher-order corrections beyond NLO!

QCD uncertainties: ratios

How to correlate these uncertainties across processes?

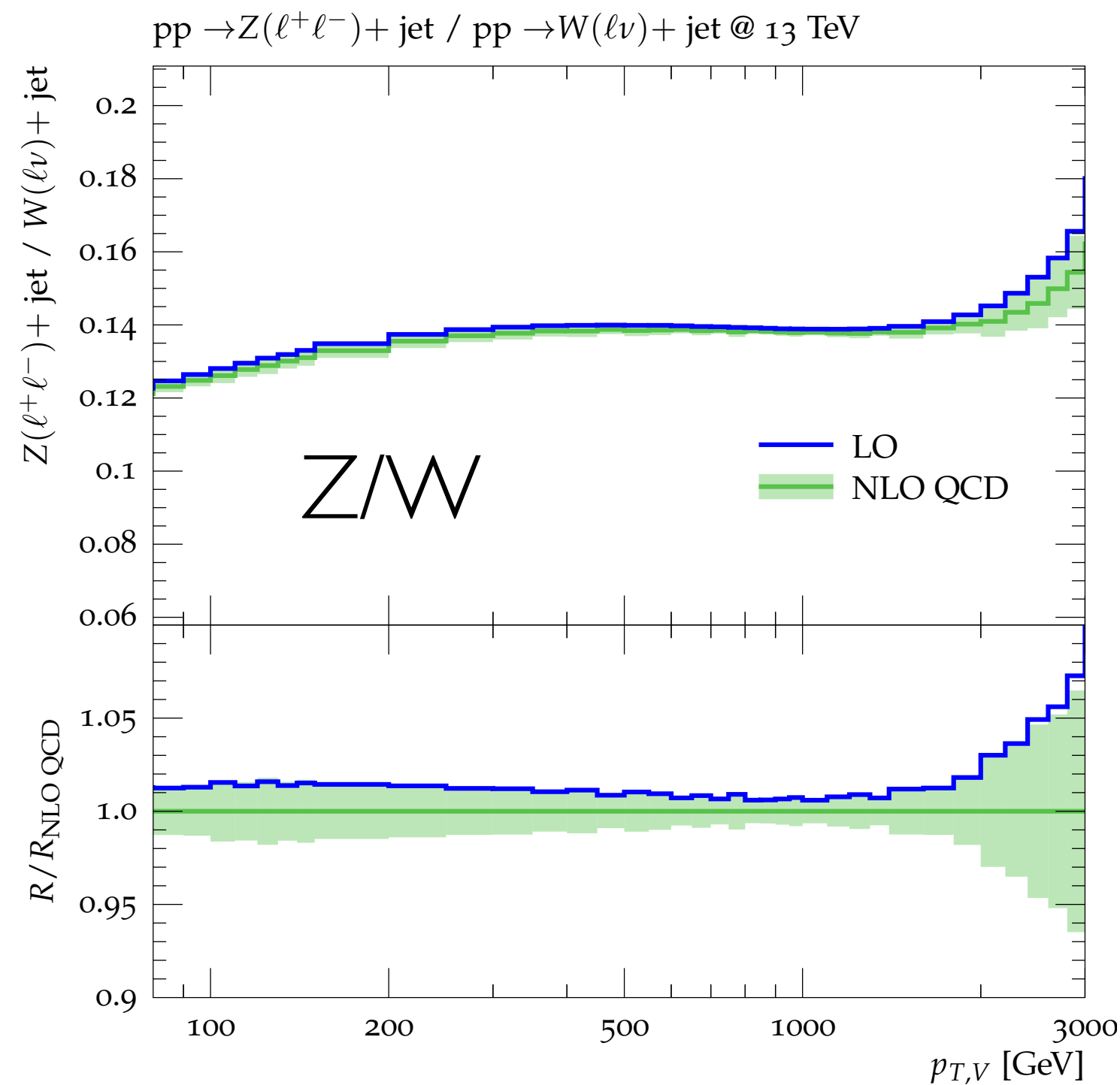
- take scale uncertainties as fully correlated:
NLO QCD uncertainties cancel at the $< \sim 1\%$ level



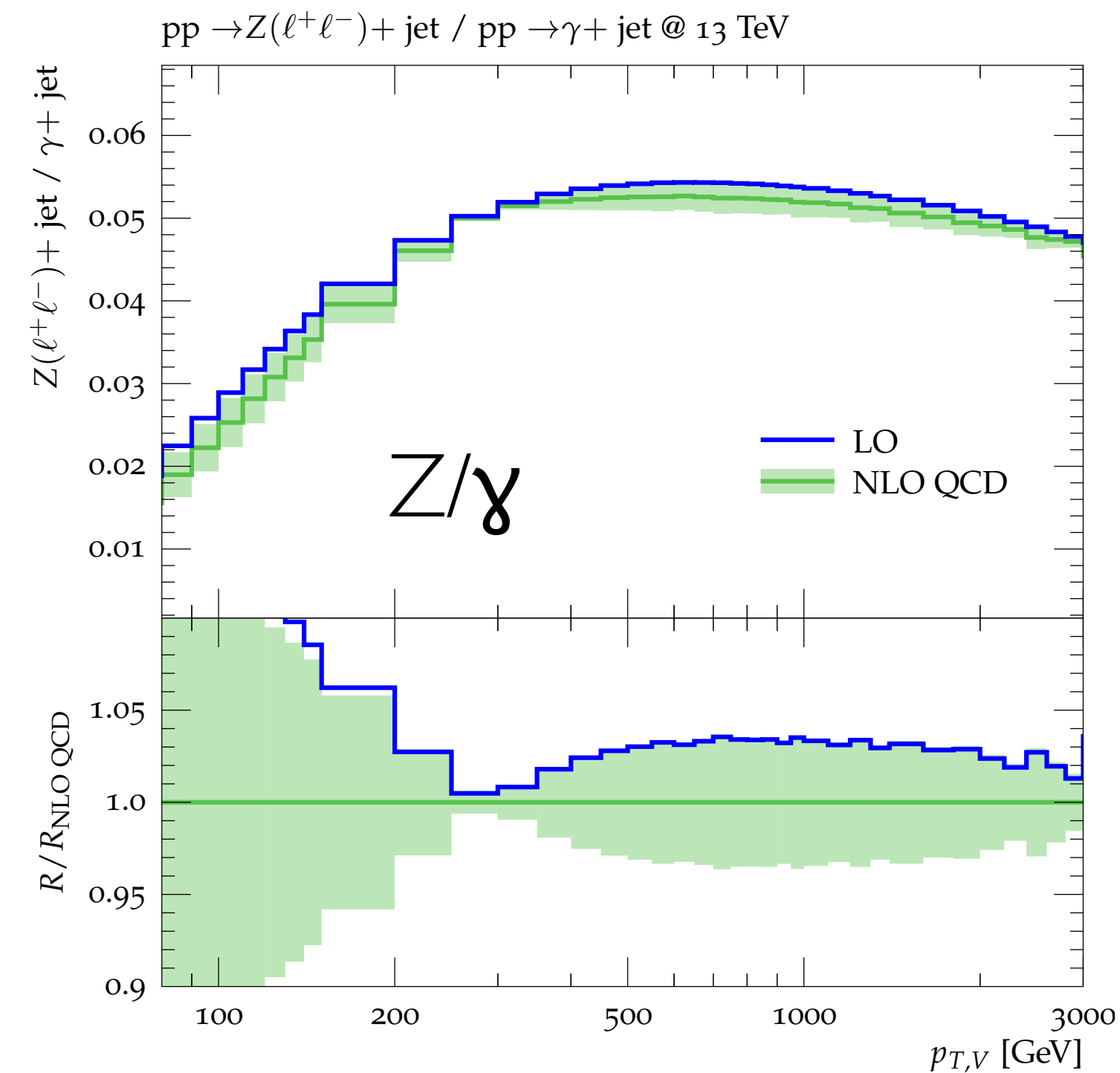
QCD uncertainties: ratios

How to correlate these uncertainties across processes?

- take scale uncertainties as fully correlated:
NLO QCD uncertainties cancel at the $< \sim 1$ % level
- introduce **process correlation uncertainty** based on K-factor difference: $\delta K_{\text{NLO}} = K_{\text{NLO}}^V - K_{\text{NLO}}^Z$
→ effectively degrades precision of last calculated order



$\delta < 2$ %

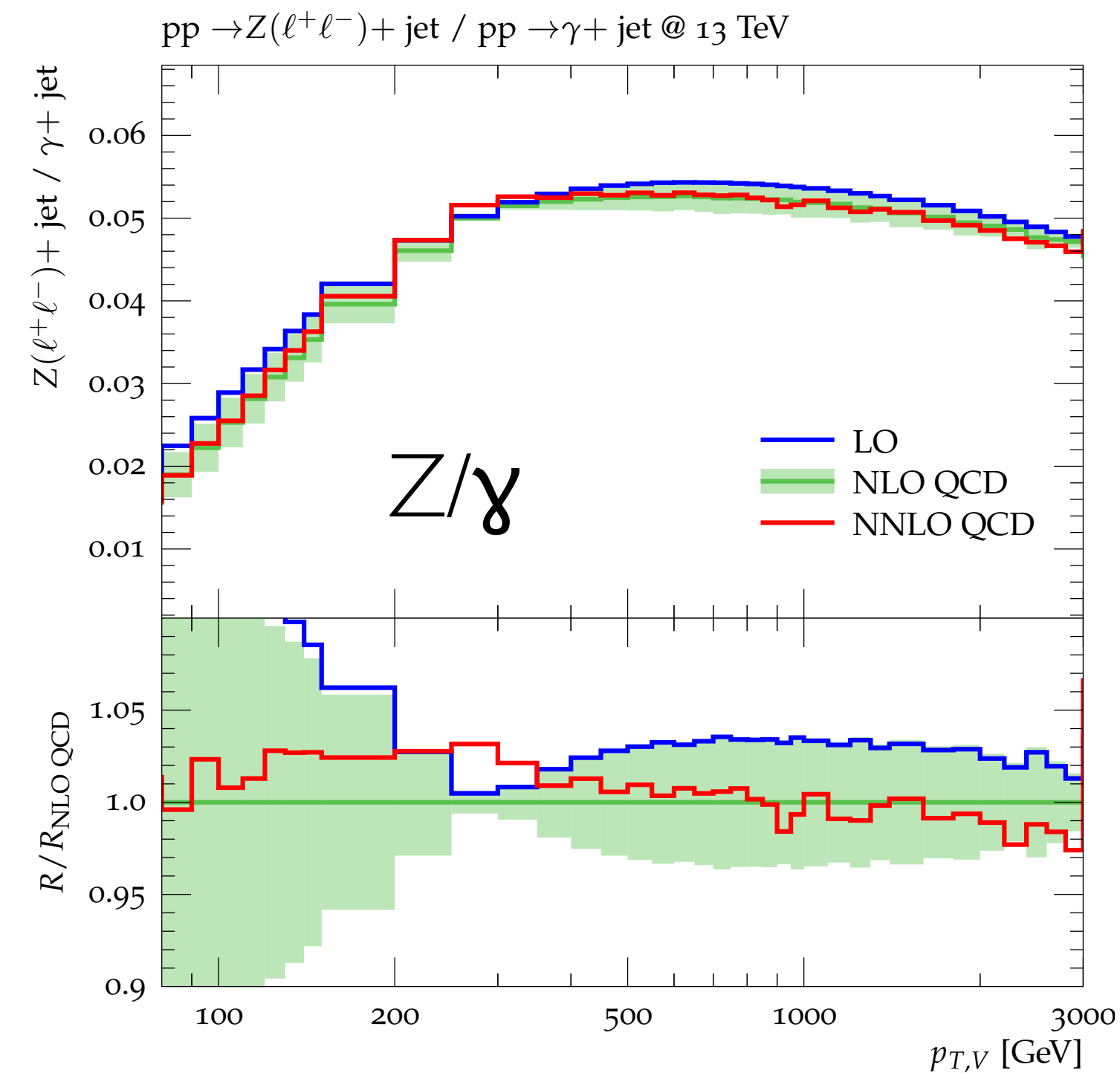
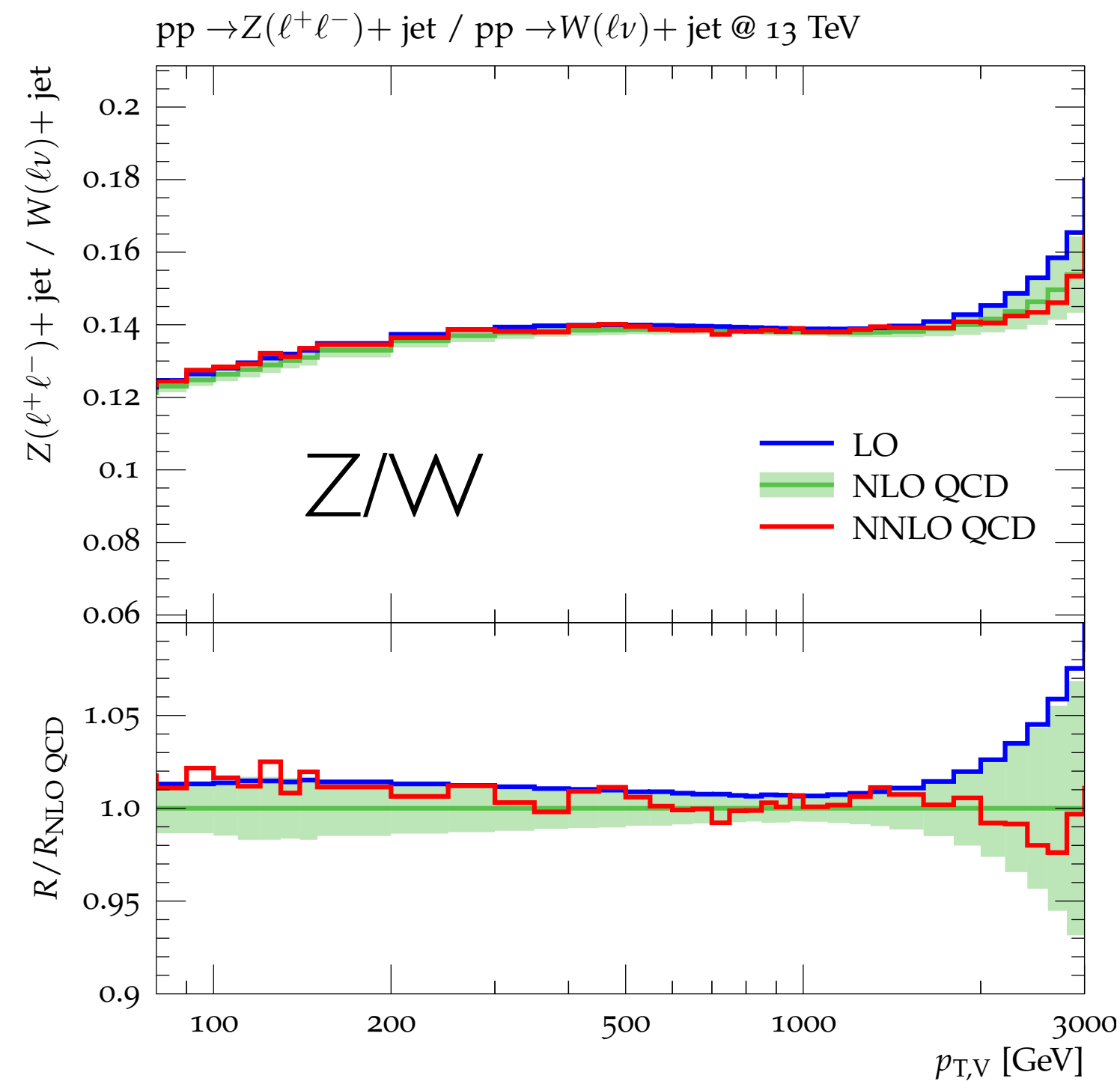


$\delta < 3-4$ %

QCD uncertainties: ratios

How to correlate these uncertainties across processes?

- take scale uncertainties as fully correlated:
NLO QCD uncertainties cancel at the $< \sim 1\%$ level
- introduce **process correlation uncertainty** based on K-factor difference: $\delta K_{\text{NLO}} = K_{\text{NLO}}^V - K_{\text{NLO}}^Z$
→ effectively degrades precision of last calculated order

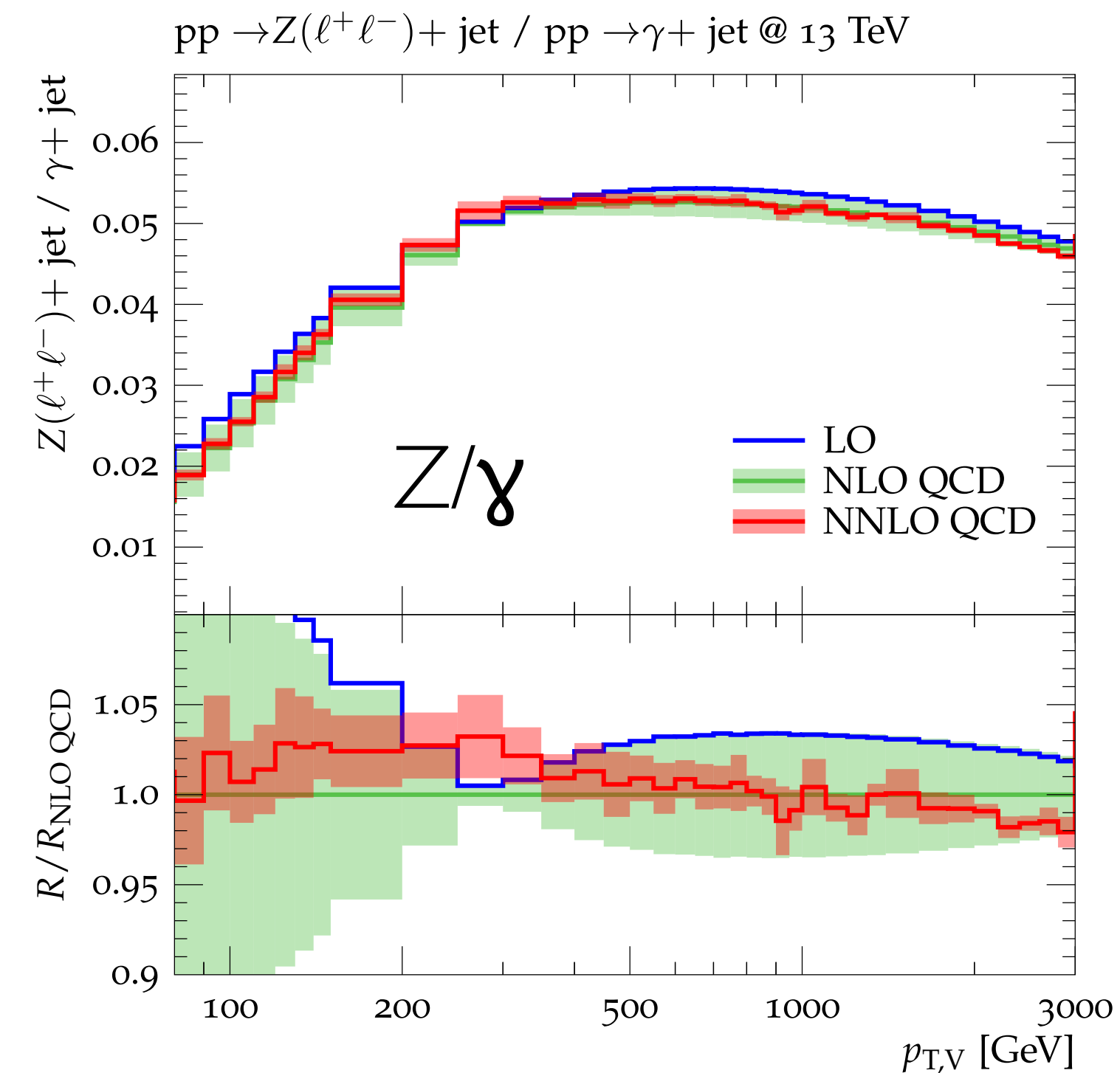
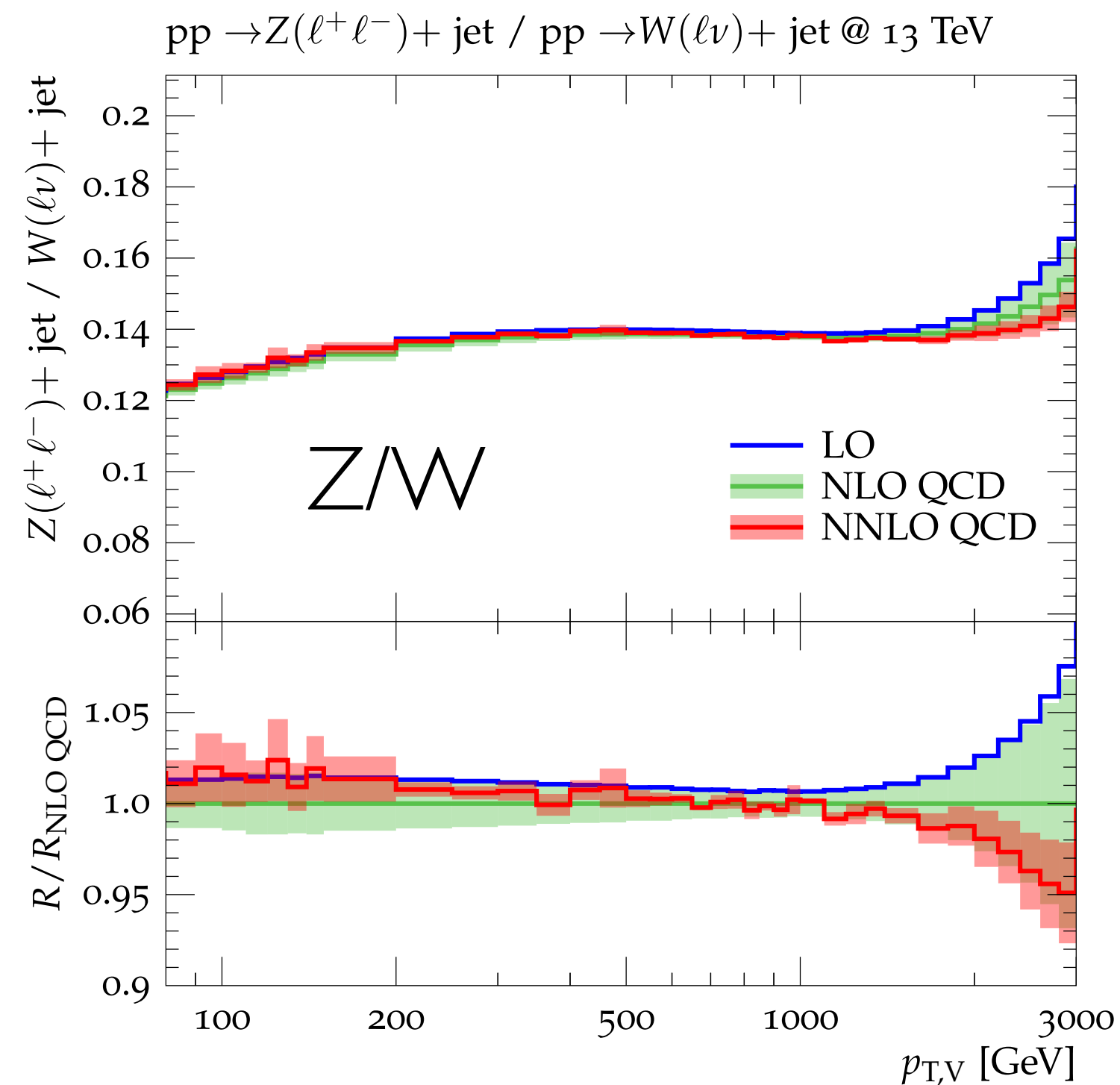


check against NNLO QCD!

QCD uncertainties: ratios

How to correlate these uncertainties across processes?

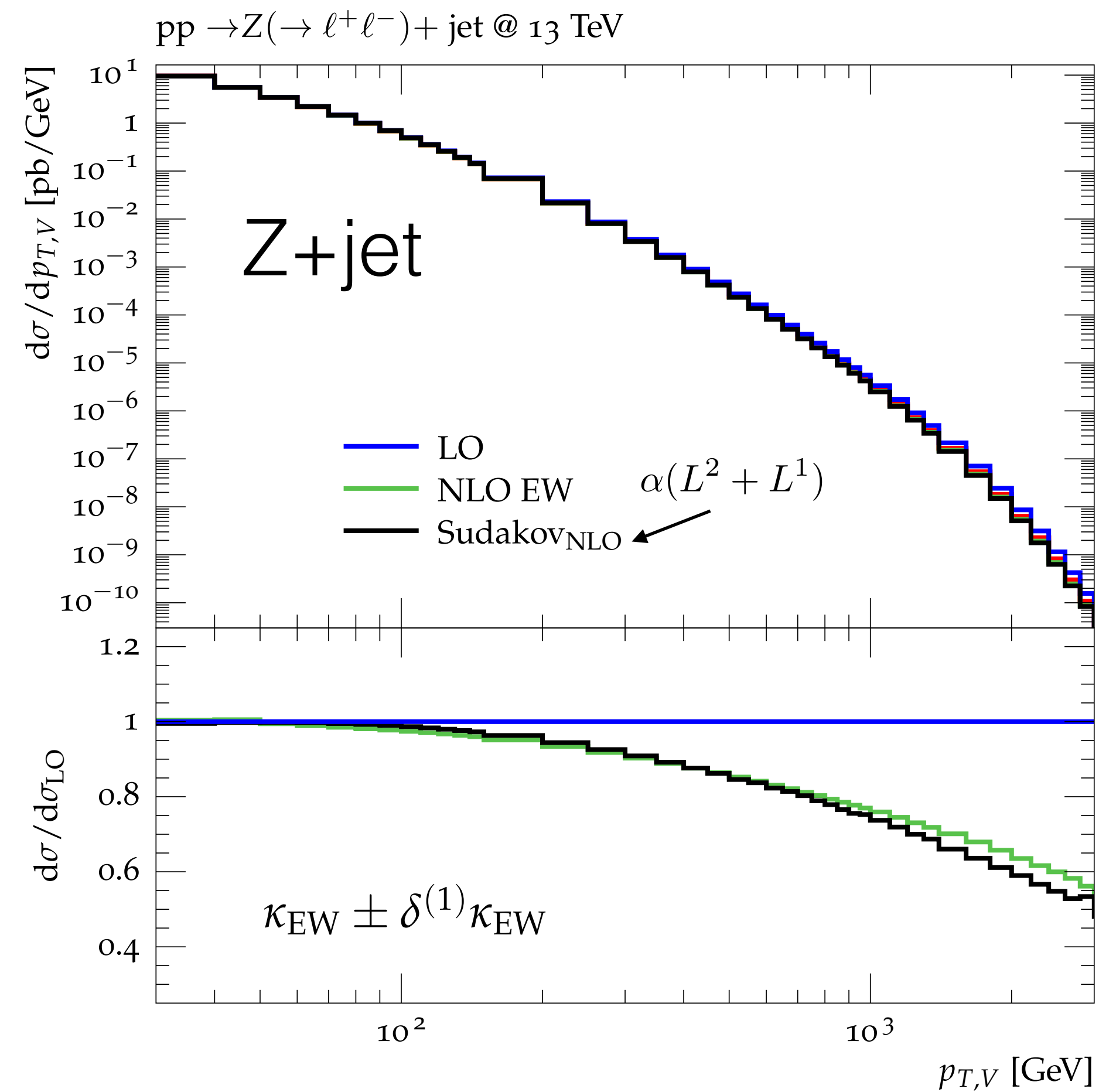
- take scale uncertainties as fully correlated:
NLO QCD uncertainties cancel at the $< \sim 1\%$ level
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→ effectively degrades precision of last calculated order



Uncertainty estimates at NNLO QCD

Pure EW uncertainties

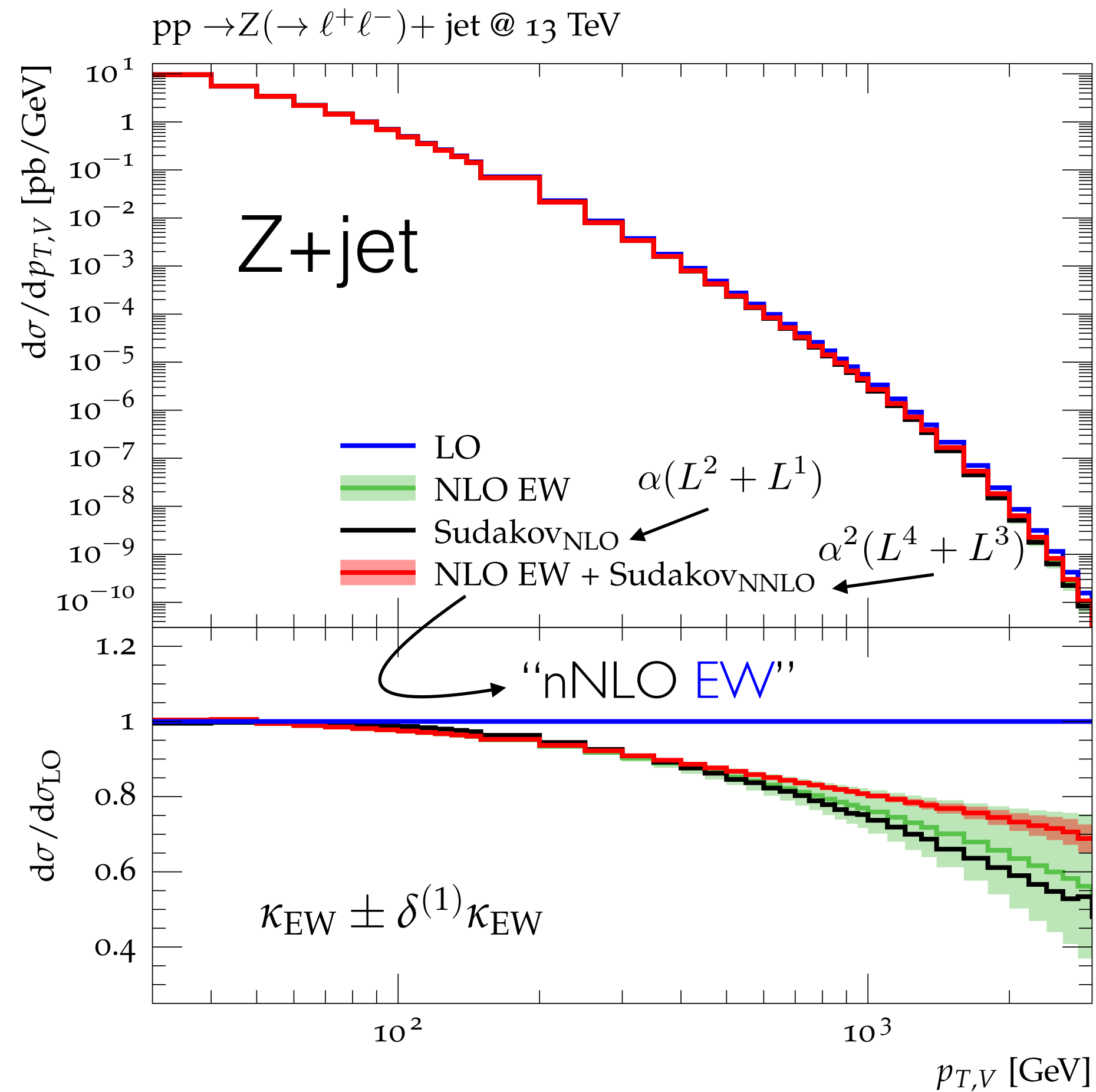
[JML et. al.: 1705.04664]



Large EW corrections dominated by Sudakov logs

Pure EW uncertainties

[JML et. al.: 1705.04664]



Large EW corrections dominated by Sudakov logs



Uncertainty estimate of (N)NLO EW from naive exponentiation $\times 2$:

$$\delta^{(1)}\kappa_{\text{EW}} \simeq \frac{2}{k!} \left(\kappa_{\text{NLO,EW}} \right)^k \quad (\text{correlated})$$



check against two-loop Sudakov logs

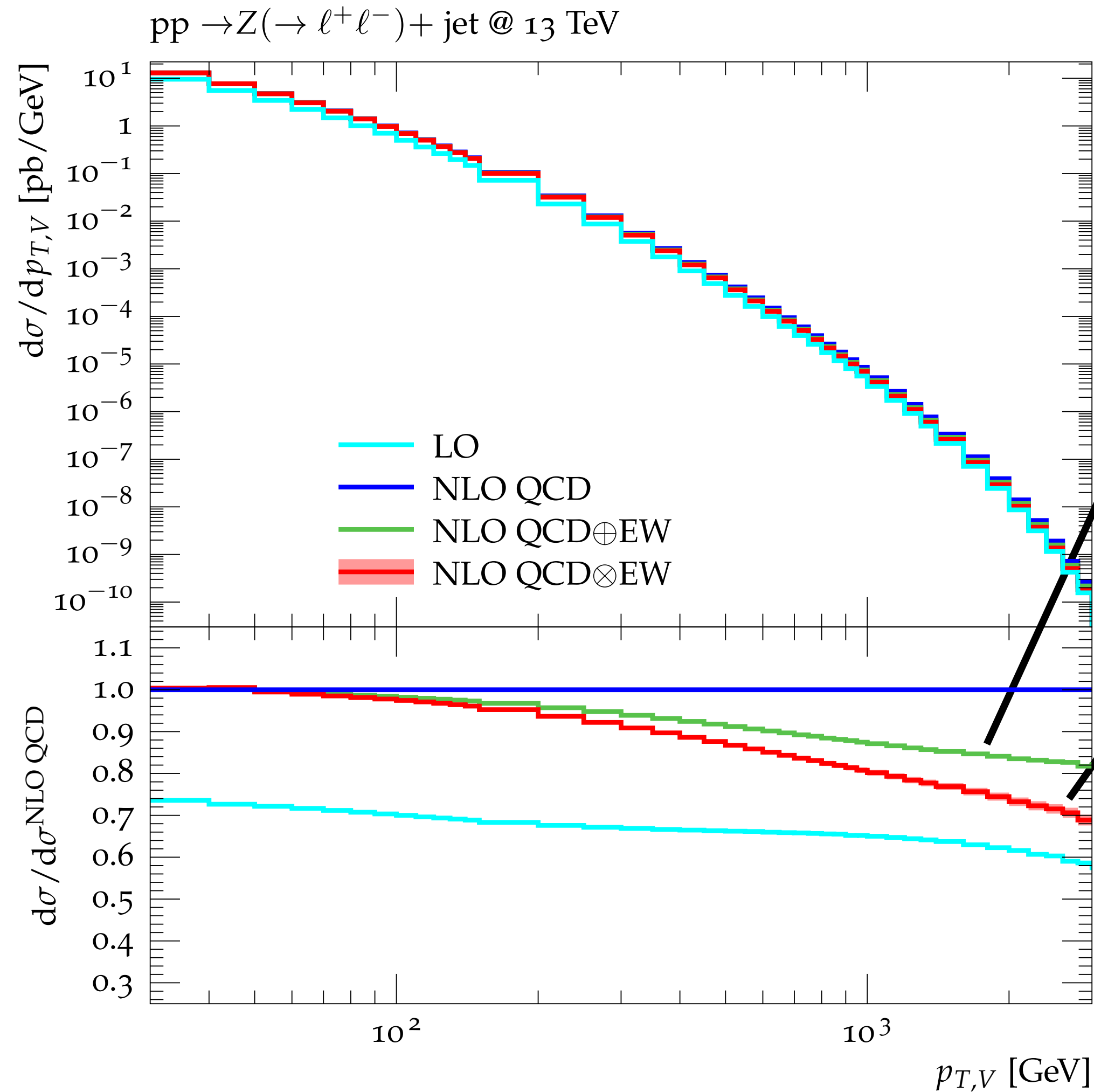
[Kühn, Kulesza, Pozzorini, Schulze; 05-07]

$$\kappa_{\text{NLO EW}}(\hat{s}, \hat{t}) = \frac{\alpha}{\pi} \left[\delta_{\text{hard}}^{(1)} + \delta_{\text{Sud}}^{(1)} \right]$$

$$\kappa_{\text{NNLO Sud}}(\hat{s}, \hat{t}) = \left(\frac{\alpha}{\pi} \right)^2 \delta_{\text{Sud}}^{(2)}$$

+ additional uncertainties for hard non-log NNLO EW effects (uncorrelated)

Mixed QCD-EW uncertainties



Given QCD and EW corrections are sizeable, also mixed QCD-EW uncertainties of relative $\mathcal{O}(\alpha\alpha_s)$ have to be considered.

Additive combination

$$\sigma_{\text{QCD}+\text{EW}}^{\text{NLO}} = \sigma^{\text{LO}} + \delta\sigma_{\text{QCD}}^{\text{NLO}} + \delta\sigma_{\text{EW}}^{\text{NLO}}$$

(no $\mathcal{O}(\alpha\alpha_s)$ contributions)

Multiplicative combination

$$\sigma_{\text{QCD} \times \text{EW}}^{\text{NLO}} = \sigma_{\text{QCD}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right)$$

(try to capture some $\mathcal{O}(\alpha\alpha_s)$ contributions, e.g. EW Sudakov logs \times soft QCD)

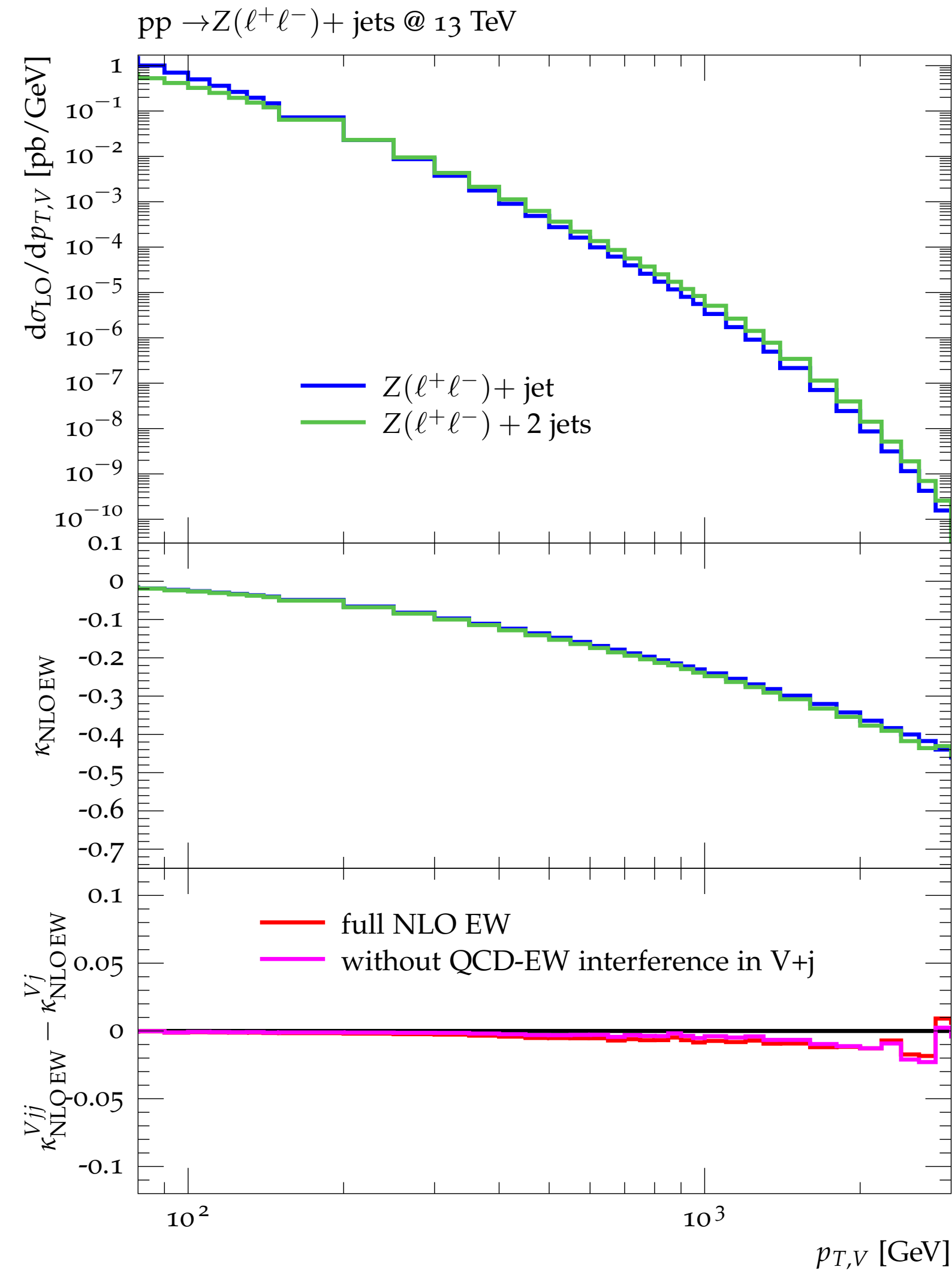
Difference between these two approaches indicates size of missing mixed EW-QCD corrections.

$$K_{\text{QCD} \otimes \text{EW}} - K_{\text{QCD} \oplus \text{EW}} \sim 10\% \quad \text{at 1 TeV}$$

Too conservative!?

For dominant Sudakov EW logarithms factorization should be exact!

Mixed QCD-EW uncertainties



Bold estimate:

Consider real $\mathcal{O}(\alpha\alpha_s)$ correction to V+jet

\simeq NLO EW to V+2jets

and we observe

$$\left. \frac{d\sigma_{\text{NLO EW}}}{d\sigma_{\text{LO}}} \right|_{V+2\text{jet}} - \left. \frac{d\sigma_{\text{NLO EW}}}{d\sigma_{\text{LO}}} \right|_{V+1\text{jet}} \lesssim 1\%$$

strong support for

- factorization
- multiplicative QCD \times EW combination

Estimate of non-factorising contributions

(correlated)

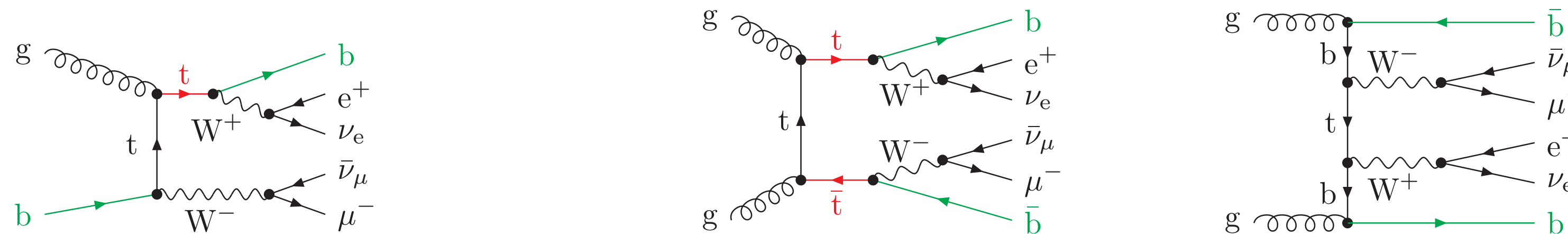
$$\delta K_{\text{mix}}^{(V)}(x) = 0.1 \left[K_{\text{TH},\oplus}^{(V)}(x, \vec{\mu}_0) - K_{\text{TH},\otimes}^{(V)}(x, \vec{\mu}_0) \right]$$

(tuned to cover above difference of EW K-factors)

Top-free W^+W^- definitions

Huge Wt and $t\bar{t}$ contamination from $\overbrace{W^+W^-b}^{+40\% \text{ NLO}}$ and $\overbrace{W^+W^-b\bar{b}}^{+400\% \text{ NNLO}}$

- intimately connected with W^+W^- through $g \rightarrow b\bar{b}$ singularities
- top subtraction** tricky and not unique \Rightarrow **theoretical ambiguity in $\sigma_{WW}^{(N)\text{NLO}}$!**



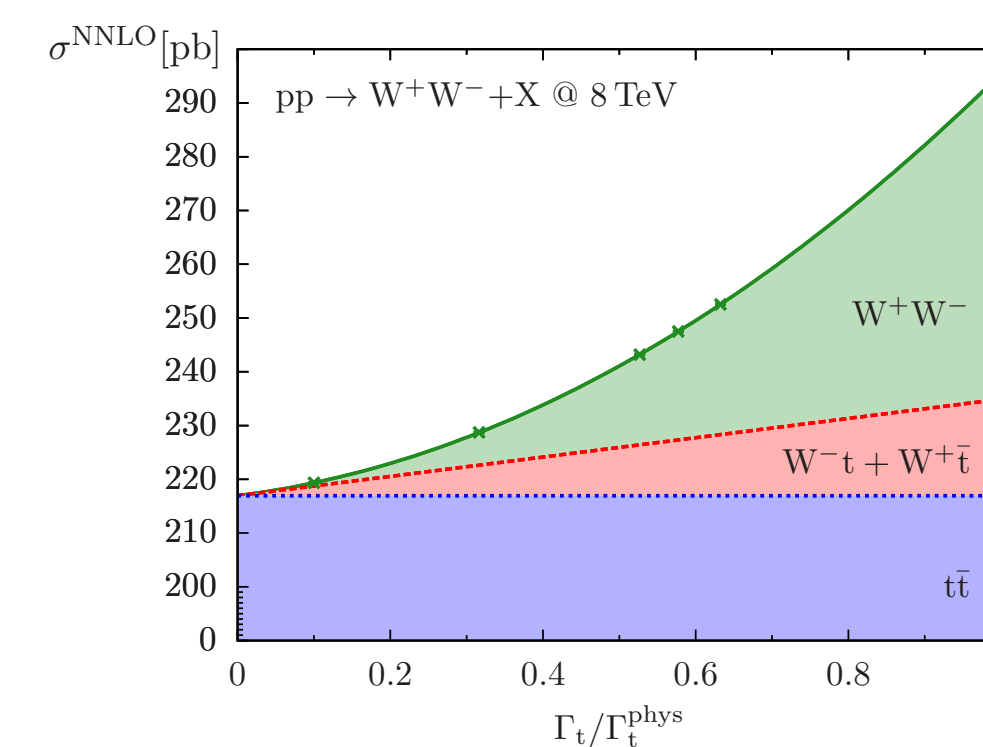
Definition A: veto b -quark emissions in 4F scheme ($m_b > 0$)

- $\Rightarrow \ln(m_b/M_W)$ terms **might jeopardize NNLO accuracy!**

Definition B: top-resonance fit in 5F-scheme ($m_b = 0$)

$$\lim_{\xi_t \rightarrow 0} \sigma_{\text{full}}^{5\text{F}}(\xi_t \Gamma_t) = \xi_t^{-2} \left[\sigma_{t\bar{t}}^{5\text{F}} + \xi_t \sigma_{Wt}^{5\text{F}} + \xi_t^2 \sigma_{W^+W^-}^{5\text{F}} \right]$$

\Rightarrow **for inclusive $\sigma_{WW}^{\text{NNLO}}$ only 1–2% ambiguity (A vs B)**



Relevant issue for percent-precision tests of W^+W^- physics! ... Relation to σ_{WW}^{EXP} ?